

Bayerische  
Akademie der Wissenschaften



Technische Universität München

# Non-collinear spin dynamics in magnetic insulators



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# Acknowledgements

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groningen**

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- Carsten Dubs
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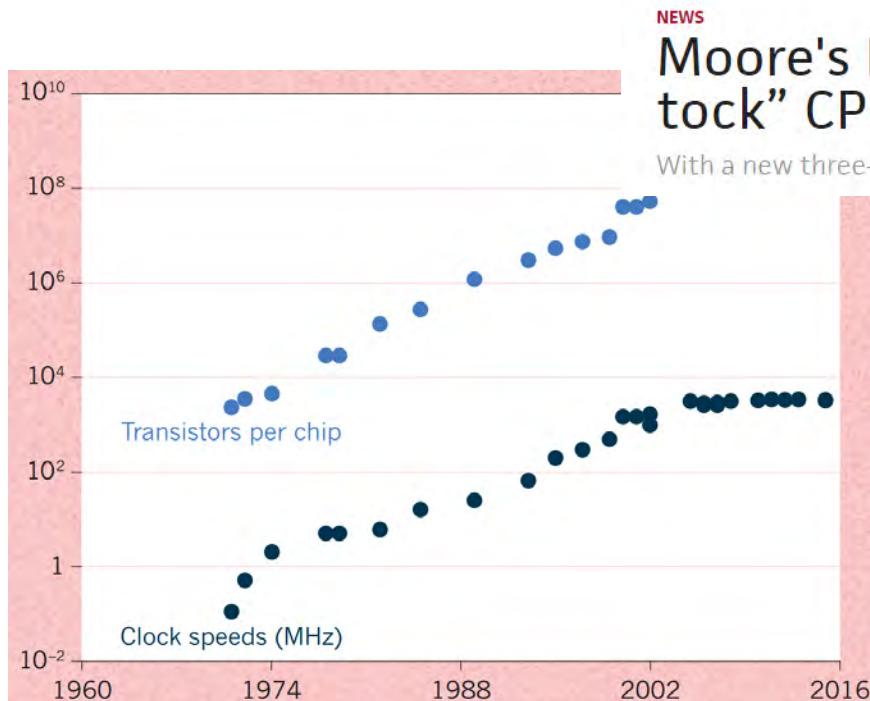
# More than Moore

## The chips are down for Moore's law

The semiconductor industry will soon abandon its pursuit of Moore's law. Now things could get a lot more interesting.

*Nature* 530, 144 (2016)

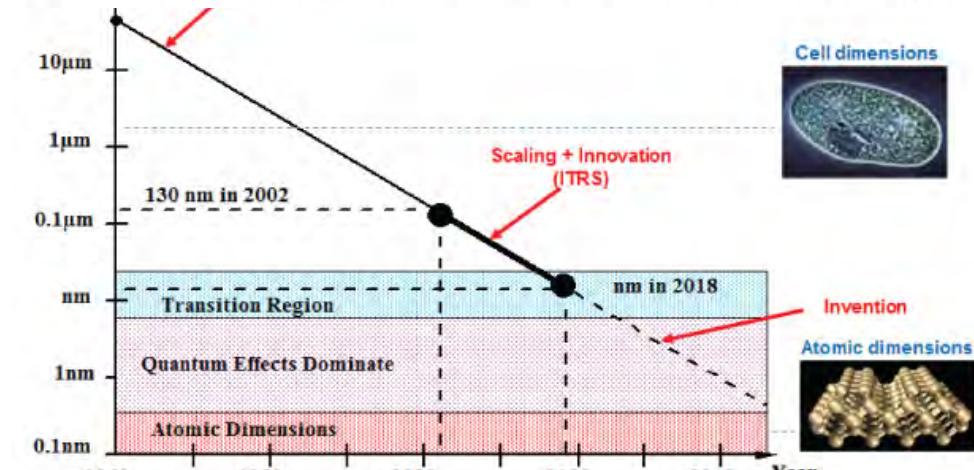
M. Mitchell Waldrop



**Moore's Law stutters: Intel officially puts "tick-tock" CPU release cycle on hiatus**

With a new three-step manufacturing cadence, Intel takes a break from its typical two-year cycle.

Pcworld, (2016)



Source: From Silicon VLSI Technology, by professors James D. Plummer, Michael D. Deal, and Peter B. Griffin, Stanford University, 2000.

Heat limit

Size and cost limit

# More than Moore



Possible alternatives: "...Spintronic materials that would compute by flipping electron spins rather than by moving electrons."

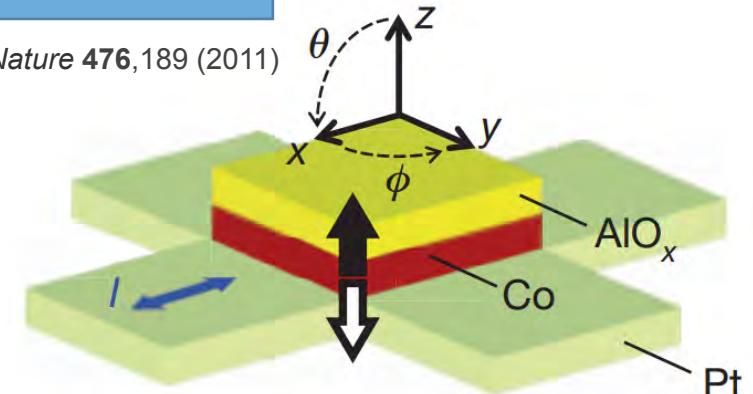
*Nature* **530**, 144 (2016)

## Spintronics

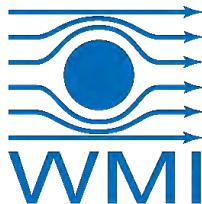


## Spin-Orbit-Torques

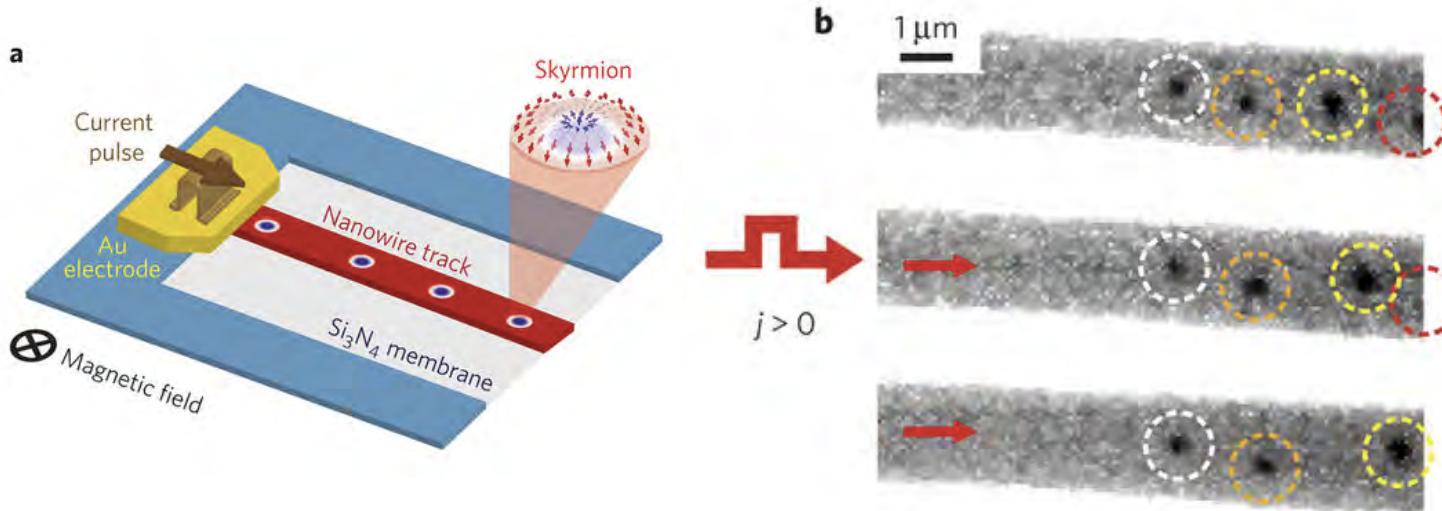
Miron et al., *Nature* **476**, 189 (2011)



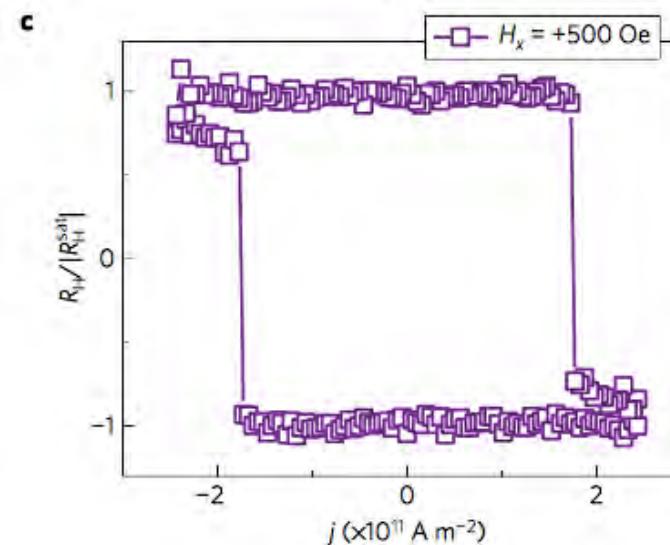
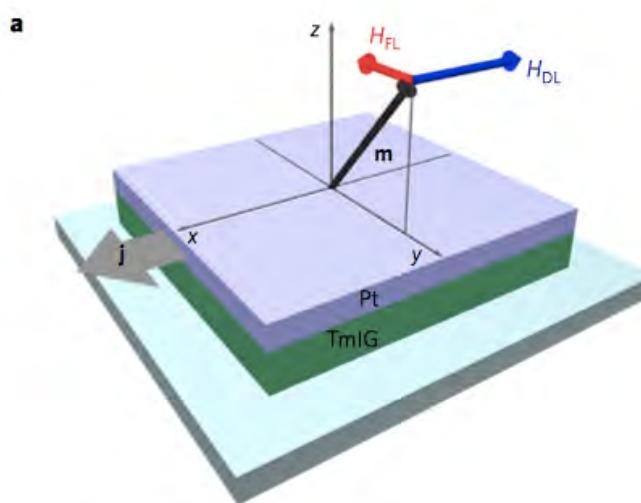
Can we use these concepts for non-collinear magnetic insulators?



# Towards insulating Skyrmionics

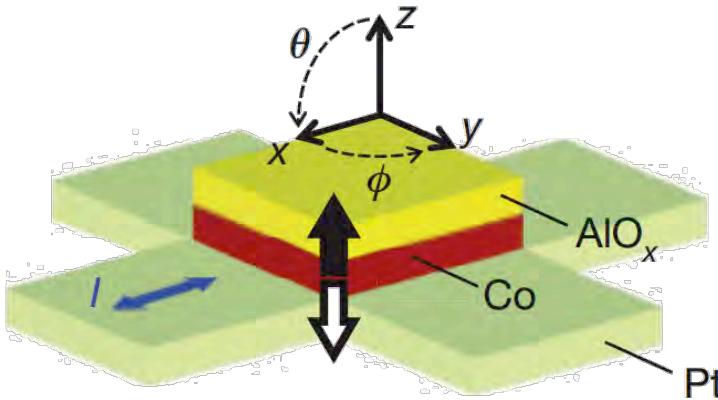


Metallic  
Skyrmions:  
Nat Mater  
**15**, 501  
(2016).



Insulating  
SOTs:  
Nature  
Materials **16**,  
309 (2017).

# Introduction



Physical mechanisms:  
**Magnetization dynamics**  
**spin orbit interaction**

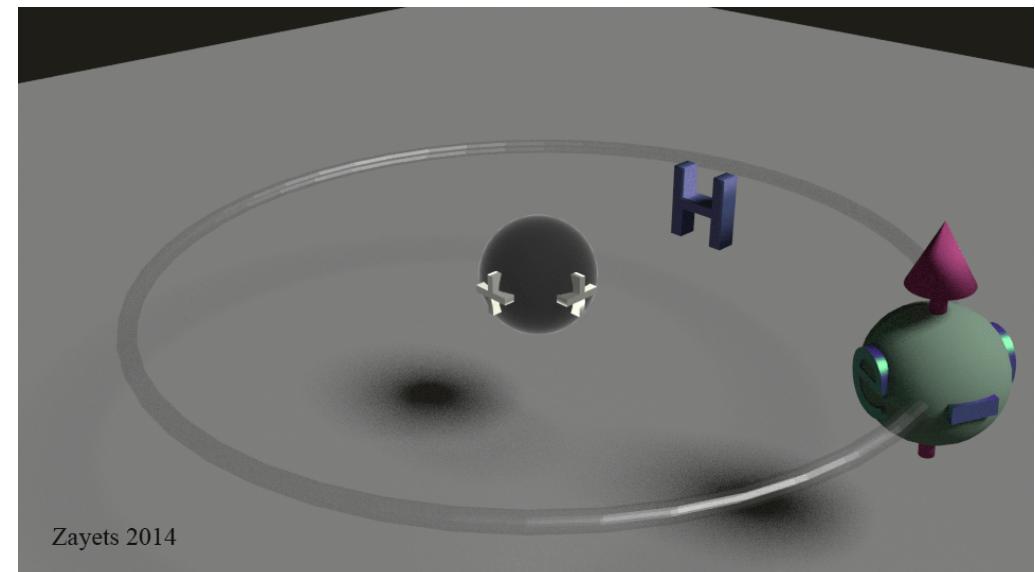
Spin orbit interaction:

- Electronic configuration
- Magnetic anisotropy
- Magnetoresistance
- Magnetoelasticity
- Skyrmions
- ...

Zayets (AIST), Tsukuba, Japan



TU Kaiserslautern



# M-Dynamics at WMI

## (inverse) Spin-orbit torques

MW et al.,  
PRL **113**, 157204 (2014)

Nembach, MW, et al.,  
Nat Phys **11**, 825 (2015)

Berger, MW et al.  
arXiv:1611.05798 (2016)

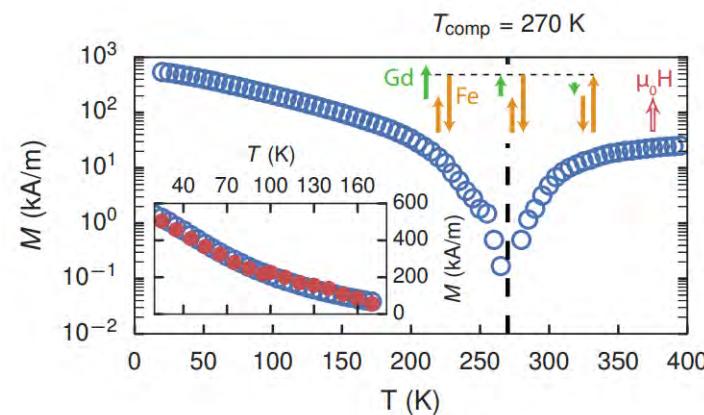
Oshima, MW, et al.,  
Nat Mat (2017)



## Non-collinear spin dynamics

MW et al., arXiv:  
1705.02874 (2017)

Maier-Flaig, MW et al.,  
APL **110**, 132401 (2017).



