

# Spin Hall Effect in Topological Semimetals

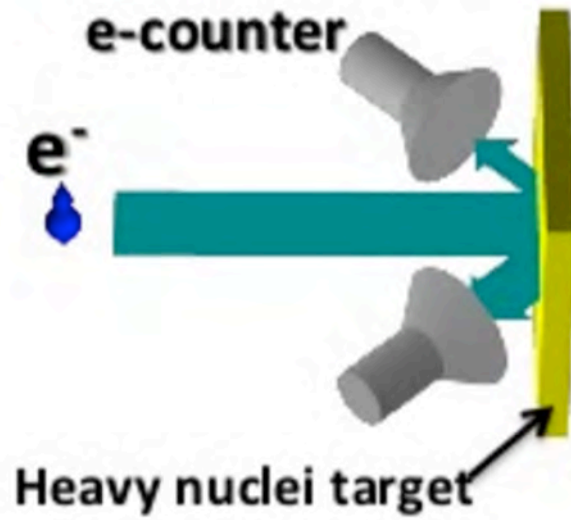
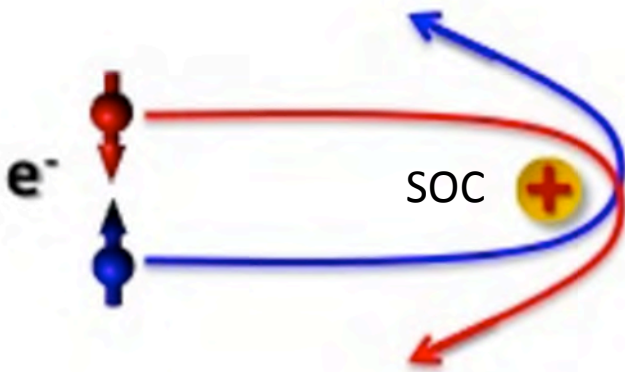


**Binghai Yan**

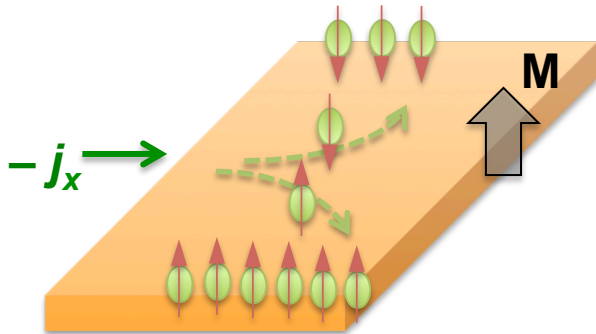
Max Planck Institute for Chemical Physics of Solids, Dresden, Germany  
[www.cfps.mpg.de/yan](http://www.cfps.mpg.de/yan)

17 Jun 2016, SPICE Young Research Leaders Group Workshop, Mainz

## Mott scattering

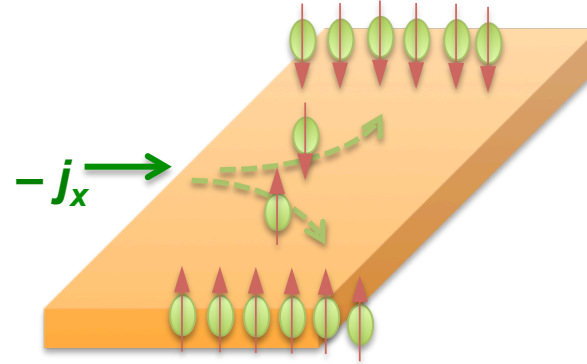


## Anomalous Hall effect



$$j^{AHE} = j^{\uparrow} - j^{\downarrow}$$

## Spin Hall Effect

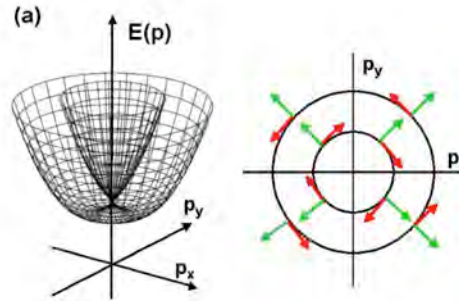
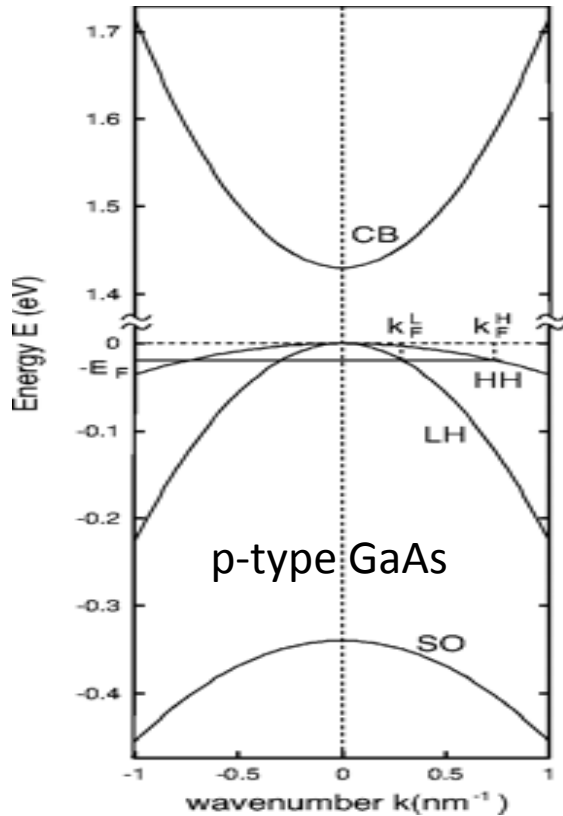


$$j^{SHE} = j^{\uparrow} + j^{\downarrow} \quad \frac{\hbar/2}{e}$$

The spin Hall effect:  
an external electric field induces a transverse spin current

An extrinsic effect, due to impurities in the presence of spin-orbit coupling (SOC).

# Intrinsic Spin Hall Effect



SHE due to the band structure of the material

$$\sigma_{xy} = -\frac{e^2}{2\pi h} \sum_n \int_{\text{BZ}} d^2k n_F(\epsilon_n(\mathbf{k})) B_{nz}(\mathbf{k}),$$

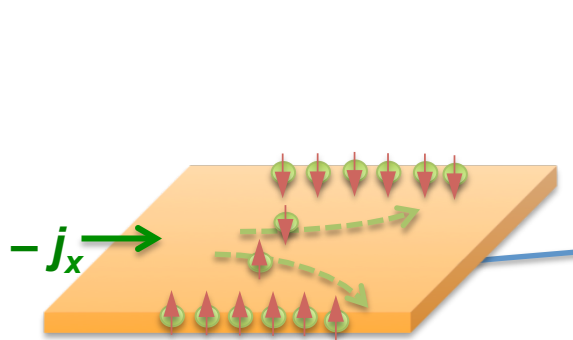
Berry curvature  
A fictitious magnetic field

SHE metals -- > SHE insulators

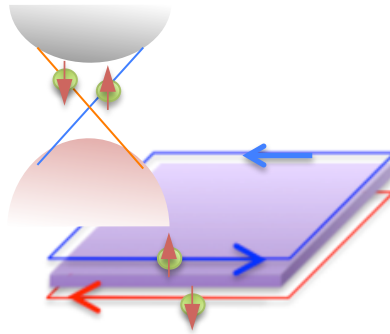
Murakami, N. Nagaosa, and S. C. Zhang, Science 301, 1348 (2003).

