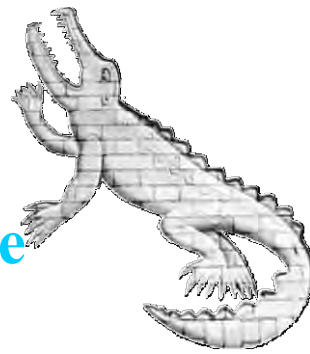


Semiconductor Physics Group
Department of Physics
Cavendish Laboratory, University of Cambridge



**Single-Electron Quantum Dots moving in Surface-Acoustic-Wave Minima:
Electron “Ping-Pong”, and Quantum Coherence,
and conversion to photons**

Chris Ford

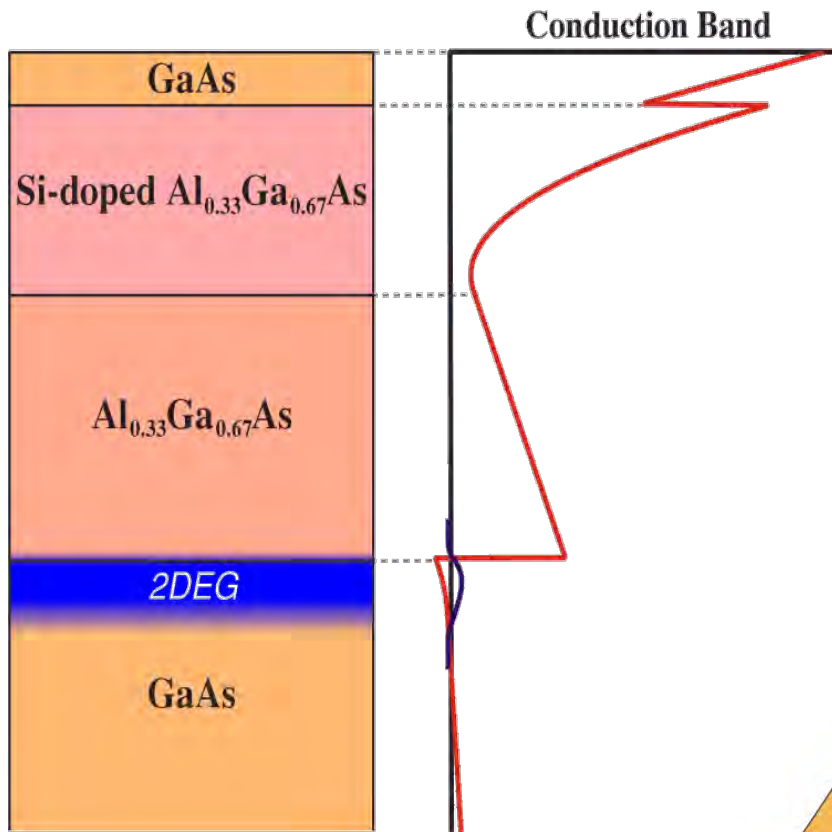
Robert McNeil, Matthew Benesh, Masaya Kataoka (NPL),
Michael Astley, Adam Thorn, Crispin Barnes, Seok-Kyun Son,
Yousun Chung, Tzu-Kan Hsiao, Hangtian Hou, Ateeq Nasir (NPL)
David Anderson, Jon Griffiths, Geb Jones, Ian Farrer, and David Ritchie



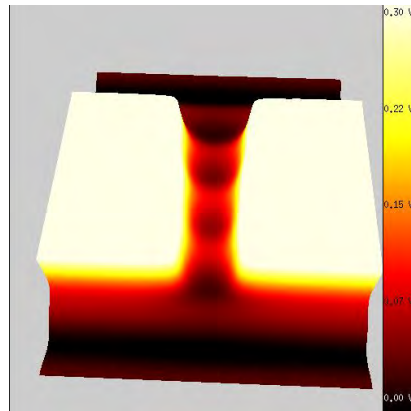
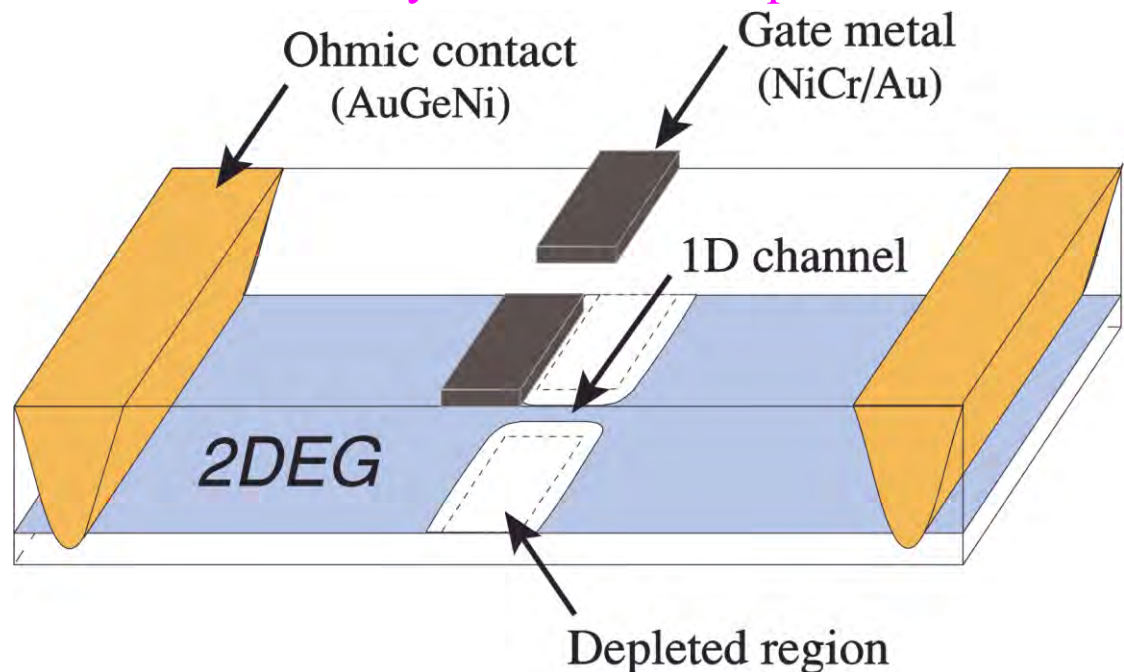
Outline

- Dynamic single-electron quantum dots driven by a surface acoustic wave (SAW)
 - current standard
 - single-photon source
 - spin readout by polarised photon emission
 - transfer of single charges
- Transfer of an electron between static dots
 - single-electron “ping pong”
- Quantum oscillations in a single SAW dot
 - initialisation and detection in same place
 - initialisation and detection in separate places
- Emission of photons from p-n junction
- Conclusions

GaAs-AlGaAs heterostructures and gates

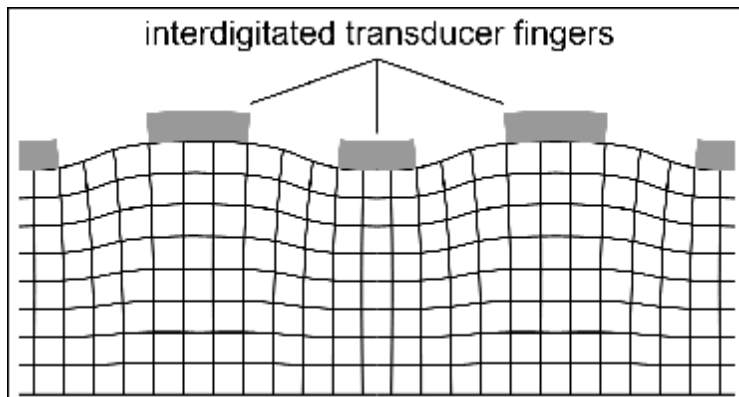
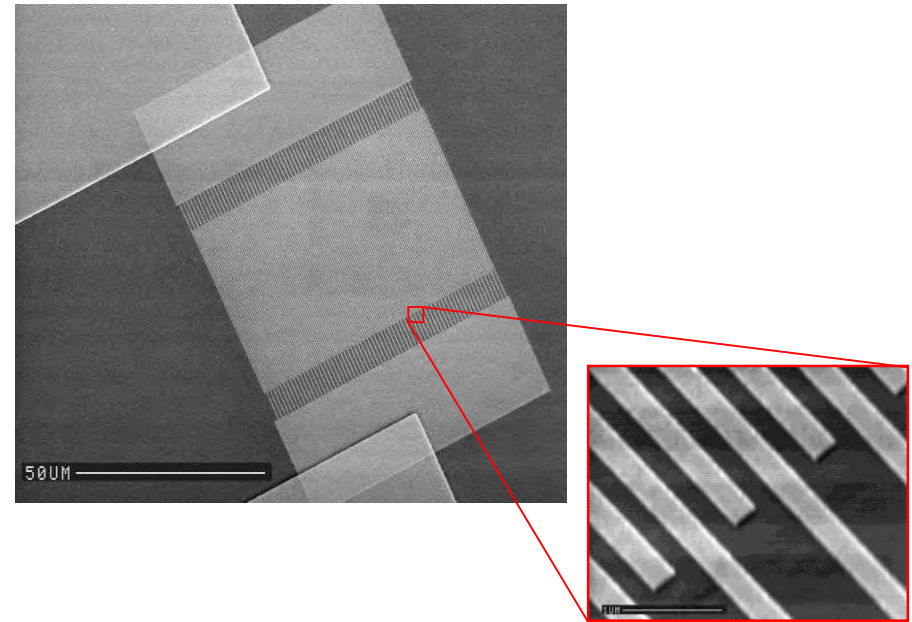


- Band offset \rightarrow 2D potential well
- Doping offset from well
 - very little scattering
 - 2D electron gas (2DEG)
- Gates on surface deplete 2DEG
 - narrow channel between split gates
 - very flexible technique



Surface acoustic waves (SAWs)

- Rayleigh waves generated on a piezoelectric material by applying a radio-frequency signal to a transducer at its resonant frequency



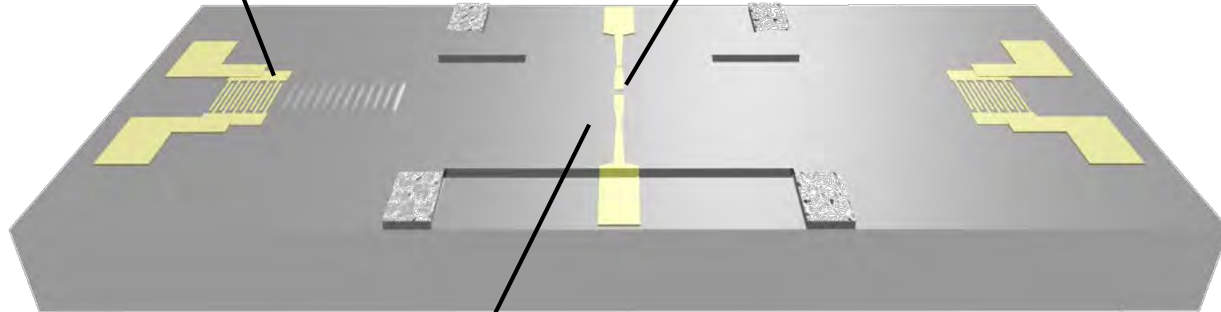
- In a piezoelectric material the strain wave is accompanied by an electric field

SAW single-electron transport

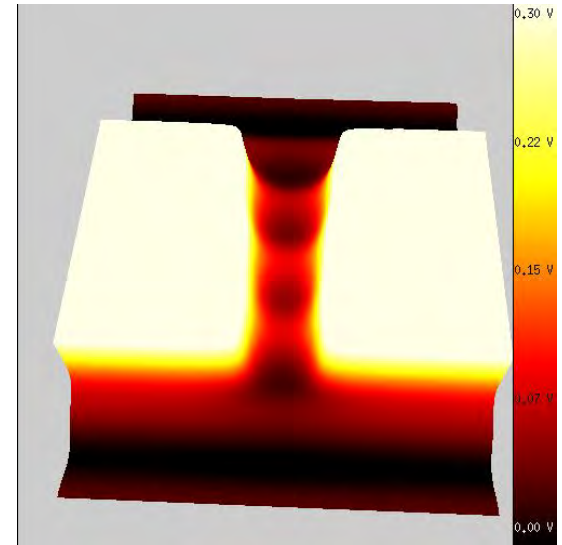
Transducer

SAW

1D channel



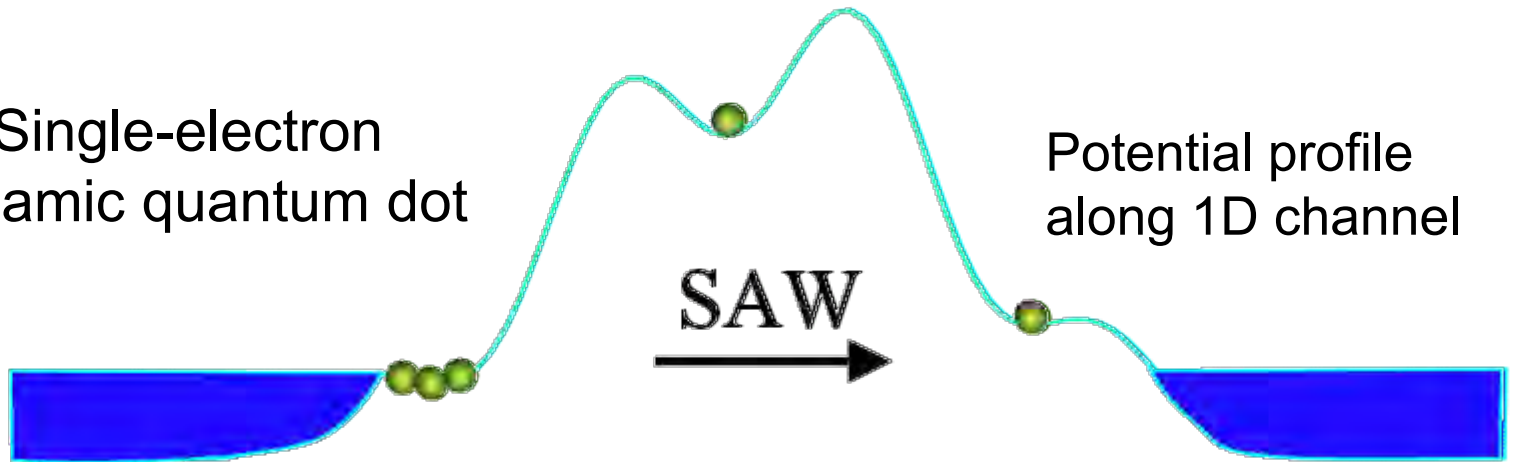
GaAs/AlGaAs heterostructure with 2DEG

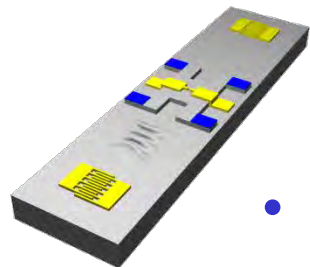


Single-electron
dynamic quantum dot

Potential profile
along 1D channel

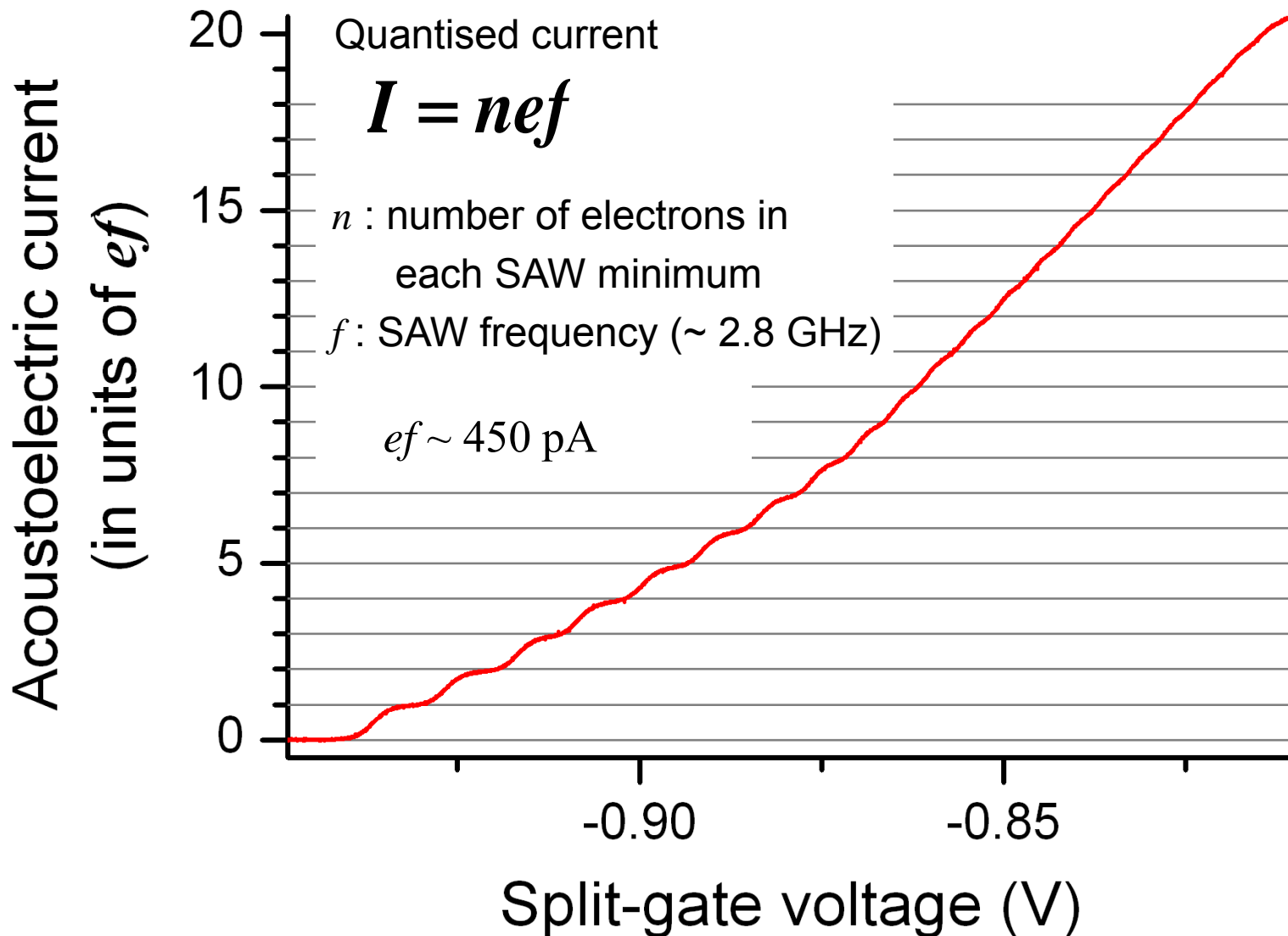
E_F

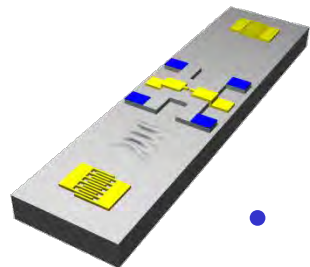




Why dynamic quantum dots?