## Cavity magnetic resonance

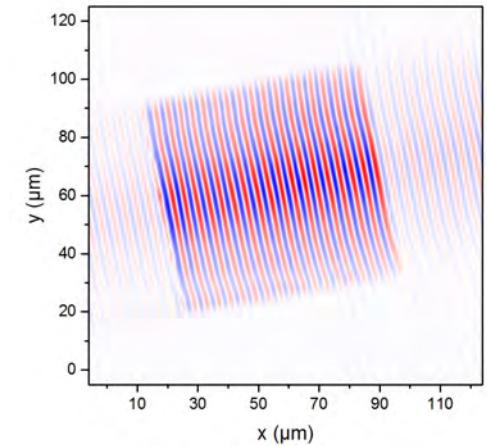
## Broadband magnetic resonance

50mK - 300K, up to 17T, up to 50 GHz

## Hybrid systems

MW et al.,  
PRL **106**, 117601 (2011)

Klingler, MW, et al.  
APL **109**, 072402 (2016)



## Brillouin light scattering

## Frequency-resolved MOKE

Spatial resolution < 1μm

## Materials for M-dynamics

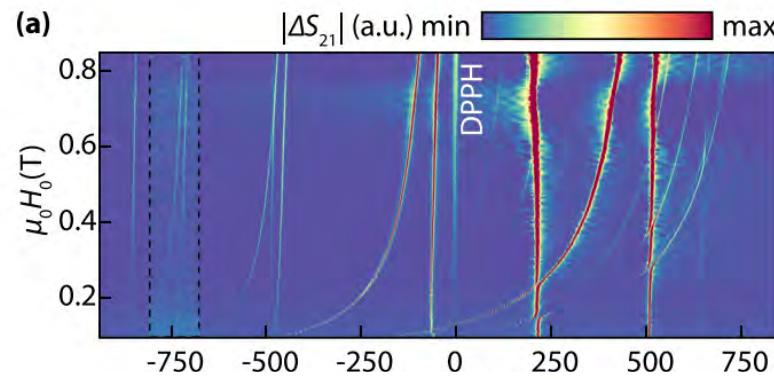
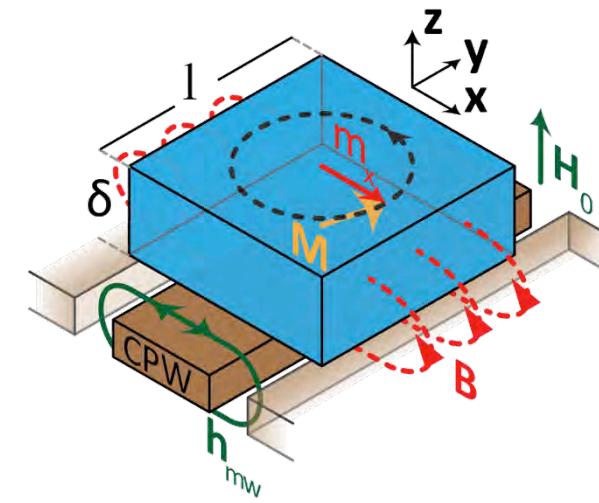
PLD, Evap, Sputter,  
E-beam lithography

# Outline

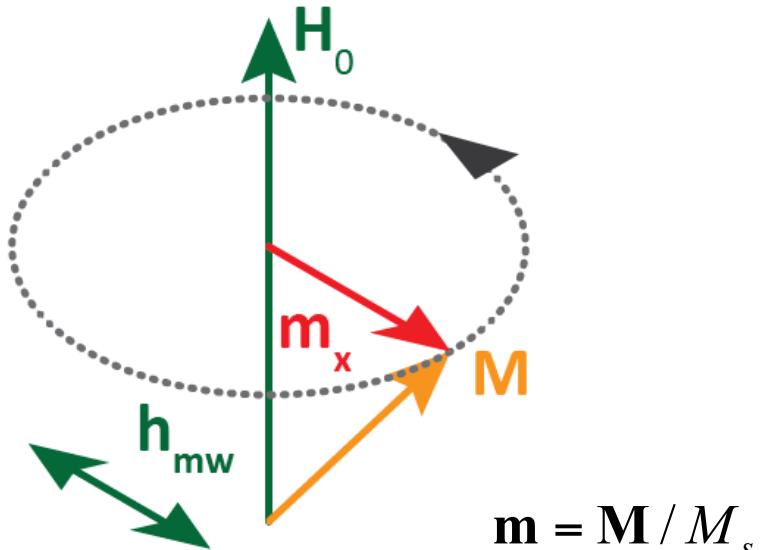
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helimagnonic crystal



# Magnetization dynamics



$$m_x = \chi h_{mw}$$

$$\chi = \chi' + i\chi''$$

Polder susceptibility (tensor)

- Damping
- Anisotropies
- g-factor

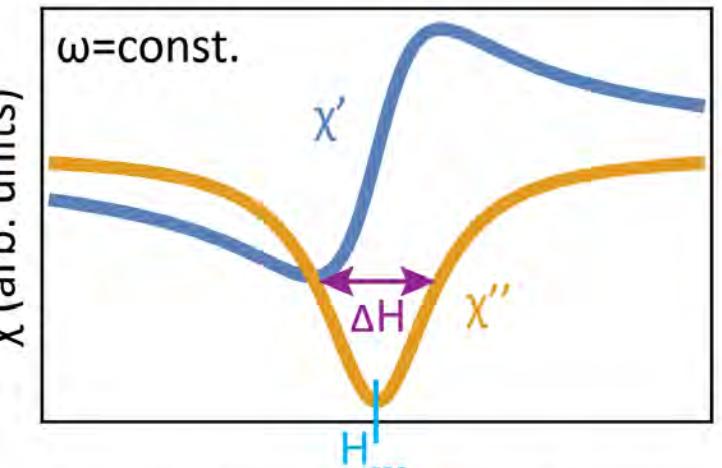
Landau-Lifshitz-Gilbert equation:

$$\frac{\partial \mathbf{m}}{\partial t} = -\gamma \mu_0 \mathbf{m} \times \mathbf{H}_{\text{eff}} + \alpha \mathbf{m} \times \frac{\partial \mathbf{m}}{\partial t}$$

precession    damping

- $\mathbf{M}$ : magnetization vector  
 $\gamma$ : gyromagnetic ratio  
 $\alpha$ : damping  
 $M_s$ : saturation magnetization

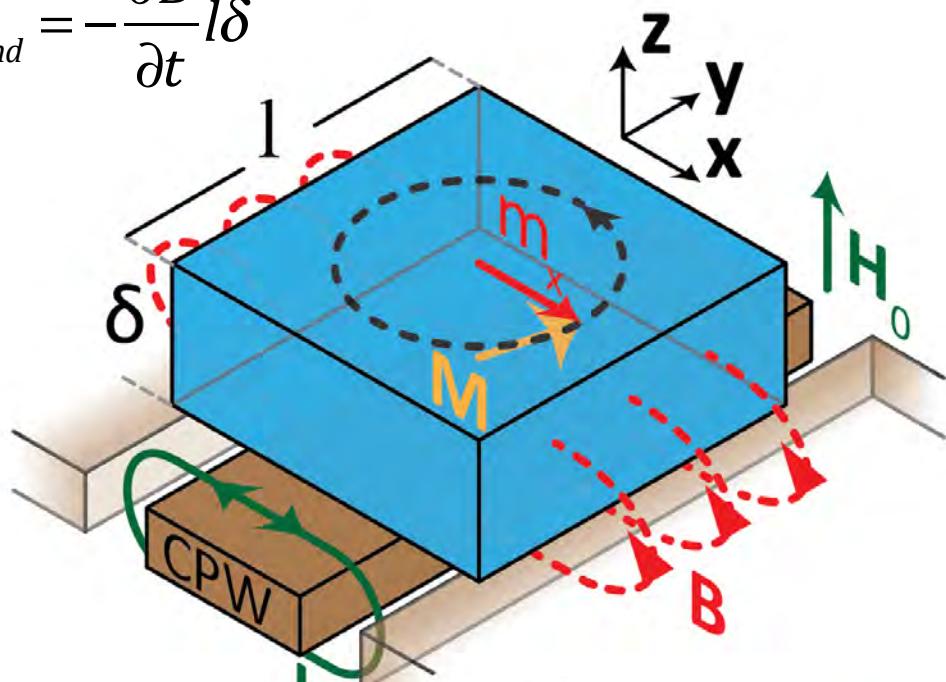
$$\mathbf{H}_{\text{eff}} = \mathbf{H}_0 + \mathbf{H}_{\text{aniso}} + \mathbf{h}_{\text{mw}}$$



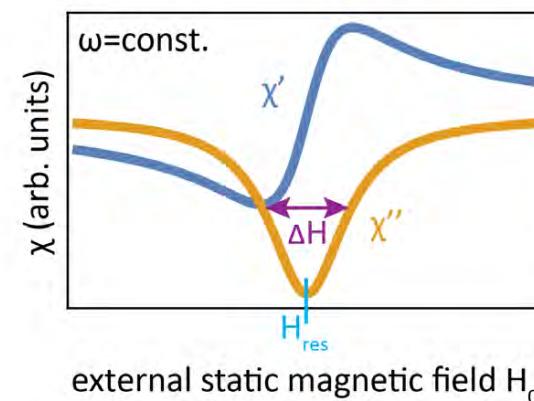
external static magnetic field  $H_0$

# Broadband magnetic resonance spectroscopy

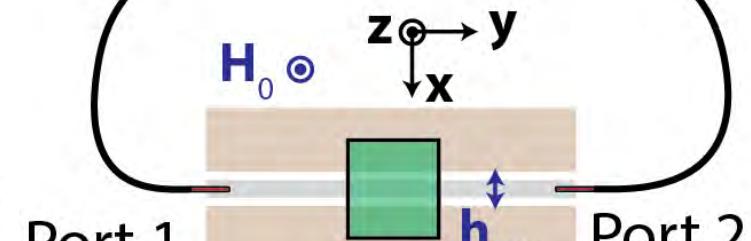
$$V_{ind} = -\frac{\partial B}{\partial t} l \delta$$



$$m_x = \chi h_{mw}$$



Vector Network Analyzer

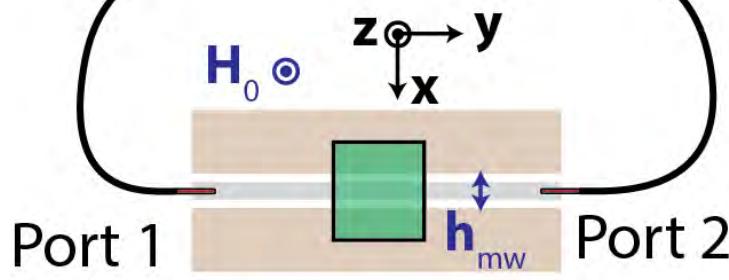


Coplanar waveguide

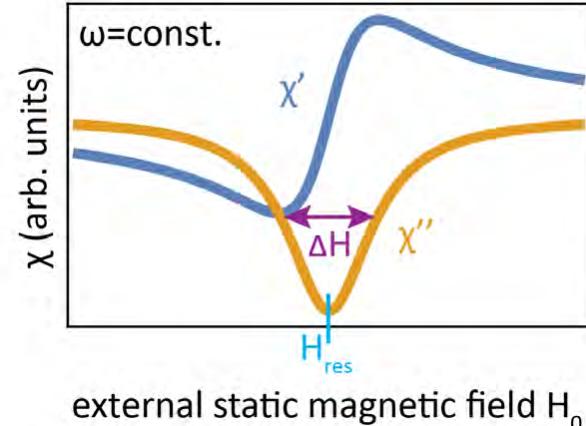
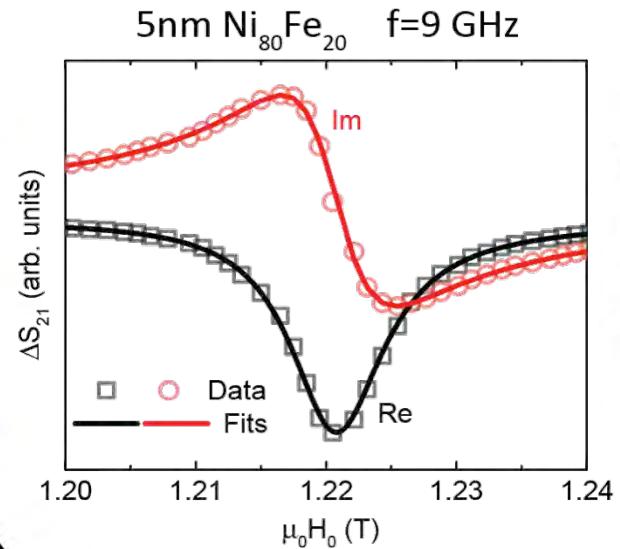
$$S_{21} = \frac{V_2}{V_1} = \frac{V_{ind}(H_0) + V_1}{V_1} \Gamma$$

# Microwave susceptibility measurement

## Vector Network Analyzer



Coplanar waveguide



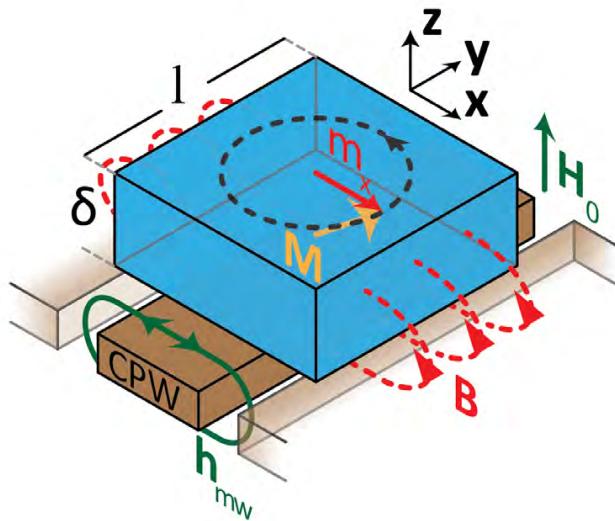
$$\Delta S_{21} = \frac{S_{21}(H_0) - S_{21}^0}{S_{21}^0}$$

$$\text{fit } \Delta S_{21} = -\frac{i\omega \tilde{L}}{2Z_0} \chi$$

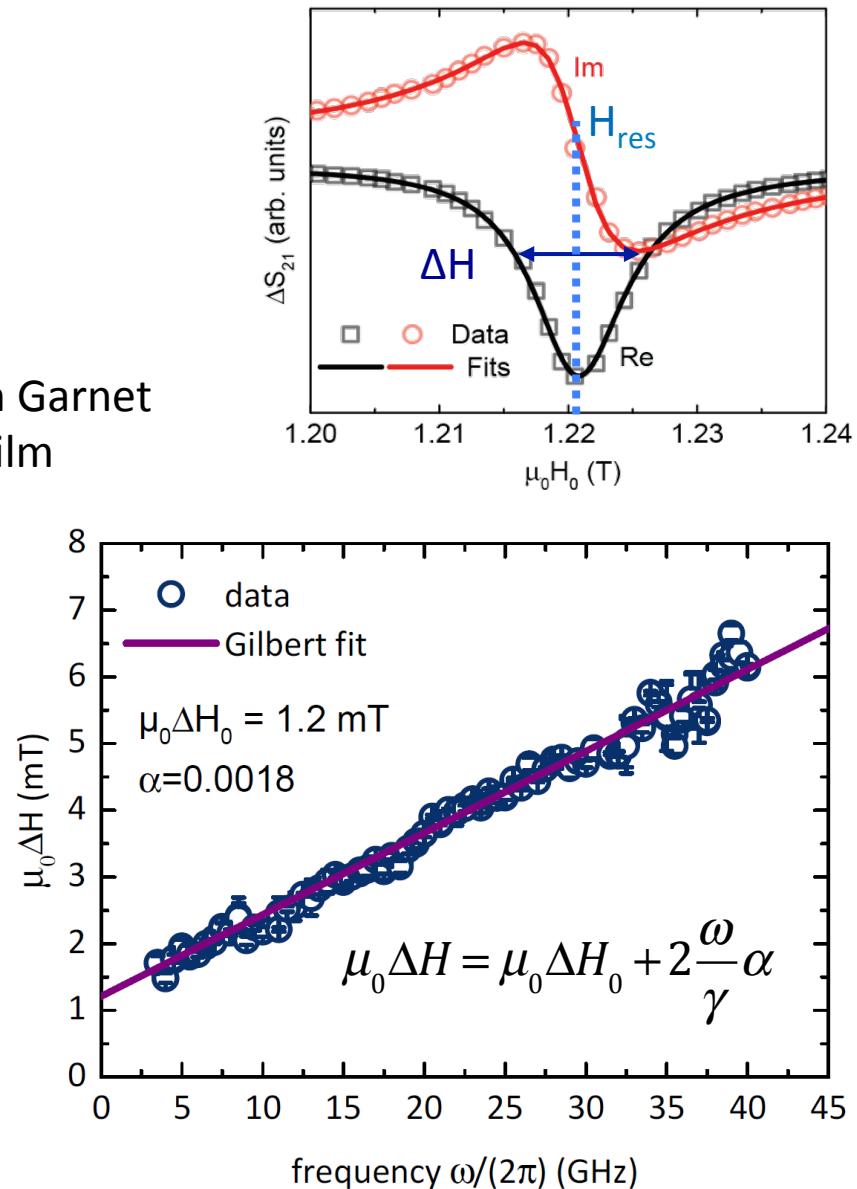
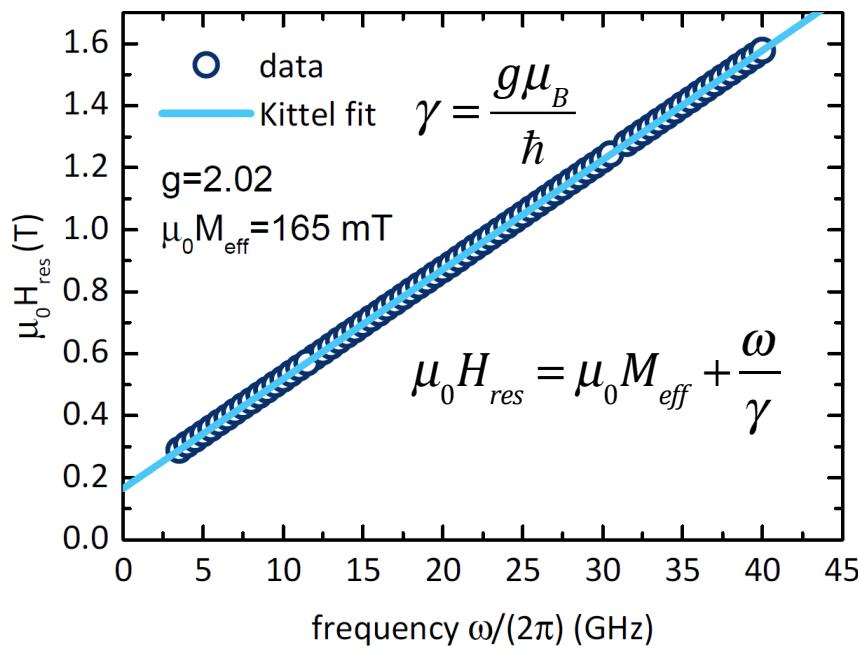
$$\tilde{L} = \mu_0 \frac{l\delta}{4W_{CPW}}$$