J. Sinova, D. Culcer, Q. Niu, N. A. Sinitsyn, T. Jungwirth, and A. H. MacDonald, Phys. Rev. Lett. 92, 126603 (2004).

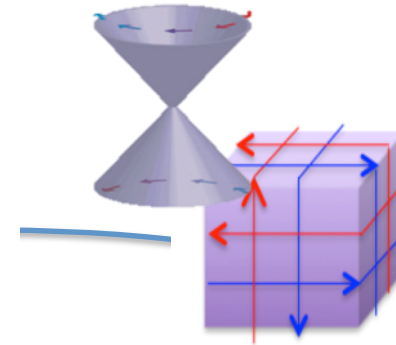
# Spin Hall Effect and other topological states



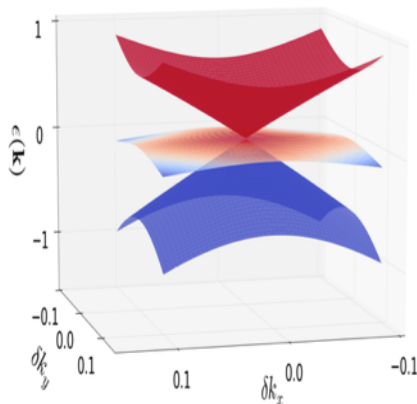
Intrinsic SHE



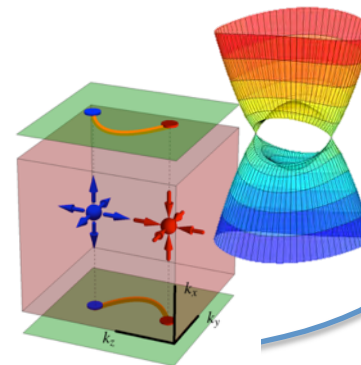
Quantum SHE (2DTI)



3D TI

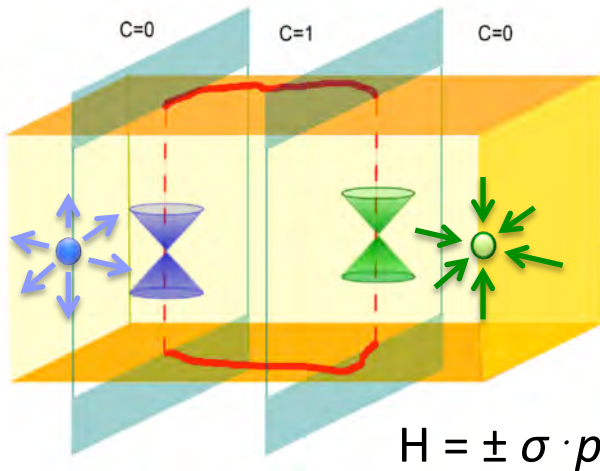


New Fermions (Bernevig 2016')

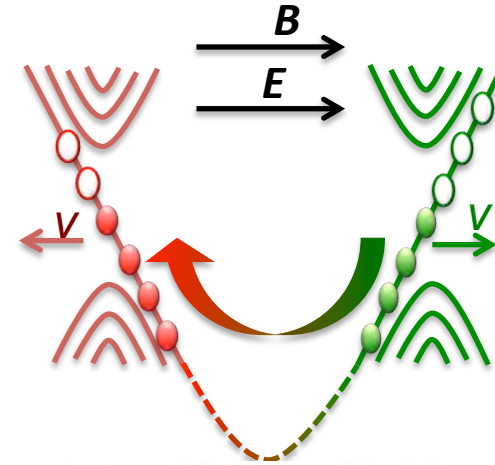
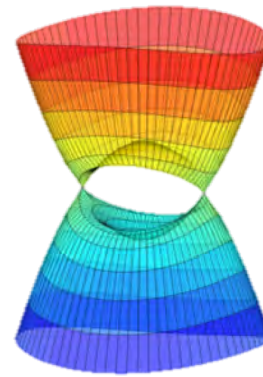


Dirac/Weyl Semimetals  
Nodal-line Semimetals

# Weyl Semimetals

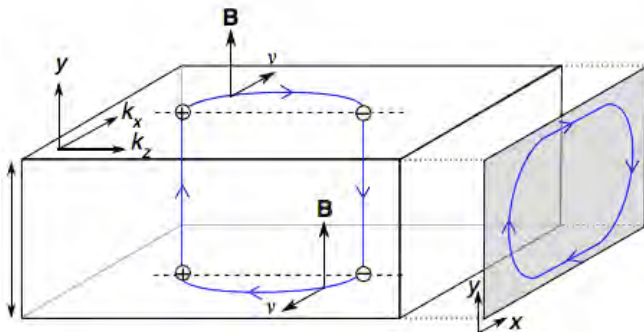


Fermi arcs



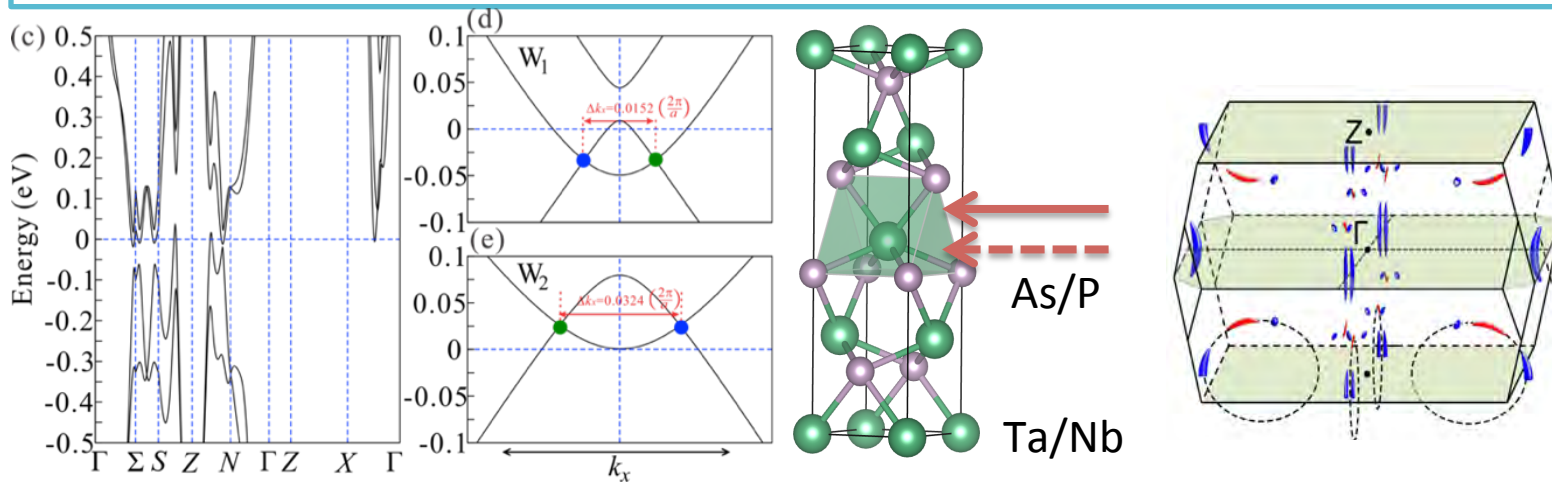
$$\frac{\partial Q_X^{3D}}{\partial t} = g \frac{\partial Q_X^{1D}}{\partial t} = -V \frac{e^3}{4\pi^2 \hbar^2} \mathbf{E} \cdot \mathbf{B}$$

