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University

# Spintronic and optoelectronic devices using topological insulators and Dirac/Weyl materials

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## Outline

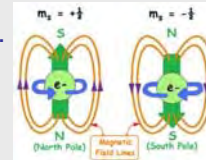
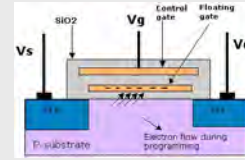
- Nanoelectronics overview
- Graphene magnetic sensors
- Graphene optoelectronics (THz devices)
- Spin-orbit torque (SOT) engineering
  - AHE & SOT in  $\text{LaAlO}_3/\text{SrTiO}_3$  oxide heterostructures
  - SOT in topological insulators ( $\text{Bi}_2\text{Se}_3$ /ferromagnet)
- Topological insulator spin detectors
- Weyl spin lifetime measurements



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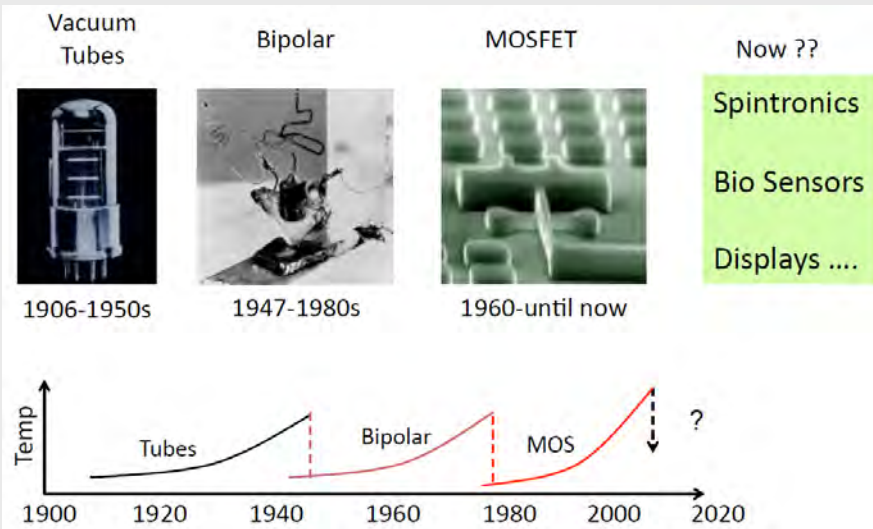
## Electron, photon, and spin

- Electronics
  - Transistor – small wavelength
  - FLASH memory – long trapping time
- Photonics
  - Optical fiber communication – long distance
  - Not compatible with nanoelectronic due to wavelength difference (diffraction limit)
- Spintronics
  - Information can be stored in magnetic materials.
  - Not easy to send for a long distance.



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## Grand challenges in electronics



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## Emergence of electronics

Biosensors    Energy    Flexible Electronics



Drug Discovery Substrates



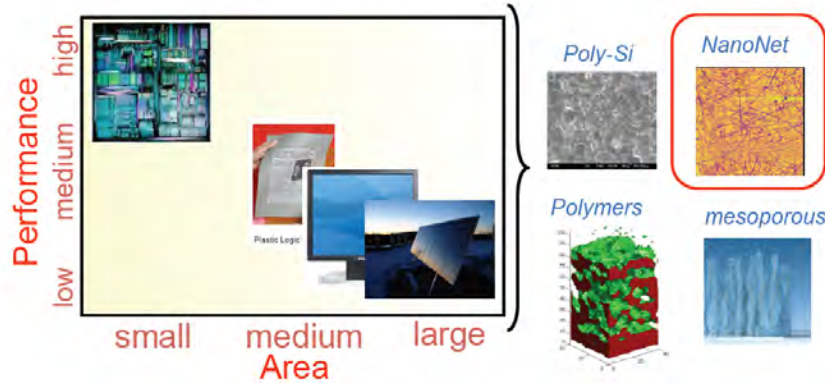
Conformal Solar Cells



Sony display 180x120 pixels

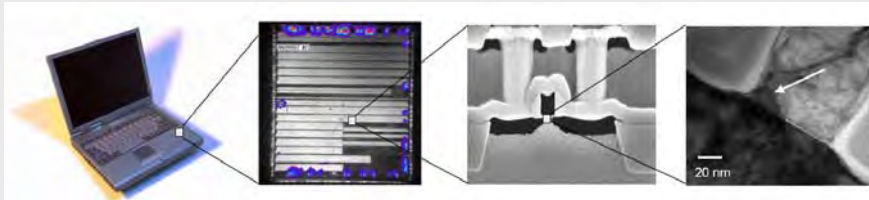


Flexible Electronics



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## A difficult problem



The ICs operate in incredibly harsh conditions, turning on and off trillions of time during its lifetime



1 CPU ~  $10^9$  Transistors

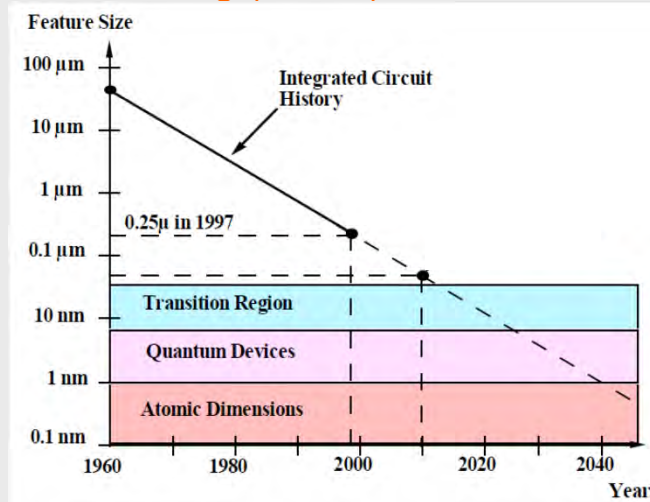
When one transistor fails, so does the IC

Uniformity issue is the challenge any new materials including graphene and 2D materials will face!



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## Transistor scaling (lateral)

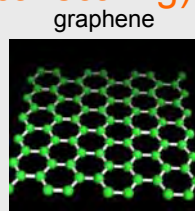


Devices are getting very small. Will they reach quantum or even atomic dimensions? What principles will they operate on? Still charge or is spin or something else possible?

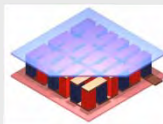
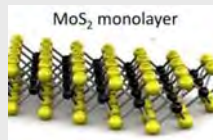


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## Thinner and thinner (vertical scaling)



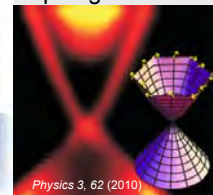
MoS<sub>2</sub>  
solid lubricant



Bi<sub>2</sub>Te<sub>3</sub> and Bi<sub>2</sub>Se<sub>3</sub>  
Wine cooler



Topological insulators



beveragefactory.com

Physics 3, 62 (2010)

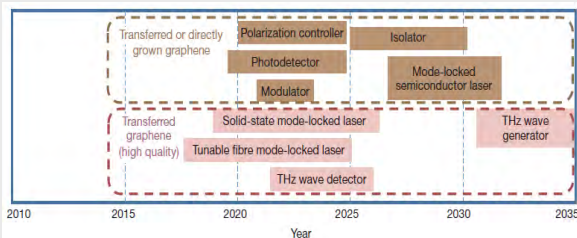
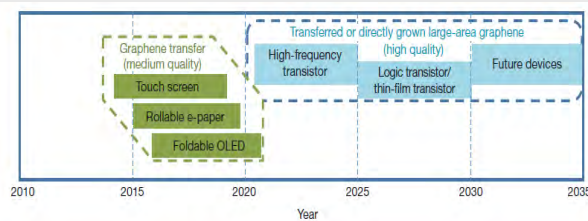
8

## Graphene applications

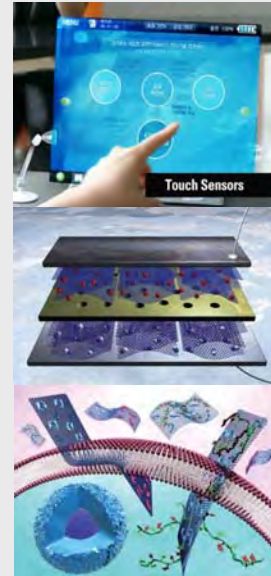
### A roadmap for graphene

K. S. Novoselov<sup>1</sup>, V. I. Fal'ko<sup>2</sup>, L. Colombo<sup>3</sup>, P. R. Gillert<sup>4</sup>, M. G. Schwab<sup>5</sup> & R. Kien<sup>6</sup>

192 | NATURE | VOL. 490 | 11 OCTOBER 2012



Sensors, optoelectronics (THz)



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## Why Silicon?

### • SiO<sub>2</sub> is a Magical Material

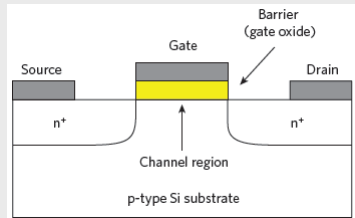
- SiO<sub>2</sub> passivates the surface of Si
- SiO<sub>2</sub> is an excellent insulator
- SiO<sub>2</sub> is an excellent barrier against impurity diffusion
- SiO<sub>2</sub> has very high etch selectivity to Si
- Si is easily purified and can be grown defect free single crystal
- Si has reasonably good electronic properties which produce a variety of devices with excellent performance
- Si and SiO<sub>2</sub> are tolerant to a variety of harsh environments used in fabrication and is highly manufacturable
- Si has excellent mechanical properties which facilitate handling and manufacturing
- Si is readily available and very plentiful in nature



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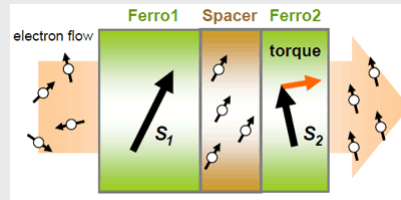
## Voltage controlled vs. current controlled

metal oxide semiconductor (MOS)



Voltage controlled (capacitive coupling)  
Suitable for parallel connection

Spin transfer torque (STT)



current controlled  
Suitable for serial connection

Spin devices may not require an oxide layer  
Need different approach



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Metal ions and alkali ions must be removed from Si device active regions

Period	I <sup>A</sup>	II <sup>A</sup>	III <sup>A</sup>	IV <sup>A</sup>	V <sup>A</sup>	VI <sup>A</sup>	VII <sup>A</sup>	VIII	I <sup>B</sup>	II <sup>B</sup>	Noble Gases							
1	1 H 1.008	2 He 4.003																
2	3 Li 6.941	4 Be 9.012																
3	11 Na 22.99	12 Mg 24.31																
4	19 K 39.10	20 Ca 40.08	21 Sc 44.96	22 Ti 47.88	23 V 50.94	24 Cr 51.99	25 Mn 54.94	26 Fe 55.85	27 Co 58.93	28 Ni 58.69	29 Cu 63.55	30 Zn 65.39	31 Ga 69.72	32 Ge 72.59	33 As 74.92	34 Se 78.96	35 Br 79.90	36 Kr 83.80
5	37 Rb 85.47	38 Sr 87.62	39 Y 88.91	40 Zr 91.22	41 Nb 92.91	42 Mo 95.94	43 Tc 98	44 Ru 101.1	45 Rh 102.9	46 Pd 106.4	47 Ag 107.9	48 Cd 112.4	49 In 114.8	50 Sn 118.7	51 Sb 121.8	52 Te 127.6	53 I 126.9	54 Xe 131.3
6	55 Cs 132.9	56 Ba 137.3	57 La 138.9	72 Hf 178.5	73 Ta 180.8	74 W 183.9	75 Re 186.2	76 Os 190.2	77 Ir 192.2	78 Pt 195.1	79 Au 197.0	80 Hg 200.6	81 Tl 204.4	82 Pb 207.2	83 Bi 209.0	84 Po 209	85 At 210	86 Rn 222
7	87 Fr 223	88 Ra 226	89 Ac 227.0	104 Unq 261	105 Unp 262	106 Unh 263	107 Uns 262											

Alkali Ions: I<sup>A</sup>, II<sup>A</sup>

Deep Level Impurities in Silicon: III<sup>A</sup>, IV<sup>A</sup>, V<sup>A</sup>, VI<sup>A</sup>, VII<sup>A</sup>

