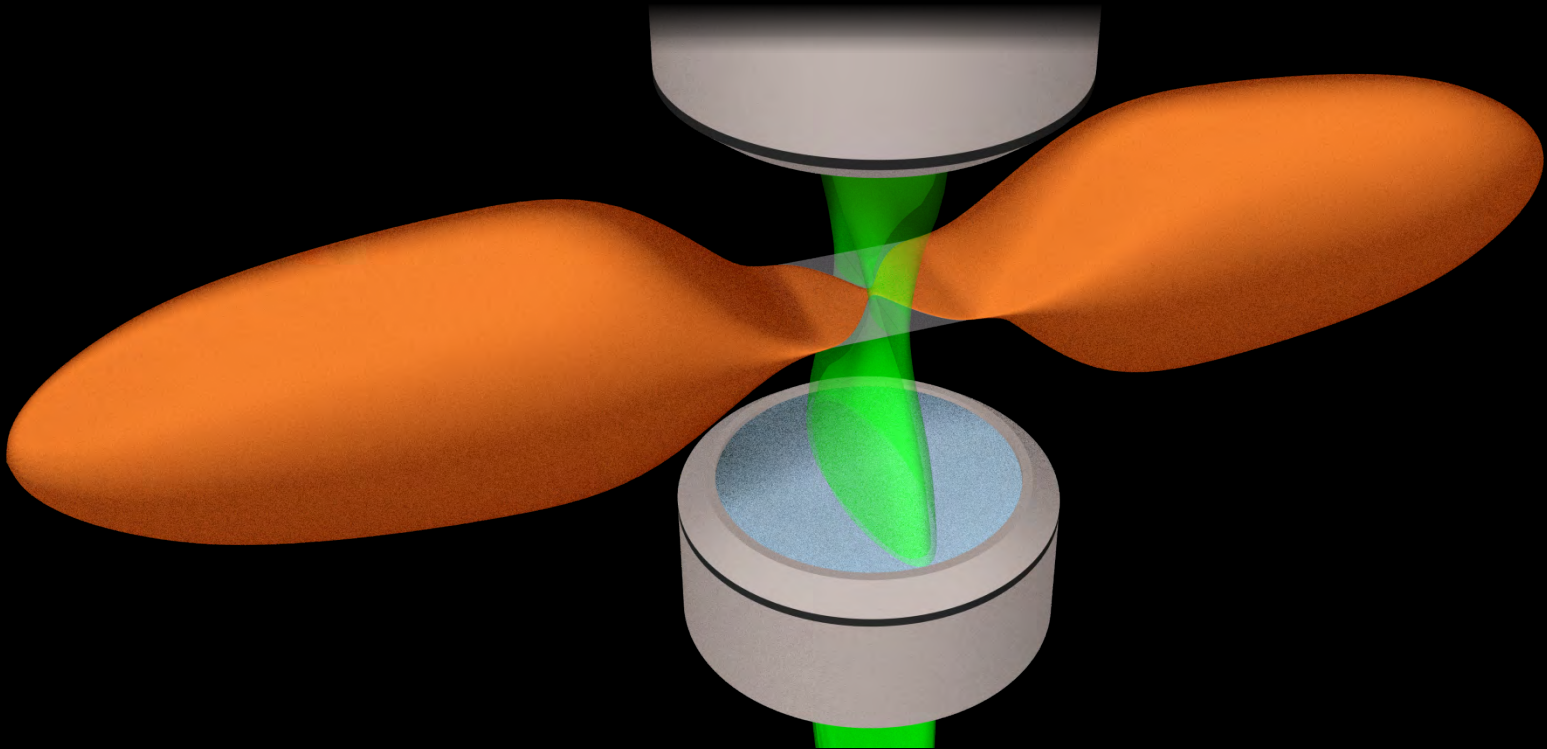


# Mesoscopic transport experiments with cold atoms



Jean-Philippe Brantut

Institute of Physics, EPFL

# Ultra-cold atoms

- Density scales:  $10^{12} \text{ cm}^{-3}$ 
  - Interparticle spacing comparable with the wavelength of visible light  
*Optical lattices, disorder, mesoscopic structures*

# Ultra-cold atoms

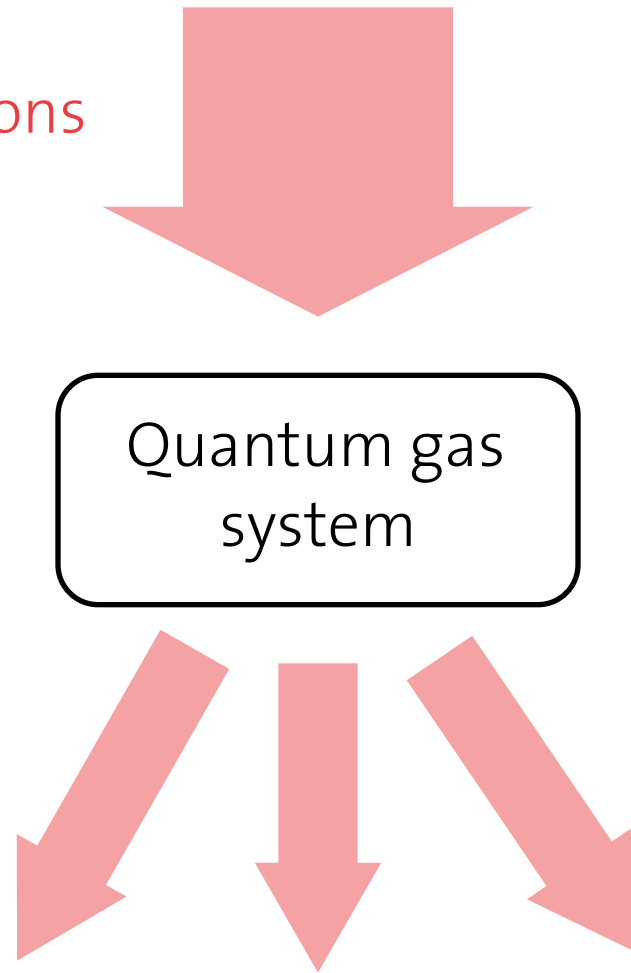
- Density scales:  $10^{12} \text{ cm}^{-3}$ 
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*Optical lattices, disorder, mesoscopic structures*
  - Energy scales in the  $\mu\text{K}$  range

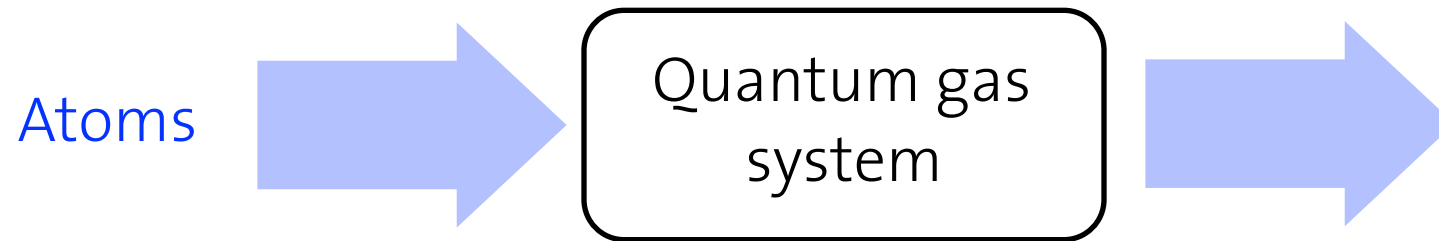
# Ultra-cold atoms

- Density scales:  $10^{12} \text{ cm}^{-3}$ 
  - Interparticle spacing comparable with the wavelength of visible light  
*Optical lattices, disorder, mesoscopic structures*
  - Energy scales in the  $\mu\text{K}$  range
  
- Neutral particles with a complex internal structure
  - Controls the mechanical action of light onto atoms
  - Spectroscopic addressing of internal degrees of freedom
  - Short range (contact) interactions tunable by control fields

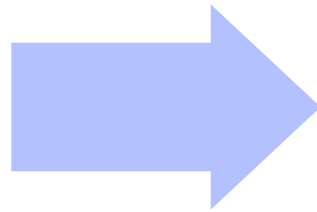
Quantum gas  
system

Photons

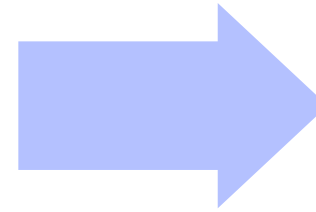




Atoms source



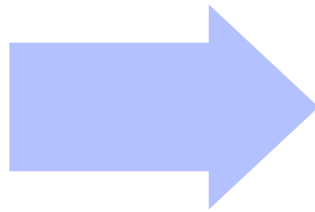
Quantum gas  
system



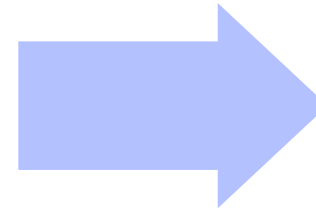
Atoms drain



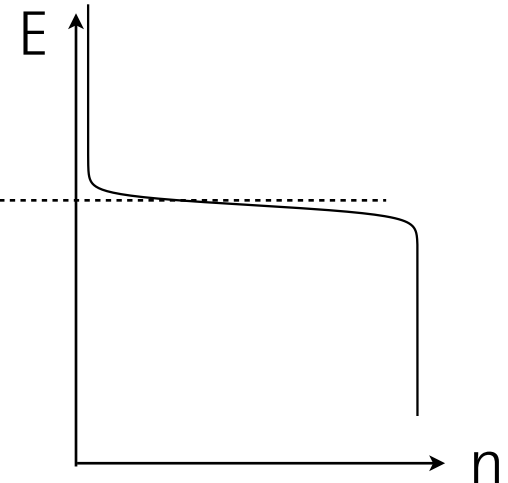
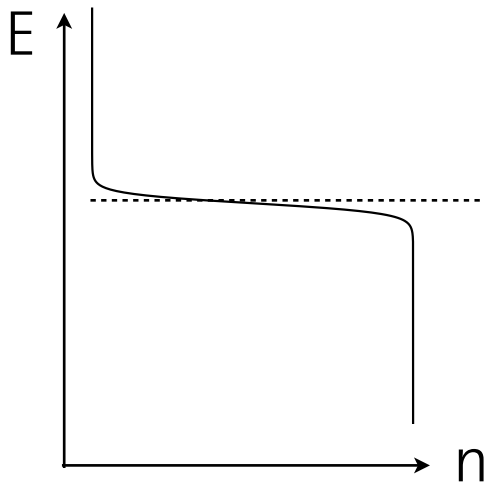
Atoms source



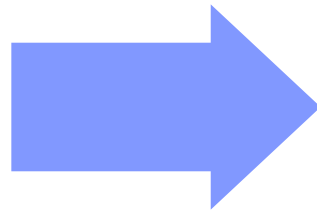
Quantum gas system



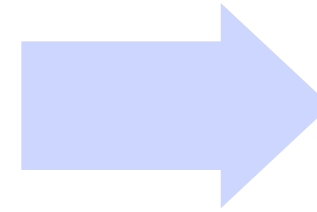
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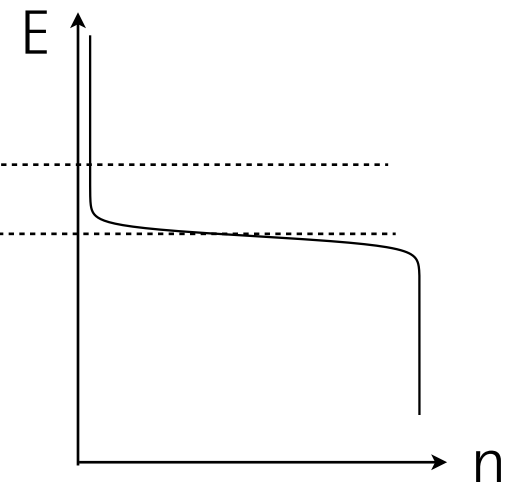
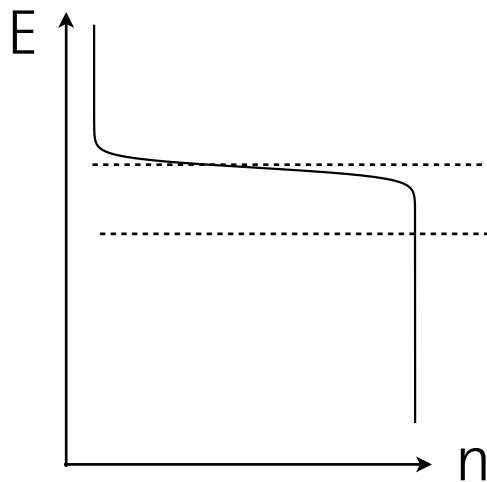
Atoms source



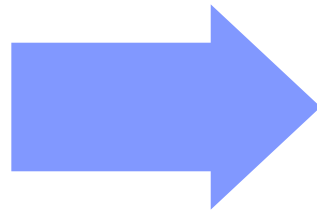
Quantum gas system



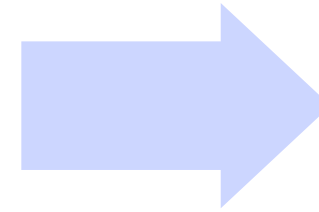
Atoms drain



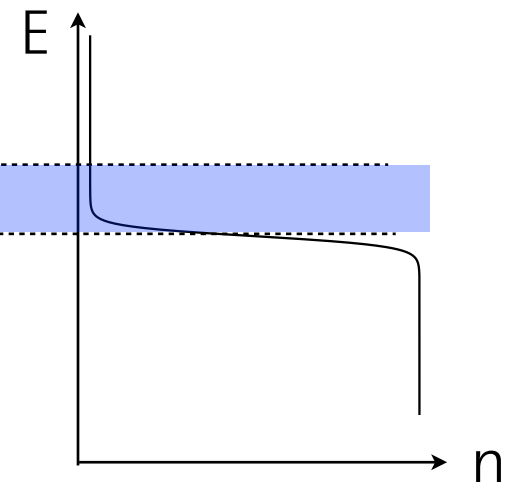
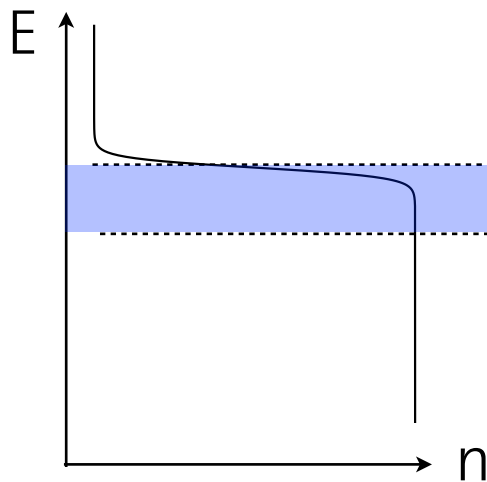
Atoms source



