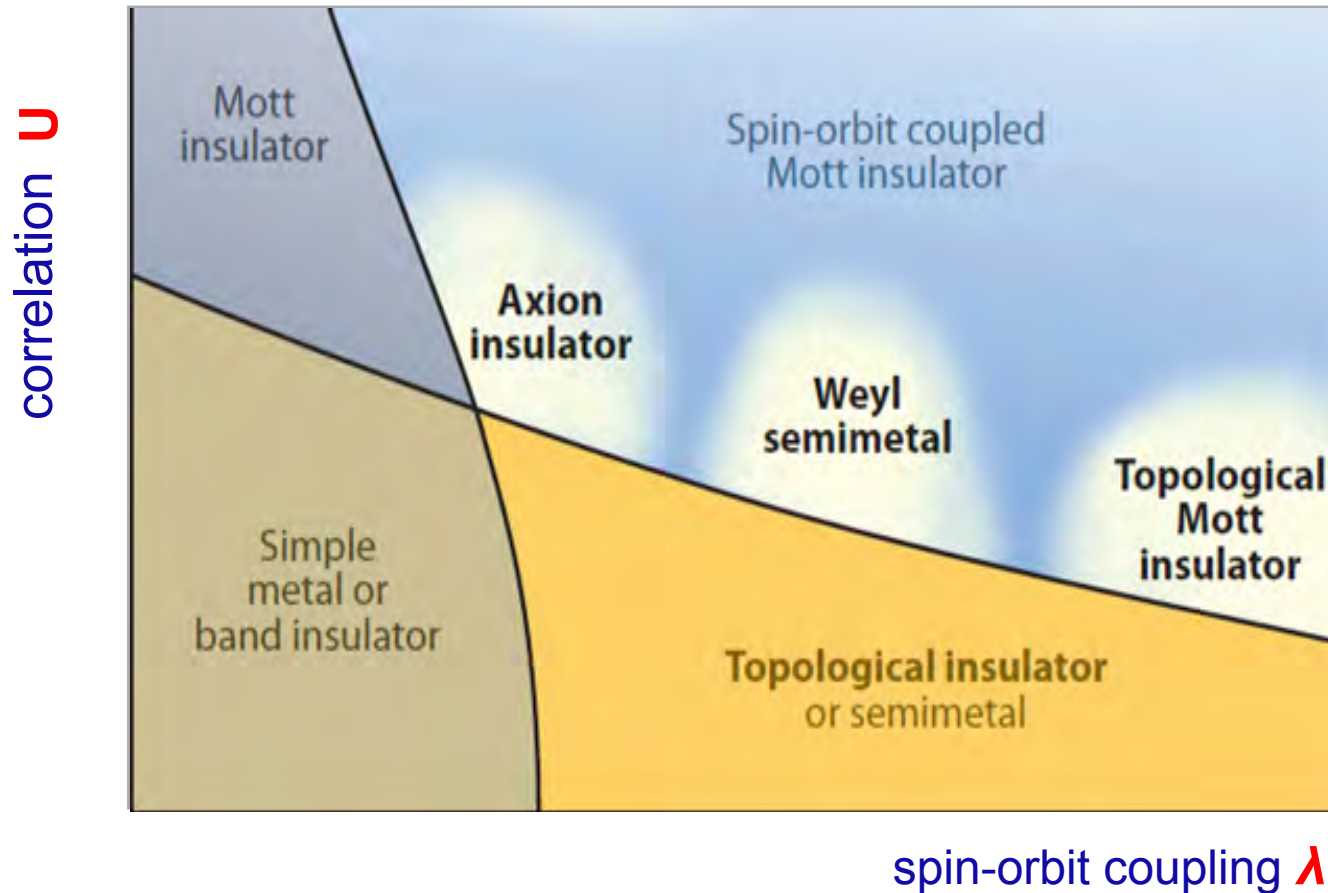


Magnetism and doping effects in spin-orbit coupled Mott insulators

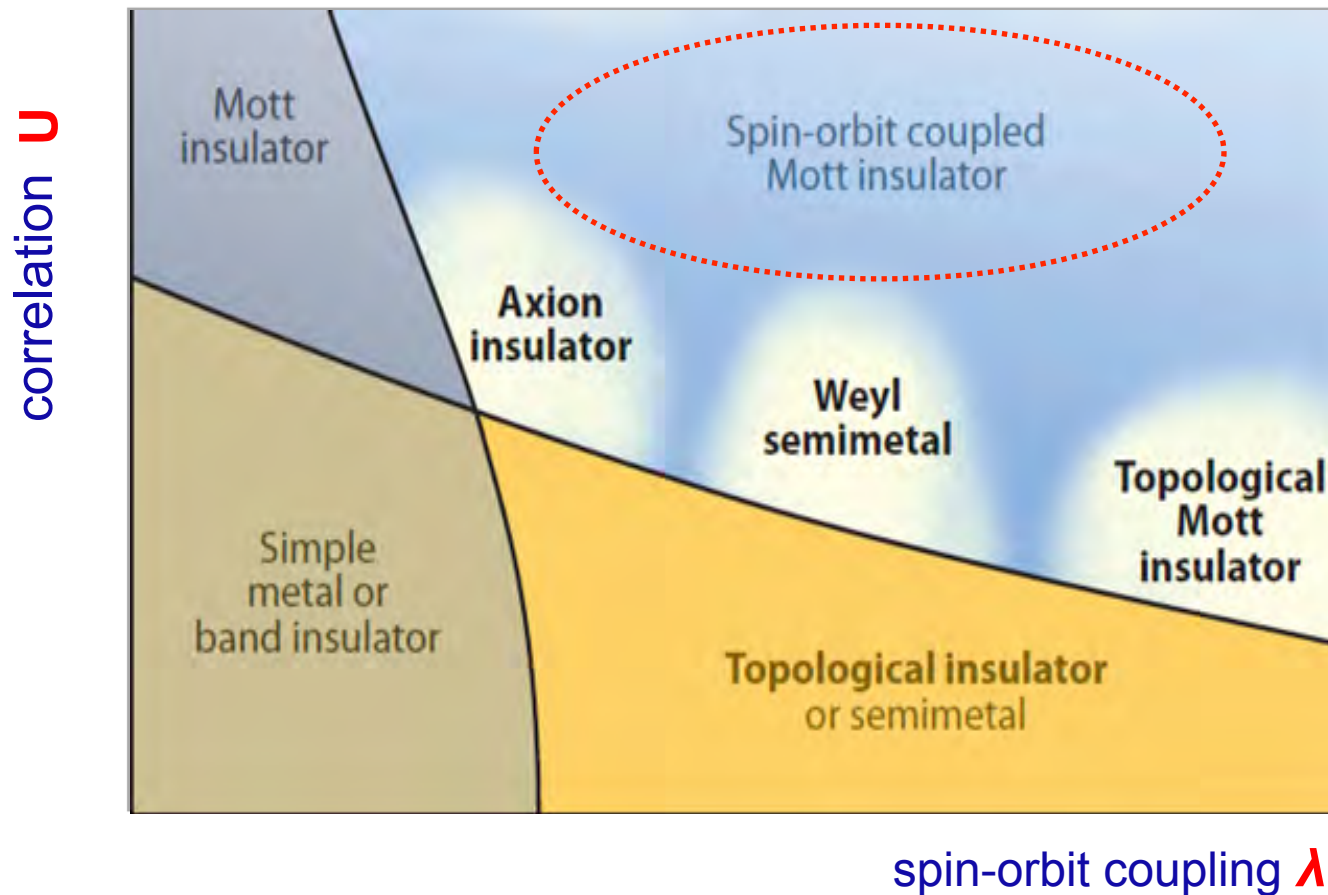
Giniyat Khaliullin

Max Planck Institute for Solid State Research, Stuttgart

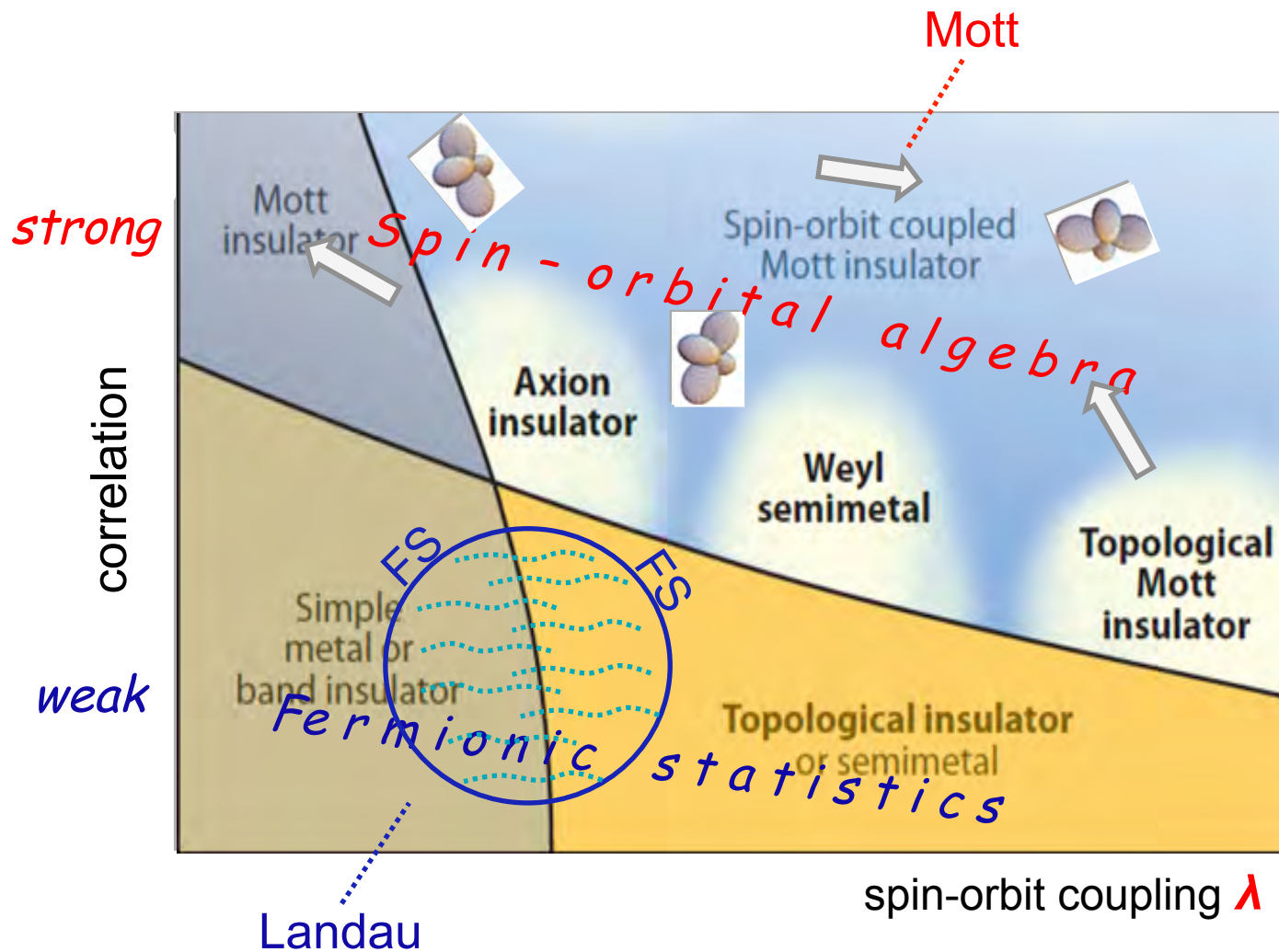
Hubbard model with spin-orbit coupling:
unconventional magnets, insulators, metals



