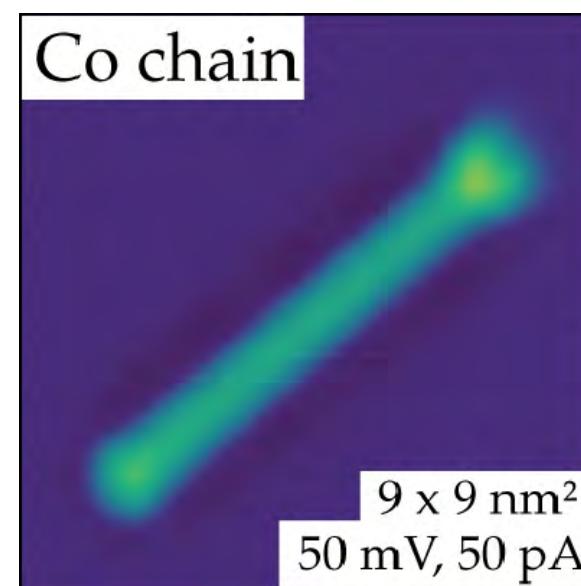
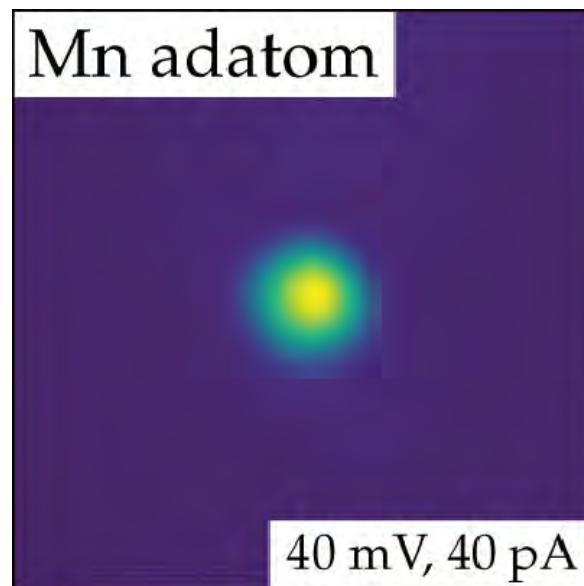
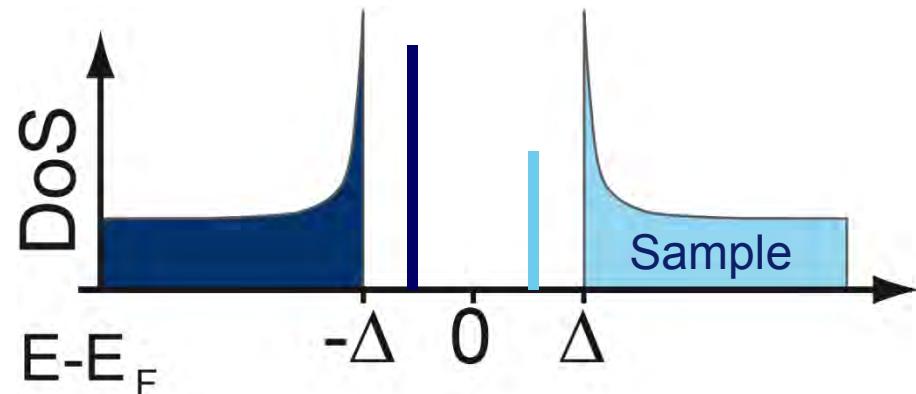
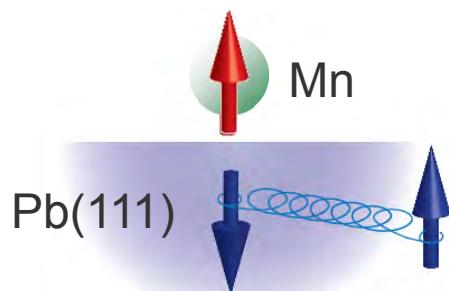
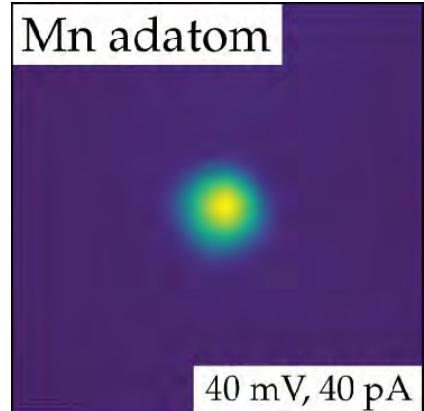
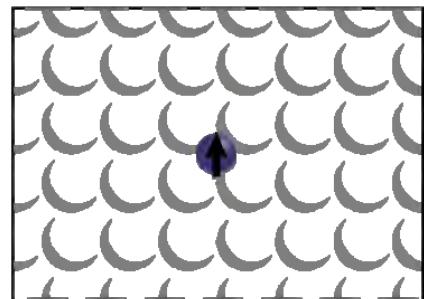


From single magnetic adatoms to coupled chains on a superconductor



Michael Ruby, Benjamin Heinrich, Yang Peng, Falko Pientka,
Felix von Oppen, Katharina Franke

Magnetic adatoms on a superconductor



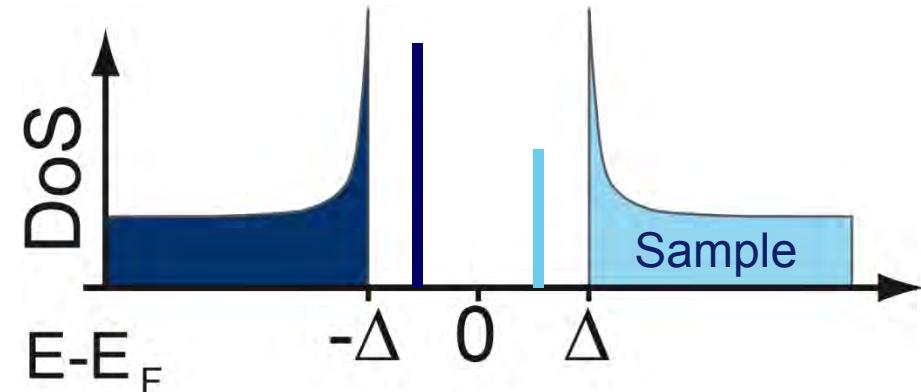
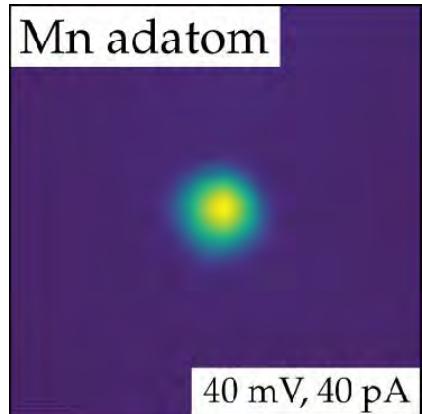
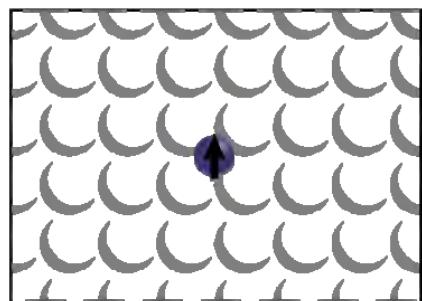
- ▶ classical spins exchange scatter at a magnetic center:

$$\epsilon_0 = \frac{E_0}{\Delta_0} = \frac{1 - (JS\pi N_0/2)^2}{1 + (JS\pi N_0/2)^2}$$

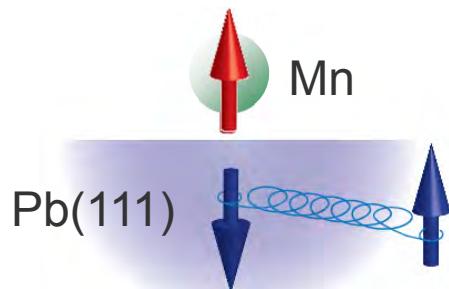
- ▶ Yu-Shiba-Rusinov states

L. Yu, Acta Phys. Sin. 21, 75 (1965)
H. Shiba, Prog. Theor. Phys. 40, 435 (1968)
A.I. Rusinov, JETP Lett. 9, 85 (1969)

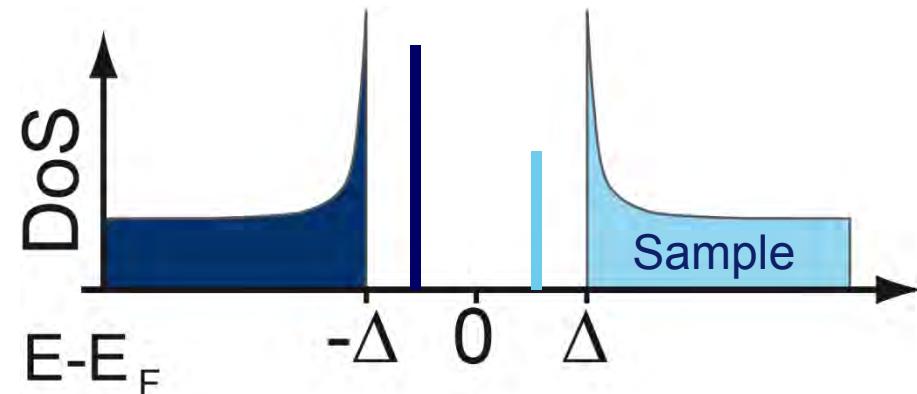
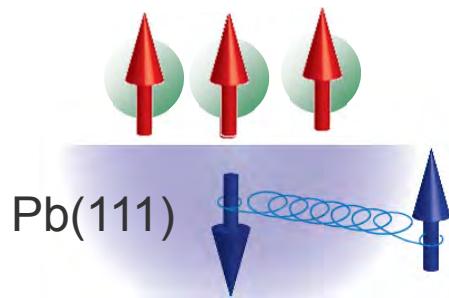
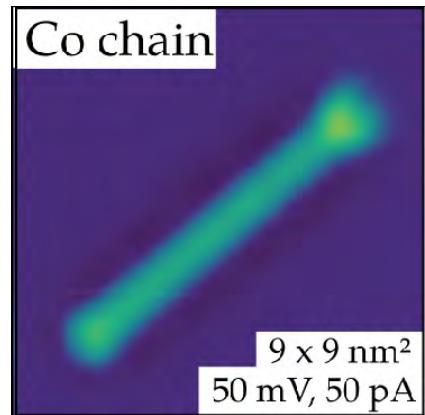
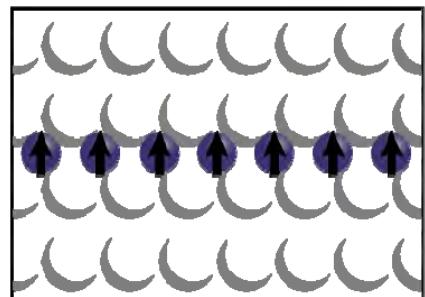
Magnetic adatoms on a superconductor



- ▶ transport through Shiba states?
- ▶ origin of multiple Shiba states?

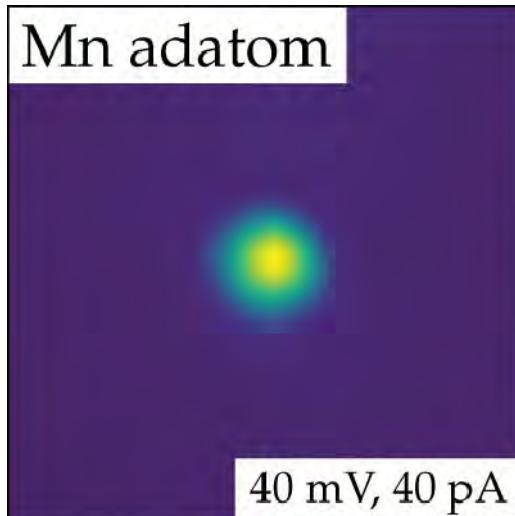


Magnetic adatoms on a superconductor



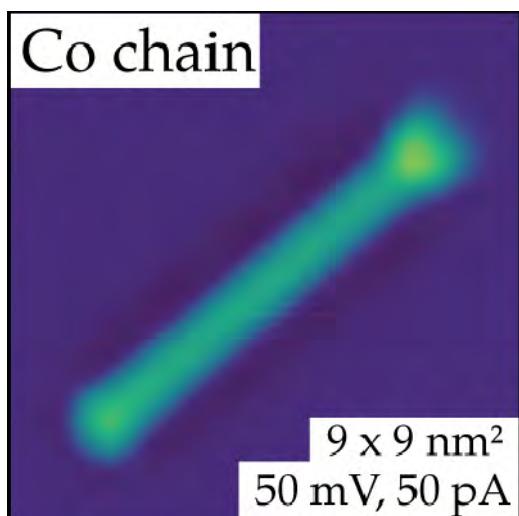
- ▶ transport through Shiba states?
- ▶ origin of multiple Shiba states?
- ▶ formation of Shiba bands?
- ▶ topological states?