$$Z_0 = 50\Omega$$

# Anisotropy and Damping



Yttrium Iron Garnet  
PLD 20nm film

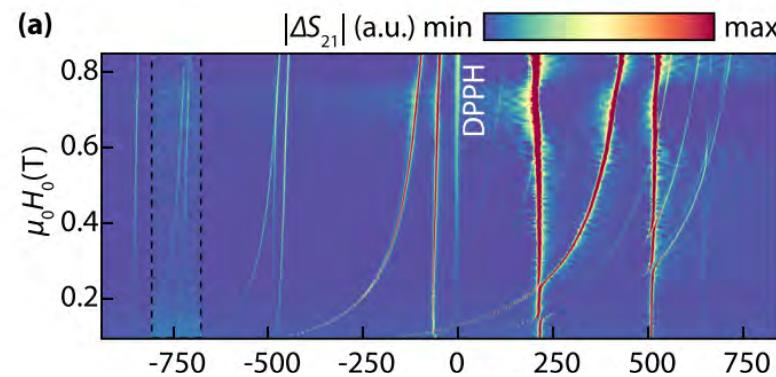
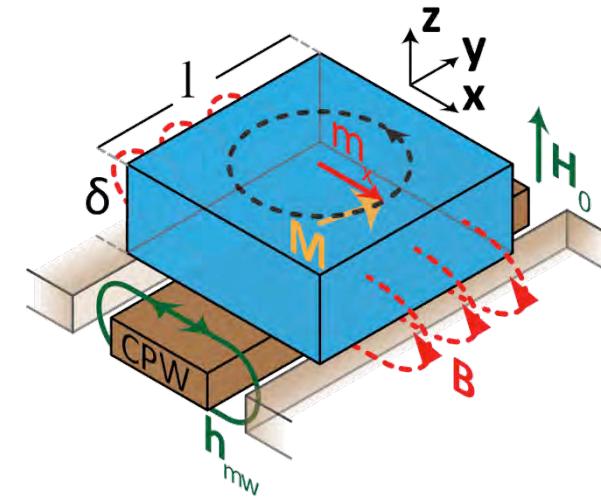


# Outline

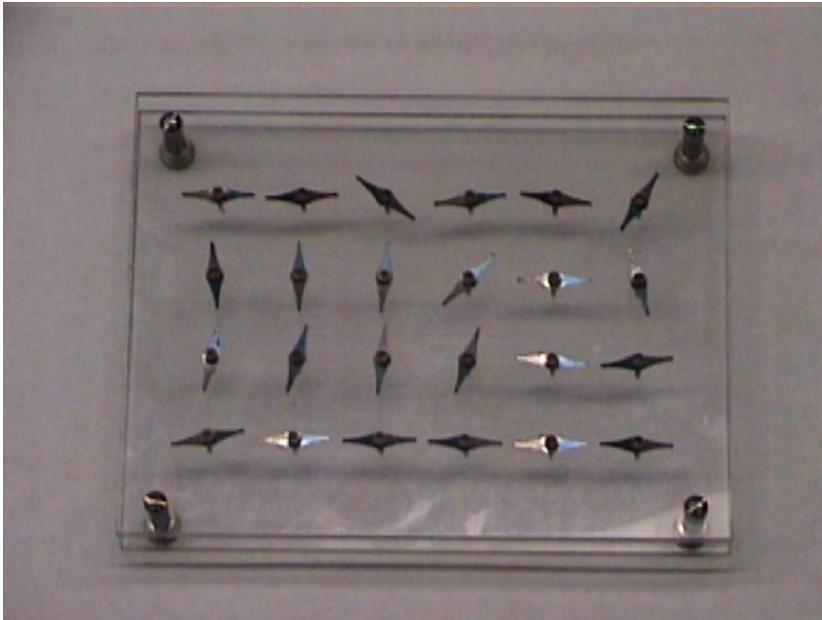
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$\text{Cu}_2\text{OSeO}_3$  as a natural  
helimagnonic crystal



# Magnetostatic modes: Theory



- Long-ranged dipolar interaction
- Sample-shape dependend
- Complicated

We are interested in dynamics  
with dipolar interactions!

Start with LL equation (no damping):

$$\partial \mathbf{m} / \partial t = -\gamma \mu_0 \mathbf{J} \times \mathbf{H}_{\text{eff}}$$

Linearized LL equation for a spherical sample:

$$i\omega \mathbf{m} = -\gamma \mu_0 [1 \times (\mathbf{M}_s \cdot \mathbf{h} - (H_0 + M_s N_z) \mathbf{m})]$$

$$N_z = 1/3$$

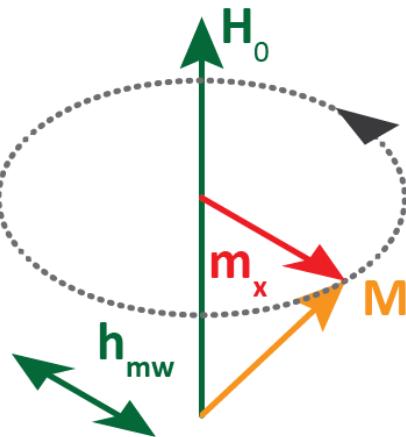
Solve with:

$$\nabla \times \mathbf{h} = 0$$

$$\nabla \cdot (\mathbf{h} + \mathbf{m}) = 0$$

$$n + 1 + \xi_0 \frac{dP_n^m(\xi_0)/d\xi_0}{P_n^m(\xi_0)} \pm m\nu = 0$$

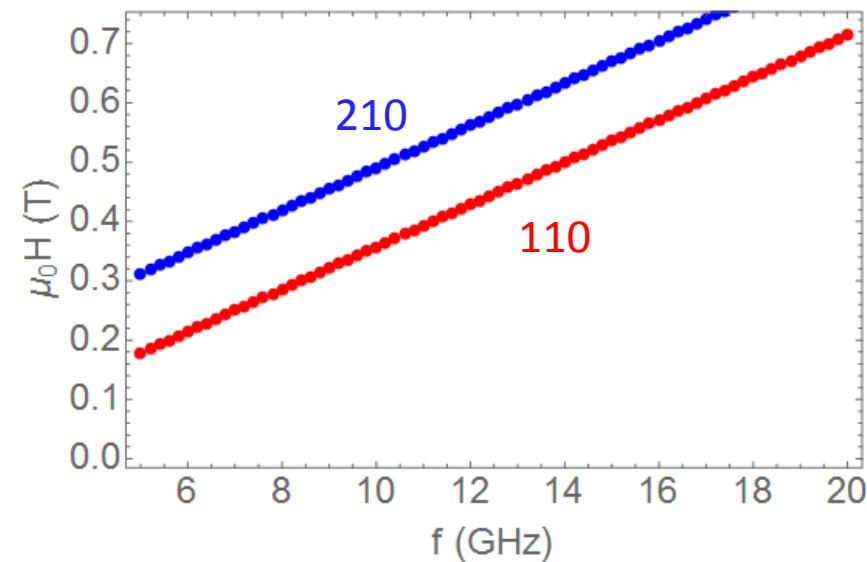
# Magnetostatic modes: Theory



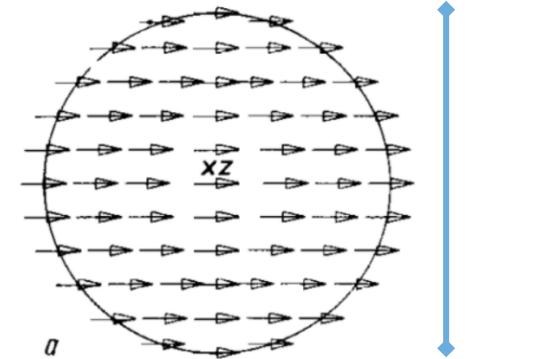
Modes are independent of  
actual sample size!

„Uniform, Kittel, FMR“

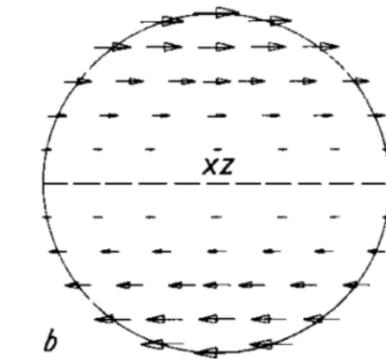
Our question:  
What about damping?



Dynamic  $m_x$

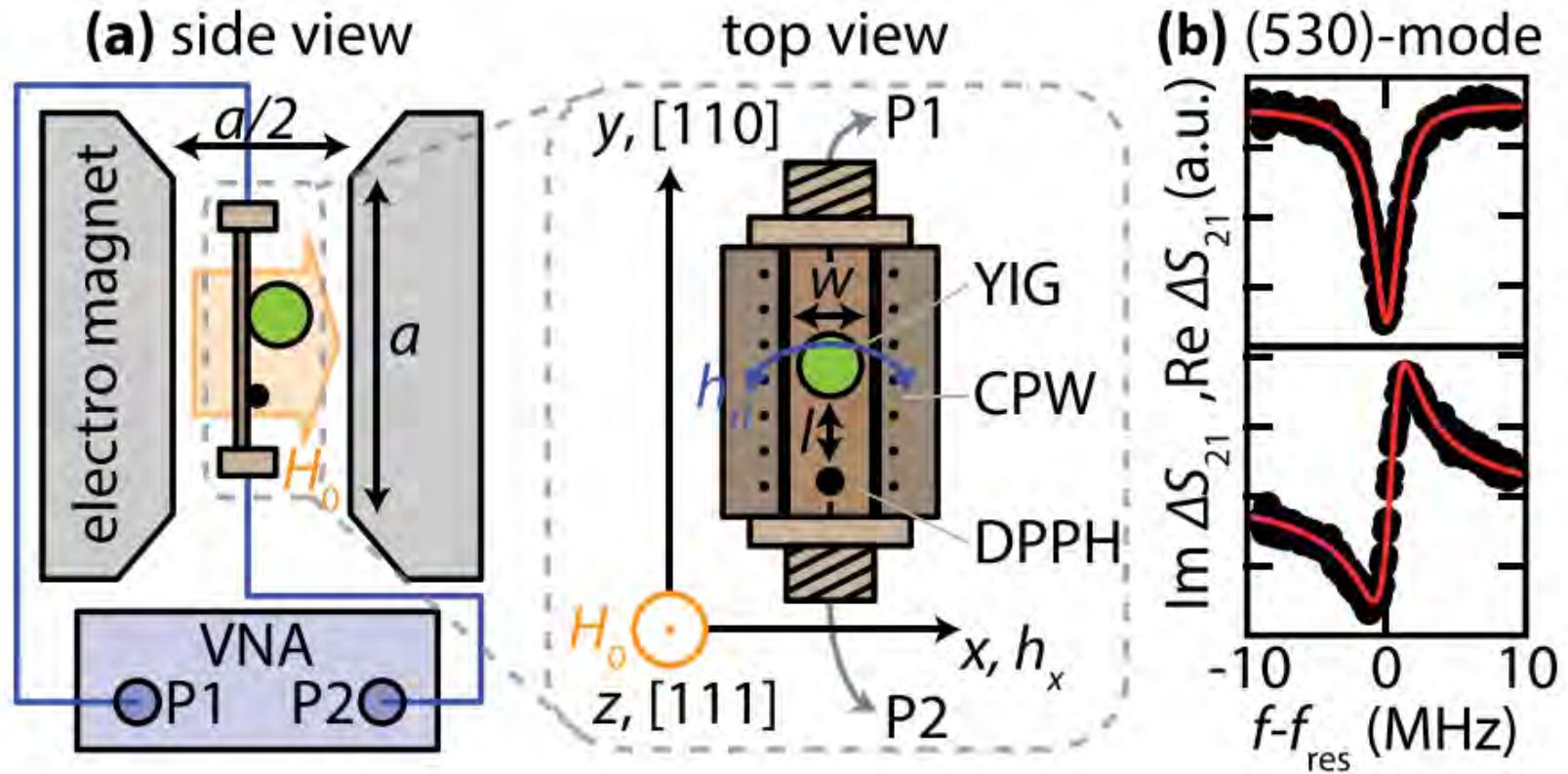


210



Mode numbering  $nmr$   
 $n$ : Surface localization  
 $m$ : angular-momentum  
 $r$ : enumerate solutions

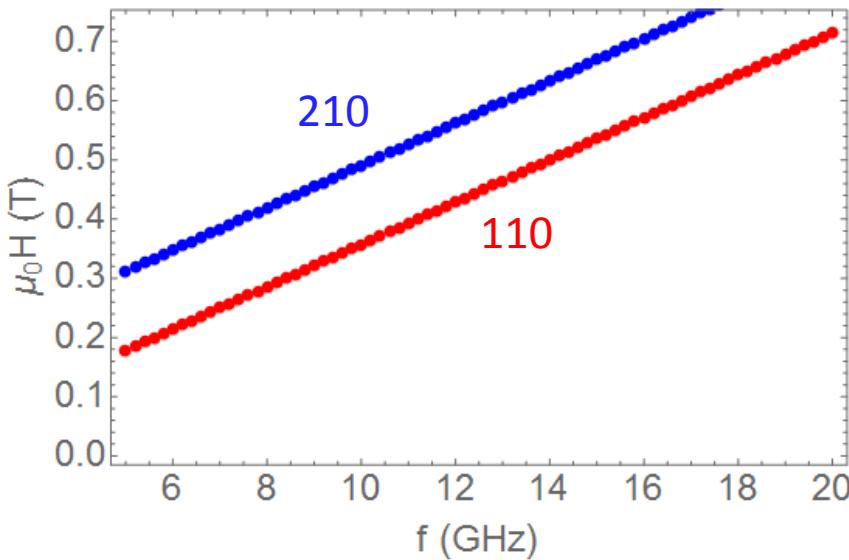
# Experimental setup



300 $\mu\text{m}$  YIG sphere grown by Innovent  
300 $\mu\text{m}$  center conductor

