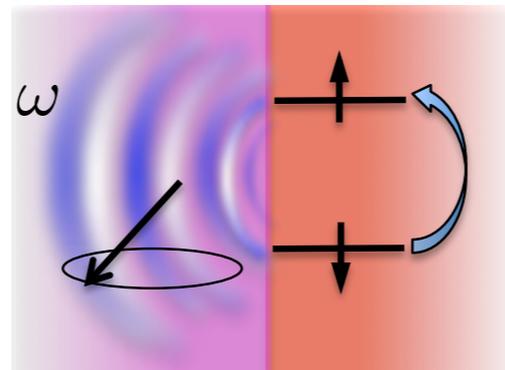


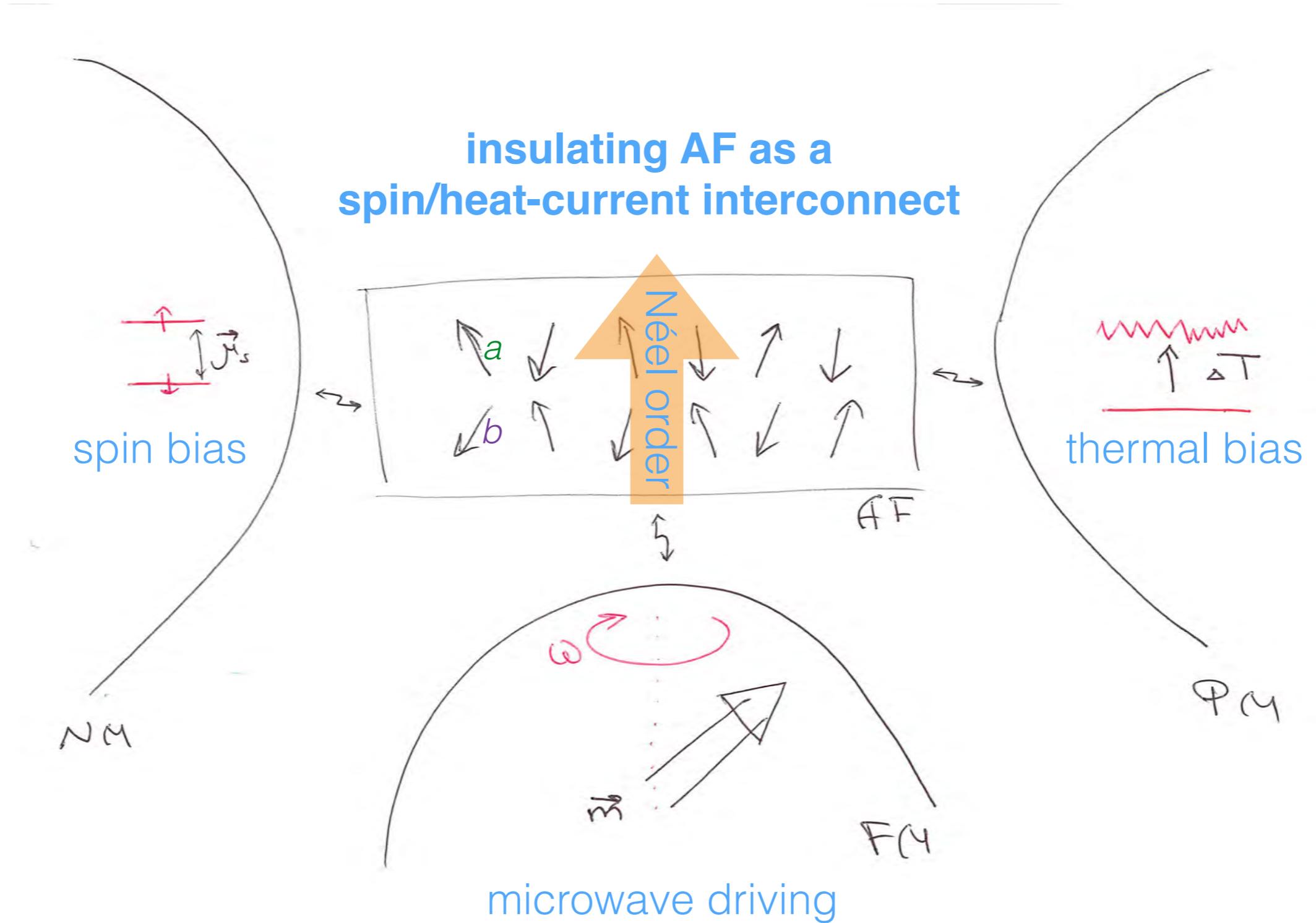
Collective spin transport through antiferromagnets

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Bert Halperin and Amir Yacoby (Harvard), Teruo Ono (Kyoto) and Eiji Saitoh (Tohoku)*



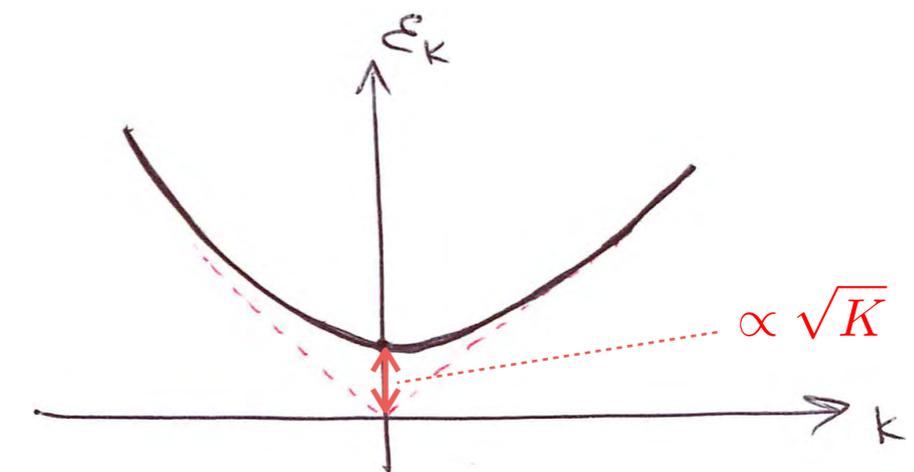
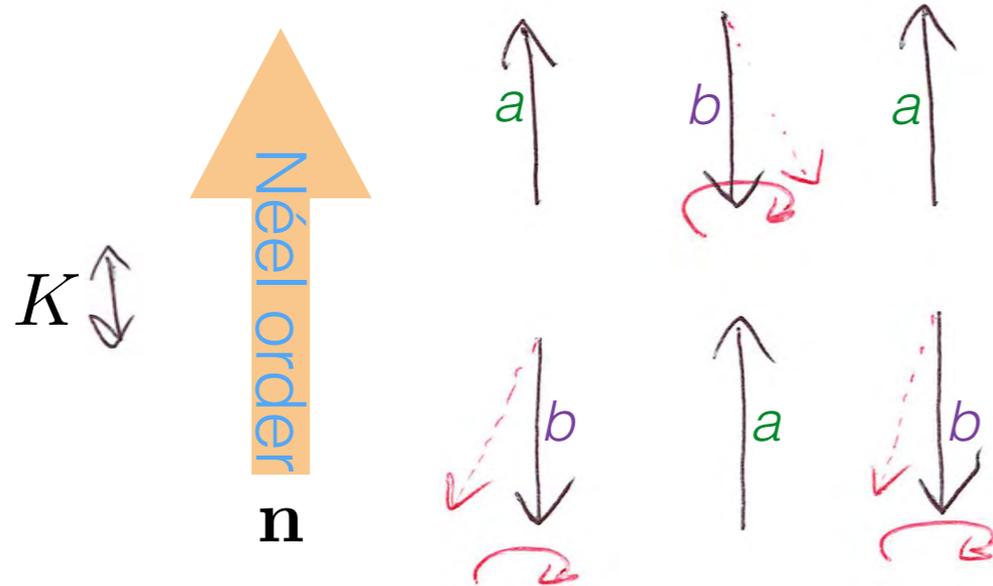
Scope