Quantum gas system




Atoms drain

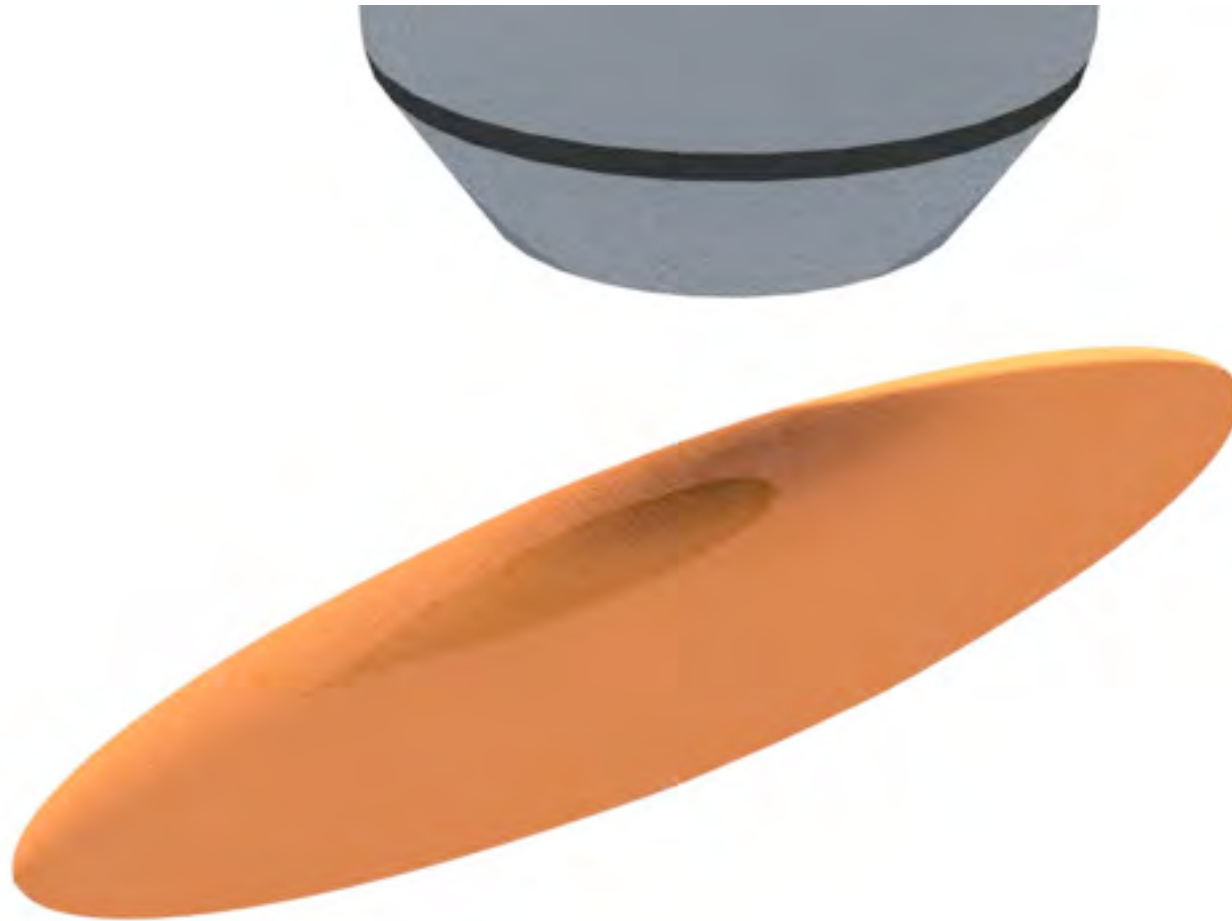


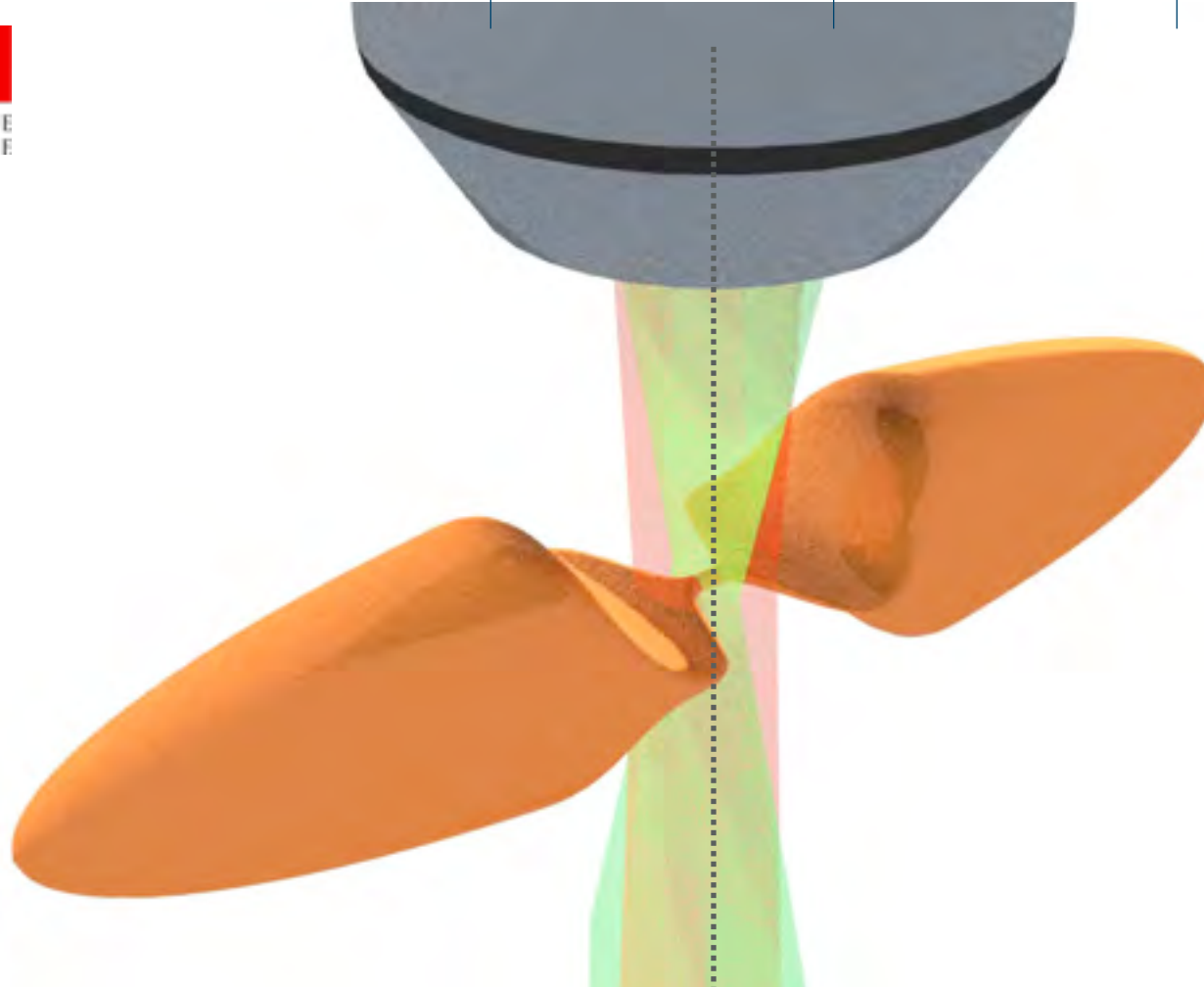
- Quantum Point Contact for cold Fermions
  - Transport measurement technique
  - Quantized conductance
- Interacting systems
  - Feshbach resonances
  - Fate of quantized conductance across the BCS-BEC crossover
  - Mesoscopic lattices
- Future prospects

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$\sim 10^5$   ${}^6\text{Li}$  atoms  
 $T = 0.1 T_F$

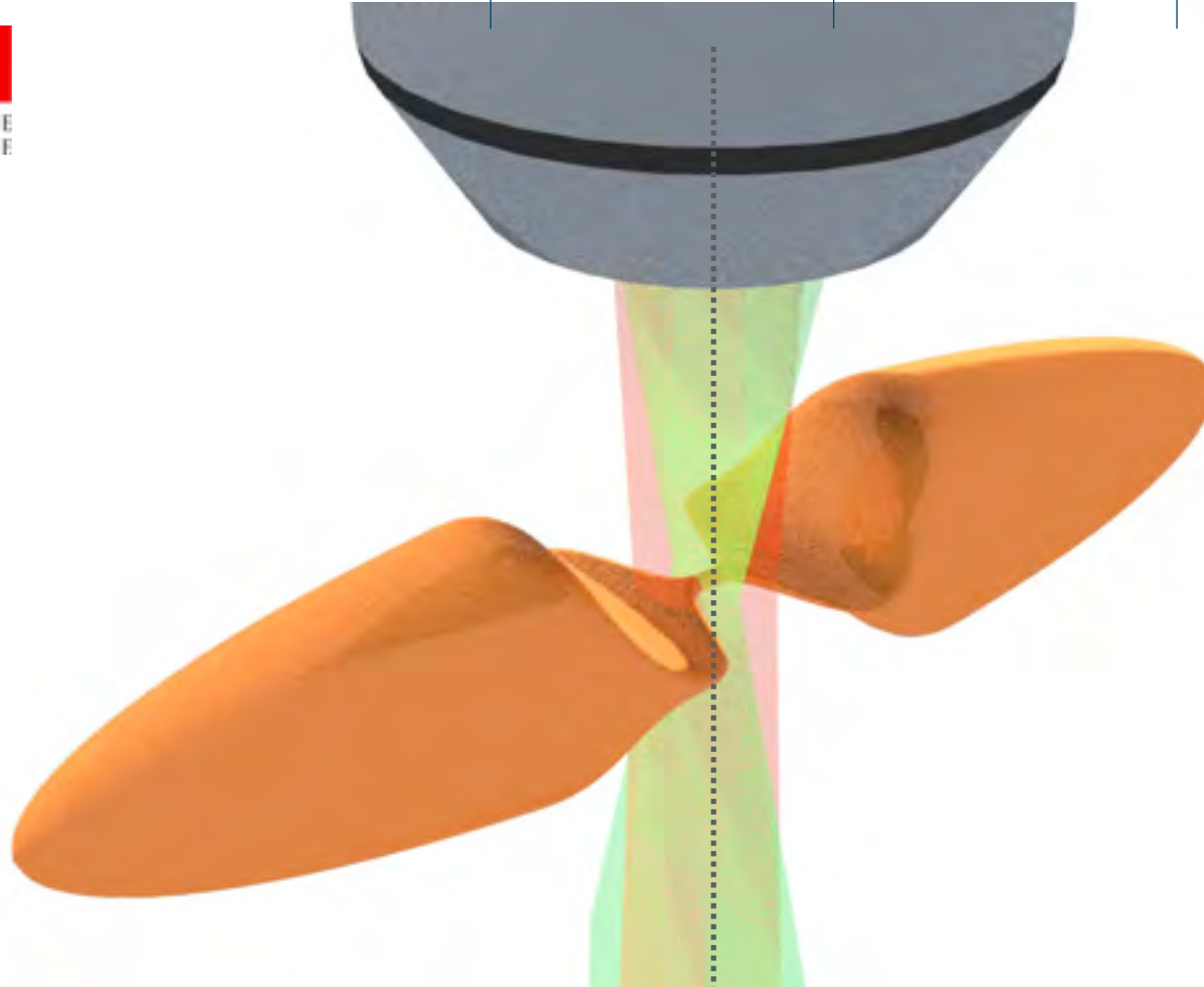




$N_{\text{Left}}$   
 $\mu_{\text{Left}}$

$N_{\text{Right}}$   
 $\mu_{\text{Right}}$

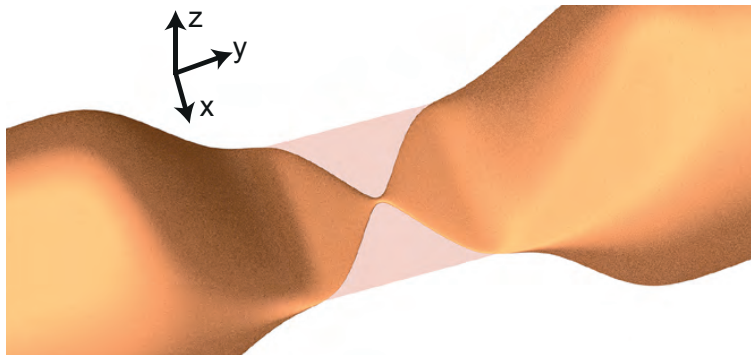




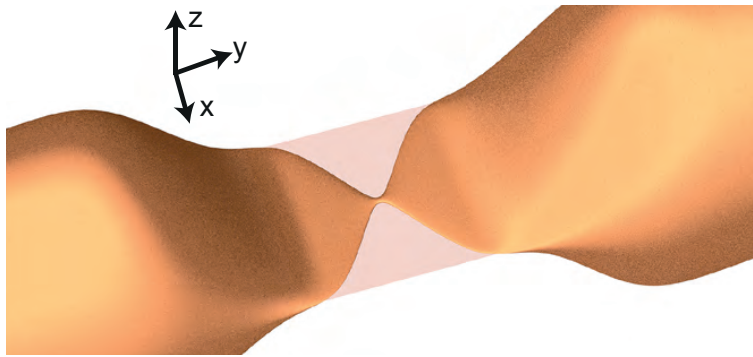
$N_{\text{Left}}$   
 $\mu_{\text{Left}}$



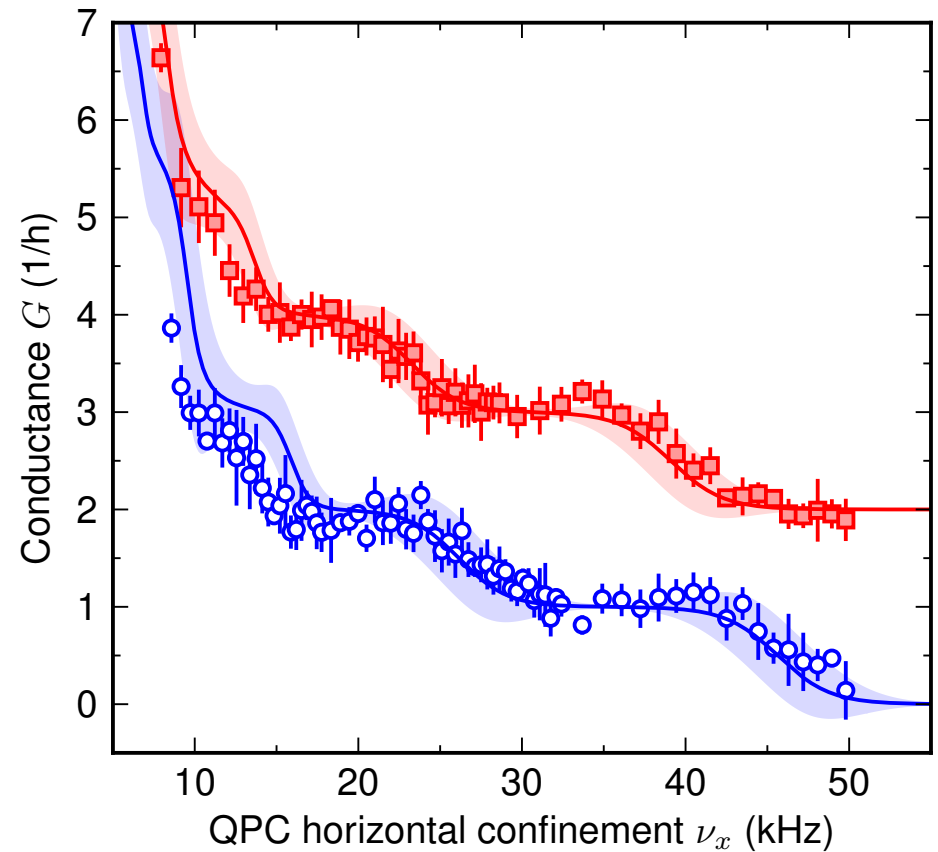
$N_{\text{Right}}$   
 $\mu_{\text{Right}}$

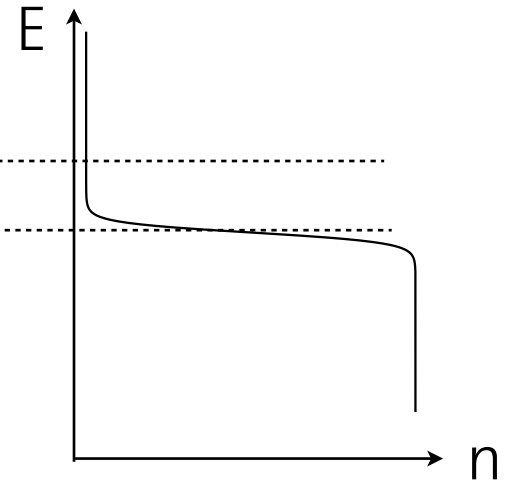
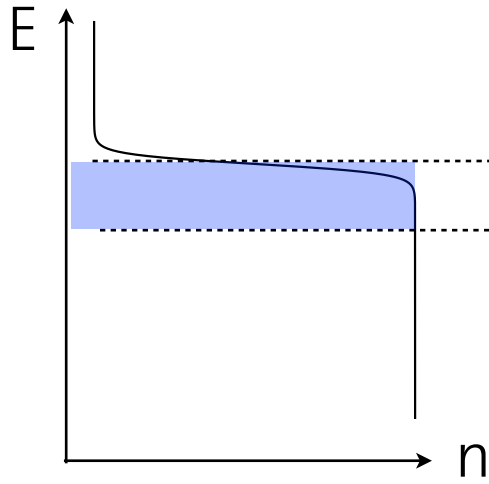


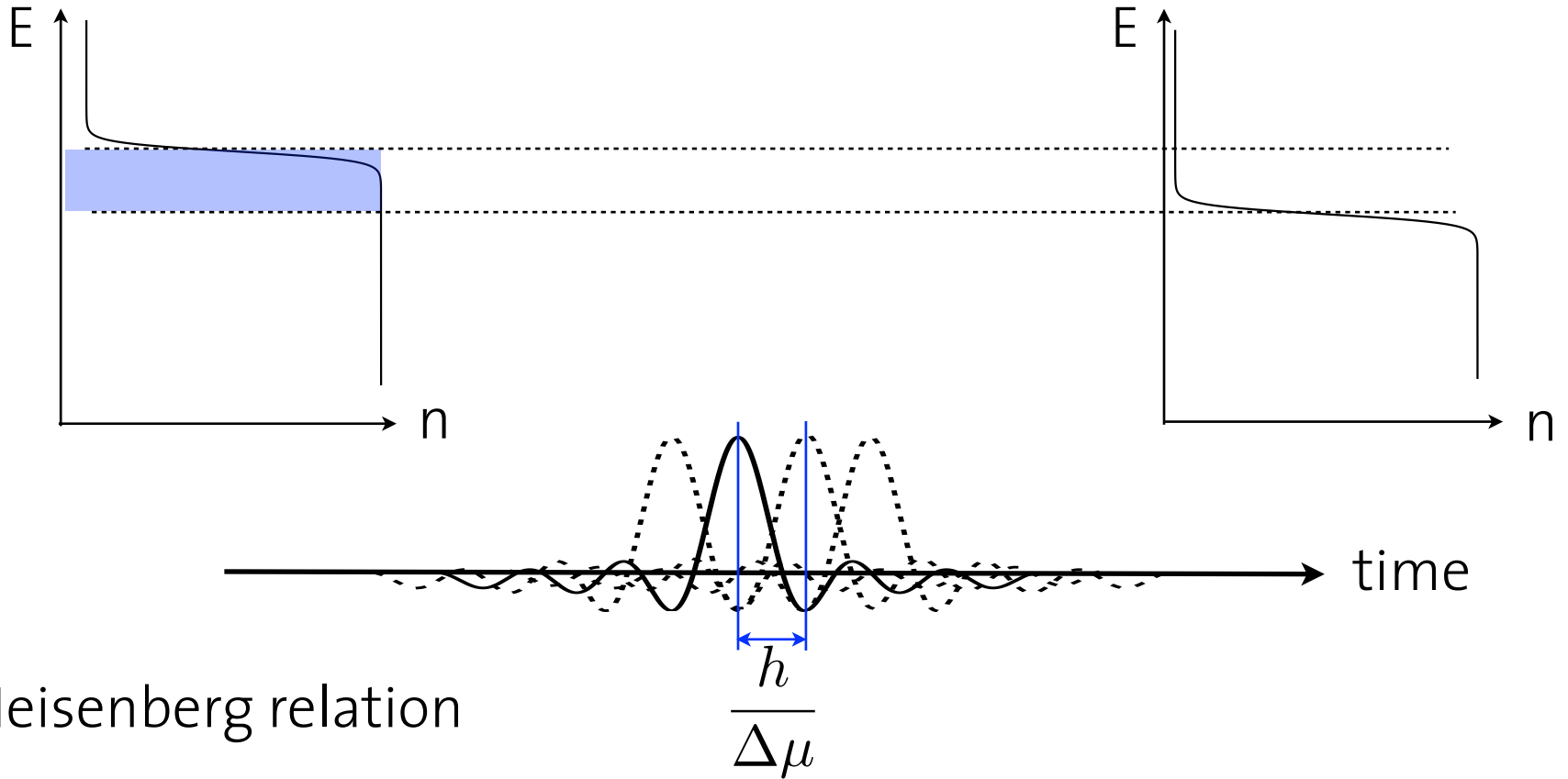
x-frequency	1 - 50 kHz
z-frequency	10 kHz
Chemical potential	$0.352 \mu\text{K} + V_g$
Temperature	42 nK

