

Superconductor-Insulator Transitions in Highly Underdoped Cuprates

Dragana Popović

*National High Magnetic Field Laboratory
Florida State University, Tallahassee, FL, USA*



Support: **NSF grants** (DMR-0905843, DMR-1307075 and previous)
NHMFL (NSF and the State of Florida)

Collaborators:

Experiments at NHMFL/FSU, USA:

Xiaoyan Shi (now at Sandia National Labs, USA → U. Texas at Dallas, USA)

Ivana Raičević (now at FPM Group, USA)

Zhenzhong Shi

Ping V. Lin

Jan Jaroszyński

Paul Baity

Single crystals: **T. Sasagawa**, Tokyo Institute of Technology, Japan

Films (MBE): **G. Logvenov**, Brookhaven National Lab., USA
(now at MPI Stuttgart, Germany)

A. Bollinger, Brookhaven National Lab., USA

I. Božović, Brookhaven National Lab., USA

C. Panagopoulos, Univ. of Crete and FORTH, Greece;
Nanyang Tech. Univ., Singapore

Theory: **V. Dobrosavljević**, Florida State University, USA

L. Benfatto, Sapienza University of Rome, Italy



Questions

1. Strongly correlated 2D systems:

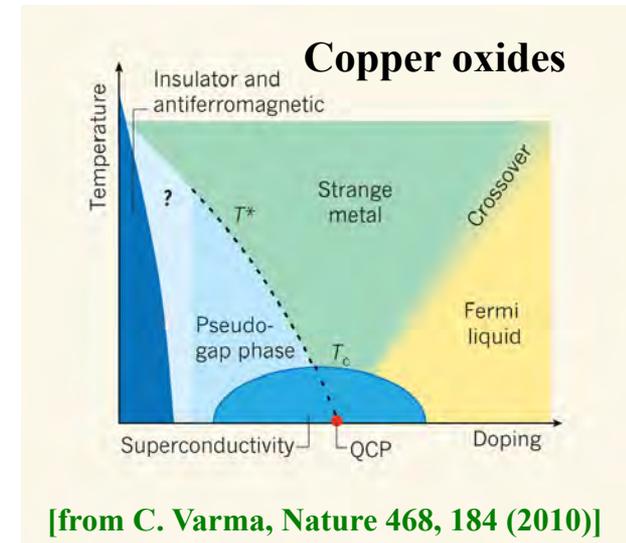
Nature of the **insulating ground state**?

Quantum phase transition from an insulator to a superconductor with doping?

2. Cuprates:

Emergence of high- T_c superconductivity from a doped Mott insulator?

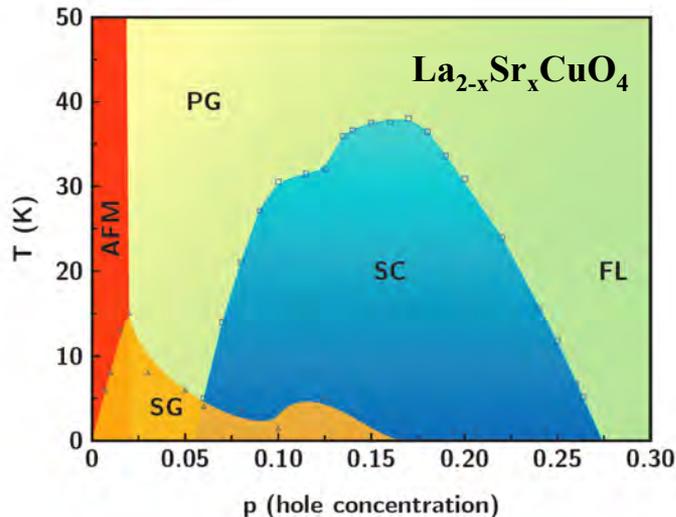
- Quantum criticality
- Role of disorder
- Competing orders
- Vortex matter physics
- ...



Outline

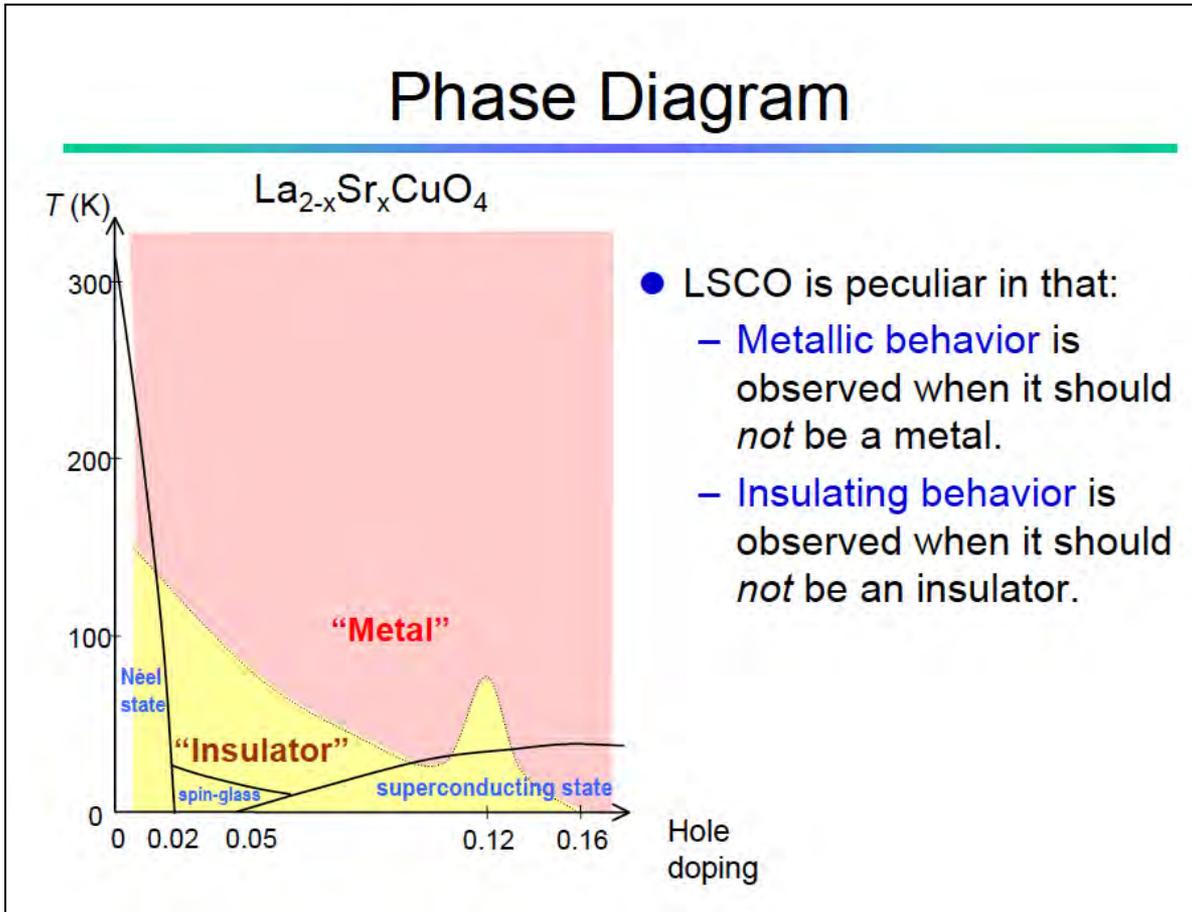
Our experiments on La-based cuprates probe charge order:

- **Nature of the insulating ground state** at low doping:
charge cluster glass
- **Doping-driven transition** from insulator to superconductor:
coexistence and competition between different orders
- **Magnetic-field-driven** superconductor-insulator transition (SIT):
the interplay of quantum criticality and vortex matter physics
- **Dynamics near thermally-driven superconducting transition:**
dynamical heterogeneities



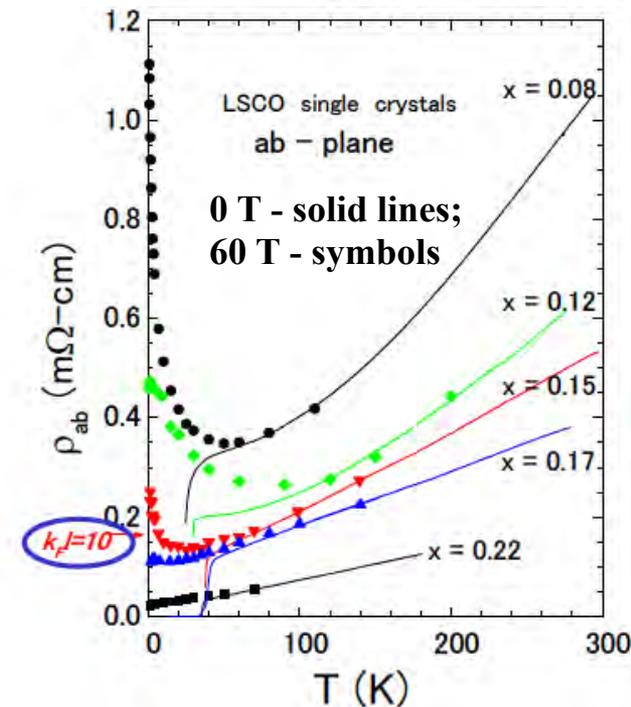
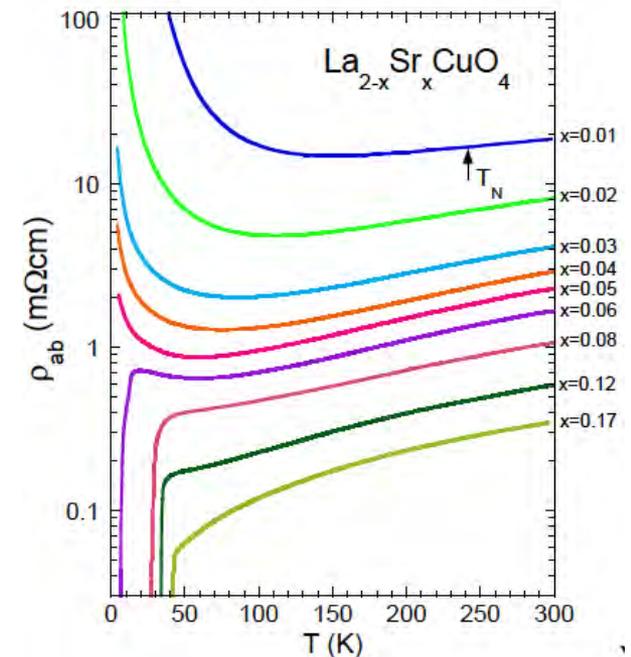
Y. Ando, May 2005 talk in Dresden:

Phase Diagram

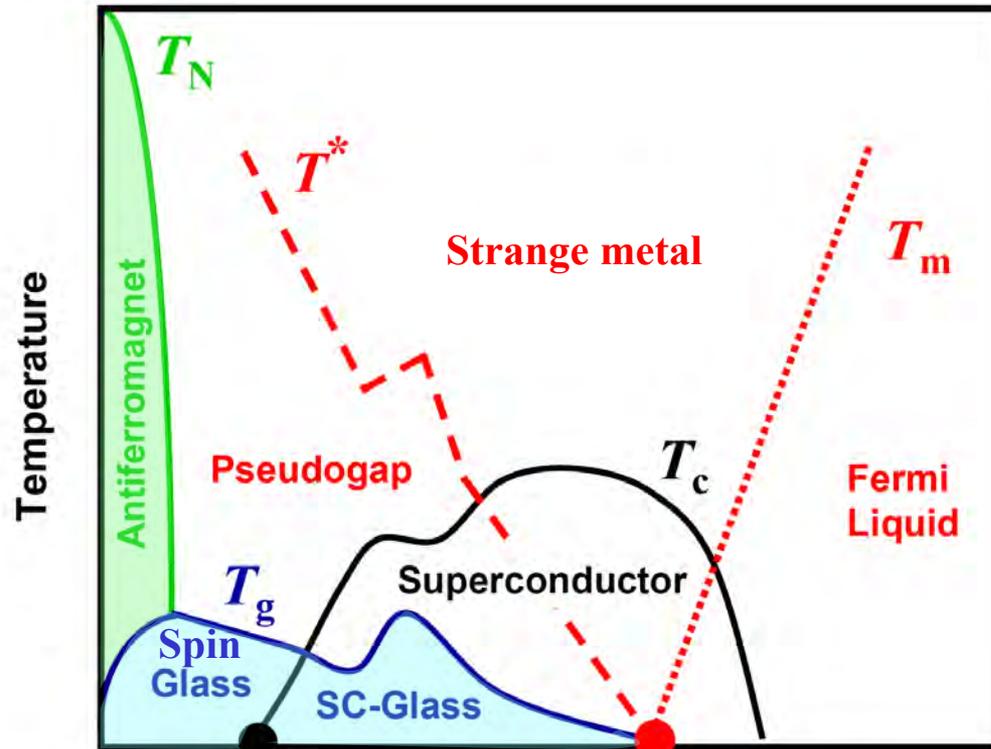


Y.A.: Electron self-organization?

Top right: Ando *et al.*, PRL 87, 017001 (2001);
 Bottom right: Boebinger *et al.*, PRL 77, 5417 (1996).



Nature of the ground states and evolution with doping?



[C. Panagopoulos and V. Dobrosavljević, PRB 72, 014536 (2005) and references therein]

Charge glass insulator
(insulating cluster or stripe glass)

Superconductor-insulator transition

x_{sc}

Carrier concentration

Inhomogeneous, conducting glassy state – bad metal?

x_{opt}

Homogeneous metal

Quantum glass transition?



Lightly doped $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$: Experimental protocols

$\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$

A. Resistance noise spectroscopy: Fluctuations

• PDFs, power spectrum, second spectrum

[Raičević *et al.*, Proc. SPIE 6600, 660020 (2007); Phys. Rev. Lett. 101, 177004 (2008); Phys. Rev. B 83, 195133 (2011)]

B. History-dependent transport

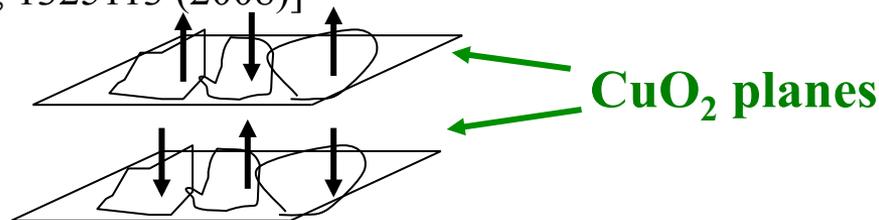
1) Zero-field cooled vs. field-cooled resistance

2) Hysteretic magnetoresistance

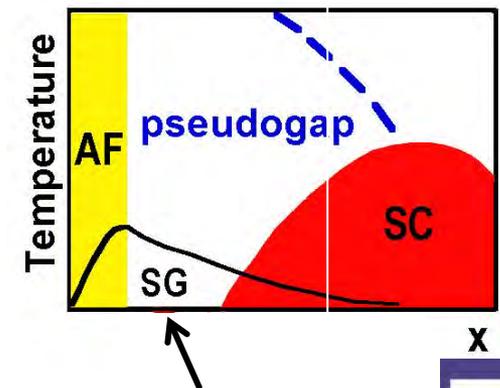
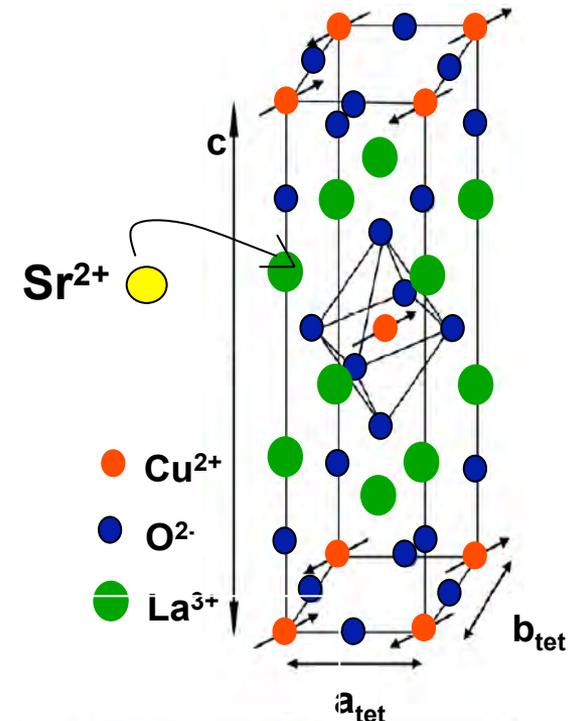
[Raičević *et al.*, Phys. Rev. B 81, 235104 (2010); J. Supercond. Nov. Magn. 25, 1239 (2012); Shi *et al.*, Physica B 86, 155135 (2012); Nature Mater. 12, 47 (2013)]

C. Dielectric measurements

[Park *et al.*, Phys. Rev. Lett. 94, 017002 (2005); Jelbert *et al.*, Phys. Rev. B 78, 1325113 (2008)]

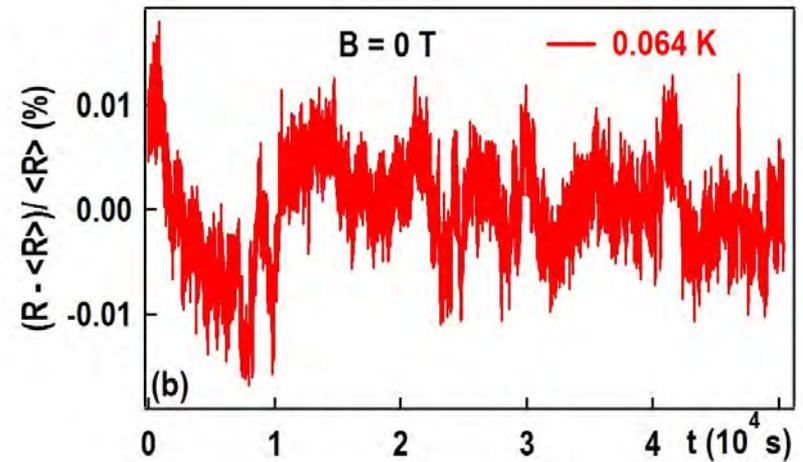
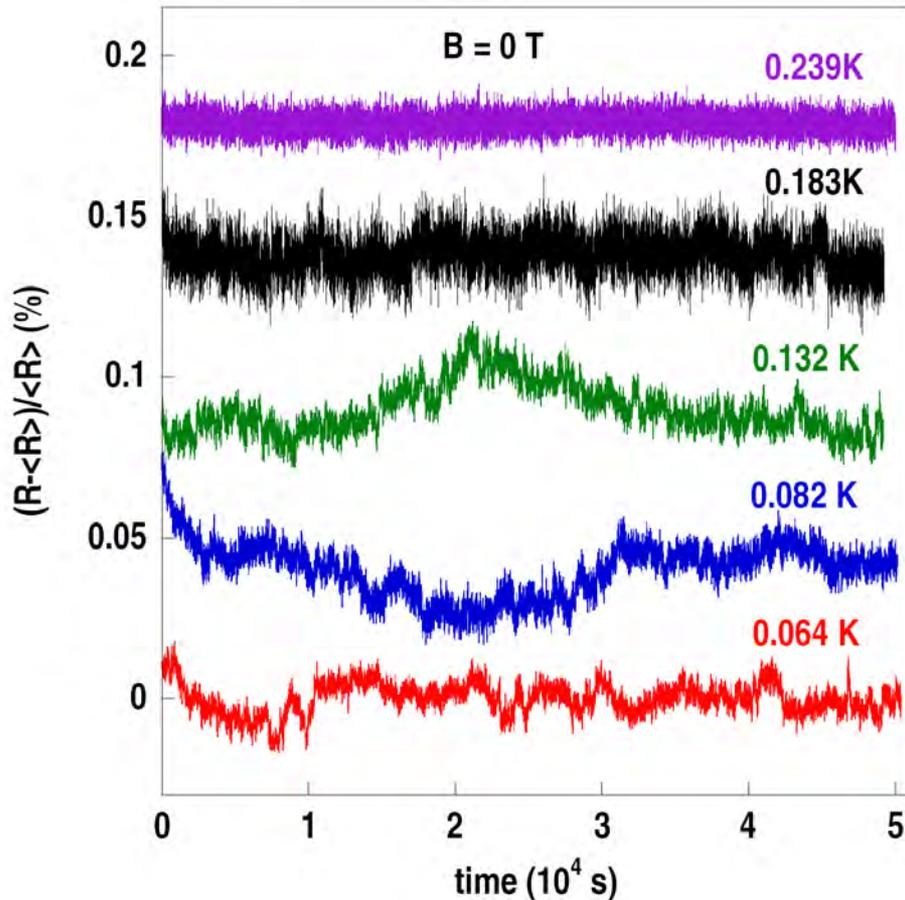