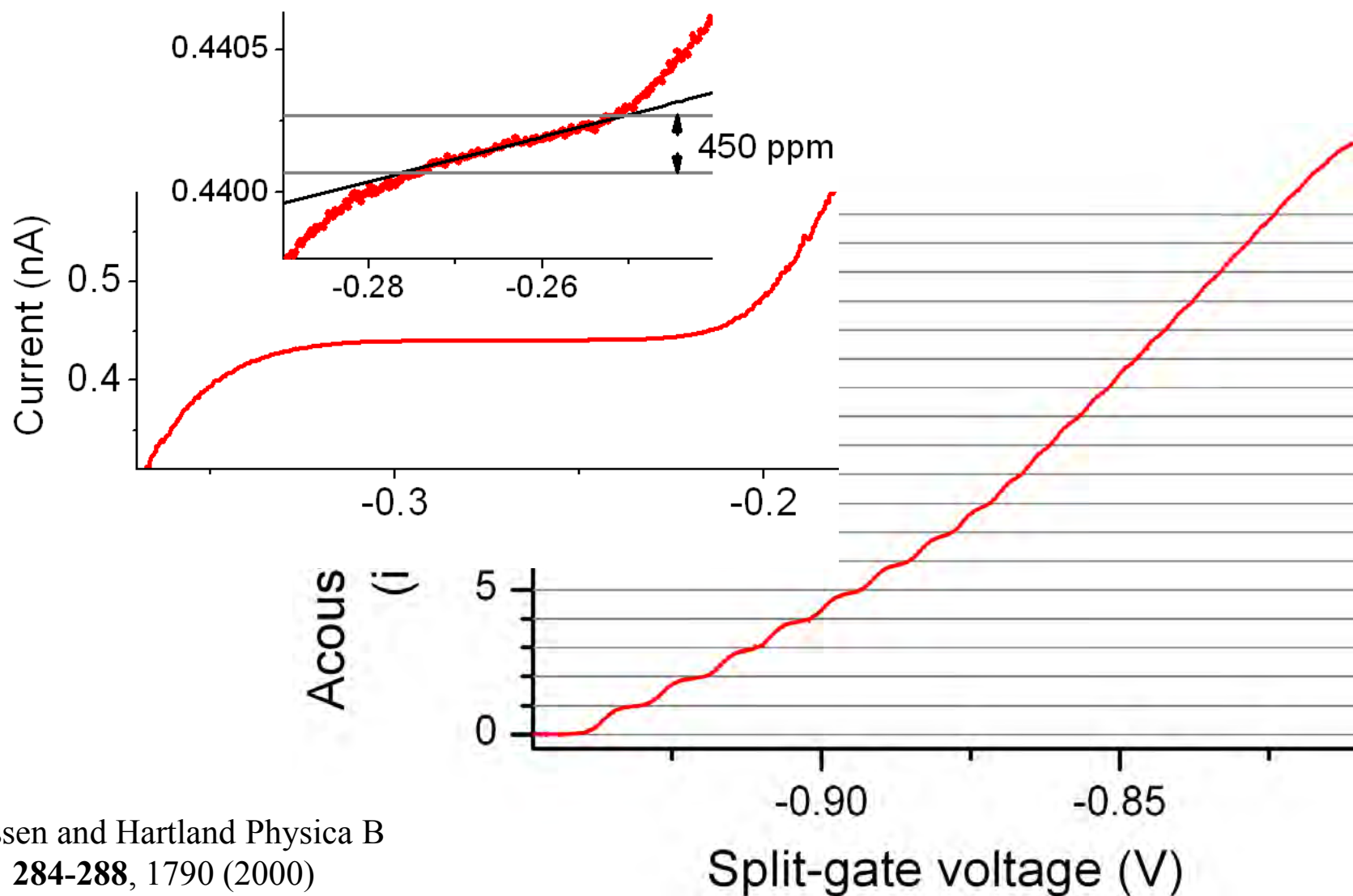
- SAW current quantisation

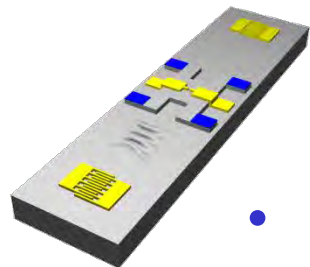




Why dynamic quantum dots?

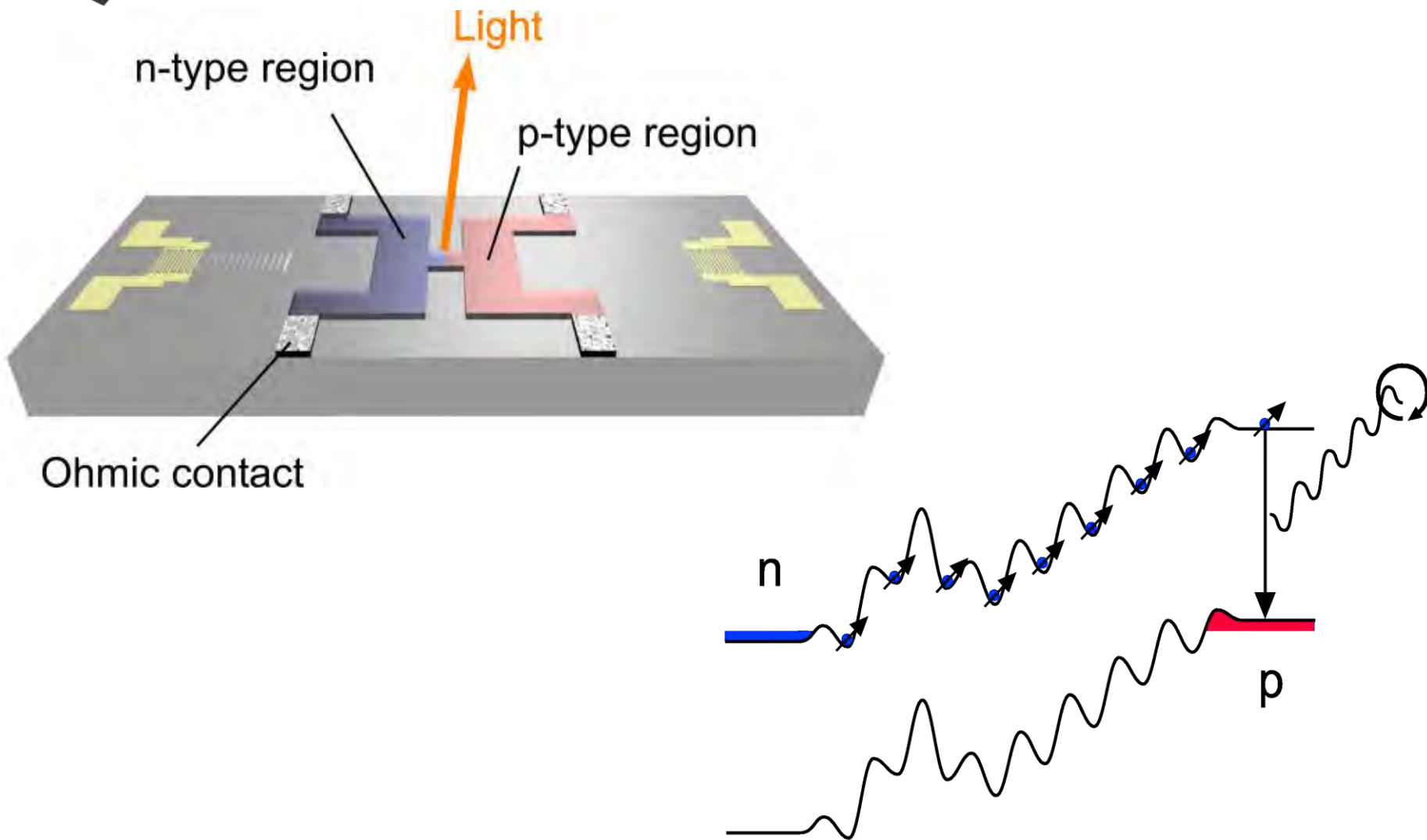
- Metrology: current standard

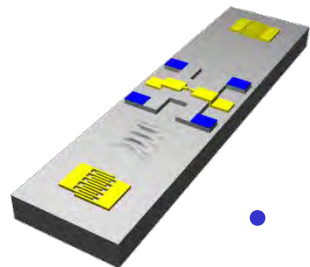




Why dynamic quantum dots?

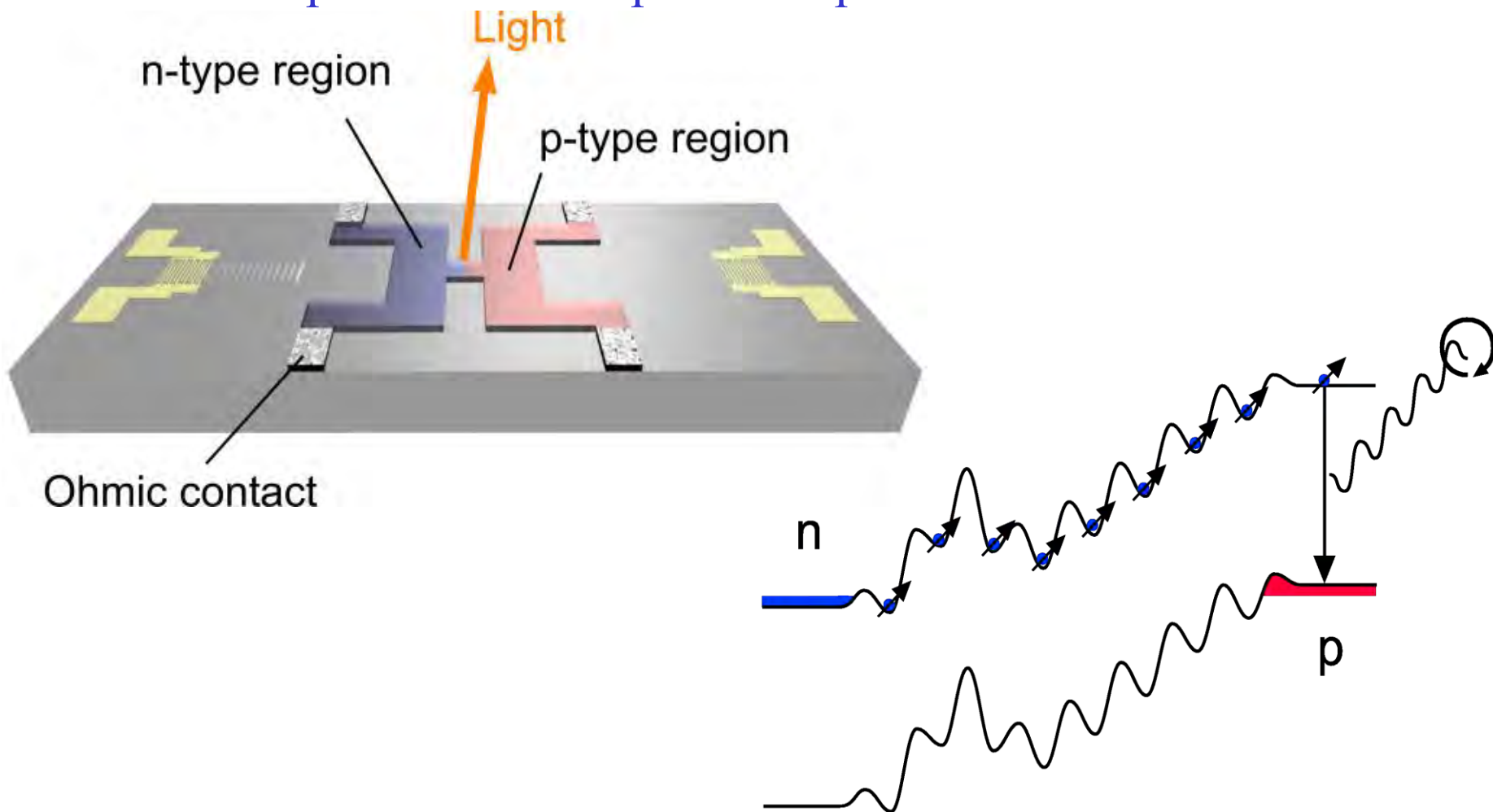
- Quantum cryptography: single-photon source

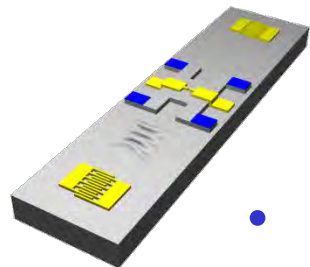




Why dynamic quantum dots?

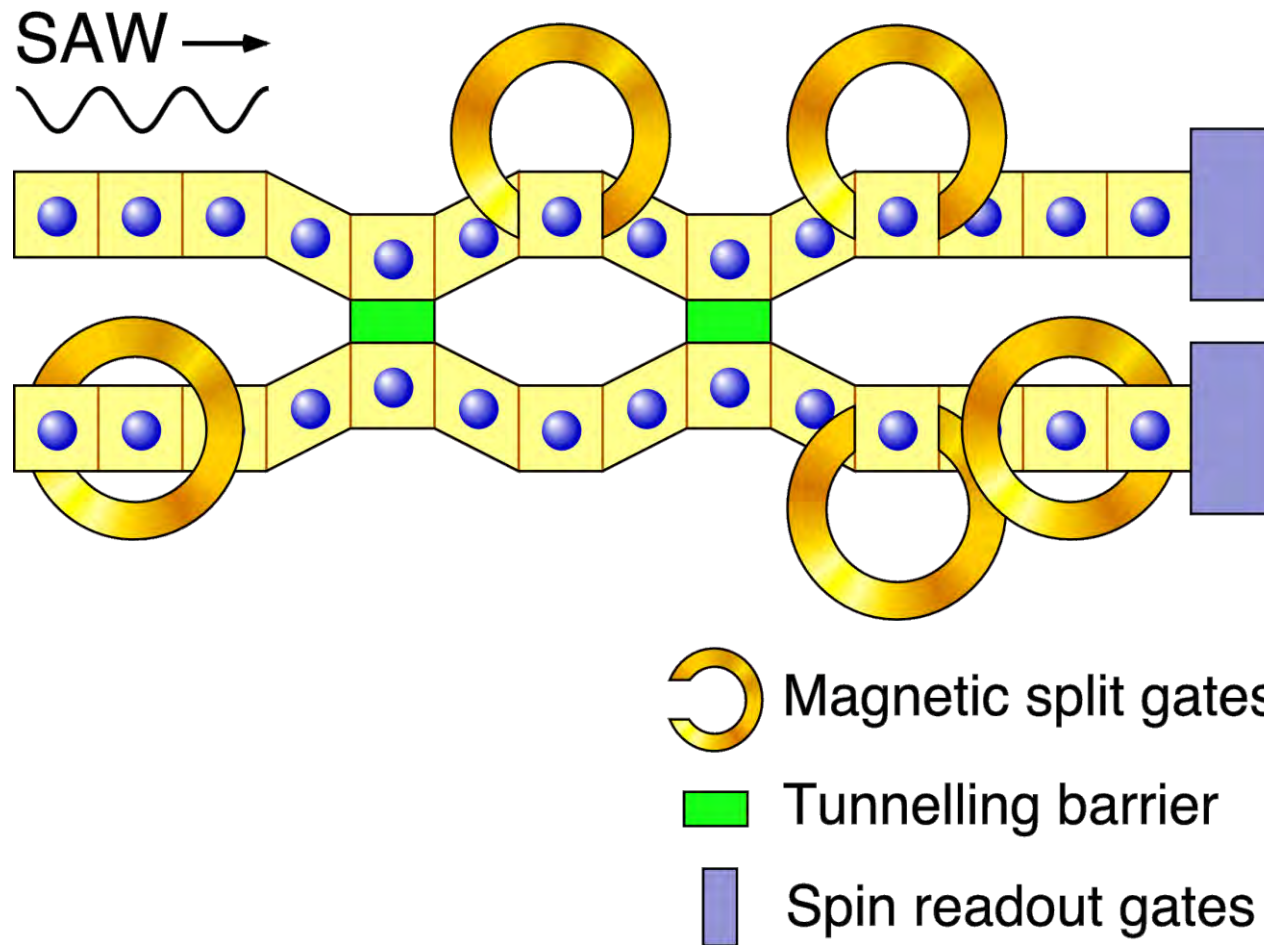
- Quantum cryptography: single-photon source
- Spin readout *via* polarised photons





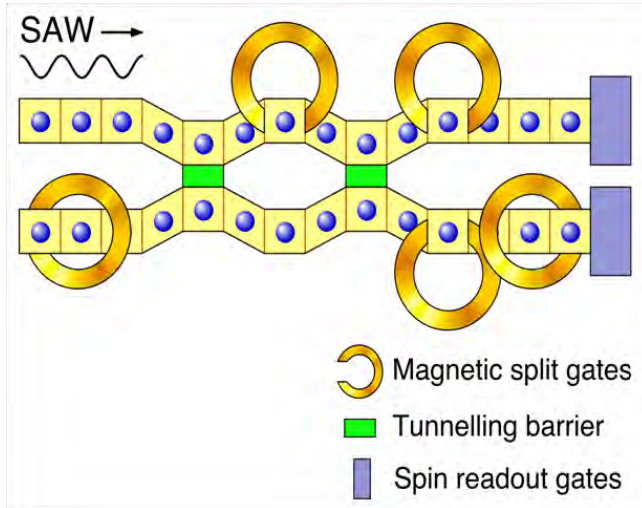
Why dynamic quantum dots?

- Quantum computation

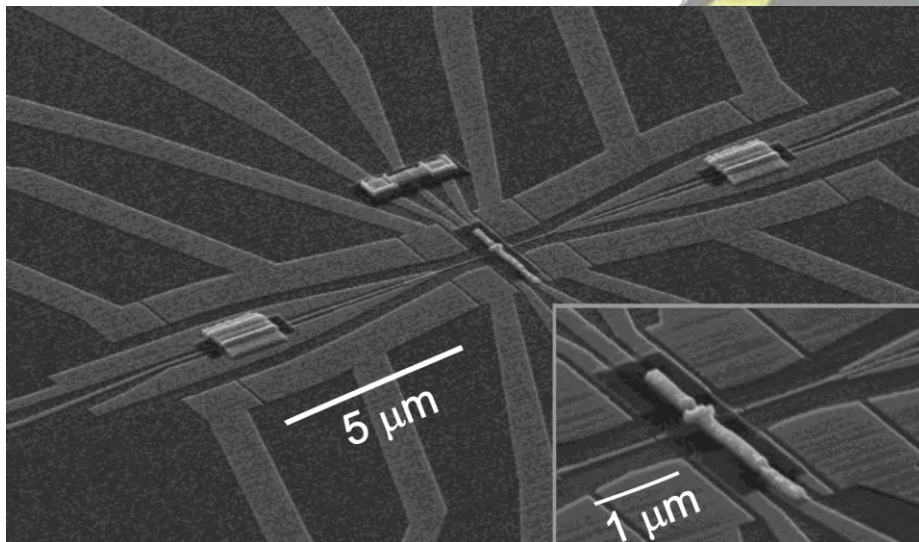
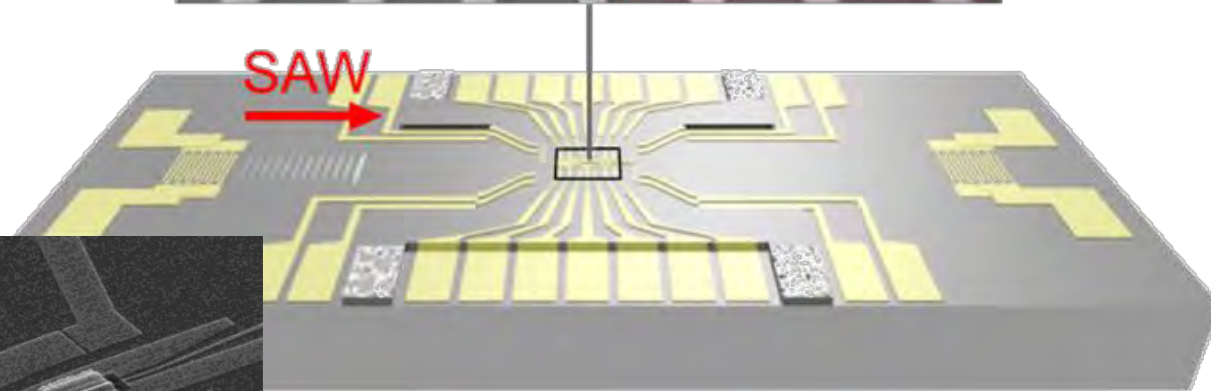
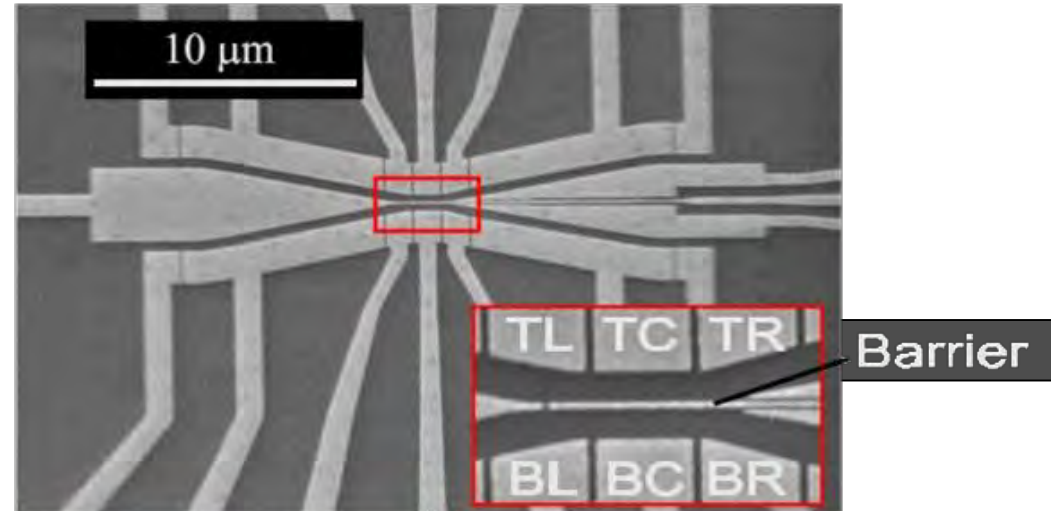


Barnes *et al.*, *Phys. Rev. B* **62**, 8410 (2000)

