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Circuit Quantum Electrodynamics with Semiconductor Quantum Dots

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QSIT Quantum
Science and
Technology

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M

Acknowledgements

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Faculty/PostDoc/PhD/Industry

A. Abdumalikov (Gorba AG)

M. Allan (Leiden)

M. Baur (ABB)

J. Basset (U. Paris Sud)

S. Berger (AWK Group)

R. Bianchetti (ABB)

D. Bozyigit (MIT)

C. Eichler (Princeton)

A. Fedorov (UQ Brisbane)

A. Fragner (Yale)

S. Filipp (IBM Zurich)

J. Fink (IST Austria)

T. Frey (Bosch)

M. Goppl (Sensirion)

J. Govenius (Aalto)

L. Huthmacher (Cambridge)

D.-D. Jarausch (Cambridge)

K. Juliusson (CEA Saclay)

C. Lang (Radionor)

P. Leek (Oxford)

P. Maurer (Stanford)

J. Mlynek (Siemens)

G. Puebla (IBM)

A. Safavi-Naeini (Stanford)

L. Steffen (AWK Group)

A. van Loo (Oxford)

S. Zeytinoglu (ETH Zurich)

Collaborations with (groups of):

A. Blais (Sherbrooke)

C. Bruder (Basel)

M. da Silva (Raytheon)

L. DiCarlo (TU Delft)

K. Ensslin (ETH Zurich)

J. Faist (ETH Zurich)

J. Gambetta (IBM)

K. Hammerer (Hannover)

T. Ihn (ETH Zurich)

F. Merkt (ETH Zurich)

L. Novotny (ETH Zurich)

T. J. Osborne (Hannover)

B. Sanders (Calgary)

S. Schmidt (ETH Zurich)

R. Schoelkopf (Yale)

C. Schoenenberger (Basel)

E. Solano (UPV/EHU)

W. Wegscheider (ETH Zurich)



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CIRCUIT AND CAVITY
QUANTUM ELECTRODYNAMICS



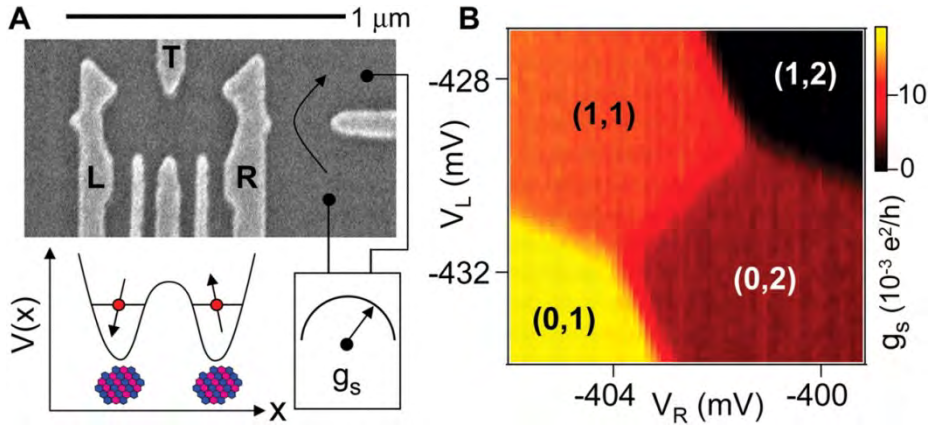
SEVENTH FRAMEWORK
PROGRAMME



Circuit QED with Quantum Dots: Motivation

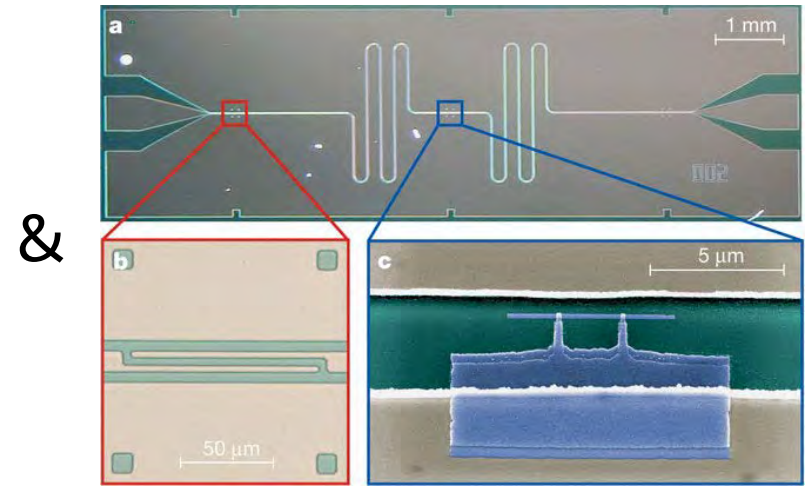
Interconnect the worlds of semiconductor and superconductor based quantum circuits

Spin qubits in quantum dots



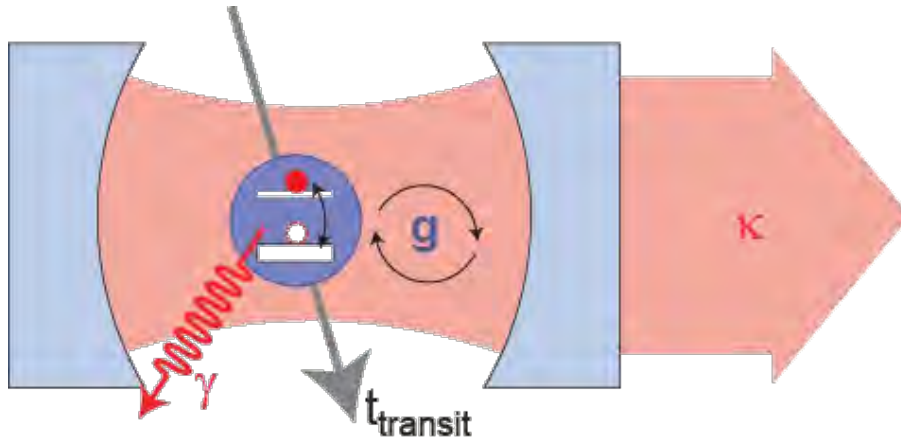
Science 309, 2180 (2005)

Circuit quantum electrodynamics



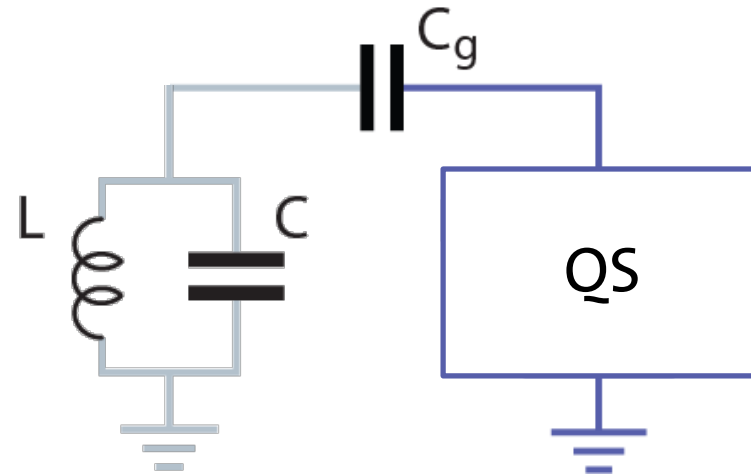
Nature 431, 162 (2004)

Attractive Features of Cavity/Circuit QED



coherent quantum mechanics
with individual photons and qubits ...

... basic approach in circuits:

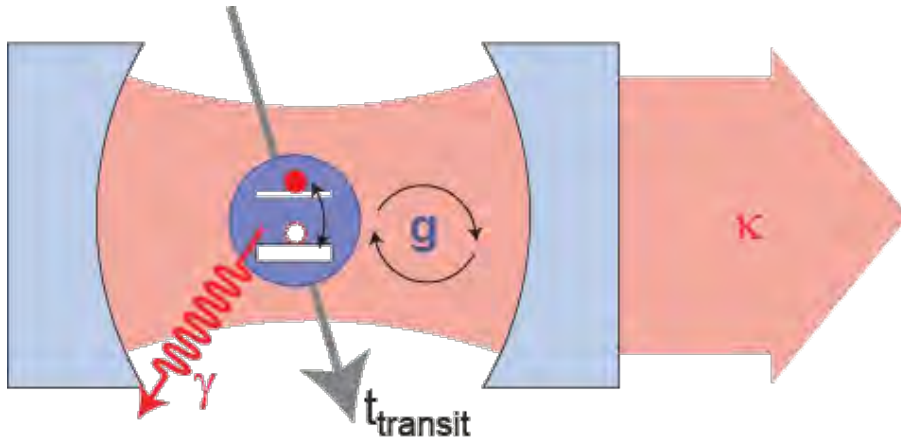


What is this good for?

- Isolate quantum system (QS) from its environment
- Maintain addressability of QS
- Read out the state of QS
- Couple QSs to each other
- Convert state of stationary QS into mobile photon



Cavity QED with Superconducting Circuits



coherent interaction of photons with quantum two-level systems ...

J. M. Raimond *et al.*, *Rev. Mod. Phys.* 73, 565 (2001)

S. Haroche & J. Raimond, *OUP Oxford* (2006)

J. Ye., H. J. Kimble, H. Katori, *Science* 320, 1734 (2008)

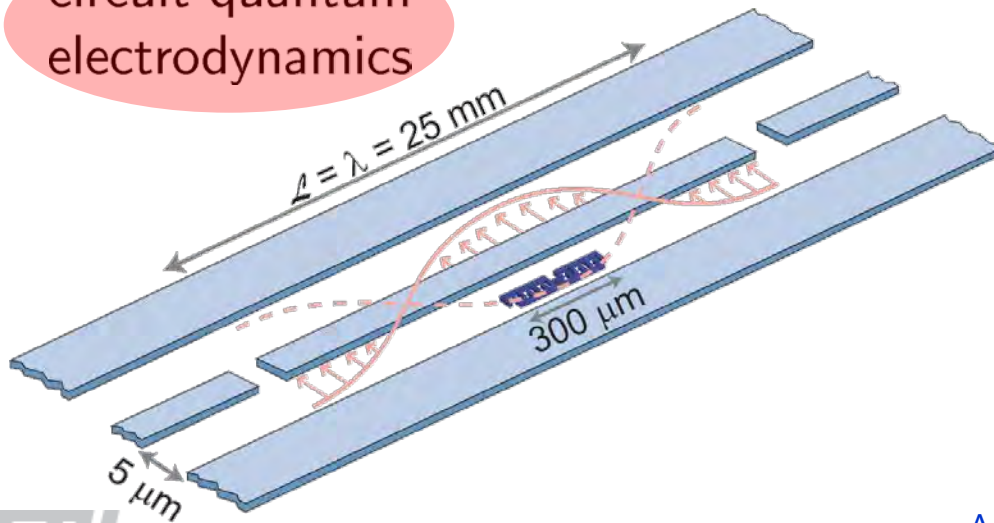
Features:

- strong coupling in solid state sys.
- 'easy' to fabricate and integrate

Research directions:

- quantum optics
- quantum information
- hybrid quantum systems

circuit quantum electrodynamics

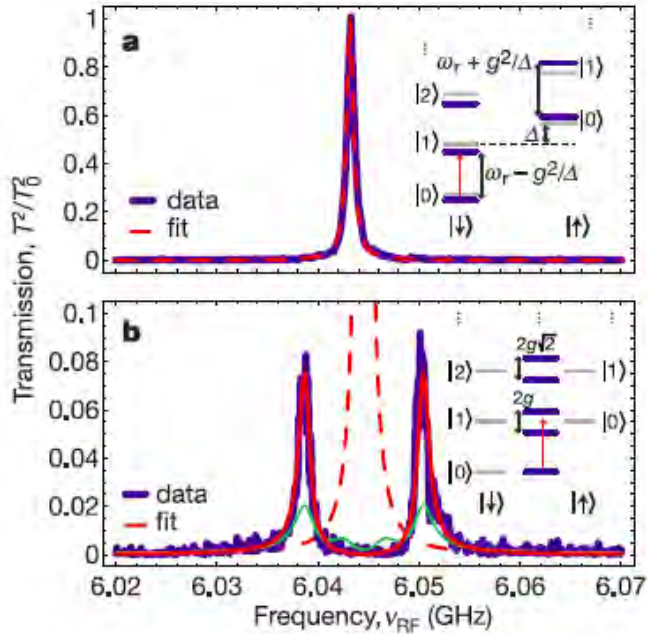


A. Blais, *et al.*, *PRA* 69, 062320 (2004)

A. Wallraff *et al.*, *Nature (London)* 431, 162 (2004)

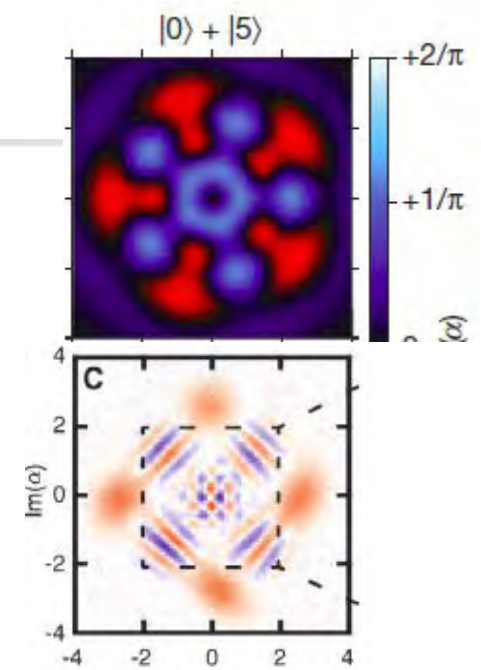
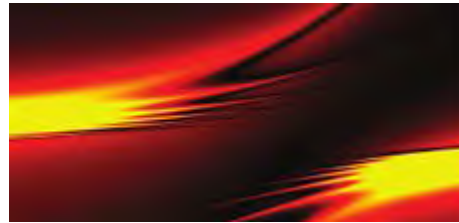
R. J. Schoelkopf, S. M. Girvin, *Nature (London)* 451, 664 (2008)

Quantum Optics

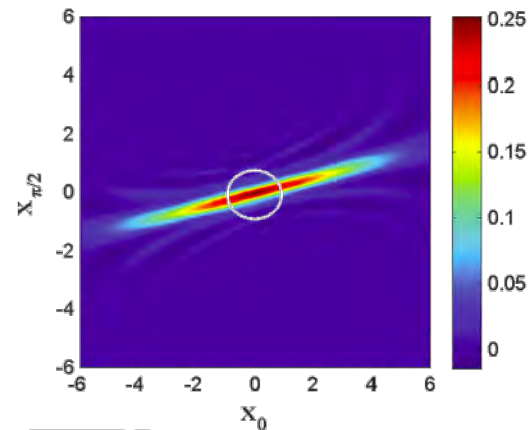


Strong Coherent Coupling
 Chiorescu *et al.*, *Nature* 431, 159 (2004)
 Wallraff *et al.*, *Nature* 431, 162 (2004)
 Schuster *et al.*, *Nature* 445, 515 (2007)

Root n Nonlinearities
 Fink *et al.*, *Nature* 454, 315 (2008)
 Deppe *et al.*, *Nat. Phys.* 4, 686 (2008)
 Bishop *et al.*, *Nat. Phys.* 5, 105 (2009)

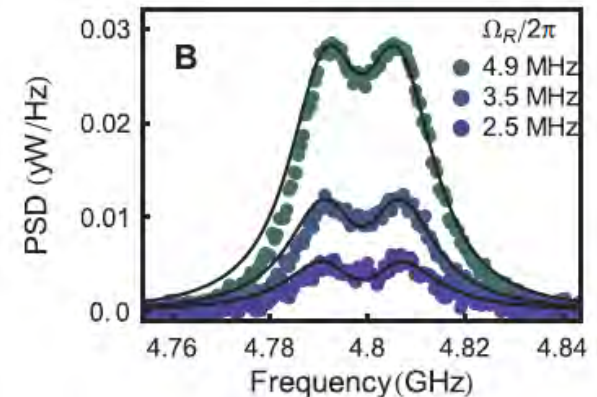


Microwave Fock and Cat States
 Hofheinz *et al.*, *Nature* 454, 310 (2008)
 Hofheinz *et al.*, *Nature* 459, 546 (2009)
 Kirchmair *et al.*, *Nature* 495, 205 (2013)
 Vlastakis *et al.*, *Science* 342, 607 (2013)



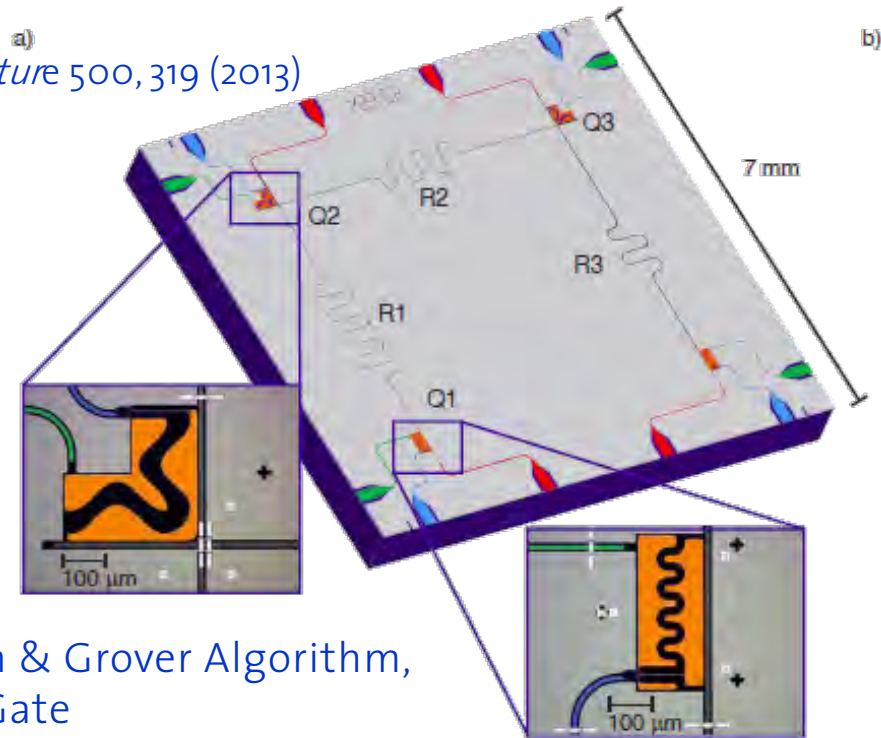
Parametric Amplification & Squeezing
 Castellanos-Beltran *et al.*, *Nat. Phys.* 4, 928 (2008)
 Abdo *et al.*, *PRX* 3, 031001 (2013)

Waveguide QED –
 Qubit Interactions in Free Space
 Astafiev *et al.*, *Science* 327, 840 (2010)
 van Loos *et al.*, *Science* 342, 1494 (2013)



Quantum Computation

Teleportation
 L. Steffen *et al.*, *Nature* 500, 319 (2013)



Circuit QED Architecture

A. Blais *et al.*, *PRA* 69, 062320 (2004)

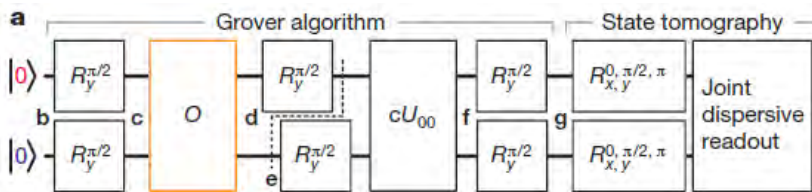
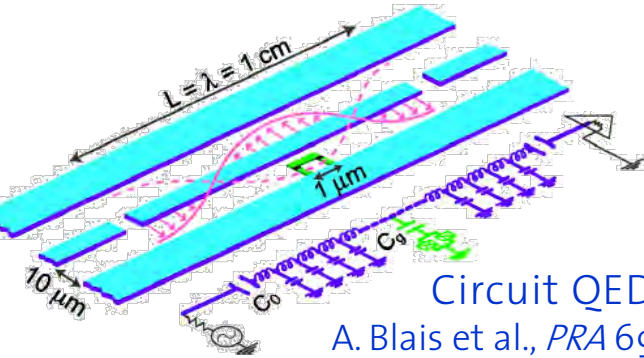
A. Wallraff *et al.*, *Nature* 431, 162 (2004)

M. Sillanpaa *et al.*, *Nature* 449, 438 (2007)

H. Majer *et al.*, *Nature* 449, 443 (2007)

M. Mariani *et al.*, *Science* 334, 61 (2011)

R. Barends *et al.*, *Nature* 508, 500 (2014)



Deutsch & Grover Algorithm,
 Toffoli Gate

L. DiCarlo *et al.*, *Nature* 460, 240 (2009)

L. DiCarlo *et al.*, *Nature* 467, 574 (2010)

A. Fedorov *et al.*, *Nature* 481, 170 (2012)

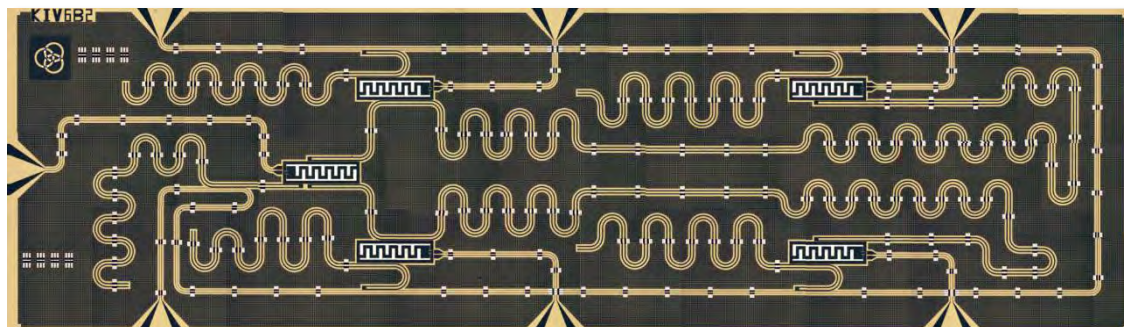
Error Correction & Logical Qubits

M. Reed *et al.*, *Nature* 481, 382 (2012)

Corcoles *et al.*, *Nat. Com.* 6, 6979 (2015)

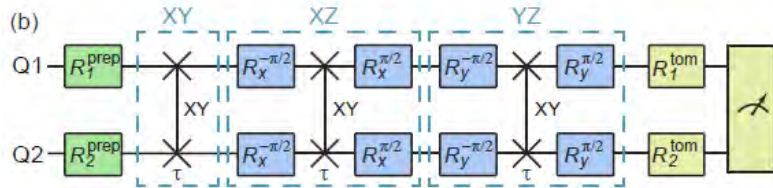
Ristè *et al.*, *Nat. Com.* 6, 6983 (2015)

