Electronic Squeezing of Pumped Phonons: Negative *U* and Transient Superconductivity

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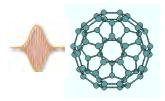
e.g. superconducting-like response in K_3C_{60} :

LETTER

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Possible light-induced superconductivity in K_3C_{60} at high temperature

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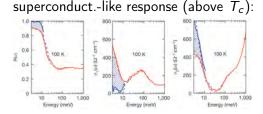
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• phonon in K_3C_{60} experiment coupled DIRECTLY to electrons only via gradient ($T_{1u} \otimes T_{1u}$ no coupling)

$$H_{
m ep} = ec{q} \cdot \sum_k \Psi_k^\dagger ec{
abla} \Psi_k$$

very weak!

• \Rightarrow seek non-linear coupling?

Non-Linear Phononics

different proposals

- Light-induced change in lattice structure via quartic (IR)phonon–(Raman)phonon coupling [Subedi, et. al. PRB **89**, 220301(R) (2014)]
- Periodic modulation of interaction by direct coupling [Singla, et. al. PRL **115**, 187401 (2015)]
- → variant applied to changes in shape of C₆₀ molecule gives orbital dependence of U promoting SC [Kim, et. al. PRB 94, 155152 (2016)]
- dynamical modulations of other phonons via (IR)phonon–(Raman)phonon coupling [Knap, et. al. PRB 94, 214504 (2016);
 M. Babadi et. al. arXiv:1702.02531)]
- Interesting different proposal: effective cooling (not Phonons) [Nava, et. al. arXiv:1704.05613]

Non-Linear Phononics

different proposals: common ground

[Subedi, et. al.; Singla, et. al.; Kim, et. al.; Knap, et. al.] light induced changes in electronic properties (distribution func., electron or electron-phonon Hamiltonian)

here: what about the phonon energetics?

the phonon properties depend on the electronic state: could this (partially) be the transduction mechanism?

simple model (symmetry allowed):

$$H_{ ext{e-ph}} = g \mathcal{K} \sum_i \hat{n}_i \hat{Q}_i^2$$

with small dimensionless coupling $g \sim 0.05 - 0.1$.

 \Rightarrow restoring force for phonon depends on electron density \hat{n}

simple model

$$H = H_{\rm e} + H_{\rm e-ph} + H_{\rm ph}$$

electron-phonon coupling

$$H_{\rm e-ph} = gK \sum_i \hat{n}_i \hat{Q}_i^2$$

bare phonon Hamiltonian

$$H_{\rm ph} = \sum_{i} \frac{K}{2} \hat{Q}_i^2 + \frac{1}{2M} \hat{P}_i^2 = \omega_0 \sum_{i} \left(b_i^{\dagger} b_i + \frac{1}{2} \right)$$

phonon energetics

$$H_{ ext{e-ph}} \Rightarrow K o K' = (1 + 2g\,\hat{n}_i)K$$

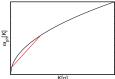
 $\omega_0 \to \omega_0 \sqrt{1 + 2g\hat{n}_i}$

 $\omega_0 \rightarrow \omega_0 \sqrt{1 + 2g\hat{n}_i}$

- shift in oscillator frequency: energy of m-th eigenstate $E = \omega_0(m + \frac{1}{2})$ depends on local electron occupancy
- electron pairing energy: $U_{\text{eff}} = E(n=2) + E(n=0) 2E(n=1)$

$$egin{split} U_{ ext{eff}}[m] &= U + \left(m + rac{1}{2}
ight) \omega_0 \left(\sqrt{1 + 4g} + 1 - 2\sqrt{1 + 2g}
ight) \ &\stackrel{g \ll 1}{pprox} U - \left(m + rac{1}{2}
ight) \omega_0 g^2 \end{split}$$

- effective interactions are:
 - negative because square root is concave down
 - increases linearly with number of phonons m
 - proportional to g^2



Minimal Model: Hubbard Model + Optical Phonons

$$H = -\sum_{ij\sigma} J_{ij} c_{i\sigma}^{\dagger} c_{j\sigma} + U_{\text{elec}} \sum_{i} \hat{n}_{i\uparrow} \hat{n}_{i\downarrow} + \sum_{i} \left(\frac{K}{2} \hat{x}_{i}^{2} + \frac{1}{2M} \hat{p}_{i}^{2} \right) \\ + gK \sum_{i} \hat{n}_{i} \hat{x}_{i}^{2}$$

electron-phonon coupling via electron density dependence of osc. stiffness

treating
$$\hat{n}\hat{x}^2 \sim \hat{n}\left(b^{\dagger}+b
ight)^2$$
 difficult

(unitary) squeezing transform $e^{S}He^{-S}$ with $e^{\hat{S}} = e^{\frac{i}{2}\sum_{j}\zeta_{j}(\hat{x}_{j}\hat{
ho}_{j}+\hat{
ho}_{j}\hat{x}_{j})}$ and

$$\begin{aligned} \zeta_{j} &= -\frac{1}{4} \ln \left[1 + 2g \left(\hat{n}_{j\uparrow} + \hat{n}_{j\downarrow} \right) \right] \\ \Rightarrow H_{\text{eff}} &= -\sum_{\langle i,j \rangle \sigma} J_{ij}^{\star} c_{i\sigma}^{\dagger} c_{j\sigma} + U_{\text{elec}} \sum_{i} n_{i\uparrow} n_{i\downarrow} + \omega_{0} \sqrt{1 + 2g \hat{n}_{i}} \left(\beta_{i}^{\dagger} \beta_{i} + \frac{1}{2} \right) \end{aligned}$$

