

Strongly correlated Dirac electrons in electron doped herbertsmithite

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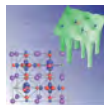


Acknowledgments

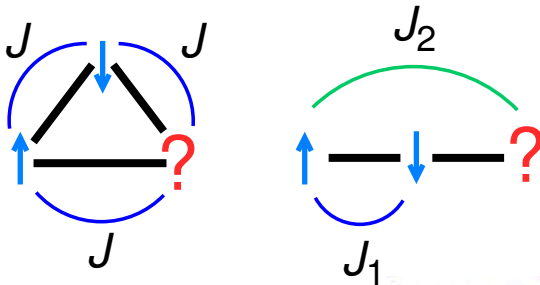
- **Frankfurt Theory:** Francesc Salvat-Pujol, Hunpyo Lee (now South Korea), Roser Valentí.
- Naval Research Lab, Washington D.C.: Igor Mazin
- Uni Hamburg: Frank Lechermann
- Uni Würzburg: M. Fink, Ronny Thomale
- Argonne National Lab: John Schlueter (now NSF)
- Frankfurt experiment: Elena Gati, N. H. Hoang, Bernd Wolf, Michael Lang

Funding:

- DFG FOR 1346 “Dynamical Mean Field Approach with Predictive Power for Strongly Correlated Materials”
- DFG TR 49 “Condensed Matter Systems with Variable Many-Body Interactions”

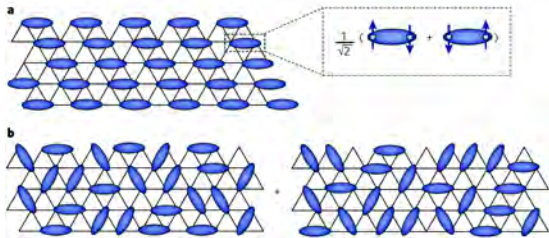


Frustrated magnetism



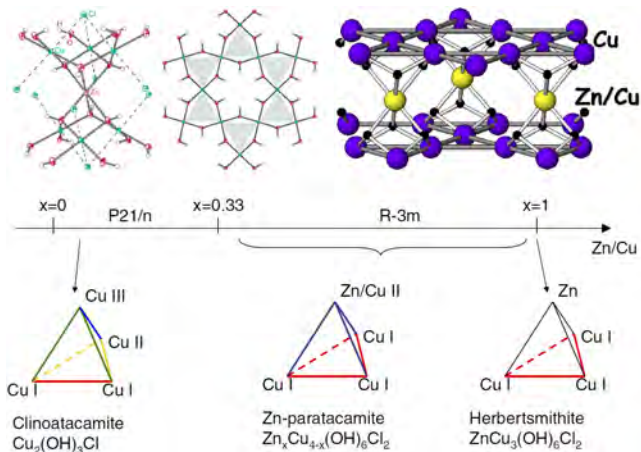
- large degeneracy of ground states
- quantum fluctuations
- spin liquid (cooperative paramagnet) as exotic state of matter

- geometrical frustration
- competition between exchange couplings



Balents, Nature 464, 199 (2010).

An end to the drought of quantum spin liquids (P. A. Lee)



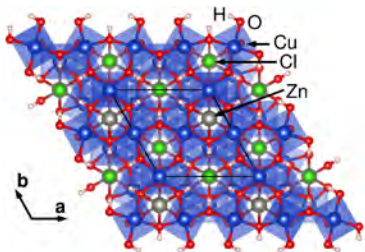
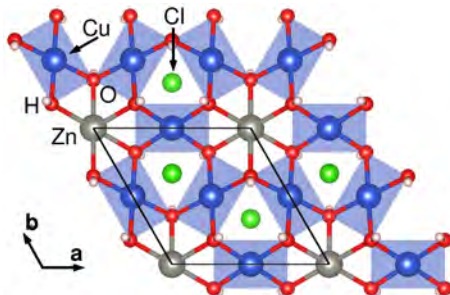
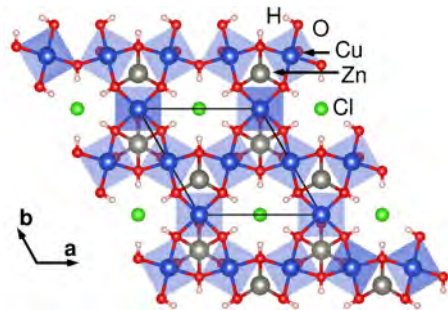
Mendels, Bert, JPSJ 79, 011001 (2010)