The SAW quantum computing project



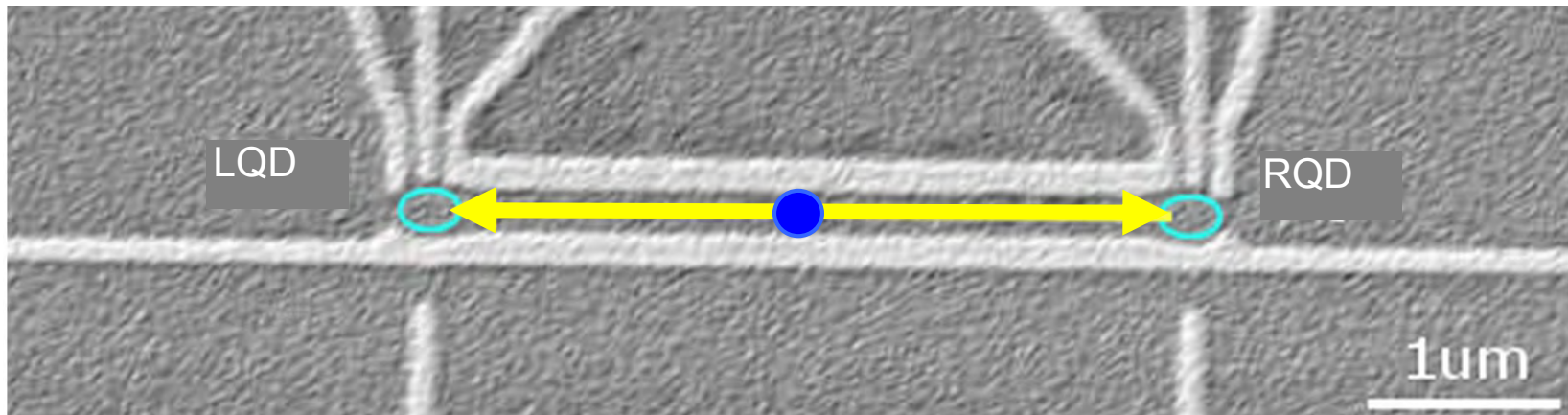
Barnes *et. al.* PRB **62** 8410 (2000)



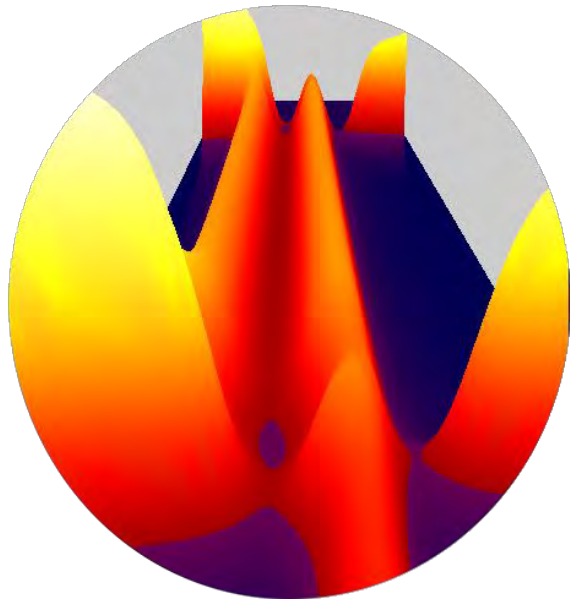
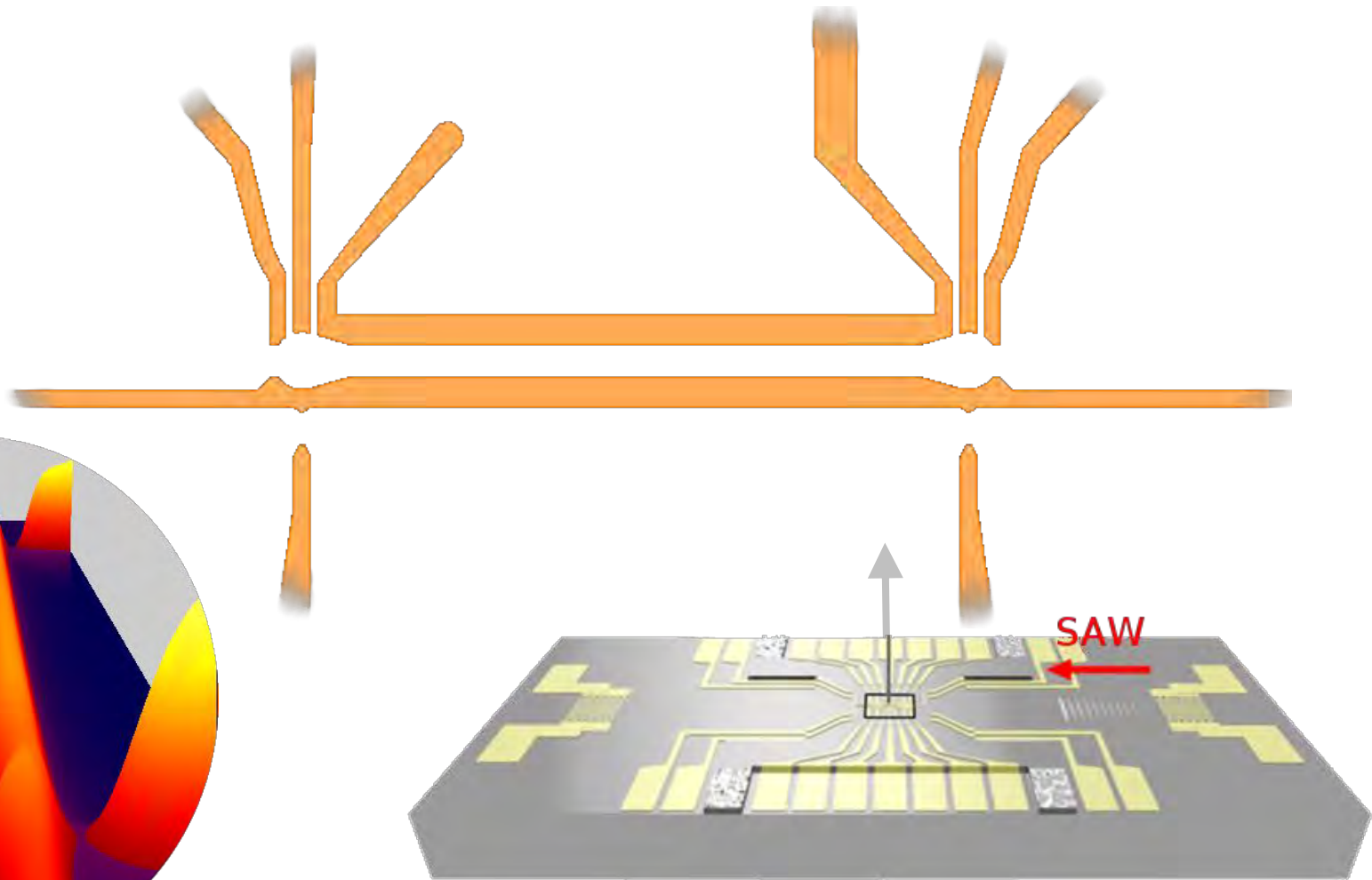
- Use many surface gates to control channels in each region

Transfer of quantum information

- A quantum computer will need to be able to move qubits to entangle adjacent ones, or to store and retrieve qubits
 - quantum repeater for cryptography?
- Transfer spin qubits from static dots to “flying” qubits
 - e.g. SAW-driven qubits, photon qubits
 - convert back once reach memory
- We have designed devices to transfer single electrons over long distances (4 μm) back and forth between static dots
 - can play with a given electron for e.g. 10 minutes
 - spin transport and coherence still remain to be demonstrated...

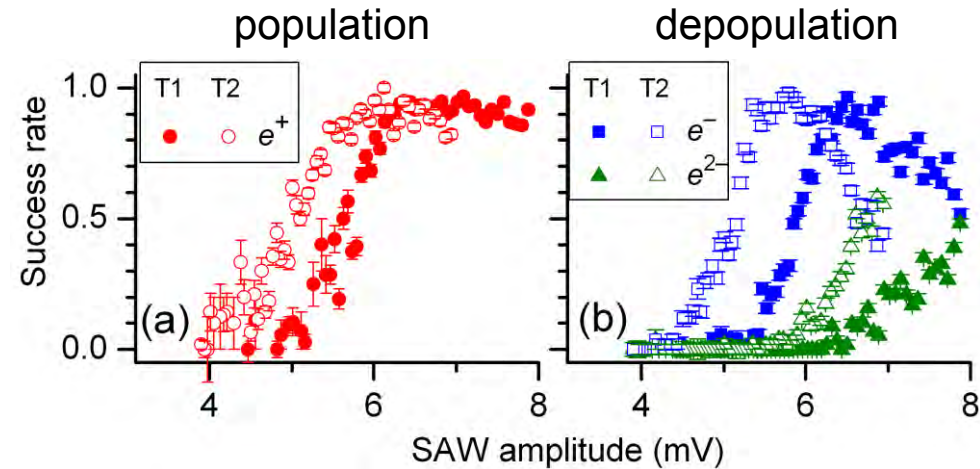
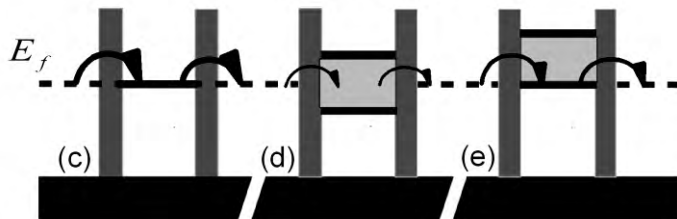
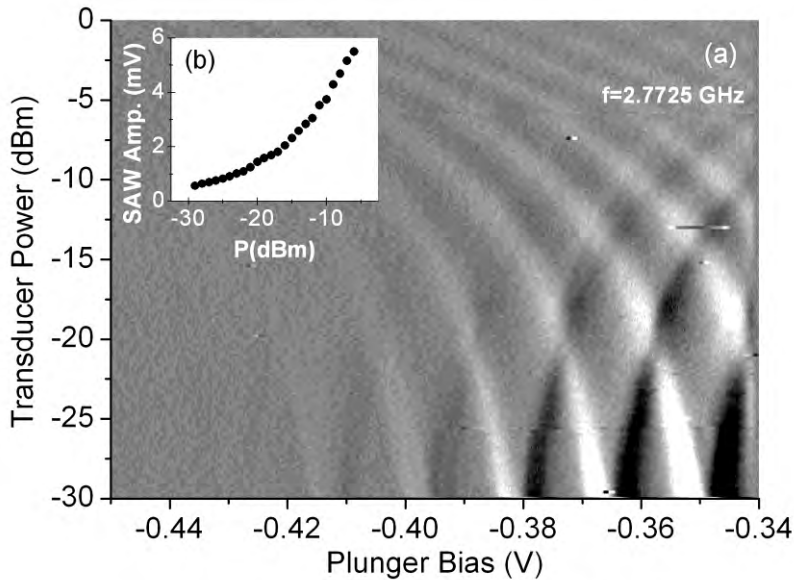


Single electron transfer between two QDs



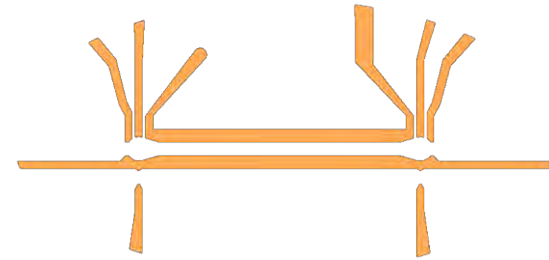
SAW amplitude dependence

- SAW potential amplitude can be calibrated by measuring conductance peak splitting

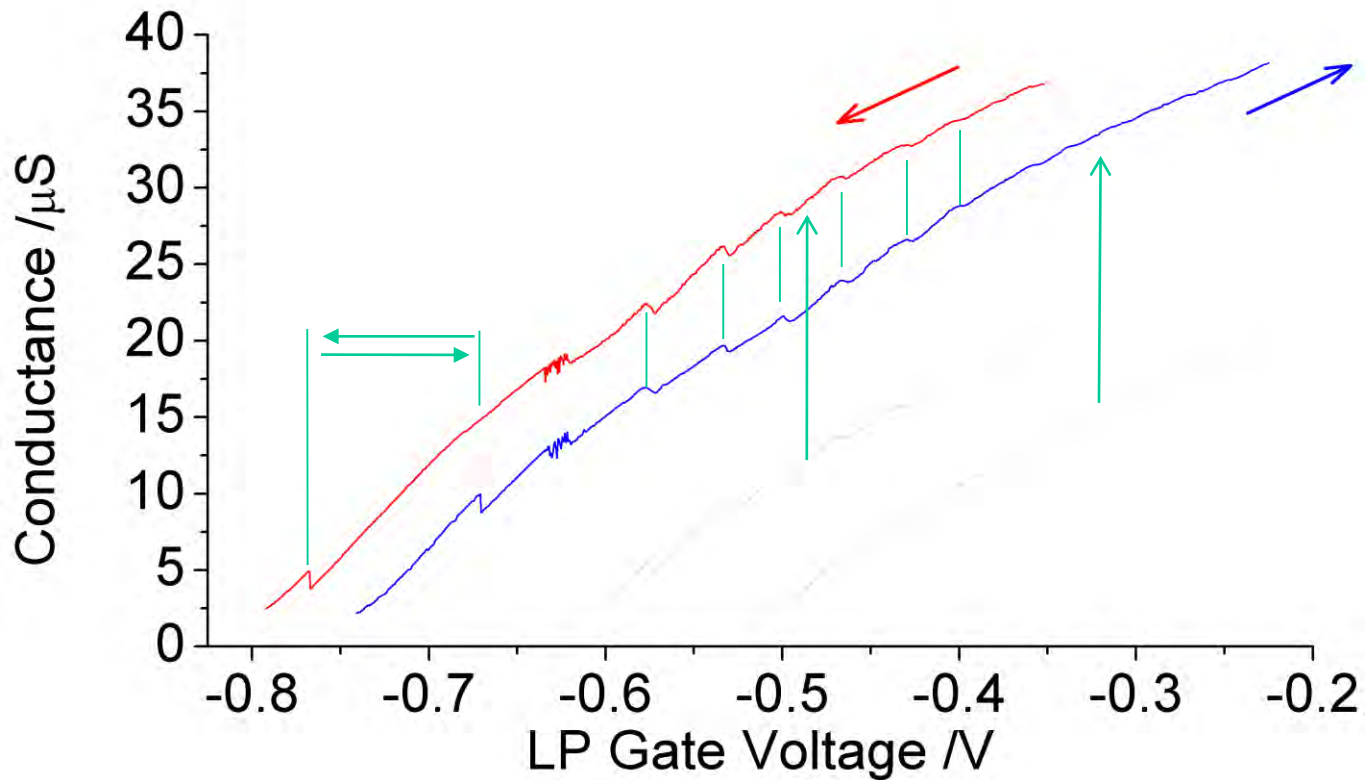


- Both transducers (T1, T2) give similar results within error
 - \Rightarrow mechanism is lowering of a barrier
- Success rate ~ 1 when SAW amplitude large enough
- If amplitude too large, double depopulation ($-2e$) occurs

Setting up a dot



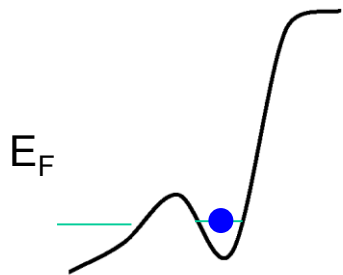
- Barriers pinched off
 - cannot measure conductance oscillations
 - use “**detector**”, look for hysteresis in losing/gaining electron



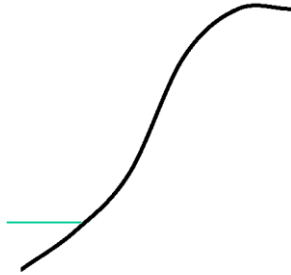
- moving from open to isolated dot, transitions become steeper and show hysteresis

Dot initialisation

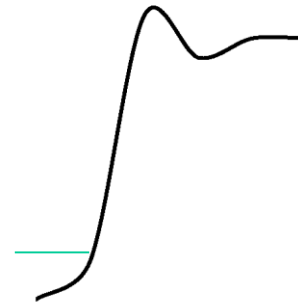
1. Start with dot below E_F



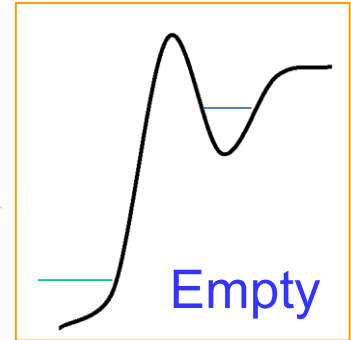
2a. Raise Plunger



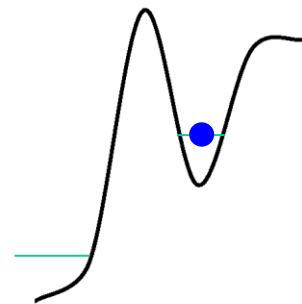
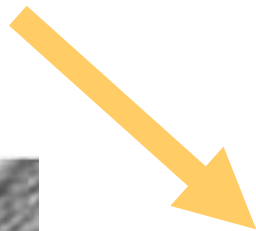
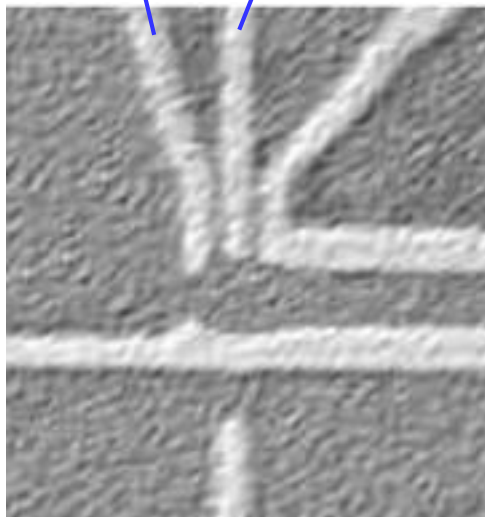
3a. Raise Barrier



