

Spin current in magnetic insulators driven by stochastic fluctuations

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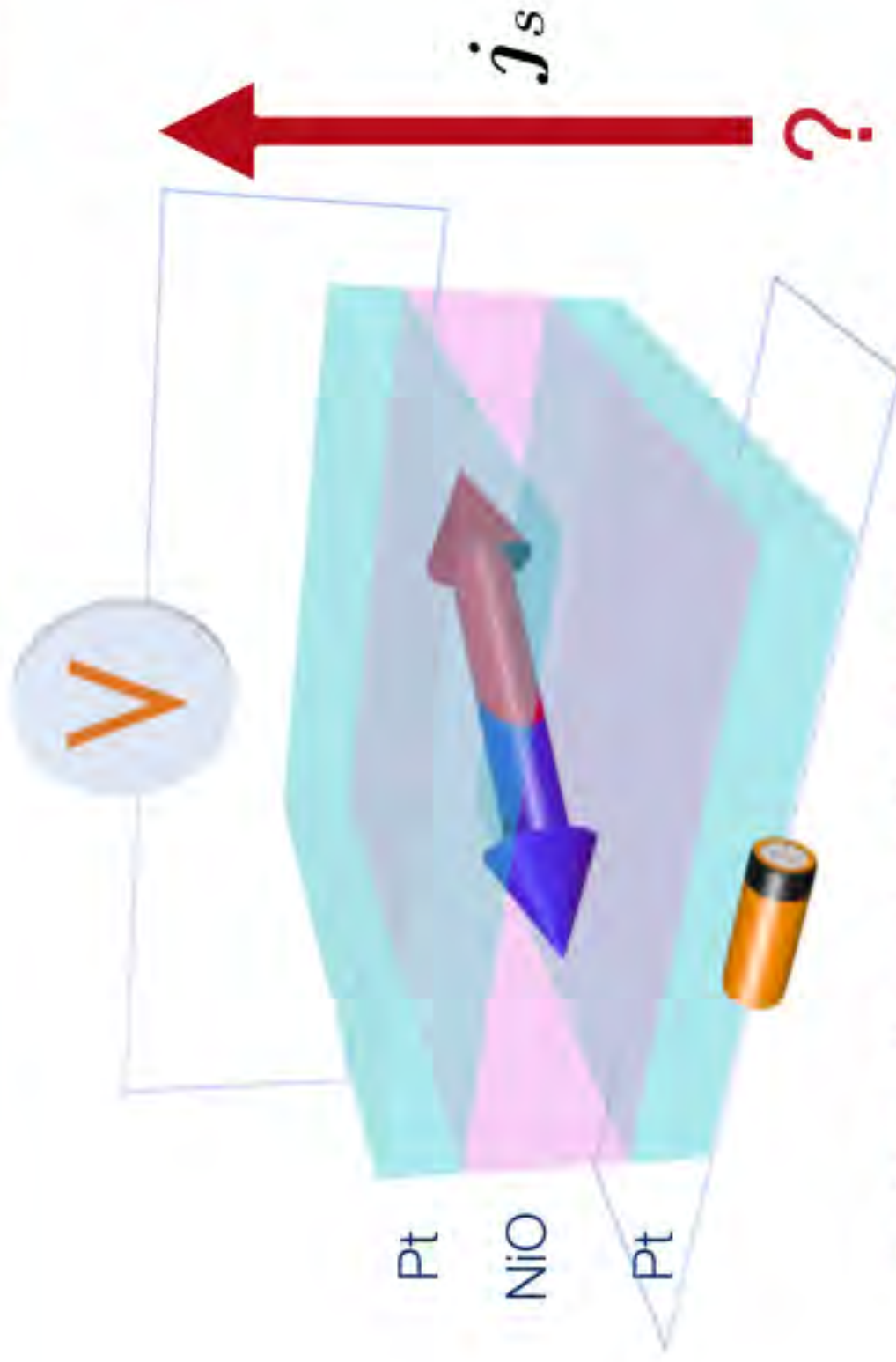
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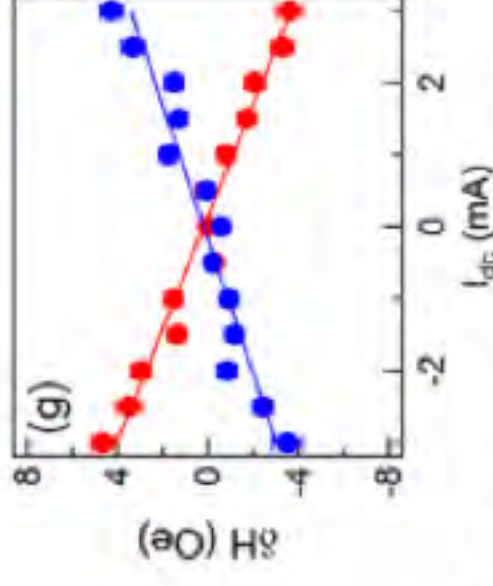
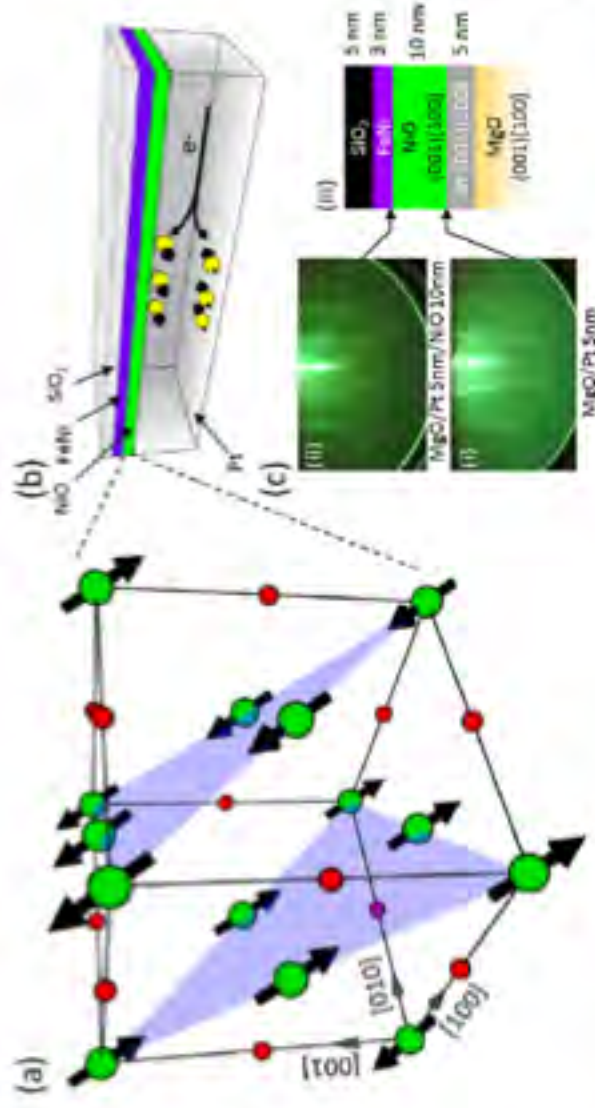


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At the stationary state, nothing depends on time

What is driving the spin current through the insulator?