Outline



Single atoms: Mn on Pb(111) and Pb(100)

- ▶ Transport mechanisms through Shiba states?
- ▶ Multiple Shiba states



Atomic chains: Co on Pb(110)

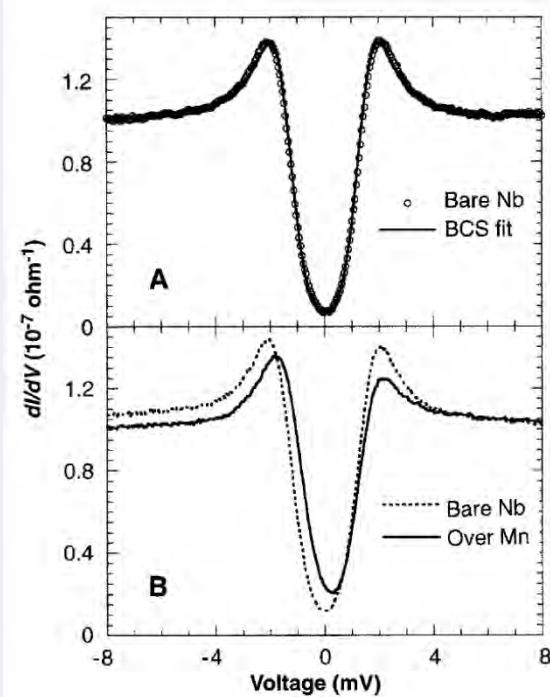
- ▶ Shiba bands and Majorana states?

Impurity induced bound states

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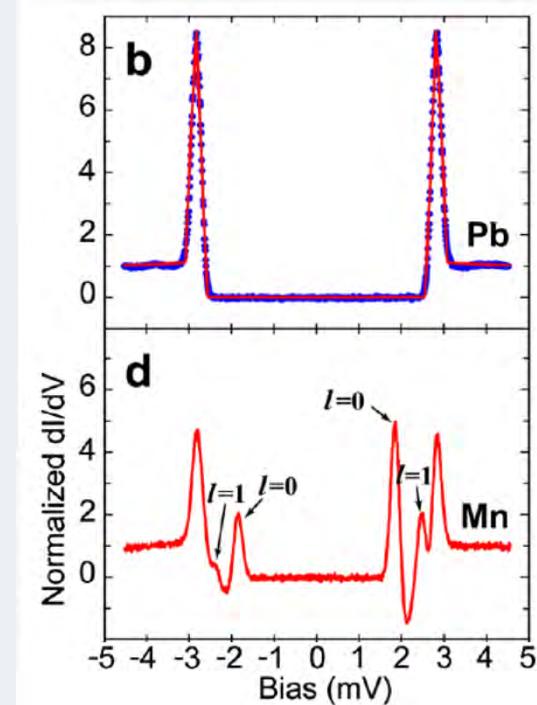


- ▶ Shiba states of Mn atoms on Nb(111) (T=4 K)



Yazdani et al, Science 275, 1767 (1997)

- ▶ Shiba states of Mn atoms on Pb(111) (T=0.3 K)

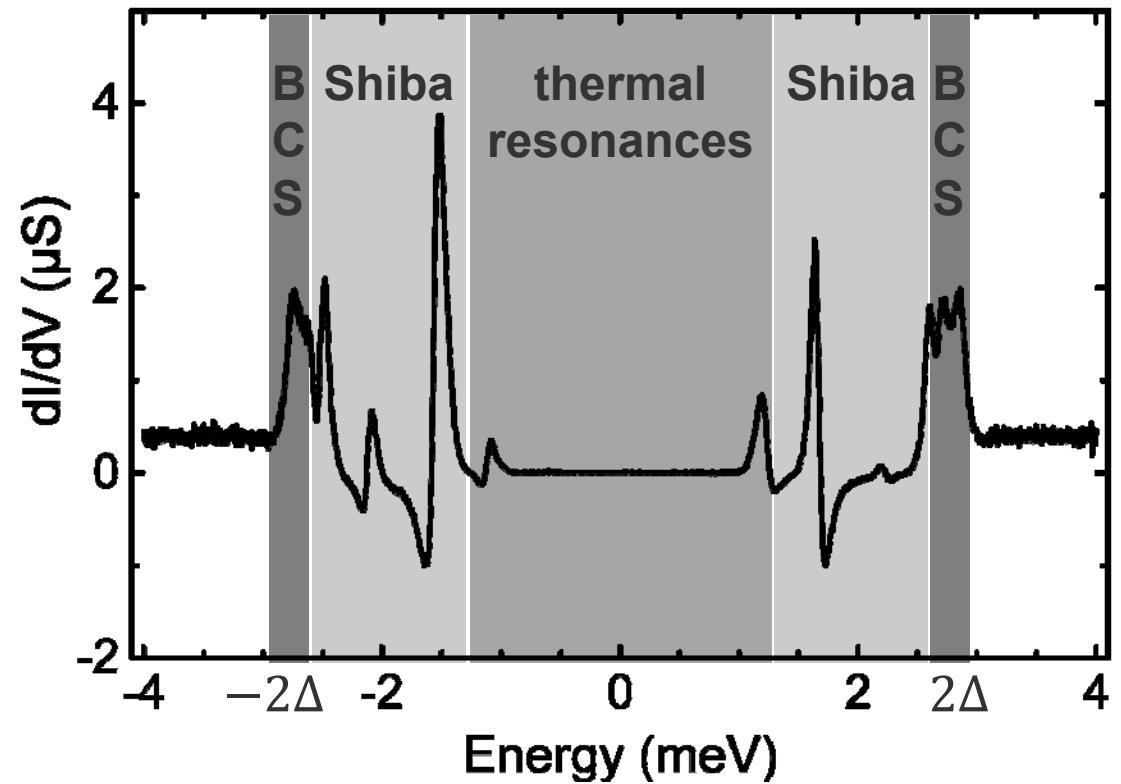
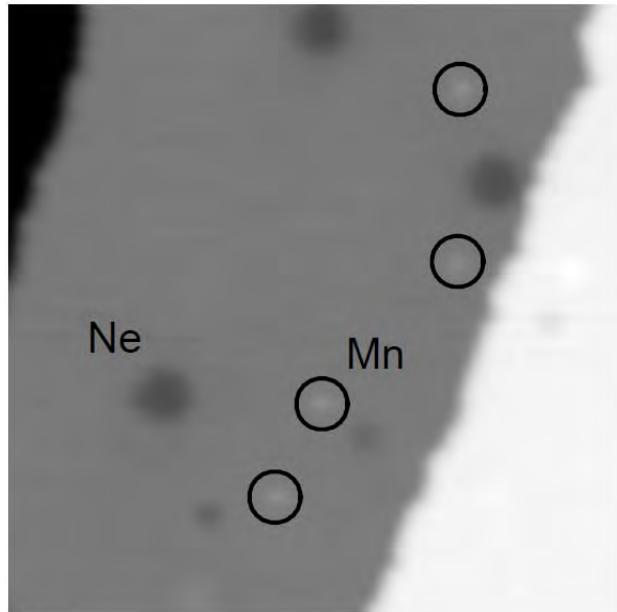


Ji et al, PRL 100, 226801 (2008)

- ▶ Shiba states interpreted in single electron tunneling picture
- ▶ Shiba height reflects amplitude of electron/hole Shiba wavefunction

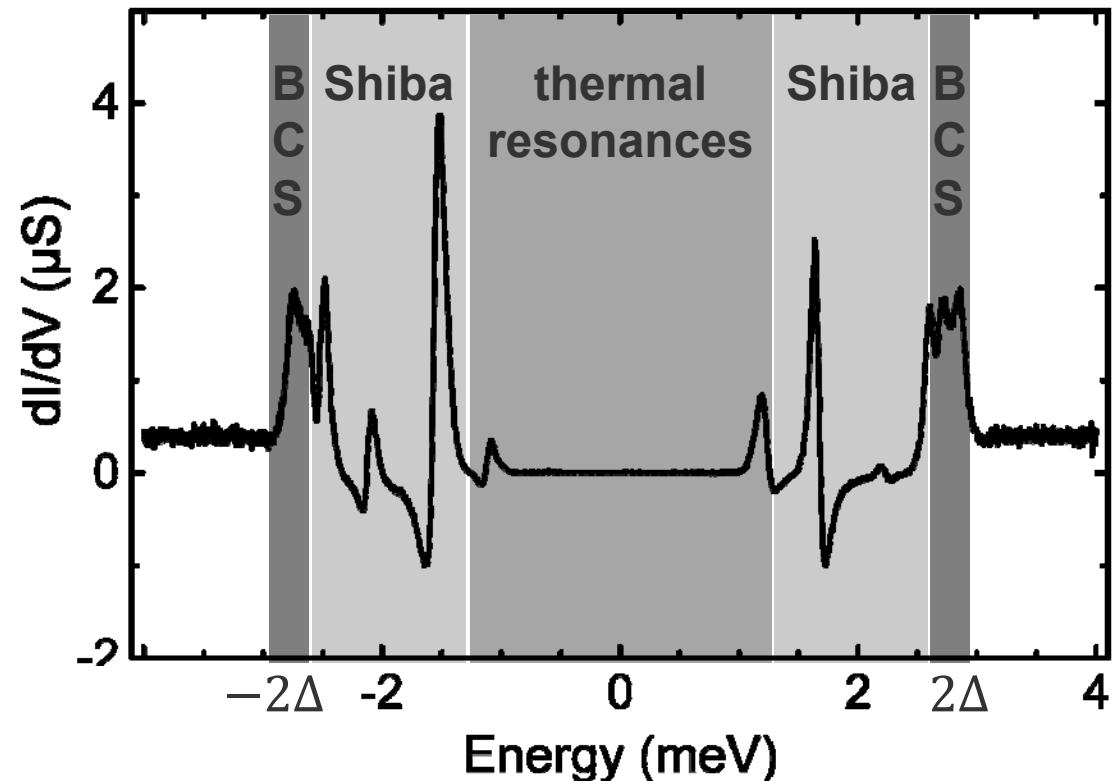
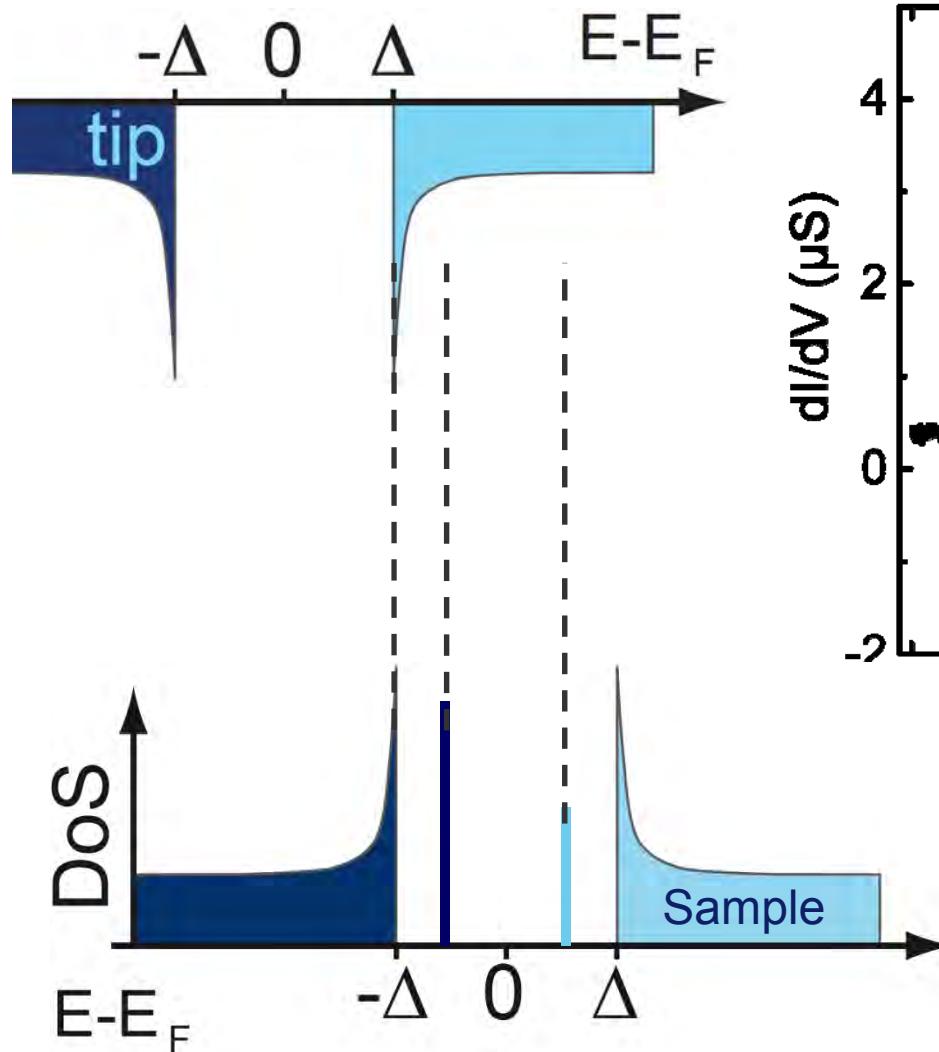
Mn atoms on Pb(111)

Freie Universität Berlin



- ▶ multiple Shiba resonances
- ▶ asymmetric peak heights

Mn atoms on Pb(111)