**Short-range AF order: in-plane AF domains;
holes in domain walls**



In-plane resistance fluctuations (noise)

- Single crystal $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$, $x=0.03$; $T_{\text{SG}} = 7-8$ K
- Variable-range hopping transport at low T



- noise: Gaussian at “high” T
- at low T (< 0.2 K), non-Gaussian noise metastable states (*out-of-equilibrium*)

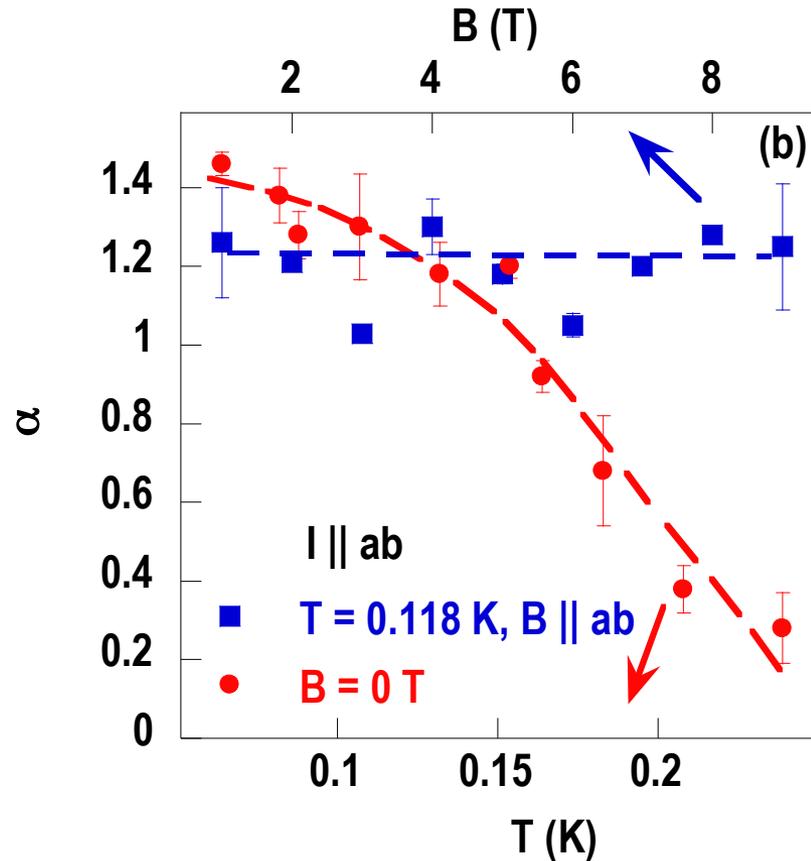


Noise statistics

- Very low T: magnetic background frozen
- Power spectrum: $S_R \sim 1/f^\alpha$

Slowing down of the dynamics
as $T \rightarrow 0$

- Increasing non-Gaussianity of the noise as $T \rightarrow 0$



Second spectrum (S_2) – “noise of the noise”

(Voss&Clarke, Restle&Weissman, Seidler&Solin)

- $S_2(f_2, f)$: power spectrum of the fluctuations of $S_R(f)$ with time
(Fourier transform of the autocorrelation function of the time series of $S_R(f)$; fourth-order noise statistic)

$$S_2 \propto 1/f_2^{1-\beta}$$

$1-\beta = 0$ \Rightarrow Gaussian (uncorrelated)

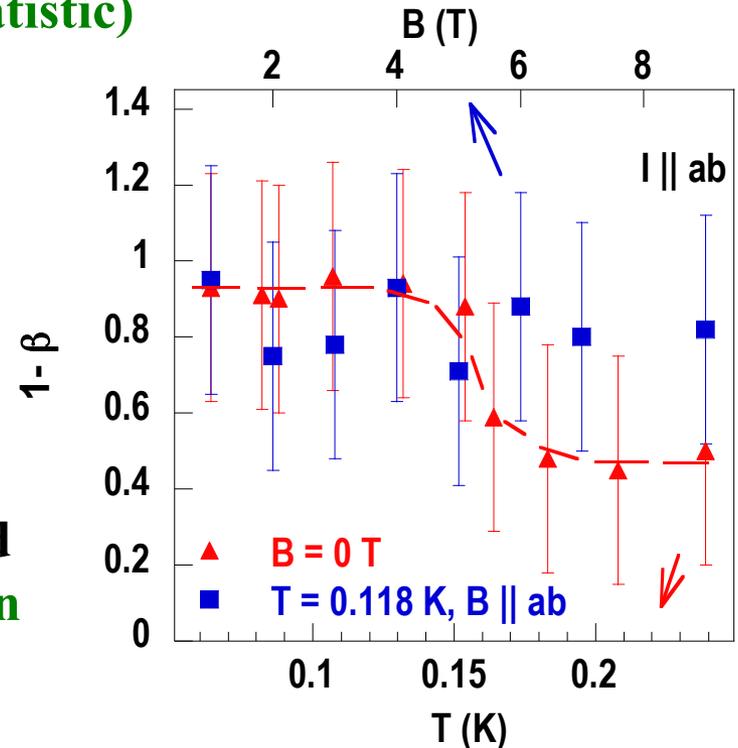
$1-\beta > 0$ \Rightarrow non-Gaussian (correlated)

Increase of correlations as $T \rightarrow 0$

- Noise statistics independent of both B and magnetic history (unlike conventional spin glasses, but like a spin-polarized 2DES)

\Rightarrow charge, not spin!

\Rightarrow Charge glass transition $T_{cg}=0$



Scaling of the second spectra

Measure of correlations

- can distinguish between different models (**Weissman**):
 - interacting droplet model
 - hierarchical, tree-like model

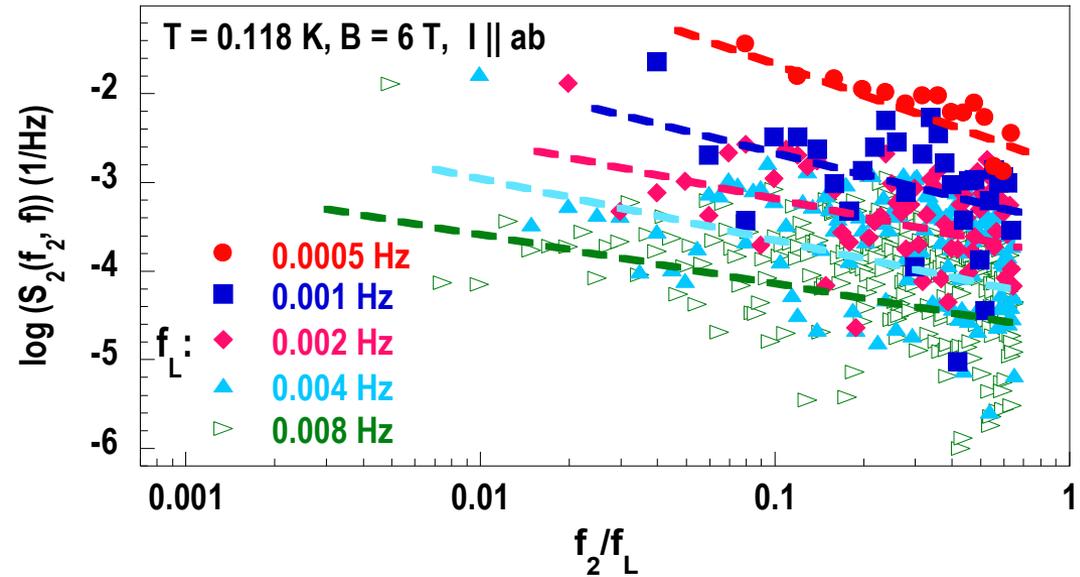
S_2 decreases with f
for a fixed f_2/f ,

consistent with **droplet** picture
(**short-range interactions**)

Competing interactions
on different length scales

Charge cluster glass

$\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$, $x=0.03$



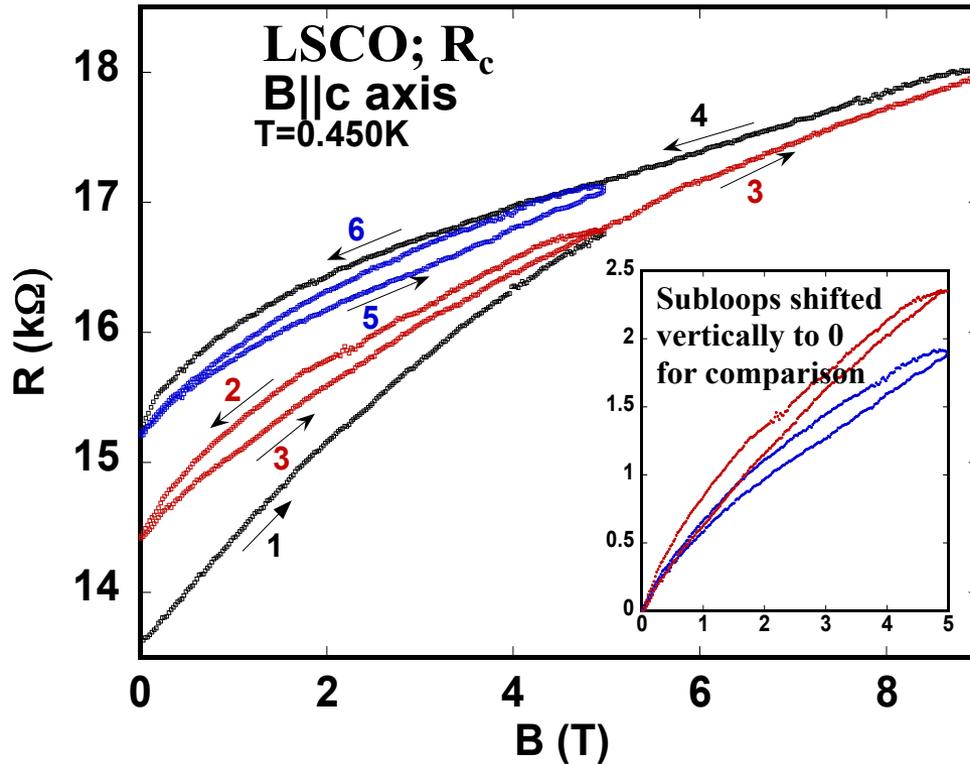
(Schmalian and Wolynes, PRL 85, 836 (2000):
“stripe” glass in a model with competing
interactions on different length scales,
NO disorder)

Different from metallic spin glasses
and a 2D Coulomb glass – systems with
long-range interactions: hierarchical!



