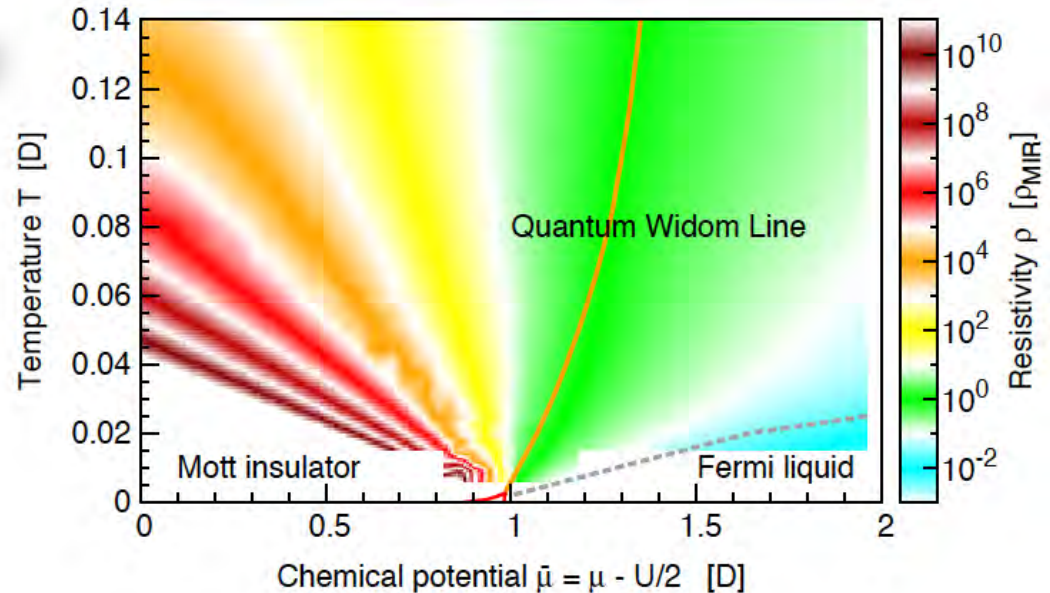
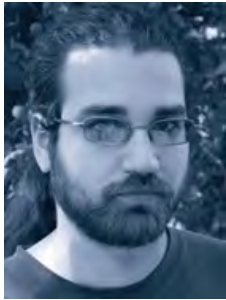


Bad Metal Behavior and Mott Quantum Criticality

Vladimir Dobrosavljevic
Florida State University

<http://badmetals.magnet.fsu.edu>



Collaborators:

Jaksa Vucicevic (Belgrade, Serbia)

Hanna Terletska (FSU, Ames Lab)

Darko Tanaskovic (Belgrade, Serbia)

Marcelo Rozenberg (Orsay)

Funding:

NSF grants:

DMR-1410132

...

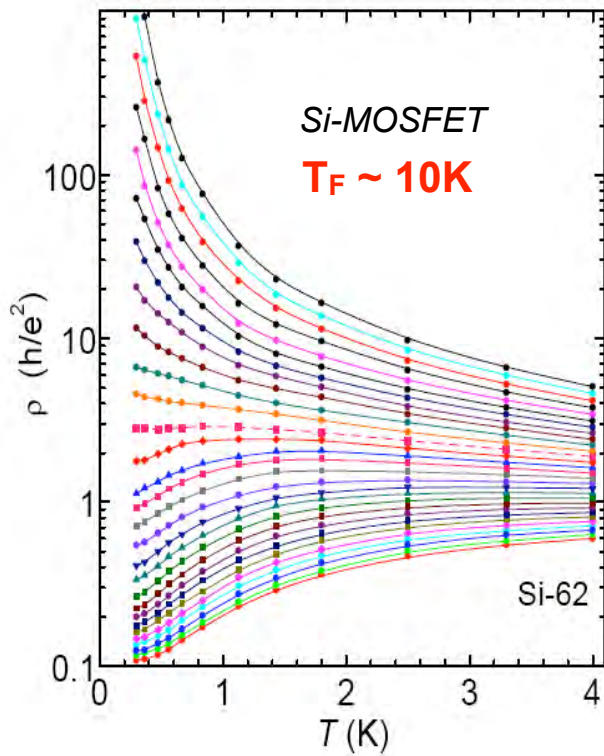


Abrahams, Chakravarty, Kotliar, Haule, Miranda, Pankov,...

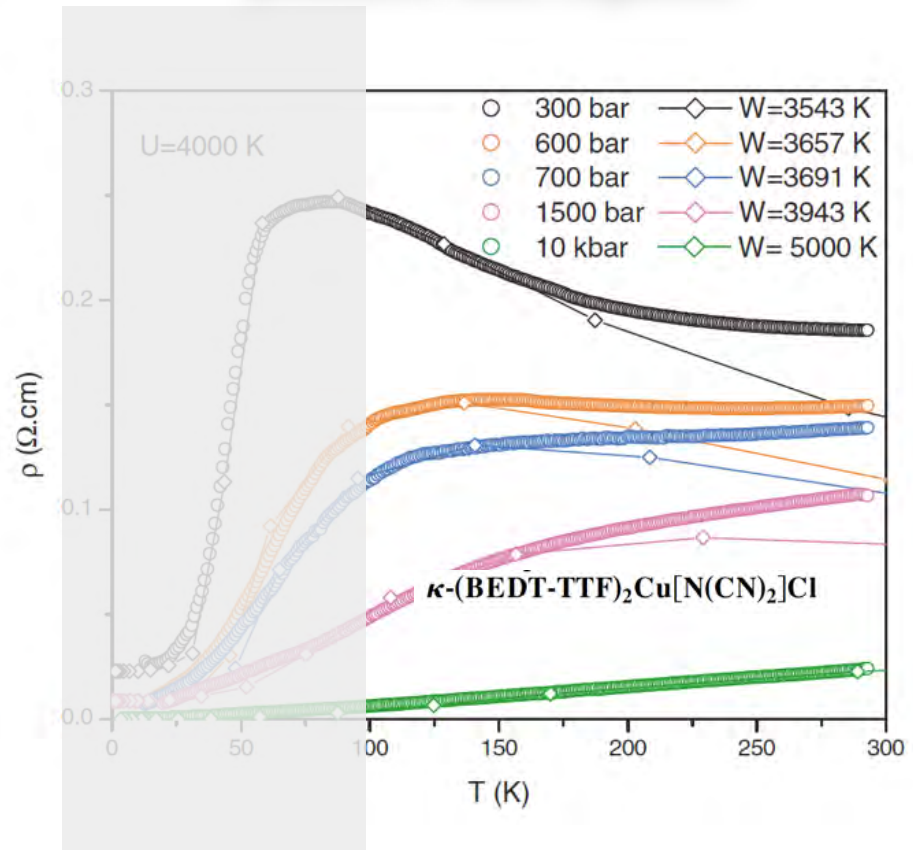
From Metals to Insulators:

universality at "high temperatures"

