

Femtosecond quantum spin dynamics in antiferromagnets

D. Bossini

JSPS "Overseas Researcher" Fellow at University of Tokyo, Japan



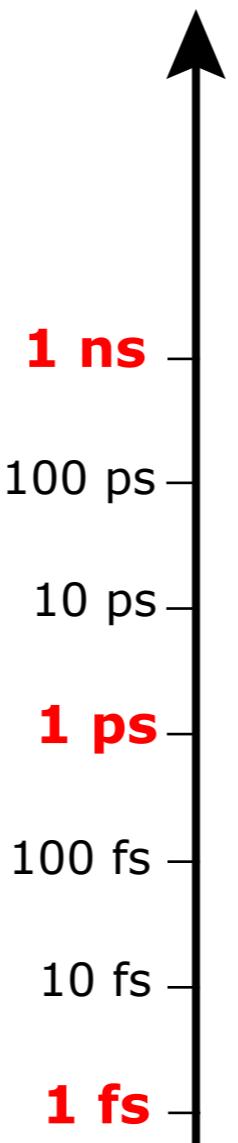
Scientific goal

Scientific goal

Ultrafast manipulation of the magnetic order

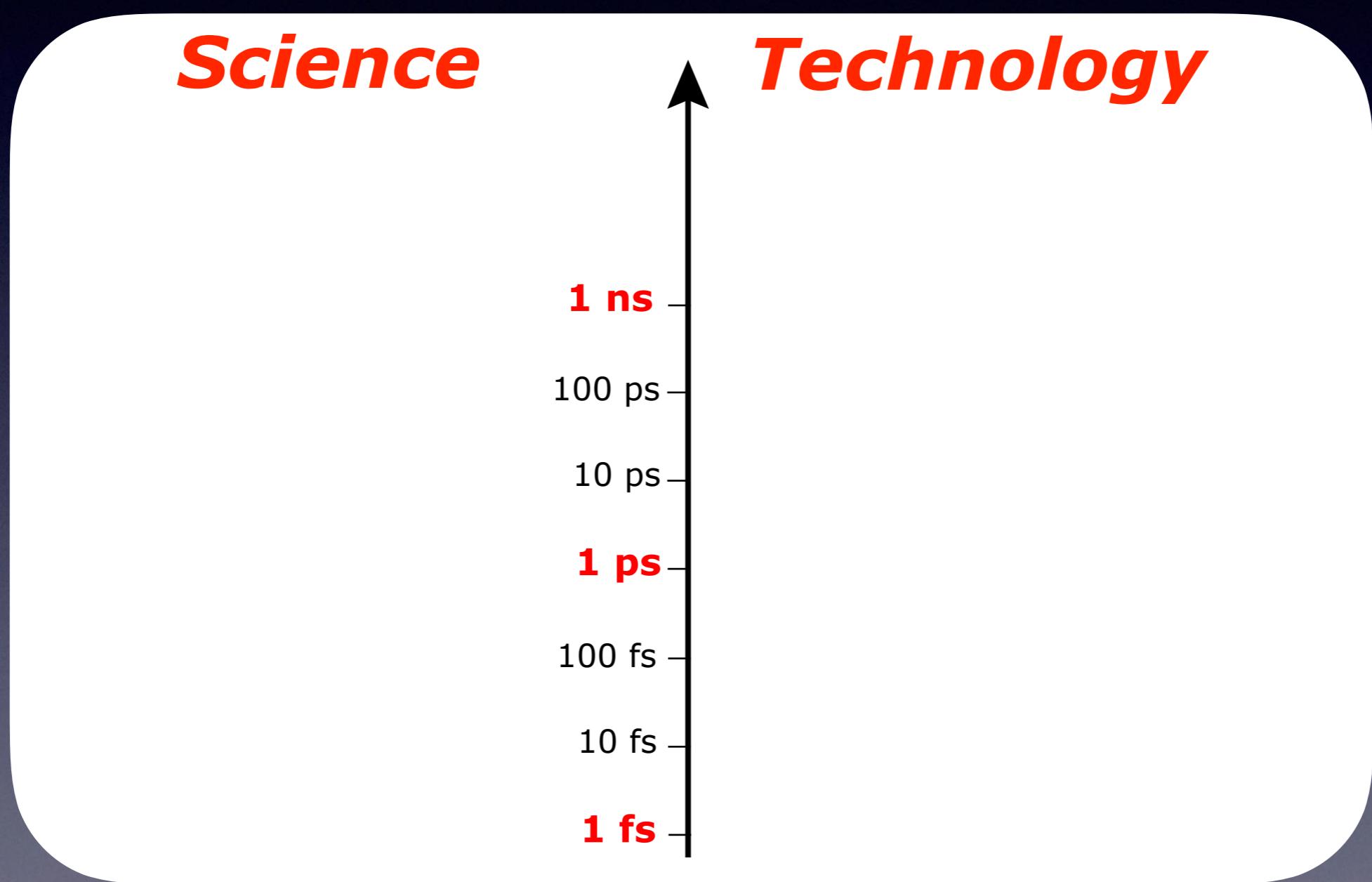
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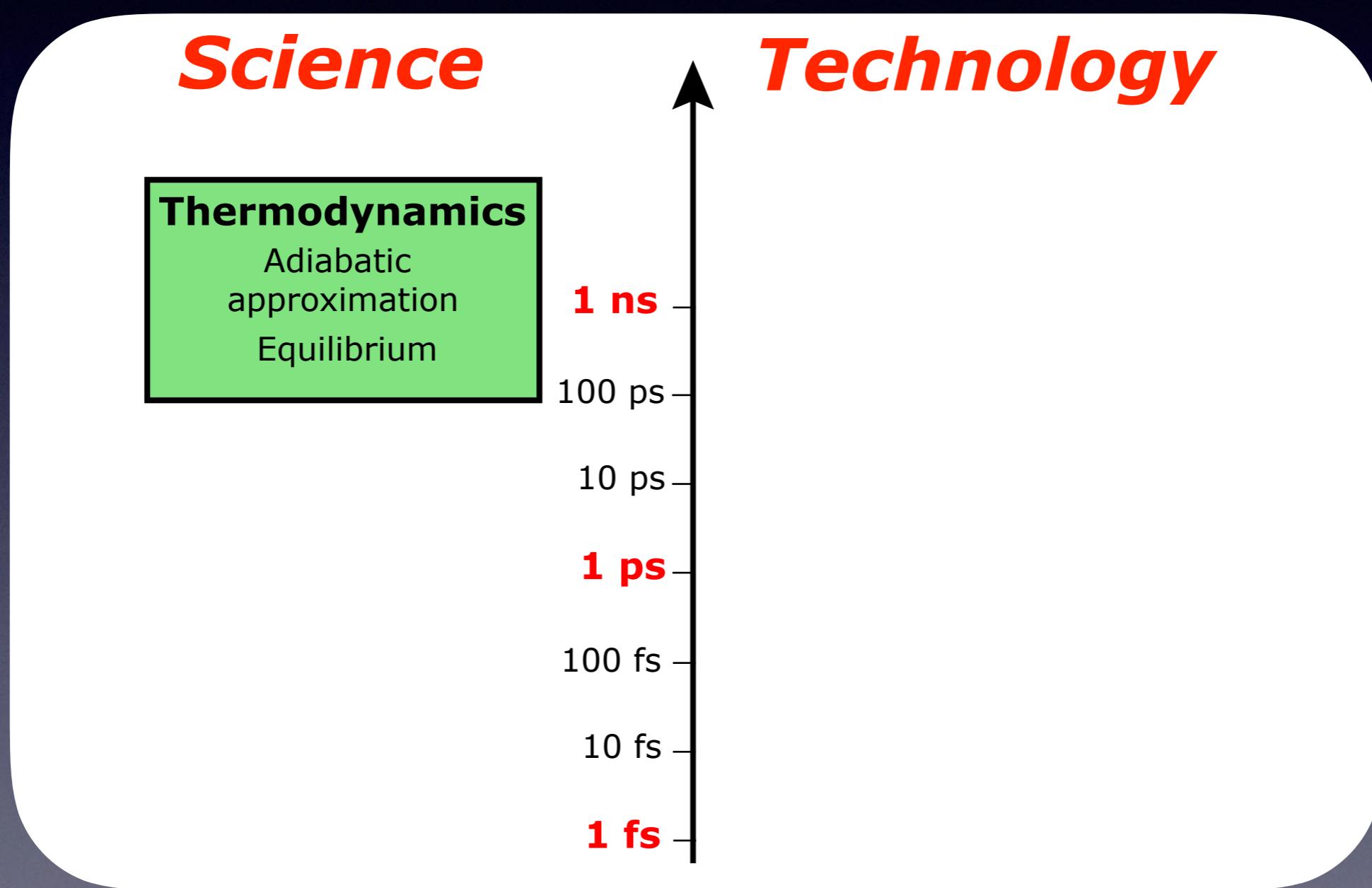
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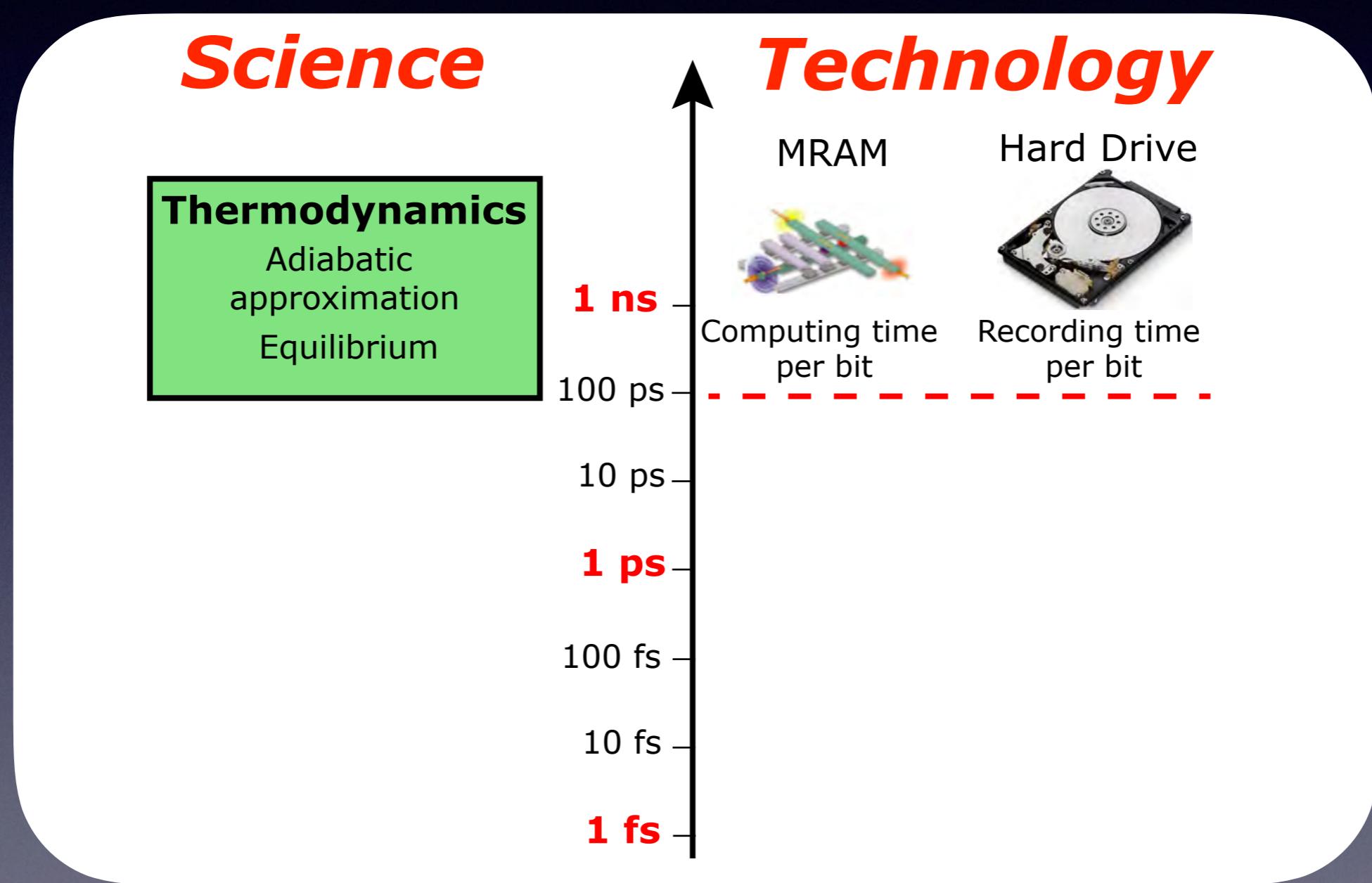
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Ultrafast manipulation of the magnetic order



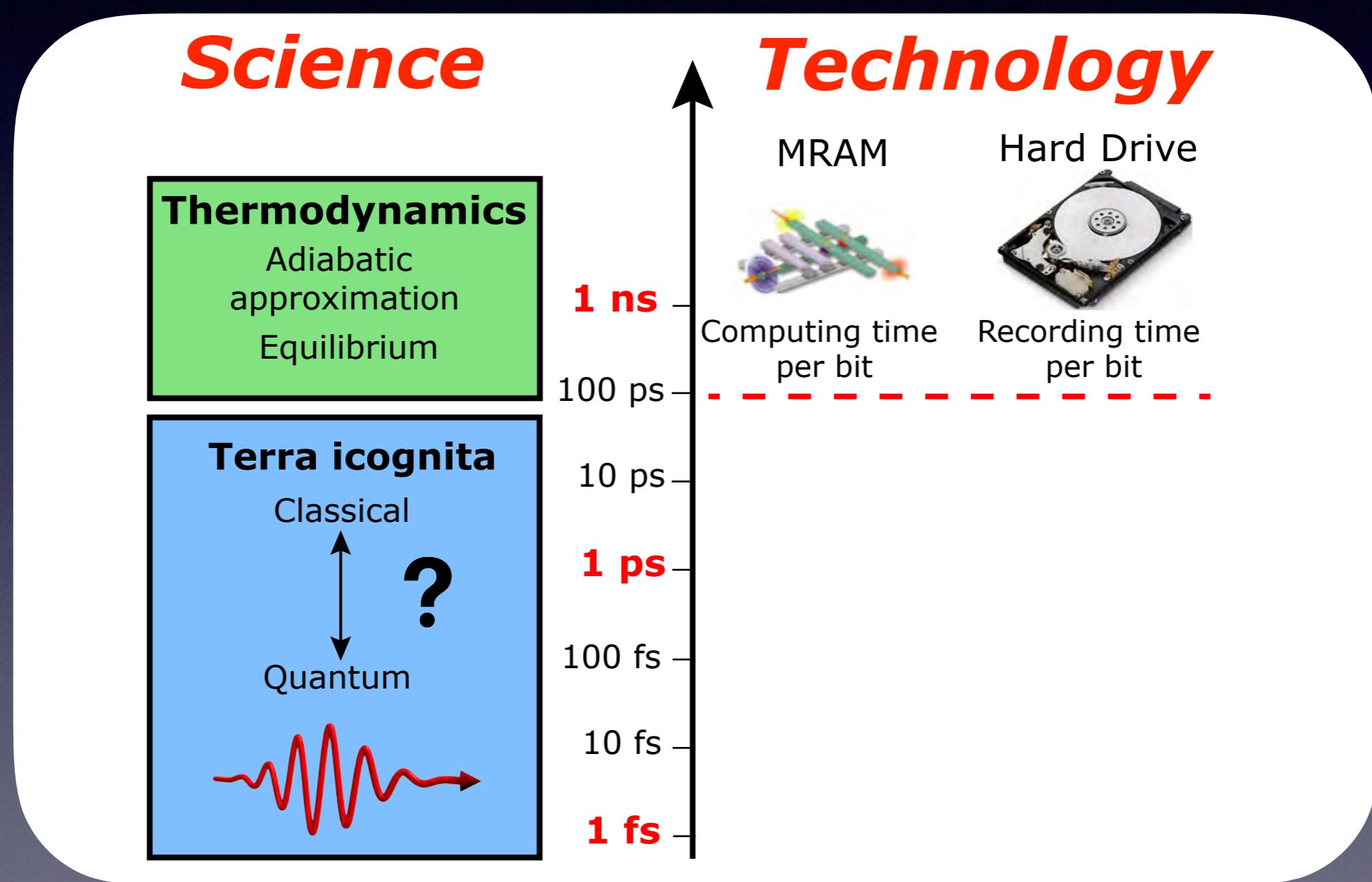
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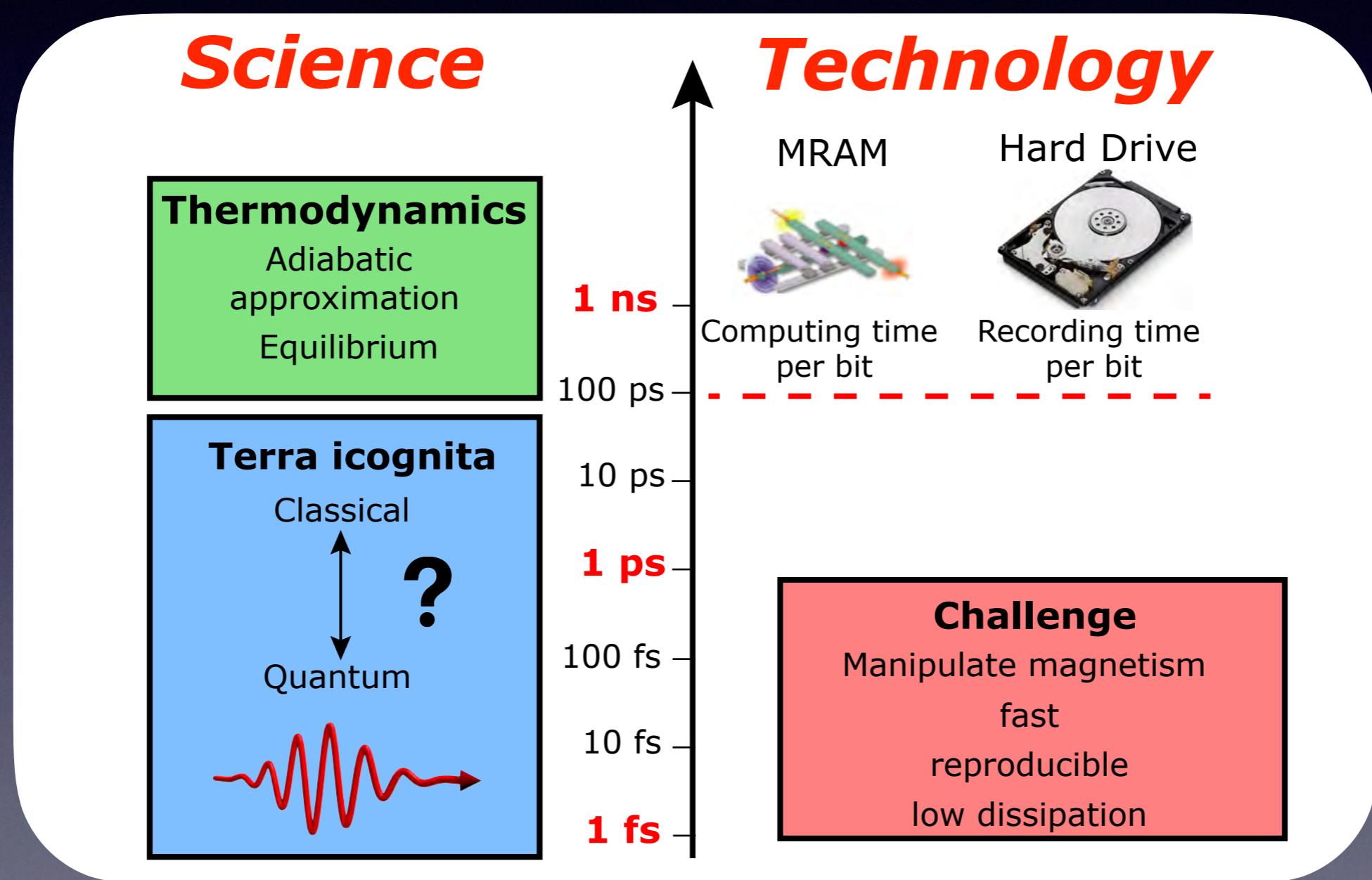
Scientific goal

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Scientific goal

Ultrafast manipulation of the magnetic order

Science

Thermodynamics

Technology

MRAM

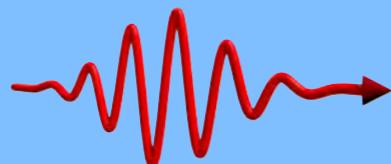
Hard Drive

Femto + Nano + Spin

Classical

Quantum

?



1 ps

100 fs

10 fs

1 fs

Challenge

Manipulate magnetism
fast
reproducible
low dissipation

Dielectric antiferromagnet

Dielectric antiferromagnet

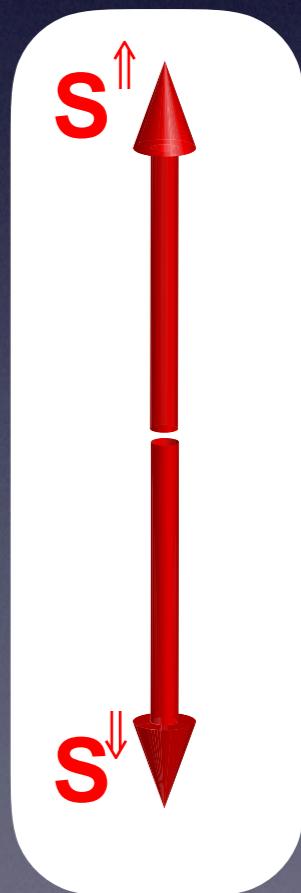
- ✓ No free electrons
- ✓ Majority of magnetically ordered materials
- ✓ No stray field, technological potential
- ✓ Intrinsically faster spin dynamics

Dielectric antiferromagnet

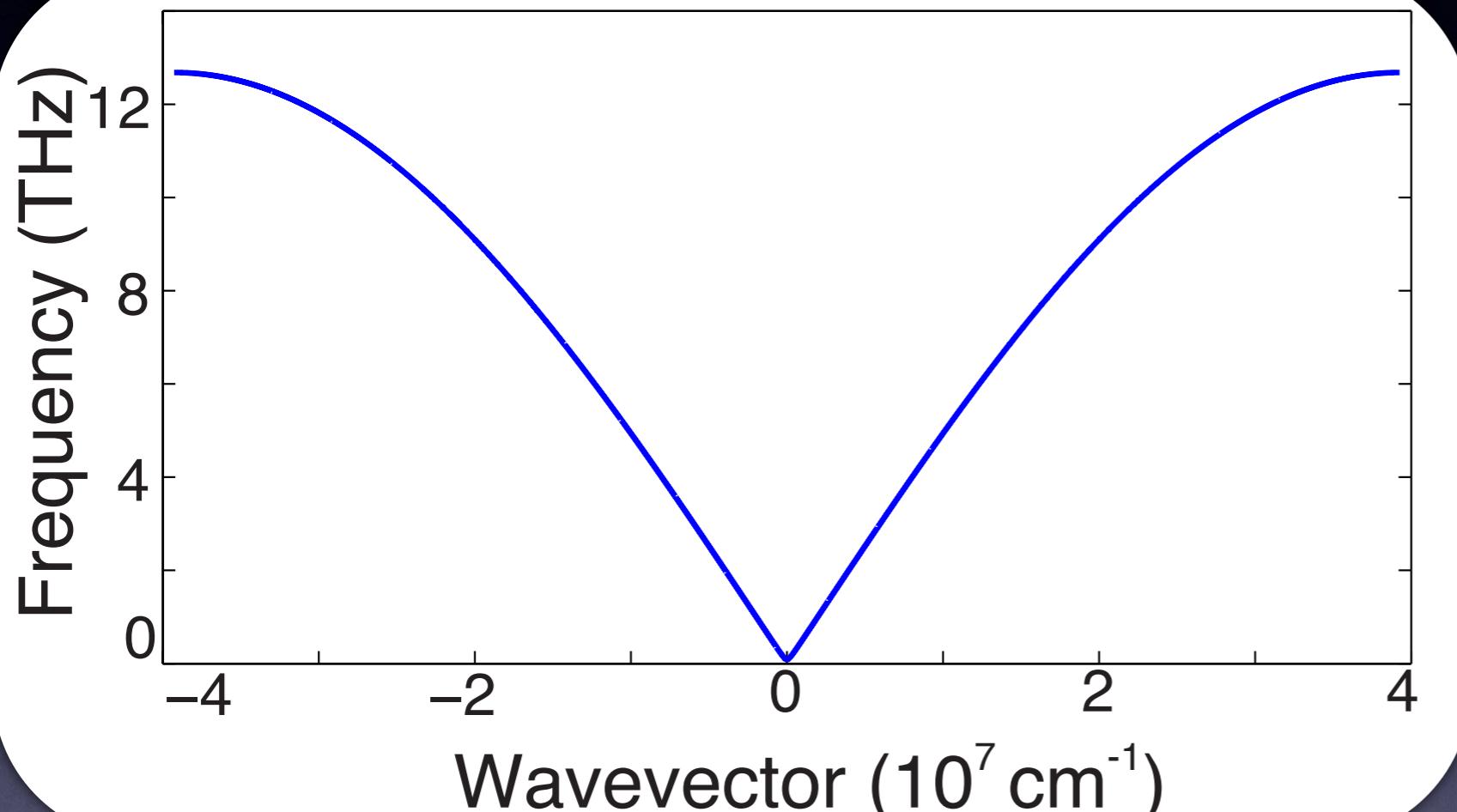
- ✓ No free electrons
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$$\hat{H} = J \sum_{\langle i,j \rangle} \hat{\mathbf{S}}_i \cdot \hat{\mathbf{S}}_j$$

