

# Giant artificial atoms coupled to a 1D waveguide

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# Outline

Introduction — Atom sizes

One giant atom coupled to a 1D waveguide —  
frequency-dependent relaxation rate and Lamb shift

Extensions — time delay, multiple giant atoms in  
various geometries

Summary

# Atom sizes

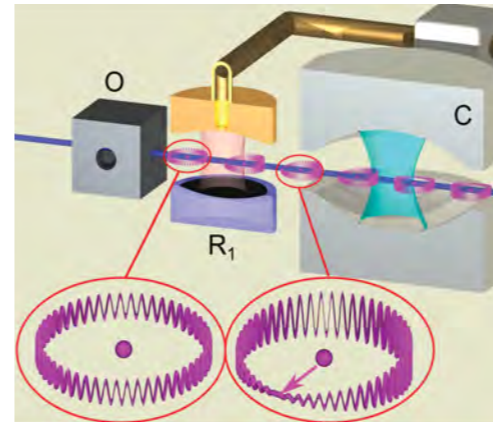
## Atom, optical light

$$r \approx 10^{-10} \text{ m}$$

$$\lambda \approx 10^{-7} - 10^{-6} \text{ m}$$

$$r/\lambda \approx 10^{-4} - 10^{-3}$$

## Rydberg atom, microwaves



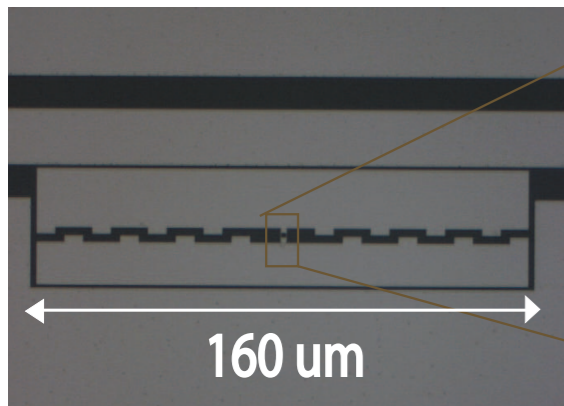
$$r \approx 10^{-8} - 10^{-7} \text{ m}$$

$$\lambda \approx 10^{-3} - 10^{-1} \text{ m}$$

$$r/\lambda \approx 10^{-7} - 10^{-4}$$

Haroche, Nobel Lecture, RMP (2013)

## Transmon, microwaves



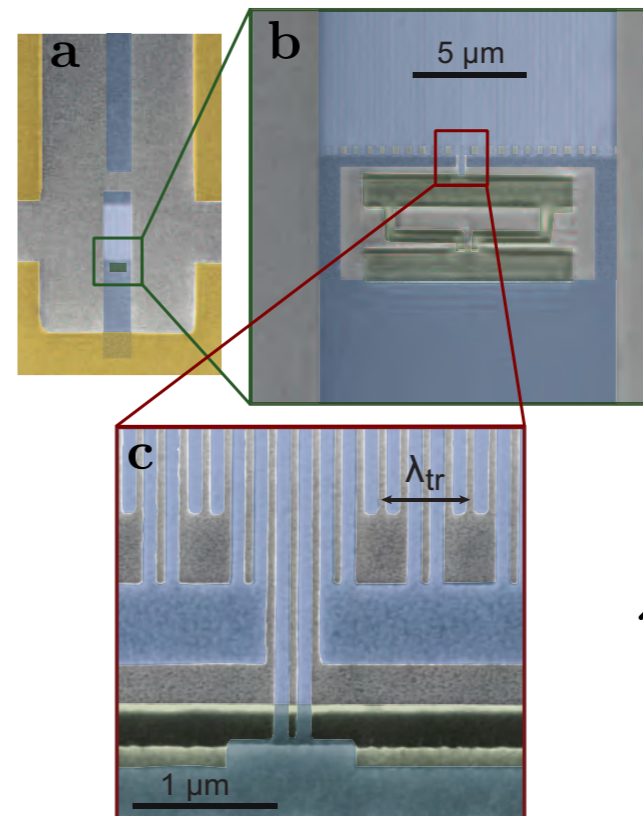
$$l \approx 10^{-5} - 10^{-3} \text{ m}$$