Kelly *et al.*, *Nature* 519, 66-69 (2015)



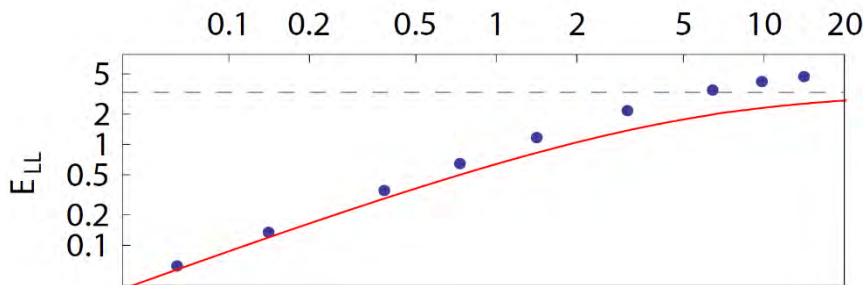
Quantum Simulation

Digital simulation of exchange, Heisenberg, Ising spin models



Salathe *et al.*, *PRX* 5, 021027 (2015)

Quantum simulation of correlated systems with variational Ansatz based on MPS

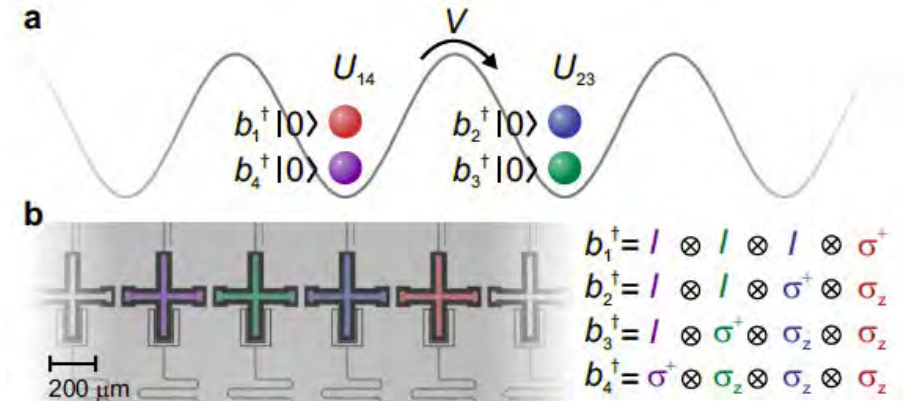


Eichler *et al.*, *Phys. Rev. X* 5, 041044 (2015)

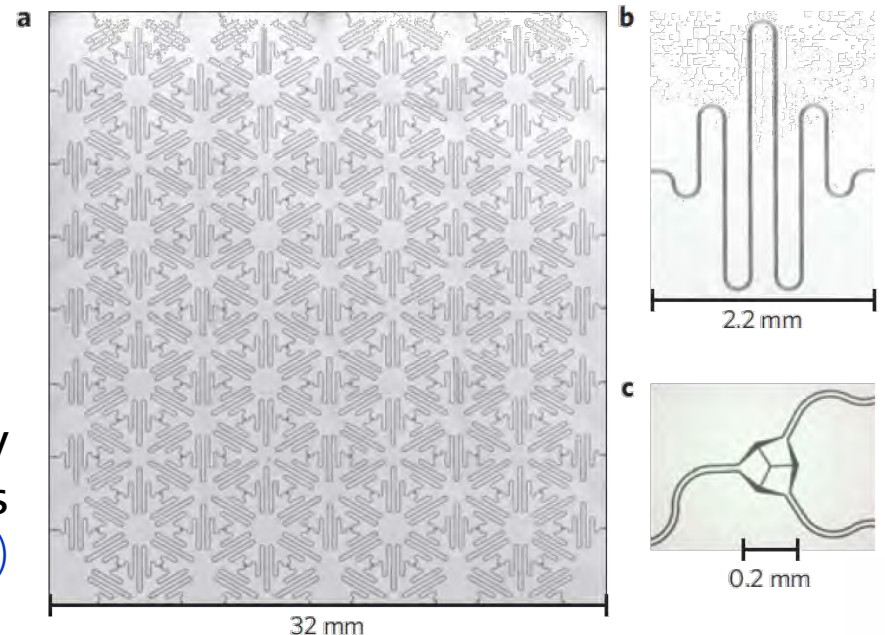
Analog simulations with cavity and/or qubit arrays

Houck *et al.*, *Nat Phys* 8, 292 (2012)

... two-mode fermionic Hubbard models

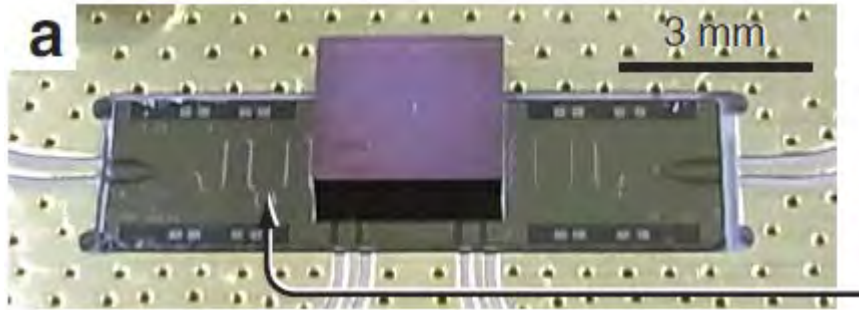


Barends *et al.*, *Nat. Com.* 6, 7654 (2015)



Hybrid Systems with Superconducting Circuits

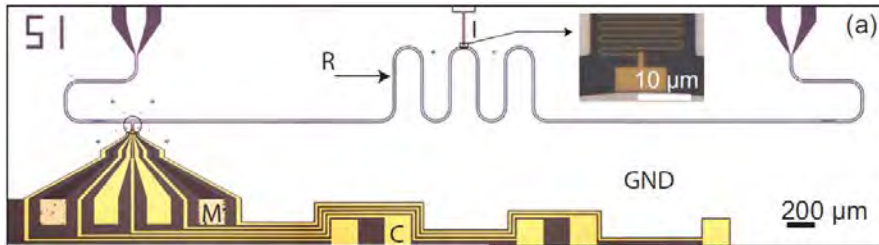
Spin Ensembles: e.g. NV centers
 D. Schuster *et al.*, *PRL* 105, 140501 (2010)
 Y. Kubo *et al.*, *PRL* 105, 140502 (2010)



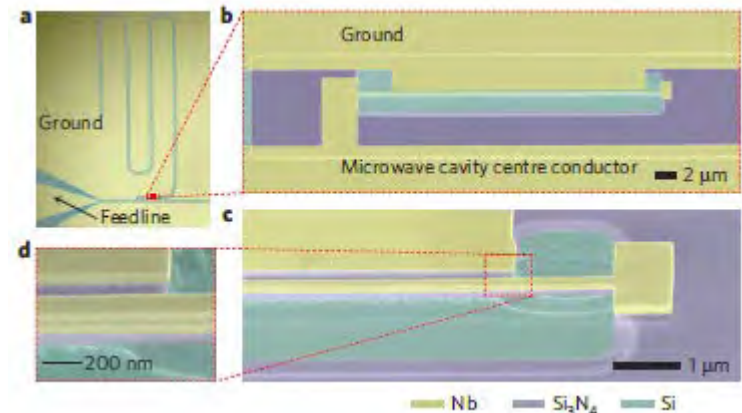
Polar Molecules, Rydberg, BEC
 P. Rabl *et al.*, *PRL* 97, 033003 (2006)
 A. Andre *et al.*, *Nat. Phys.* 2, 636 (2006)
 D. Petrosyan *et al.*, *PRL* 100, 170501 (2008)
 J. Verdu *et al.*, *PRL* 103, 043603 (2009)



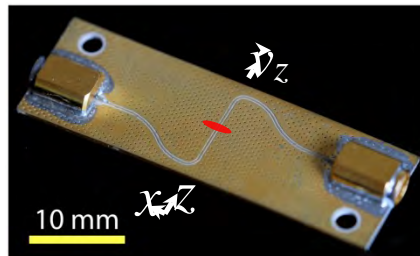
CNT, Gate Defined 2DEG, or nanowire Quantum Dots
 M. Delbecq *et al.*, *PRL* 107, 256804 (2011)
 T. Frey *et al.*, *PRL* 108, 046807 (2012)
 K. Petersson *et al.*, *Nature* 490, 380 (2013)



Nano-Mechanics
 J. Teufel *et al.*, *Nature* 475, 359 (2011)
 X. Zhou *et al.*, *Nat. Phys.* 9, 179 (2013)



Rydberg Atoms
 S. Hogan *et al.*, *PRL* 108, 063004 (2012)

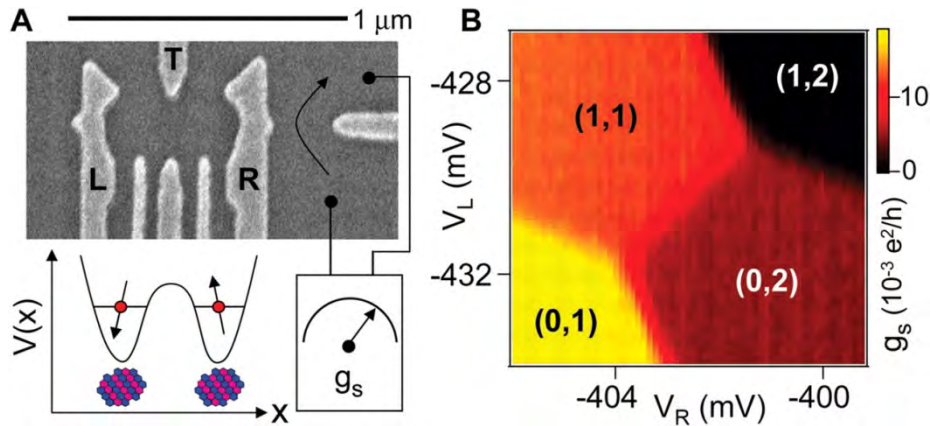


... and many more

Circuit QED with Quantum Dots: Motivation

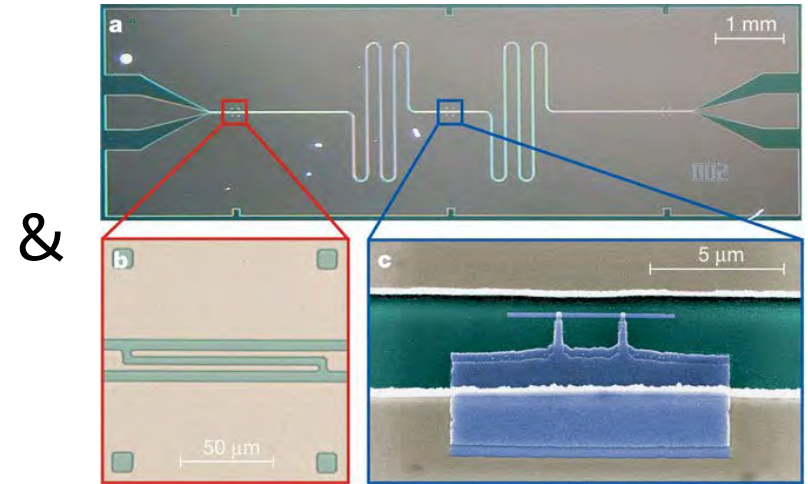
Interconnect the worlds of semiconductor and superconductor based quantum circuits

Spin qubits in quantum dots



Science 309, 2180 (2005)

Circuit quantum electrodynamics



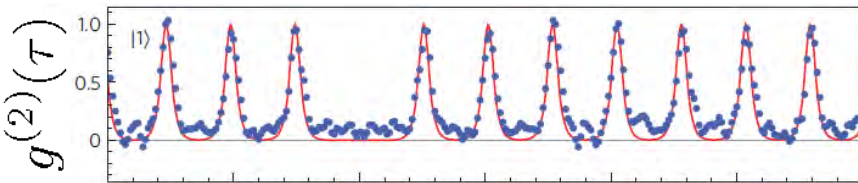
Nature 431, 162 (2004)

Potential benefits:

- realize interfaces between quantum systems
- allow for coherent control while isolating from environment
- achieve long distance coupling
- implement alternative measurement/read-out schemes
- explore correlations between charge transport and radiation emission

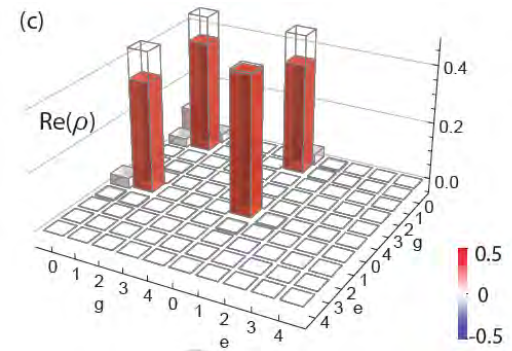
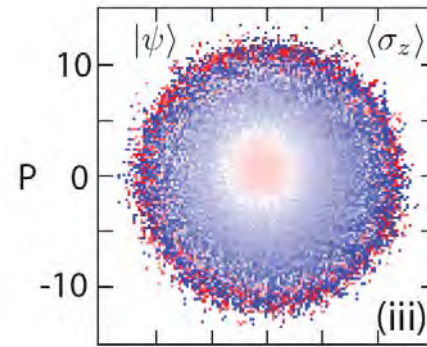
Experiments with Propagating Quantum Microwaves

Single photon sources and their anti-bunching



Houck *et al.*, *Nature* 449, 328 (2007)
 Bozyigit *et al.*, *Nat. Phys* 7, 154 (2011)
 Lang *et al.*, *PRL* 107, 073601 (2011)

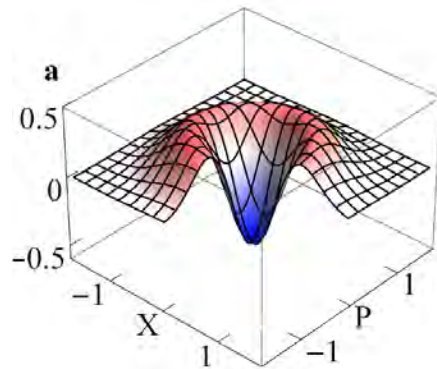
Creation and characterization of entanglement of qubits with propagating photons



Eichler *et al.*, *PRL* 109, 240501 (2012)
 Eichler *et al.*, *PRA* 86, 032106 (2012)

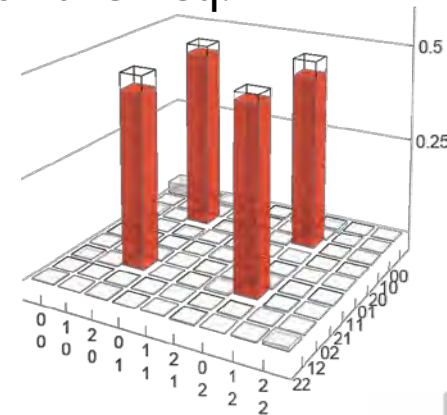
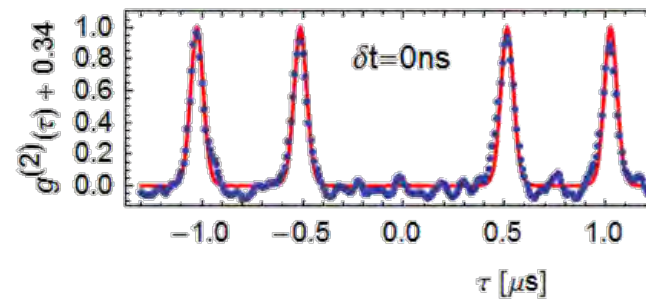
Full state tomography and Wigner functions of propagating photons

Eichler *et al.*, *PRL* 106, 220503 (2011)

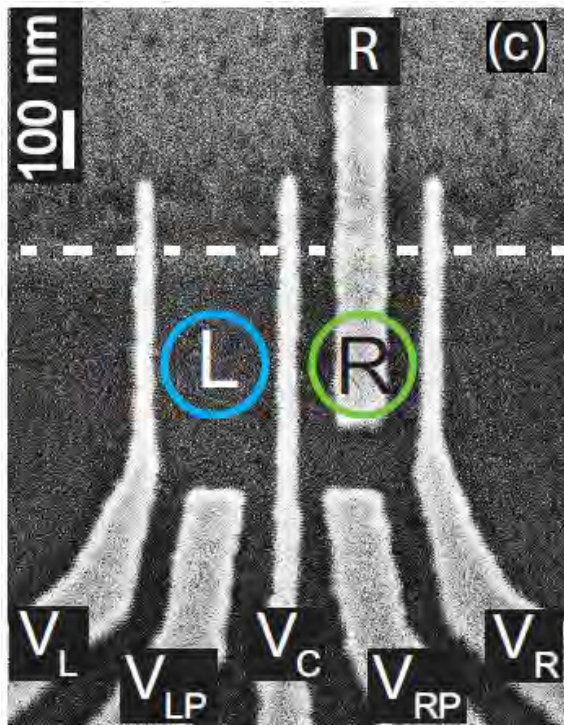
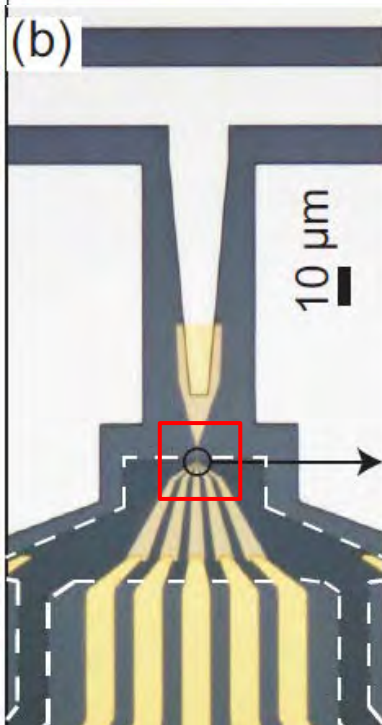
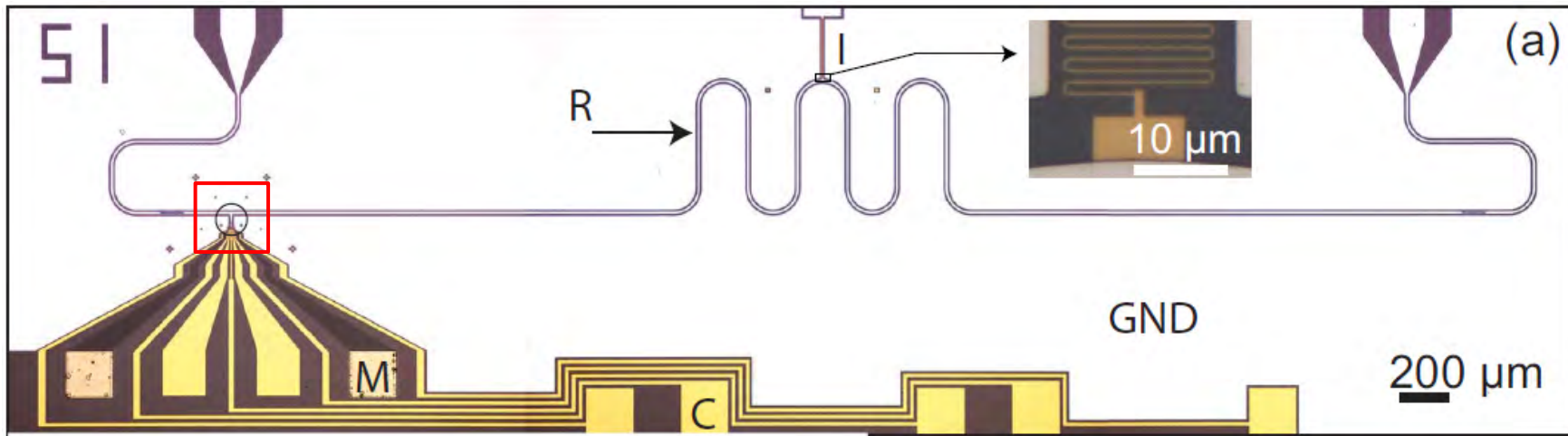


Hong-Ou-Mandel: Two-photon interference incl. msrmnt of coherences at microwave freq.