- Herbertsmithite $ZnCu_3(OH)_6Cl_2$ reported to be very good realization of a quantum spin liquid (Shores *et al.*, JACS **127**, 13462 (2005)).
- part of a family with tunable properties

Topic 1: Barlowite $Cu_4(OH)_6FBr$

Topic 2: Ga-Herbertsmithite

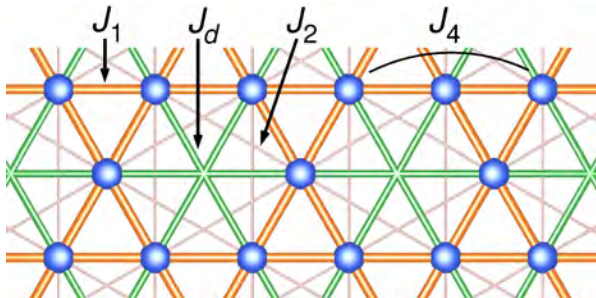
Herbertsmithite and kapellasite: different kagome systems



- same stoichiometry $\text{ZnCu}_3(\text{OH})_6\text{Cl}_2$
- different Zn positions, different stacking
- ➔ very different properties!

H. O. Jeschke, F. Salvat-Pujol, R. Valentí,
Phys. Rev. B **88**, 075106 (2013).

Kapellasite as test case: competing interactions

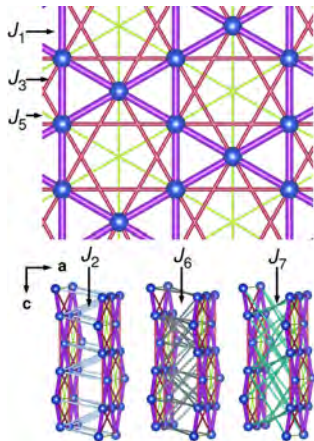


name	d_{Cu-Cu}	type	J_i (K)
			$U = 6$ eV
J_1	3.15	kagome nn	-14.2
J_2	5.45596	kagome 2nd nn	-0.7
J_4	6.3	kagome 3rd nn	-0.3
J_d	6.3	kagome 3rd nn	24.0

- Janson *et al.*, PRL **101**, 106403 (2008) values $J_1 = 29$ K and $J_d = 10$ K in **contrast** to experiment Fåk *et al.*, PRL **109**, 037208 (2012).
- Latest exp./series expansion yields $J_1 = -12$ K, $J_2 = -4$ K, $J_d = 15.6$ K (Bernu *et al.*, Phys. Rev. B **87**, 155107 (2013)).

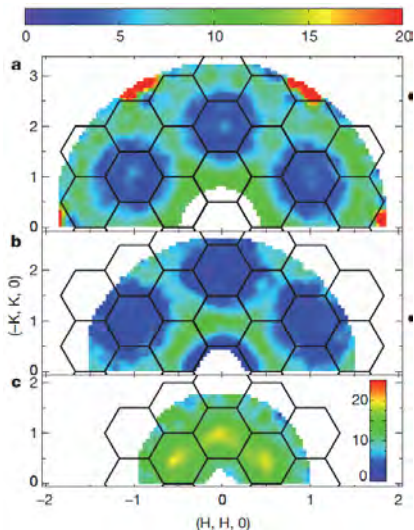
Herbertsmithite: beyond simple kagome antiferromagnet