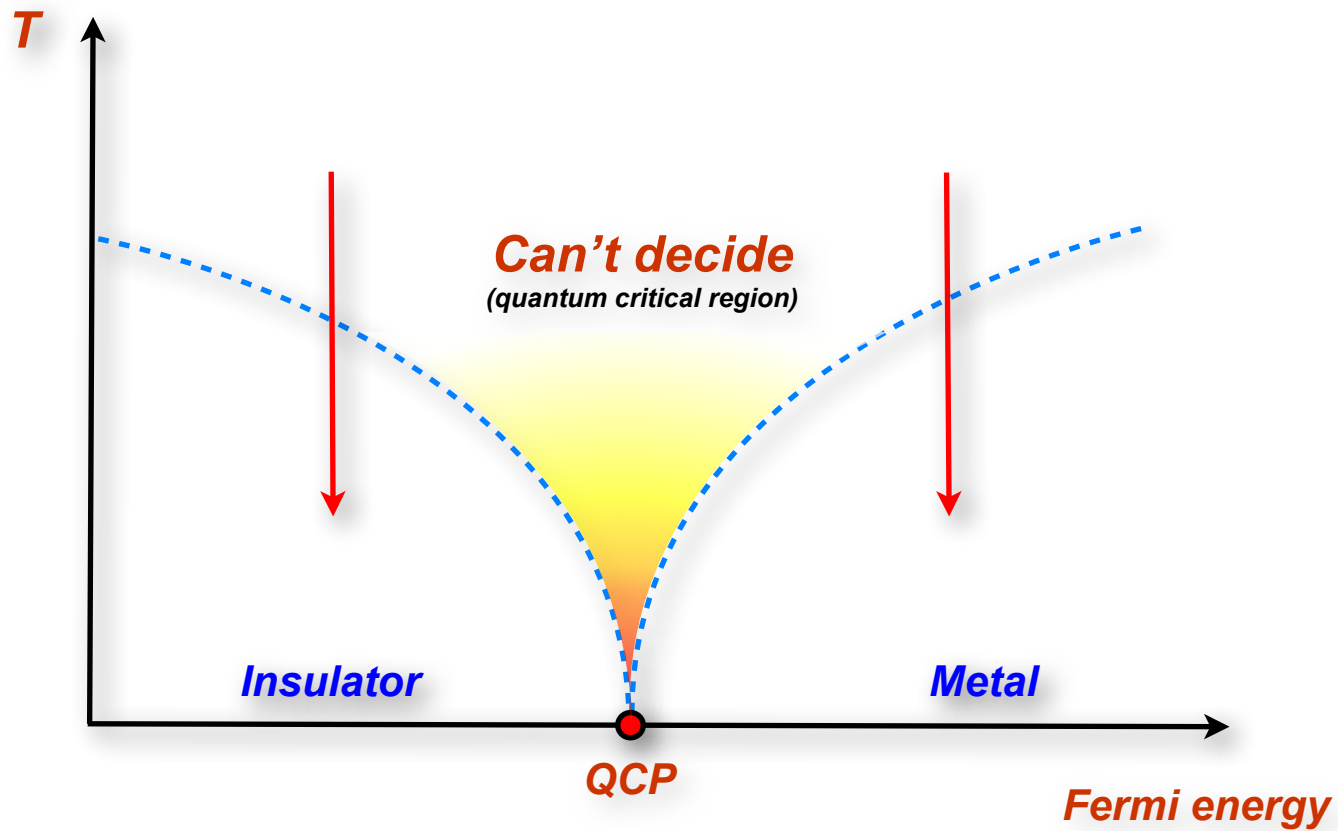
carrier density: Wigner-Mott 2DEG



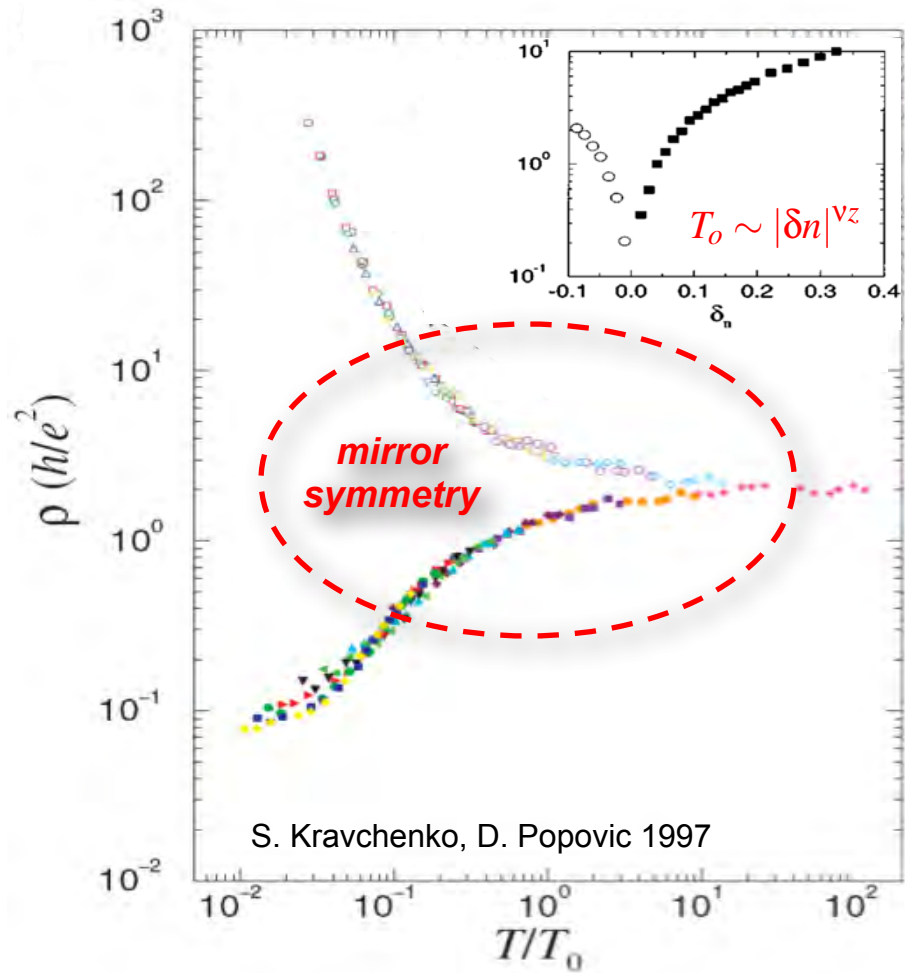
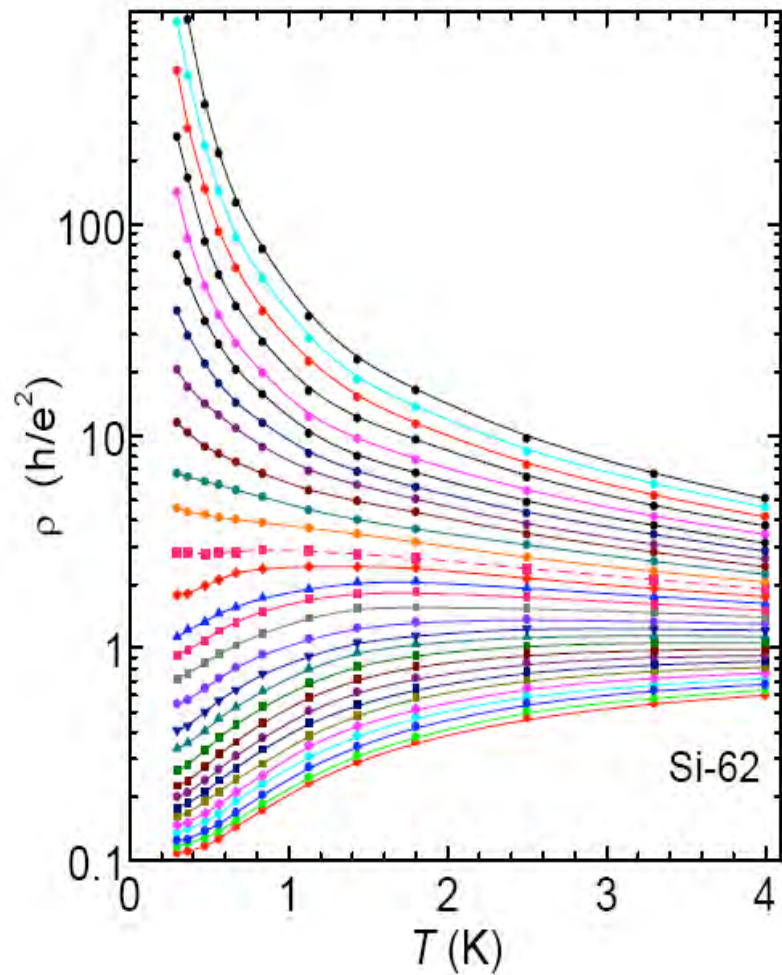
pressure: Mott organics



MIT Quantum Criticality?



2D-MIT: "Duality" Scaling???



Scaling Theory Redux

VOLUME 79, NUMBER 3

PHYSICAL REVIEW LETTERS

21 JULY 1997

Scaling Theory of Two-Dimensional Metal-Insulator Transitions

V. Dobrosavljević,¹ Elihu Abrahams,^{1,2} E. Miranda,¹ and Sudip Chakravarty³

¹National High Magnetic Field Laboratory, Florida State University 1800 E. Paul Dirac Drive, Tallahassee, Florida 32306

²Serin Physics Laboratory, Rutgers University, Piscataway, New Jersey 08855-0849

³Department of Physics and Astronomy, University of California Los Angeles, Los Angeles, California 90095-1547

(Received 10 April 1997)

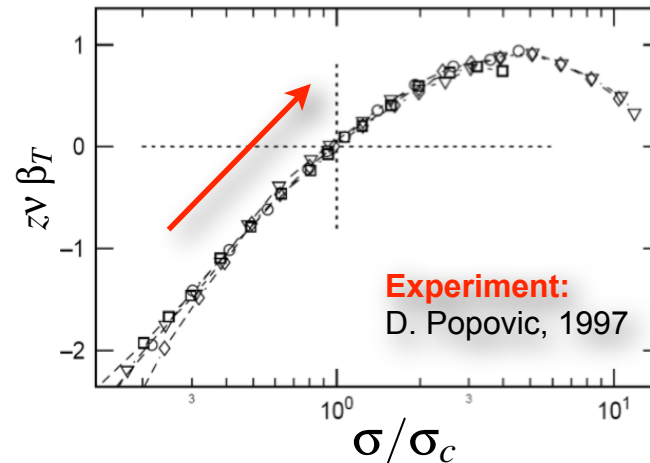
We discuss the recently discovered two-dimensional metal-insulator transition in zero magnetic field in the light of the scaling theory of localization. We demonstrate that the observed symmetry relating conductivity and resistivity follows directly from the quantum critical behavior associated with such a

$$\beta_T(g) = -\frac{d \ln g}{d \ln T} \approx \frac{1}{\nu z} \ln g$$

$$g(T) \approx g_o \exp\{\delta n (T_o/T)^{1/\nu z}\}$$

$$g^*(\delta n, T) = 1/g^*(-\delta n, T)$$

“strong coupling” - dominated by insulator?



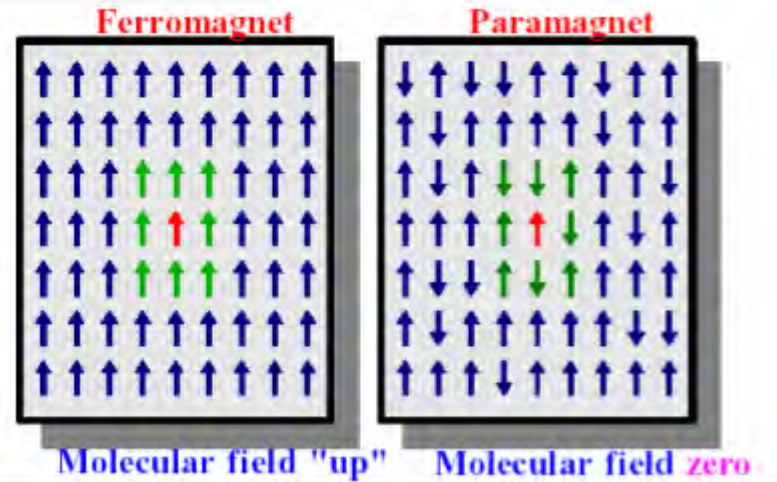
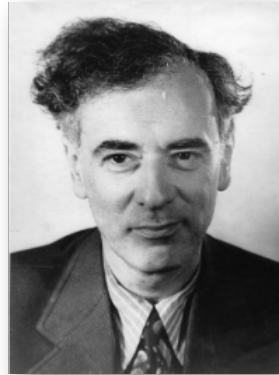
How to tackle Phase Transitions?

Standard critical points:

Spontaneous symmetry breaking

Order parameter, Landau-Ginzburg

Renormalization group, field theory



Metal-Insulator Transitions:

NO symmetry breaking!

Order parameter???

"...orthodox phase transition theory will be of little help to us for the time being, and thus the great body of literature in the field is **simply irrelevant...**"
III-Condensed Matter, 1979



Phillip W. Anderson

Maximally Frustrated Hubbard Model

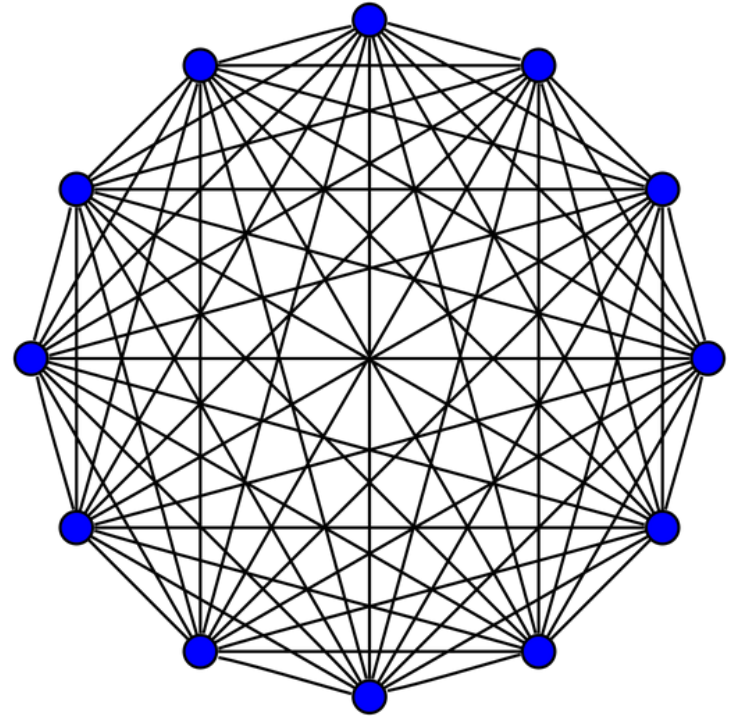
$$H = -t \sum_{\langle i,j \rangle, \sigma} (c_{i\sigma}^\dagger c_{j\sigma} + \text{h.c.}) + U \sum_i n_{i\uparrow} n_{i\downarrow} - \mu \sum_{i,\sigma} c_{i\sigma}^\dagger c_{i\sigma}$$

Infinite-range model

Suppress all orders: “pure Mott”

Local self-energy: DMFT solution

“Kondo physics” forms Fermi liquid



Finite temperature transport: the Mott transition at half-filling

PRL 107, 026401 (2011)

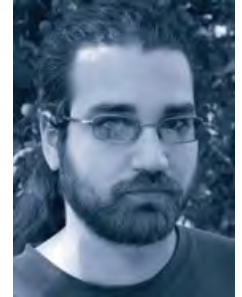
PHYSICAL REVIEW LETTERS

week ending
8 JULY 2011

Quantum Critical Transport near the Mott Transition

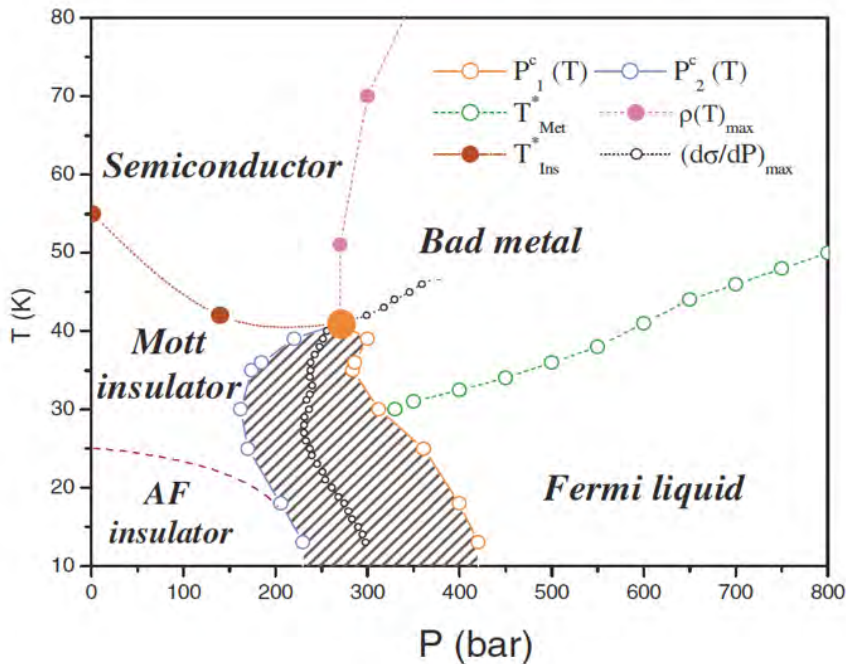
H. Terletska,¹ J. Vučićević,² D. Tanasković,² and V. Dobrosavljević¹