Lang *et al.*, *Nat. Phys.* 9, 345 (2013)



Hybrid Quantum Dot / Circuit QED Device



resonator circuit:
superconducting aluminium
 $f_o = 6.75 \text{ GHz}$ ($28 \mu\text{eV}$, 280 mK)

quantum dot based on standard
Ga[Al]As heterostructure
with 2D electron gas

Frey et al., PRL 108, 046807 (2012)

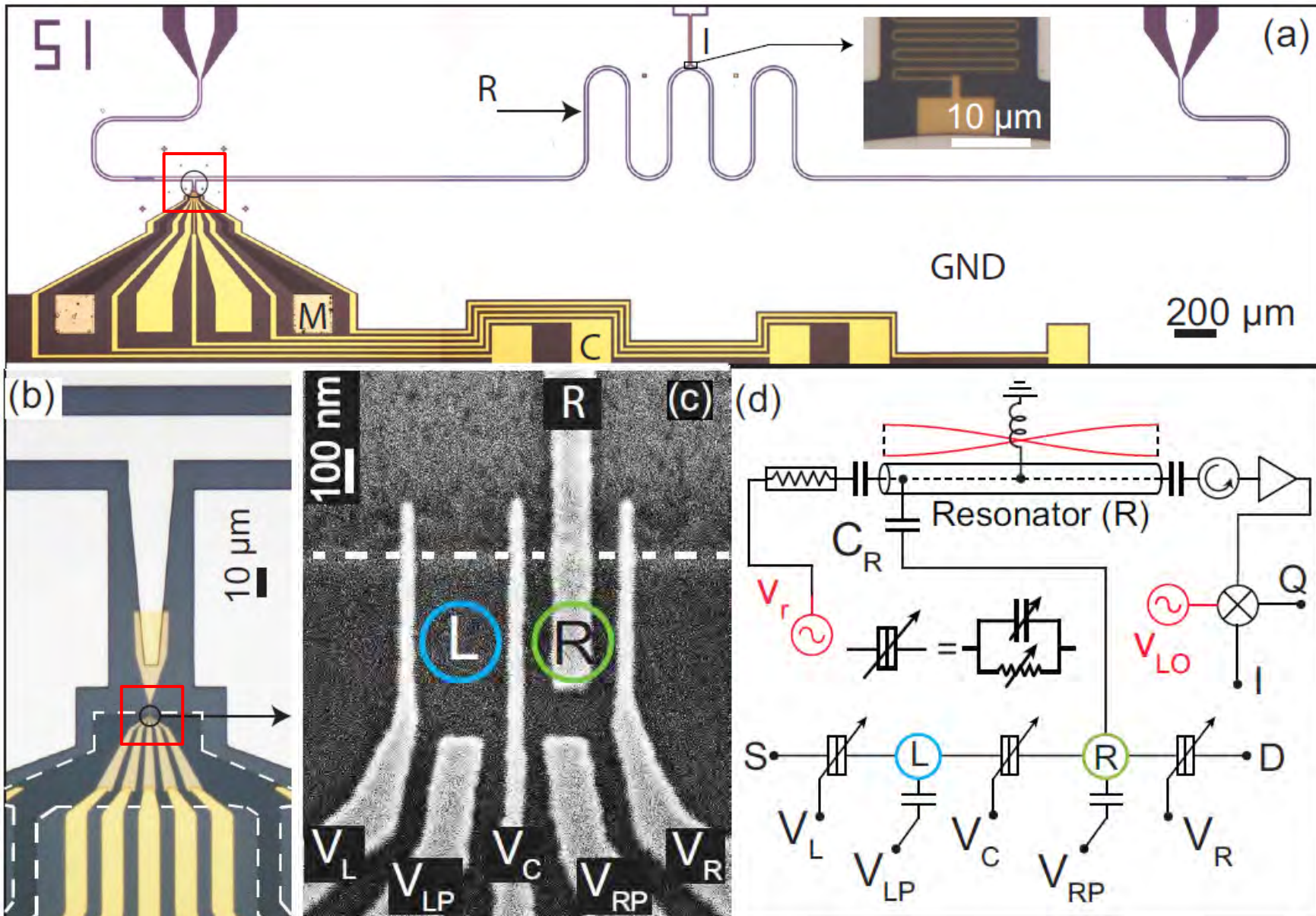
related work:

Delbecq et al., PRL 107, 256804 (2011)

Petersson et al., Nature 490, 380 (2012)

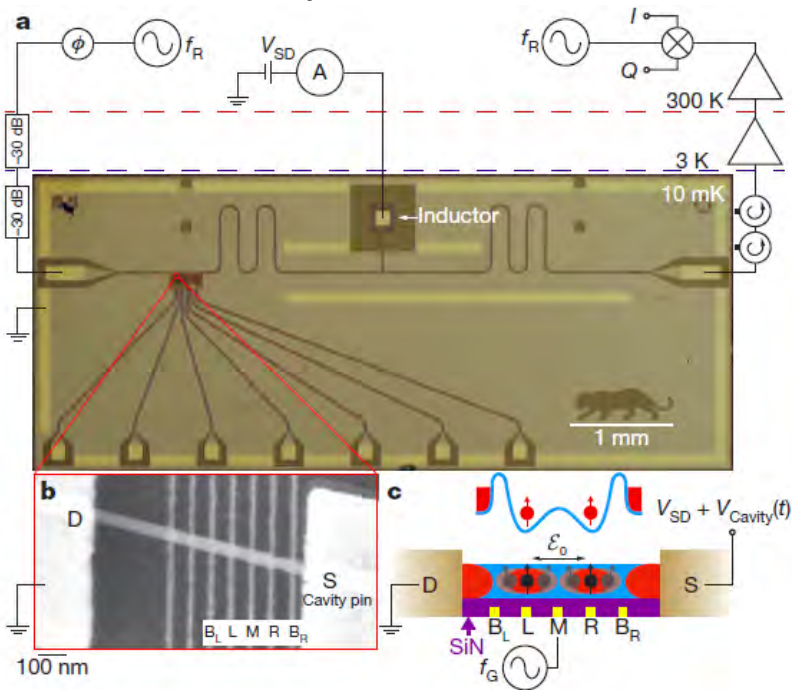
Toida et al., PRL 110, 066802 (2013)

Hybrid Quantum Dot / Circuit QED Device



Semiconductor Circuit QED Hybrid Systems

InAs nano-wire quantum dots:



K. D. Petersson et al., *Nature* 490, 380-383 (2012)

Liu et al., *PRL* 113, 036801 (2014)

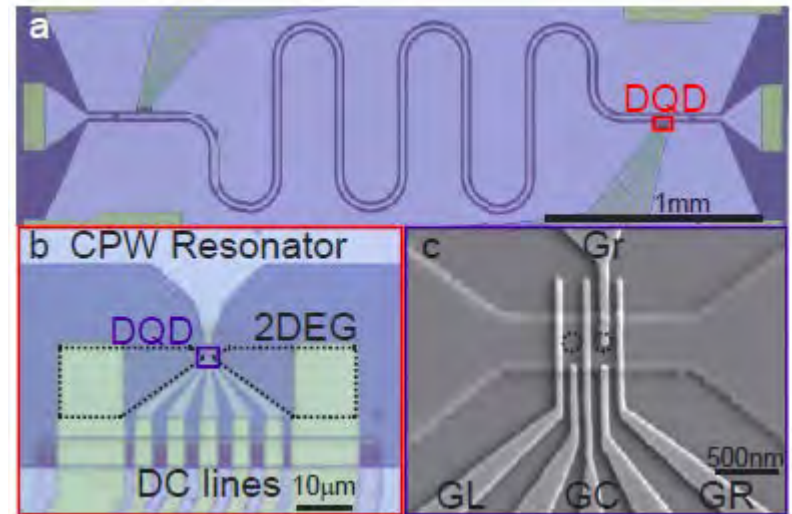
Liu et al., *Science* 347, 285-287 (2015)

Carbon nanotube quantum dots:

M. Delbecq et al., *PRL* 107, 256804 (2011)

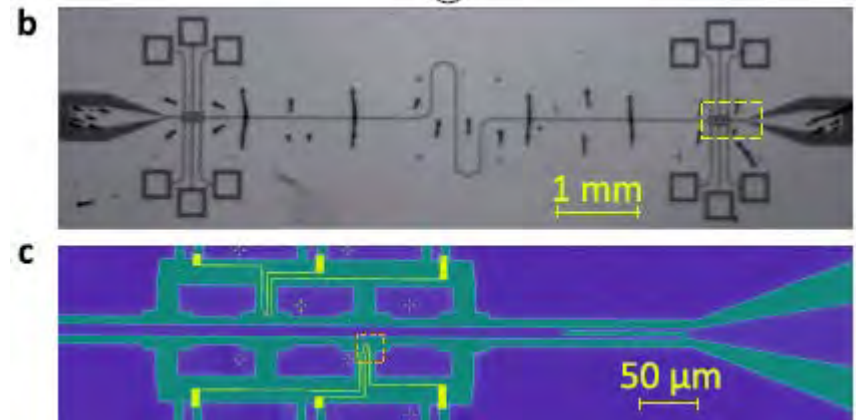
J. Viennot et al., *Science* 349, 408 (2015)

GaAs quantum dots:

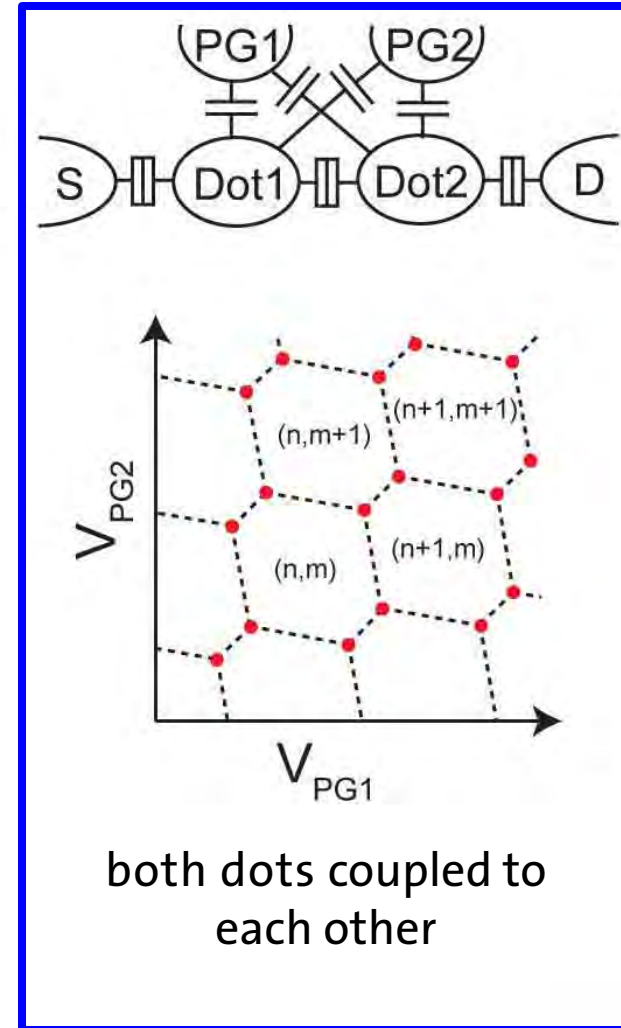
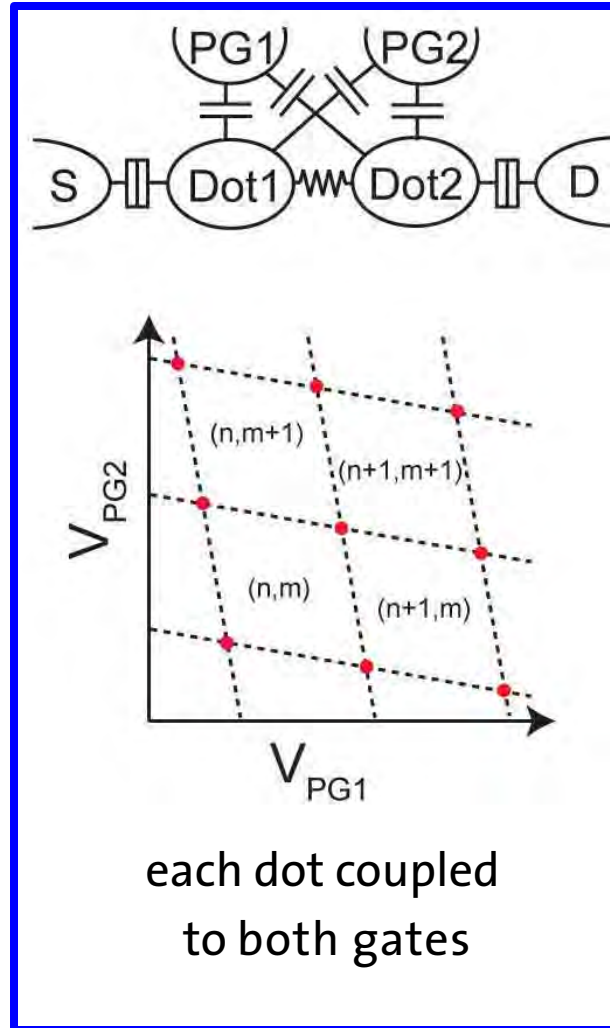
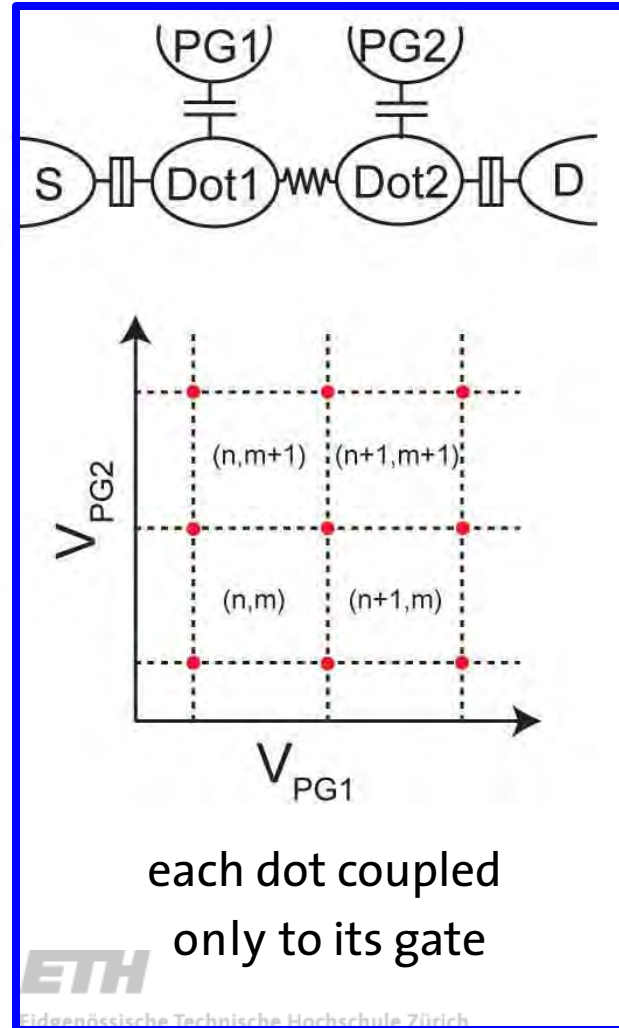
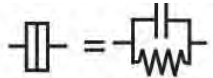


H. Toida et al., *PRL* 110, 066802 (2013)

A. Wallraff et al., *PRL* 111, 249701 (2013)



Double Dot Charge Stability Diagram



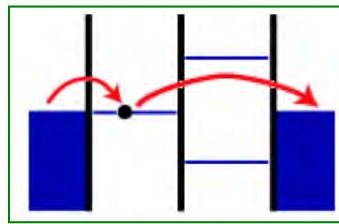
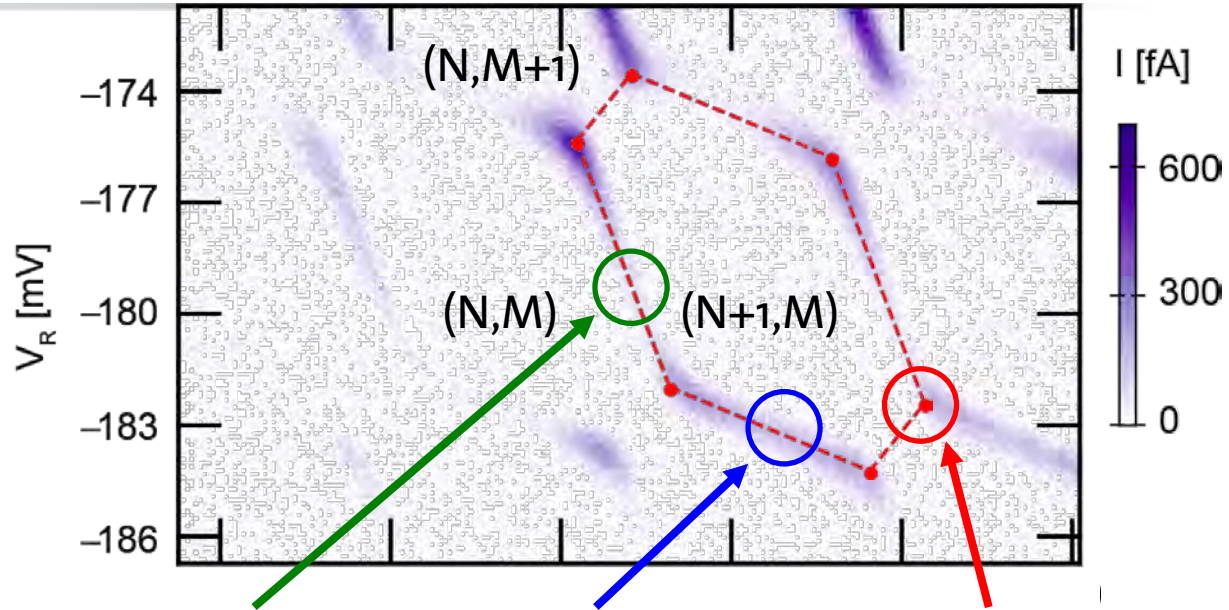
Double Dot Current and Resonator Transmission

Transport measurements:

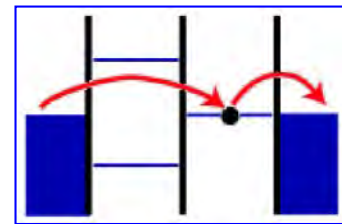
- Charging diagrams

dot properties:

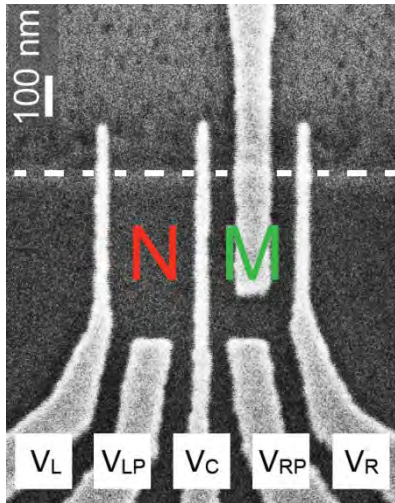
- many electron regime
- large charging energy
- consider two-level approx.



co-tunneling



sequential tunneling



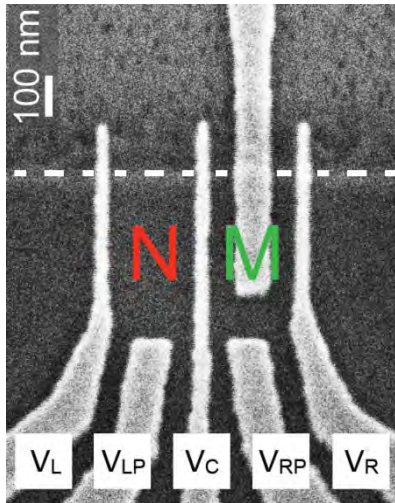
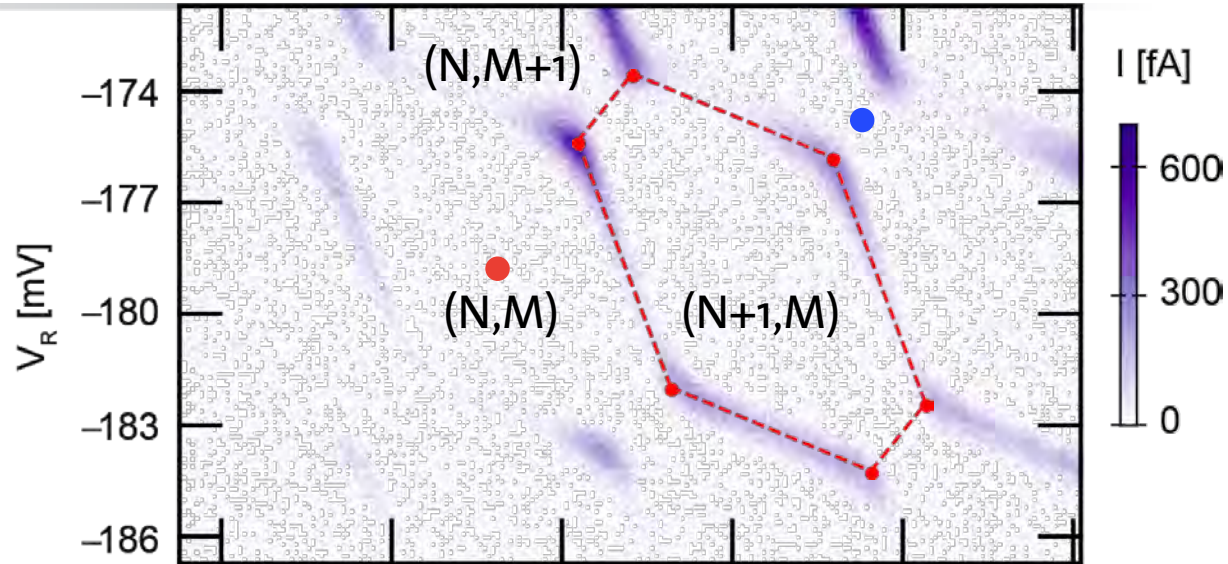
Double Dot Current and Resonator Transmission

Transport measurements:

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Double Dot Current and Resonator Transmission

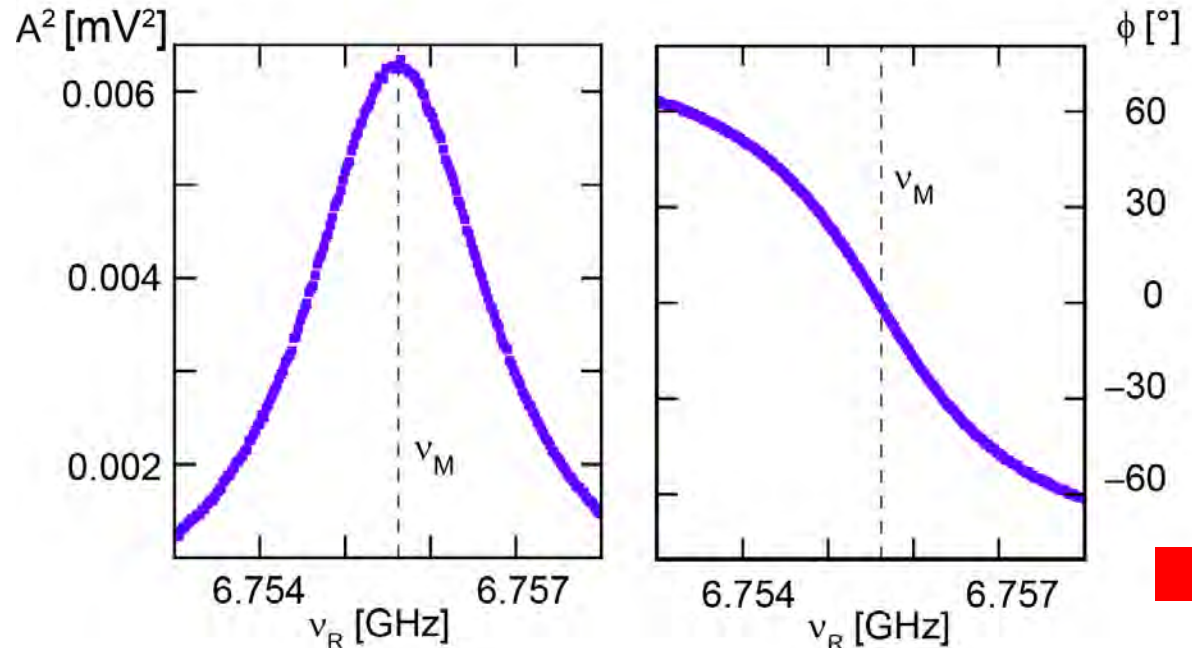
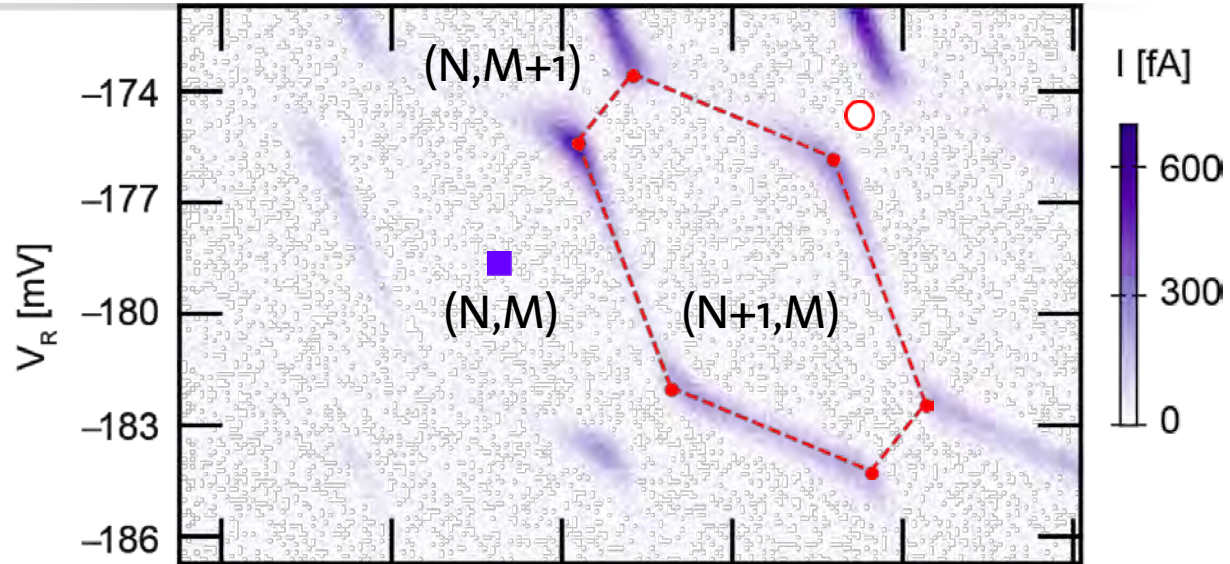
Transport measurements:

- Charging diagrams

dot properties:

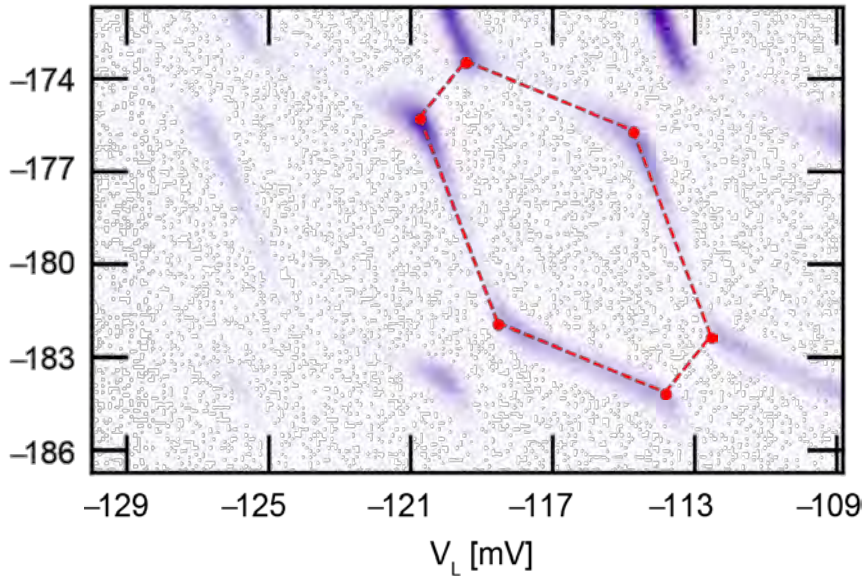
- many electron regime
- large charging energy
- consider two-level approx.

Resonator transmission:

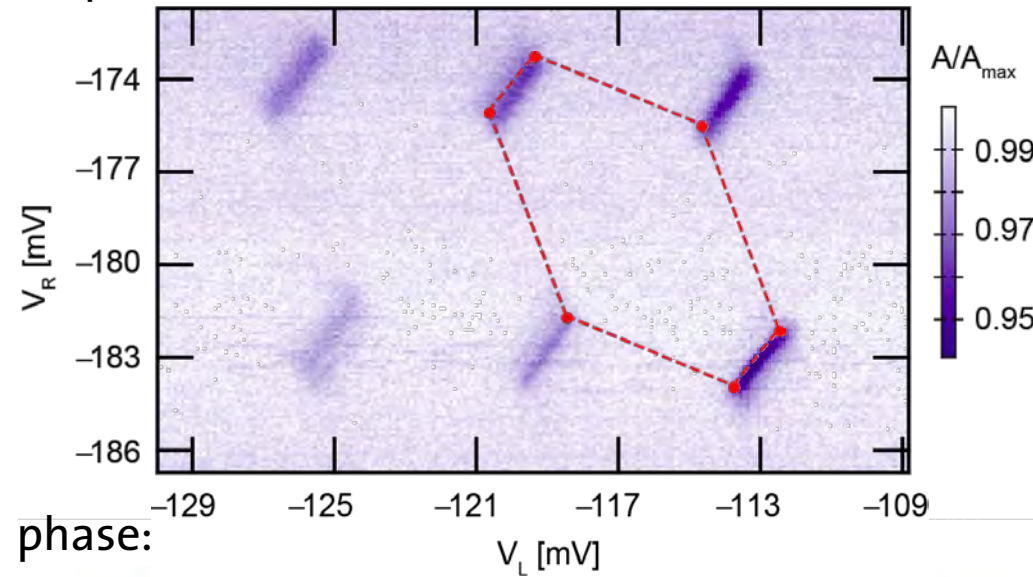


Charging Diagrams in Current, Amplitude and Phase

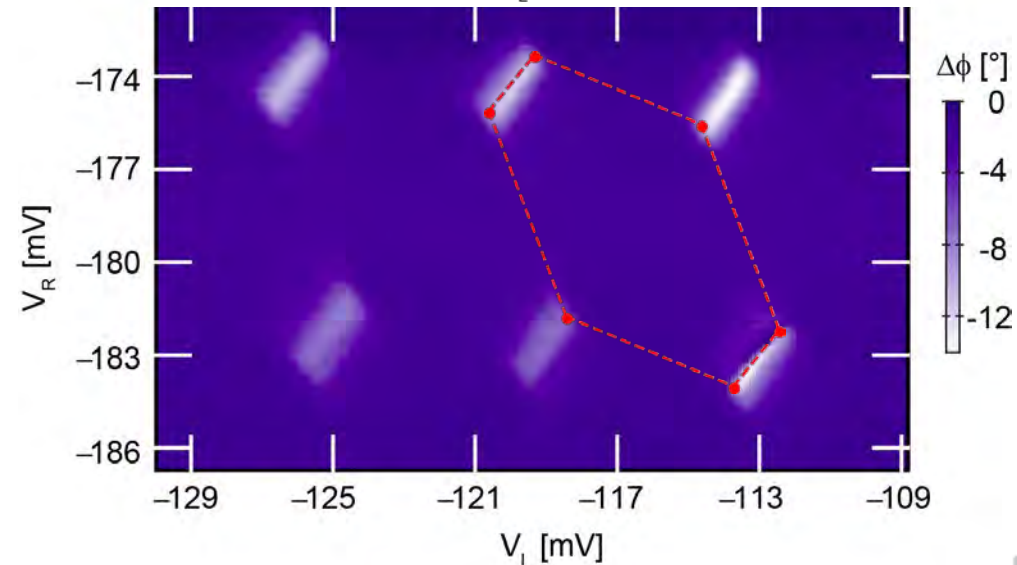
current:



amplitude:



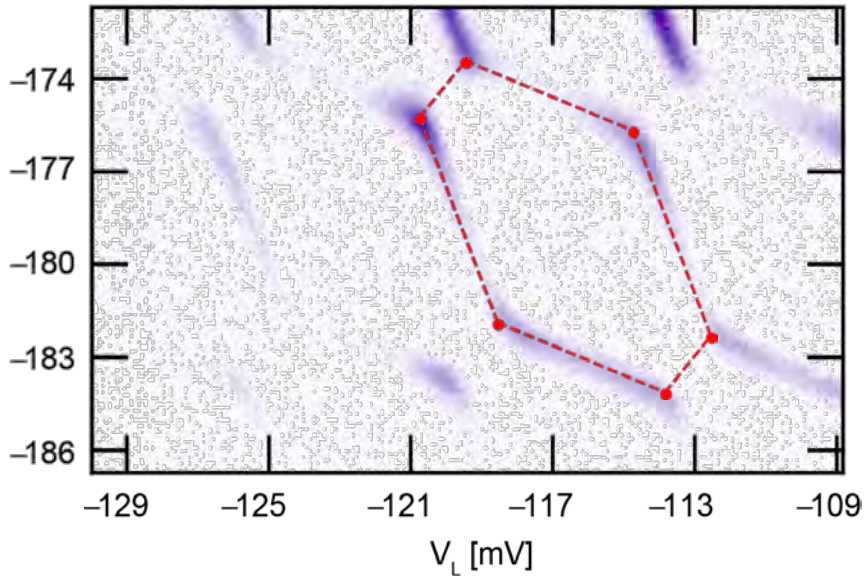
phase:



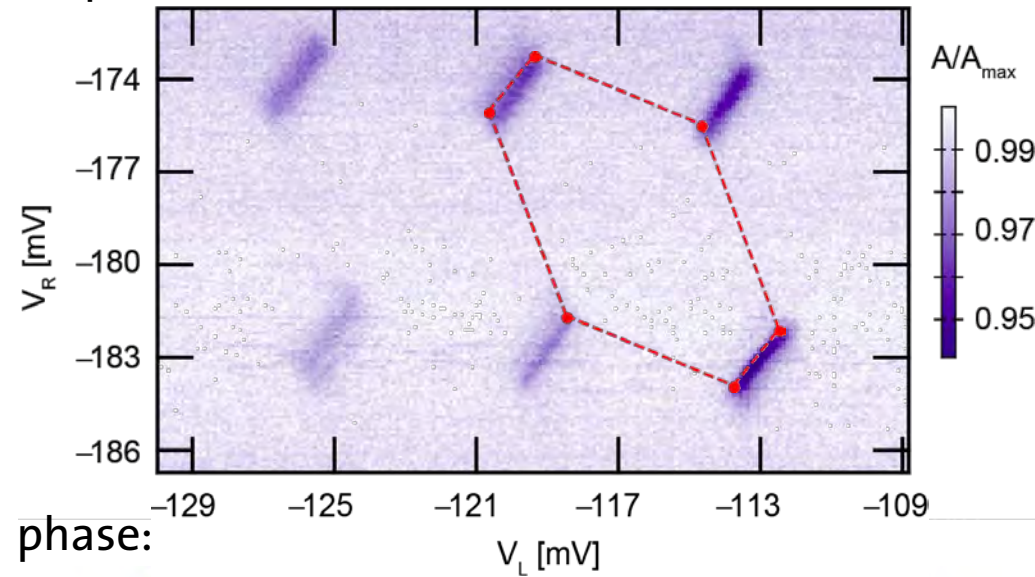
- systematic changes in transmission amplitude and phase
- equivalent charging diagrams ...
- ... but different physical origin of signal

Charging Diagrams in Current, Amplitude and Phase

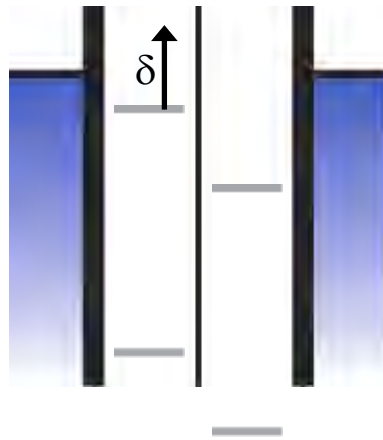
current:



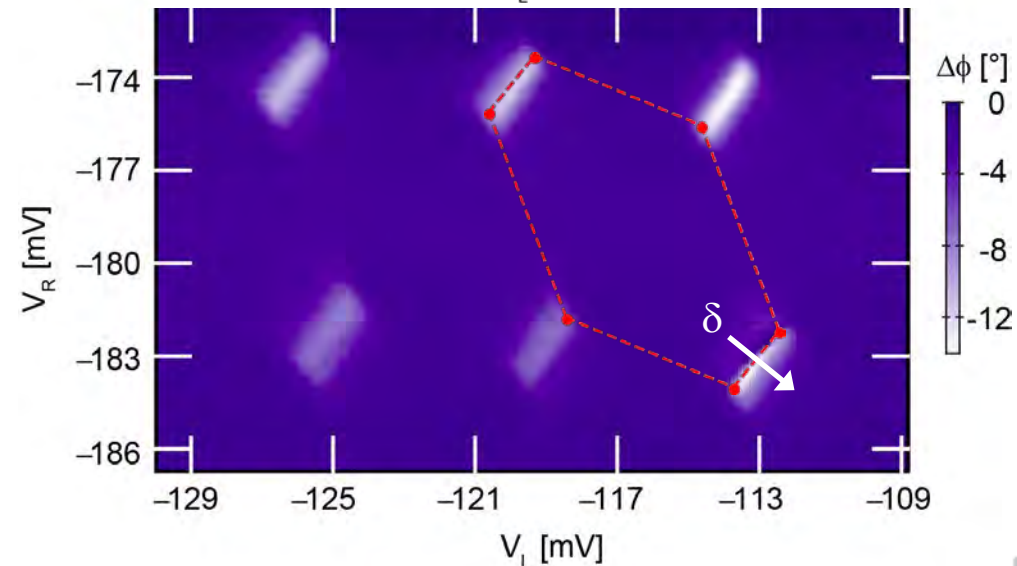
amplitude:



detuning δ :

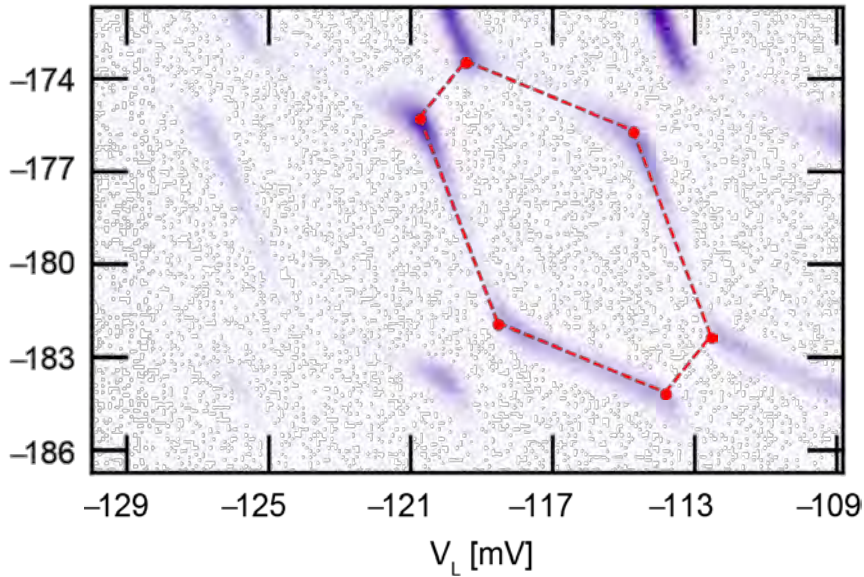


phase:

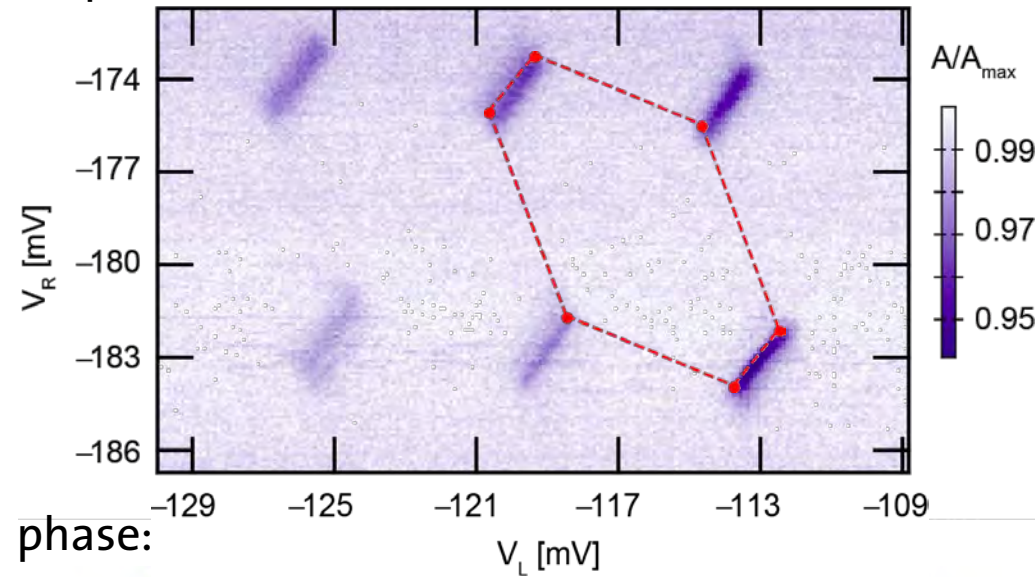


Charging Diagrams in Current, Amplitude and Phase

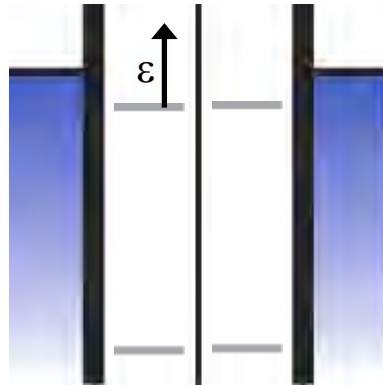
current:



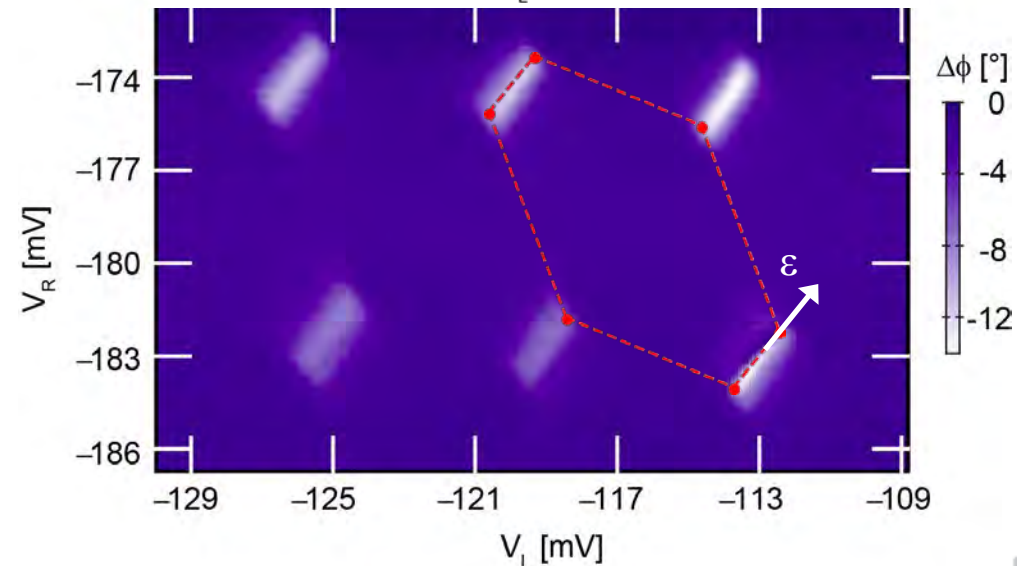
amplitude:



total energy ε :

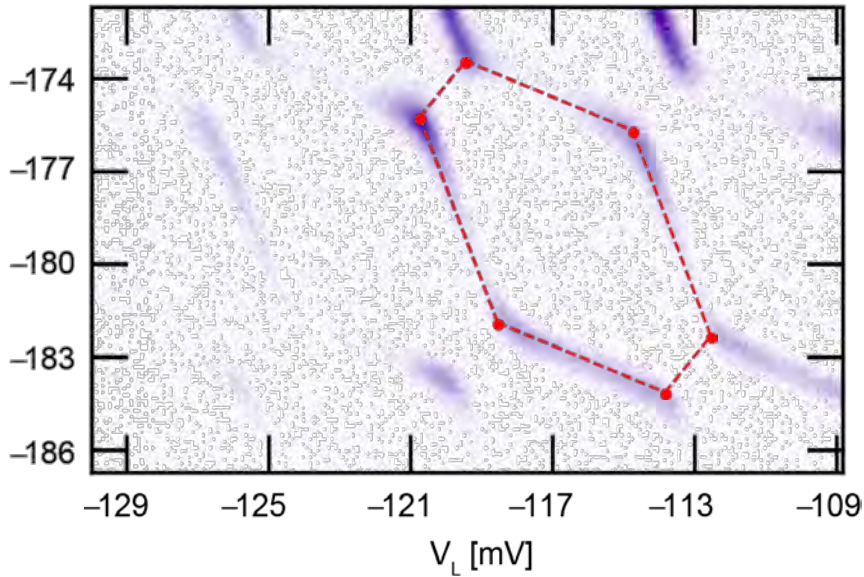


phase:

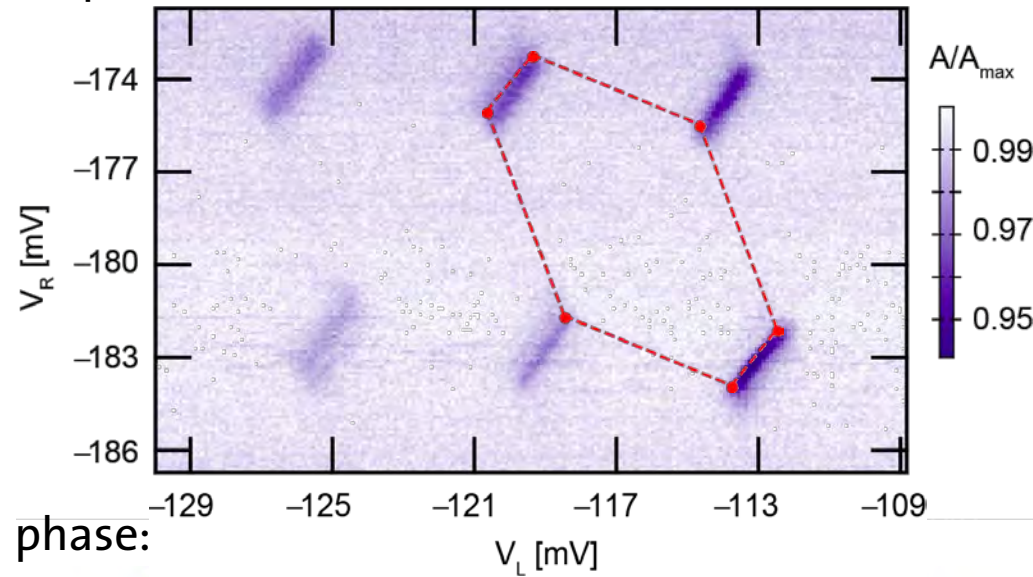


Charging Diagrams in Current, Amplitude and Phase

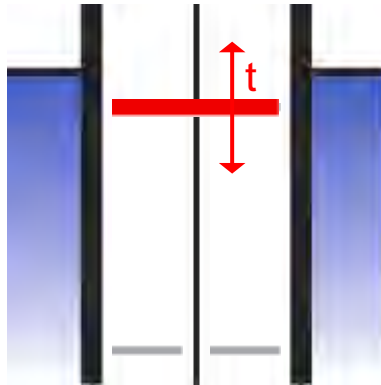
current:



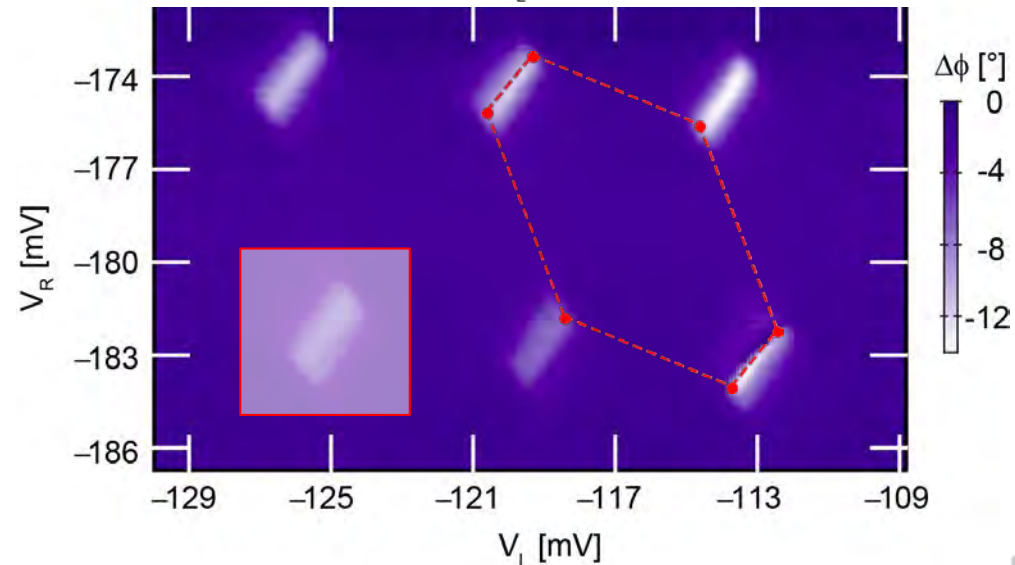
amplitude:



tunnel coupling t :

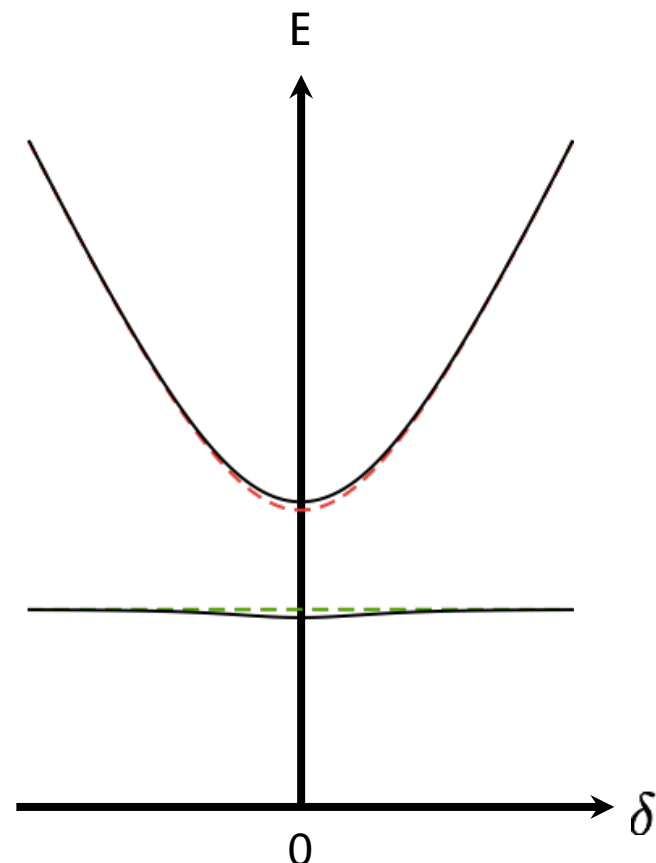
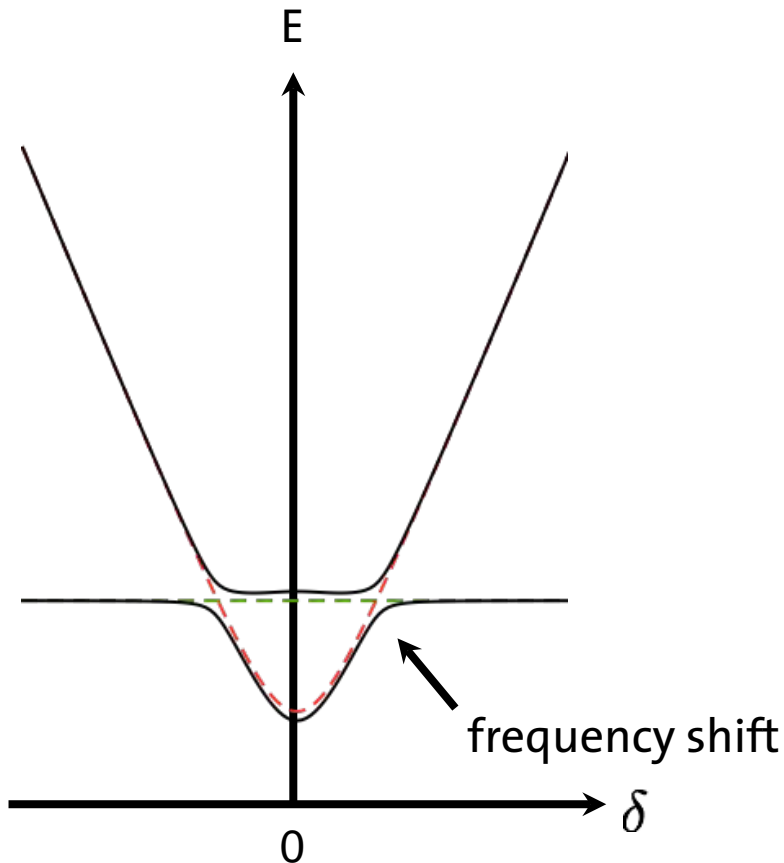


phase:



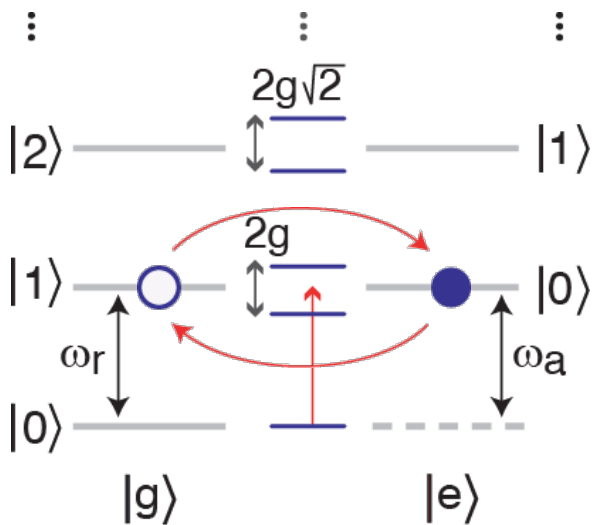
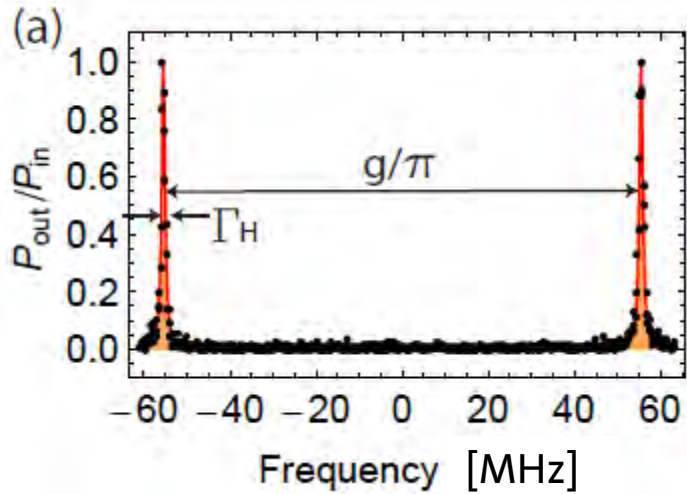
Model of the Coupled Resonator–Dot System

$$H = \underbrace{h\nu_0\left(\hat{n} + \frac{1}{2}\right)}_{\text{resonator}} + \underbrace{\frac{h\nu_q}{2}\hat{\sigma}_z}_{\text{qubit}} + \underbrace{\hbar g \sin \theta (\hat{a}^\dagger \hat{\sigma}^- + \hat{a} \hat{\sigma}^+)}_{\text{coupling}}$$

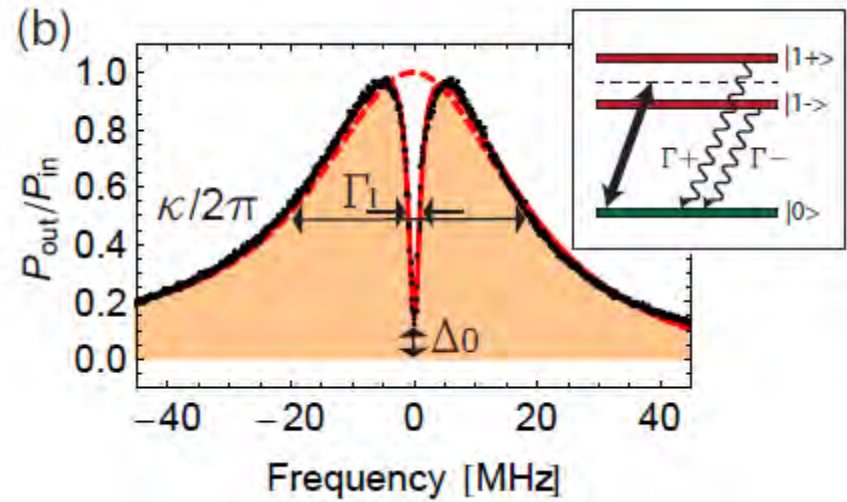


Regimes of Resonant Circuit/Cavity QED

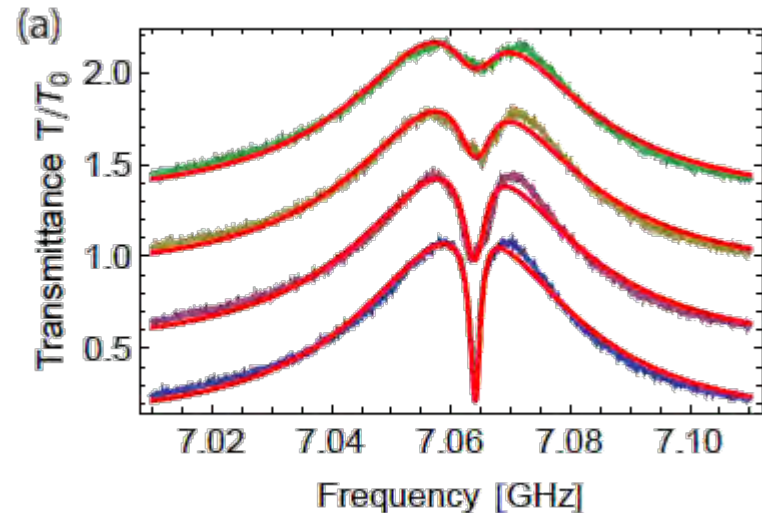
- strong coupling limit ($g > \kappa, \gamma$)



- bad (or fast) cavity limit ($\kappa > g > \gamma$)

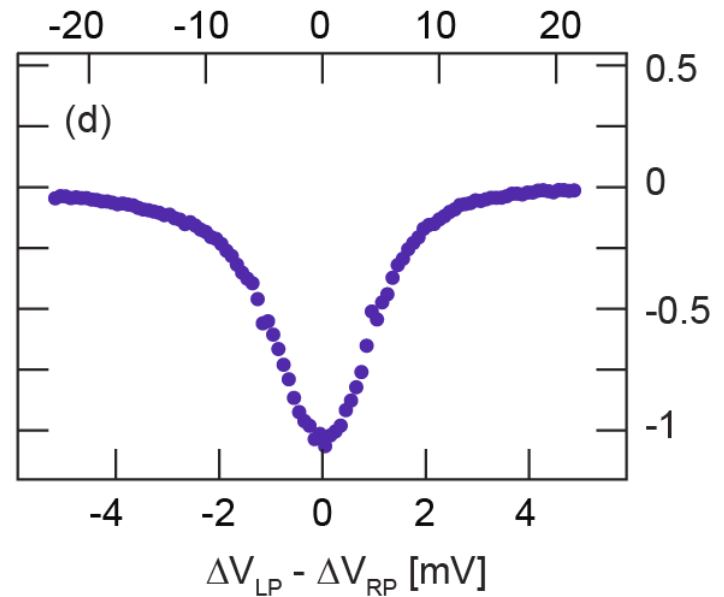
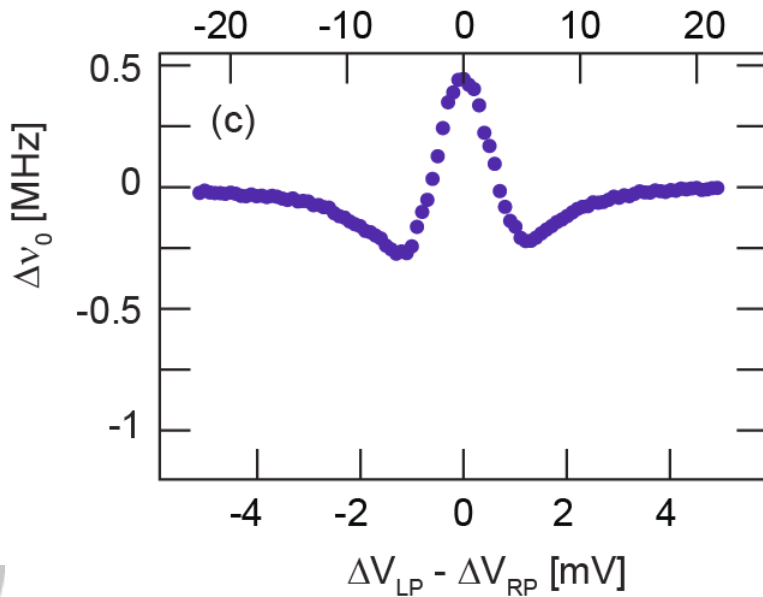
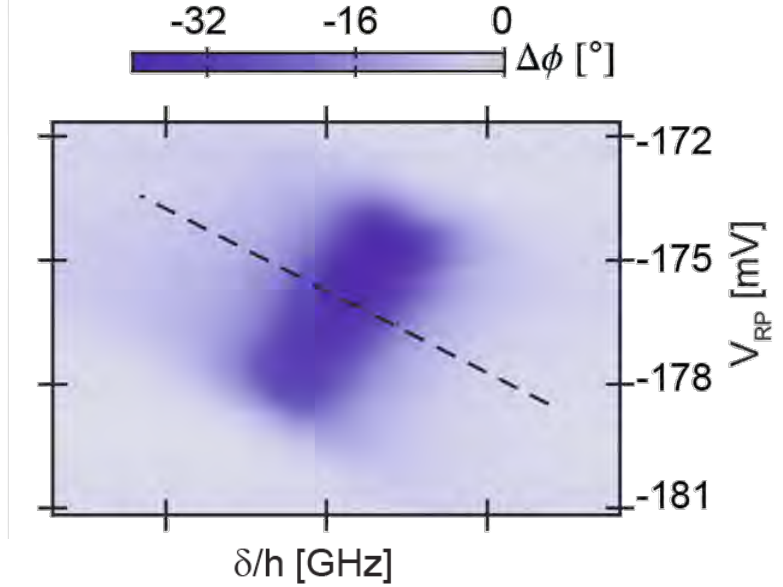
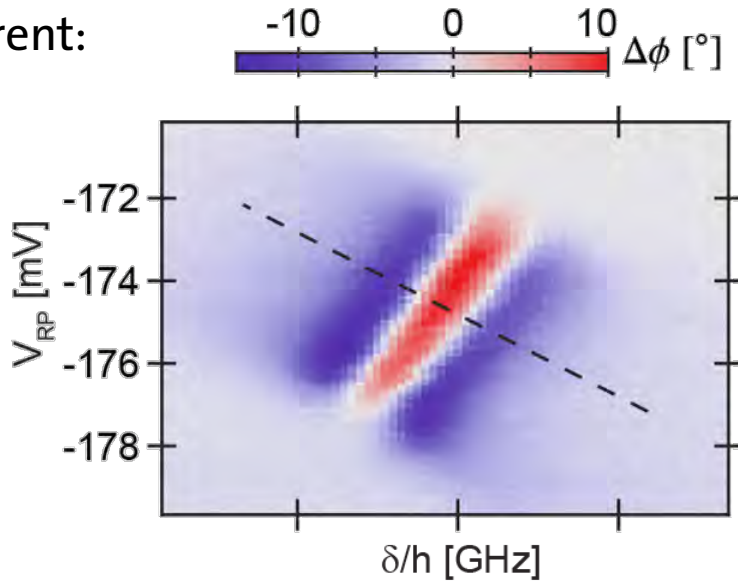


- weak coupling ($\kappa, \gamma > g$)



Resonator/Double-Dot Interaction

current:

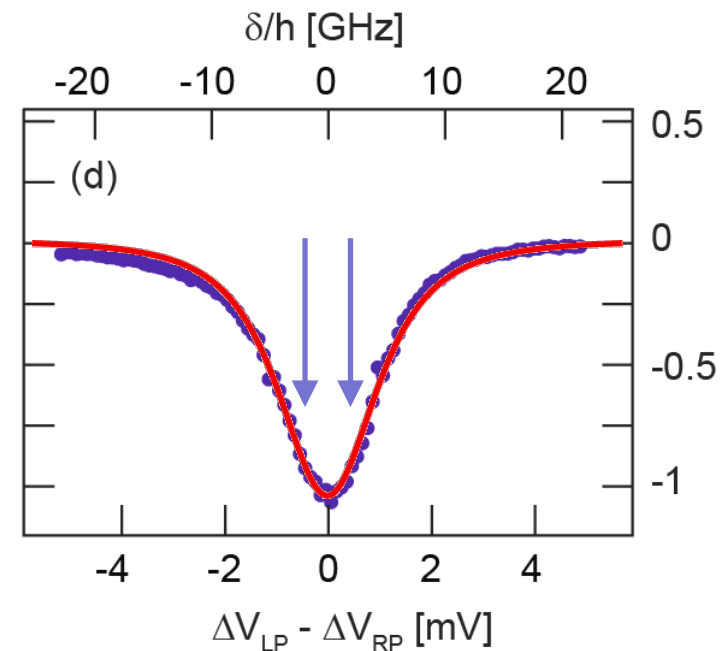
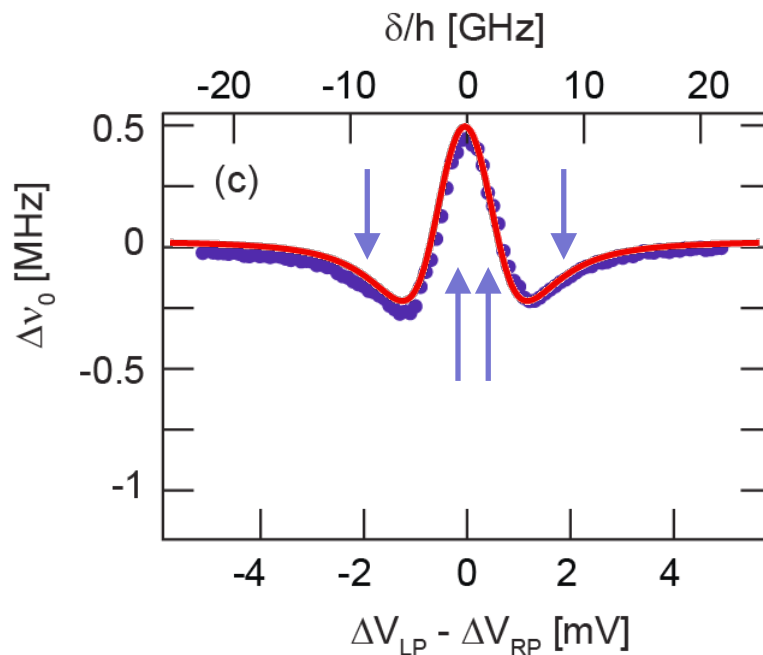


Quantitative Evaluation of Dipole-Coupling

$$H = \underbrace{h\nu_0(\hat{n} + \frac{1}{2})}_{\text{resonator}} + \underbrace{\frac{h\nu_q}{2}\hat{\sigma}_z}_{\text{qubit}} + \underbrace{\hbar g \sin \theta(\hat{a}^\dagger \hat{\sigma}^- + \hat{a}\hat{\sigma}^+)}_{\text{coupling}}$$

Coupling strength $2t/h = 6.1$ GHz
 $g/2\pi = 50$ MHz $\gamma_\phi/2\pi = 3.3$ GHz

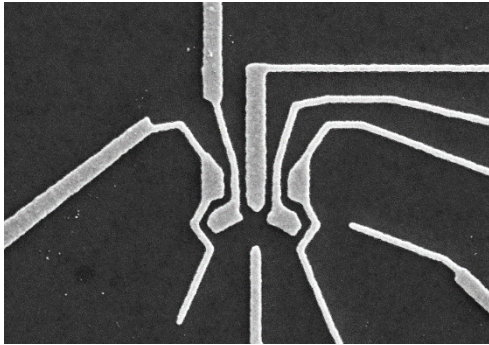
$2t/h = 9.0$ GHz
 $\gamma_\phi/2\pi = 0.9$ GHz