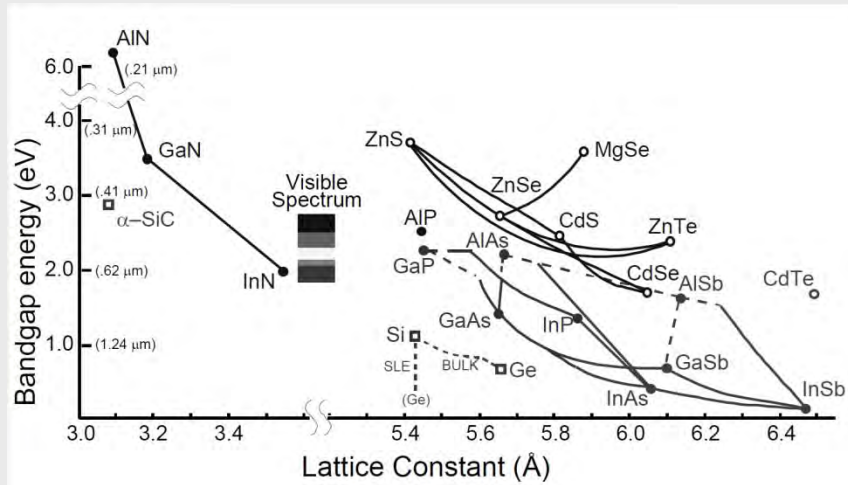
Shallow Acceptors: III<sup>A</sup>, IV<sup>A</sup>, V<sup>A</sup>, VI<sup>A</sup>, VII<sup>A</sup>

Elemental Semiconductors: III<sup>A</sup>, IV<sup>A</sup>, V<sup>A</sup>, VI<sup>A</sup>, VII<sup>A</sup>

Shallow Donors: I<sup>B</sup>, II<sup>B</sup>

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## Technologically accessible photonic materials



Mostly single or binary element (solid state chemists are way ahead!)  
 Silicon cannot emit light, but works as photodetectors (PDs)  
 Topological insulators and Weyl → spin selective PDs



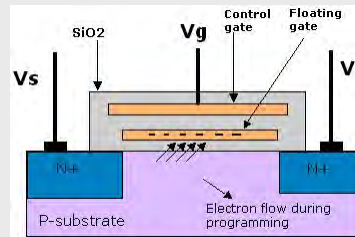
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RRAM: random material breakdown  
 → Stochastic

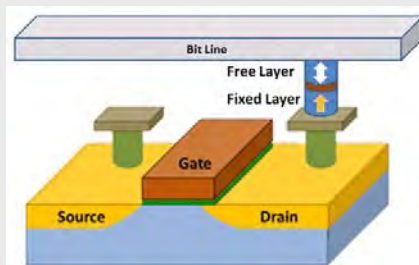


Figure 5: How it Works — In a switching media, nanoparticles form a conduction path between the top and bottom electrodes. from Crossbar

FLASH: tunneling (writing)  
 → Endurance issue (million cycles)



www.eeherald.com/



www.eetimes.com

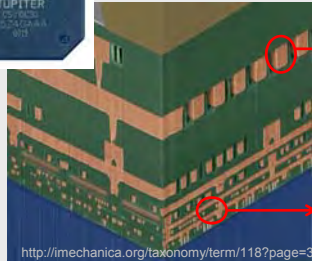
MRAM: intrinsic material property  
 → Deterministic

Spin transfer torque writing  
 → Full selectivity  
 → Smaller cell size



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## Charge electronics → Spin electronics

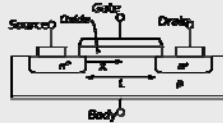


<http://imechanica.org/taxonomy/term/118?page=3>

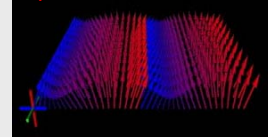
Information transfer  
= electron transfer



Information processing  
= processing electron flow



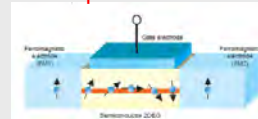
### Spin wave interconnect



### MTJ memory



### Spin transistor

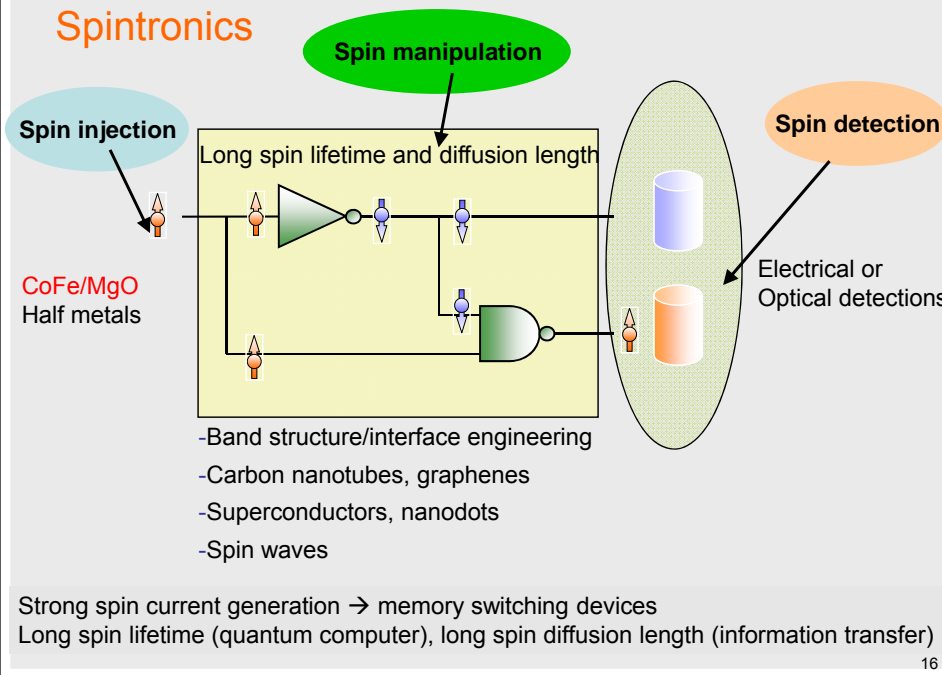


Charge transfer and processing energy loss is huge  
→ All spin electronics



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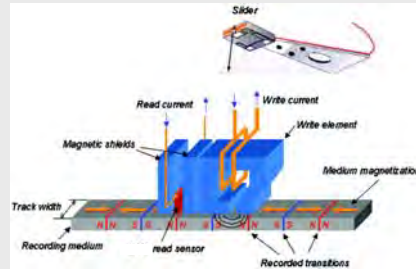
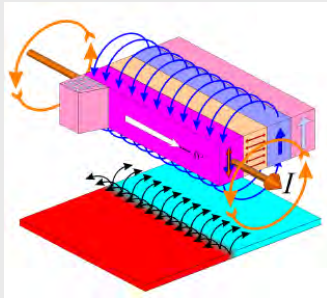
## Spintronics



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## MTJ read sensors in HDD



GMR ~ 10%  
TMR ~ 50%

We understand MTJ sensor very well  
Building high density MTJ array for MRAM is a different story



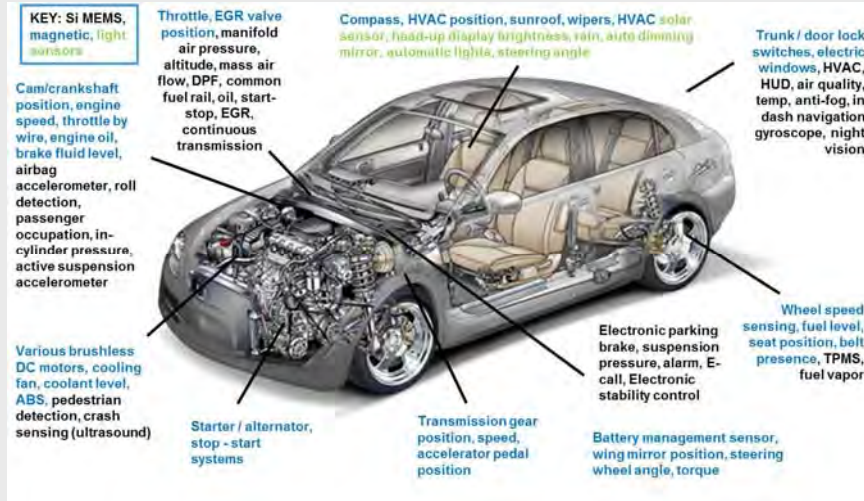
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## Magnetic sensor applications



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## Magnetic sensors in a car

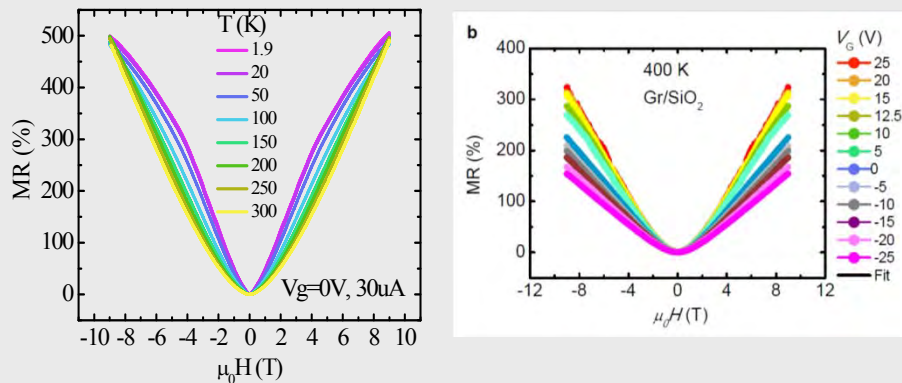


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## Graphene magnetic sensors



Temperature insensitive giant magneto-resistance (MR)  
 Gate tunable property  
 Giant MR is explained by inhomogeneous charge distribution

Phys. Rev. B **88**, 195429 (2013)



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## Systems showing linear MR

1. InSb Nat. Mater. 7, 697 (2008), Science **289**, 1530 (2000)
2. Ag<sub>2</sub>Te and Ag<sub>2</sub>Se Nature **390**, 57 (1997)
3. (Multilayer) graphene Nat. Comm. **6**, 8337 (2015), Phys. Rev. B 88, 195429 (2013)  
Nano Lett. **10**, 3962 (2010)
4. TI (Bi<sub>2</sub>Se<sub>3</sub>, Bi<sub>2</sub>Te<sub>3</sub>) APL **102**, 012102 (2013), PRL **108**, 266806 (2012)
5. Weyl-WTe<sub>2</sub> Nature **514**, 205 (2014)

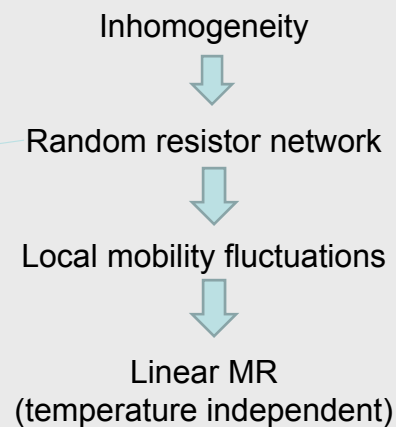
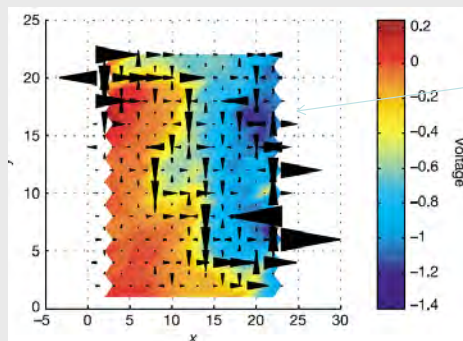
## Theoretical explanation of linear MR

- Classical model Nature **426**, 162 (2003)
- Quantum model PRB **58**, 2788 (1998)



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## Classical model



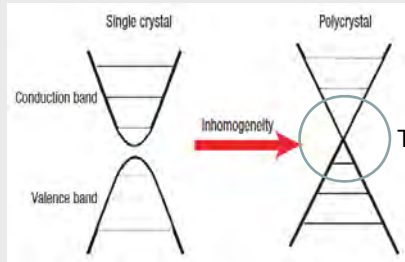
Nature **426**, 162 (2003), Nature **477**, 304 (2011)



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## Quantum model

Low band-gap + small eff. mass



$$\rho_{xx} = \rho_{yy} = \frac{N_H}{\pi n^2 e c}$$

Inhomogeneity

$$\hbar\omega > E_F$$

Tail formation

Linear E-k

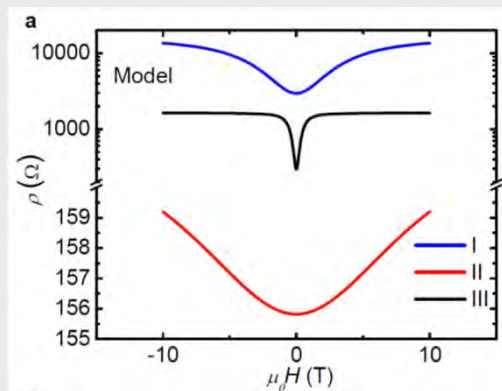
Linear MR  
(temperature independent)



Abrikosov, A. A. Quantum magnetoresistance. *Physical Review B* **58**, 2788 (1998)

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## Two channel model



High sensitivity at low field is important for applications

$$MR_{\infty} \approx \frac{n_1 n_2}{(n_1 + n_2)^2} \frac{\mu_1}{\mu_2} \gg 1$$

- Case I  $m_1=10^{11} \text{ cm}^{-2}, m_2=1.1 \times 10^{11} \text{ cm}^{-2}, \mu_1=20,000 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}, \mu_2=1,000 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$
- Case II  $m_1=8 \times 10^{12} \text{ cm}^{-2}, m_2=1.1 \times 10^{11} \text{ cm}^{-2}, \mu_1=5,000 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}, \mu_2=1,000 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$
- Case III  $m_1=10^{11} \text{ cm}^{-2}, m_2=1.1 \times 10^{11} \text{ cm}^{-2}, \mu_1=200,000 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}, \mu_2=10,000 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ .

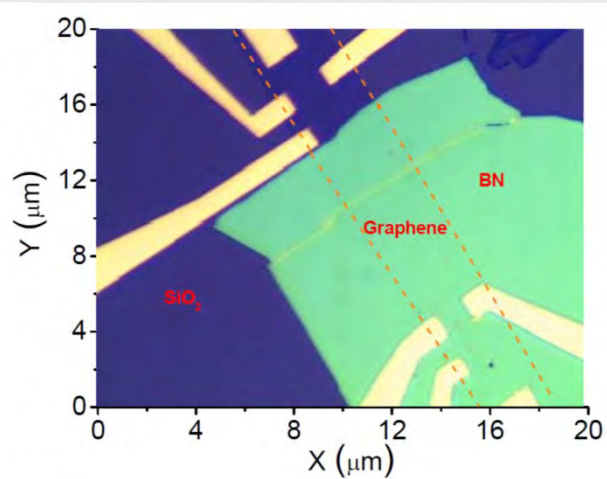
Large mobility difference is important for a large MR



Nat. Comm. **6**, 8337 (2015)

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## BN/graphene heterostructures



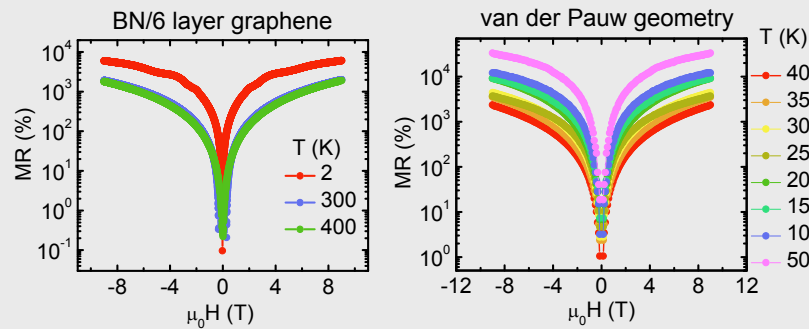
- Boron nitride (BN)/graphene heterostructures can provide a big mobility difference

Nat. Comm. 6, 8337 (2015)



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## Giant MR from BN/graphene heterostructures



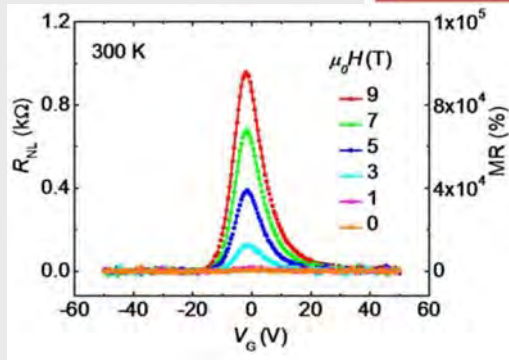
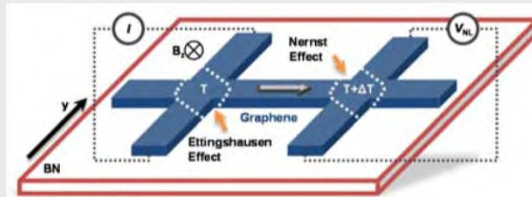
BN/6 layer graphene → Giant local MR of 2000% at 400 K  
 van der Pauw geometry → 35,000% at 50 K

Nat. Comm. 6, 8337 (2015)



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## Non-local MR



4 layer graphene/BN at 300 K  
 non-local MR value of 90,000%  
 Ettingshausen-Nernst effect



Nat. Comm. 6, 8337 (2015)

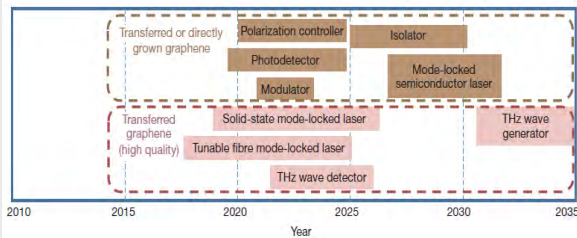
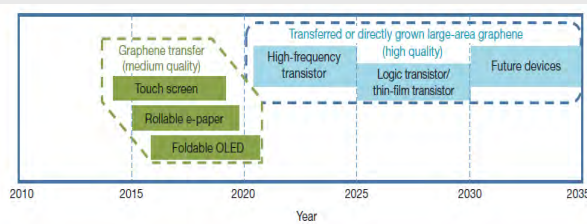
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## Graphene applications

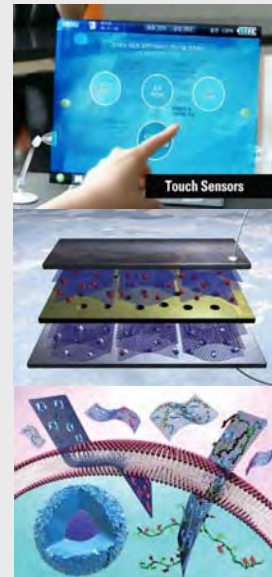
### A roadmap for graphene

K. S. Novoselov<sup>1</sup>, V. L. Fal'ko<sup>2</sup>, L. Colombo<sup>3</sup>, P. R. Geilker<sup>4</sup>, M. G. Schwab<sup>5</sup> & K. Kim<sup>6</sup>

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THz



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## Applications of Terahertz Light

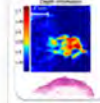
### Stand-off detection of hidden objects and weapons

Safe, non invasive and quick imaging through different types of clothing, concealments and other confusion materials.



### Non-invasive medical and dental diagnostics

High-sensitivity, safe detection of cancerous tissue and dental caries for earlier and more accurate diagnosis.



### Drug discovery and formulation analysis of coatings and cores

In-line control of pharmaceutical products for better understanding of product and process design.



### Characterisation of electron carriers and metamaterials

Improving the performance and quality of solid-state properties of semiconductors and metamaterials.



### Non-contact material integrity imaging of coatings and composites

Imaging of coating layers on metal and polymer automotive structures to identify presence of defects in paints.



### Non-destructive rapid fault isolation in IC packages

High-accuracy isolation of shorts, dead opens, and resistive opens for localising defects in complex packages.



### Detection of cracks and defects in solar panels

Inspection and quality control of crucible coatings, silicon and thin films cracks and defects in solar panels.



### Non-contact imaging for conservation of paintings, manuscripts and artefacts

Perform spectroscopic analysis without any contact with valuable and delicate paintings and artefacts.

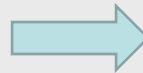


<http://www.teraView.com/applications/>



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## Giant THz machine



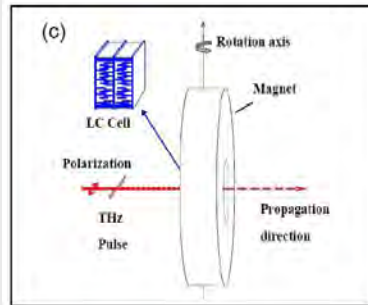
- We need to miniaturize big THz machine.
- For this we need various small THz devices, such as phase shifters, modulators, generators, etc.



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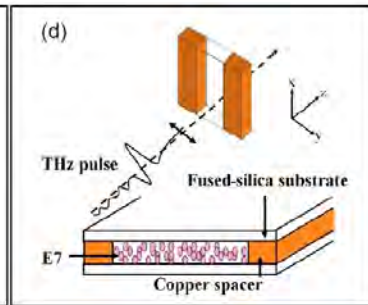
## Problems in conventional THz phase shifters

Bulky magnets required



Chen C. Y. *et al.* Magnetically tunable room-temperature  $2\pi$  liquid crystal terahertz phase shifter. *Optical Express*. (2004)

High voltage (200 V) required

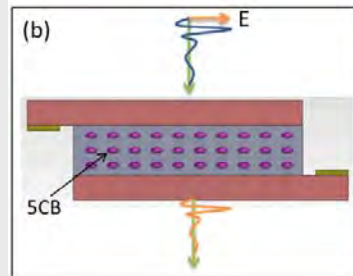
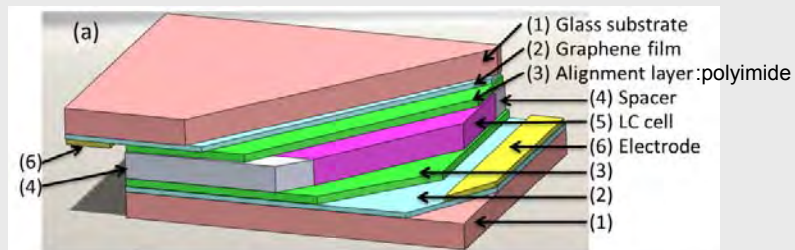


Hsieh C. F. *et al.* Voltage-controlled liquid-crystal terahertz phase shifter and quarter-wave plate. *Optical Letters*. (2006)

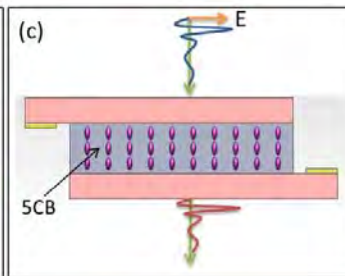


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## Schematic diagram of the THz phase shifters



Without applying voltage



With bias voltage

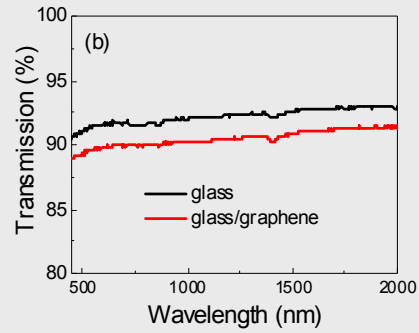
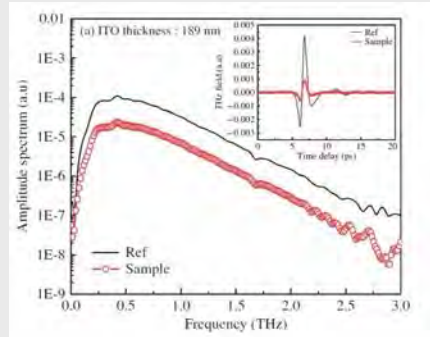


Optics Express 21, 21395 (2013)

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## Transmittance of ITO vs. graphene



Ching-Wei Chen, *et al.* IEEE Journal of Quantum Electronics (2010)

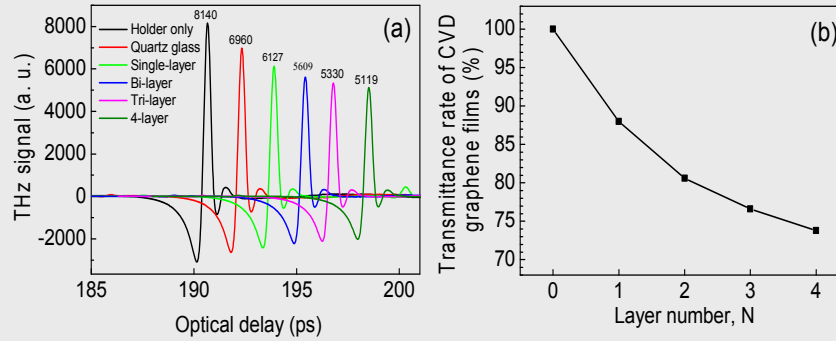
Transparency of ITO films is poor at THz frequencies  
ITO : < 10% transmission at 0.2 -1.2 THz

Graphene: ~98% transmission in visible & NIR  
How about in THz?