\Rightarrow two-“fluid” dynamics

Two types of spin current

easy-axis AF



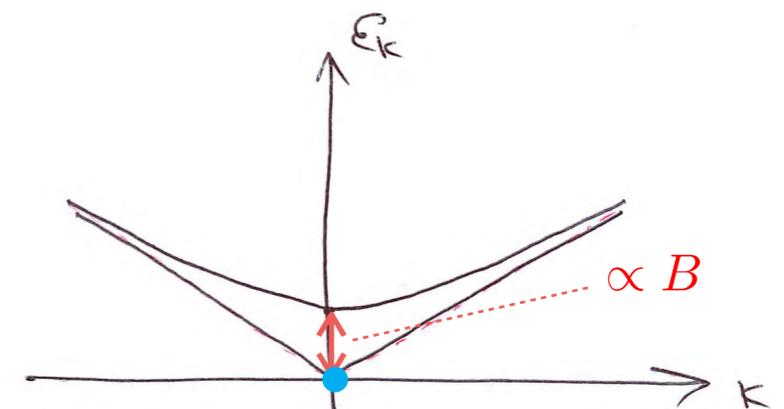
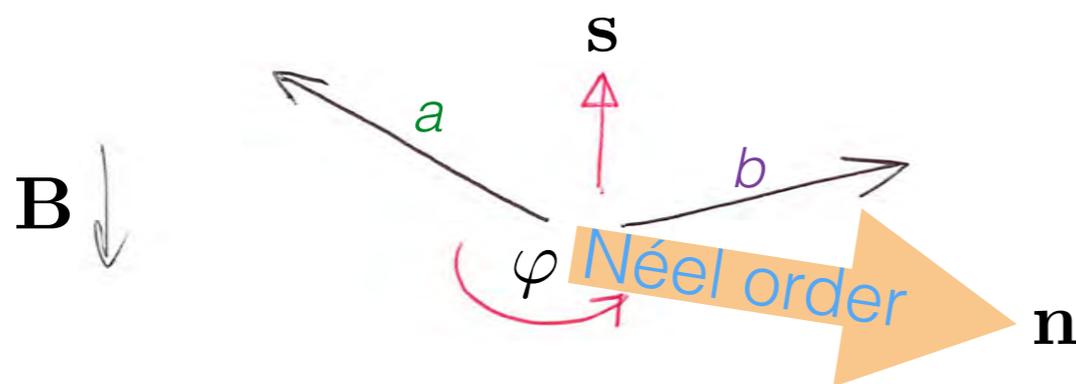
spin-degenerate spectrum

spin $+\hbar$ magnon (spin wave) along \mathbf{n}

thermal spin transport (vanishes at zero temperature)

See, however, Meier and Loss, PRL (2003) cf. spin liquids

canted AF



Goldstone mode

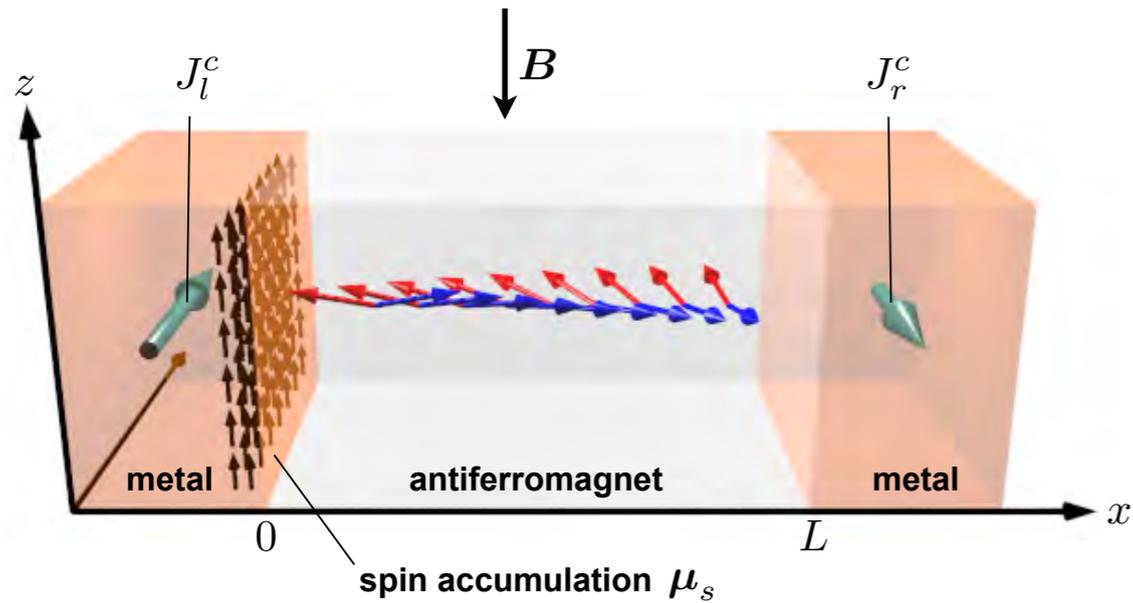
s_z is momentum canonically conjugate to φ

$$s_z \propto \partial_t \varphi \quad \text{and} \quad \mathbf{j}_z \propto -\nabla \varphi$$

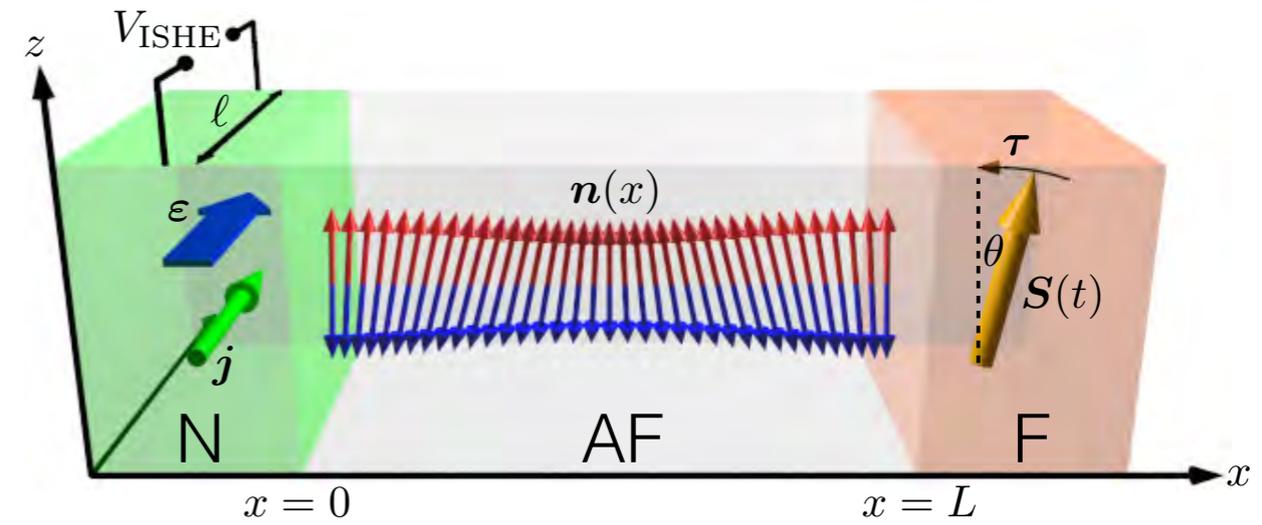
superfluid spin transport (maximized at zero temperature)