Moriyama et al. (2016)

Theoretical attempts so far;

1. Bulk diffusion equation approach (Rezende et al. 2016, cf. Zhang & Zhang 2012)
2. Evanescent mode (Khymyn et al. 2016)
3. Linear response to spin accumulation (Bender et al. 2017)

- I. Spin fluctuations and spin Seebeck effect
- II. Spin transfer torque and damping modulation
- III. Spin current through antiferromagnetic insulators

Damping-like torque + thermal fluctuation -> Spin current



Spin fluctuations and spin Seebeck effect

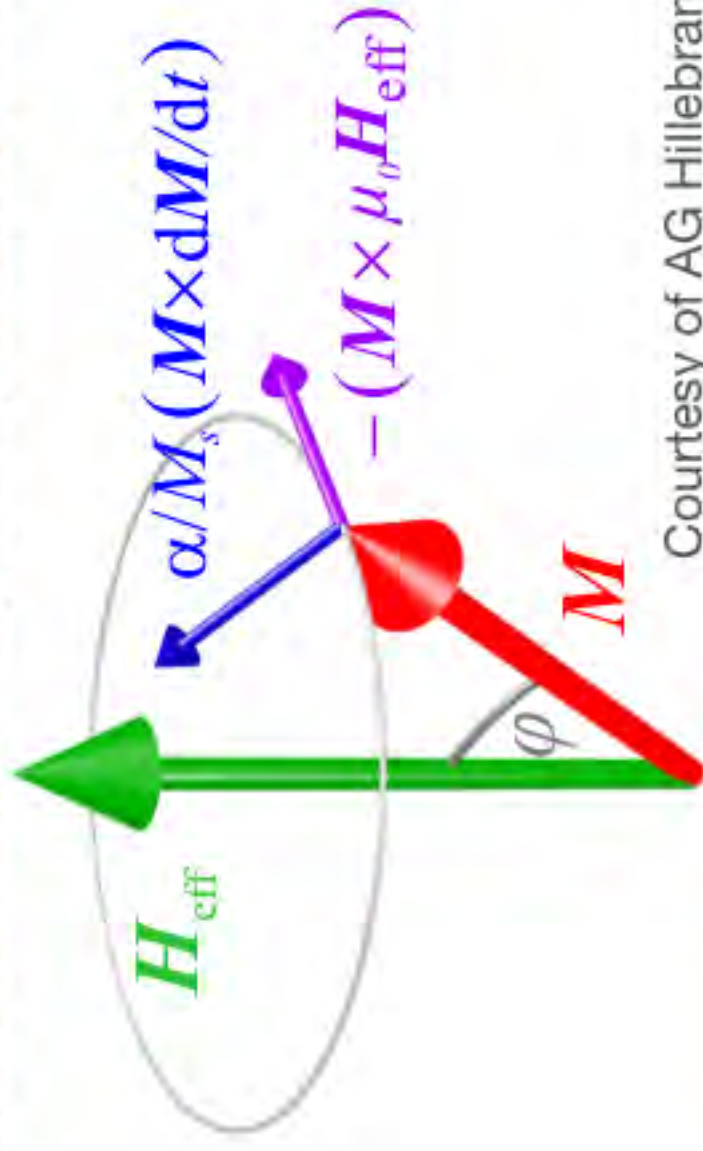


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Precession of spins

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Courtesy of AG Hillebrands

Precession is always **chiral** and **non-reciprocal**

Precession \rightarrow angular momentum $L \propto M \times \frac{dM}{dt}$



Courtesy of Prof. Eiji Saitoh

Random motion -> Nonzero expectation value of angular momentum



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Temperature induced angular momentum



- Random precession -> nonzero angular momentum on average

$$\left\langle \delta \mathbf{M} \times \frac{d\delta \mathbf{M}}{dt} \right\rangle \neq 0$$

- Higher temperature -> more fluctuations

$$\langle \delta \mathbf{M}^2 \rangle \propto T \quad (\text{High } T \text{ approximation})$$

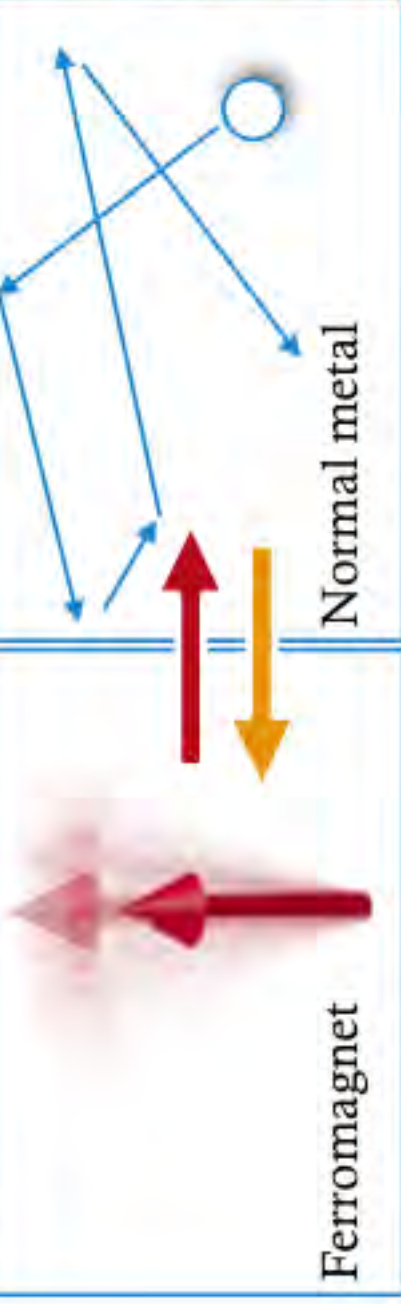
- Temperature generates angular momentum