Onsite Terms: Expand in g

$$\begin{split} \omega_0 \sqrt{1 + 2g \hat{n}_i} \left(\beta_i^{\dagger} \beta_i + \frac{1}{2} \right) &\approx \quad \omega_0 \left(\beta_i^{\dagger} \beta_i + \frac{1}{2} \right) \\ &+ \frac{g \omega_0}{2} \left(1 - \frac{g}{2} \right) \left(2\beta_i^{\dagger} \beta_i + 1 \right) n_{i\sigma} \\ &- \frac{g^2 \omega_0}{2} \left(2\beta_i^{\dagger} \beta_i + 1 \right) n_{i\uparrow} n_{i\downarrow} \end{split}$$

Three contribution:

- 1. usual phonon
- 2. onsite potential (will lead to effective disorder)
- 3. onsite attraction (will promote SC in the right parameter regime)

Hopping Term: Complicated

$$\tilde{H}_{hop}\left[\{n_i, n_j\}\right] = -\sum_{ij\sigma} J_{ij} c_{i\sigma}^{\dagger} c_{j\sigma} e^{i(\zeta[n_i+1]-\zeta[n_i])\mathcal{O}_i} e^{i(\zeta[n_j-1]-\zeta[n_j])\mathcal{O}_j}$$
with: $\mathcal{O}_j = \frac{\beta_j^{\dagger} \beta_j^{\dagger} - \beta_j \beta_j}{2}$

- hopping process involves pair creation or destruction of phonons
- because $\ensuremath{\mathcal{O}}$ is quadratic in phonon operators the usual Feynman disentangling does not work
- checked in exactly solvable 2-site version of model \Rightarrow assume light field puts oscillators in coherent state that instantly looses coherence between different *m* sectors
- $\zeta[n_i \pm 1] \zeta[n_i] = \pm \frac{g}{2} + \mathcal{O}(g^2 \hat{n})$ and expanding to leading contribution (with non-zero expectation value):

$$J^{\star} = e^{-\frac{g^2}{8}(n_{\rm B}^2 + 2n_{\rm B} + 1)}J.$$

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$$|\alpha\rangle &= e^{-|\alpha|^{2}/2}\sum_{m}\frac{\alpha^{m}}{\sqrt{m!}}|m\rangle\\ \rho_{\alpha} &= |\alpha\rangle\langle\alpha| = e^{-|\alpha|^{2}}\sum_{m,m'}\frac{\alpha^{m}\alpha^{m'}}{\sqrt{m!m'!}}|m\rangle\langle m'|\\ \rho_{deph} &= e^{-|\alpha|^{2}}\sum_{m}\frac{\alpha^{2m}}{m!}|m\rangle\langle m| \end{split}$$

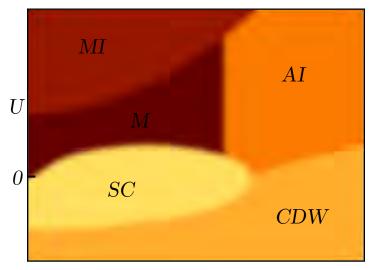
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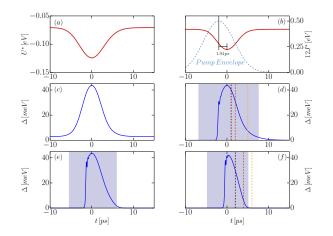
"Phases"



 $F \sim n_{\rm B}$

Experimental Parameters

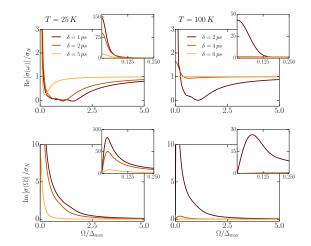
- neglect disorder
- BCS treatment (+ phenomenological electron and phonon relaxation mechanism)



Optical Conductivity: Adiabatic Approximation

• define as Fourier transform of $j(t) = \int dt' \sigma(t, t') E_{\text{probe}}(t')$ with $E_{\text{probe}}(t) = E_P \delta(t - t_D)$

• adia. approx. for conductivity: $\sigma(T, t_{rel}) \approx \sigma_{equil}^{\Delta(T)}(t_{rel})$



so far:

- new generic mechanism connecting phonon drive to changed interaction parameters
- plausible for light induced SC, but our value of g is a factor of 2-4 to large compared to the one estimated from experiments!
- see also M.A. Sentef [Phys. Rev. B 95, 205111 (2017)]

- Energy flow and heating?
 - DMRG and perturbation theory
- calculation of the non-equilibrium conductivity (not adiabatic)
 - arXiv:1703.07248
- inclusion of other phonon modes
- interplay with other mechanisms
- Application to other materials (optical control of Mott insulators)

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