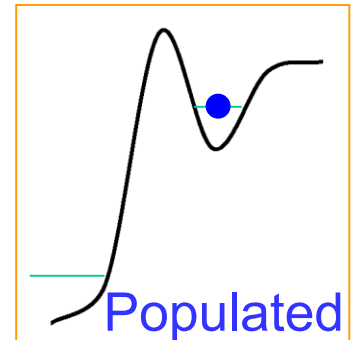
4a. Lower Plunger



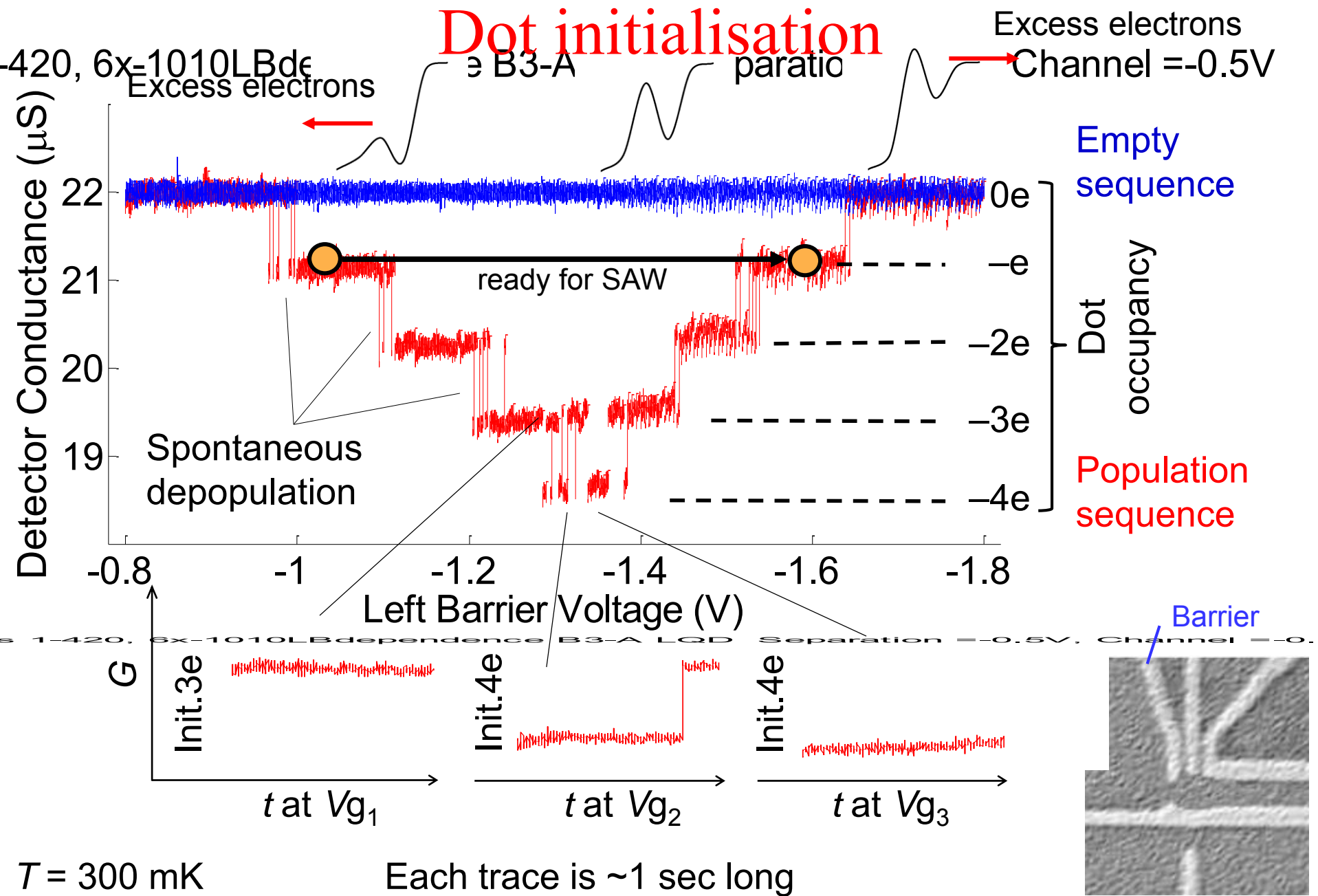
Barrier Plunger



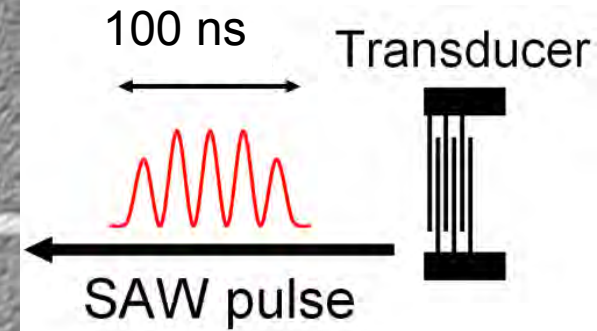
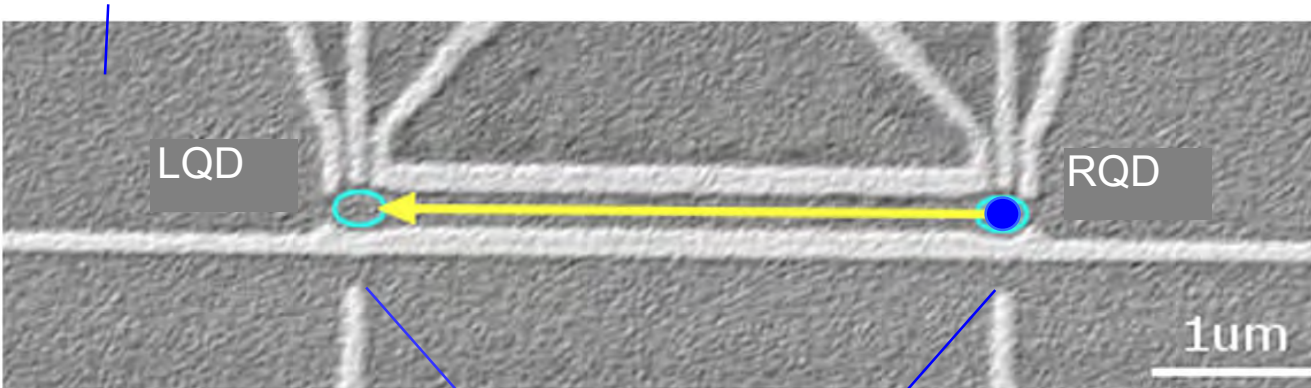
2b. Raise Barrier



3b. Raise Plunger

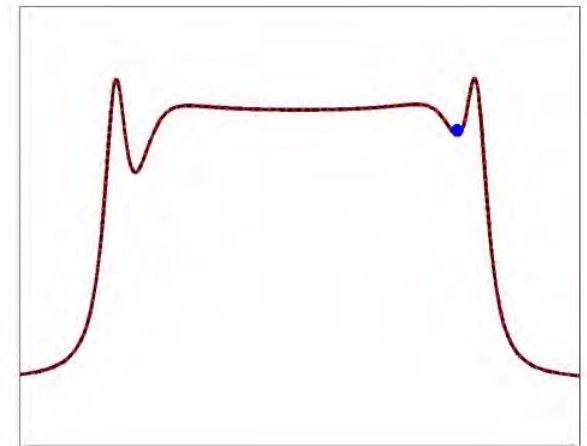


Pulse sequence

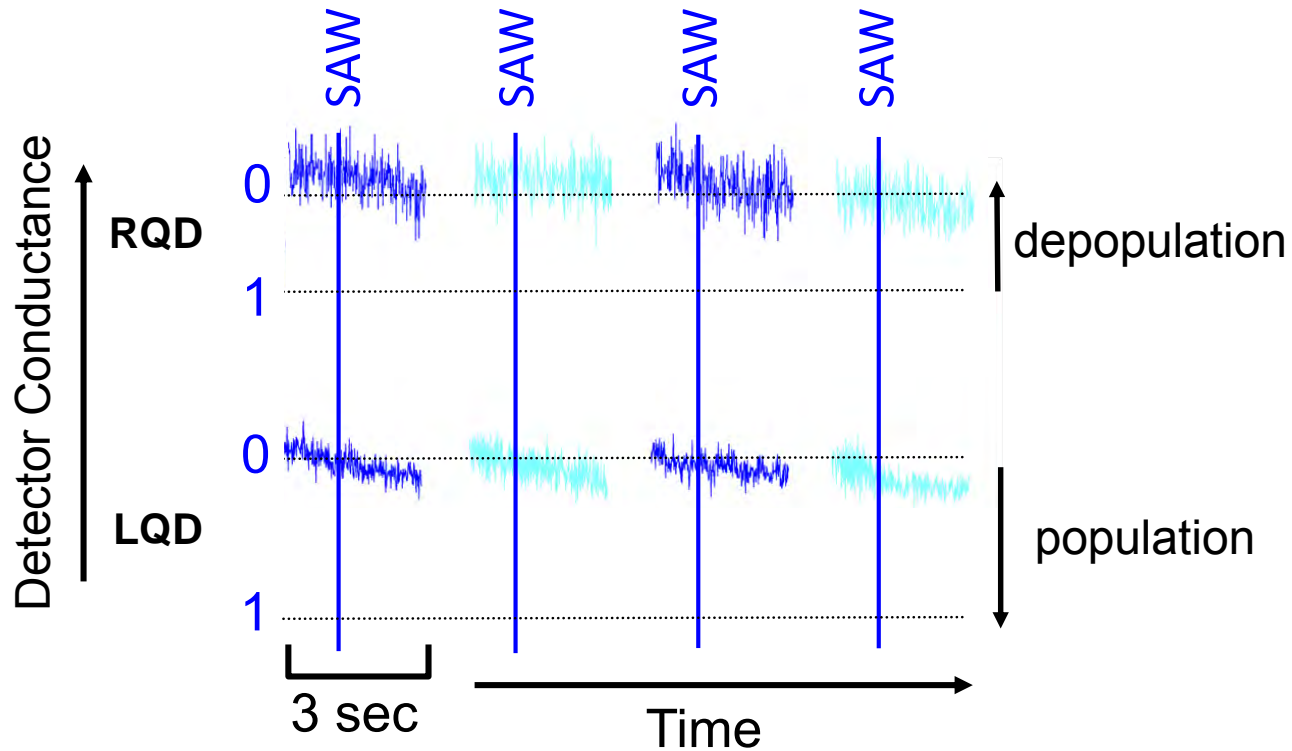
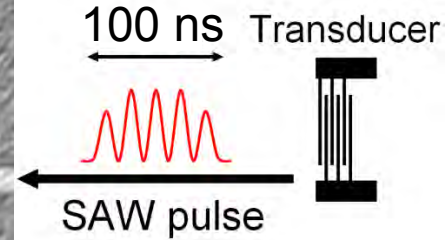
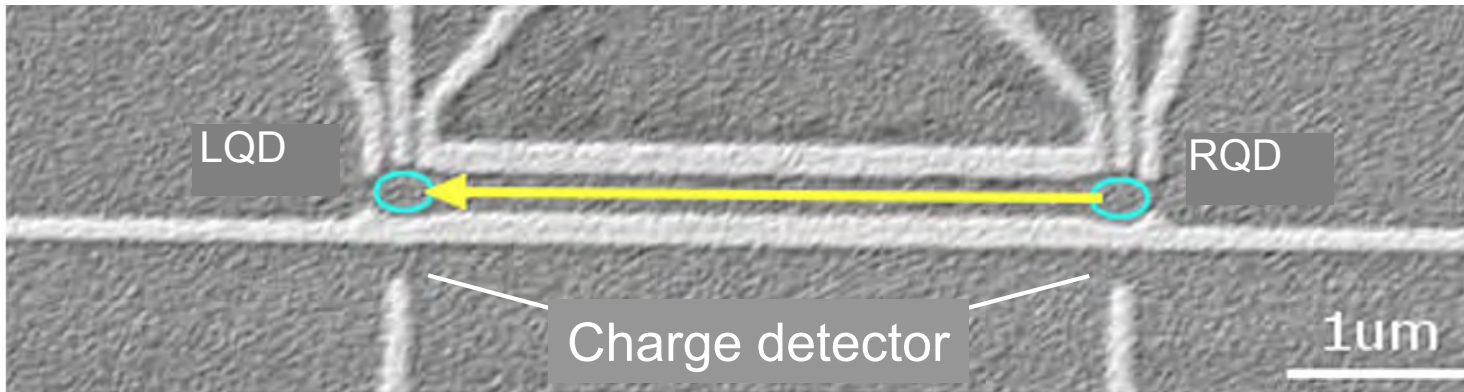


Charge detector

- Prepare channel
 - SAW pulse to clear channel
- Initialise dots
- Fire a SAW pulse (100 ns)
 - monitor **detectors** before and after
- Detect electron population/depopulation
 - electron disappears from one dot, reappears in the other

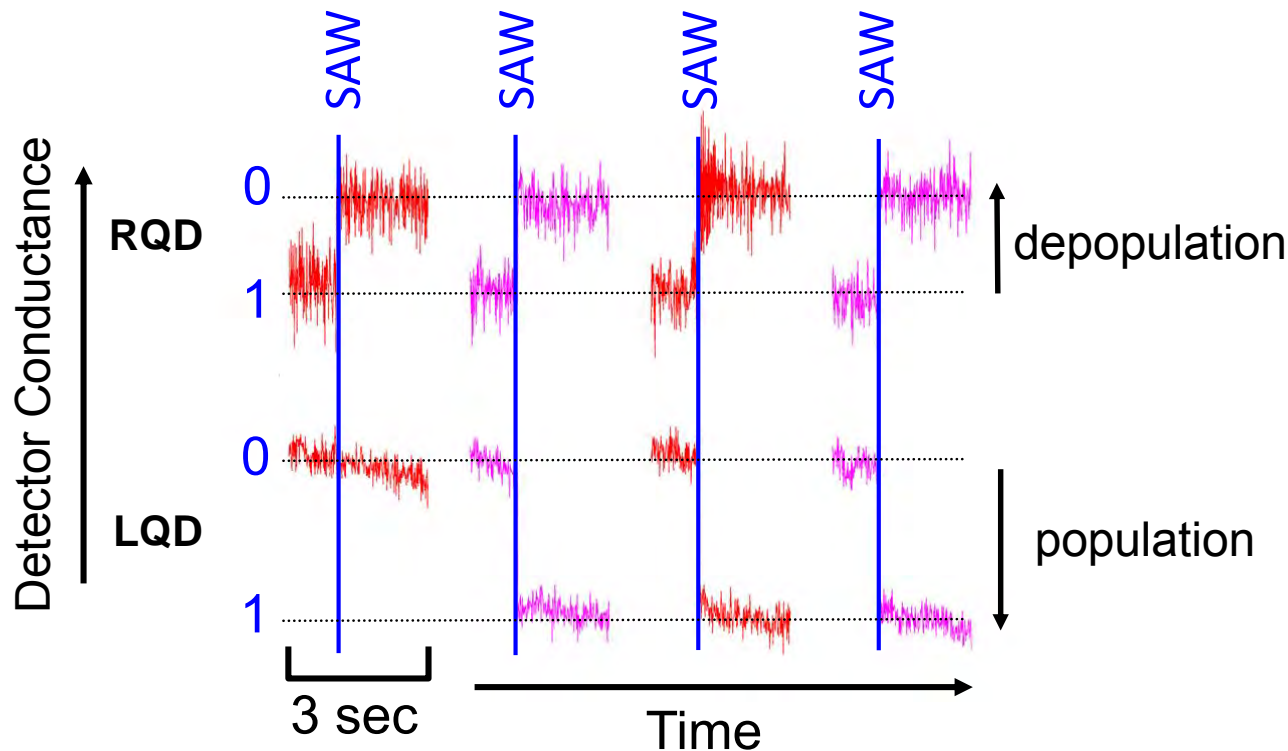
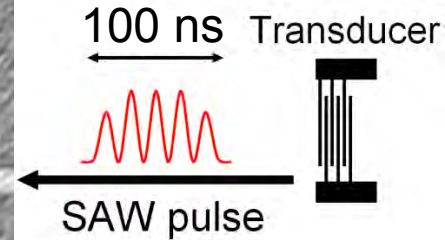
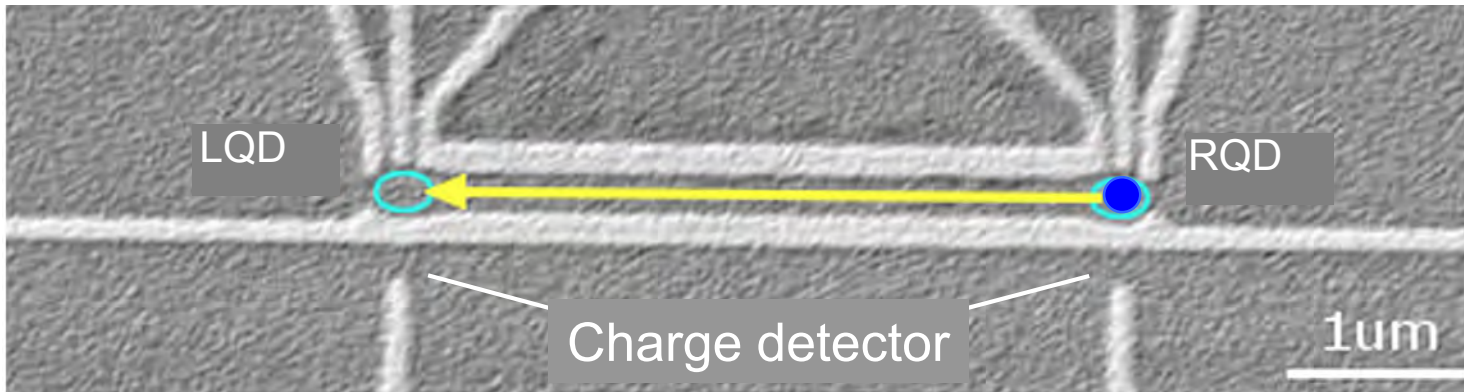


Single-electron transfer



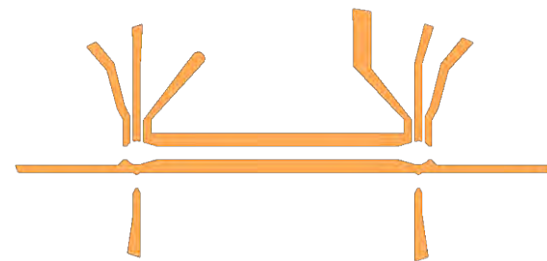
- RQD empty
- LQD empty
- Send SAW pulse
 - no electrons appear from channel after SAW pulse

Single-electron transfer

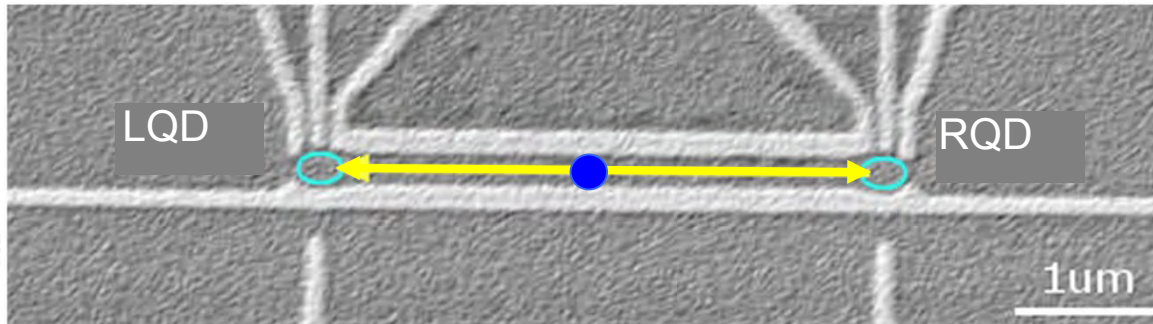


- RQD starts with one electron
- LQD empty
- Send SAW pulse
 - Electron occasionally gets stuck in channel, but usually reaches other dot

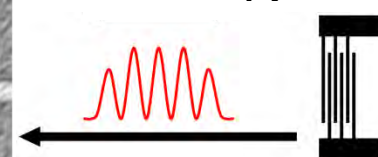
Single-electron “ping pong”



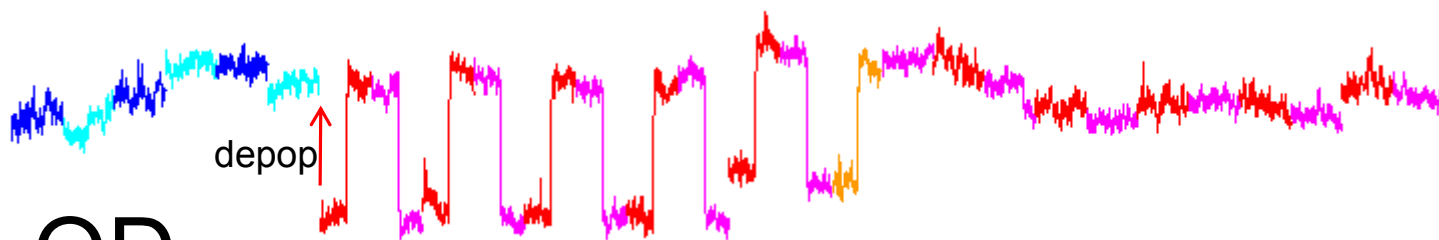
T_L



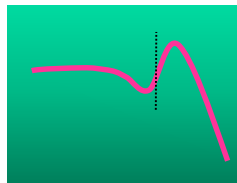
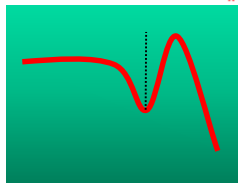
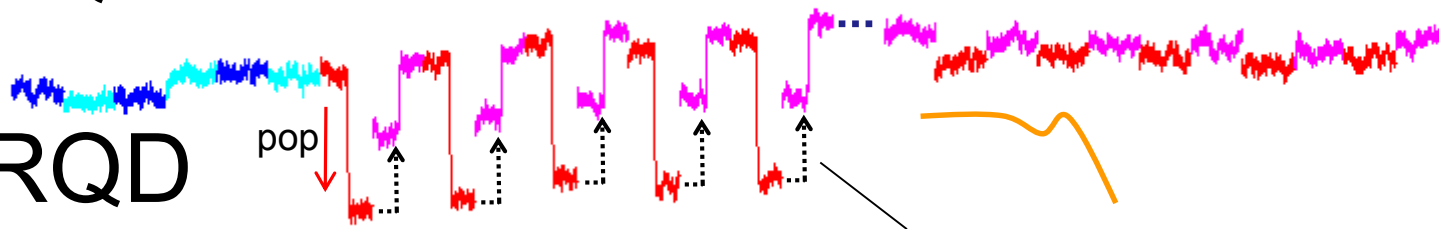
T_R