Chiral anomaly



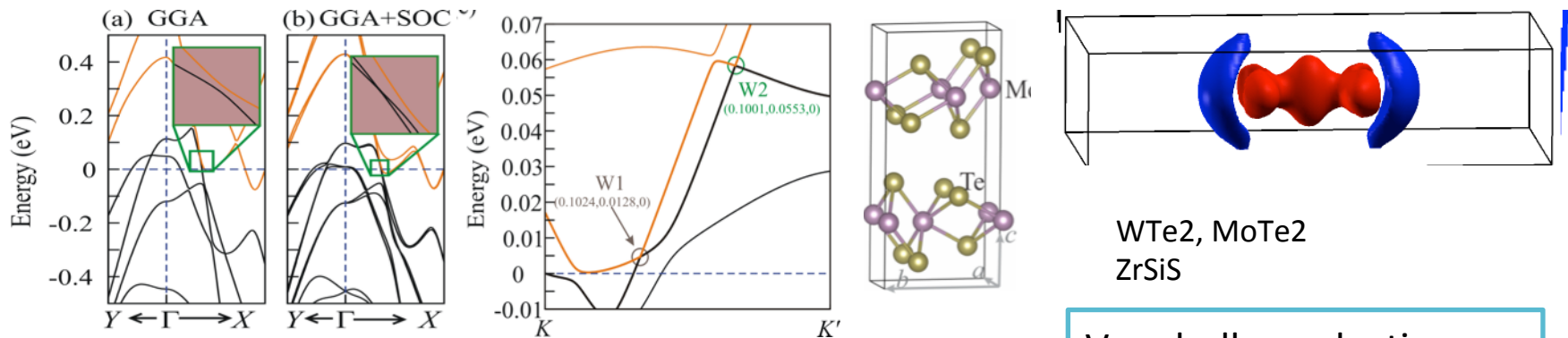
- Bulk, 3D analogue of graphene
- Surface, Fermi arcs

# Reality in materials: bulk



Weng, H. *et al.* *Phys. Rev. X* **5**, 011029 (2015).  
 Huang, S.-M. *et al.* *Nature Commun.* **6**, 7373 (2015).

F. Arnold *et al.*, *Nature Commun.* **7**, 11615 (2016).  
 C. Shekhar *et al.* *Nature Physics* **11**, 645 (2015).



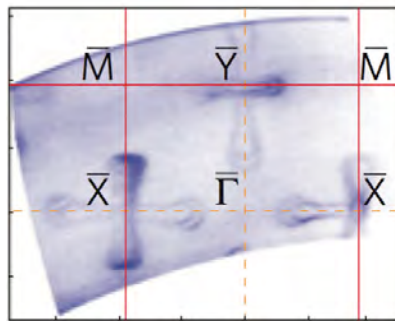
A. A. Soluyanov *et al.* *Nature* **527**, 495 (2015).  
 Y. Sun *et al.* *PRB* **92**, 161107(R) (2015).  
 L. M. Schoop *et al.* *Nature Comm.* **7**, 11696 (2016).  
 M. N. Ali *et al.* *Nature* **514**, 205 (2014).

Very bulk conductive

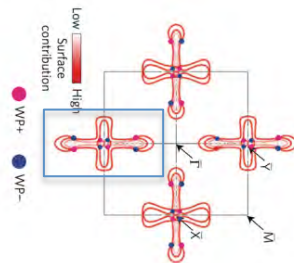
- High mobility
- Large MR

# Reality in materials: Fermi arcs

TaAs



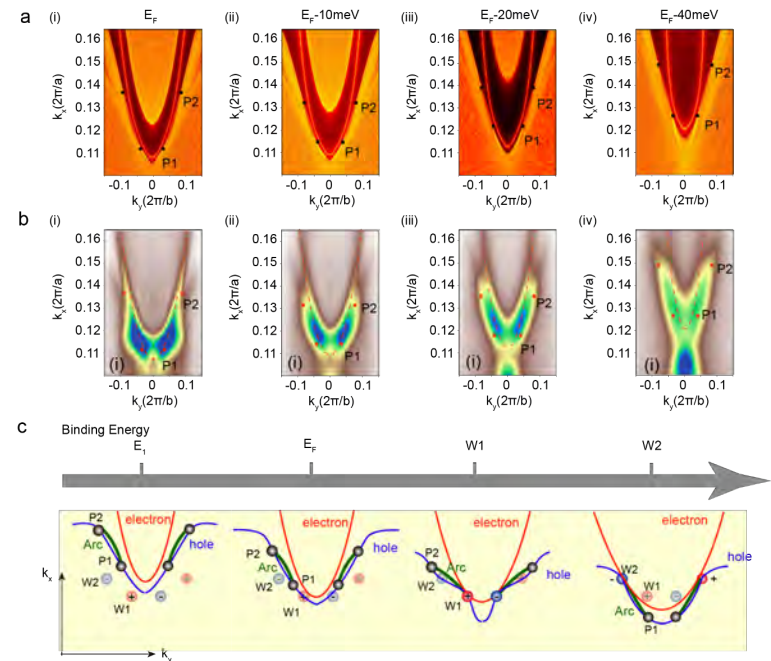
ARPES



Calculation

L.X. Yang et al. *Nature Physics* 11, 728–732 (2015)  
 B. Q. Lv et al., *Phys. Rev. X* 5, 031013 (2015).  
 S.-Y. Xu et al., *Science* 349, 613 (2015).