Bloch's law

$$\langle M_s - M_z \rangle \propto T^{3/2}$$

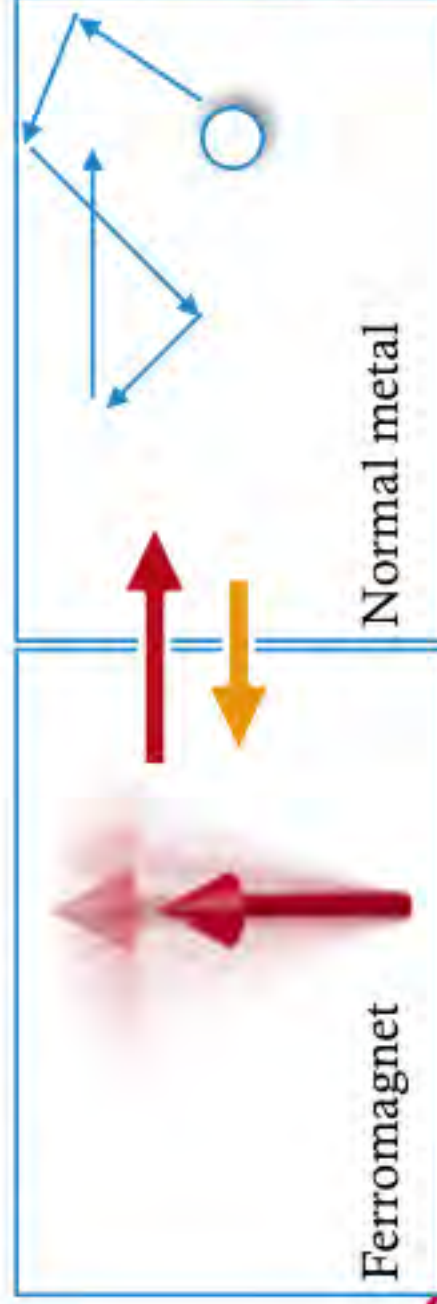


$$T_F = T_N$$



Complete compensation of incoming and outgoing spin

$$T_F \neq T_N$$



Net spin current

Spin Seebeck effect (Xiao et al.)

Spin transfer torque and damping modulation



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Slonczewski's damping-like torque



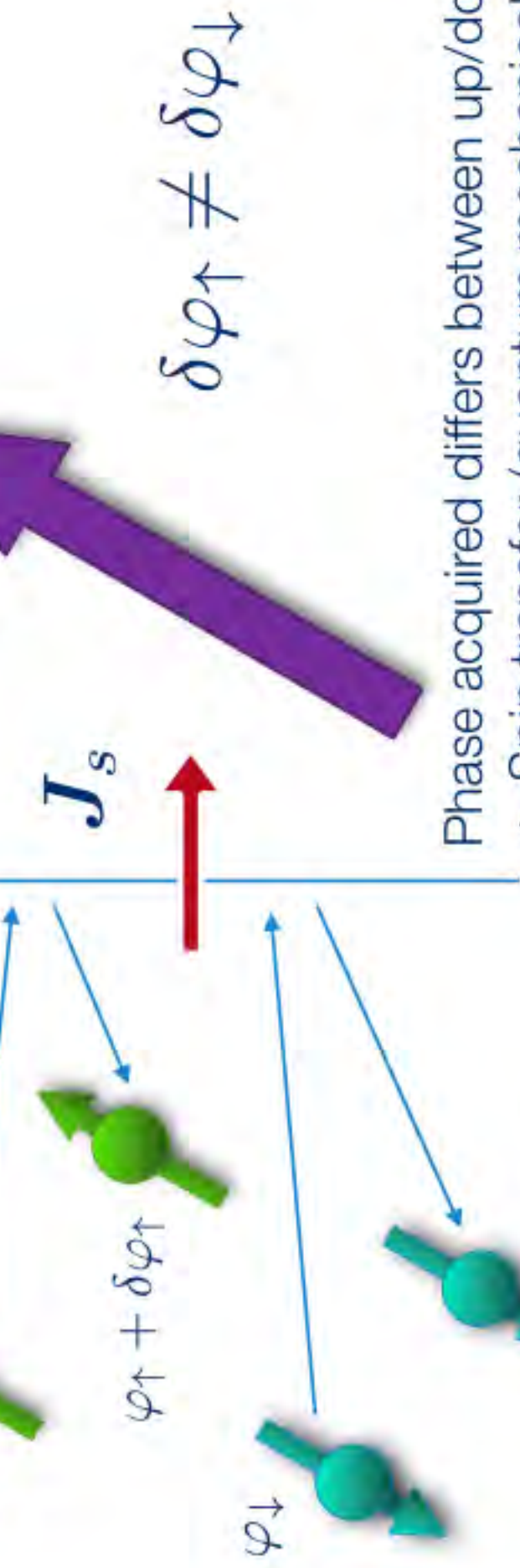
Elastic spin conserving scatterings at the interface



\uparrow

M





Phase acquired differs between up/down
 -> Spin transfer (quantum mechanical!)

$$\frac{d\mathbf{M}}{dt} \propto \mathbf{M} \times (\mathbf{M} \times \mathbf{J}_s)$$

Damping modulation

Landau-Lifshitz-Gilbert equation

$$\frac{d\mathbf{M}}{dt} = \gamma \mathbf{M} \times \left(\mathbf{H}_{\text{eff}} + \frac{\alpha}{\gamma M_s} \frac{d\mathbf{M}}{dt} + \frac{\sigma}{M_s} \mathbf{M} \times \mathbf{J}_s \right)$$

Landau-Lifshitz equation

$$\frac{d\mathbf{M}}{dt} = \gamma \mathbf{M} \times \mathbf{H}_{\text{eff}} + \gamma \mathbf{M} \times \left[\frac{\mathbf{M}}{M_s} \times (\alpha \mathbf{H}_{\text{eff}} + \sigma \mathbf{J}_s) \right]$$

If $\mathbf{H}_{\text{eff}} \parallel \mathbf{J}_s$, the torque effectively shifts the damping by

$$\alpha \rightarrow \alpha + \text{sgn}(J_s) \sigma \frac{|J_s|}{|H_{\text{eff}}|}$$