name	d_{Cu-Cu}	type	J_i (K) $U = 6 \text{ eV}$
kagome layer couplings			
J_1	3.4171	kagome nn	182.4
J_3	5.91859	kagome 2nd nn	3.4
J_5	6.8342	kagome 3rd nn	-0.4
interlayer couplings			
J_2	5.07638	interlayer 1st nn	5.3
J_4	6.11933	interlayer 2nd nn	-1.5
J_6	7.00876	interlayer 3rd nn	-6.4
J_7	8.51328	interlayer 4th nn	3.0
J_9	9.17347	interlayer 6th nn	2.5

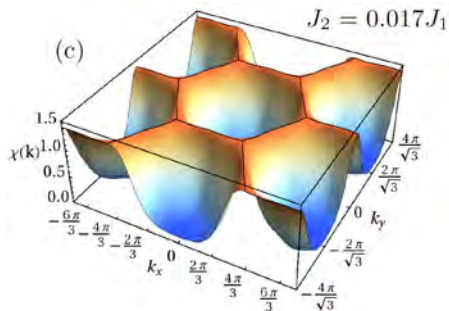


- J_1 agrees very well with literature values ($\sim 190 \text{ K}$)
- new aspects: (i) inplane $J_3/J_1 = 0.019$, and (ii) interplane couplings

Jeschke, Salvat-Pujol, Valentí, Phys. Rev. B **88**, 075106 (2013).

Herbertsmithite: J_3/J_1 ratio

Han *et al.*, Nature **492**, 406 (2012).



Suttner *et al.*, PRB **89**, 020408(R) (2014).

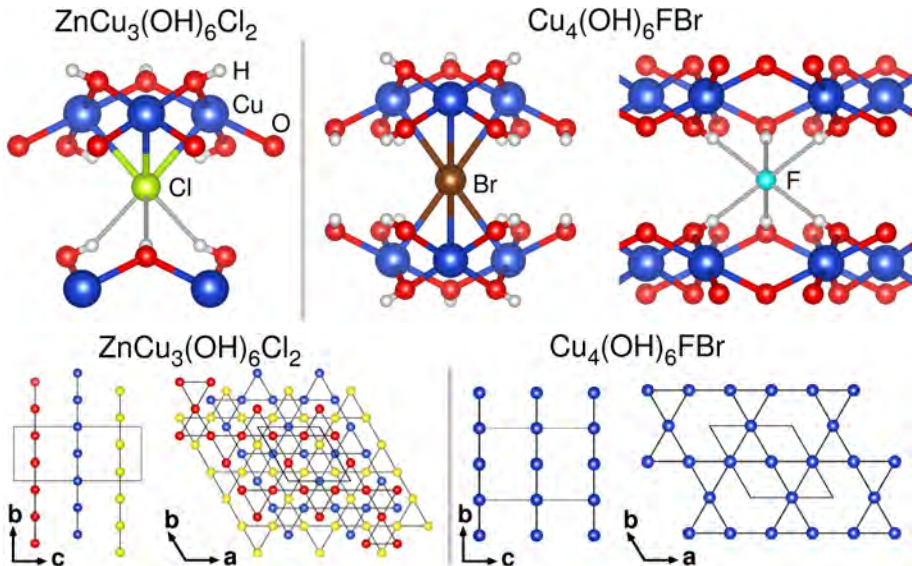
- our result: $J_3/J_1 = 0.019$
- Functional renormalization group (Suttner *et al.*, PRB **89**, 020408(R) (2014)) needs $J_3/J_1 = 0.017$ to explain inelastic neutron scattering experiment Han *et al.*, Nature **492**, 406 (2012).