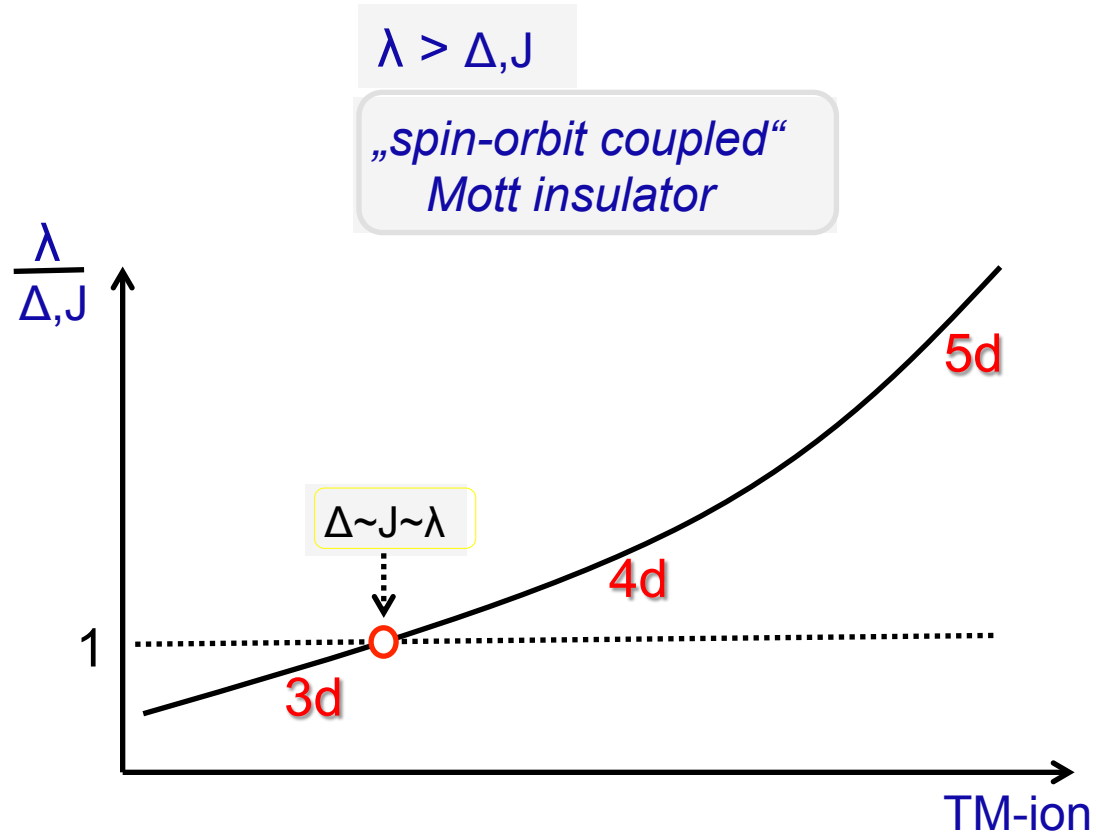
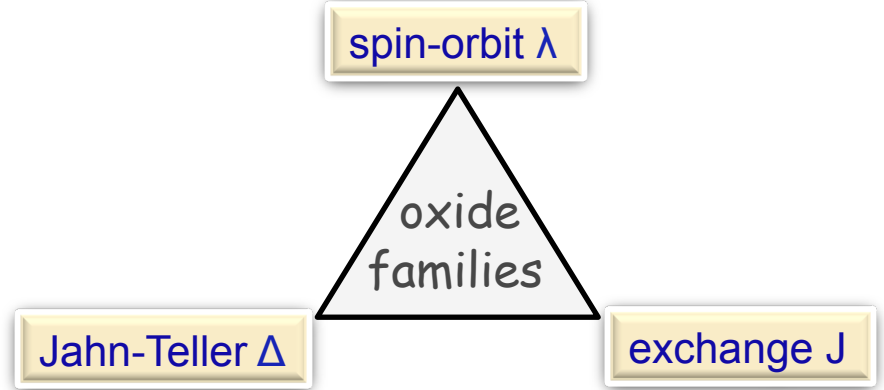
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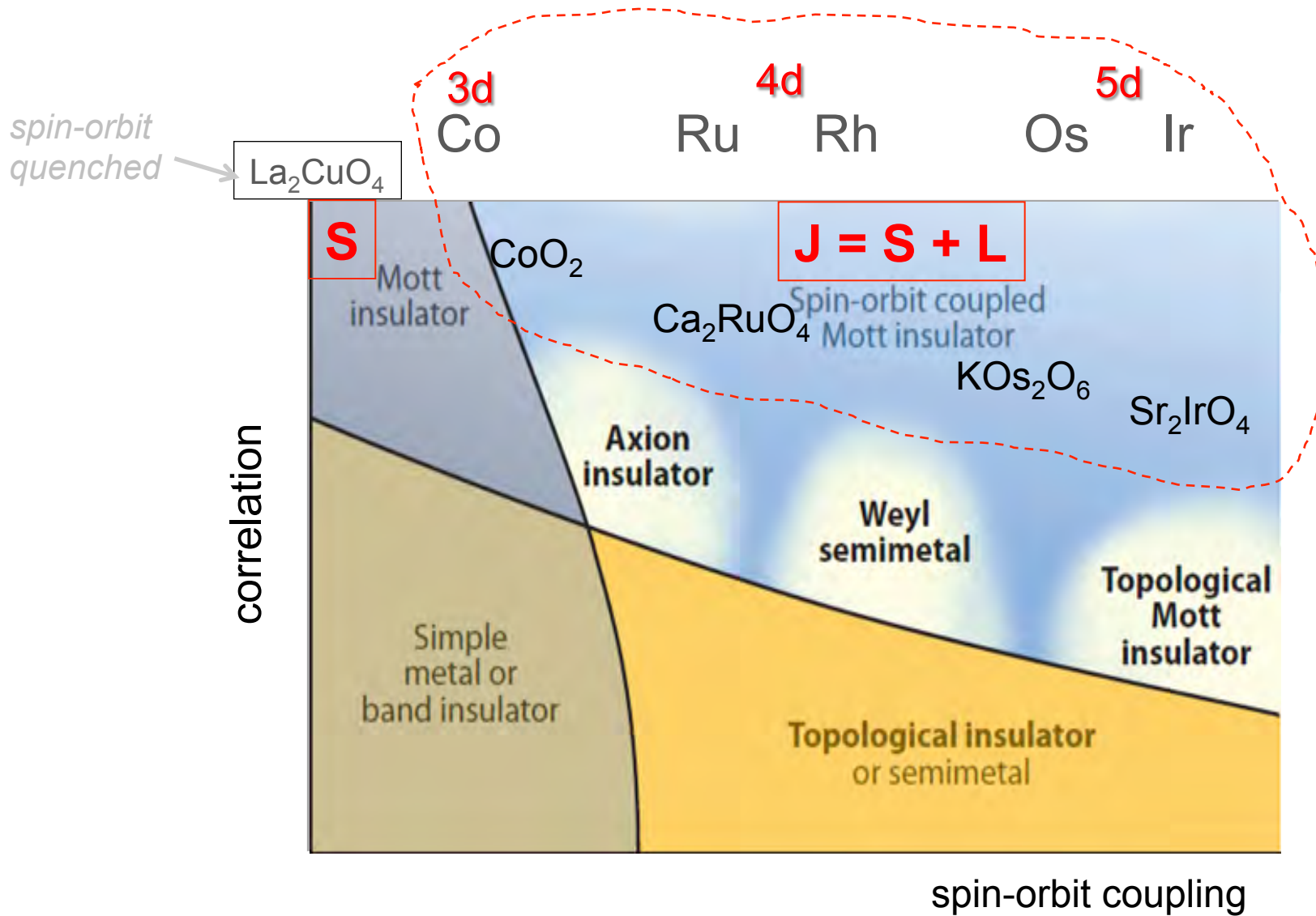
Ionic multiplets vs Fermionic bands



Three competitors:



Spin-orbit coupled Mott insulators



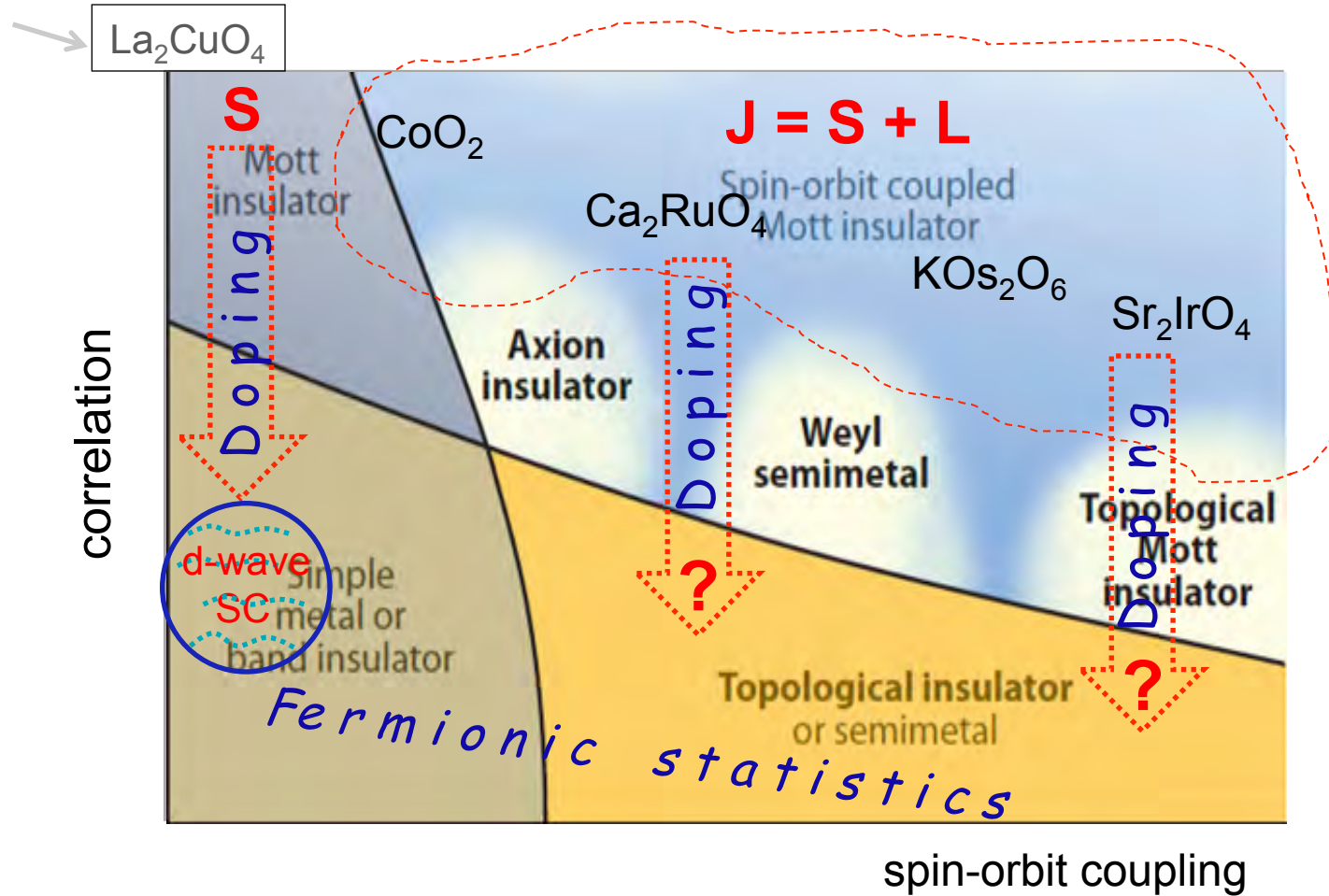
„unconventional“ J-magnetism

D O P I N G:



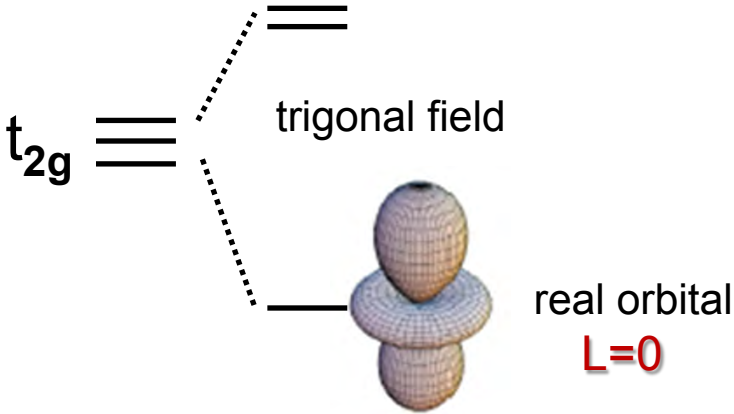
„unconventional“ metal & SC?

spin-orbit quenched



Lifting the orbital degeneracy

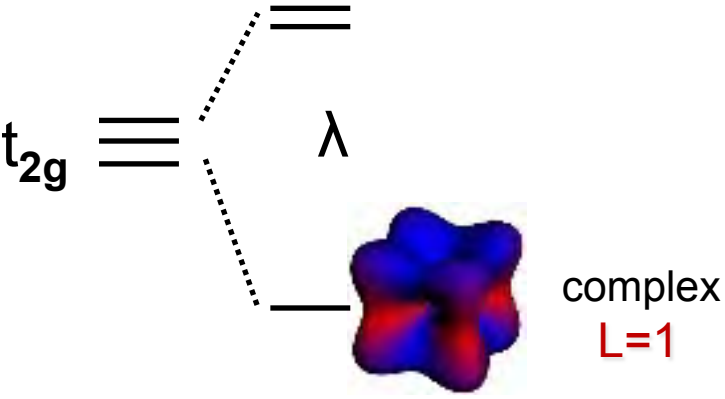
Jahn-Teller



$$|xy + yz + zx\rangle \times |\uparrow\uparrow\rangle$$

quadrupole spin

Spin-orbit



$$|xy \uparrow\rangle + |yz \downarrow\rangle + i|zx \downarrow\rangle$$

pseudospin $J=S+L$

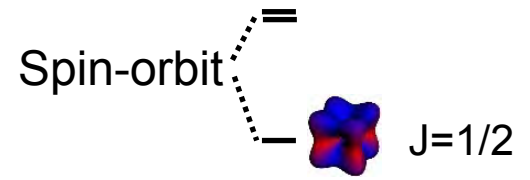
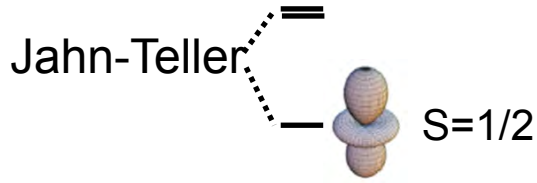


spin \Rightarrow
 $g=2$

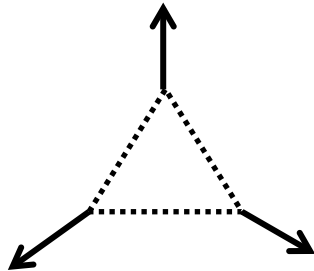
Spin $\frac{1}{2}$ algebra

\Leftarrow pseudospin
 $g=-2$

Magnetism

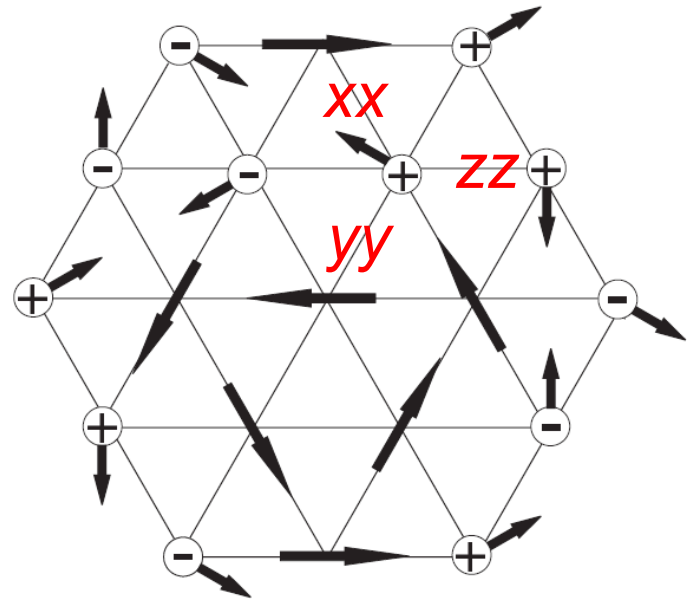


$$H = (SS)$$



*coplanar,
single-Q*

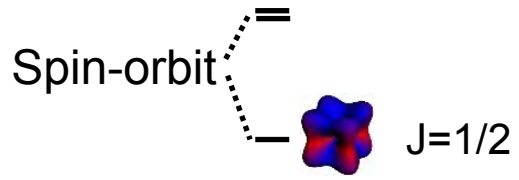
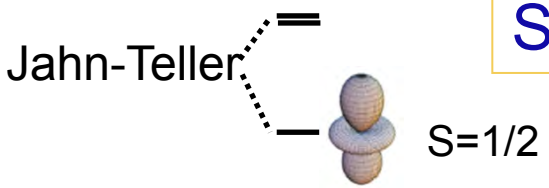
$$H = - (SS) + ISING(\alpha)$$