History dependence in transport in non-SC samples: $T_{\text{onset}} \ll T_{\text{sg}}$

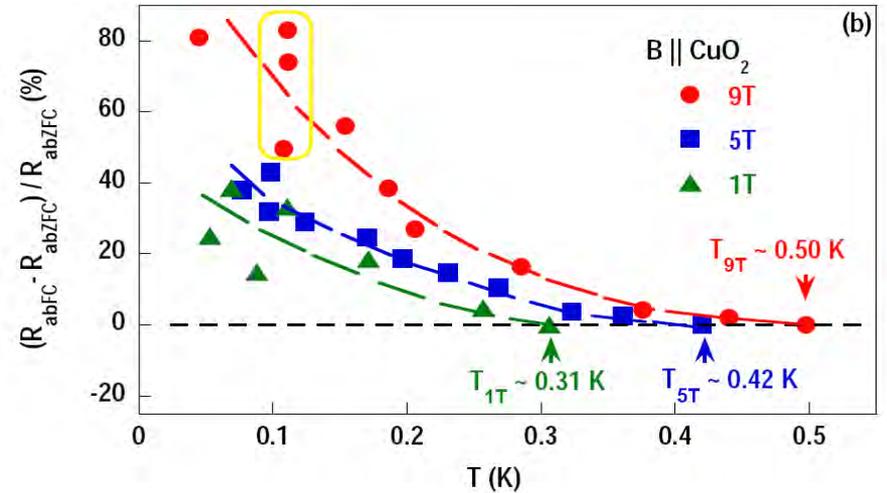
Hysteretic behavior of the low-T positive MR



Memory in R erased for $T \geq 1\text{K}$, $T_{\text{SG}} \approx 7\text{K}$: holes do not merely “follow” the spins

$(R_c, R_{ab}; B \parallel c$ and $B \parallel ab)$

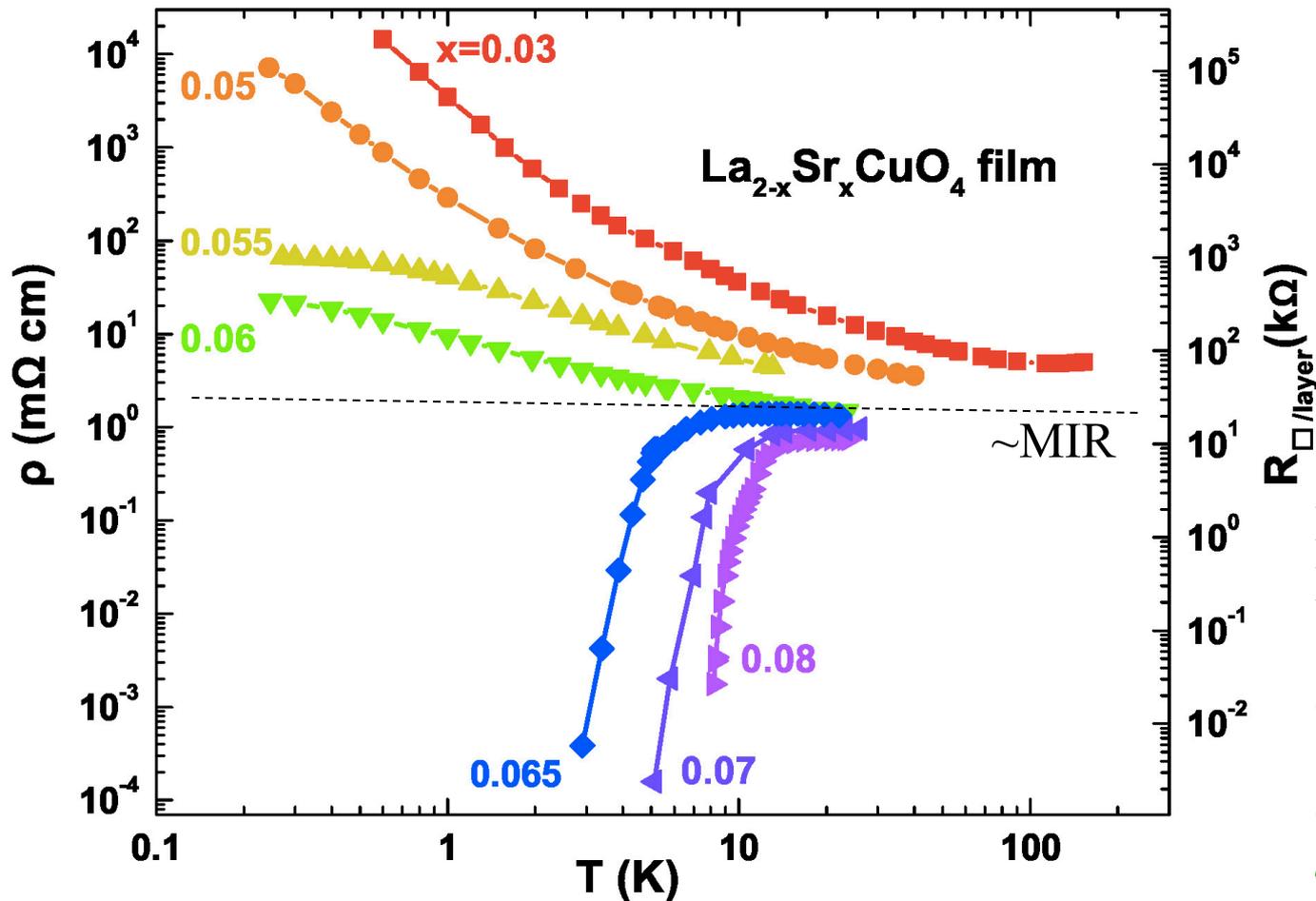
Difference between field-cooled and zero-field cooled resistance $R(B=0)$



Use these effects as “easy tools” for detecting charge glassiness as a function of doping.



Temperature dependence of the in-plane resistivity



x	T_c (K) (midpoint)
0.065	6 ± 1
0.07	9 ± 1
0.08	12 ± 1

$$R_{\square} = \rho / d,$$

$$R_{\square/\text{layer}} = \rho / l,$$

d – sample thickness
(~100 nm);
 $d = nl$; n - # of layers;
 $l = 6.6 \text{ \AA}$ – thickness of
 one layer

$x=0.03$ and $x=0.05$: 2D variable-range hopping

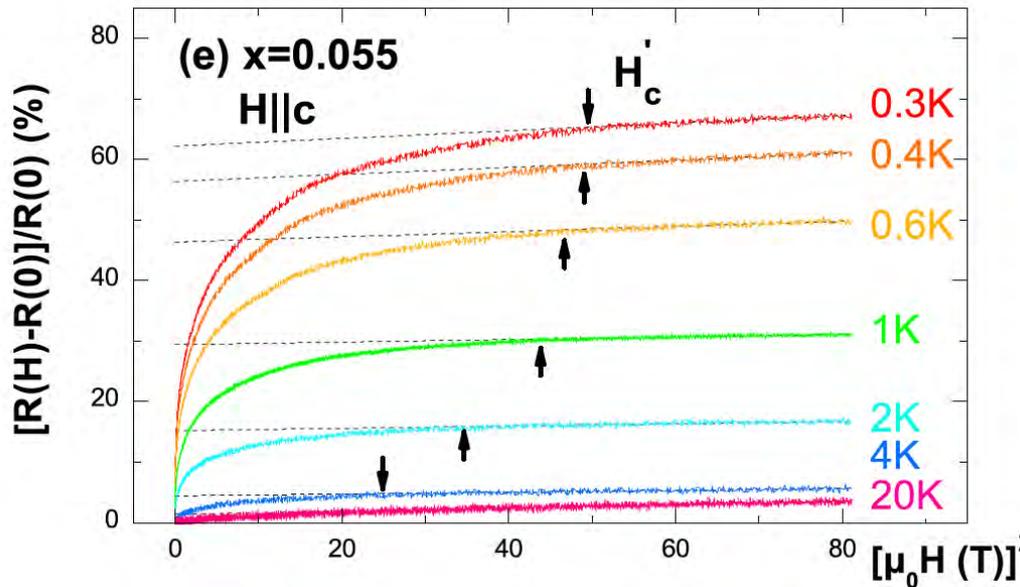
$x=0.055$ and $x=0.06$: non-SC; $\rho(T)$ cannot be fitted to any simple form

$x \geq 0.065$: SC



High-field magnetoresistance and superconducting fluctuations

Non-SC sample



Normal-state resistivity (dashed lines) at low fields:

$$\rho_n(H) = \rho_n(H=0) + \alpha H^2$$

(Max $\omega_c \tau \approx 0.01$ at ~ 10 T)