$$\lambda \approx 10^{-3} - 10^{-1} \text{ m}$$

$$l/\lambda \approx 10^{-4} - 1$$

Picture by I.-C. Hoi

## Transmon, surface acoustic waves

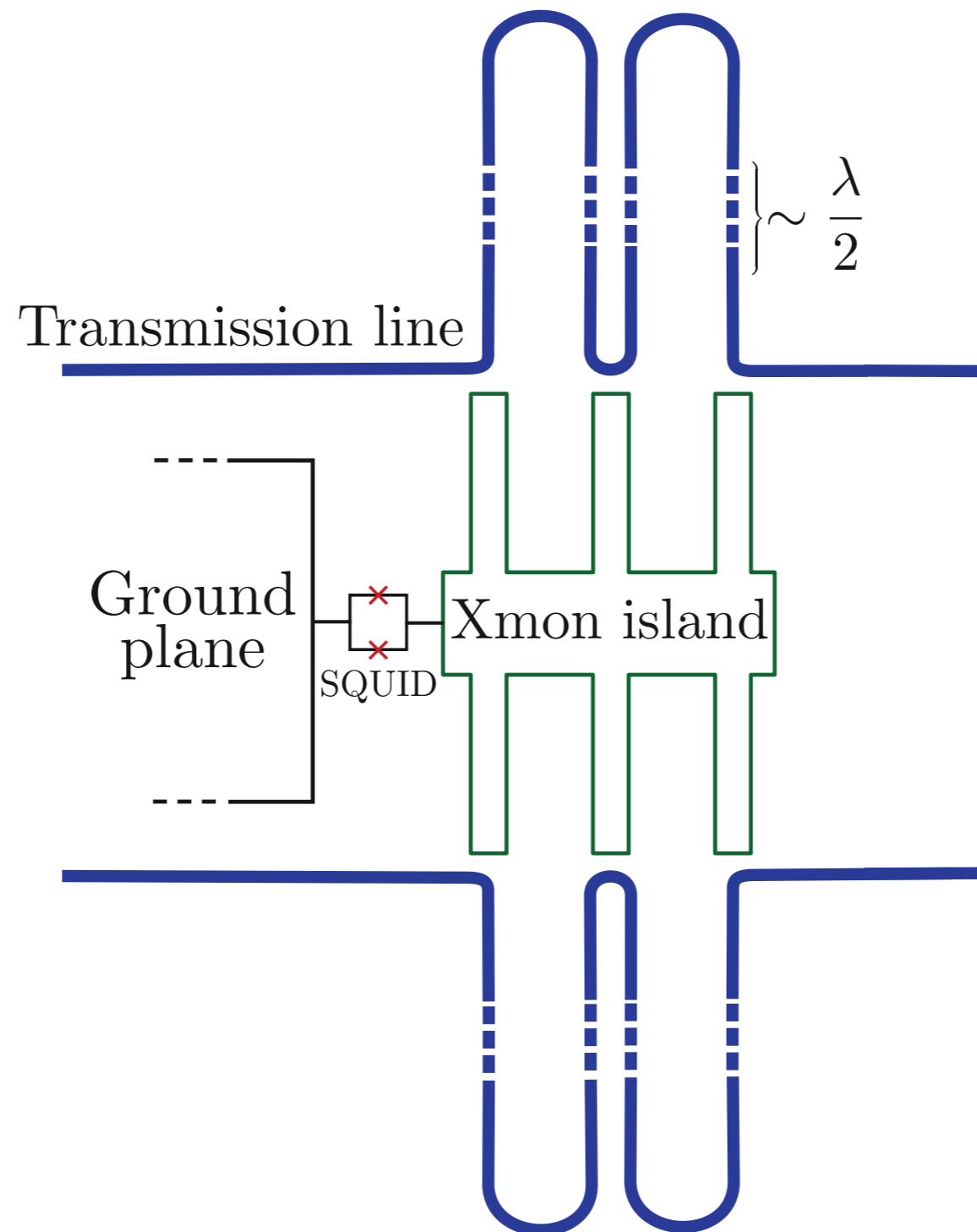


$$l \approx 10^{-5} - 10^{-4} \text{ m}$$

$$\lambda \approx 10^{-6} - 10^{-5} \text{ m}$$

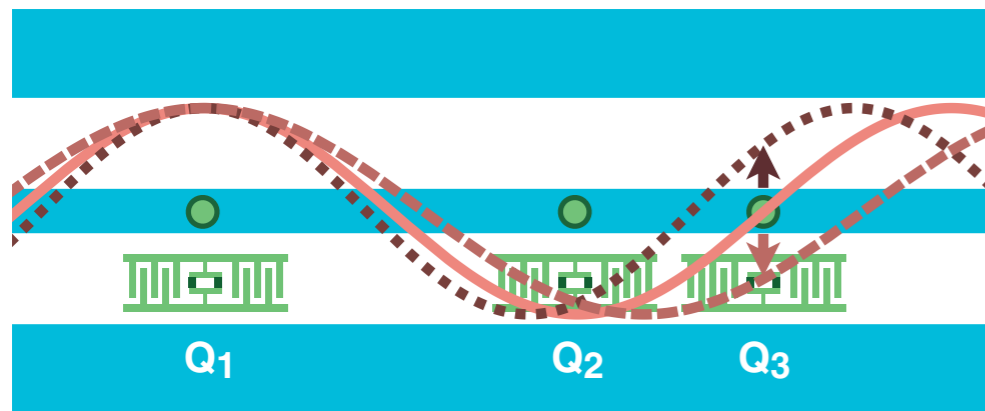
$$l/\lambda \approx 1 - 100$$

# Giant atoms in circuit QED?



# Interference effects

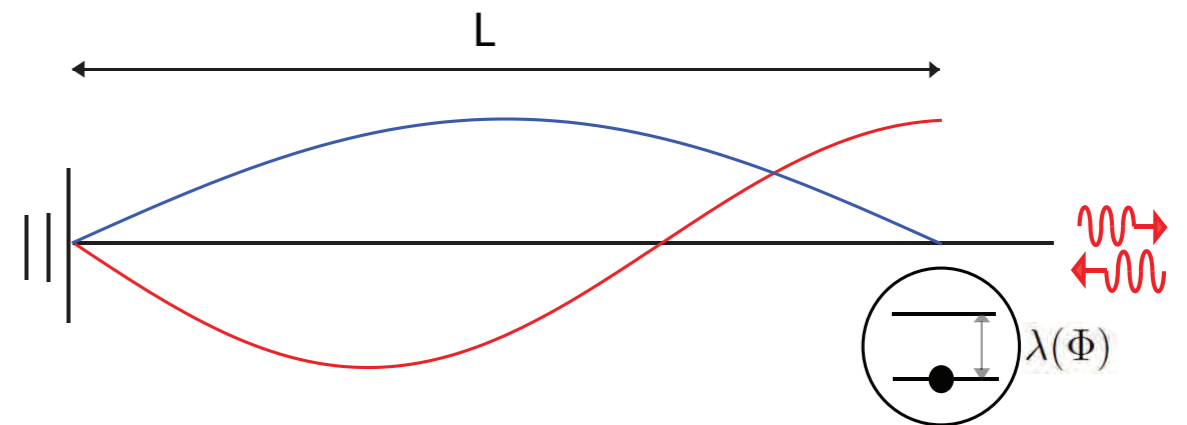
Several small atoms  
spaced wavelengths apart



Lalumière *et al.*, PRA **88**, 043806 (2013)

van Loo *et al.*, Science **342**, 1494 (2013)

One small atom in front of a mirror



Hoi *et al.*, Nature Physics **11**, 1045 (2015)

Koshino and Nakamura, NJP **14**, 043005 (2012)

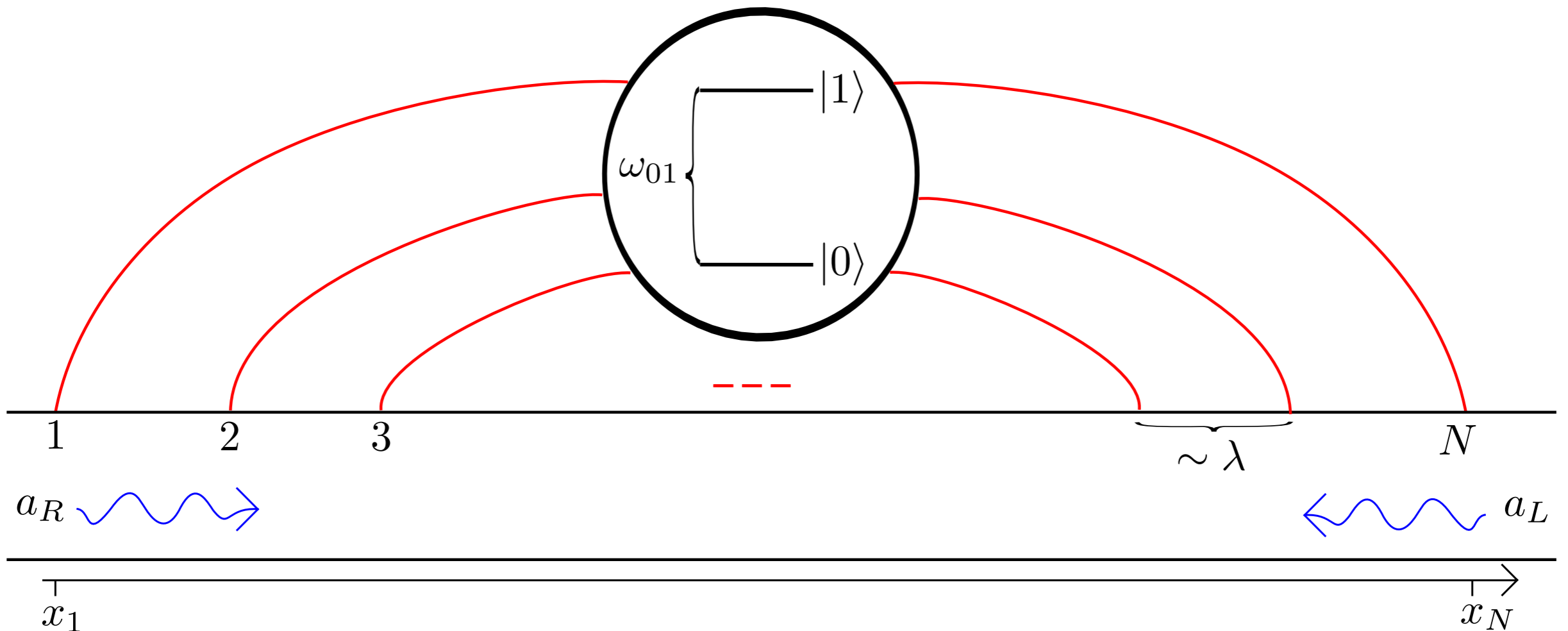
Eschner *et al.*, Nature **413**, 495 (2001)

Dorner and Zoller, PRA **66**, 023816 (2002)

Classical SAW  
filters in mobile phones, TVs, etc.