*large magnetic unit cell
non-coplanar, multi-Q
hosts spin vortex*

GKh (PTPS, 2005)

SC pairing



**Spin-singlet
d-wave SC**

$|\uparrow\downarrow - \downarrow\uparrow\rangle$

Baskaran (2003)
Kumar, Shastry (2003)
Ogata (2003)
P. Lee et al. (2004)

**Pseudospin-triplet
p-wave SC**

$$\Delta_{tr} = \alpha_0 |\tilde{\uparrow}\tilde{\downarrow} + \tilde{\downarrow}\tilde{\uparrow}\rangle_j + \alpha_1 e^{i\varphi_{ij}} |\tilde{\uparrow}\tilde{\uparrow}\rangle_j + \alpha_2 e^{-i\varphi_{ij}} |\tilde{\downarrow}\tilde{\downarrow}\rangle_j$$

nondegenerate

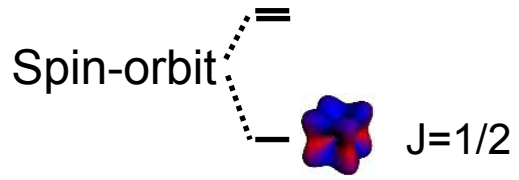
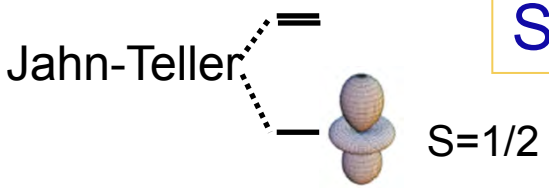
\vec{d} -vector pattern on FS:

$d_x, d_y, d_z \neq 0$

Knight-shift finite in all directions

GKh, Koshibae, Maekawa (PRL 2004)
GKh (PTPS, 2005)

SC pairing



**Spin-singlet
d-wave SC**

Baskaran (2003)
Kumar, Shastry (2003)
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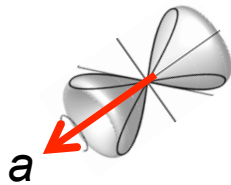
GKh, Koshibae, Maekawa (PRL 2004)
GKh (PTPS, 2005)

	3d	4d	5d
	Co ⁴⁺	Rh ⁴⁺	Ir ⁴⁺
λ :	80 meV	190 meV	380 meV



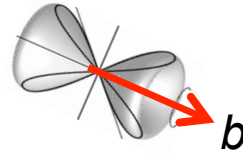
The origin of „unconventionality“: ORBITAL magnetism

Orbital moment **L** has a „shape“:



$$L_x=1$$

$$x(y+iz)$$



$$L_y=1$$

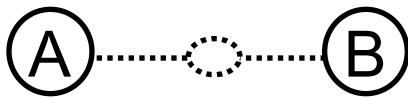
$$y(z+ix)$$



$$L_z=1$$

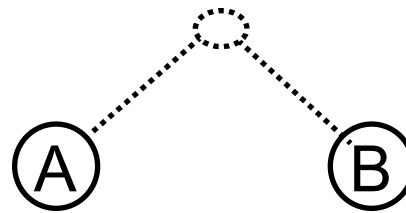
$$z(x+iy)$$

Hopping amplitude:



real

(inversion)



complex

(no inversion)



nontrivial band topology
Shitade *et al.* (2009)

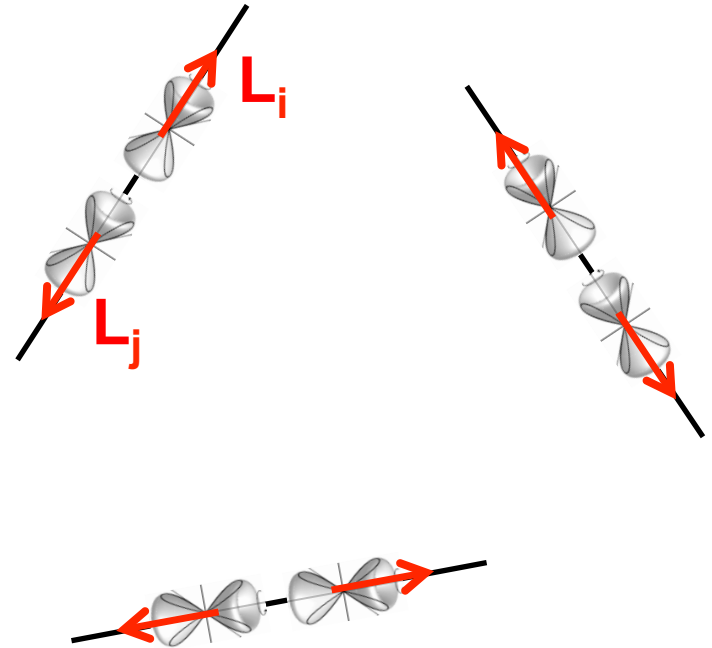
ORBITAL MAGNETISM

L-moment direction and chemical bonding:
one-to-one correspondence

L - moment
interactions:

anisotropic, bond-dependent

„orbital frustration“



non-Heisenberg models:
pseudodipolar, biquadratic...

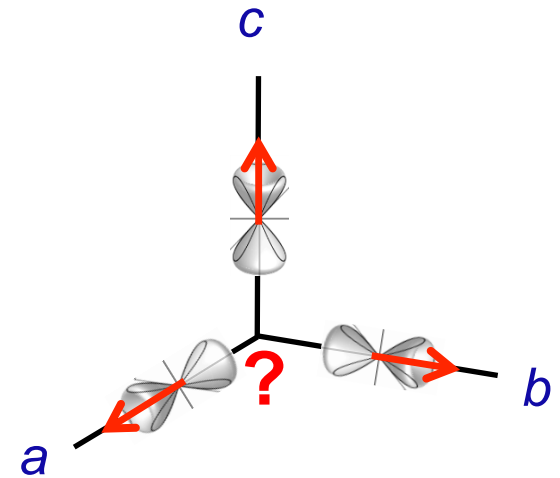
ORBITAL MAGNETISM

Orbital moment **L** interactions:

1) non-Heisenberg

2) bond-dependent

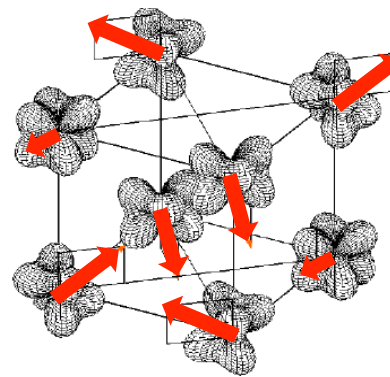
„orbital frustration“



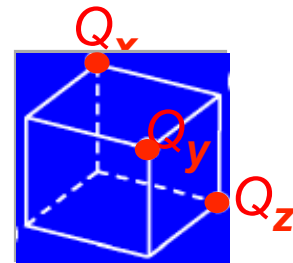
► Simple cubic lattice:

$$\mathcal{H}_{ij}^{(c)} = (L_i^x L_j^x)^2 + (L_i^y L_j^y)^2 + L_i^x L_i^y L_j^y L_j^x + L_i^y L_i^x L_j^x L_j^y$$

GKh & Okamoto (PRL 2002)

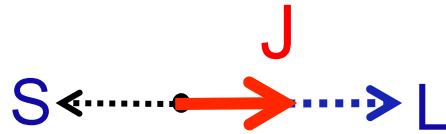


non-coplanar



multi-Q

no LRO at finite T



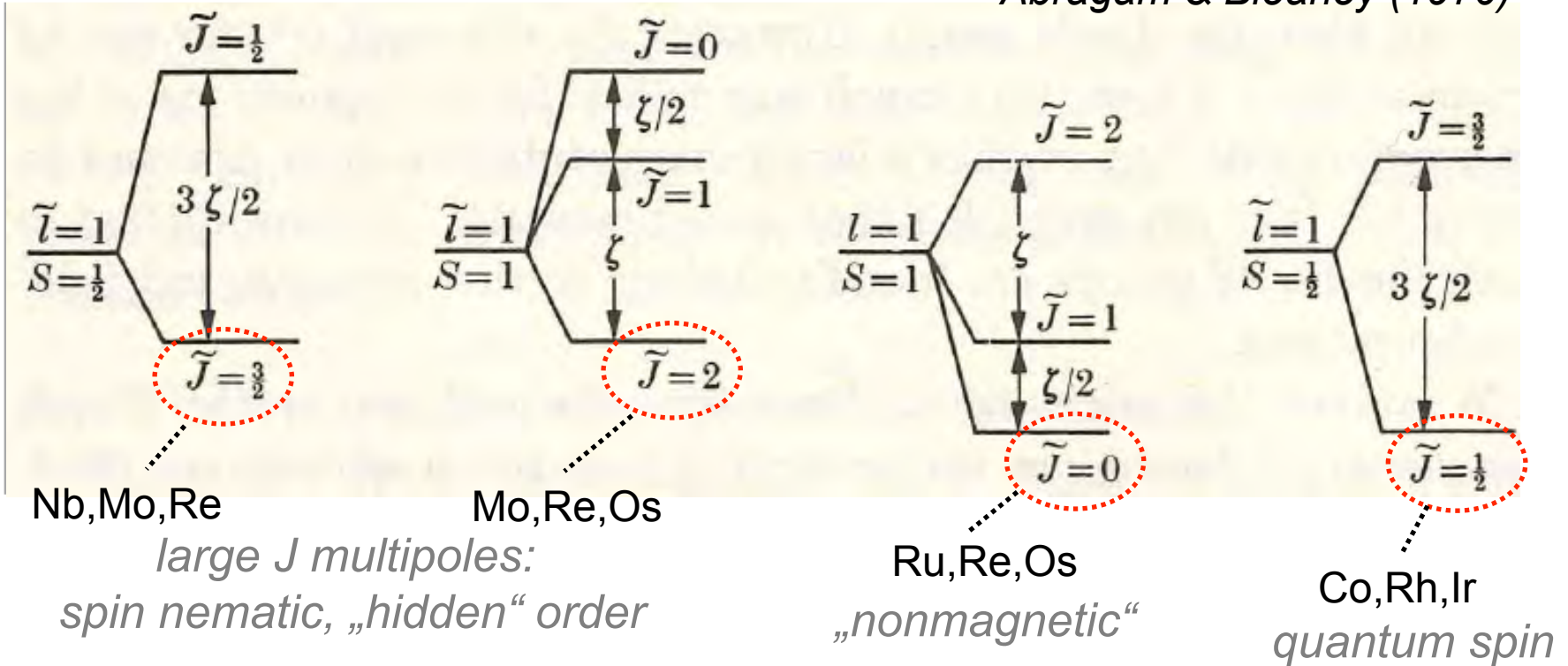
*Pseudospin $J=S+L$ inherits
bond-dependent and frustrated
nature of orbitals*



„unconventional“ magnetism

Spin-orbit multiplets of TM-ions

Abragam & Bleaney (1970)

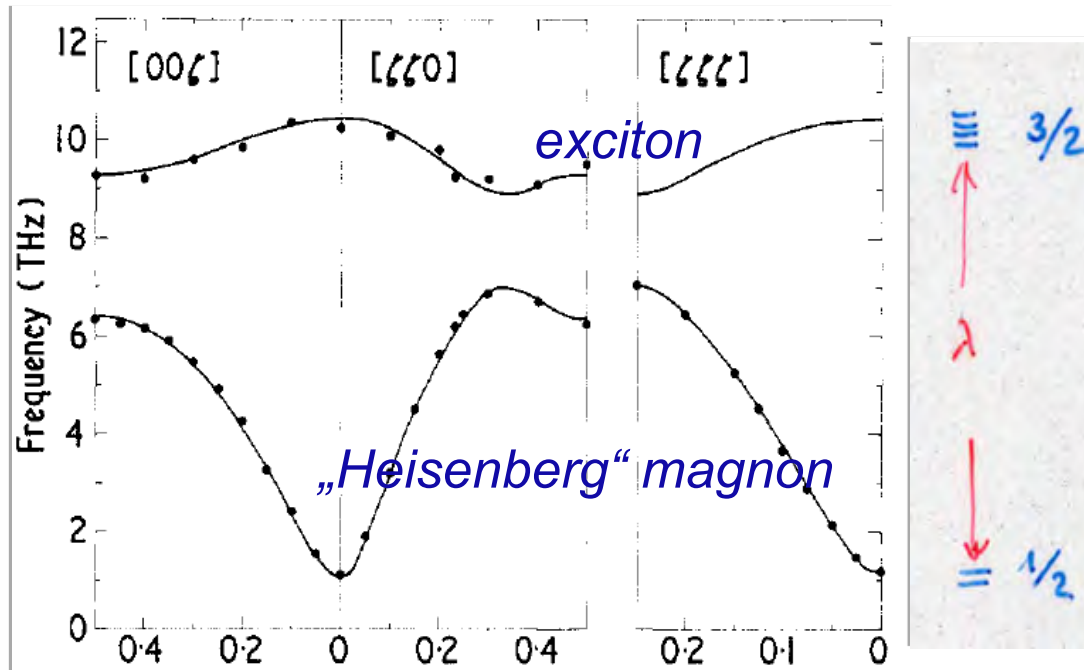


GS-degeneracy: „pseudospin“ \tilde{J}

Kramers: dipole, octupole, ...
non-Kramers: quadrupole, ...