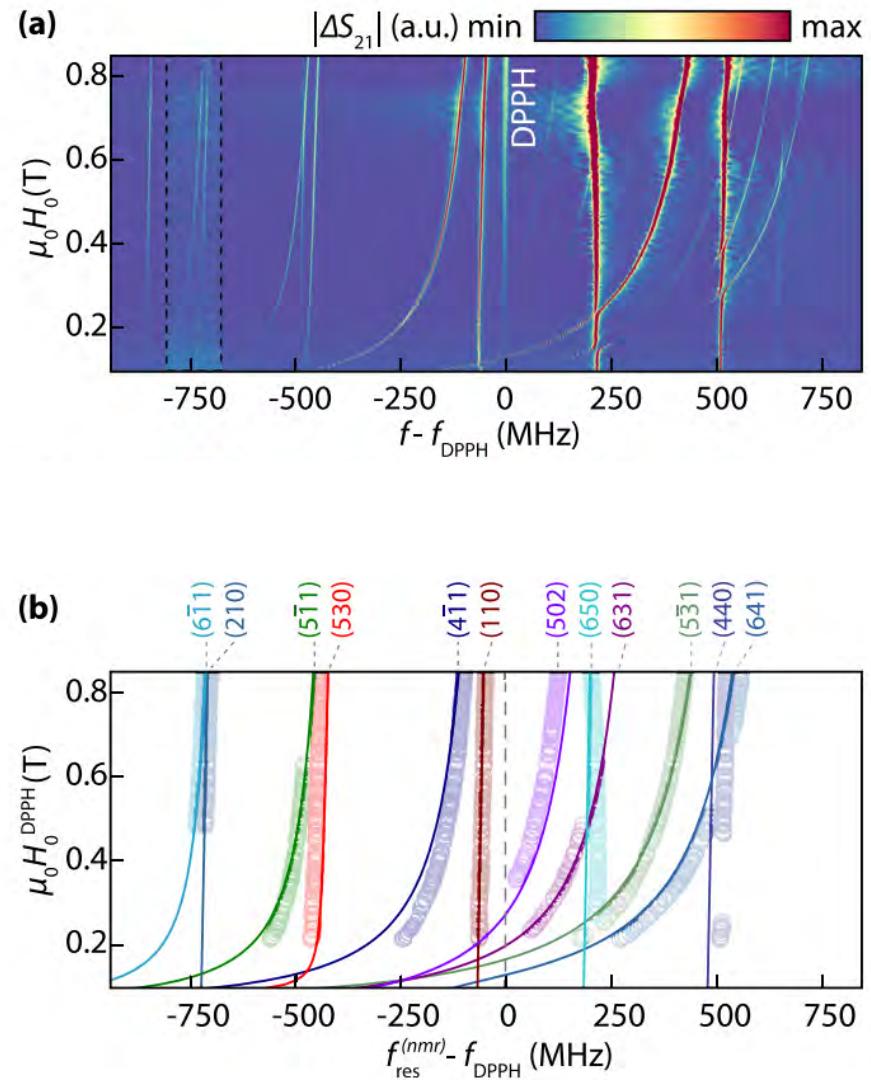
Non-uniform driving field required for excitation of MSMs

# Mode identification

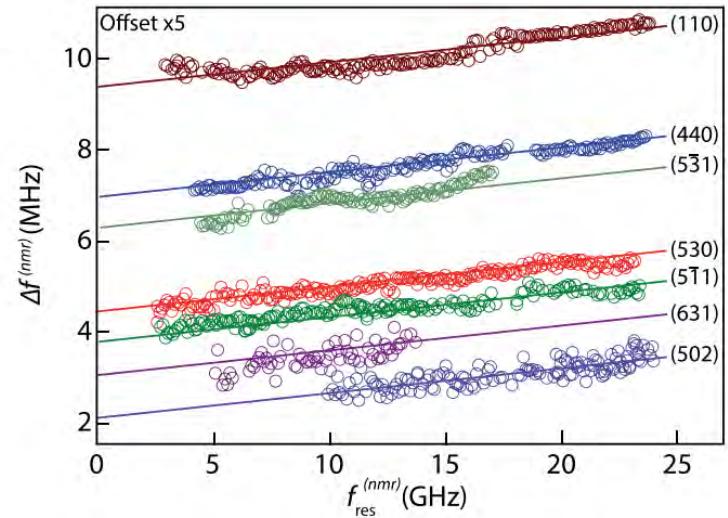
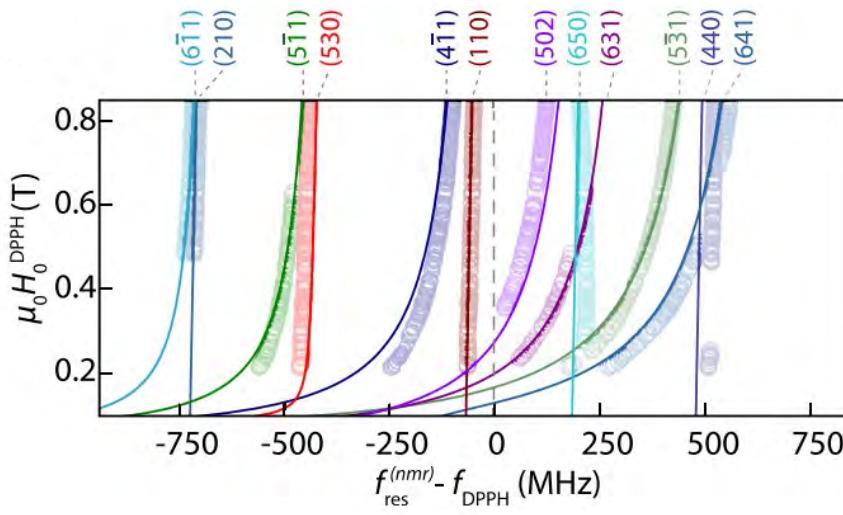


Mode intensity: overlap integral of driving field and MSM

DPPH is used for absolute field calibration



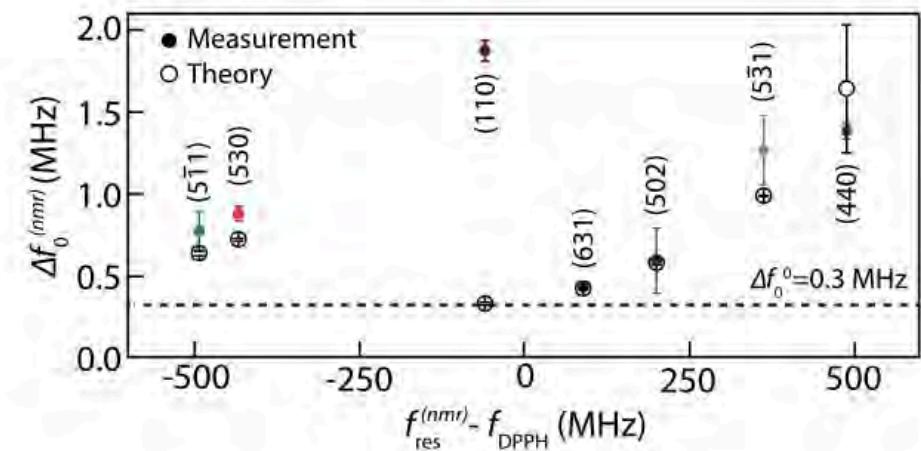
# Linewidth and damping



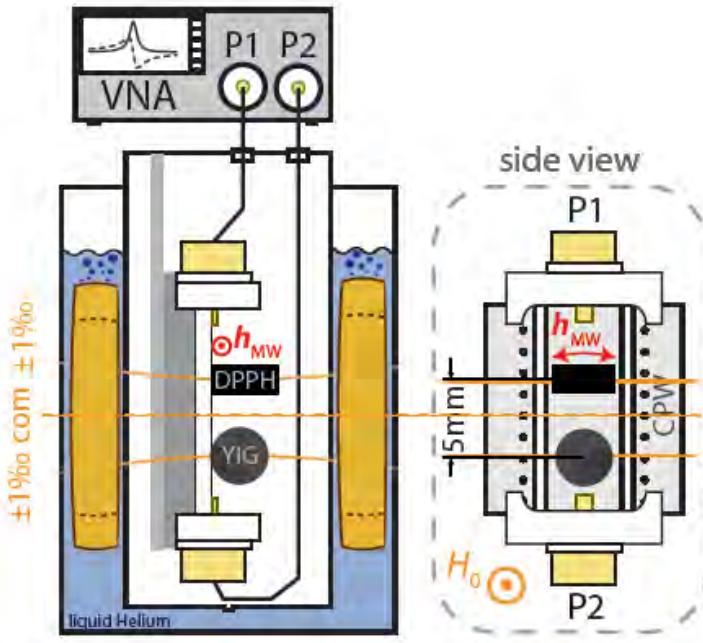
Record-low damping for Yttrium Iron Garnet (or any material)

$$\alpha = \Delta f - \Delta f^0 / 2 f_{\text{res}} = 3 \times 10^{-5}$$

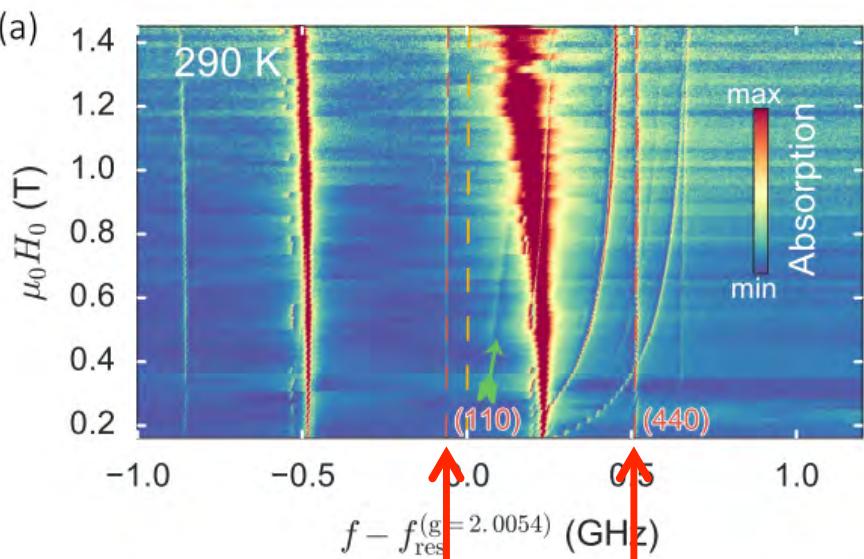
Inhomogeneous broadening from surface pit scattering



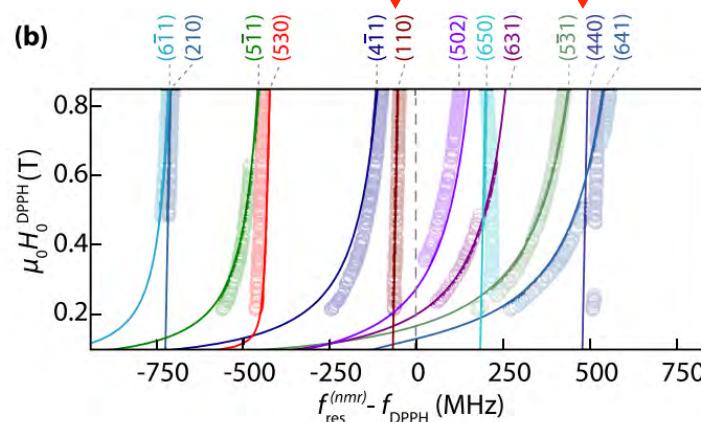
# Temperature-dependent damping in YIG



Same sample: now mounted in magnet cryostat



Maier-Flaig, MW et al., PRB **95**, 214423 (2017).

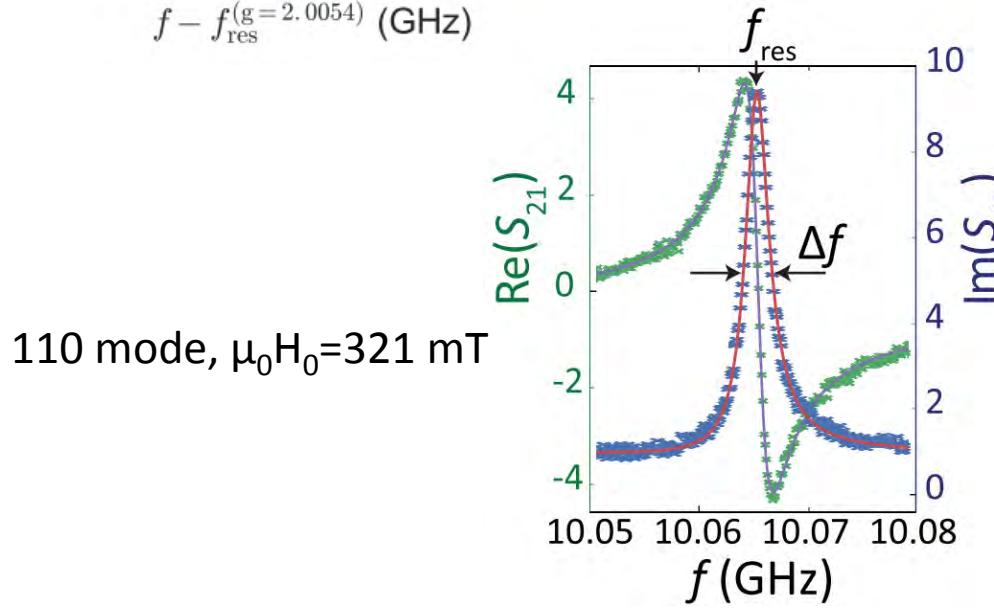
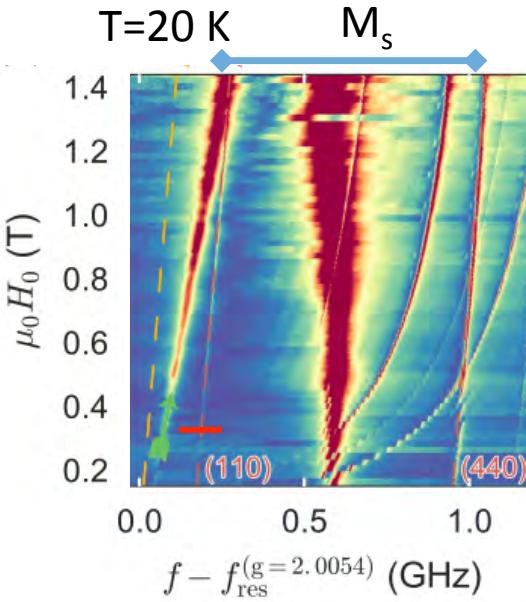


Thin film damping vs temperature:

M. Haidar et al., JAP **117**, 17D119 (2015)

C. L. Jermain et al., Phys. Rev. B **95**, 174411 (2017).

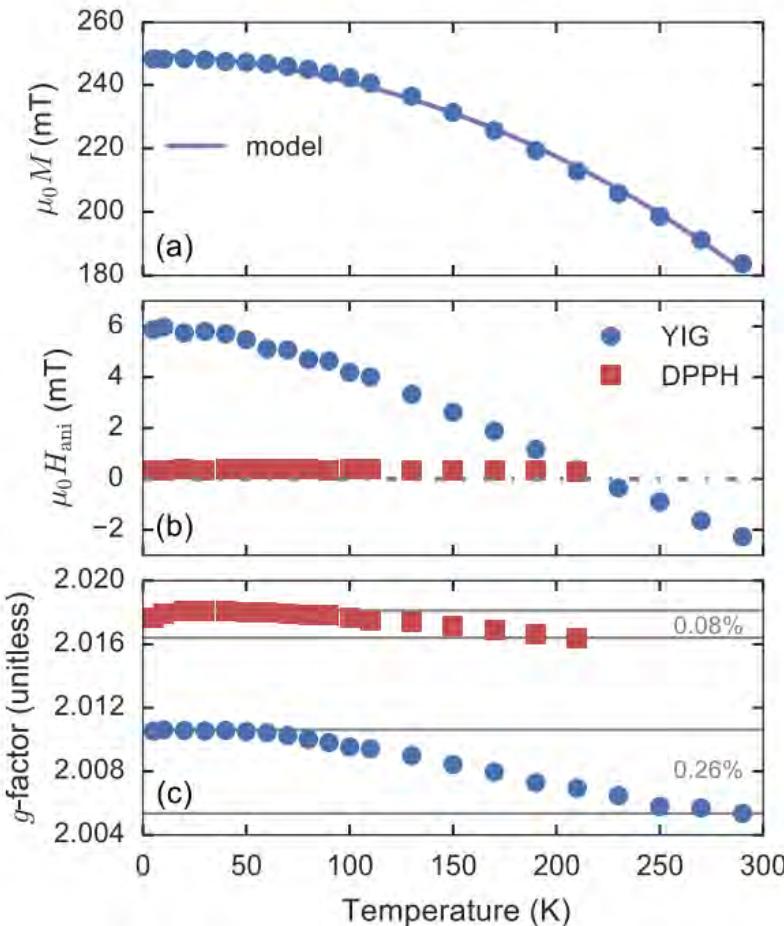
# Resonance frequency



$$\omega_{\downarrow \text{res} \uparrow 110} = \mu_0 \gamma (H \downarrow 0 + H \downarrow \text{ani})$$