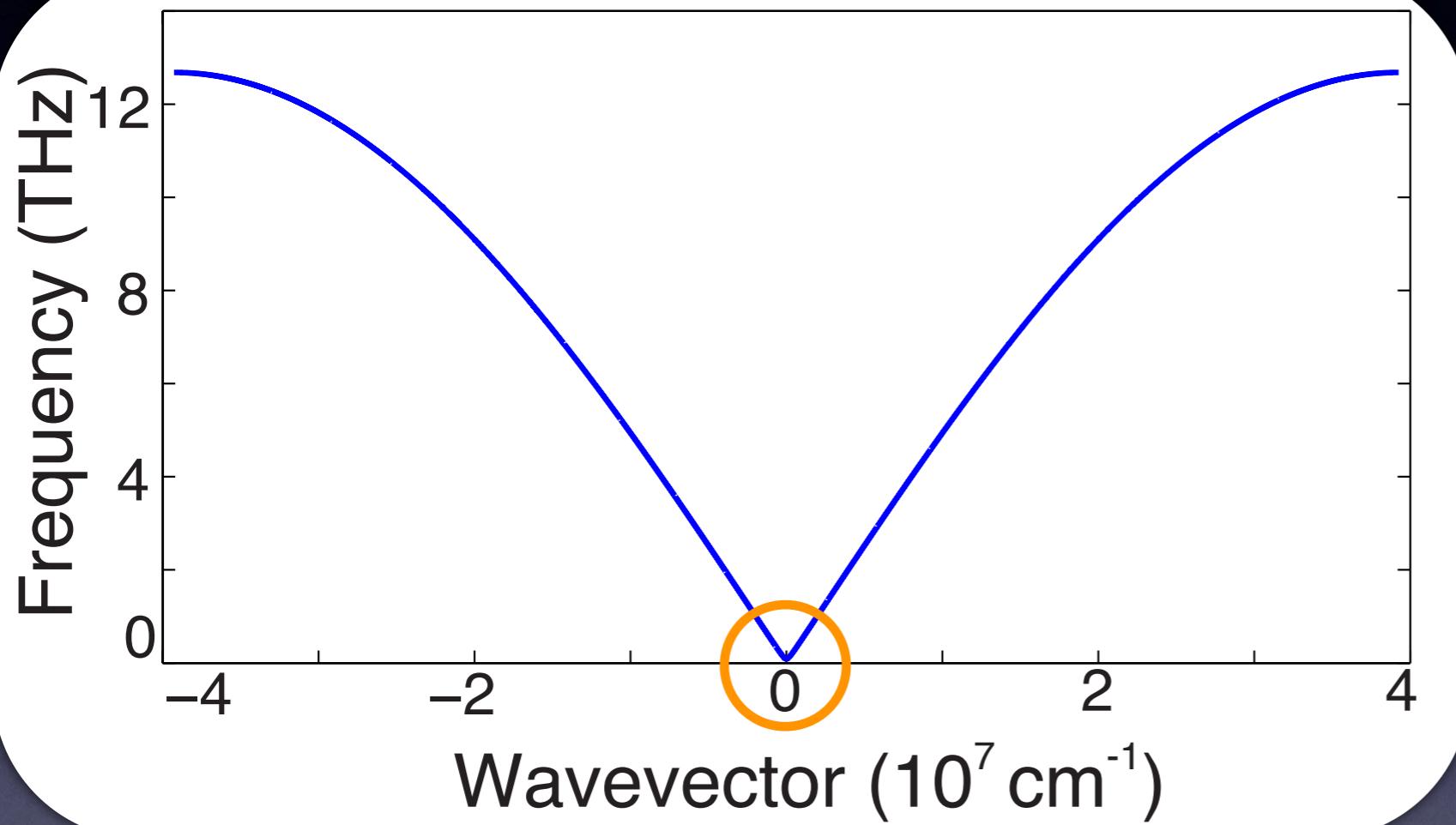
Collinear magnetic sublattices



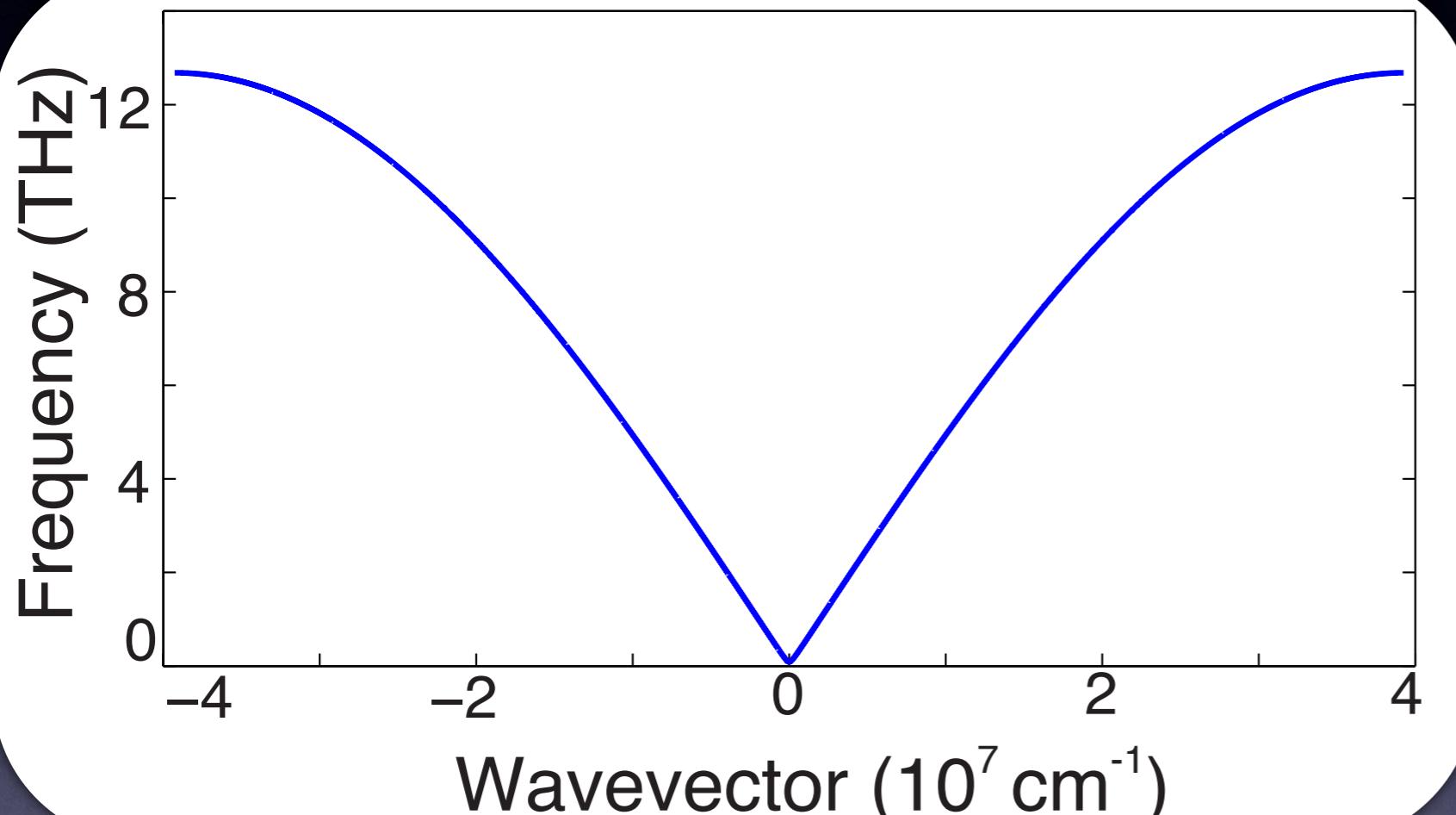
Femto-nanomagnonics



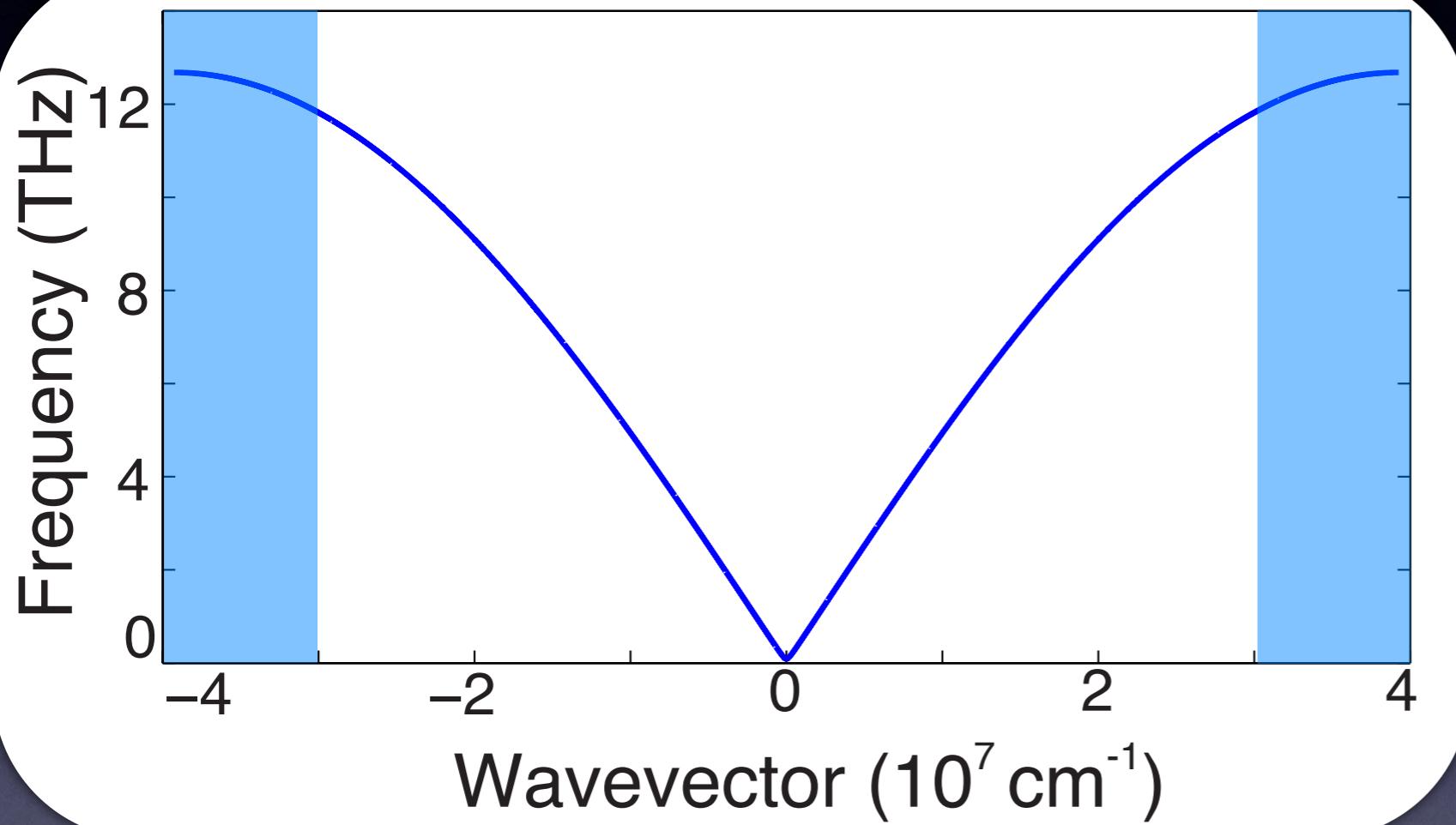
Femto-nanomagnonics



Femto-nanomagnonics

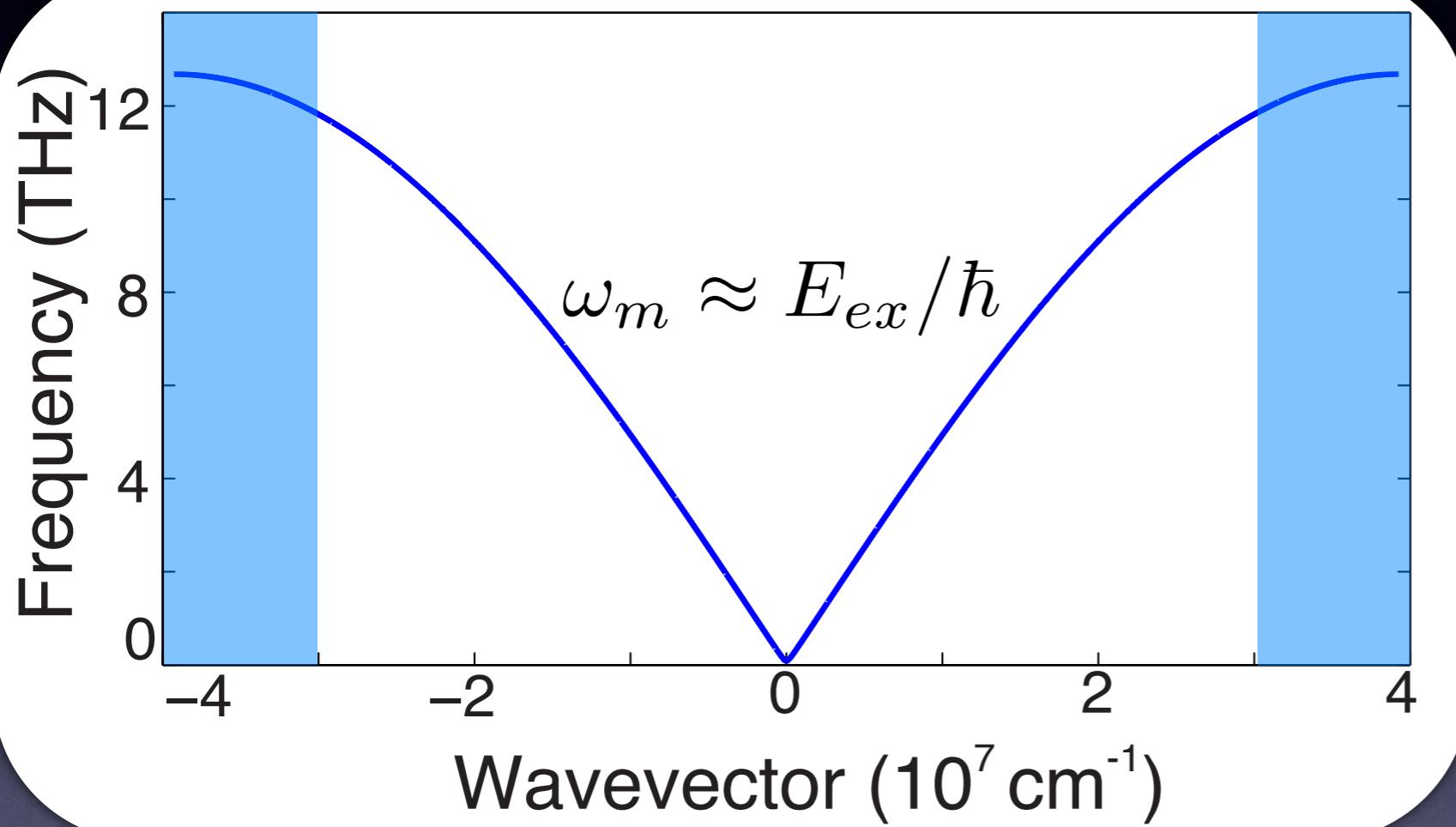


Femto-nanomagnonics



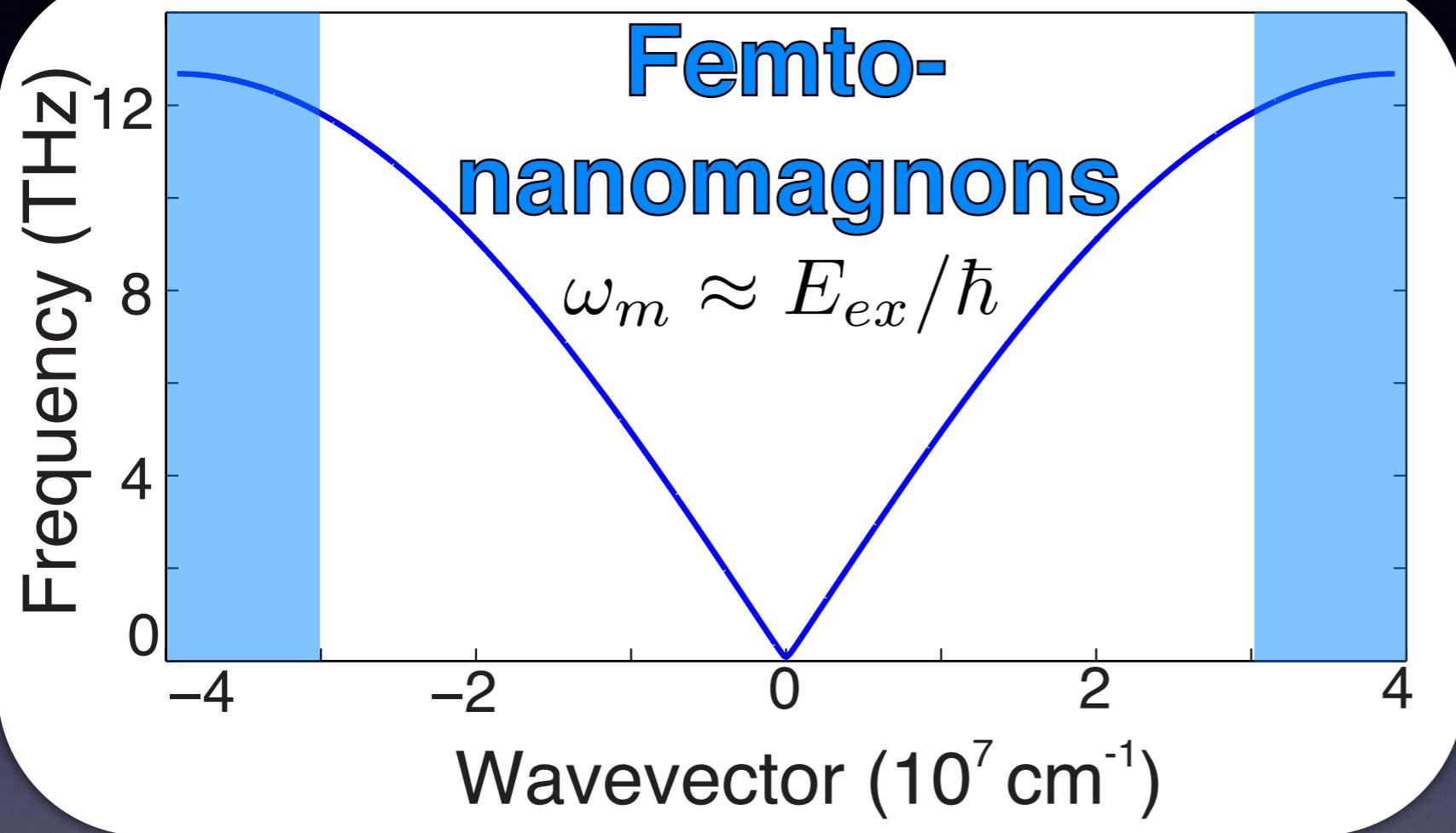
- ✓ Femtosecond period
- ✓ Nanometer wavelength
- ✓ Defined by E_{ex}

Femto-nanomagnonics



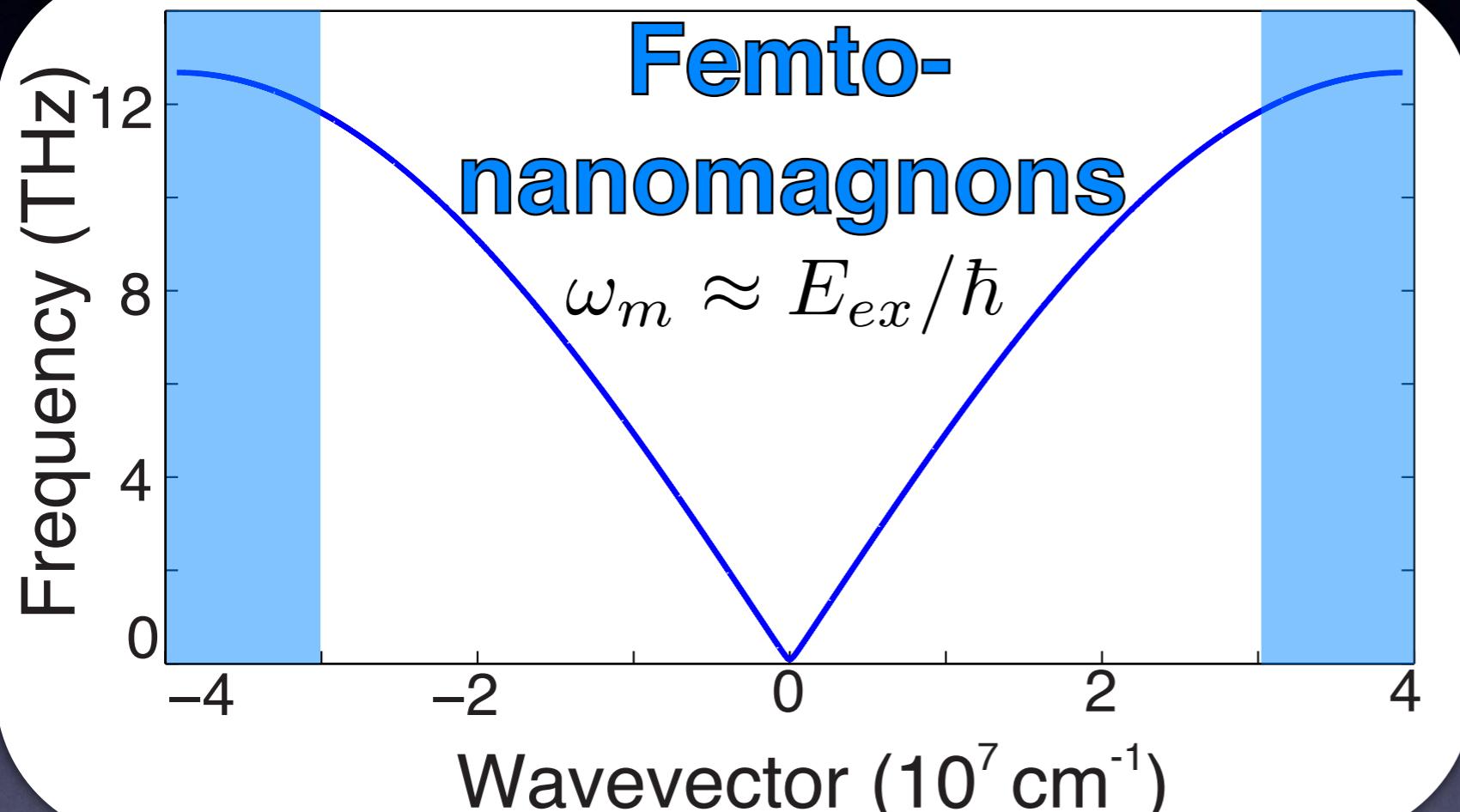
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Femto-nanomagnonics



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Femto-nanomagnonics



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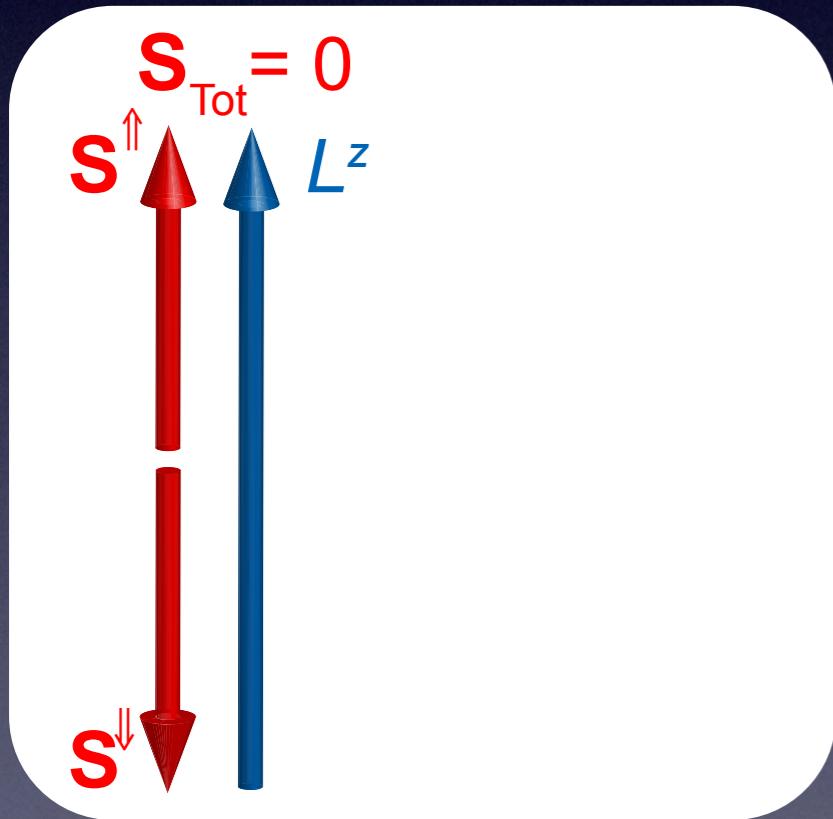
Measure spin dynamics
triggered by femto-nanomagnons

Generation

Problem: high-wavevector magnons are usually unaccessible

Generation

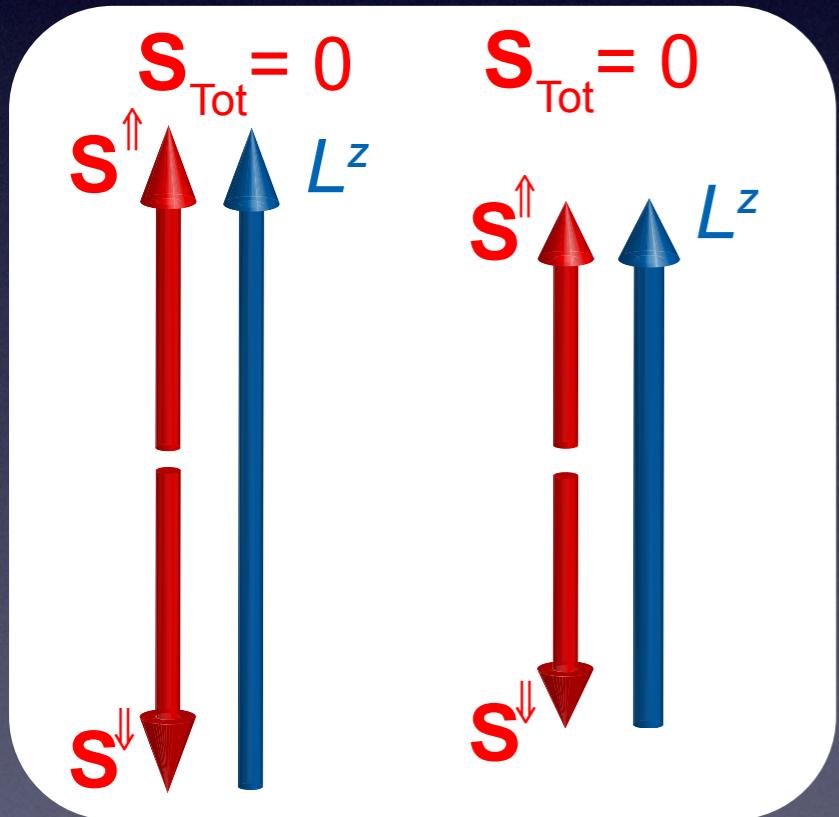
Problem: high-wavevector magnons are usually unaccessible



$$L \equiv S^{\uparrow} - S^{\downarrow}$$

Generation

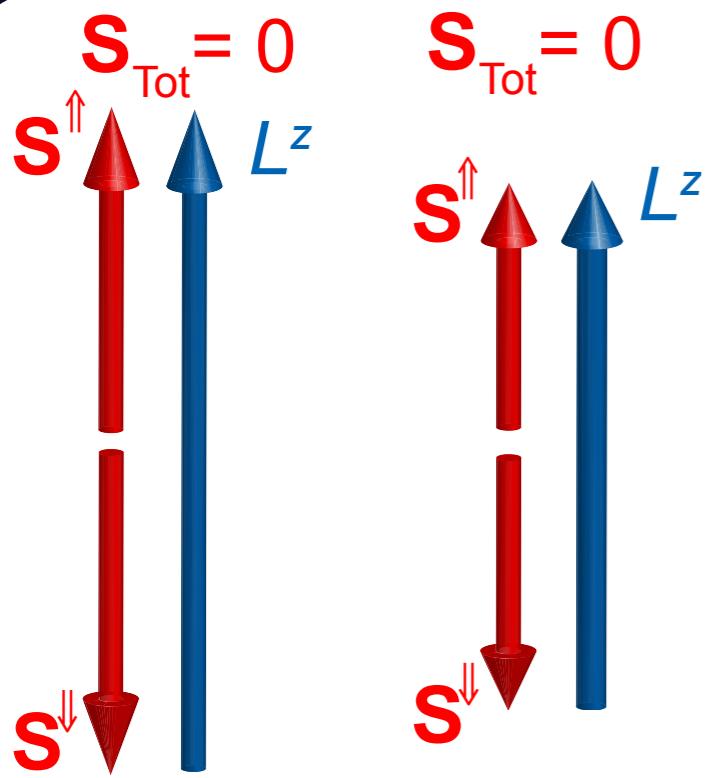
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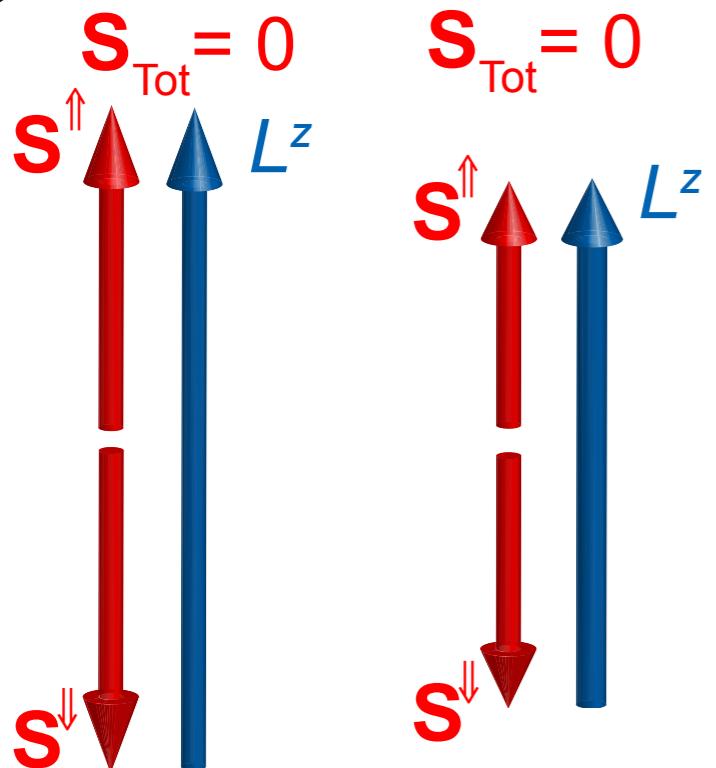


$$L \equiv S^{\uparrow\uparrow} - S^{\downarrow\downarrow}$$

- ✓ Spin and momentum conservation
- ✓ Light-induced bound state of a magnon pair: ***two-magnon mode***
- ✓ High-wavevector region: DOS

Generation

Problem: high-wavevector magnons are usually unaccessible



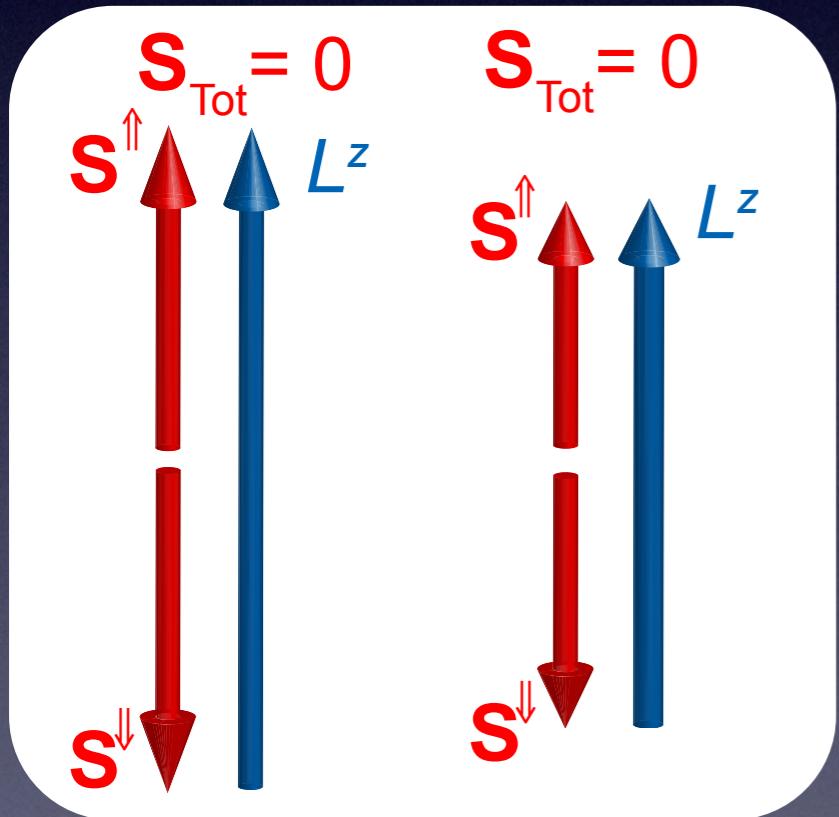
- ✓ Spin and momentum conservation
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- ✓ High-wavevector region: DOS

$$E_{2M} = E_{ex} + \Delta$$

$$L \equiv S^{\uparrow\uparrow} - S^{\downarrow\downarrow}$$

Generation

Problem: high-wavevector magnons are usually unaccessible

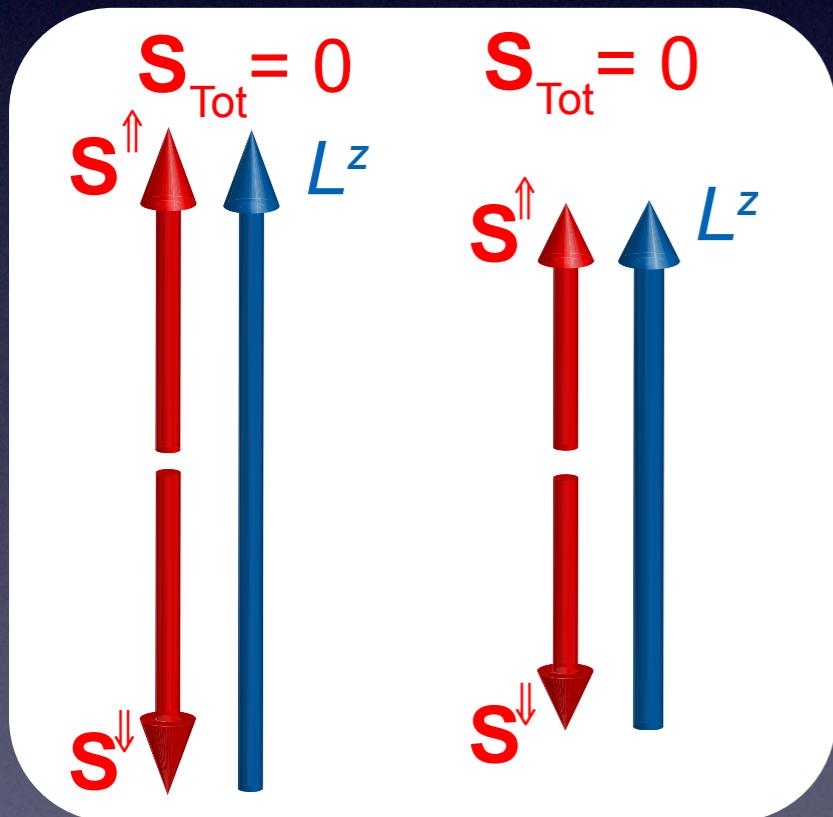


$$E_{2M} = E_{ex} + \Delta$$

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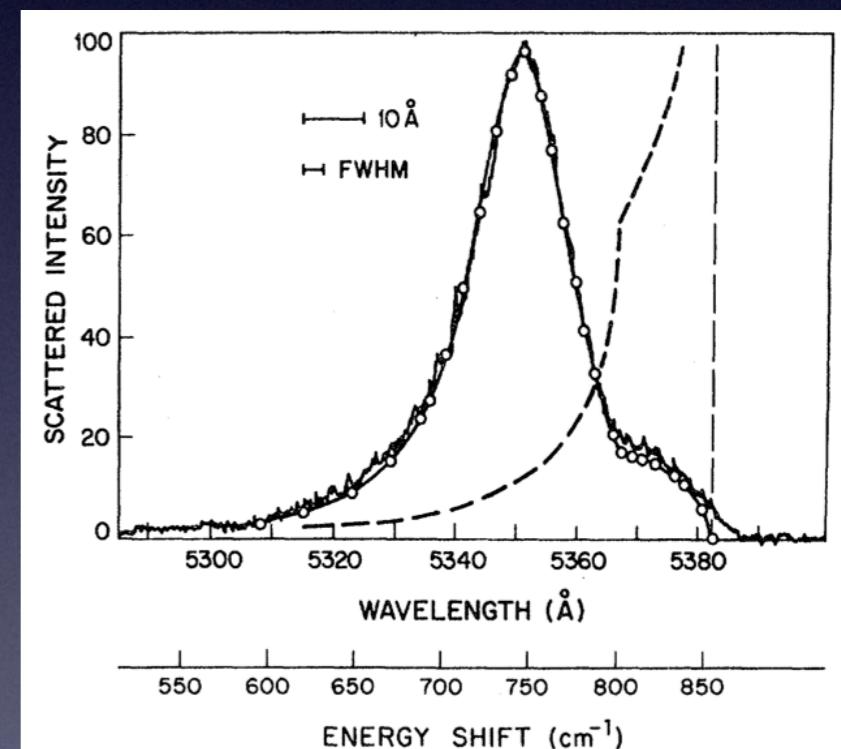
Generation