The „old“ pseudospin $J=1/2$

3d Co-fluoride, neutron scattering



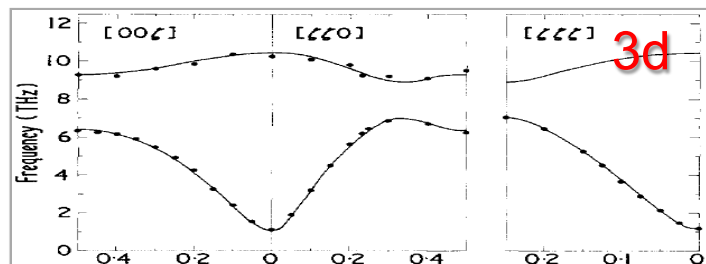
Holden et al. (1971)

$KCoF_3$
 $d^7, S=3/2, \tilde{L}=1$

Two branches split by spin-orbit:
magnon & exciton

from **3d** Co to **5d** Ir

B.J.Kim et al., ...



K_2CoF_3

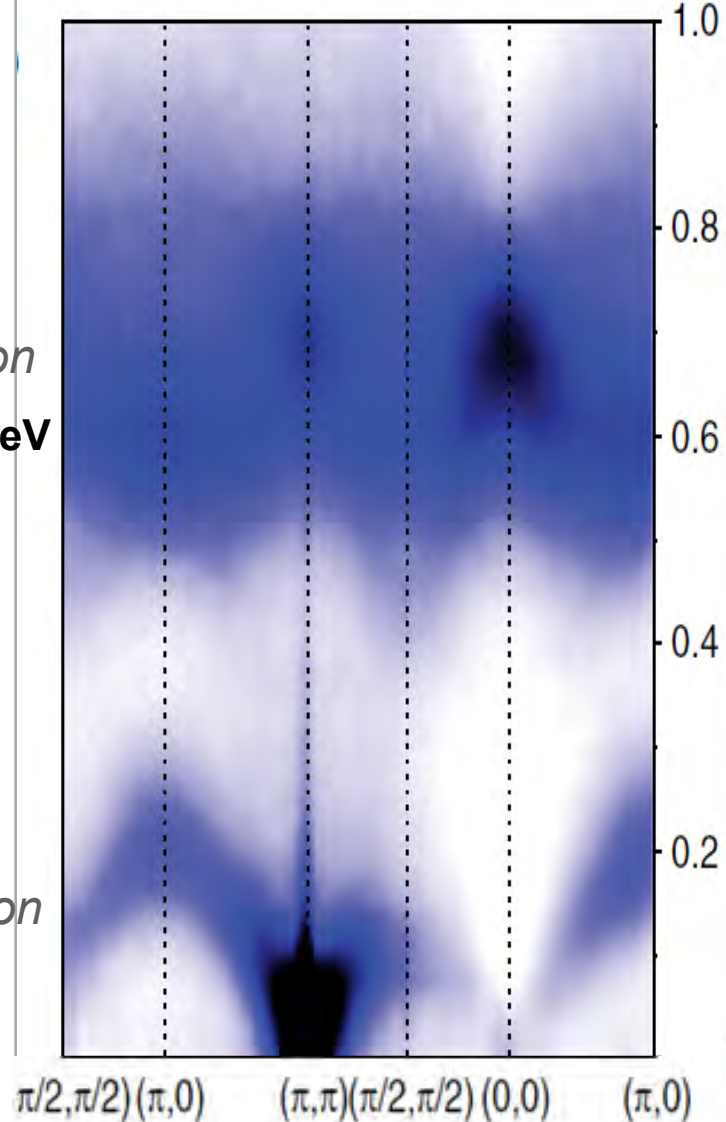
Holden et al. (1971)
neutron scattering

$\times 10$

5d 600 meV

Exciton

Magnon



Sr_2IrO_4

Kim et al. (2012)
RIXS data

spin one-half 2D Mott systems similar to cuprates ?

d^1

|
t_{2g} electron

Ti

...

d^5

|
t_{2g} hole

Co

...

d^7

|
e_g electron

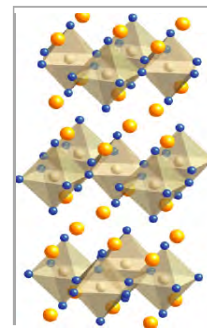
Ni

...

d^9

|
e_g hole

Cu



La₂CuO₄

J_{AF} = 130 meV

spin one-half 2D Mott systems similar to cuprates

d^1

t_{2g} electron

d^5

t_{2g} hole

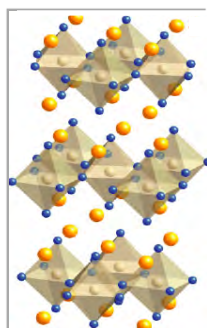
d^7

e_g electron

d^9

e_g hole

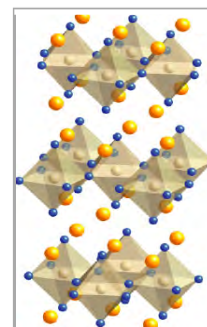
Ir



Sr_2IrO_4

$T_N \sim 240$ K

Cu



La_2CuO_4

$J_{AF} = 130$ meV

$T_N \sim 320$ K

Cuprate-like magnetism and SC?

(Cava, Cao, ... 1990's)

„...apart from cuprates, Sr_2IrO_4 would be the second $S=1/2$ 2D AF “

spin one-half 2D Mott systems similar to cuprates

d^1

t_{2g} electron

d^5

t_{2g} hole

d^7

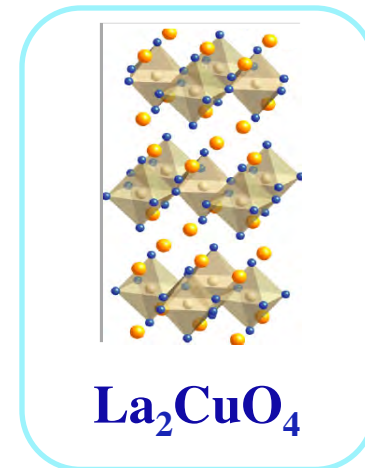
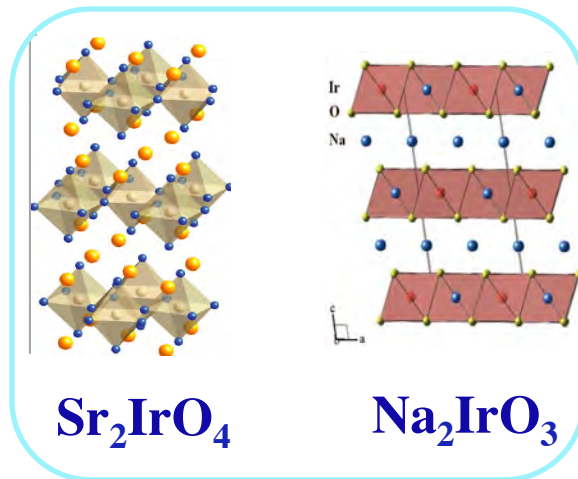
e_g electron

d^9

e_g hole

Ir

Cu



t_{2g}
spin-orbit coupling

different orbitals

e_g

$J=1/2$ magnetism in iridates: *basic theory*

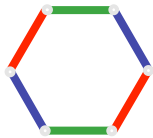
Jackeli, GKh (2009)

Chaloupka, Jackeli, GKh (2010, 2013)

Two-parameter Hamiltonian = Ising^(x,y,z) + Heisenberg:

$$\mathcal{H}_{ij}^{(\gamma)} = 2K S_i^\gamma S_j^\gamma + J \mathbf{S}_i \cdot \mathbf{S}_j$$

dominant in 90-bonding
(honeycomb Na_2IrO_3)



= *Kitaev model* (2006)



„Majorana world“ ?

dominant in 180-bonding
(Sr_2IrO_4 perovskite)



= „*cuprate*“ model



high- T_c SC ?

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„Majorana world“ ?

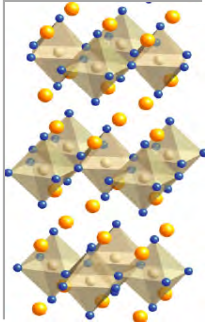
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= „*cuprate*“ model



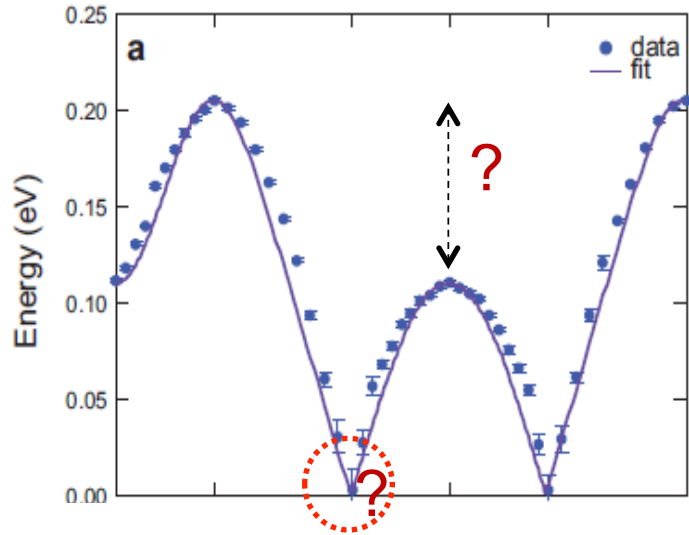
high-T_c SC ?



Sr₂IrO₄

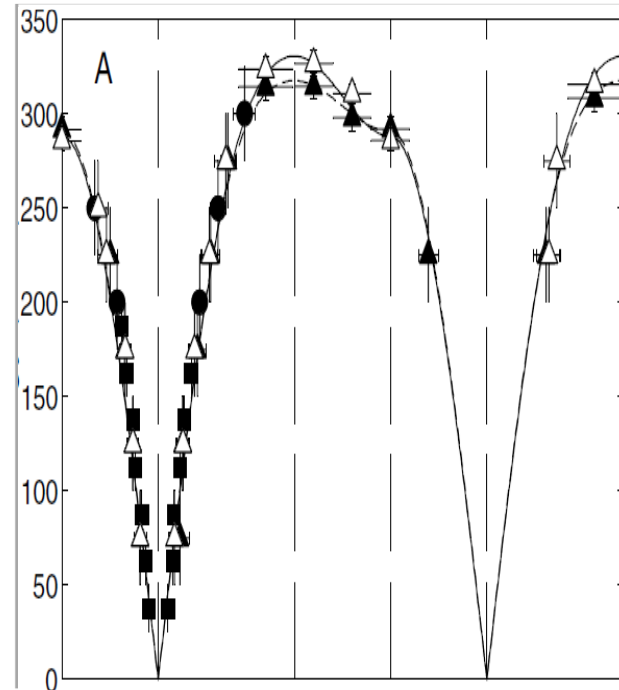
Pseudospin 1/2 in perovskites:

-theory predicts
„nearly“ Heisenberg AF



Sr₂IrO₄
T_N~240 K

Kim et al.(2012)



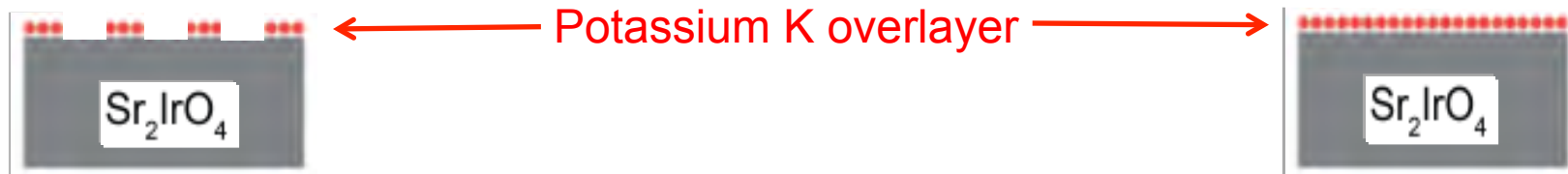
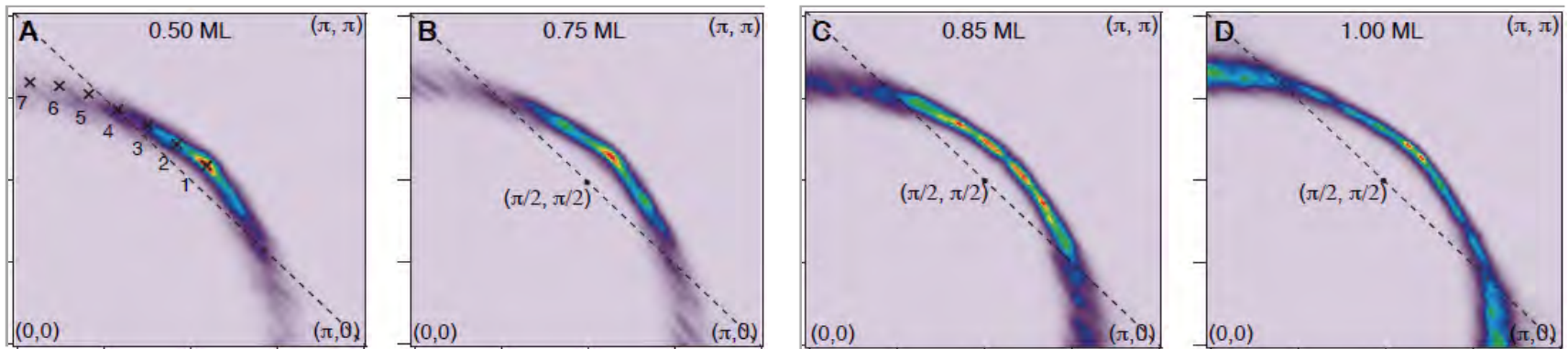
La₂CuO₄
T_N~320 K