Single-Electron Regime

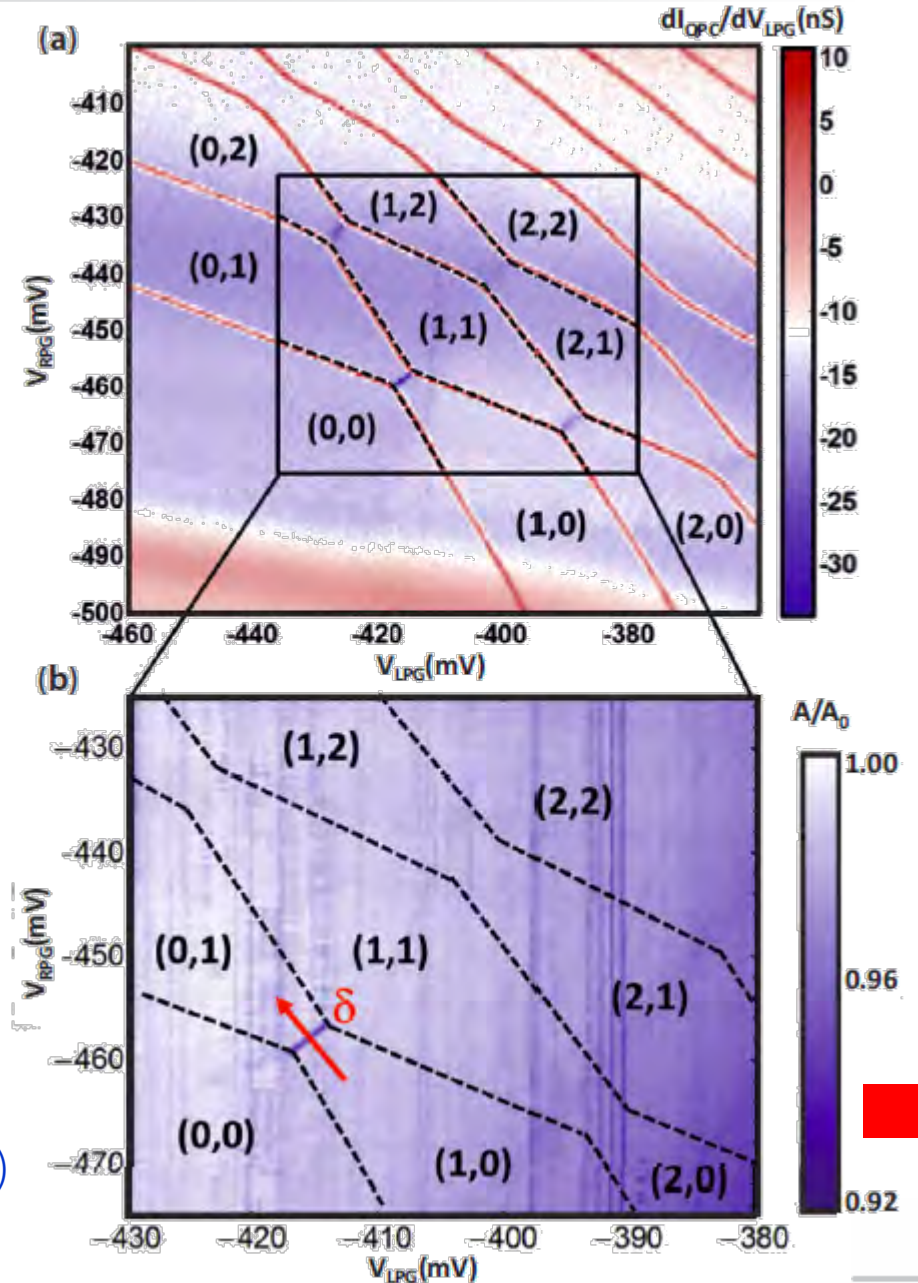
Optimized gate geometry for single electron regime of DQD coupled to resonator

- Expectation: improved coherence



However:

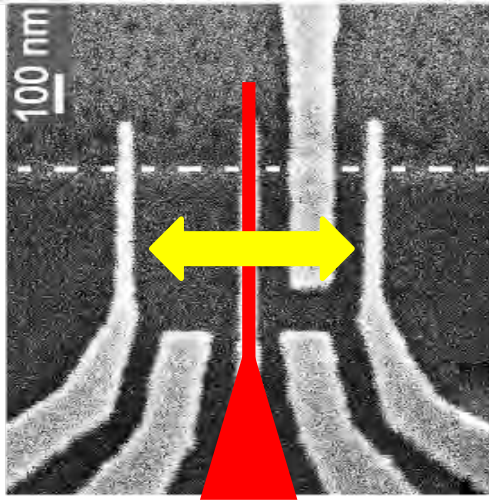
- same large dephasing ($\gamma \gg g$)
- similar dephasing rates in many (all?) other hybrid DQD experiments independent of material



J. Basset *et al.*, *Phys. Rev. B* 88, 125312 (2013)

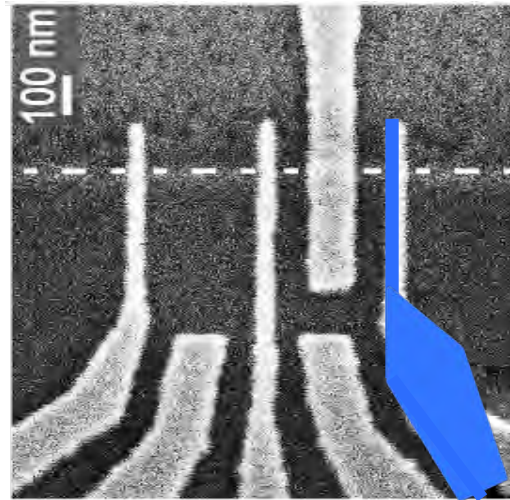
Quantum Dot Bias Regimes

tunnel coupling
between dots



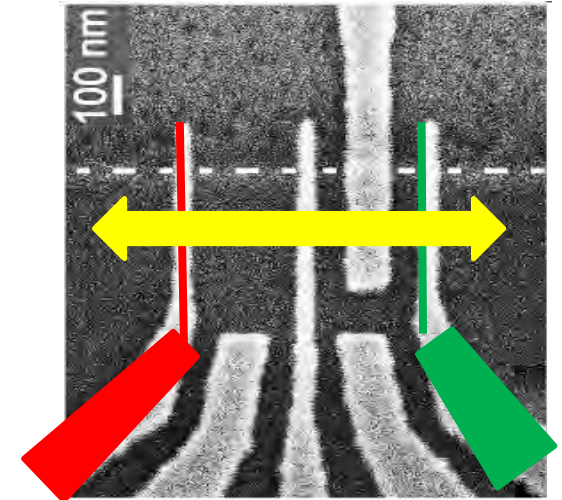
- tunnel coupling (t) similar to resonator frequency
- coupling to leads (Γ) small

tunnel coupling
between lead and dot



- coupling to leads (Γ) similar to resonator frequency
- tunnel coupling (t) small

tunnel coupling to
both leads

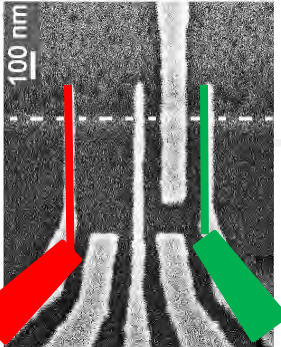


- coupling to leads (Γ) similar tunnel coupling (t) similar to resonator frequency



Investigation of tunnel coupling to leads at GHz frequencies: [T. Frey et al., PRB 86, 115303 \(2012\)](#)

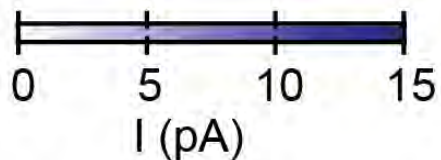
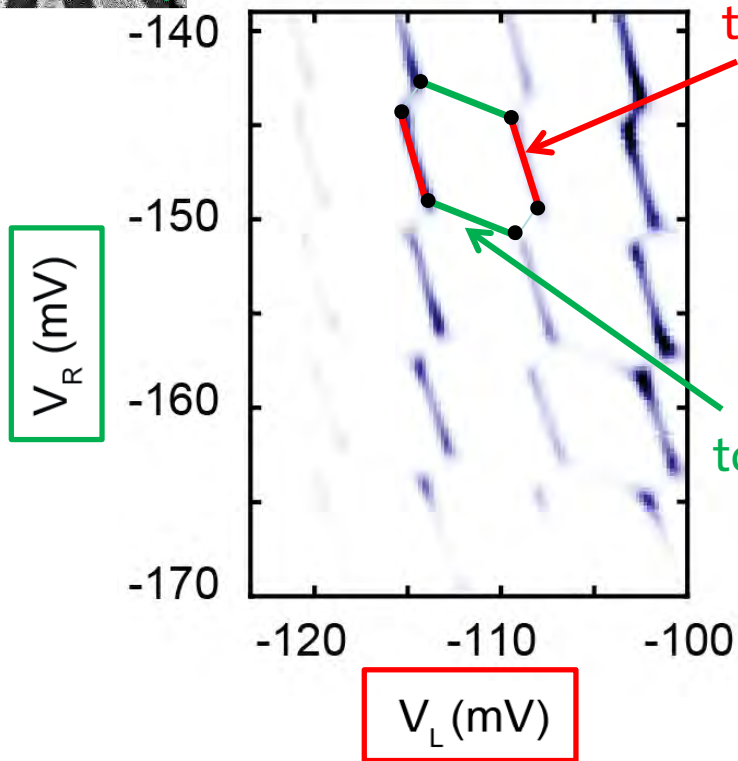
Charge Stability Diagram



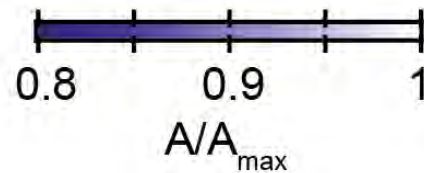
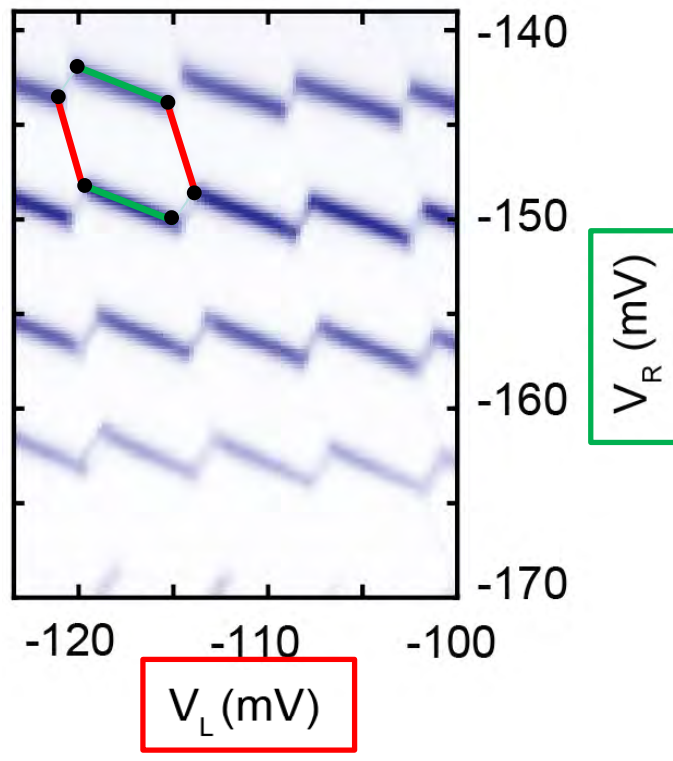
Direct Current

Resonance
to the left lead

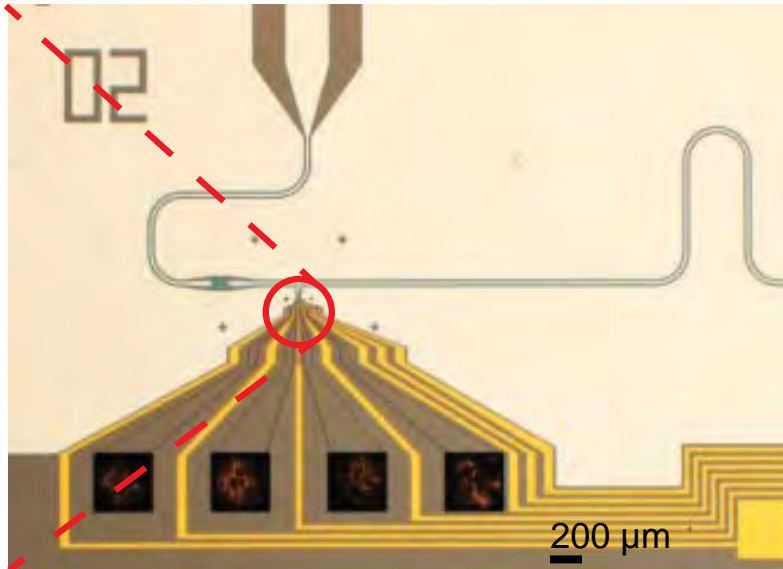
Resonance
to the right lead



Microwave Amplitude



Improved Cavity-Coupled GaAs Double Quantum Dot



Device design:

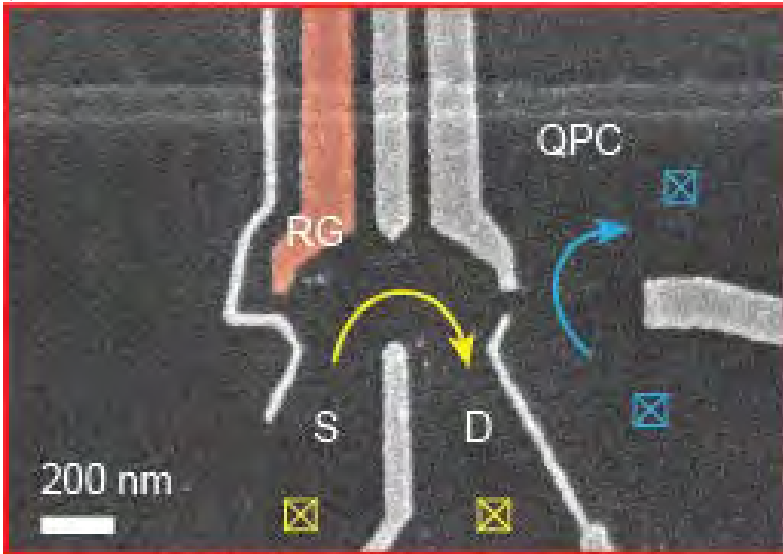
- iterated from previous versions
[T. Frey *et al.*, PRL 108, 046807 \(2012\)](#)
- cavity frequency $\nu \sim 6.85$ GHz ($28 \mu\text{eV}$)
- QD charging energies $E_c \sim 200$ GHz (1 meV)

improved charge coherence properties

- $\gamma_\phi \sim 200$ MHz
- previously several GHz

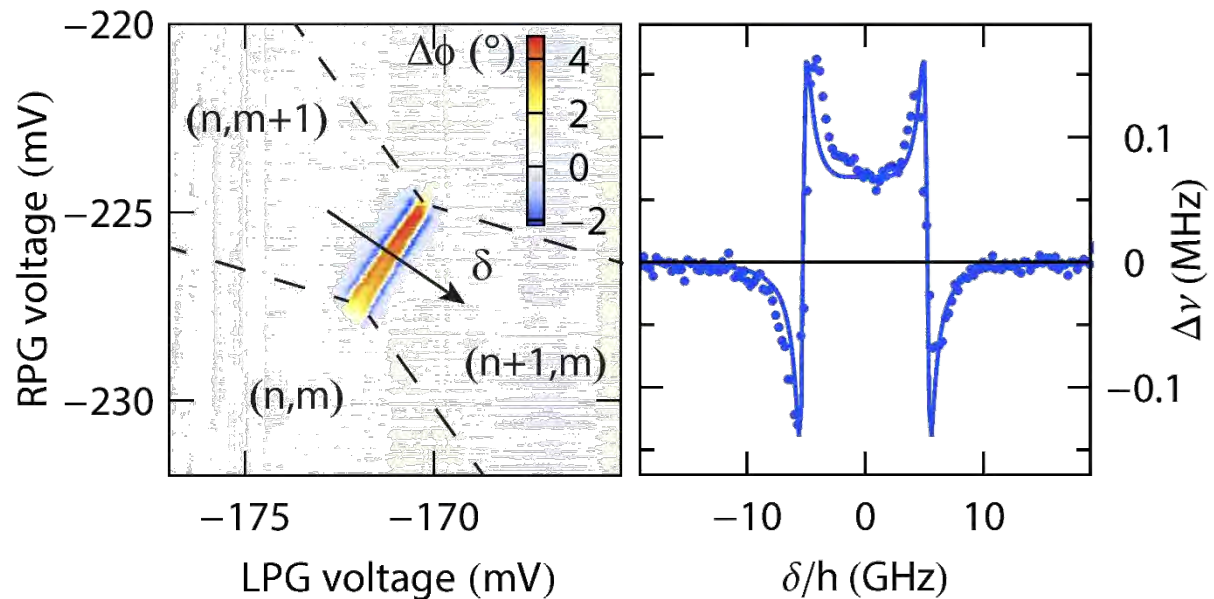
likely affected by:

- reduced overlap between gates and 2DEG
- different wafer material
- improved filtering



Device Characterization

dispersive resonator
shift versus QD bias:



parameters:

- constant cavity coupling strength $g \sim 13$ MHz
- adjustable inter-dot coupling $t \sim 1$ to 10 GHz
- adjustable inter-dot detuning $\delta \sim 0$ to 100's GHz
- approx. energy relaxation rate $\gamma_1 \sim 100$ MHz
- dephasing rate $\gamma_\phi \sim 0.2$ to 1.2 GHz (depending on bias)
- approx. # charges $(n, m) \sim 10$

Radiation Emission Experiments: Motivation

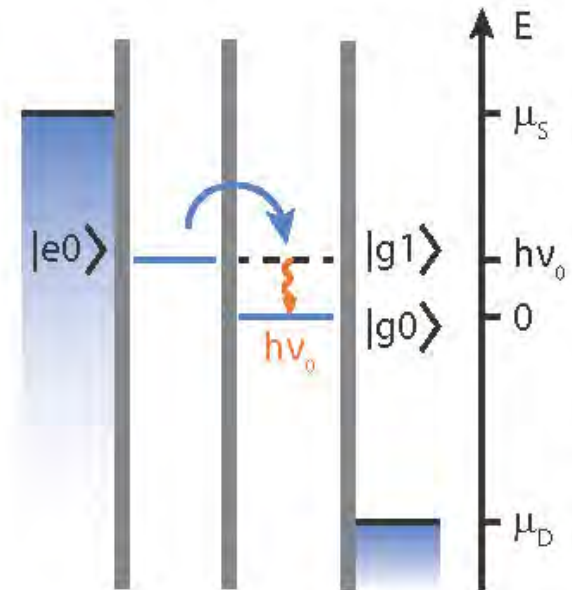
- explore radiation emission from semiconductor nanostructure
- investigate correlations between charge transport and radiation emission
- characterize inelastic tunneling processes

Approach:

- voltage bias DQD
- adjust DQD energy levels
- detect emitted radiation

Use techniques known from circuit QED:

- sensitive parametric amplifiers
- quadrature amplitude measurements
- power measurements
- correlation function measurements

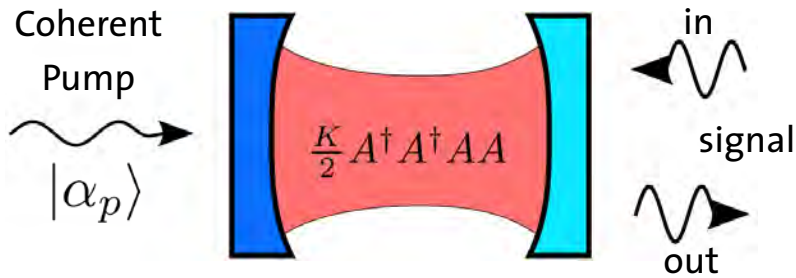


A. Stockklauser *et al.*, *Phys. Rev. Lett.* 115, 046802 (2015)

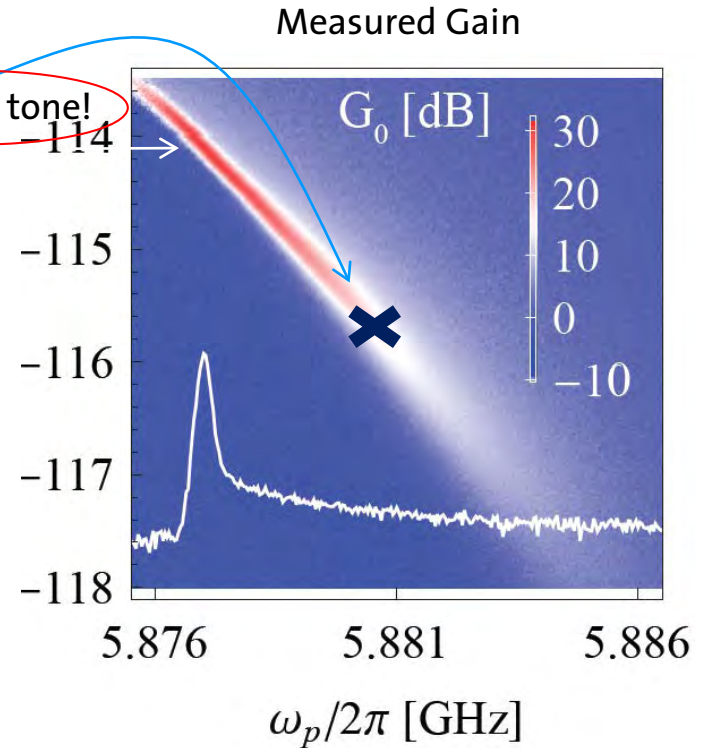
Related work on radiation emission and micro-maser action

Liu *et al.*, *PRL* 113, 036801 (2014), *Science* 347, 285-287 (2015)

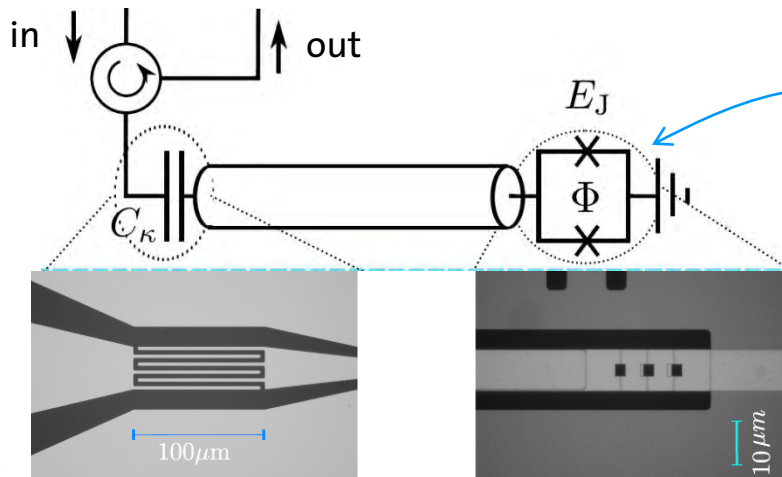
Parametric Amplifier



fix pump tone!



