

Bayerische  
Akademie der Wissenschaften



Technische Universität München

# All Acoustic Manipulation and Probing of Spin Ensembles

Hans Huebl, Sebastian T.B. Goennenwein,  
Rudolf Gross, Mathias Weiler



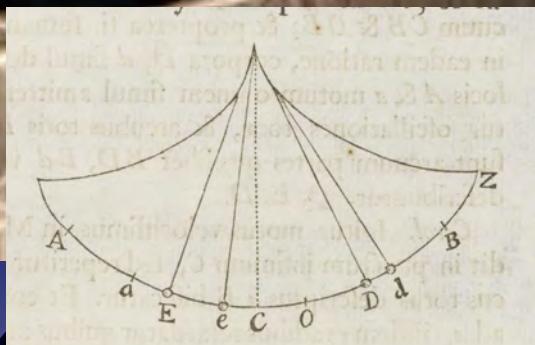
Walther-Meißner-Institut  
Bayerische Akademie der Wissenschaften



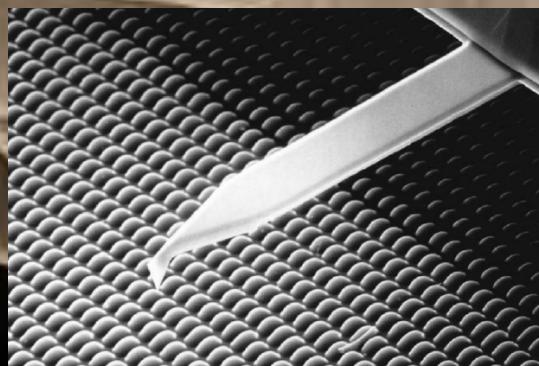
# Mechanical Oscillators



Gina Waga (2014) –  
National Geographic



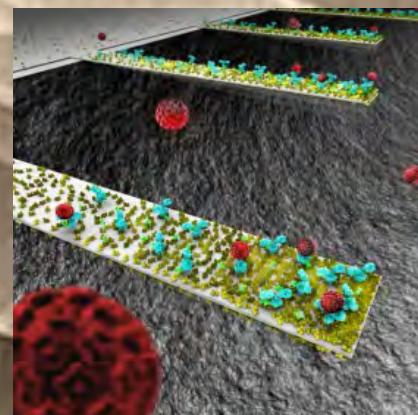
Newton, Philosophiae  
Naturalis Principia  
Mathematica (1687)



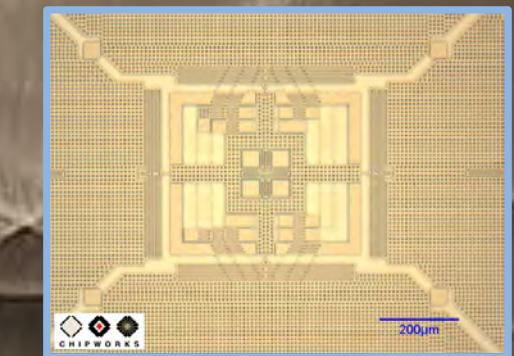
AFM, Giessibl, Rev. Mod. Phys. 79, 949 (2003)



[beginnersguitarstudio.com](http://beginnersguitarstudio.com)

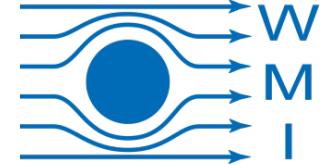


Perdue – Bashir group (2006)



iPhone4 gyroscope - iFixit

# *Mechanics with magnetic systems*



## Magnetism



typical classical representation:  
magnetization vector

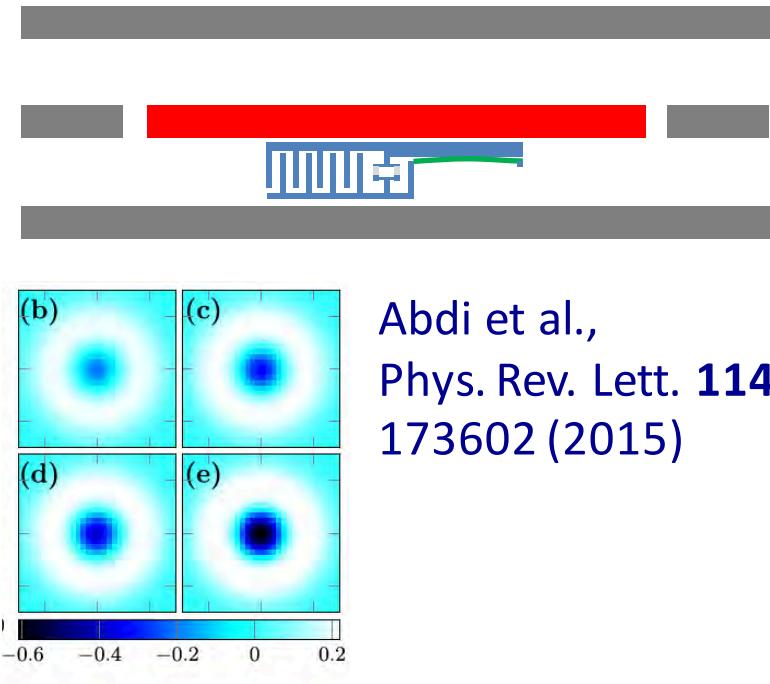
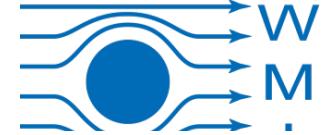
## Mechanics



motional amplitude

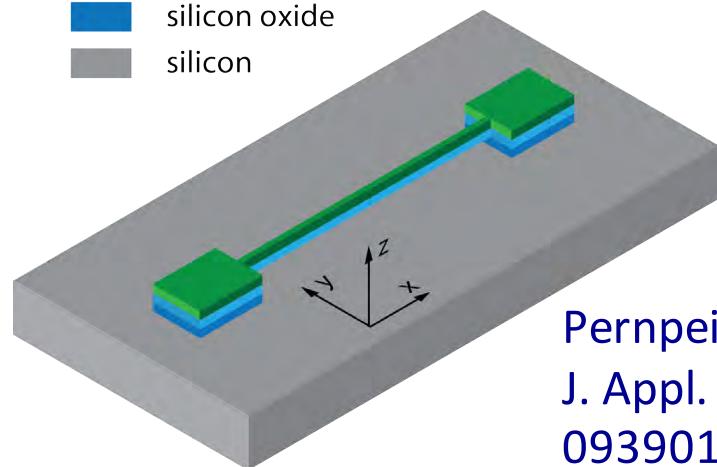
- quantum effects in large objects

# Acoustics @ Walther-Meißner-Institute

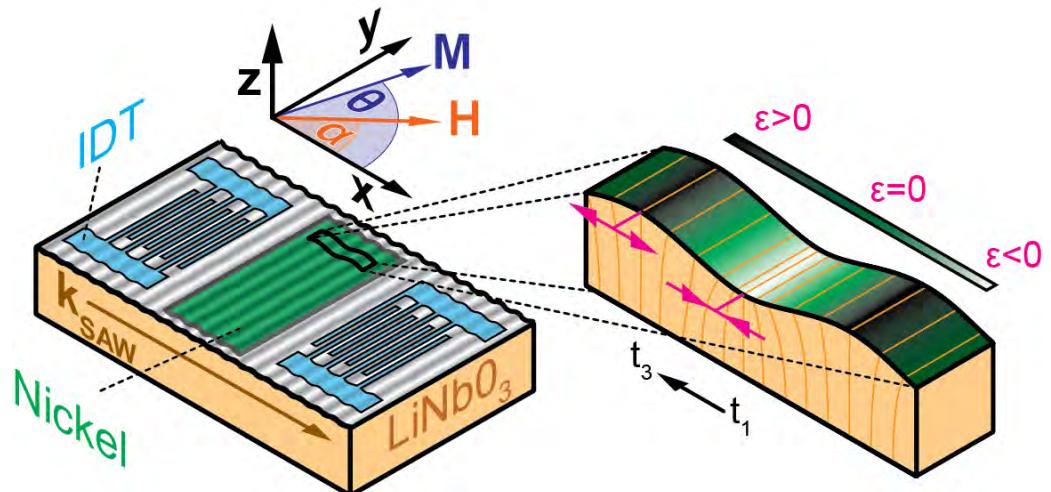


Abdi et al.,  
Phys. Rev. Lett. **114**,  
173602 (2015)

- cobalt
- silicon nitride
- silicon oxide
- silicon

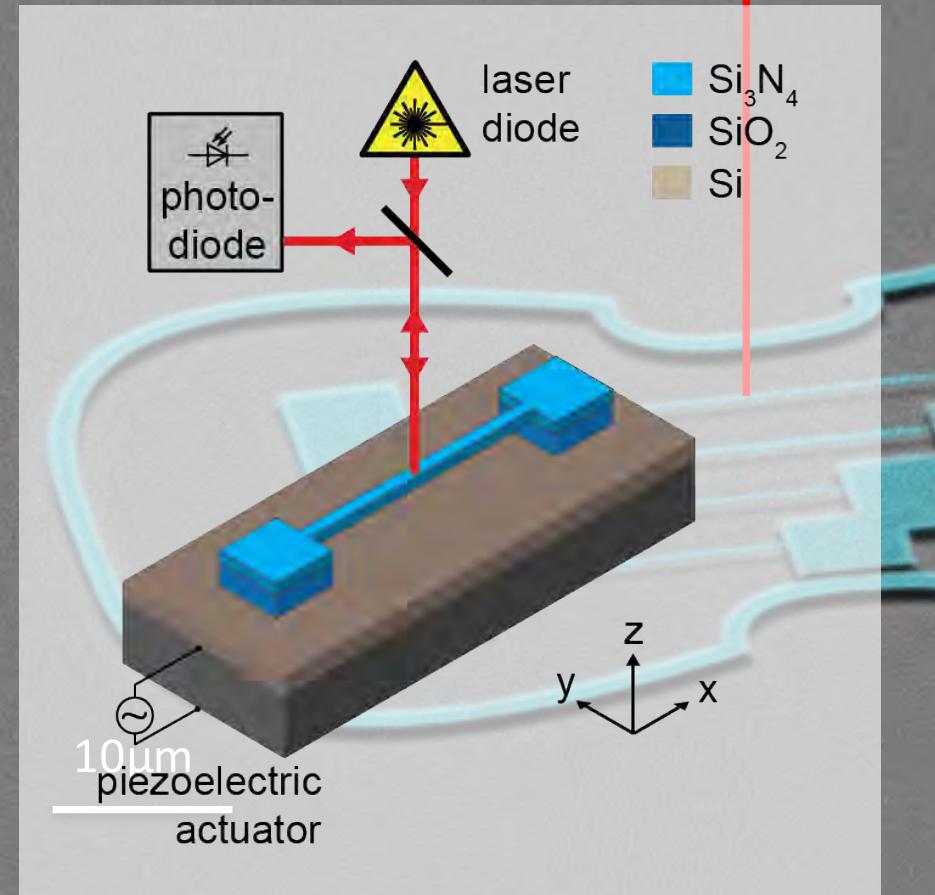


Pernpeintner et al.,  
J. Appl. Phys. **119**,  
093901 (2016)



Weiler et al.,  
Phys. Rev. Lett. **106**, 117601 (2011)  
Dreher et al.,  
Phys. Rev. B **86**, 134415 (2012)  
Weiler et al.,  
Phys. Rev. Lett. **108**, 176601 (2012)

# Strings



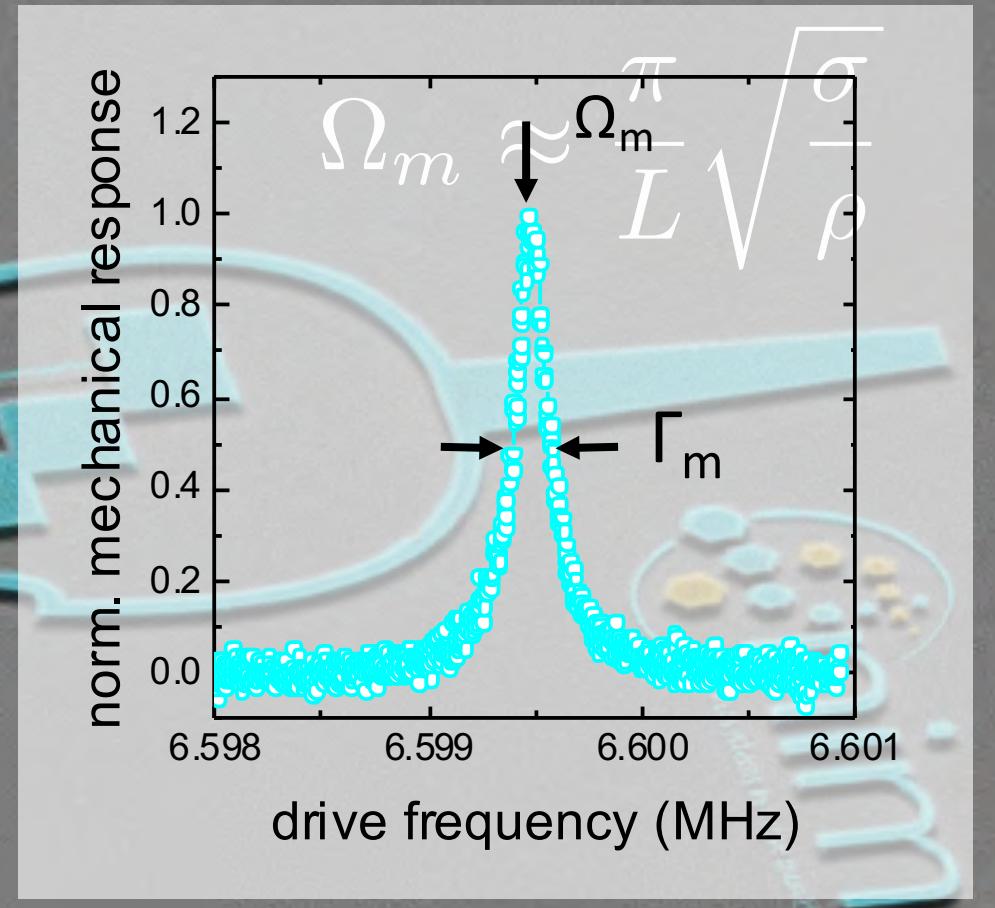
nano-string

$\sigma \equiv$  tensile stress ( $\approx 800 \text{ MPa}$ )

$\rho \equiv$  material density ( $\approx 2700 \text{ kg/m}^3$ )

$L \equiv$  length of the nanostring ( $\approx 30 \mu\text{m}$ )