$H'_c(T)$ – field above which SCFs are suppressed and normal state is restored

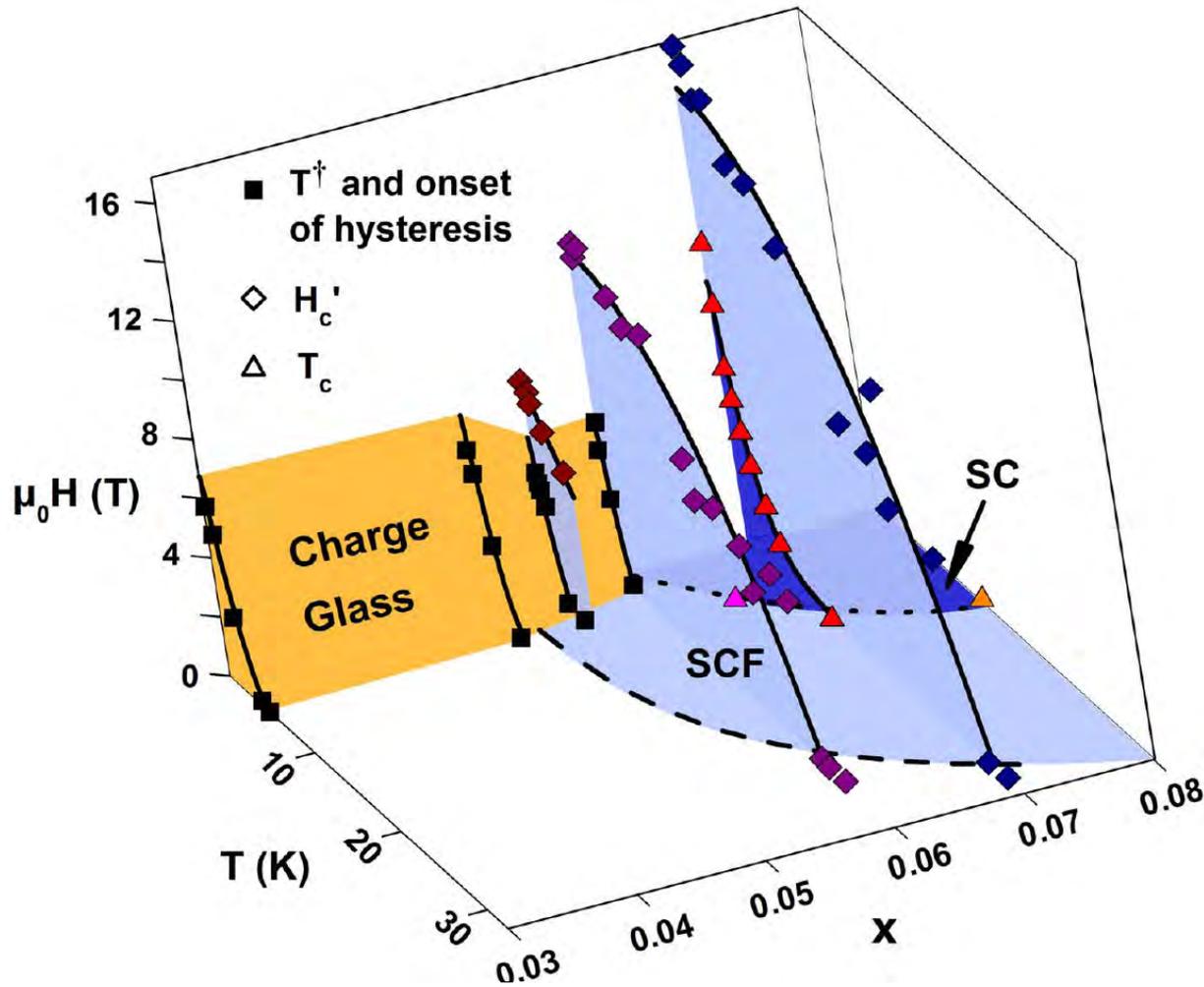
Contribution to conductivity from SCFs:

$$\Delta\sigma_{SCF}(T,H) = \rho^{-1}(T,H) - \rho_n^{-1}(T,H)$$

LSCO: Harris *et al.*, PRL 75, 1391 (1995), Rourke *et al.*, Nature Phys. 7, 455 (2011); Shi *et al.*, Nature Mater. 12, 47 (2013); Shi *et al.*, Nature Phys. 10, 437 (2014)
YBCO: Rullier-Albenque *et al.*, PRL 99, 027003 (2007); PRB 84, 014522 (2011)



Doping-driven superconductor-insulator transition in $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$



- Charge glass in the insulating regime at low doping

- Suppression of charge glassiness with doping

- Coexistence and competition of charge glass with superconducting fluctuations (SCFs) on the insulating side of the superconductor-insulator transition (SIT)

Onset of SIT influenced by charge glass order

[X. Shi *et al.*, *Nature Mater.* 12, 47 (2013)]

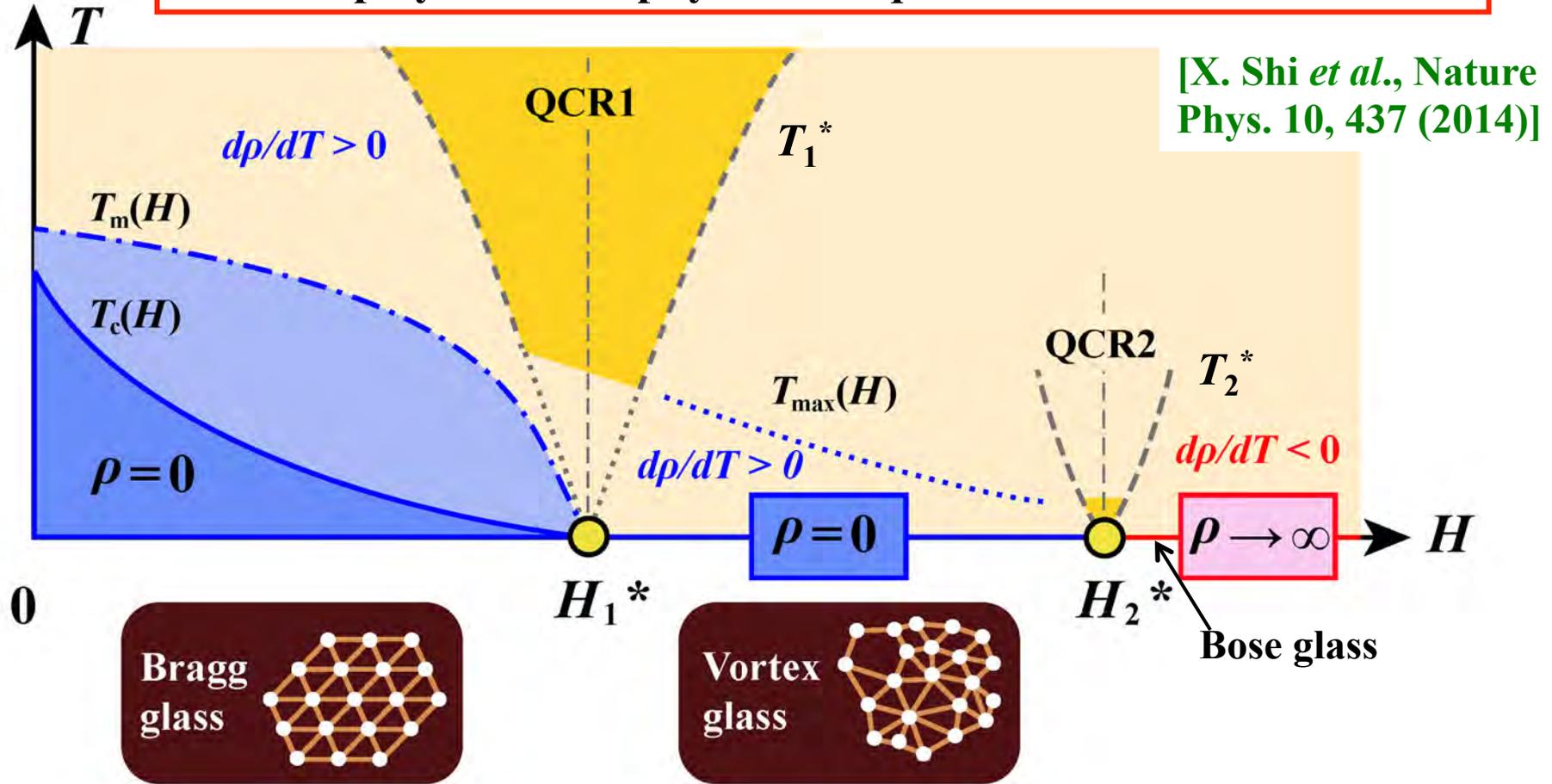


***H*-field-driven superconductor-insulator transition in cuprates**

- **Questions:**
 - **Zero-temperature *H*-field-driven superconductor-insulator transition (SIT) in 2D? Quantum criticality? (scaling)**
(See “Conductor-Insulator Quantum Phase Transitions”, ed. by Dobrosavljević, Trivedi, Valles; Oxford University Press, 2012, for review and open questions)
 - **Nature of the field-induced resistive state?**
 - **Interplay of quantum criticality and vortex matter physics?**
- **Experiments:**
 - **Magnetoresistance over a wide range of *H* and *T* (down to 0.09 K)**
 - **Low- T_c (~ 4 K) $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ samples grown using different methods**
- **Conclusions:**
 - **Three distinct phases as $T \rightarrow 0$; two quantum critical points**