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## Transparency of CVD graphene at THz



Pulses are shifted for clarify

- Excellent transmission in THz
- Non-linear transmittance decay
- Uniform absorption within 0.5 – 4 THz

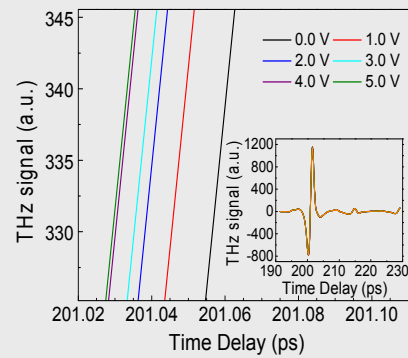


Optics Express 21, 21395 (2013)

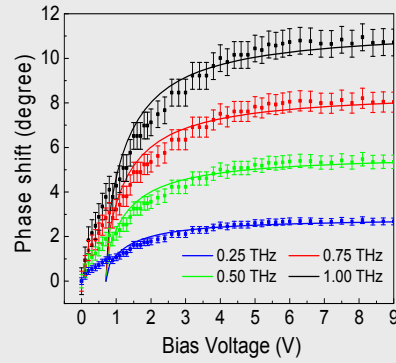
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## THz phase shift measurements

THz time delay under different bias voltages



Voltage controlled phase shifts



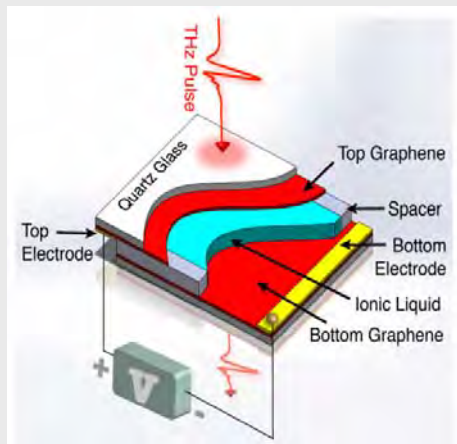
Low bias voltage operation (~ 5 V for saturation).  
Linear controllability in low bias voltages.

Optics Express 21, 21395 (2013)



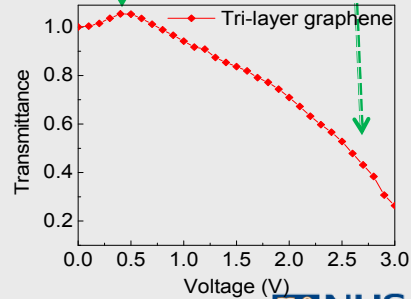
62

## Graphen/ionic liquid THz modulation



Utilizing intra-band absorption

$$\sigma(\omega) = \sigma_{DC}(E_F) / (1 + \omega^2 \tau^2)$$



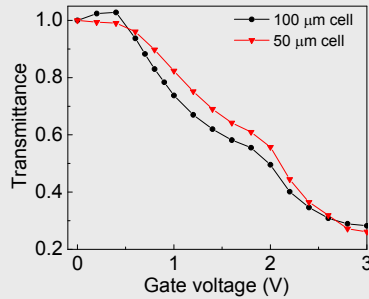
Adv. Mat. 27, 1874 (2015)



64

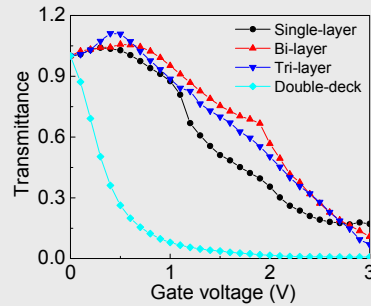
## Geometry & layer thickness dependence study

Modulators with 50  $\mu\text{m}$  & 100  $\mu\text{m}$  ionic liquid cells



Similar modulation depth for devices with different cell thickness

Multilayer & double-deck modulators



Transmittance

- Mono-layer 83%
- Bi-layer 89%
- Tri-layer 93%
- Double deck 99%



Adv. Mat. 27, 1874 (2015)

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## Logic device (switch) applications

For switch applications, on/off current ratio should be

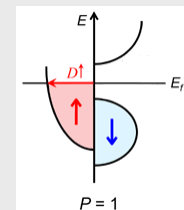
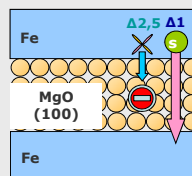
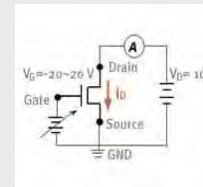
(TFT panel) > 100, Conventional logic CMOS > 1000

Need to increase TMR ( $\rightarrow$  Need a high spin polarization)

$$MR = \frac{R_{AP} - R_P}{R_P} = \frac{2P_1P_2}{1 - P_1P_2}$$

New material for electrodes and barriers

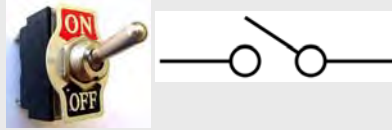
- MgO spin filter (on/off ration < 10)
- Half metals (only at low temp.)



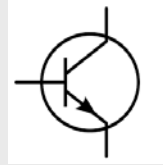
75

## Almost perfect switches/filters → nonreciprocity

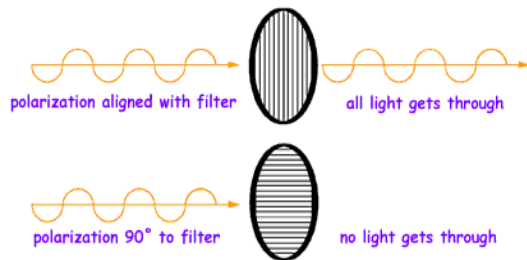
Mechanical switch



Transistor

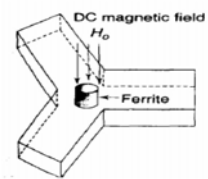


Optical filter



Microwave circulator

3 Port Circulator



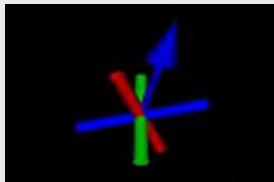
Is there any similar component in spintronics?



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## Describing spin waves

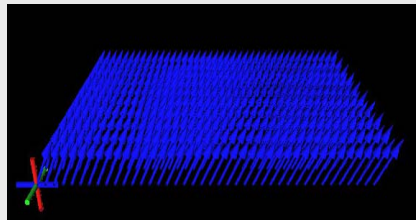
Single electron spin



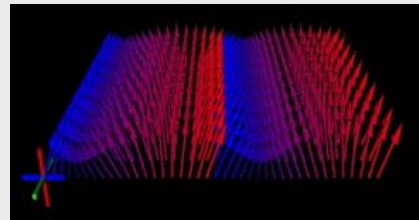
1D chain of (dipolar/exchange) coupled electrons



Collective magnetization dynamics: spin waves



FMR  
Uniform precession (standing waves)

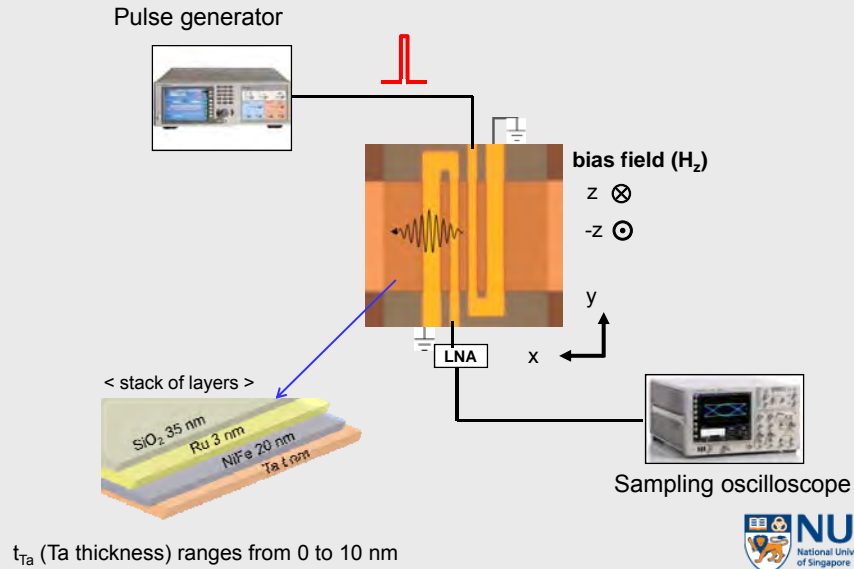


Spin waves  
Travelling waves



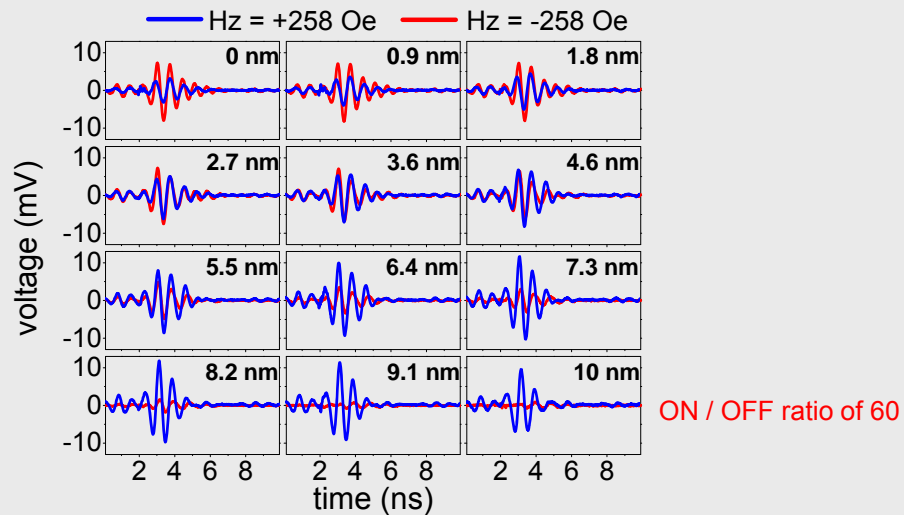
77

## Measurements set-up and layer structure of spin wave device



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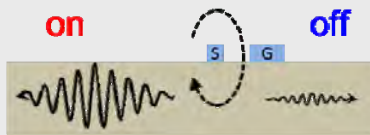
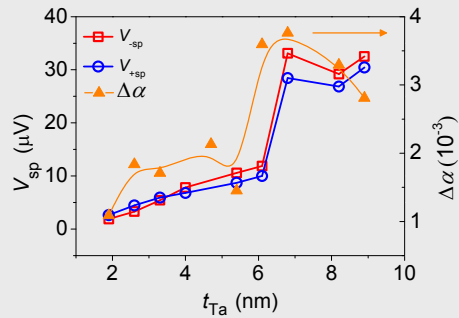
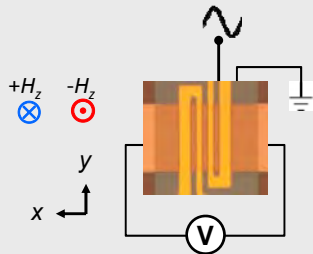
## Giant nonreciprocal emission of spin wave in Ta/Py



- The amplitude at -258 Oe is higher than that at +258 Oe in the device for  $0 < t_{Ta} < 2.7$  nm.
- However, the amplitude at +258 Oe is higher than that at -258 Oe for  $4.6$  nm  $< t_{Ta} < 10$  nm

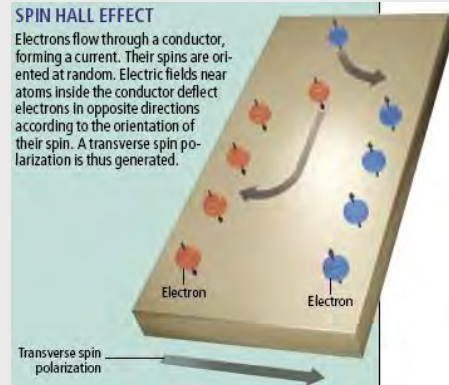
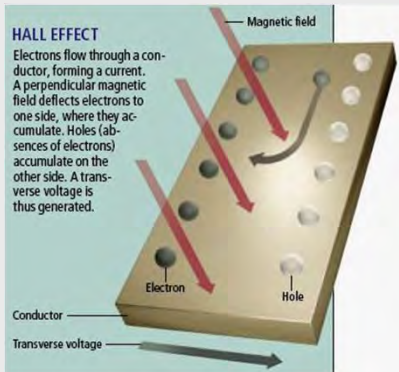
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## Giant nonreciprocity due to spin pumping



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## Hall effect & spin Hall effect (SHE)



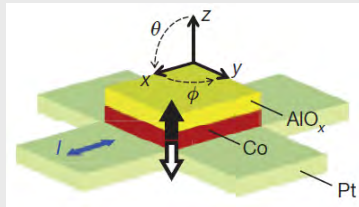
SHE: Separate electrons of different spins **without** using a magnetic field



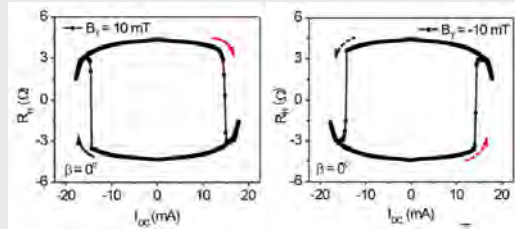
Y.K. Kato, Sci. Am. 2007

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## Spin-orbit torques (SOT)



Miron *et al.* Nature **476**, 189 (2011)



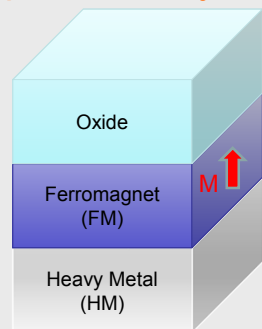
Liu *et al.* PRL **109**, 096602 (2012)

- Heavy metal/ferromagnetic material/oxide layer.
- Current induced magnetization switching is observed (longitudinal field needed).
- Magnetization states depend on both current and field directions.
- Possible mechanisms: Rashba effect & spin Hall effect (SHE).