- mechanical resonance frequency



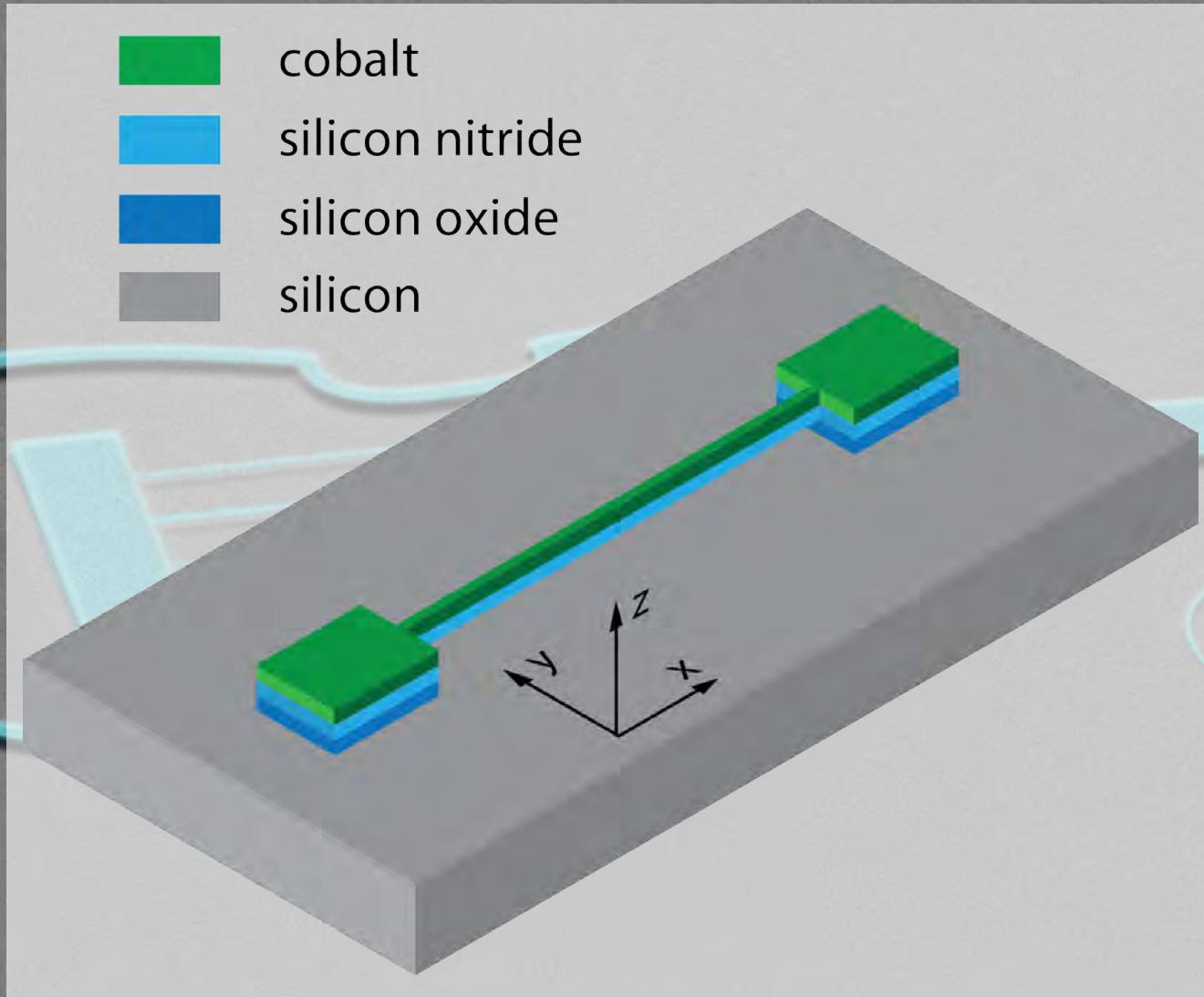
violine

$\sigma \equiv$  tensile stress ( $\approx 1200 \text{ MPa}$ )

$\rho \equiv$  material density ( $\approx 7800 \text{ kg/m}^3$ )

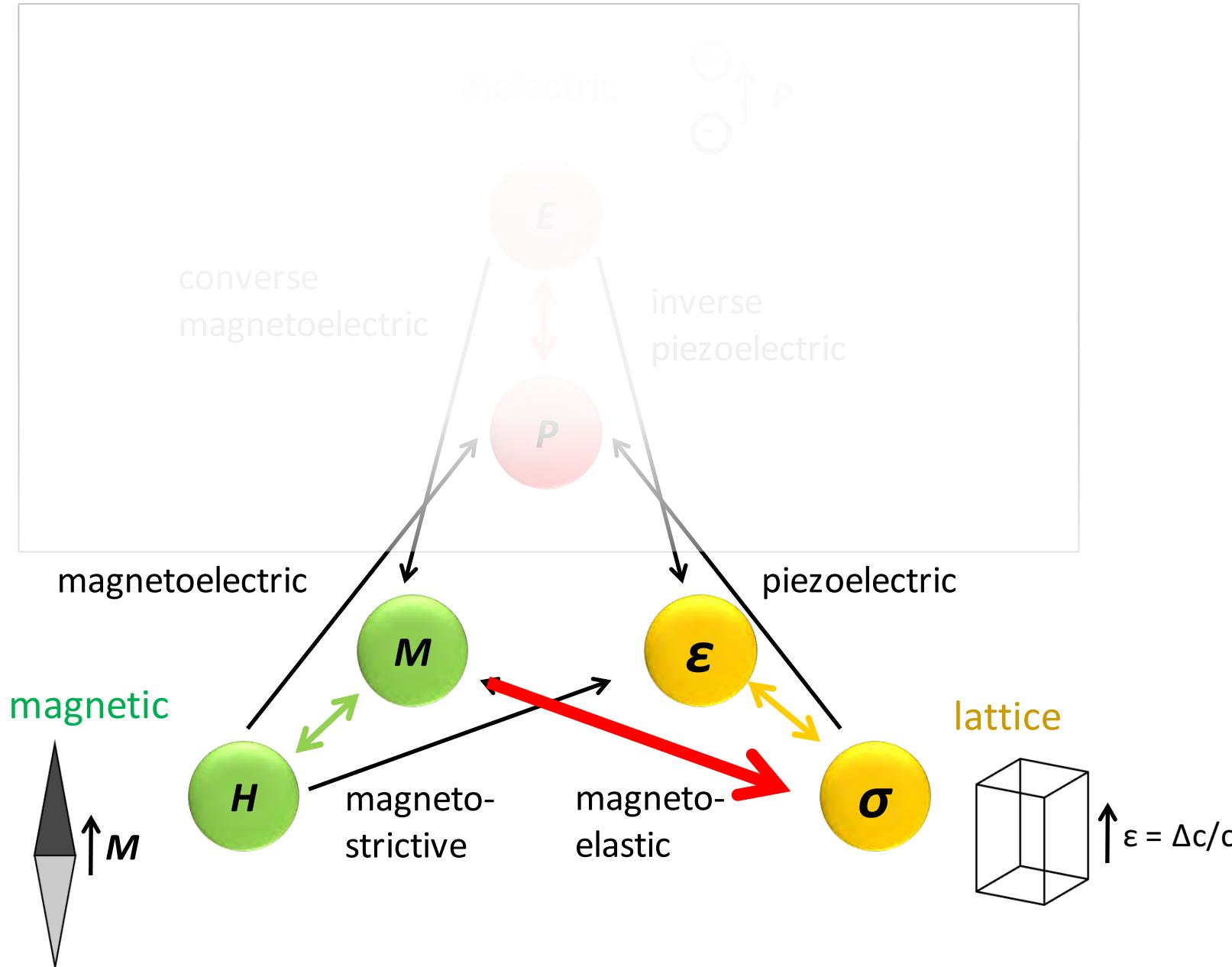
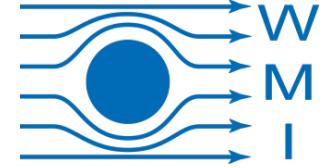
$L \equiv$  length of the string ( $\approx 300 \text{ mm}$ )

# Nano-spinmechanics - magnetostriction

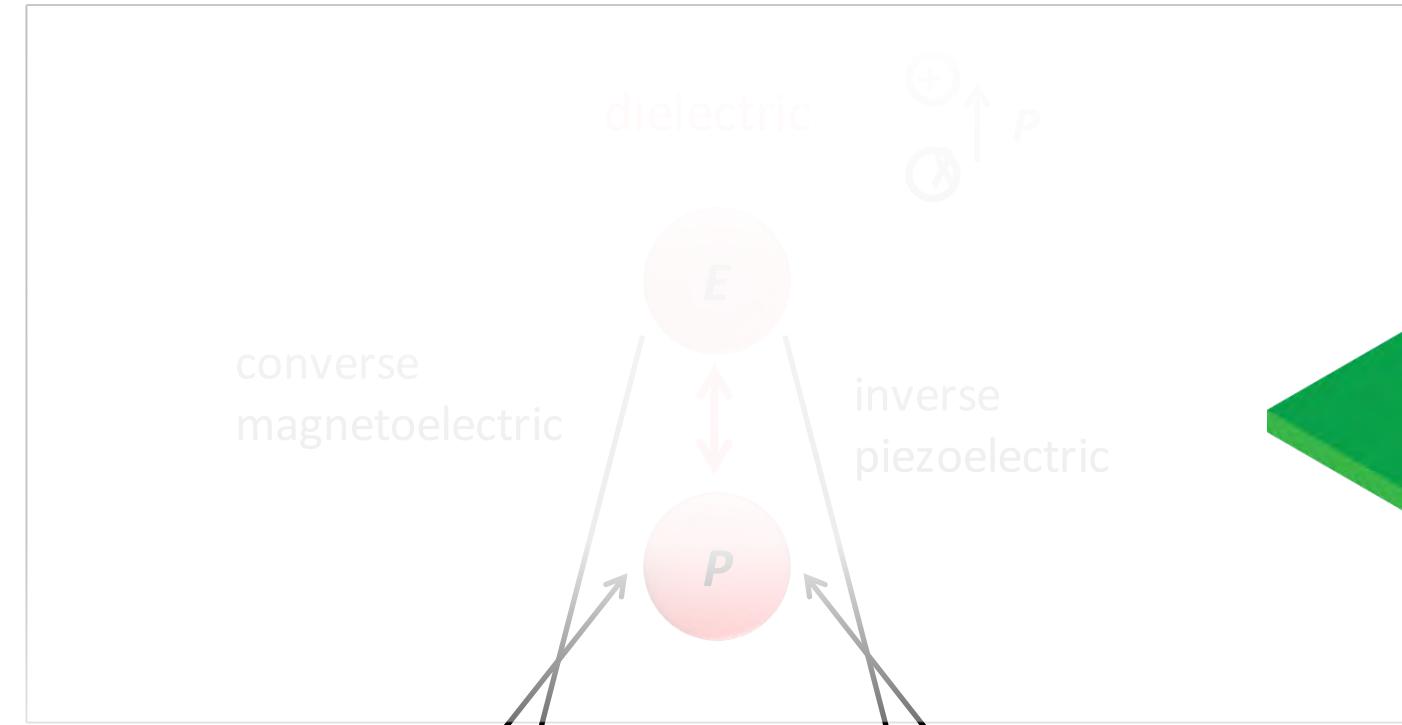
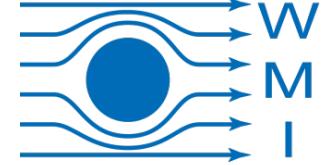


- Magnetostriction in thin magnetic films
- Magnet-phonon interaction

# Magnetic strain control

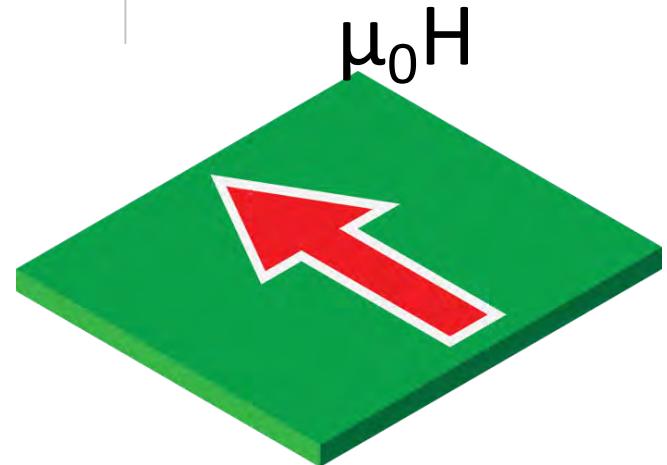
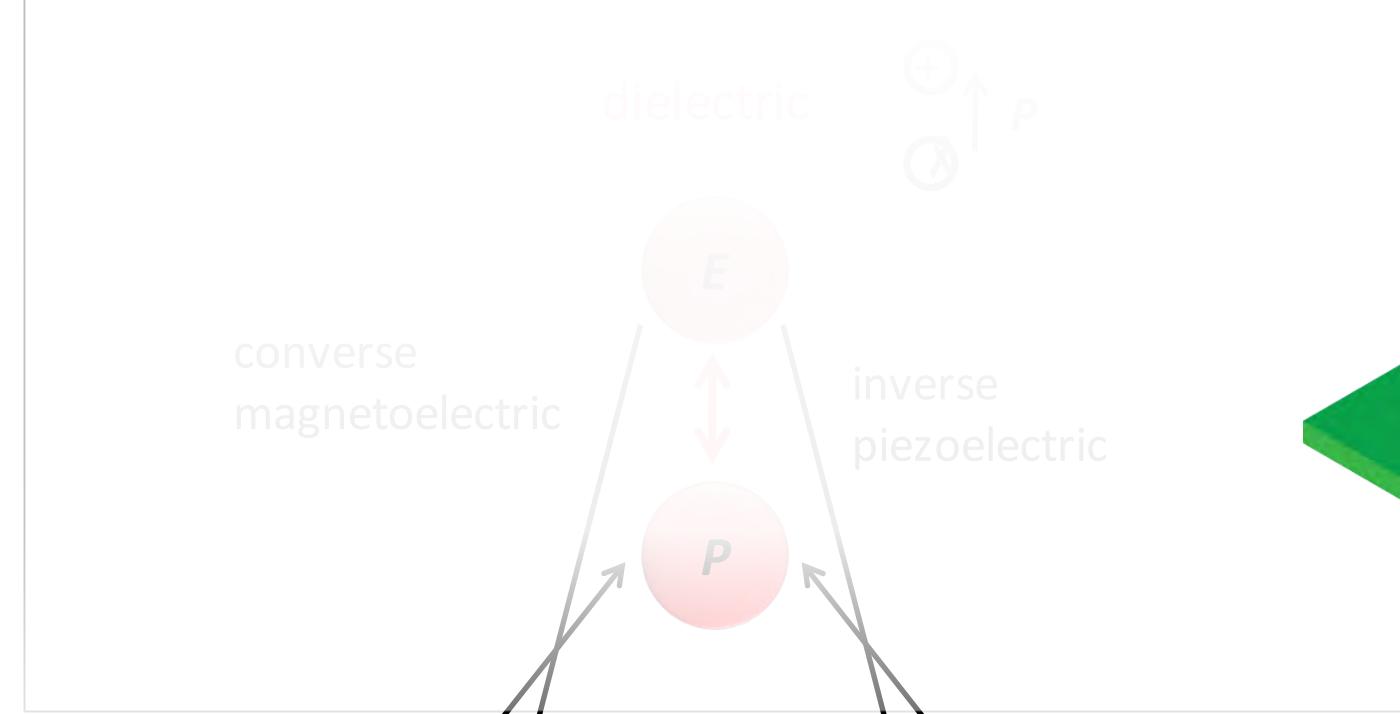
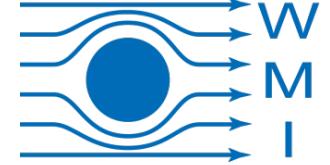