Herbertsmithite summary

- Heisenberg Hamiltonians for herbertsmithite and other kagome systems
- DFT yields insight into subleading couplings
- Role of corrections to perfect kagome Hamiltonian needs to be worked out using manybody techniques
- Role of Zn/Cu disorder? (a) diluted kagome, and (b) interplane Cu?
- Potential for materials design:
 - 1 Can we have a **disorder free kagome system**?
 - 2 Can we **electron dope the kagome layer**?

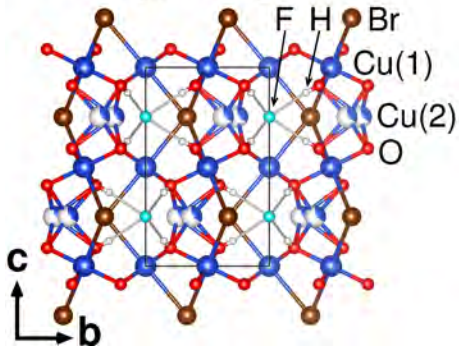
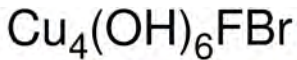
Improving on herbertsmithite: A road towards new spin liquids?

Barlowite: fixing the halogen environment



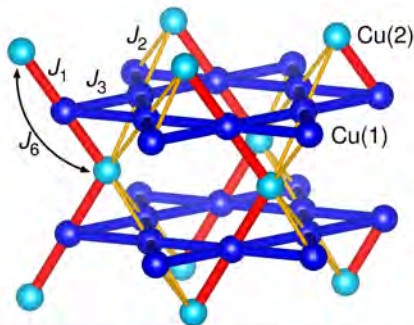
Jeschke, Salvat-Pujol, Jeschke, Gati, Hoang, Wolf, Lang, Schlueter, Valentí, arXiv:1412.4668

Barlowite: Structure and exchange couplings



Cavity at Cu(2) site: room for large nonmagnetic metal ion

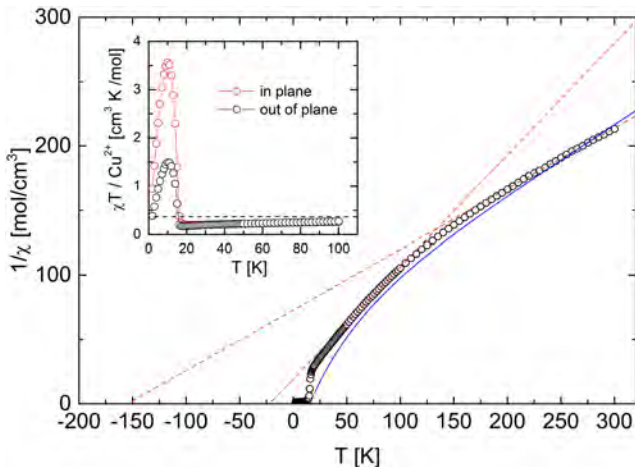
All electron full potential local orbital (FPLO) calculation of spin configurations



antiferromagnetic kagome: $J_3=178$ K
ferromagnetic interplane: $J_1=-205$ K

Jeschke, Salvat-Pujol, Jeschke, Gati, Hoang, Wolf, Lang, Schlueter, Valentí, arXiv:1412.4668

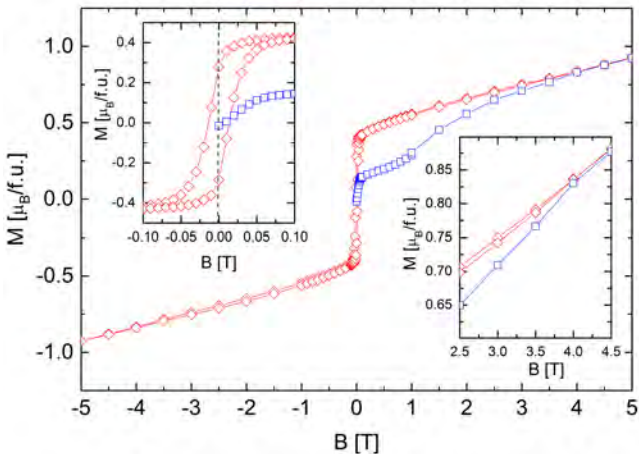
Barlowite: Magnetic properties



Circles: Single crystal inverse molar susceptibility (at $B = 0.1 \text{ T}$, $B \parallel c$).