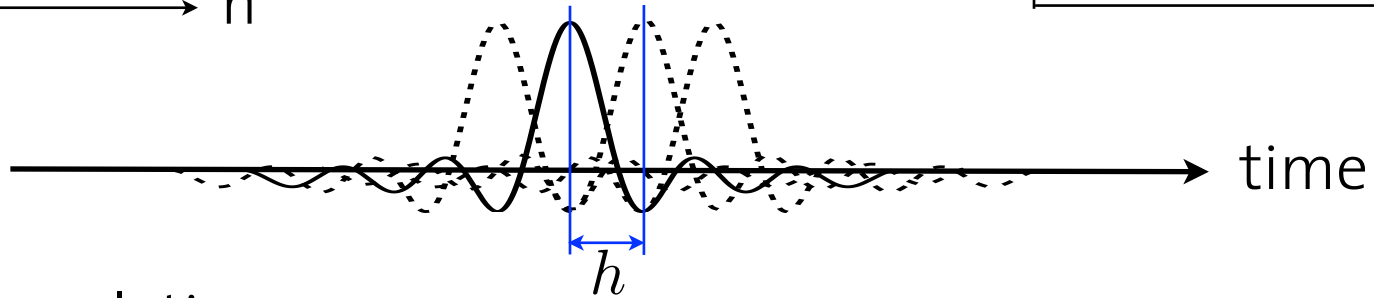
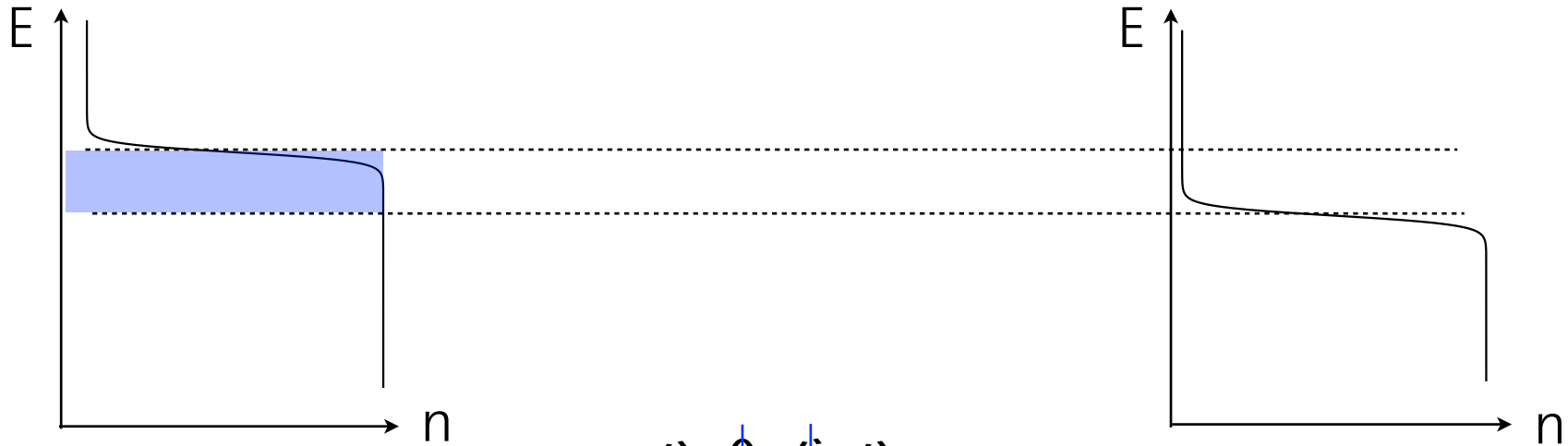


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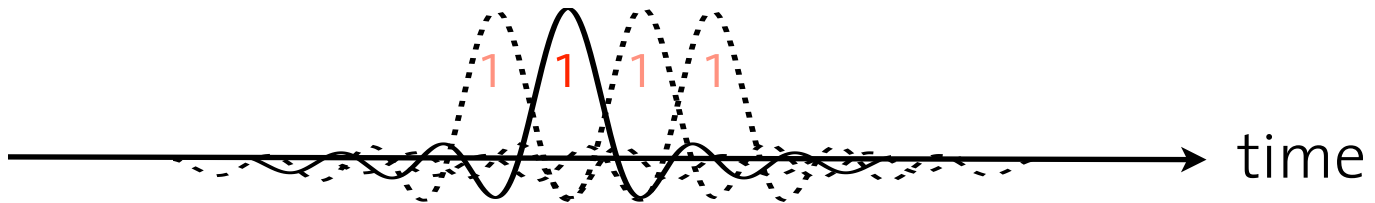




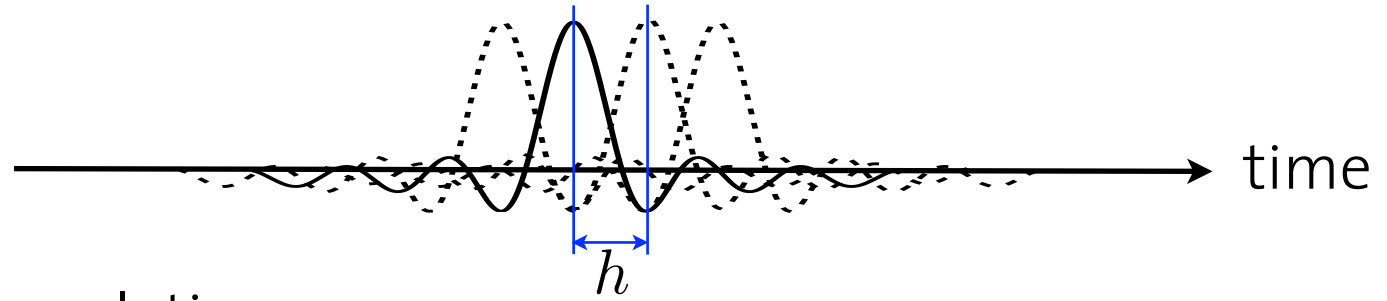


Heisenberg relation

$$\frac{h}{\Delta\mu}$$

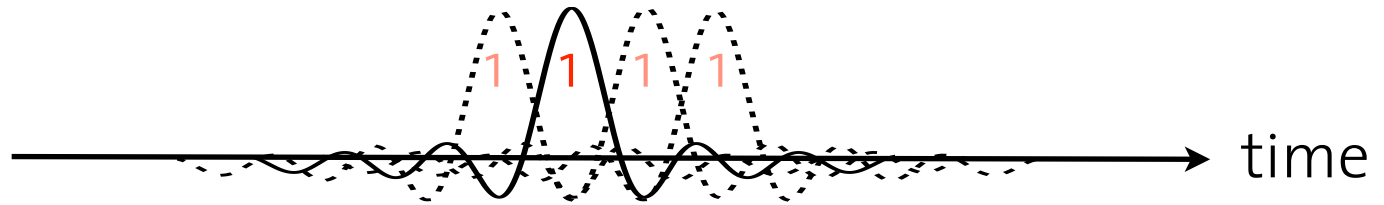


Pauli principle



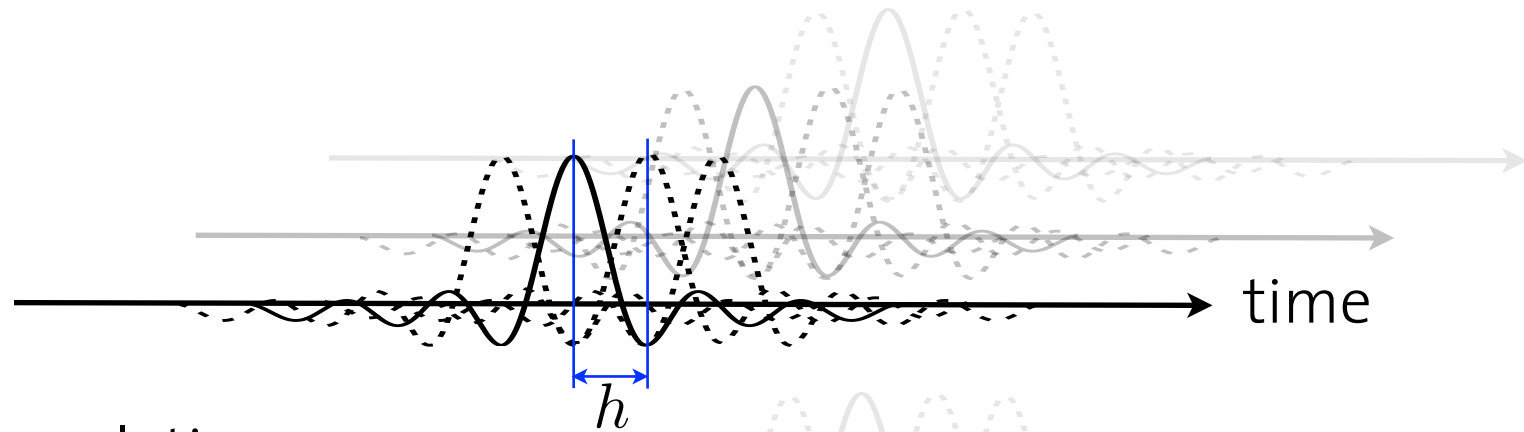
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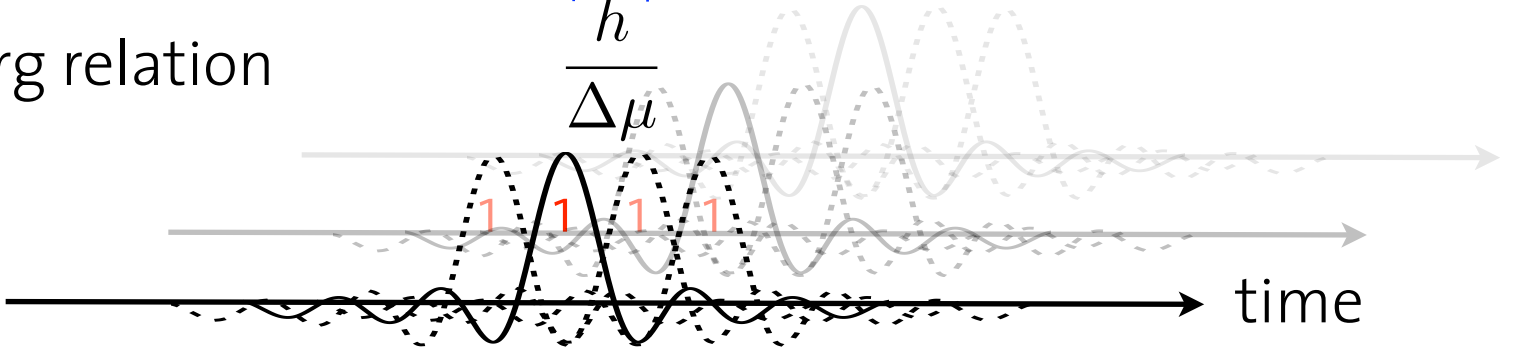


Pauli principle

$$I = \frac{\Delta\mu}{h}$$



Heisenberg relation



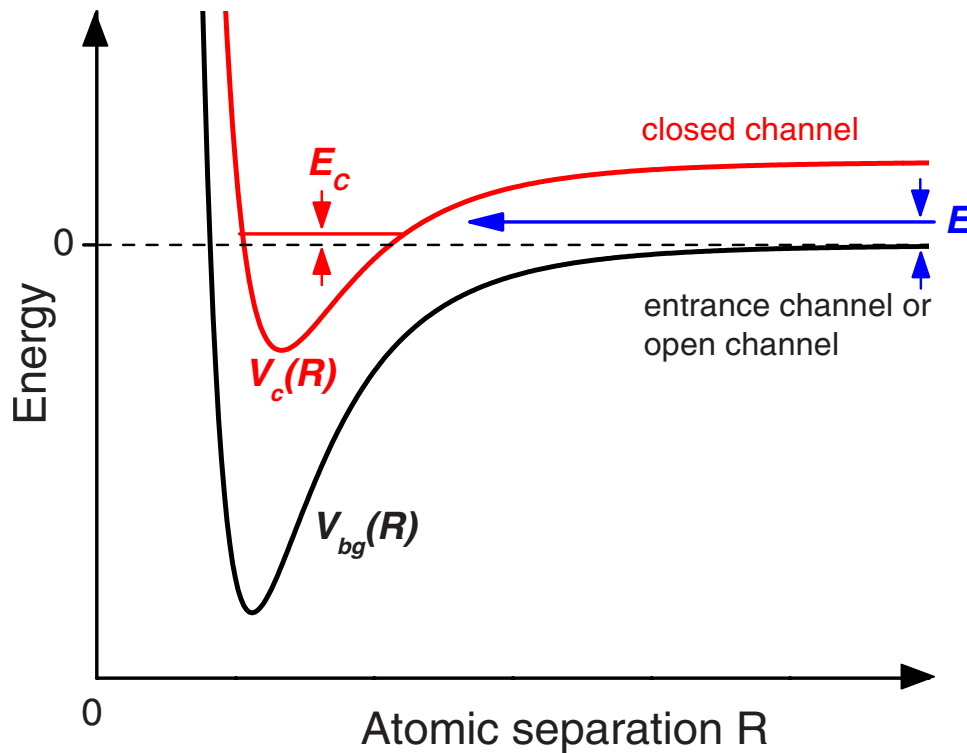
Pauli principle

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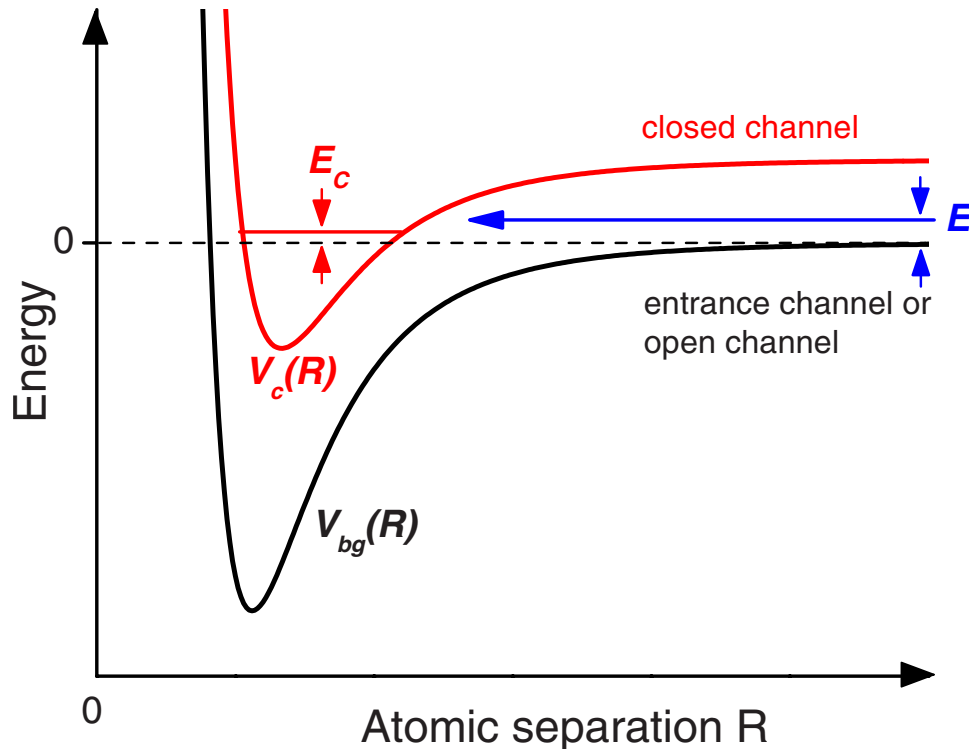
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# How do atoms interact ?