Sonin, AP (2010)

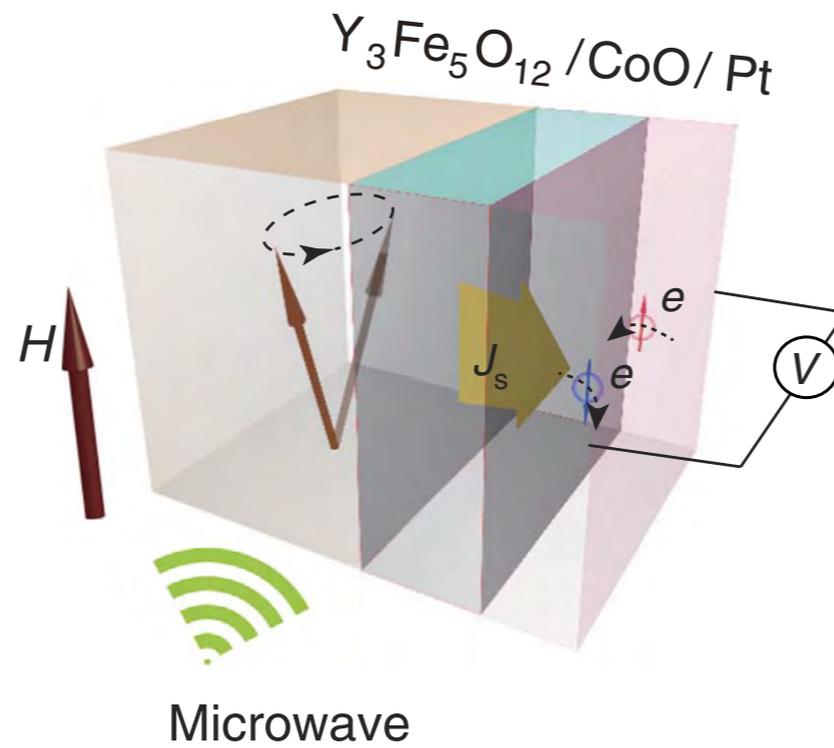
Overview



Takei, Halperin, Yacoby, and YT, *PRB* (2014)

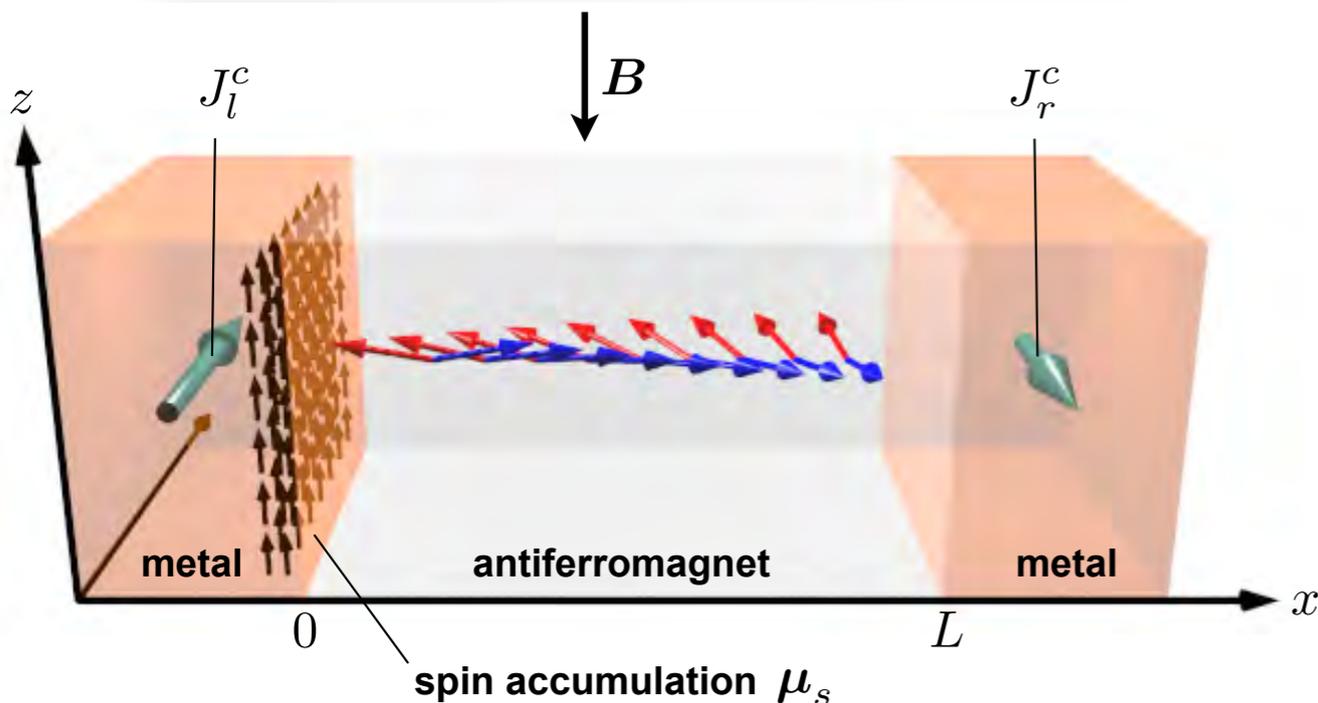


Takei, Moriyama, Ono, and YT, *PRB* (2015)



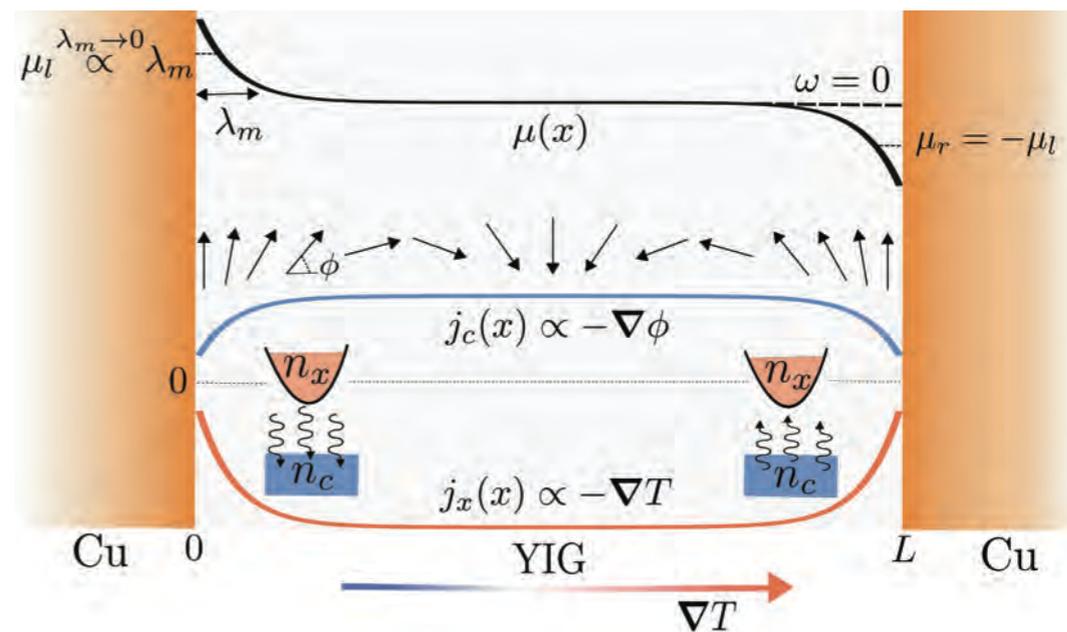
Qiu et al., *Nat. Comm.* (2016)