Blue: high temperature series expansion (10th order code written by Lohmann *et al.*, PRB **89**, 014415 (2014)).

Barlowite: Evidence for canted antiferromagnetism



Magnetization as function of magnetic field at $T = 2$ K. Remanent magnetization of $0.3 \mu_B/f.u.$ indicates **canted antiferromagnet** with 4.5° canting angle. DM coupling estimate: $|\mathbf{D}|/J_3 \approx \Delta g/g = 0.1$.

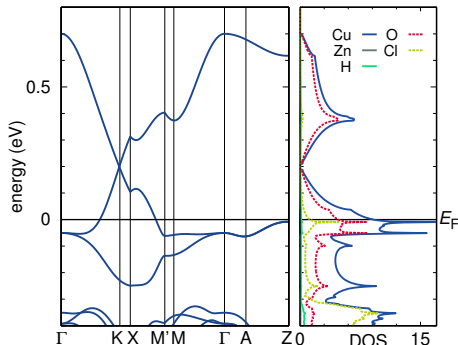
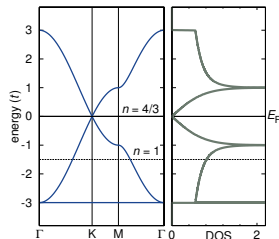
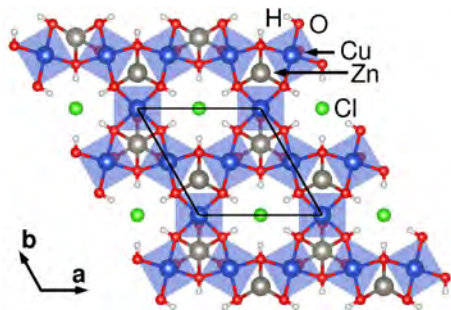
Barlowite conclusions

- Crystallization of barlowite $\text{Cu}_4(\text{OH})_6\text{FBr}$ leads to a perfect kagome lattice system
- Replacement of Cu(2) in large cavity as design path for new spin liquid compounds
- Material promises to have less disorder problems than herbertsmithite

Jeschke, Salvat-Pujol, Jeschke, Gati, Hoang, Wolf, Lang, Schlueter, Valentí, arXiv:1412.4668

Doping the spin liquid:
Theoretical prediction of a strongly correlated
Dirac metal

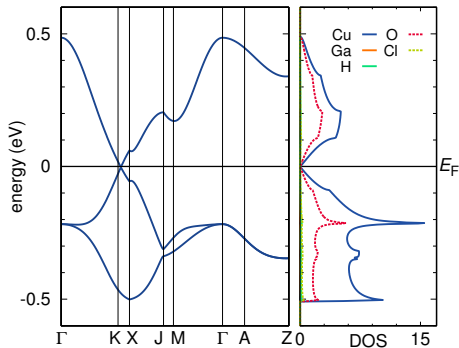
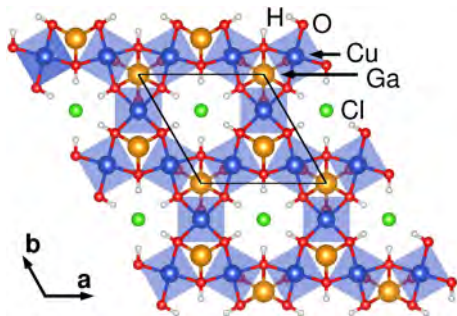
How about electron doping Herbertsmithite?