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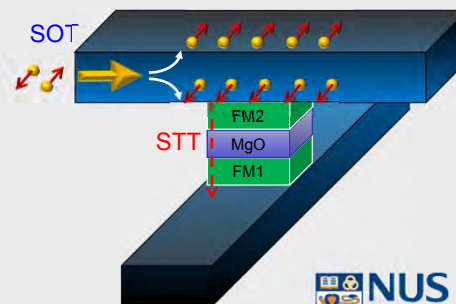
## Perpendicularly magnetized trilayer structures



Strong Rashba field arises from asymmetric interfaces

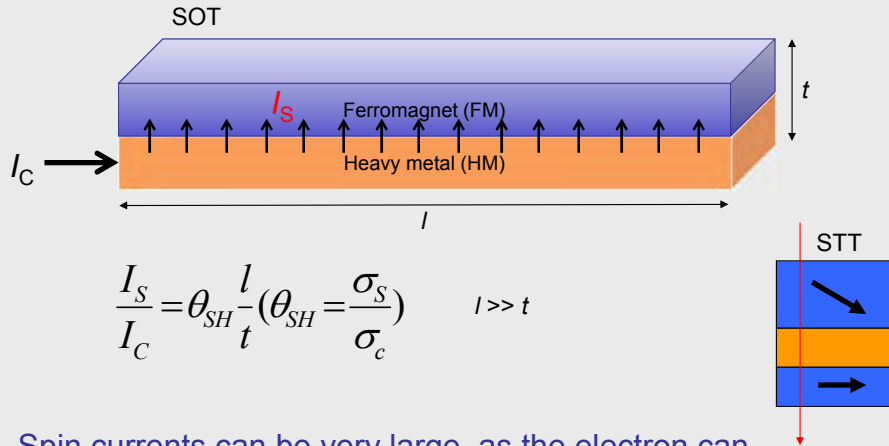
Spin Hall effect arises from HM

In-plane currents can switch the magnetization



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## Spin Hall angle ( $\theta_{SH}$ )

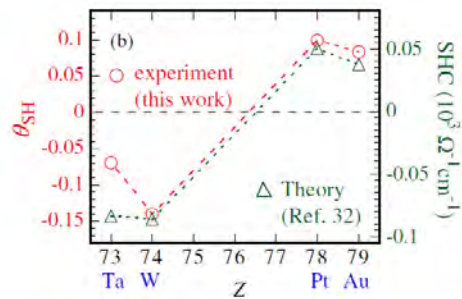
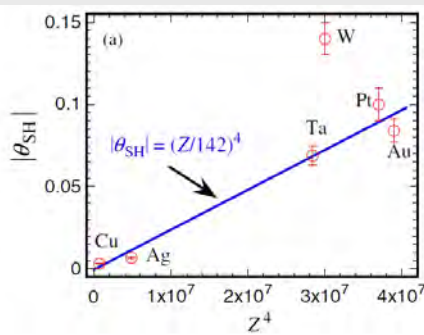


Spin currents can be very large, as the electron can interact with the FM many times (lateral scattering)



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## Spin Hall angle is a material parameter



Number of d-electrons

Luckily some CMOS compatible materials show large spin Hall angles.

PRL **112**, 197201 (2014), Phys. Rev. B **77**, 165117 (2008), Phys. Rev. B **83**, 174405 (2011)

Heavy Weyl semimetals → strong spin orbit coupling

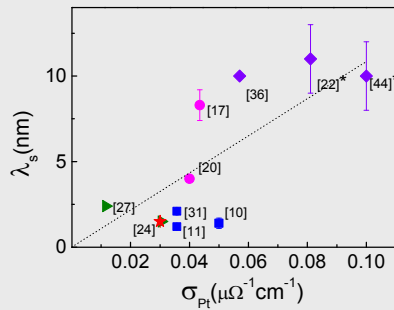
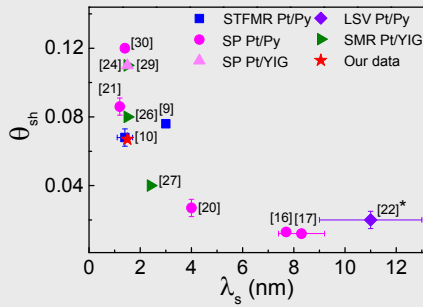


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## Various reported $\theta_{SH}$ in Pt

Is it a constant value for a given material?



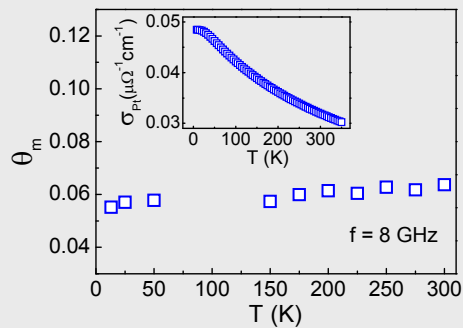
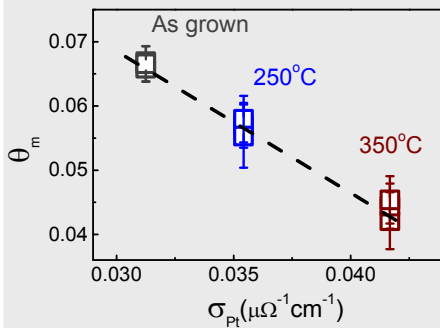
- Relationship of  $\theta_{SH}\lambda_S \sim 0.13 \text{ nm}$  &  $\lambda_S \propto \sigma_{Pt}$
- Can we engineer  $\theta_{SH}$  by changing  $\sigma_{Pt}$ ?



APL 105, 152412 (2014)

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## Spin Hall angle engineering



- Annealing condition can change  $\theta_{SH}$  for the same material.
- Dominant mechanism for  $\theta_{SH}$  in Pt is not intrinsic.
- Can we increase  $\theta_{SH}$ ?

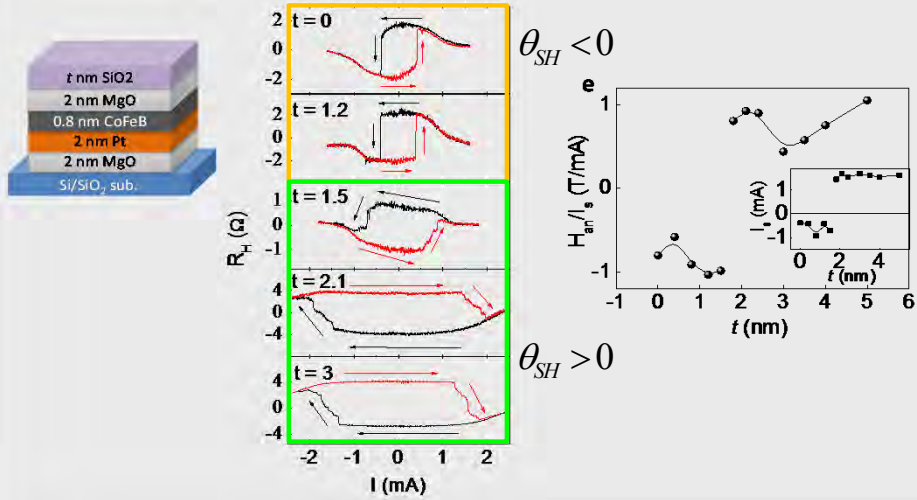


APL 105, 152412 (2014)

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## Spin Hall vs. interfacial Rashba

Reverse switching polarity by oxygen engineering



- Sign of spin Hall angle changes across a transition thickness of SiO<sub>2</sub> ( $t = 1.5$  nm)
- Cannot be understood by spin Hall physics  $\rightarrow$  suggest the role of interface

Nat. Nanotech. 10, 333 (2015)

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## Spin-orbit torque switching currents

The diagram shows a magnetic junction with a Free FM layer, a Spacer, and a Pinned FM layer. A current  $I_1$  flows through the Free FM layer, labeled SOT. A current  $I_2$  flows through the Pinned FM layer, labeled STT.

$$I_c \approx \frac{2e}{\hbar} \left( \frac{\alpha M_S V}{\eta P} \right) H_{eff} \quad \text{STT}$$

$$I_c \approx \frac{e}{\hbar} \left( \frac{M_S t_{FM} A_{HM}}{\theta_{SH}} \right) H_{eff} \quad \text{SOT}$$

K.J.Lee, APL (2013)

- No damping term  $\rightarrow$  great flexibility for choosing FM, high speed
- No spin polarization term  $\rightarrow$  no need to use MgO
- Can use thick MgO  $\rightarrow$  eliminate MgO breakdown issue
- Large spin Hall angle ( $\theta_{SH}$ ) or effective field ( $H_{eff}$ ) is the key

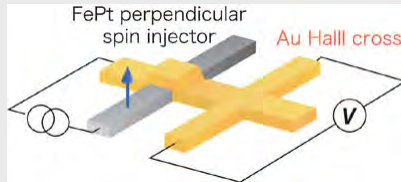
$$H_{eff} = \hbar \theta_{SH} |j_e| / (2|e| M_S t_F)$$



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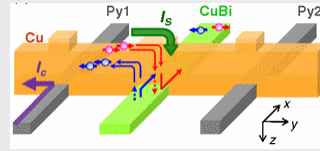
## Large spin Hall angles from various materials

FePt/Au spin Hall angle ( $\theta_{SH}$ ) = 0.1 (Takanashi group)



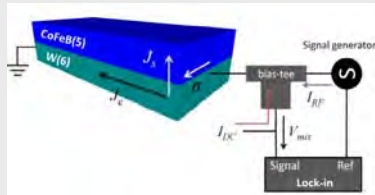
Nat. Mater. 7, 125 (2008)

CuBi  $\theta_{SH} = -0.24$  (Otani group)



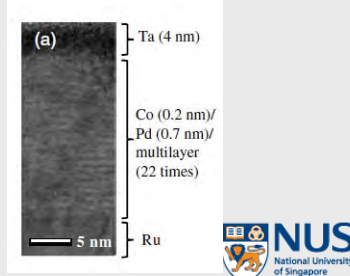
Phys. Rev. Lett. 109, 156602 (2012)

$\beta$ -W  $\theta_{SH} = 0.3$  (Cornell)



Appl. Phys. Lett. 101, 122404 (2012)

Co/Pd multilayer  $\theta_{SH} = 4$  (NUS)



Phys. Rev. Lett. 111, 246602 (2013)

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## Spin orbit torques in Co/Pd multilayers

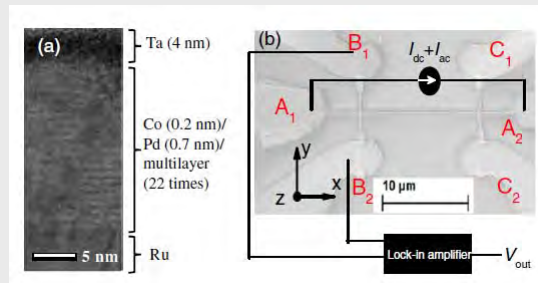
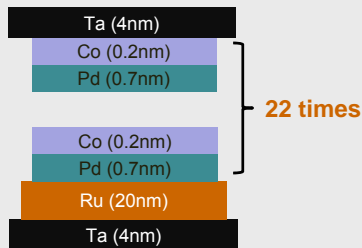


TABLE I. Summary of the reported longitudinal and transverse torque components and the extracted dimensionless coefficients. The values in the brackets indicate the corresponding effective efficiency  $\alpha_{\parallel,\perp}$ . For the present work we used  $t = 20$  nm and  $M_S = 6.23 \times 10^5$  A/m. Note that the torques from Ref. [27] are taken at  $\theta = 0$ .