Morgan, *Surface Acoustic Wave Filters* (2007)

# Giant artificial atom

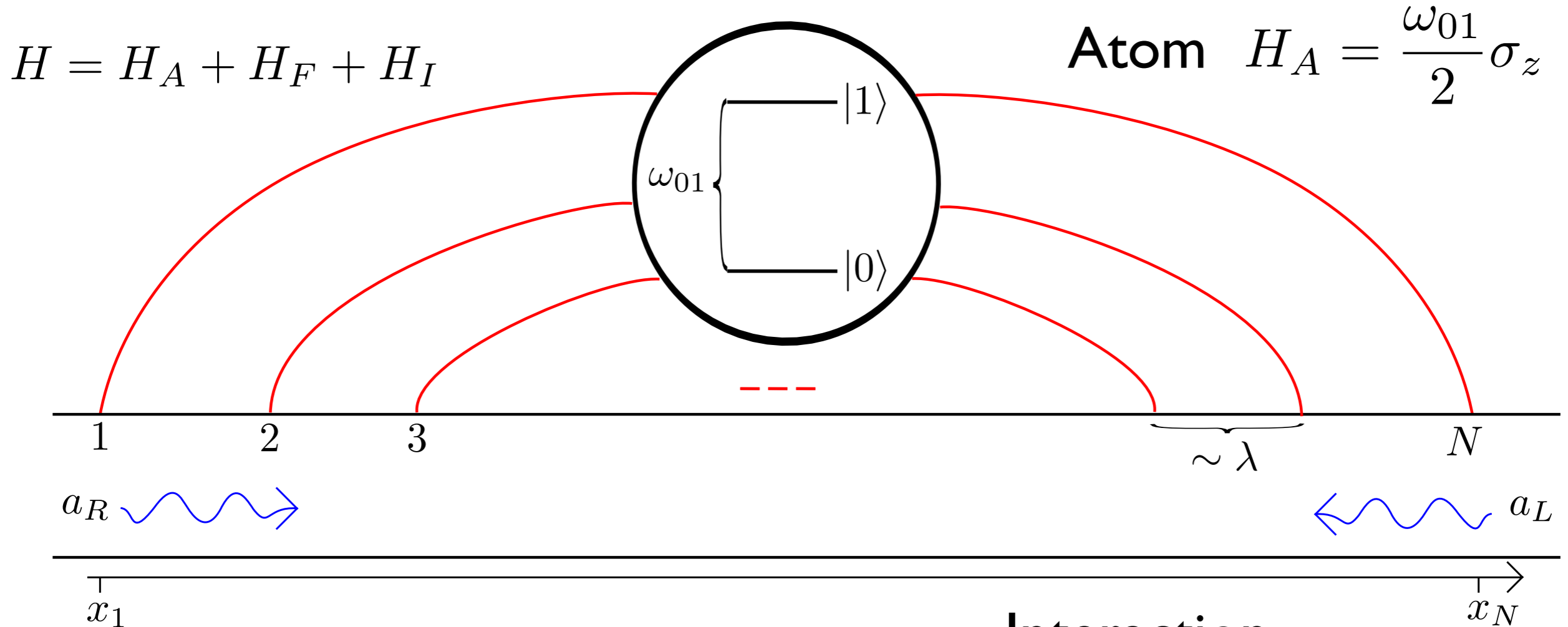


Multiple coupling points  $\rightarrow$  strong interference effects

Additional time scale: travel time across the atom  $(x_N - x_1)/v$

We work in the limit where this is negligible compared to  $1/\Gamma$

# Hamiltonian



## Interaction

All field modes

$$H_F = \sum_j \omega_j \left( a_{Rj}^\dagger a_{Rj} + a_{Lj}^\dagger a_{Lj} \right)$$

$$H_I = \sum_{j,k} g_k \left[ \left( a_{Rj} e^{i\omega_j x_k/v} + a_{Lj} e^{-i\omega_j x_k/v} \right) |1\rangle\langle 0| + \left( a_{Rj}^\dagger e^{-i\omega_j x_k/v} + a_{Lj}^\dagger e^{i\omega_j x_k/v} \right) |0\rangle\langle 1| \right]$$

# Frequency dependence

Interference

$$A(\omega_j) = \sum_k g_k e^{-i\omega_j x_k / v}$$

$k$  Coupling point

$j$  Field mode

Relaxation rate

$$\Gamma = 4\pi J(\omega_{10}) |A(\omega_{10})|^2$$

Lamb shift

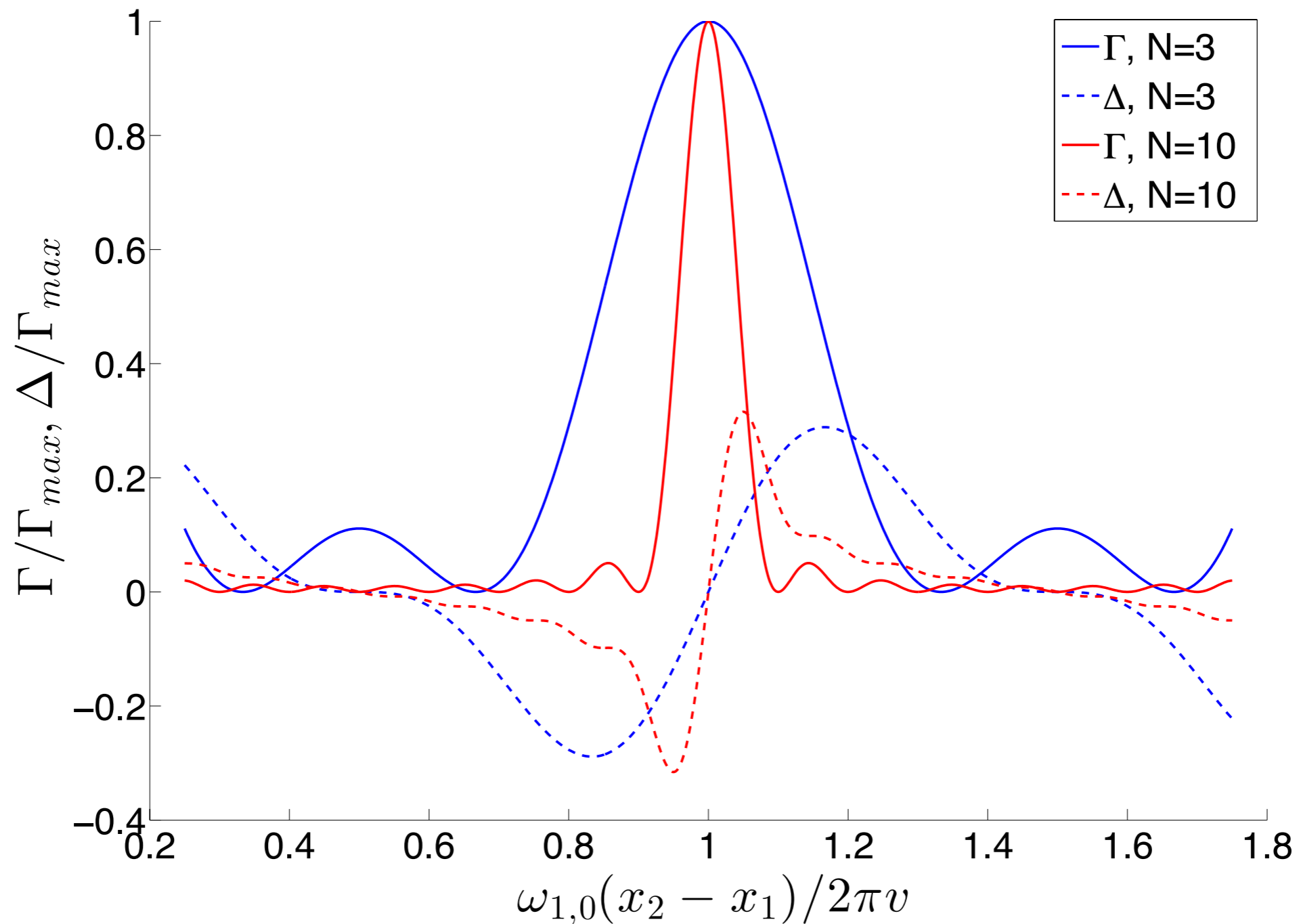
$$\Delta = -2\mathcal{P} \int_0^\infty d\omega \frac{2\omega_{10} J(\omega) |A(\omega)|^2}{\omega^2 - \omega_{10}^2}$$