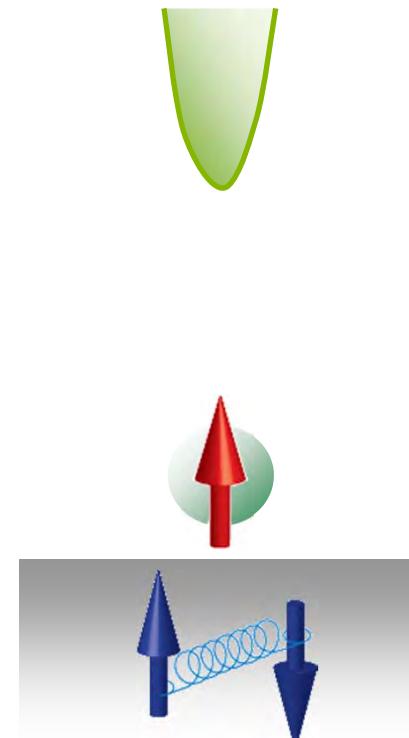
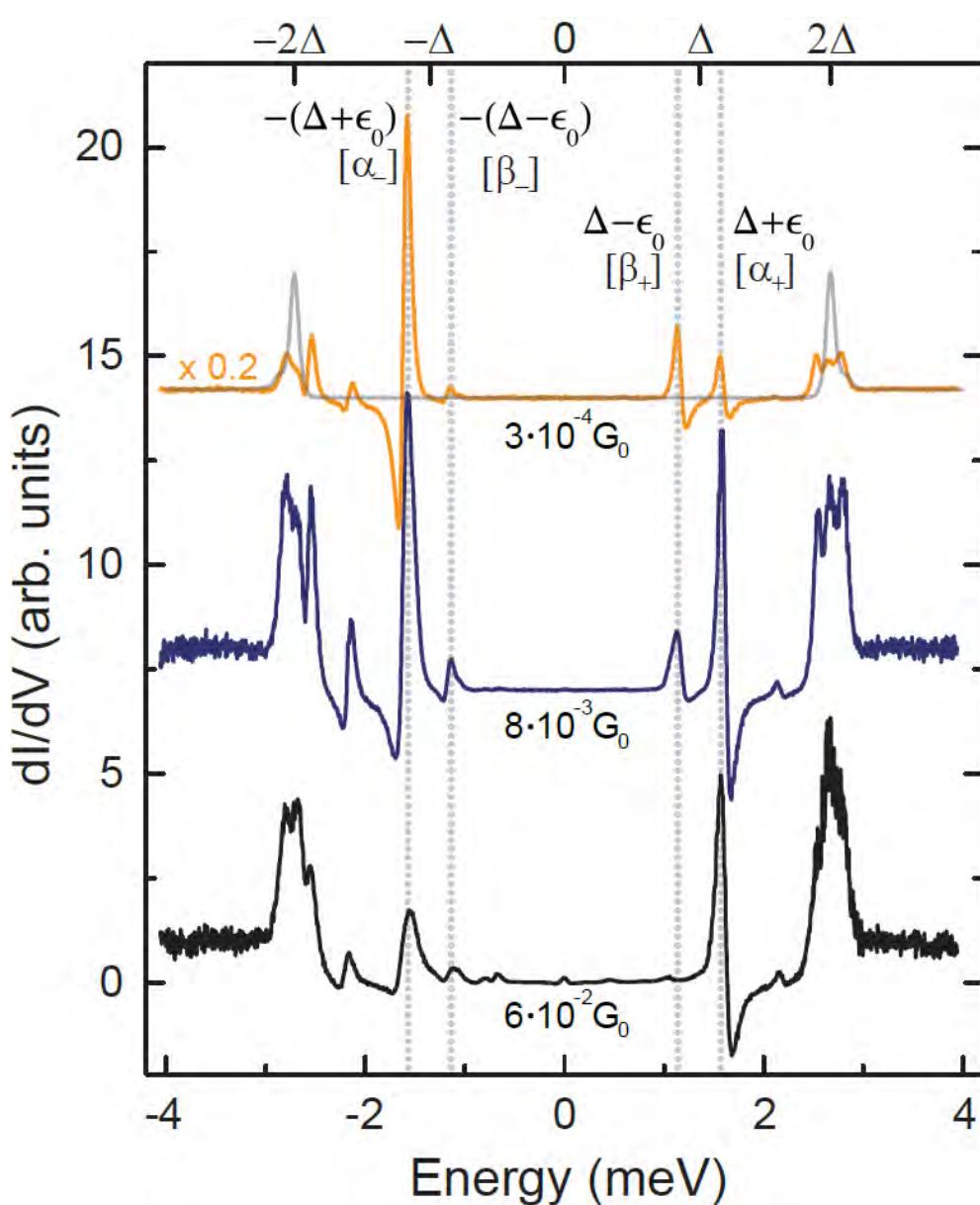
- ▶ BCS peaks
- ▶ multiple Shiba resonances
- ▶ thermally excited Shiba states

Shiba states at different junction conductances

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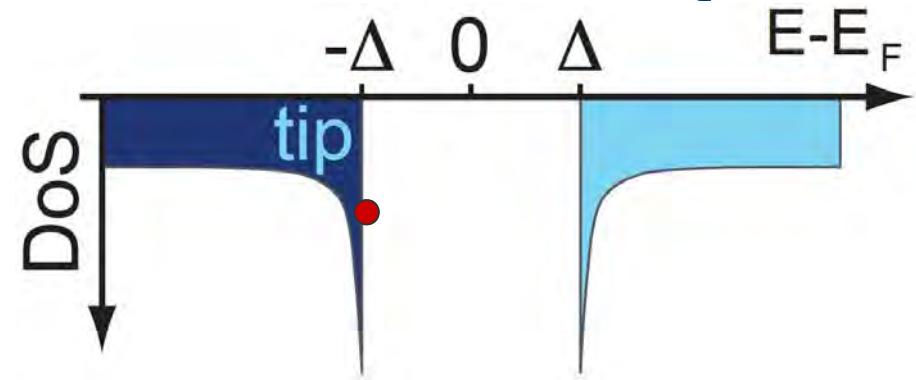
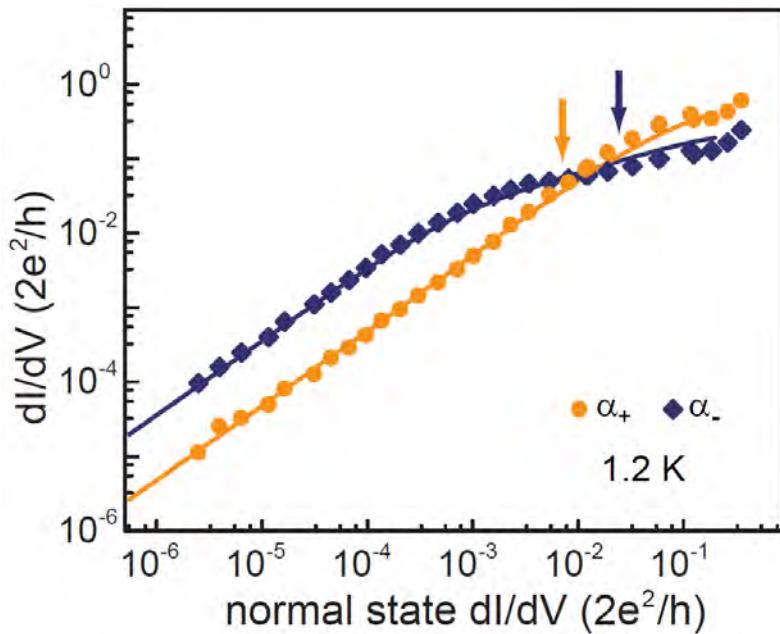
Berlin



- ▶ symmetry of Shiba intensity varies with junction conductance
- ▶ intensity cannot be interpreted as density of states

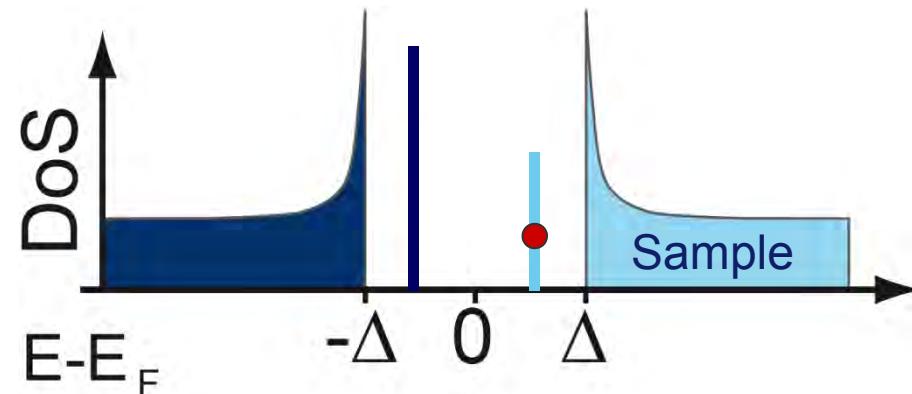
Shiba states at different junction conductances

Freie Universität Berlin



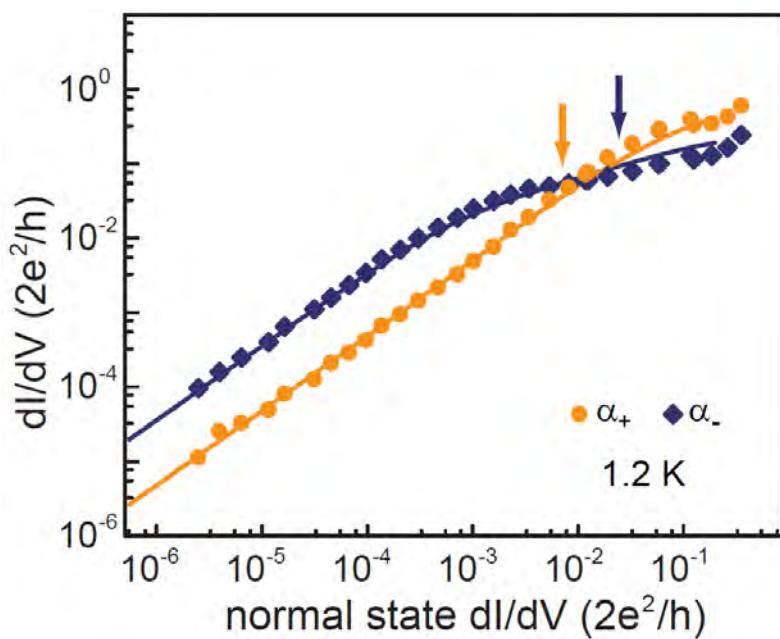
Low junction conductance:

- ▶ single particle current
- ▶ tunneling into Shiba state changes occupancy
- ▶ relaxation necessary

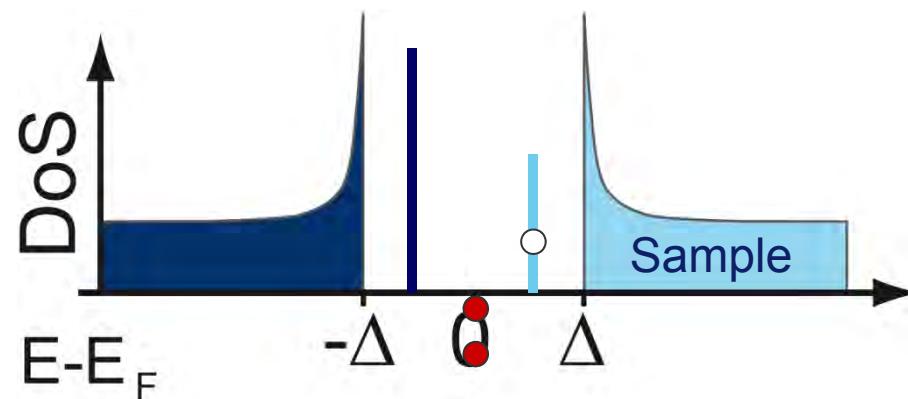
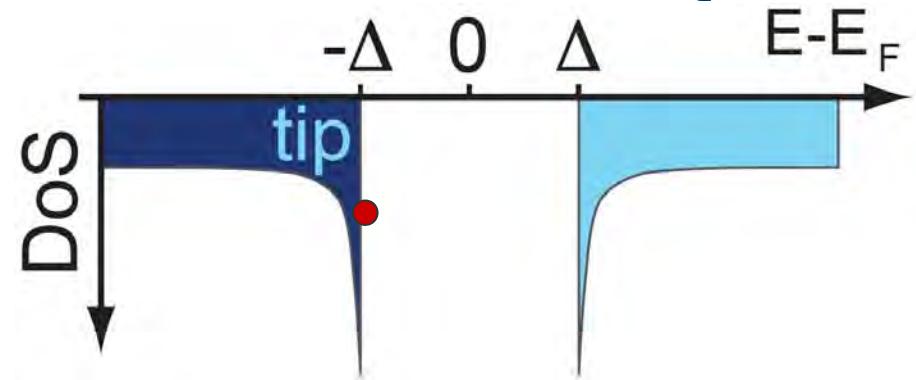


$$I^s \propto t^2 \Gamma_1$$

Shiba states at different junction conductances

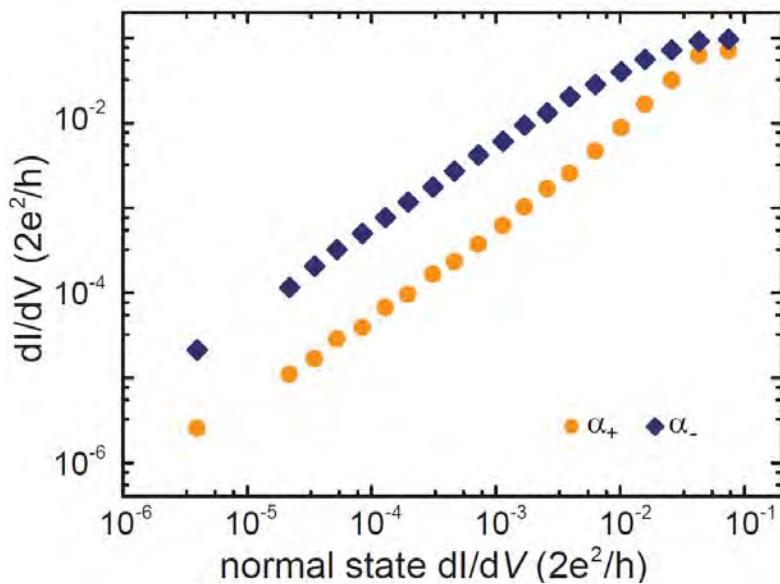


- ▶ sublinear increase of Shiba state conductance at high tunnel rates
- ▶ inversion of Shiba intensity