Two-terminal spin superfluid



spin bias

Takei, Halperin, Yacoby, and YT, *PRB* (2014)



thermal bias

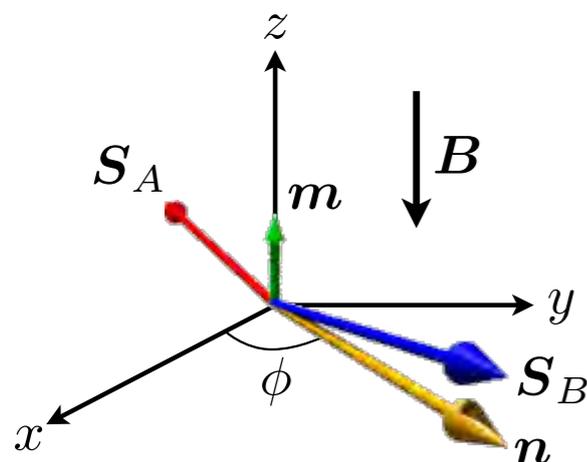
Flebus, Bender, YT, and Duine, *PRL* (2016)

nonlinear σ model:

$$\mathcal{L}_{\text{AF}}[\mathbf{m}, \mathbf{n}] = \mathcal{L}_k - \frac{A}{2} (\partial_\mu \mathbf{n})^2 - \frac{\mathbf{m}^2}{2\chi} - \mathbf{b} \cdot \mathbf{m}$$

kinetic term (Berry phase):

$$\mathcal{L}_k = s\mathbf{m} \cdot (\mathbf{n} \times \partial_t \mathbf{n})$$



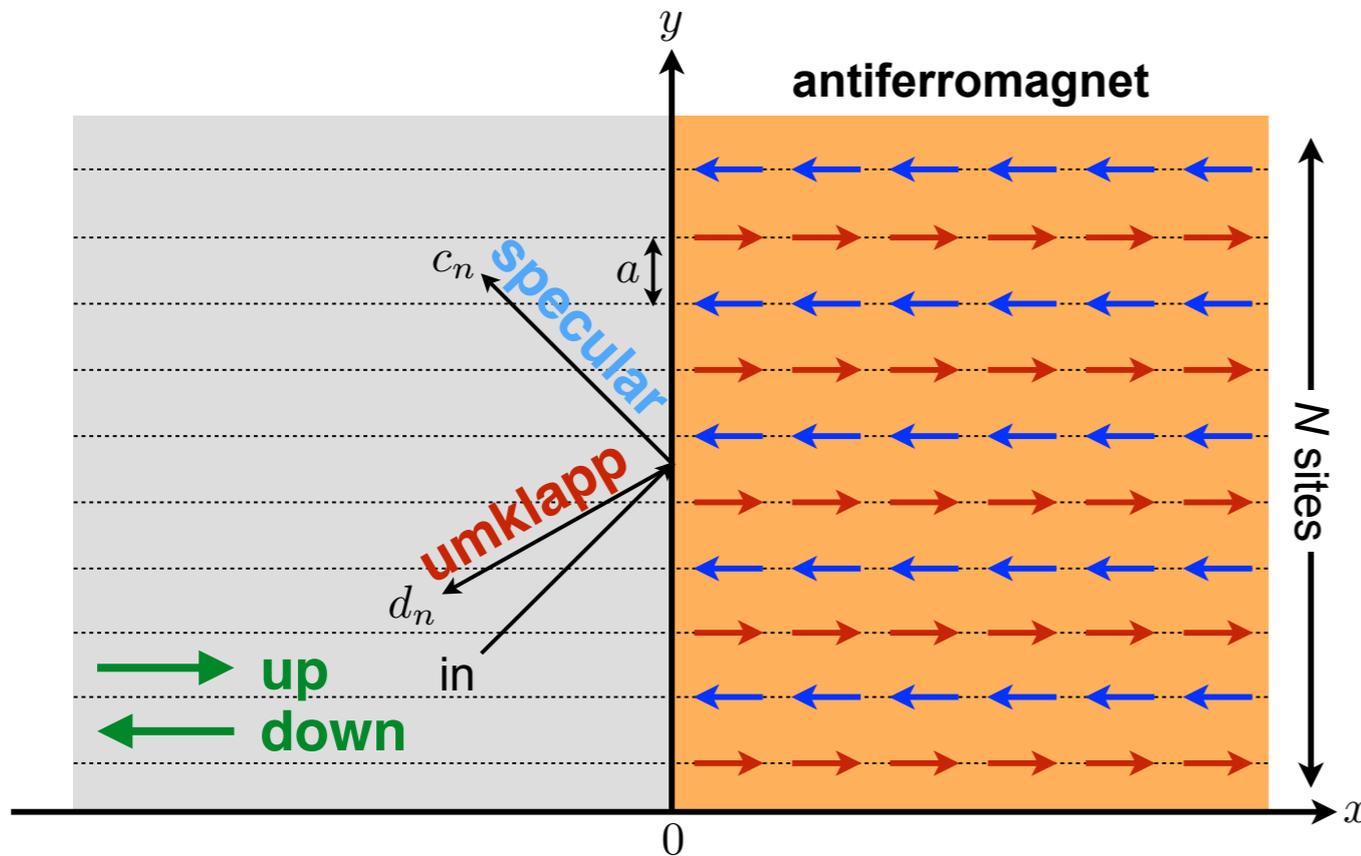
collective spin current: $\mathbf{J}_s = -A\mathbf{n} \times \nabla \mathbf{n} \rightarrow -A\nabla \varphi$

Gilbert damping: $s\dot{\mathbf{m}} = -\alpha \mathbf{n} \times \dot{\mathbf{n}} + \dots$

Halperin and Hohenberg, *PR* (1969); Sonin, *JETP* (1978) and *AP* (2010); König, Bønsager, and MacDonald, *PRL* (2001)

Interfacial spin transfer

- In the absence of spin-orbit interactions and spin-order inhomogeneities, the collinear spin of scattered electrons is conserved; the phase shift governs the *spin-mixing conductance*:



$$r_{n'n}^{\sigma} = \underbrace{c_n}_{\text{specular}} \delta_{n'n} + \underbrace{\sigma d_n}_{\text{umklapp}} \delta_{\bar{n}'n}$$

$$\bar{n} = (n + N/2) \bmod N$$

$$g^{\uparrow\downarrow} = \sum_{nm} (\delta_{nm} - r_{nm}^{\uparrow} r_{nm}^{\downarrow*})$$

the interfacial spin current density:

$$\mathbf{J}_s = \frac{\text{Re } g^{\uparrow\downarrow}}{4\pi} \mathbf{n} \times \tilde{\boldsymbol{\mu}}_s \times \mathbf{n} + \frac{\text{Im } g^{\uparrow\downarrow}}{4\pi} \tilde{\boldsymbol{\mu}}_s \times \mathbf{n}$$