Density of states  $J(\omega)$

Small atom  $|A(\omega_{10})|^2 = g^2$

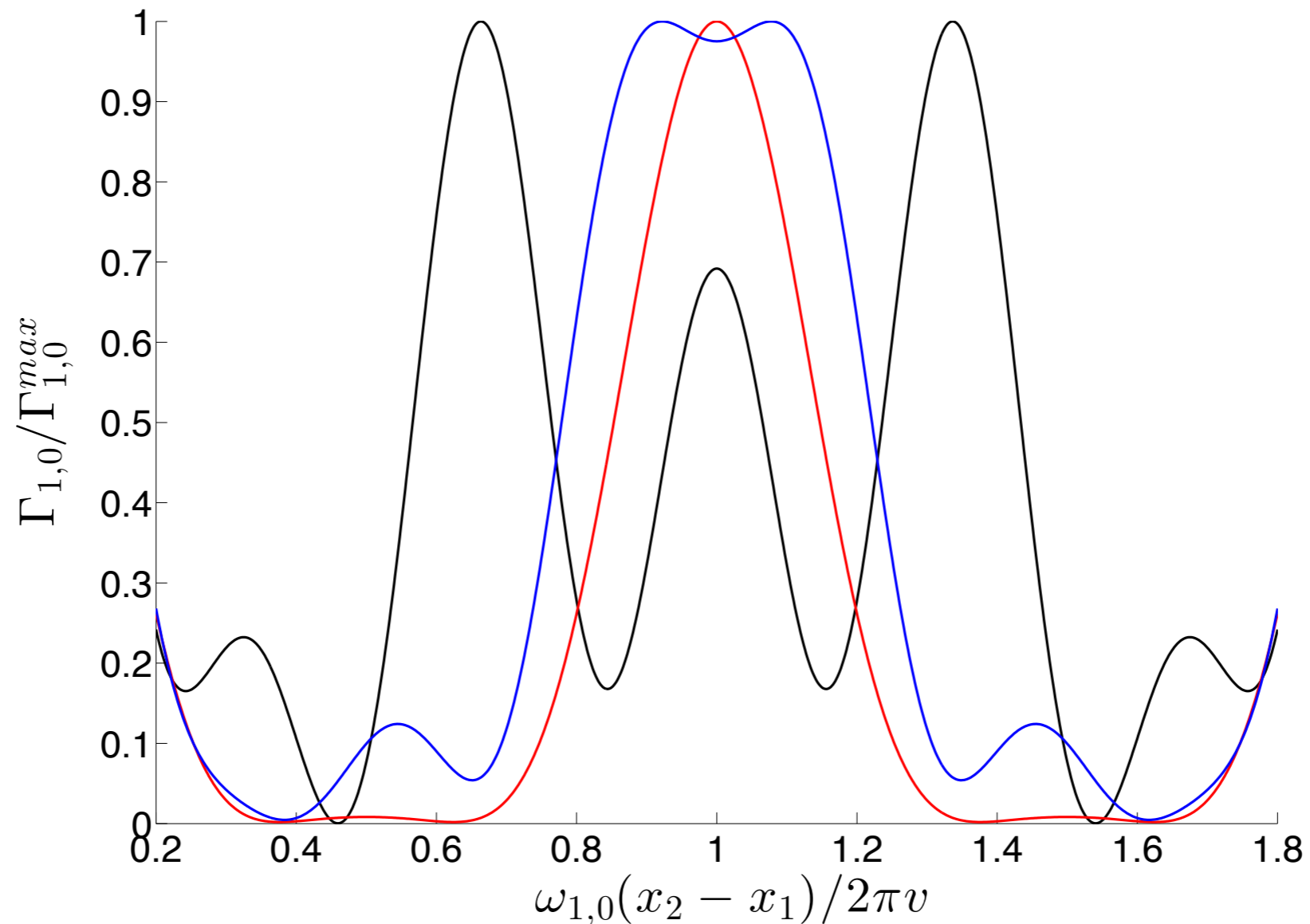


# Giant artificial atom



Frequency-dependent relaxation rate  $\Gamma$  and Lamb shift  $\Delta$

# Designing relaxation rates

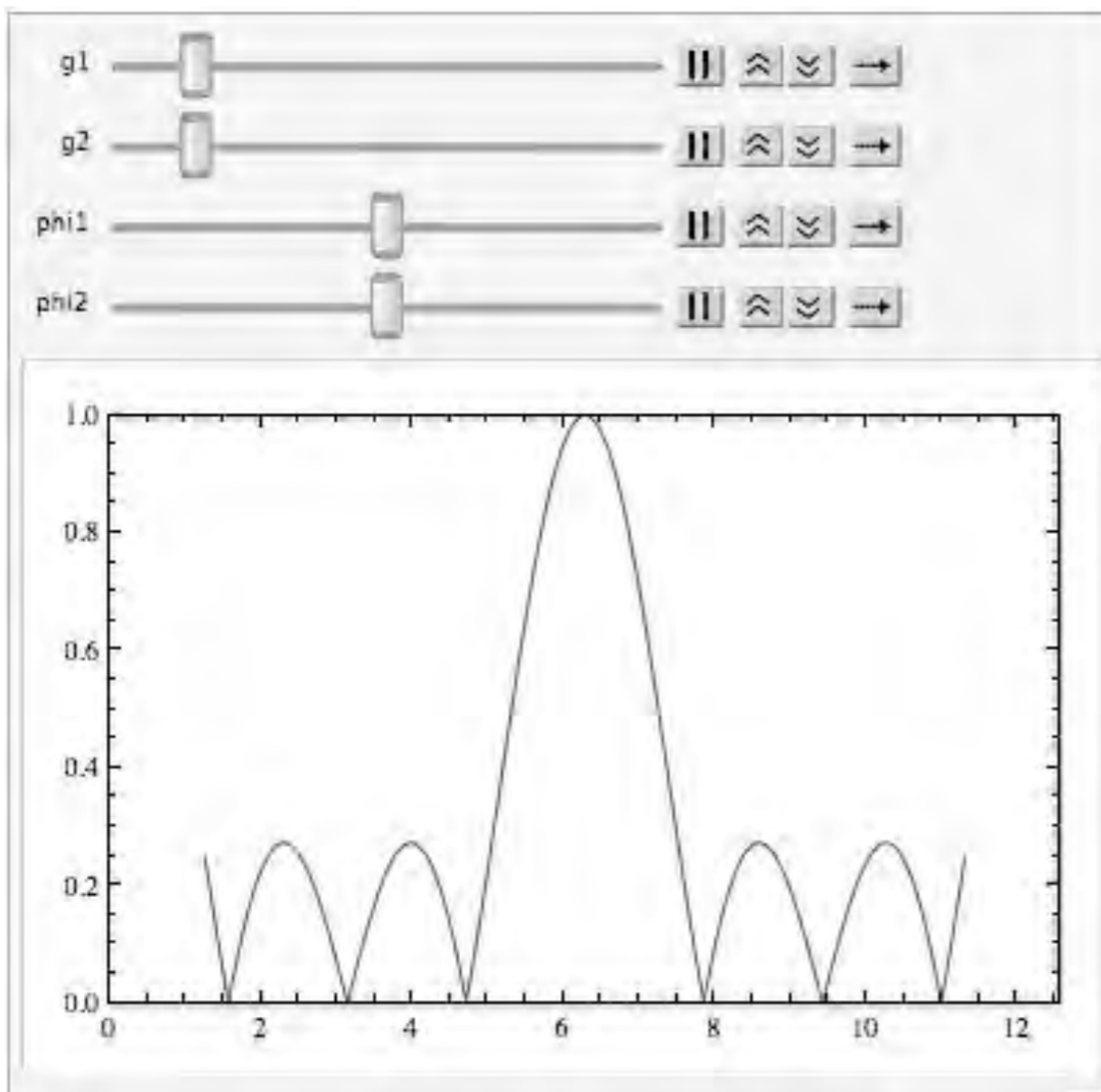