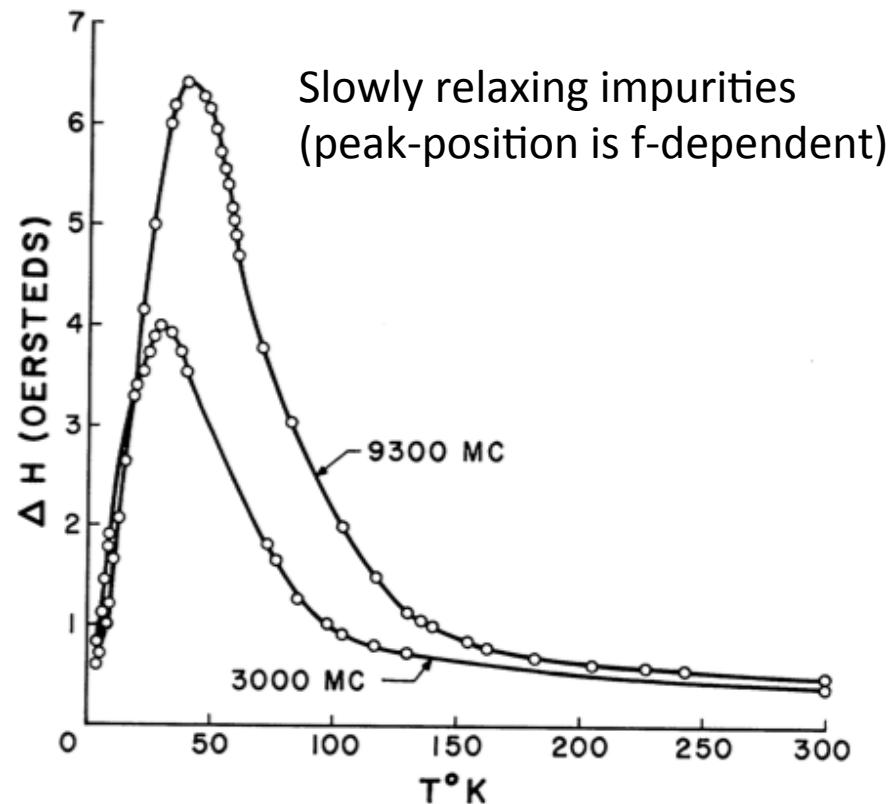
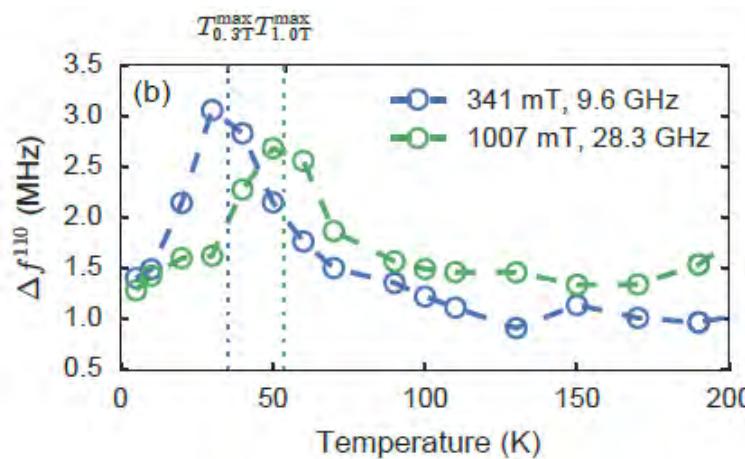
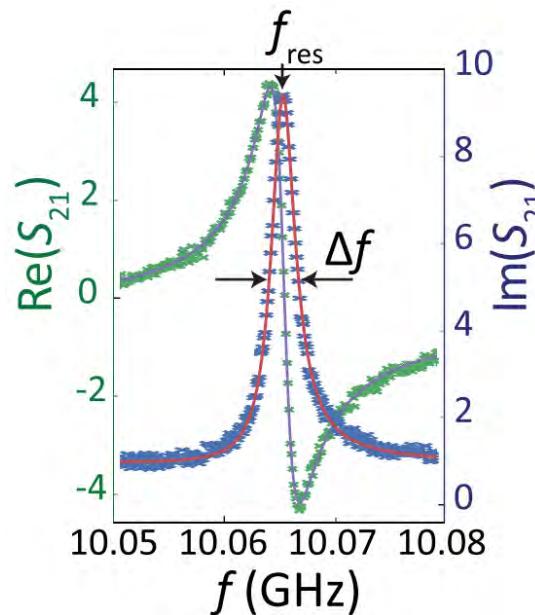
$$\omega_{\downarrow \text{res} \uparrow 440} = \mu_0 \gamma (H \downarrow 0 + H \downarrow \text{ani} + M \downarrow s / 9)$$

$$\omega_{\downarrow \text{res} \uparrow \text{DPPH}} = \mu_0 \gamma H \downarrow 0$$



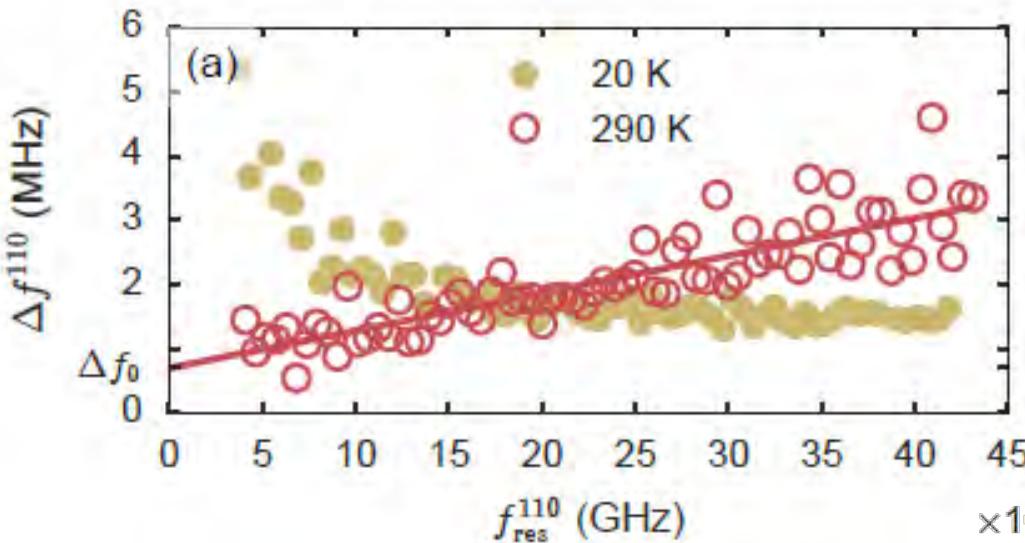
# Linewidth

110 mode:



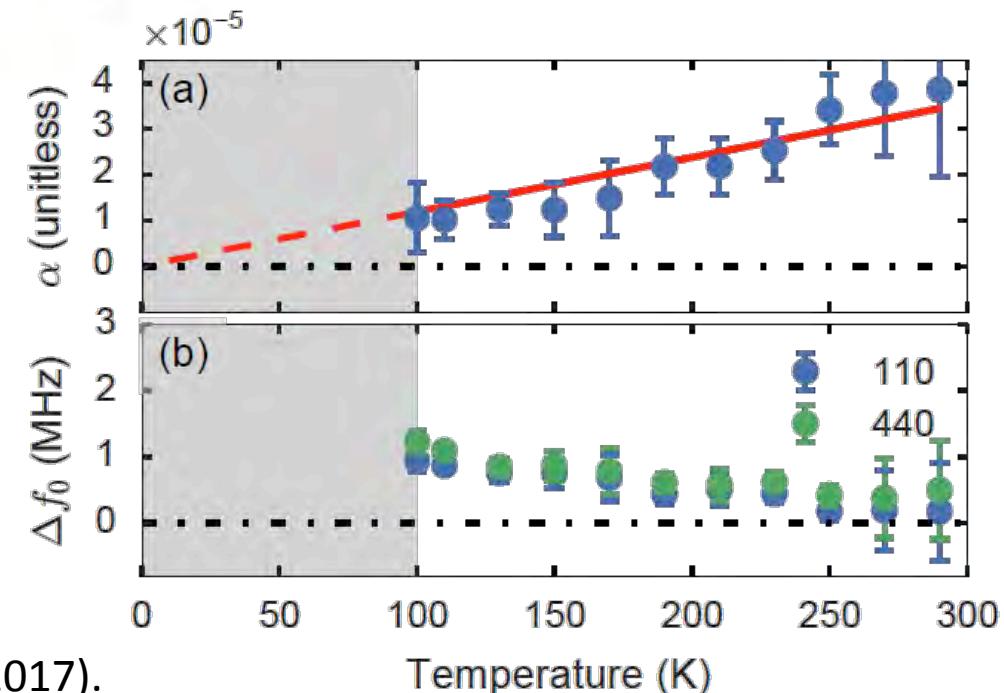
E. G. Spencer, R. C. LeCraw, and A. M. Clogston, Phys. Rev. Lett. **3**, 32 (1959).

# Damping



$$\Delta f = 2\alpha f \downarrow_{\text{res}} + \Delta f \downarrow 0$$

- Room temperature damping confirmed
- Damping decreases for low T

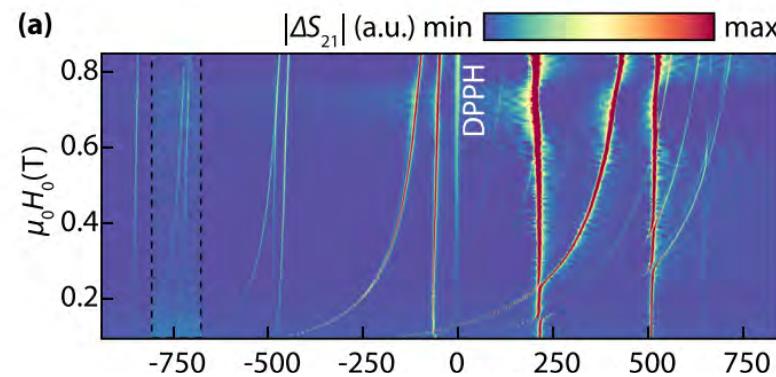
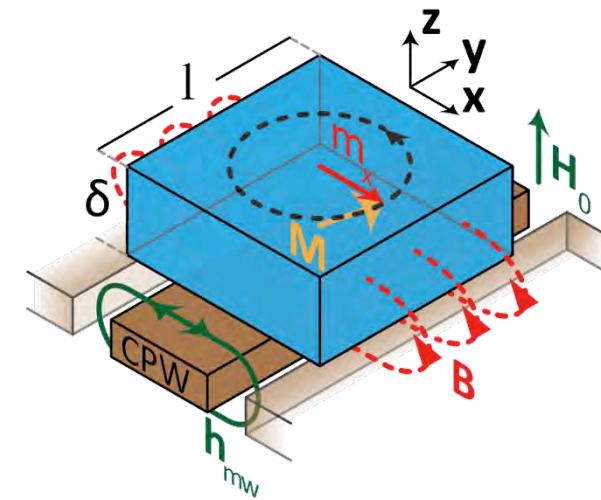


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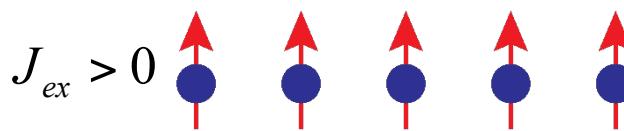


# Dzyaloshinskii-Moriya interaction

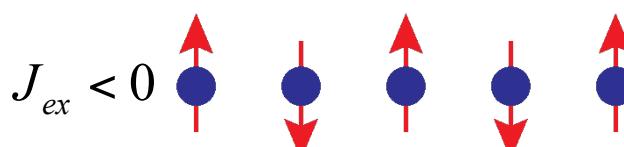
Heisenberg exchange

$$H_H = -J_{ex} \mathbf{S}_1 \cdot \mathbf{S}_2$$

$$J_{ex} \propto A$$



parallel

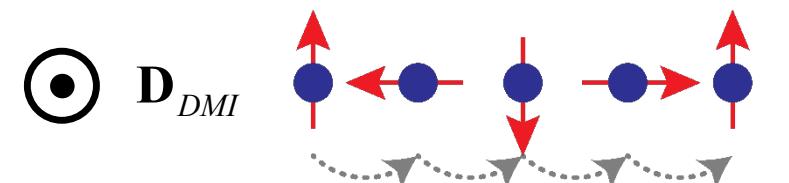


antiparallel

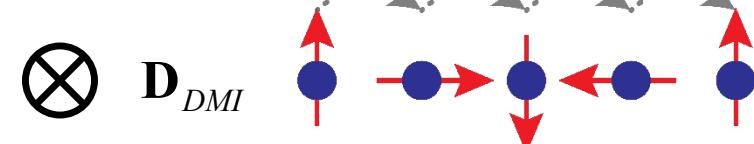
Dzyaloshinskii-Moriya exchange

$$H_{DM} = -\mathbf{D}_{DMI} \cdot (\mathbf{S}_1 \times \mathbf{S}_2)$$

Broken inversion symmetry  
Spin-orbit interaction

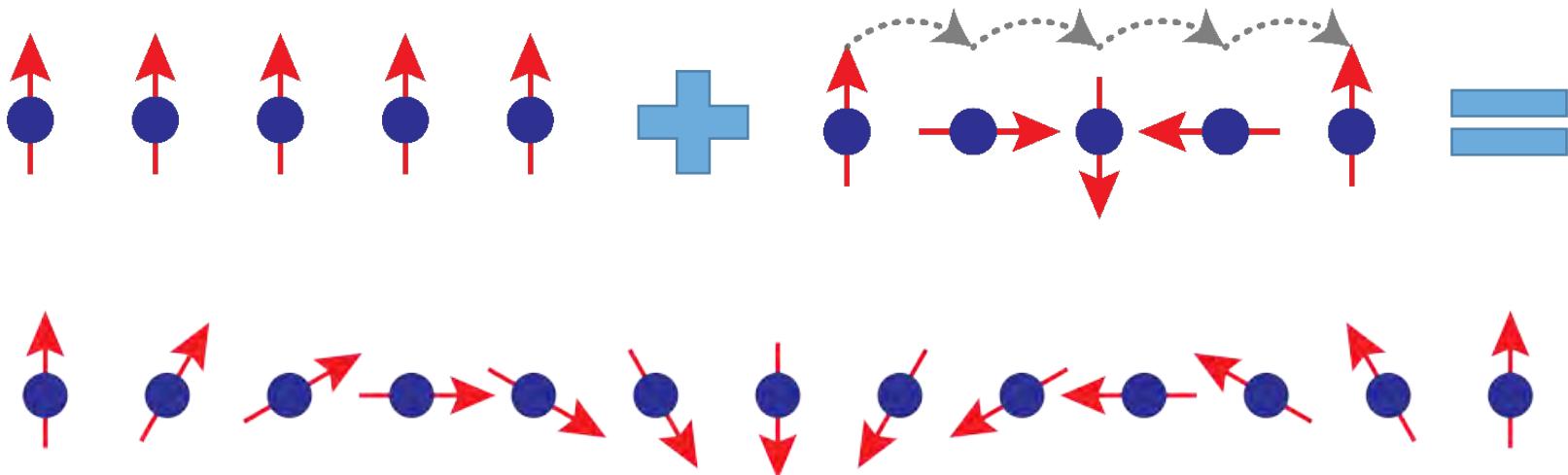


Orthogonal (counterclockwise)



Orthogonal (clockwise)

# Chiral magnetic ordering



Non-collinear equilibrium spin ordering!