Problem: high-wavevector magnons are usually unaccessible



$$E_{2M} = E_{ex} + \Delta$$

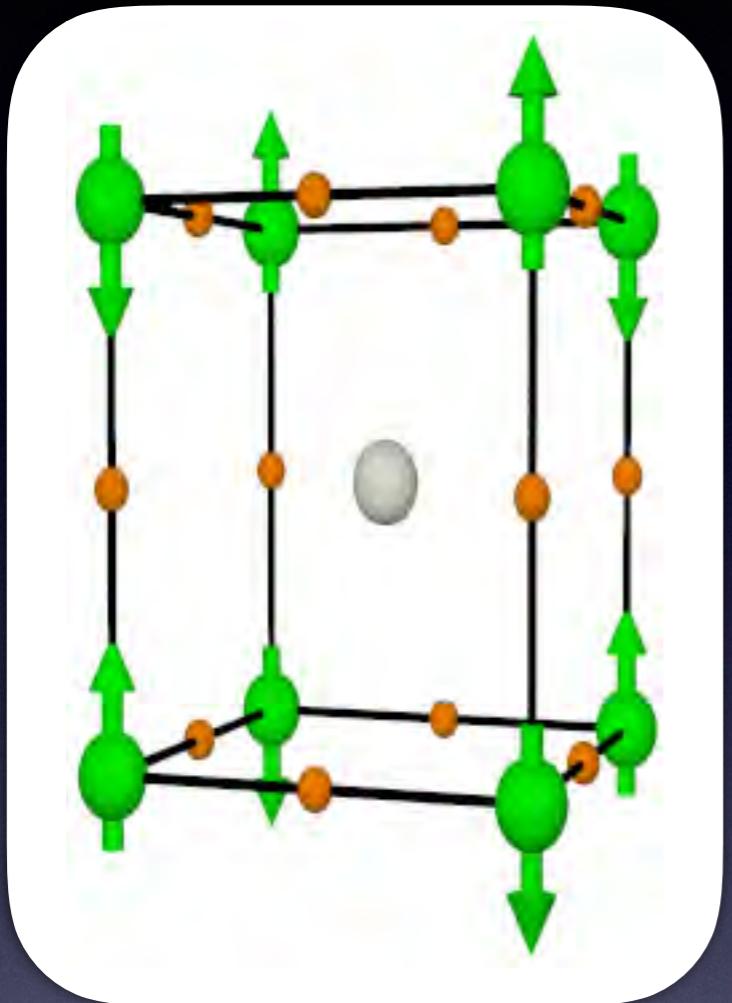
$$L \equiv S^{\uparrow\uparrow} - S^{\downarrow\downarrow}$$



S. Chinn et al. PRB **3**, 1709 (1971)

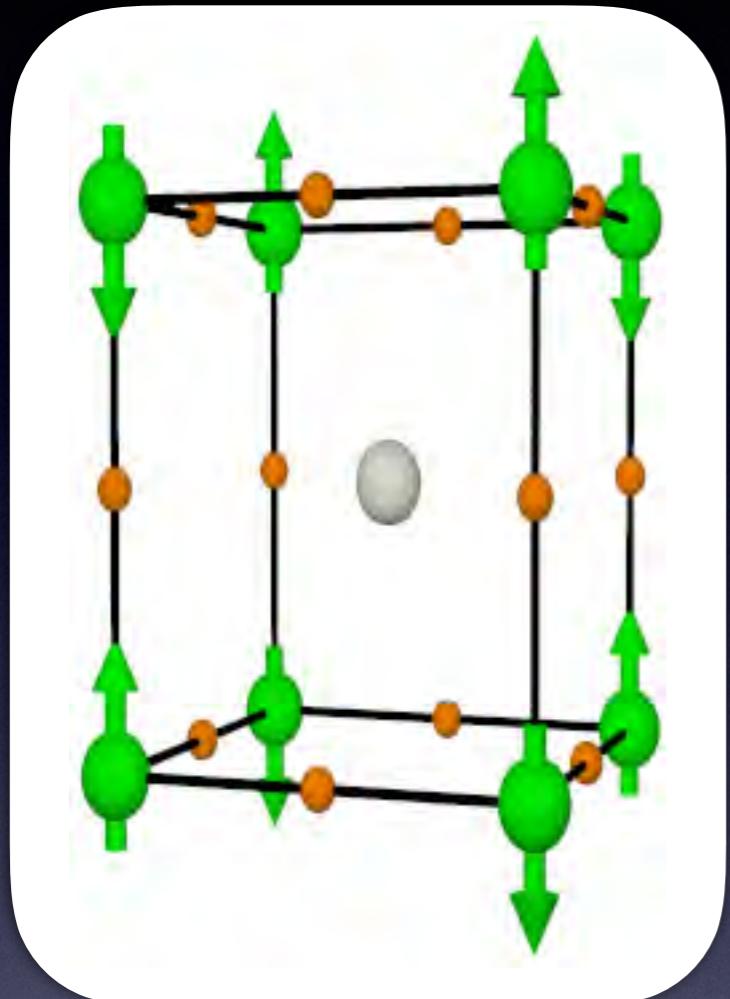
U. Balucani et al. PRB **8**, 4247 (1973)

Sample: KNiF₃

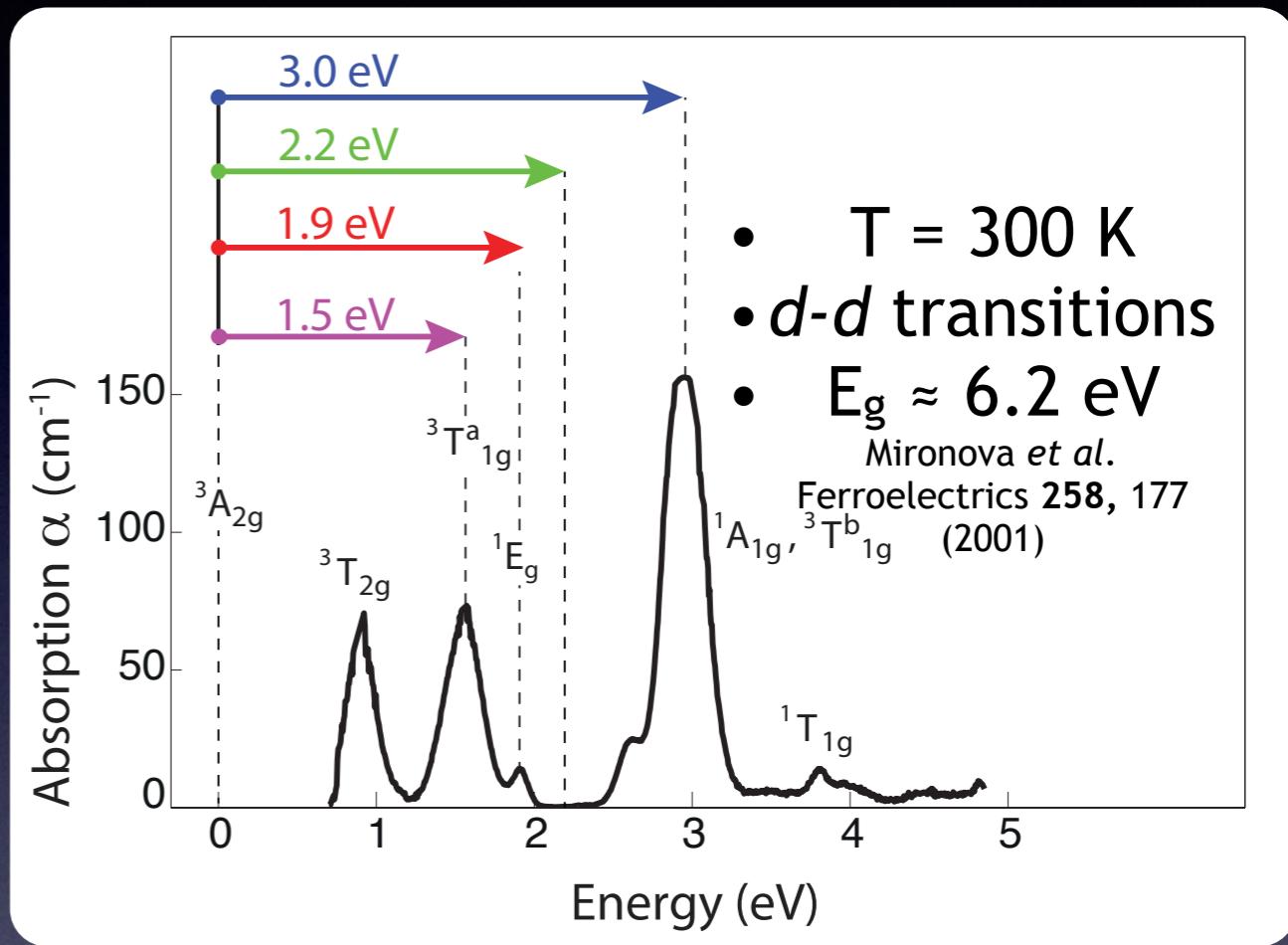


$T_N = 246$ K

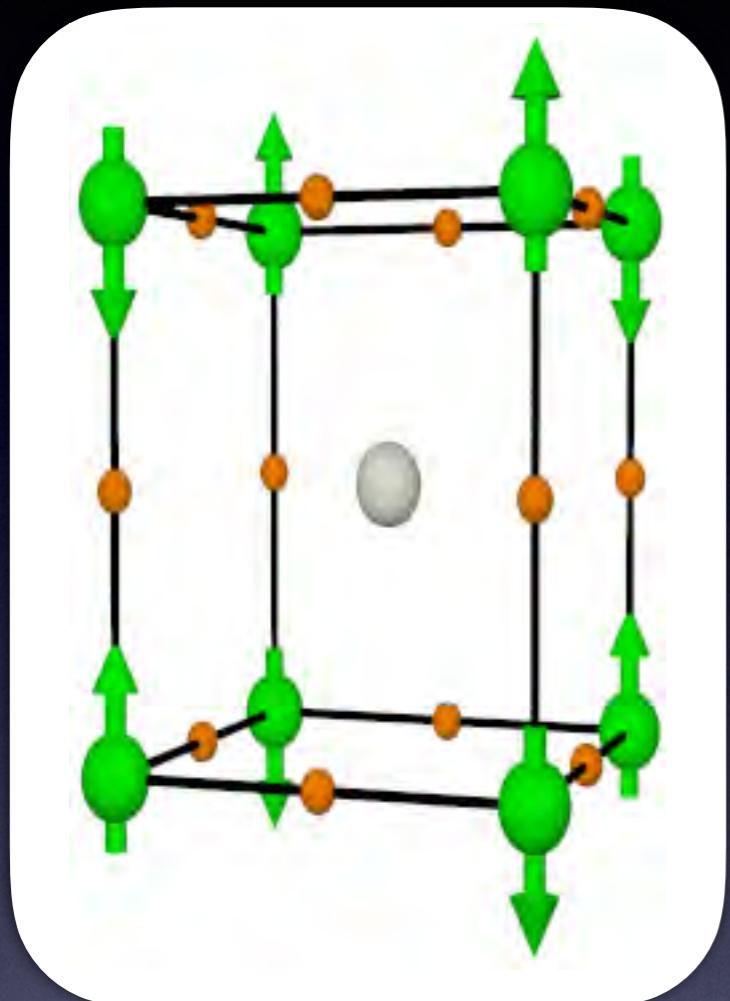
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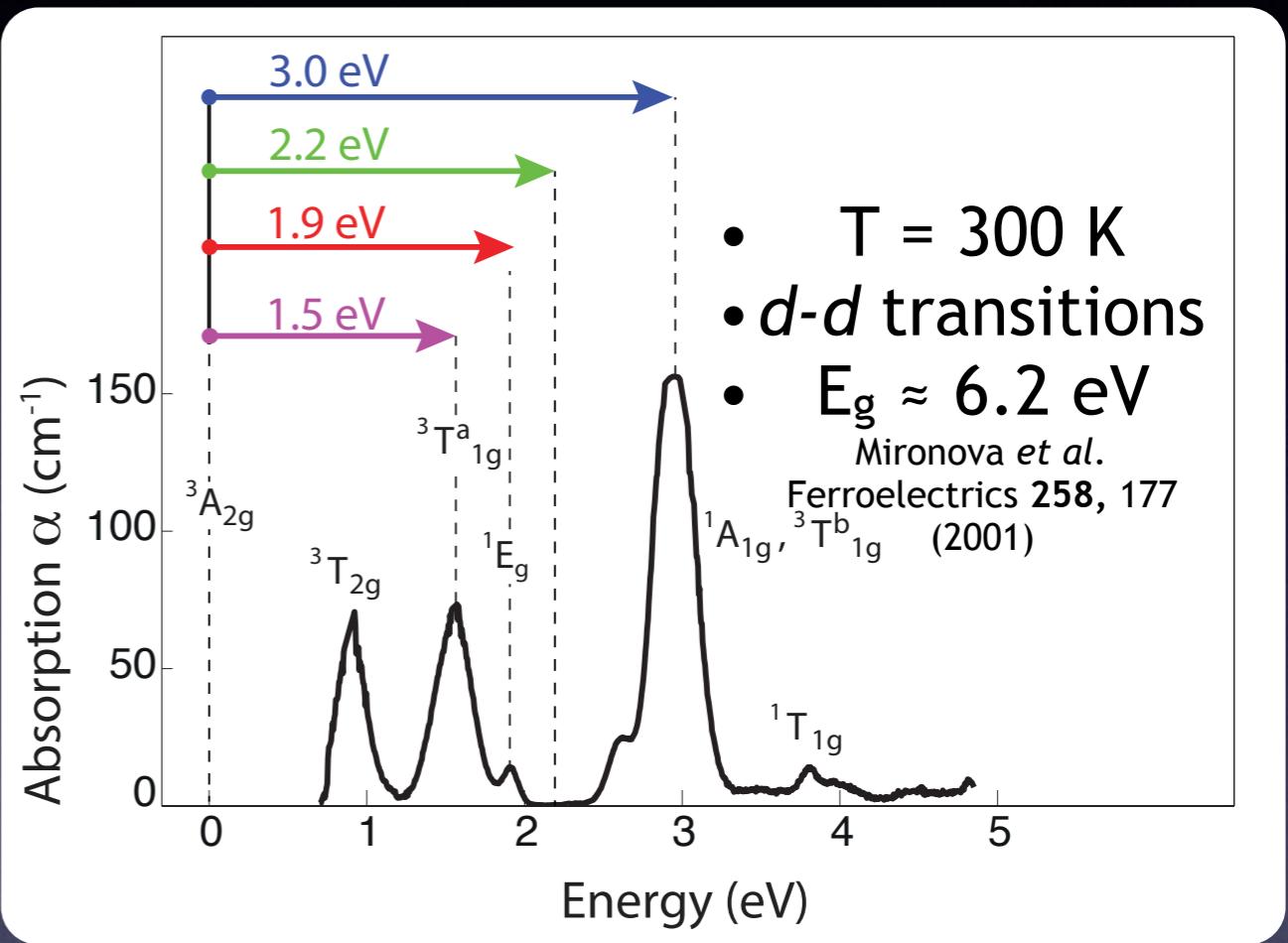
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Sample: KNiF₃



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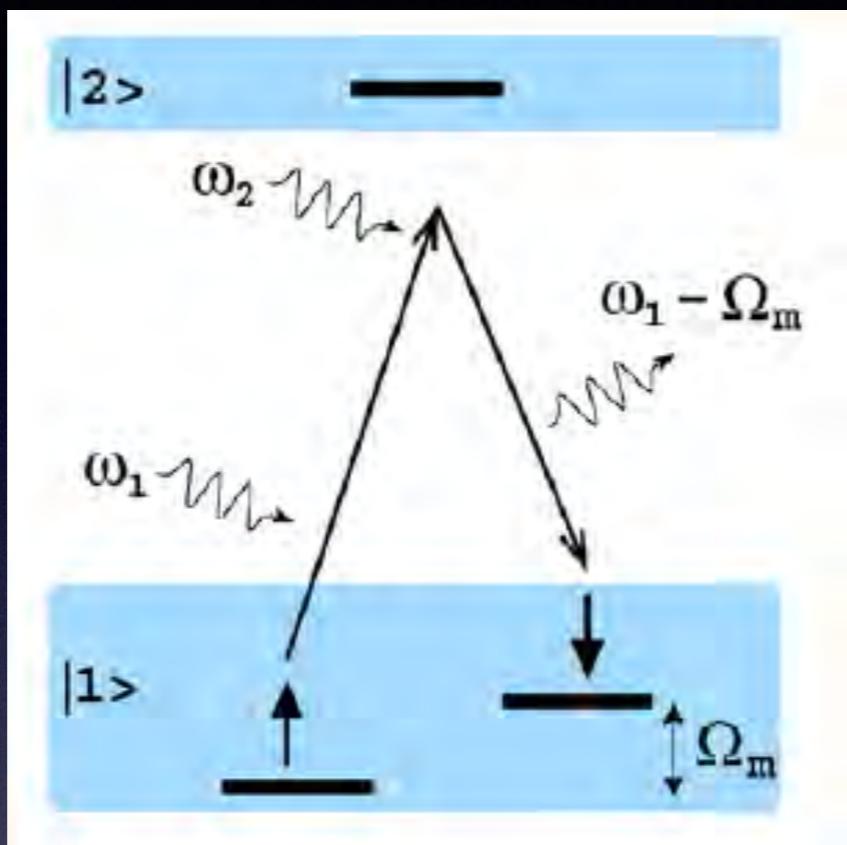


Zero-absorption regime of spin dynamics

D. Bossini et al. PRB (R) 89, 060405 (2014)

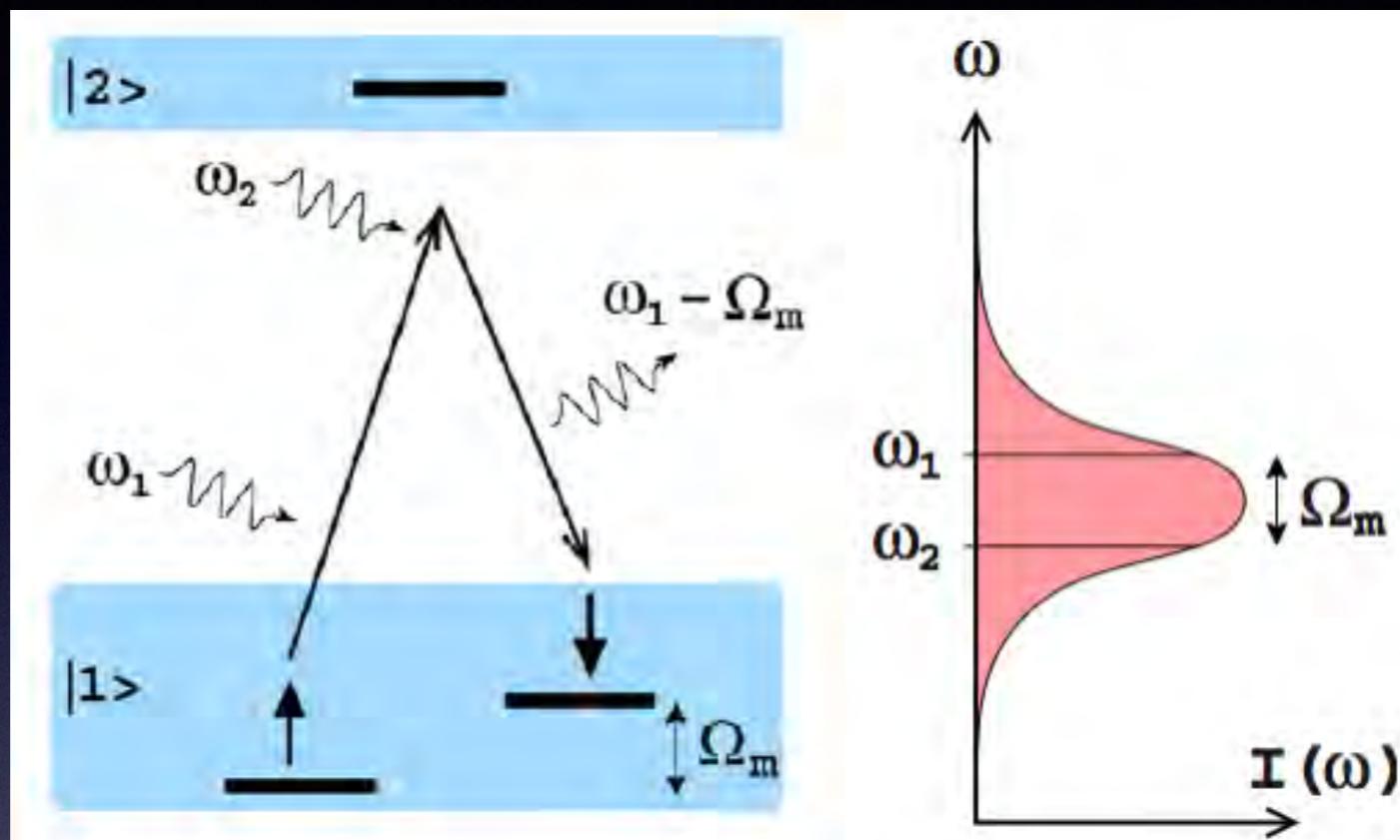
Impulsive Stimulated Raman

ISRS



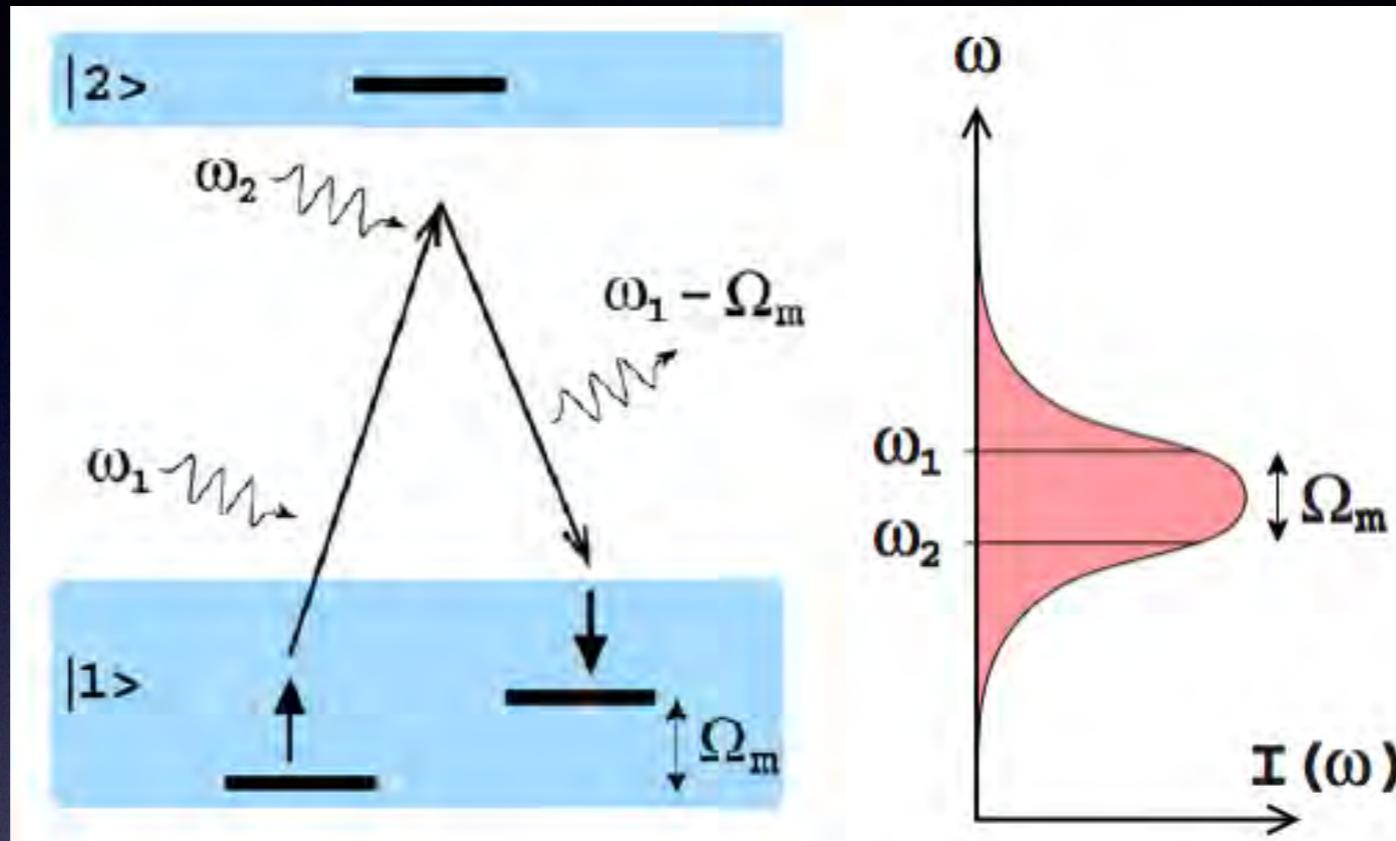
Impulsive Stimulated Raman

ISRS



Impulsive Stimulated Raman

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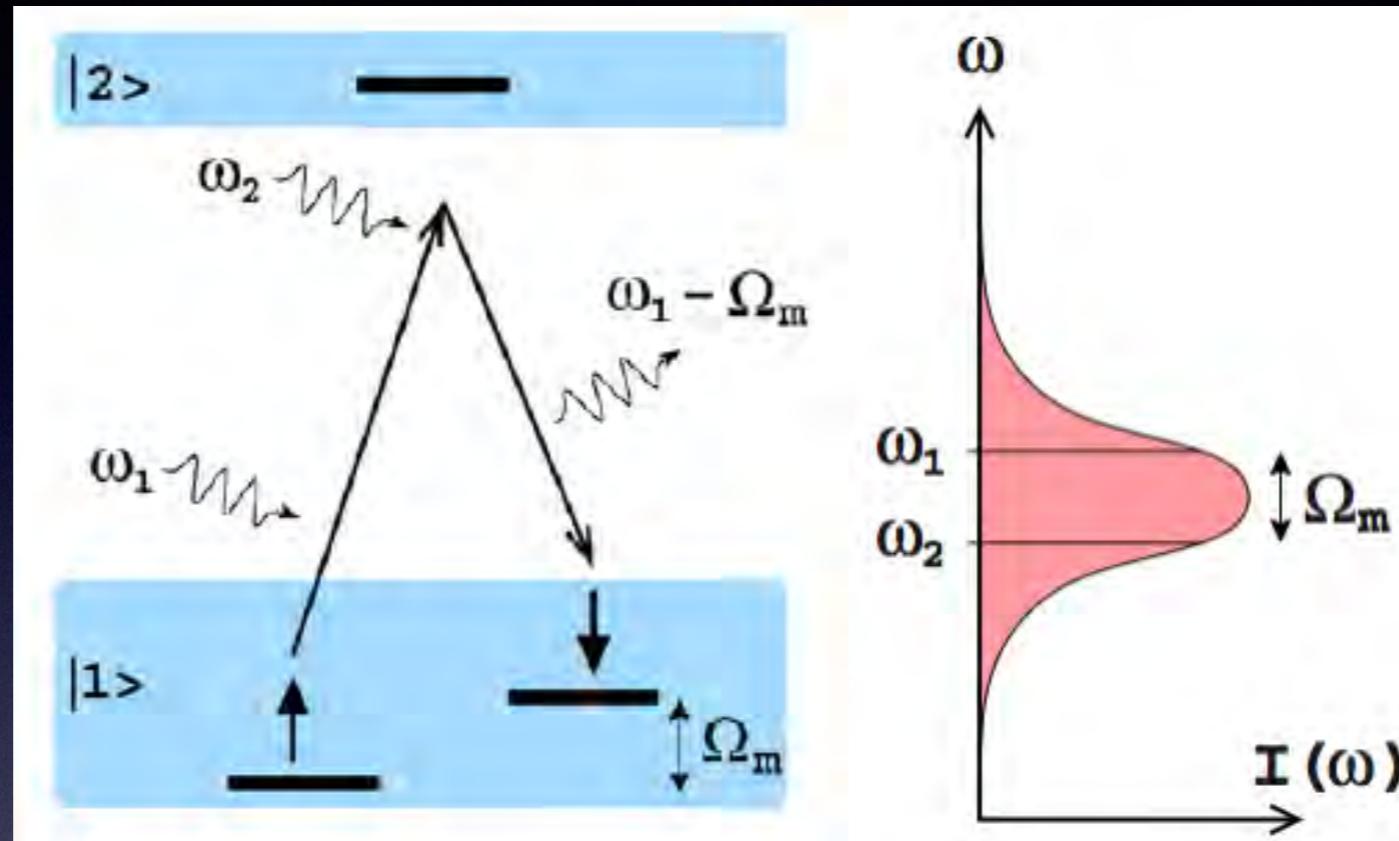