(also J. Vučićević, et al., *Phys. Rev. B*, 88, 075143 (2013))



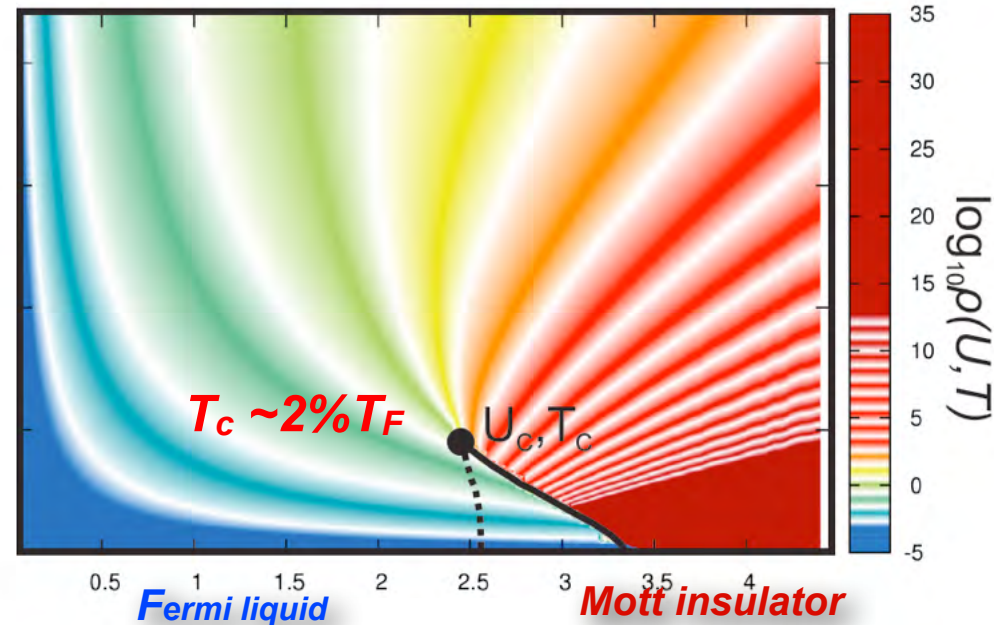
Experiment: organic Mott system

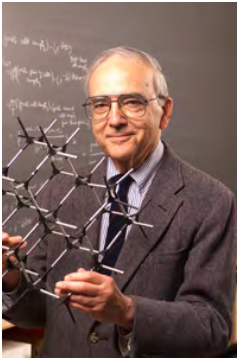
Jerome, PRL 2003



Theory (DMFT)

Early work: Kotliar, Rozenberg 1992, etc.



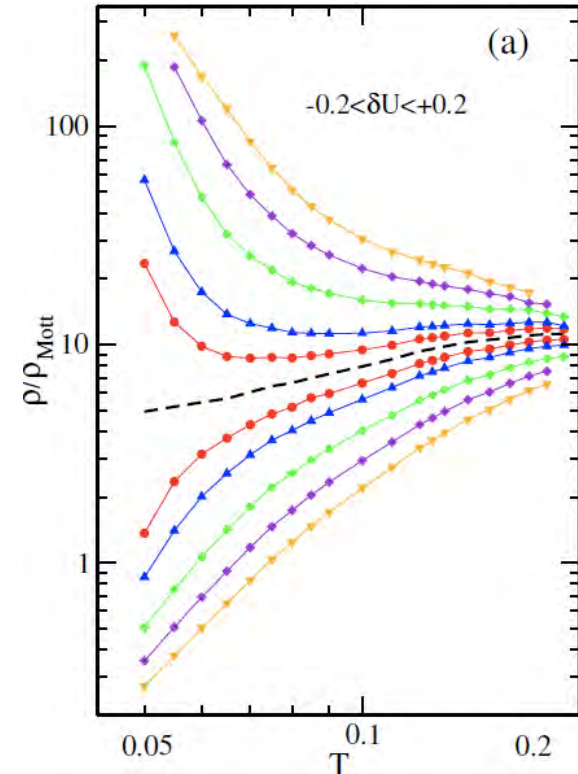
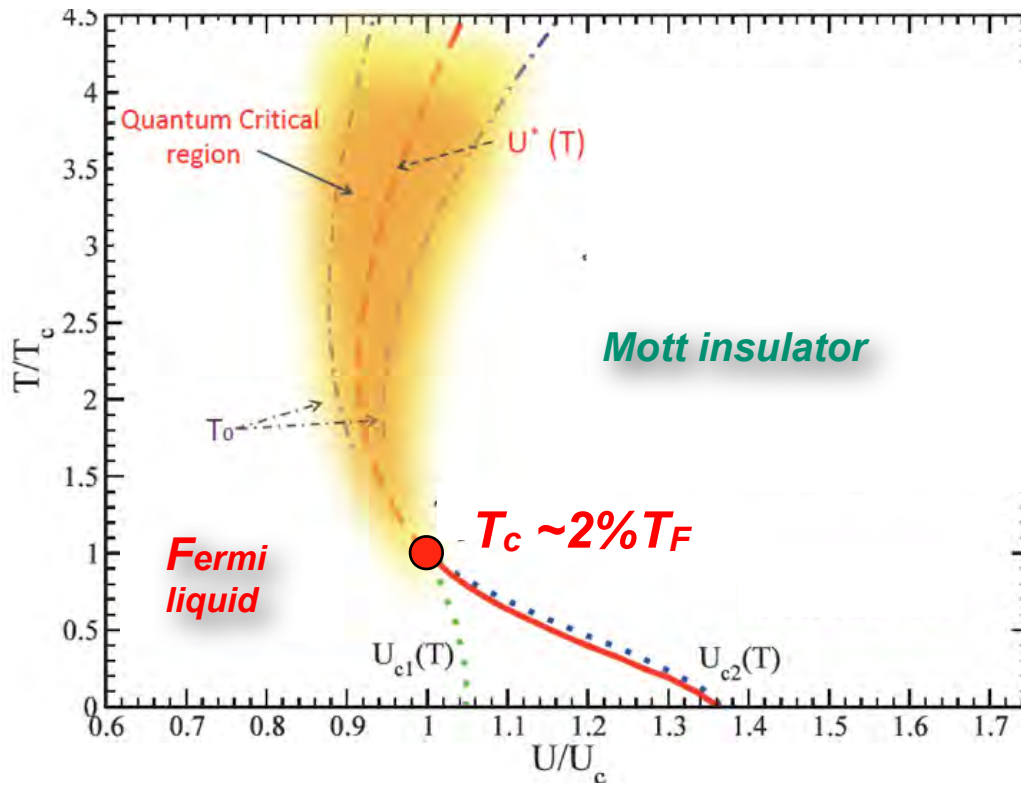


Crossover - “*quantum Widom line*” !

Recent work: Sordi, Trambly, 2012, etc.

DMFT theory

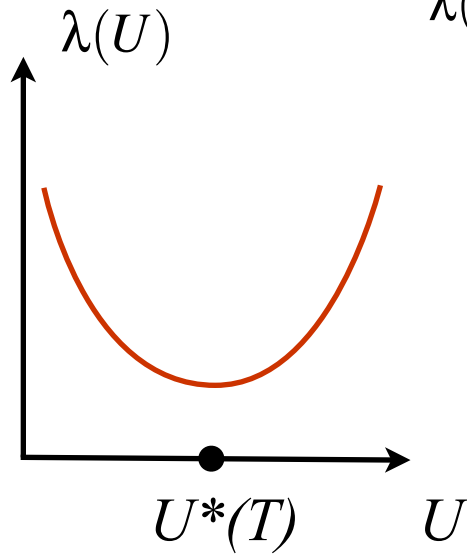
around Widom line



MOSFET: $T_c \sim 2\% T_F \sim 200\text{mK}$

Crossover line: eigenvalue analysis

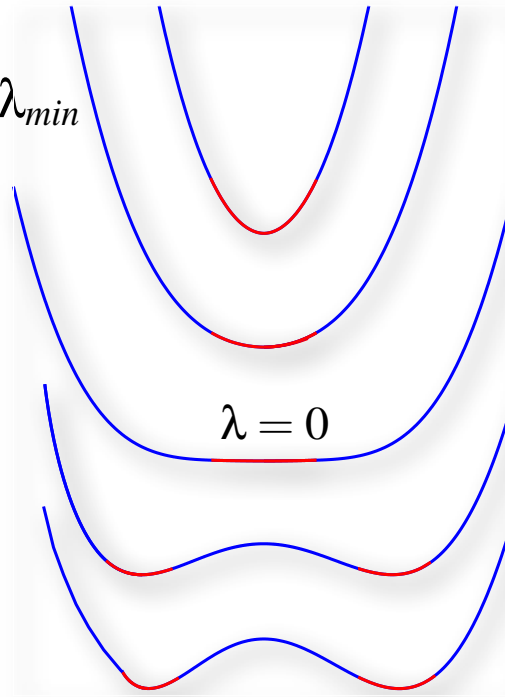
Curvature - eigenvalue



$$\delta U = U - U^*(T)$$

Free energy landscape (actual quantitative results!)