Coldea et al.(2001)

Fermiology of electron doped Sr_2IrO_4

„Fermi-arcs“ at low doping

„normal“ FS

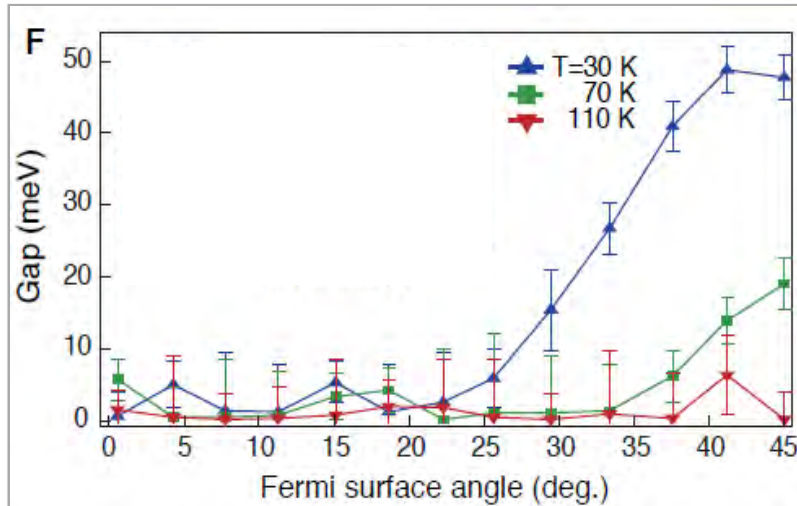
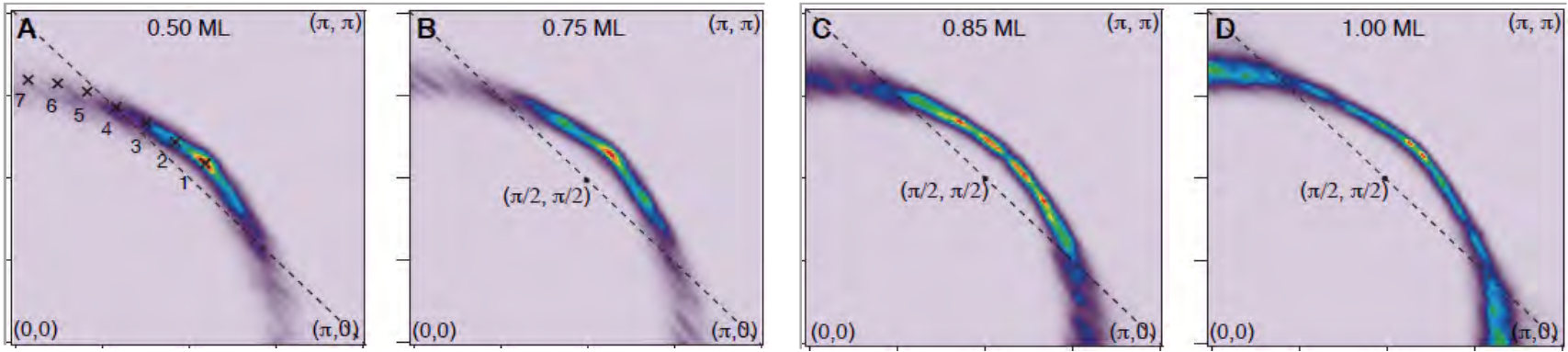


B.J. Kim *et al.* (Science 2014)

T-dependent „pseudogap“ in Sr₂IrO₄

„Fermi-arcs“ at low doping

„normal“ FS



Pseudogap opens at low T

many-body effect !

...and closes at 110 K

Sr_2IrO_4 magnetism, fermiology & lattice: *same as in* La_2CuO_4



superconductivity?

YES

SUPER!
GREAT!

NO

.....find 10 differences..."

Sr_2IrO_4



La_2CuO_4



YES or NO? -- no definite answer yet...

$J=1/2$ magnetism in iridates: *basic theory*

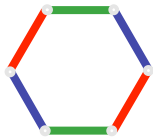
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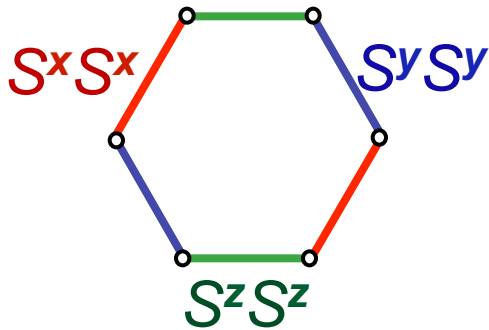


= „cuprate“ model

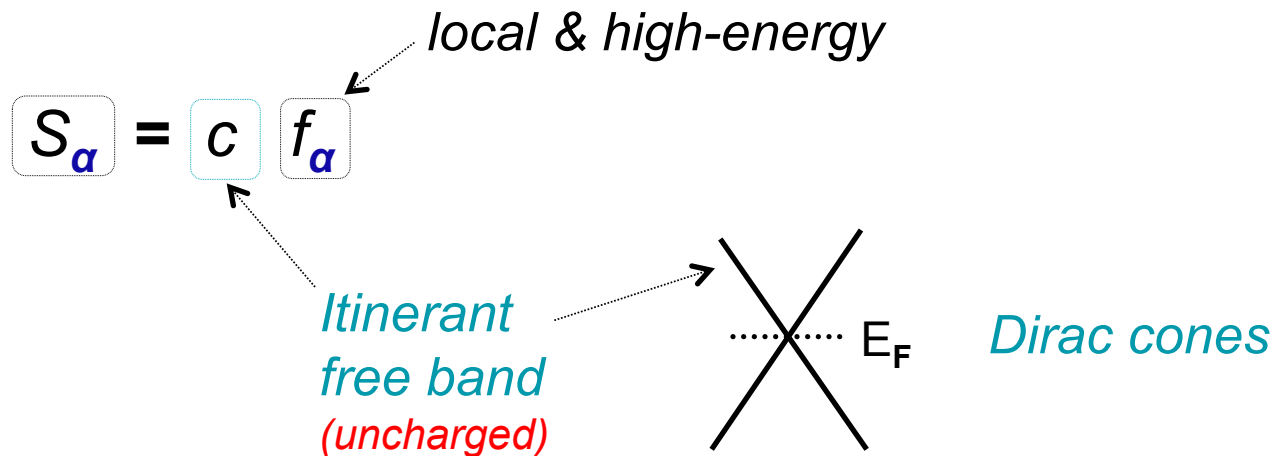


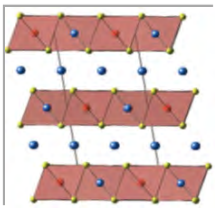
high- T_c SC ?

The Kitaev model



- Exactly solvable
- Short-range RVB, large spin gap
- Low-energy excitations: free Majorana fermions





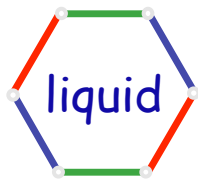
Na₂IrO₃

Honeycomb lattice:

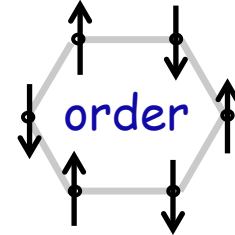
-- *Kitaev term is dominant*
but J is present as well

$$\mathcal{H}_{ij}^{(\gamma)} = 2K S_i^\gamma S_j^\gamma + J \mathbf{S}_i \cdot \mathbf{S}_j$$

Kitaev model

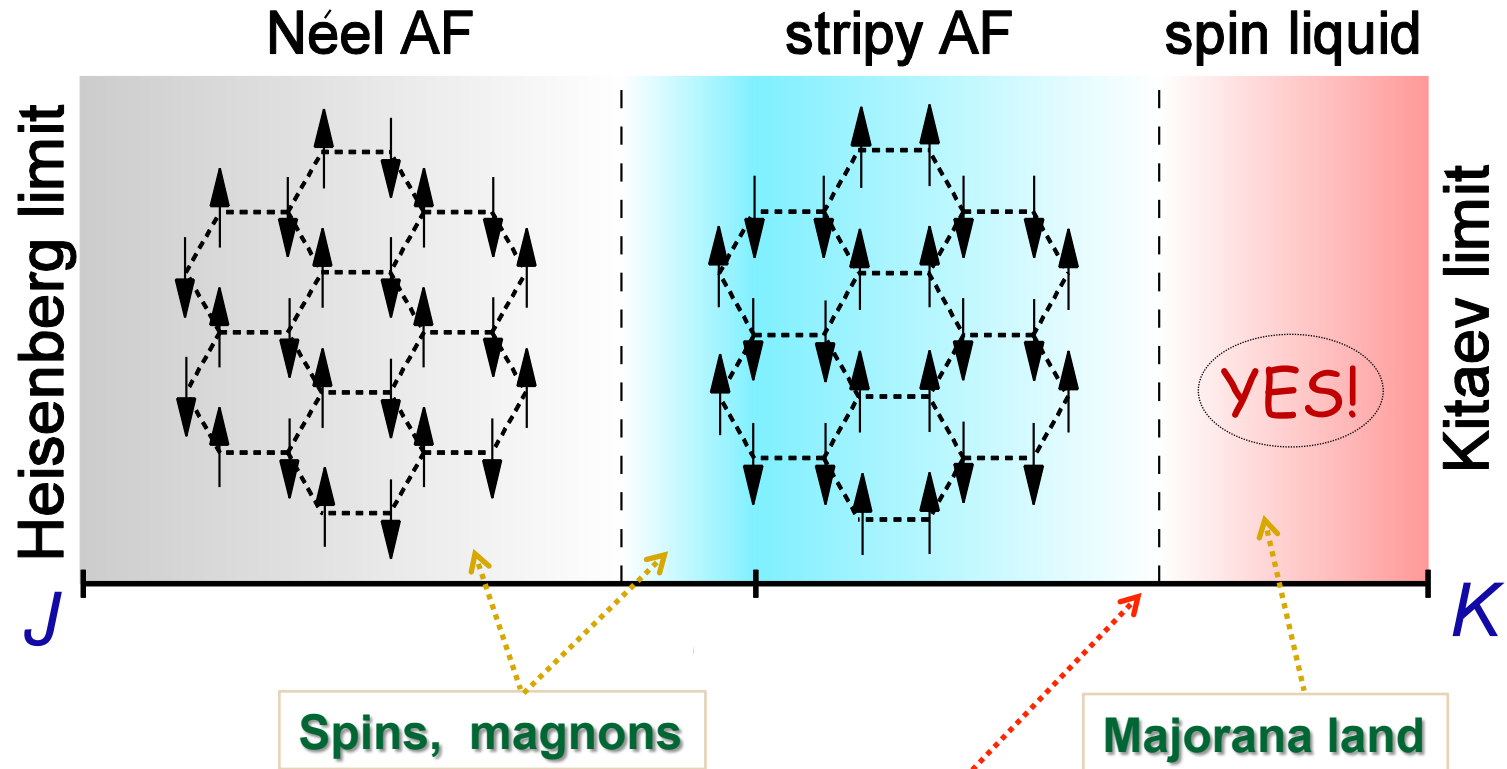
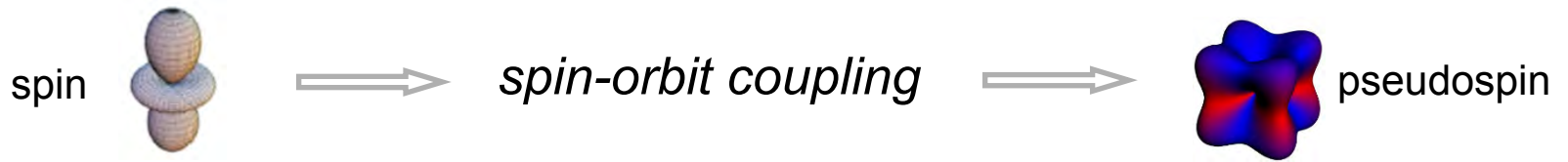


Heisenberg model



What is in between ?

-If „some liquid“ is still left ?