Time domain

Pulses
shorter than
period

Impulsive Stimulated Raman

ISRS



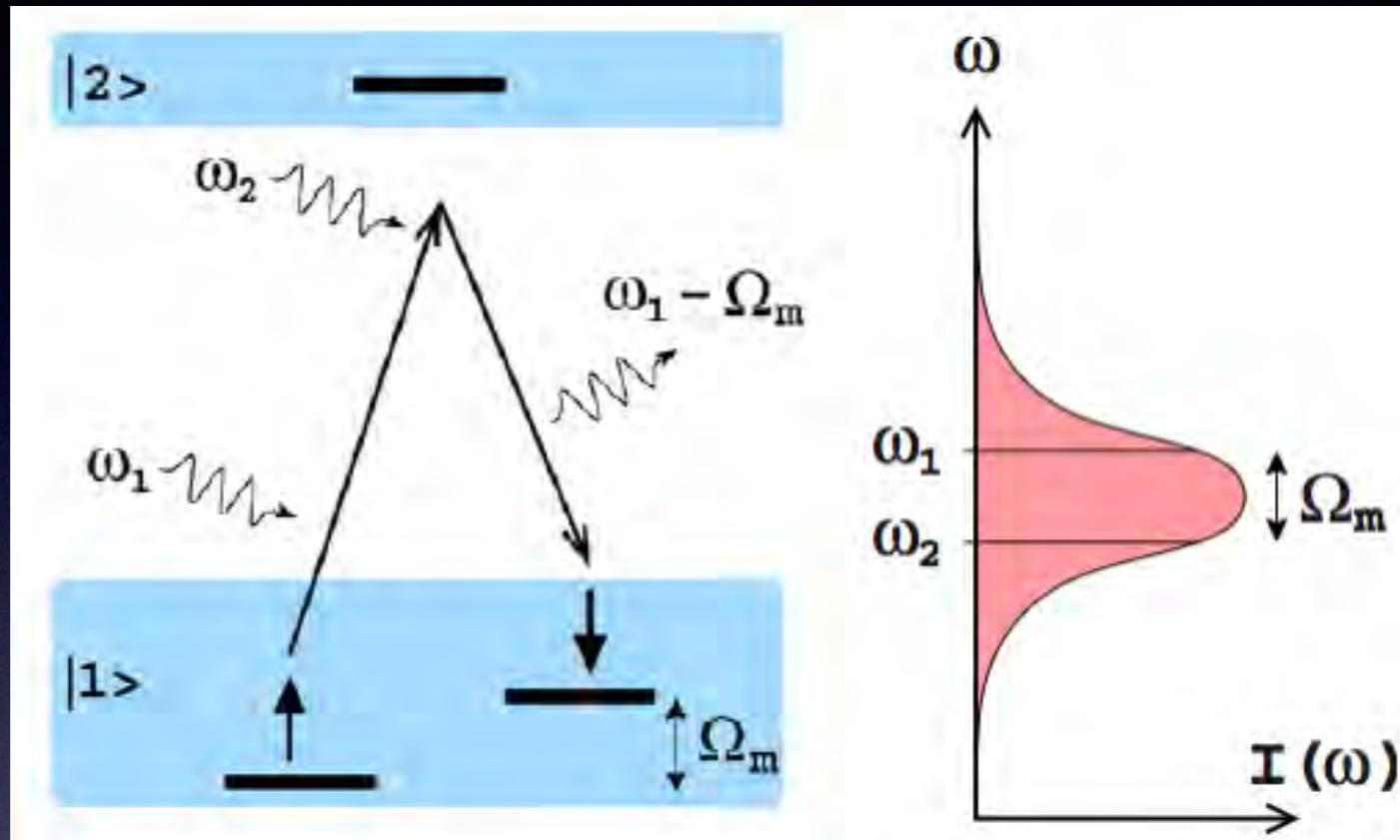
2M period in KNiF₃: 45 fs

Pulses
shorter than
period

Time domain

Impulsive Stimulated Raman

ISRS



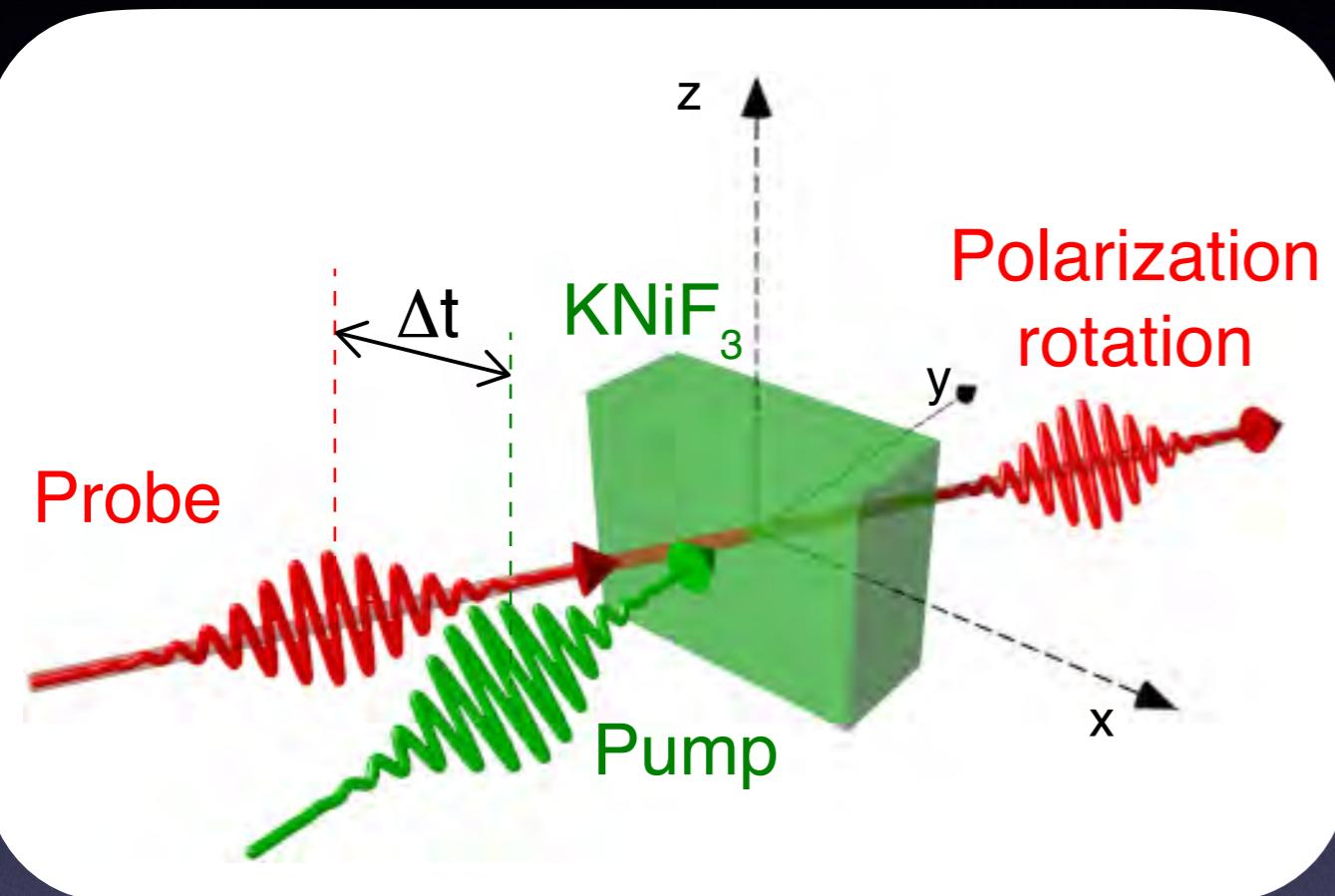
2M period in KNiF_3 : 45 fs

Pulses
shorter than
period

10 fs
laser pulses

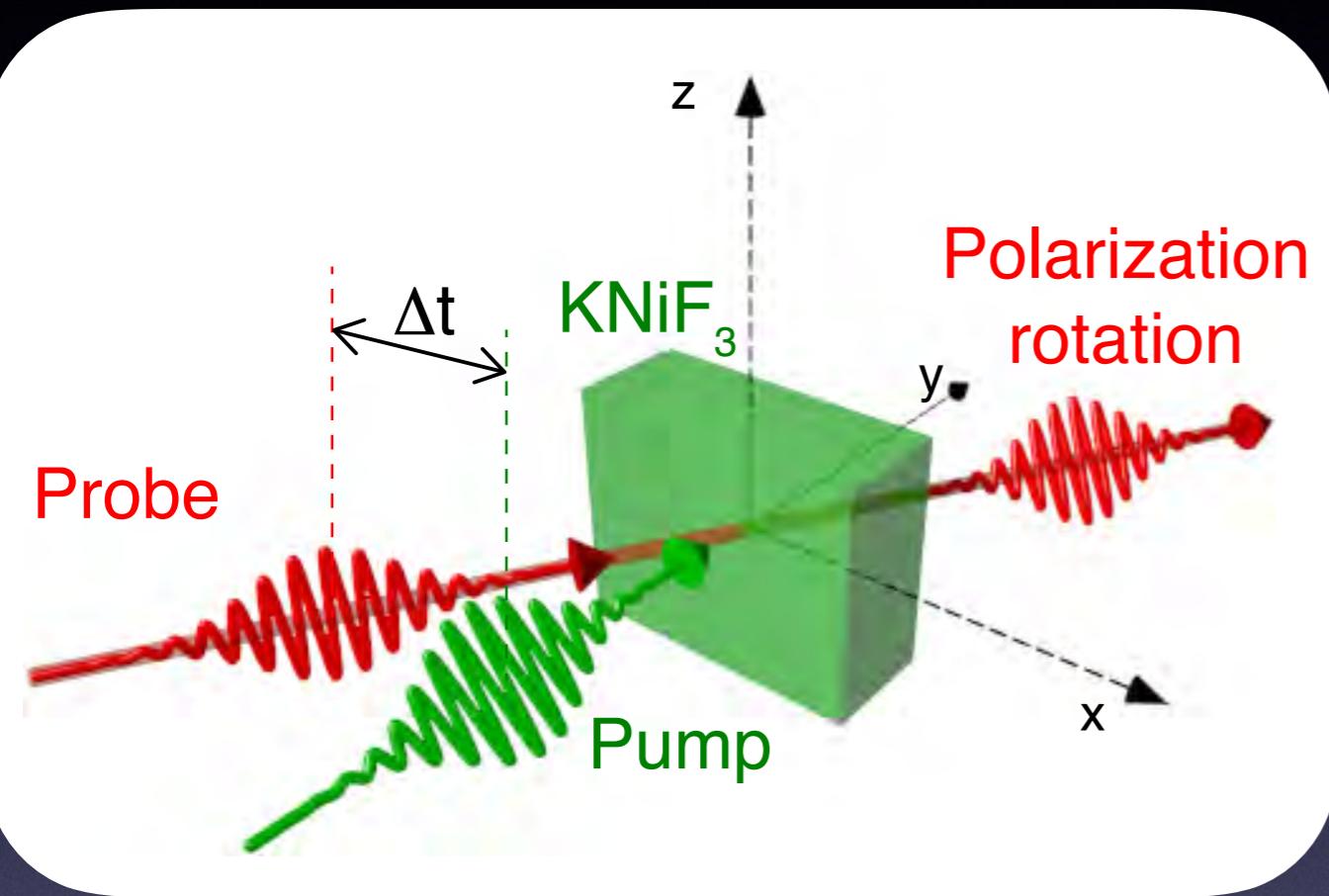
Time domain

Detection



Pump-probe technique
Magneto-optical response
to the photo-excitation
measured as a function of
the delay

Detection



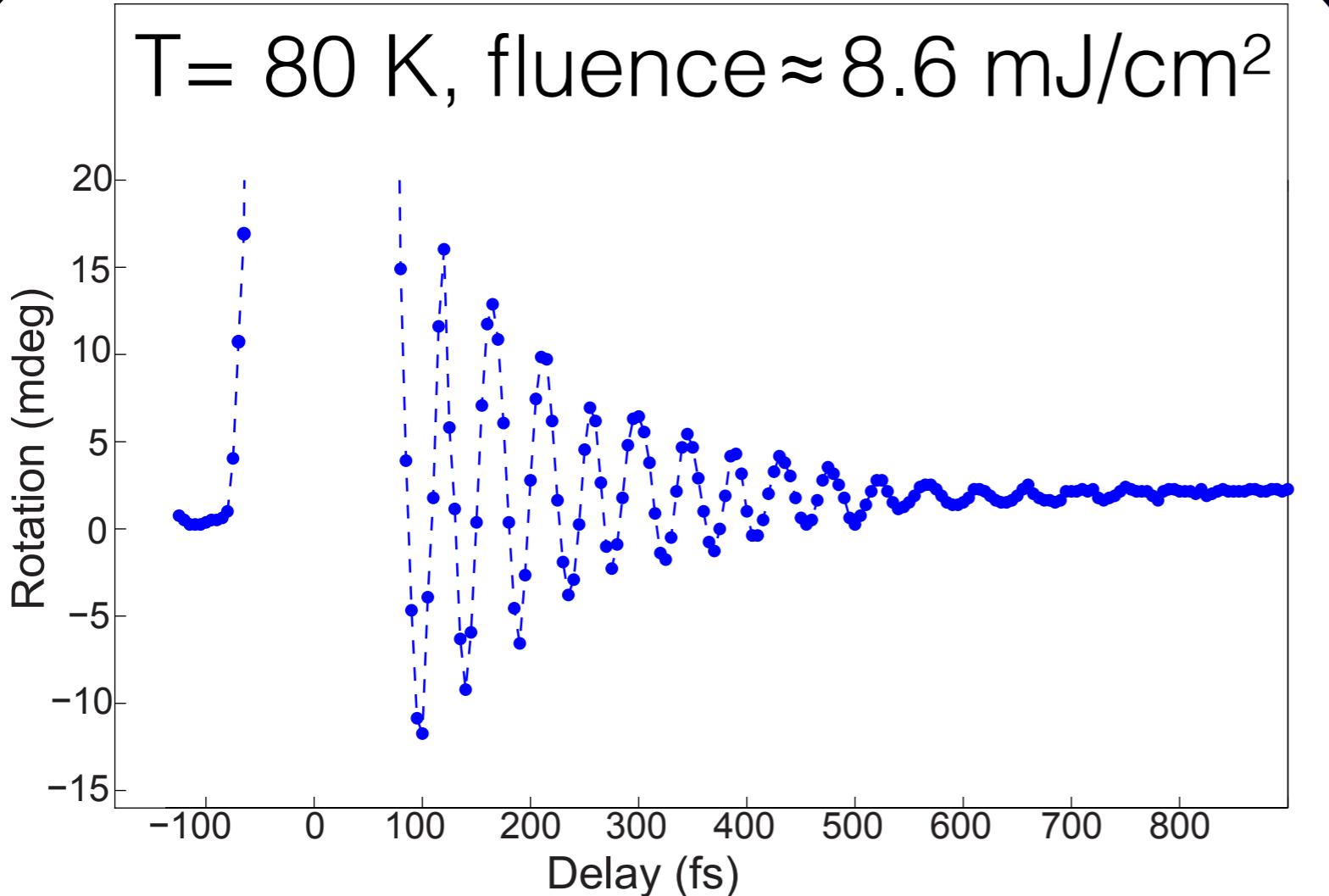
All-optical detection
via a **second-order**
magneto-optical effect

Pump-probe technique
Magneto-optical response
to the photo-excitation
measured as a function of
the delay

$$\epsilon_s^{\lambda\nu} = \sum_{ij} \sum_{\gamma\delta} \rho^{\lambda\nu\gamma\delta} \langle \hat{S}_i^{\gamma\uparrow} \hat{S}_j^{\delta\downarrow} \rangle$$

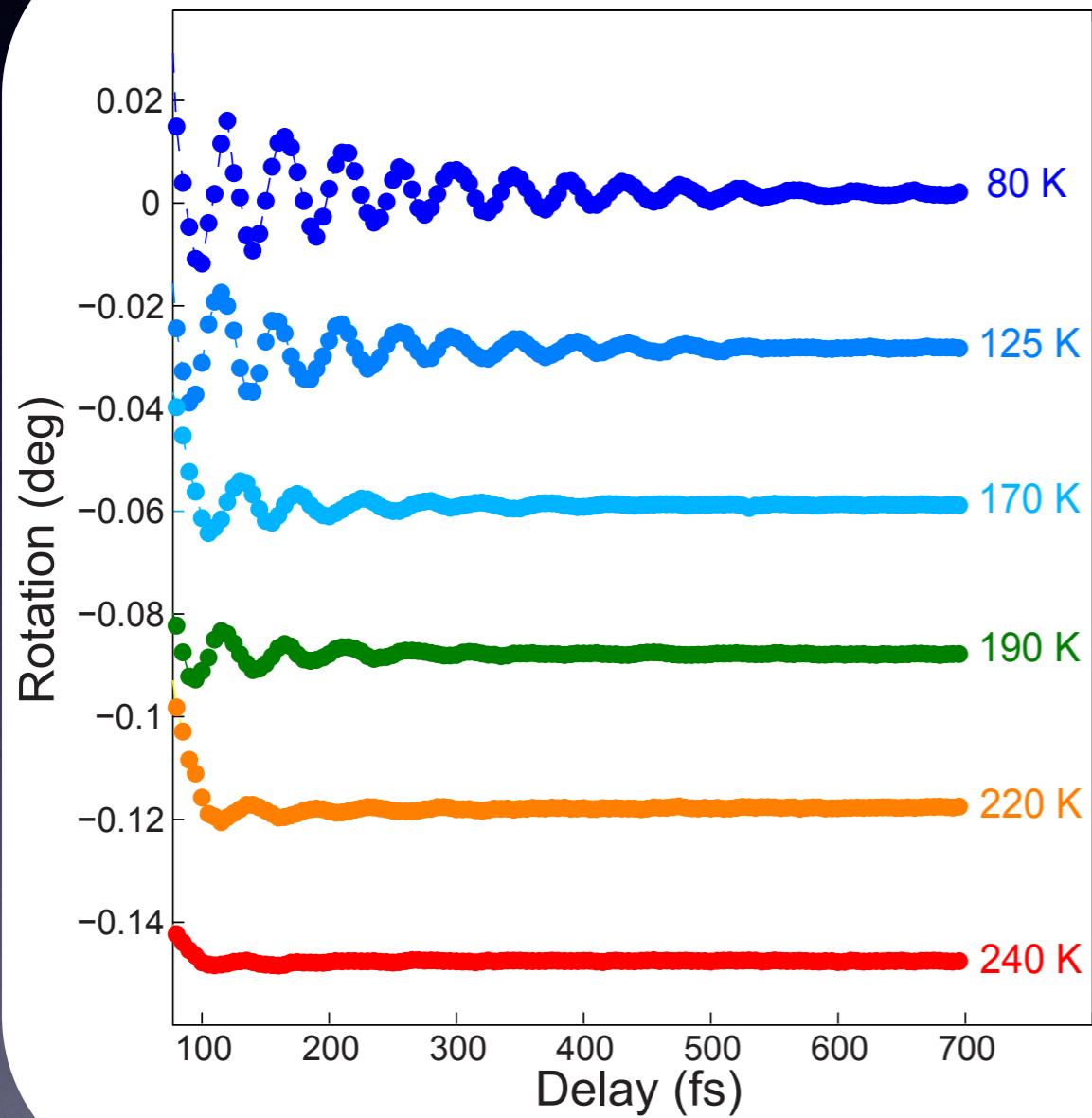
J. Ferrè *et al.* Rep. Prg. Phys 47, 513 (1984)

Laser-induced dynamics

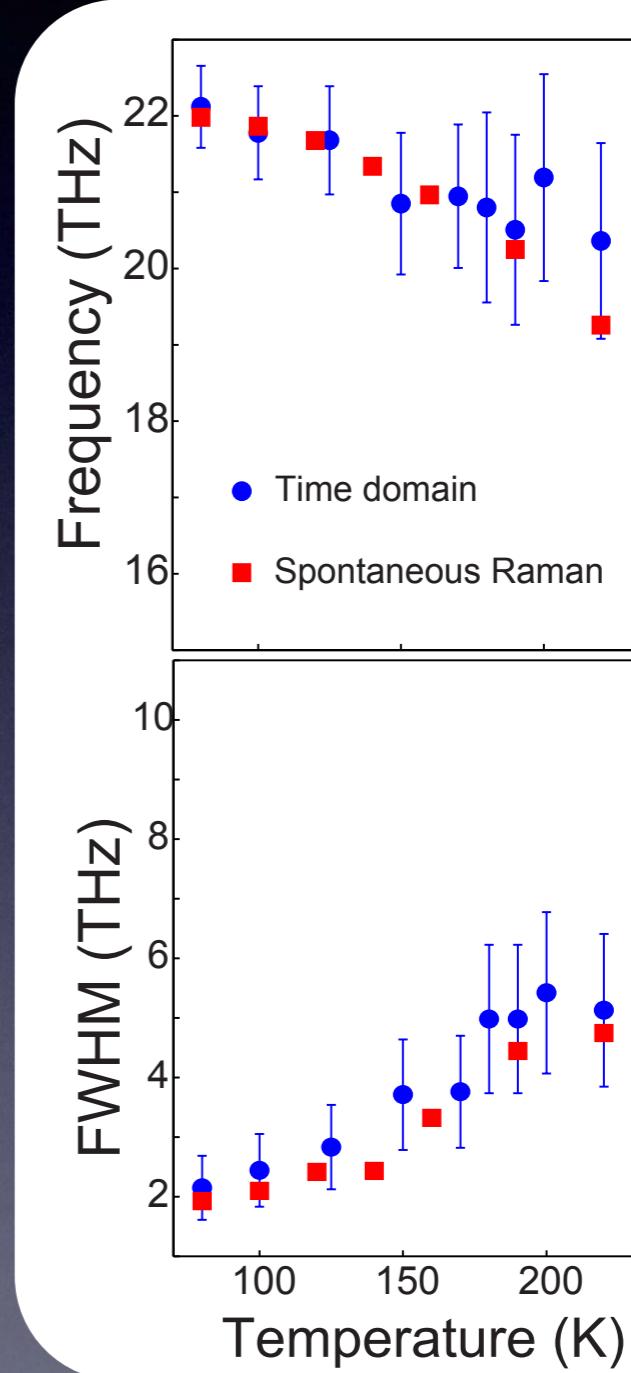
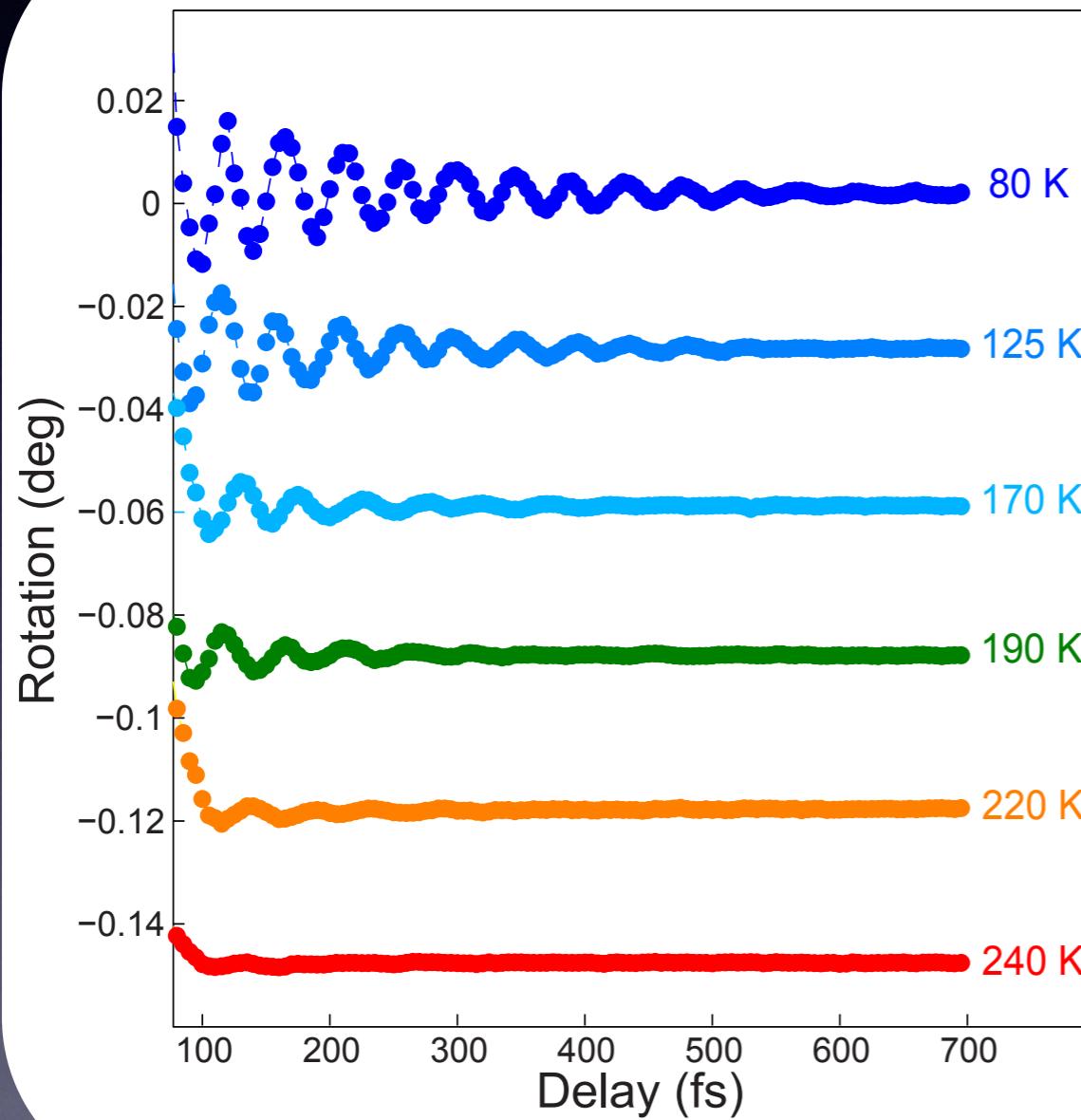


- ✓ Pump and probe linearly and orthogonally polarized
- ✓ Oscillations @ 22 THz ($T=45 \text{ fs}$)
- ✓ Lifetime $\approx 500 \text{ fs}$