MoTe2



Jiang et al. 2016. arXiv:1604.00139

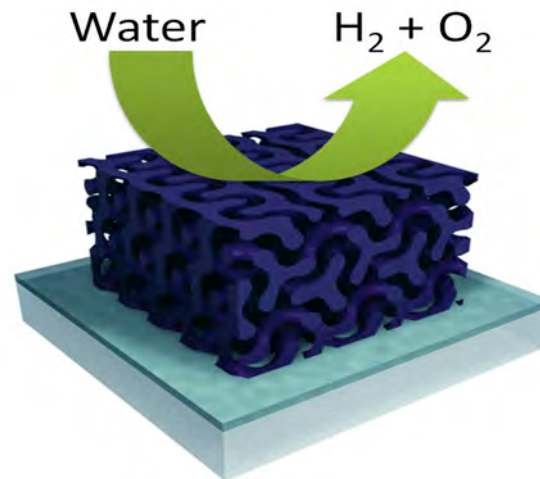
- Bulk bands
- Trivial surface states



# Topological states for catalysis

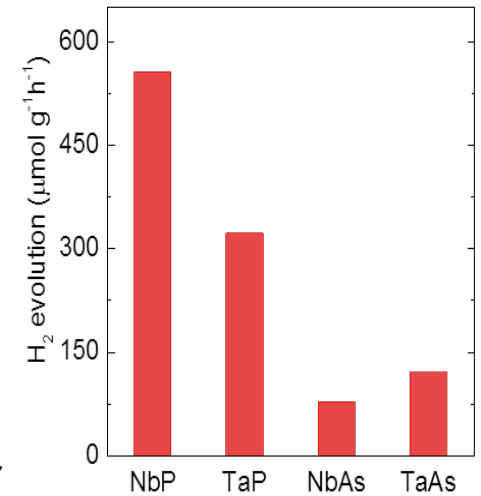
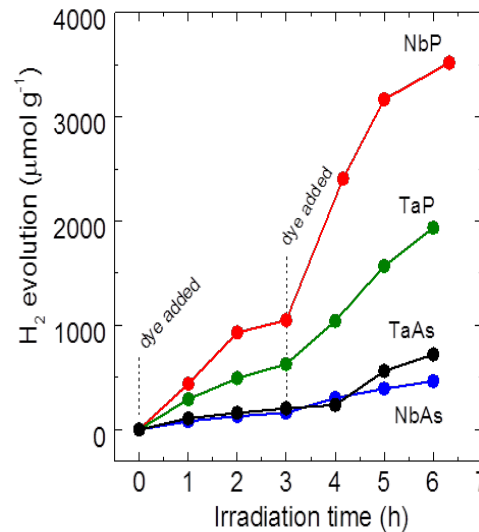
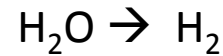
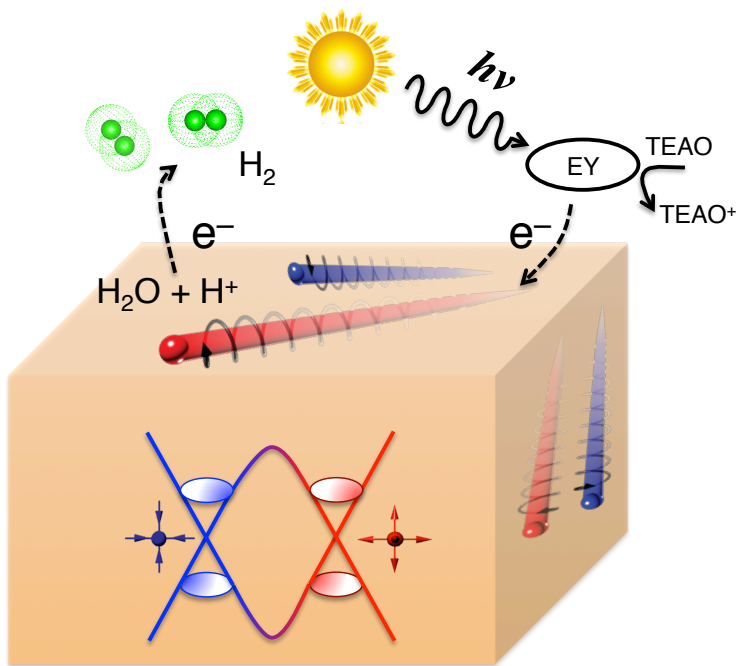
## Topological chemistry

- Impact of topological states in the surface-related process e.g. catalysis
- Discovery of topological states on Au, Pt and Pd. [Nat. Comm. 6, 10167(2015)]
- Design of new catalysts from topological insulators and semimetals



# Topological states for catalysis

Proof of the principles: Solar hydrogen evolution catalyzed by WSMs



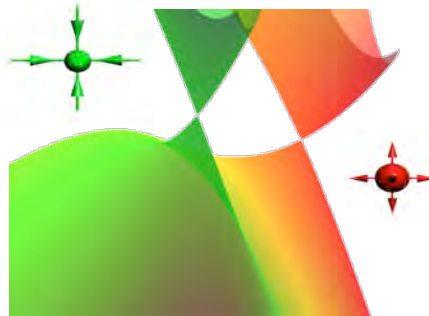
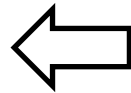
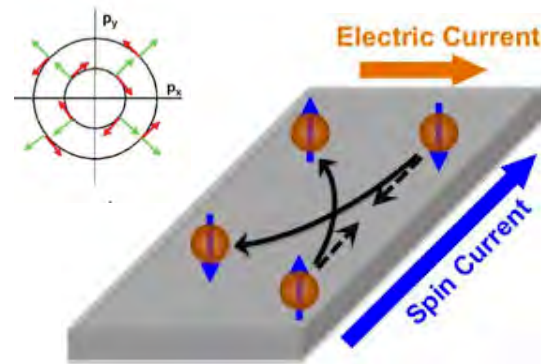
Rajamathi et al. submitted.

Comparable to MoS<sub>2</sub> in the photocatalytic HER.

- Stable surface states
- Surface-bulk-surface tunneling
- Highly mobile electrons

# WSMs/DSMs for Spintronics

Spin Hall Effect for room temperature devices  
(talks of Hyunsoo Yang & Timothy Phung)

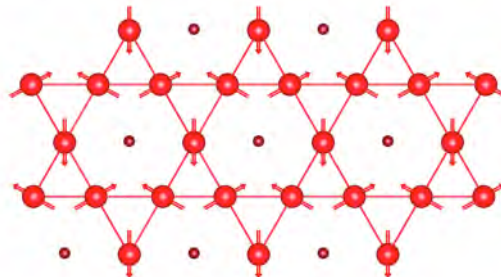


$$\sigma_{xy}^z = \frac{e}{\hbar} \sum_{\mathbf{k}} \Omega^z(\mathbf{k}) = \frac{e}{\hbar} \sum_{\mathbf{k}} \sum_n f_{\mathbf{k}n} \Omega_n^z(\mathbf{k}),$$

$$\Omega_n^z(\mathbf{k}) = \sum_{n' \neq n} \frac{2\text{Im}[\langle \mathbf{k}n | j_x^z | \mathbf{k}n' \rangle \langle \mathbf{k}n' | v_y | \mathbf{k}n \rangle]}{(\epsilon_{\mathbf{k}n} - \epsilon_{\mathbf{k}n'})^2},$$