- $\text{ZnCu}_3(\text{OH})_6\text{Cl}_2$ at half filling of Cu $3d_{x^2-y^2}$ bands
- Doping to 4/3 filling to reach Dirac point?
- $\text{Zn}^{2+} \rightarrow$ some M^{3+} ion?

Mazin, Jeschke, Lechermann, Lee, Fink, Thomale, Valentí, Nature Commun. **5**, 4261 (2014).

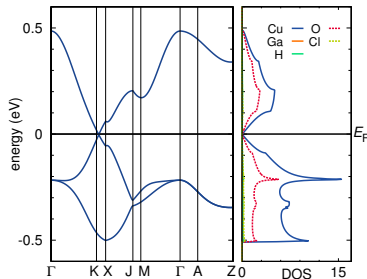
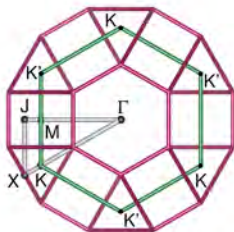
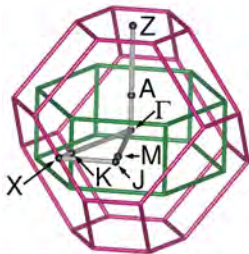
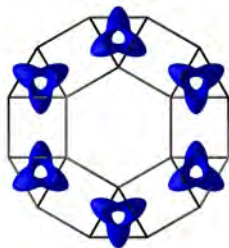
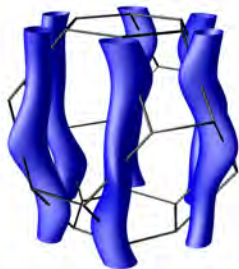
Ga-Herbertsmithite: a Dirac metal?



- $\text{GaCu}_3(\text{OH})_6\text{Cl}_2$ predicted using projector augmented wave basis (VASP) relaxation; tested for dynamical stability
- Filling is $4/3$!
- DFT electronic structure shows Dirac points exactly at the Fermi level

Mazin, Jeschke, Lechermann, Lee, Fink, Thomale, Valentí, Nature Commun. **5**, 4261 (2014).

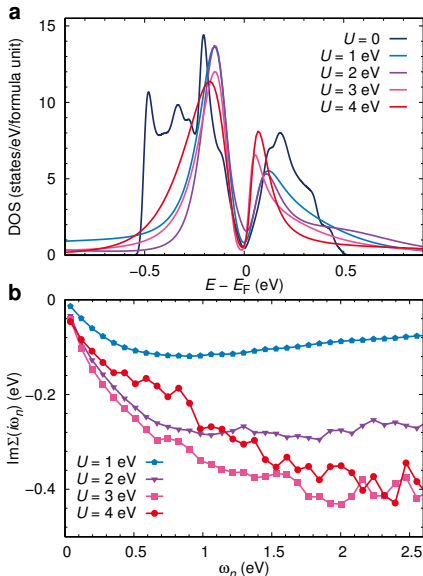
Ga-Herbertsmithite Fermi surface



- Fermi surface at $E = -60 \text{ meV}$
- Dirac points at E_F twist around K point
- rhombohedral $R\bar{3}m$ space group

→ Need to check stability of metallic state!

Mott-Hubbard instability? Dynamical cluster approximation



Dynamical mean field theory test for instability against large onsite interaction U