# Magnetic strain control

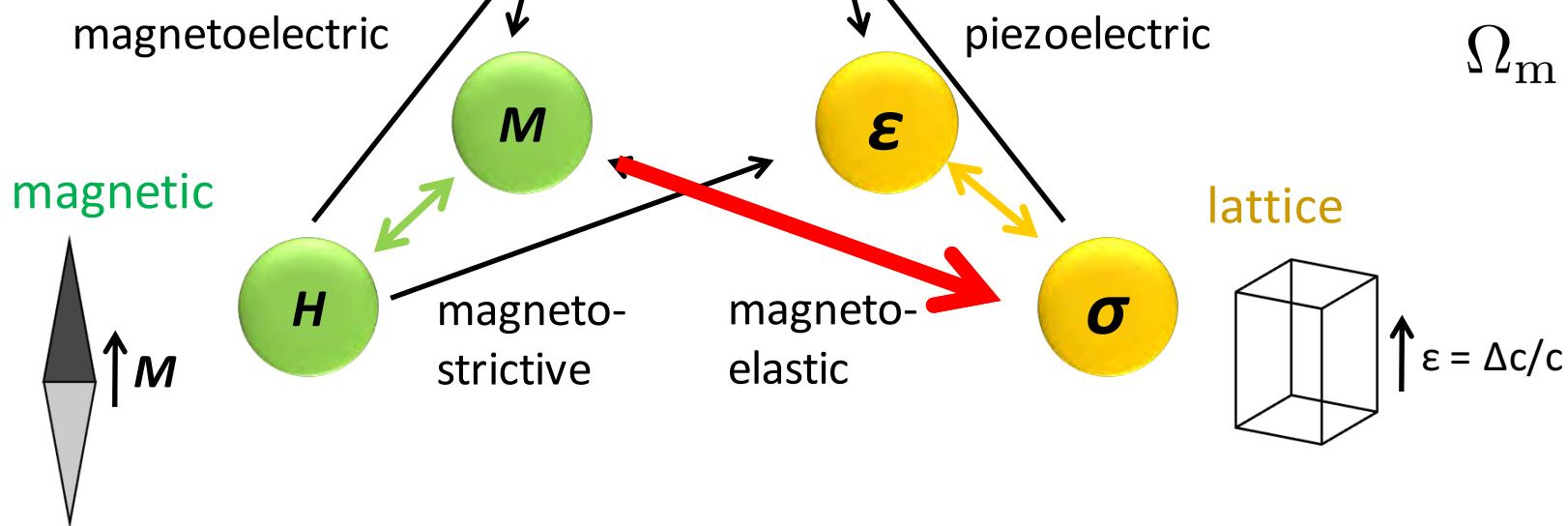
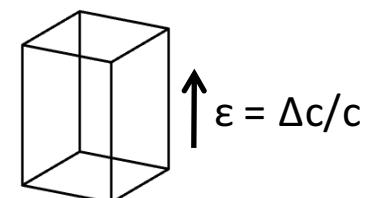


$$\Omega_m \approx \frac{\pi}{L} \sqrt{\frac{\sigma}{\rho}}$$
A diagram of a cubic lattice structure. An upward-pointing arrow labeled  $\varepsilon = \Delta c/c$  indicates the strain vector. To the left of the cube, there is a green circle labeled  $H$  with a grey arrow labeled  $M$  pointing upwards, representing a magnetic dipole.

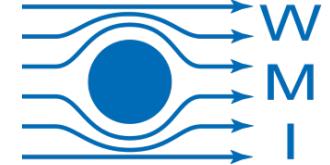
# Magnetic strain control



$$\Omega_m \approx \frac{\pi}{L} \sqrt{\frac{\sigma}{\rho}}$$

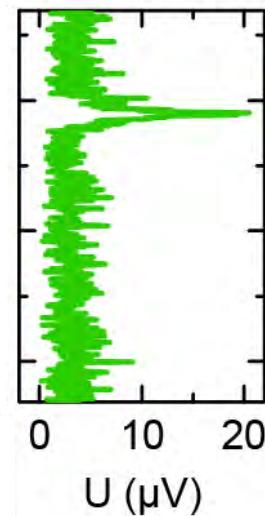


# Magnetostriction – nanomechanical detection



$\omega/2\pi$  (MHz)

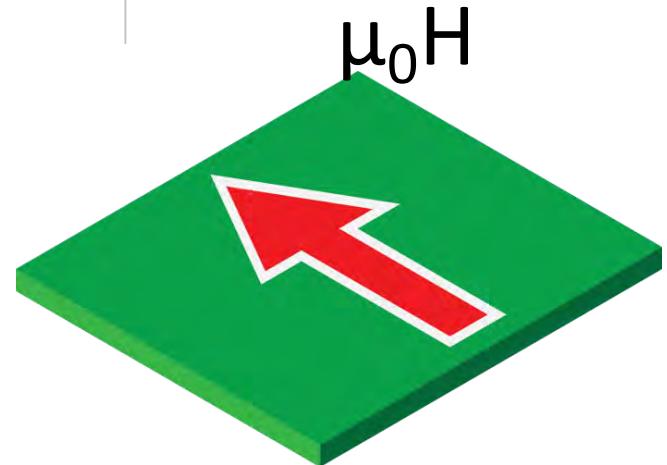
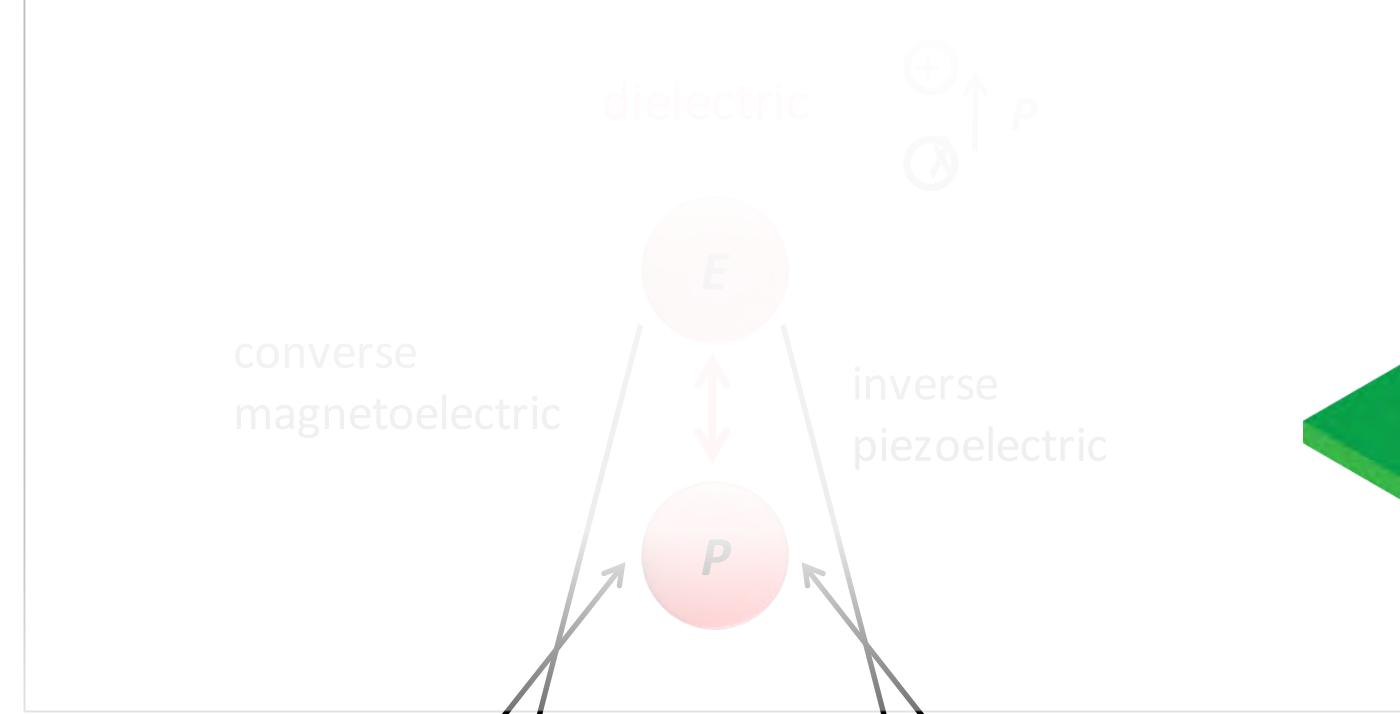
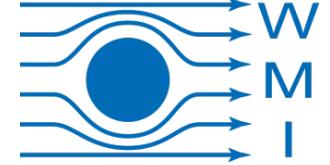
10.240  
10.235  
10.230



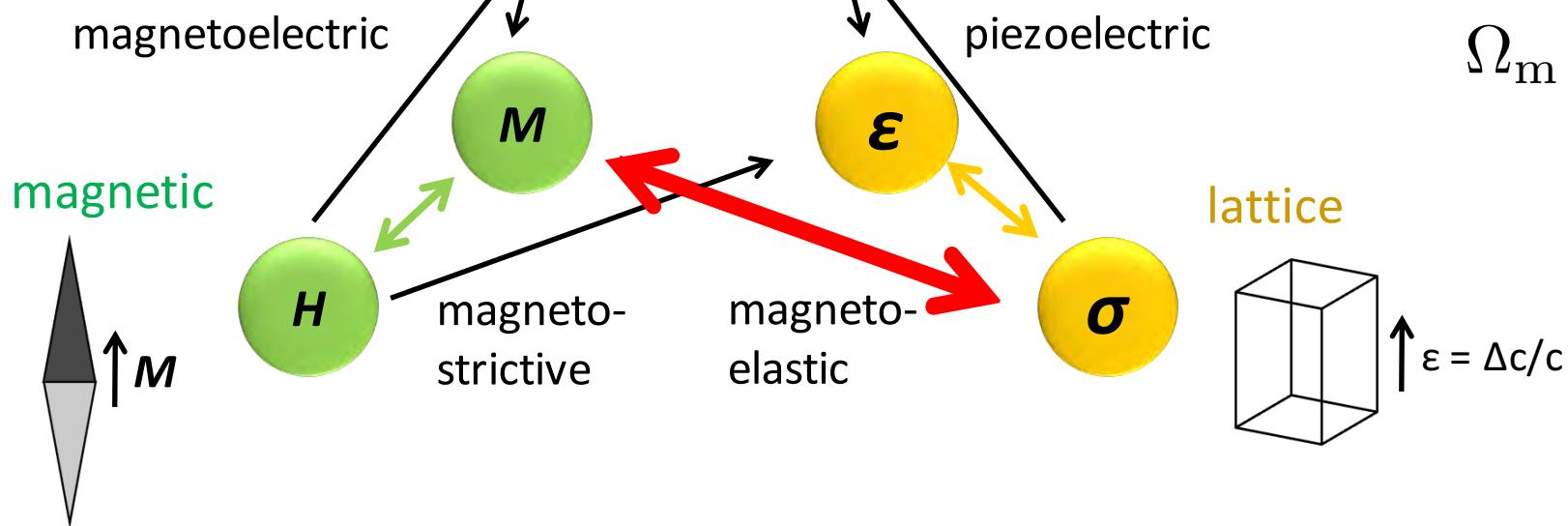
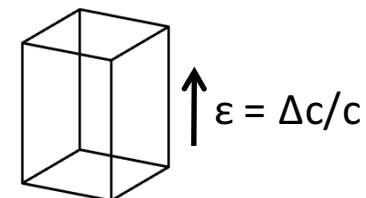
- 10 nm thin magnetic Co film

$$\frac{\omega_{\text{res}}(\phi)}{2\pi} = \frac{1}{2l} \sqrt{\frac{\sigma_{\text{eff}}}{\rho_{\text{eff}}}} = \frac{1}{2l} \sqrt{\frac{\sigma_0 - \sigma_1 \cos^2(\phi)}{\rho_{\text{eff}}}}$$
$$\sigma_1 = Et_{\text{film}}\lambda_{||}/(t_{\text{SiN}} + t_{\text{film}})$$

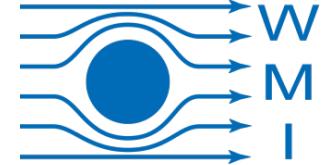
# Magnetic strain control



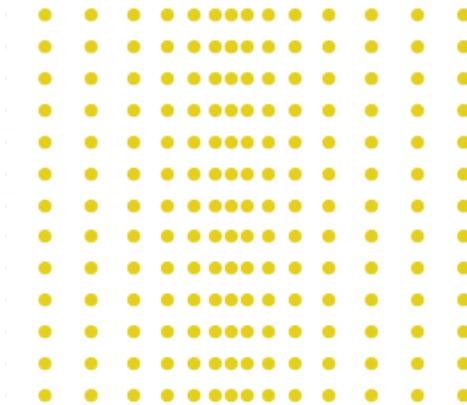
$$\Omega_m \approx \frac{\pi}{L} \sqrt{\frac{\sigma}{\rho}}$$



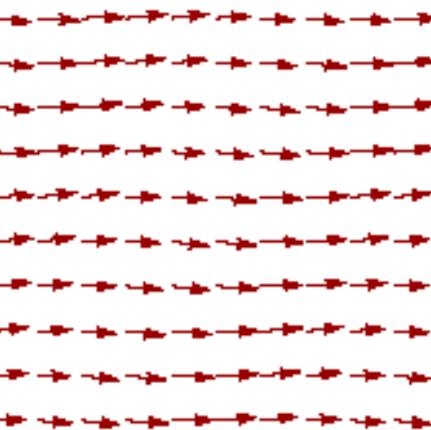
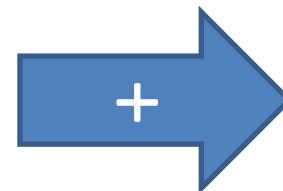
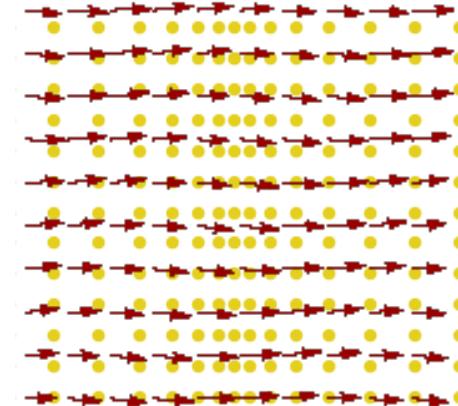
# Dynamic strain – magnetization coupling



phonons (sound wave)



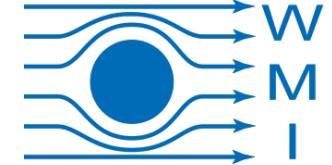
magnon-phonon-coupling  
(spin-sound-wave)



magnons (spin wave)