Lengthscale about 10nm-100nm

# Dynamics of the chiral magnet $\text{Cu}_2\text{OSeO}_3$

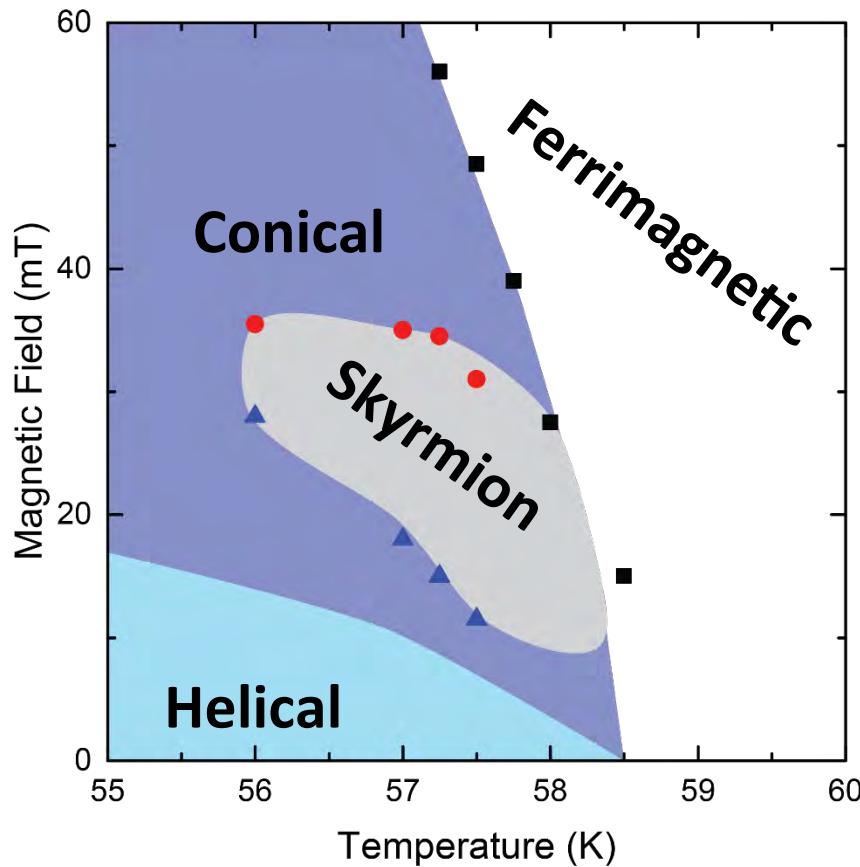
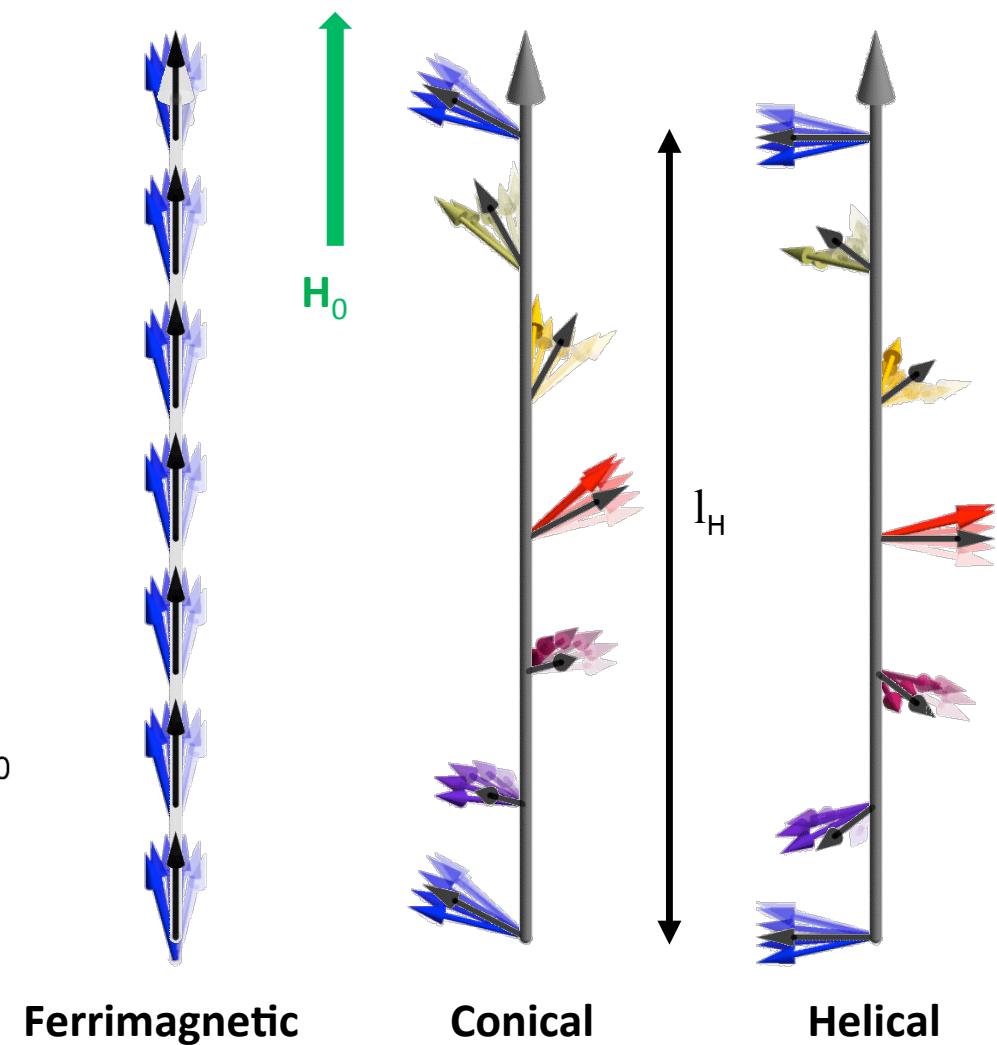
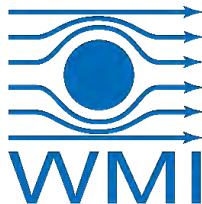


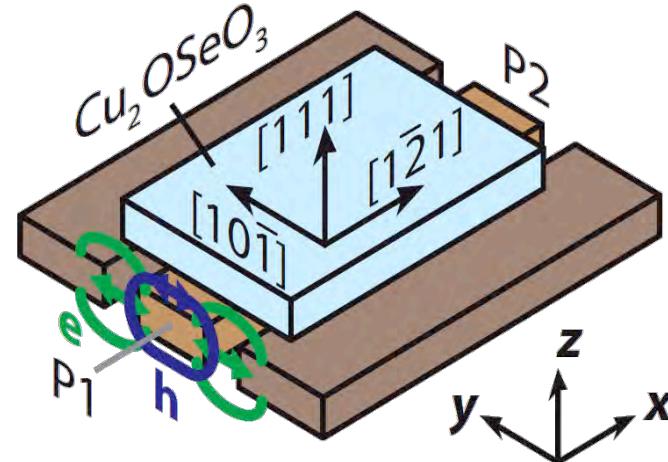
Image: K. Everschorr-Sitte



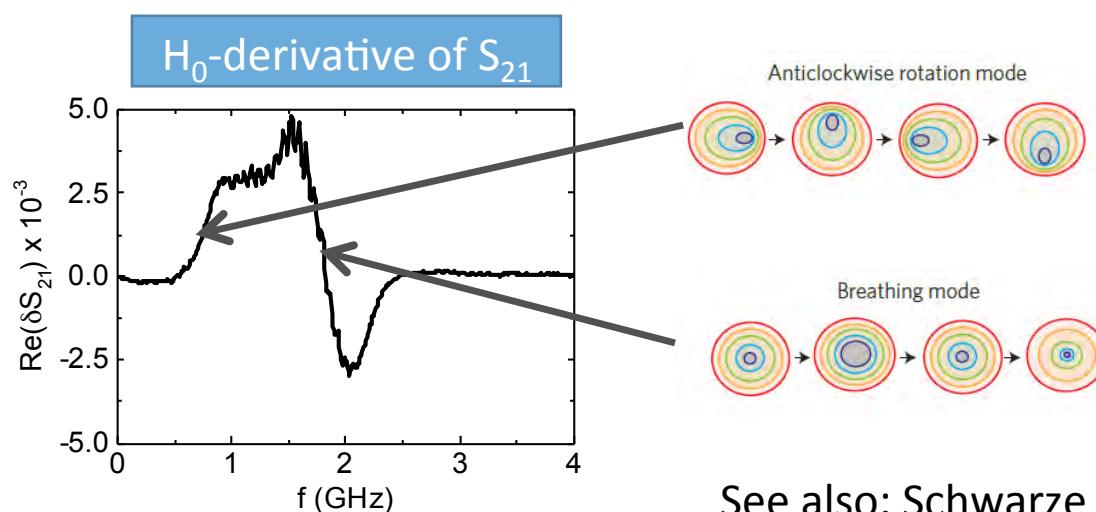
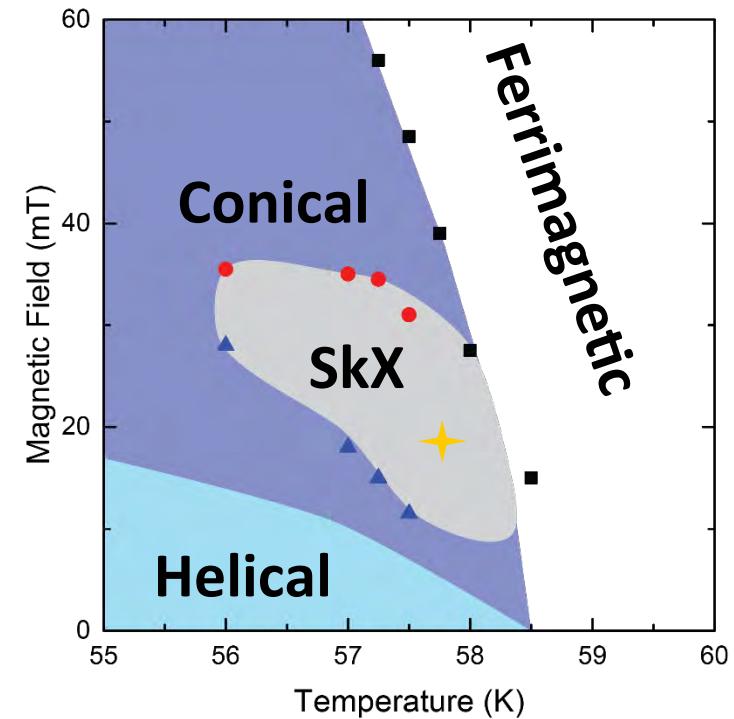
See also: Schwarze et al., Nat. Mat. 14, 478 (2015)



# Skyrmion resonance at T=57K



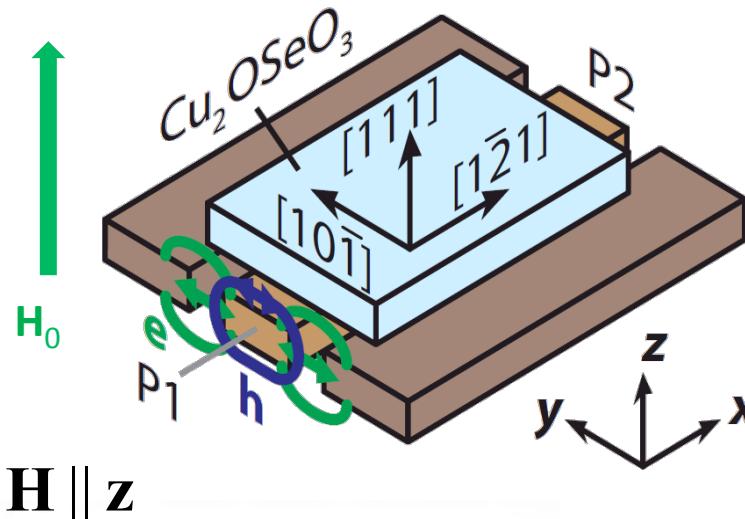
$$\delta S_{21}(f, H_0) \equiv \frac{S_{21}(f, H_0 + \delta H_0) - S_{21}(f, H_0 - \delta H_0)}{S_{21}(f, H_0)}$$



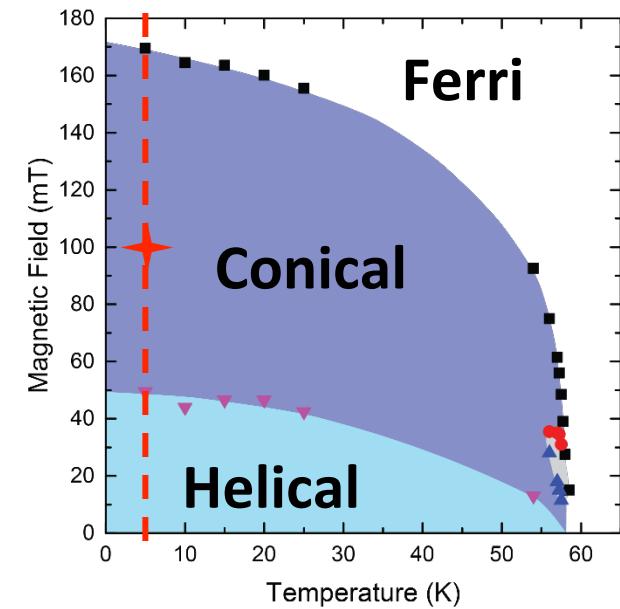
See also: Schwarze et al., Nat. Mat. 14, 478 (2015)



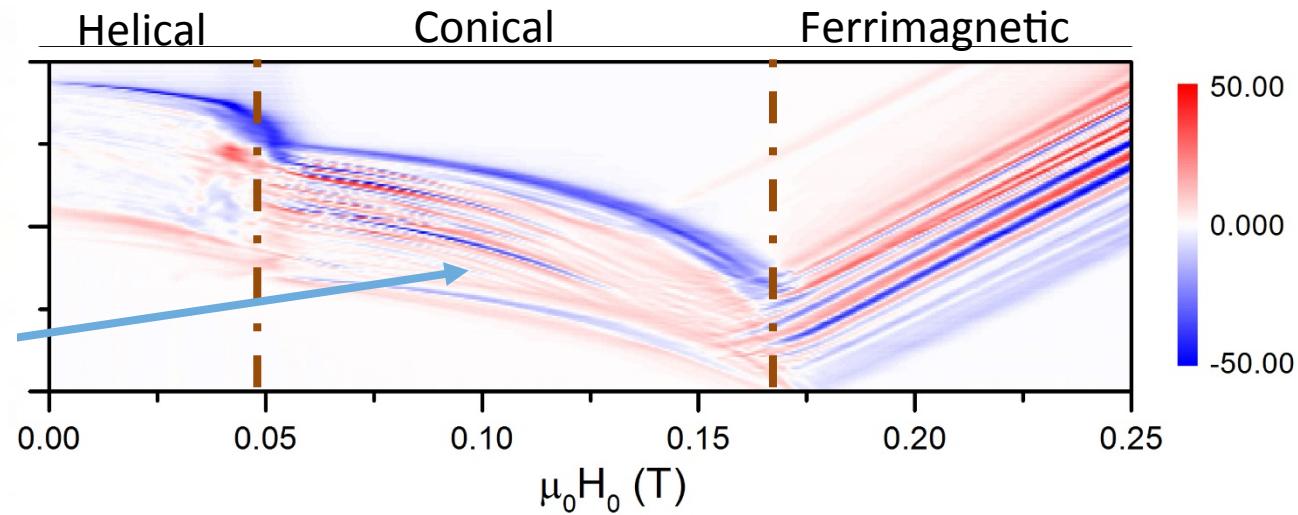
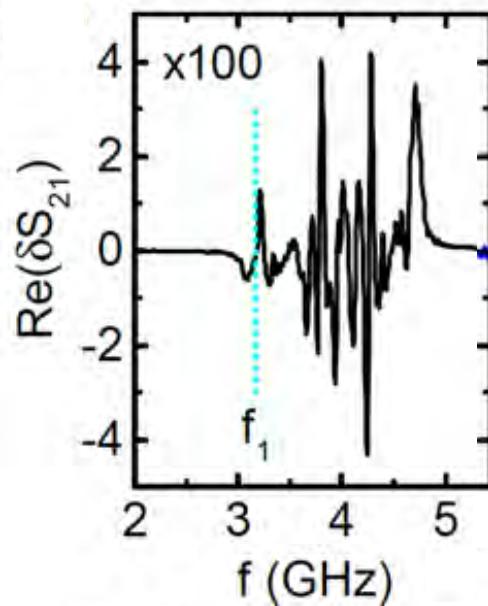
# Chiral magnetic excitations