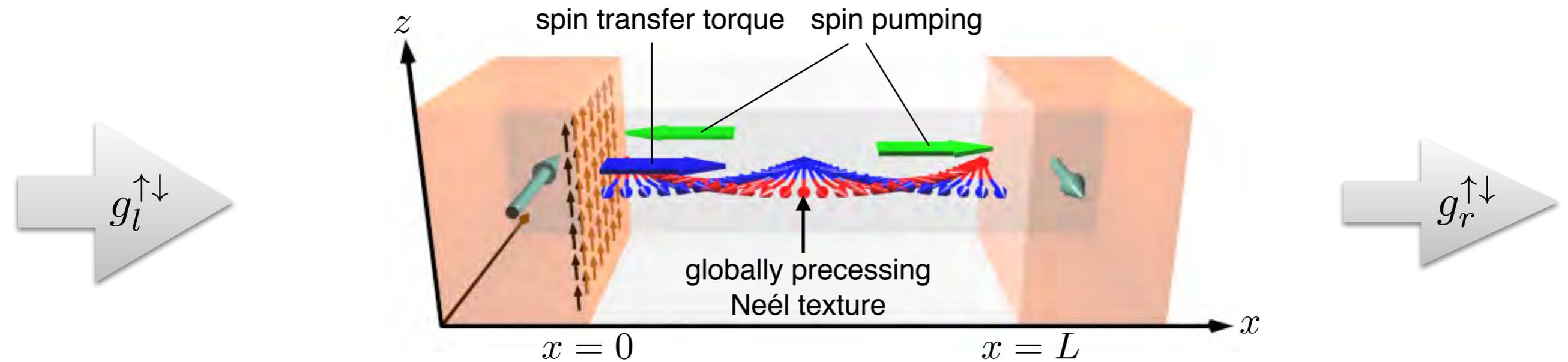
$$\tilde{\boldsymbol{\mu}}_s \equiv \underbrace{\boldsymbol{\mu}_s}_{\text{torque}} - \underbrace{\hbar \mathbf{n} \times \dot{\mathbf{n}}}_{\text{pumping}}$$

YT, Brataas, Bauer, and Halperin, *RMP* (2005)

$$\text{Unitarity: } |c_n|^2 + |d_n|^2 = 1 \quad \Rightarrow \quad g^{\uparrow\downarrow} = 2 \sum_n |d_n|^2$$

Takei, Halperin, Yacoby, and YT, *PRB* (2014); see also Jia, Liu, Xia, and Bauer, *EPL* (2011) for YIG

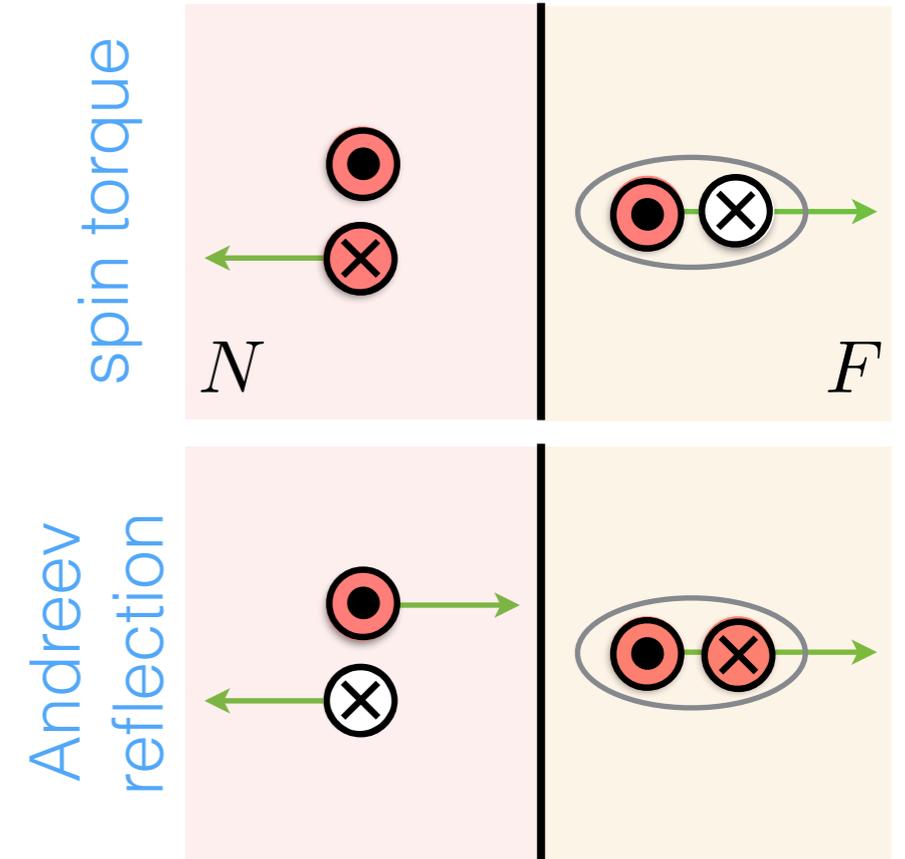
Spin-current circuit



$$g_\alpha = \frac{4\pi\alpha sL}{\hbar} \quad (\text{mechanical torque})$$

$$\Omega = \frac{\mu_s}{\hbar} \frac{g_l^{\uparrow\downarrow}}{g_l^{\uparrow\downarrow} + g_r^{\uparrow\downarrow} + g_\alpha}, \quad J_r^s = \frac{\mu_s}{4\pi} \frac{g_l^{\uparrow\downarrow} g_r^{\uparrow\downarrow}}{g_l^{\uparrow\downarrow} + g_r^{\uparrow\downarrow} + g_\alpha}$$

Negative DC electron drag (revealed by SHE)



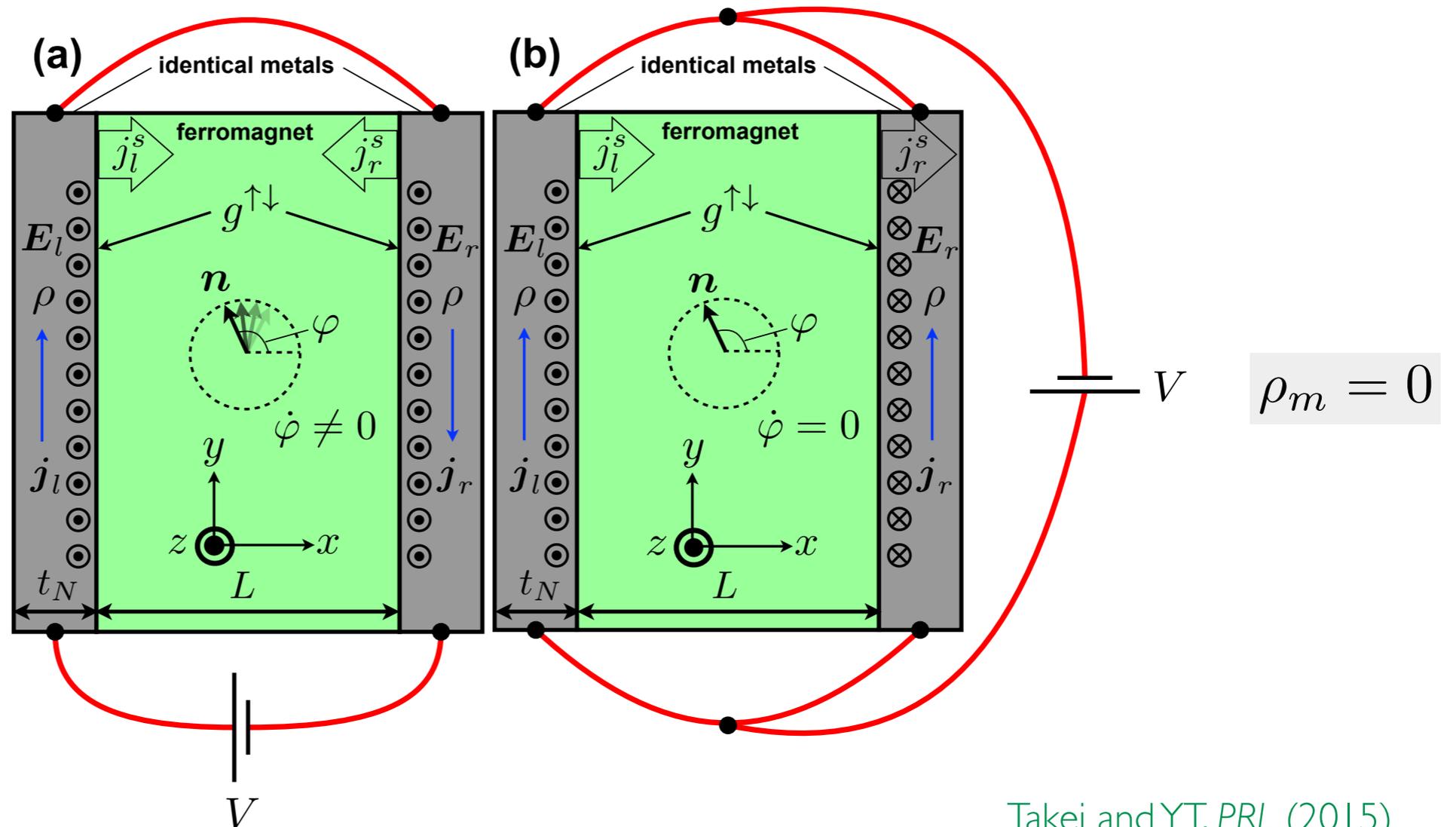
$$J_{\text{SH}}^s = \frac{\hbar}{2e} \theta_{\text{SH}} J_l^c \quad \text{Onsager} \quad J_r^c = -\frac{\hbar}{2e} \theta_{\text{SH}} \frac{\sigma}{d} \Omega$$