LQD



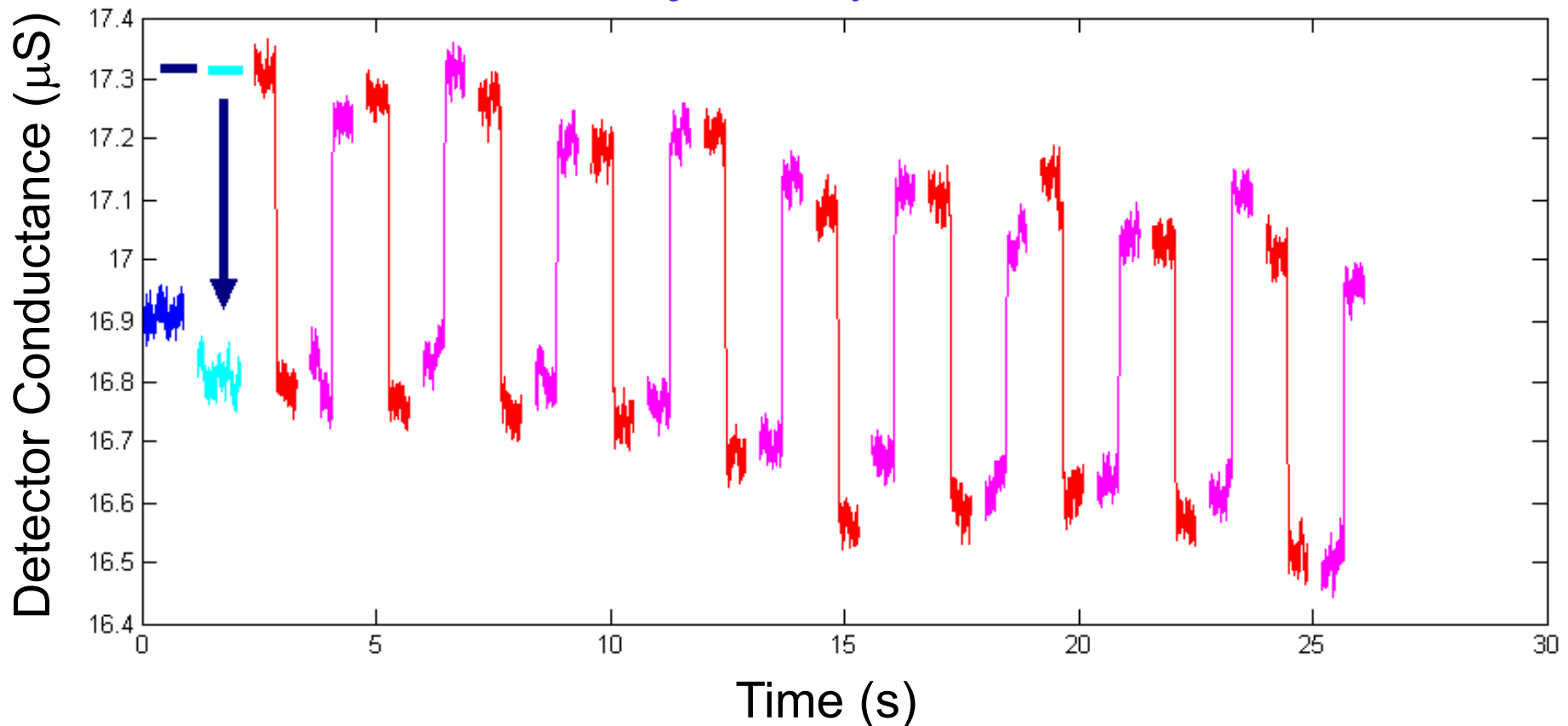
RQD



electron shifted as dot is set up for return

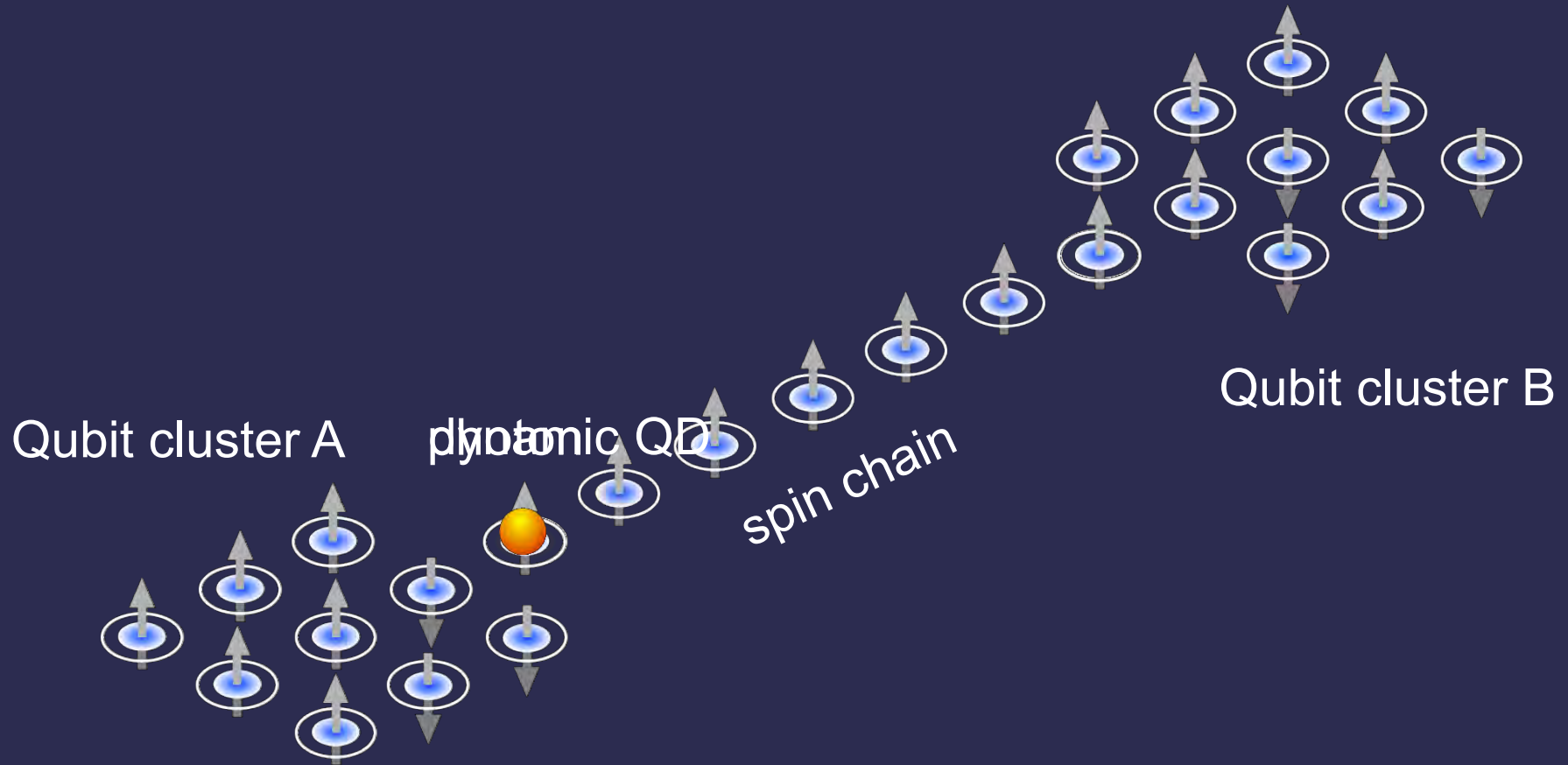
Reliability of transfer

- Can transfer same electron at least 60 times (0.25mm!) along the channel before it is joined by another from outside

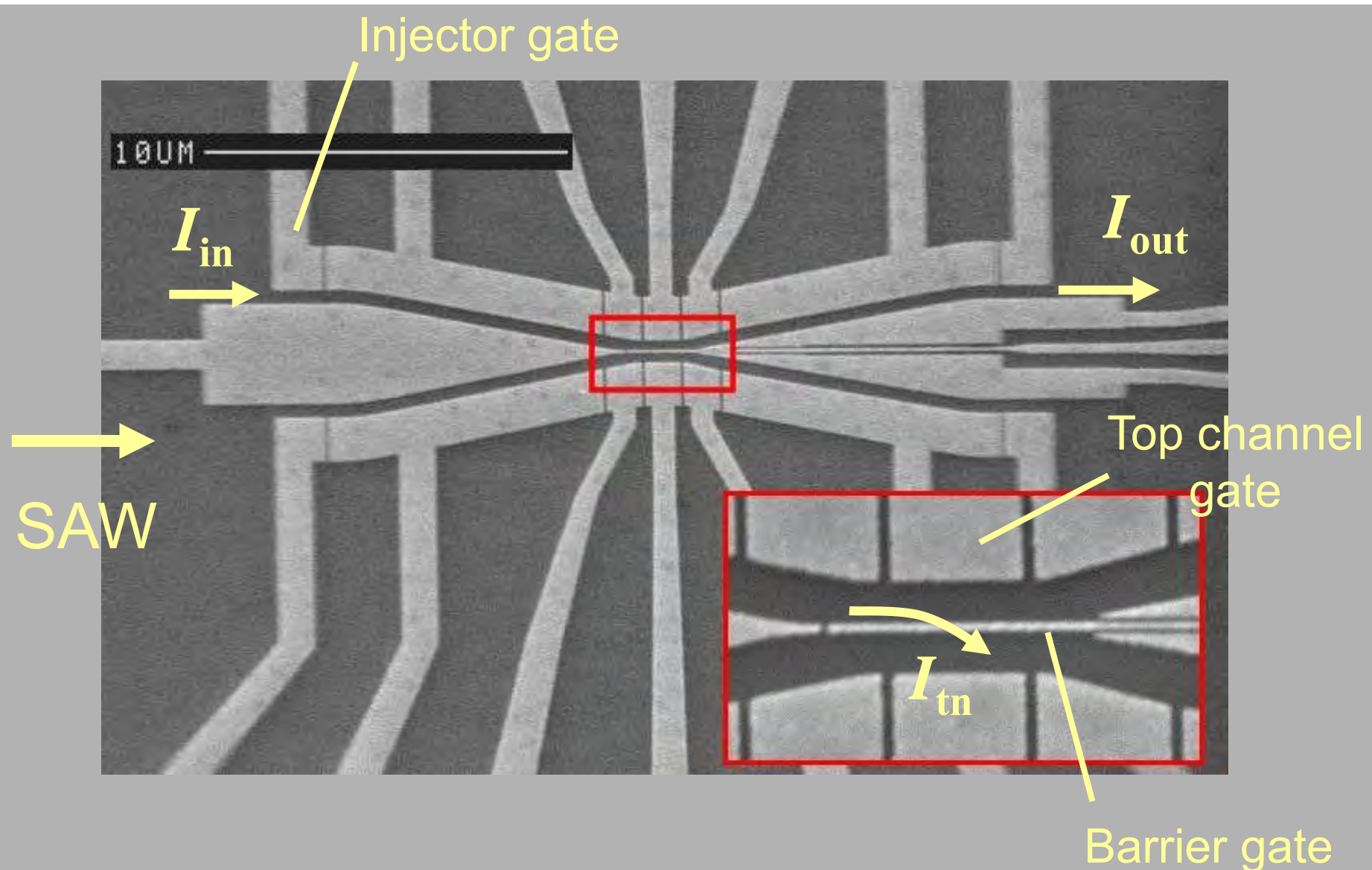


- Next step: convert spin polarisation to photon polarisation
 - we have just finished building a cryogenic microscope for our 300mK cryostat

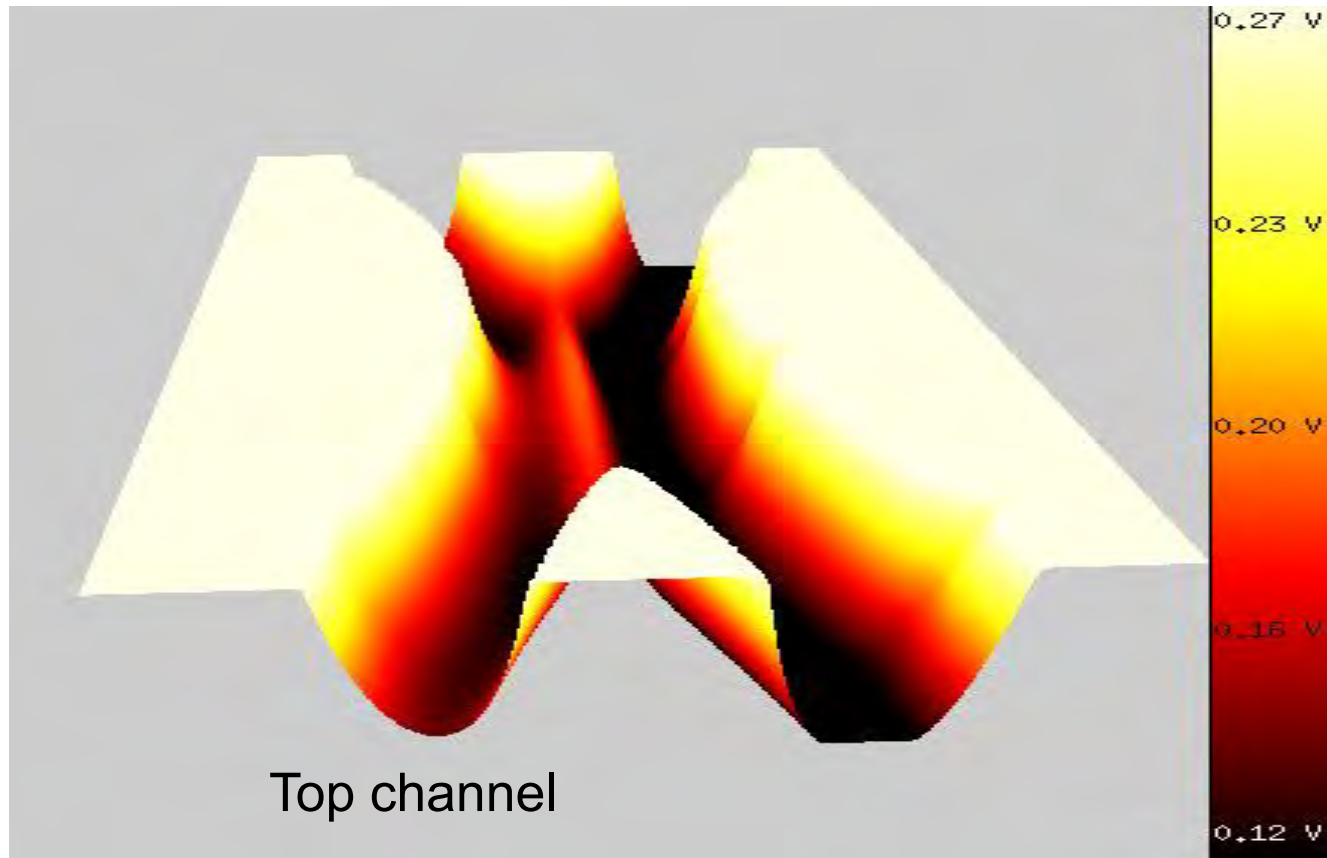
Quantum information transfer



Electron tunnelling out of dynamic dots

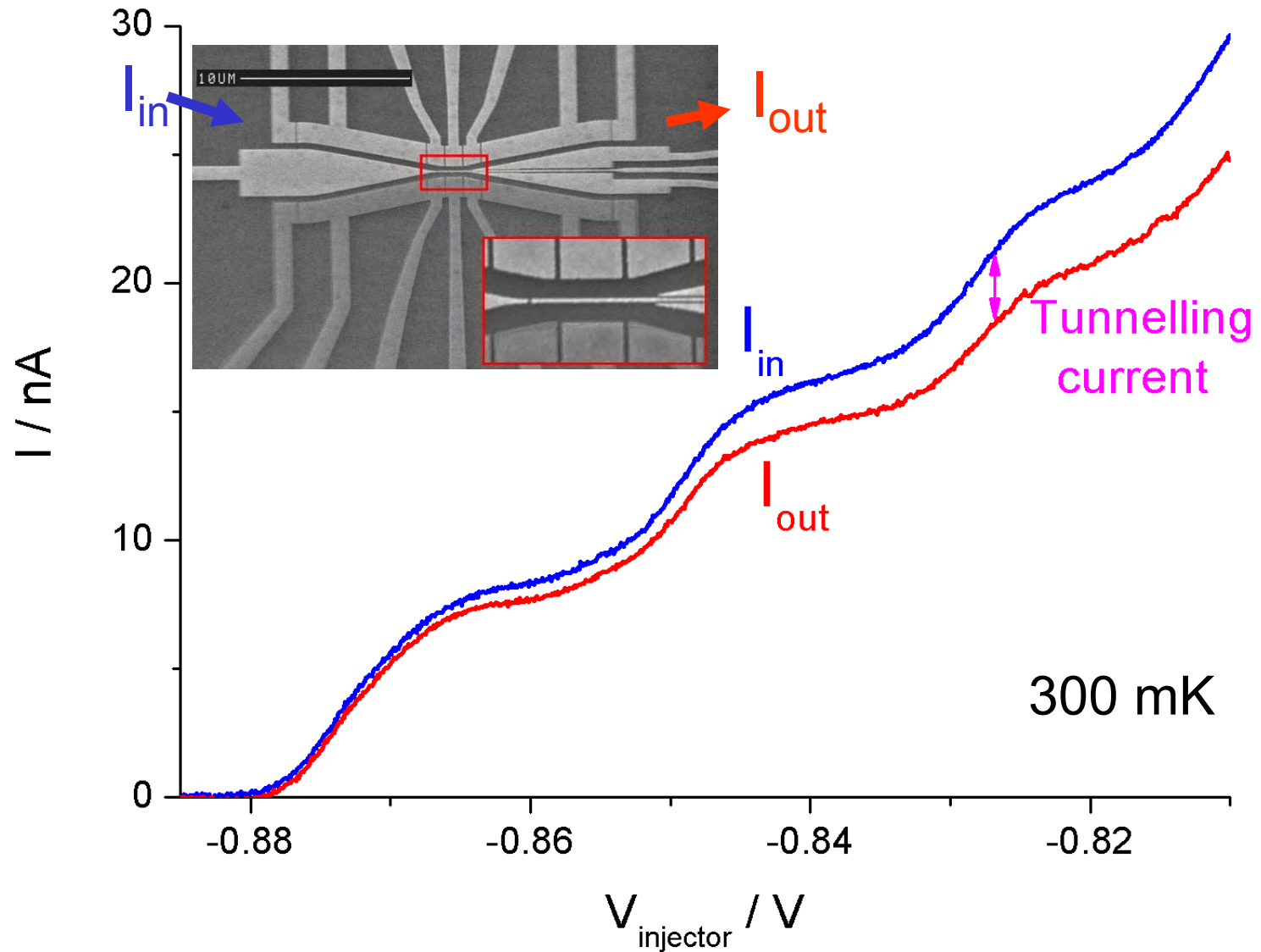


Channel potential landscape

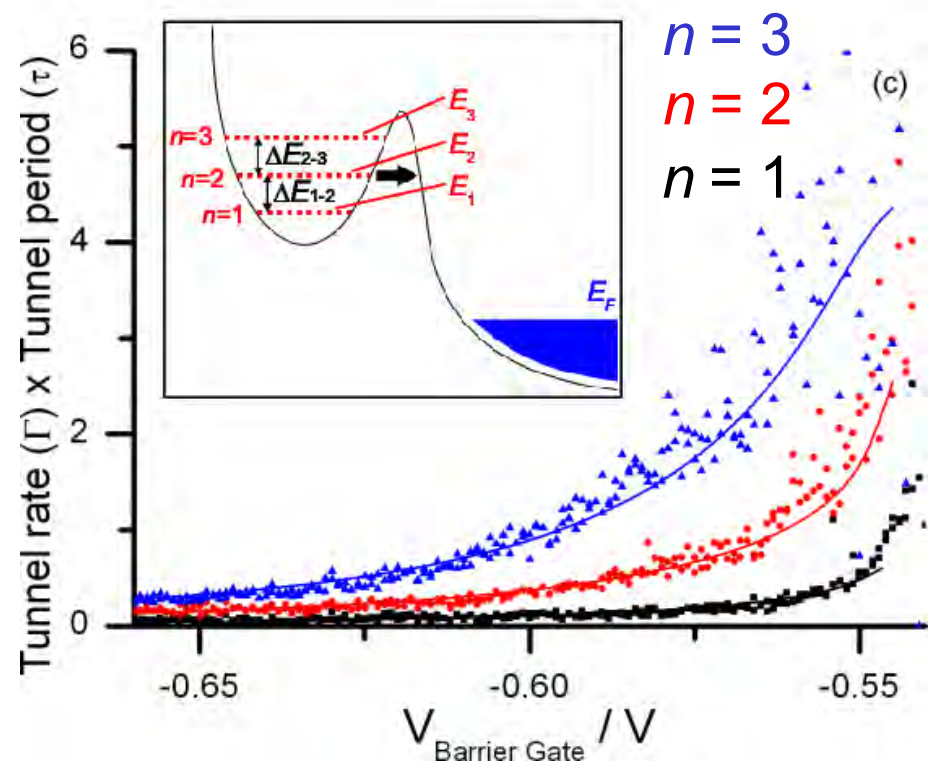
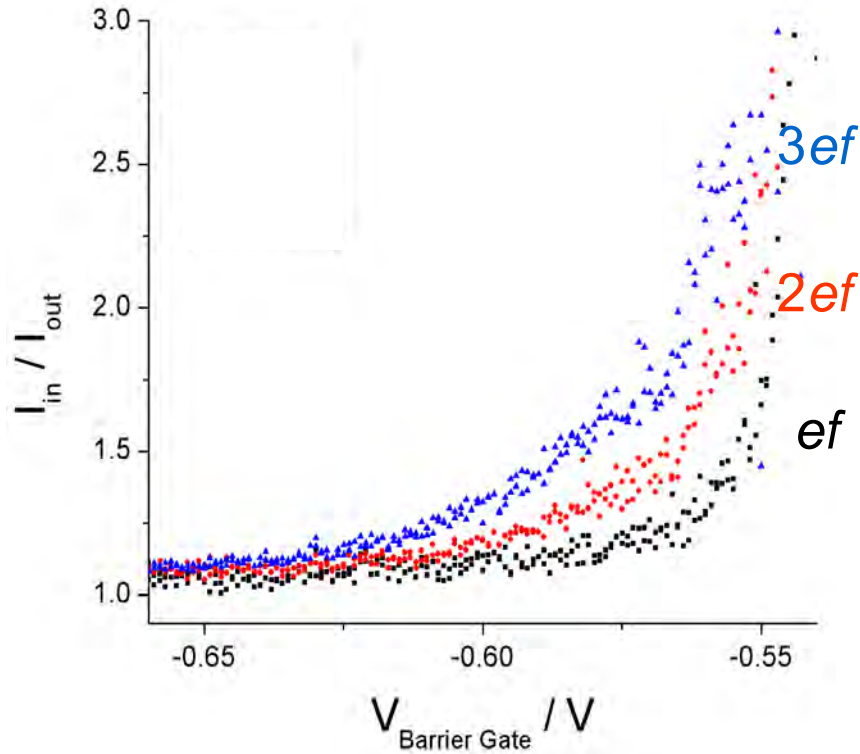