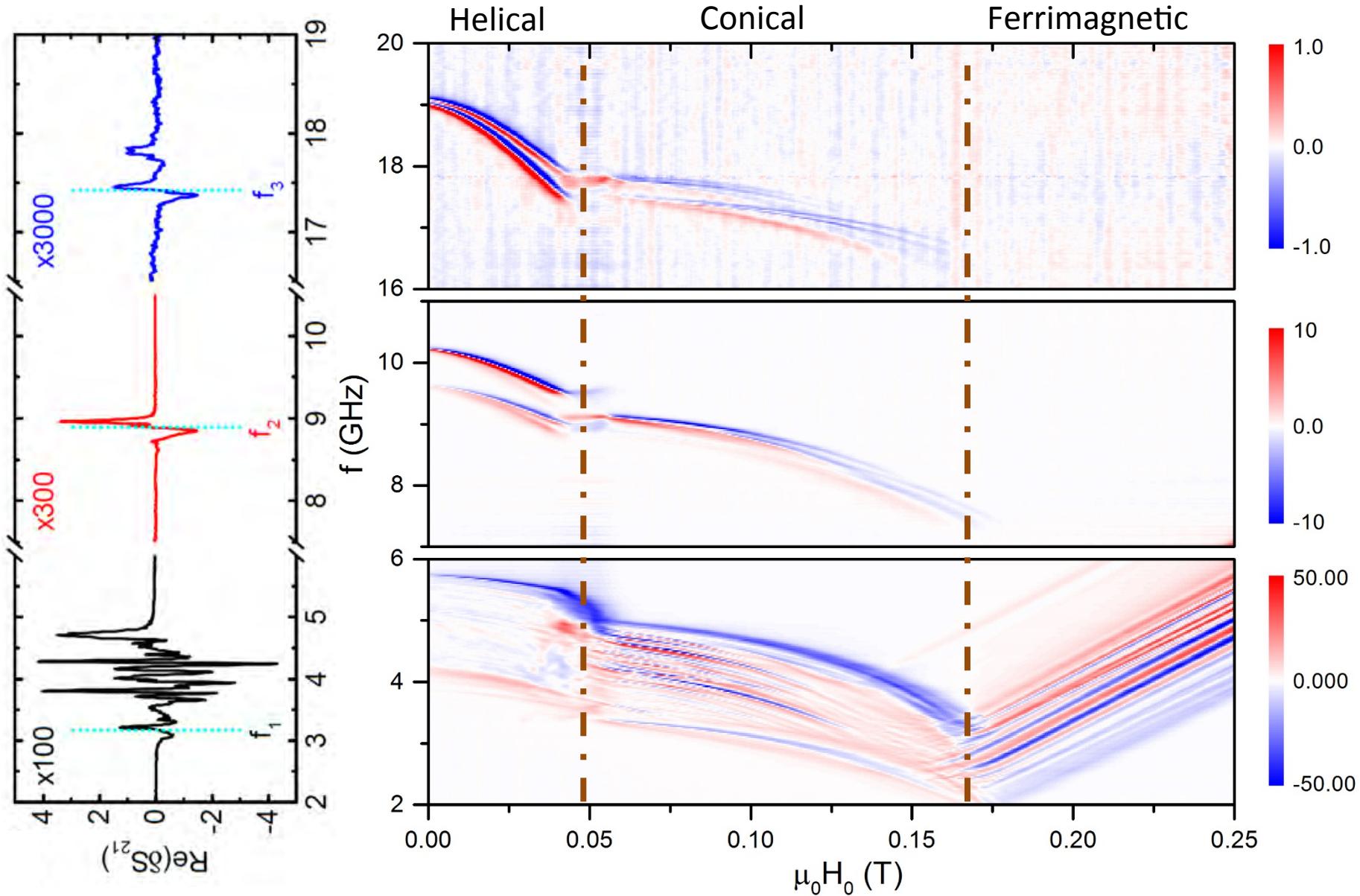
$T = 5\text{K}$   
 $\mu_0 H = 100\text{mT}$



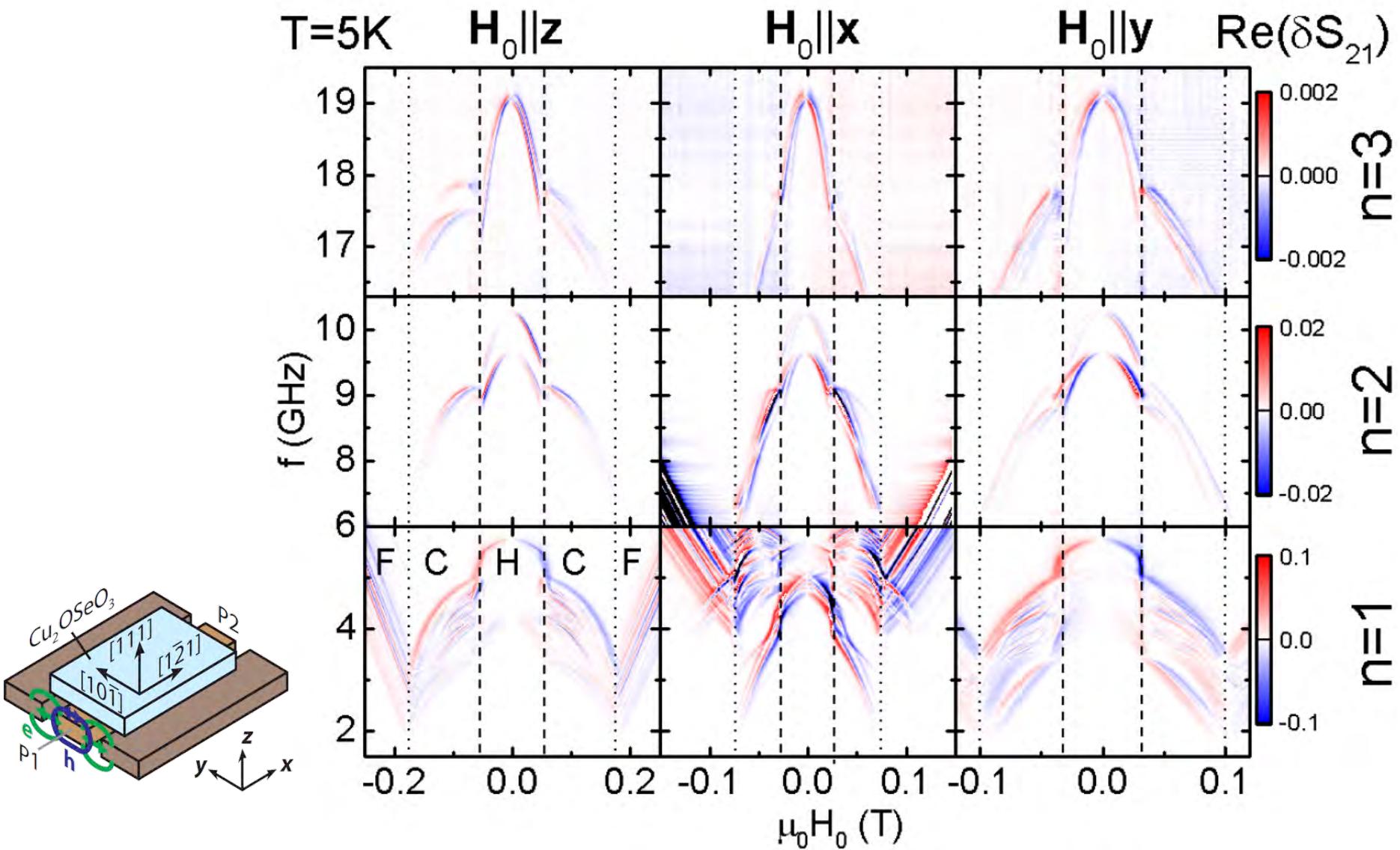
See also: Schwarze et al.,  
Nat. Mat. 14, 478 (2015)



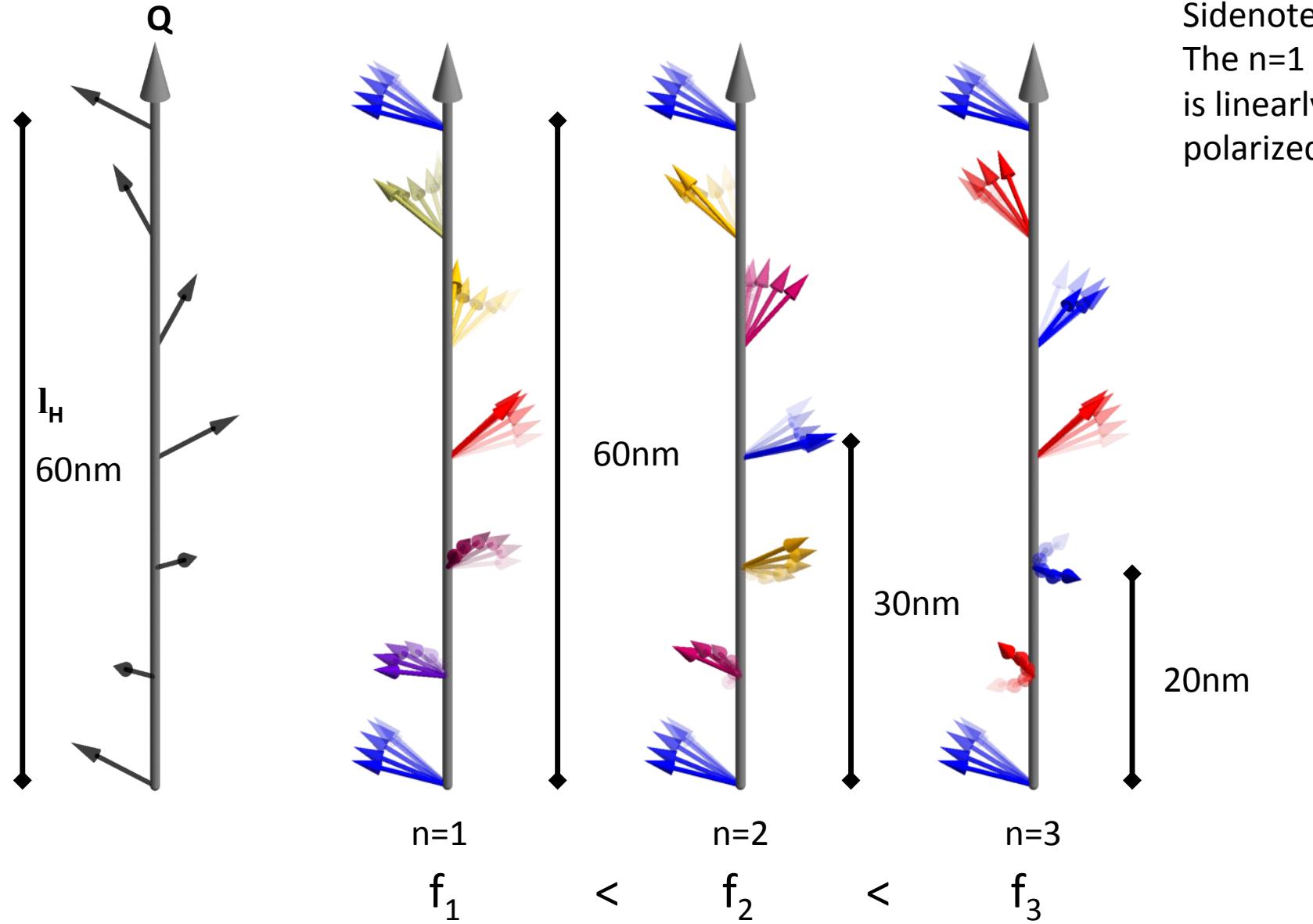
# Chiral magnetic excitations



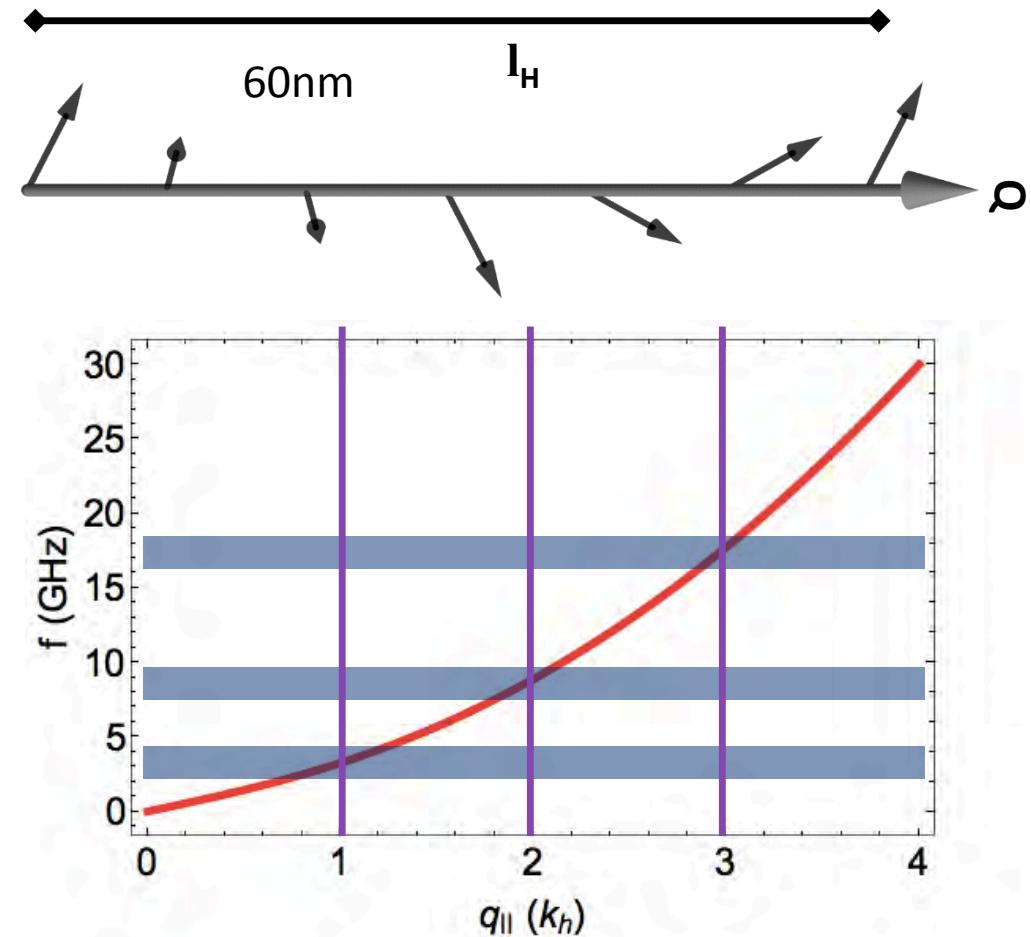
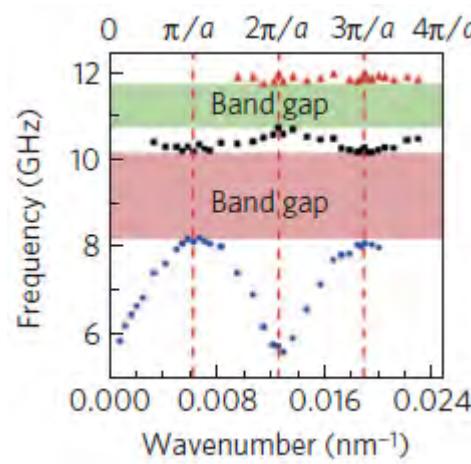
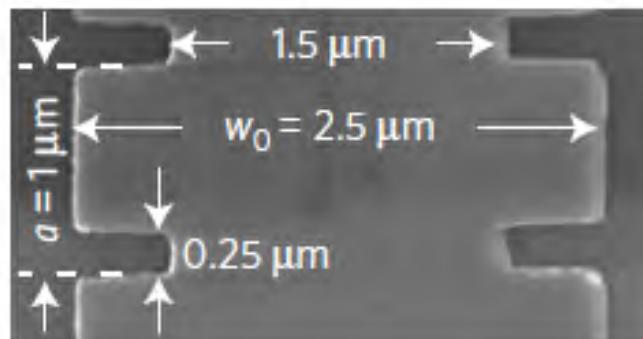
# Excitation spectrum