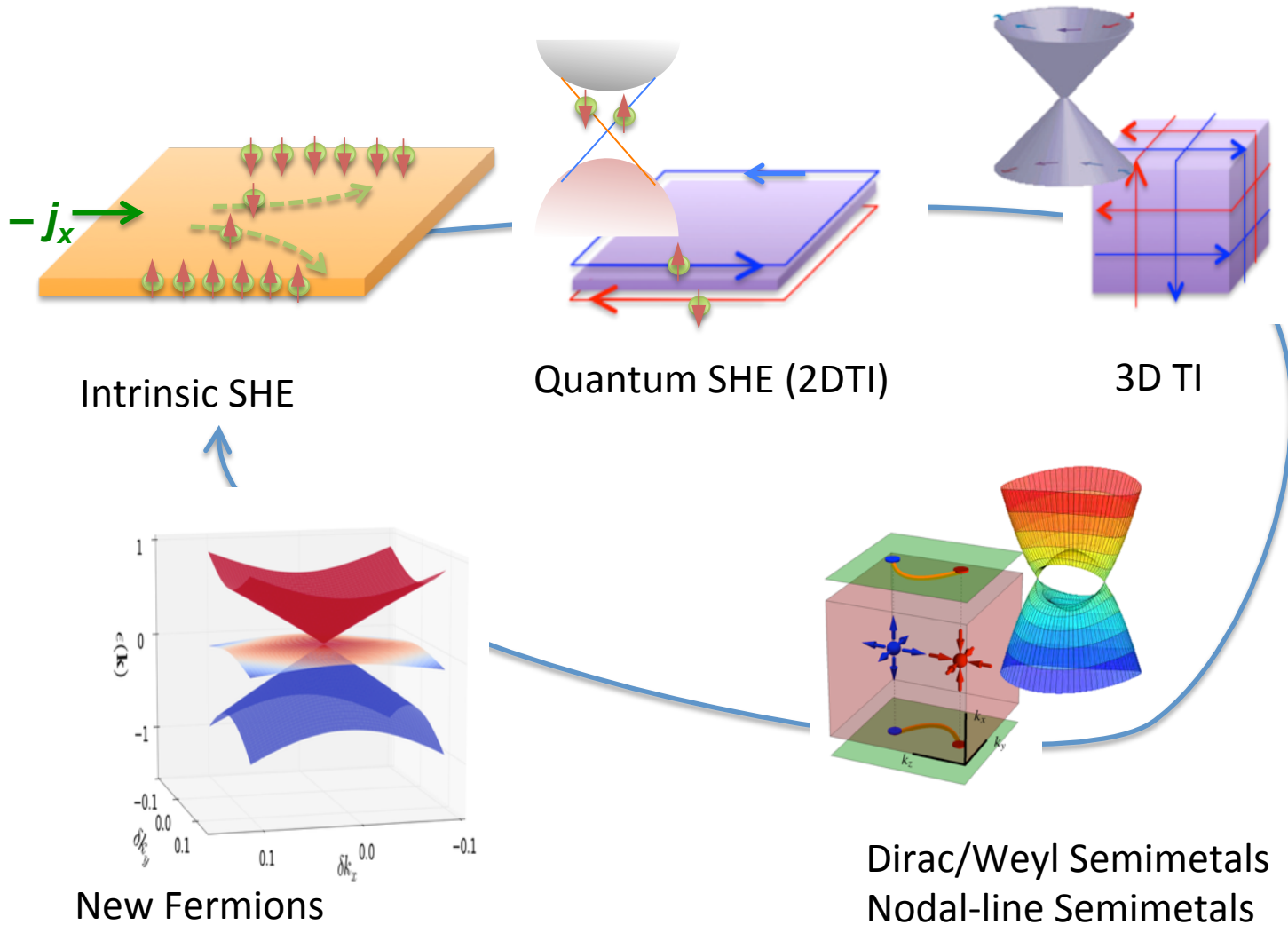
Spin Hall Effect

Monopoles of Berry curvature in a WSM e.g. TaAs, WTe<sub>2</sub>, MoTe<sub>2</sub>

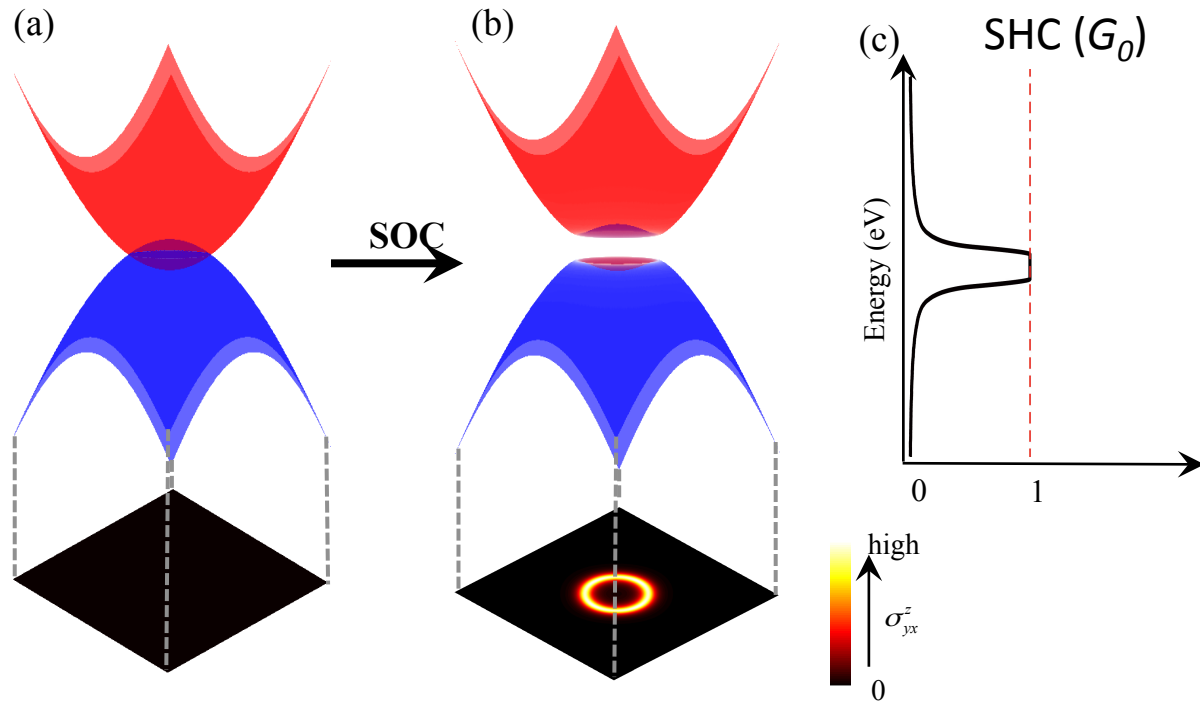


Noncollinear AFM  
Mn<sub>3</sub>X (X=Ir, Ge, Sn)