New physics  
(e.g. acoustic FMR)  
Natural mode matching  
 $v_{\text{sound}} \approx v_{\text{magnon}}$

# Ferromagnetic resonance



In equilibrium:  $M \parallel H_{\text{eff}}$



$H_{\text{eff}} \approx \text{external magnetic field}$

Dynamics: Landau-Lifshitz-Gilbert equation

$$\partial_t \mathbf{m} = -\gamma \mathbf{m} \times \mu_0 \mathbf{H}_{\text{eff}}$$

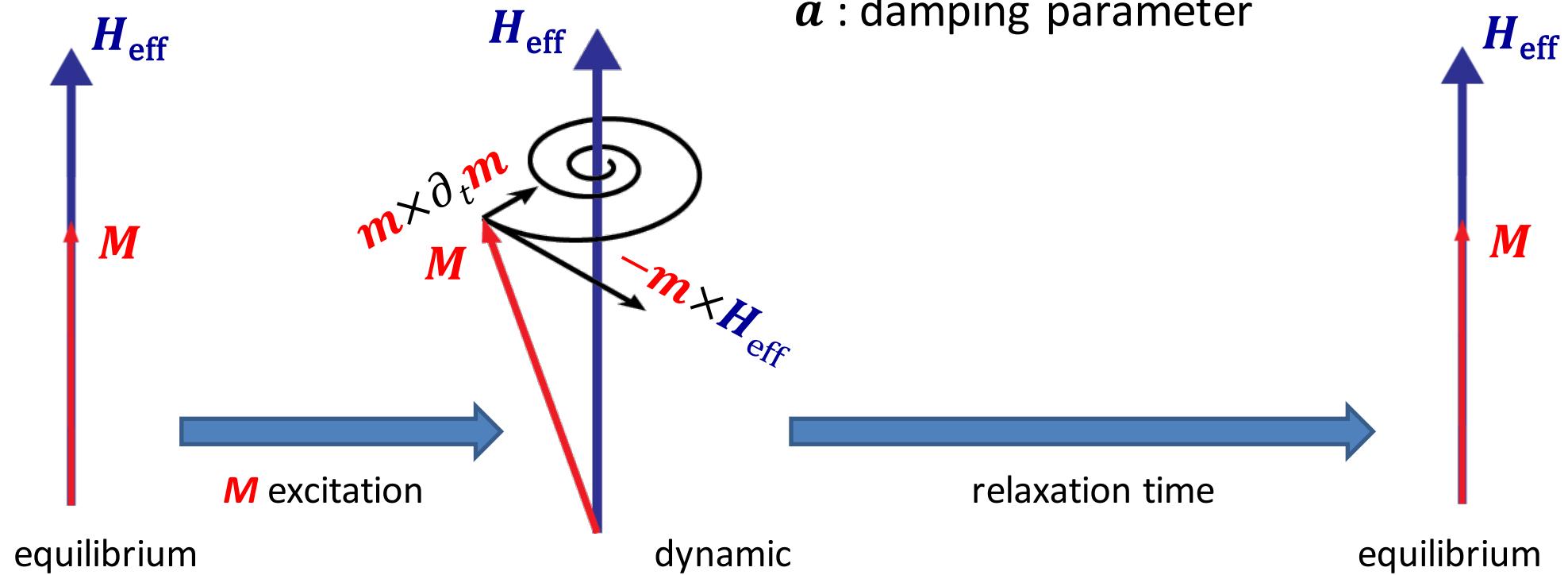
$$+ a \mathbf{m} \times \partial_t \mathbf{m}$$

precession

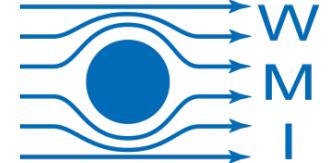
damping

$\gamma$ : gyromagnetic ratio

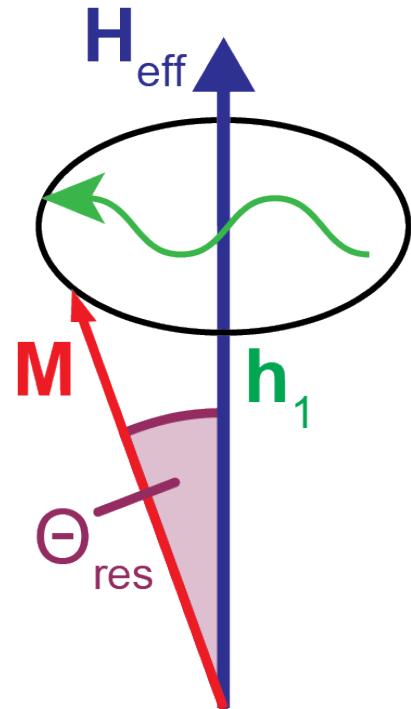
$a$  : damping parameter



# Ferromagnetic resonance – excitation schemes



(microwave) photon-driven  
ferromagnetic resonance



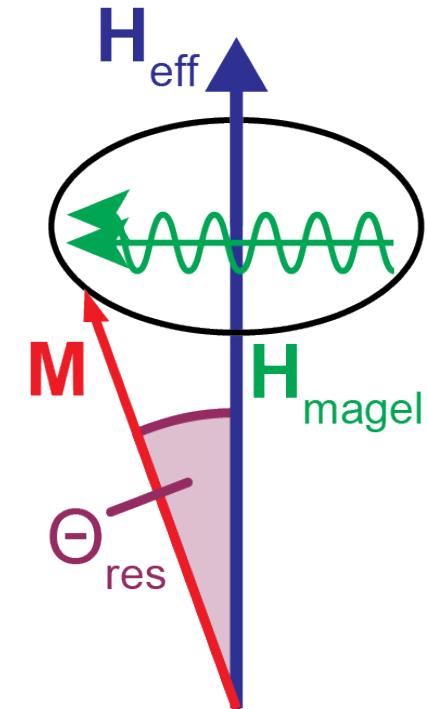
$$h_1(t) = h_1 \cos(\omega_{\text{res}} t)$$

real, external magnetic driving field

$$\omega_{\text{res}} = \gamma \mu_0 H_{\text{eff}}$$



phonon-driven  
ferromagnetic resonance

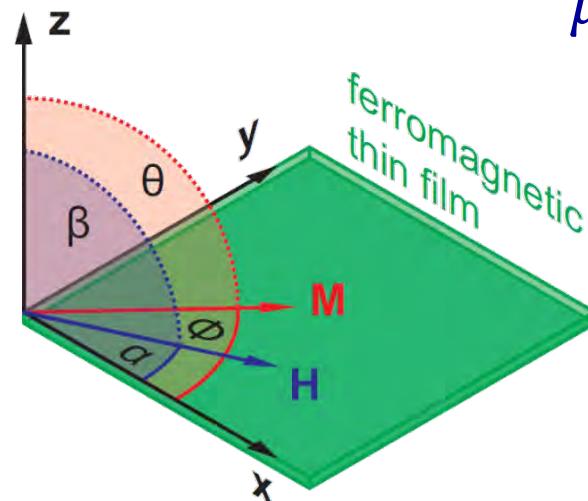
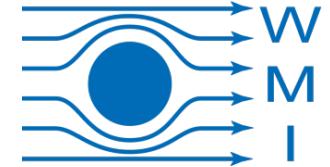


$$H_{\text{magel}}(t) = H_{\text{magel}} \cos(\omega_{\text{res}} t)$$

virtual, internal magnetic driving field

this talk

# Ferromagnetic resonance – free energy



$$\mu_0 \mathbf{H}_{\text{eff}} = -\nabla_{\mathbf{m}} F^{DC}$$

effective magnetic field

$$F^{DC} = -\mu_0 \mathbf{H} \cdot \mathbf{m} + B_u (\mathbf{u} \cdot \mathbf{m})^2 + B_d m_z^2$$

Zeeman term

in-plane anisotropy

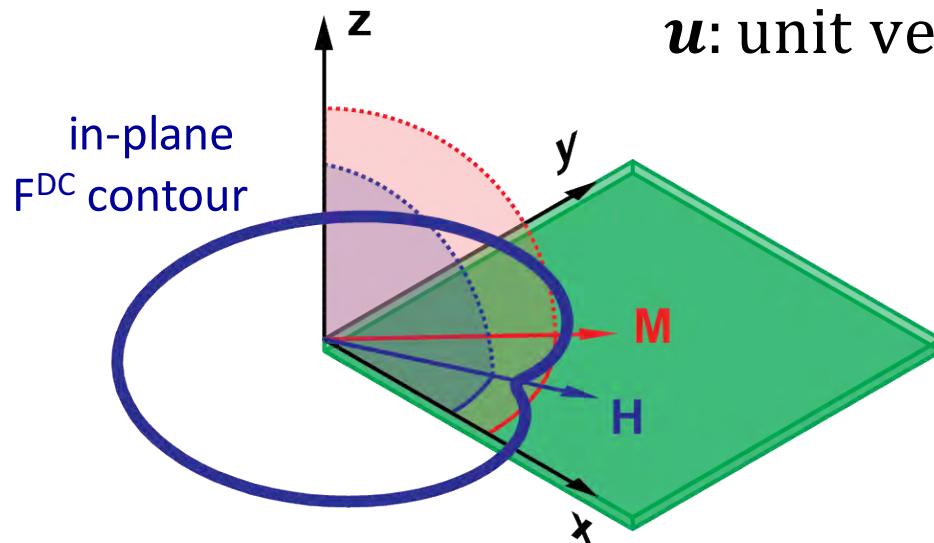
$$2B_u \approx 10 \text{ mT}$$

shape anisotropy

$$2B_d \approx 1 \text{ T}$$

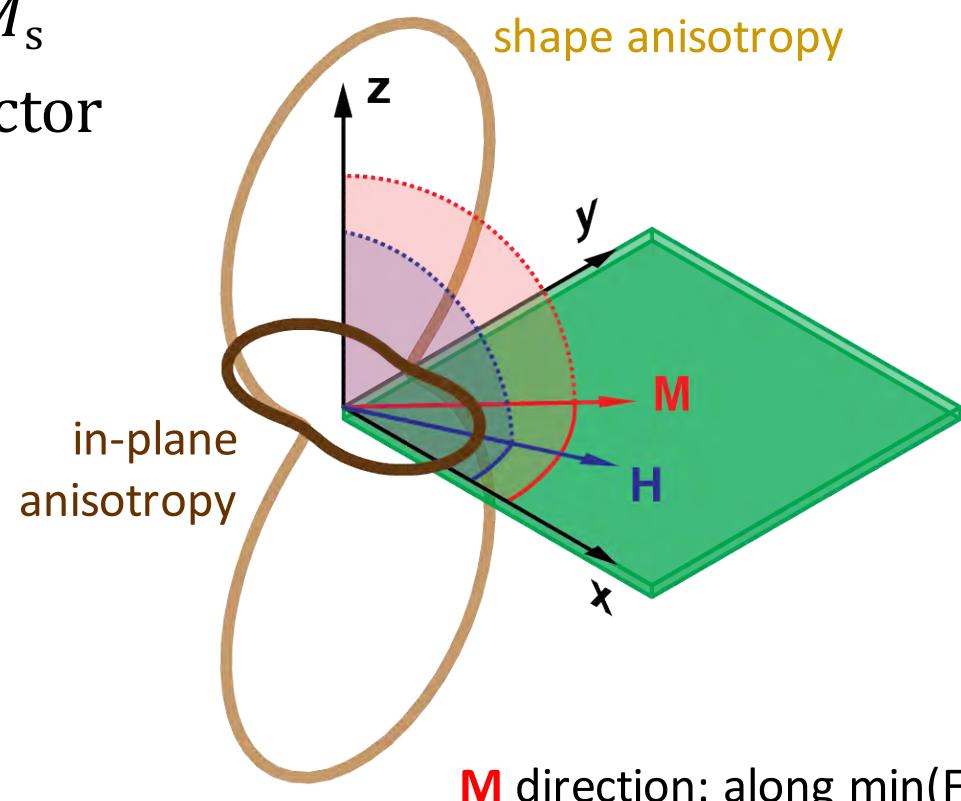
$$\mathbf{m} = \mathbf{M}/M_s$$

$\mathbf{u}$ : unit vector



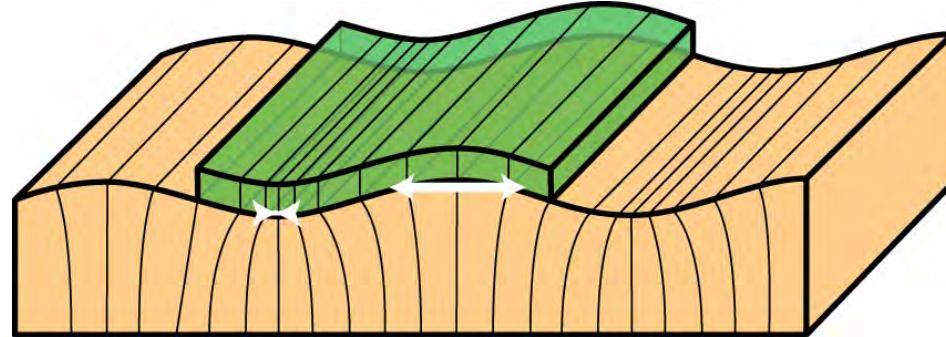
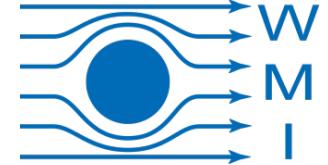
$\mathbf{M}$ : magnetization

$\mathbf{H}$ : external magnetic field

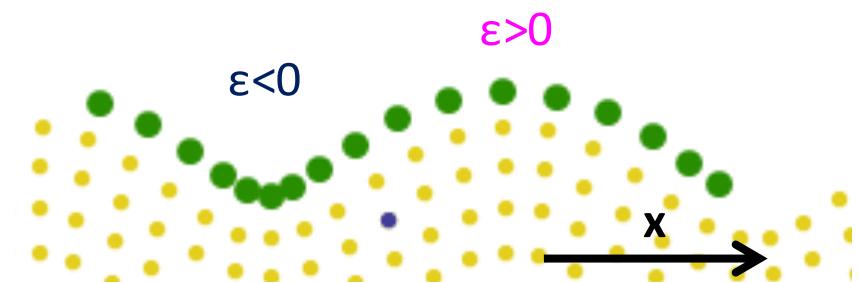
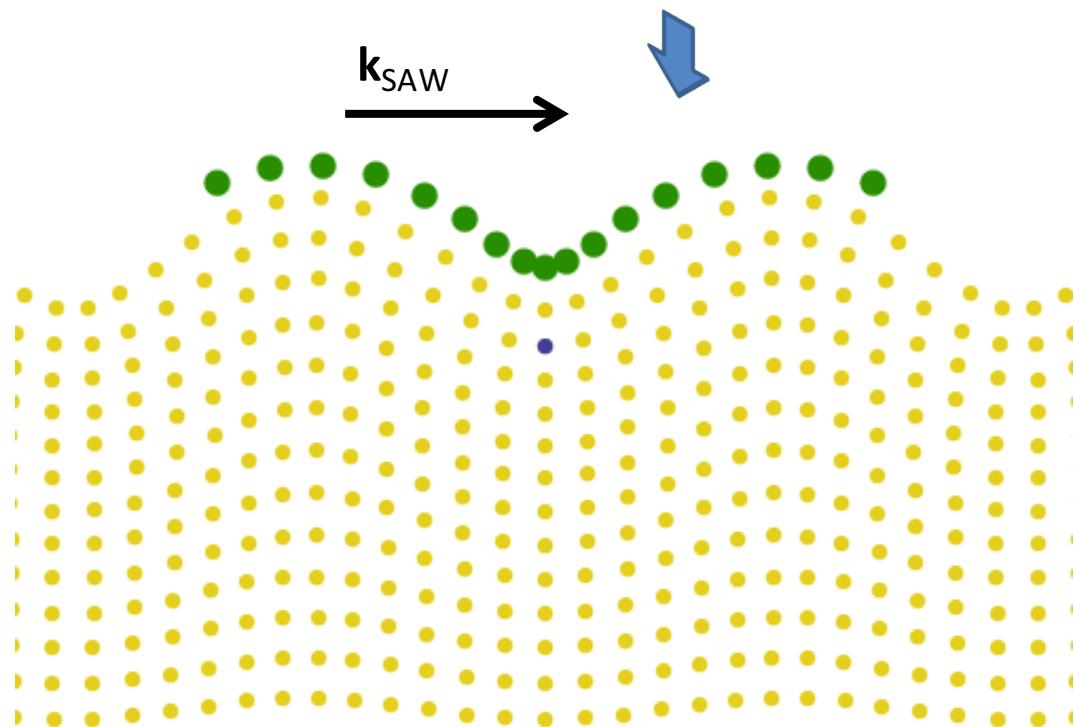