“Damping-like”

Ando et al., PRL (2008)

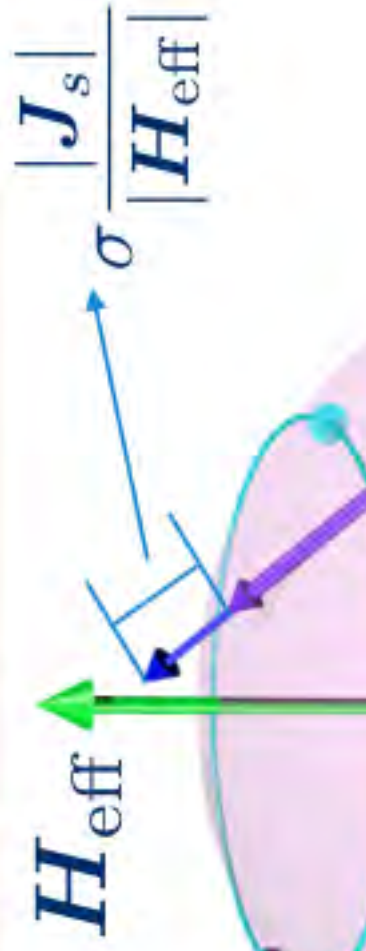


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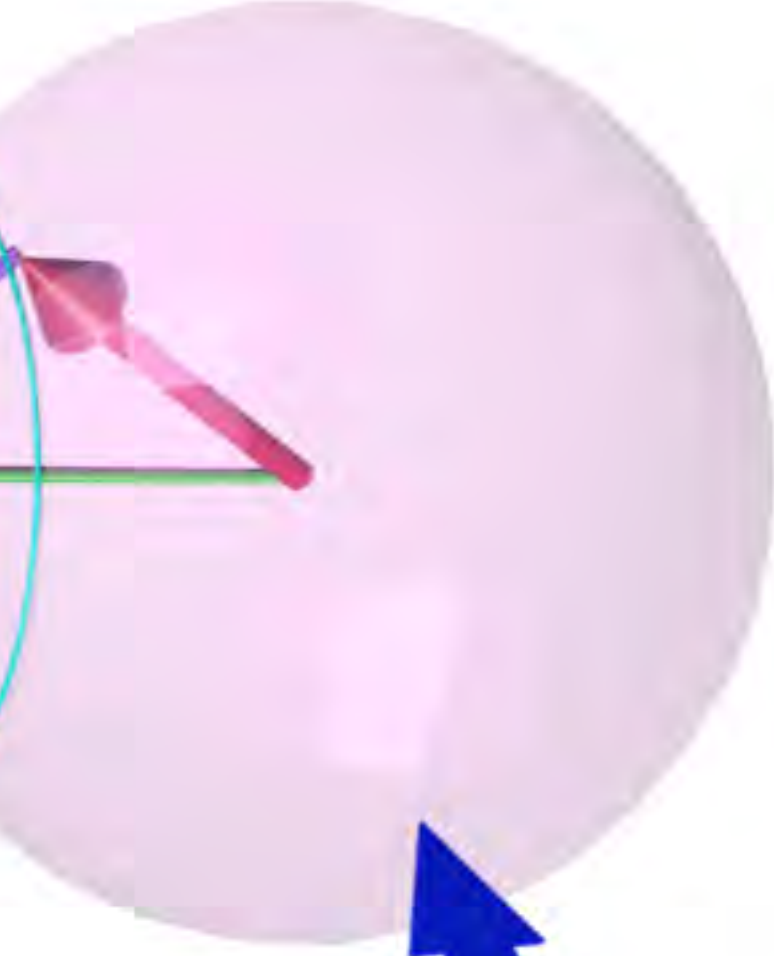
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Damping modulation

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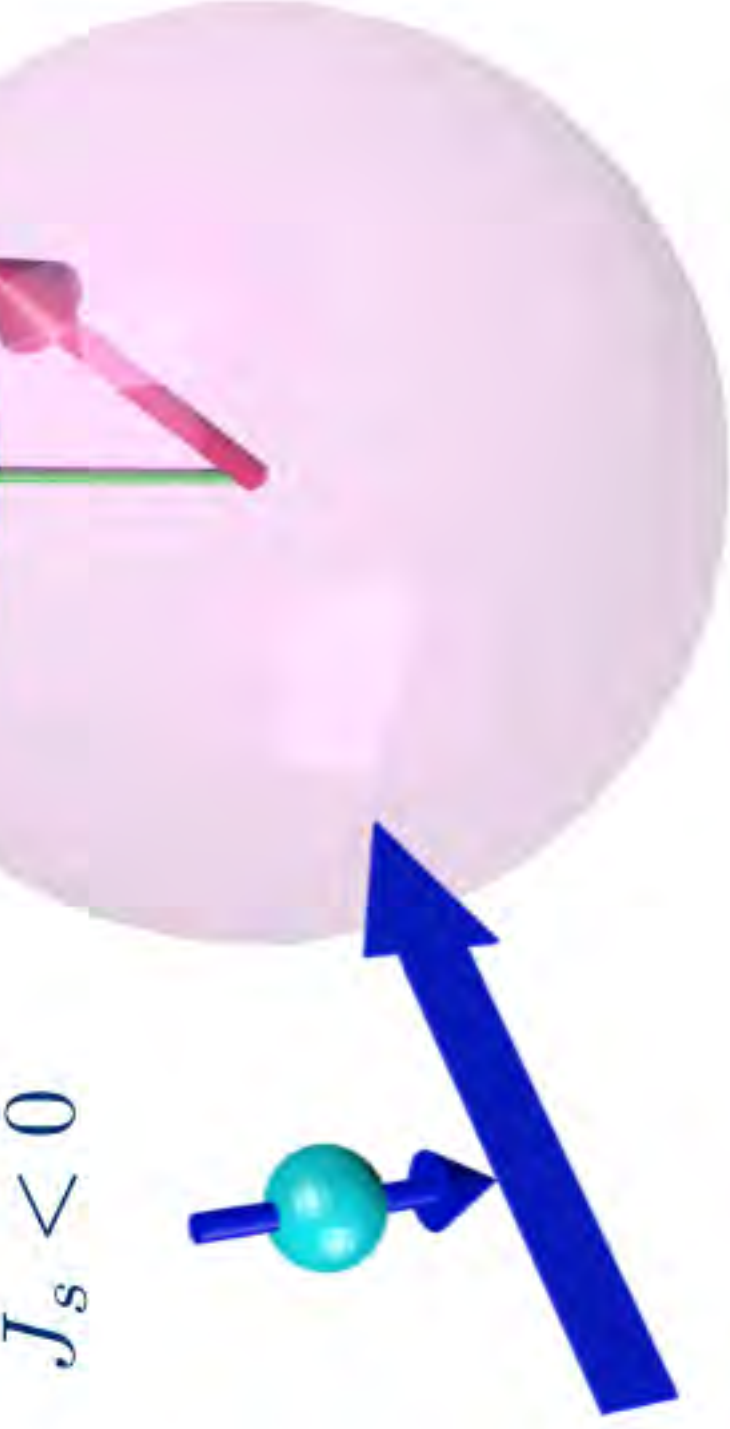
$$J_s > 0$$