- Potential calculated by solving Laplace's equation

Measurement of electron tunnelling



Signature of dynamic QD confinement



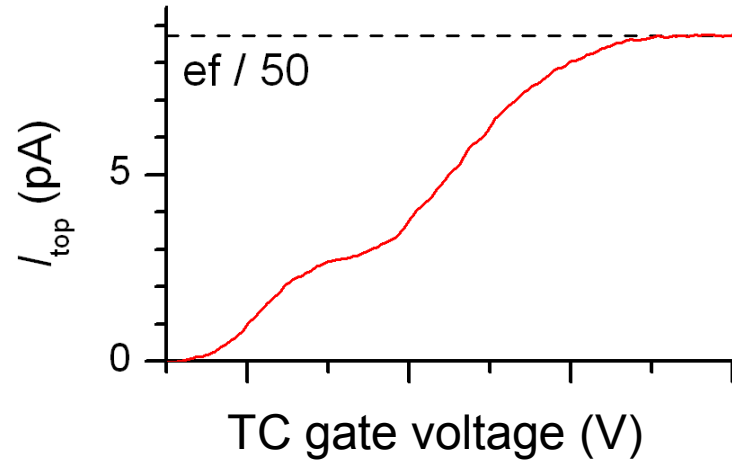
- Ratio I_{in} / I_{out} dependent on number of injected electrons
- Evidence of addition energy

$$\Delta\varepsilon_{1-2} \sim 2.6 \text{ meV}$$

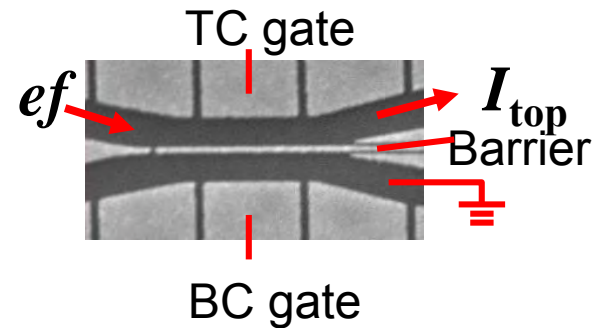
$$\Delta\varepsilon_{2-3} \sim 14 \text{ meV}$$

Astley *et al.*, PRL **99**, 156802 (2007)

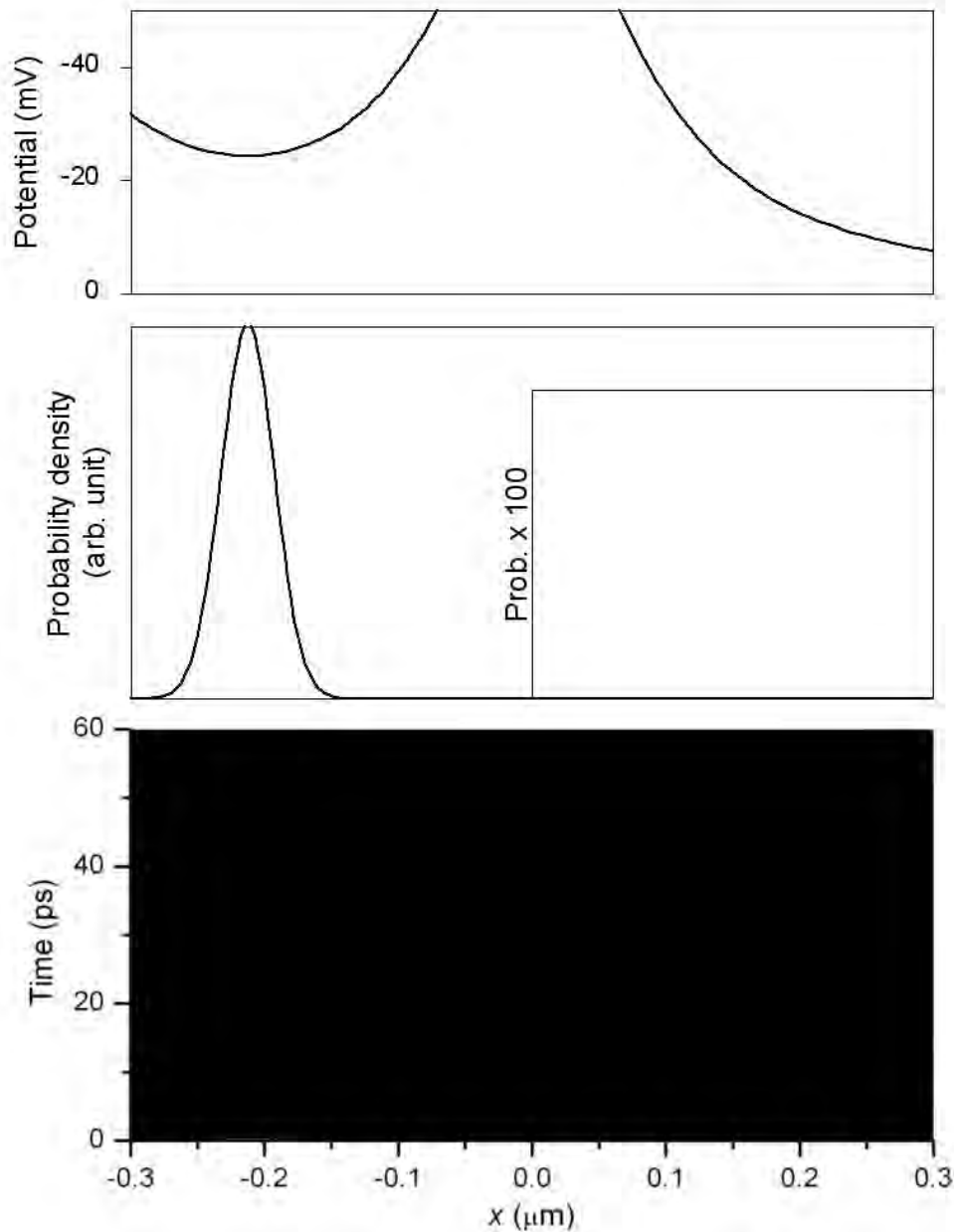
Behaviour of tunnel current



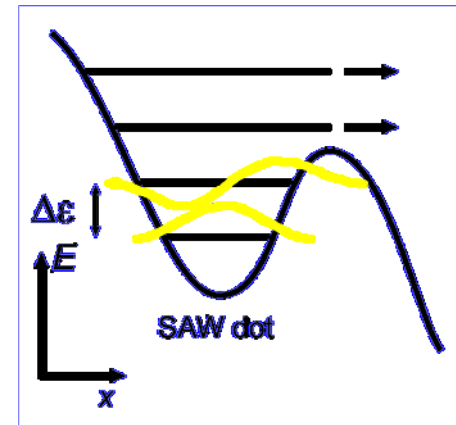
TC gate voltage (V)



Modelling



- Solve t -dependent Schrödinger Eqn (in 1D or 2D)
- Realistic gate potentials

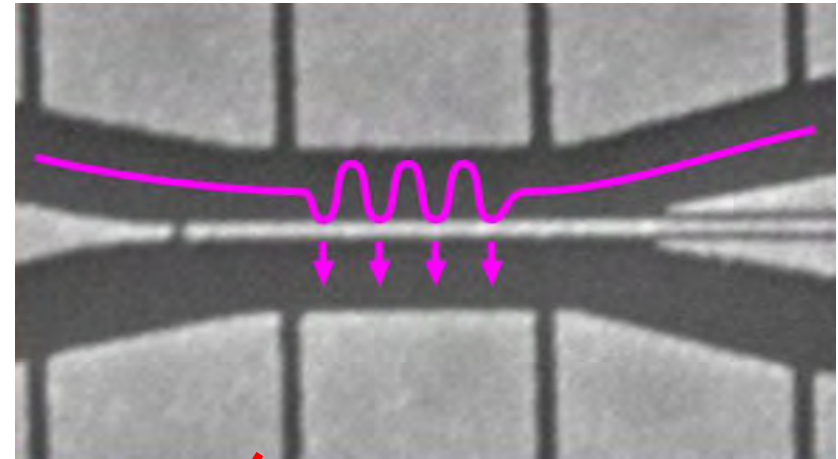
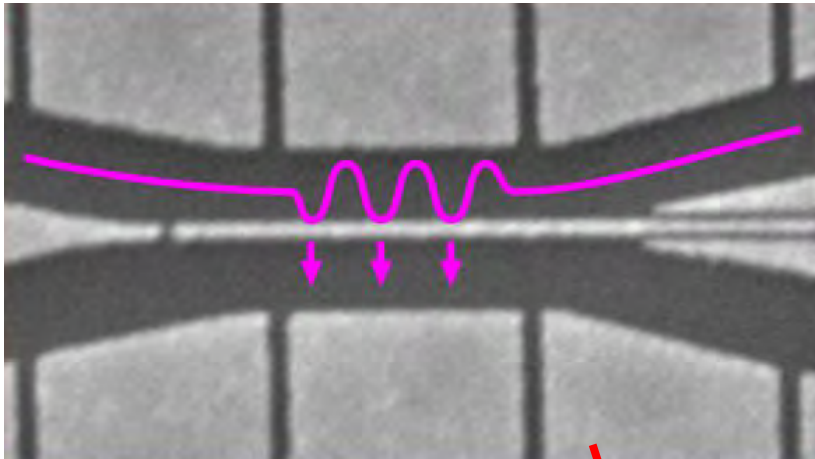
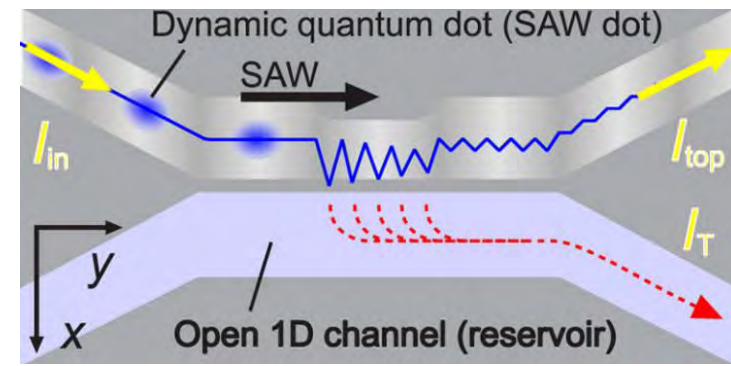


← Coherent oscillations

← All but lowest 2 modes escape rapidly

A. L. Thorn, "Electron dynamics in surface acoustic wave devices", PhD thesis, Cambridge University (2009)

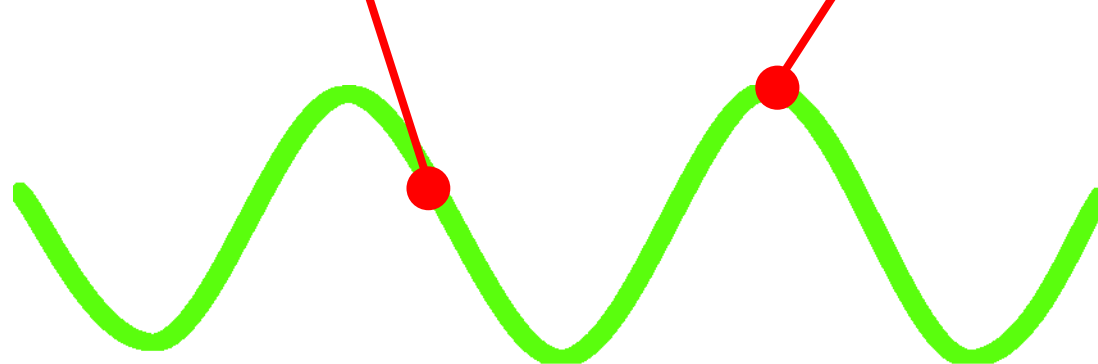
Tunnel-current oscillations



time spent near barrier decreases

extra oscillation fits in

Tunnel current

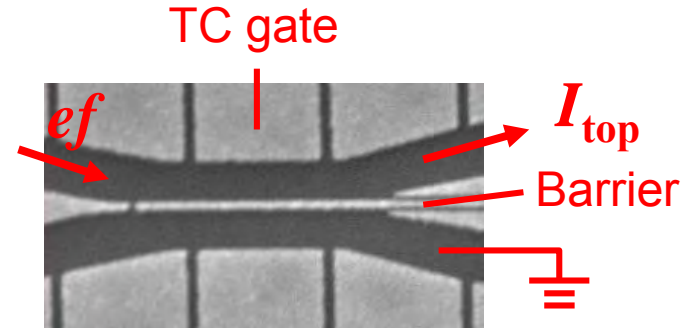
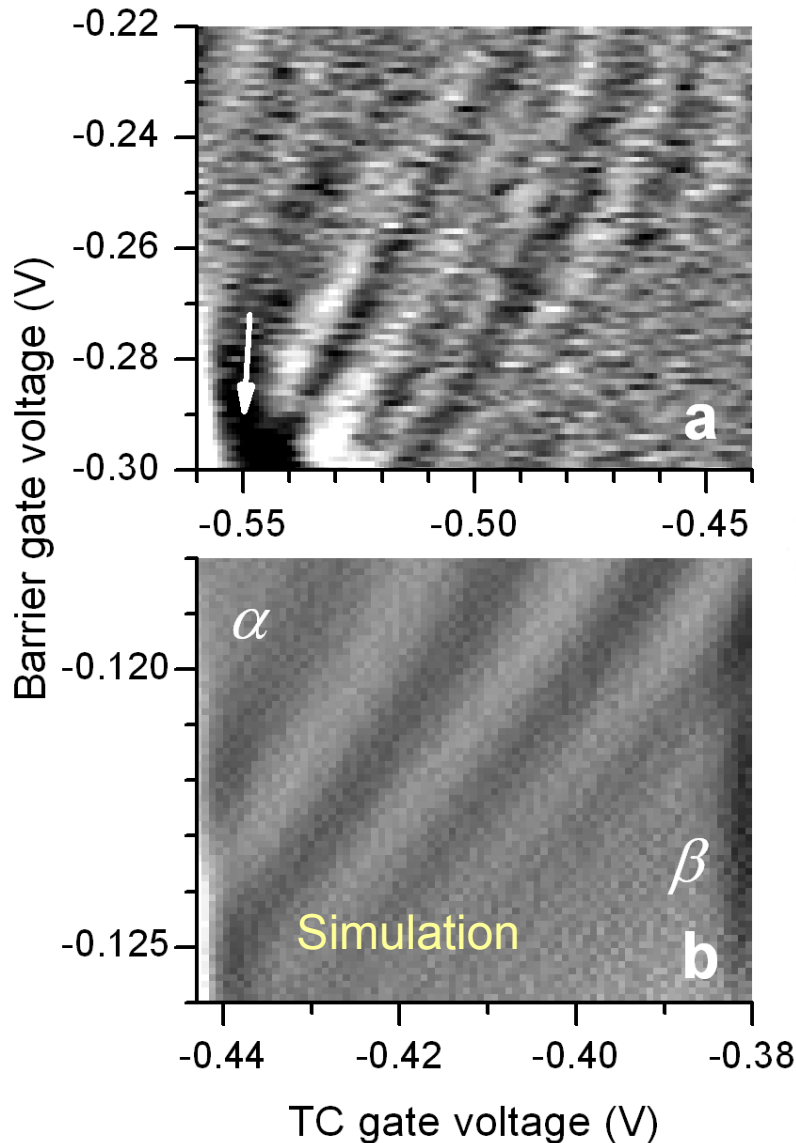


Gate voltage / Oscillation frequency

“Weak” measurement – hardly disturbs wave function

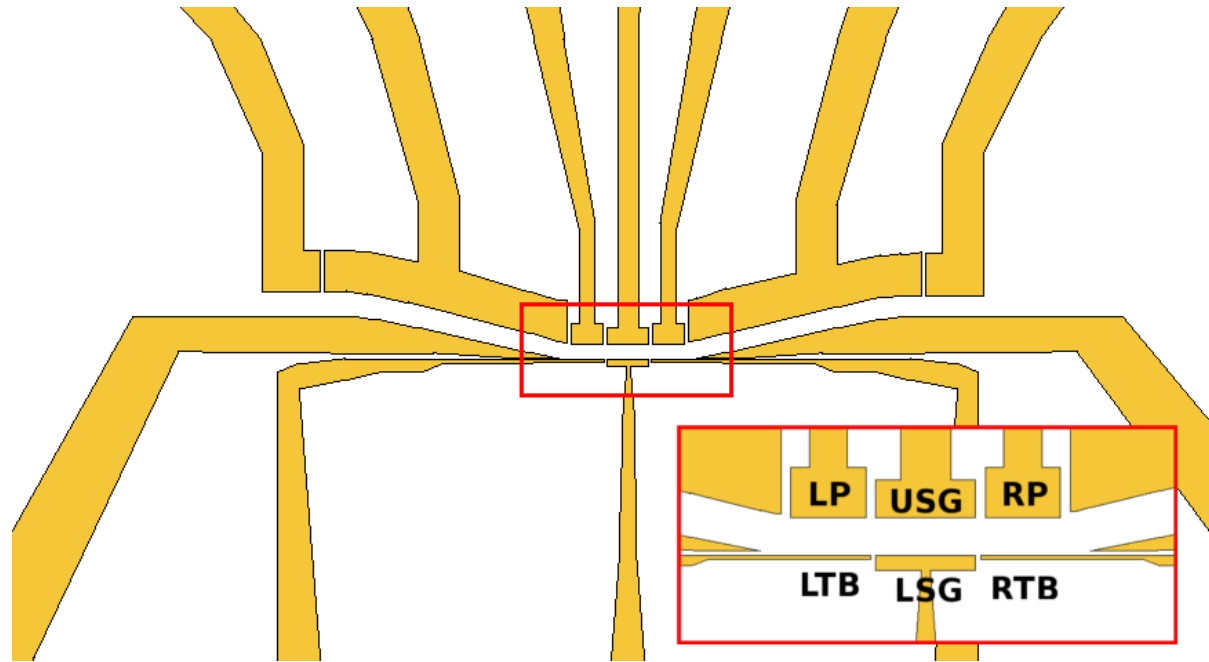
Kataoka *et al.*, PRL 102, 156801 (2009)