# Helimagnon modes



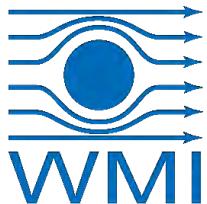
# An intrinsic, chiral magnonic crystal

**b**

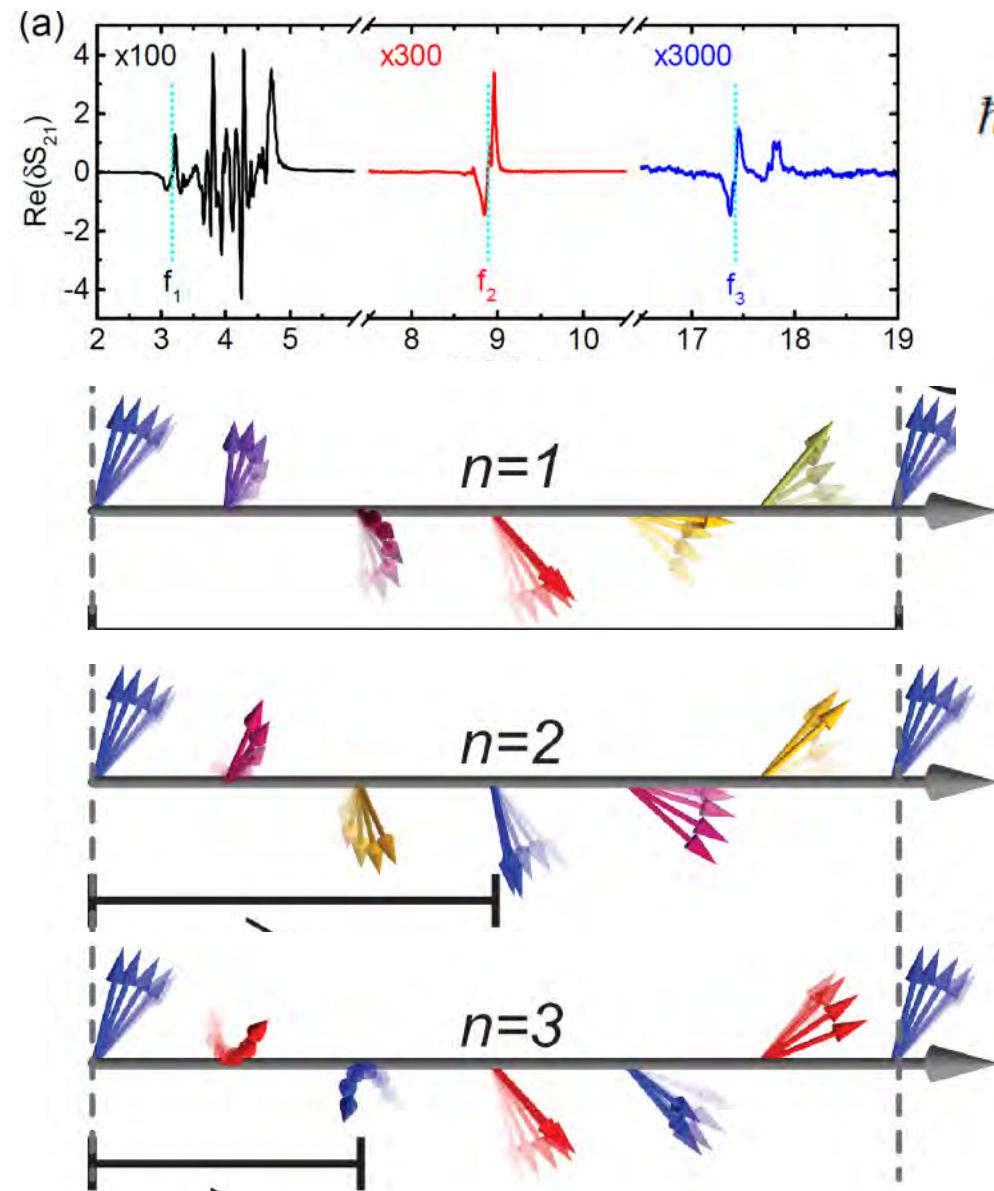
Conventional Magnonic Crystal:  
Bandstructure from extrinsic, periodic modulation

Chumak, et al., Nat Phys **11**, 453 (2015).

Kugler et al., PRL **115**,  
097203 (2015).  
Spin Helix:  
Intrinsic, 60-nm periodicity



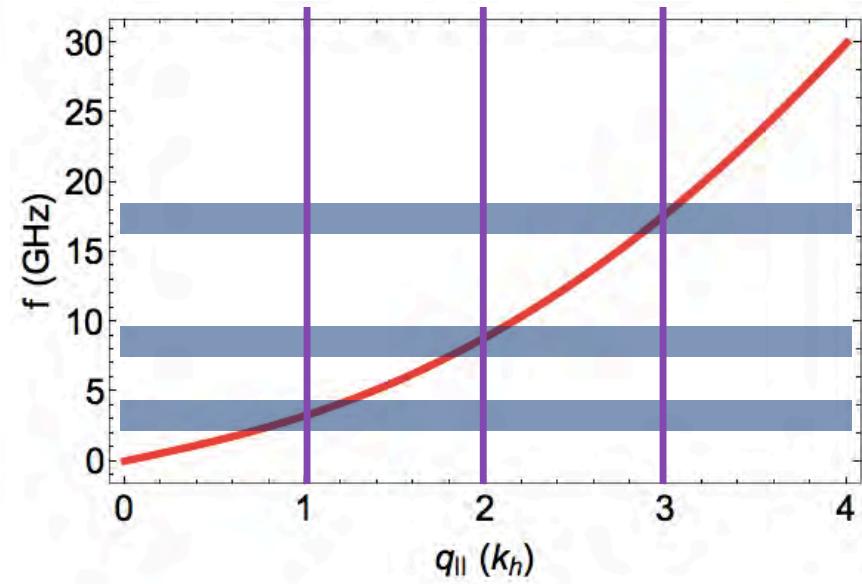
# Analytical model



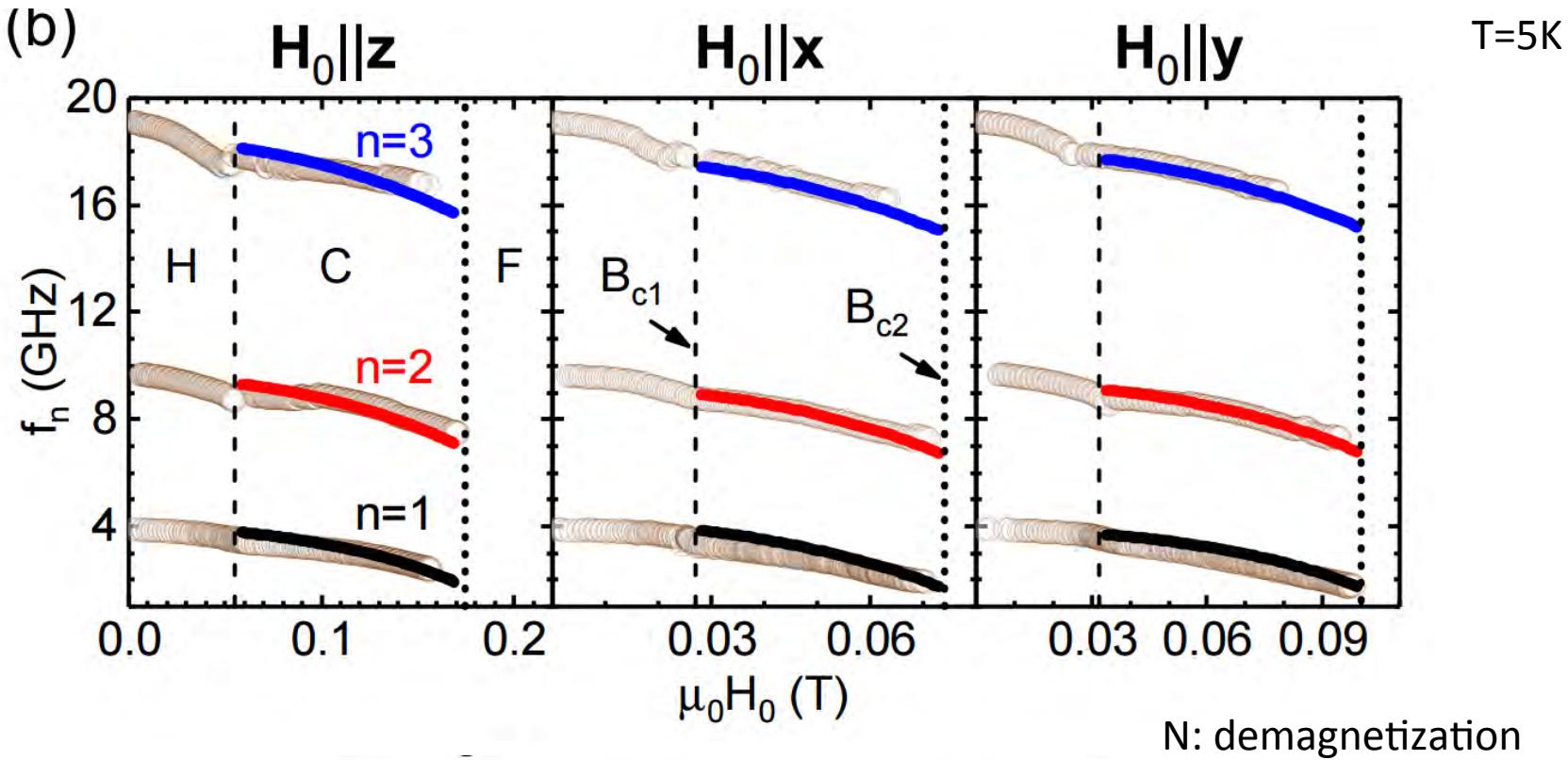
$$\hbar\omega_n = n \frac{g\mu_B B_{c2}}{1 + N\chi} \sqrt{n^2 + (1 + \chi) \sin^2 \Theta}$$

$$\chi = \mu_0 \frac{M_s^2}{DQ}$$

$$\cos\Theta = \frac{\mu_0 H_0}{B_{c2}}$$



# Fits to the conical resonance frequencies



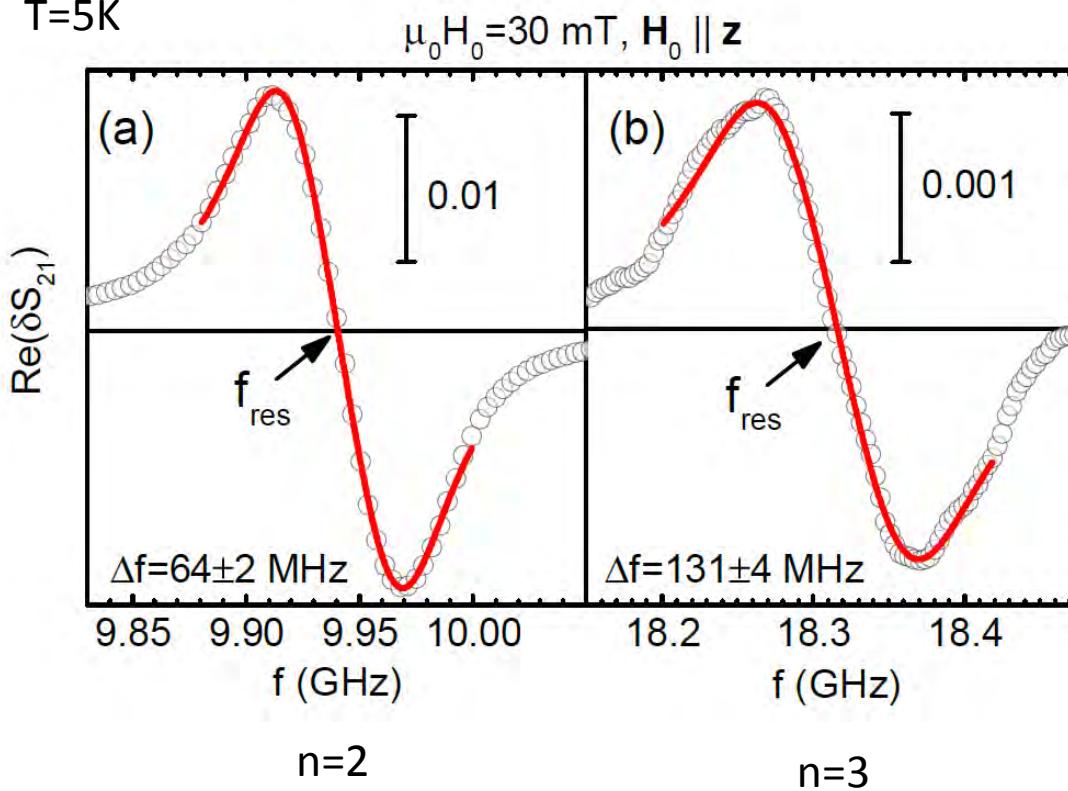
	$H_0 \parallel z$	$H_0 \parallel x$	$H_0 \parallel y$
$B_{c1}$ (T)	0.055	0.027	0.032
$B_{c2}$ (T)	0.175	0.074	0.1
$N$	$0.670 \pm 0.001$	$0.089 \pm 0.001$	$0.241 \pm 0.001$
$\chi$		$2.76 \pm 0.01$	

$$\chi = \mu_0 \frac{M_s^2}{DQ}$$

$$Q = D / J$$

# Low damping in Cu<sub>2</sub>OSeO<sub>3</sub>

T=5K



$$\alpha = \frac{\Delta f}{2f} \leq 0.003$$

In ferrimagnetic phase at T=5K:  
 $\alpha = 0.001$

arXiv:1705.03416 (2017).

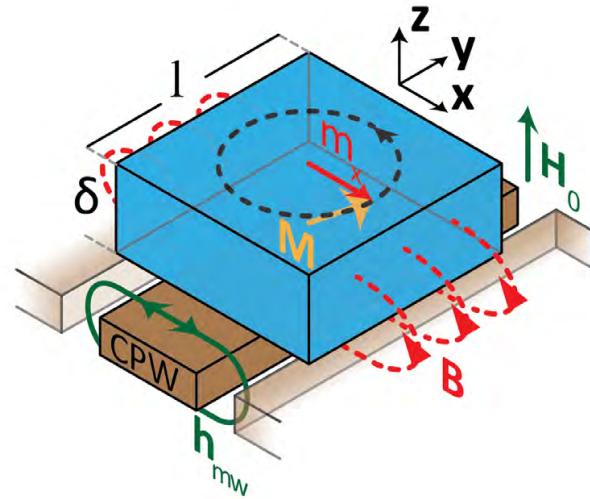
$$\delta S_{21} = \chi(f - \delta f) - \chi(f + \delta f)$$

$$\chi(f) = \frac{C_0}{f_{\text{res}}^2 - f^2 - i f \Delta f}$$

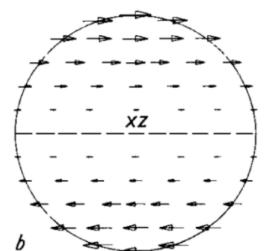
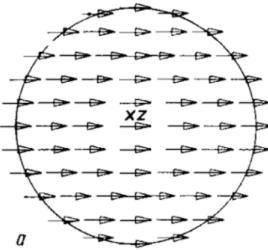
Lowest magnetic damping for helimagnons reported so far

# Summary

Non-collinear magnetization dynamics



Magnetostatic Modes



- Uniform equilibrium spin alignment
- Long-ranged dipolar interaction
- Very small damping in YIG spheres, independent of MSM mode number
- Damping decreases for low T

- Spiral equilibrium spin alignment
- Exchange and DMI
- Low damping at T=5 K
- Natural magnonic crystals

Broadband spectroscopy

Helimagnons