Wide maxima, wide minima, multiple maxima — take your pick

# Designing relaxation rates

$$A(\omega_j) = \sum_k g_k e^{-i\omega_j x_k / v}$$

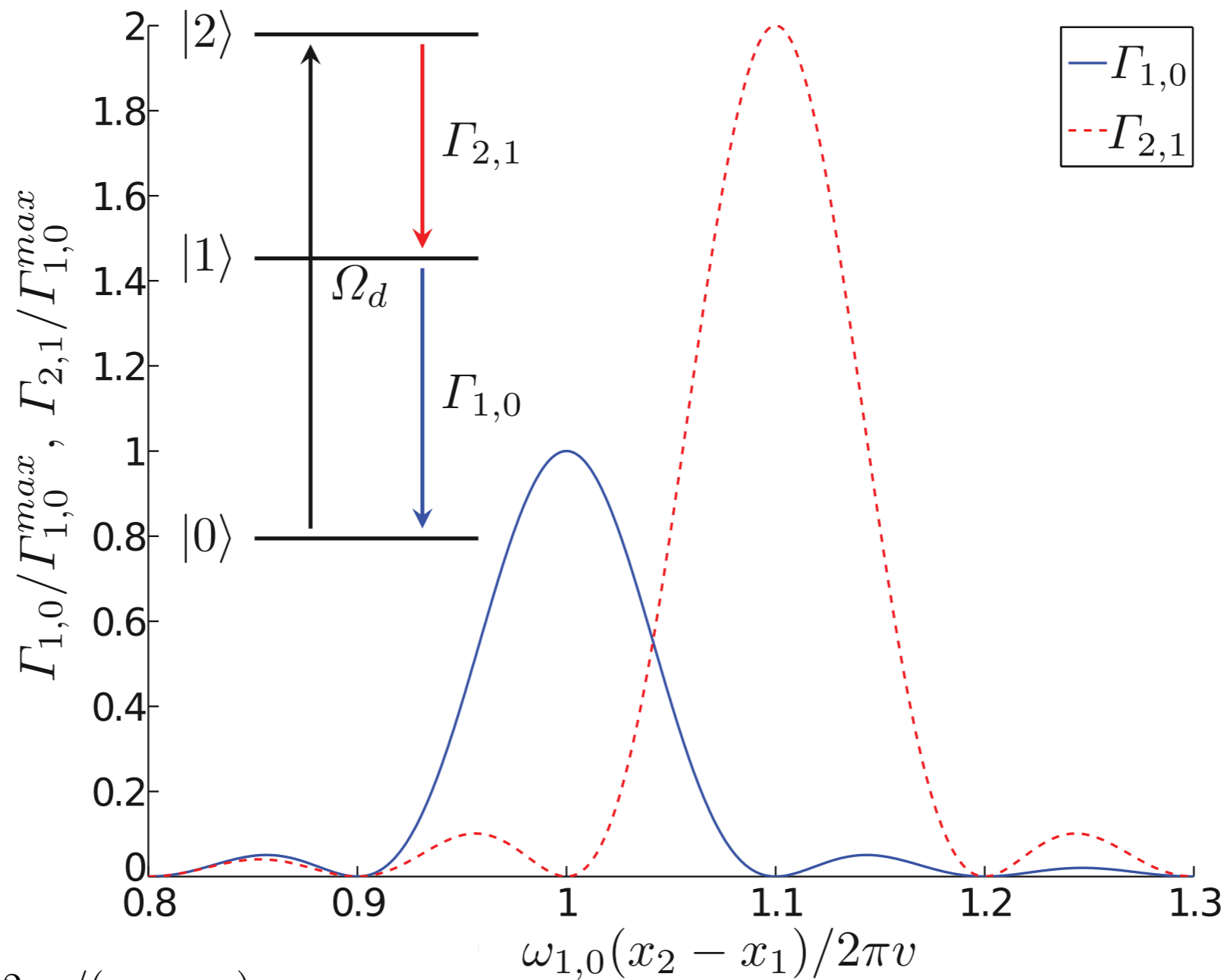
Discrete Fourier transform



$$N = 4$$

Instead of being protected  
by a cavity, the atom  
”creates its own cavity”