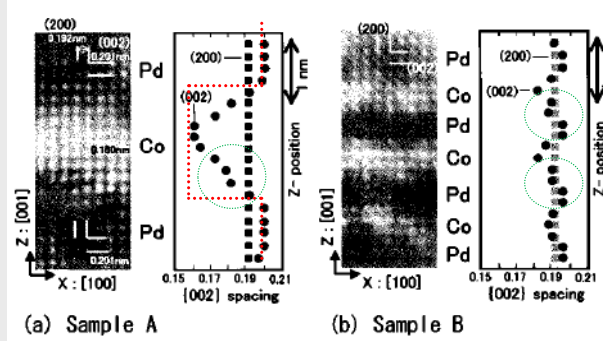
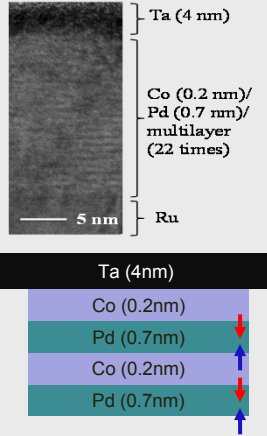
Structure (nm)	$\beta_{\parallel}$ (Oe/ $10^8$ A/cm $^2$ ) [ $\alpha_{\parallel}$ ]	$\beta_{\perp}$ (Oe/ $10^8$ A/cm $^2$ ) [ $\alpha_{\perp}$ ]	$\beta_{\perp}/\beta_{\parallel}$	Ref.
Ta(4)/Co $_{40}$ Fe $_{40}$ B $_{20}$ (1)/MgO(1.6)	350 [0.12]	-	-	[6]
Ta(3)/Co $_{30}$ Fe $_{30}$ B $_{20}$ (0.9)/MgO(2)	240 [0.07]	450 [0.13]	1.9	[27]
Ta(1.5)/Co $_{40}$ Fe $_{40}$ B $_{20}$ (1)/MgO(1.6)	135 [0.078]	472 [0.27]	4	[10]
Pt(3)/Co(0.6)/AlO $_x$ (1.6)	690 [0.13]	400 [0.073]	0.58	[27]
Ta(4)/Ru(20)/(Co/Pd) $_{22}$ /Ta(4)	1170 [4.4]	5025 [19.1]	4.3	This work

Phys. Rev. Lett. 111, 246602 (2013)

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## Structural asymmetry can be added up

TEM data



Maesaka, IEEE Trans. Magn. 38, 2676 (2002)

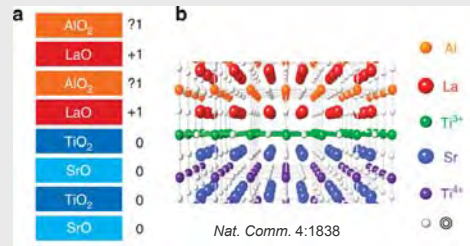
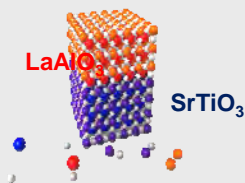
- Two successive Co/Pd and Pd/Co interfaces are structurally dissimilar.
- Lattice mismatch (9%) between Pd and Co



Phys. Rev. Lett. 111, 246602 (2013)

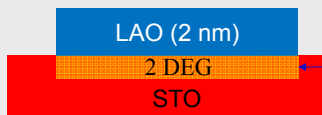
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## LAO/STO – 2DEG formation



LaAlO<sub>3</sub> grown on TiO<sub>2</sub> terminated SrTiO<sub>3</sub> (100)

- SrTiO<sub>3</sub> (Insulator 3.2 eV)
- LaAlO<sub>3</sub> (Insulator 5.6 eV)

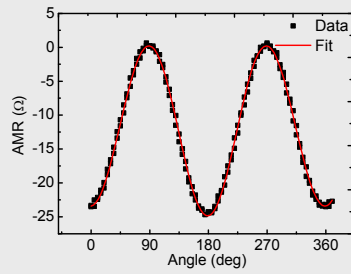
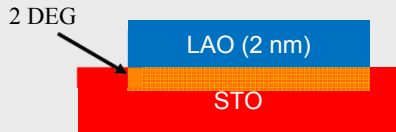


2 DEG formed inside the STO side

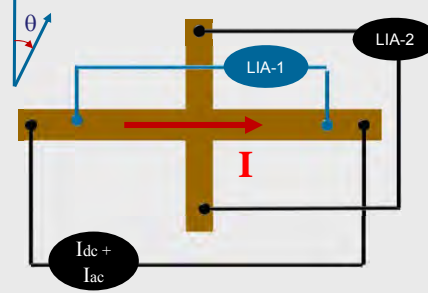


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## Magnetism in LaAlO<sub>3</sub>/SrTiO<sub>3</sub> heterostructures



In-plane angular measurements



AMR measurements at  $H = 9$  T,  $T = 4$  K

$$R_{XX} = a_0 + a_1 \cos^2(\theta + \phi) + a_2 \cos^4(\theta + \phi)$$

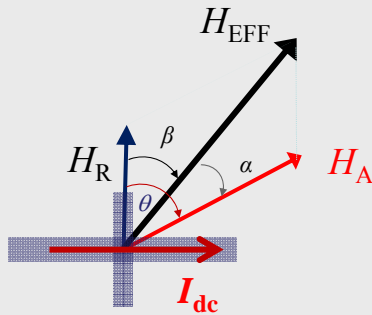
$a_0, a_1, a_2$  are constants



Appl. Phys. Lett. 105, 162405 (2014)

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## Asymmetric spin-orbit fields



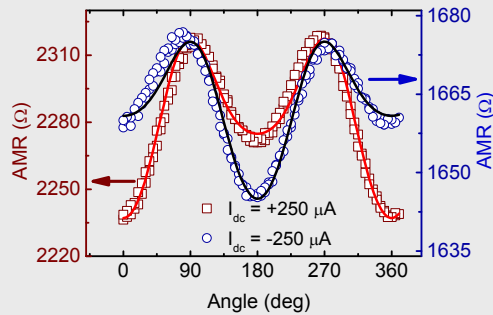
$$H_{EFF}^2 = H_A^2 + H_R^2 + 2H_A H_R \cos \theta$$

$$R_{XX} = b_0 + b_1 H_{EFF} \cos^2 \alpha + b_2 H_{EFF} \cos^4 \alpha$$

$H_R, H_A, H_{EFF}$  are Rashba, applied and effective fields

$b_0, b_1, b_2$  are constants

Appl. Phys. Lett. 105, 162405 (2014)



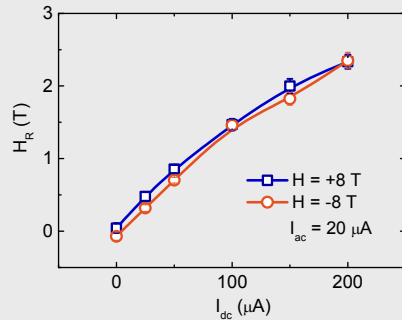
$$H_R (+I) = 1.26 \text{ T}$$

$$H_R (-I) = -1.48 \text{ T}$$



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## Current induced spin-orbit fields in 2DEG



Assuming thickness of 2DEG  
 $t_{2\text{DEG}} = 7 \text{ nm}$   
*Nat. Mater.* 7, 621 (2008)

current density =  $7.14 \times 10^8 \text{ A/m}^2$

2.35 T @ 200  $\mu\text{A}$   
 $\rightarrow 32.9 \text{ Tesla}/10^6 \text{ A/cm}^2$

The highest current induced torque reported in metallic system is only 0.5 T.

PRL 111, 246602 (2013)

$$\alpha_R = \sqrt{\hbar^3 e H_{so} / m^{*2}} \quad H_{so} = 1.48 \text{ T}, \alpha_R = 12 \text{ meV}\cdot\text{\AA}, \text{ spin splitting } \Delta = 3 \text{ meV } (\sim 30 \text{ T})$$

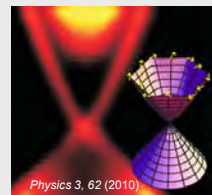
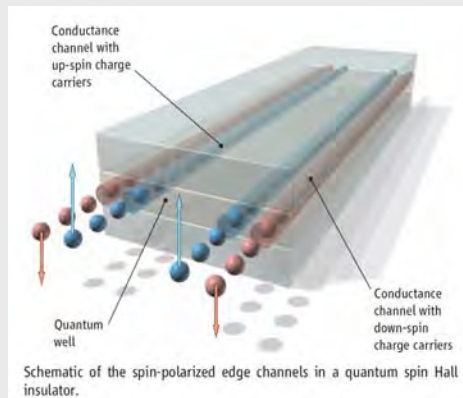
cf. Co/Pd multilayer  $\alpha_R = 360 \text{ meV}\cdot\text{\AA}$



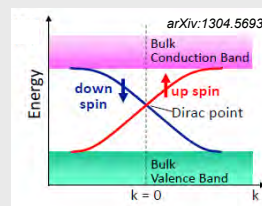
Appl. Phys. Lett. 105, 162405 (2014)

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## Topological insulators (TIs)



ARPES spectra showing a linear band structure of the surface states on a 3D TI



□ Linear dispersion

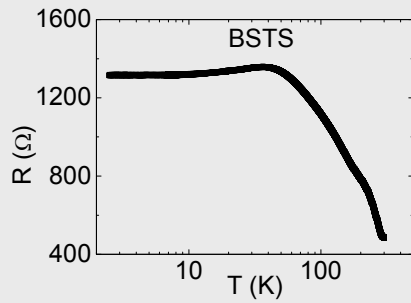
- Spin polarized surface currents
- Spin-momentum locking  $\rightarrow$  giant spin Hall angle ?



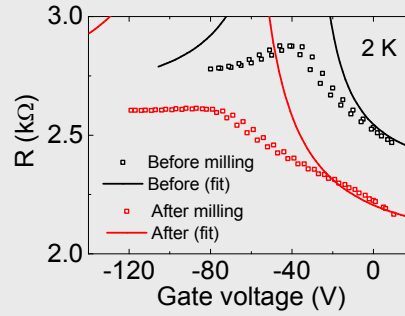
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## BiSbTeSe<sub>2</sub> topological insulators

Can TI survive after etching process?



BiSbTeSe<sub>2</sub> is semiconducting



Sample has become more heavily n-doped after ion milling

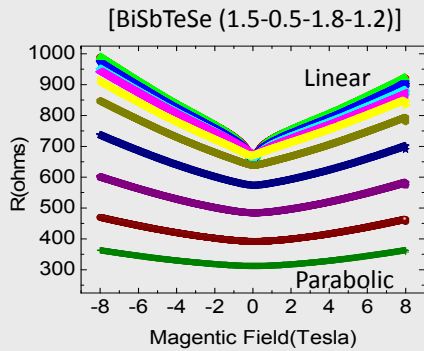
- Charged impurity density ( $n_{imp}$ ):  $7 \times 10^{12} \rightarrow 1.33 \times 10^{13}/\text{cm}^2$
- Carrier concentration:  $2.36 \times 10^{13} / \text{cm}^2 \rightarrow 5.53 \times 10^{13} / \text{cm}^2$
- Mobility ( $\mu_e$ ):  $106 \rightarrow 52 \text{ cm}^2/(\text{V}\cdot\text{s})$



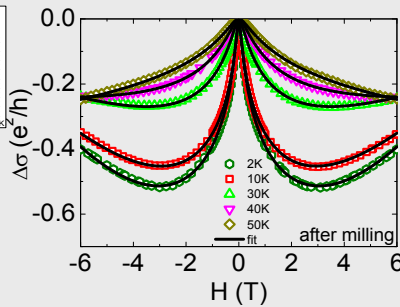
Phys. Rev. B, **90**, 235427 (2014)

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## Ar ion milling effects



Linear MR at LT  
Parabolic MR at RT



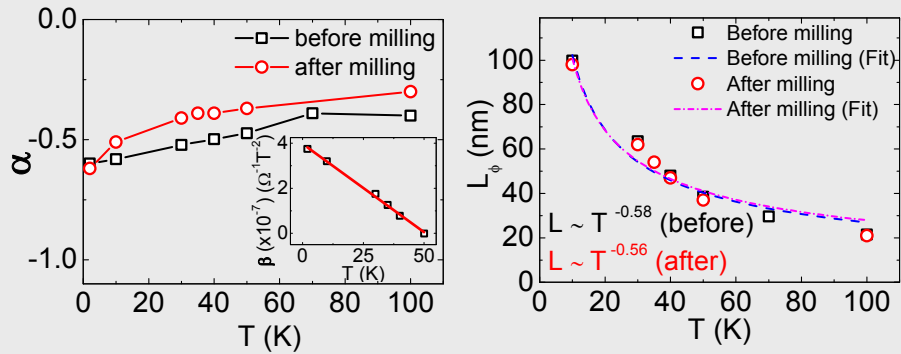
Negative MR originates from disorder



Phys. Rev. B, **90**, 235427 (2014)

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## Robustness of the topological surface states



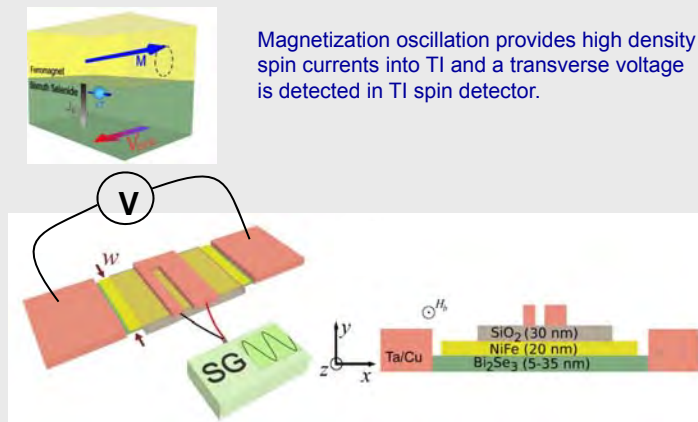
- A decay constant of -0.5 in  $L_\phi$  indicates two-dimensional (2D) electron-electron scattering for the sample before and after milling.
- The behavior of surface states is unaffected by the introduction of disorder, as inferred from the similar values of  $\alpha$  and the behavior of  $L_\phi$ .
- Surface states are remarkably robust against external damage induced by ion milling.