Sketch of the (T, H) phase diagram in underdoped $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$:
Interplay of vortex physics and quantum critical behavior



$$T_1^* \sim |\delta|^{z\nu}, z\nu \sim 0.7$$

2D SIT in the clean limit

$$(R_{\square}/\text{layer} \approx 18 \text{ k}\Omega)$$

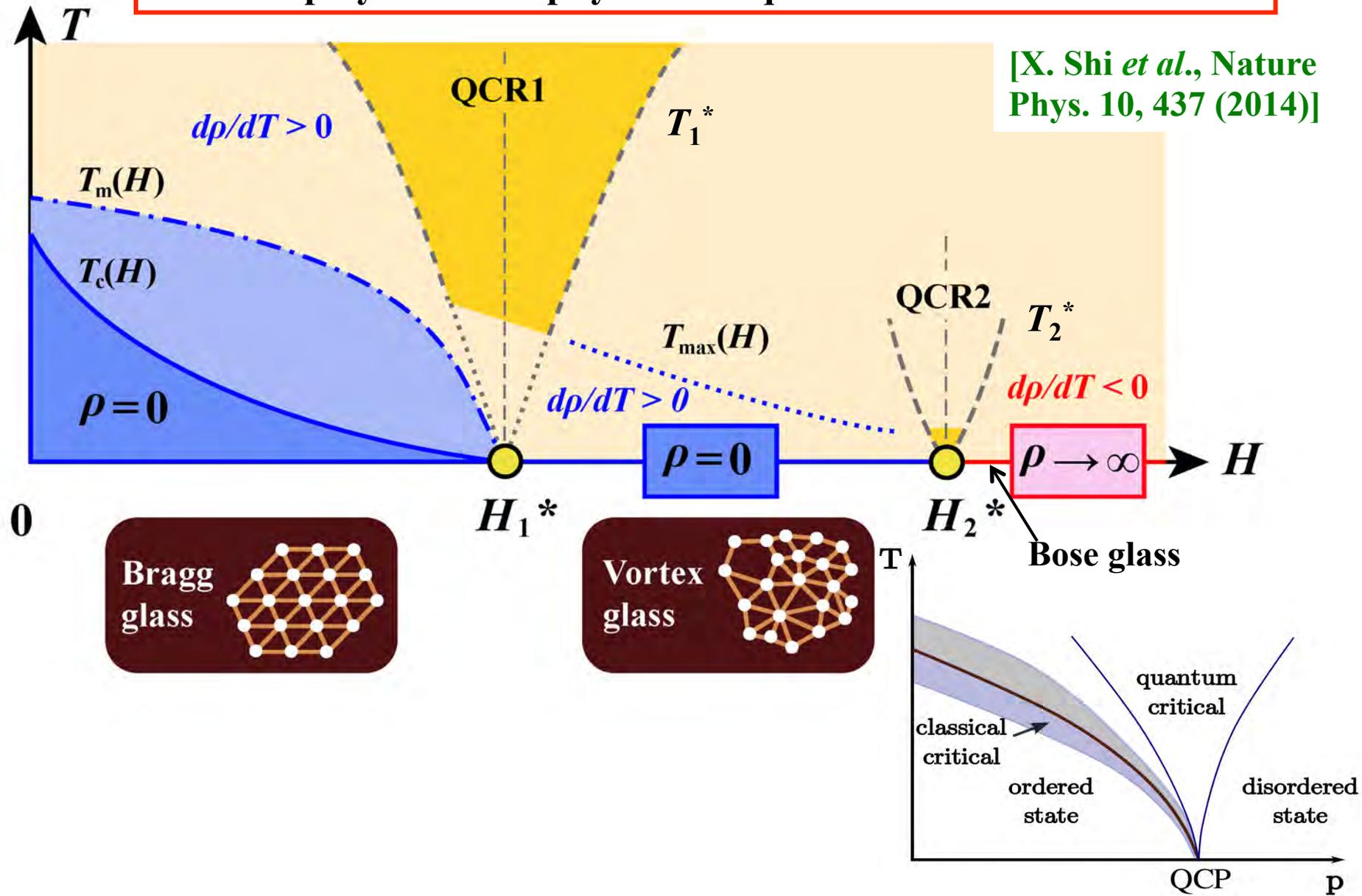
$$T_2^* \sim |\delta|^{z\nu}, z\nu \approx 1.15$$

2D SIT in the dirty limit

$$(R_{\square}/\text{layer} \approx 97 \text{ k}\Omega)$$

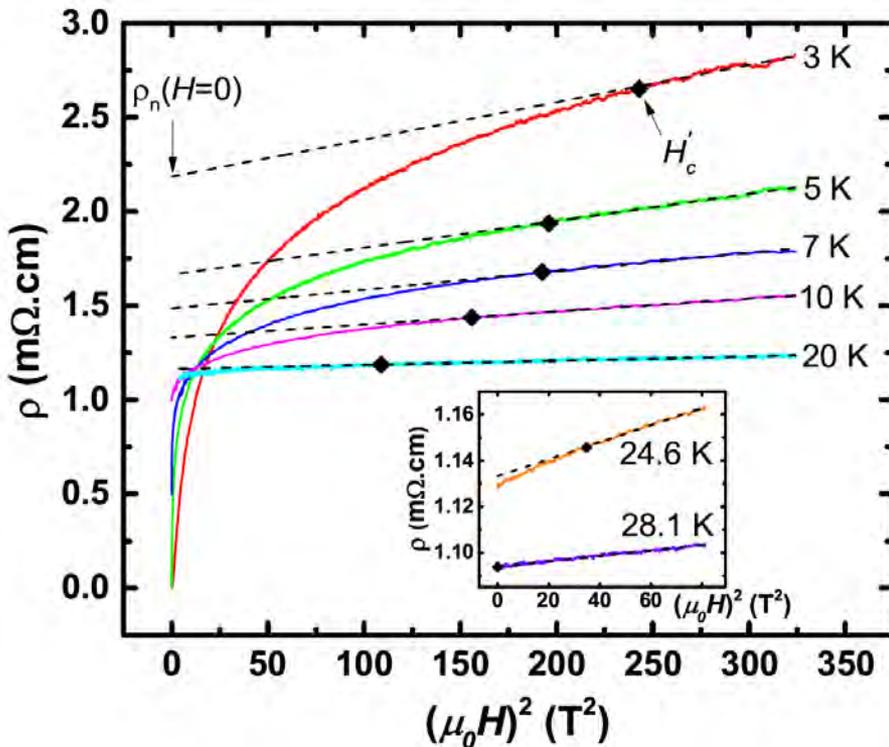


Sketch of the (T, H) phase diagram in underdoped $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$:
Interplay of vortex physics and quantum critical behavior



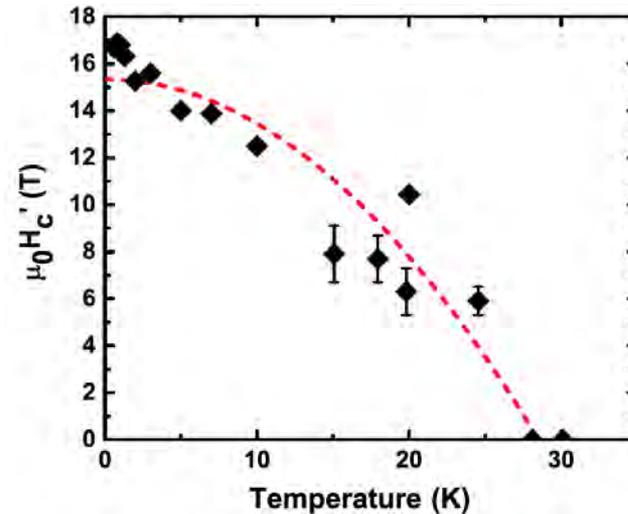
$H=0$ thermally-driven superconducting transition in a highly underdoped $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$

Extent of SCFs from MR:

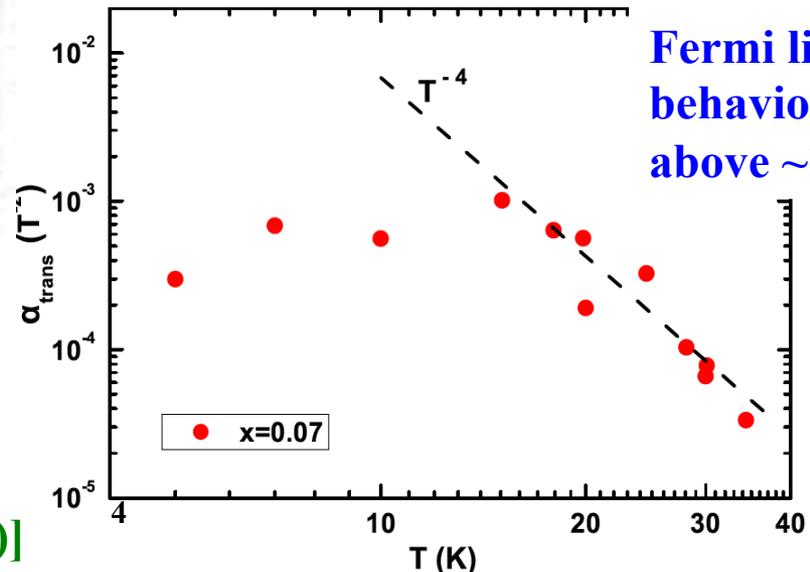


$$[\rho_n(H) - \rho_n(0)]/\rho_n(0) = \alpha_{\text{trans}} H^2$$

[X. Shi *et al.* (unpublished)]