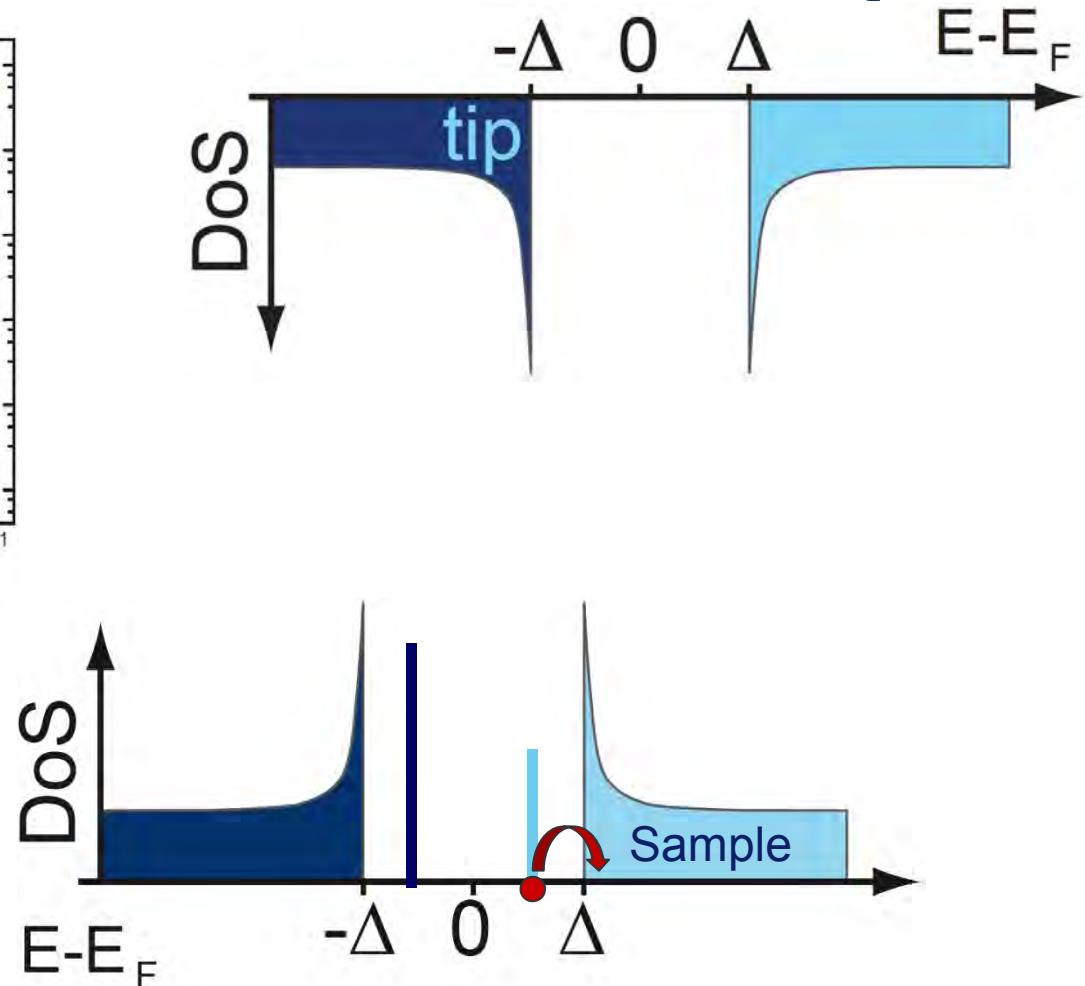


Shiba states at different junction conductances

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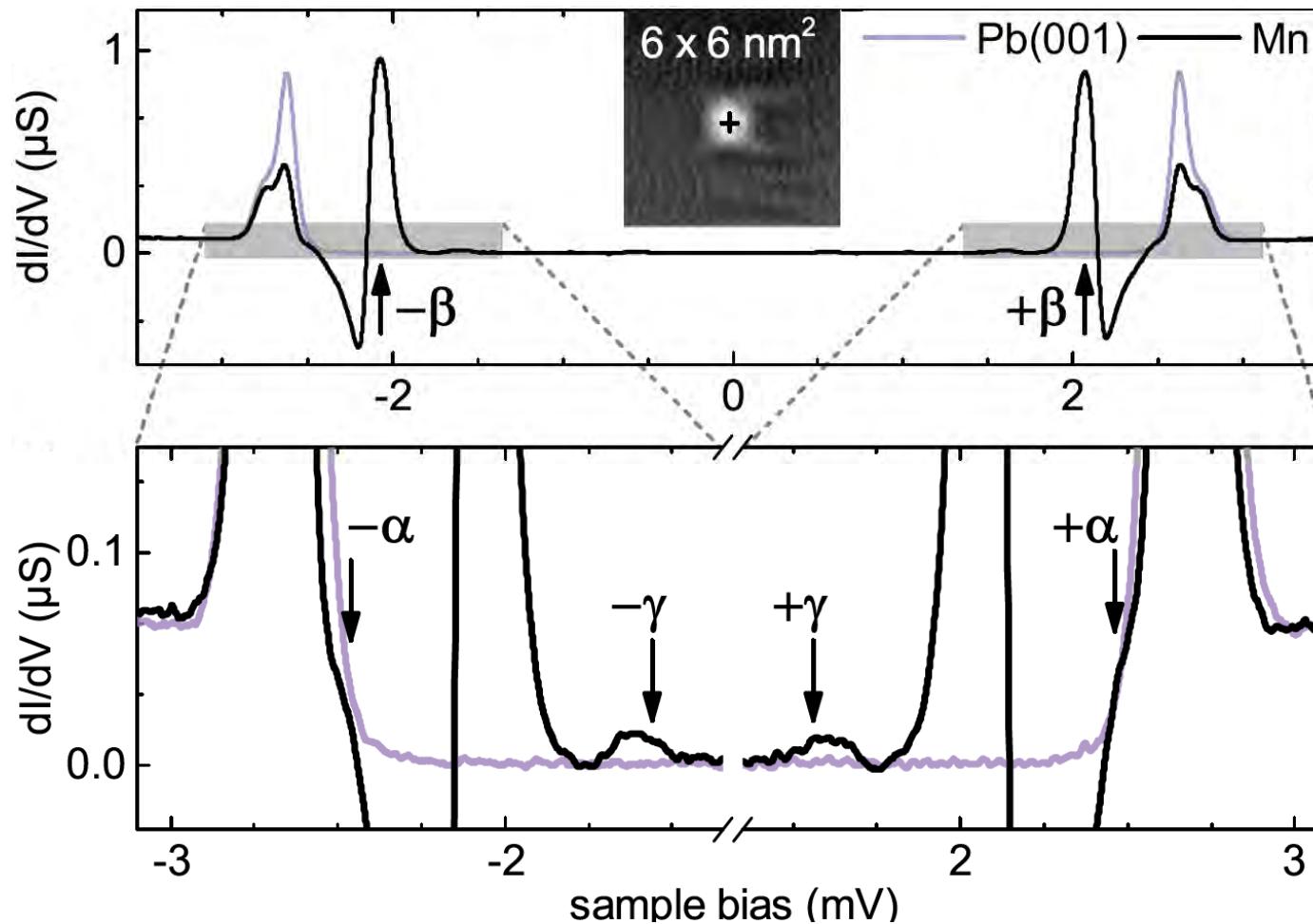


- ▶ sublinear increase of Shiba state conductance at high tunnel rates
- ▶ inversion of Shiba intensity
- ▶ higher temperatures: cross over at larger tunnel rates
- ▶ thermally activated relaxation



Theory: Pientka, Peng, von Oppen

Lifetimes:
0.2 ns at 1.2 K
6 ps at 4.8 K

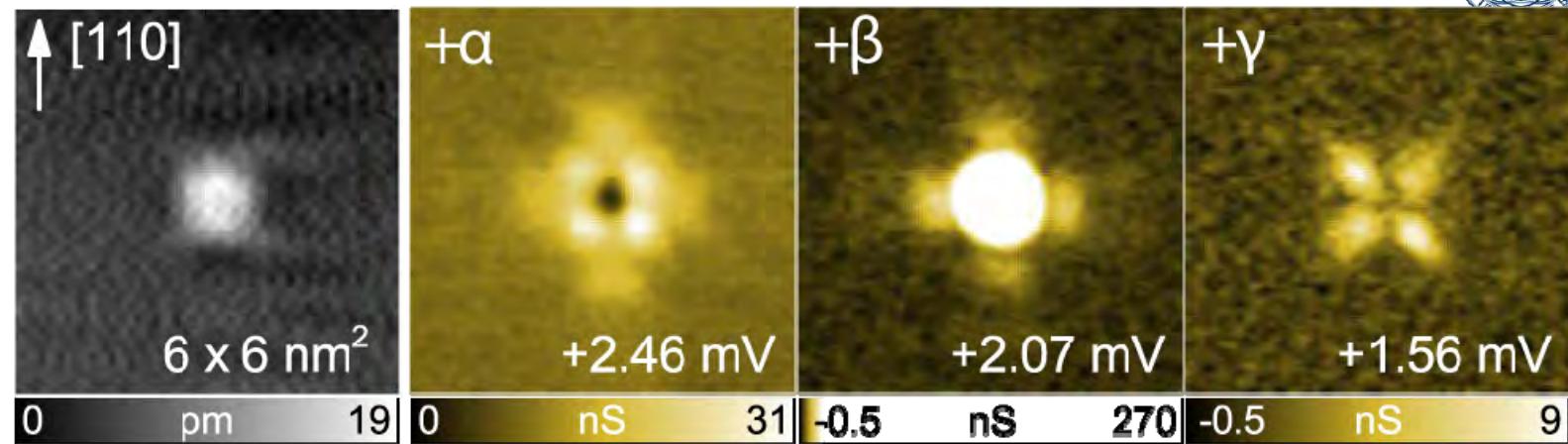


► three Shiba states of Mn atoms

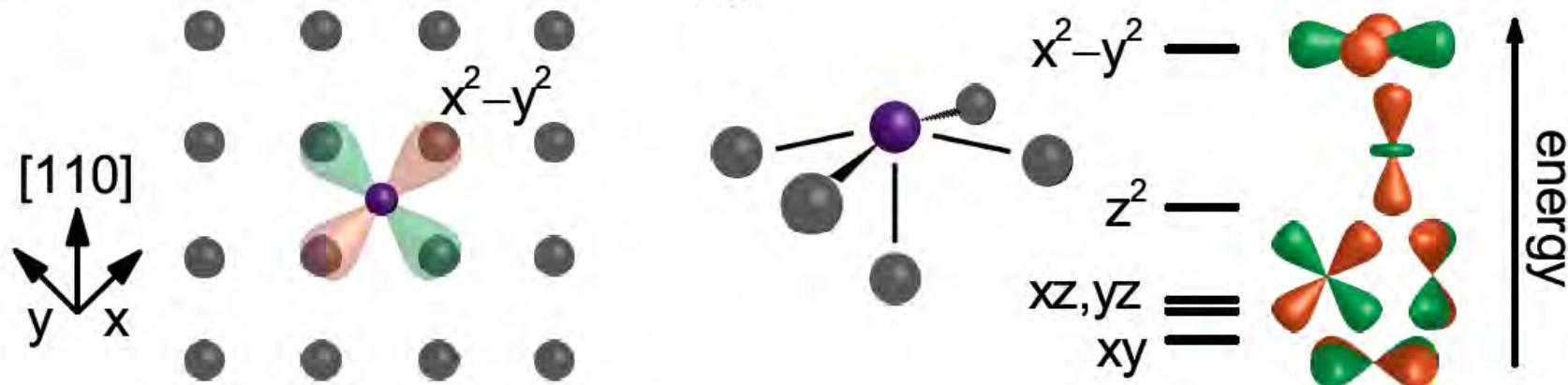
M. Ruby et al., Phys. Rev. Lett. 117, 186801 (2016)