$$\lambda(U) = \lambda_{min}$$



On crossover line

$$\delta U(T) = 0$$

$$T > T_c$$

$$\lambda(U) > \lambda_{min}$$

$$T = T_c$$

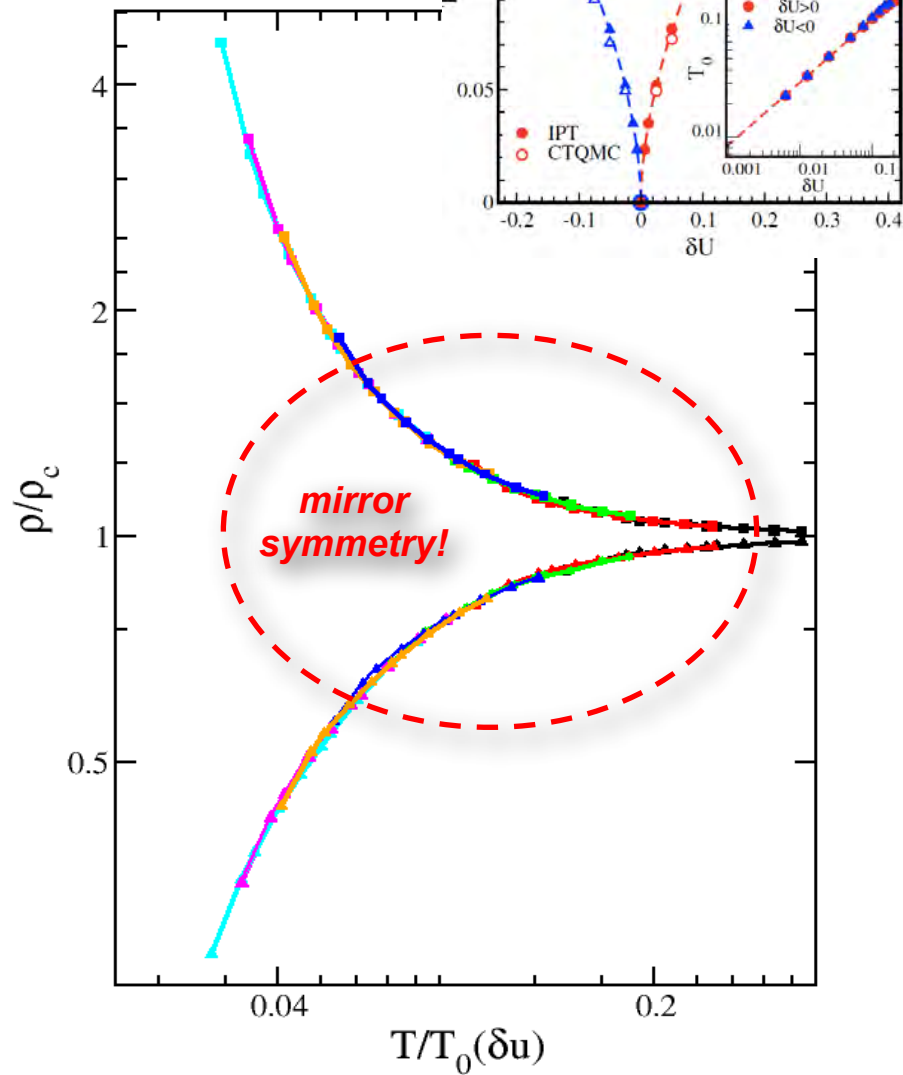
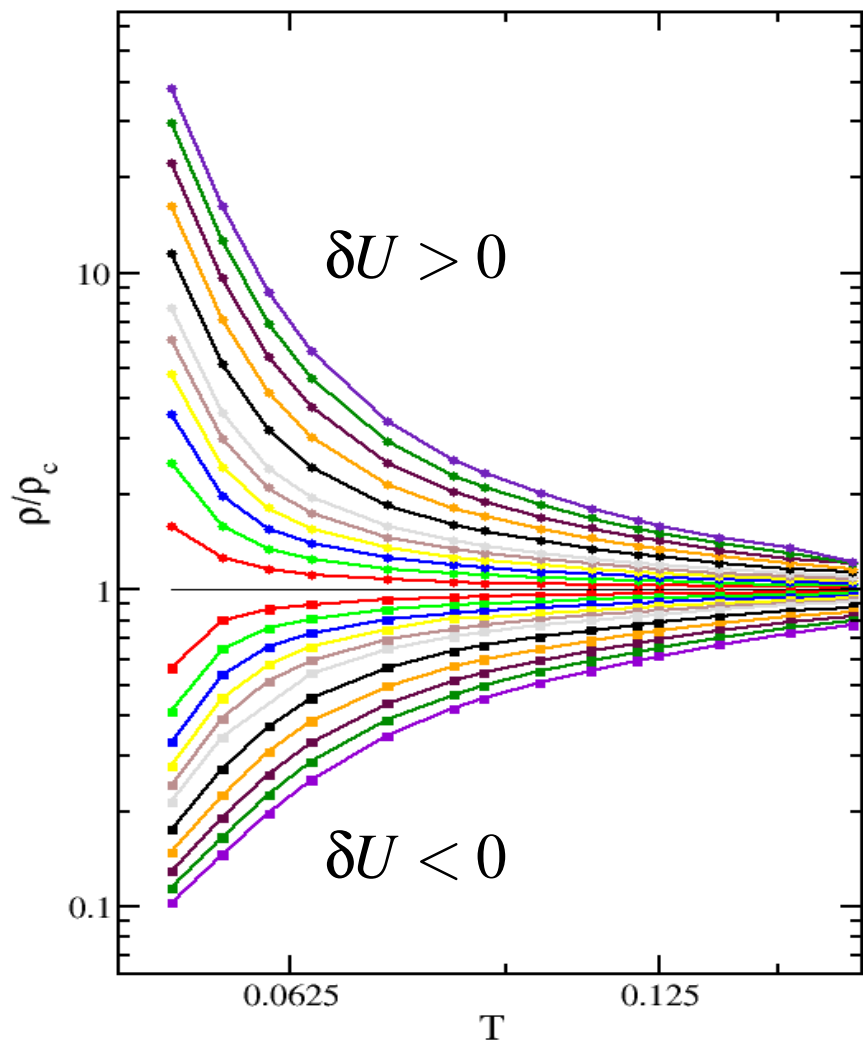
$$T < T_c$$

**Away from
crossover line**

$$\delta U(T) \neq 0$$

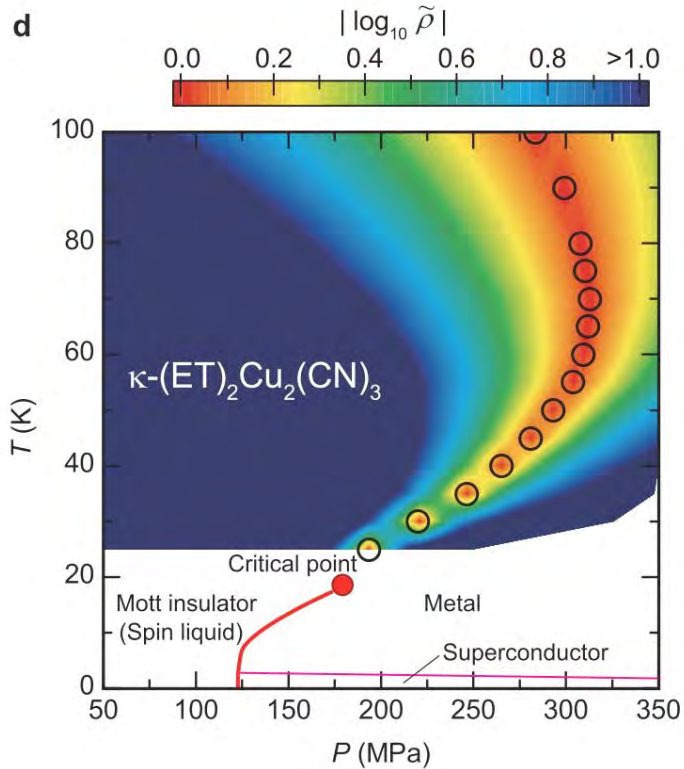
Scaling

$$\rho(\delta U, T) / \rho_c(T) = f(T / T_o(\delta U))$$

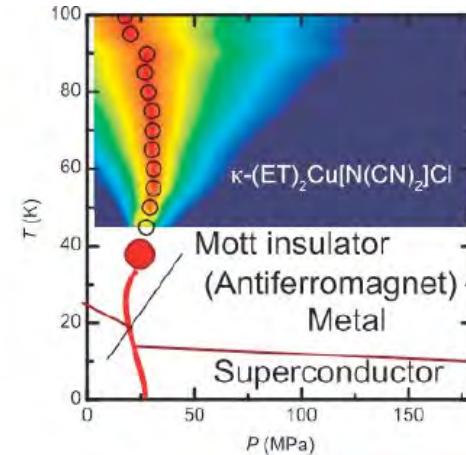


Mott organics: universal high-T scaling

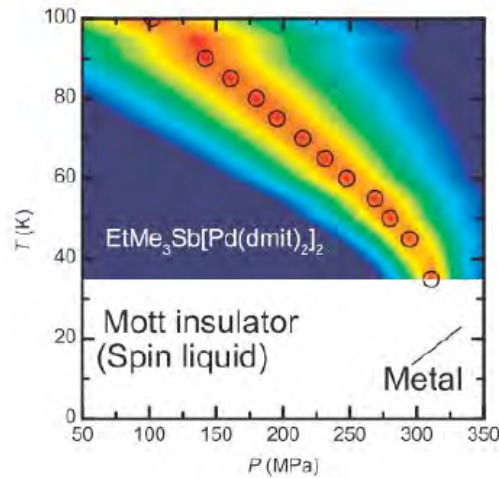
K. Kanoda et al., Nature Physics (2015)