*Quantum phase transition:
spin fractionalization*

real world: Na_2IrO_3



Exp. data

AM order $T_N \sim 15\text{K}$

(1) Mag. bandwidth: $40 \text{ meV} \sim 30 T_N$
(*Gretarrson et al.*)

(2) Intense $q=0$ scattering
(*Gretarrson et al.; B.J. Kim et al.*)

(3) SW gap is small $< 2 \text{ meV}$
(*Coldea et al.; B.J. Kim et al.*)

Interactions:

strongly frustrated

non-Heisenberg

C3 symmetric

Kitaev-Heisenberg K-J model **with large $K > J$**

makes all these „for free“ but...

real world: Na_2IrO_3



Exp. data

AM order $T_N \sim 15\text{K}$

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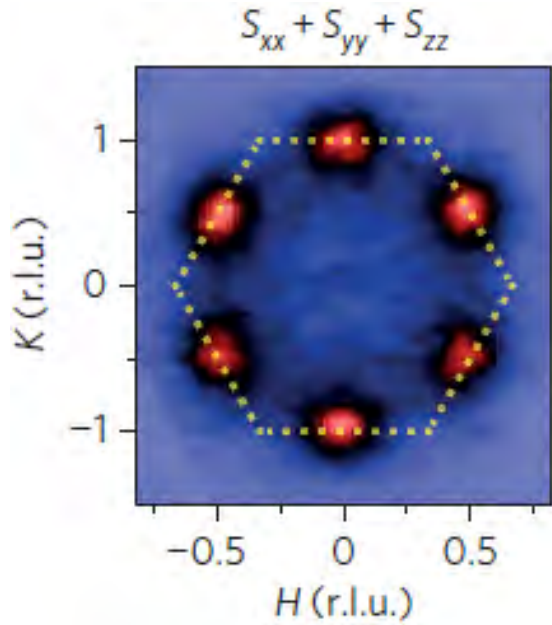
C3 symmetric

B.J. Kim et al., 2015:

*Unusual moment direction
away from symmetry axes*

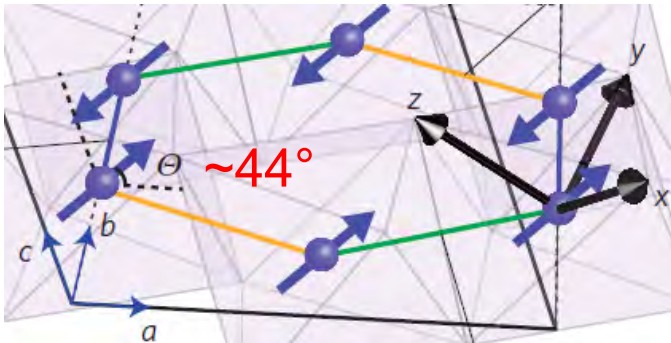
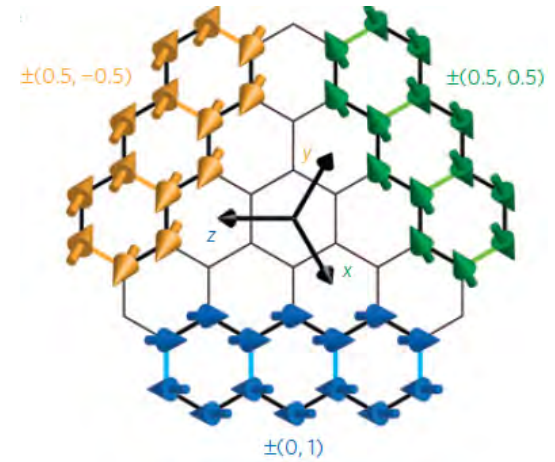
*need more terms beyond
Kitaev-Heisenberg model*

Diffuse magnetic X-ray scattering intensities above T_N



three equivalent zigzag
quasielastic peaks

C3 symmetry



**Unusual moment direction
away from symmetry axes**



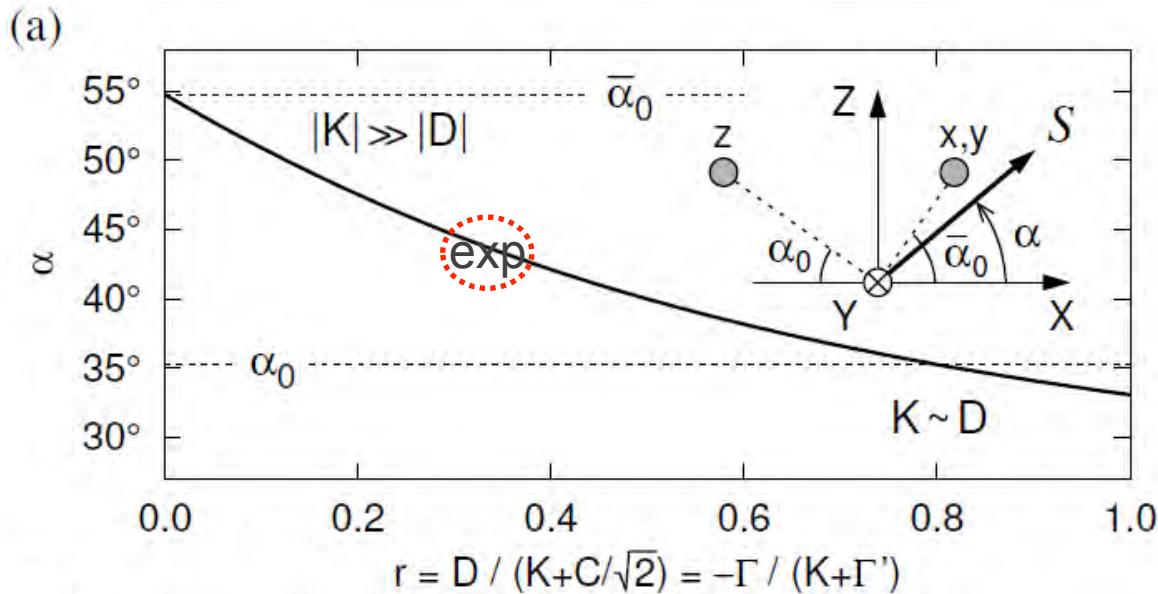
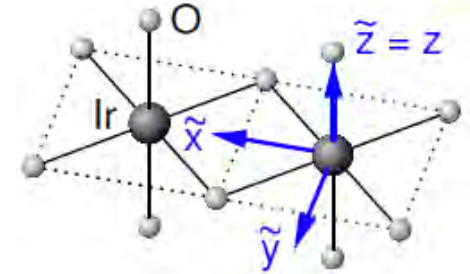
inconsistent with pure KH-model

Phenomenological model („extended-KH“):

(H.Y. Kee et al.,
van den Brink et al, ...)

$$\mathcal{H}_{\langle ij \rangle \| c} = J \mathbf{S}_i \cdot \mathbf{S}_j + K S_i^z S_j^z + D (S_i^x S_j^x - S_i^y S_j^y) + C (S_i^y S_j^z + S_i^z S_j^y)$$

Two new terms: D and C



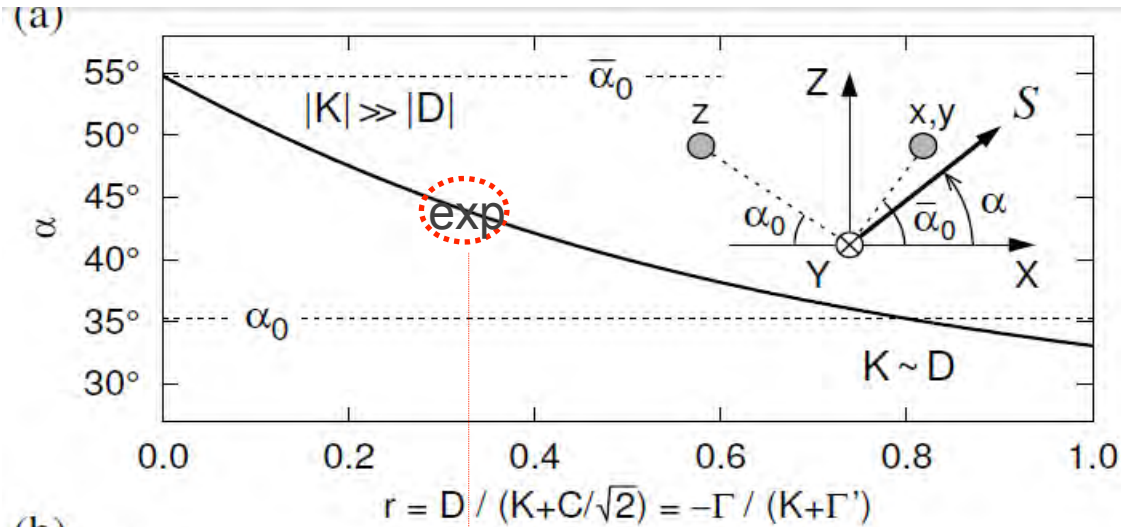
Chaloupka & GKh,
condmat 2015

K,J,D,C model can make the moment angle 40°-45°.

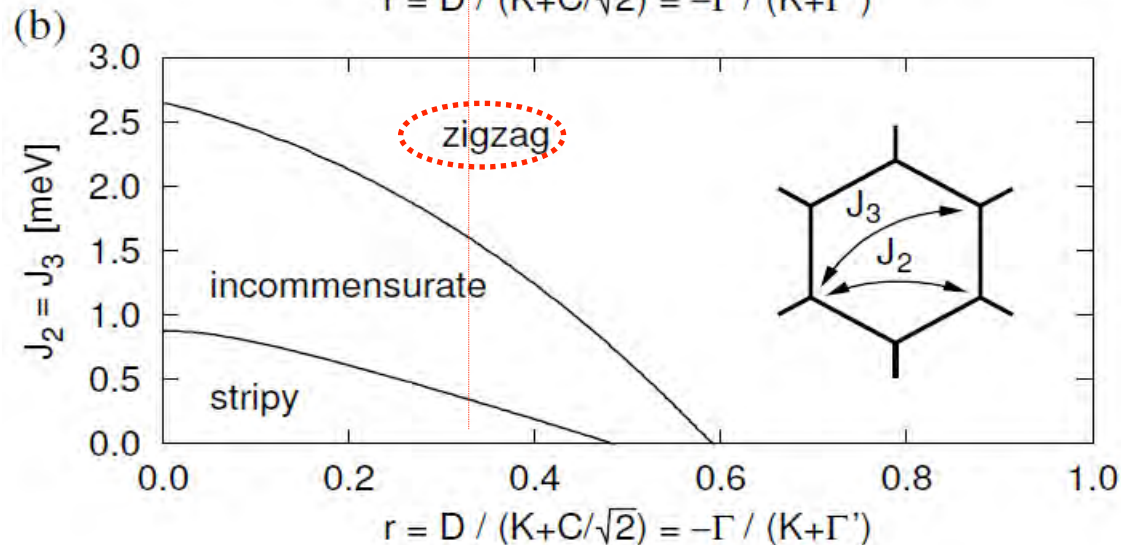
However, zigzag is not then stable.
We need longer range interactions.

... adding $J_{2,3}$ (Coldea et al. 2012)

$$\mathcal{H}_{\langle ij \rangle \parallel c} = J \mathbf{S}_i \cdot \mathbf{S}_j + K S_i^z S_j^z + D (S_i^x S_j^x - S_i^y S_j^y) + C (S_i^y S_j^z + S_i^z S_j^y) + J_{2,3}(\text{SS})$$



Sizable anisotropy D
&
long-range $J_{2,3}$



Right moment
direction
&
zigzag order

PHYSICAL REVIEW B 88, 035107 (2013)

***Ab initio* analysis of the tight-binding parameters and magnetic interactions in Na_2IrO_3**

Kateryna Foyevtsova,¹ Harald O. Jeschke,¹ I. I. Mazin,² D. I. Khomskii,³ and Roser Valentí¹



... the nnKH model, is, apparently, inadequate.

Spatially extended, „quasimolecular“ orbitals:
longer-range couplings $J_{2,3}$

Ab initio analysis of the tight-binding parameters and magnetic interactions in Na_2IrO_3

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... the nnKH model, is, apparently, ~~inadequate.~~
insufficient

Yes, indeed

Spatially extended, „quasimolecular“ orbitals:
longer-range couplings $J_{2,3}$

Yes, indeed



(current status)

Data collected so far suggests that

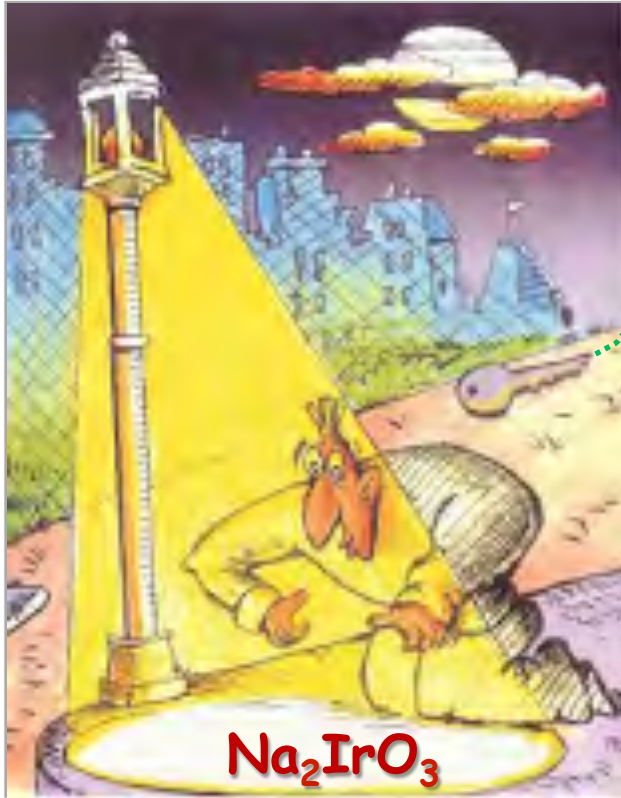
- Kitaev term seems to be dominant
- Other terms are substantial, yet to be sorted out

*measure and fit,
measure and fit..*

*most wanted:
single-crystal
 $S(q,w)$*

for more details, see:
Chaloupka & GKh, condmat 2015

The streetlight effect



Pseudospin one-half ions
Co⁴⁺, Ru³⁺, Rh⁴⁺, Os³⁺ ...

Non-oxides: F, Cl, S, Se ...

spin liquid

„dreamland“

Kitaev limit

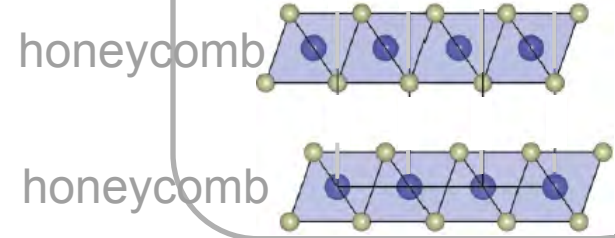
Majorana fermions

- Did you lose your Majoranas here?
- No, but the light is much better over here !