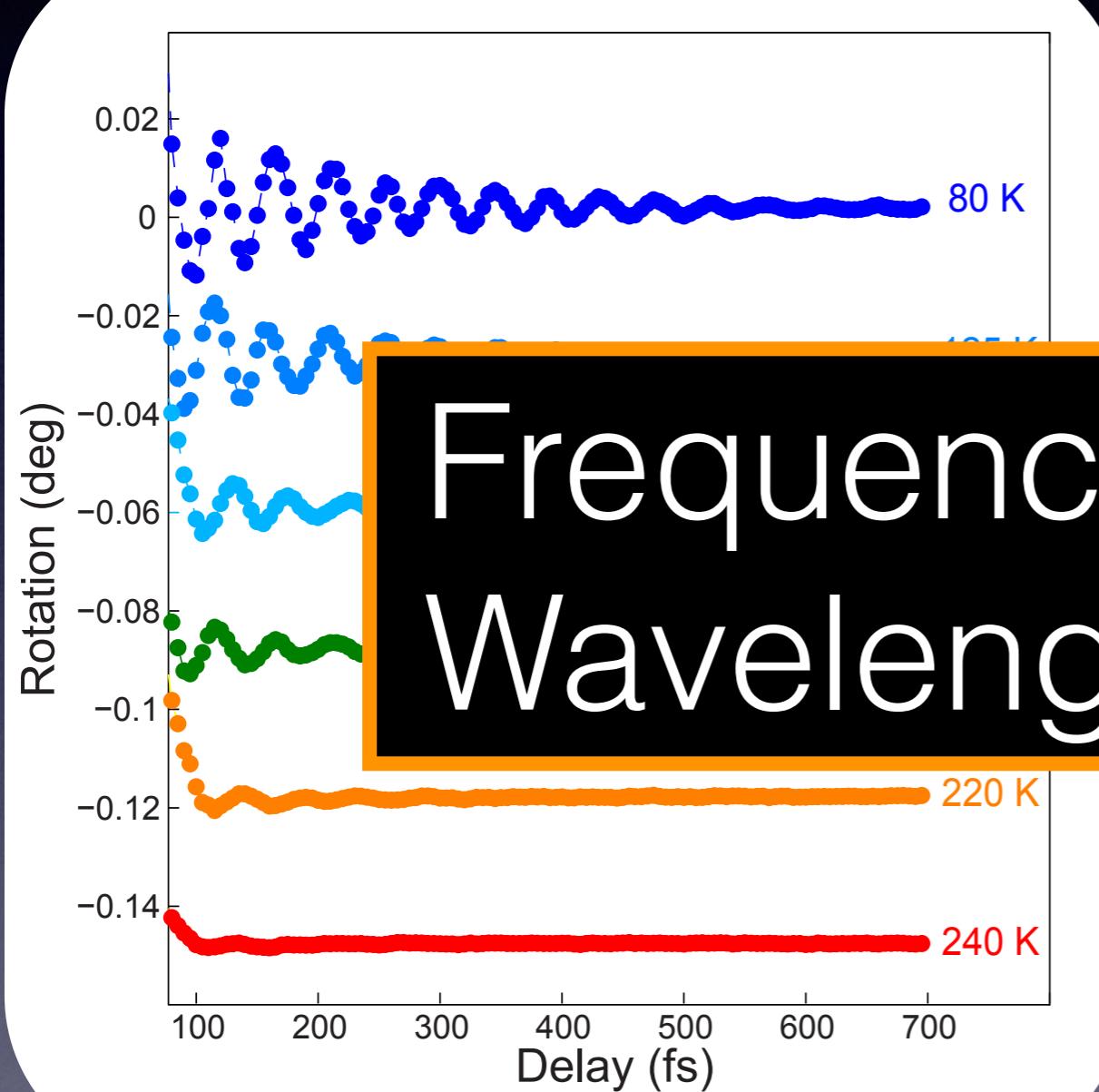
Temperature dependence



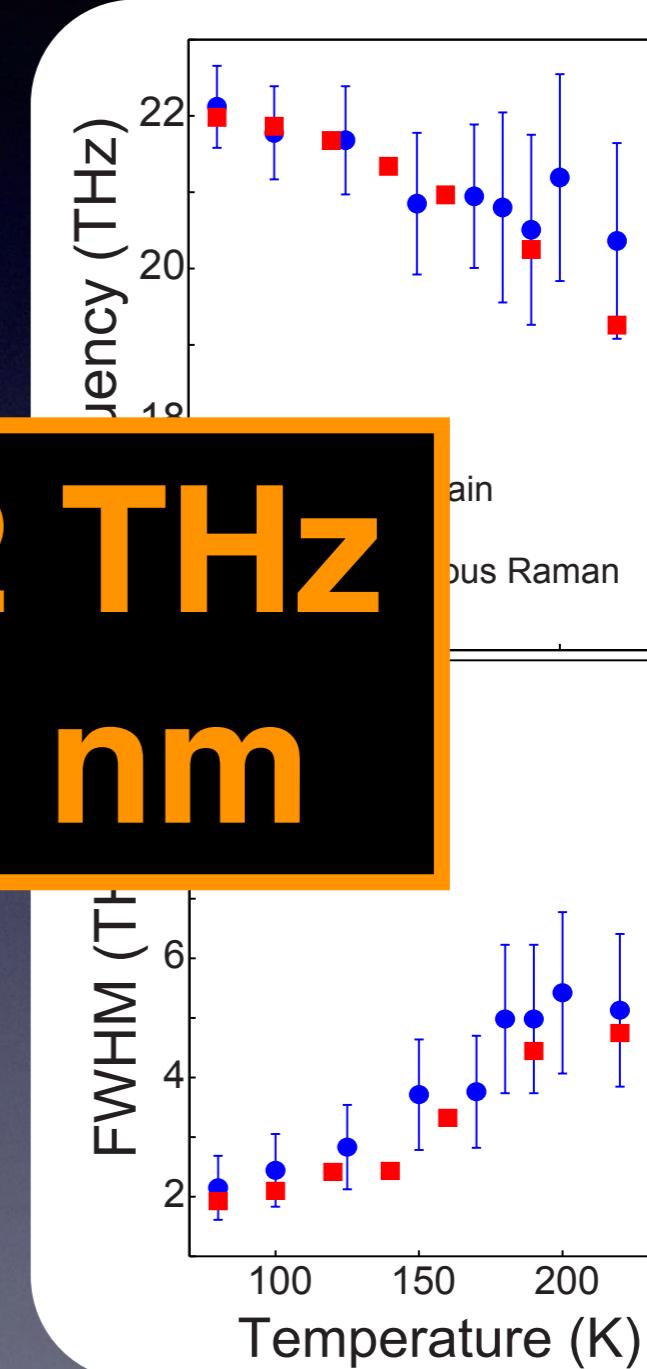
Temperature dependence



Temperature dependence



Frequency: **22 THz**
Wavelength: **1 nm**



Macrospin dynamics

$$\langle \hat{S}_i^{z\uparrow} \hat{S}_j^{z\downarrow} \rangle \quad L^z(t)$$

Macrospin dynamics

$$\langle \hat{S}_i^{z\uparrow} \hat{S}_j^{z\downarrow} \rangle$$

$$L^z(t)$$

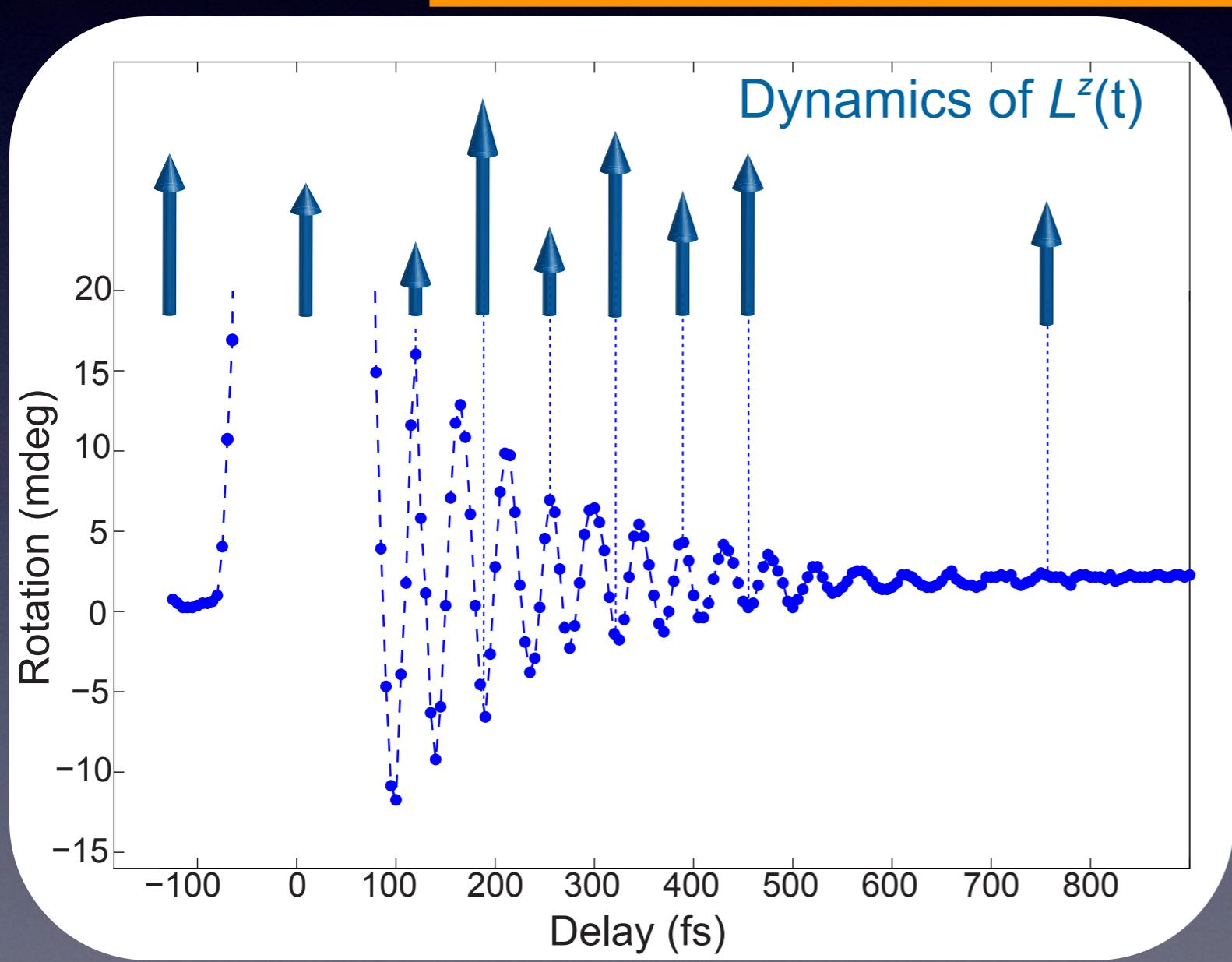
Same time-dependence

Macrospin dynamics

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Same time-dependence



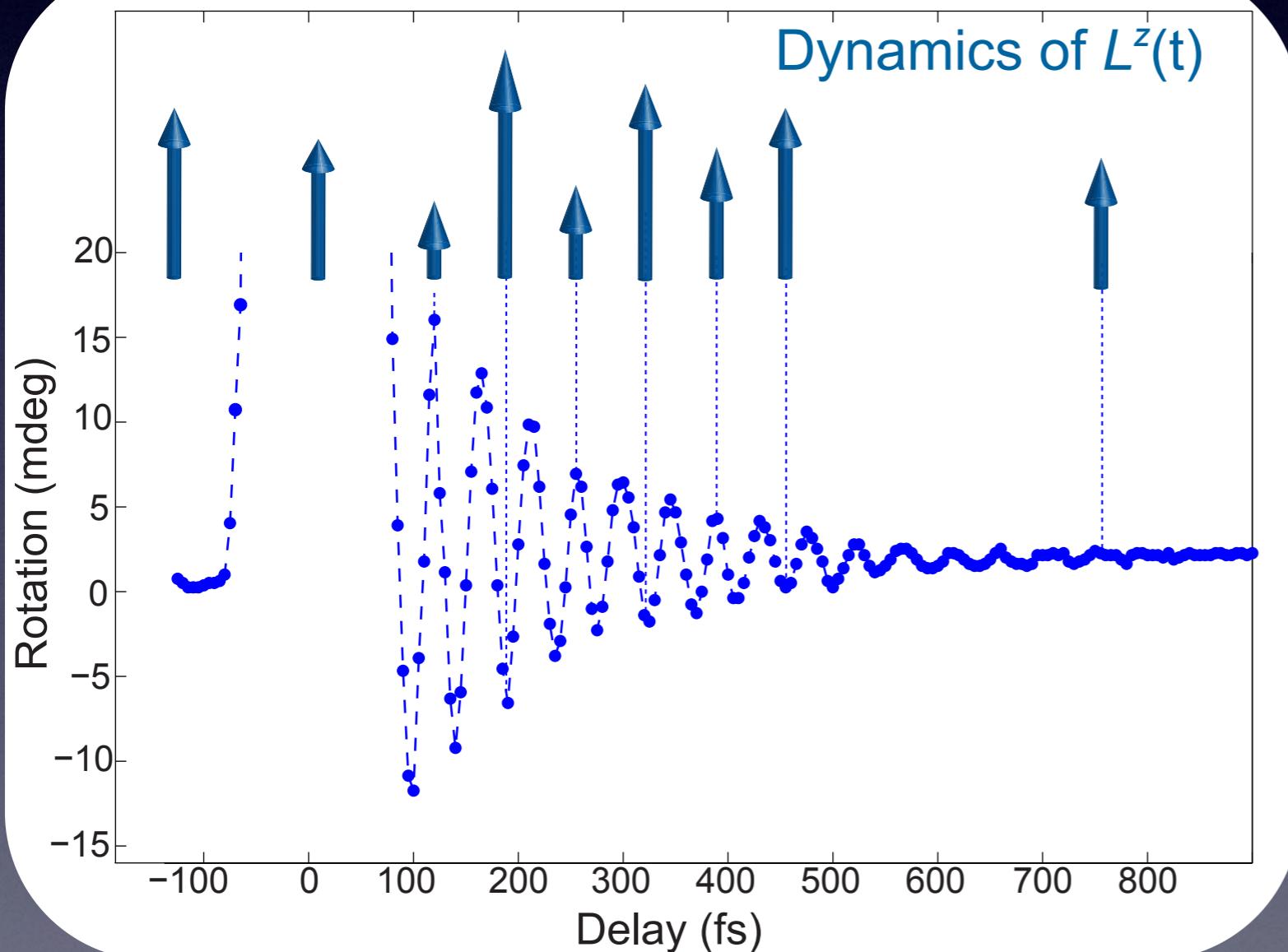
Macrospin dynamics

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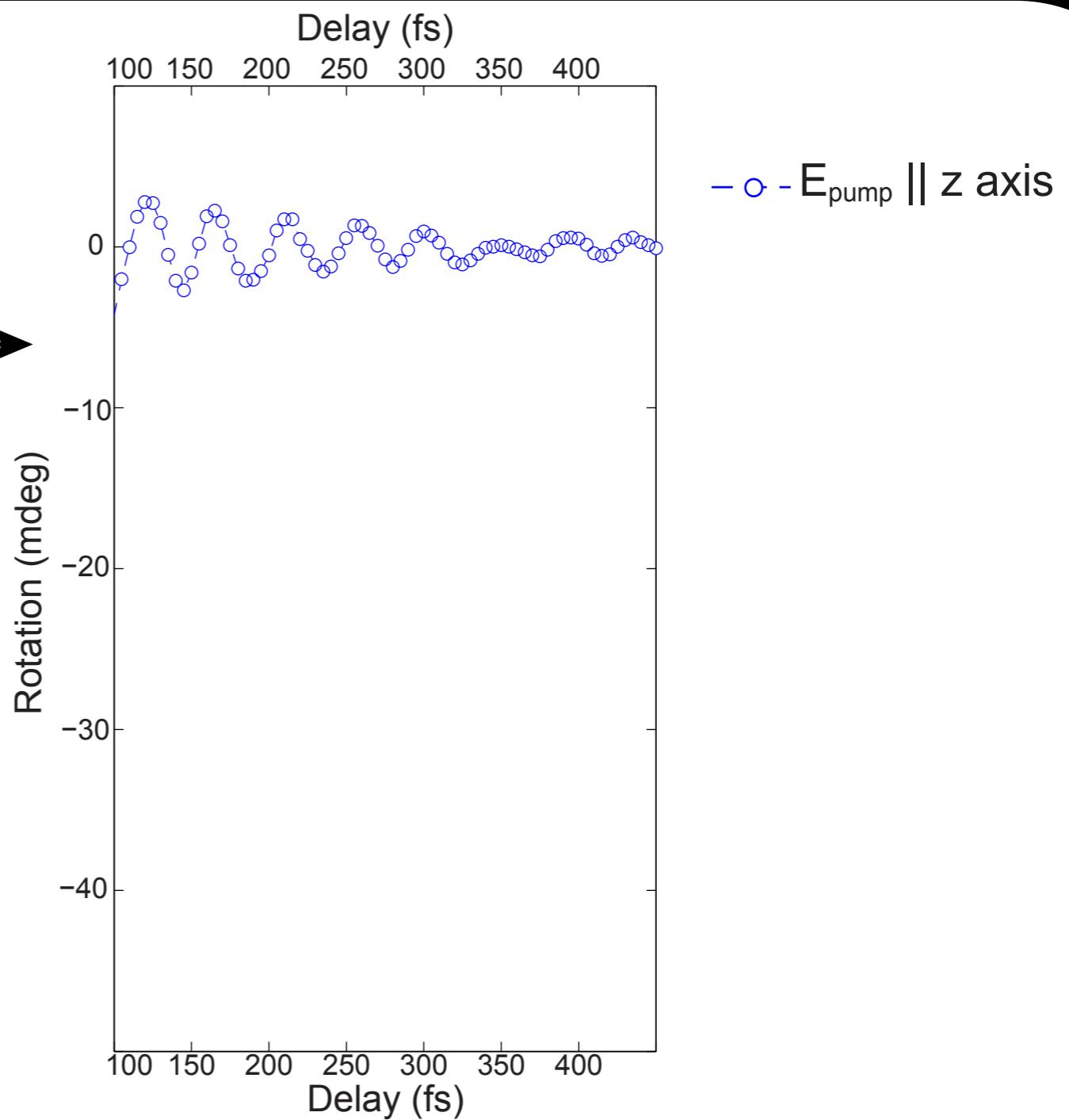
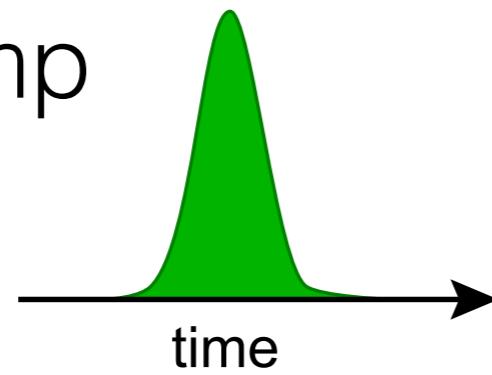
Same time-dependence

Macroscopic probe of the **femtosecond dynamics of nanometer spin correlations**



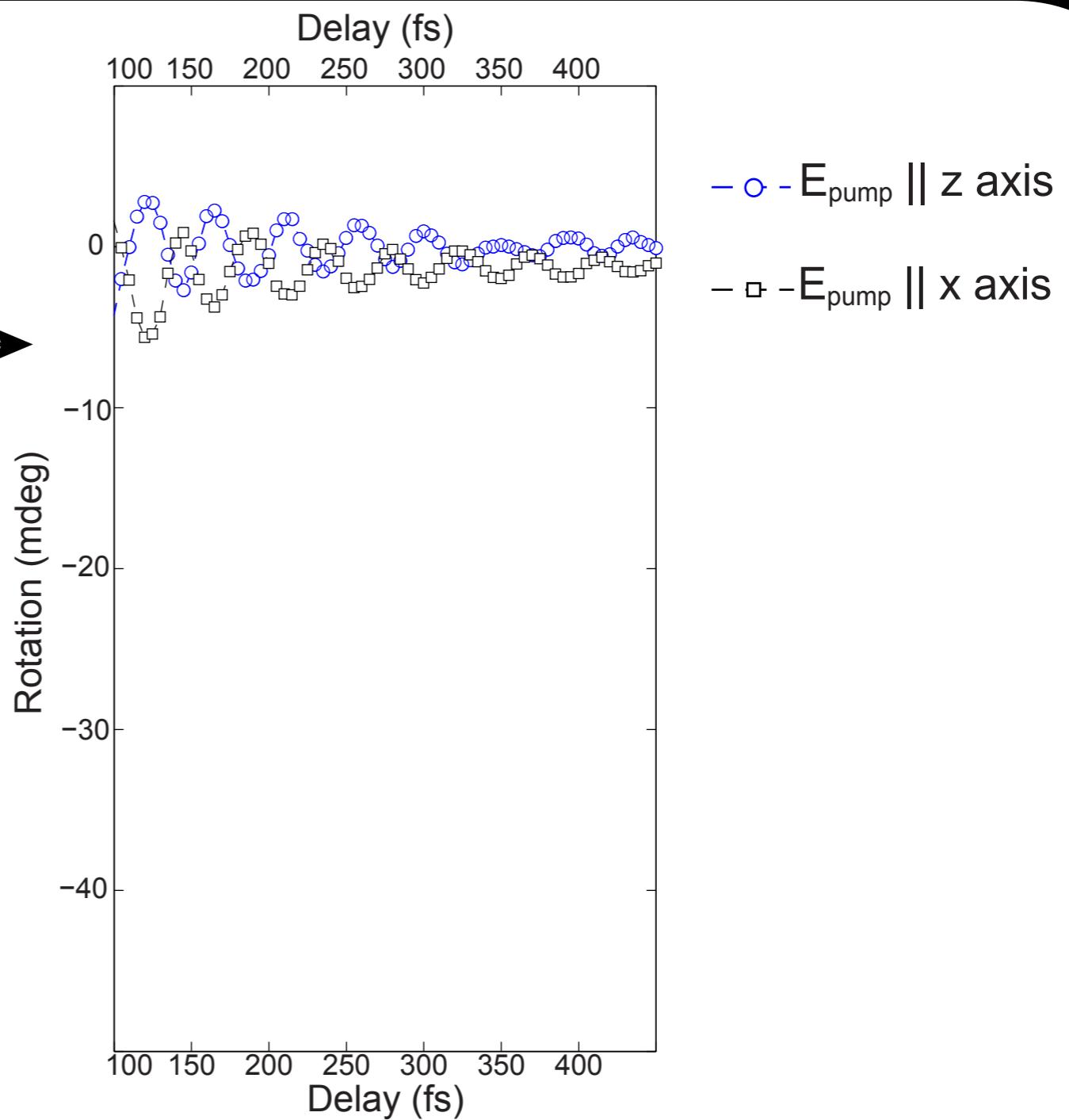
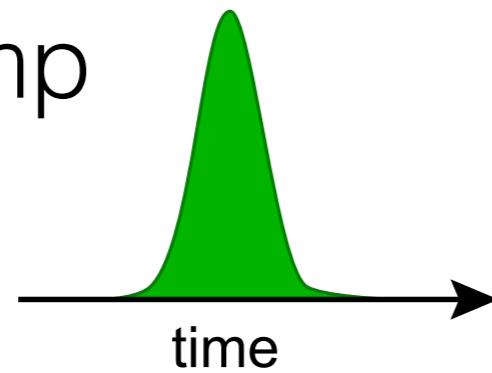
Control the dynamics

One pump
pulse



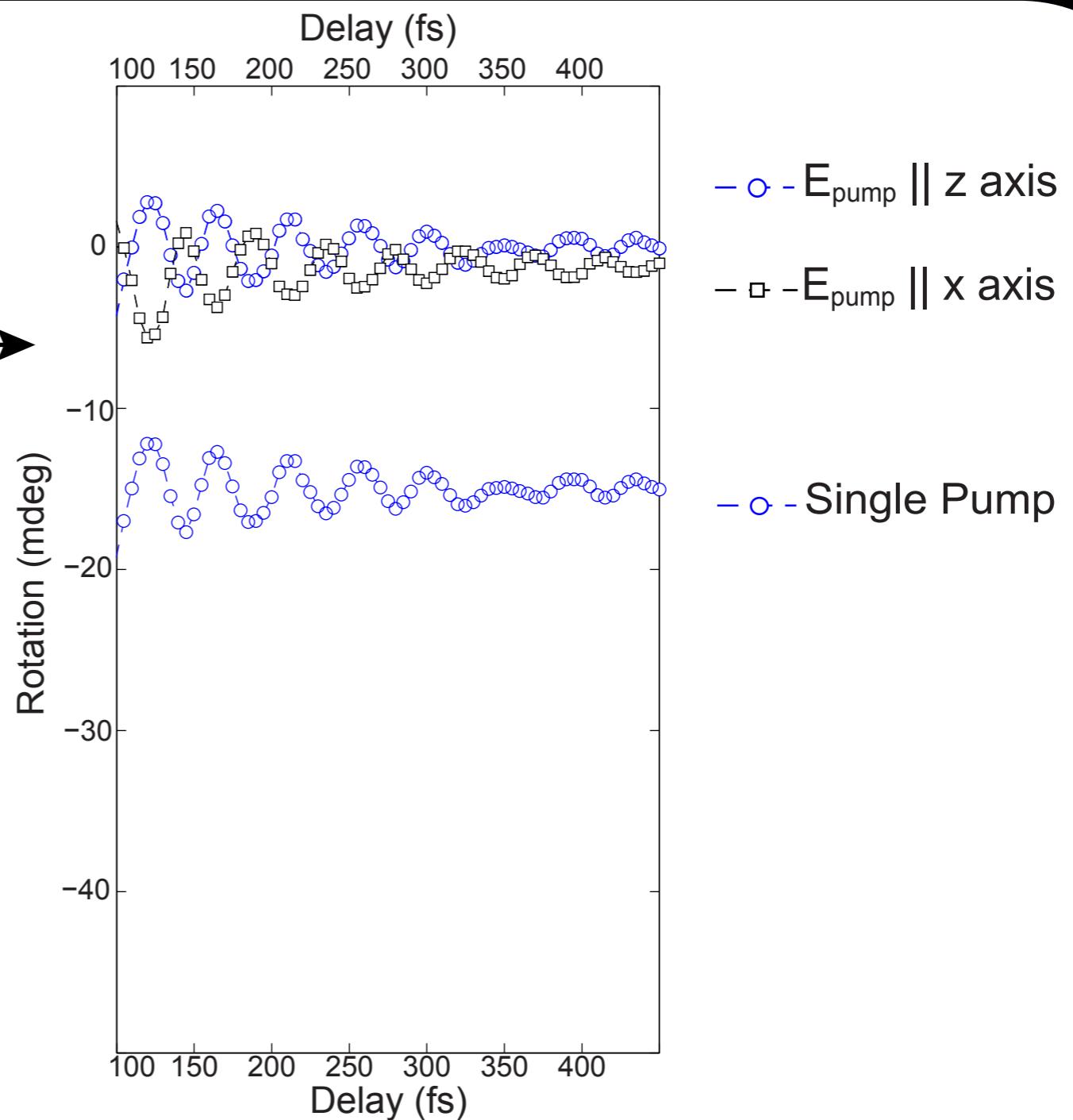
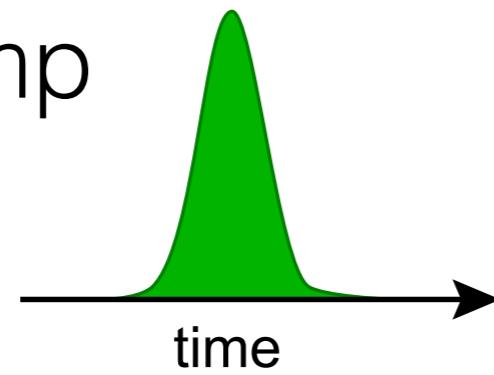
Control the dynamics

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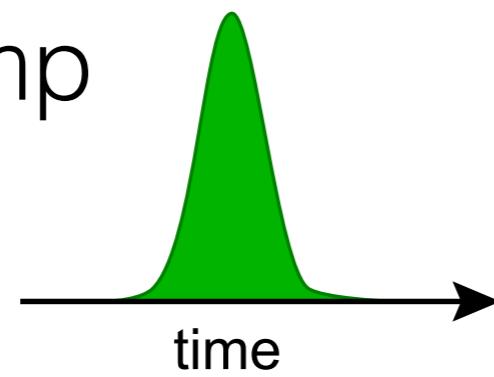
Control the dynamics

One pump
pulse

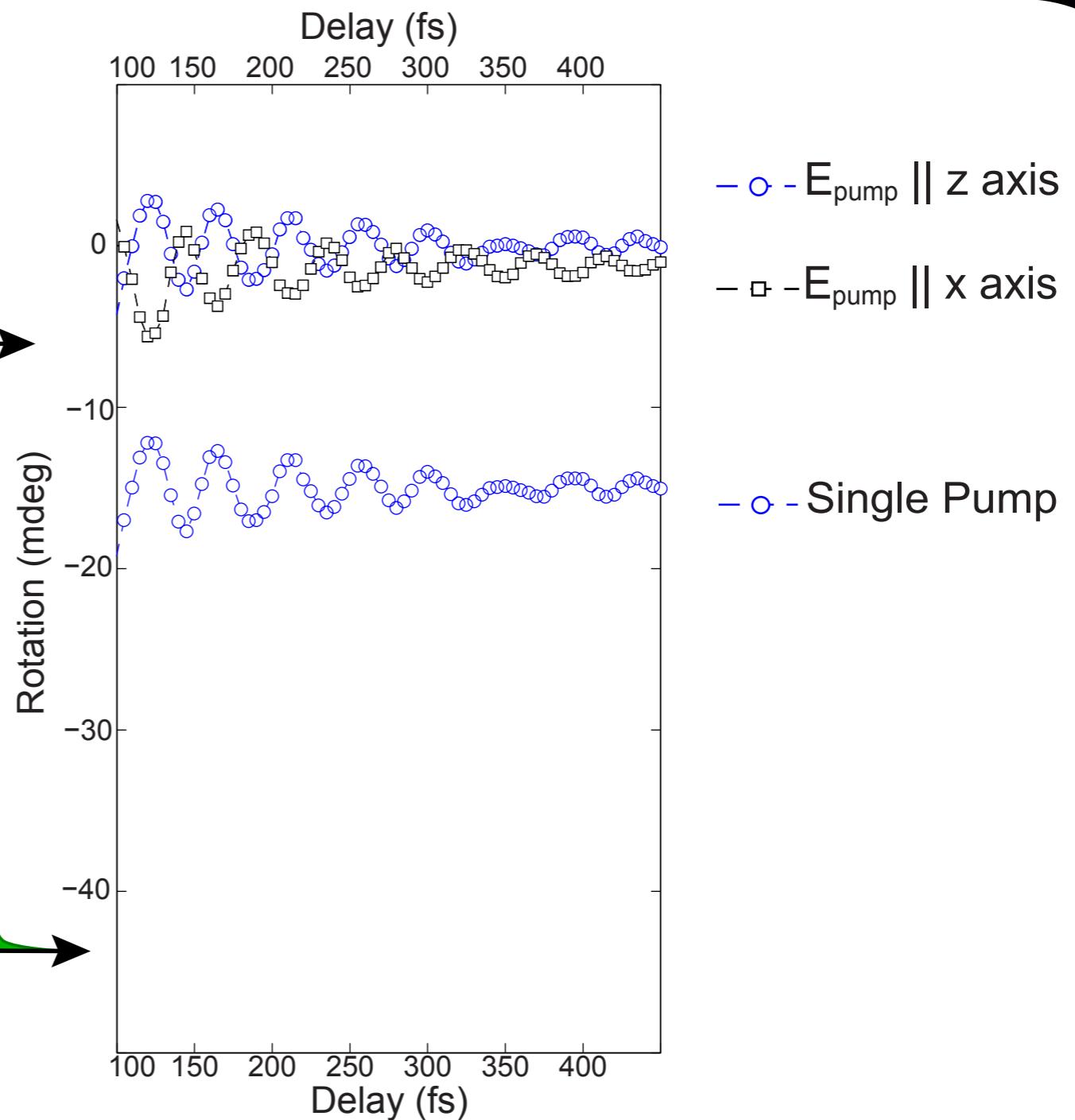
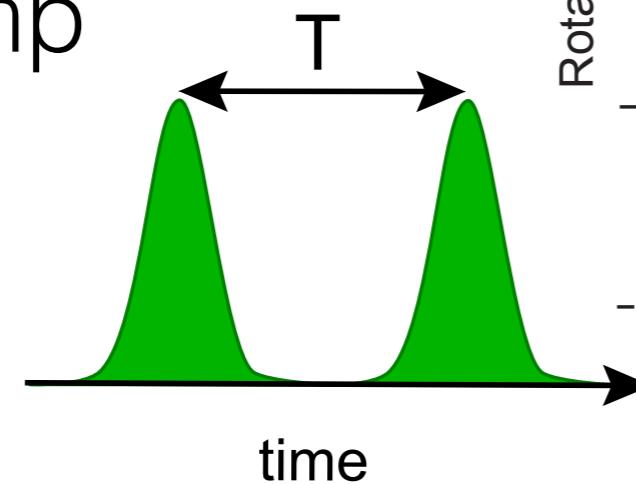