$$\mathcal{D} \equiv -\frac{J_r^c}{J_l^c} = \frac{h}{4e^2} \left(\frac{\theta_{\text{SH}}^2}{g^{\uparrow\downarrow}} \right)_{N|F} \left(\frac{\sigma}{\lambda_s} \right)_N \quad \text{assuming} \quad L < L_\alpha \equiv \frac{\hbar g^{\uparrow\downarrow}}{4\pi\alpha s}$$

for Pt|YIG|Pt heterostructure: $L_\alpha \sim 1 \mu\text{m}$ and $\mathcal{D} \sim 0.1$

Nonlocal magnetoresistance

- ◆ Circulating current through two metal films in series (a) spins the order, reducing the overall dissipation

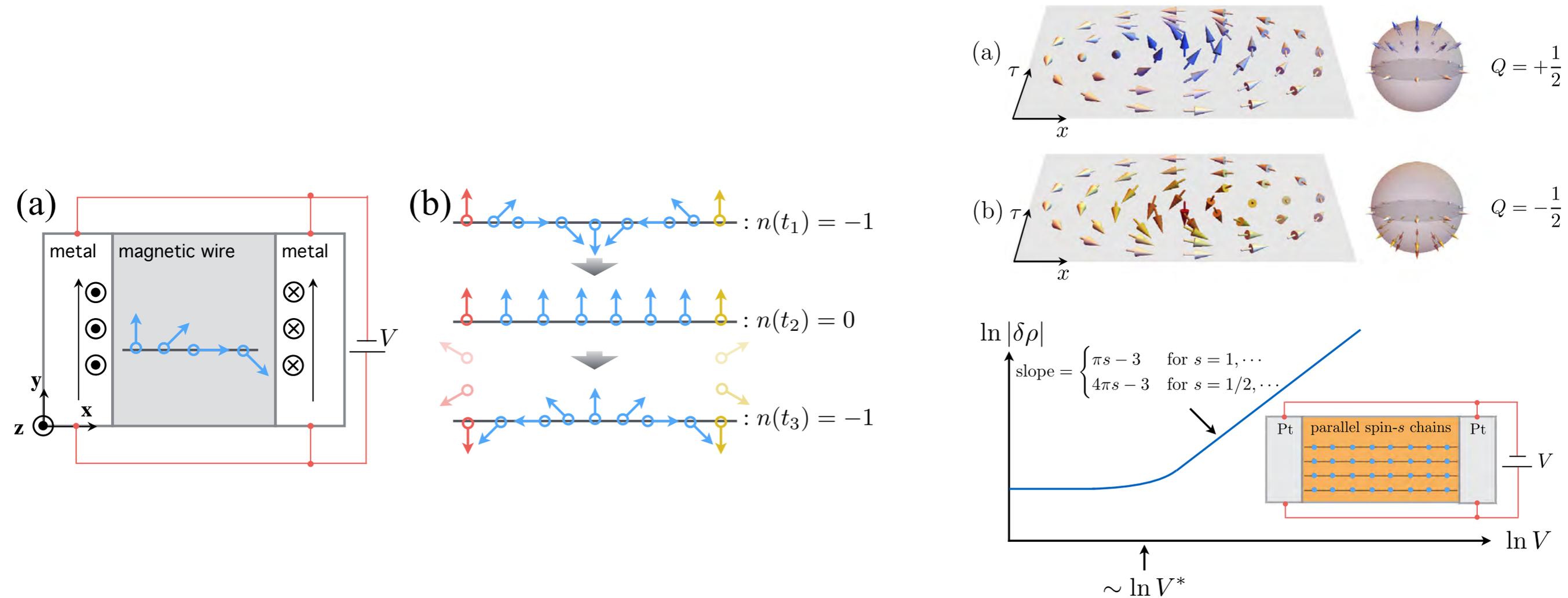


- ◆ In the parallel configuration (b), the torques are balanced, and the magnet remains stationary, causing more friction

Cf. Eisenstein and MacDonald, *Nature* (2004) for BEC of excitons in bilayer electron systems

Quantum phase slips

- The parallel magnetoresistance geometry can be used to extract the thermal and quantum phase slip rates:



- The effective action for a gas of QPS's in the presence of a spin superflow:

$$S_{\text{eff}} = nS_{\text{core}} - \mu \sum_{i < j} q_i q_j \ln(d_{ij}/\lambda) + j_s \sum_i q_i \tau_i$$

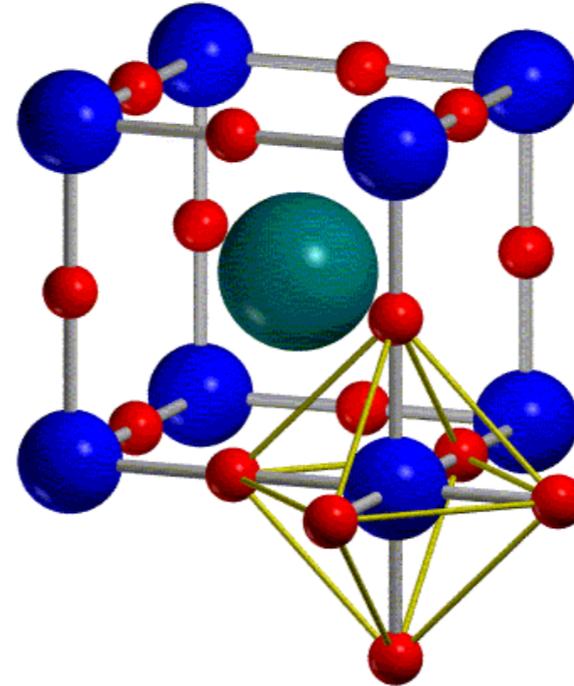
Possible materials: Perovskites



RbMnF₃

$$S = 5/2$$

$$T_N \approx 83 \text{ K}$$



KNiF₃

$$S = 1$$

$$T_N \approx 275 \text{ K}$$

$$\alpha \sim 10^{-4} \rightarrow \text{damping length } L_\alpha \sim 100 \text{ nm}$$