Phys. Rev. B, **90**, 235427 (2014)

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## Experimental setup



Magnetization oscillation provides high density spin currents into TI and a transverse voltage is detected in TI spin detector.

- Signal generator to excite magnetization dynamics in NiFe through a coplanar waveguide
- Voltmeter to measure spin pumping induced ISHE
- Vector network analyzer for FMR measurements

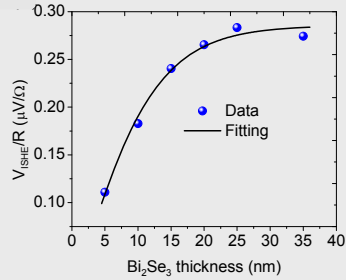
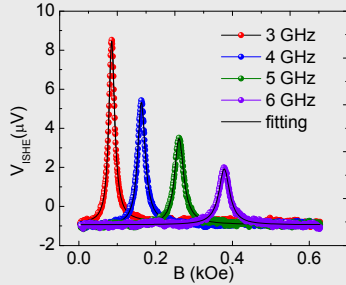


Phys. Rev. B **90**, 094403 (2014)

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## ISHE measurements



$$V_{ISHE} \sim R \cdot J_s \cdot \theta_{SH}$$

$$\frac{V_{ISHE}}{R} = \theta_{sh} w d_{BiSe} \left( \frac{2e}{\hbar} \right) \frac{\hbar g_{r\uparrow\downarrow} \gamma^2 \hbar^2}{8\pi\alpha^2 (M^2 \gamma^2 + 4\omega^2)} \left( M\gamma + \sqrt{M^2 \gamma^2 + 4\omega^2} \right) \frac{\lambda_{sf}}{d_{BiSe}} \tanh\left(\frac{d_{BiSe}}{2\lambda_{sf}}\right)$$

$R$  is resistance of the film  
 $J_s$  is induced spin current  
 $\theta_{SH}$  is spin Hall angle

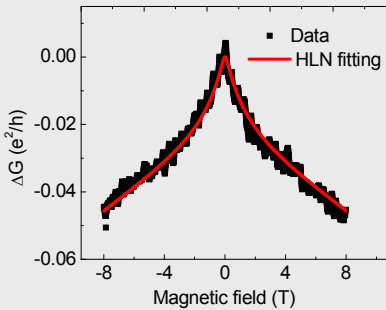
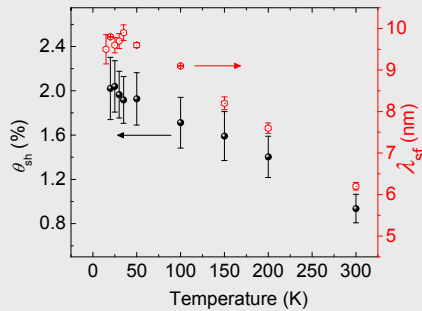
$$\Rightarrow \begin{cases} \theta_{sh} = 0.01 \\ \lambda_{sf} = 6.2 \text{ nm} \end{cases}$$

Phys. Rev. B **90**, 094403 (2014)



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## Extracted spin Hall angle



Spin orbit length,  $l_{so} = 6.9 \text{ nm}$

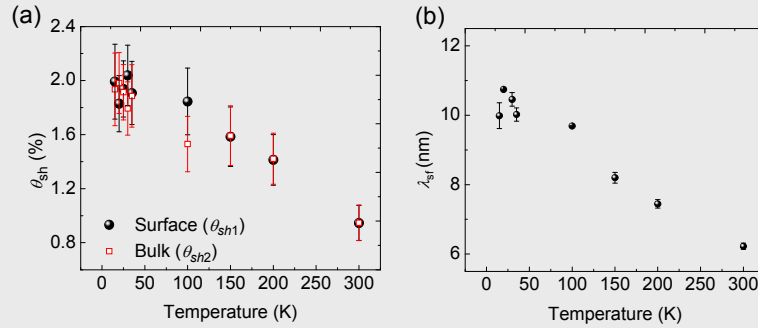
- 1-2% of spin Hall angle is identified, which is already comparable to the best data from heavy metals (Pt, Ta).
- $l_{so} \sim \lambda_{sf}$  suggest that spin-orbit coupling is dominant source of spin scattering

Phys. Rev. B **90**, 094403 (2014)



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## No spin momentum locking



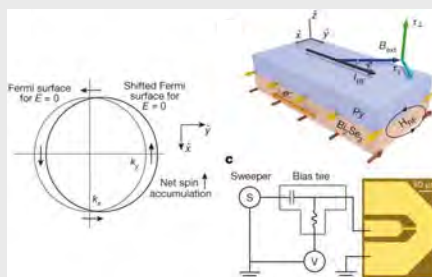
- Assumed spin Hall angle at opposite surfaces was taken to be of opposite signs.
- Spin Hall angle does not show any clear distinction between the surface and bulk value
- Momentum locking signature is not detected.

Phys. Rev. B **90**, 094403 (2014)



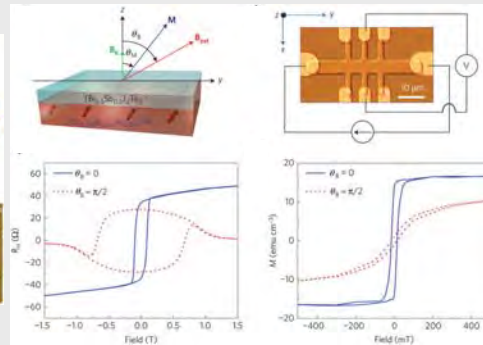
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## Comparison with other reports



Nature **511**, 449 (2014)

Spin torque ferromagnetic resonance measurements  $\rightarrow \theta_{SH} = 2.0 - 3.5$



Nat. Mater. **13**, 699 (2014)

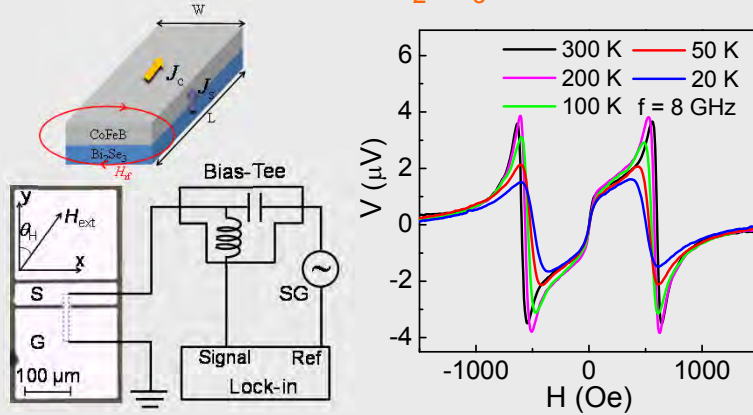
Magnetization switching by current induced spin orbit torque  $\rightarrow \theta_{SH} = 140 - 425$

In these experiments, a charge current flows through the TI material, unlike ours.



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## ST-FMR measurement of Bi<sub>2</sub>Se<sub>3</sub>/CoFeB



- ST-FMR measurements with a lock-in amplifier at  $\theta_H = 35^\circ$ .
- ST-FMR signal ( $V_{\text{mix}}$ ) can be fitted by a sum of symmetric and antisymmetric Lorentzian functions:

$$V_{\text{mix}} = V_s F_{\text{sym}}(H_{\text{ext}}) + V_a F_{\text{asym}}(H_{\text{ext}})$$

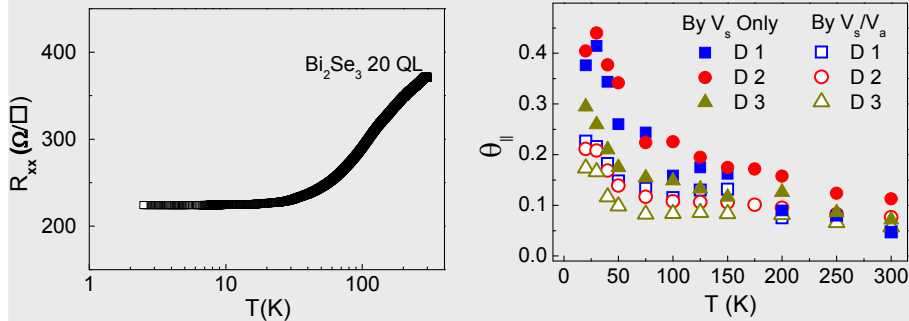
$V_s$ : in-plane torque  $\tau_{\parallel}$  on CFB  
 $V_a$ : total out-of-plane torque



PRL 114, 257202 (2015)

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## In-plane spin-orbit torque ratio in Bi<sub>2</sub>Se<sub>3</sub>/CoFeB



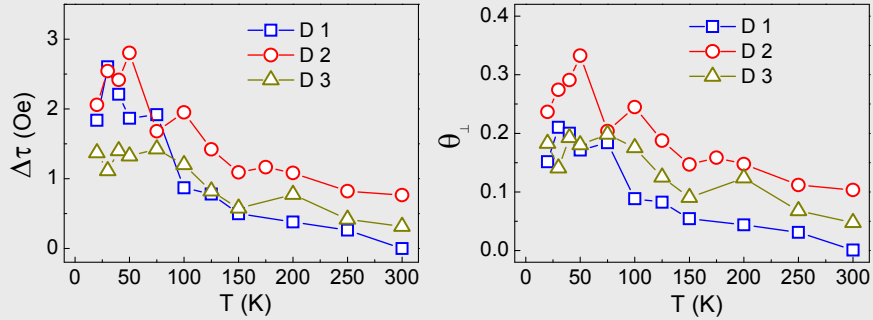
- $\tau_{\parallel}(\theta_{\parallel})$  increases steeply and nonlinearly to  $\sim 0.42$  at low temperature and could be almost 10 times larger than that at 300 K.
- The polarization direction of  $\tau_{\parallel}$  is consistent with spin-momentum-locked TSS.
- $\theta_{\parallel}$  by 1<sup>st</sup> and 2<sup>nd</sup> methods shows a significant difference below  $\sim 50$  K, other out-of-plane torque may contribute besides  $\tau_{\text{Oe}}$ .



Wang *et al.*, PRL 114, 257202 (2015)

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## Out-of-plane spin-orbit torque ratio in Bi<sub>2</sub>Se<sub>3</sub>/CoFeB



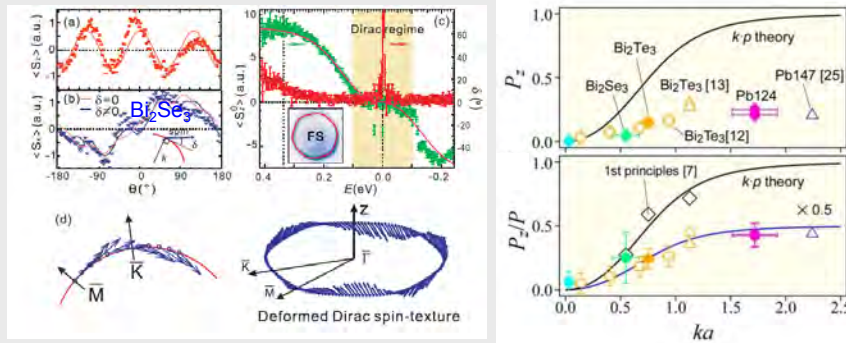
- $\Delta\tau(\theta_{\perp})$  also increases at low temperature similar to  $\tau_{\parallel}(\theta_{\parallel})$ .
- Rashba-split state in 2DEG of Bi<sub>2</sub>Se<sub>3</sub> is not the main mechanism for  $\Delta\tau$ .
- Hexagonal warping in the TSS of Bi<sub>2</sub>Se<sub>3</sub> can account for  $\Delta\tau(\theta_{\perp})$ .