Damping modulation

$$H_{\text{eff}} \quad \sigma \frac{|J_s|}{|H_{\text{eff}}|}$$

$$J_s < 0$$



Stochastic equation of motion

- Damping torque itself **cannot** induce any dynamics
- Solution of LLG $M \rightarrow (M \parallel H_{\text{eff}})$
- Temperature induces random magnetic field

$$\langle h_i(t) \rangle = 0, \quad \langle h_i(t) h_j(t') \rangle = \frac{2\alpha k_B T}{|\gamma M_s|} \delta_{ij} \delta(t - t')$$

- Langevin-type probabilistic dynamical equation

$$\frac{d\mathbf{M}}{dt} = \gamma \mathbf{M} \times \left(\mathbf{H}_{\text{eff}} + \mathbf{h}(t) \right) + \frac{\alpha}{\gamma M_s} \frac{d\mathbf{M}}{dt} + \frac{\sigma}{M_s} \mathbf{M} \times \mathbf{J}_s$$

Time dependent field \rightarrow stochastic dynamics of \mathbf{M}



Fluctuation-dissipation relation

- Solution of stochastic LLG = Probability distribution of \mathbf{M}

$$P(\mathbf{M}) \leftrightarrow \langle \mathbf{M} \rangle, \langle \mathbf{M}^2 \rangle, \dots$$

- Without the torque, the solution should describe equilibrium

$$[F(\mathbf{M})]$$

$$P(\mathbf{M}) \propto \exp \left[-\frac{E(\mathbf{M})}{k_B T} \right]$$

Boltzmann distribution

- This is true only if the damping and random field compensate

$$\langle h_i(t) h_j(t') \rangle = \frac{2\alpha k_B T}{|\gamma M_s|} \delta_{ij} \delta(t - t')$$

Fluctuation-Dissipation Theorem (FDT)



Deviation from FDT

- Spin torque modifies effective damping
- Assumption: the random field is unchanged by the torque

$$\alpha \rightarrow \alpha \pm \sigma \frac{|J_s|}{|H_{\text{eff}}|}$$

$$\langle h_i(t) h_j(t') \rangle = \frac{2\alpha k_B T}{|\gamma M_s|} \delta_{ij} \delta(t - t')$$

- FDT does not hold, system out of equilibrium

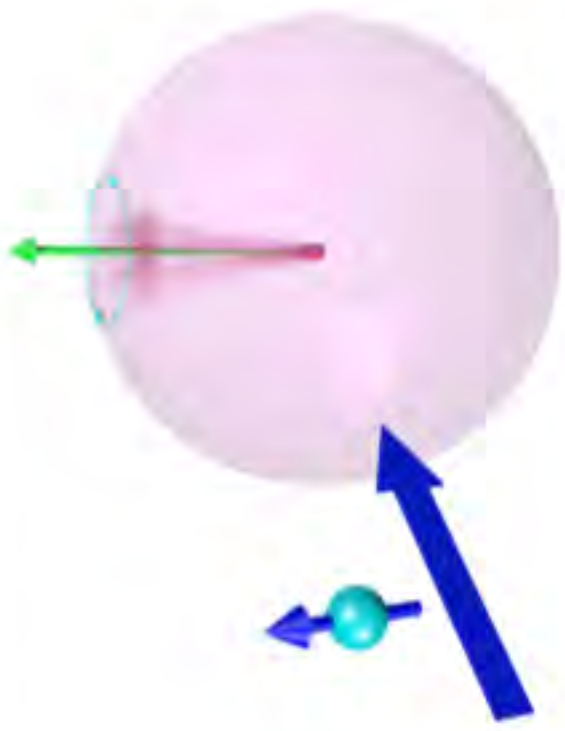
Caveat

Temperature here is the temperature of a heat bath.

Temperature of the magnetic system in general cannot be defined because the system is out of equilibrium.



Deviation from FDT



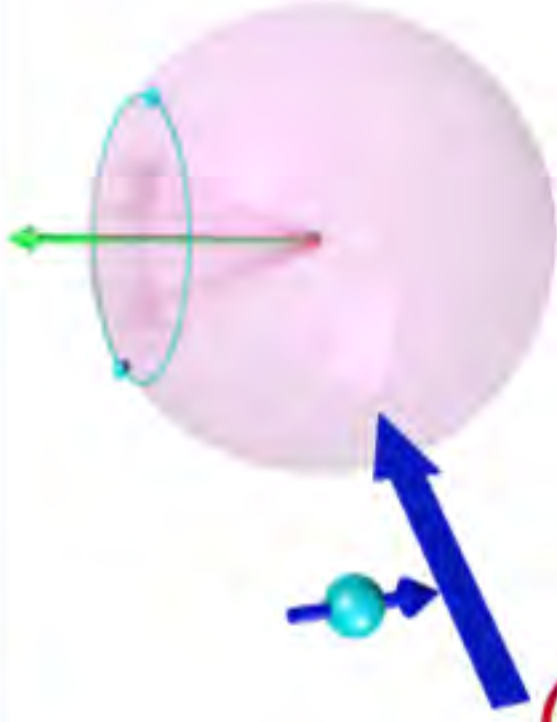
$$J_s > 0 (H_{\text{eff}} \parallel J_s)$$