$\mathbf{M}$  direction: along  $\min(F^{DC})$

# Surface acoustic waves (SAWs)

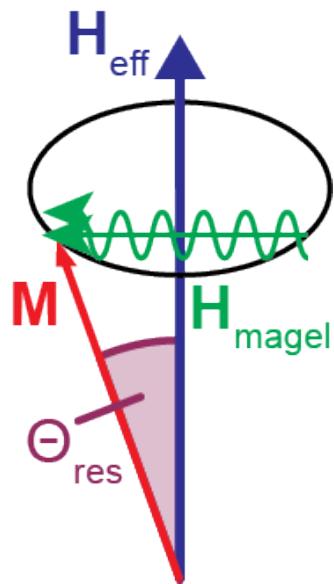


- Nickel/Cobalt thin film
- LiNbO<sub>3</sub> substrate
- Surface acoustic wave
- Magnetoelastic coupling



- rf strain  $\epsilon(t) \approx 10^{-5}$  along  $x$
- velocity  $\approx 3500$  m/s  
( $\lambda_{\text{SAW}}=20\mu\text{m}$ ,  $f=175$  MHz)

# Magnetoelastic drive



$$\mu_0 \mathbf{H}_{\text{magel}} = -\nabla_{\mathbf{m}} F^{\text{AC}}$$

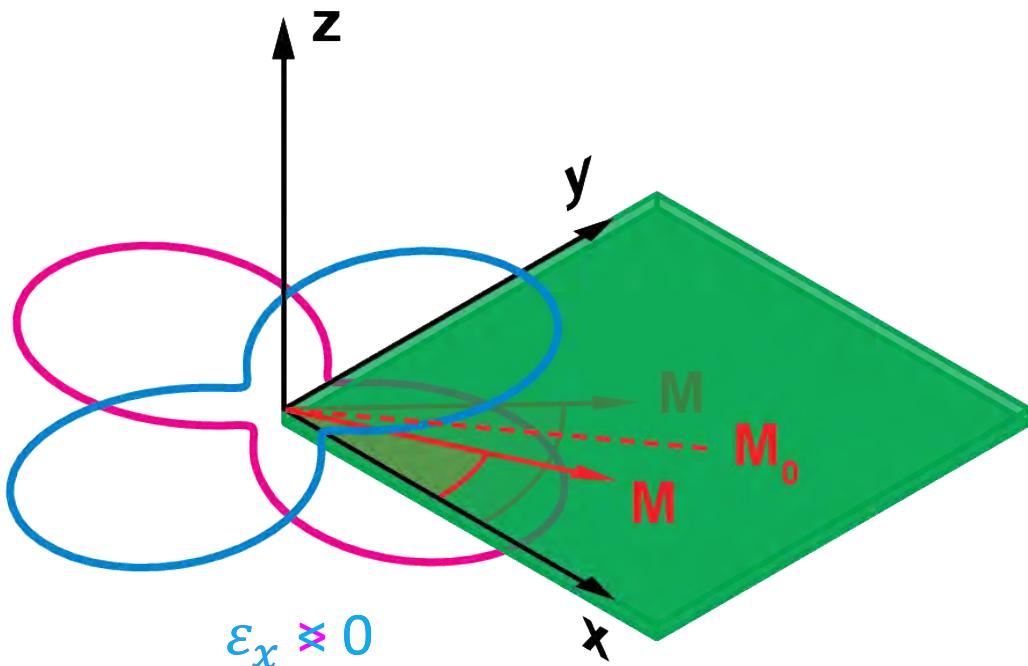
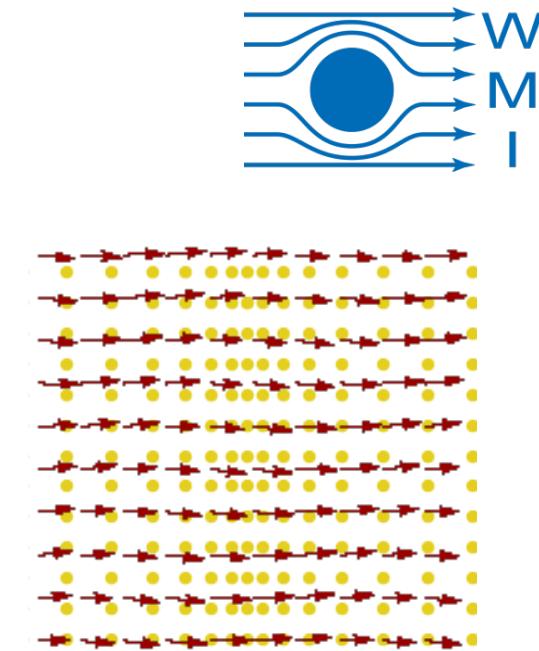
$$F^{\text{AC}}(t) = B_1 \varepsilon_x(t) m_x^2$$

magnetoelastic coupling constant ( $\approx 20 \text{ T}$ )



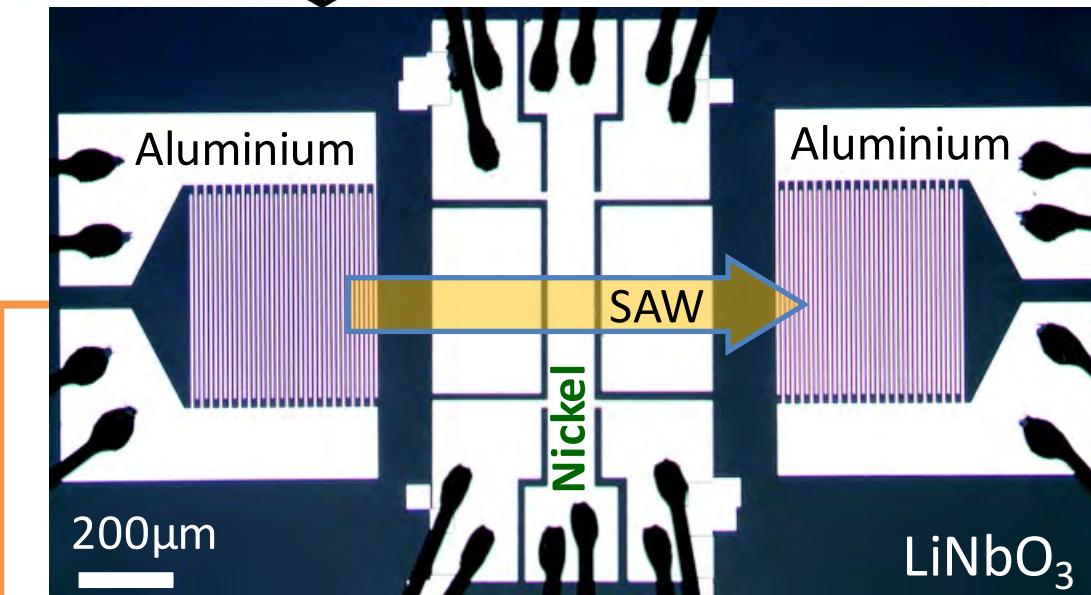
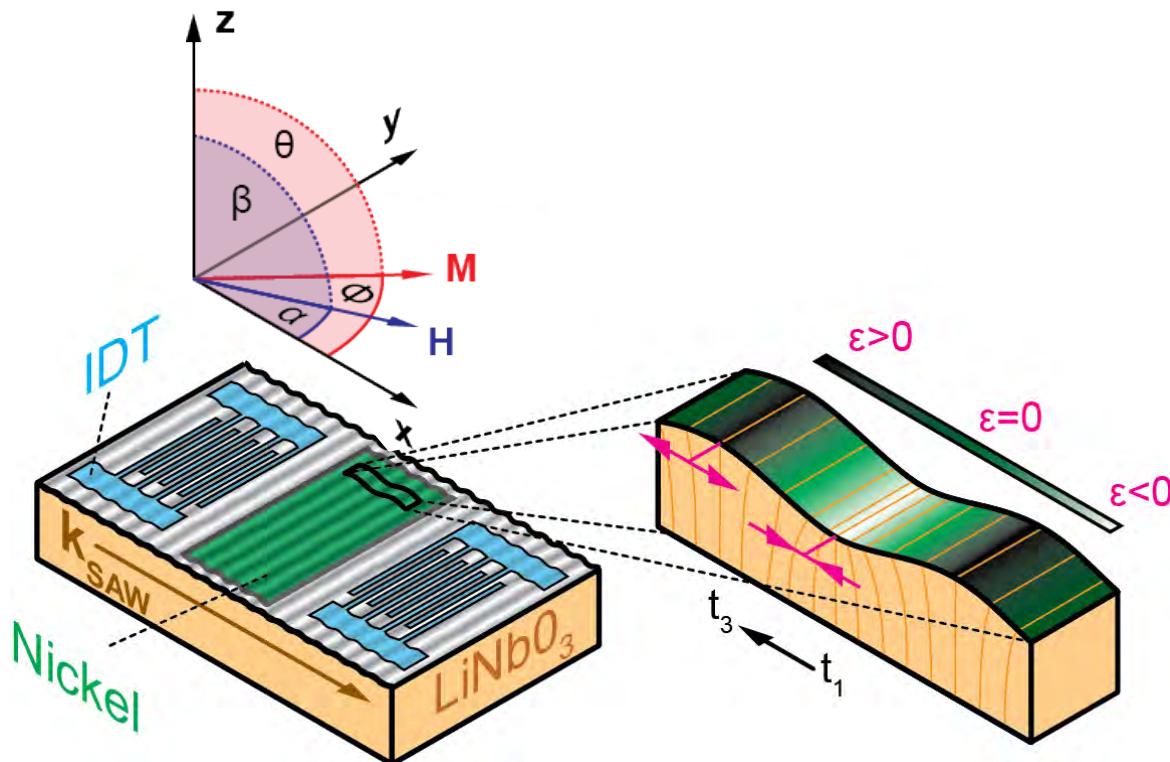
strain ( $\approx 10^{-5}$ )

Pure strain  $\varepsilon$  along x



Magnetoelastic material  
( $B_1 \neq 0$ ): Nickel thin film

radio frequency strain  $\varepsilon$ :  
surface acoustic wave



micrograph of actual sample

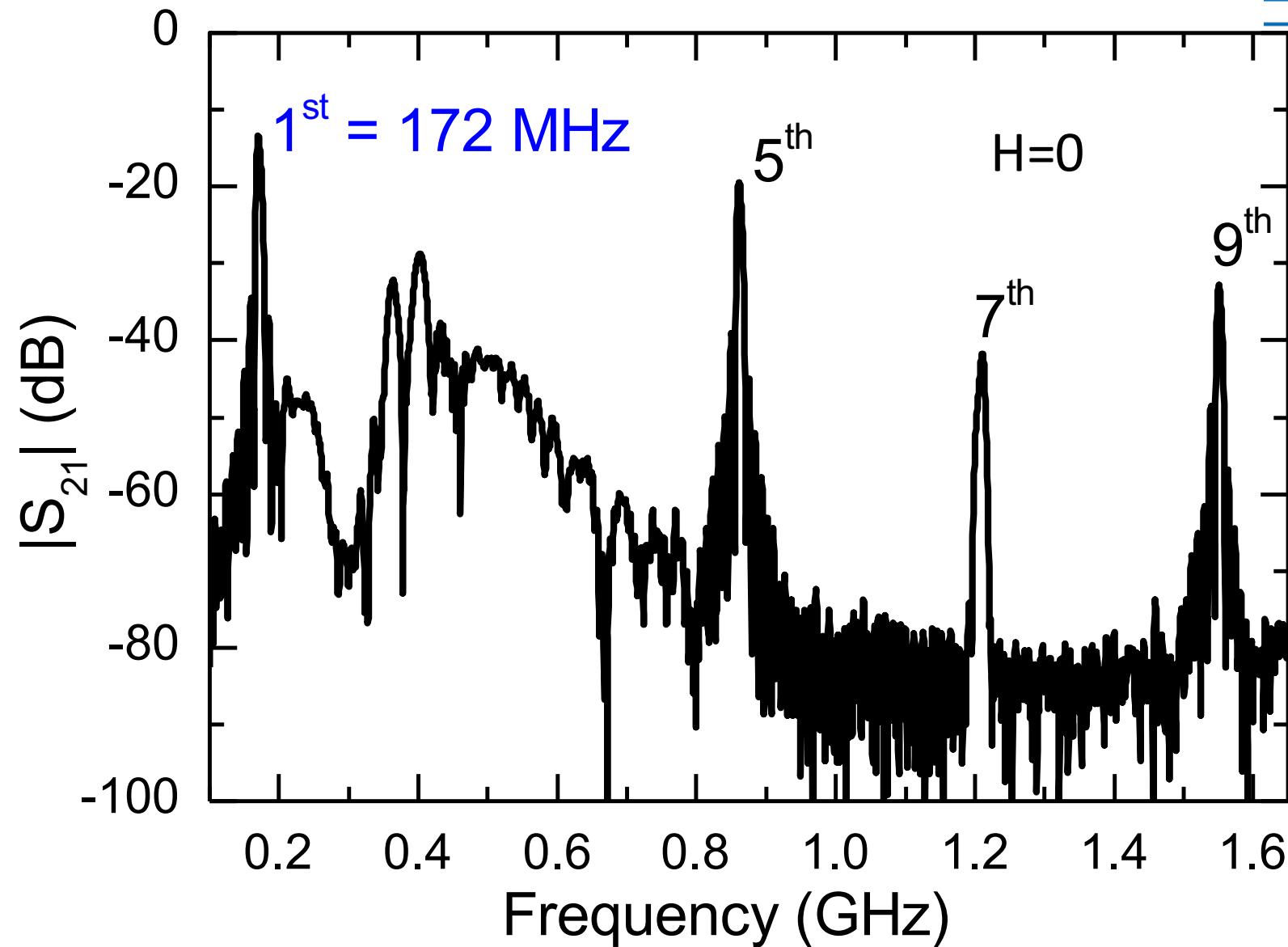
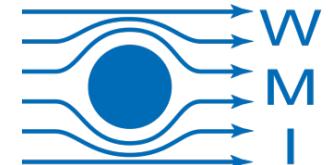