New candidate:

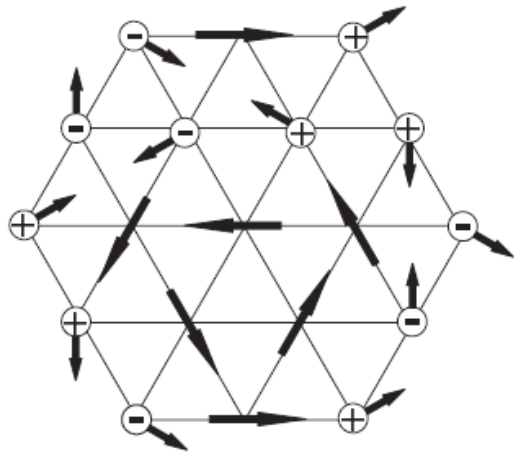


Plumb et al, 2014



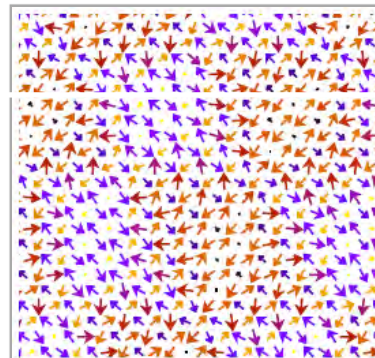
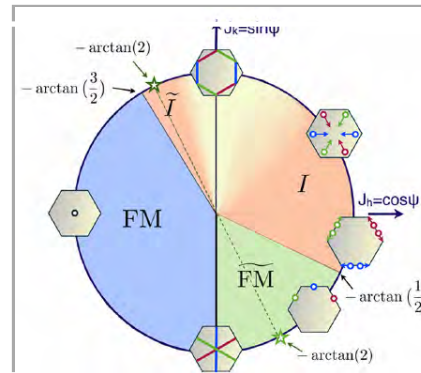
...and look for $J=1/2$ K-J model on other lattices

GKh (PTPS, 2005)



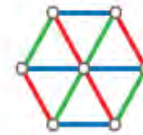
spin vortex condensate
multi-Q order
„hidden“ Goldstone

Rouschatzakis et al.
(condmat, 2012)

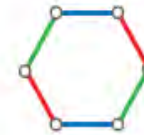


Kimchi & Vishwanath
(PRB, 2014)

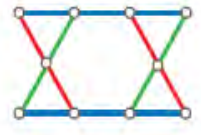
Triangular
 Na_xIrO_2



Honeycomb
 A_2IrO_3



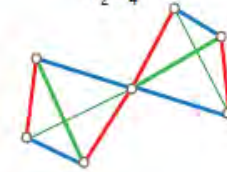
Kagome



Face-centered
cubic



Pyrochlore
 Ir_2O_4



Hyperkagome
 $\text{Na}_4\text{Ir}_3\text{O}_8$



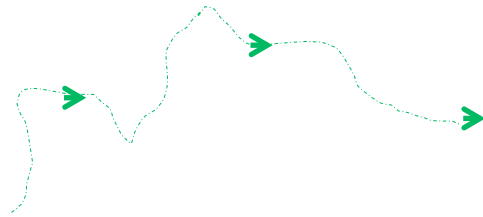
Pseudospin **AND** geometrical frustration:

- amplify the chances to find exotic states!

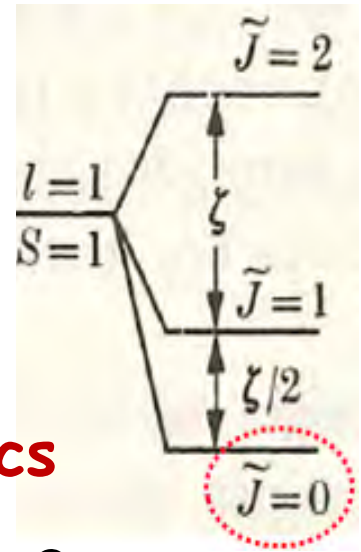
...farther away from the streetlight



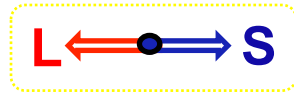
d^5 Co, Rh, Ir



J=0 physics

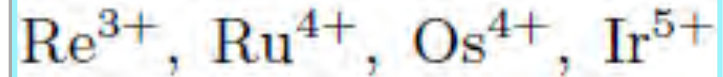


d^4 Ru, Os, ...



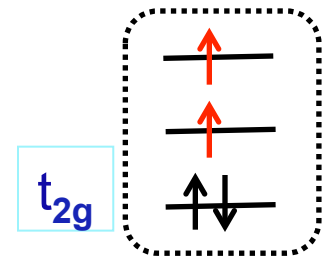
„nonmagnetic“ Mott insulators

d^4 Mott insulators



4d, 5d electrons

1. Low-spin $S=1$
2. Unquenched $L=1$



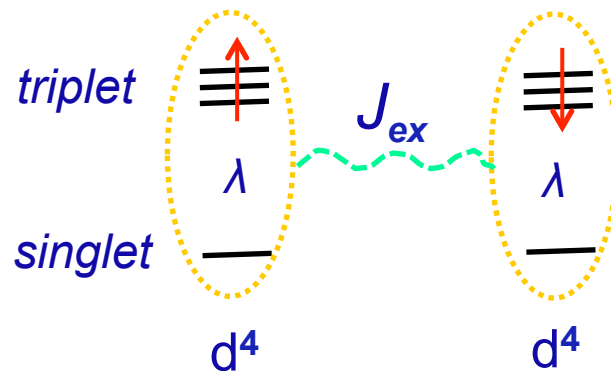
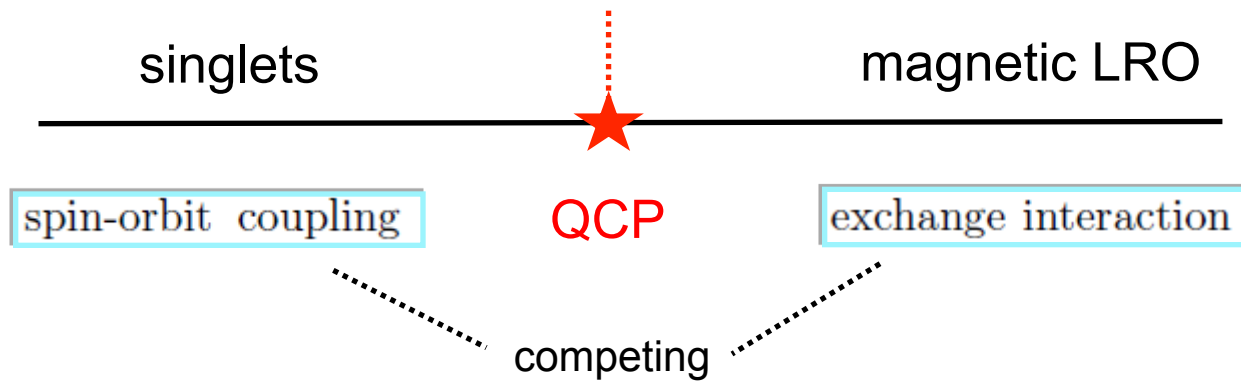
$\lambda(\text{LS})$



$$J=S+L=0$$

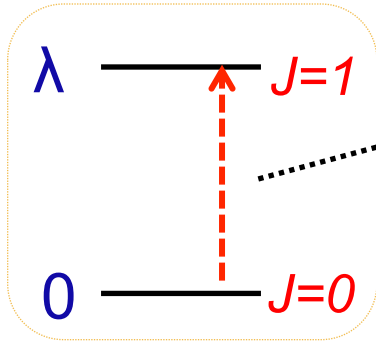
...no spin left to play with ...

J=0 physics: *spin-orbit driven magnetic QCP*



d⁴ ion: Van-Vleck magnetism

(i) *There are no „pre-existing“ moments*

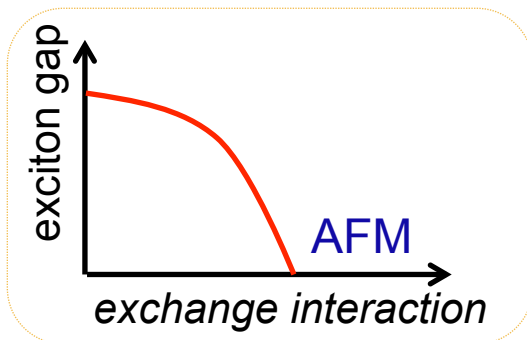


(ii) *J=0 to J=1 transition: off-diagonal magnetic moment $M=2S-L$ („spin-orbit exciton“)*

(iii) *Condensation of spin-orbit exciton*

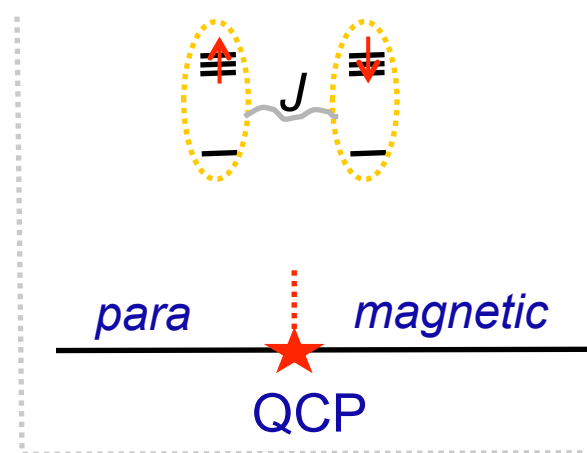
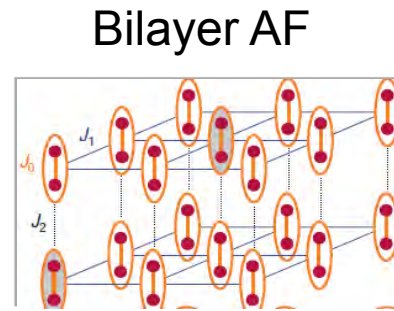
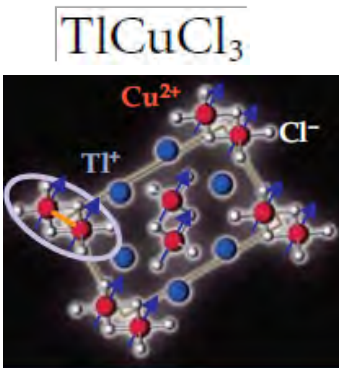


„excitonic“ magnetism



Singlet-triplet examples

(A) Weakly coupled dimers



THIERRY GIAMARCHI^{1*}, CHRISTIAN RÜEGG^{2*}
AND OLEG TCHERNYSHYOV^{3*} (*Nat.Phys.* 2009)

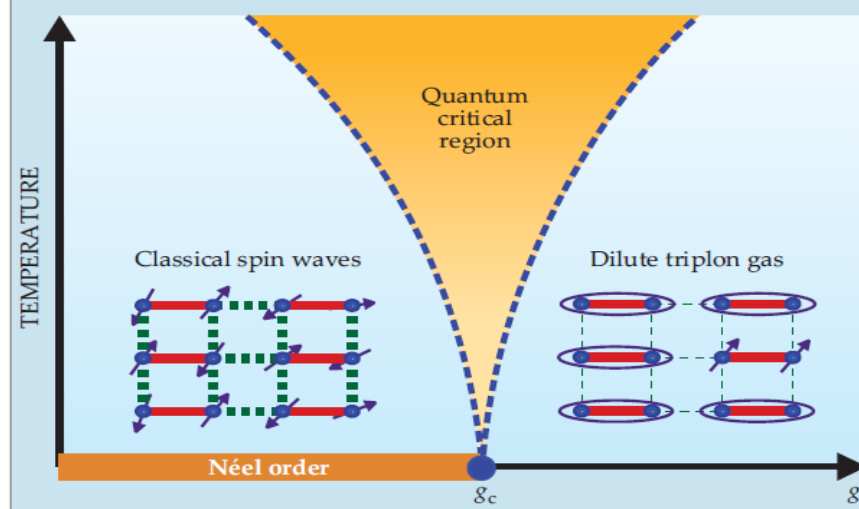
(B) *4f Pr compounds* (broad literature since 1970's)

(C) e_g orbital FeSc_2S_4 (Chen, Balents, Schnyder, 2009)

(D) Spin-state-crossover in Fe-based SC (Chaloupka & GKh, 2013)

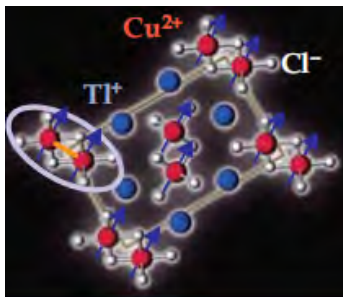
QUANTUM CRITICALITY

Sachdev, Keimer,
Phys.Today, 2011



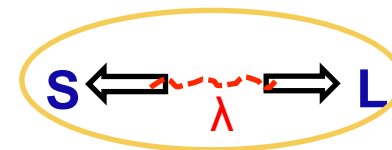
*birthplace for
„unconventional“ physics*

Inter-ionic dimers



-small energies
-special geometry

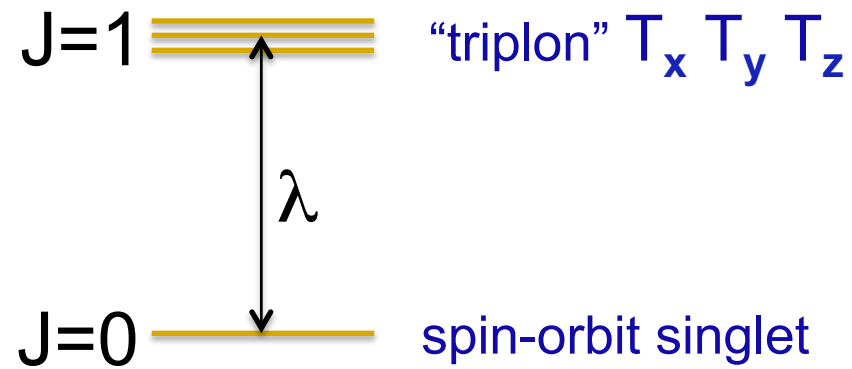
d^4 : Intra-ionic „dimer“
made of S and L