# Designing relaxation rates



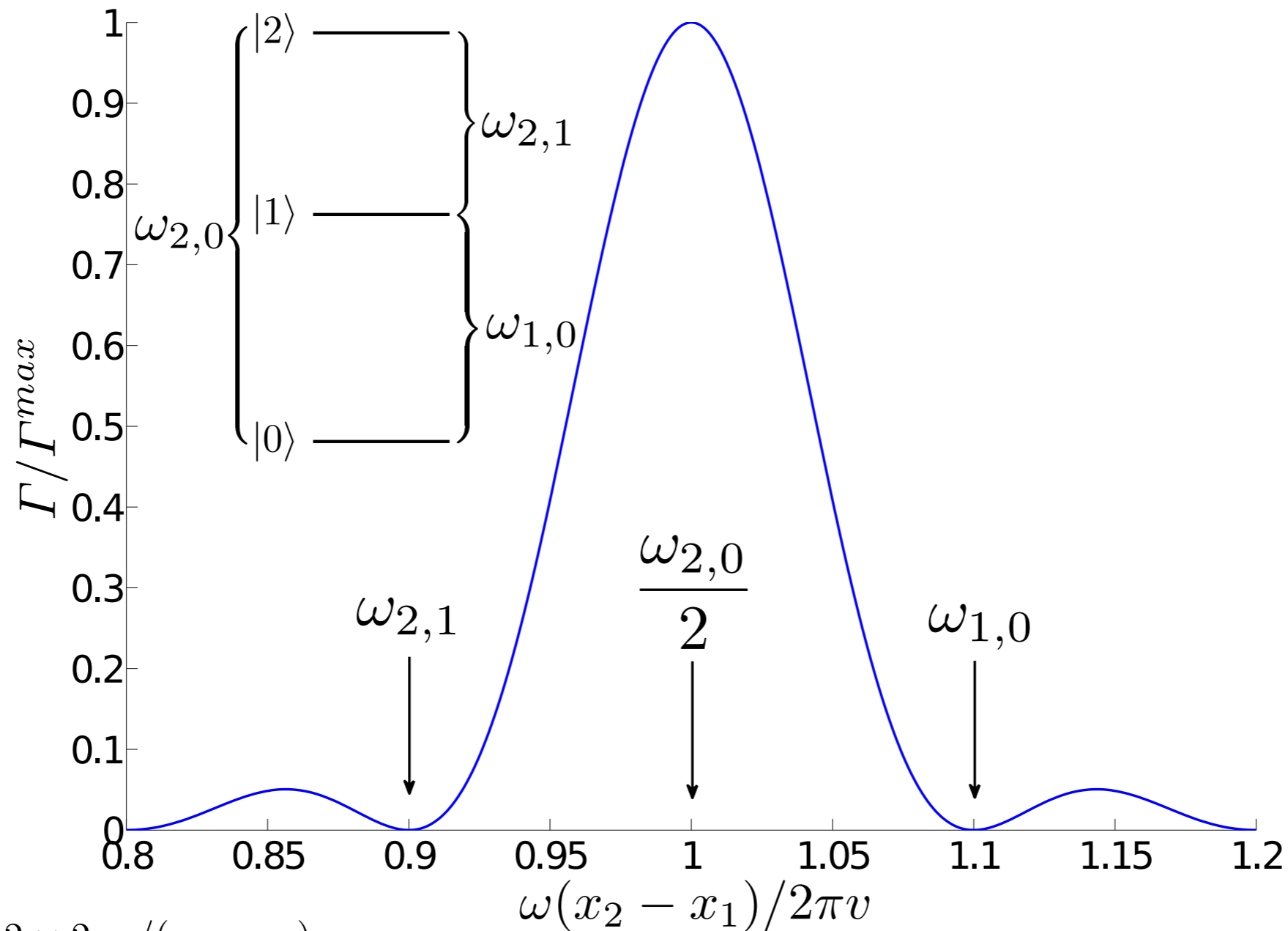
Anharmonicity

$$\omega_{1,0} - \omega_{2,1} = 0.1 \times 2\pi\nu / (x_2 - x_1)$$

$N = 10$

Can be used to create population inversion  $\rightarrow$  lasing

# Designing relaxation rates



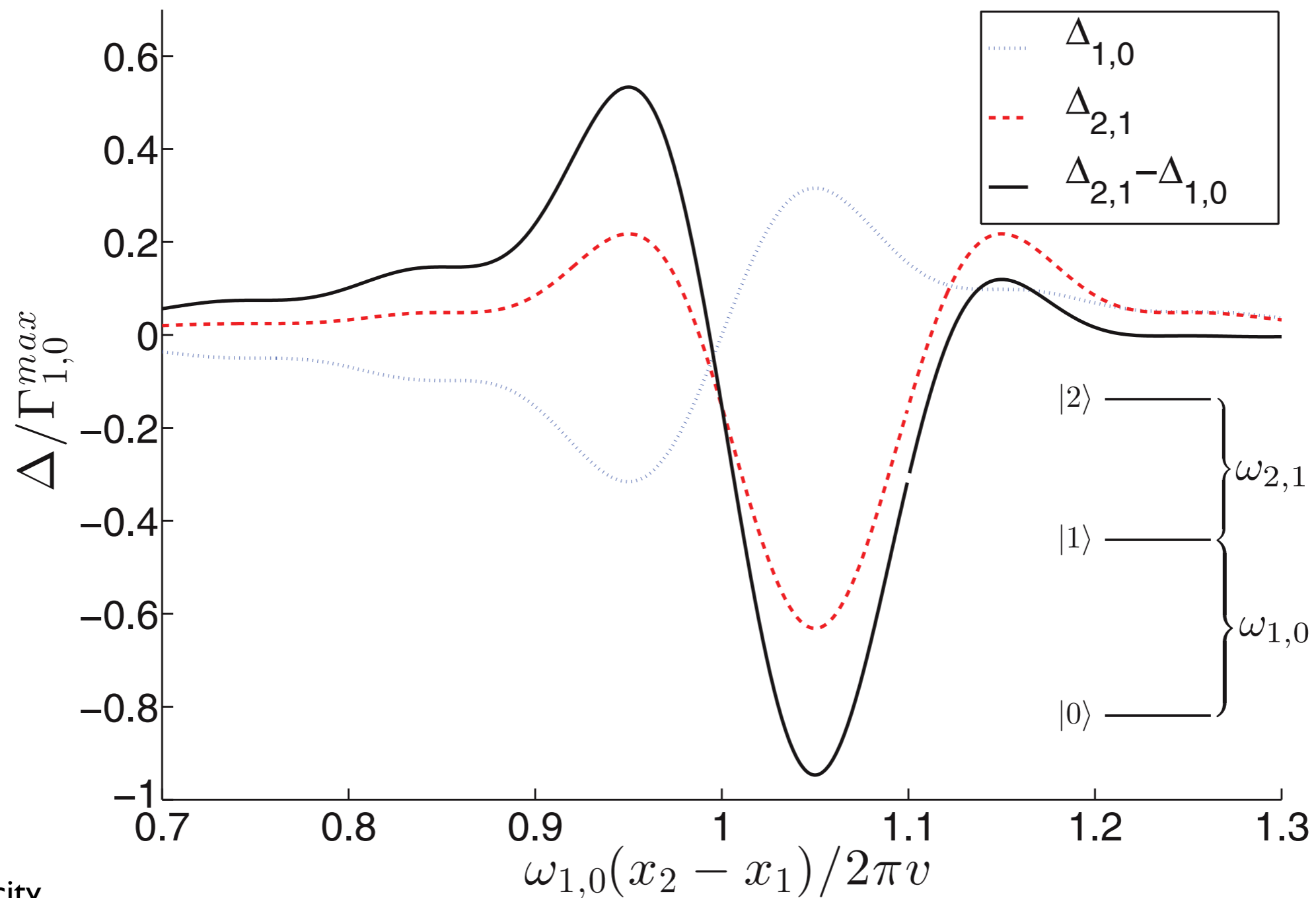
Anharmonicity

$$\omega_{1,0} - \omega_{2,1} = 0.2 \times 2\pi\nu/(x_2 - x_1)$$

$N = 10$

## Enhancing a two-phonon process

# Designing Lamb shift and anharmonicity

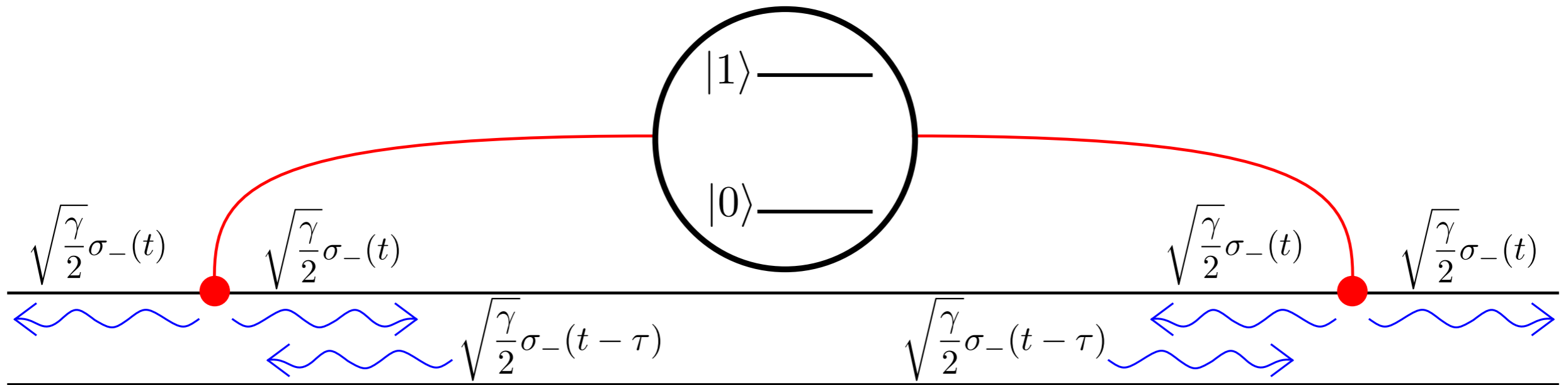