rotatable Electromagnet:  
 $\mu_0 |H| \leq 1 \text{ T}$

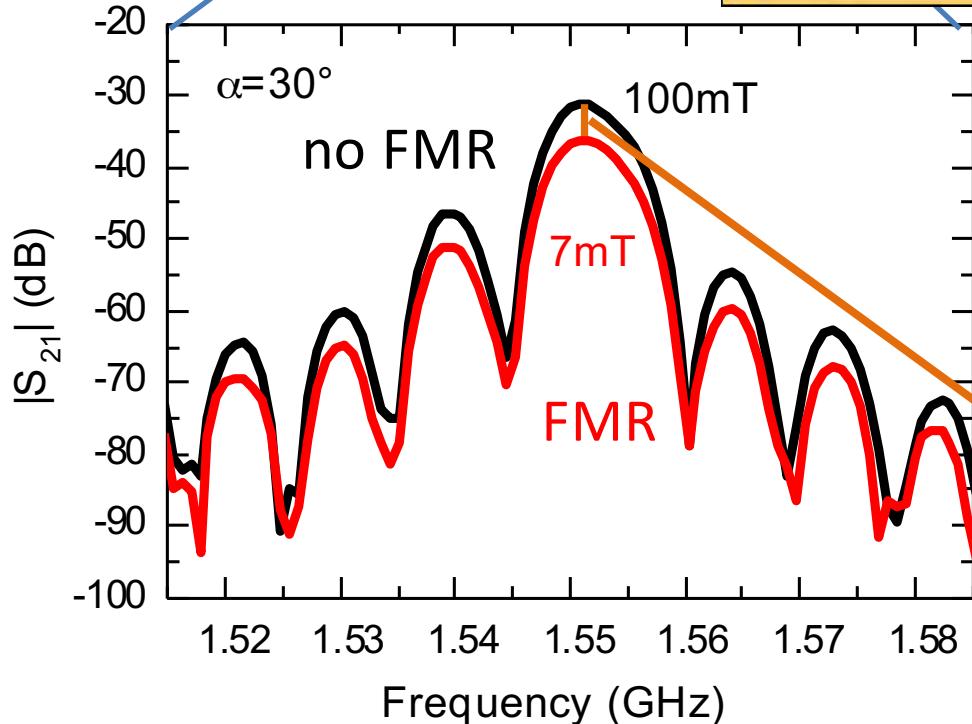
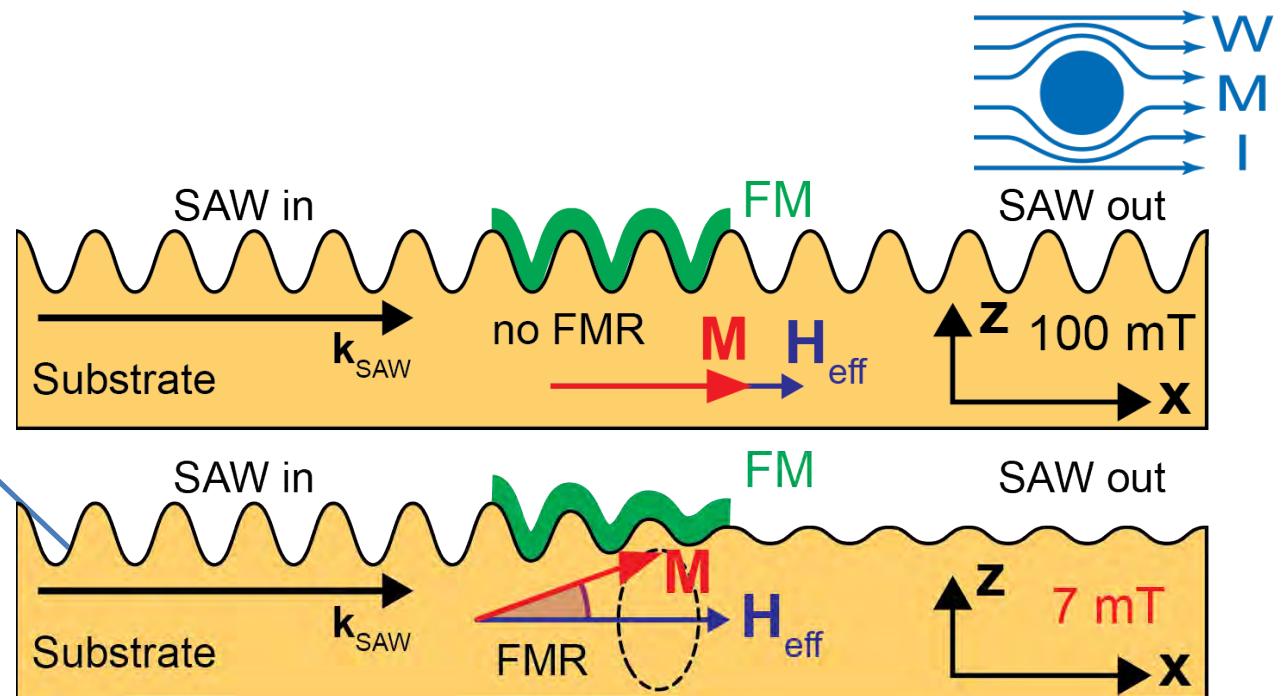
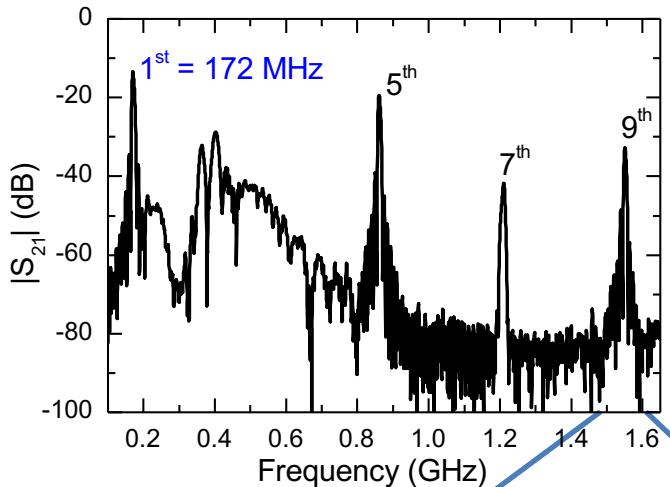


VNA: measure complex  $S_{21}$   
 (transmitted SAW power and phase)

# Microwave transmission

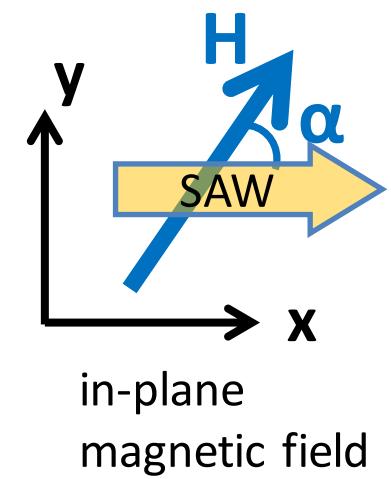


Several SAW transmission maxima

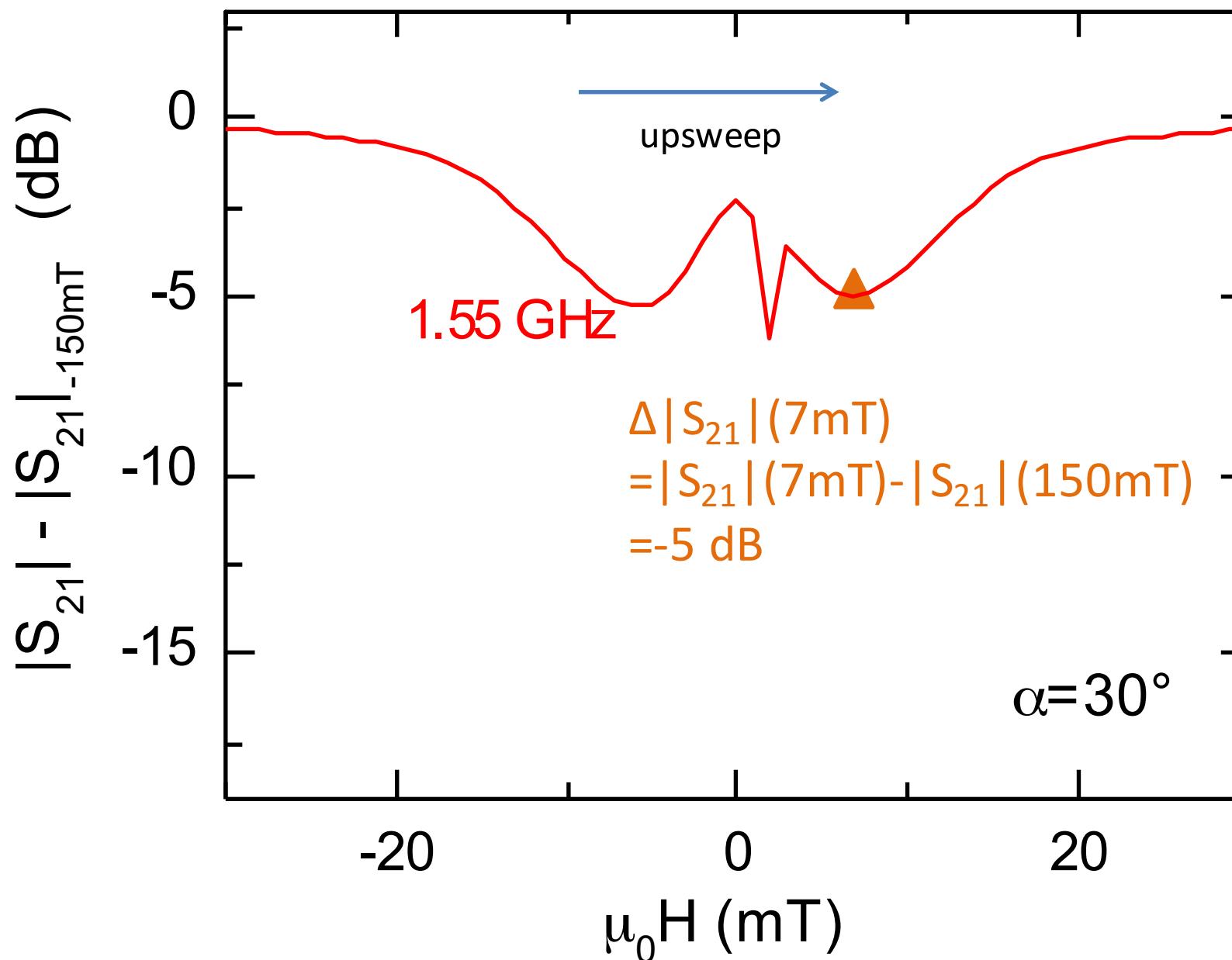
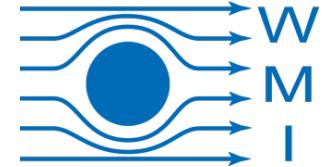


**strong change in SAW transmission as a function of magnetic field strength !**

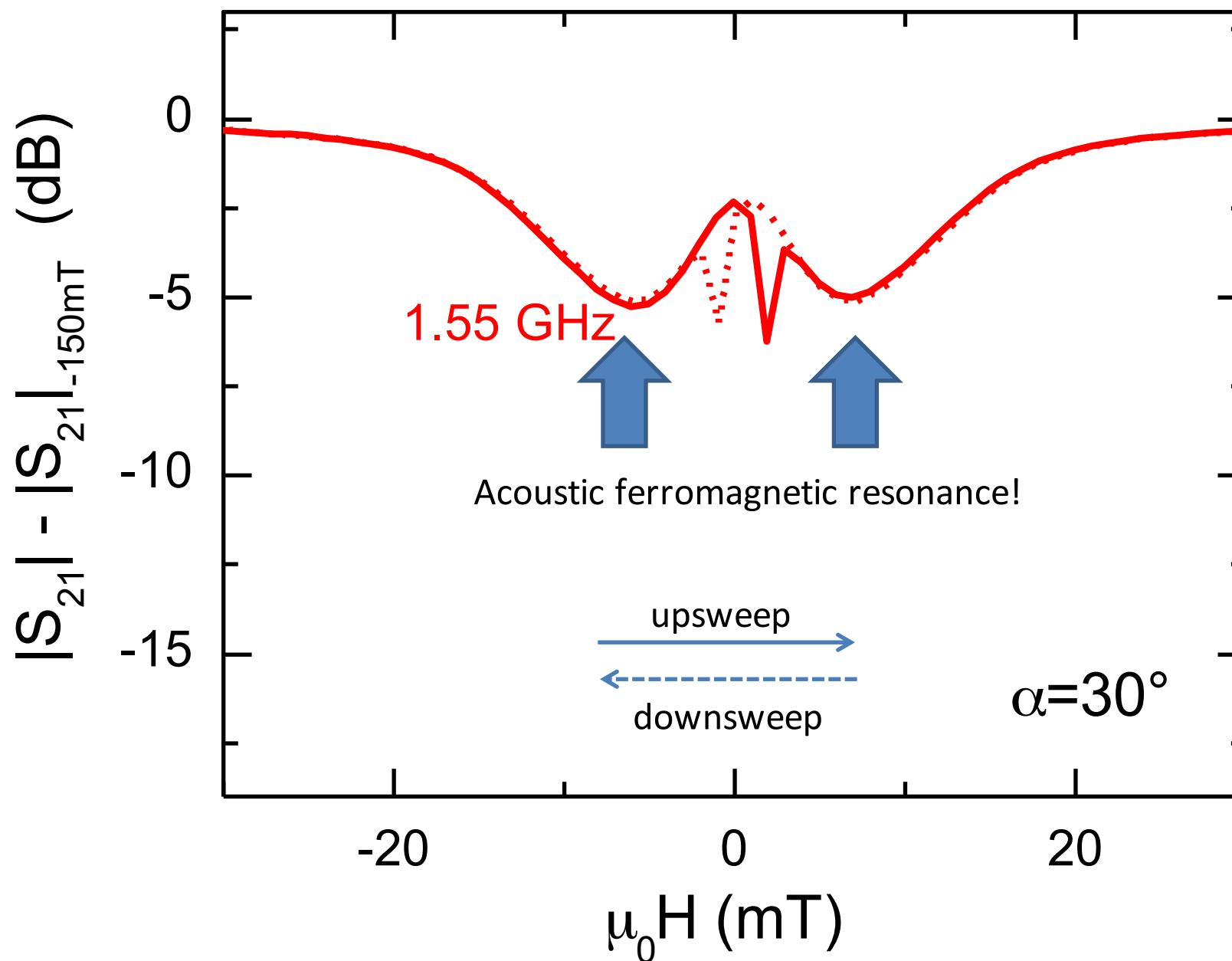
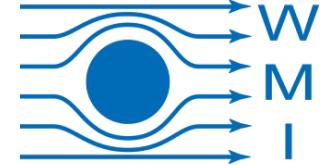
$$\Delta |S_{21}|(7 \text{ mT}) = -5 \text{ dB}$$