# Spin Hall Effect and other topological states



# Spin Hall Effect

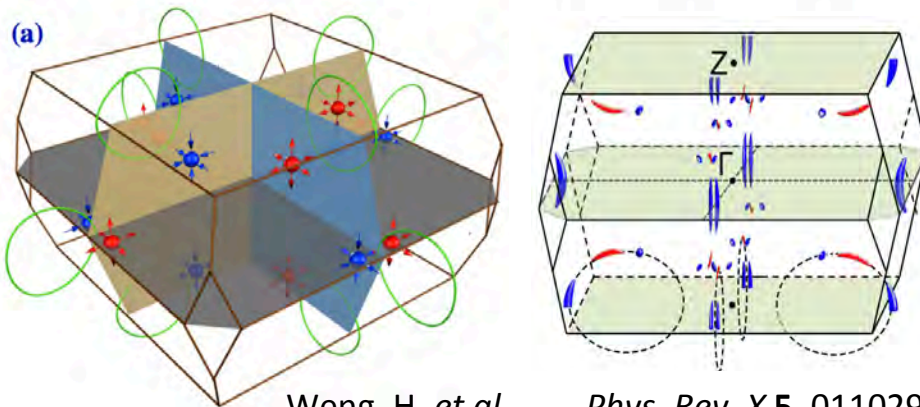
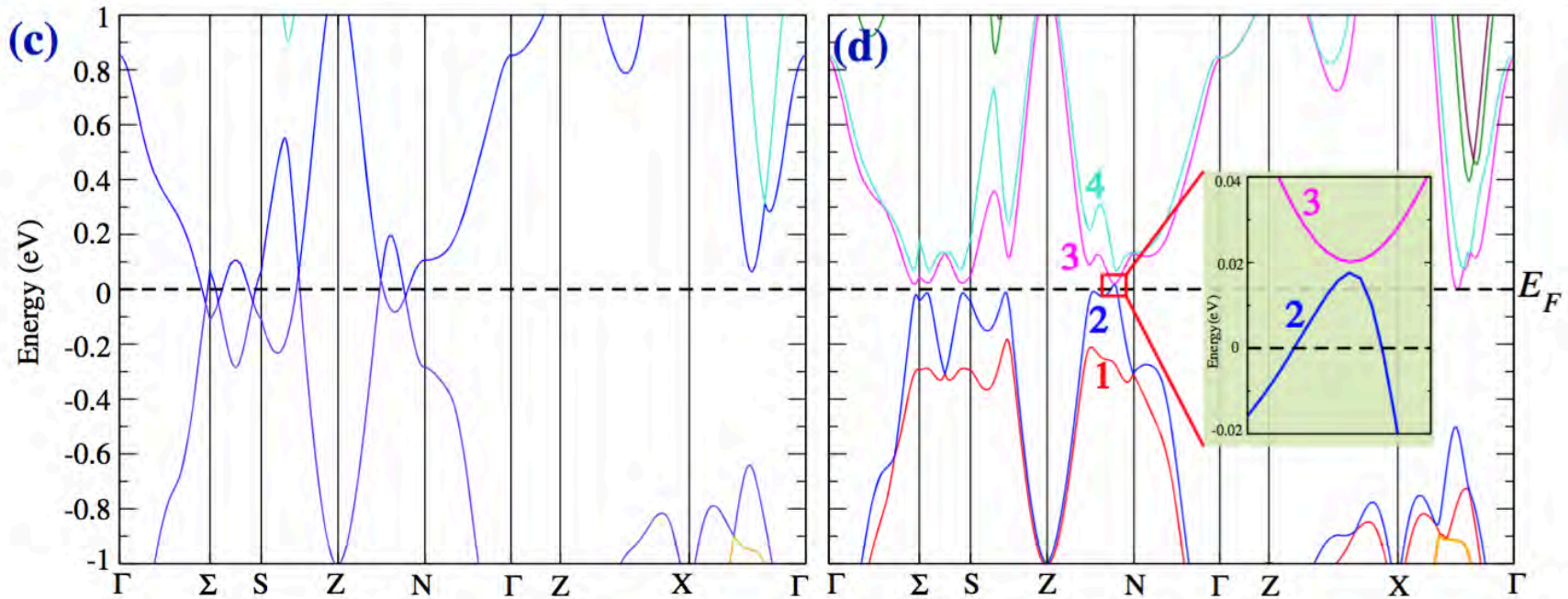


QSHE in a toy model that preserves  $S_z$ .

$$\Omega_n^z(\mathbf{k}) = \sum_{n' \neq n} \frac{2\text{Im} [\langle \mathbf{k}n | j_x^z | \mathbf{k}n' \rangle \langle \mathbf{k}n' | v_y | \mathbf{k}n \rangle]}{(\epsilon_{\mathbf{k}n} - \epsilon_{\mathbf{k}n'})^2},$$