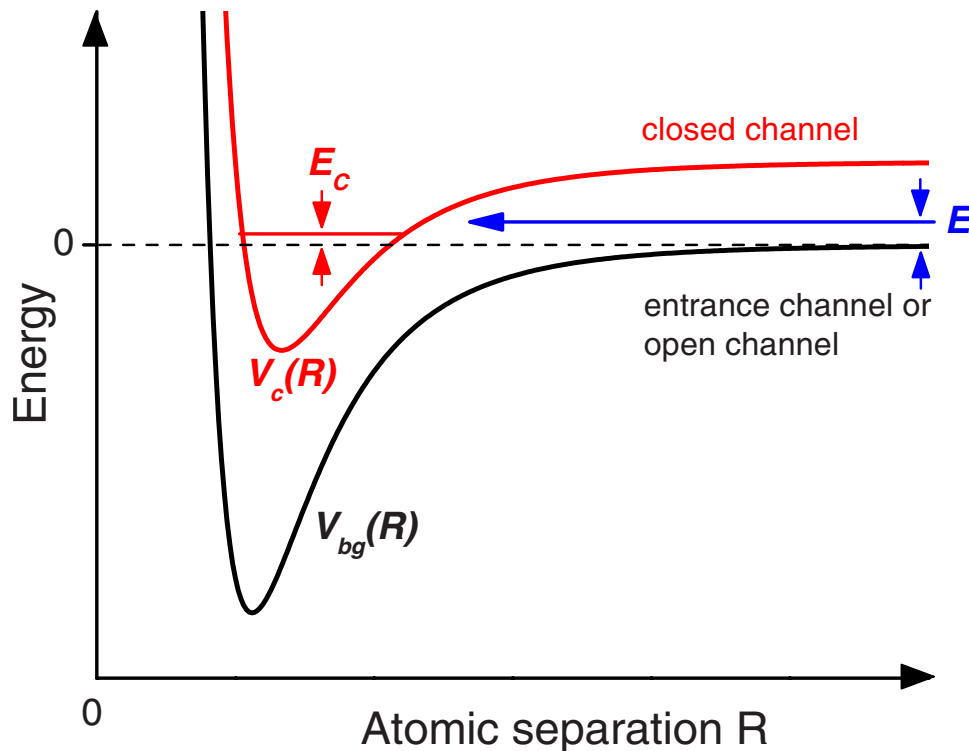
- van der Waals potential
- Depends on electrons spin orientation

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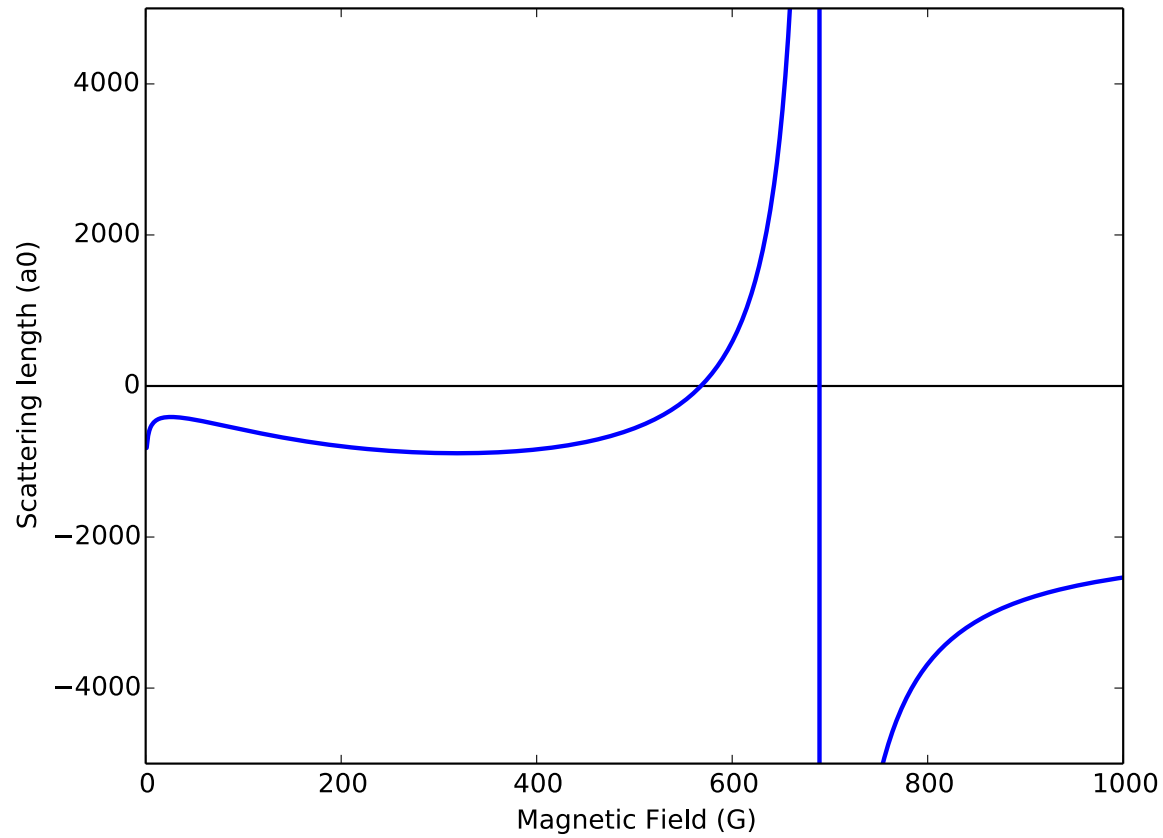
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  - Bound states in the singlet potential
  - B field: brings the bound state at the dissociation threshold of the triplet potential

# How do atoms interact ?

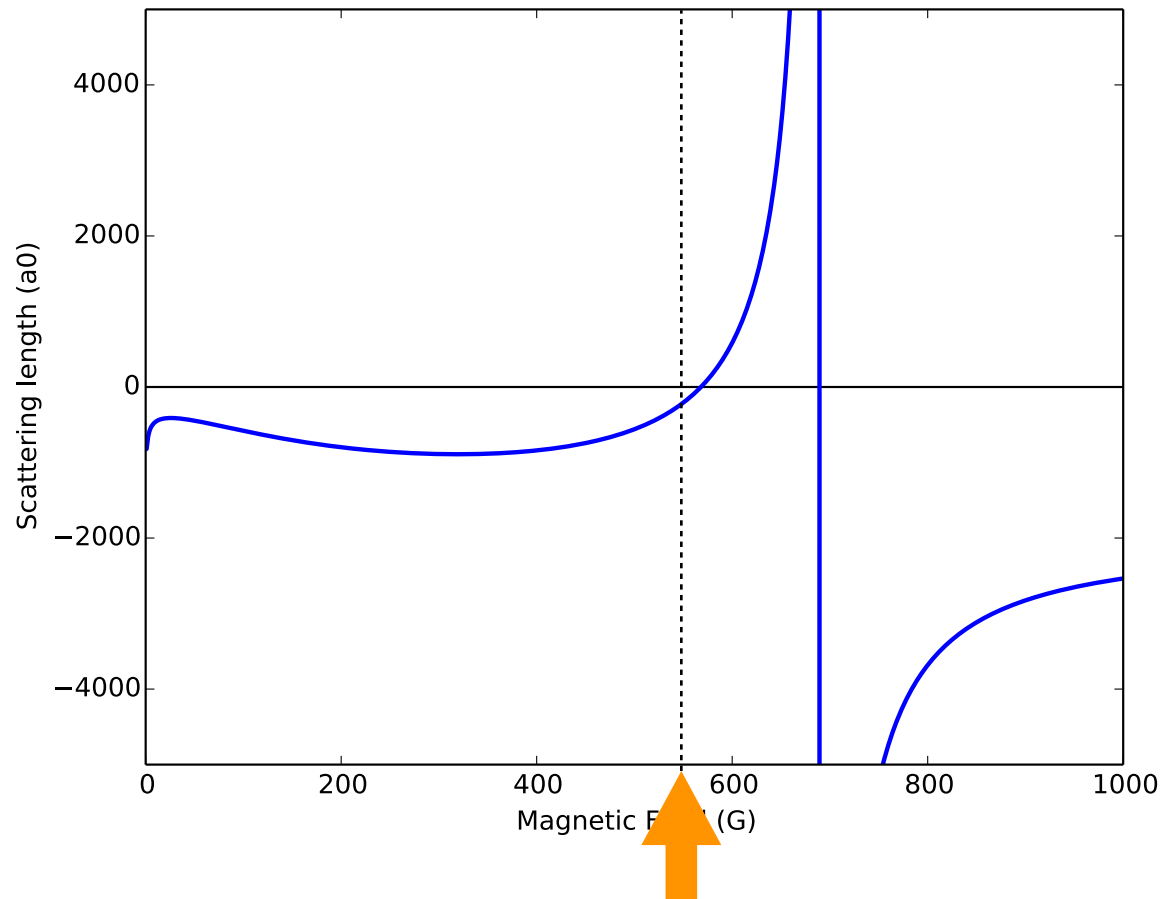


- van der Waals potential
  - Depends on electrons spin orientation
  - Bound states in the singlet potential
  - B field: brings the bound state at the dissociation threshold of the triplet potential
- Scattering resonance for any small channel coupling

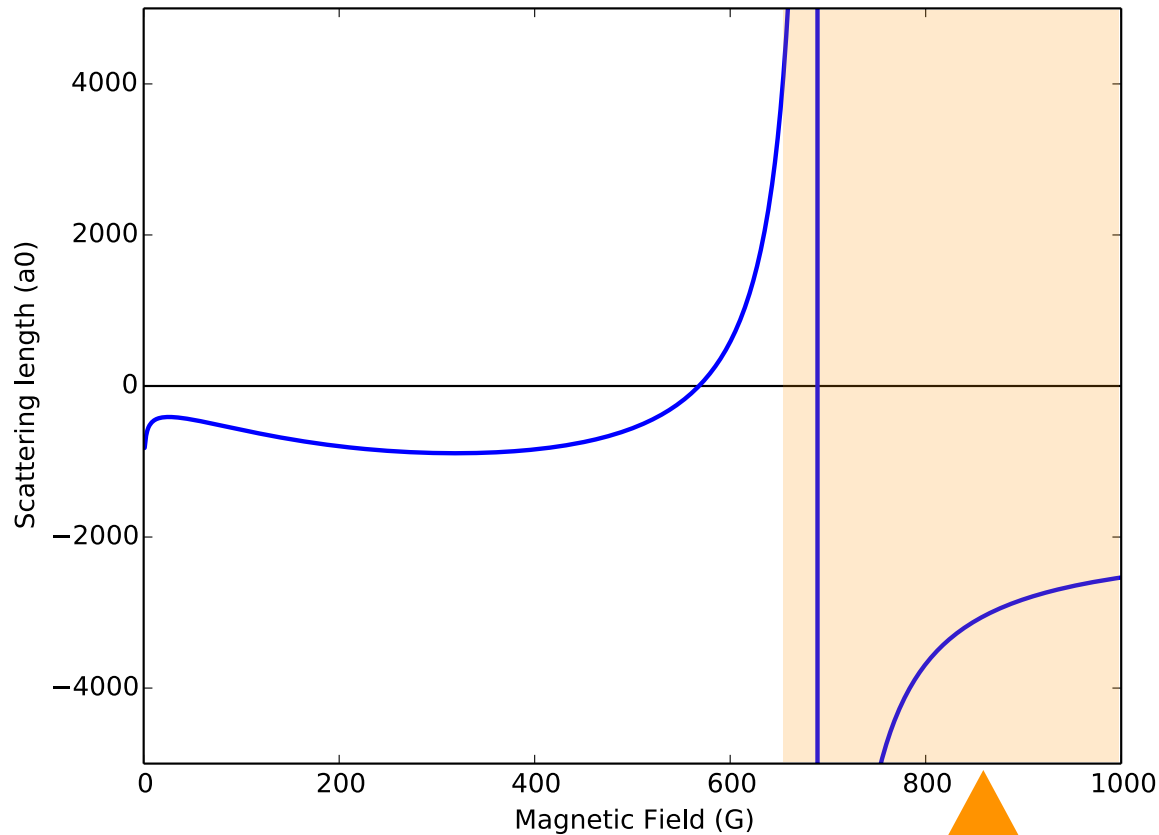
# Feshbach resonance



# Feshbach resonance

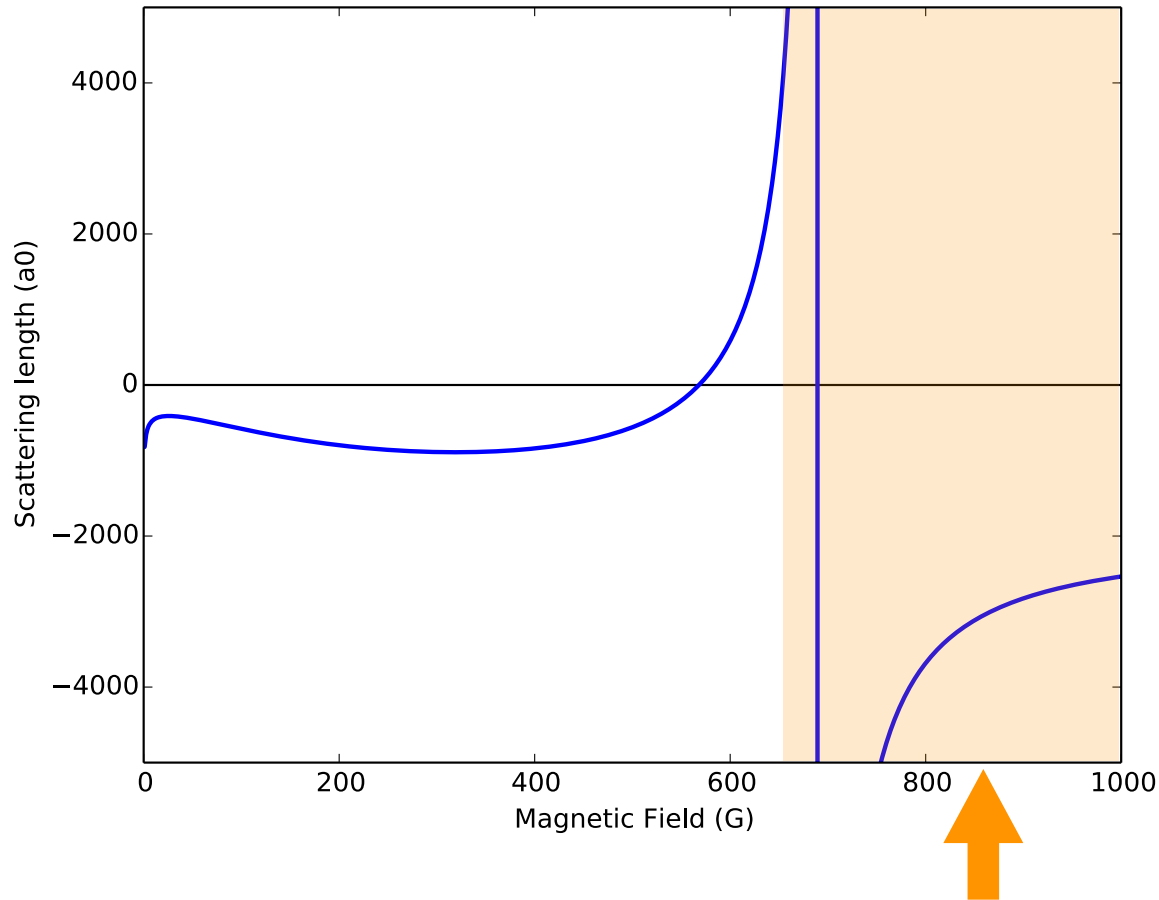


# Feshbach resonance



Equation of state : N. Navon *et al*, Science **328** 729 (2010)

# Feshbach

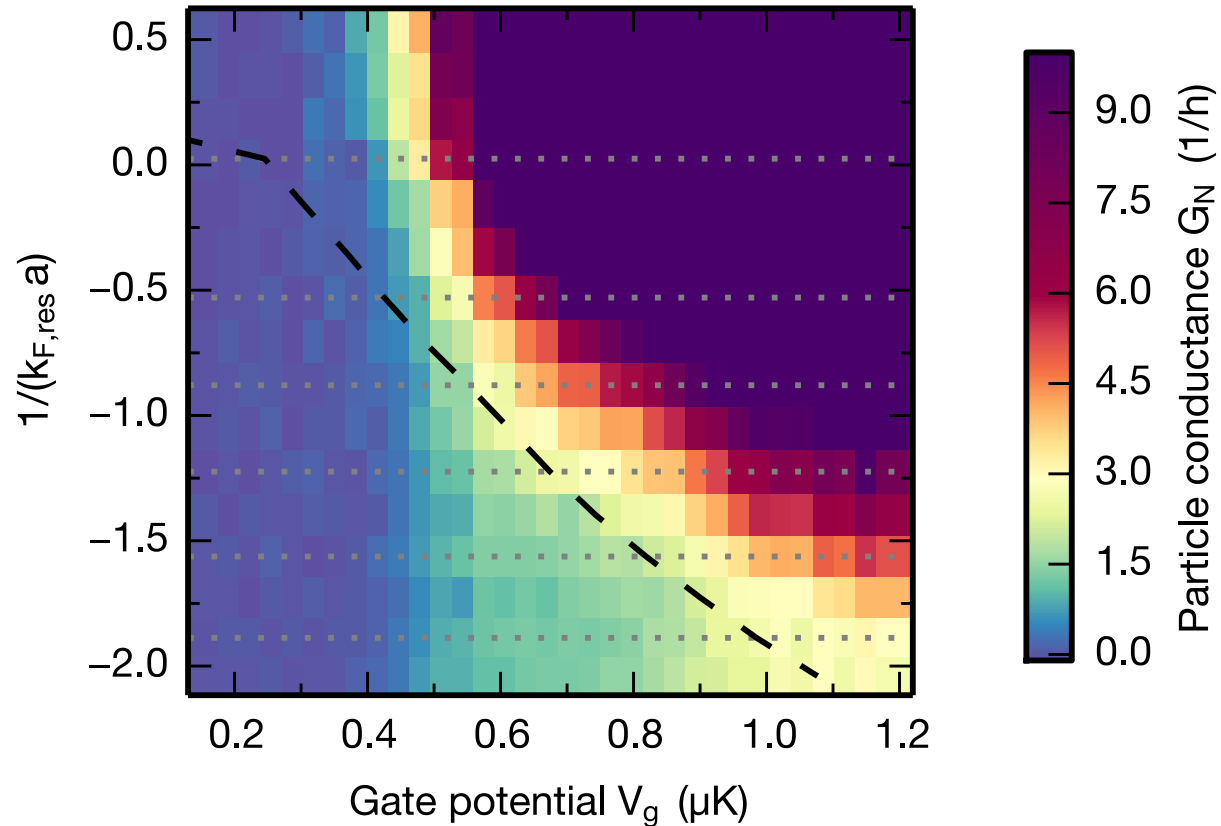


Equation of state : N. Navon *et al*, Science **328** 729 (2010)