Control the dynamics

One pump pulse

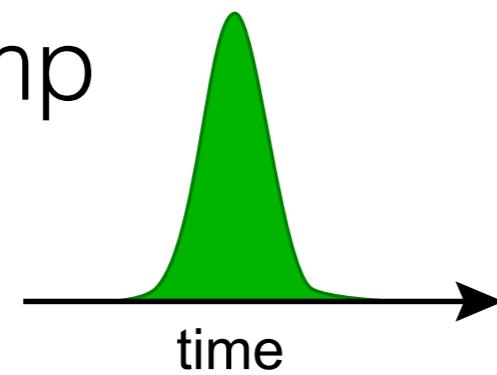


Two pump pulses

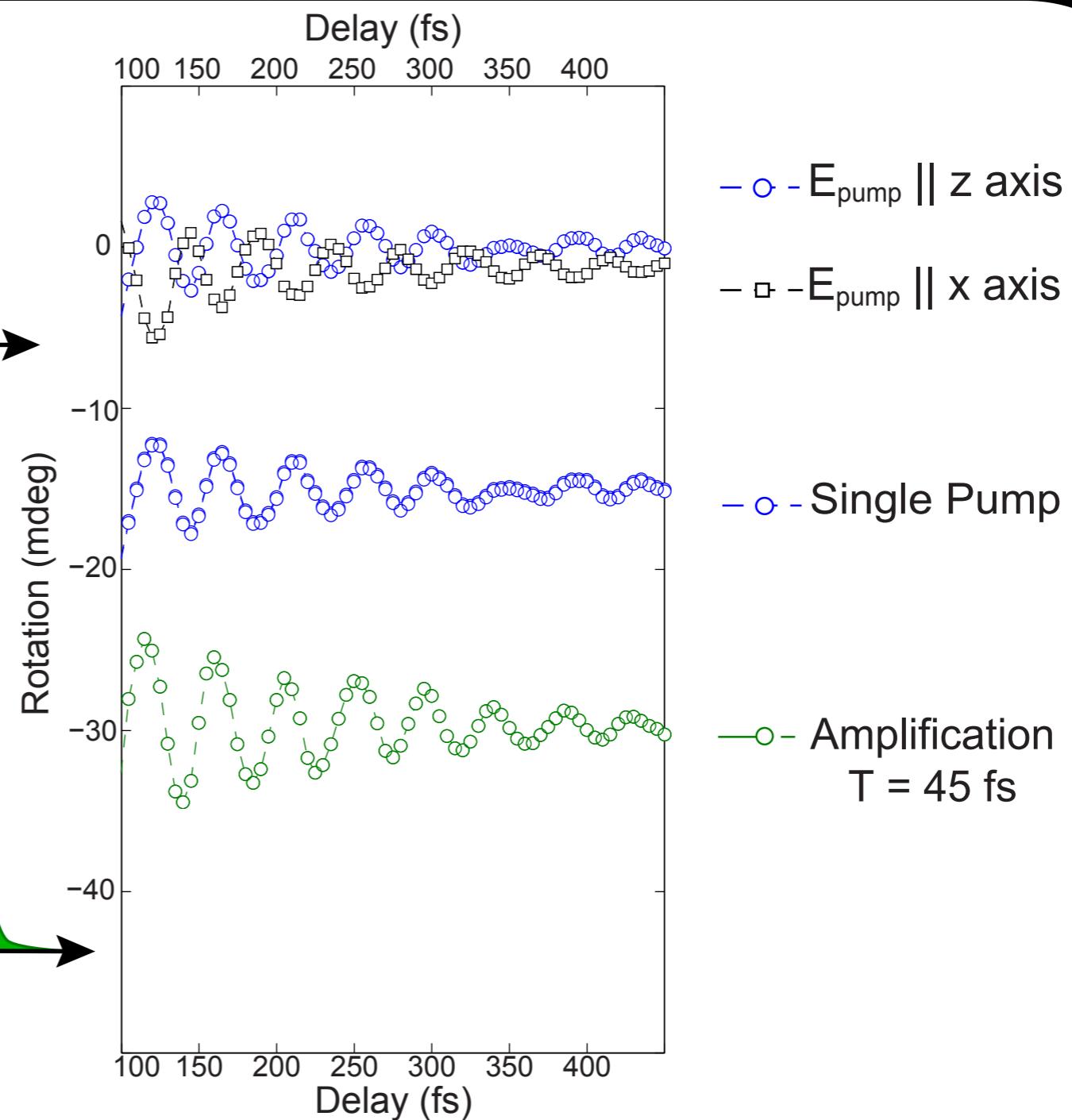
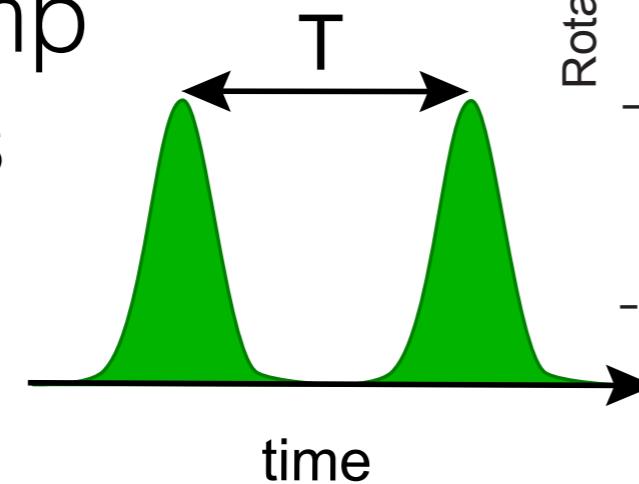


Control the dynamics

One pump pulse

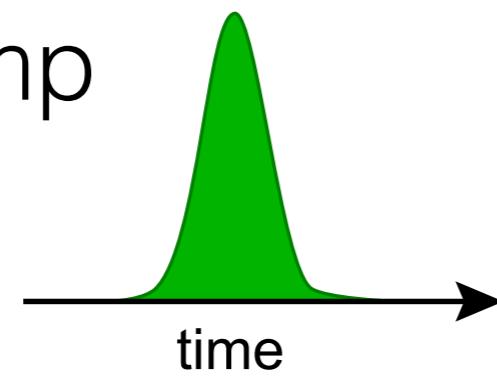


Two pump pulses

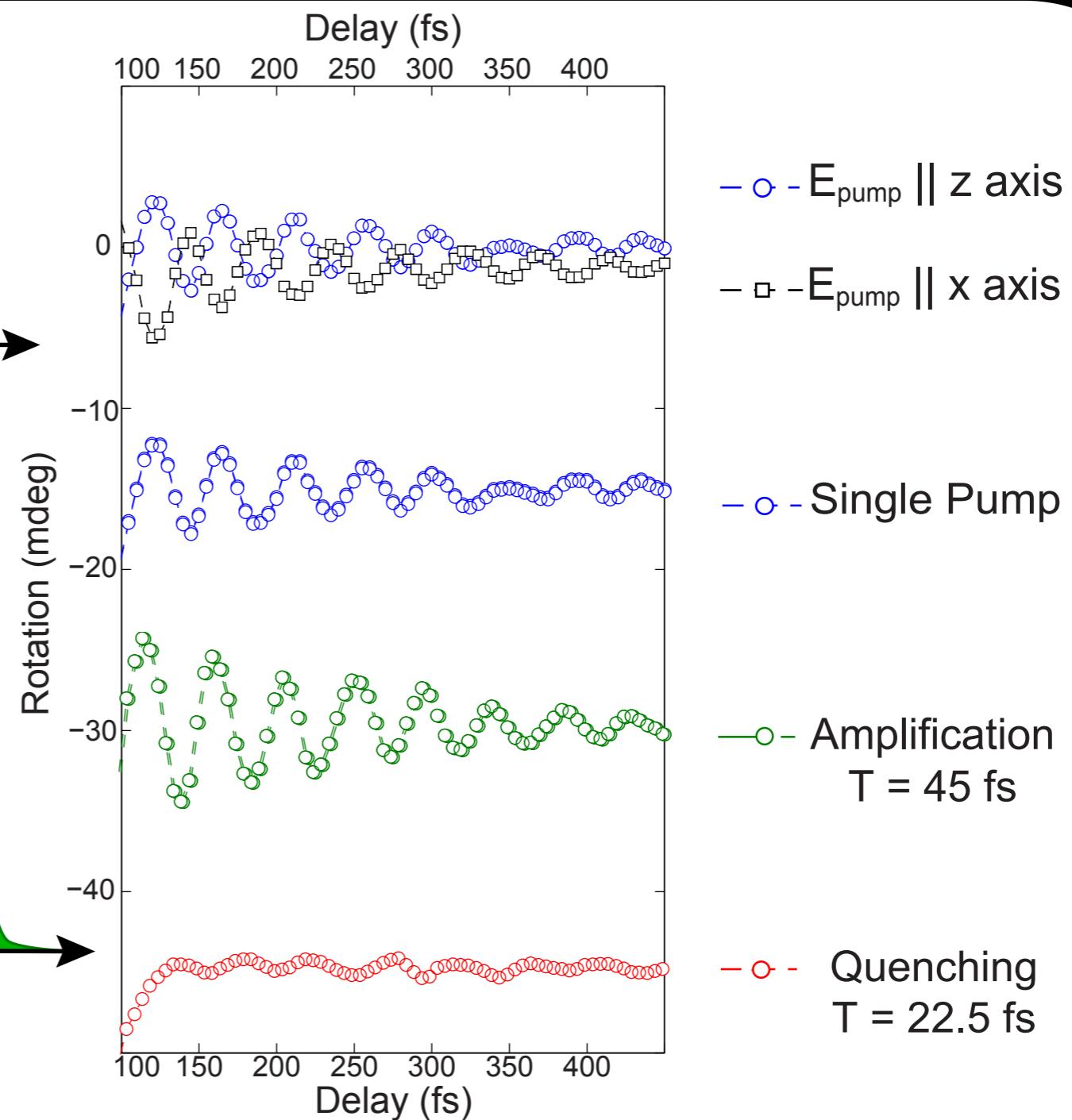
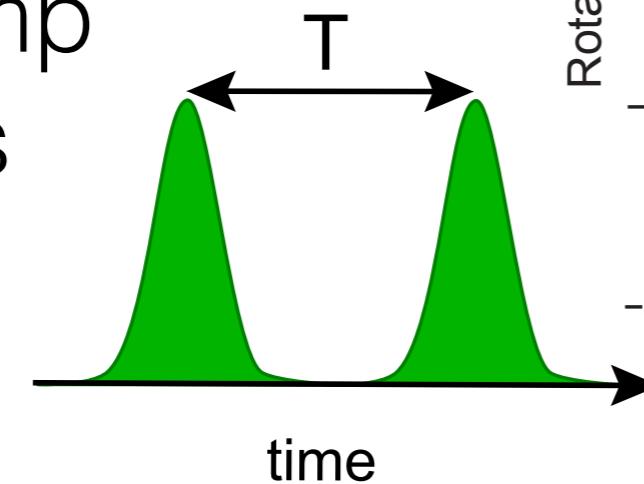


Control the dynamics

One pump pulse

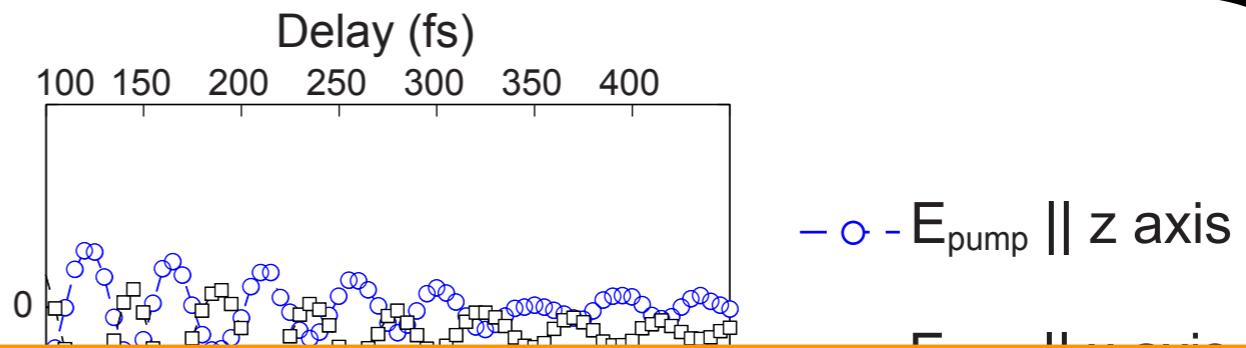


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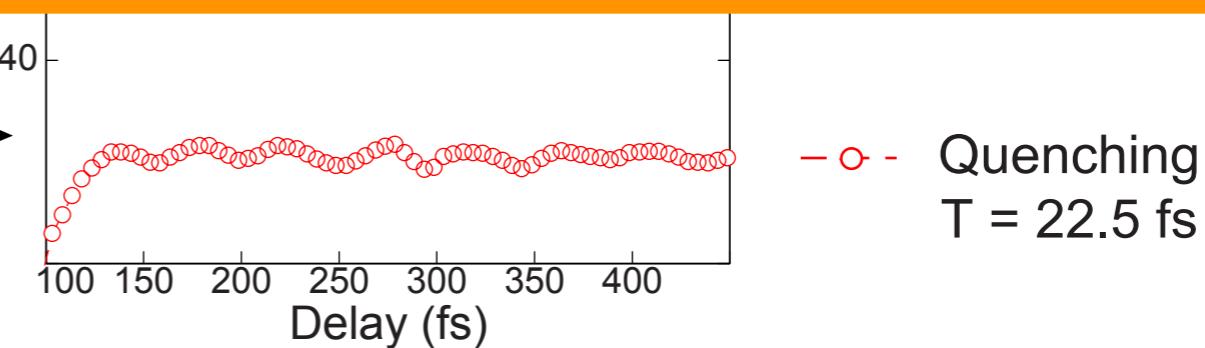


Control the dynamics

One pump
pulse

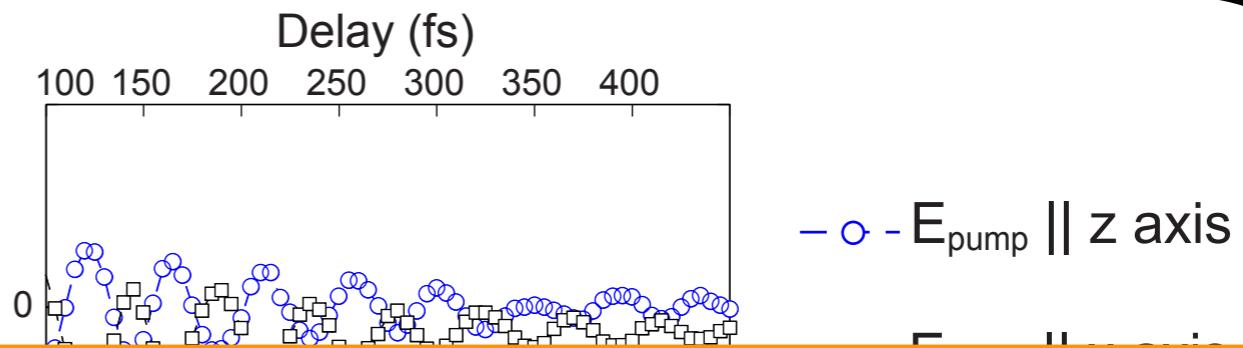


Coherent femtosecond
manipulation of
the order parameter

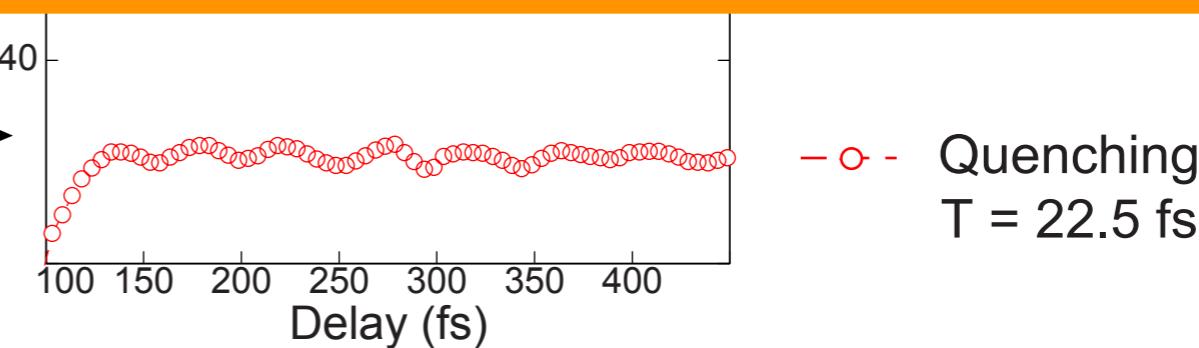
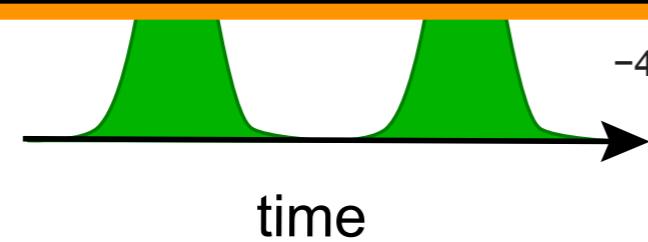


Control the dynamics

One pump
pulse



Coherent femtosecond manipulation of the order parameter



D. Bossini et al. Nat. Comm. 7, 10645 (2016)

Length-scale dynamics

Nearest-neighbors correlations

Length-scale dynamics

Nearest-neighbors correlations

Counterintuitive: MO macroscopic probe

Length-scale dynamics

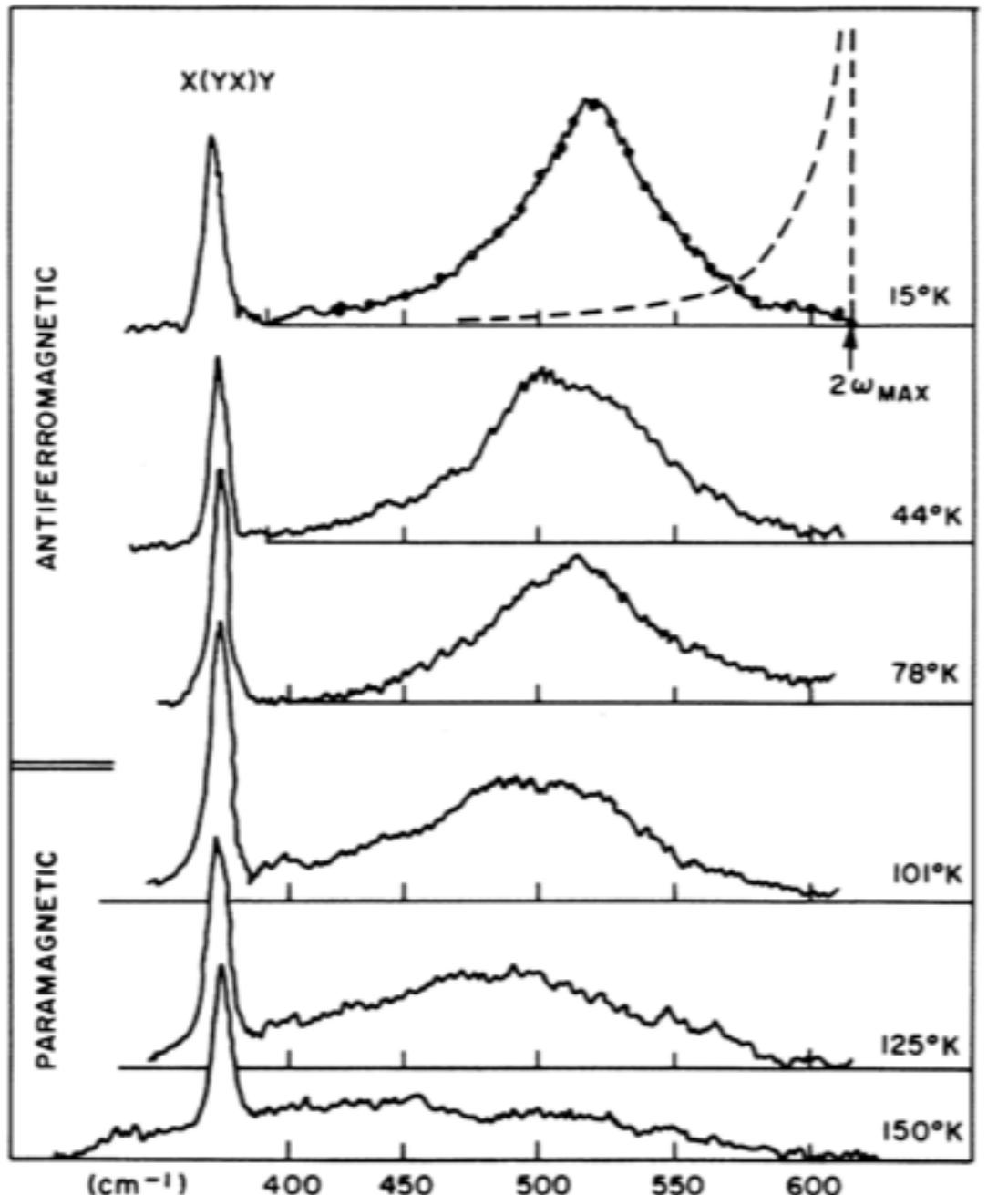
Nearest-neighbors correlations

Counterintuitive: MO macroscopic probe

Experimental evidence of
short-range nature
of the interaction ?

Length-scale dynamics

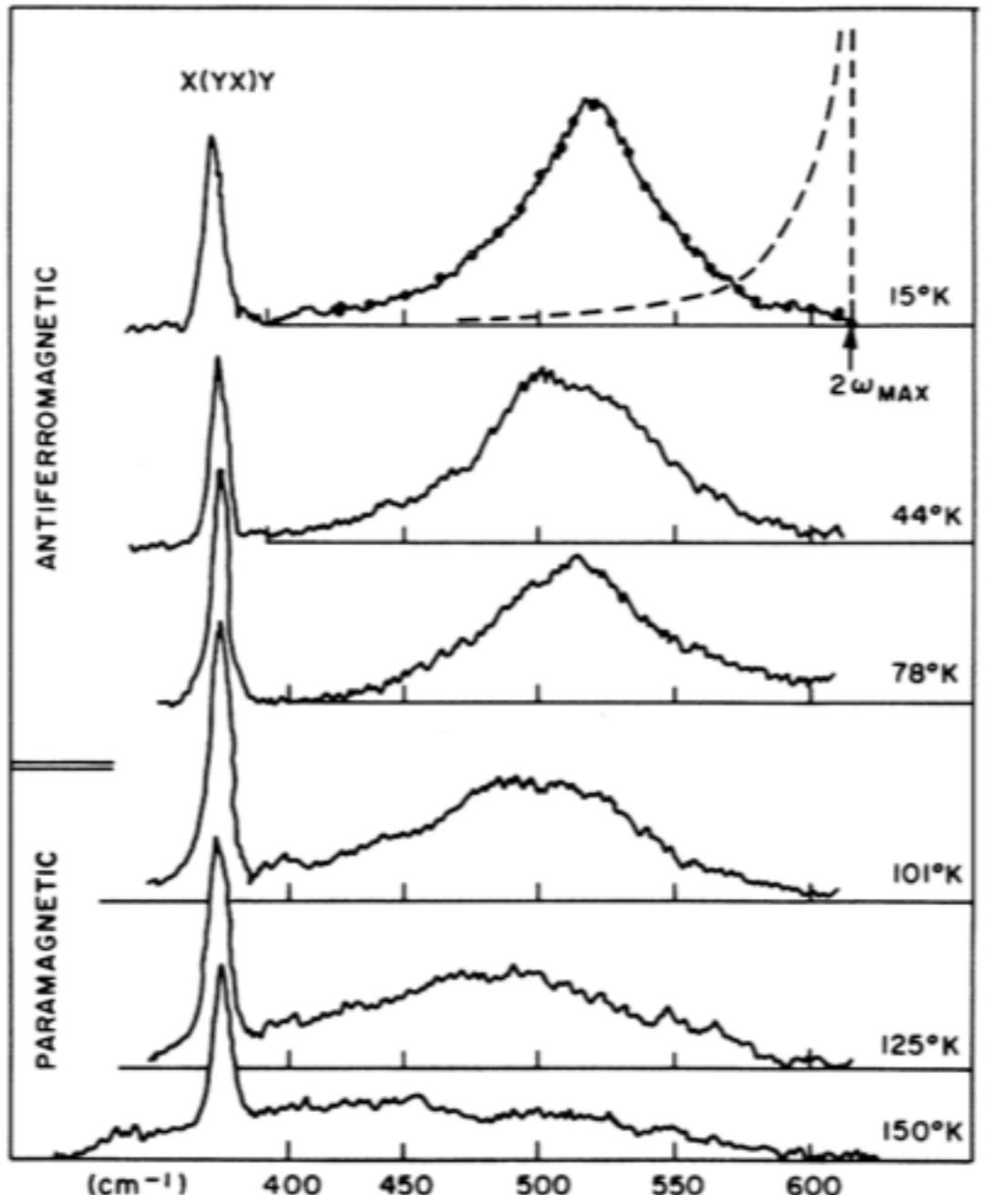
P. Fleury *et al.* PRL 24, 1347 (1970)



- K_2NiF_4 , $T_N = 96 \text{ K}$
- 2M-mode up to $T \sim 1.5 \times T_N$

Length-scale dynamics

P. Fleury *et al.* PRL 24, 1347 (1970)



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Long-range order

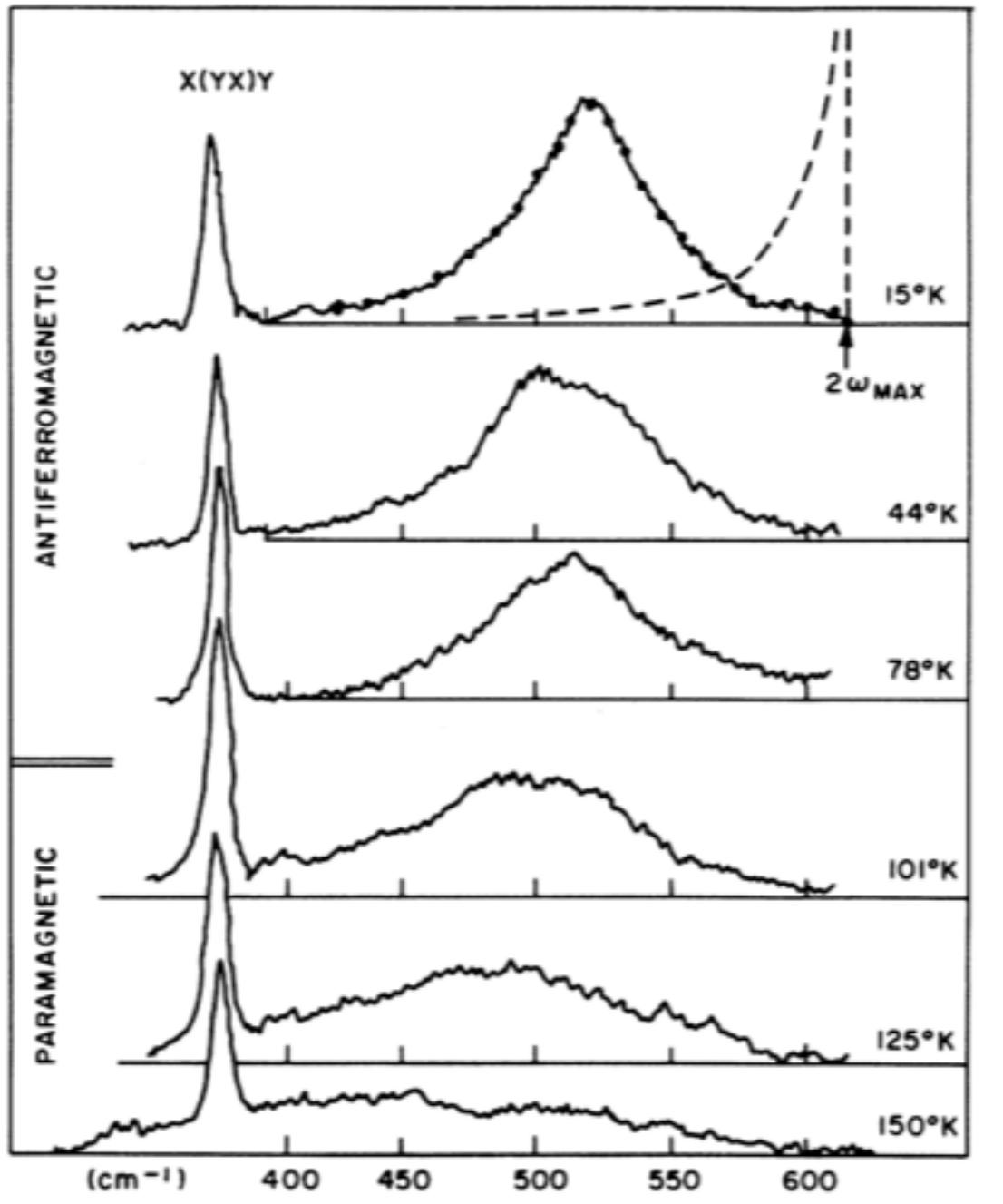
T

T_N



Length-scale dynamics

P. Fleury *et al.* PRL 24, 1347 (1970)



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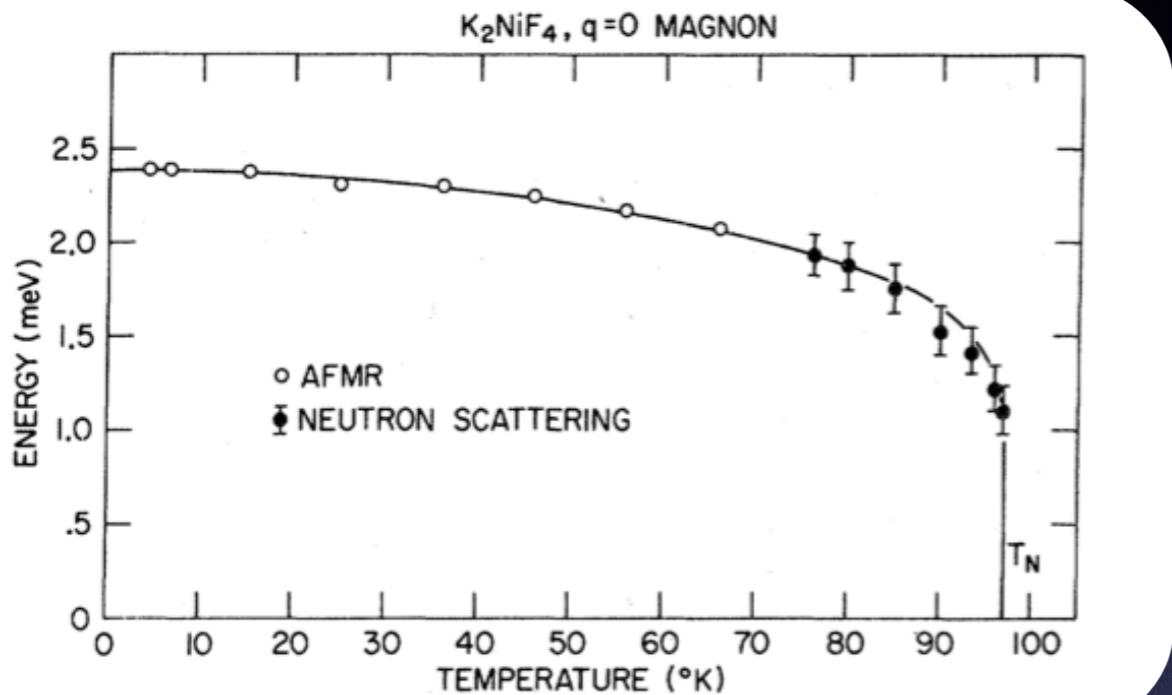
Long-range order