$$j_x^z = (s_z v_x + v_x s_z) / 2$$

# Band structure of TaAs-type WSMs

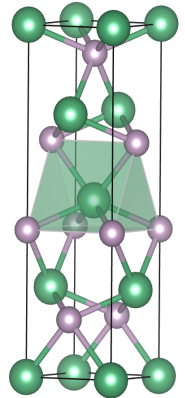
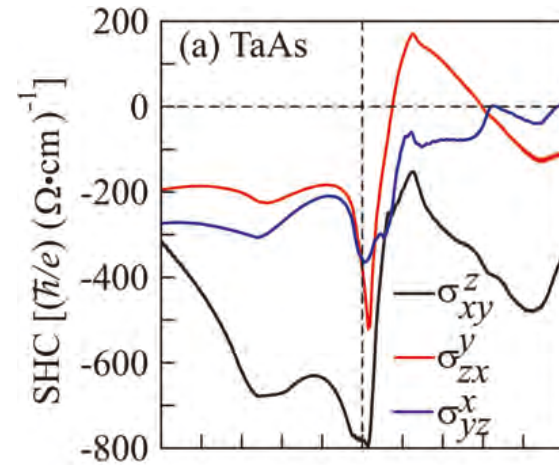
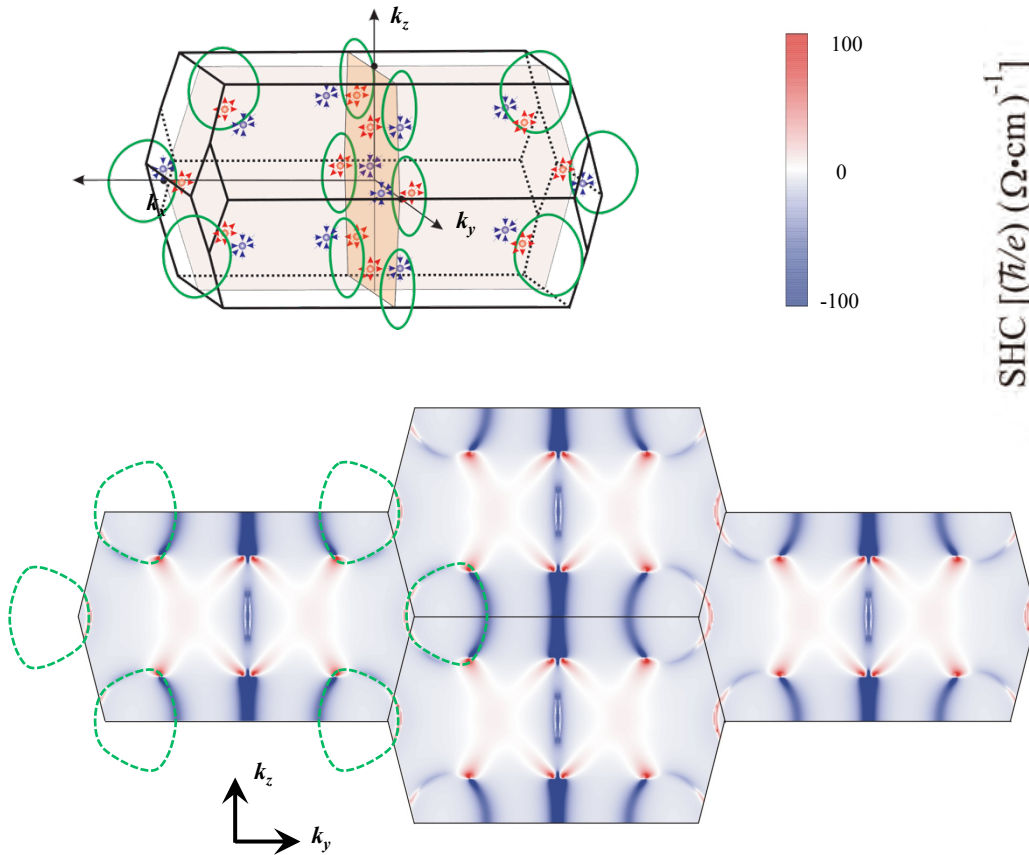


Weng, H. *et al.*

*Phys. Rev. X* **5**, 011029 (2015).

- Full of band crossing due to SOC
- Bulk carriers are not necessarily negative

# Spin Hall Conductivity

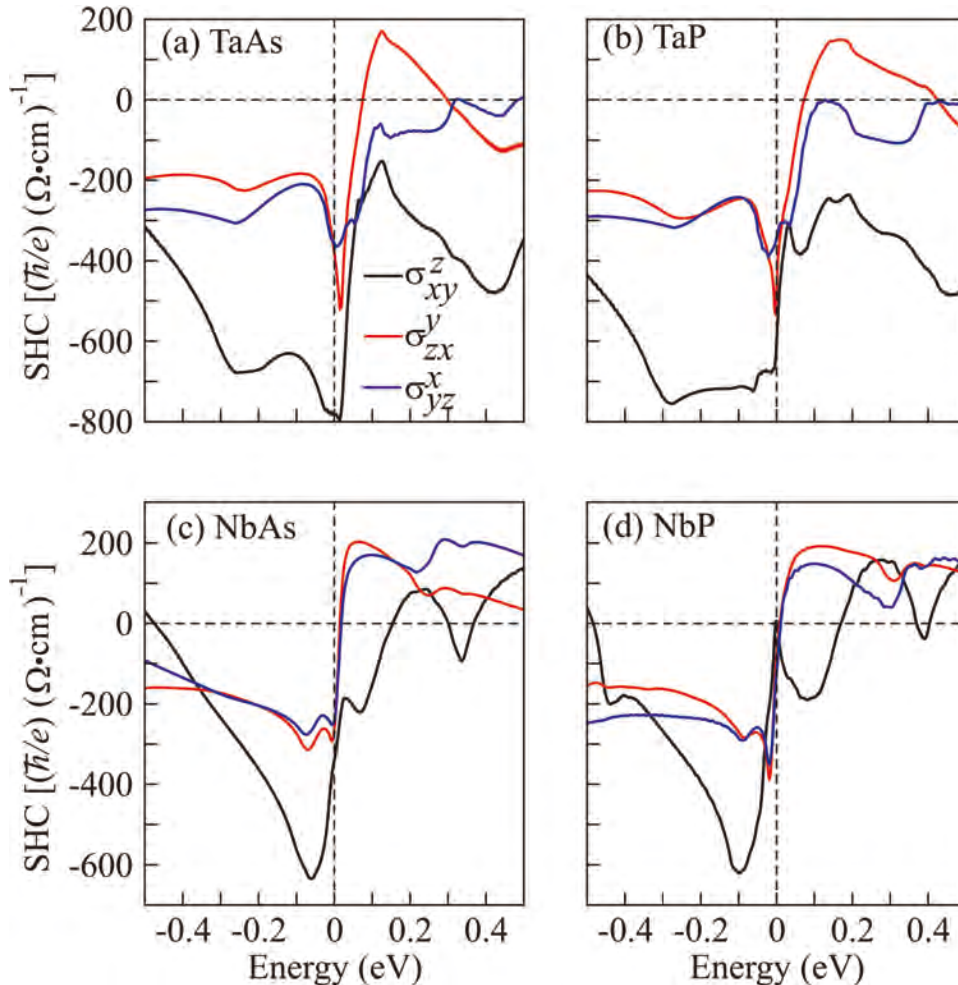


Anisotropic  
 $\sigma_{xy}^z \sim 800$  (TaAs)

$\sim 2000$  (Pt)