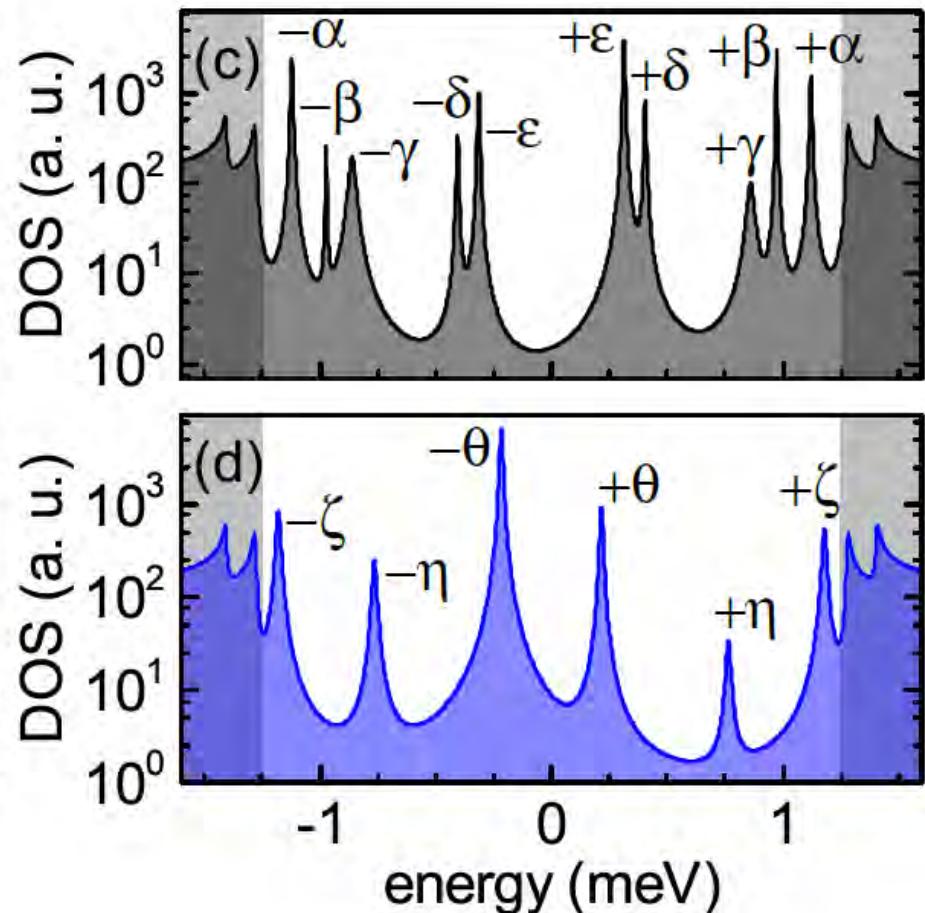
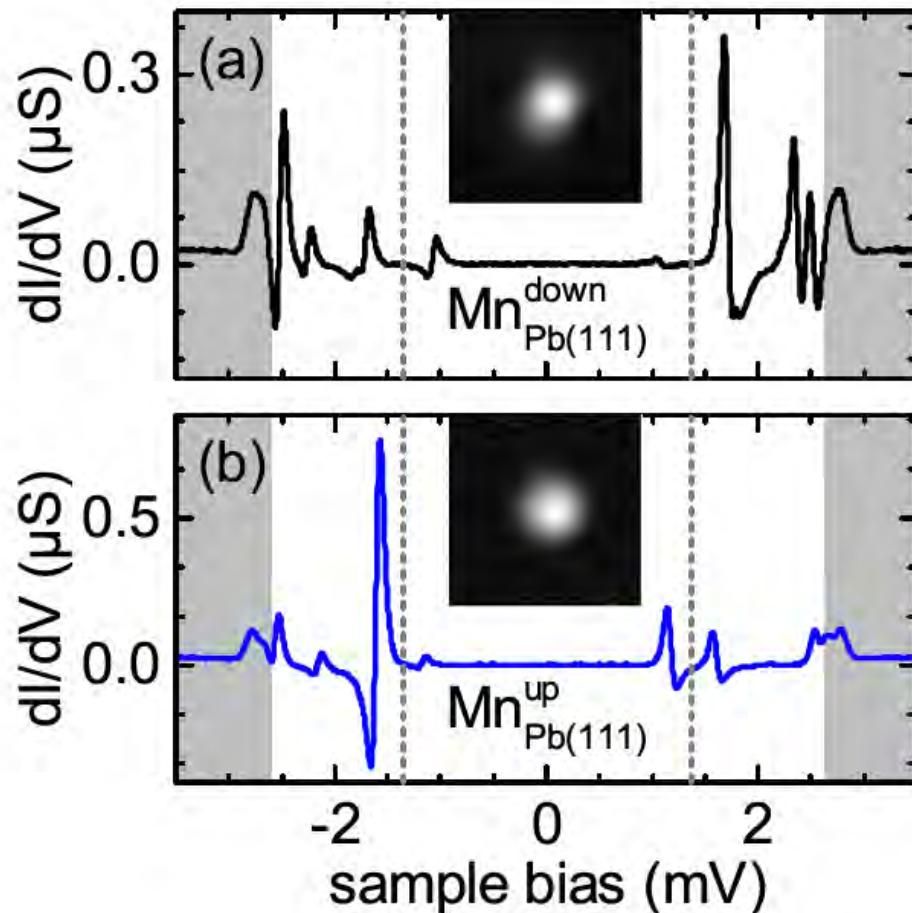
Related: Choi, et al., arXiv:1608.03752 (2016)

Origin of multiple Shiba states



- ▶ characteristic shape of Shiba states resembles d-orbitals





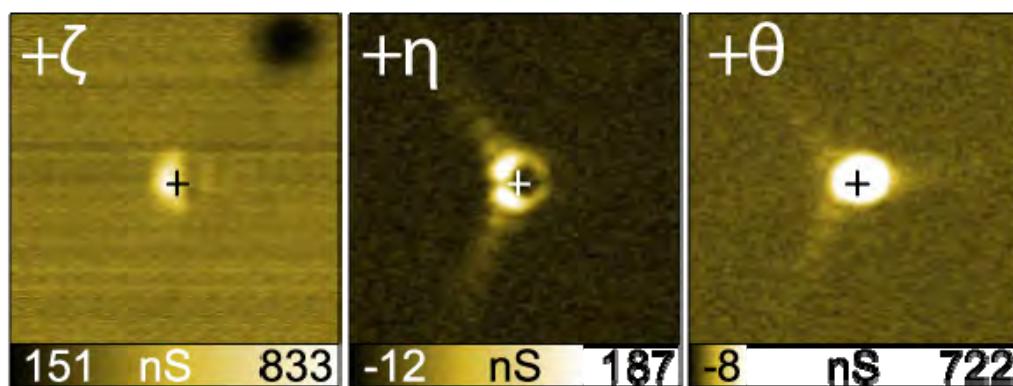
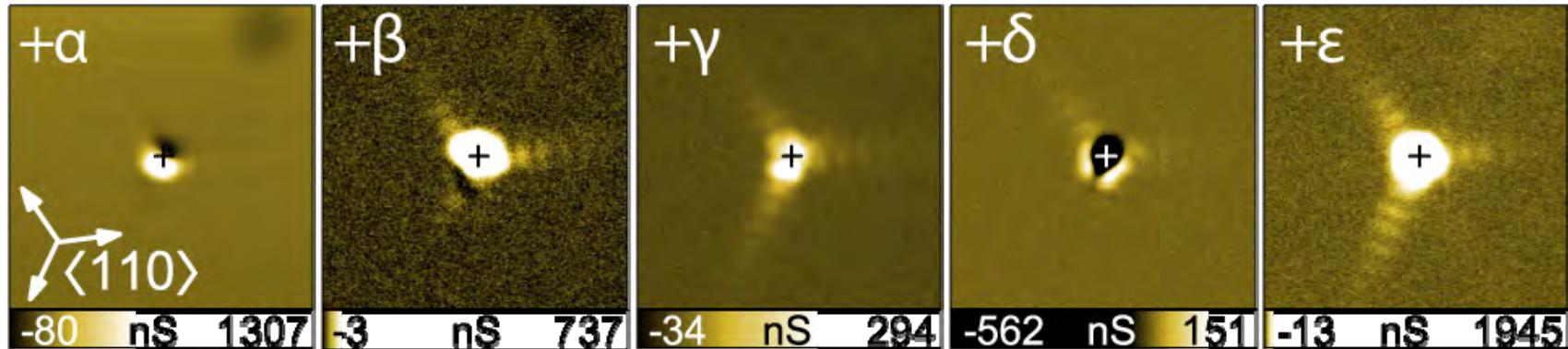
- ▶ different adsorption sites yield different Shiba splittings
- ▶ crystal field splitting

Pb(111): shape and extension of Shiba states

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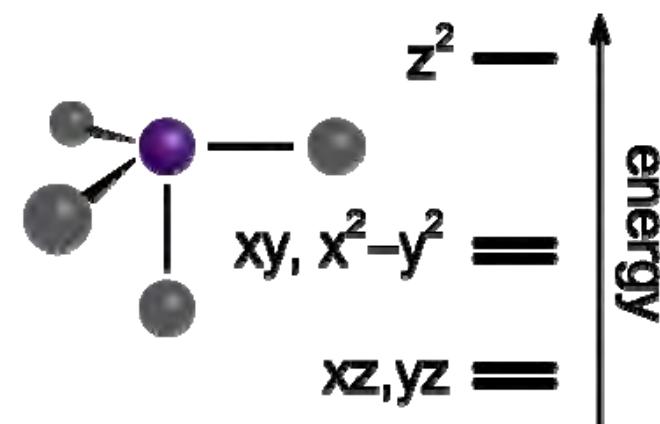
dI/dV maps, $8.8 \times 8.8 \text{ nm}^2$

d_{xy,x^2-y^2}

$d_{xz,yz}$

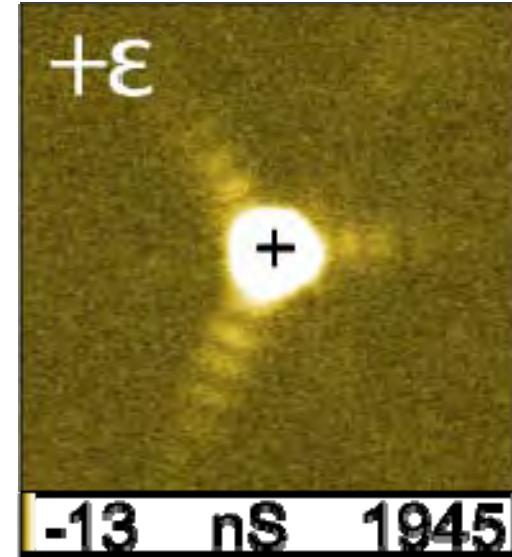
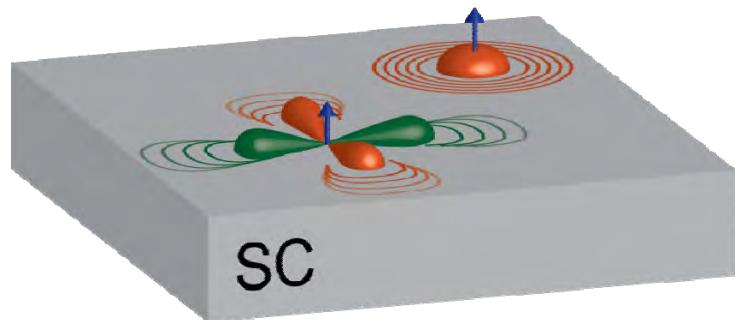
d_{z^2}

- ▶ all degeneracies lifted
- ▶ crystal field splitting:



Shape and extension of Shiba states

Freie Universität Berlin



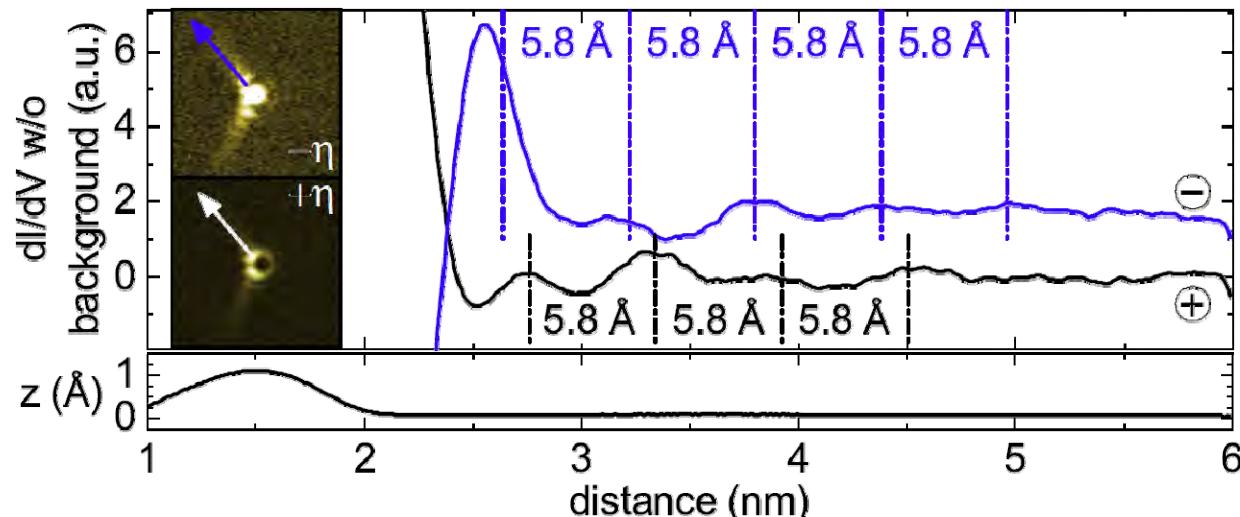
- ▶ maps reflect symmetry of singly occupied states
- ▶ extension?