Short-range spin-spin correlations



Length-scale dynamics

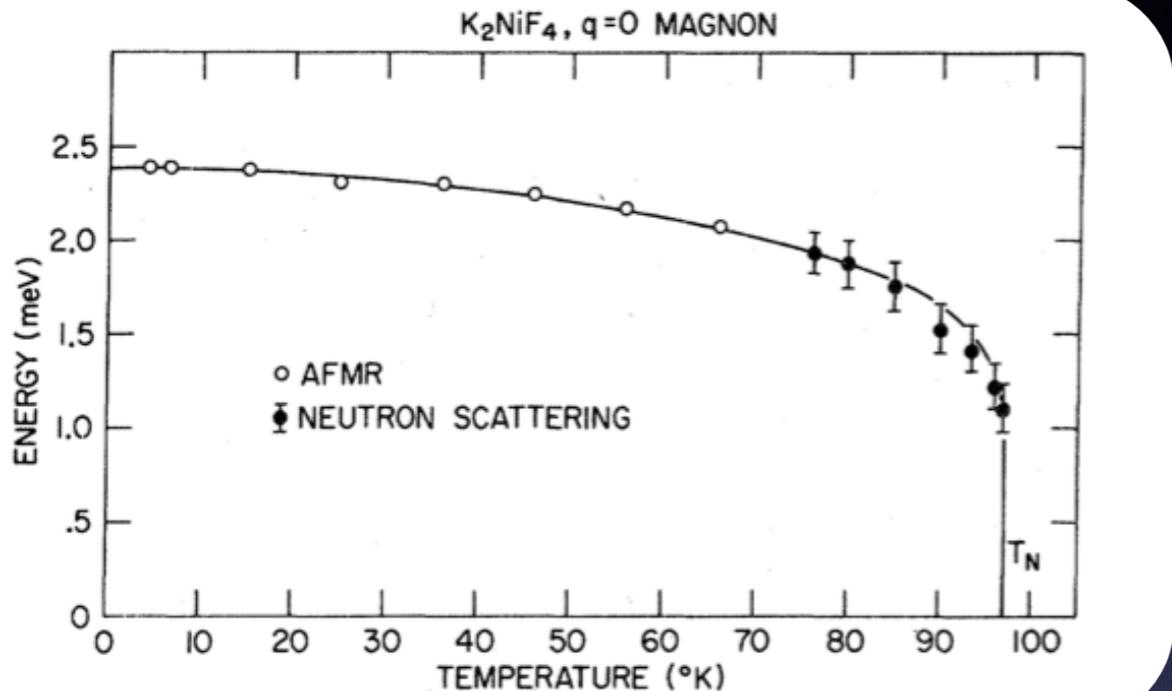
R. Birgenau *et al.* PRB 3, 1736 (1971)



$k \sim 0$ magnons soften at T_N

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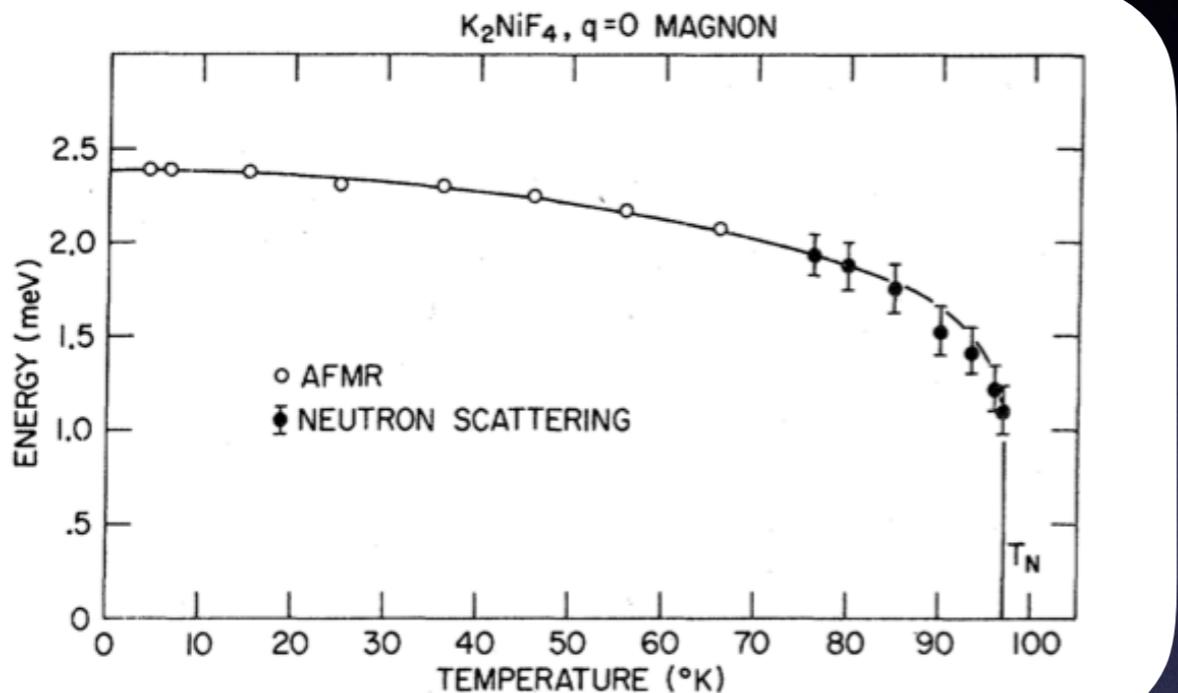


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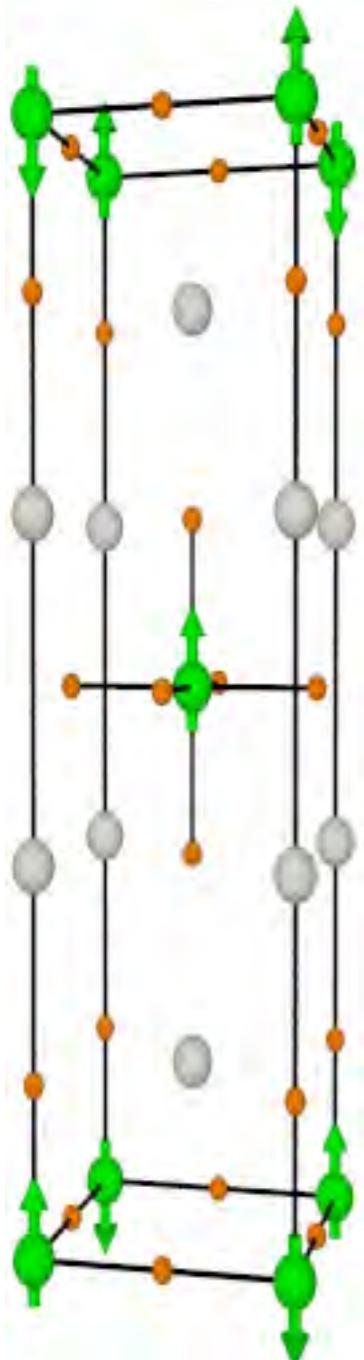
J. Zhao *et al.* PRB 73, 184434 (2006)

Long-wavelength magnons contributions ?

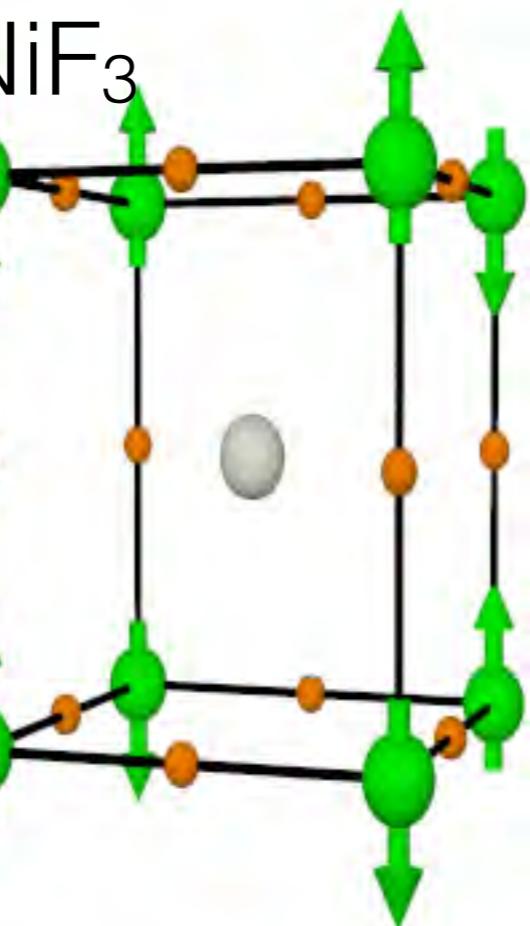
Our approach

Our approach

K_2NiF_4



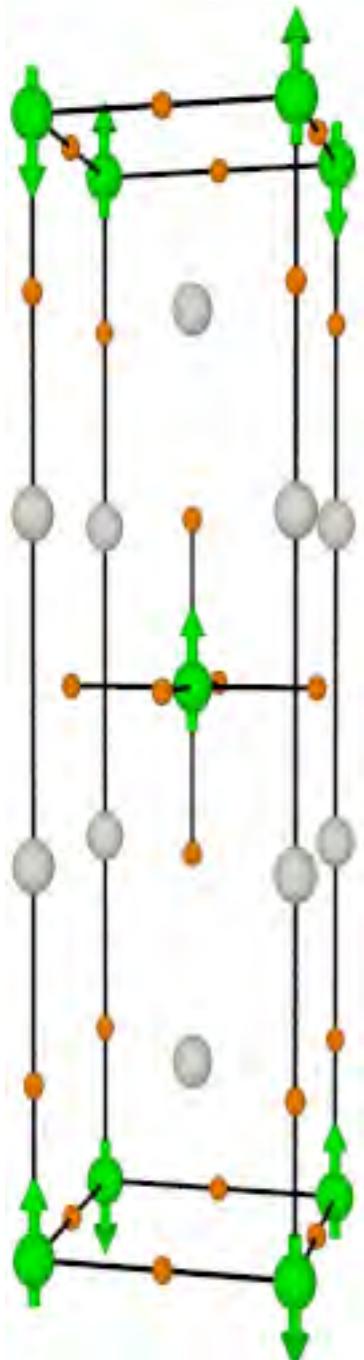
$KNiF_3$



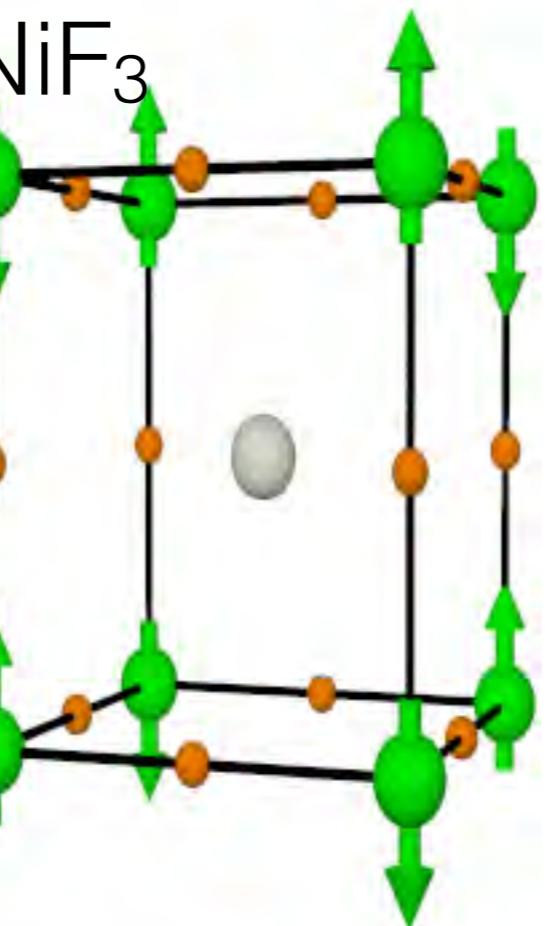
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(short-range)
- different anisotropy
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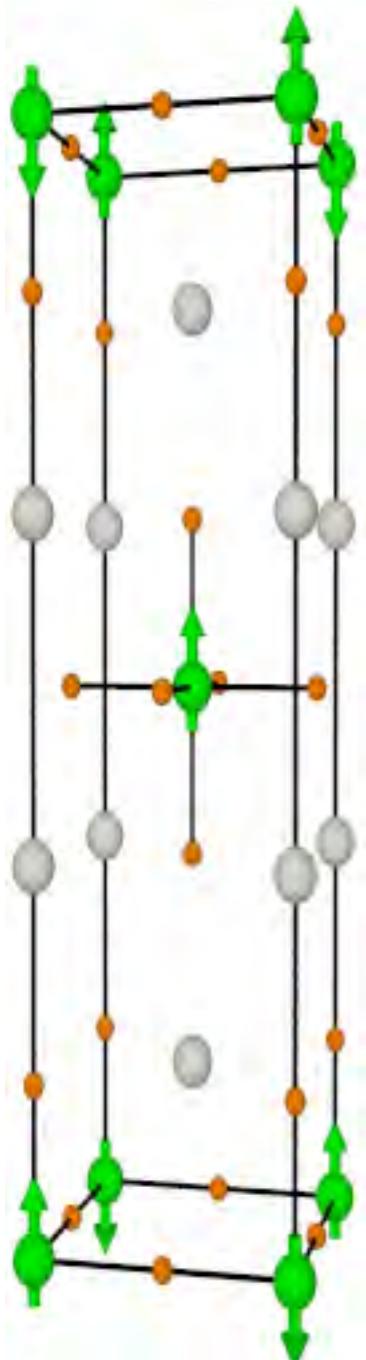


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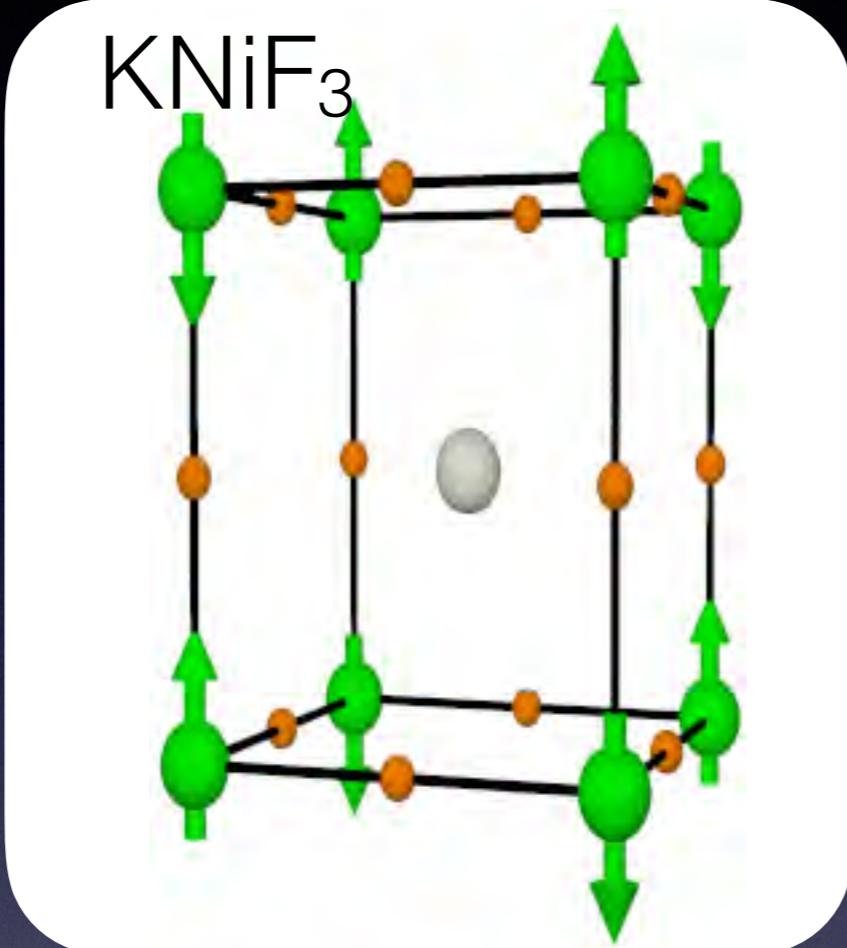
**Temperature dependence
femto-nanomagnonics**

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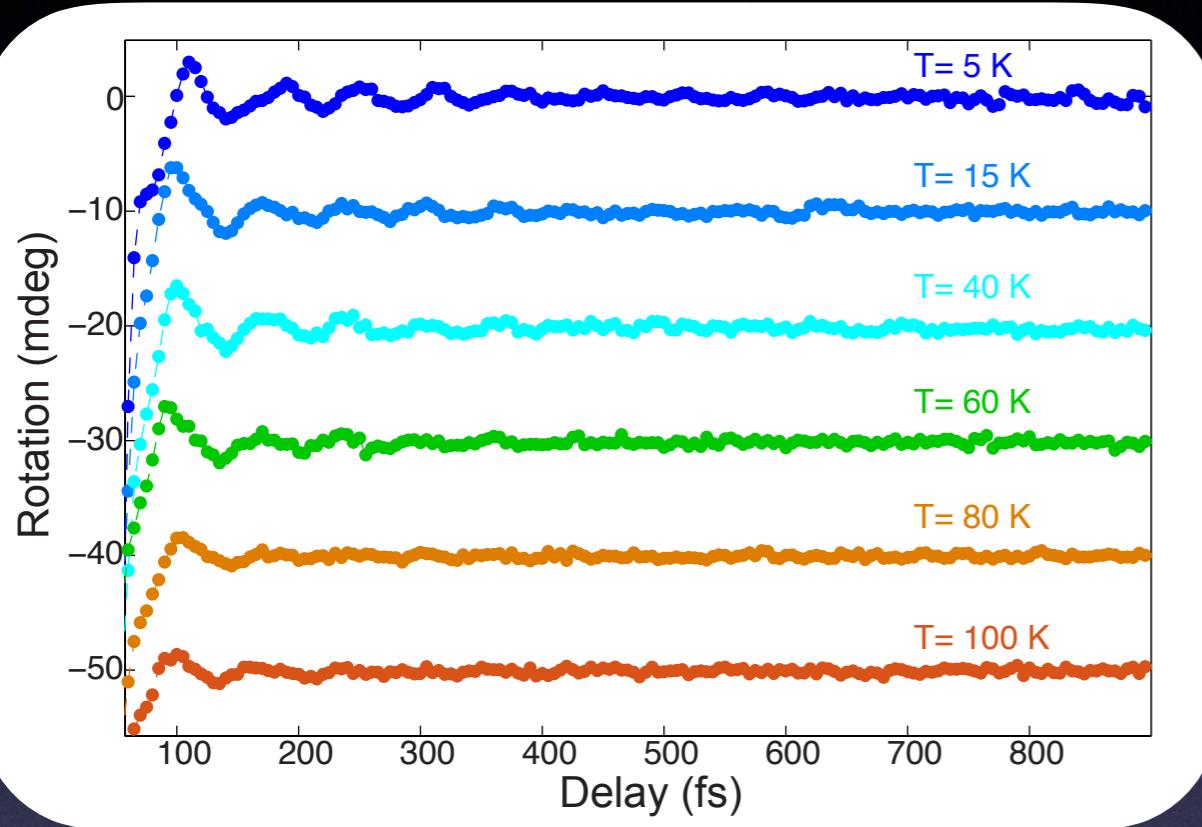


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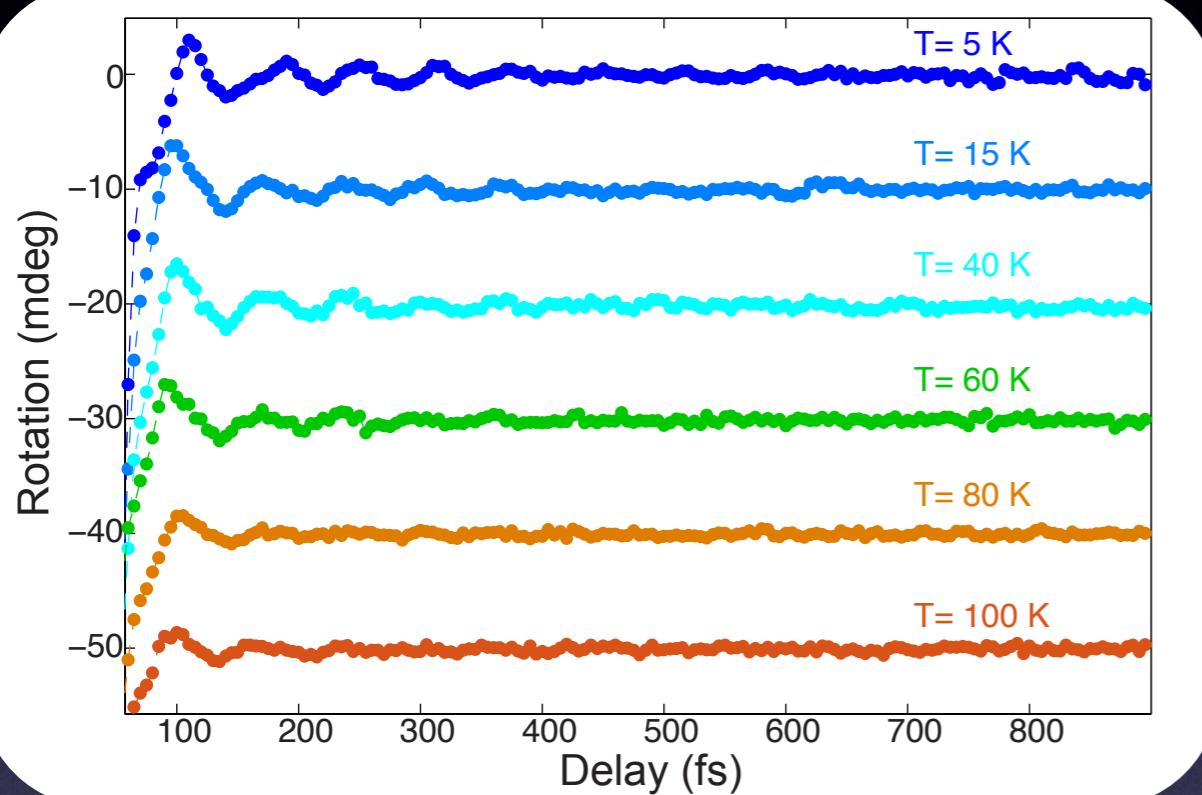
Softening and/or divergence
evidence of long-range

Temperature dependence

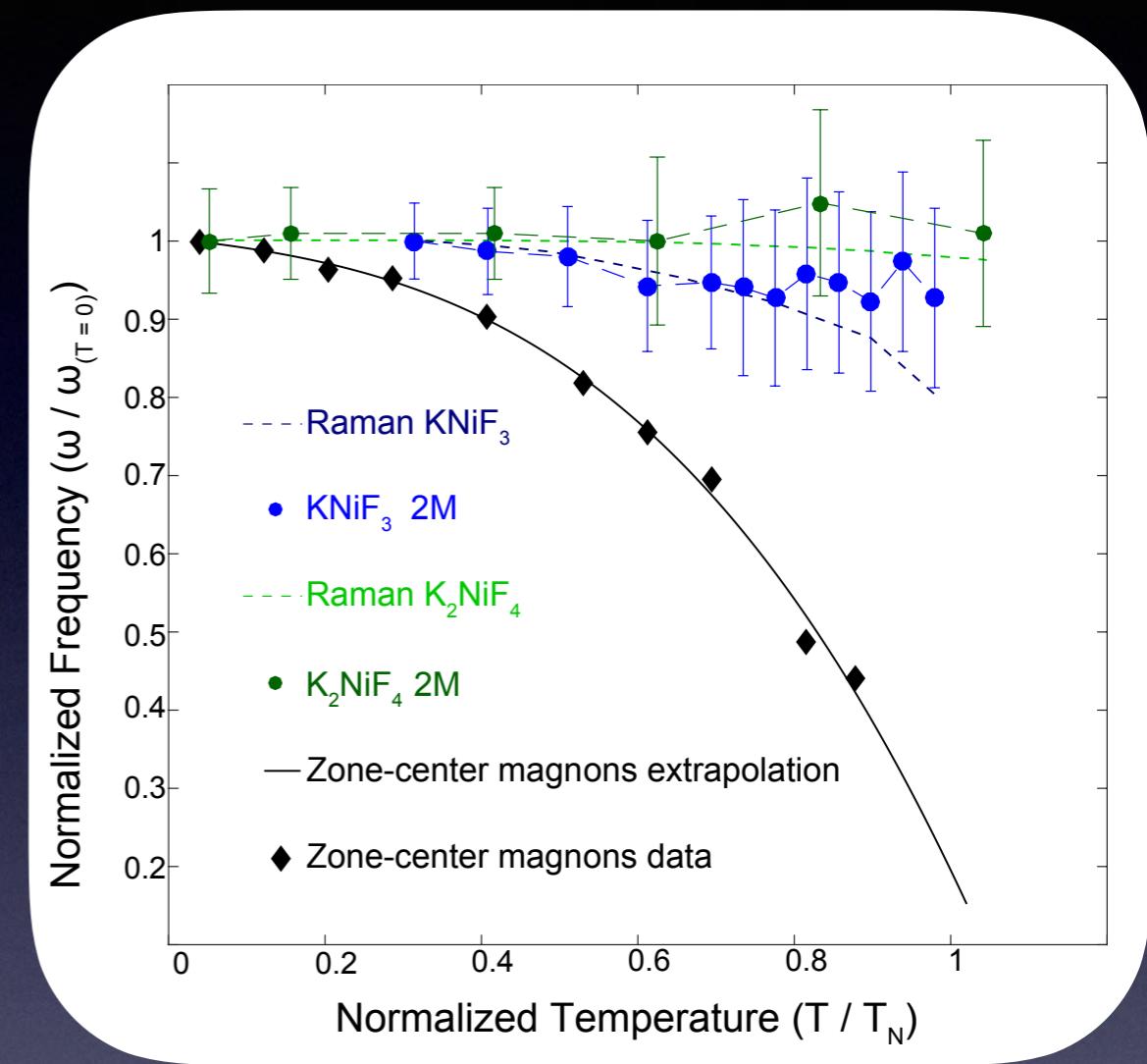


- Pump: 1.9 eV, Probe = 1.3 eV
- Fluence = 4.5 mJ/cm²

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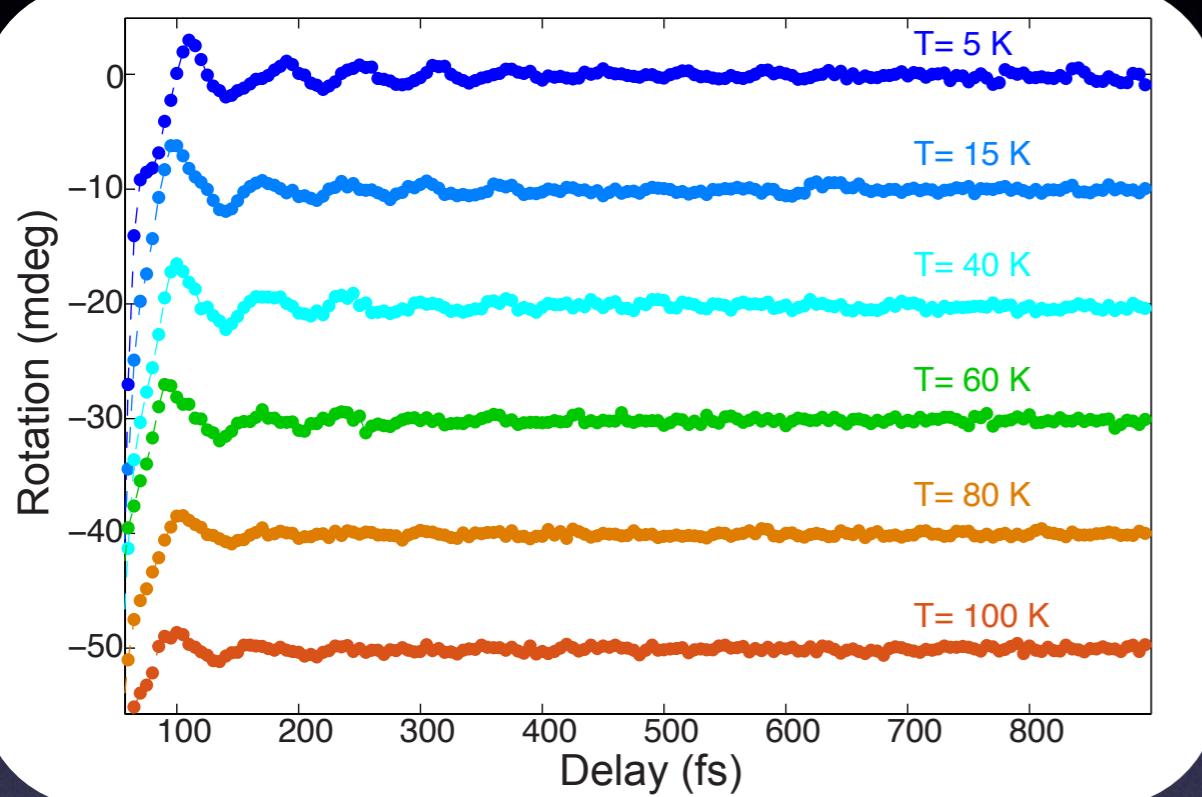