- Many-body physics (BCS-BEC crossover):
  - Attractive interactions lead to Cooper pairing at low Temperature
  - Negative  $a$ : BCS type pairing / Positive  $a$ : chemically bound molecules form a BEC

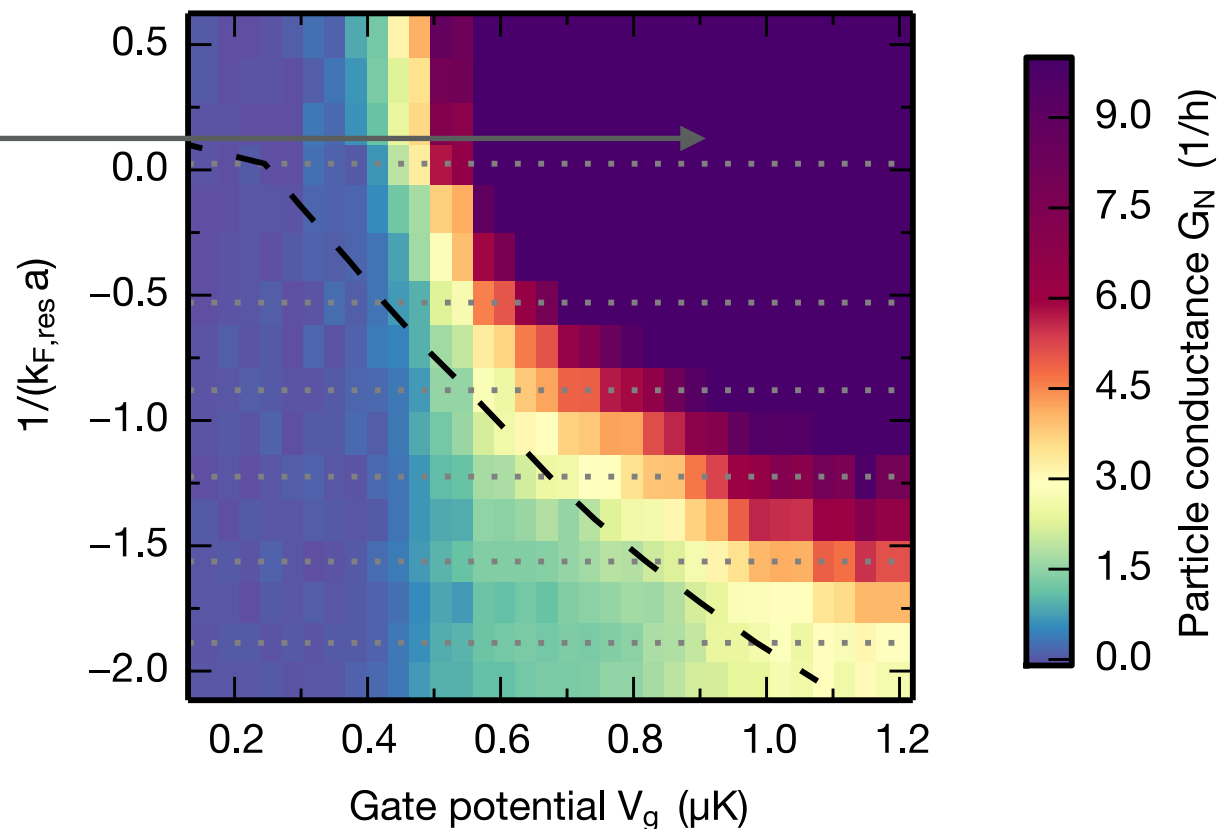


# Interactions: from weak to strong

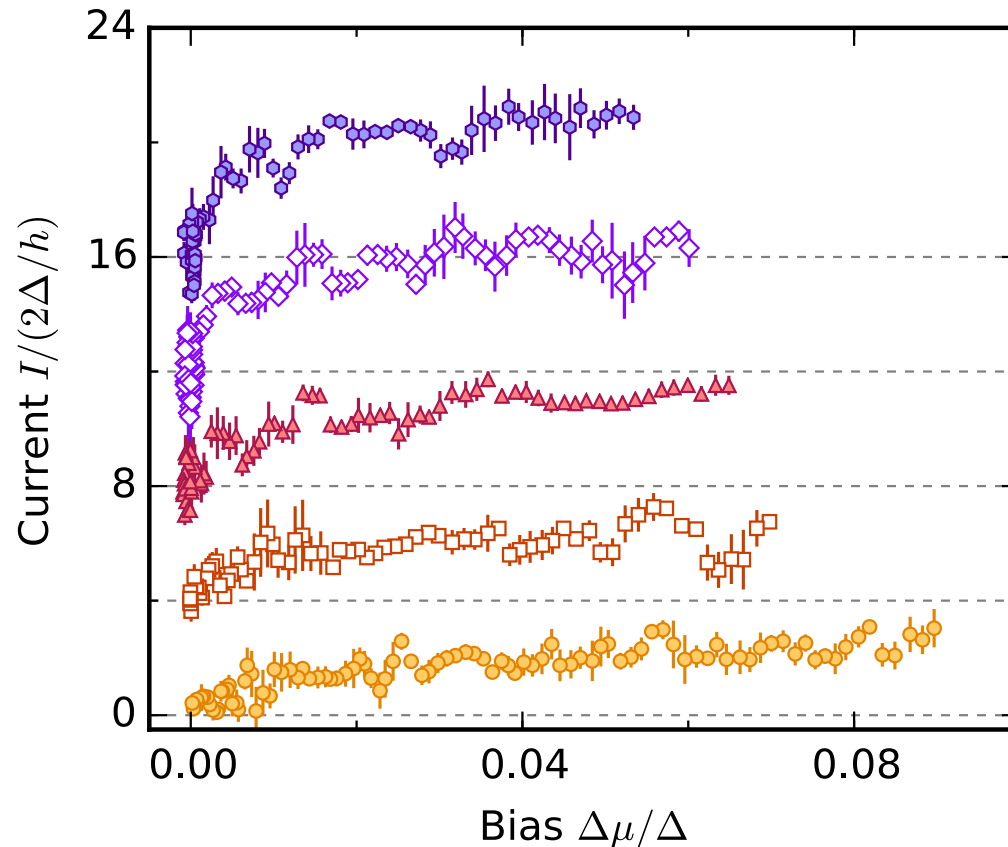


# Interactions: from weak to strong

Superfluid regime

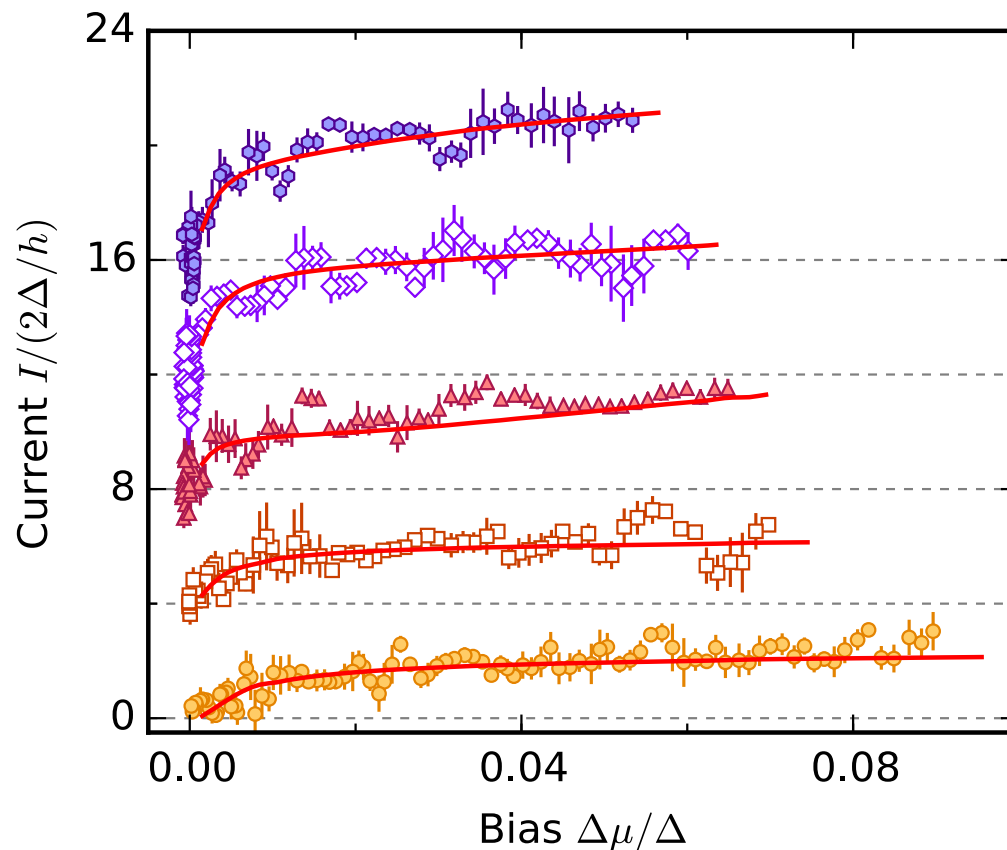


# Superfluid regime: non linear response



*At unitarity, the physics is universal:  
equation of state and pairing gap are known*

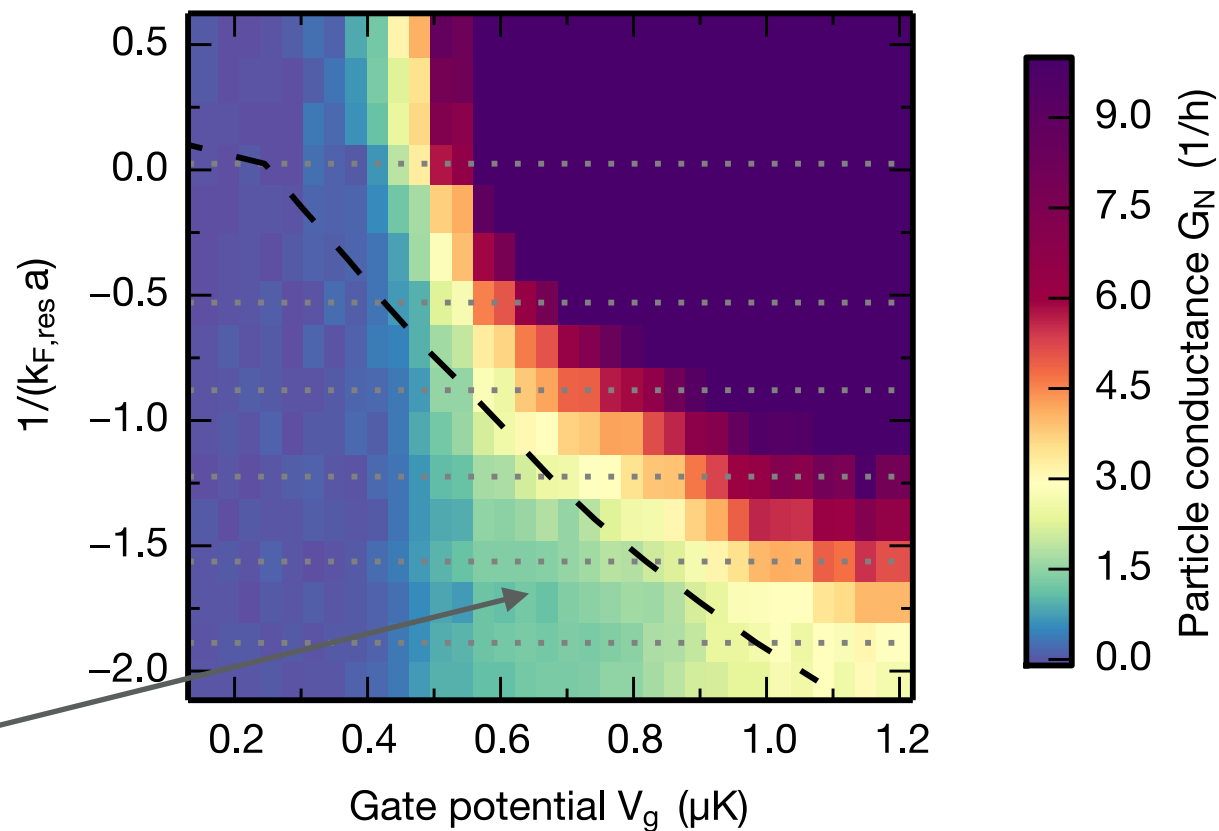
# Superfluid regime: non linear response



Multiple Andreev Reflection theory

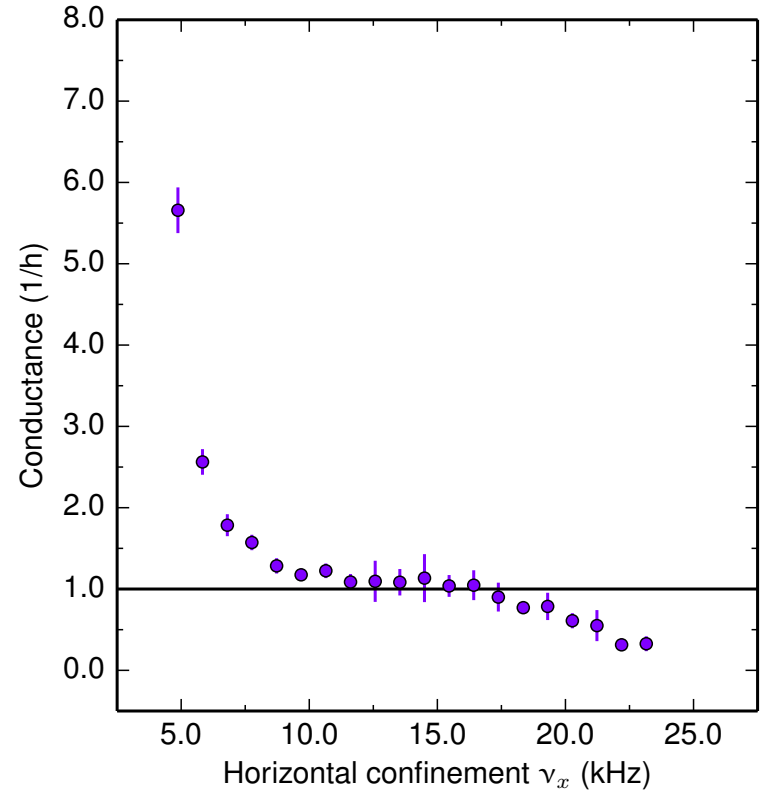
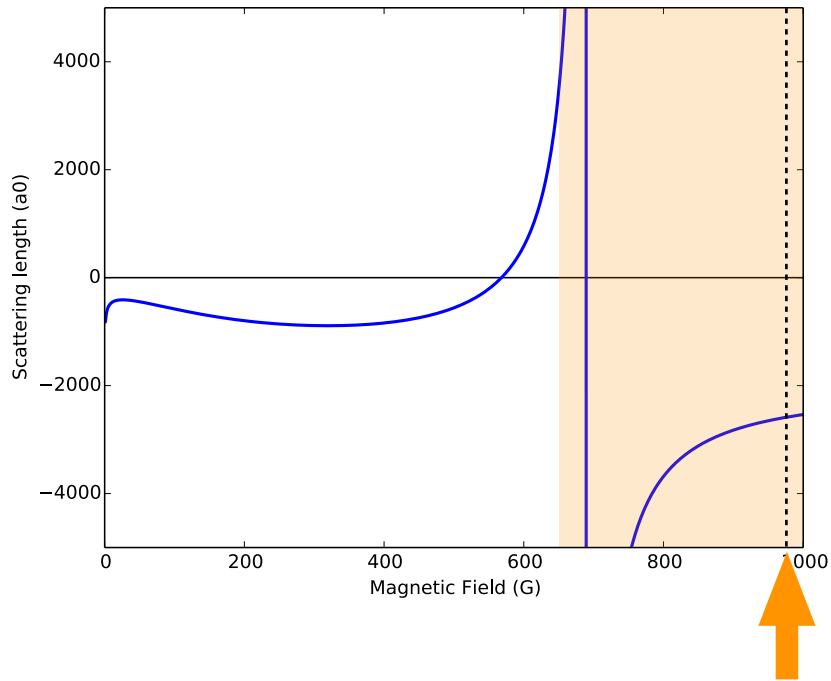
*S. Uchino and T. Giamarchi*