Anharmonicity

$$\omega_{1,0} - \omega_{2,1} = 0.1 \times 2\pi\nu / (x_2 - x_1)$$

$N = 10$

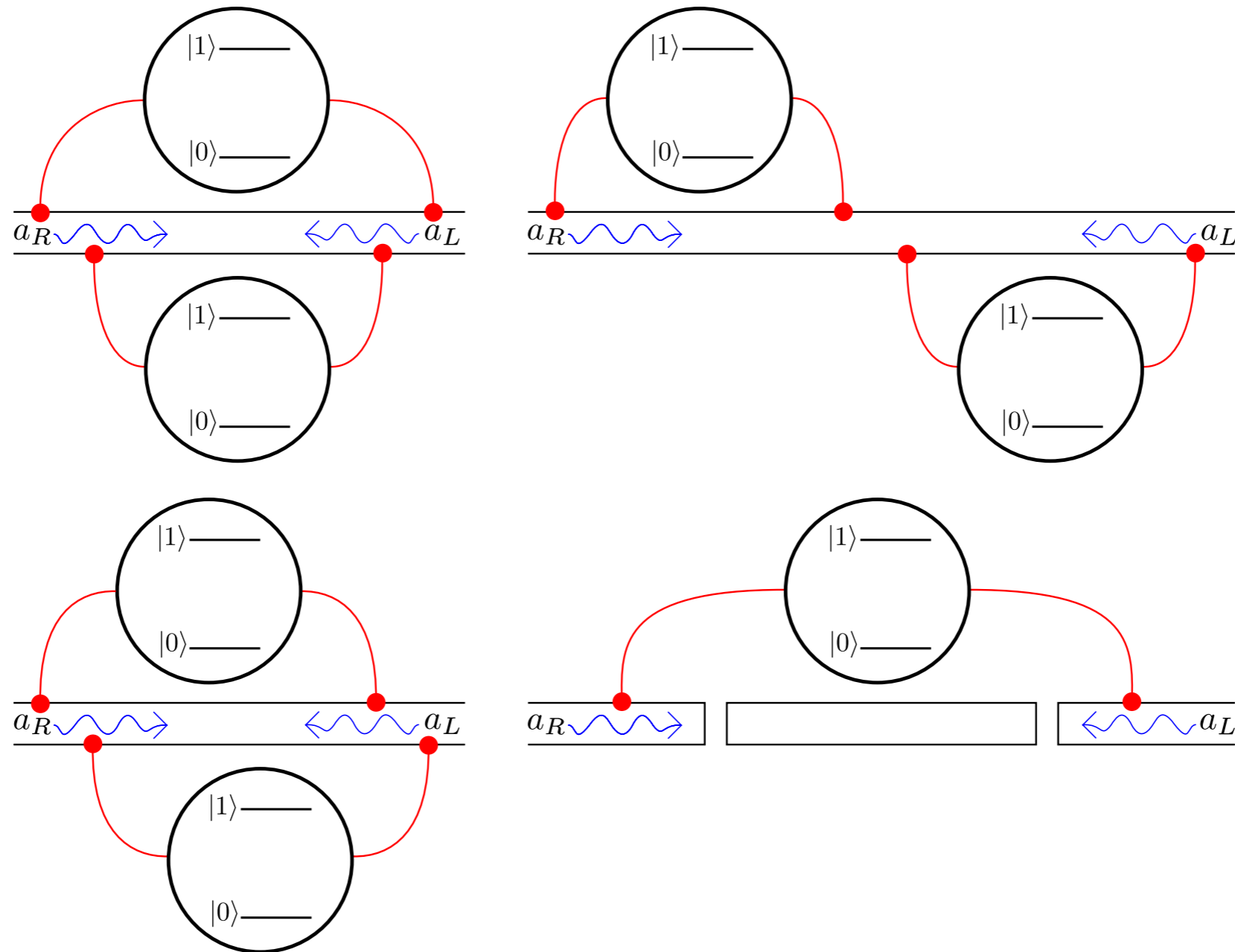
# Extensions: time delay



Nonexponential decay, interesting features in the second-order correlation function for scattered phonons, etc.

Posters by Lingzhen Guo and Gustav Andersson

# Extensions: two giant atoms

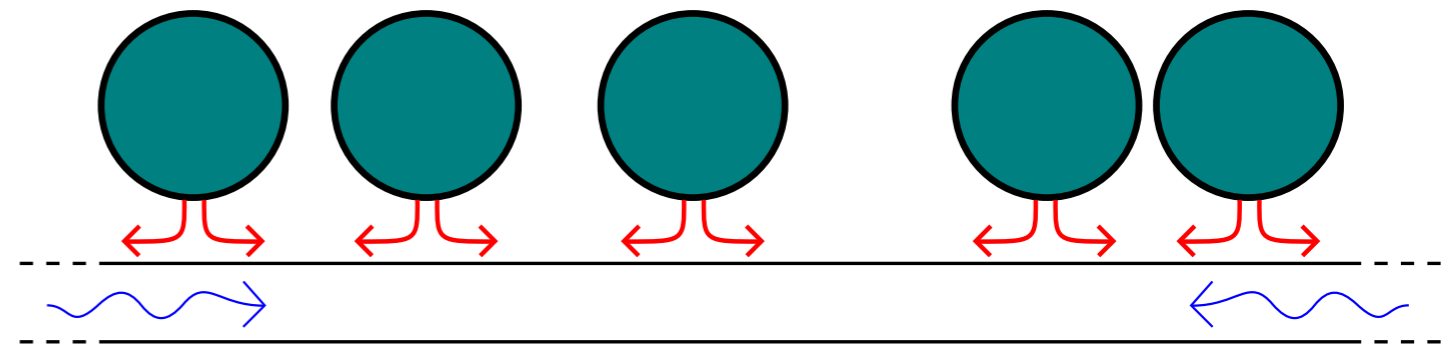
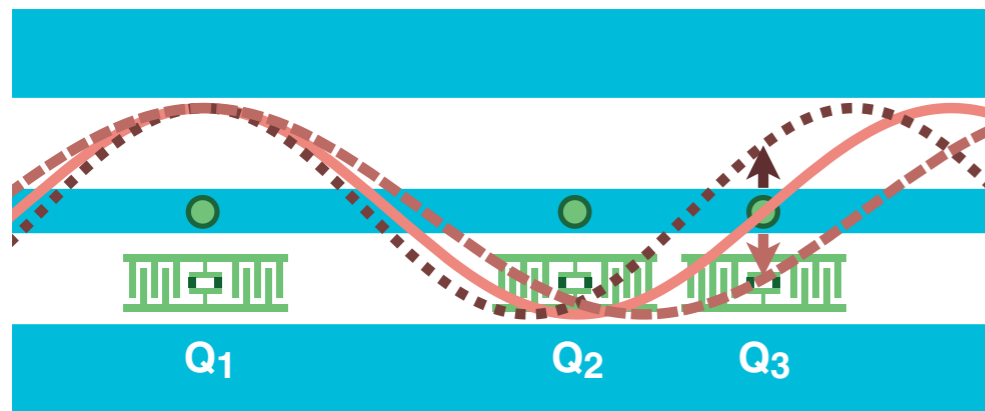


Various geometries possible  
With more atoms: "matryoshka atom"