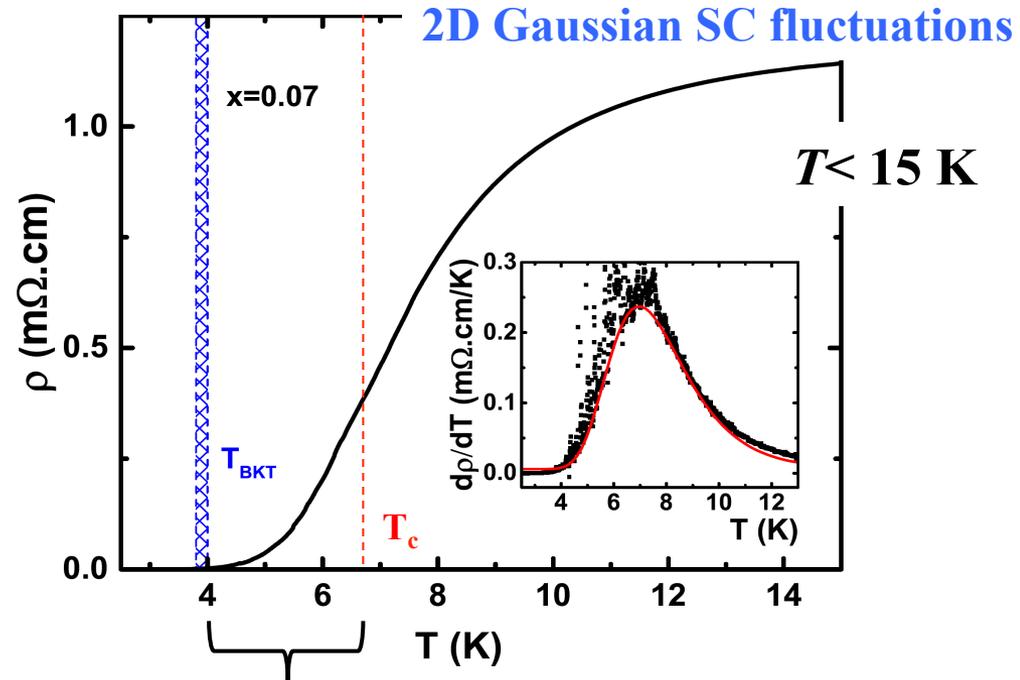
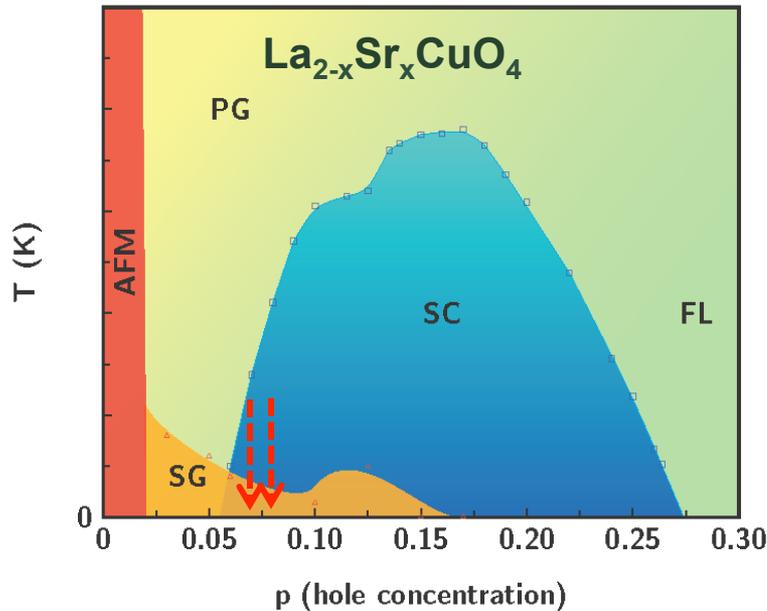
$x=0.07$
 $T_{R=0} \approx 4 \text{ K}$



Fermi liquid
behavior
above $\sim 15 \text{ K}$



$H=0$ thermally-driven superconducting transition in a highly underdoped $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$



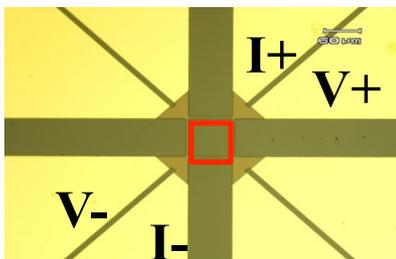
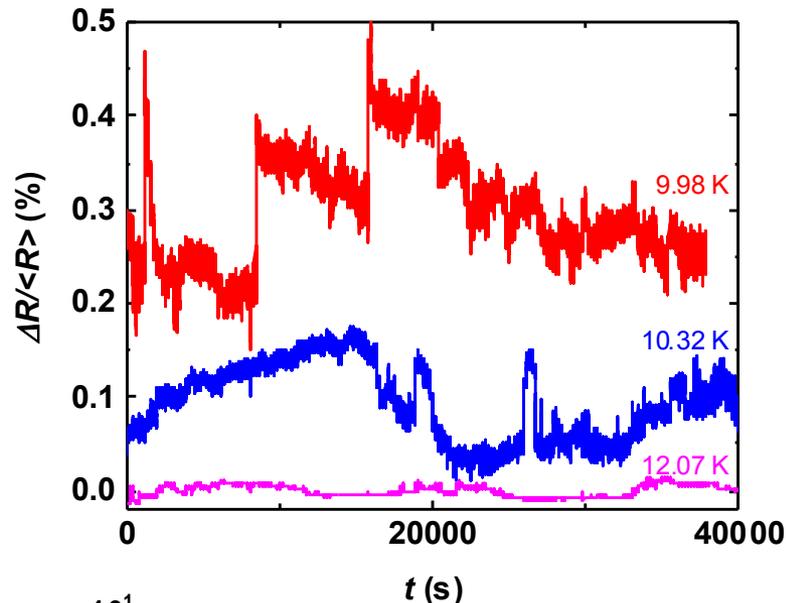
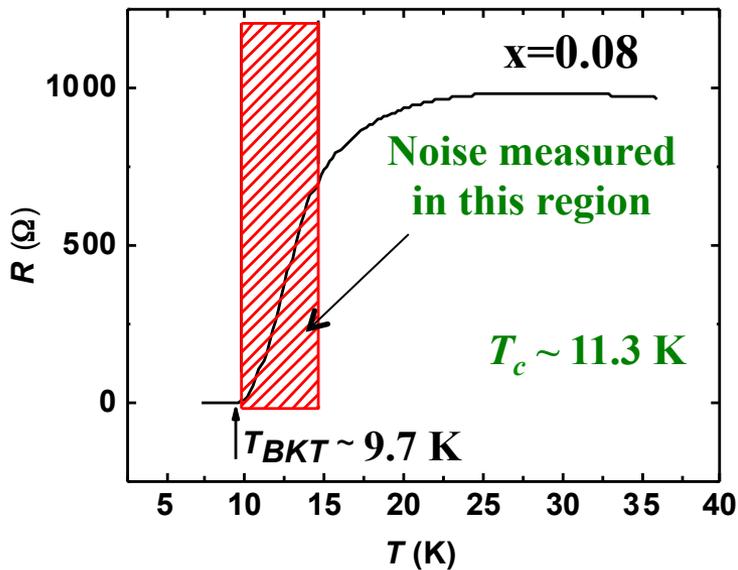
Phase fluctuations (BKT regime)

- Signatures of the 2D, Berezinskii-Kosterlitz-Thouless (BKT) transition (**thermal unbinding of vortex-antivortex pairs**) in bulk samples: **paraconductivity, current-voltage characteristics**
- **Good agreement with theory by Benfatto, Castellani, Giamarchi** (PRLs, PRBs since 2007)

[P. Baity *et al.* (unpublished)]



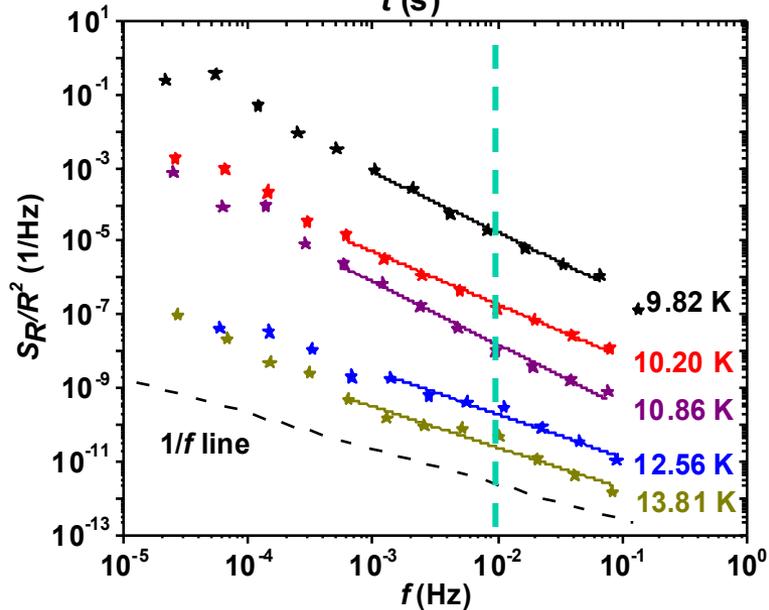
Time-domain spectroscopy of the BKT transition in a highly underdoped $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$



Power spectral density:

$$\frac{S_R}{R^2} \propto 1/f^\alpha$$

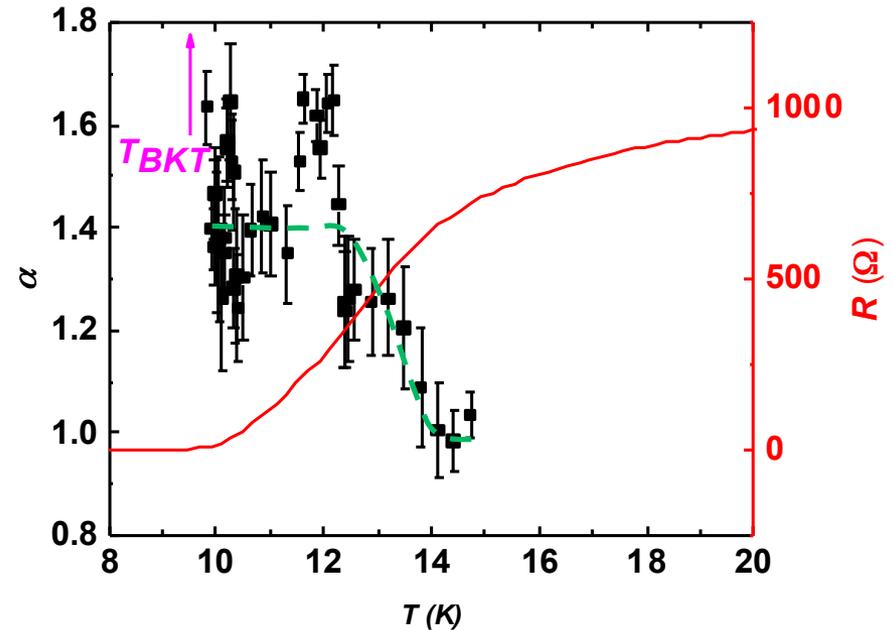
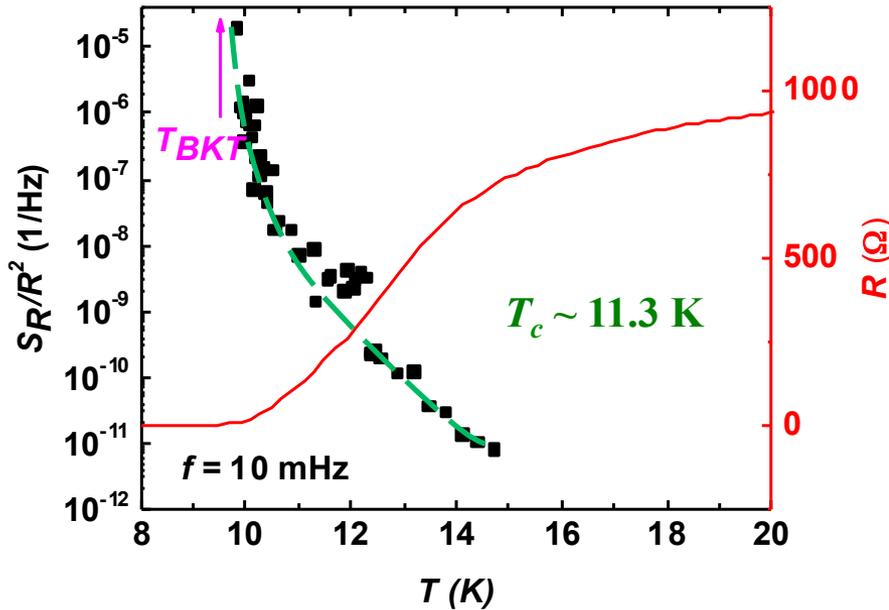
Arm size: $20 \mu\text{m} \times 200 \mu\text{m}$