Enhanced damping

Unchanged random field



Less fluctuation -> less spin



$$J_s < 0 \quad (\mathbf{H}_{\text{eff}} \parallel -\mathbf{J}_s)$$

Reduced damping
Unchanged random field

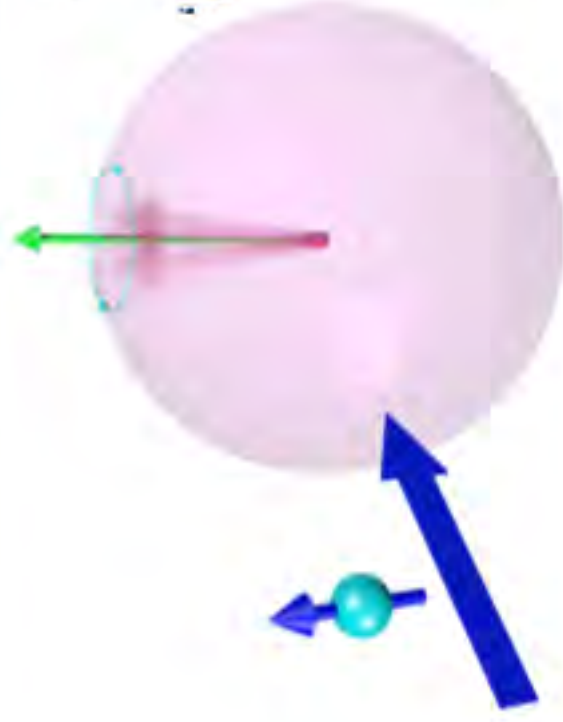


More fluctuation -> more spin



Effective temperature

$$P(\mathbf{M}) \propto \exp \left[-\frac{E(\mathbf{M})}{k_B(T - \delta T)} \right], \quad \delta T \propto |J_s|$$



'Loose' angular momentum

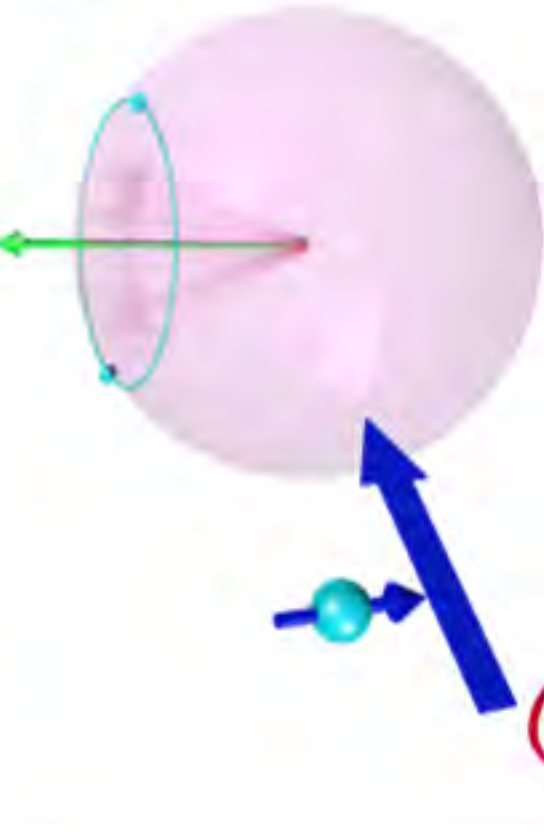
$$\langle M_s - M_z \rangle$$



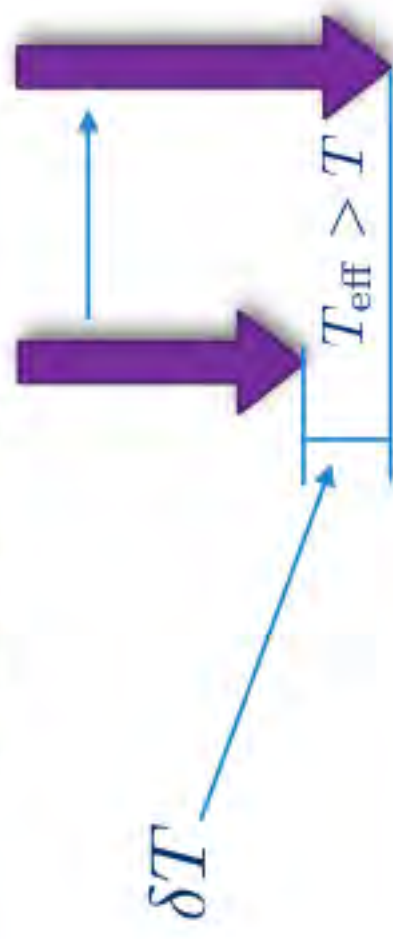
\mathbf{J}_s

$$T_{\text{eff}} < T$$

Equilibrium



$$P(\mathbf{M}) \propto \exp \left[-\frac{E(\mathbf{M})}{k_B(T + \delta T)} \right], \quad \delta T \propto |J_s|$$