Effect of gates



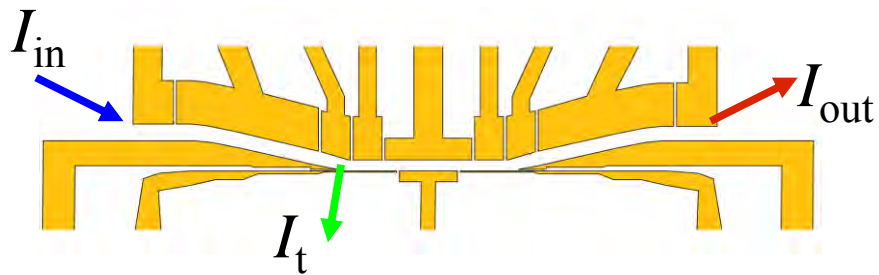
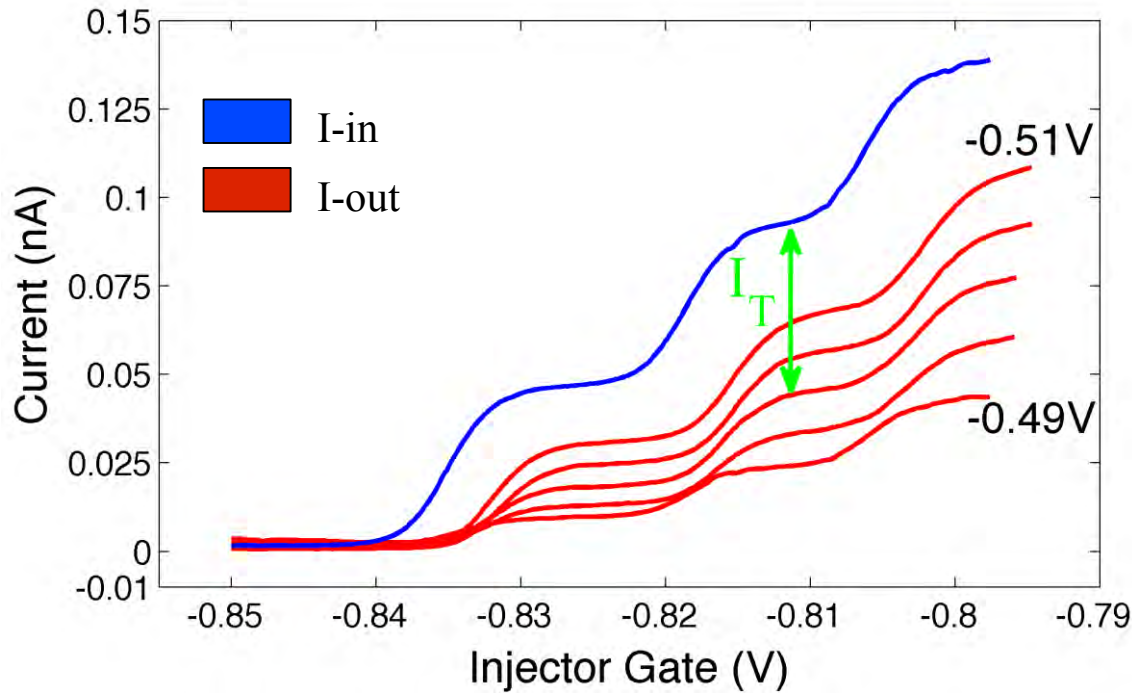
- Simulation using potential calculated by solving Laplace's equation
- Sweeping to a more negative value:
 - TC gate: $\Delta\epsilon$ decreases
 - Barrier gate: $\Delta\epsilon$ increases

Double-barrier device



- Single 1D channel with two tunnelling regions
- Tunnel coupling separately controlled by respective plungers
- Single-electron dots injected from the left and measured at both the upstream and downstream tunnel barriers

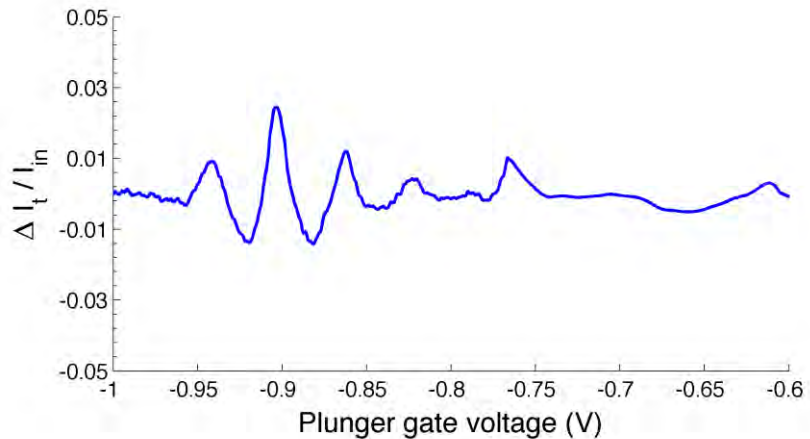
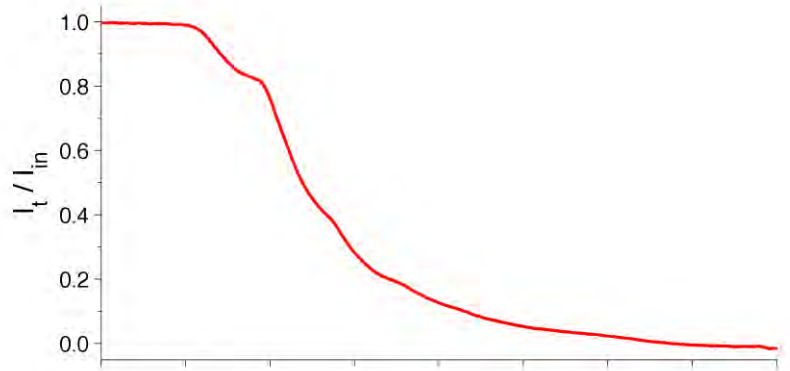
Double-barrier device: tunnel current



- Injector gate can be tuned to low- ef plateaux
- For a range of barrier voltages, the exit current I_{out} shows reduced plateaux
- The exit current is reduced by the barrier-dependent tunnel current

Double barrier: tunnel-current oscillations

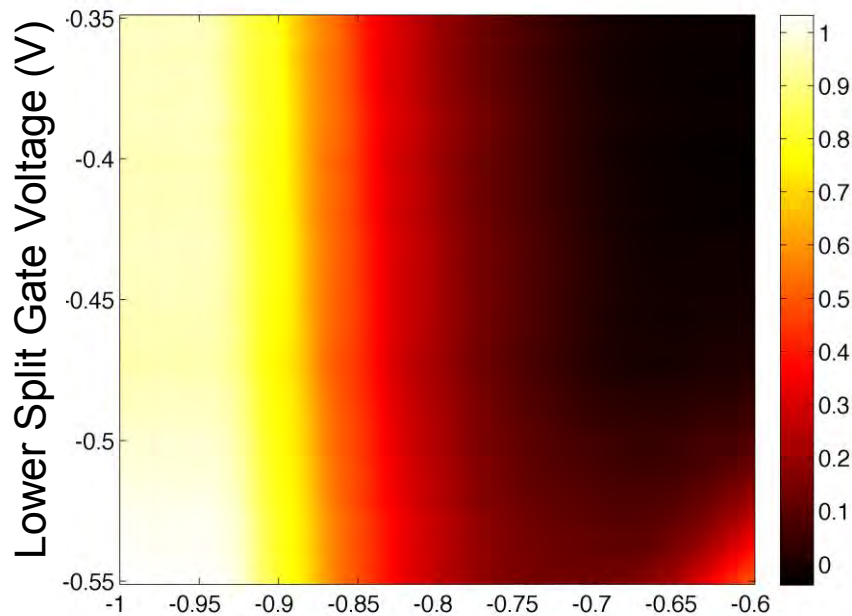
- Typical current variation as plunger gate is swept for a fixed barrier
- Tunnel current varies from 0% to 100% of injected current
- Removal of slowly-varying contributions reveals periodic oscillations



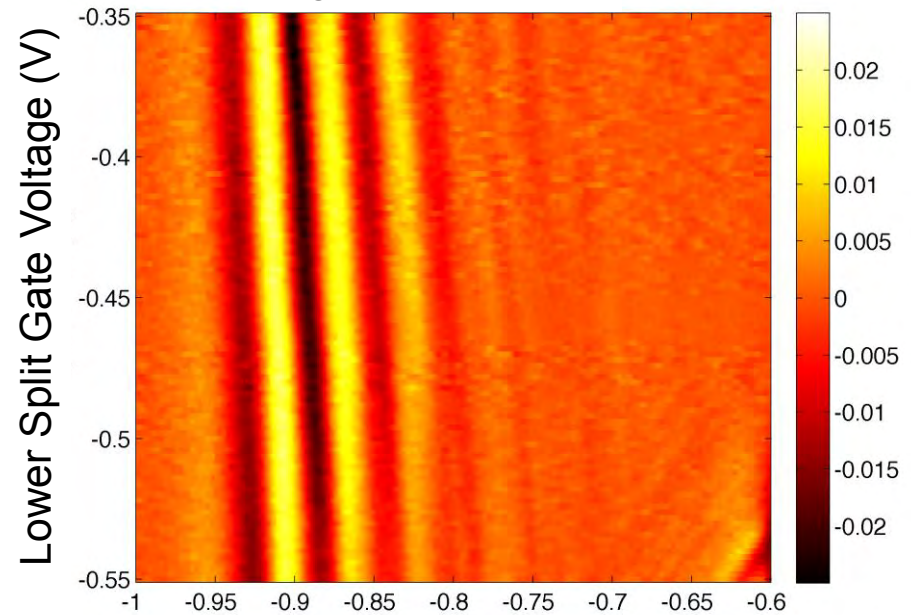
Coherent Oscillations – First Barrier

- Single-electron QDs injected from left
- Vary nearby gate voltages
- Oscillations appear consistently across large voltage ranges

Unfiltered



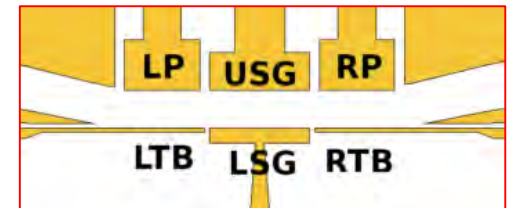
High-pass filtered



Left Plunger Voltage (V)



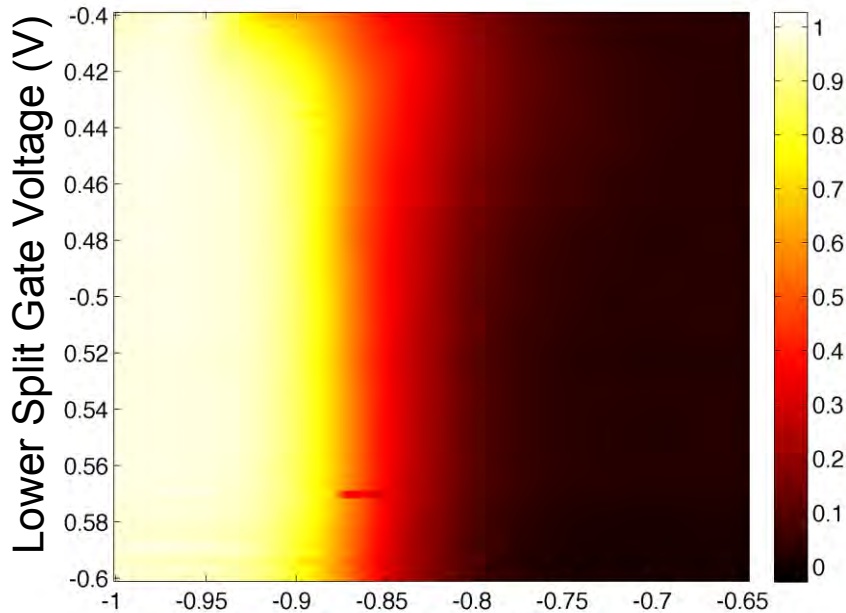
Left Plunger Voltage (V)



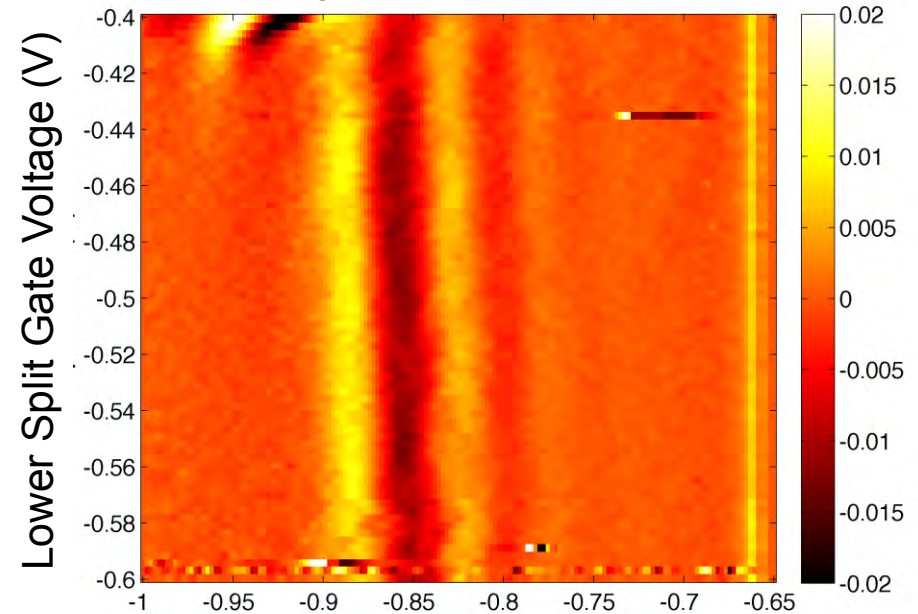
Coherent Oscillations – Second Barrier

- Single-electron QDs injected from left
- LTB is pinched off to prevent tunnelling
- Tunnelling occurs through RTB

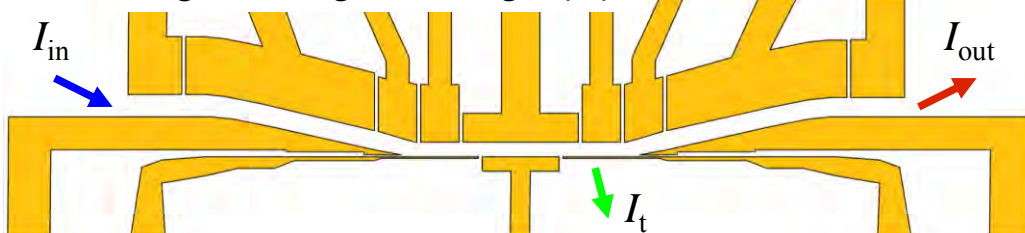
Unfiltered



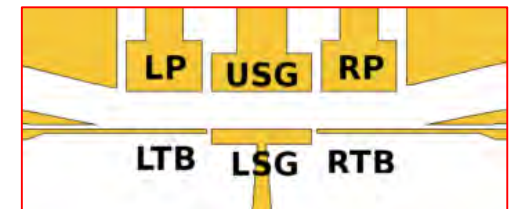
High-pass filtered

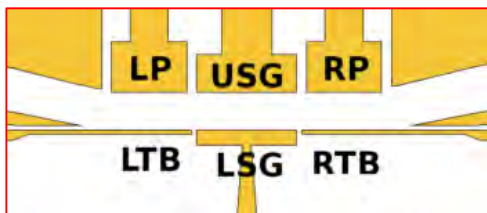


Right Plunger Voltage (V)

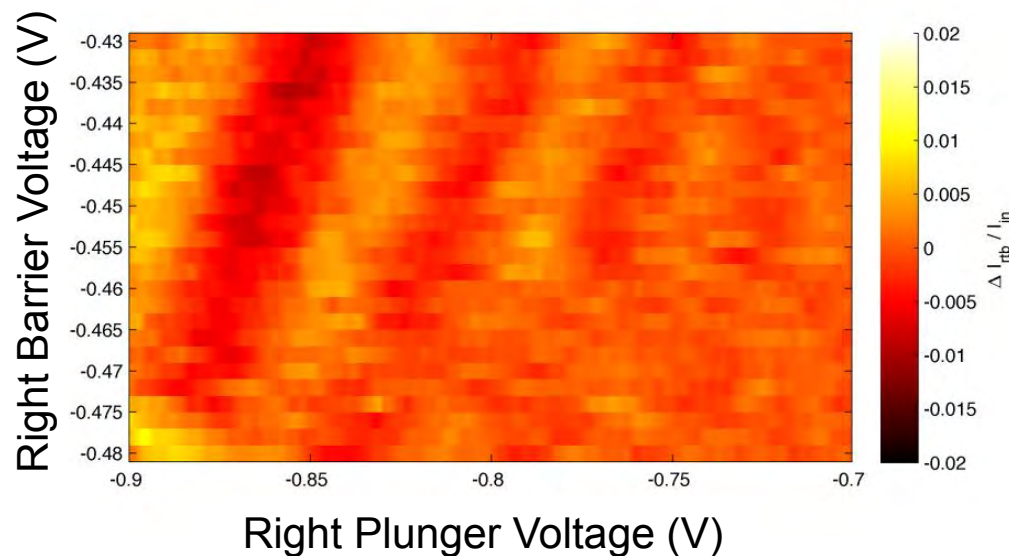
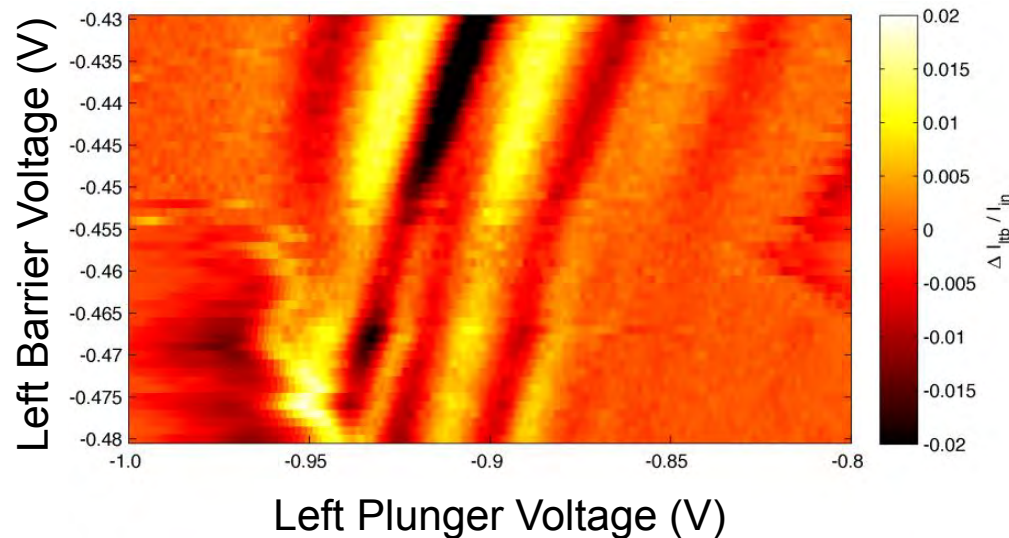


Right Plunger Voltage (V)