Circuit QED implementation:



SQUID provides nonlinearity!

Caves, *Phys. Rev. D* 26, 1817 (1982)

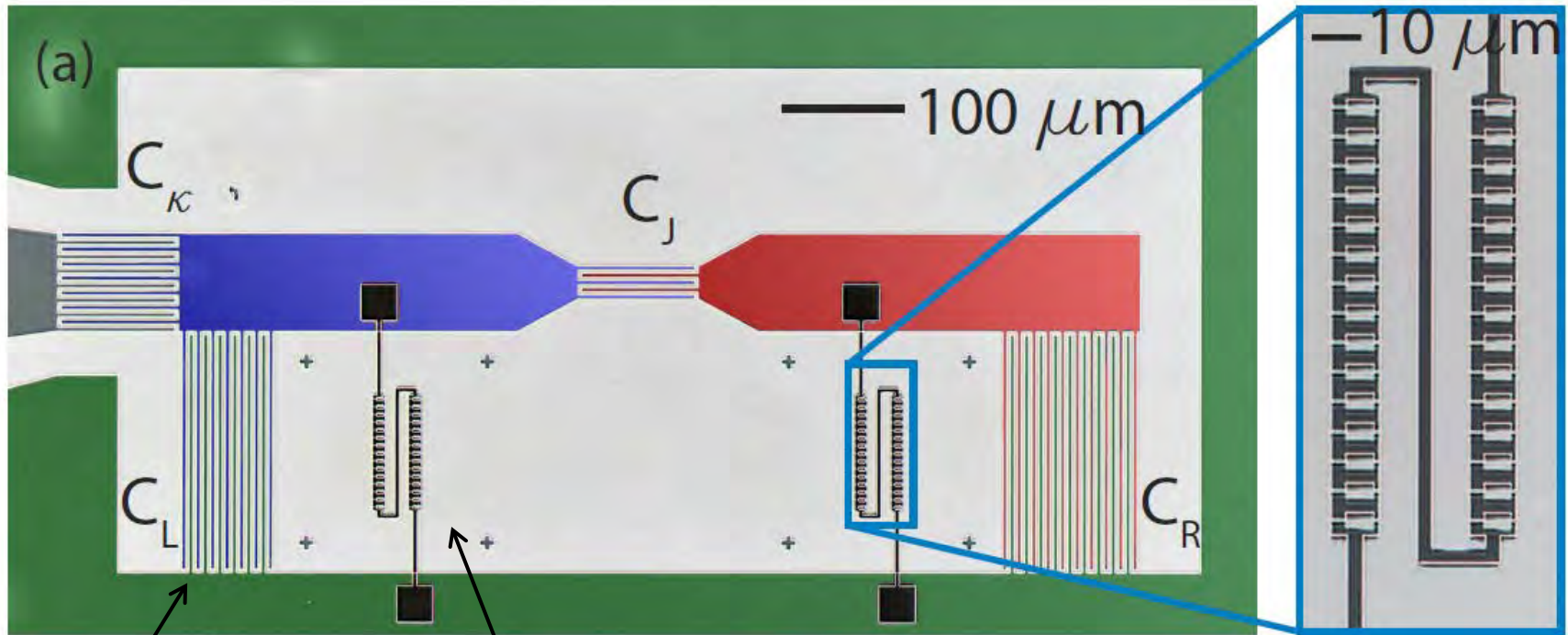
Yurke and Buks, *J. Lightwave Tech.* 24, 5054 (2006)

Castellanos-Beltran et al., *Nat. Phys.* 4, 929 (2008)

Eichler et al., *Phys. Rev. Lett.* 107, 113601 (2011)



JPD amplifier: implementation



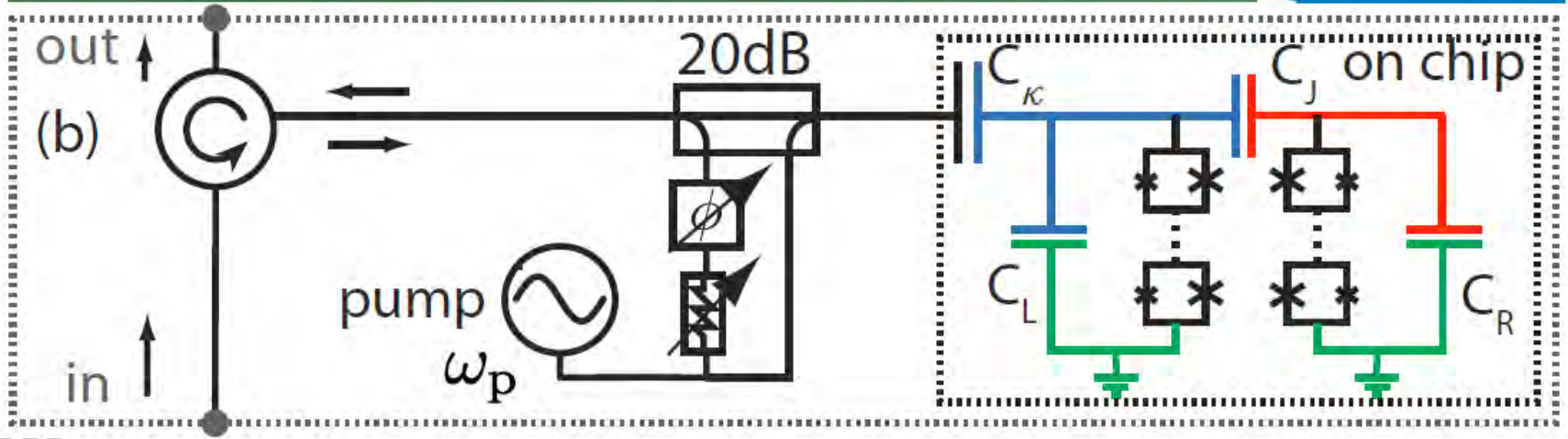
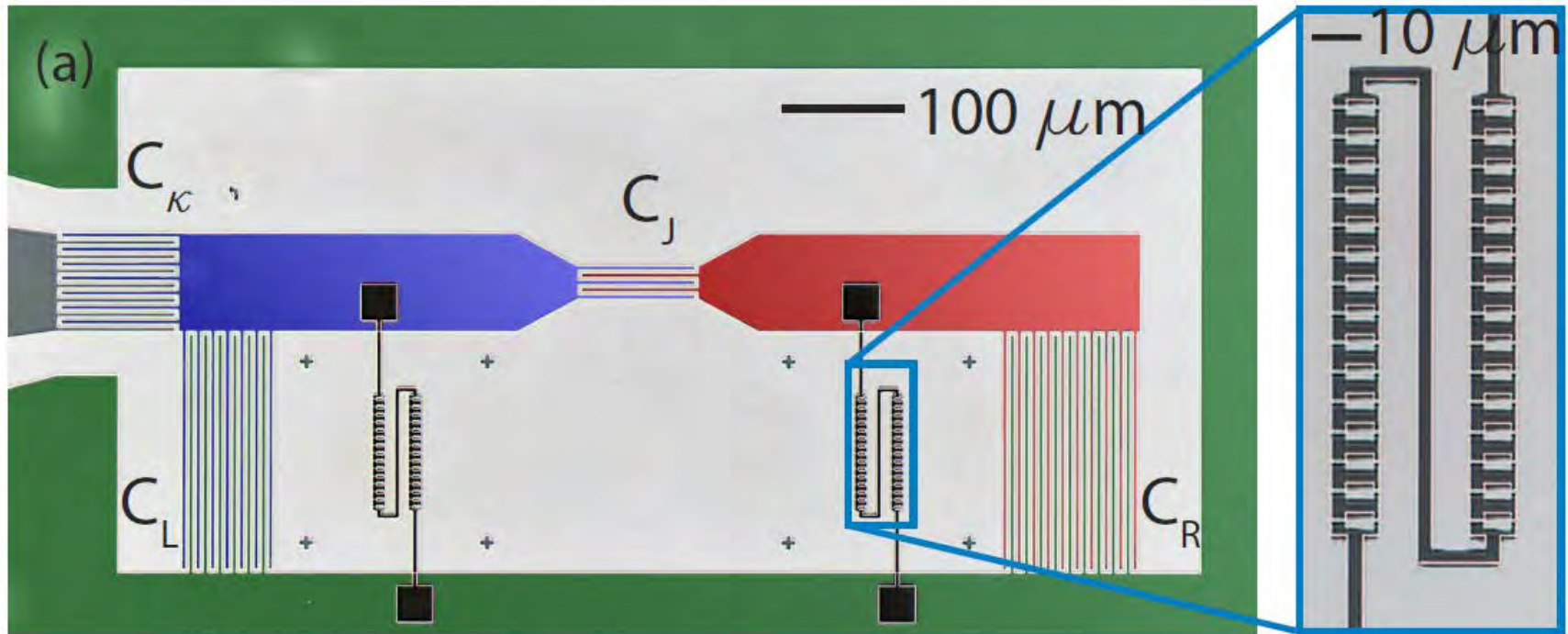
finger
capacitor

array of
SQUIDs

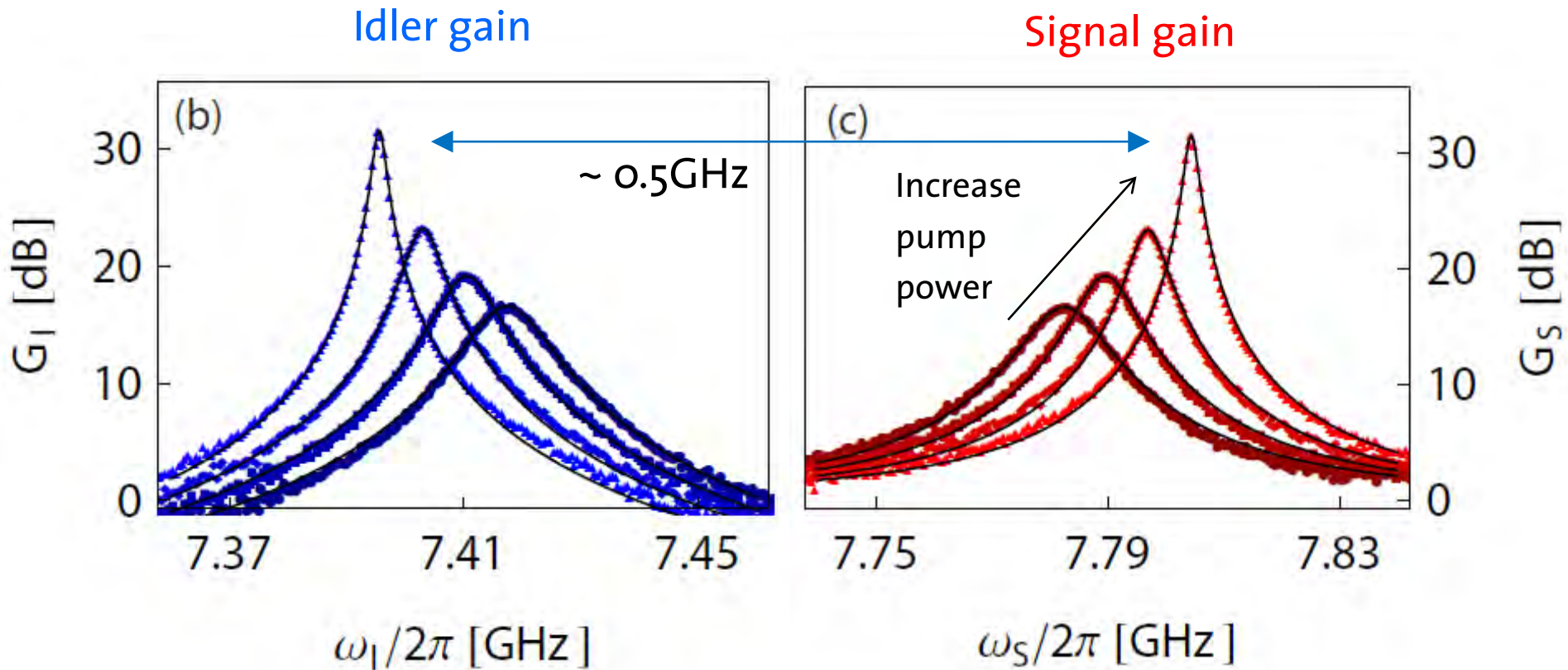
Features:

- Arrays with M SQUIDs to control nonlinearity: $U \sim E_c/M^2$
- asymmetric SQUIDs \rightarrow homogeneous coupling to external flux

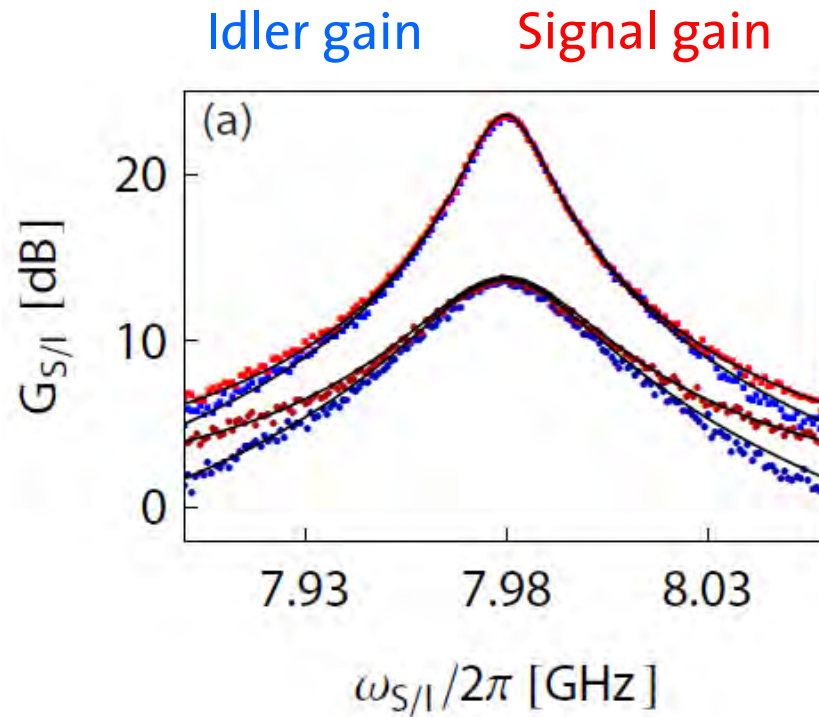
JPD amplifier: implementation



JPD amplifier: non-degenerate operation



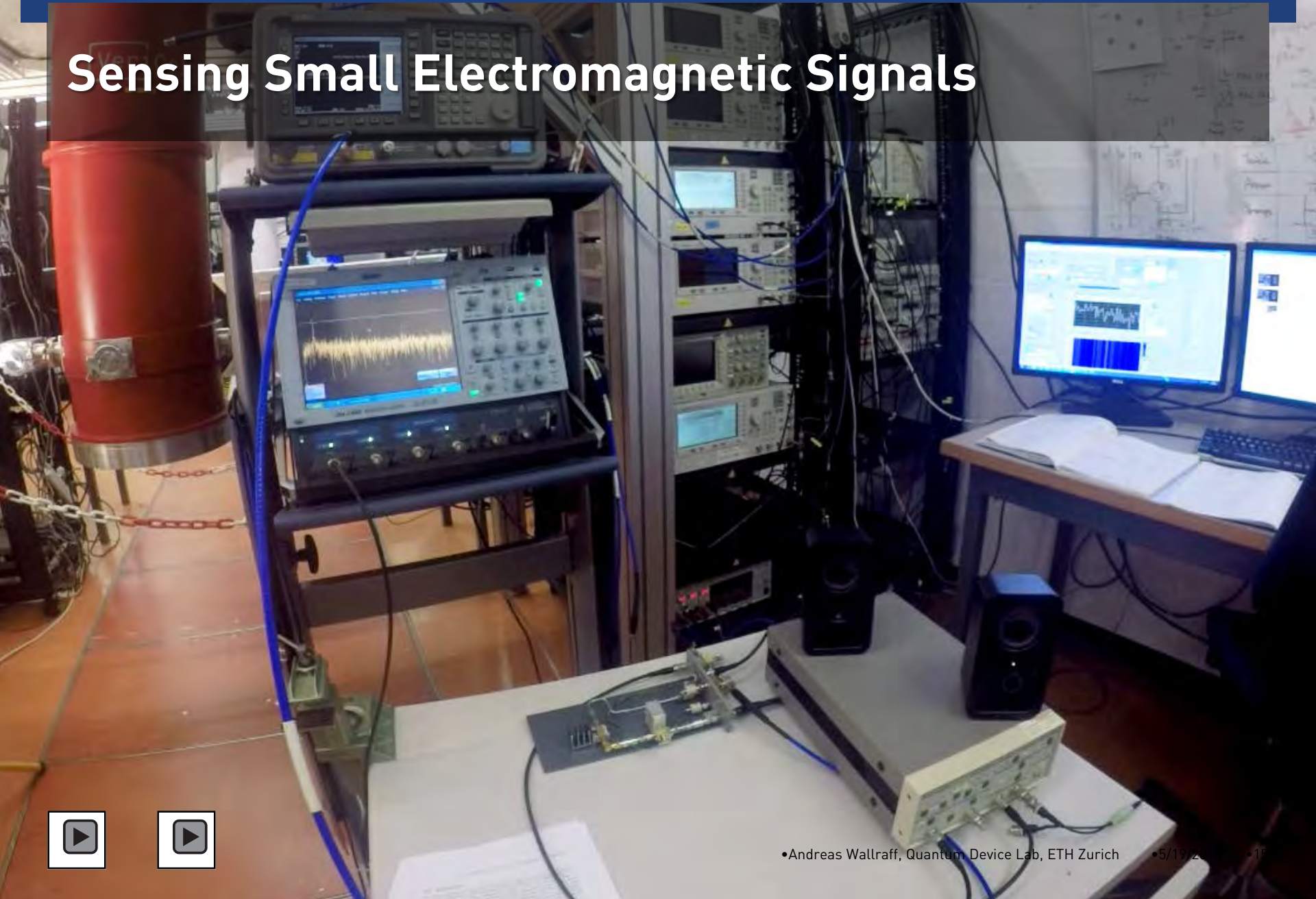
JPD amplifier: degenerate operation



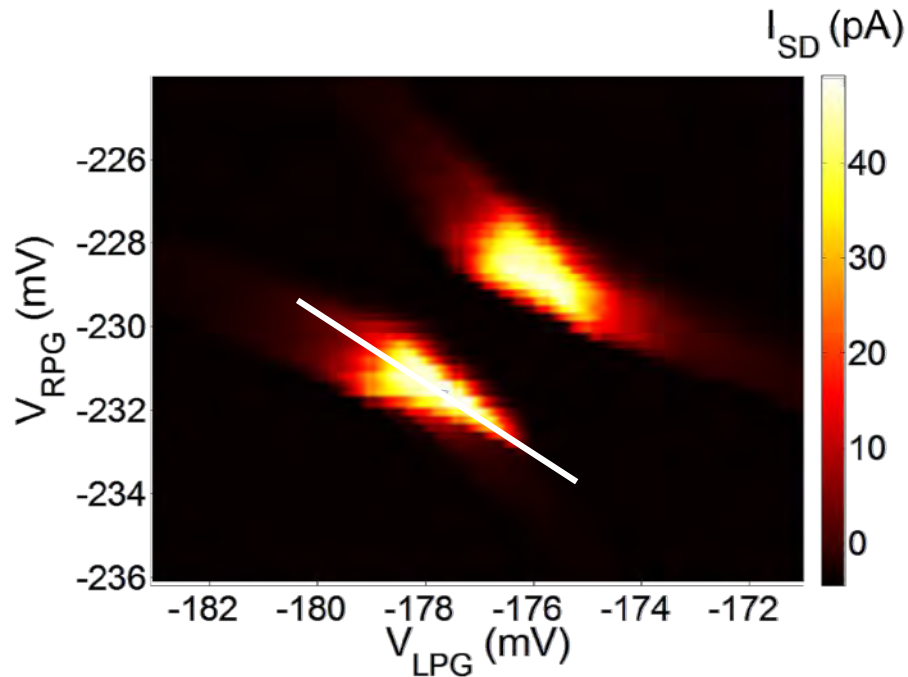
Control



Sensing Small Electromagnetic Signals

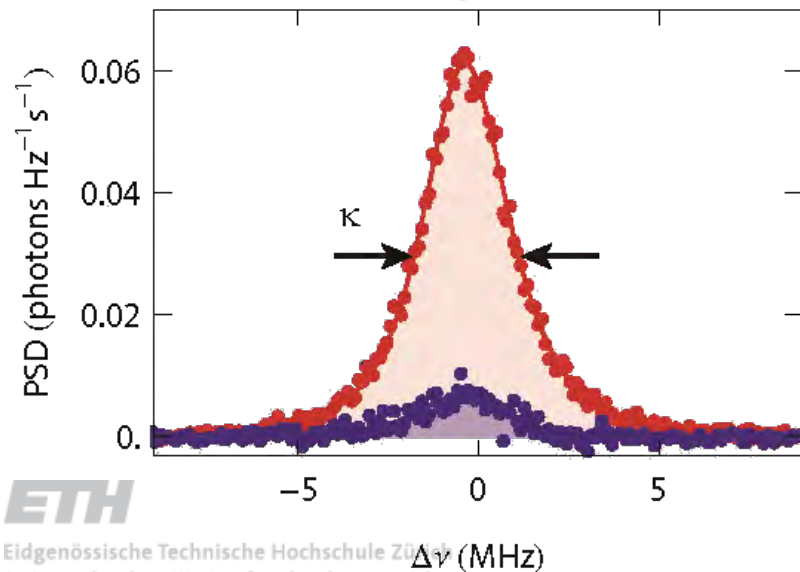


Radiation Emission at Finite Bias



measured source/drain current at bias voltage $V_{SD} = -200 \mu\text{V}$ ($\sim 50 \text{ GHz}$)