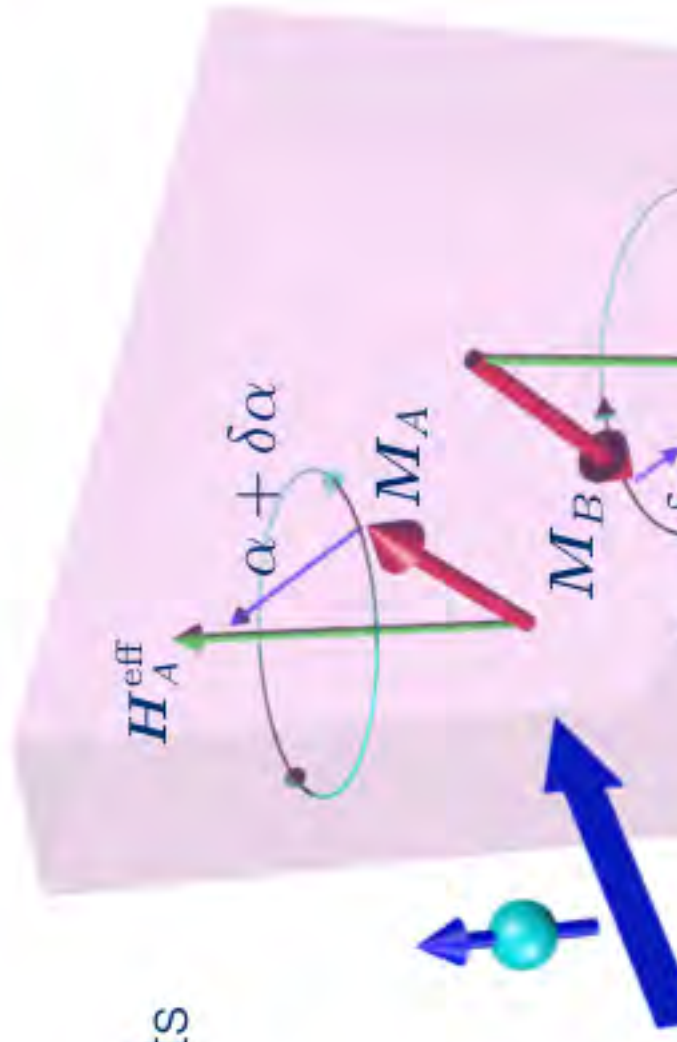


Spin current through antiferromagnetic insulators

Two sublattice model of AFM

Two antiferromagnetically coupled ferromagnetic moments

$$\frac{1}{\gamma} \frac{d\mathbf{M}_{A,B}}{dt} = \mathbf{M}_{A,B} \times (\mathbf{H}_{A,B}^{\text{eff}} + \mathbf{h}_{A,B}) + \frac{\alpha}{\gamma} \mathbf{M}_{A,B} \times \frac{d\mathbf{M}_{A,B}}{dt}$$



$$\gamma M_s \frac{d\alpha}{dt} + \frac{\sigma}{M_s} M_{A,B} \times (M_{A,B} \times J_s)$$

$$H_A^{\text{eff}} \sim -H_B^{\text{eff}} \quad \delta\alpha = \sigma \frac{|J_s|}{|H_{A,B}^{\text{eff}}|}$$



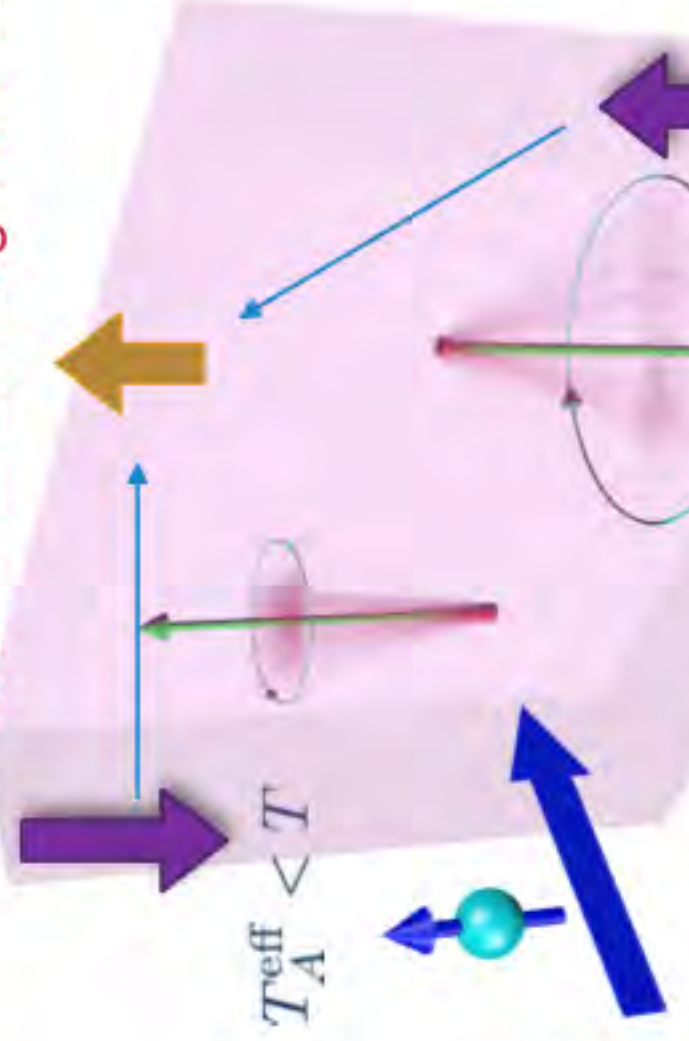
Qualitative picture

Spin transfer torque acts oppositely for the two sublattices

-> Generate different effective temperature

Assumption: the random fields are identical and independent for the two sublattices

Total induced magnetisation



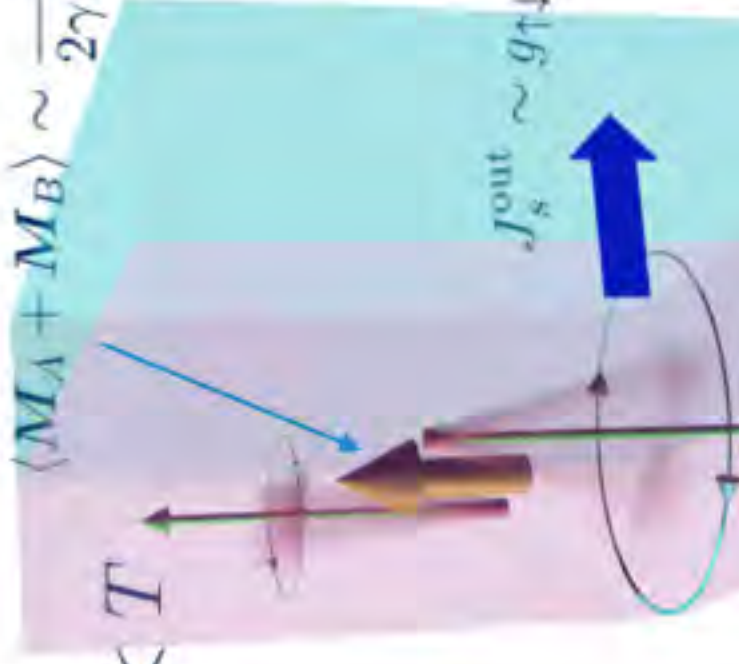
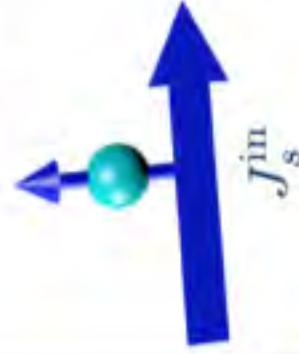
$$\begin{aligned} \langle h_{A_i}(t) h_{A_j}(t') \rangle &= \langle h_{B_i}(t) h_{B_j}(t') \rangle \\ &= \frac{2\alpha k_B T}{\gamma M_s} \delta_{ij} \delta(t - t'), \end{aligned}$$

$$\langle h_{A_i}(t) h_{B_j}(t') \rangle = 0$$



Induced magnetisation and spin pumping

$$T_A^{\text{eff}} < T \quad \langle M_A + M_B \rangle \sim \frac{1}{2\gamma M_s H_E} \left\langle \mathbf{L} \times \frac{d\mathbf{L}}{dt} \right\rangle, \quad \mathbf{L} = M_A - M_B$$