# Interactions: from weak to strong

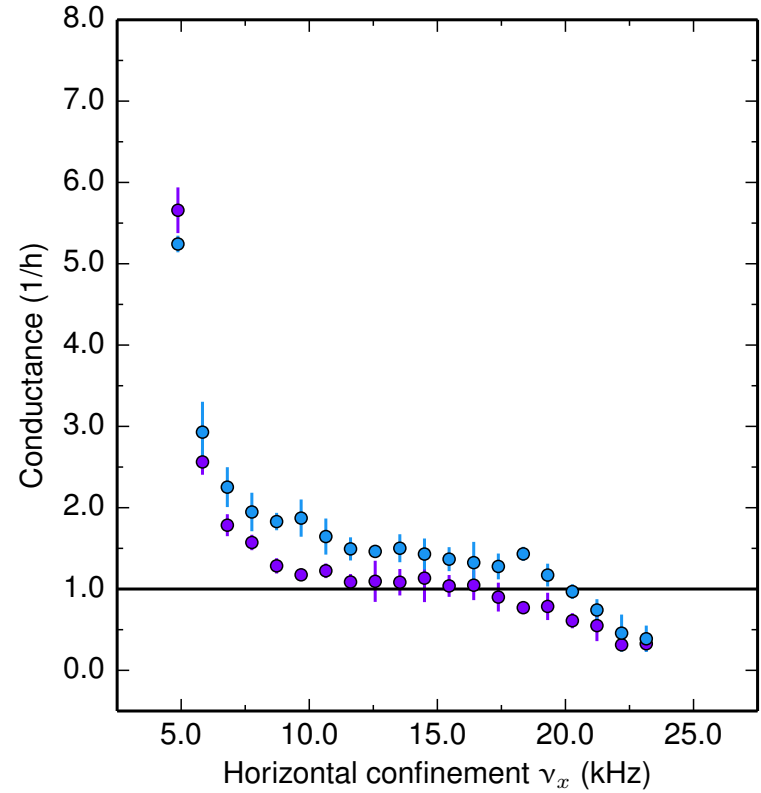
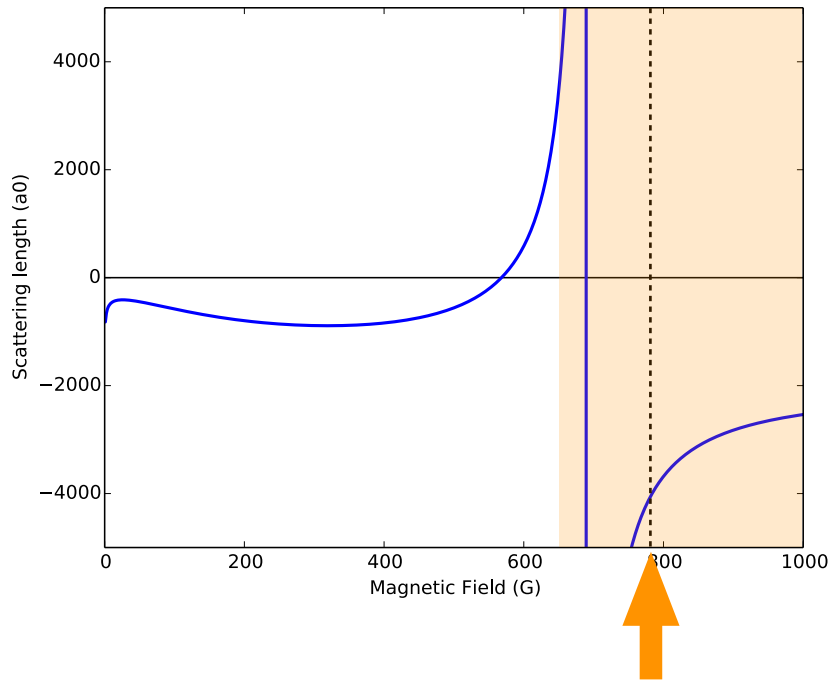


Normal regime

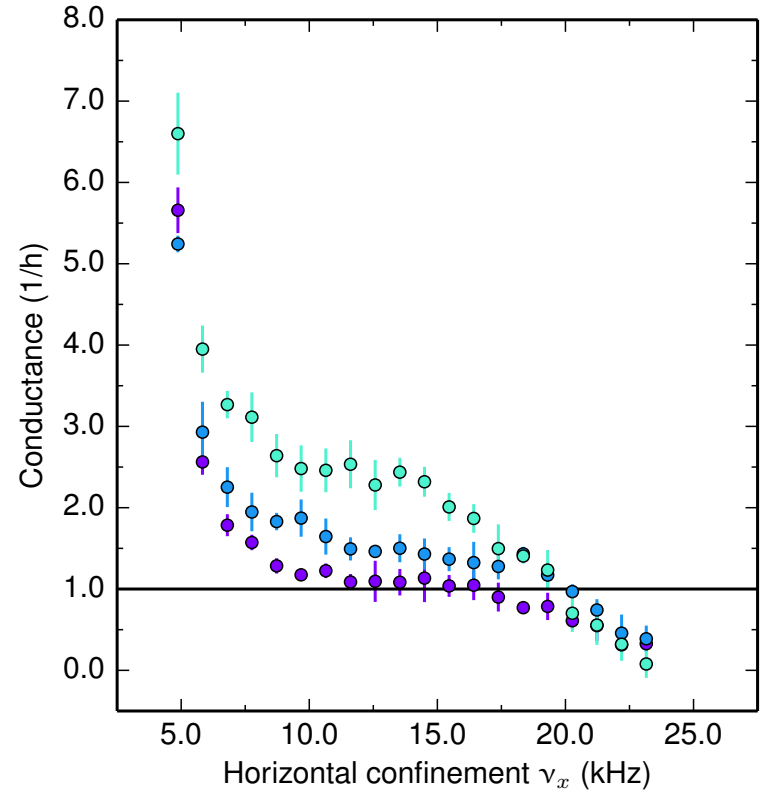
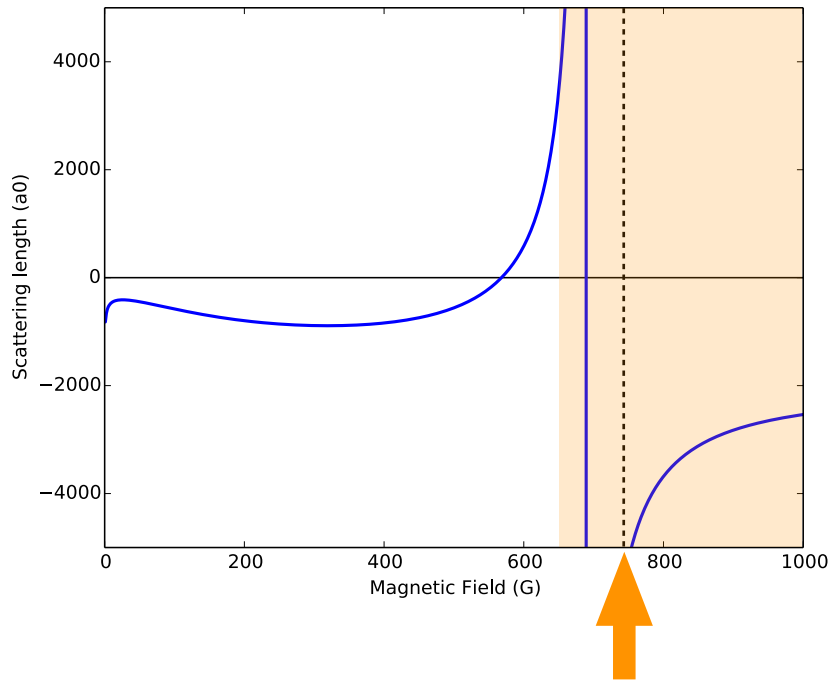
# How normal is the 'normal' regime ?



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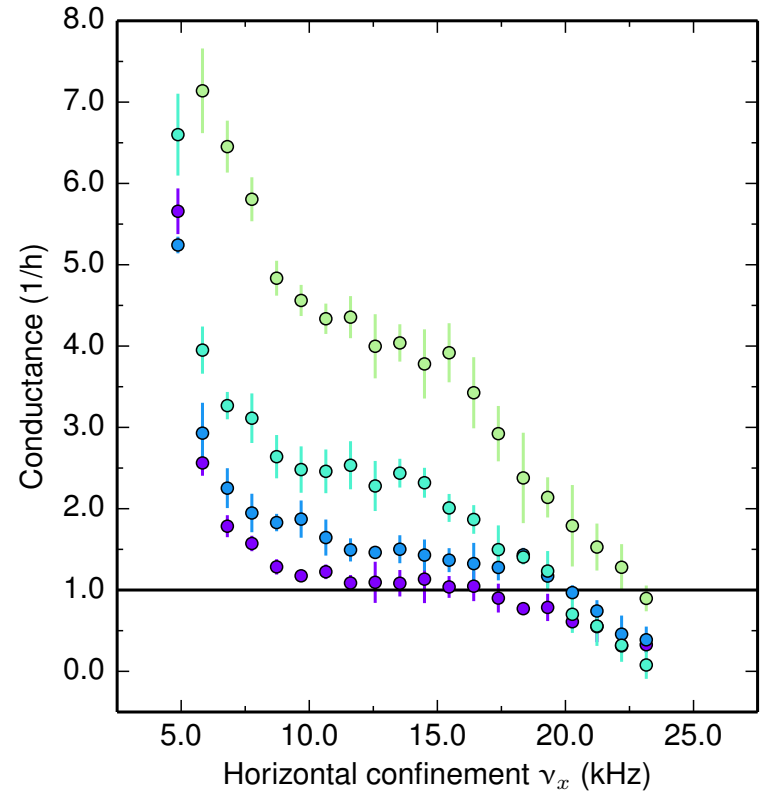
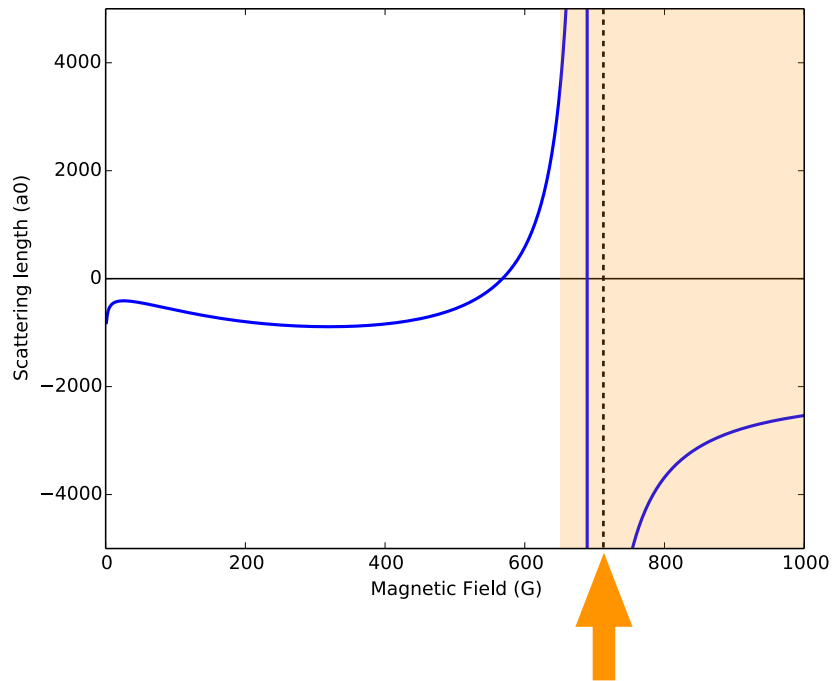


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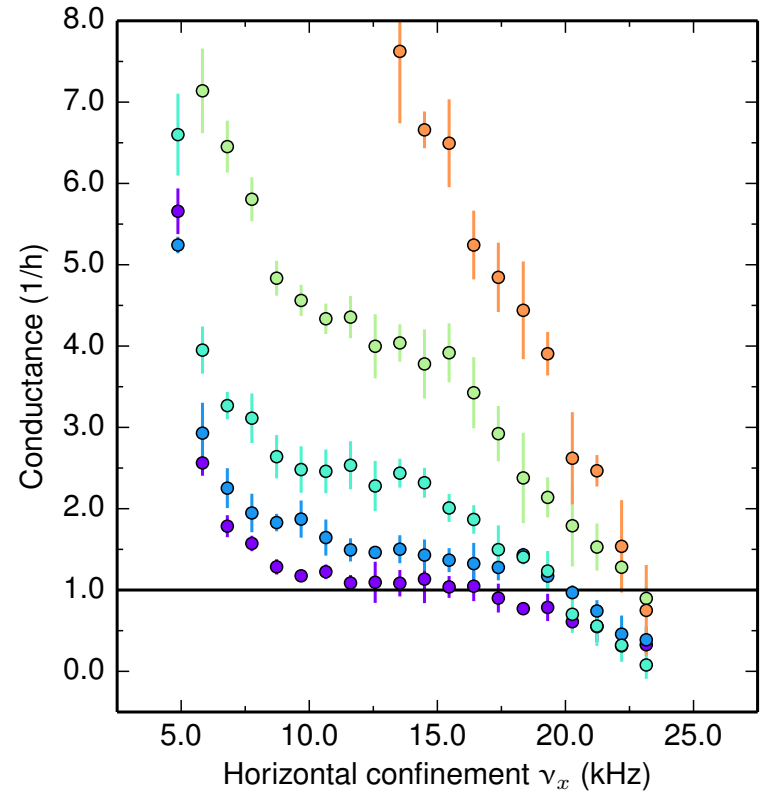
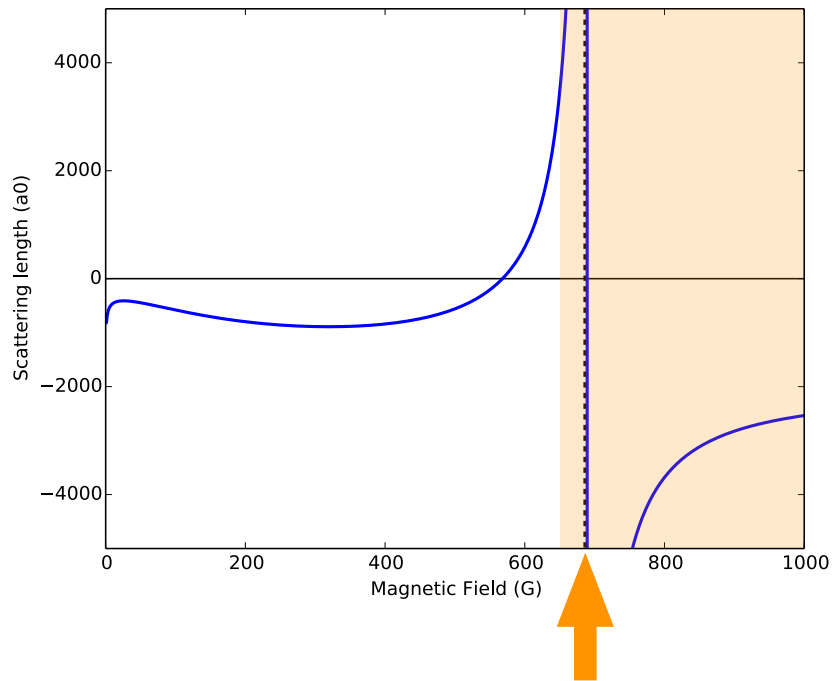




# How normal is the 'normal' regime ?



# How normal is the 'normal' regime ?



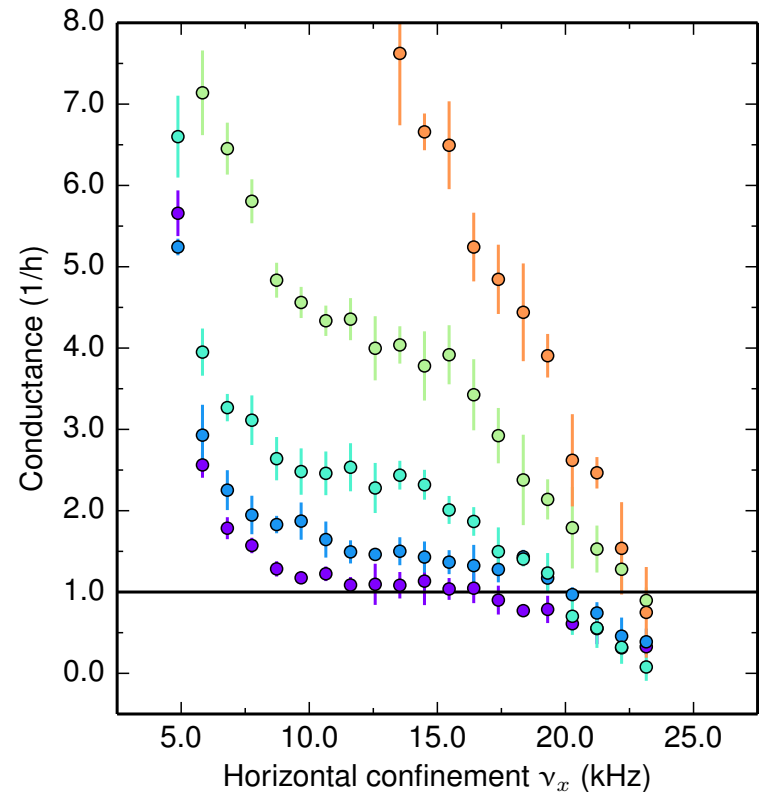
## How normal is the 'normal' regime ?