$$\mathcal{H} = \mathcal{H}_0 + \mathcal{H}_{\text{int}}$$

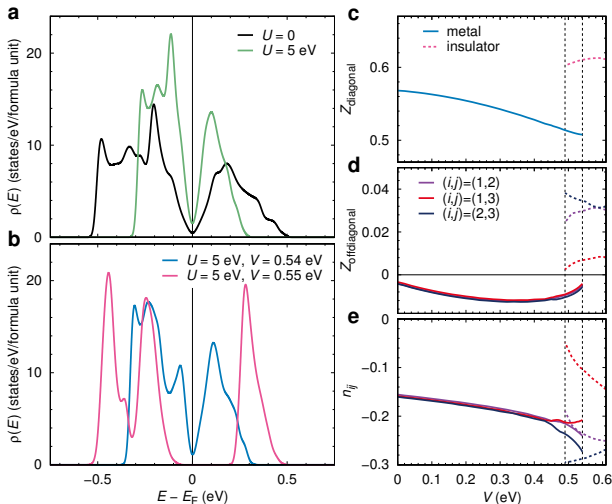
$$\mathcal{H}_0 = \sum_{i,j} \sum_{\sigma} t_{ij} c_{i,\sigma}^{\dagger} c_{j,\sigma} + \mu \sum_{i,\sigma} c_{i,\sigma}^{\dagger} c_{i,\sigma}$$

$$\mathcal{H}_{\text{int}} = U \sum_i n_{i,\uparrow} n_{i,\downarrow} + \frac{V}{2} \sum_{\langle i,j \rangle} \sum_{\sigma,\sigma'} n_{i,\sigma} n_{j,\sigma'}$$

- DCA solved with interaction expansion continuous time QMC impurity solver
- cluster size $N_c = 3$, $T = 150$ K
- system remains metallic for all U values

Mazin, Jeschke, Lechermann, Lee, Fink, Thomale, Valentí, Nature Commun. **5**, 4261 (2014).

Mott-Hubbard instability? Rotationally invariant slave boson approximation



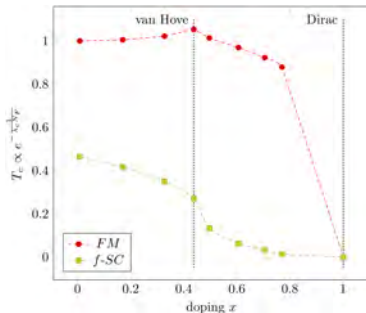
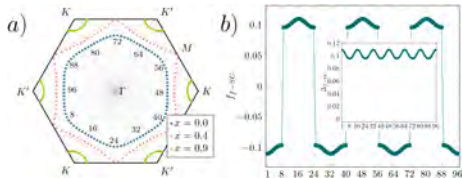
- LMTO estimate of $U = 5 - 7$ eV; Thomas-Fermi theory estimate of $V = 0.11$ eV for $\text{GaCu}_3(\text{OH})_6\text{Cl}_2$.
- Strongly correlated Dirac metal stable up to $V \approx 0.48$ eV
- Instability to charge order at large V

Robust metallic state!

Mazin, Jeschke, Lechermann, Lee, Fink, Thomale, Valentí, Nature Commun. **5**, 4261 (2014).

Possible ferromagnetic and superconducting instabilities

- $\text{GaCu}_3(\text{OH})_6\text{Cl}_2$ is far from the regime of Nagaoka ferromagnetism
- DFT sees tendency to ferromagnetism
- DCA(RISB) stabilizes FM state for $n > 4/3$
- weak coupling functional renormalization group (fRG) for effective 2D Hamiltonian sees FM instability at all n
- fRG predicts a nodeless f -wave superconducting ground state



Mazin, Jeschke, Lechermann, Lee, Fink, Thomale, Valentí, Nature Commun. **5**, 4261 (2014).

Electron doped herbertsmithite conclusions

- Electron doped herbertsmithite ($\text{Zn}_{1-x}\text{Ga}_x\text{Cu}_3(\text{OH})_6\text{Cl}_2$) would interpolate between frustrated magnetism at $x = 0$ and a strongly correlated Dirac metal at $x = 1$
- Solid solution at finite x and near $x = 1$ promises phases with unconventional physics like f -wave superconductivity
- Challenge to solid state chemists and crystal growers
- There is hope for more unusual compounds in the paratacamite family of materials

Mazin, Jeschke, Lechermann, Lee, Fink, Thomale, Valentí, Nature Commun. **5**, 4261 (2014).