Interface spin-pumping formula

$$J_s^{\text{out}} \sim g_{\uparrow\downarrow} \left\langle \mathbf{L} \times \frac{d\mathbf{L}}{dt} \right\rangle \propto - (T_A^{\text{eff}} - T_B^{\text{eff}}) \propto J_s^{\text{in}}$$

Out-of-equilibrium magnetisation

flows out into the adjacent lead
in search of equilibrium



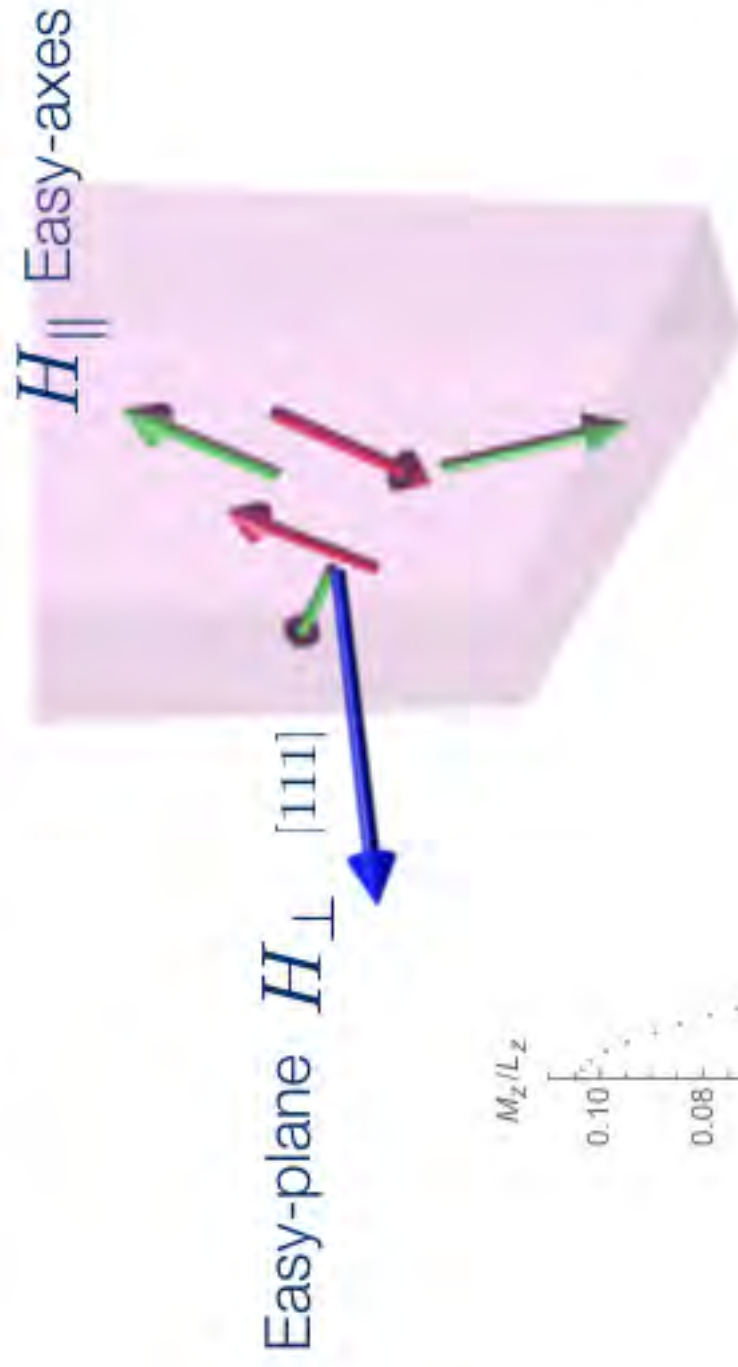
$$T_{\text{lead}} = T$$



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Dependence on biaxial anisotropy

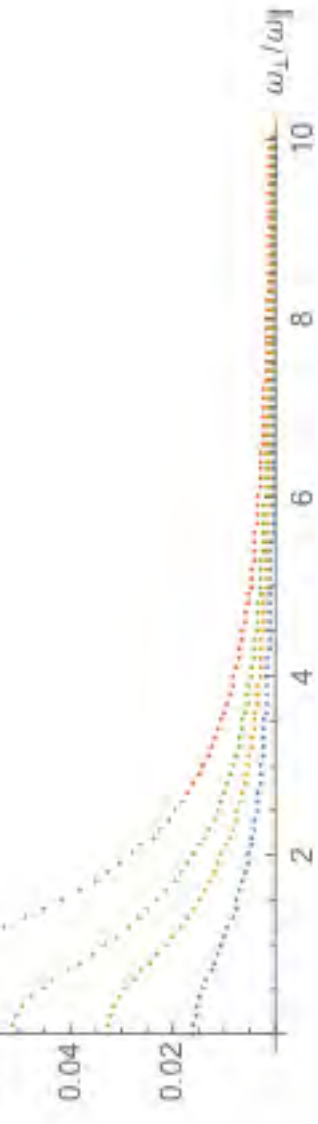


$$\frac{\delta\alpha}{\alpha} = 0.1$$

$$\frac{\delta\alpha}{\alpha} = 0.2$$

$$\frac{\delta\alpha}{\alpha} = 0.3$$

$$\frac{\delta\alpha}{\alpha} = 0.5$$



Summary



- Spin is a ratchet -> fluctuations generate loose angular momenta
- In equilibrium, there is a balance between random force fields that completely cancel any transport current (FDT)
- Damping-like torque drives system out of equilibrium by modulating the damping constants and breaking FDT
- Damping-like torque induces out-of-equilibrium net magnetisation

in AFMs, which is converted to spin current via spin-pumping



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THANK YOU

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CMYK: 100 C, 80 M, 40K

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