Wang *et al.*, PRL **114**, 257202 (2015)

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## Out-of-plane torque in Bi<sub>2</sub>Se<sub>3</sub>



Wang *et al.*, PRL **107**, 207602 (2011)

Nomura *et al.*, PRB **89**, 045134 (2014)

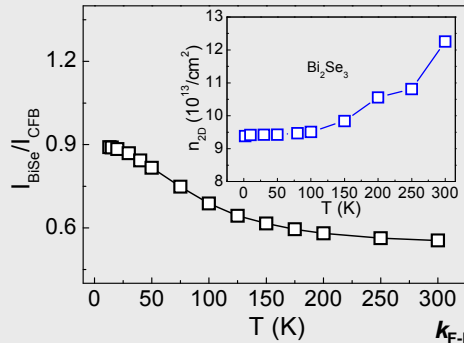
-Recent reports showed there is substantial out-of-plane spin polarization due to Hexagonal warping.

-Hexagonal warping in the TSS of Bi<sub>2</sub>Se<sub>3</sub> can account for  $\Delta\tau(\theta_{\perp})$ .



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## Estimation of $\theta_{||}$ from topological surface states (TSS)



$$k_{F-TSS} \sim 0.14 - 0.17 \text{ \AA}^{-1}$$

$$k_{F-2DEG} \sim 0.1 - 0.12 \text{ \AA}^{-1}$$

$$n_{2D} = 2n_{TSS} + 2n_{2DEG} + n_{bulk}d$$

$$n_{TSS} \sim 1.56 - 2.3 \times 10^{13} \text{ cm}^{-2}$$

$$n_{2DEG} \sim 1.59 - 2.3 \times 10^{13} \text{ cm}^{-2}$$

$$n_{bulk} \sim 1 - 3.1 \times 10^{19} \text{ cm}^{-3}$$

$$(\sim 1 - 3.1 \times 10^{13} \text{ cm}^{-2})$$

$$k_{F-bulk} \sim 0.066 - 0.097 \text{ \AA}^{-1}$$

$$k_{F-bulk} < k_{F-2DEG} < k_{F-TSS} \text{ and } n_{2DEG} < 2 n_{TSS}$$

By estimating  $I_{TSS} : I_{2DEG} : I_{bulk}$ ,  $\theta_{||}$  from only TSS at low temperature is  $\sim 2.1 \pm 0.39$  (with bulk contribution)  $\sim 1.62 \pm 0.18$  (without bulk contribution)

If we assume TSS thickness  $\sim 1$  nm, the 2D spin orbit torque efficiency

$$\lambda_{SOT} \sim 0.8-1.05 \text{ nm.}$$

$$\lambda_{IREE} \sim 0.2-0.33 \text{ nm in Ag/Bi interface [Nat. Commun. 4, 2944 (2013)]}$$

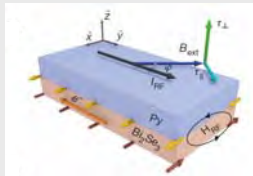


Wang et al., PRL 114, 257202 (2015)

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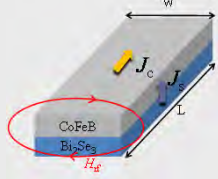
## Exotic spin Hall angles from topological insulators

spin Hall angle ( $\theta_{SH}$ ) = 2~3.5  
ST-FMR (Cornell)



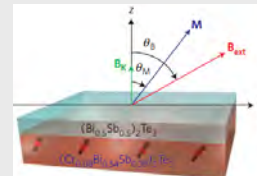
Nature 511, 449 (2014)

$\theta_{SH} = 2$  (low temp)  
ST-FMR (NUS)



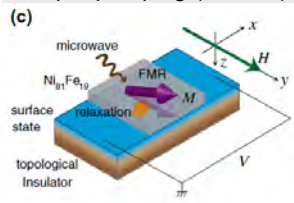
PRL 114, 257202 (2015)

$\theta_{SH} = 140-425$  (low temp)  
spin-orbit switching (UCLA)



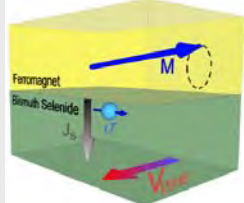
Nat. Mater. 13, 699 (2014)

$\theta_{SH} = 0.01$   
Spin-pumping (Tohoku)



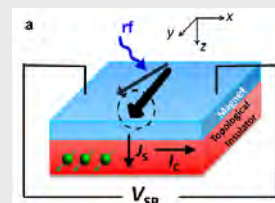
PRL 113, 196601 (2014)

$\theta_{SH} = 0.01$   
Spin-pumping (NUS)



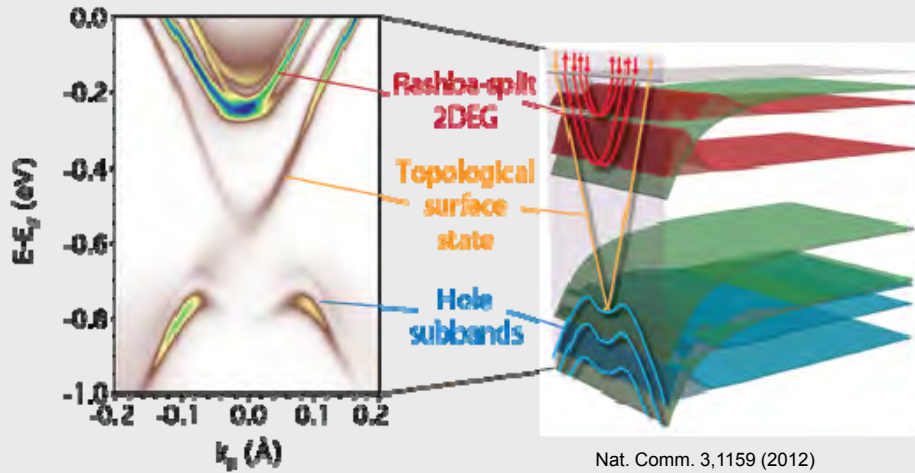
PRB 90, 094403 (2014)

$\theta_{SH} = 0.01-0.4$   
Spin-pumping (Minnesota)



Nano Lett 15, 7126 (2015) 180

## Coexistence of surface states and Rashba bands



Nat. Comm. 3,1159 (2012)

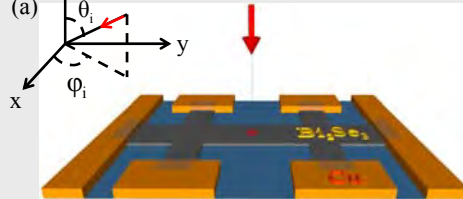
Surface vs. bulk contribution to spin Hall angle ?



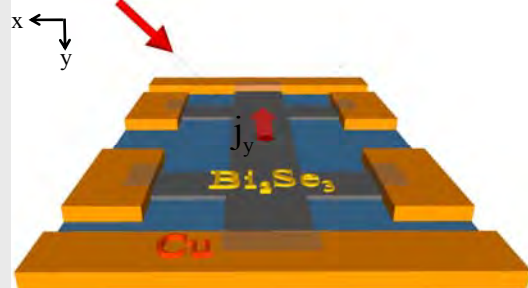
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## Spin dependent photocurrents in $\text{Bi}_2\text{Se}_3$

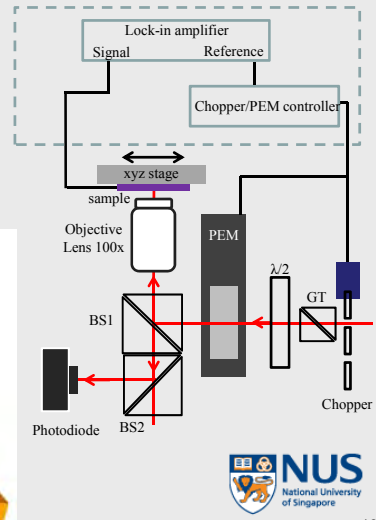
(a) Normal incidence  $\theta_i = 0^\circ$   $\varphi_i = 0$



(b) Oblique incidence  $\theta_i = 45^\circ$   $\varphi_i = 0$



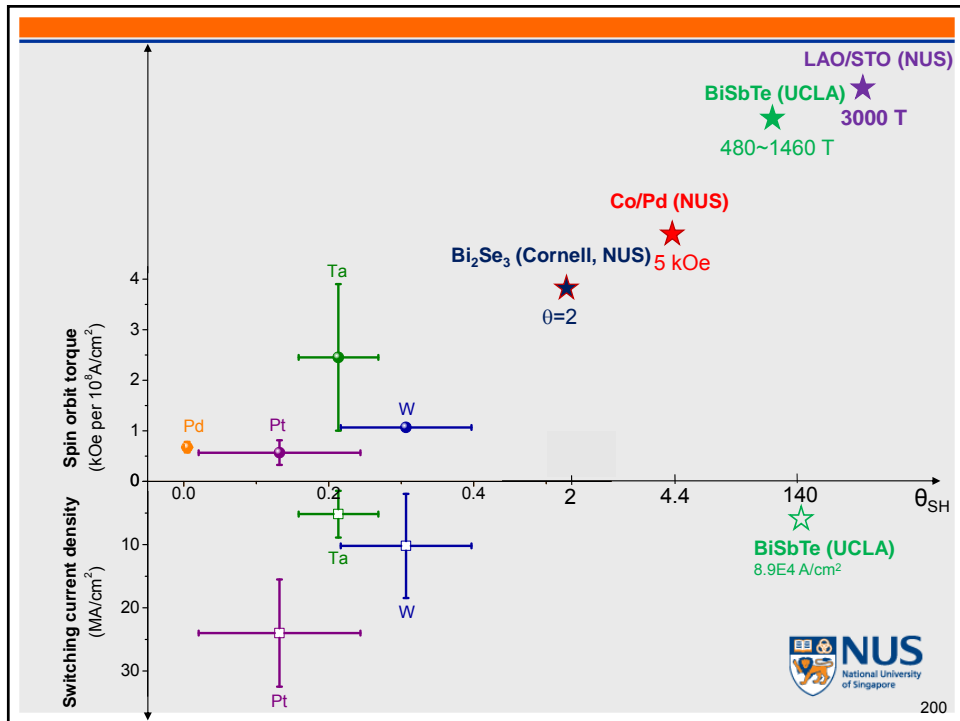
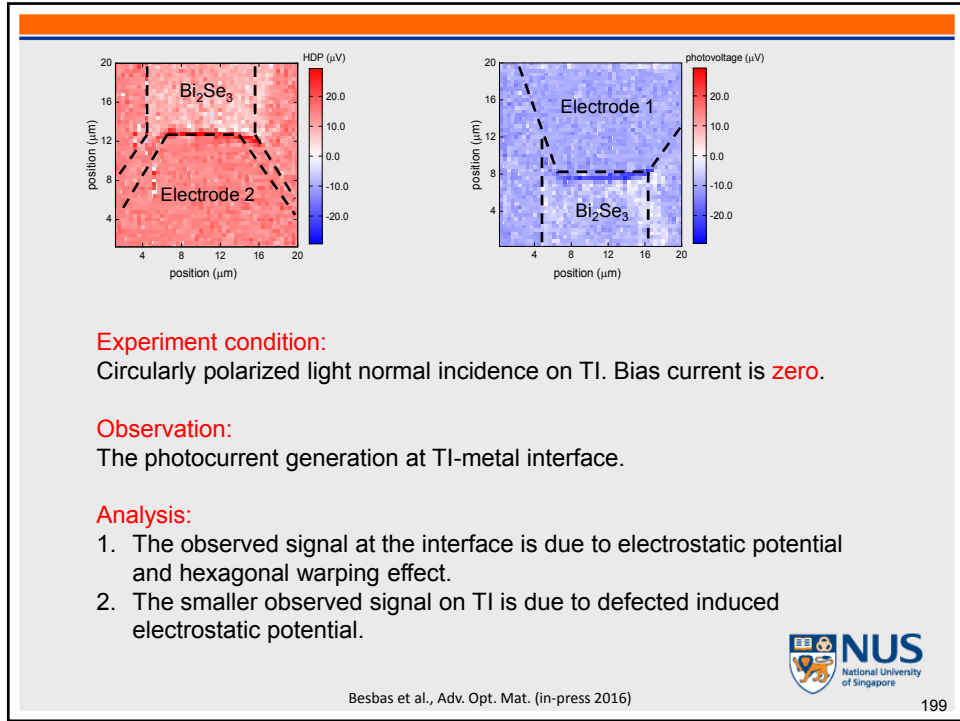
(c)



Besbas et al., Adv. Opt. Mat. (in-press 2016)



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## Open questions

- What is beyond band structures in Dirac/Weyl field?
- Can we make useful devices?
- Then what properties do we need to utilize?
  - Spintronics – spin momentum locking
  - Optoelectronics (THz) – intraband transition



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Aurelien Manchon (KAUST)  
Lan Wang (RMIT Univ.)  
K-J. Lee (Korea Univ.)



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