**Strong frustration:
spin liquid at low T**

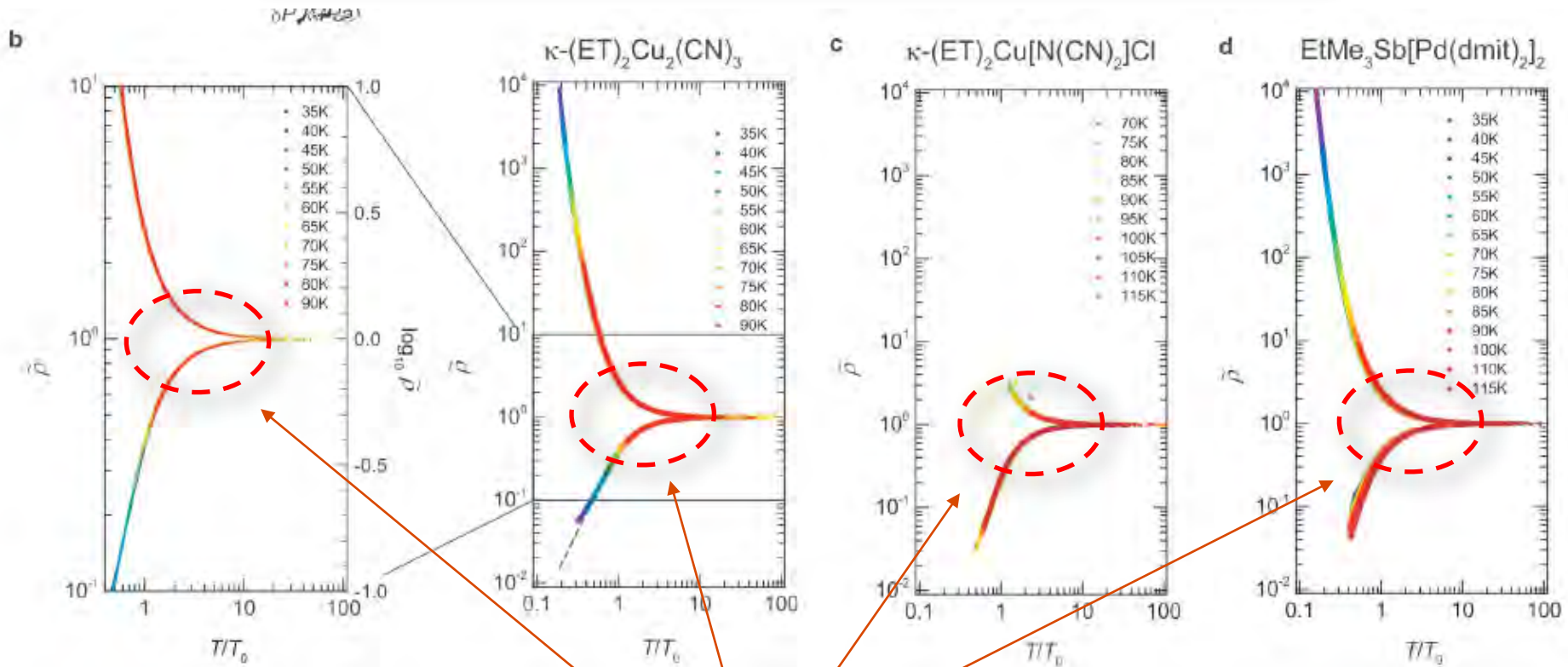


**Weaker frustration:
AFM at low T**



Mott organics: **universal** high-T scaling

K. Kanoda et al., Nature Physics (2015)



$z\nu = 0.60$ and $c = 25.3$ for $\kappa\text{-Cu}_2(\text{CN})_3$

$z\nu = 0.55$ and $c = 65.8$ for $\kappa\text{-Cl}$

$z\nu = 0.65$ and $c = 18.9$ for $\text{EtMe}_3\text{Sb-dmit}$

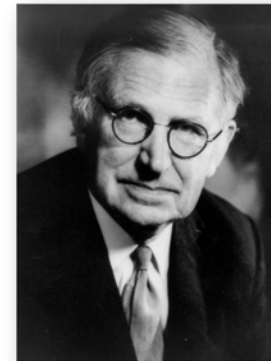
**mirror
symmetry!**

$$\tilde{\rho} = \exp[\pm(T/T_0)^{-1/z_\nu}]$$

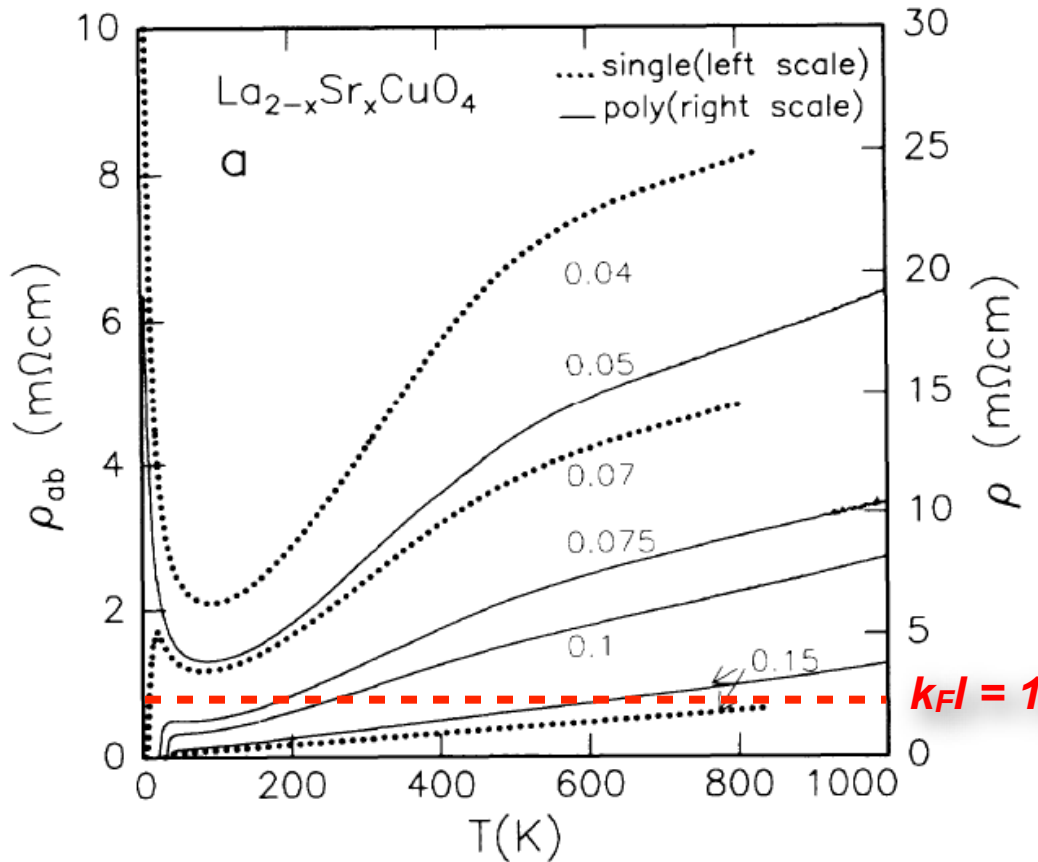
“stretched exponential”



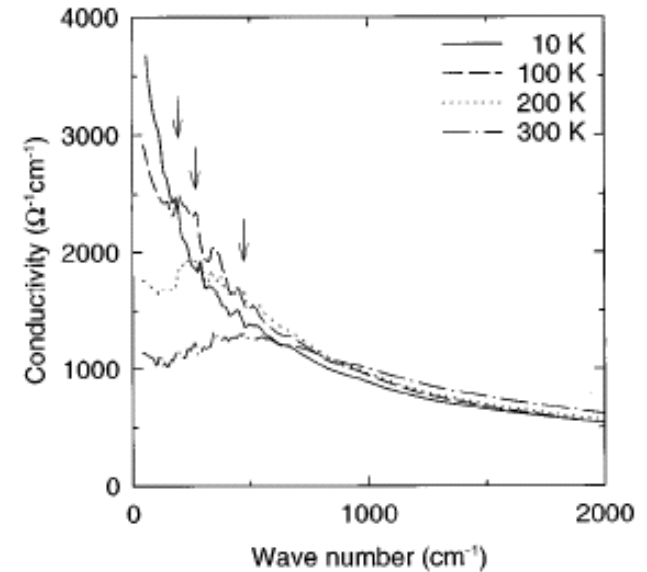
Doped Mott insulators: Bad Metals vs. Quantum Criticality??



**Mott-Ioffe-Regel
limit: $k_{FI} > 1$**

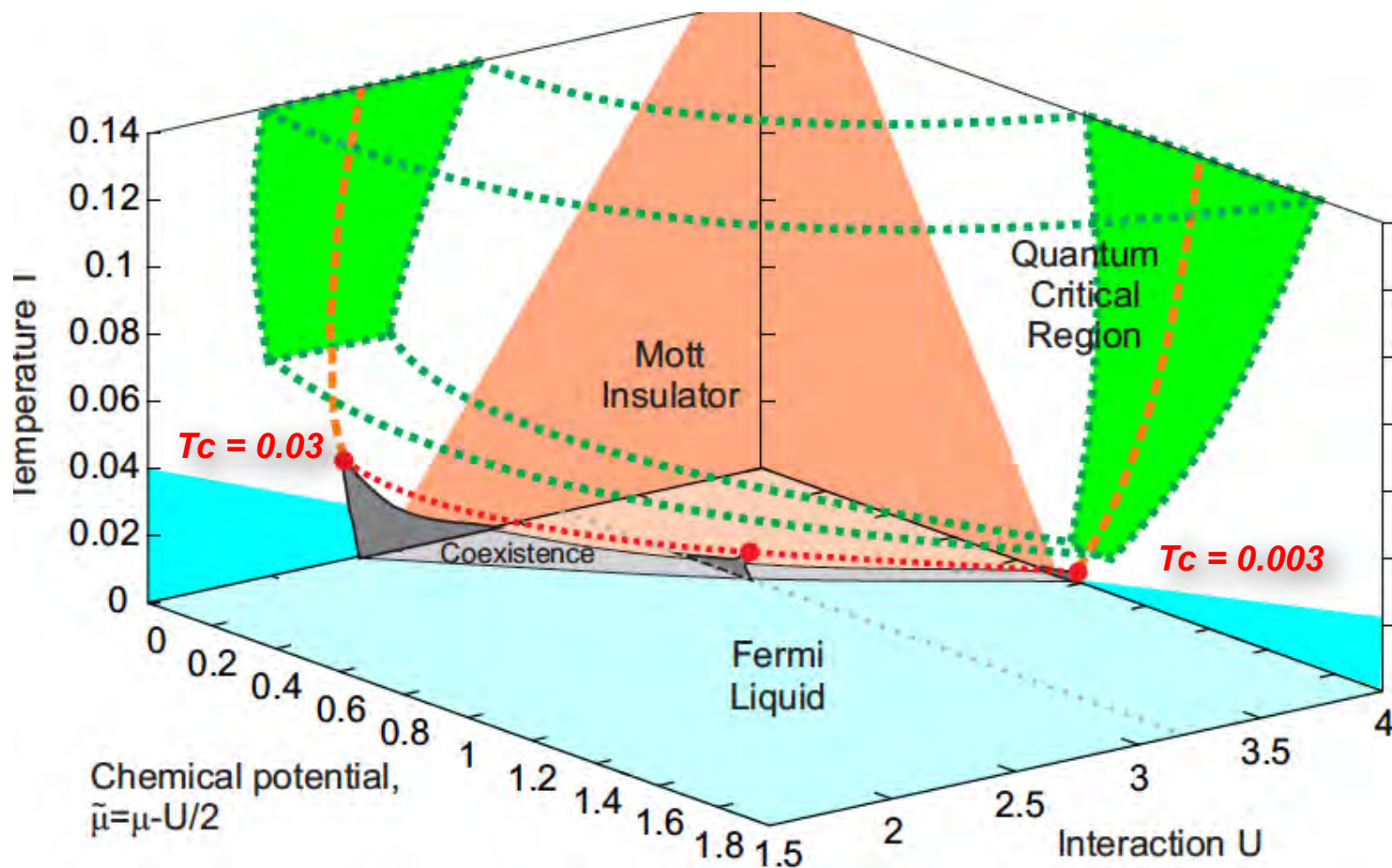


Experiment: H. Takagi, 1992



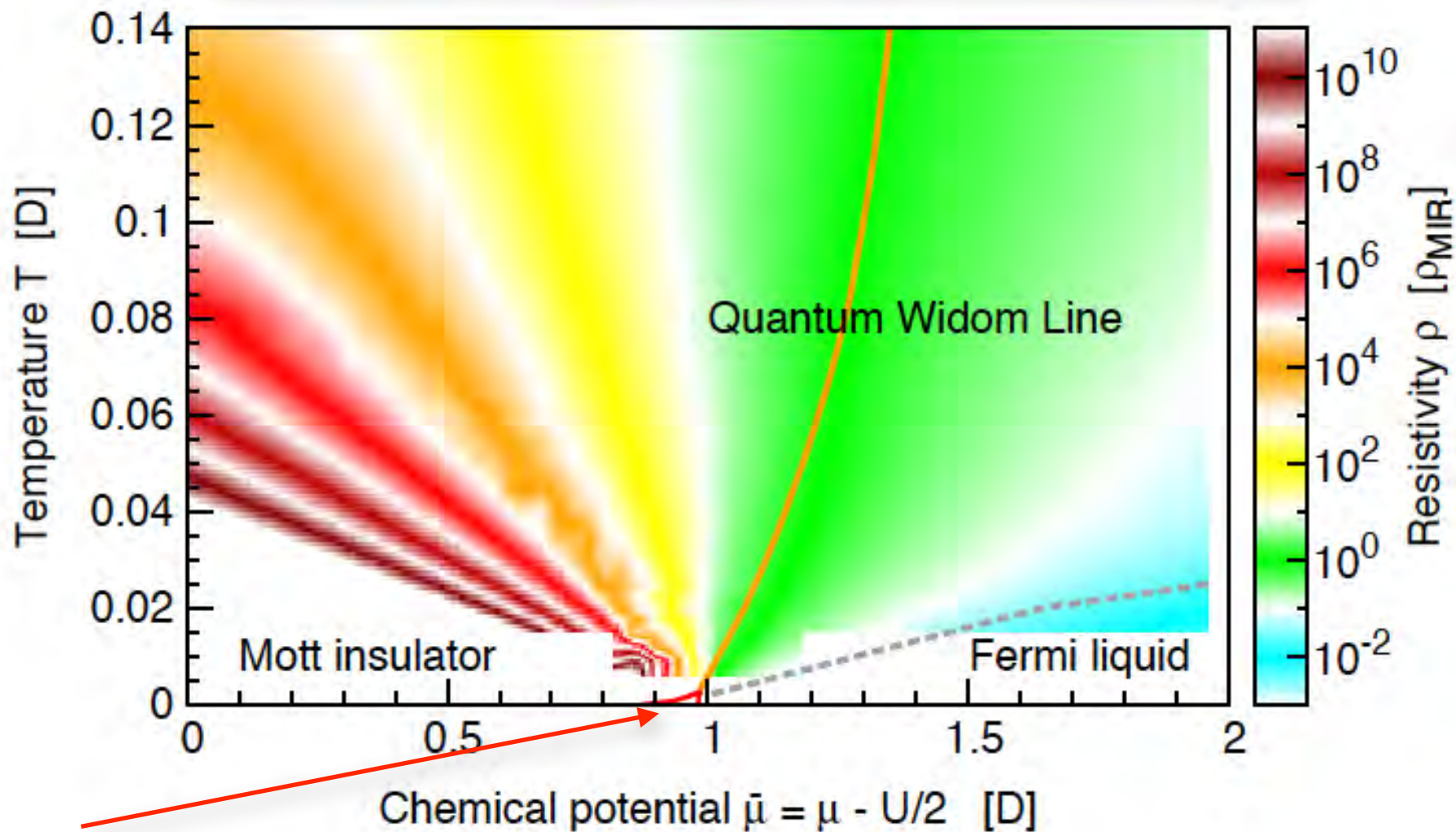
Bad-Metal Behavior Reveals Mott Quantum Criticality in Doped Hubbard Models

J. Vučićević,¹ D. Tanasković,¹ M.J. Rozenberg,² and V. Dobrosavljević³



Doped Mott: DMFT vs. QCP?