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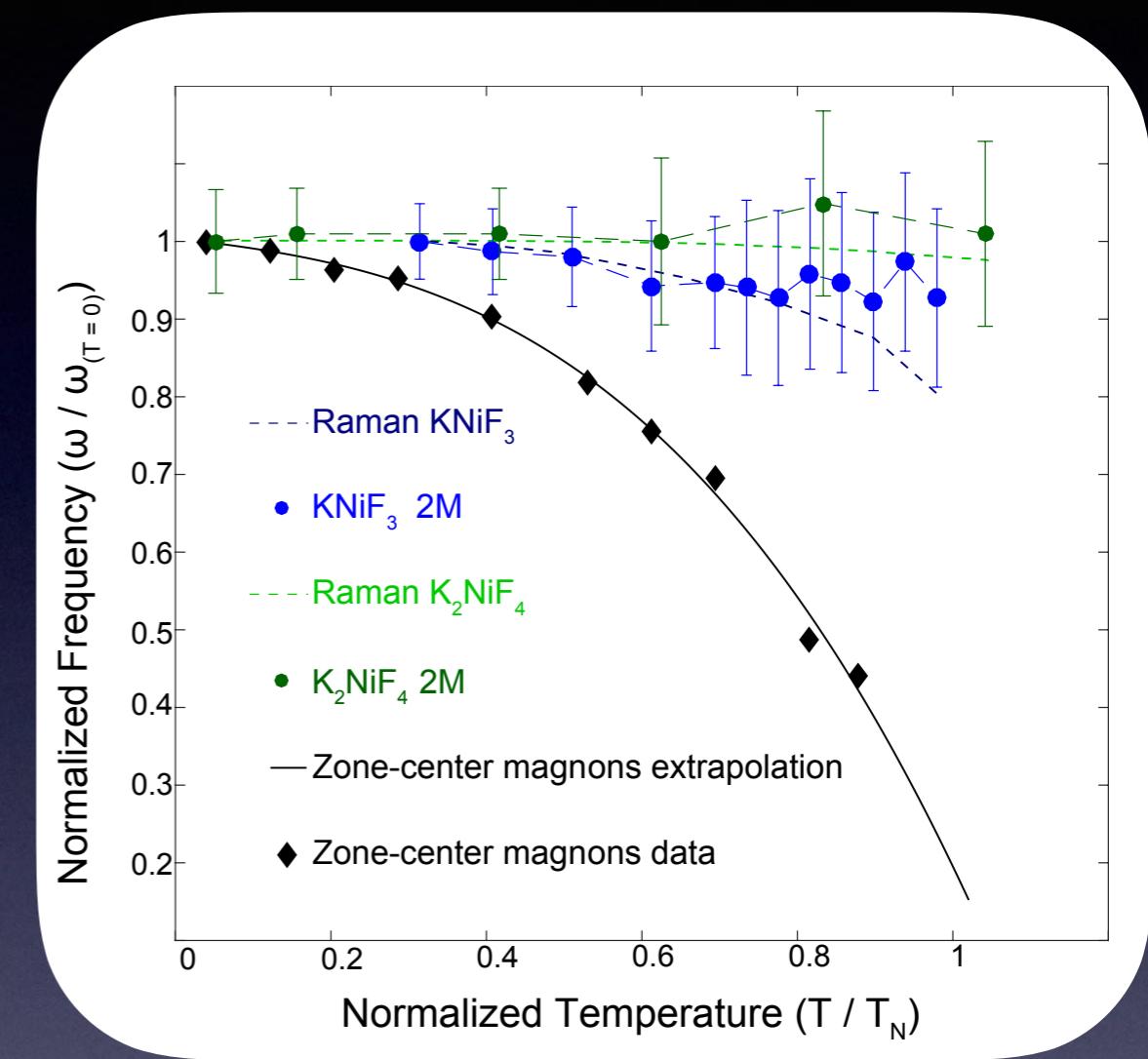


D. Bossini *et al.* in preparation

Temperature dependence



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D. Bossini *et al.* in preparation

Contribution only from femto-nanomagnons

Role of temperature

Temperature defines the amplitude and lifetime
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S. Chinn et al. PRB **3**, 1709 (1971)

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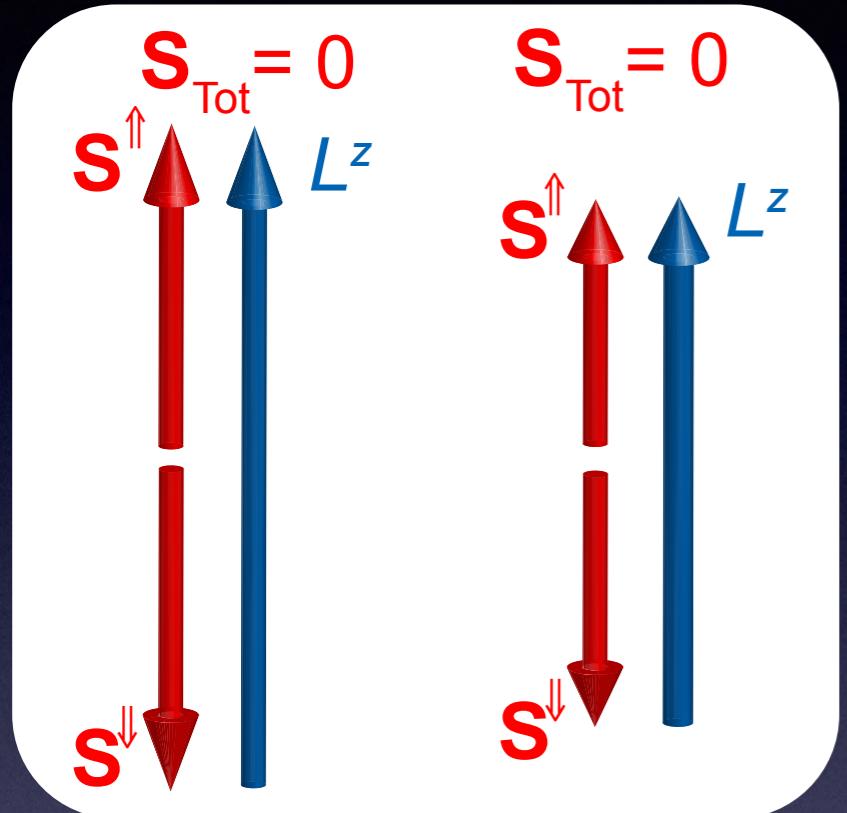
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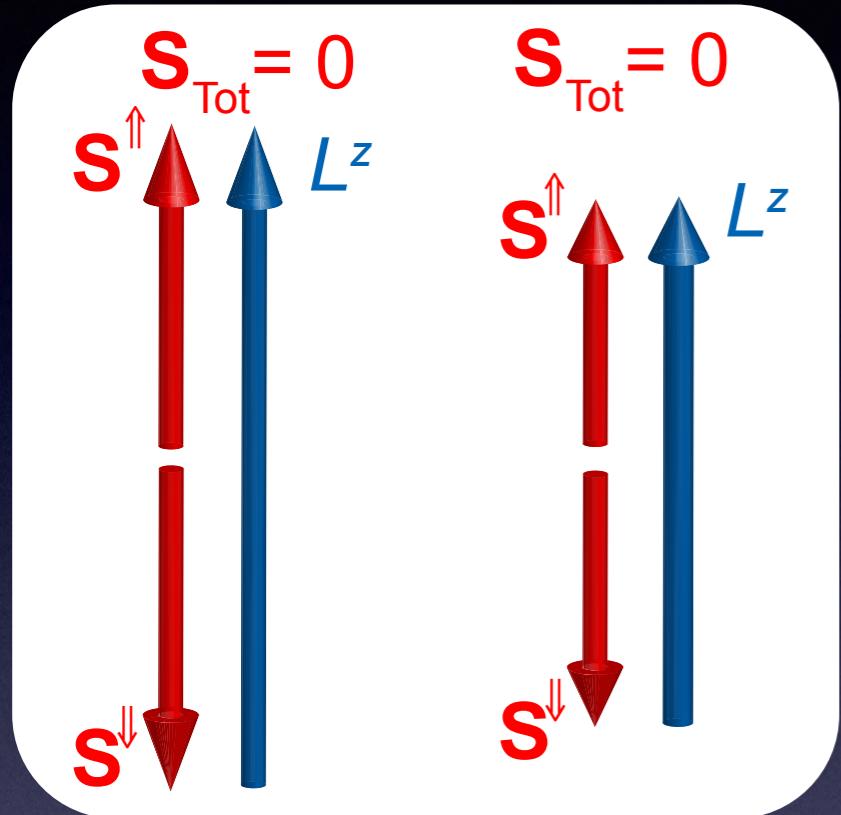
Dynamics order parameter



$$\Delta S = 0$$

$$L \equiv S^{\uparrow\uparrow} - S^{\downarrow\downarrow}$$

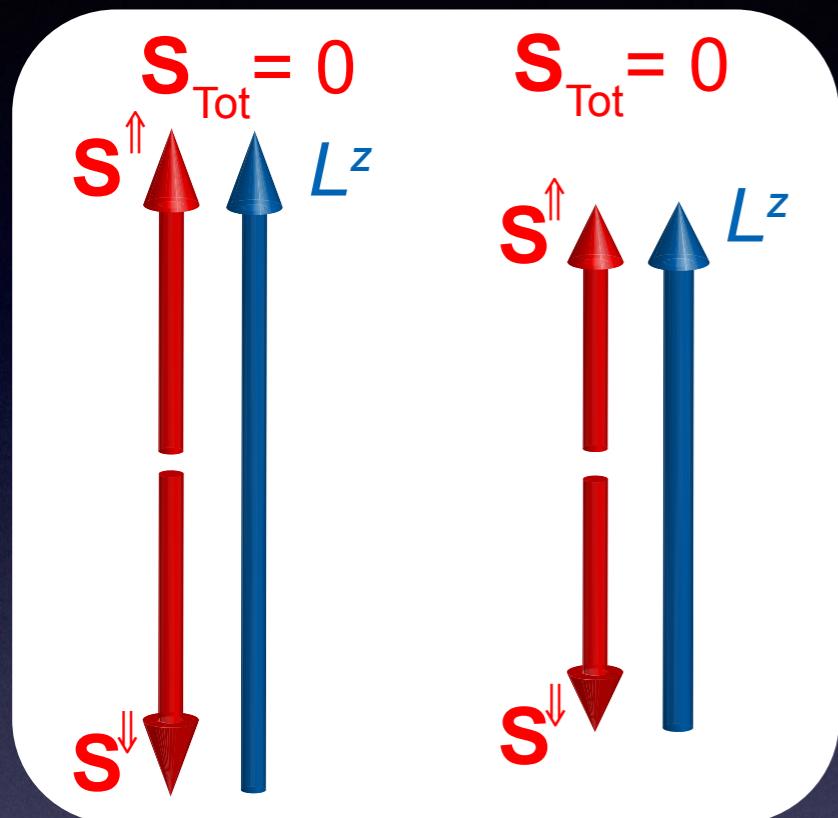
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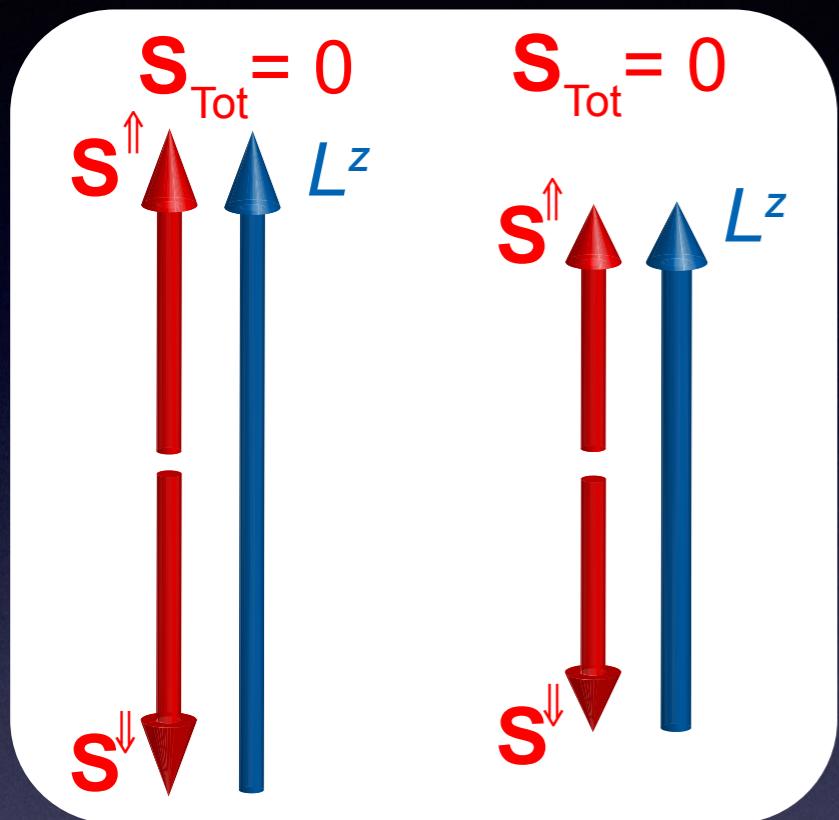


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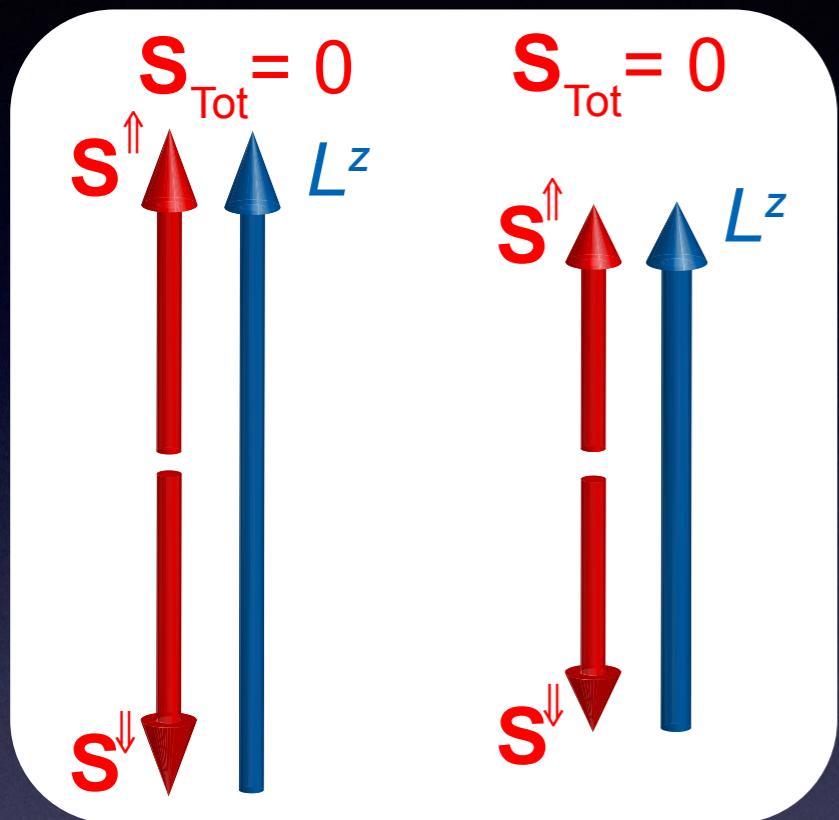
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J. Zhao et al. PRL **93**, 107203 (2004)

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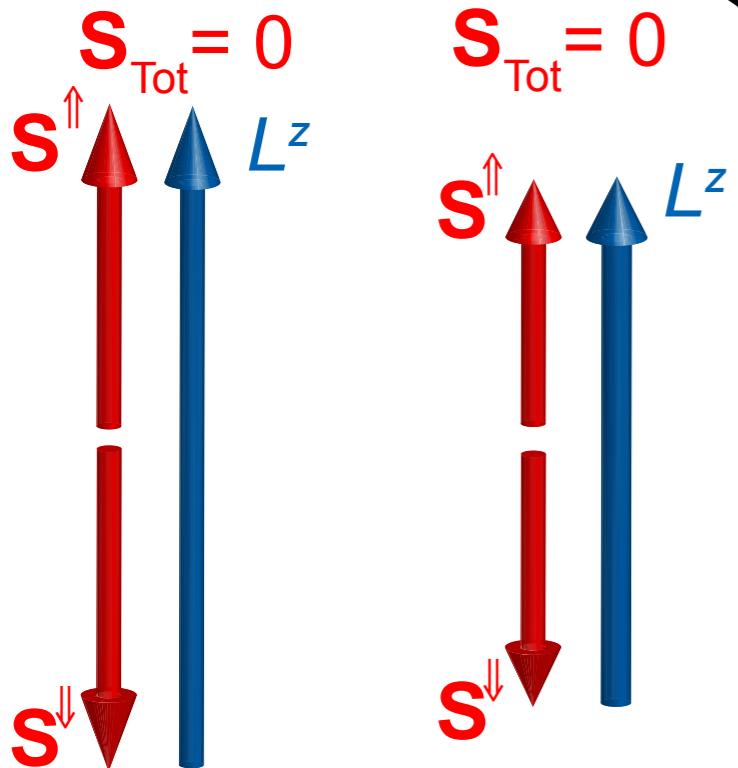
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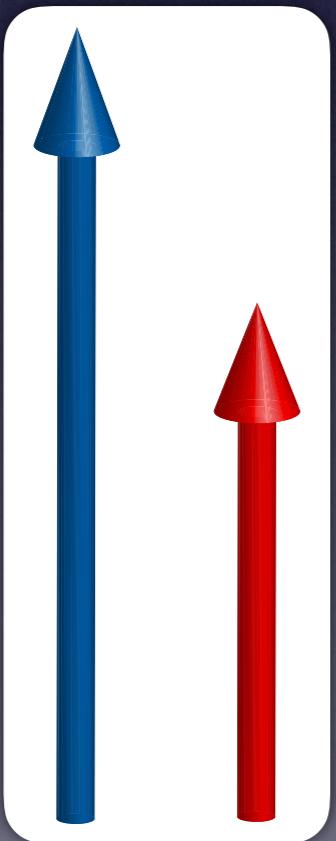
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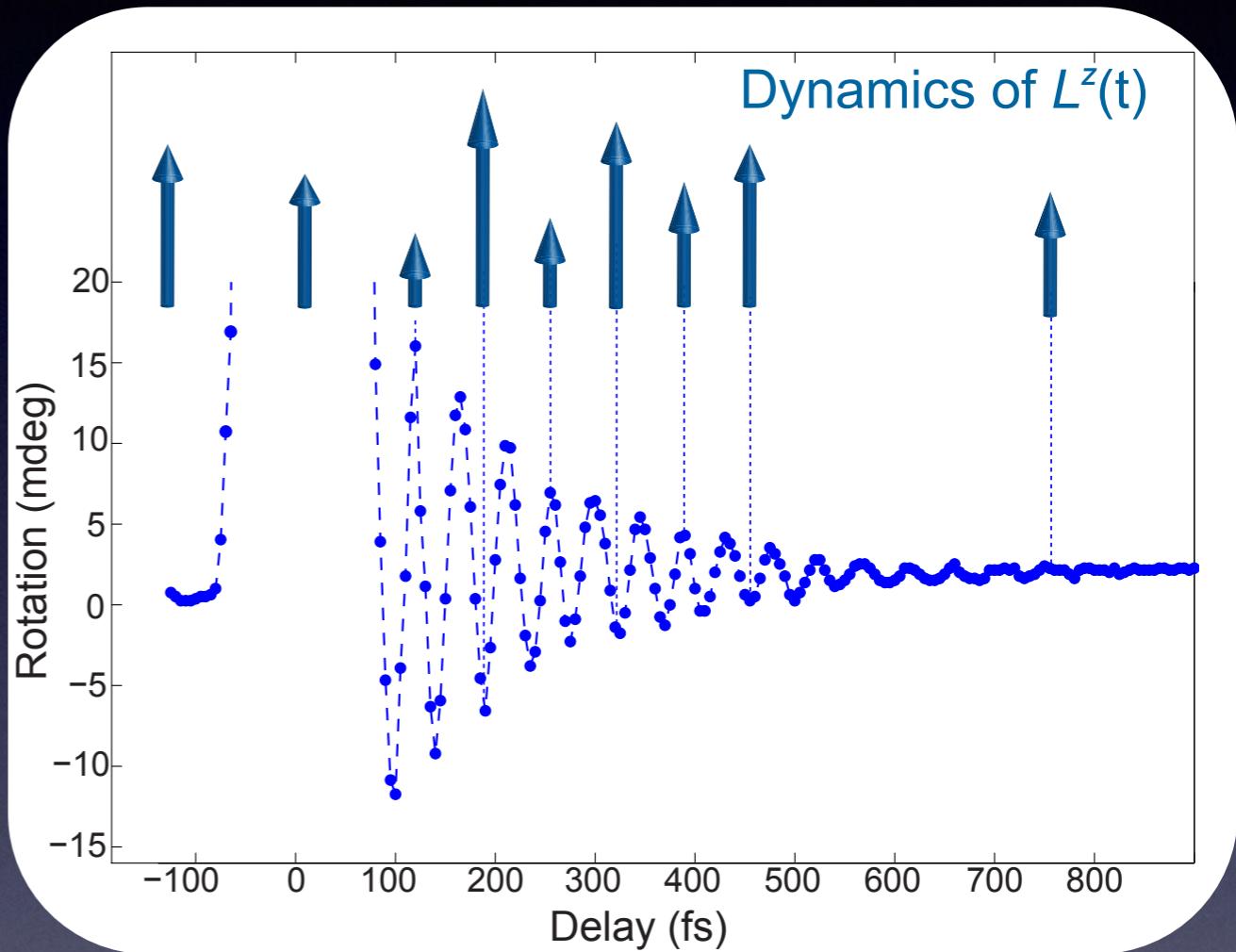
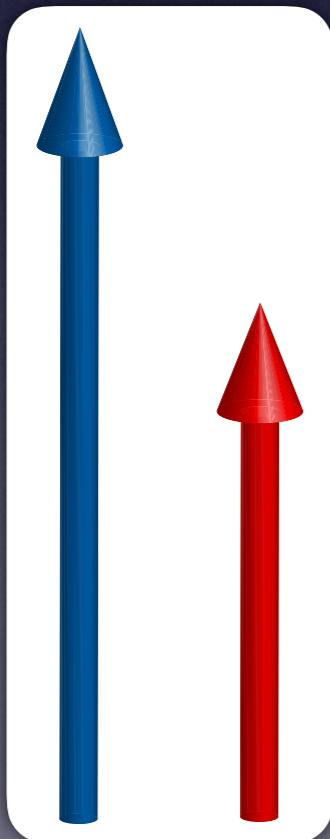


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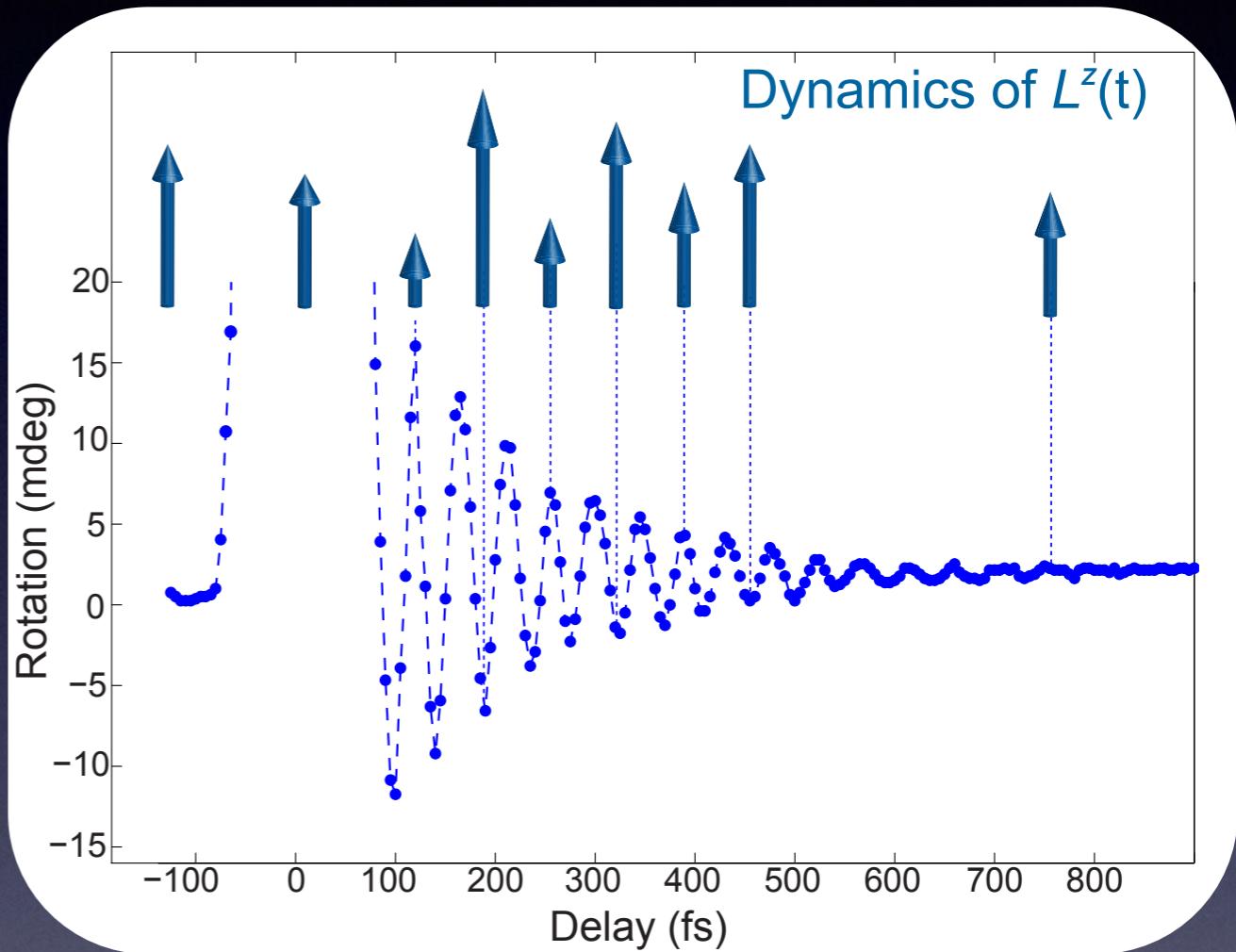
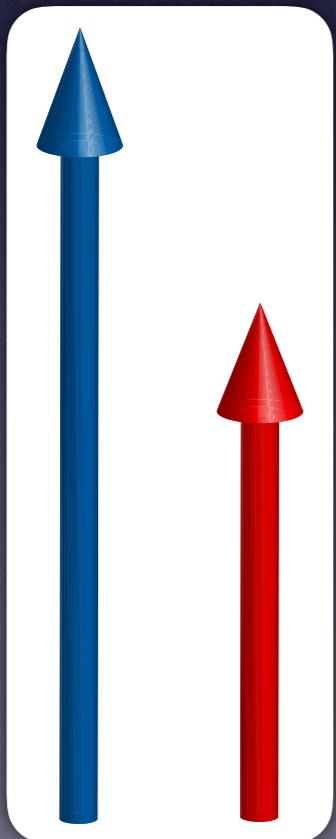


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Femto-nanomagnonics: dynamics of
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$$\cancel{\langle \mathbf{S}_i \cdot \mathbf{S}_j \rangle} = \langle \mathbf{S}_i \rangle \langle \mathbf{S}_j \rangle$$

Femto-nanomagnonics: dynamics of nearest neighbors correlations

Quantum modelling

Goal: equation of motion

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$$H_0 = J \sum_{i,\delta} \hat{\mathbf{S}}_i \cdot \hat{\mathbf{S}}_{i+\delta} \quad \delta H = \frac{1}{2} f(t) \sum_{i,\delta} \Delta J(\delta) \hat{\mathbf{S}}_i \cdot \hat{\mathbf{S}}_{i+\delta},$$

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$$L_z = L_z(0) - z S \sum_{\mathbf{k}} \frac{\gamma_{\mathbf{k}}}{\sqrt{1 - \gamma_{\mathbf{k}}^2}} \frac{2 \operatorname{Re} \mu_{\mathbf{k}}}{1 - |\mu_{\mathbf{k}}|^2}$$

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What's next

Femto-nanomagnonics

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Coherent control (ISRS excitation)

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Conclusions

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D. Bossini et al. Nat. Comm. **7**, 10645 (2016)

D. Bossini et al. Physica Scripta **92**, 024002 (2017)

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- Experimental prove of quantum nature
- Spatial propagation

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