Spin Hall Angle  $\sigma^{\text{Spin}}/\sigma^{\text{charge}}$

# Spin Hall Conductivity



$E_F$  at zero

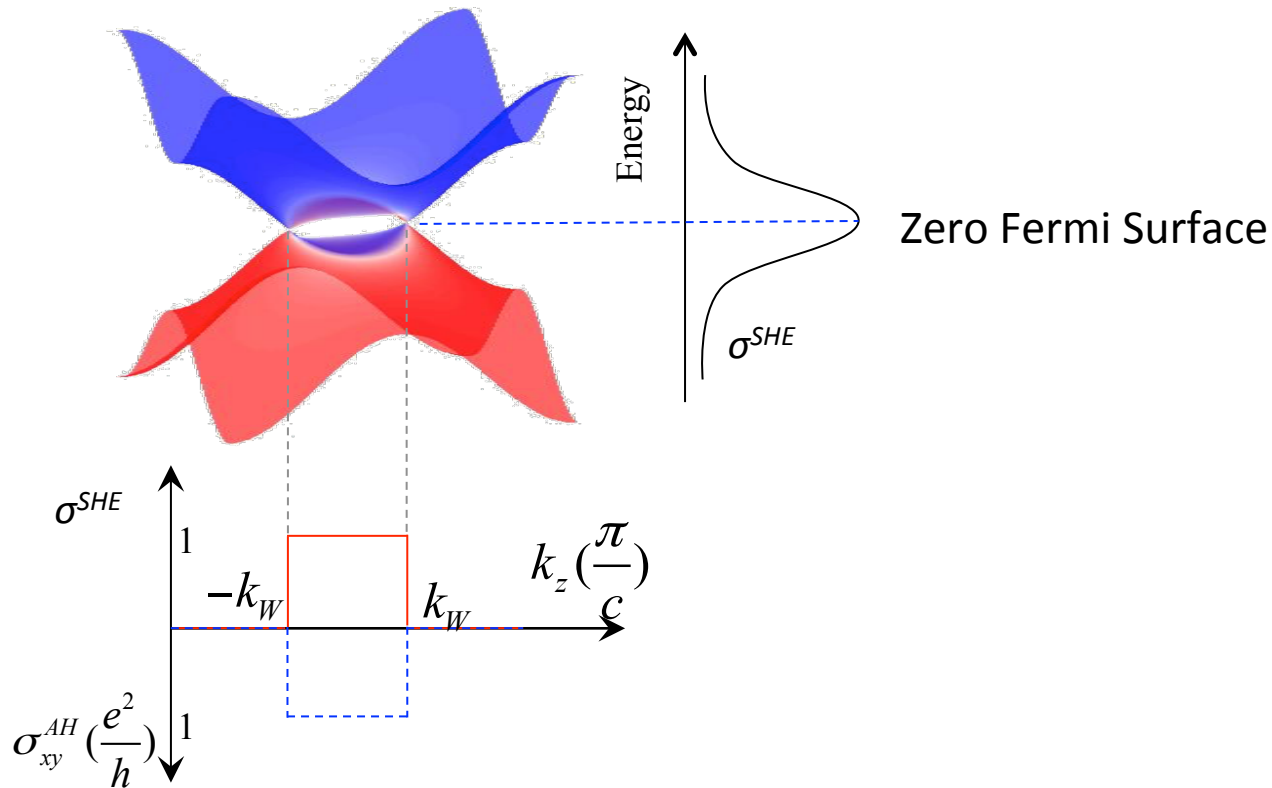
	TaAs	TaP	NbAs	NbP
$\sigma_{xy}^z$	-762	-537	-326	7
$\sigma_{zx}^y$	-363	-457	-320	-83
$\sigma_{yz}^x$	-364	-346	-272	-135

Peaks of SHC are not Weyl points

Y Sun, Y Zhang, C Felser, B Yan  
**arXiv:1604.07167 (2016)**

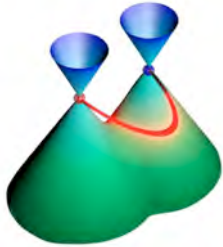


# How does Weyl play?



Weyl band structure

# Topological SMs vs TIs



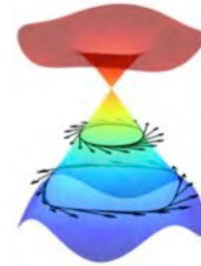
Bulk 3D Weyl cones + Surface Fermi arcs

Bulk conductive

No chemical potential problem

Materials:

TaAs, WTe<sub>2</sub>, MoTe<sub>2</sub> ZrSiS .....



Surface Dirac cones

Bulk conductive --- weak SHE

Bulk insulating --- non-conducting

# Acknowledgement

Postdocs: Yan Sun

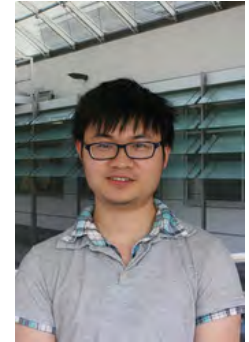
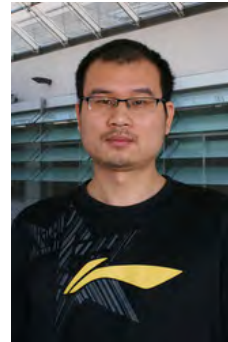
PhDs: Yang Zhang, Hao Yang

Collaborators

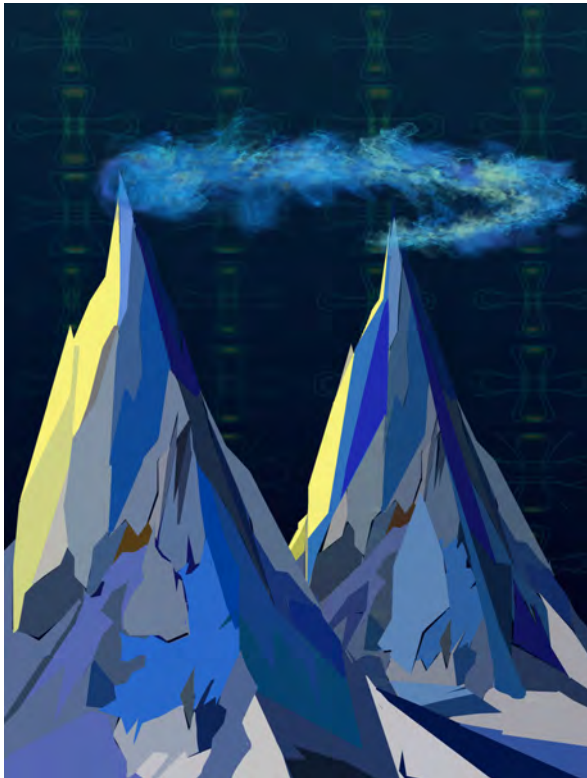
- Claudia Felser (MPI Dresden)
- Stuart Parkin (MPI Halle)
- Yulin Chen (Oxford)
- Haim Beidenkopf (Weizmann Institute)

Fruitful discussions

- Leslie Schoop (MPI Stuttgart)
- Andrei Bernevig (Princeton)
- Jairo Sinova (Mainz)



Thank you for your attendance!



**YOUNG RESEARCH LEADERS  
GROUP WORKSHOP**

NEW PARADIGMS IN DIRAC-WEYL NANO-ELECTRONICS  
JGU MITP, Mainz, Germany  
June 13<sup>th</sup> - 17<sup>th</sup> 2016

ORGANIZERS:  
Mazhar Ali (MIT-Halle)  
Binghai Yan (Singapore)

SPICE CO-ORGANIZER:  
J. Strova (Mainz)

SP/CE

A circular inset showing a microscopic view of a quantum dot array. The dots are arranged in a circular pattern and are colored in shades of red, orange, and purple. The background is dark. The SP/CE logo is overlaid on the top right of the inset.