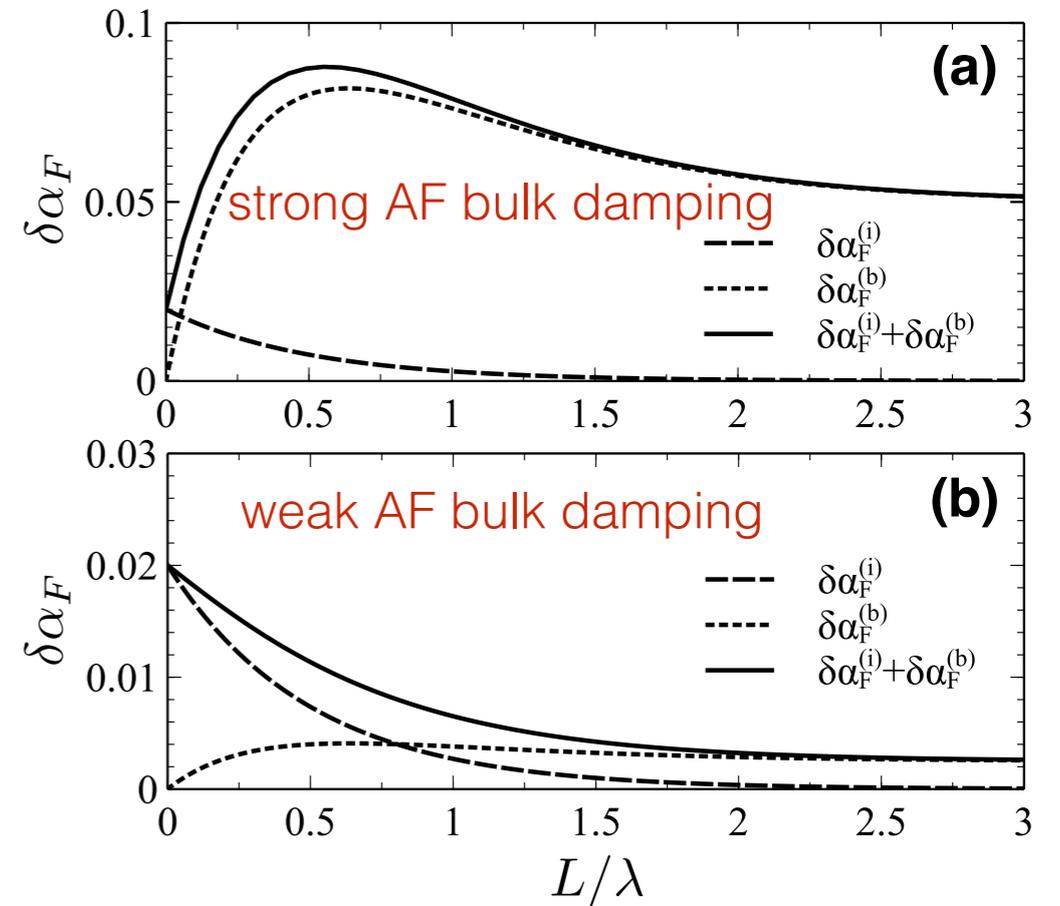
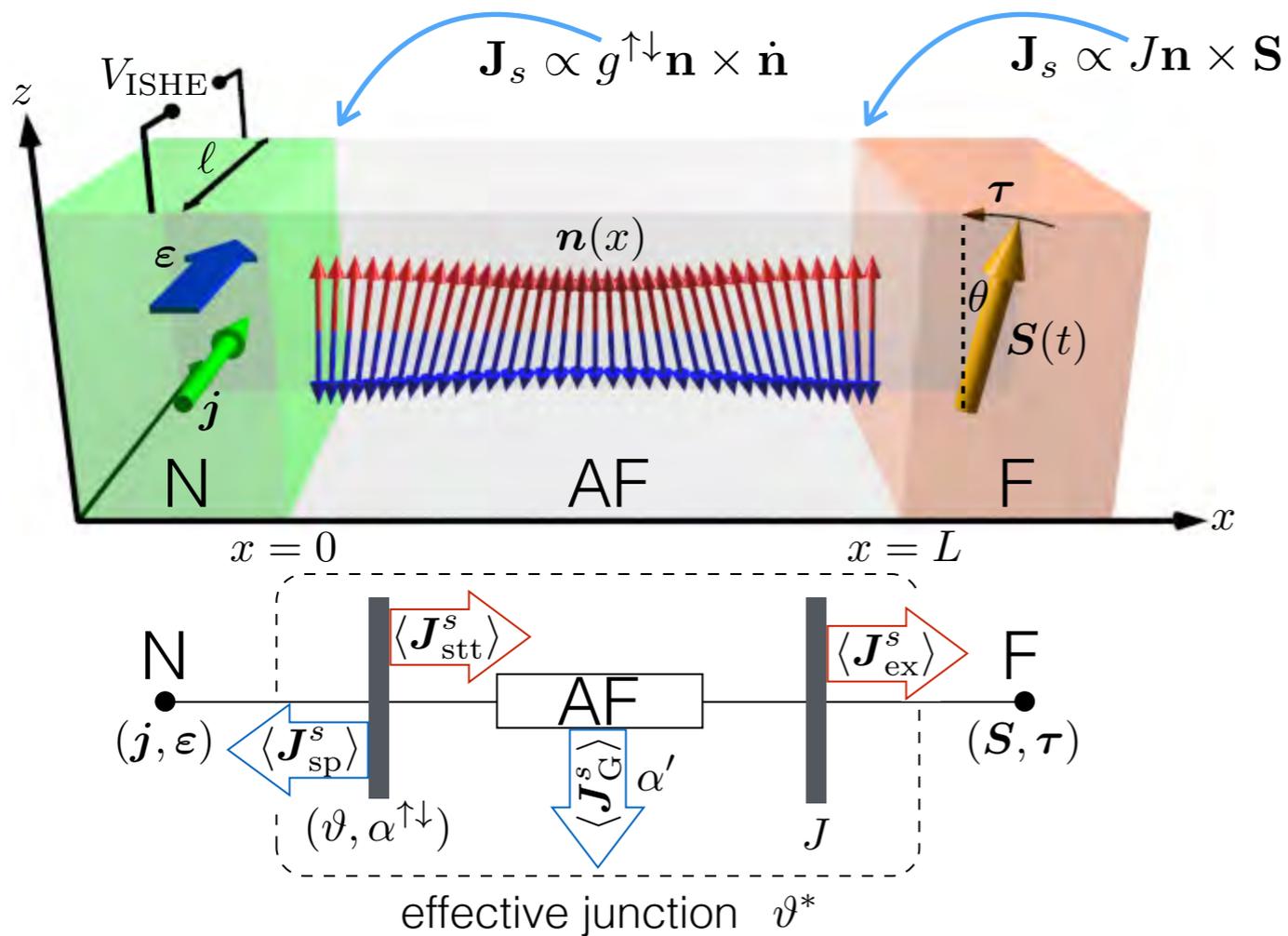
$$\text{anisotropy: } \kappa/J \sim 10^{-5} \rightarrow \text{healing length } L_c = \sqrt{A/\kappa} \sim 100 \text{ nm}$$

$$J_c^{(s)} = \kappa L_c = \sqrt{A\kappa} \rightarrow J_c \sim 10^{12} \text{ A/m}^2$$

$$\text{minimal magnetic field providing easy plane: } B_c = \sqrt{\kappa J} \sim 1 \text{ T}$$

AF-mediated (coherent) spin transfer

- Spin-transfer torque and spin pumping mediated by AF (NiO):