$$\psi^{\pm}(r) \propto \frac{\sin(k_F r + \delta^{\pm})}{k_F r} \exp\left[-|\sin(\delta^+ - \delta^-)| \frac{r}{\xi}\right]$$

$$\epsilon = \Delta \cos(\delta^+ - \delta^-)$$

Shape and extension of Shiba states

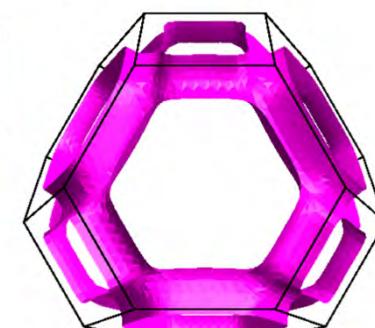
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- ▶ oscillation with the Fermi wave length / 2
- ▶ phase shift between negative and positive energy

$$\psi^\pm(r) \propto \frac{\sin(k_F r + \delta^\pm)}{k_F r} \exp\left[-|\sin(\delta^+ - \delta^-)| \frac{r}{\xi}\right]$$

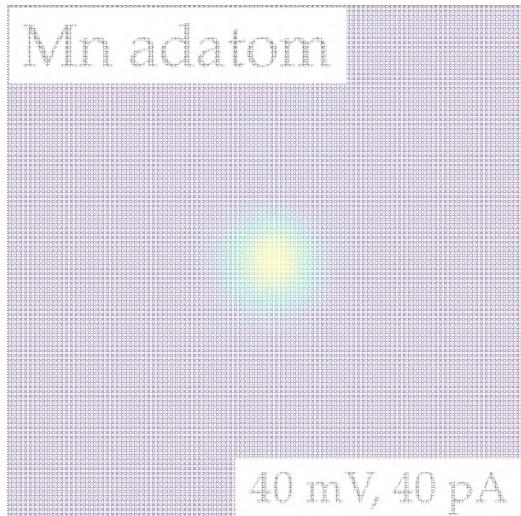
- ▶ anisotropic scattering due to anisotropic Fermi surface
- ▶ identification of Fermi sheet



(p-d character)

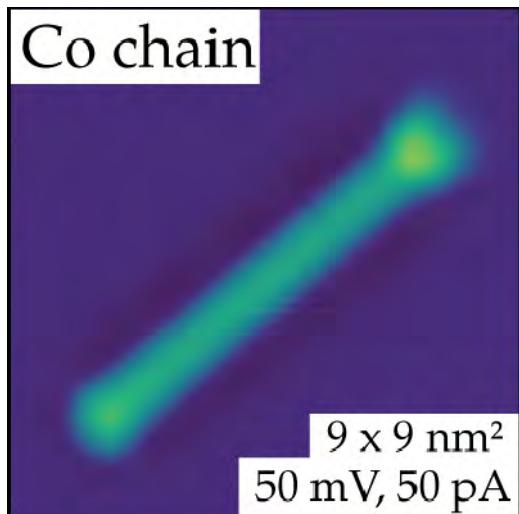
$\langle 110 \rangle$ direction $\lambda_F = 12.1 \pm 0.5$ Å

Outline



Single atoms: Mn on Pb(111) and Pb(100)

- ▶ Transport mechanisms through Shiba states?
- ▶ Multiple Shiba states



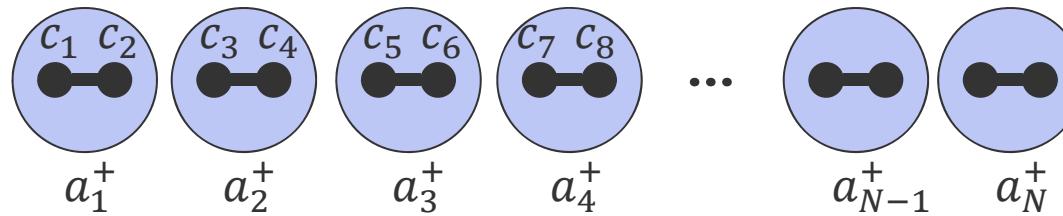
Atomic chains: Co on Pb(110)

- ▶ Shiba bands and Majorana states?

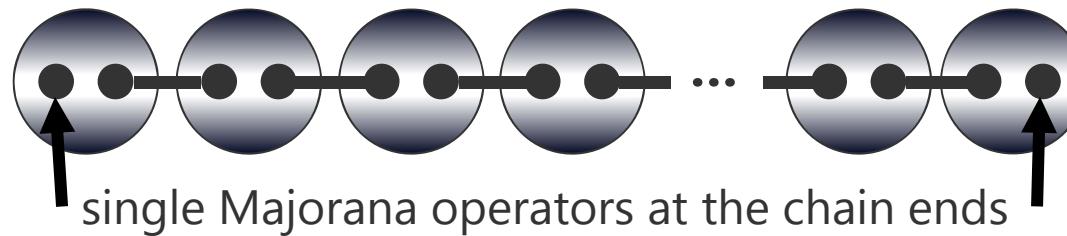
Toy model: Kitaev chain



- ▶ 1D chain of atomic sites



non-topological



topological

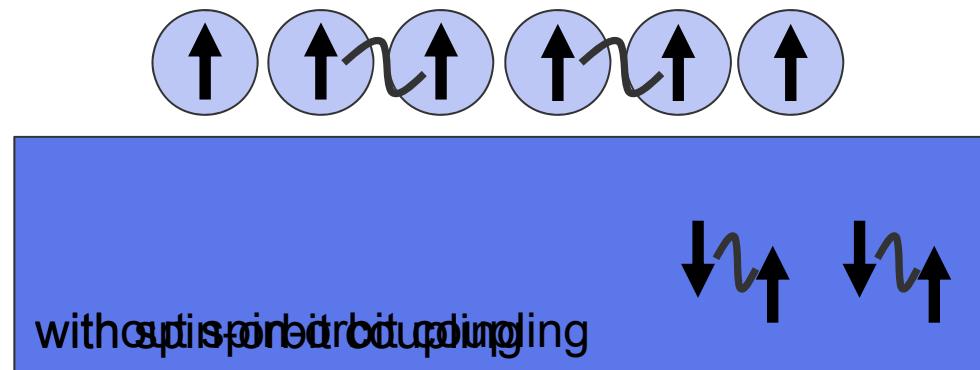
- ▶ conditions for the topological state:
 - ▶ spin-less bands along the chain
 - ▶ superconductivity within the chain

Transition metal chains on Pb(110)



► concept:

couple a ferromagnetic chain to a superconductor with spin-orbit coupling



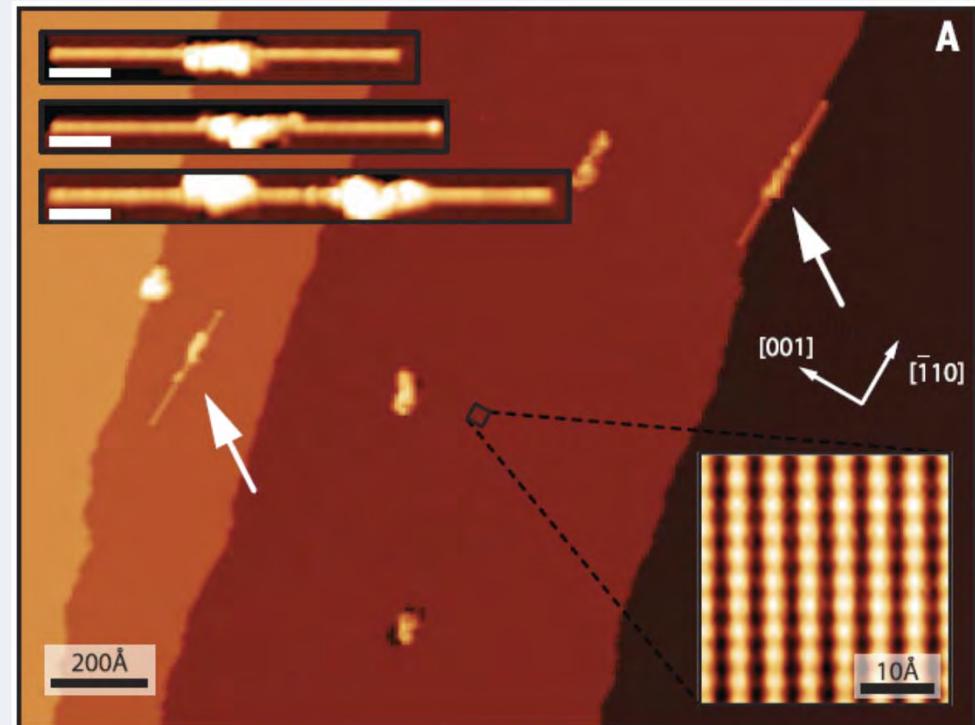
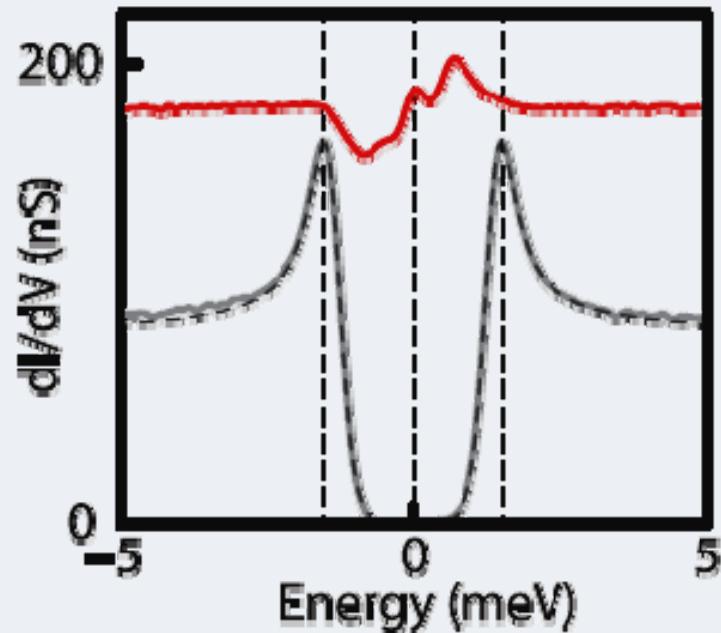
- p-wave superconductivity by proximity
- transition metal chains on Pb(110)

Sub-gap structure in Fe chains

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Nadj-Perge *et al.*, Science 346, 6209 (2014):



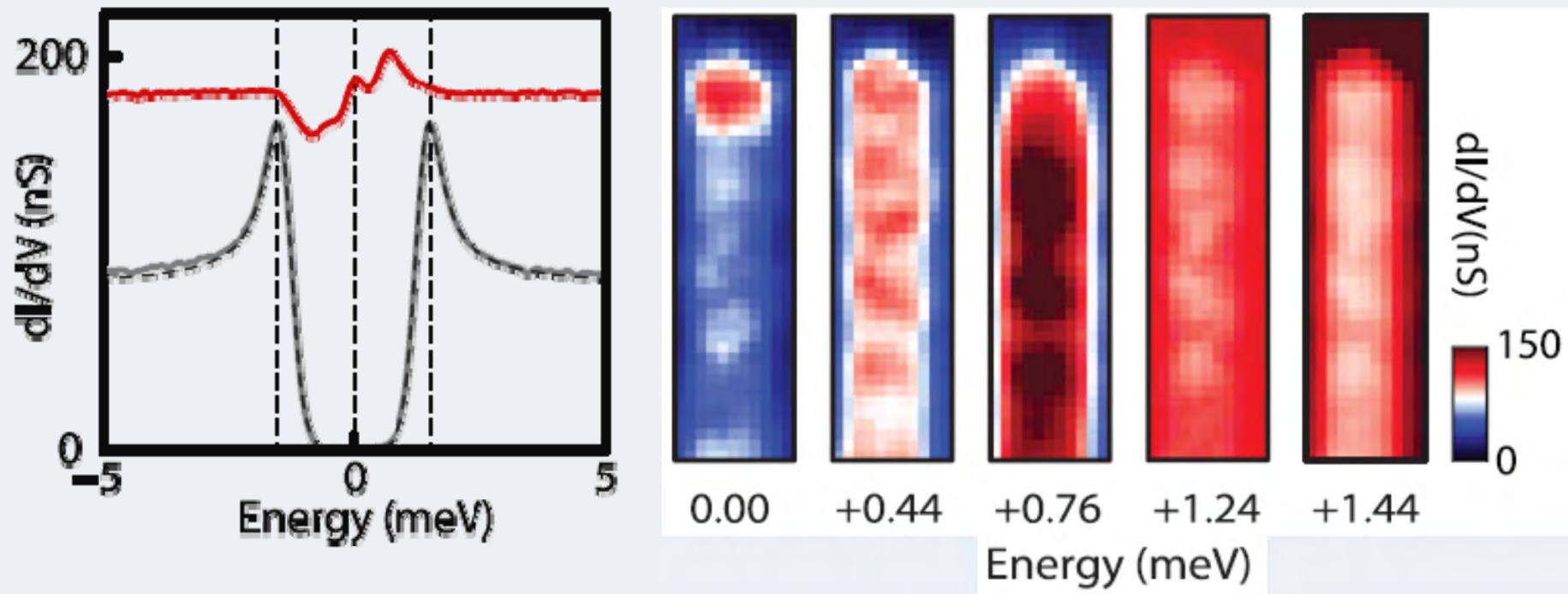
- ▶ Peak at zero bias
- ▶ Localized at chain end
- ▶ Interpretation as Majorana states
- ▶ Topological gap 200-300 μ eV