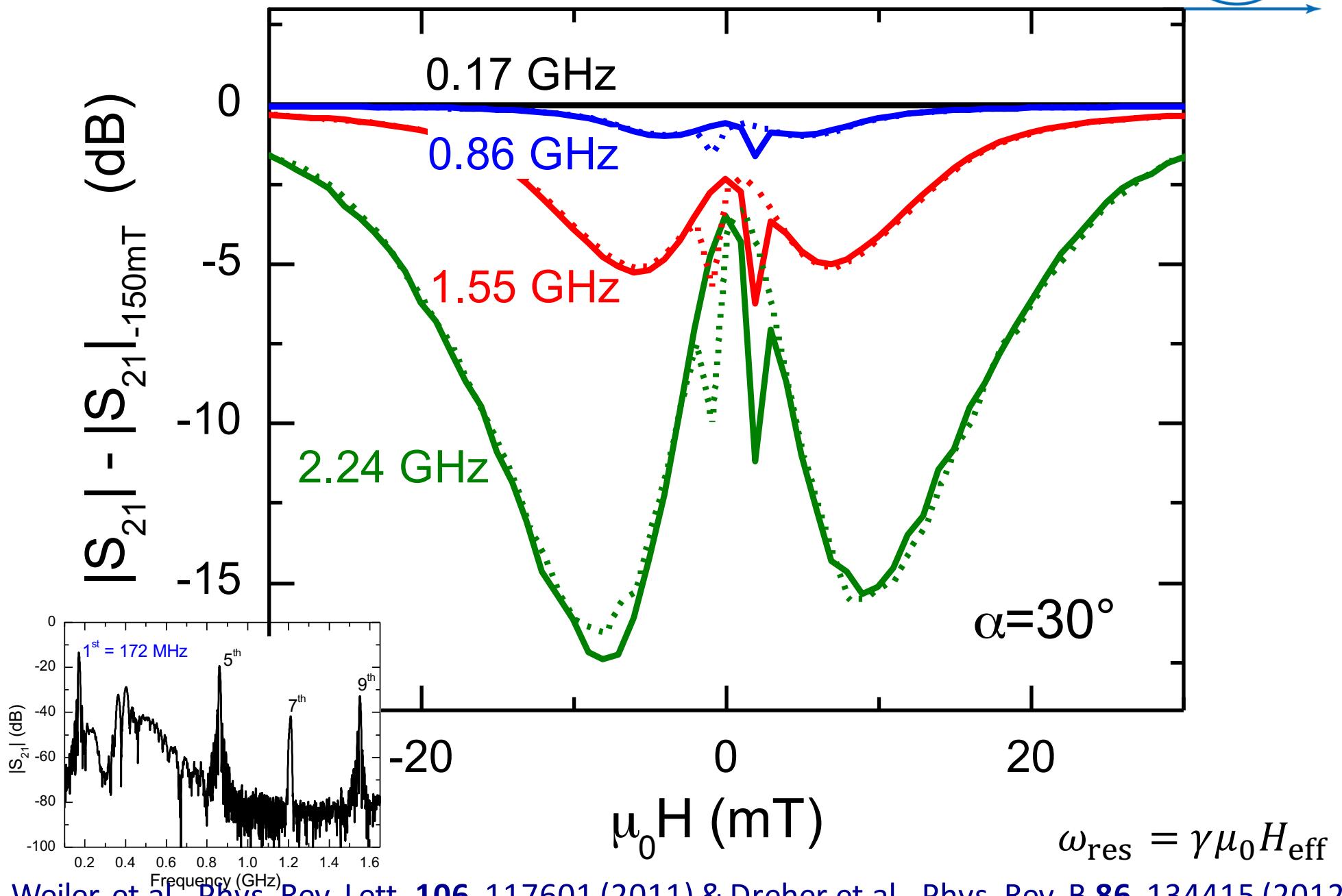
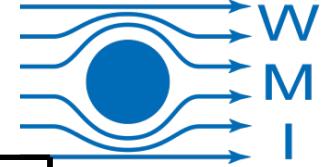
# Acoustic ferromagnetic resonance



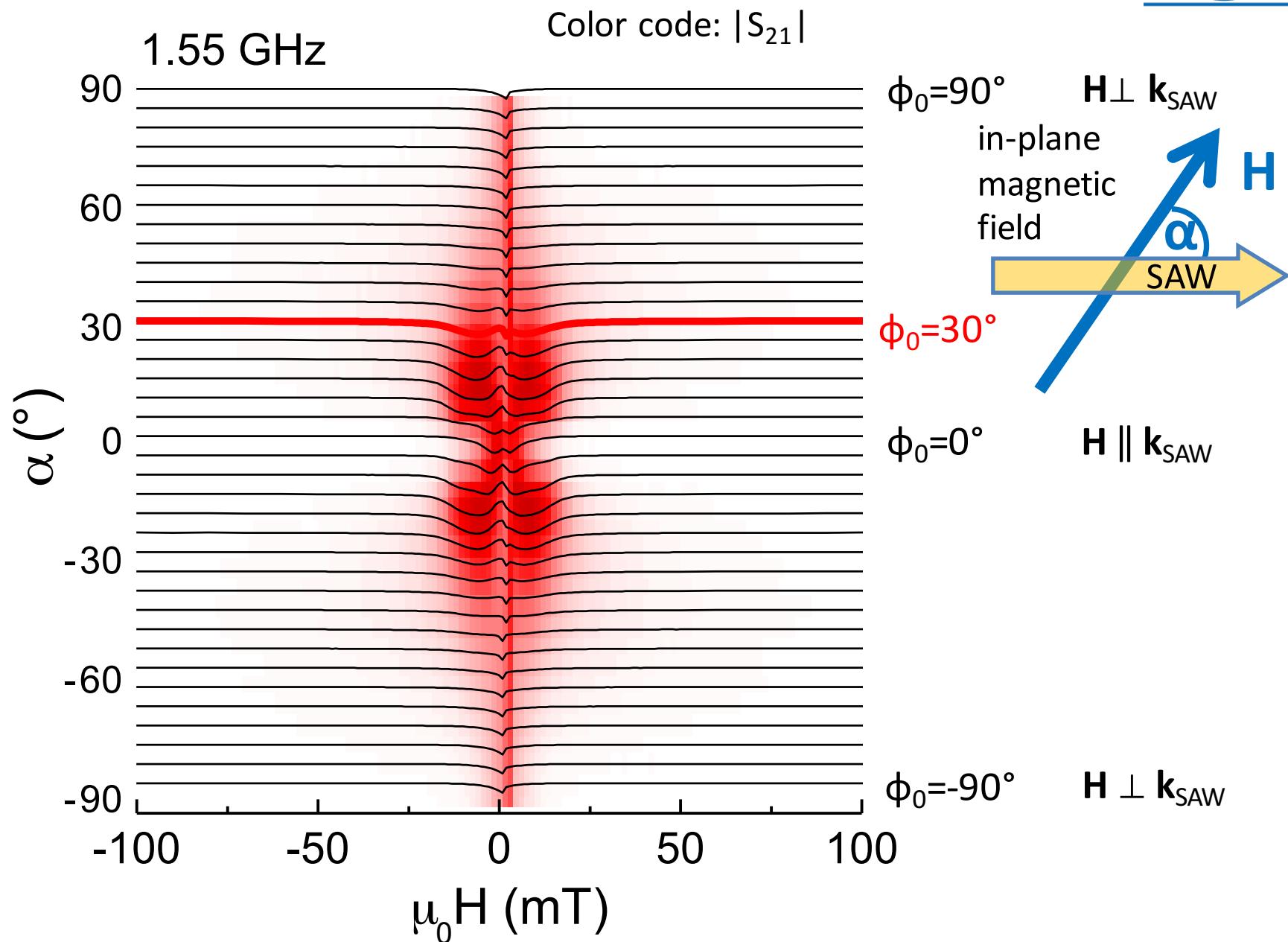
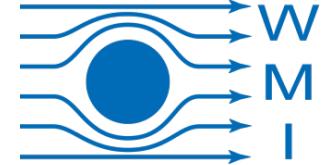
# Acoustic ferromagnetic resonance

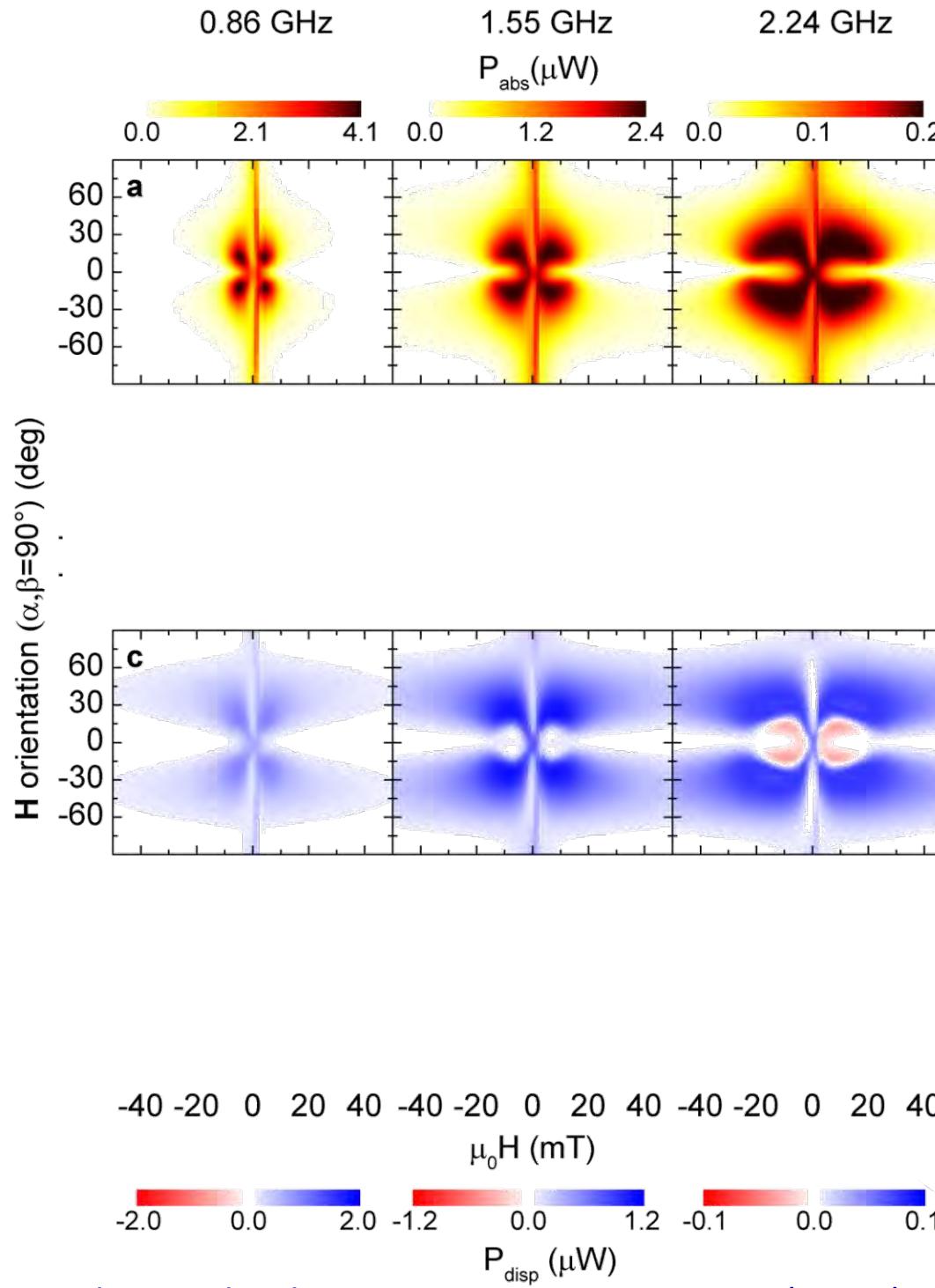


# Acoustic ferromagnetic resonance



# Acoustic ferromagnetic resonance





Comparison:  
Measurement vs.  
simulation

Measurement

$P_{\text{abs}}$

Simulation

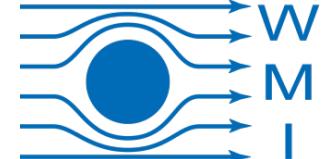
Measurement

$P_{\text{disp}}$

Simulation

in-plane  
rotation

$\varepsilon \approx 5 \times 10^{-7}$   
(measured)