# Multiple small atoms

Several small atoms  
spaced wavelengths apart



$$\dot{\rho} = -\frac{i}{\hbar} \left[ H_{\text{sys}} + \hbar\gamma \sum_{j,l} \sin(k|x_j - x_l|) \sigma_j^\dagger \sigma_l, \rho \right] + 2\gamma \sum_{j,l} \cos(k|x_j - x_l|) \left( \sigma_l \rho \sigma_j^\dagger - \frac{1}{2} \{ \sigma_j^\dagger \sigma_l, \rho \} \right)$$

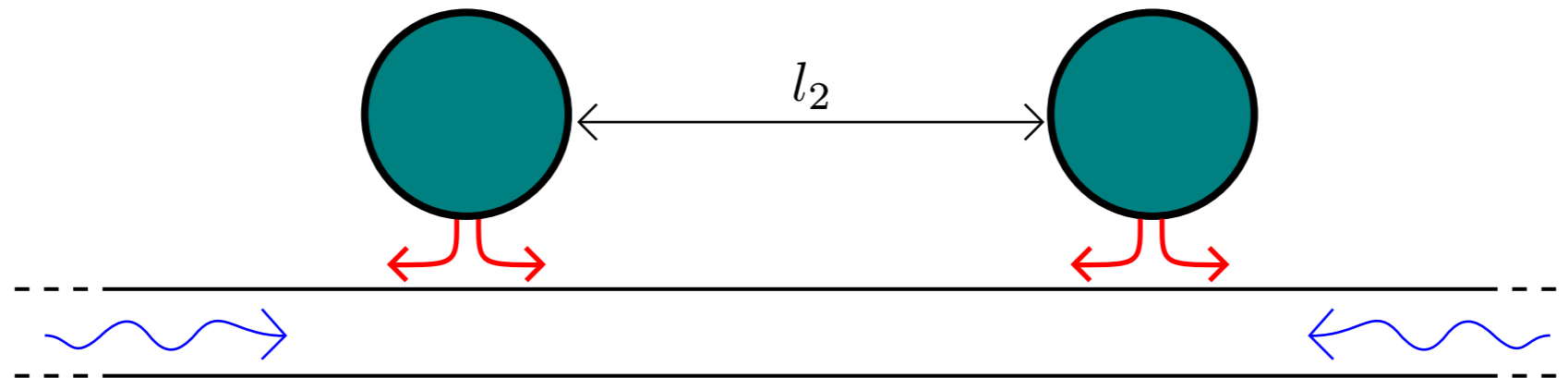
Lalumière *et al.*, PRA **88**, 043806 (2013)

van Loo *et al.*, Science **342**, 1494 (2013)

Lehmberg, PRA **2**, 883342 (1970)

Exchange interaction  $\sin(\text{phase})$   
Collective decay  $\cos(\text{phase})$

# Two small atoms



$$l_2 = \lambda$$

No exchange interaction  
Maximal collective decay

Dark state  $|D\rangle = \frac{|ge\rangle - |eg\rangle}{\sqrt{2}}$

Bright state  $|B\rangle = \frac{|ge\rangle + |eg\rangle}{\sqrt{2}}$

Sub- and  
superradiance

Lalumière et al., PRA 88, 043806 (2013)

$$l_2 = 3\lambda/4$$

Maximal exchange interaction  
No collective decay  
Individual decay remains

$$\dot{\rho} = -\frac{i}{\hbar}[H, \rho] + \gamma \sum_{i=B,D} \mathcal{D}[\sigma_-^i] \rho$$

$$H = \sum_{i=B,D} \hbar\omega_i \sigma_+^i \sigma_-^i$$

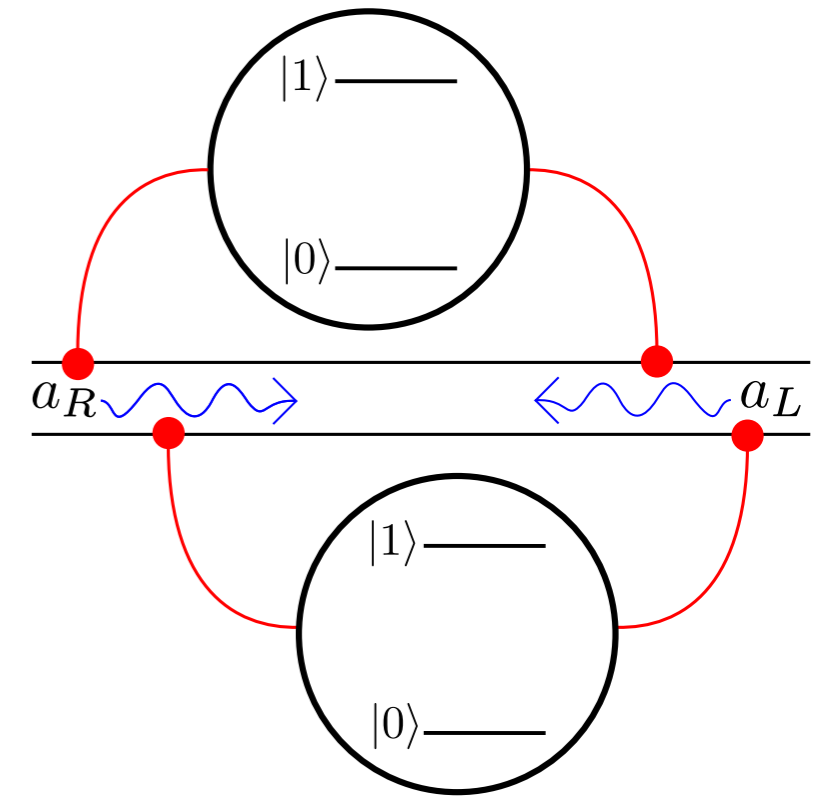
$$\omega_{B/D} = \Delta \pm J$$

$$\sigma_-^{B/D} = \frac{\sigma_-^1 \pm \sigma_-^0}{\sqrt{2}}$$

# Two giant atoms

A. F. Kockum *et al.*, in preparation (2016)

Master equation with equal phase shifts  
between subsequent coupling points



$$\begin{aligned} \dot{\rho} = & -i \left[ \frac{\Delta_a + \gamma \sin 2\varphi}{2} \sigma_z^a + \frac{\Delta_b + \gamma \sin 2\varphi}{2} \sigma_z^b + \frac{\gamma}{2} (3 \sin \varphi + \sin 3\varphi) (\sigma_+^a \sigma_-^b + \sigma_+^b \sigma_-^a), \rho \right] \\ & + 2\gamma (1 + \cos 2\varphi) (\mathcal{D} [\sigma_-^a] \rho + \mathcal{D} [\sigma_-^b] \rho) \\ & + \gamma (3 \cos \varphi + \cos 3\varphi) \left( \sigma_-^a \rho \sigma_+^b + \sigma_-^b \rho \sigma_+^a - \frac{1}{2} ((\sigma_+^a \sigma_-^b + \sigma_+^b \sigma_-^a) \rho + \rho (\sigma_+^a \sigma_-^b + \sigma_+^b \sigma_-^a)) \right) \end{aligned}$$

No collective decay

No individual decay

Nonzero exchange interaction

Different from the single dark state for small atoms!

$$\varphi = \frac{\pi}{2}$$

## Summary

A transmon qubit coupled to SAW is a "giant artificial atom"

Multiple coupling points  $\rightarrow$  interference  $\rightarrow$  frequency-dependent relaxation rate and Lamb shift

Can design the frequency-dependence for various applications

Two giant artificial atoms can completely decouple from the transmission line (no decay) but still have an exchange interaction mediated by the transmission line

A. F. Kockum *et al.*, Phys. Rev. A **90**, 013837 (2014)

A. F. Kockum *et al.*, in preparation (2016)