J. Vučićević, D. Tanasković, M. Rozenberg, and V. D., 2014

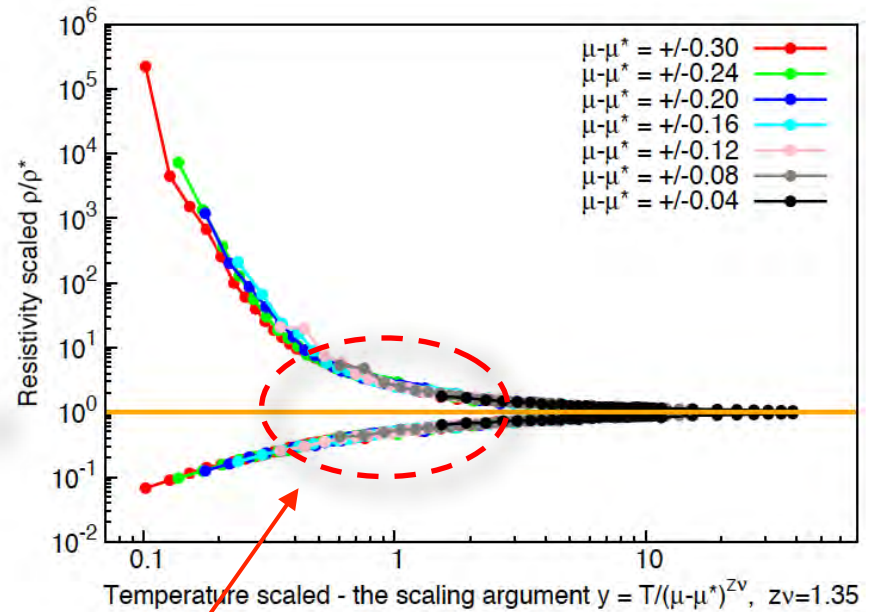
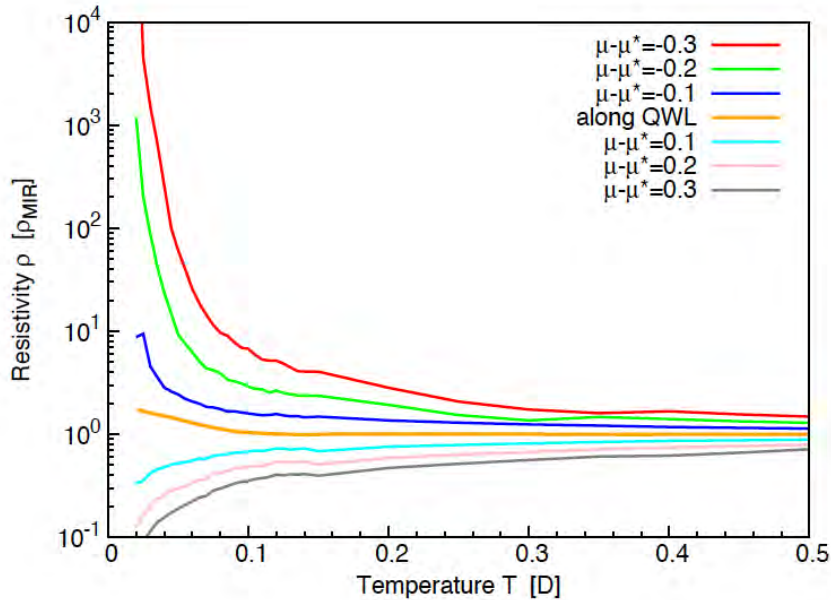


TINY coexistence dome

$T_c = 0.003$

Doped Mott: QC Scaling

J. Vučićević, D. Tanasković, M. Rozenberg, and V. D., 2014



New feature:

Quantum Widom Line - MIR limit

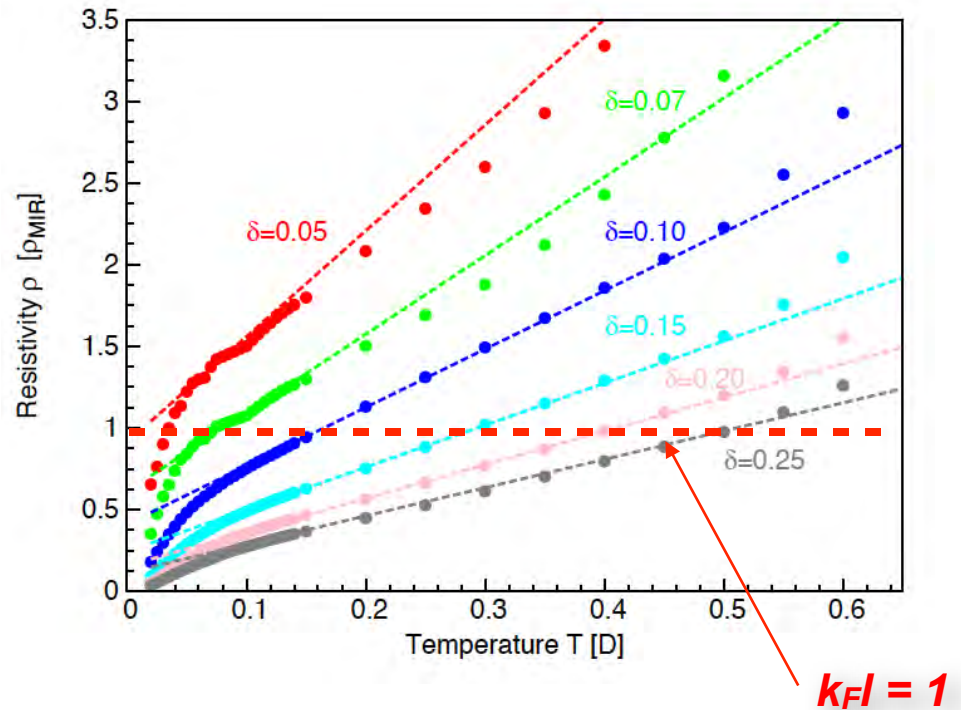
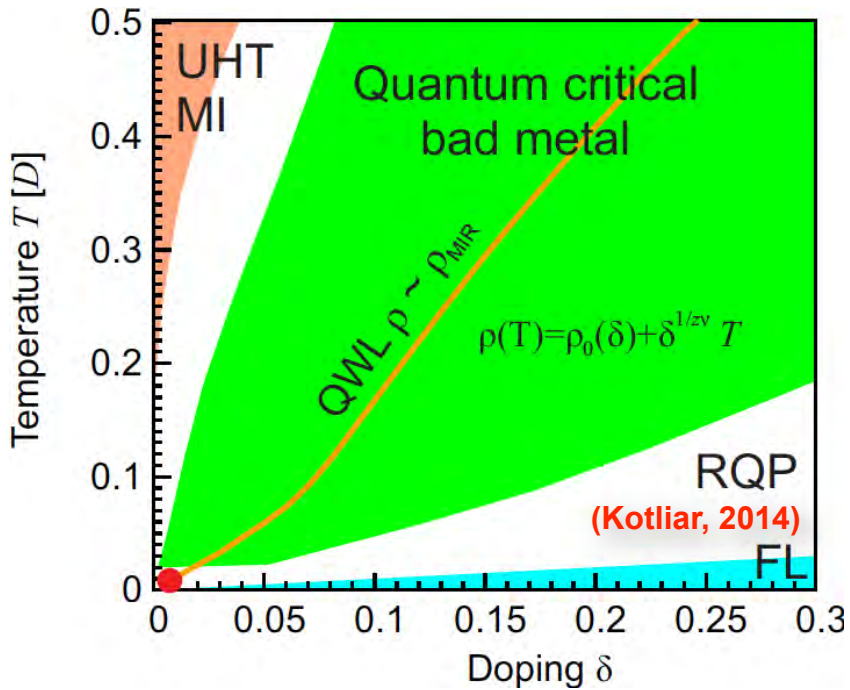
**mirror symmetry:
defines QC region**

$$\rho(T, \mu) = \rho^* \exp\left\{A(\mu - \mu^*(T))/T^{\nu z}\right\}$$

“stretched exponential”

Doped Mott: Quantum Critical Region?

J. Vučićević, D. Tanasković, M. Rozenberg, and V. D., 2014



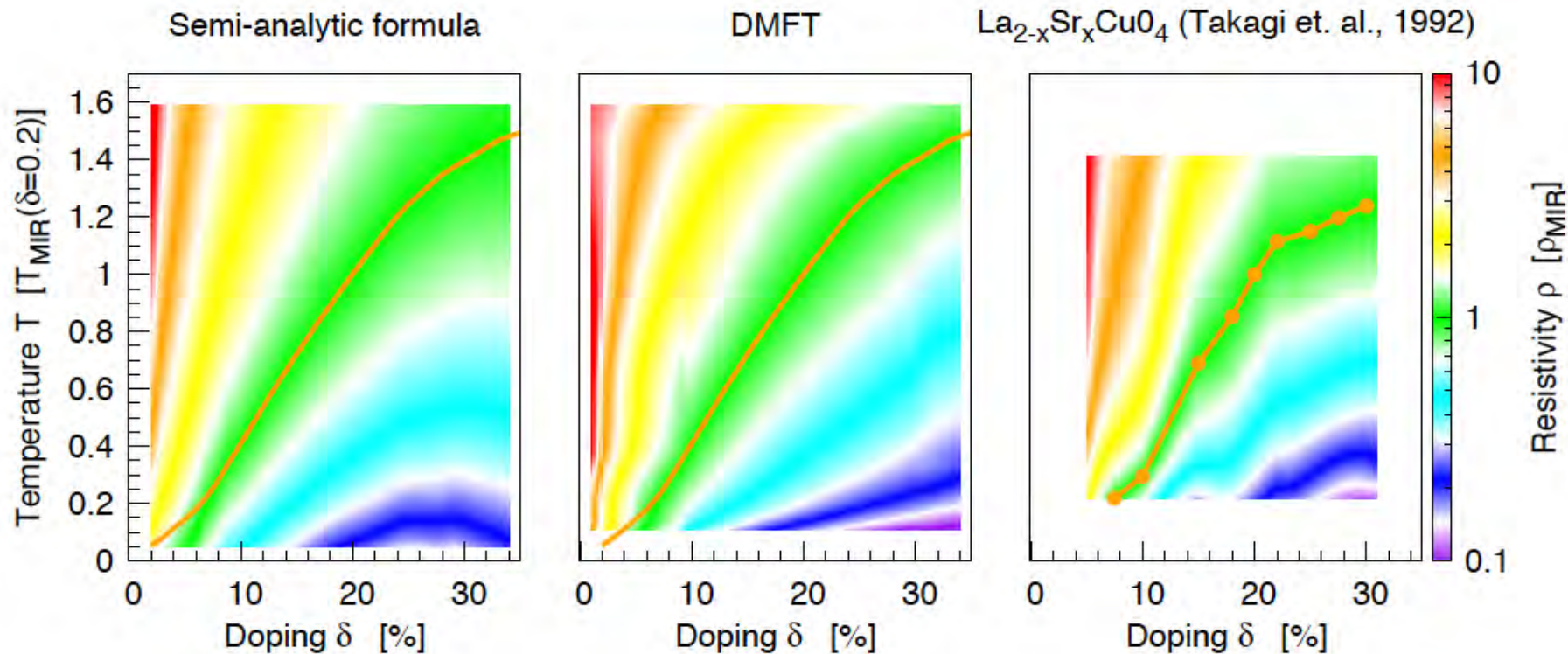
Key Results:

Bad Metal (linear resistivity \sim MIR limit) = Mott QC region

QC Scaling - (semi) analytical formula for linear-T resistivity

Doped Mott: Theory vs. Experiment

J. Vučićević, D. Tanasković, M. Rozenberg, and V. D., 2014



Mott QC region: universal behavior at high temperatures

Moral of the story

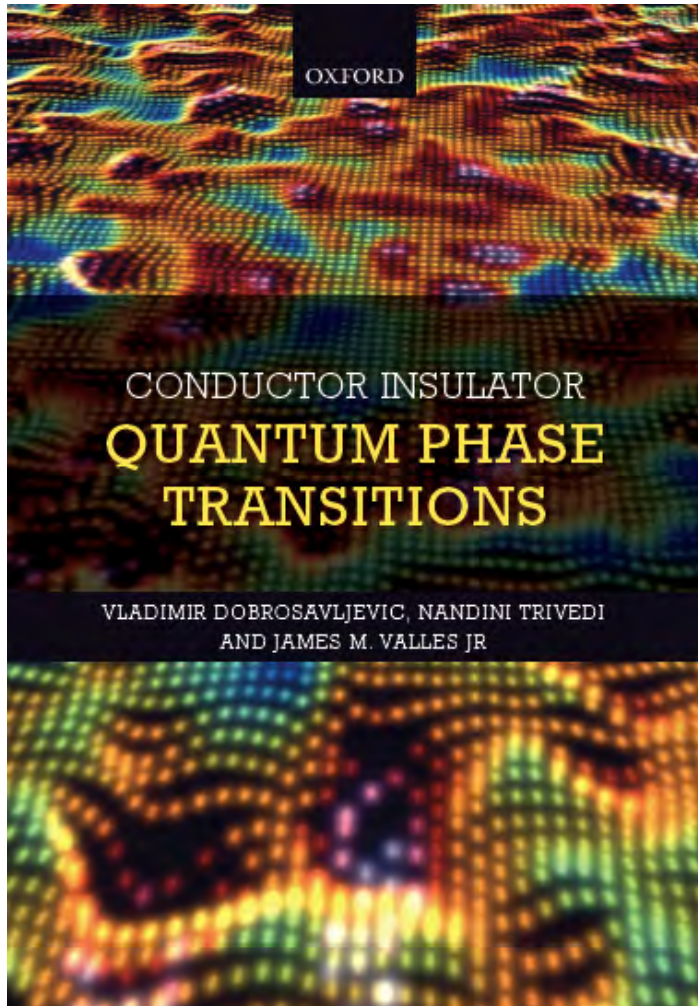
- using words anyone can understand -

*Bad Liquid:
AdS-CFT??*



Viscous (quantum) liquid is not a gas (Landau quasiparticles)

To learn more:



<http://badmetals.magnet.fsu.edu>
(just Google “Bad Metals”)

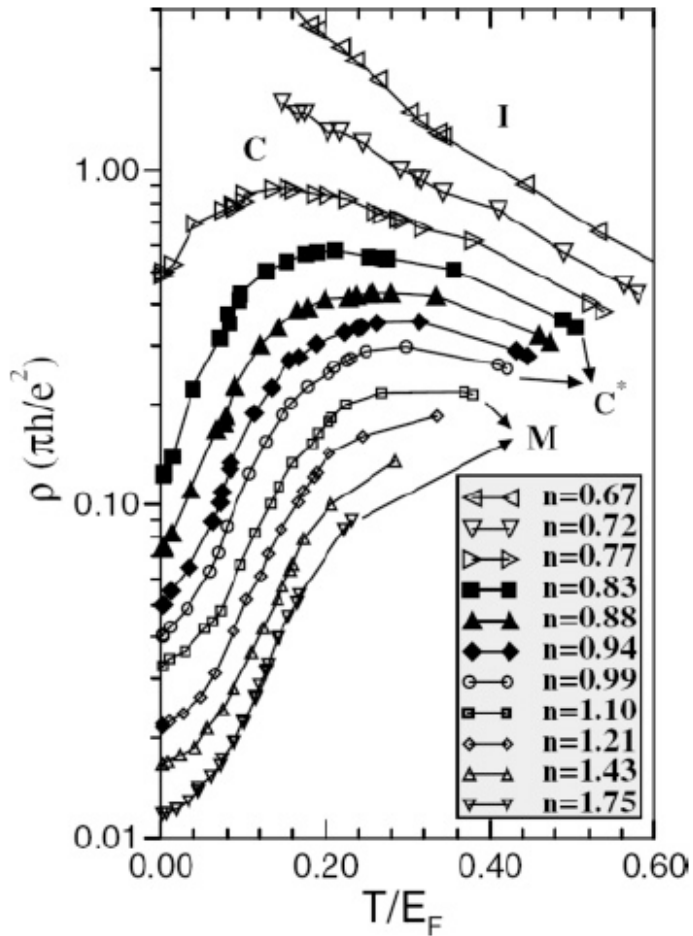
Book:

Oxford University Press, 2012

ISBN 9780199592593

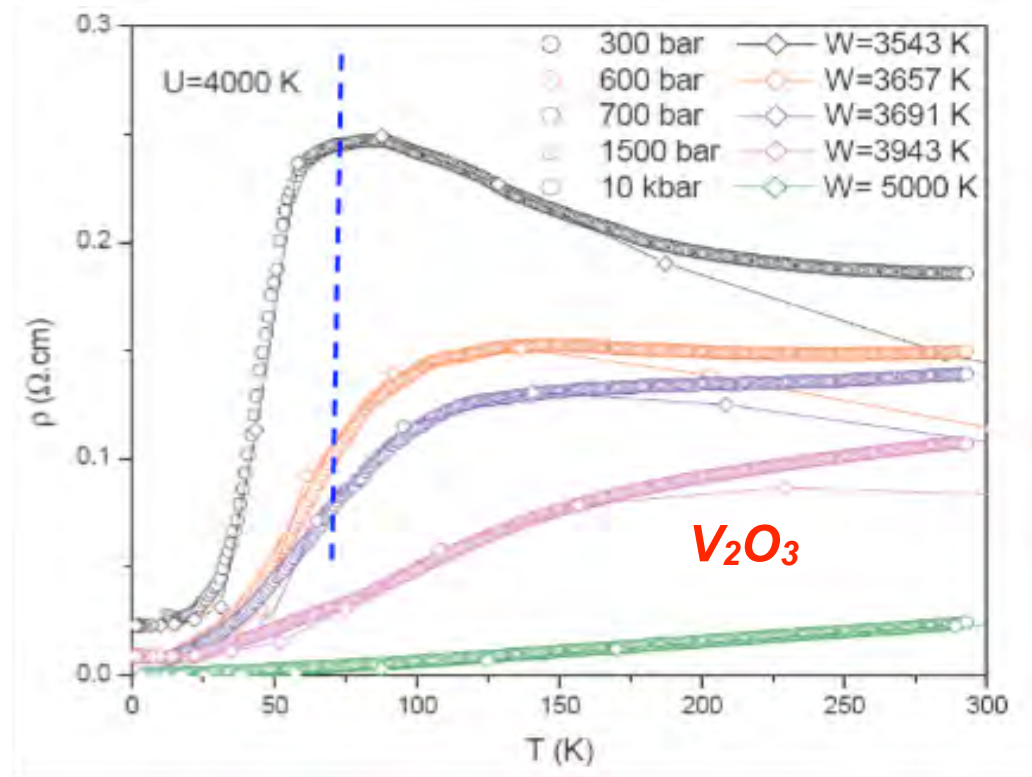
Really, but really bad metals: resistivity maxima (experiments)

MOSFETs



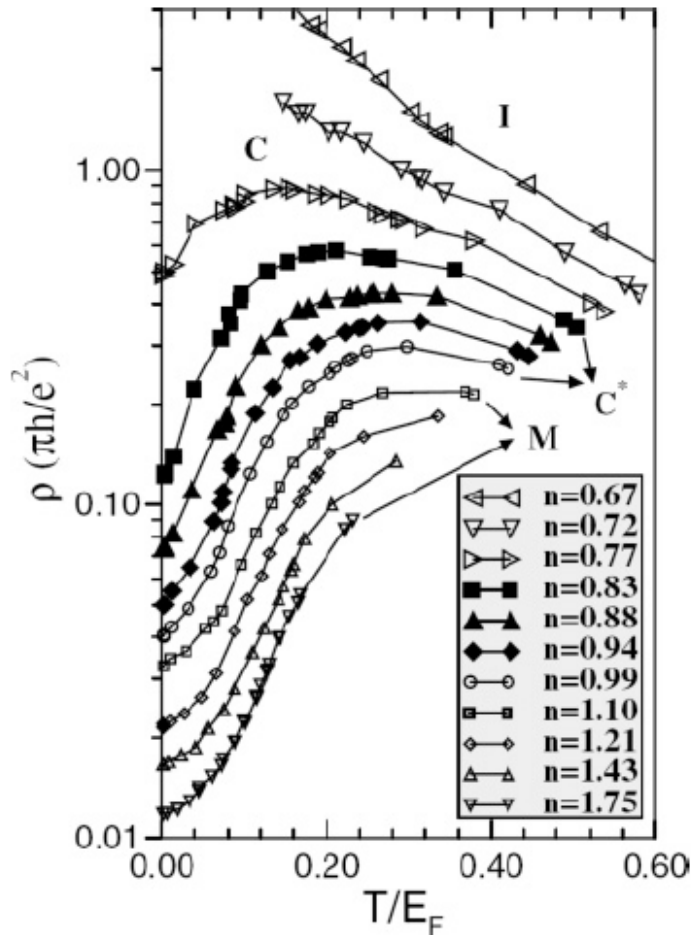
And now...

something completely different



Phenomenological scaling (experiments)