$$u=x$$

$$B_u=2.5 \text{ mT}$$

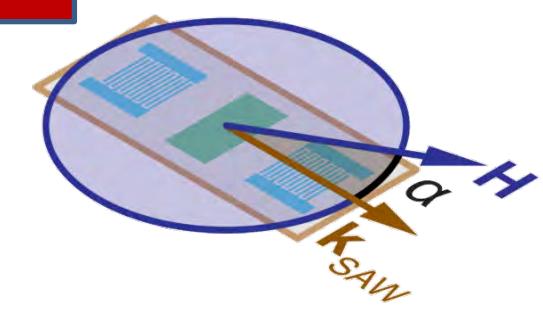
$$B_d=400 \text{ mT}$$

$$B_1=25 \text{ T}$$

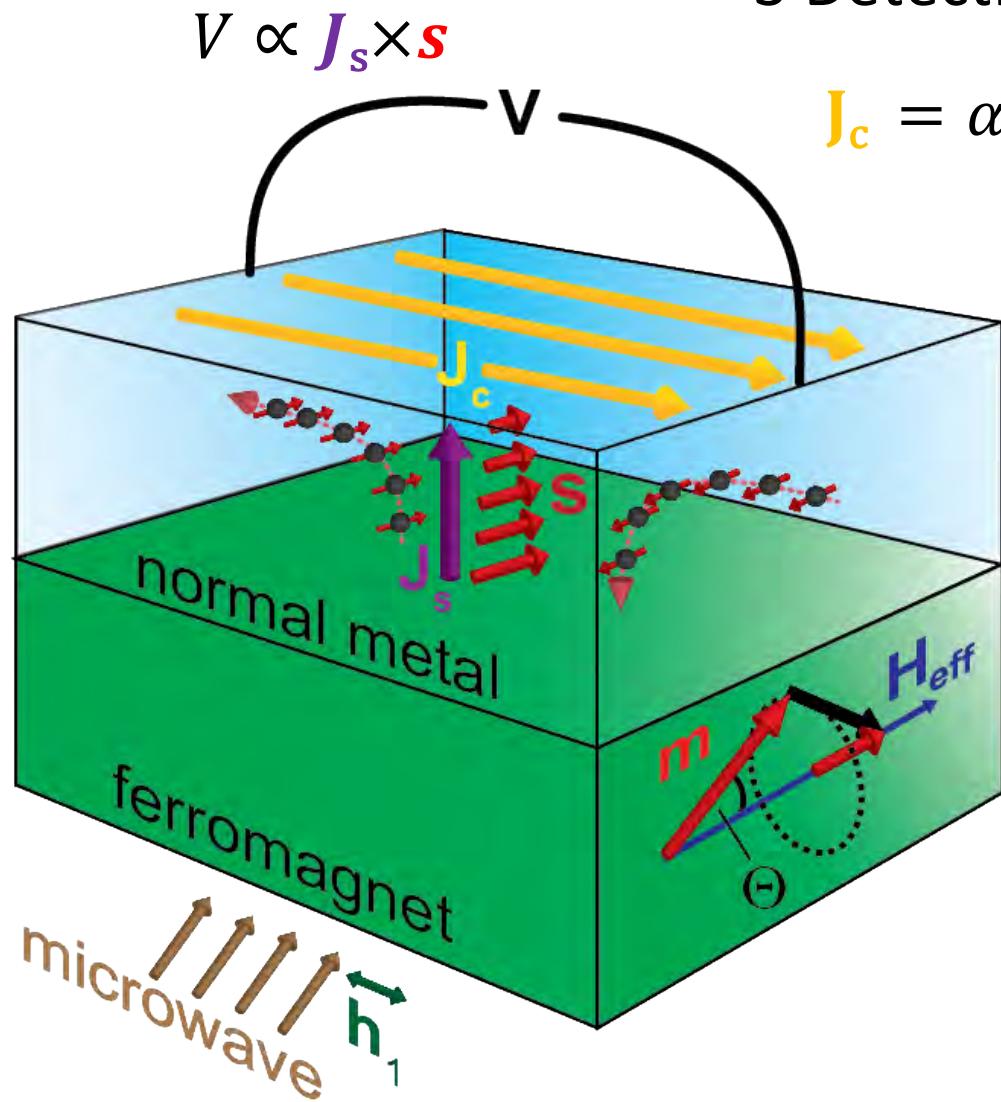
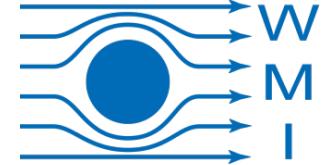
$$M_s=370 \text{ kA/m}$$

$$a=0.1$$

quantitative  
Simulation  
no further  
parameters



# Spin pumping in a nutshell



## 3 Detection: Inverse spin Hall effect

$$J_c = \alpha_{\text{SHE}} \frac{2e}{\hbar} [J_s \times s]$$

$\alpha_{\text{SHE}}$  : Spin Hall angle  
 $\alpha_{\text{SHE}} \approx 0.01$  (Pt)

## 2 Relaxation (Spin pumping contribution)

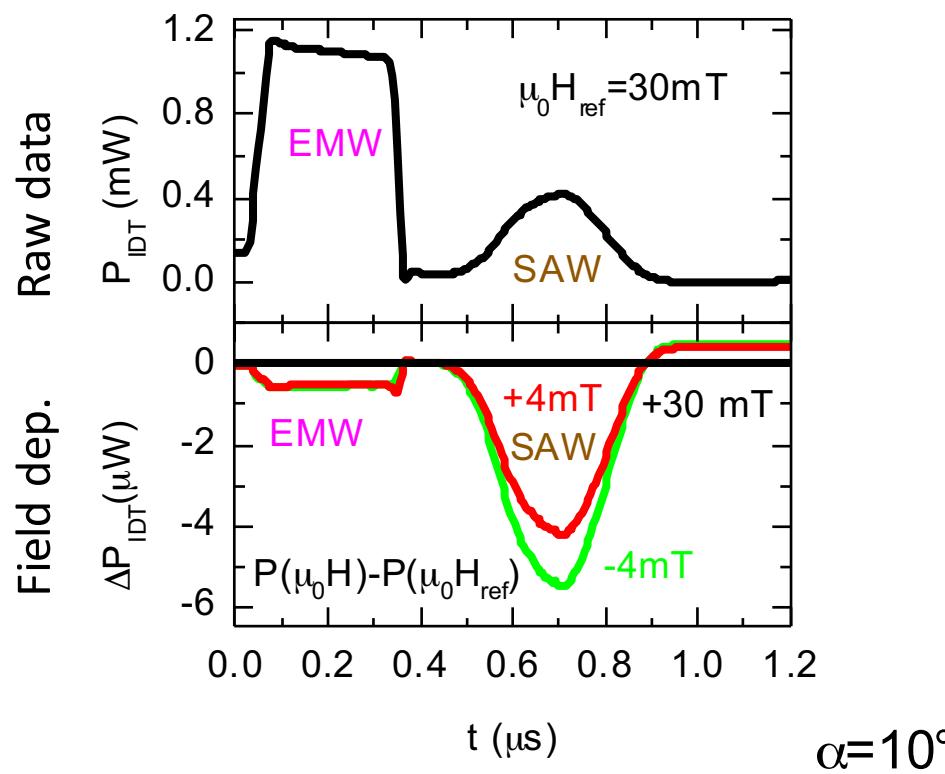
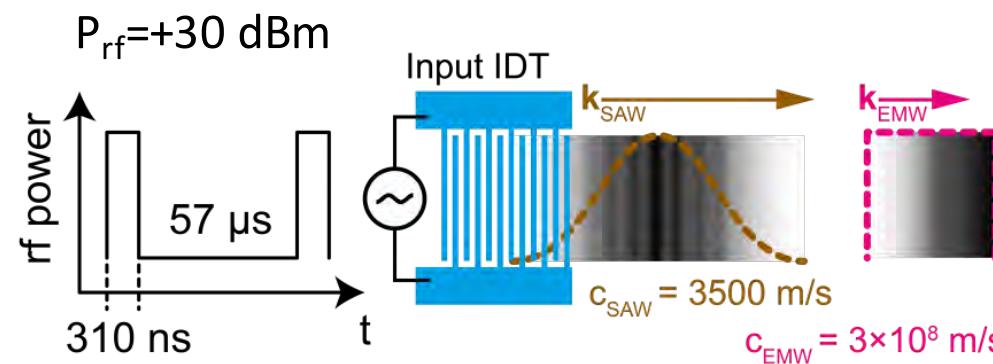
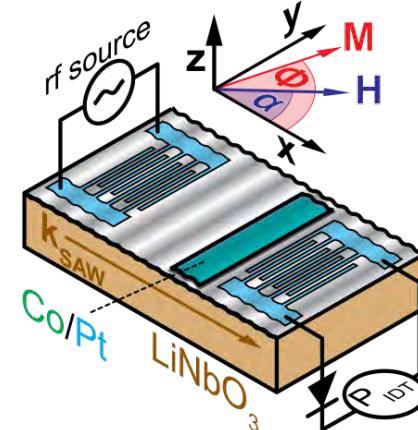
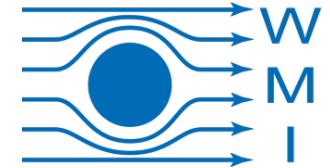
$$J_s = \frac{\hbar}{4\pi} g^{\uparrow\downarrow} \mathbf{m} \times \partial_t \mathbf{m}$$

$$\langle J_s \rangle \approx \frac{\hbar\nu}{2} g^{\uparrow\downarrow} \sin^2 \Theta$$

## 1 Ferromagnetic resonance

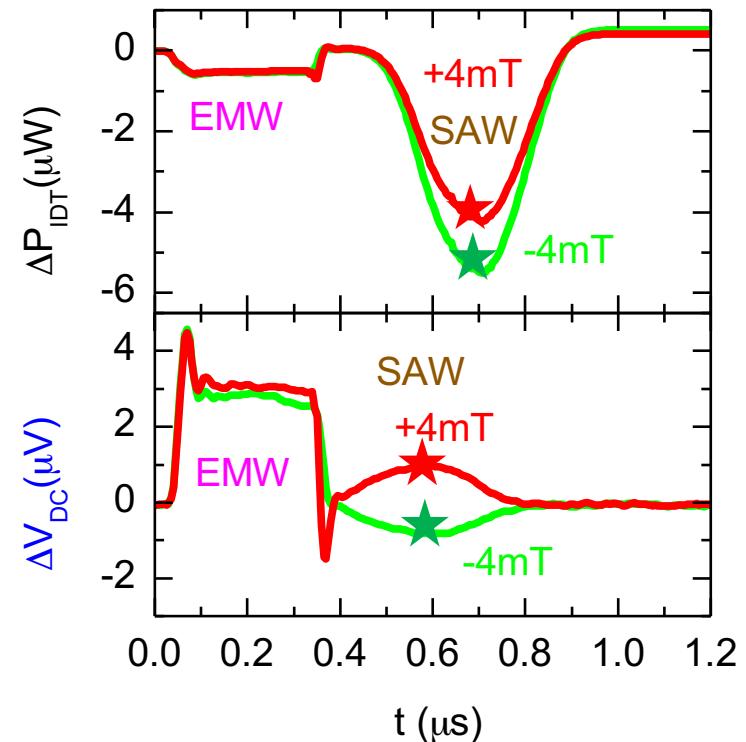
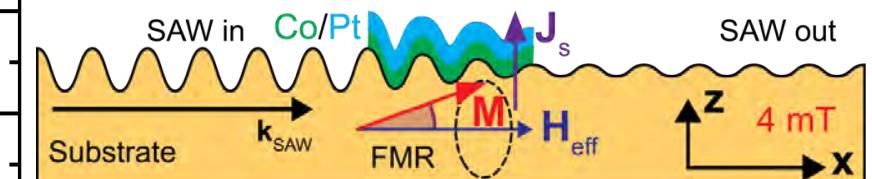
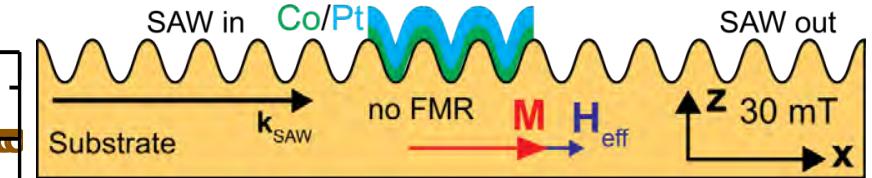
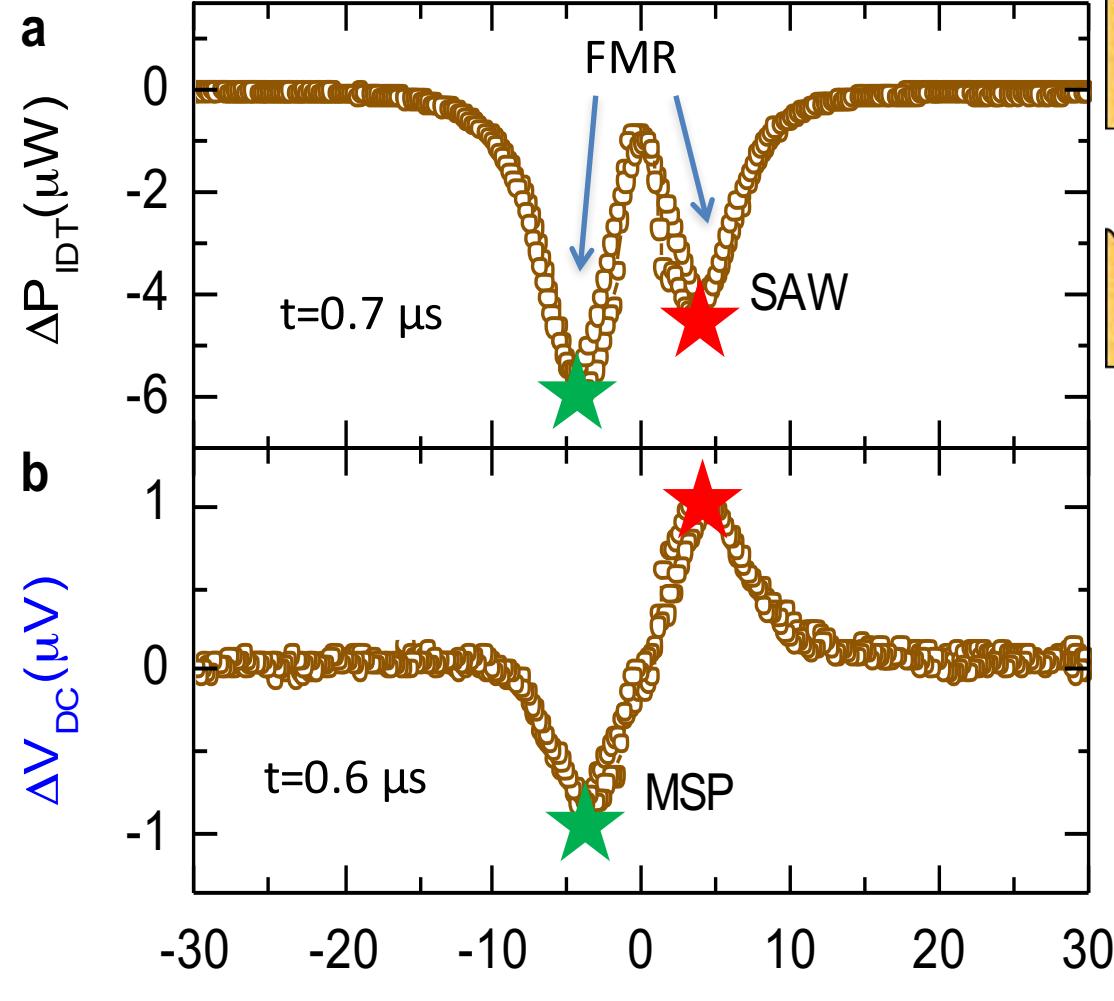
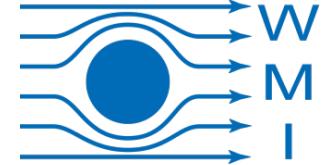
$$\begin{aligned} \partial_t \mathbf{m} = & -\gamma \mathbf{m} \times \mu_0 \mathbf{H}_{\text{eff}} \\ & + a \mathbf{m} \times \partial_t \mathbf{m} \end{aligned}$$

# Acoustically driven spin pumping / time domain

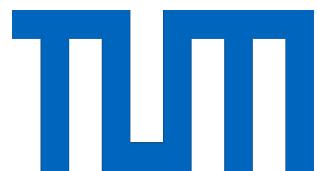


Separation of  
EMW-driven  
and  
SAW-driven  
contributions

# Acoustically driven spin pumping



# Acknowledgements



Lukas Dreher

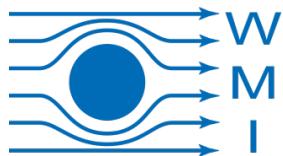
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Fredrik Hocke

Anh Tu Bohn

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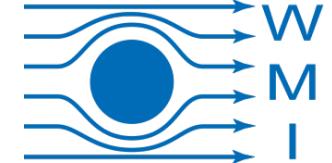
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# Summary

- Sensing magnetoelastics in nanostructures
- Acoustically driven ferromagnetic resonance
- Acoustically driven spin pumping