Sub-gap structure in Fe chains

Freie Universität Berlin



Nadj-Perge *et al.*, Science 346, 6209 (2014):

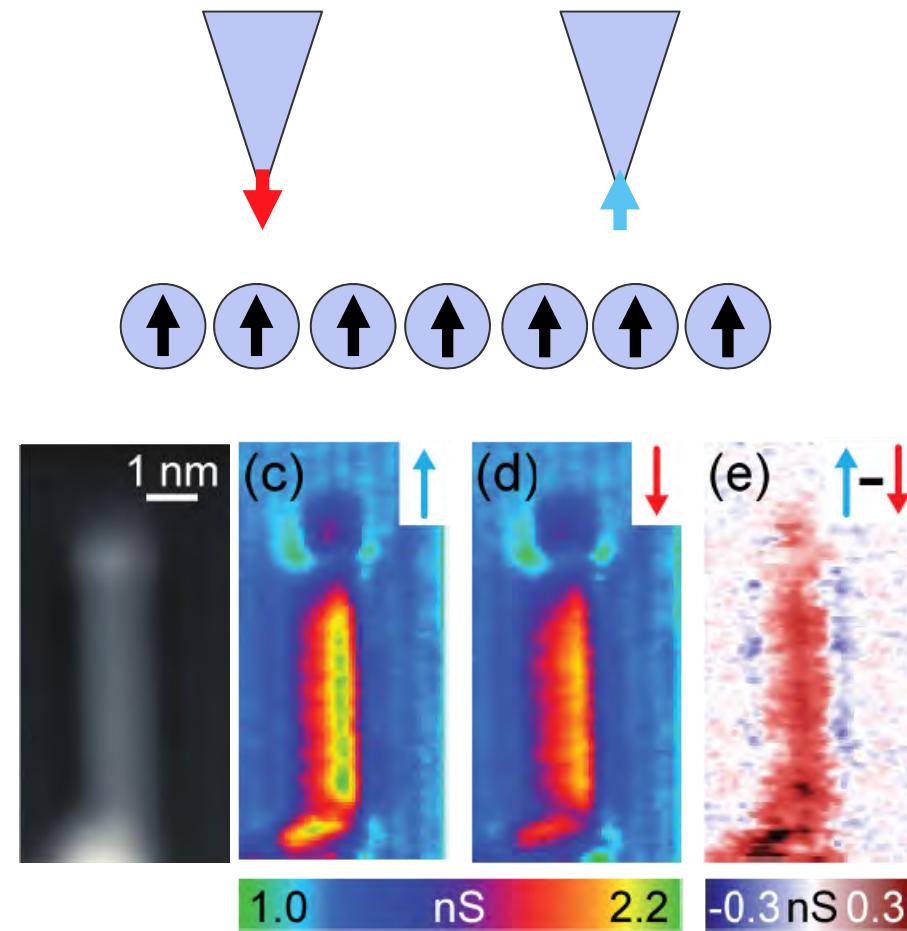
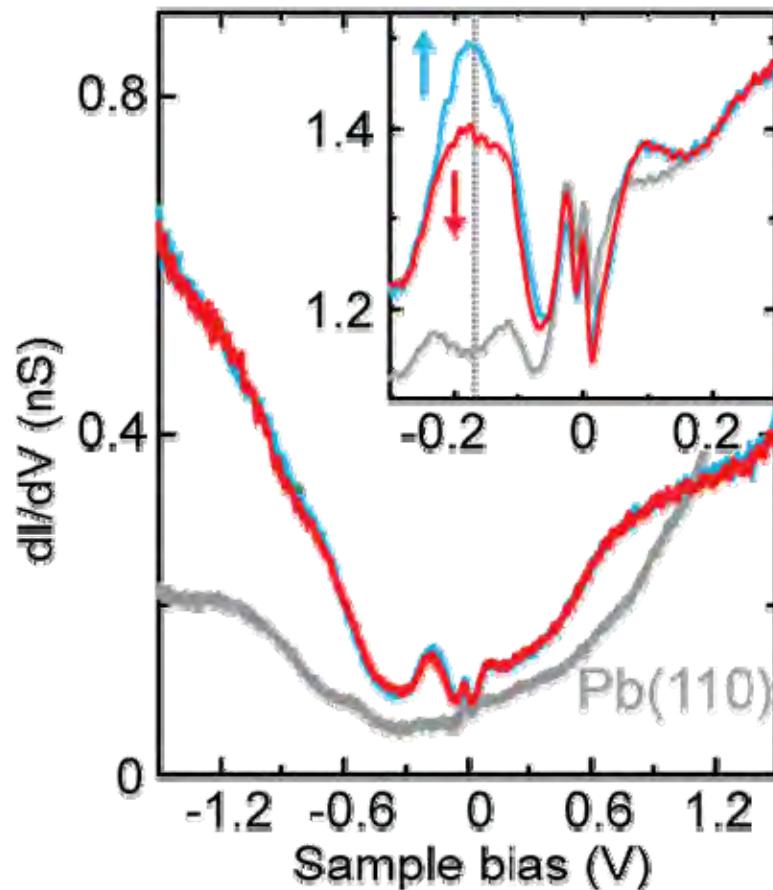


- ▶ Peak at zero bias
- ▶ Localized at chain end
- ▶ Interpretation as Majorana states
- ▶ Topological gap 200-300 μ eV

Co chains on Pb(110): ferromagnetism



- check for ferromagnetism with spin-polarized tips

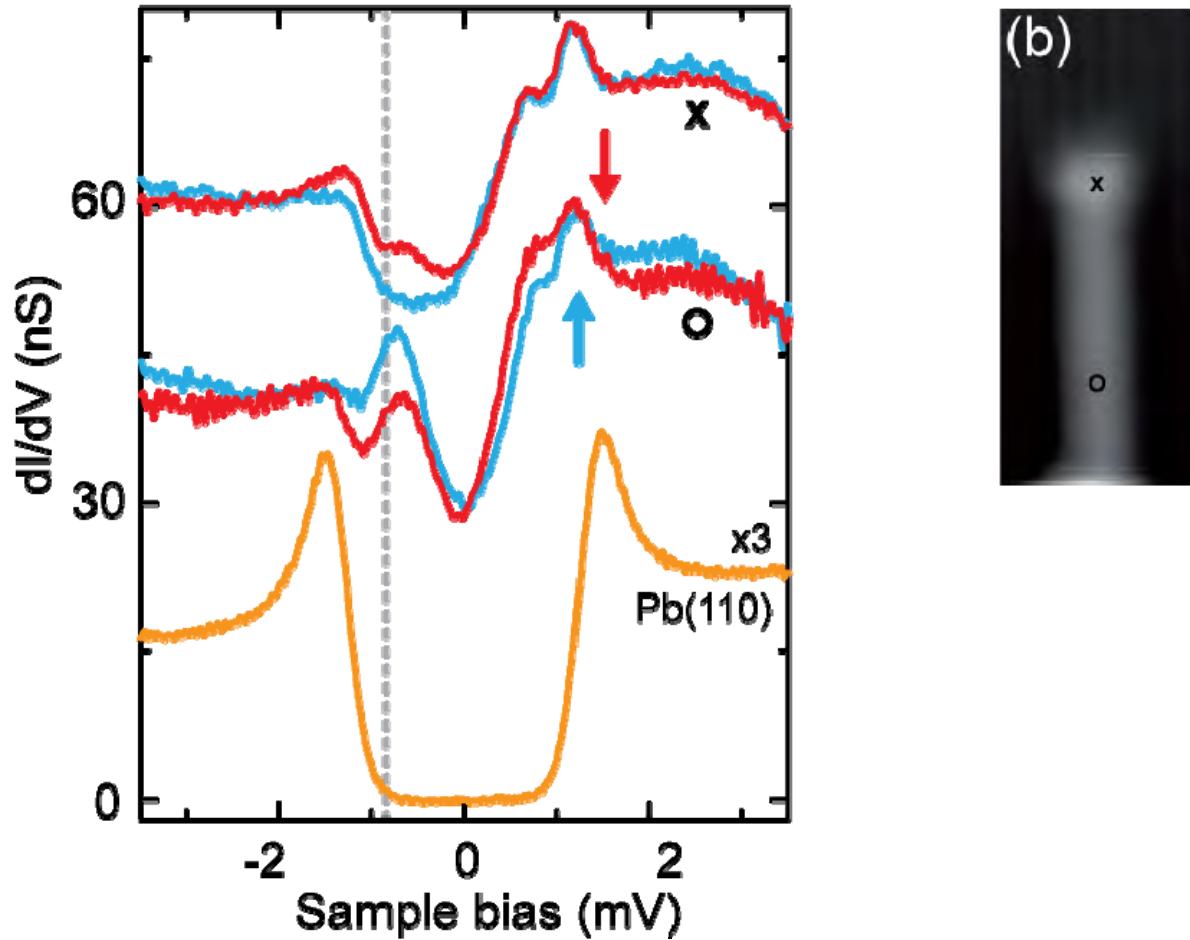


- spin-polarized d-bands
- ferromagnetic coupling

Co chain on Pb(110): Shiba bands



- check for Shiba bands with spin-polarized tips

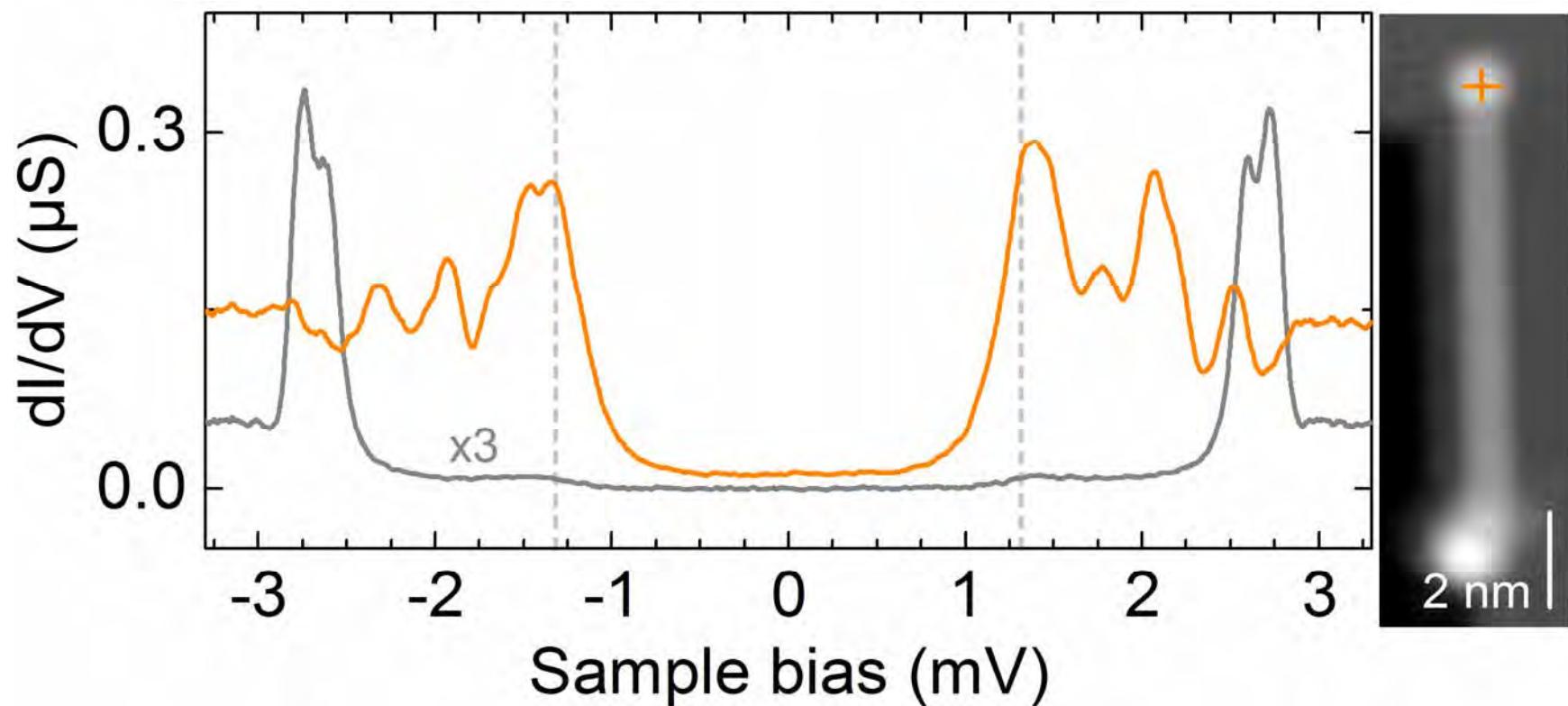


- spin-polarized Shiba-bands

Co chains on Pb(110)



- check for superconductivity within the chain



- signatures for a topological gap observed?