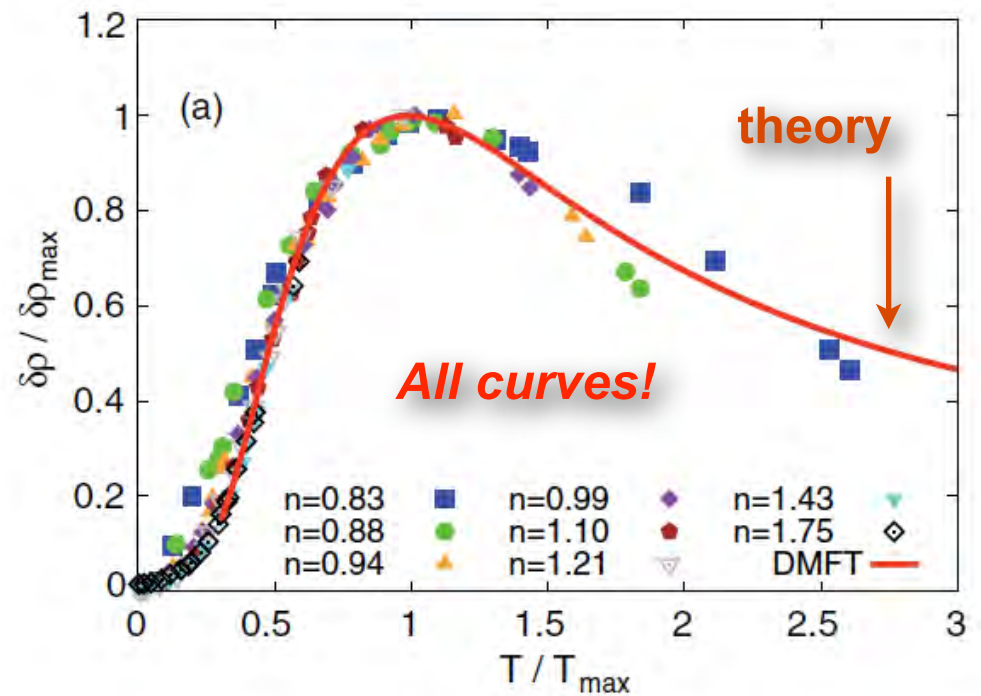
MOSFETs



$$\rho(T) = \rho_o + \delta\rho(T)$$

$$\delta\rho(T) = \delta\rho_{\max} f(T/T_{\max})$$

$$\delta\rho_{\max} = \rho_{\max} - \rho_o$$



Evaporating the Fermi liquid

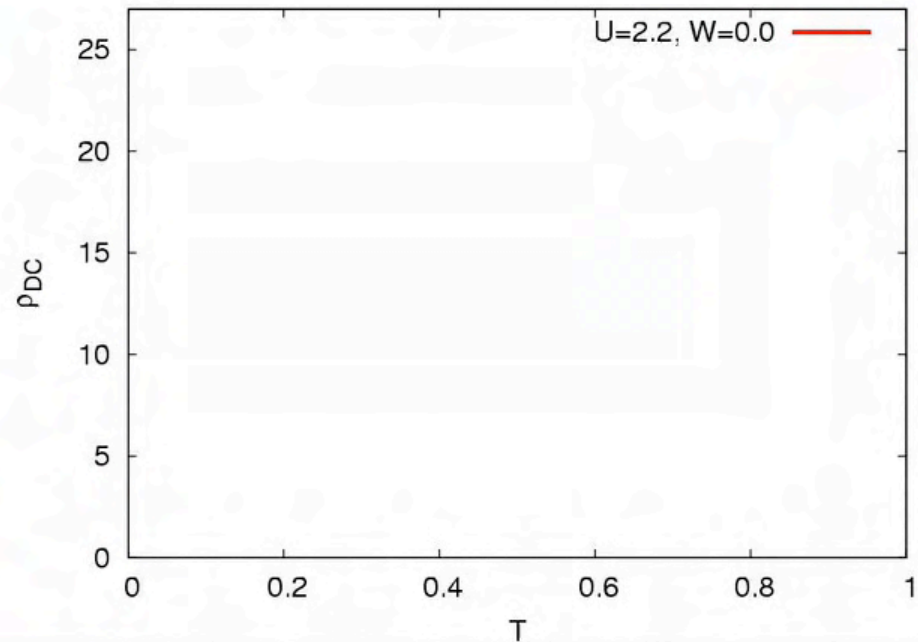
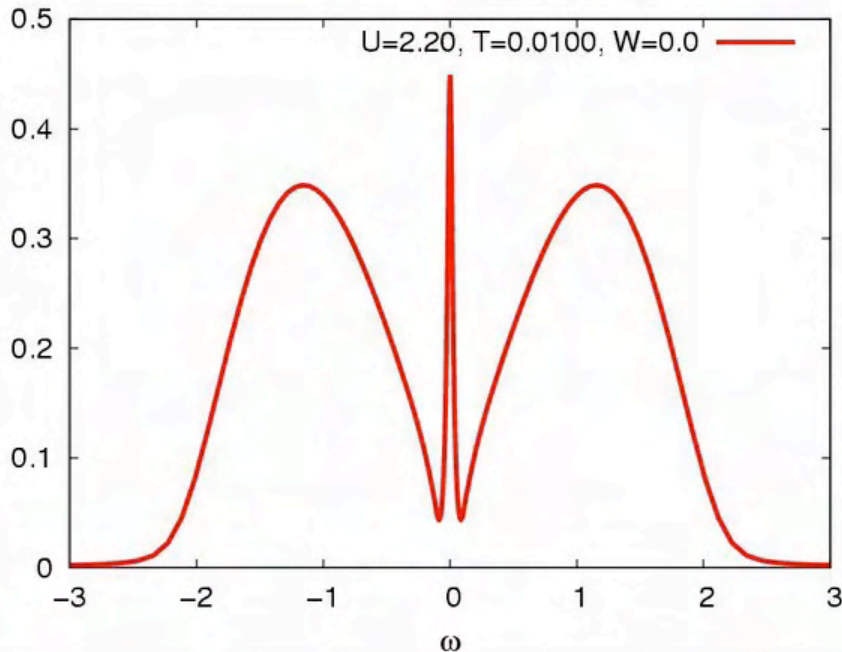
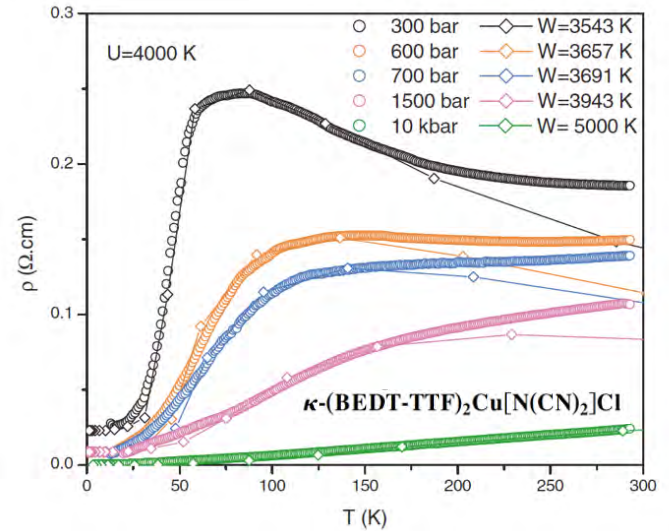


Darko Tanaskovich

Low Fermi liquid
coherence scale

$$T_{FL}^* \sim ZT_F \sim T_F / m^*$$

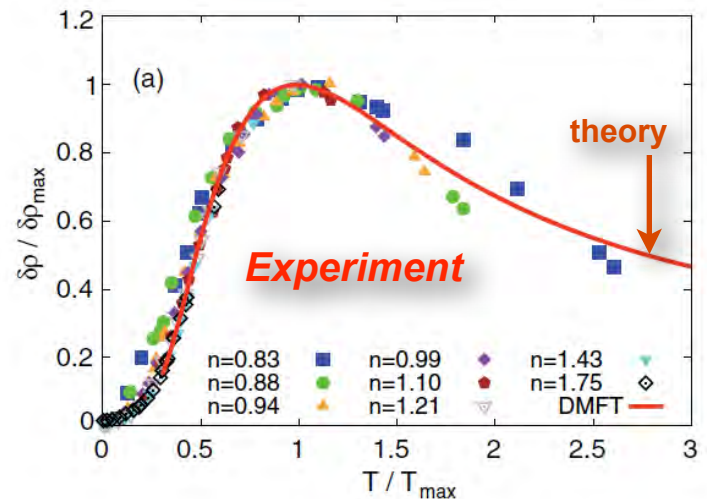
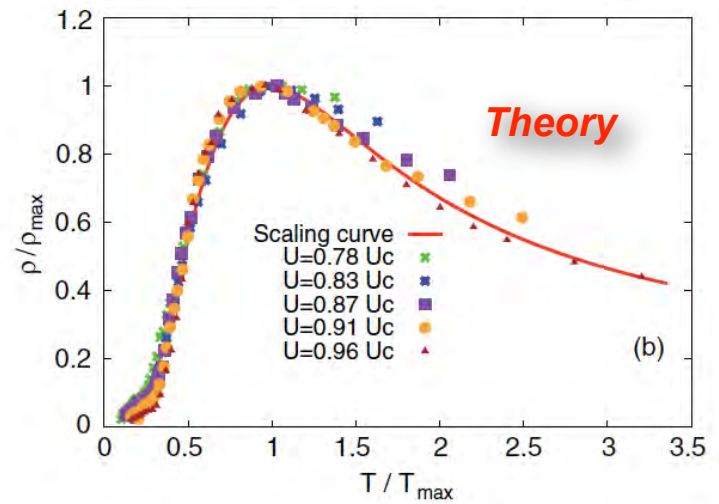
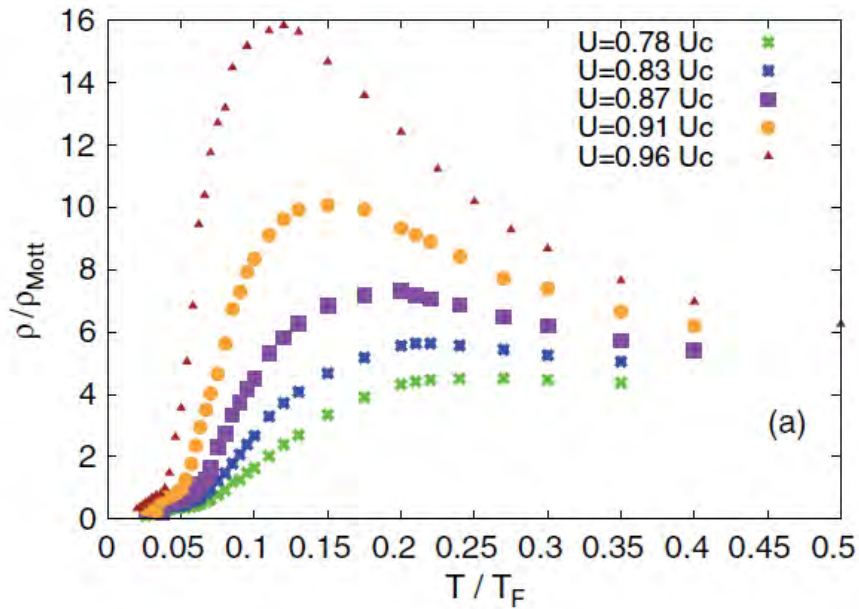
Thermal death of quasi-particles?



Wigner-Mott scaling of transport near the two-dimensional metal-insulator transition

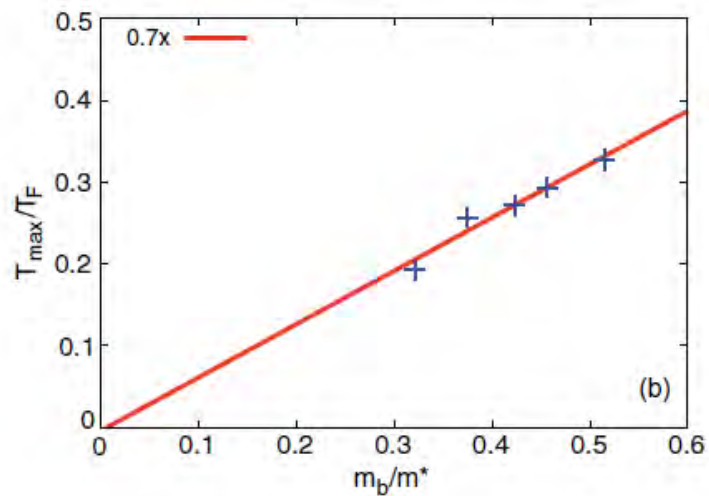
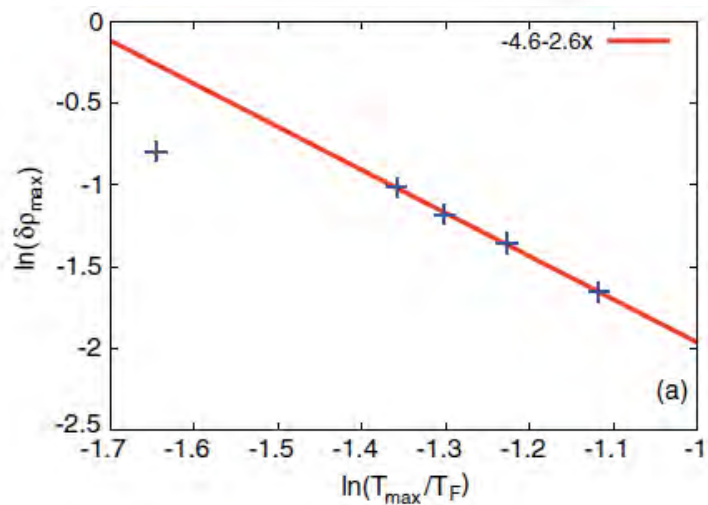
M. M. Radonjić,¹ D. Tanasković,¹ V. Dobrosavljević,² K. Haule,³ and G. Kotliar³

DMFT theory



Approaching the transition - trends

DMFT Theory



Experiments