- Conductance plateau above  $1/h$  ?
- confinement induced pairing
- superfluid fluctuations in the leads

M. Kanász-Nagy, L. Glazman, T. Esslinger, E. A. Demler  
PRL **117**, 255302 (2016)

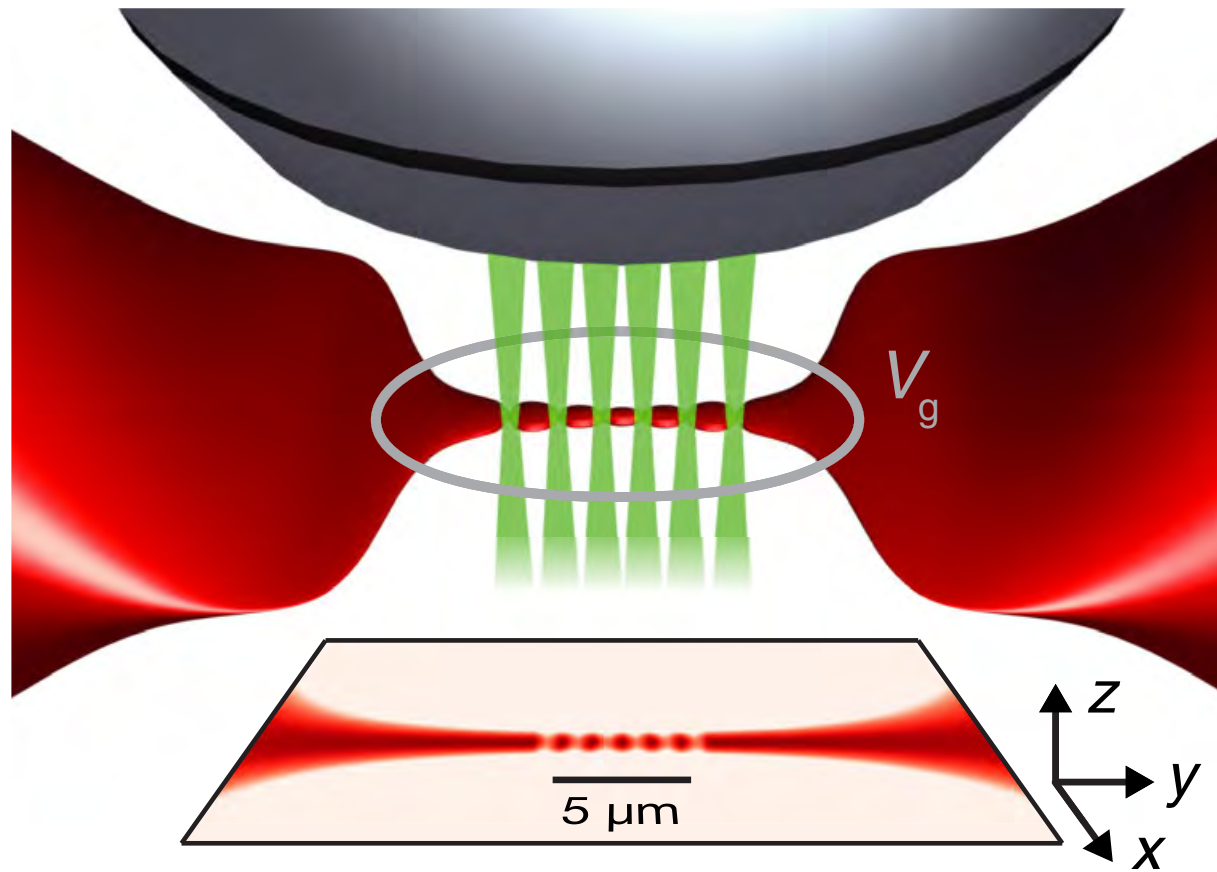
S. Uchino and M. Ueda  
PRL **118**, 105303 (2017)

B. Liu, H. Zhai and S. Zhang  
PRA **95**, 013623 (2017)



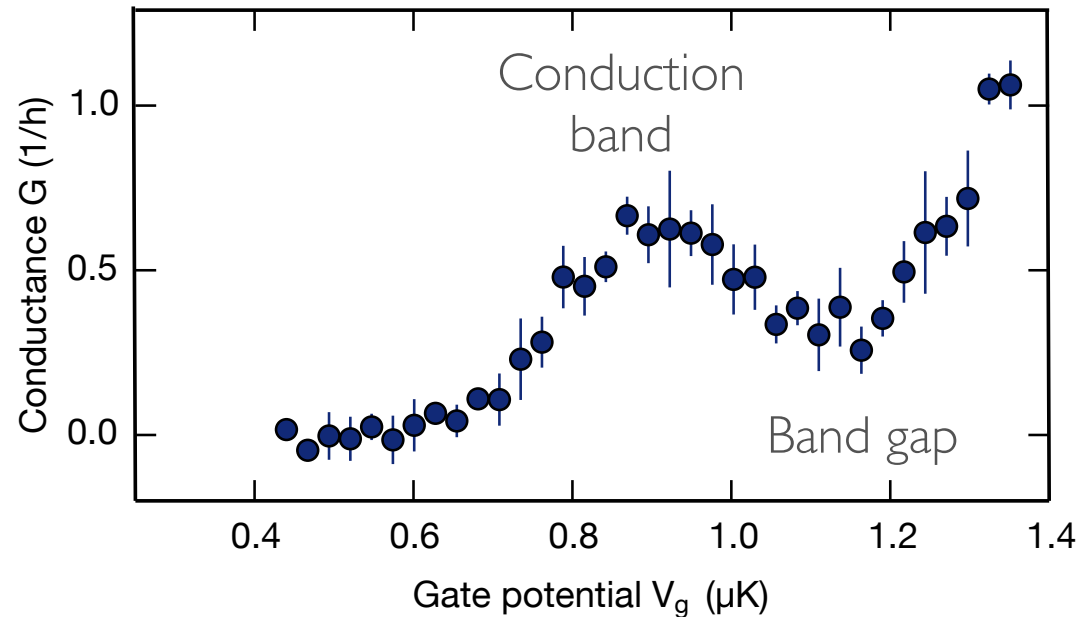
# Microscopic control: lattice patterns

Theory by P. Grisins and T. Giamarchi, University of Geneva

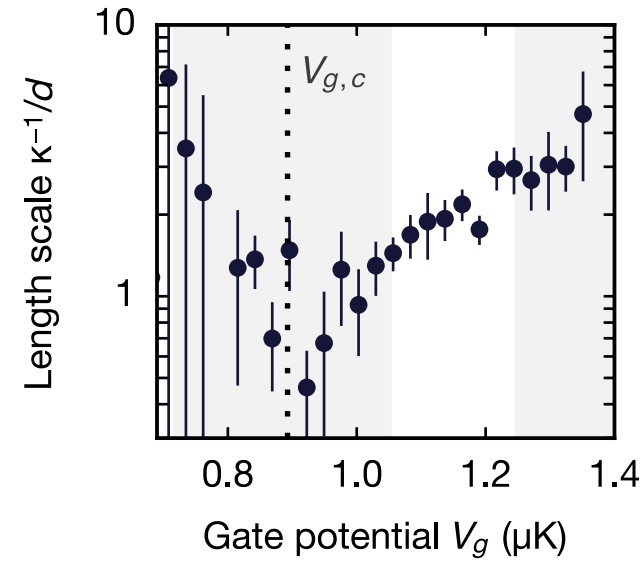
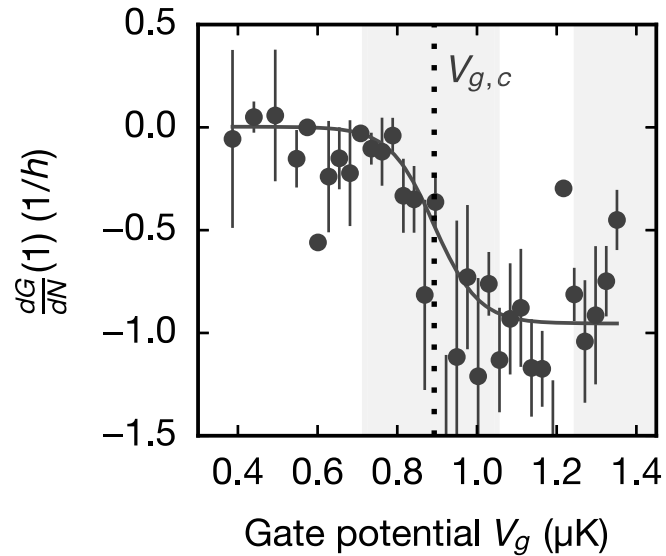
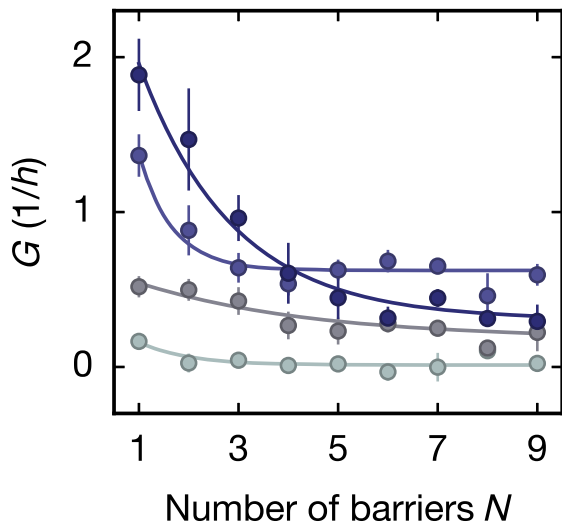


# Band structure in transport

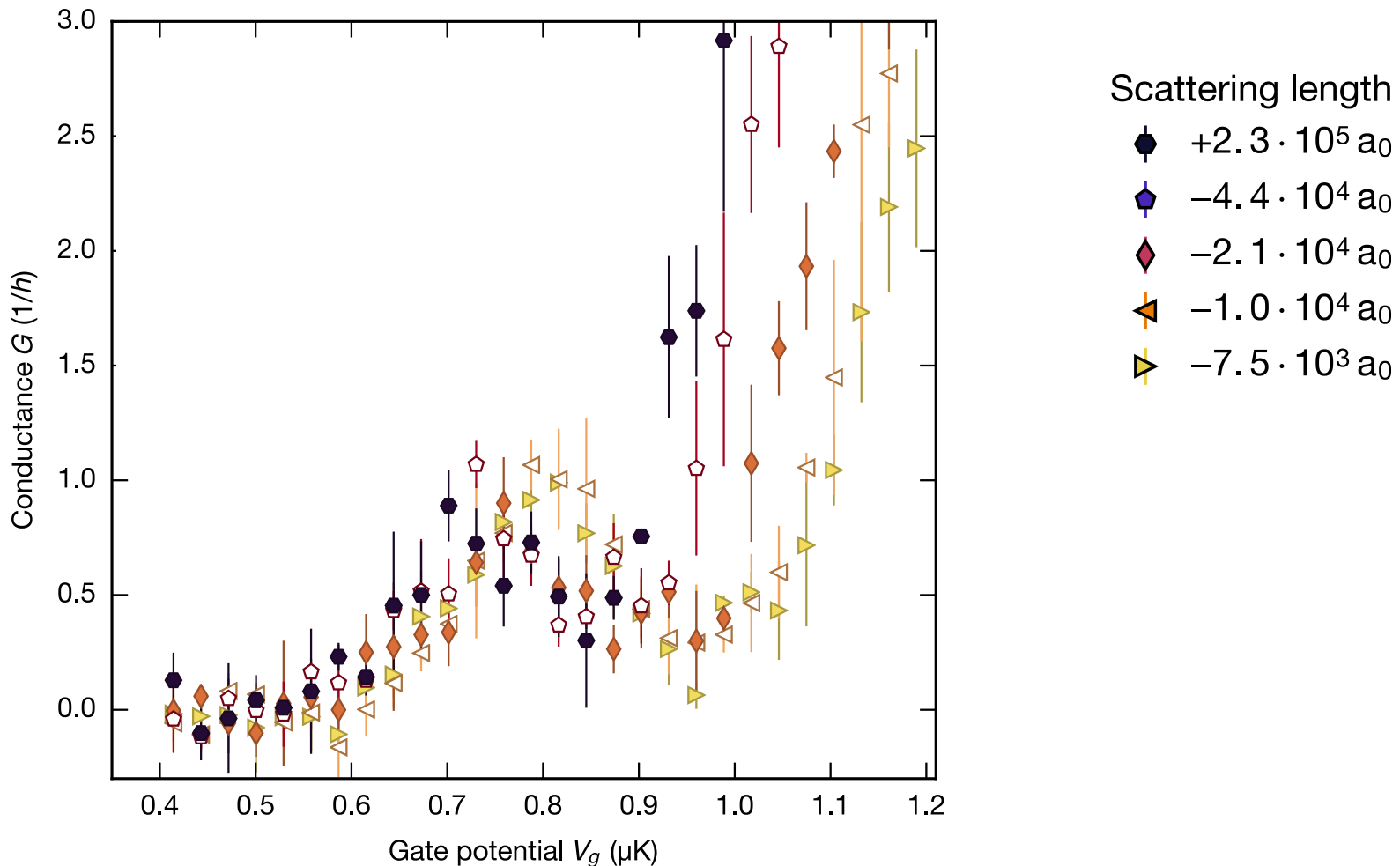
- 9 consecutive barriers
- Single mode quantum wire
- Height  $0.95 E_R$