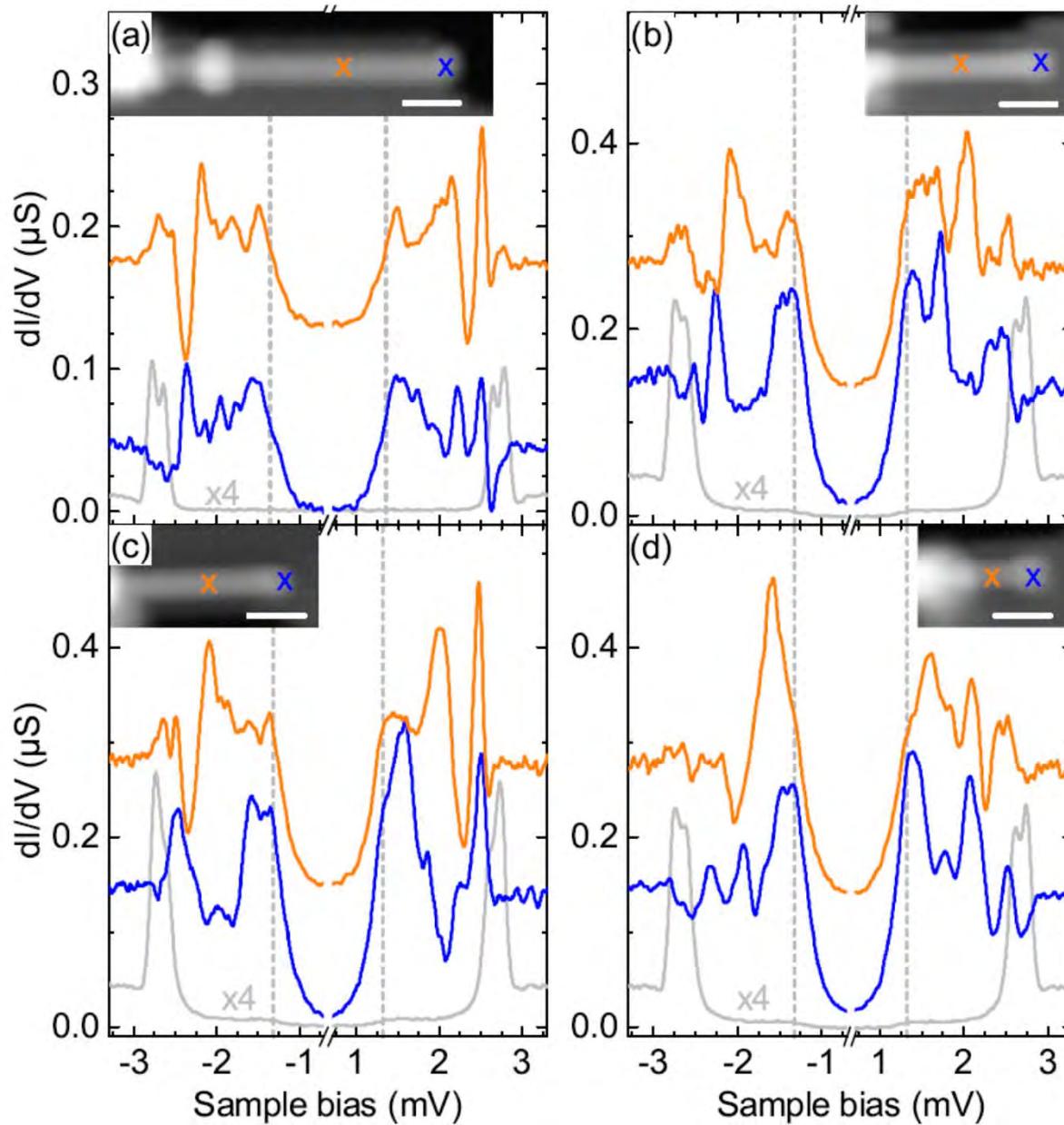
M. Ruby, et al., Nano Lett. 17, 4473 (2017)

Co chains on Pb(110): high resolution subgap structure

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Berlin

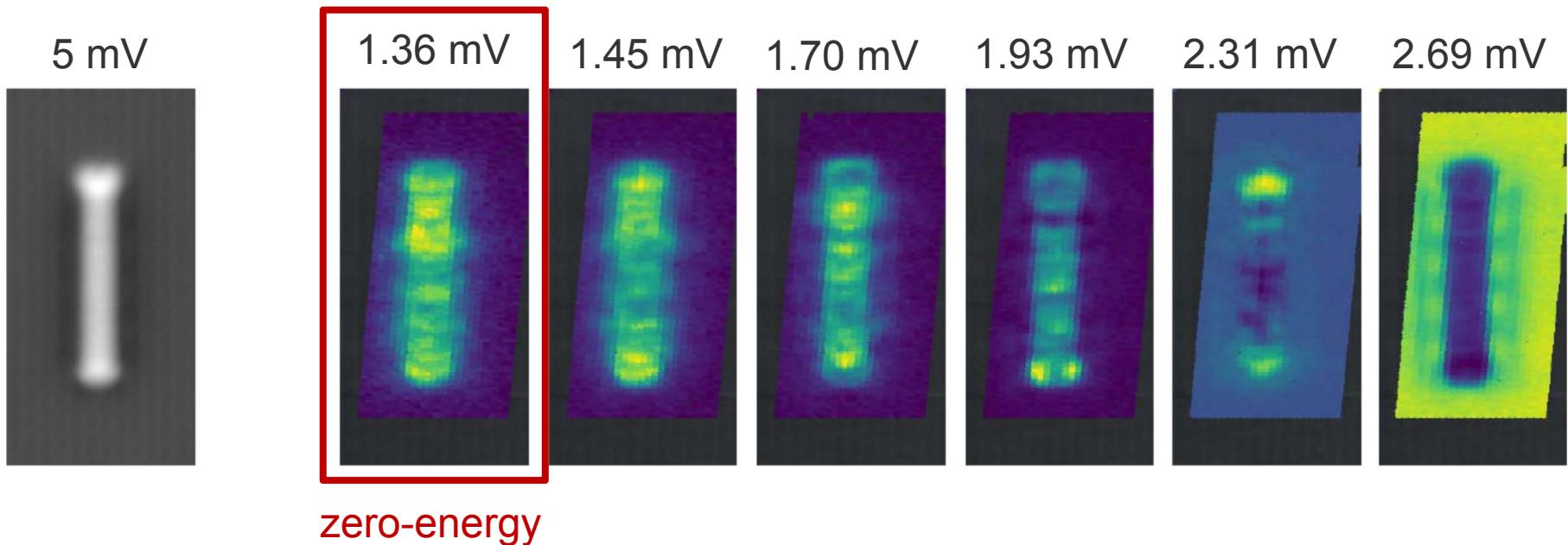


- ▶ peaks/shoulders close to zero energy
- ▶ chains look similar: 2.5-9.4 nm length

Co chains on Pb(110): localization of states



► Conductance maps



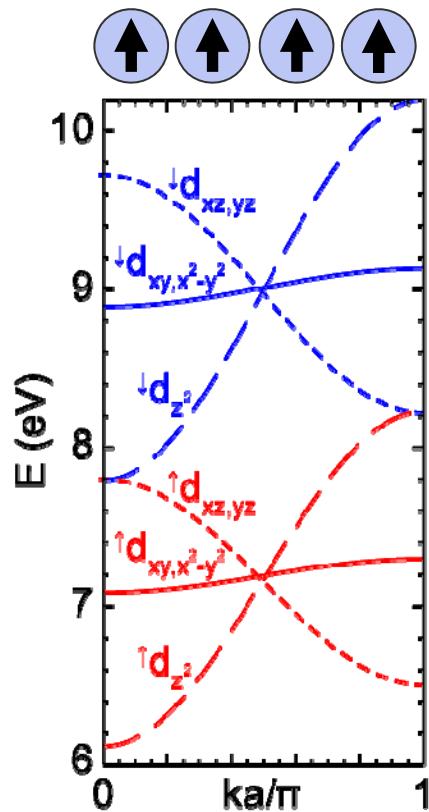
► Homogenous distribution of zero-energy signal

- No sign of Majorana modes
- Why are Fe and Co different?

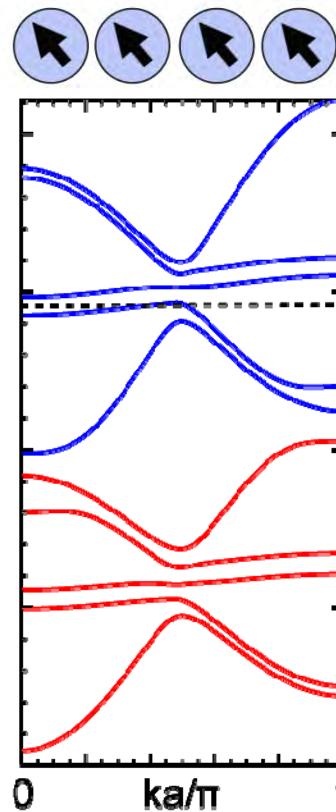
Band structure of Co chains



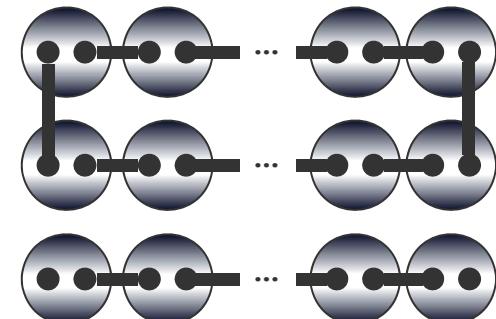
without spin-orbit coupling



with spin-orbit coupling



► # crossings at E_F :

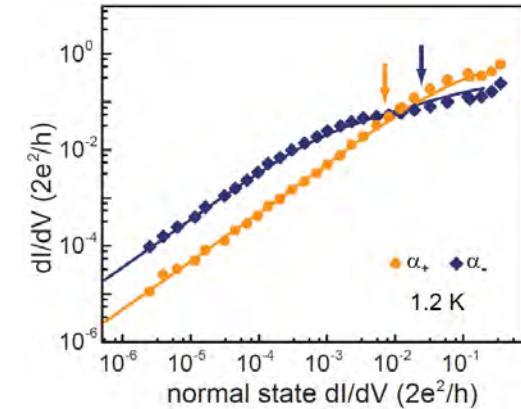


► odd number required

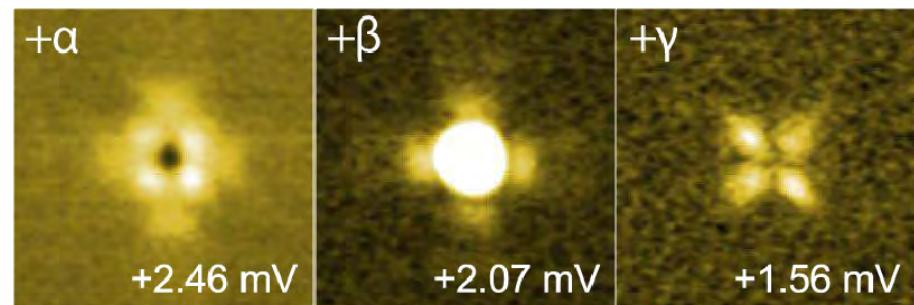
- Fe could have odd number of Fermi points
- Co could have even number of Fermi points

Conclusions

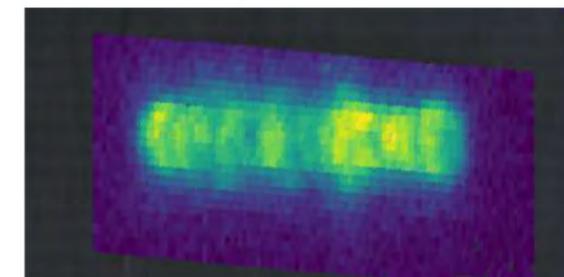
- ▶ Two transport mechanisms through Shiba states:
 - ▶ Single electron tunneling
 - ▶ Resonant Andreev reflections
 - ▶ Thermal relaxation from Shiba states



- ▶ Shiba states of single atoms:
 - ▶ d-level character



- ▶ Rich subgap structure on proximity coupled chains
 - ▶ Co chains do not show localized zero-energy modes



Thanks!

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Gelavizh Ahmadi, Laetitia Farinacci, Marc Font Gual, Nino Hatter, Benjamin Heinrich,
Nils Krane, Eva Liebhaber, Christian Lotze, Olof Peters, Gael Reecht, Daniela Rolf,
Michael Ruby, Lisa Rütten, Max Weigand, Asieh Yousofnejad

Yang Peng, Falko Pientka, Felix von Oppen