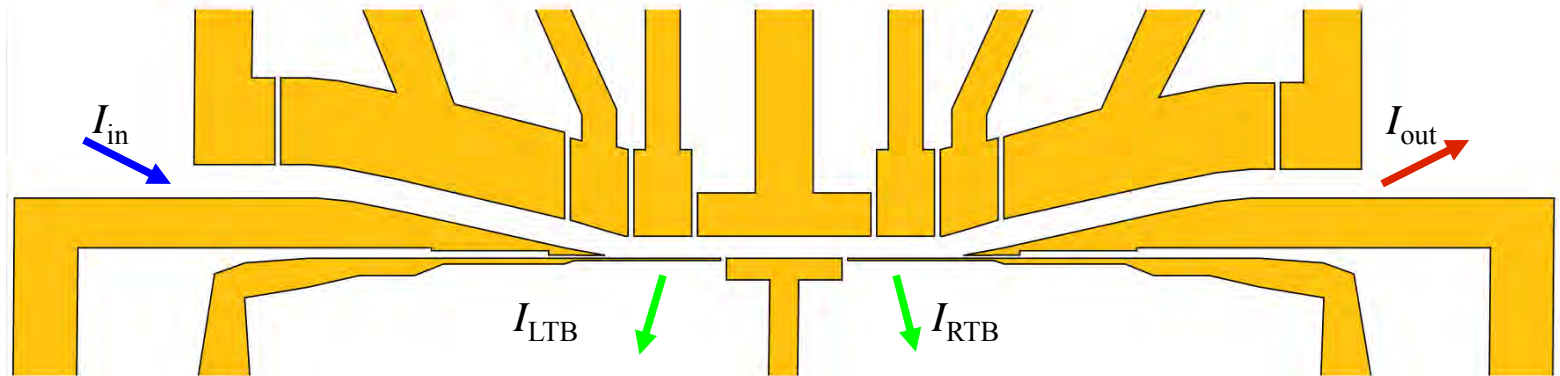
Comparison of barriers



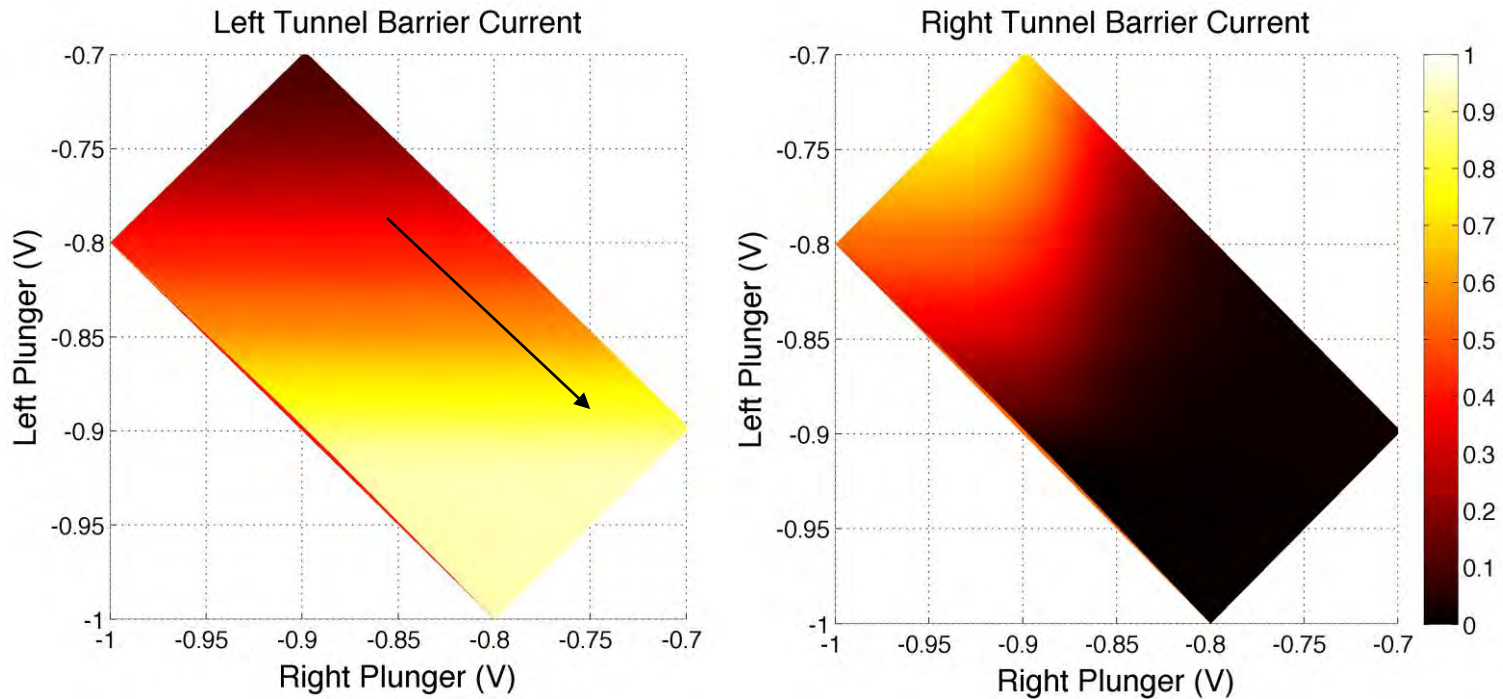
- Measure tunnelling current for each barrier as a function of its own plunger gate
 - when measuring RTB, LTB is pinched off to prevent tunnelling
 - filter out background
- Quite similar oscillations for each

Comparison of tunnelling currents

- Gate voltages are arranged to allow tunnelling through both upstream and downstream tunnel barriers
- Both plungers are swept simultaneously so that filtering along the sweep direction will reveal oscillations caused by either plunger

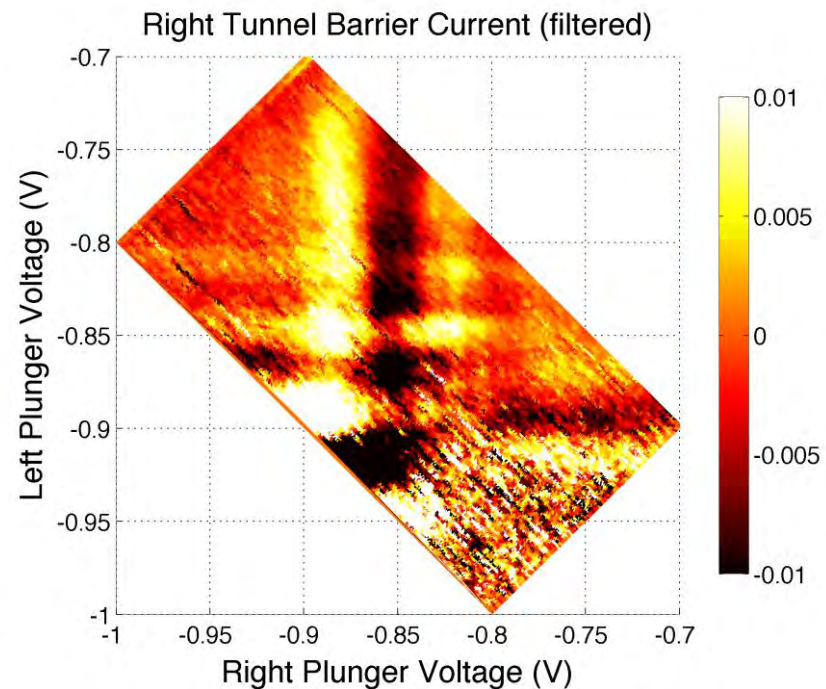
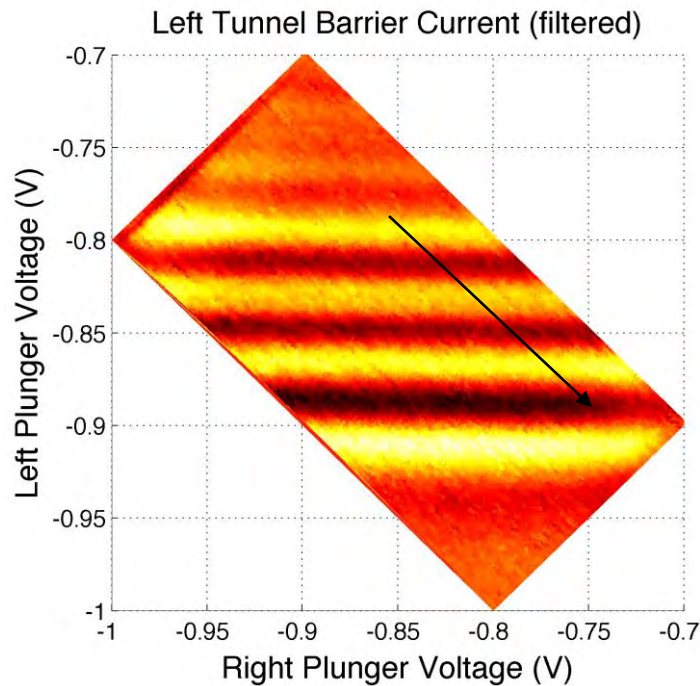


Comparison of tunnelling currents



- I_{LTB} exhibits normal transition to 100% of I_{in}
- I_{RTB} responds as expected
 - reduced by I_{LTB} , as that current has already left the channel

Comparison of tunnelling currents



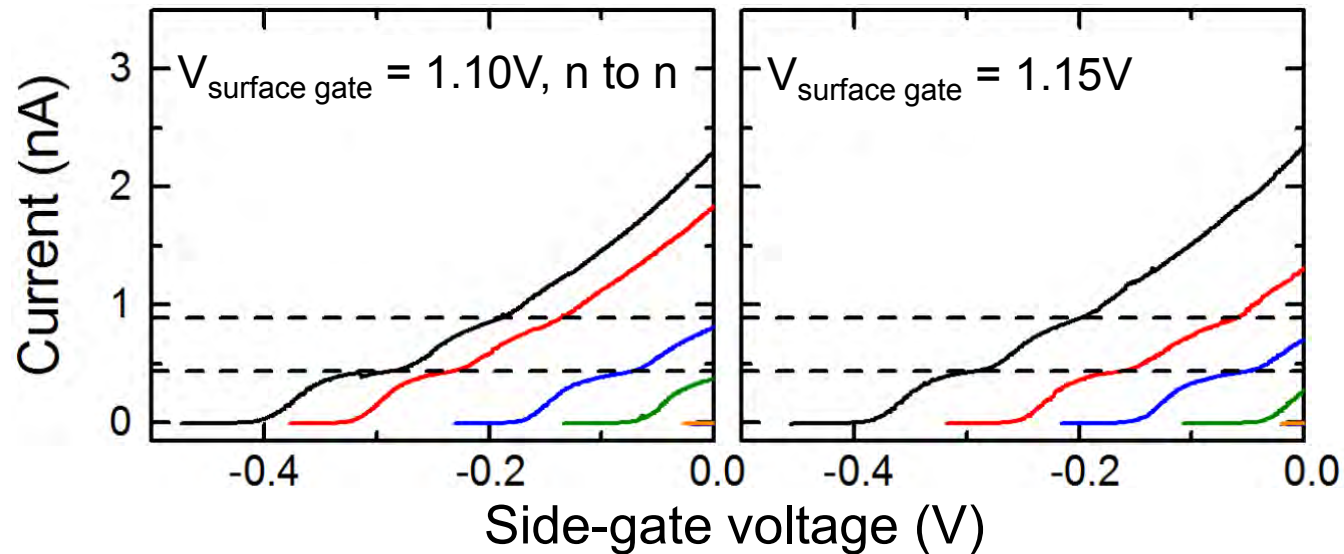
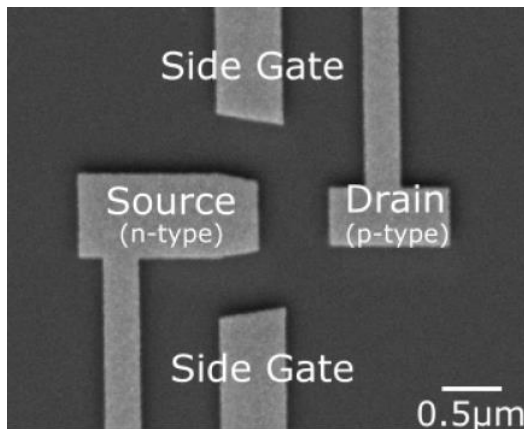
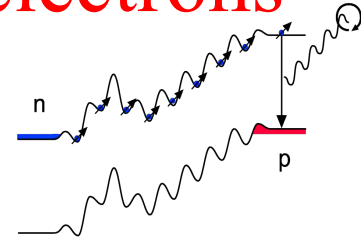
- Oscillations in I_{LTB} appear as previously measured, with no dependence on the right plunger
 - not cross-capacitance
- I_{RTB} shows significant dependence on both plungers, leading to a checkerboard oscillation pattern

Coherence length

- Oscillations in RTB tunnelling current occur as a function of the *left* plunger
- Oscillations were initialised in the left region, so they must have continued for at least part of the left region and the central region (1.5–3 μm)
 - suggests a coherence time of $\sim 500\text{ps}$ or more (SAW travels $1\mu\text{m}$ in 300ps)

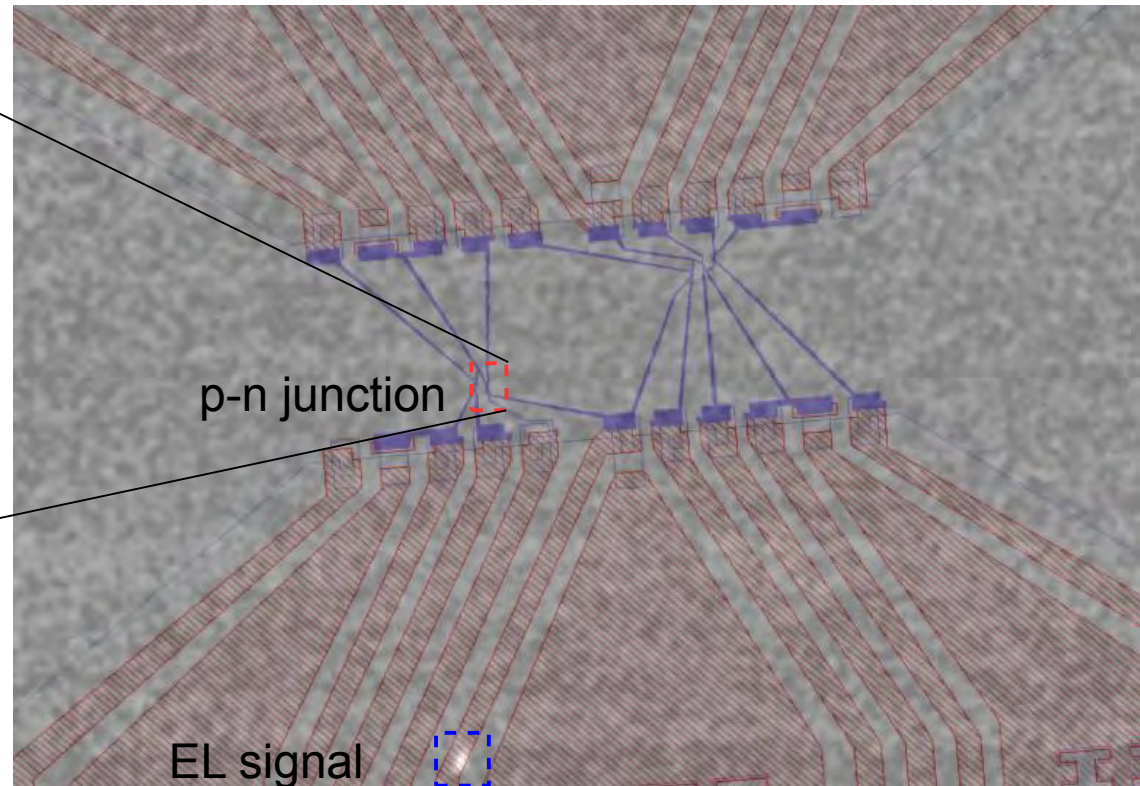
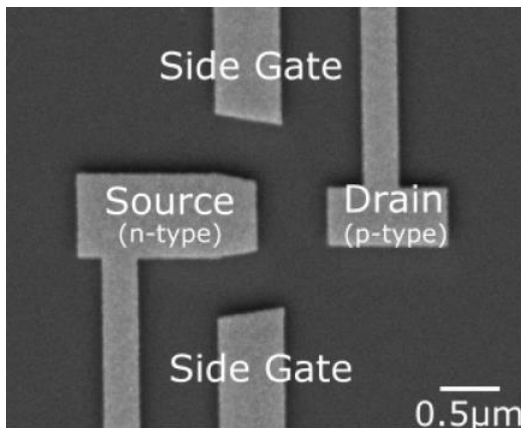
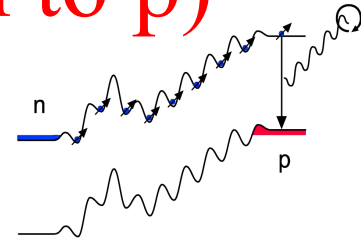
Generating photons from SAW-pumped electrons

- The SAW can pump electrons uphill
 - can it pump them into a sea of holes?
- Cannot dope a wafer differently in different places, so use undoped wafer and induce electrons and holes
 - we have developed quite reliable ohmic contacts for e and h
 - gates on surface bring electrons and/or holes within $1\mu\text{m}$
 - quantised current n to n (two regions of electrons)



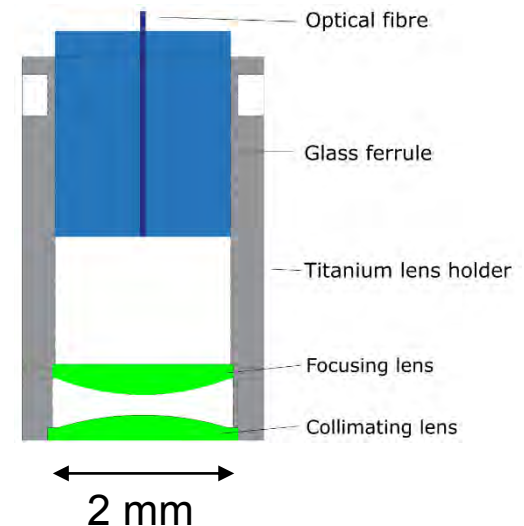
Pumping from electrons to holes (n to p)

- Induce electrons and holes close together
 - forward-bias the p-n junction to reduce barrier slope
 - SAW can pump electrons into conduction band above the holes
 - so far, light comes out from the wrong place!
 - need to etch around junction to confine electrons in same place as holes until they recombine



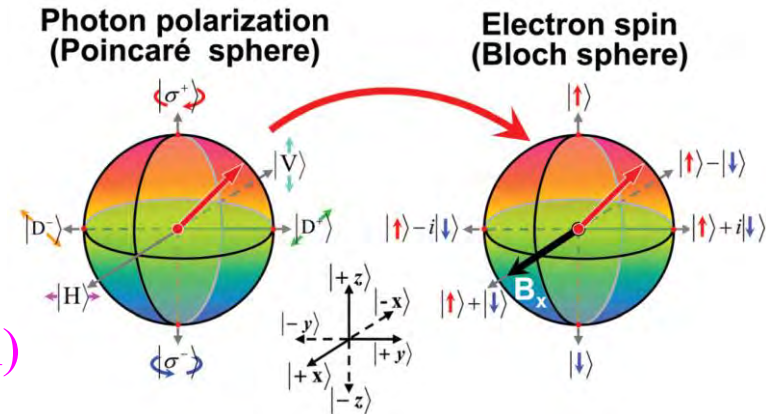
^3He microscope

- We have constructed a scanning optical microscope
 - works in ^3He top-loading cryostat at $T \geq 300$ mK
 - optical fibre, piezo stage, $1\mu\text{m}$ resolution
 - should preserve polarisation (with calibration)
 - sample holder (and coax cables) is fixed
 - lens assembly is scanned
 - available for other applications...

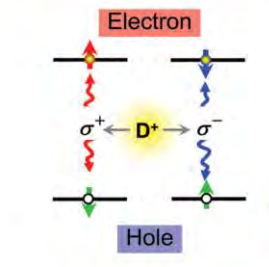


Conversion between photon and electron qubits

- Convert electron's spin to circular polarisation of a photon
 - absence of the hole is information that decoheres rapidly (or no-cloning theorem)
 - so cannot convert a spin qubit (superposition) to photon polarisation qubit coherently
- Kosaka showed that can arrange to have all holes in state $|\rightarrow\rangle = (|\uparrow\rangle + |\downarrow\rangle)/\sqrt{2}$
 - any electron in $\alpha|\uparrow\rangle + \beta|\downarrow\rangle$ can recombine with such a hole, photon will maintain the superposition as $\alpha|\sigma^+\rangle + \beta|\sigma^-\rangle$
 - $g = 0$ for electrons (15 nm $\text{Al}_{0.14}\text{Ga}_{0.86}\text{As}$ QW)
 - use the light (not heavy) holes (large enough g)
 - H. Kosaka, *J. Appl. Phys.* **109**, 102414 (2011), *Nature* **457**, 702 (2009); *PRL* **100**, 096602 (2008); Vrijen, Yablonovitch, *Physica E* **10**, 569 (2001)



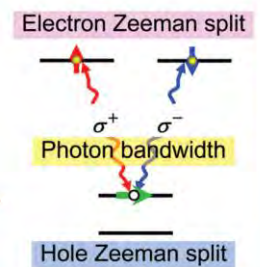
Heavy-hole exciton



Entangle

$$|\uparrow\rangle_e \otimes |\downarrow\rangle_h + |\downarrow\rangle_e \otimes |\uparrow\rangle_h$$

Light-hole exciton



Separable

$$(|\uparrow\rangle_e + |\downarrow\rangle_e) \otimes |+\rangle_h$$

$$\begin{matrix} g_e \mu_B \\ \wedge \\ \Delta \omega_{ph} \\ \wedge \\ g_h \mu_B \end{matrix}$$

Conclusions

- Dynamic dots are interesting objects with applications in quantum computing
 - generate with a SAW in a long channel
- SAWs can transfer an electron back and forth between two dots
 - couple qubits, transfer to/from quantum memory?
 - electron “ping pong”
 - next step: polarise spin and read it optically
- Single electron in a moving quantum dot can oscillate coherently
 - non-adiabatic transition in channel excites electron into combination of ground and first excited states, producing coherent oscillations that persist for more than 500ps
 - tunnelling probability sensitive to dynamics of single-electron wave function in dot
 - inclusion of multiple tunnelling regions allows initialisation of the oscillation phase, which is then detectable at tunnelling regions downstream
 - can repeatedly make a weak measurement that does not collapse the wave function (Schrödinger’s cat still wouldn’t know if it was alive or dead!)
- Electron and hole regions, (single-)photon emission, qubit conversion?