- observation of finite bias triangles



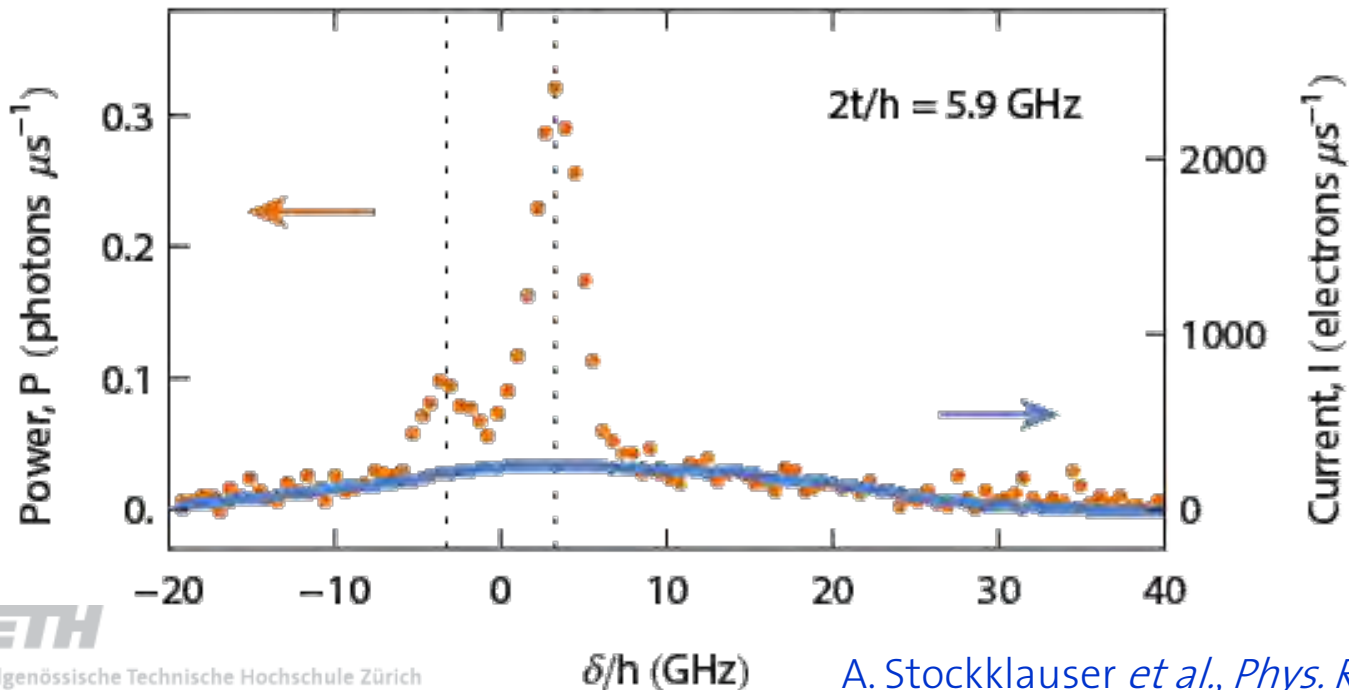
measured power spectral density (PSD) as a function of inter-dot detuning δ

- line-width given by cavity
 $\kappa \sim 3.3 \text{ MHz}$
- power is strongly δ -dependent

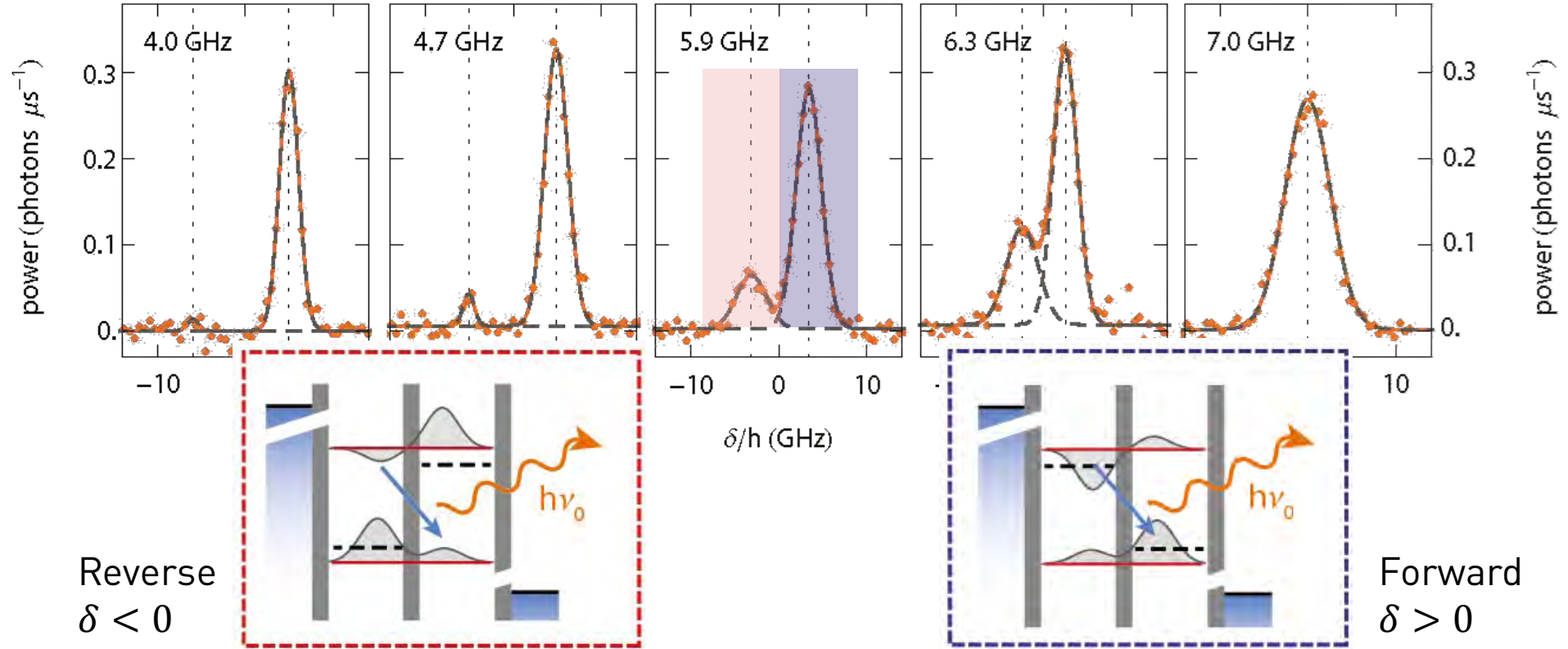
Integrated Emitted Power vs. Inter-Dot Detuning

Observations:

- weak emission over broad range in δ proportional to bias current
- emission rate: 10^{-4} photons per electron
- two pronounced maxima in emission symmetric around $\delta=0$
- emission rate increased 10x

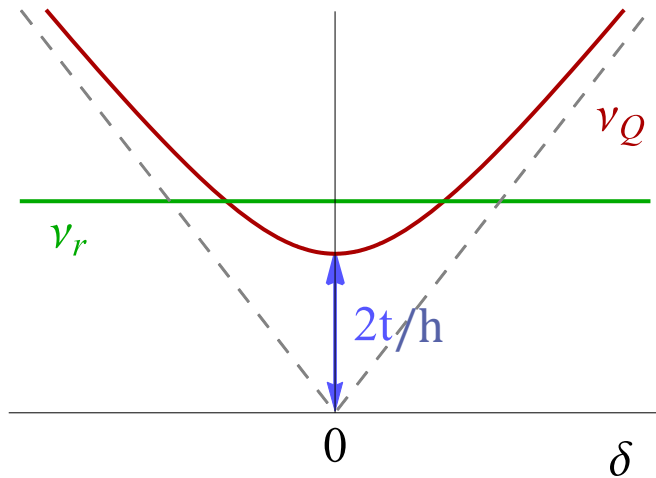


Emission Resonances vs. Inter-Dot Tunnel Coupling



- inter-dot tunneling t -independent background emission (subtracted)
- maxima in emission symmetric about inter-dot detuning $\delta = 0$
- emission gaussian in detuning δ (FWHM ~ 1.5 GHz)
- large (approx. δ -independent) emission for forward bias $\delta > 0$
- small (δ -dependent) emission for reverse bias $\delta < 0$

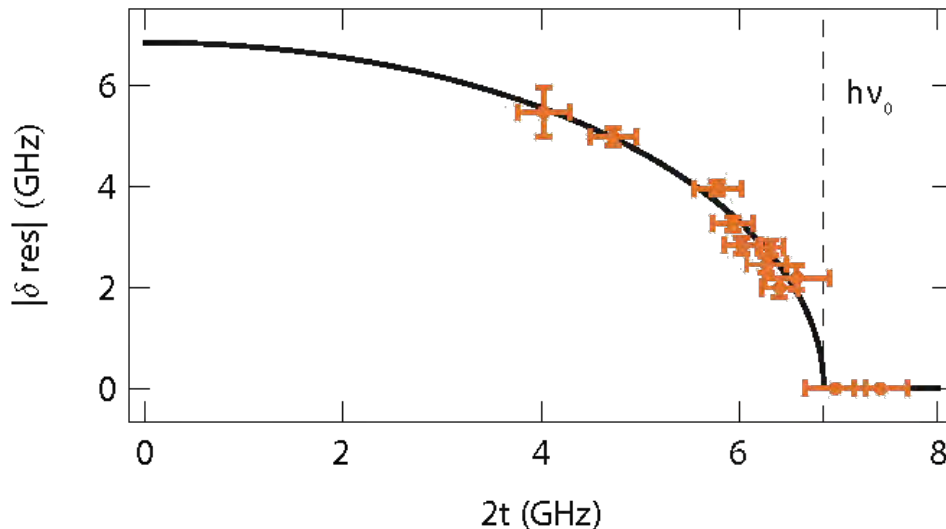
Tunnel-Coupling Dependence of Emission Maxima



Interpretation:

- Inter-dot detuning δ_r resonance with cavity depends on tunnel coupling $2t$

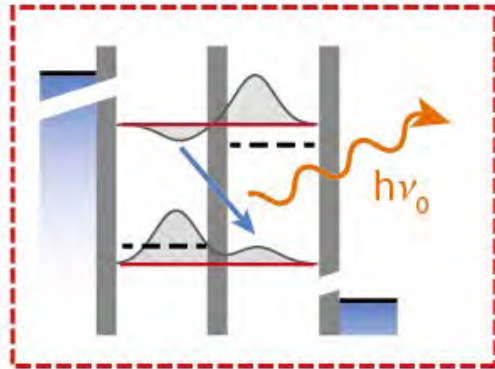
$$\delta = \pm \sqrt{(h\nu_r)^2 - (2t)^2}$$



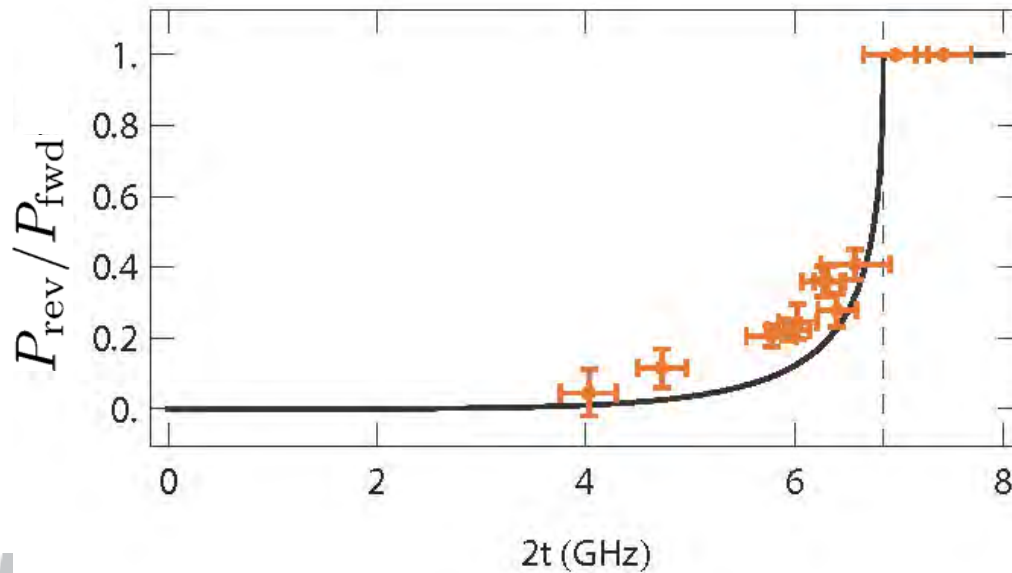
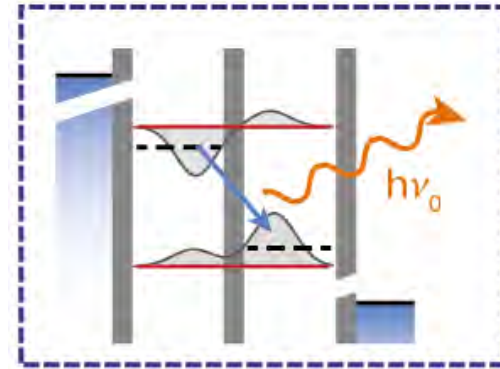
- good agreement with observed bias at emission maxima

Scaling of Forward and Reverse Bias Emission with $2t$

Reverse
 $\delta < 0$



Forward
 $\delta > 0$



Ratio of peak emission between reverse and forward bias

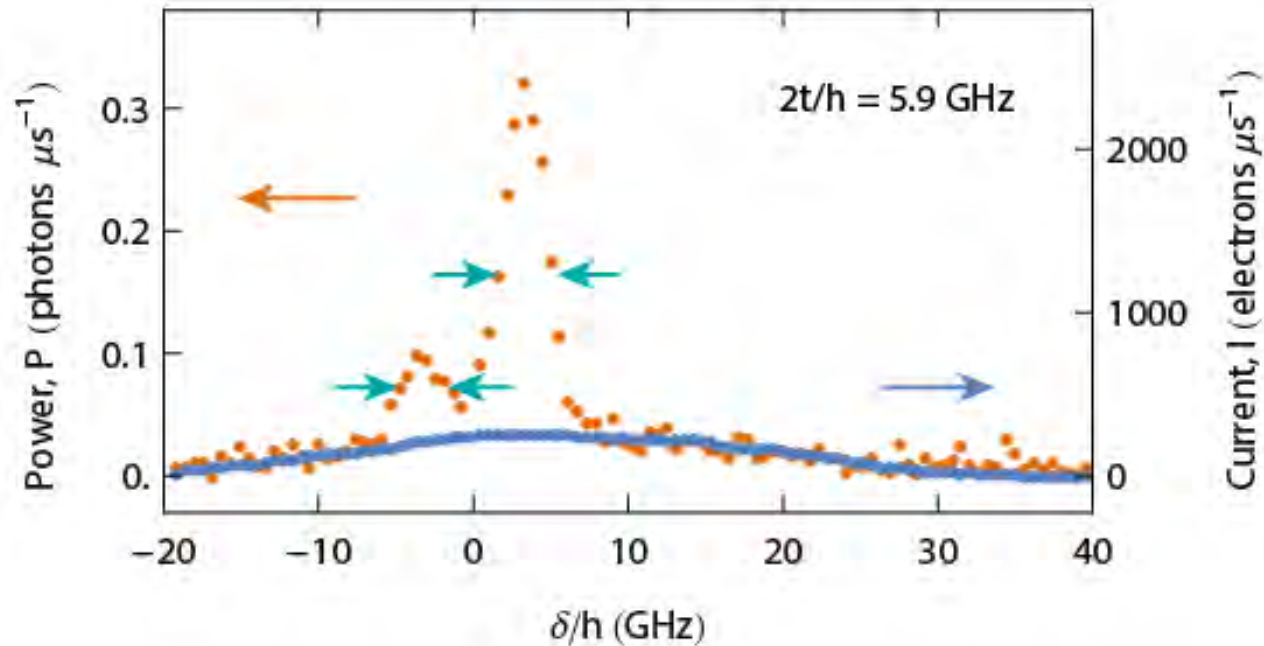
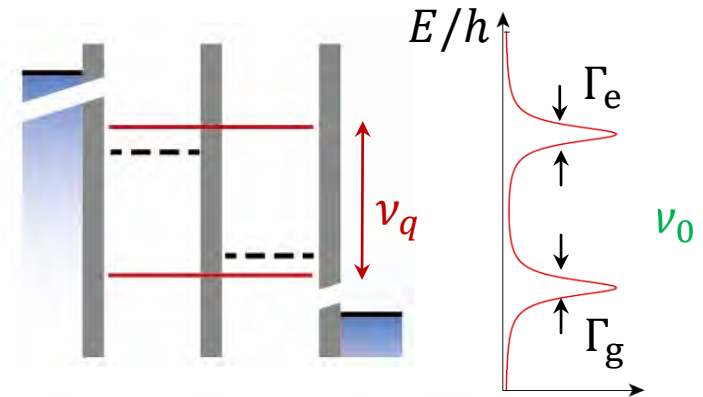
$$\frac{P_{\text{rev}}}{P_{\text{fwd}}} = \frac{\alpha^2}{(1 - \alpha)^2}$$

$$\text{with } \alpha = \frac{1}{2} \left[1 + \sqrt{1 - \left(\frac{2t}{hv_r} \right)^2} \right]$$



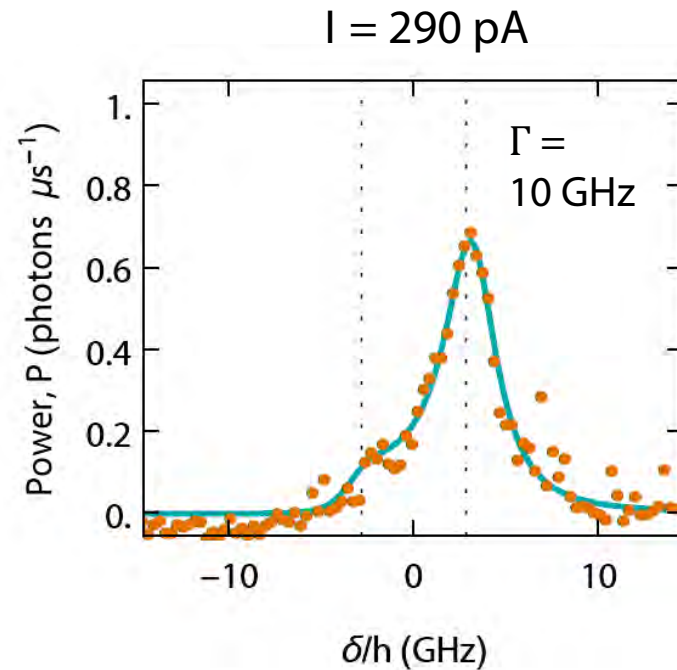
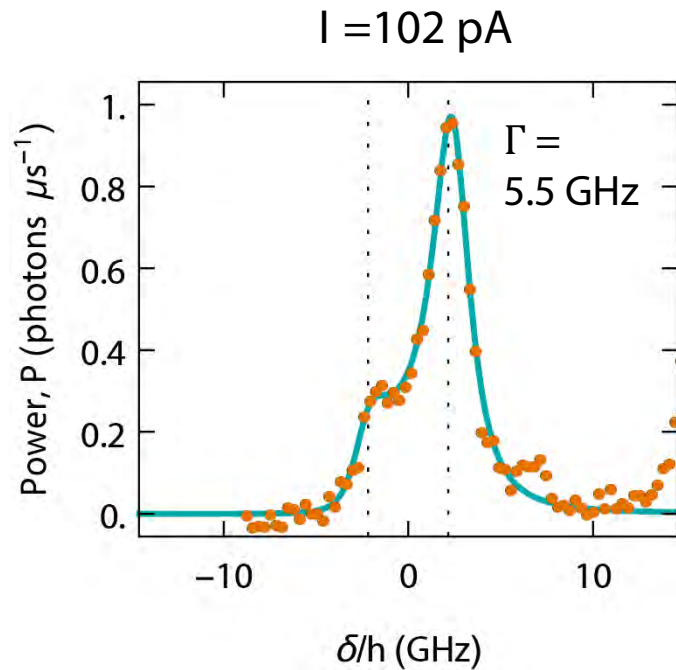
Dependence of Emission on Coupling to Leads

- Investigation of width of emission resonances in dependence on broadening of quantum dot levels due to coupling to leads

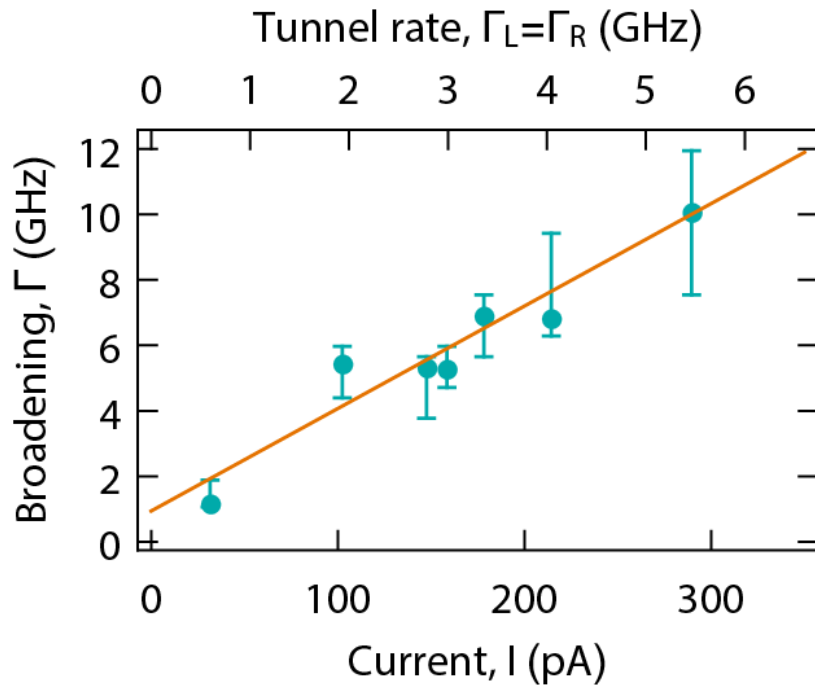


Dependence of Emission on Coupling to Leads

- Symmetric configuration $\Gamma_L = \Gamma_R$, constant t, V_{SD}
- Elastic current $I = I_{el} \propto \Gamma_R$
- Resonance width increases with Γ_L, Γ_R



Dependence of Emission on Coupling to Leads



- Approximately linear increase with the current
- Expected level broadening: $\Gamma = \Gamma_R + \tilde{\gamma}$
- $\gamma/2\pi \leq 250$ MHz in the entire range of source-drain coupling
- $I = I_{el}$ converted to tunnel rate $\Gamma_L = \Gamma_R$
- Emission linewidth and qubit level broadening proportional to tunnel rates to leads

Summary

- Performed photon emission measurements from semiconductor DQD
- Used circuit QED measurement techniques for characterization of emission
- Obtained good understanding of emission process

Outlook

- Investigate radiation emission using correlation function measurements
- Work towards strong coupling to charge (overcome 100 MHz scale dephasing rate)
- Use resonator as a coupling bus in semiconductor-based QIP

- Explore benefits of circuit QED in semiconductor structures

A. Stockklauser *et al.*, *Phys. Rev. Lett.* 115, 046802 (2015)

J. Basset *et al.*, *Phys. Rev. B* 88, 125312 (2013)

T. Frey *et al.*, *Phys. Rev. B* 86, 115303 (2012)

T. Frey *et al.*, *Phys. Rev. Lett.* 108, 046807 (2012)

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incl. undergrad and summer students



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