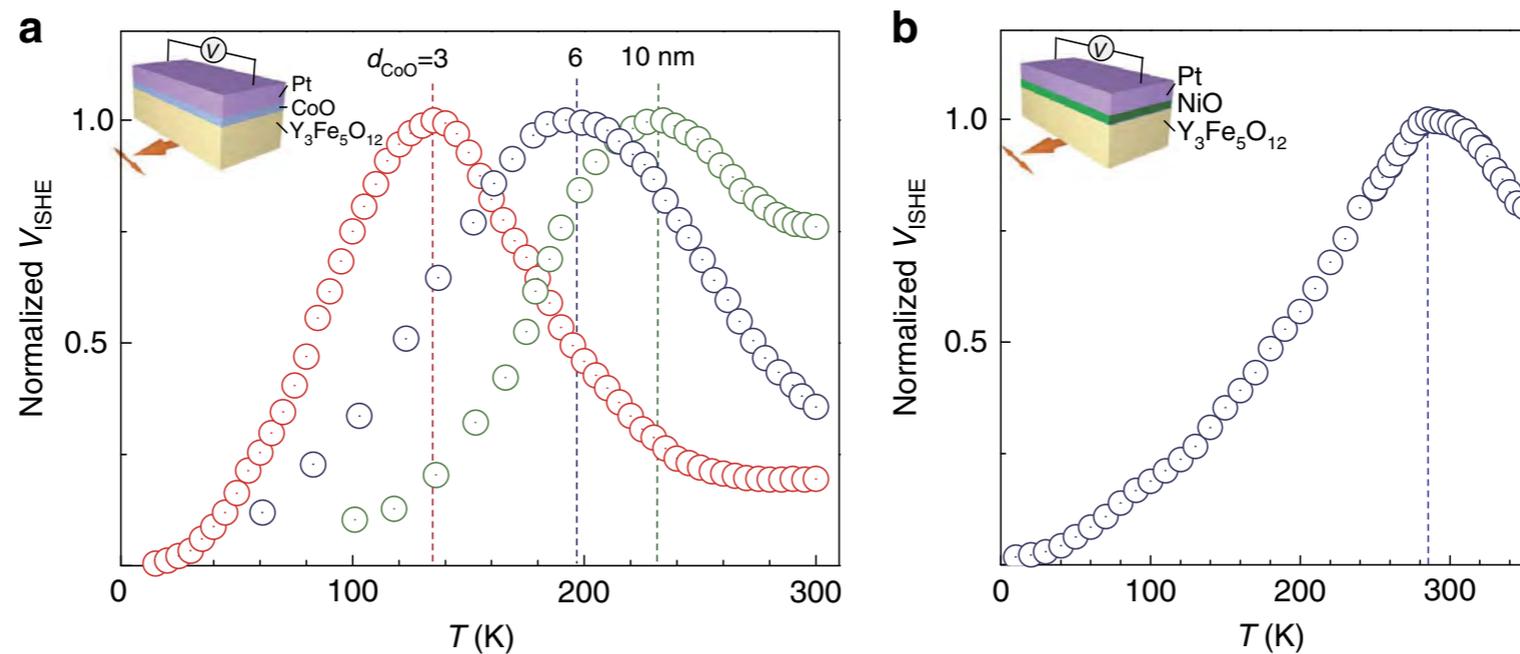
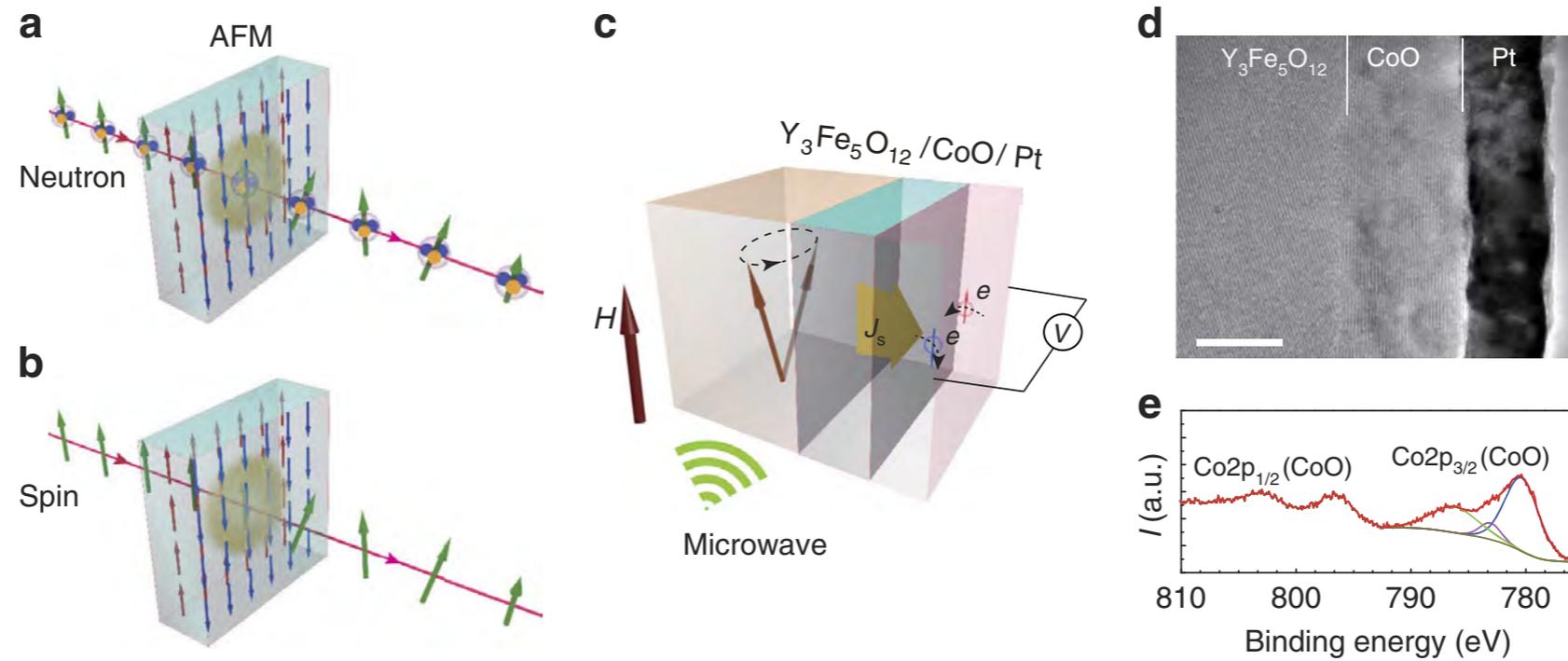


$$\alpha_F^{(i)} = \frac{1}{S} \frac{g^{\uparrow\downarrow} + \frac{\vartheta}{\omega_F} j}{\left(\cosh \frac{L}{\lambda} + \frac{1}{\eta} \sinh \frac{L}{\lambda} \right)^2} \vartheta^*$$

$$\alpha_F^{(b)} = \frac{\alpha_{AF}}{S} \frac{\frac{L}{\lambda} + \frac{1}{2} \sinh \frac{2L}{\lambda}}{\left(\cosh \frac{L}{\lambda} + \frac{1}{\eta} \sinh \frac{L}{\lambda} \right)^2}$$

AF-mediated (thermal) spin transfer

- Spin pumping mediated by AF (CoO and NiO):



Summary

- ◆ While antiferromagnets possess magnetic order that is hidden from generic electromagnetic probes, they may serve as efficient interconnects for spin transport (manifested, e.g., through spin Hall, spin Seebeck, and FMR probes)
- ◆ It is natural to invoke a two-fluid picture, with the spin superfluid taking over the transport at low temperatures and thermal magnons at elevated temperatures
- ◆ Quantum phase slips, which exhibit unique properties in the AFM materials, dominate dissipation of spin transport at low temperatures



“KITP-style” program in Natal, Brazil (~May, 2017)



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