Power spectrum vs. temperature

$$\frac{S_R}{R^2} \propto 1 / f^\alpha$$

Magnitude of the resistance noise

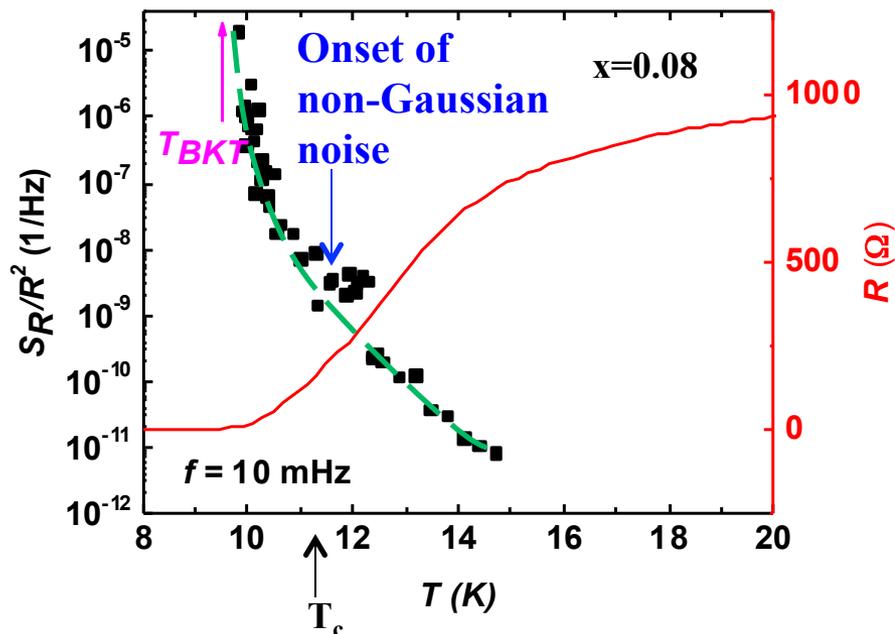


- Normalized power spectral density **increases by several orders of magnitude** as $T \rightarrow T_{BKT}$
- Below ~ 14 K, α increases from ~ 1.0 and reaches ~ 1.4 at ~ 12 K: **slowing down of the dynamics**

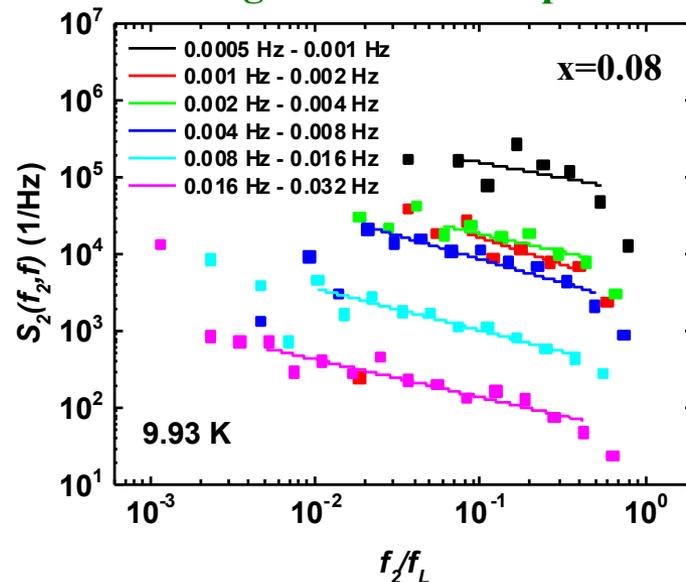


Time-domain spectroscopy of the BKT transition in a highly underdoped $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$

Magnitude of the resistance noise



Scaling of the second spectra



In the BKT regime ($T_{\text{BKT}} < T < T_c$):

- **Exponential** increase of noise as $T \rightarrow T_{\text{BKT}}$
- Slow, **correlated** dynamics for $T < T_c$
- **Interacting domains**/clusters
- Non-Gaussian noise suppressed in $x=0.07$ sample \rightarrow **not due to disorder**

Cluster/stripe glass:
competing interactions
on different length scales?

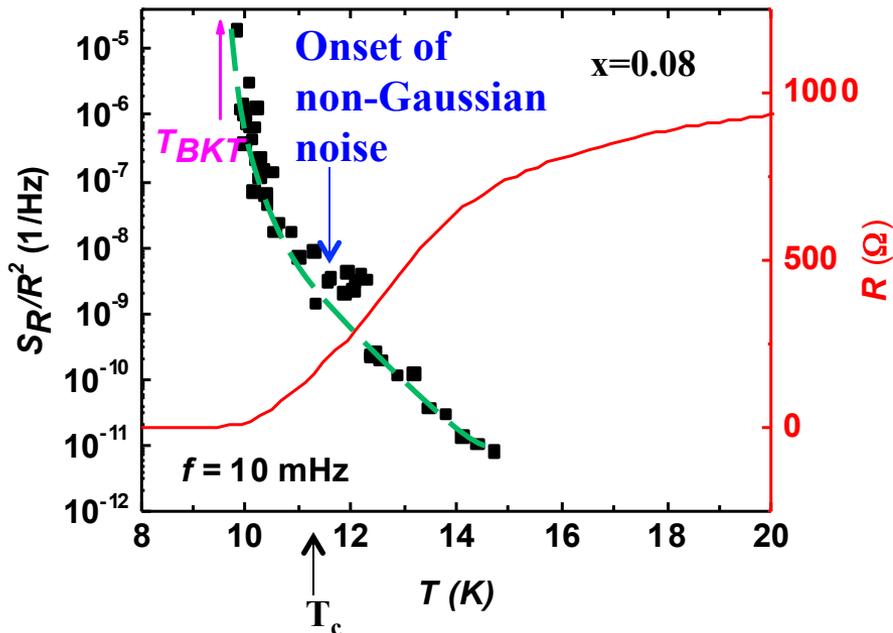
Dynamic stripes?

[Z. Shi *et al.* (unpublished)]

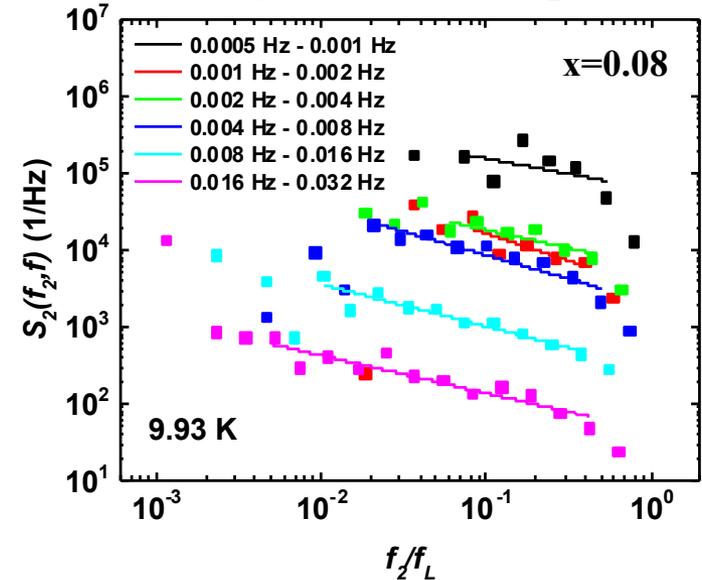


Time-domain spectroscopy of the BKT transition in a highly underdoped $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$

Magnitude of the resistance noise



Scaling of the second spectra



In the BKT regime ($T_{\text{BKT}} < T < T_c$):

- **Exponential** increase of noise as $T \rightarrow T_{\text{BKT}}$
- Slow, **correlated** dynamics for $T < T_c$
- **Interacting domains**/clusters
- Non-Gaussian noise suppressed in $x=0.07$ sample \rightarrow **not due to disorder**

Cluster/stripe glass:
competing interactions
on different length scales?

Intermediate, bad
metal phase?

[Z. Shi *et al.* (unpublished)]



Conclusions

- 1) Nature of the insulating ground state in $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ at low doping
 - Doped holes form **charge cluster glass** (dynamic charge heterogeneities) in CuO_2 planes
- 2) Doping-driven SIT ($H=0$) in LSCO
 - Formation of **localized Cooper pairs** within the insulating, charge glass state
 - Onset of SIT influenced by a **competing charge order**
- 3) Thermally-driven ($H=0$) SC transition
 - **BKT transition**
 - **Fluctuating, interacting clusters/domains; dynamical heterogeneities**
- 4) H -field-driven SIT
 - **Three distinct phases at $T=0$ in underdoped $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$:**
 - superconductor with $T_c(H) \neq 0$ (pinned vortex solid/Bragg glass)
 - superconductor with $T_c = 0$ (vortex glass)
 - high-field insulator (Mott hopping)