- 1) energetic (~ 100 meV)
- 2) generic (any lattice)

GKh (2013)

d^4 Mott insulator: single-ion states



d⁴ Mott insulator: singlet-triplet model (180°)

GKh (2013)

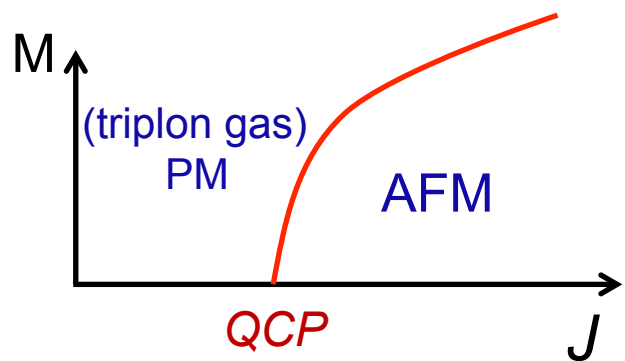
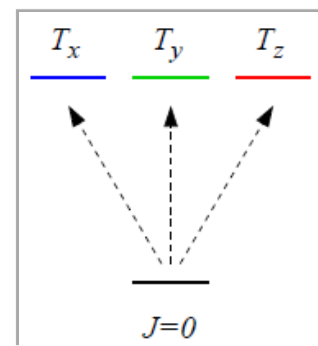
(e.g. 214-perovskite)

$$H = \lambda \sum_i n_i + J \frac{2}{9} \sum_{ij} [T_i^\dagger \cdot T_j - \frac{7}{16} (T_i \cdot T_j + H.c.)]$$

spin-orbit

exchange

S=1 boson



LRO moment:

$$M_z = 2\sqrt{6\rho(1-\rho)}$$

$$\rho = \frac{1}{2}(1 - \tau^{-1})$$

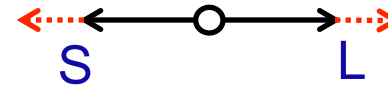
cond. density

$$\tau = \kappa/\kappa_c > 1$$

distance from QCP

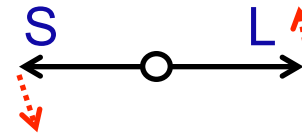
Excitations:

1. The amplitude mode
changing the lengths of S & L



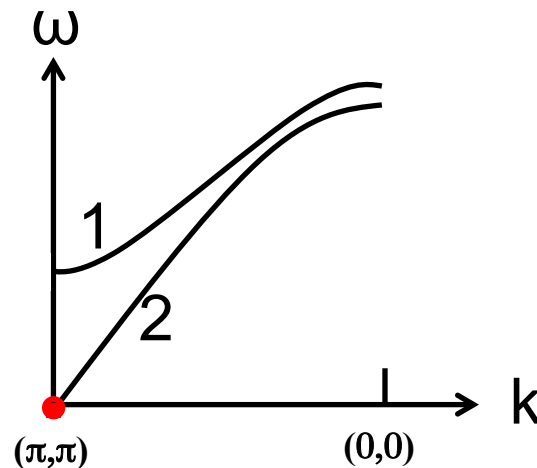
„Higgs“

2. The phase modes
in-phase rotation of S & L



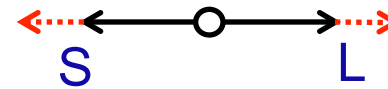
Goldstone

*magnons in
excitonic AF*



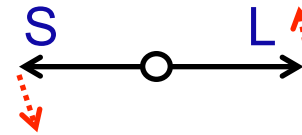
Excitations:

1. The amplitude mode
changing the lengths of S & L

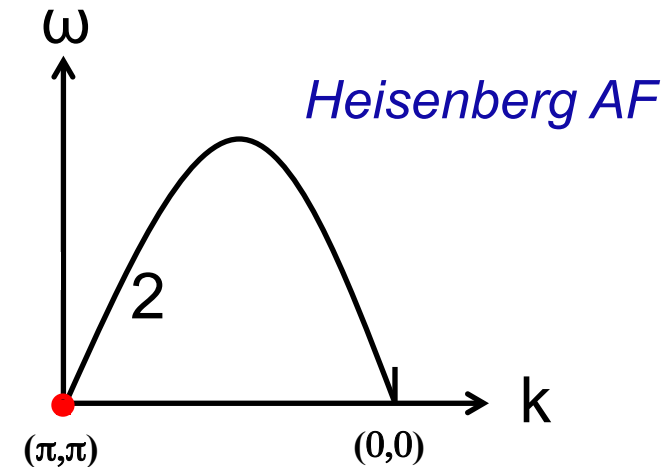
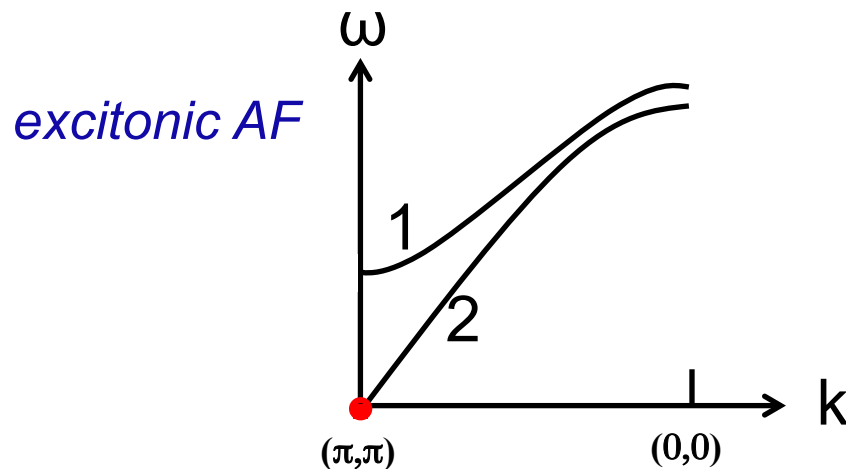


„Higgs“

2. The phase modes
in-phase rotation of S & L



Goldstone

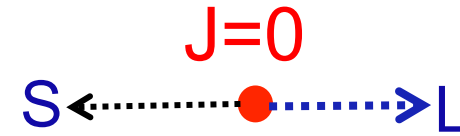
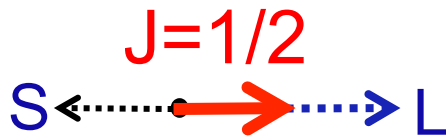


Van Vleck-type d^4 Mott insulators:
EXCITONIC magnetism

Candidate material:



Summary



$J=S+L$ inherits bond-dependent
& frustrated nature of orbitals

„nonmagnetic“ $J=0$
Mott insulators



unconventional magnetism



...unconventional SC?

Spin-Orbit Coupling in the Mott Insulator Ca₂RuO₄

T. Mizokawa,^{1,2} L. H. Tjeng,² G. A. Sawatzky,² G. Ghiringhelli,^{3,4} O. Tjernberg,^{3,5} N. B. Brookes,³ H. Fukazawa,⁶
S. Nakatsuji,⁶ and Y. Maeno^{6,7}

$\langle \sum_i l_{x'}(i) \cdot s_x(i) \rangle$ is about -0.28 ± 0.07 , using $N_d = 4$. This value is comparable to that measured for CoO [16], where the orbital moment was found to be of the order of 1 μ_B . These measurements thus demonstrate that the

**unquenched L-moment
in ruthenates**

PRL **112**, 127002 (2014)

Spin-Orbital Entanglement and the Breakdown of Singlets and Triplets in Sr₂RuO₄

C. N. Veenstra,¹ Z.-H. Zhu,¹ M. Raichle,¹ B. M. Ludbrook,¹ A. Nicolaou,^{1,2,7} B. Slomski,^{3,4} G. Landolt,^{3,4}
S. Kittaka,^{5,6} Y. Maeno,⁵ J. H. Dil,^{3,4} I. S. Elfimov,^{1,2} M. W. Haverkort,^{1,2,7} and A. Damascelli^{1,2,*}

Singlet-triplet model $H_{eff}(90^\circ)$

(triangular, honeycomb, kagome...)

c-bond exchange:

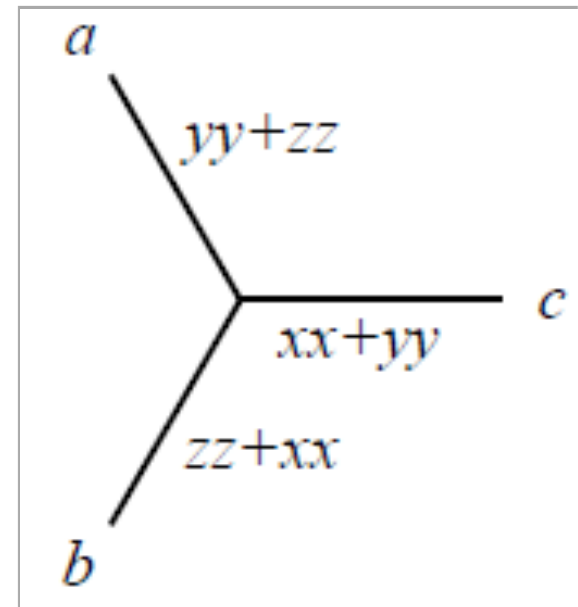
$$\frac{2}{3}(T_{ix}^\dagger T_{jx} + T_{iy}^\dagger T_{jy}) - \frac{5}{6}(T_{ix} T_{jx} + T_{iy} T_{jy}) + H.c.,$$

hopping

pair-generation

x and y type bosons only involved

Bond-dependent „xy-model“:



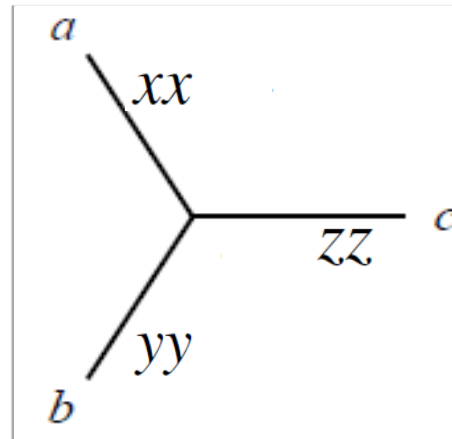
Exchange anisotropy, 90° bonding: d^4 vs d^5

(triangular, honeycomb, kagome...)

d^5 (Co, Rh, Ir)

bond-dependent Ising:

spin $\frac{1}{2}$



GKh (2005)

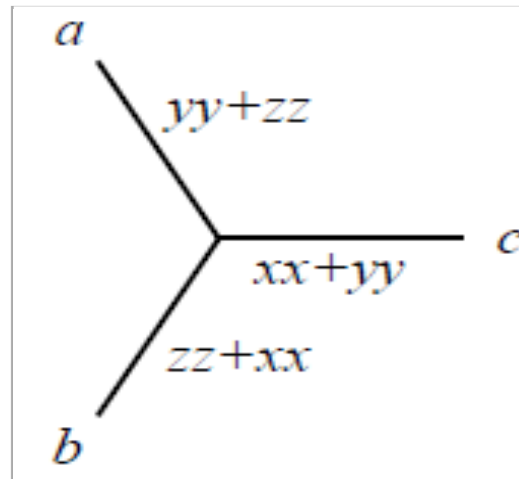
Chen & Balents (2008)

Jackeli & GKh (2009)

d^4 (Ru, Re, Os)

bond-dependent „xy“:

spin-one T boson



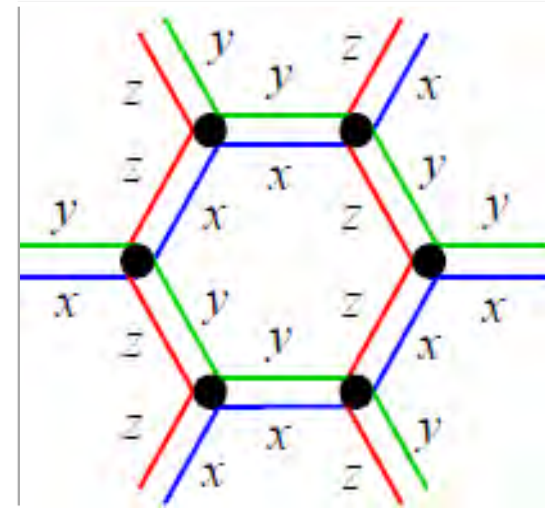
GKh (2013)

Honeycomb lattice: dimensionality reduction

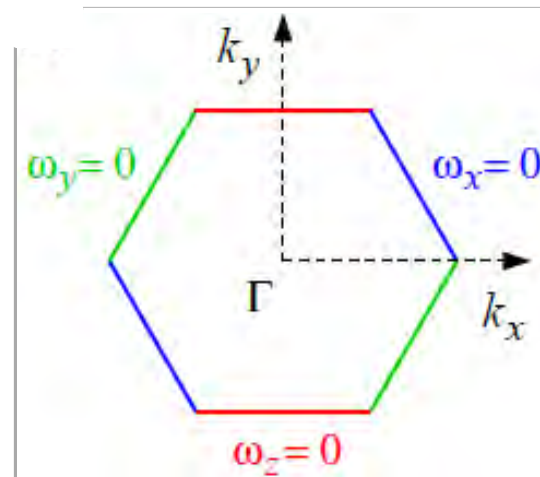
□ Each flavor T_x , T_y , T_z has its own zigzag to move along

□ 1D dispersion:

$$|\omega_z(\mathbf{k}) \equiv \omega_z(k_y) \simeq \lambda \sqrt{1 + (\kappa/\kappa_c) c_y}$$



□ $J=J_{\text{crit}}$: zero-energy lines



unusual singlet-triplet model, yet to be solved...

VBS?
zigzag order?
spin nematic?
...