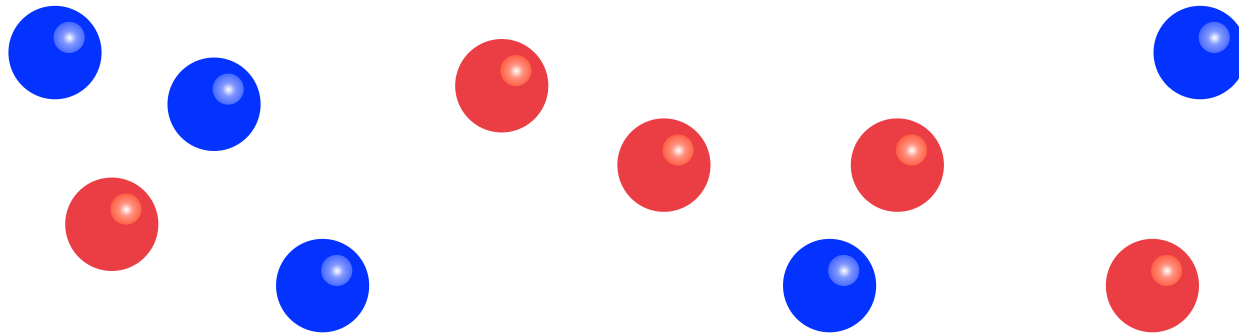
# Finite size scaling



# From weak to strong interactions

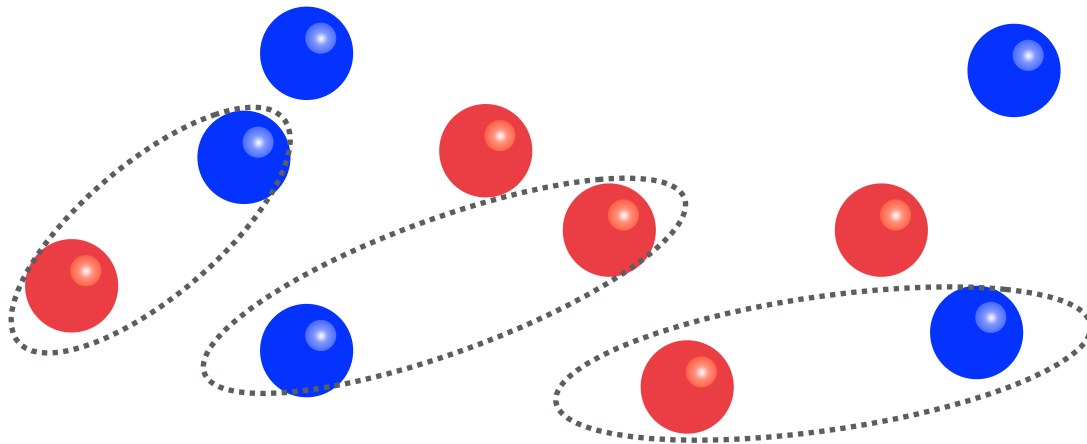


# From weak to strong interactions

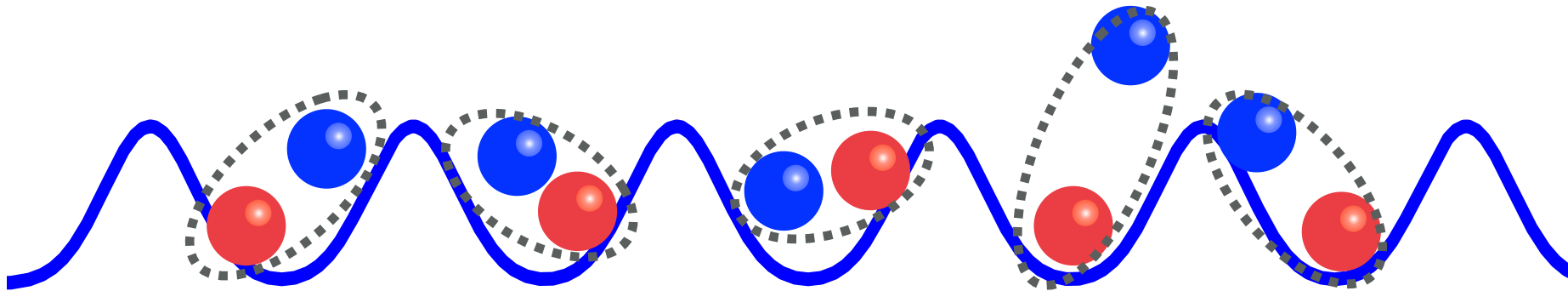




# From weak to strong interactions



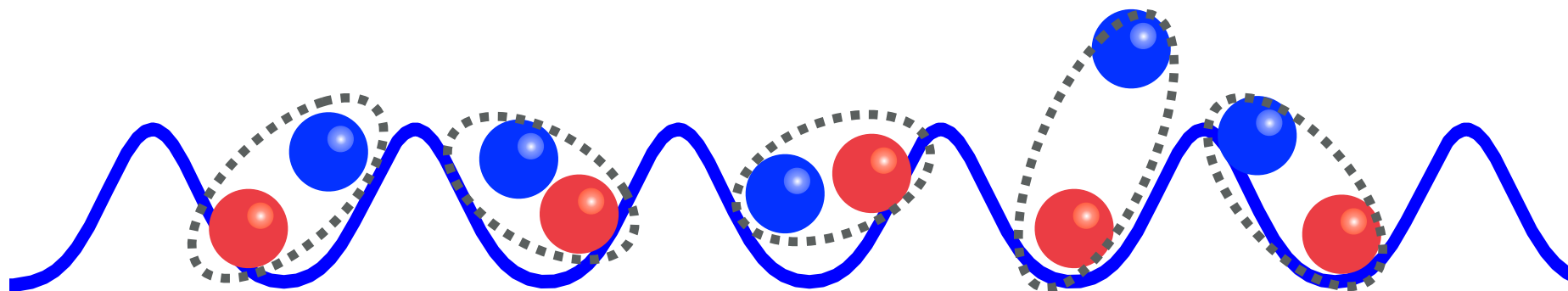
# From weak to strong interactions



# From weak to strong interactions

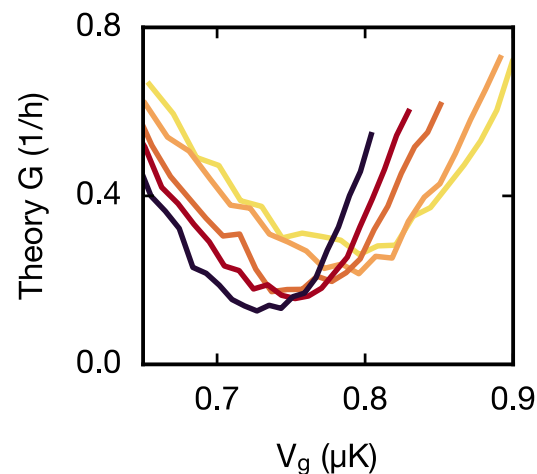
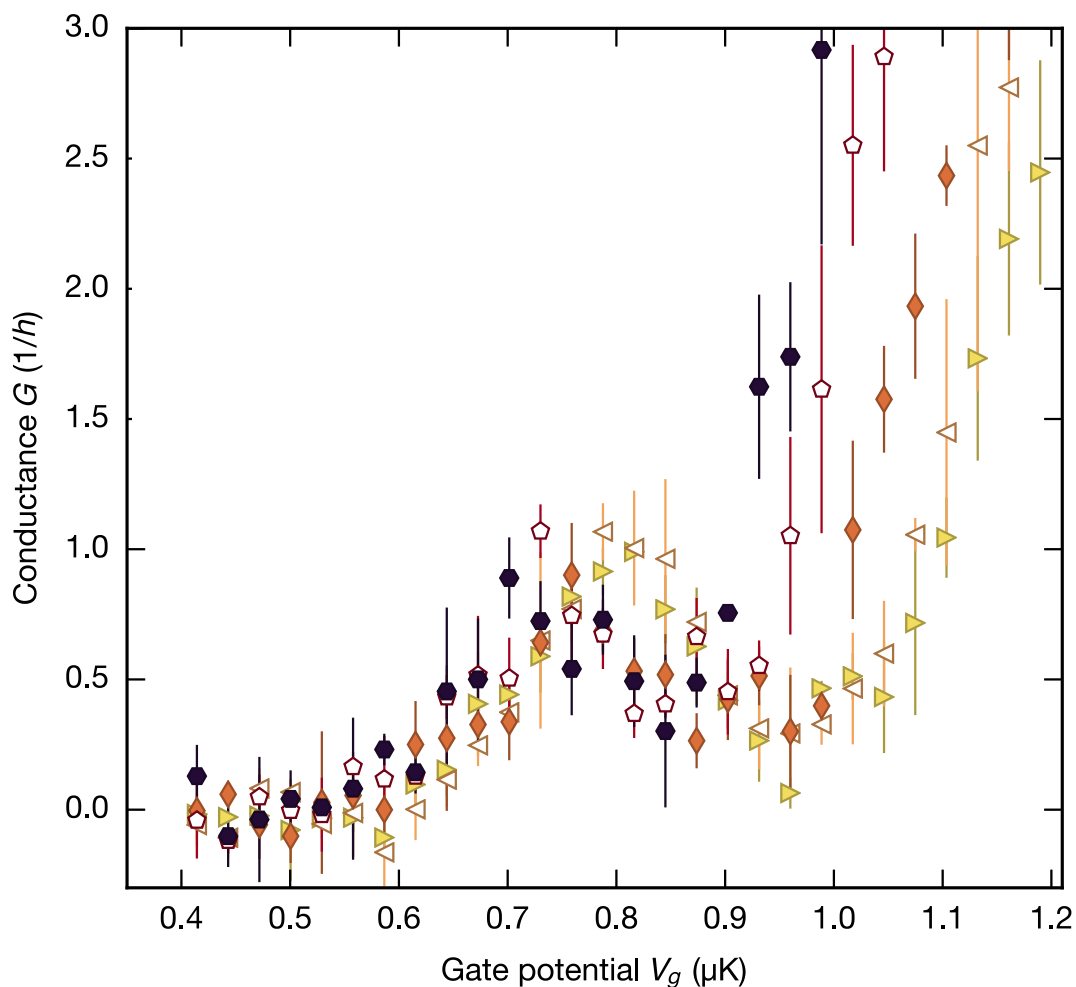
Gapped spin excitations + strong pair repulsion

*Luther-Emery liquid  
pinned to the weak lattice*



*Theory by P. Grisins and T. Giamarchi, University of Geneva*

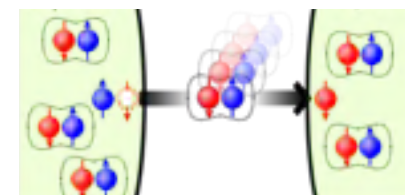
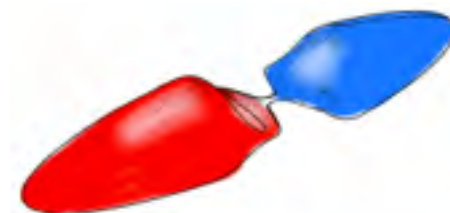
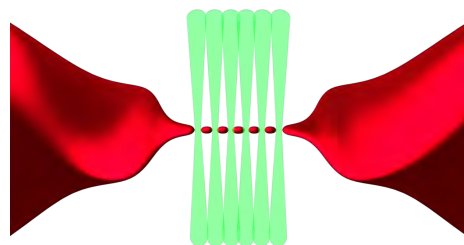
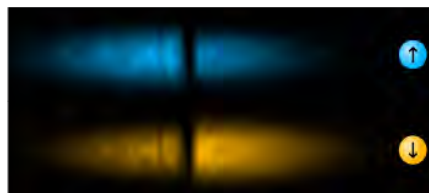
# Luttinger liquid model



# Summary

## Mesoscopic transport

- Quantum point contact
- Thermoelectric transport
- Spin Transport
- Superfluid flow
- Scanning gate microscope
- ...



*Review Article:*

S. Krinner, T. Esslinger and J.P. Brantut,  
Journal of Physics: Condensed Matter **29**, 343003 (2017)

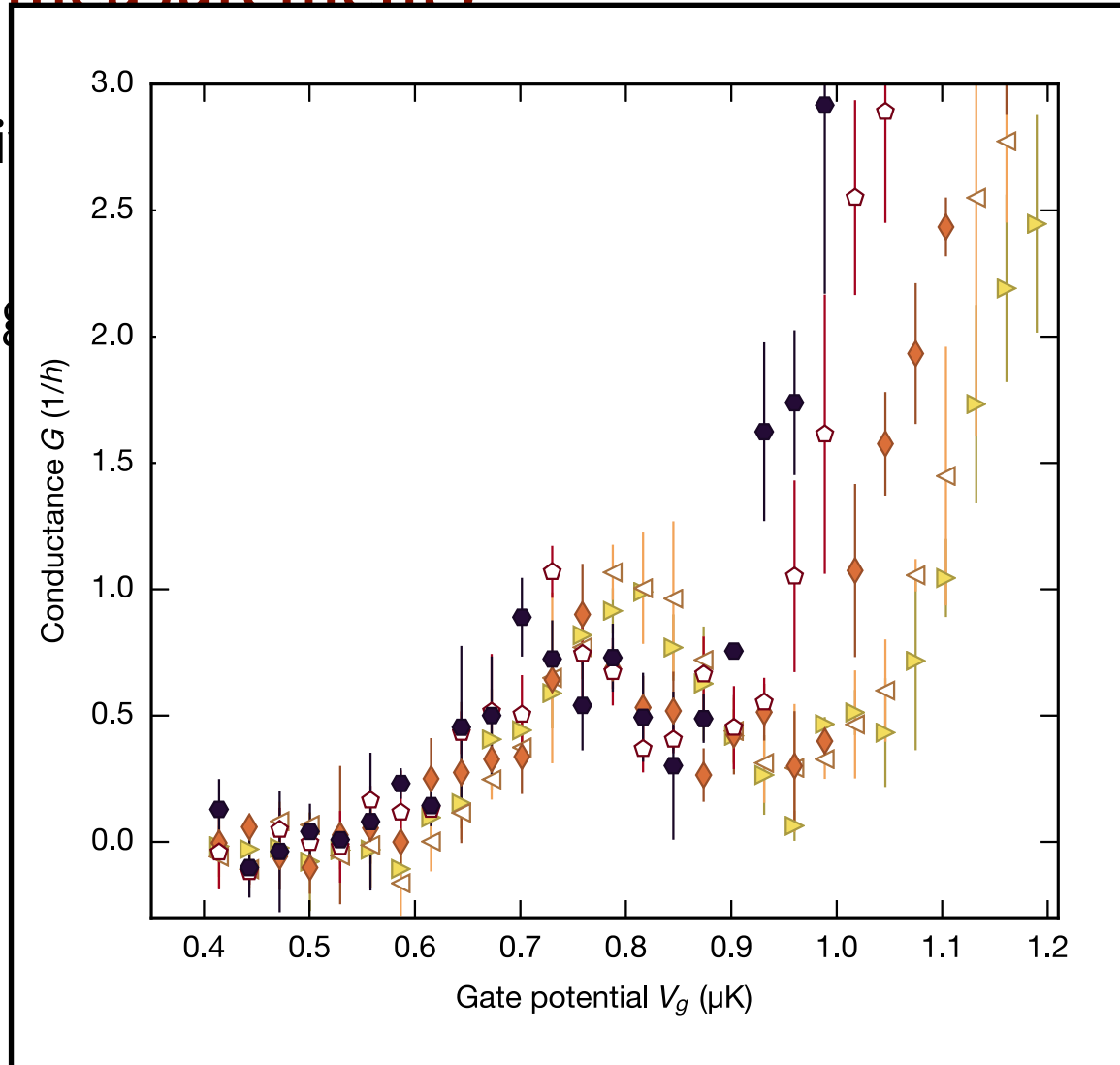
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# Transport measurements

- **Destructive** measurements of the **total** atom number
- Observing transport implies **sample-to-sample comparison**

# Transport measurements

- Destructive
- Observing



er  
parison

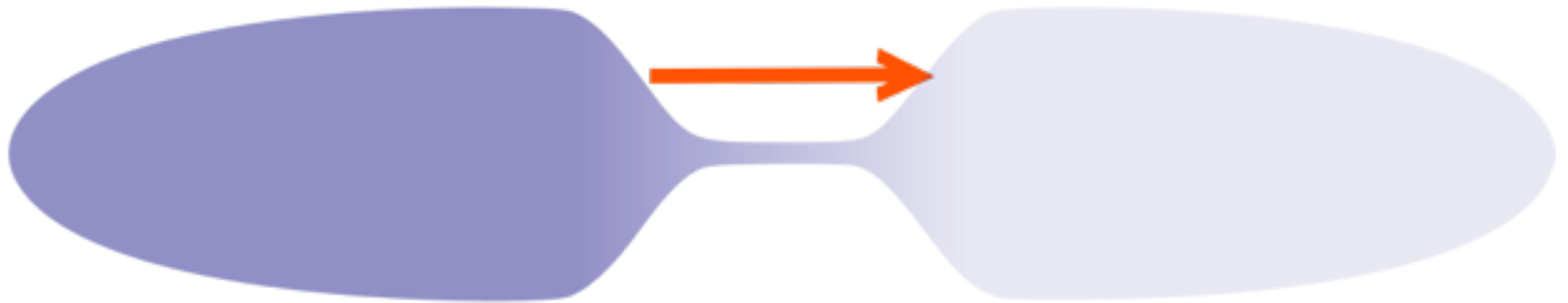


# Transport measurements

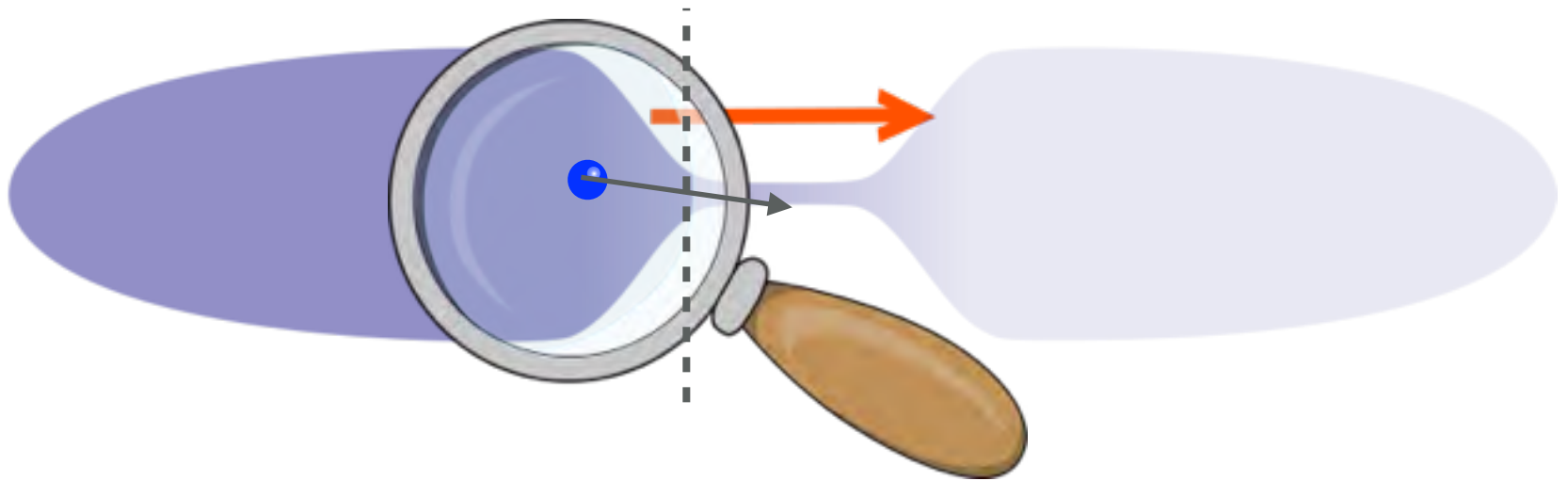
- **Destructive** measurements of the **total** atom number
- Observing transport implies **sample-to-sample comparison**
  - Total number of atoms :  $10^5$
  - Chemical potential : 10 kHz
  - Chemical potential bias : 1 kHz  $\implies I = 1000 \text{ at.s}^{-1}$

*Signal is about 1% for a fully open point contact*

# 'Ideal' transport measurement

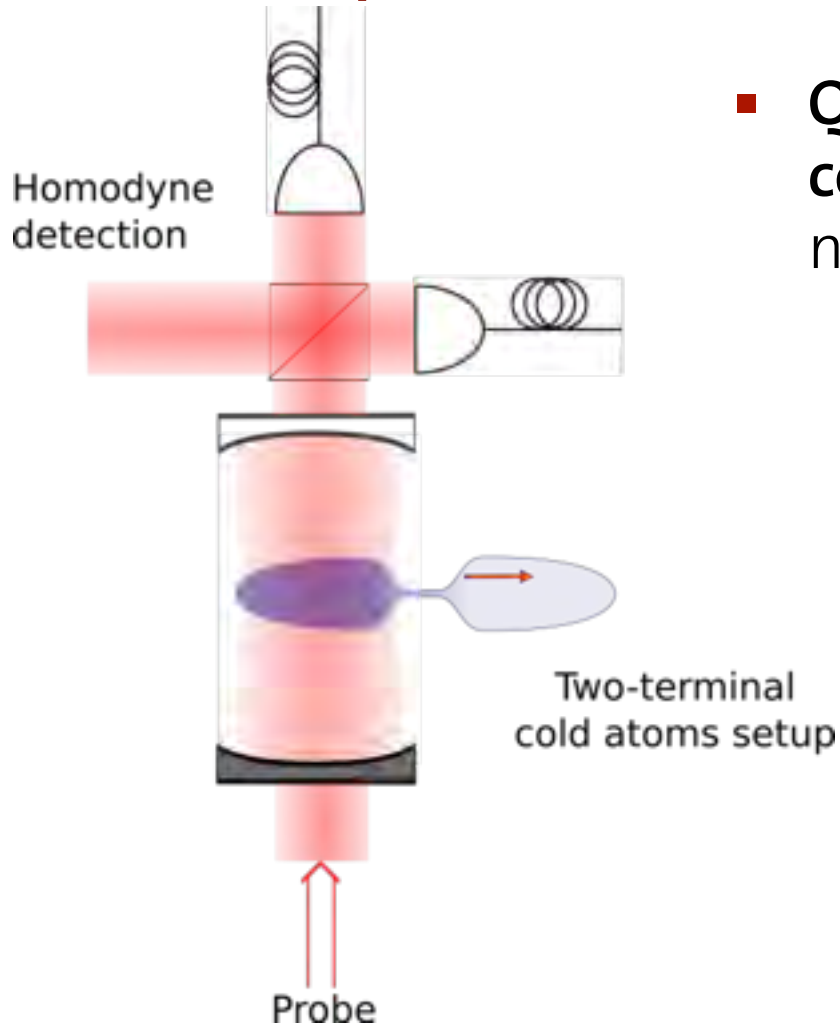


# 'Ideal' transport measurement



*Watch the particles entering and leaving the reservoirs in real time*

# 'Ideal' transport measurement



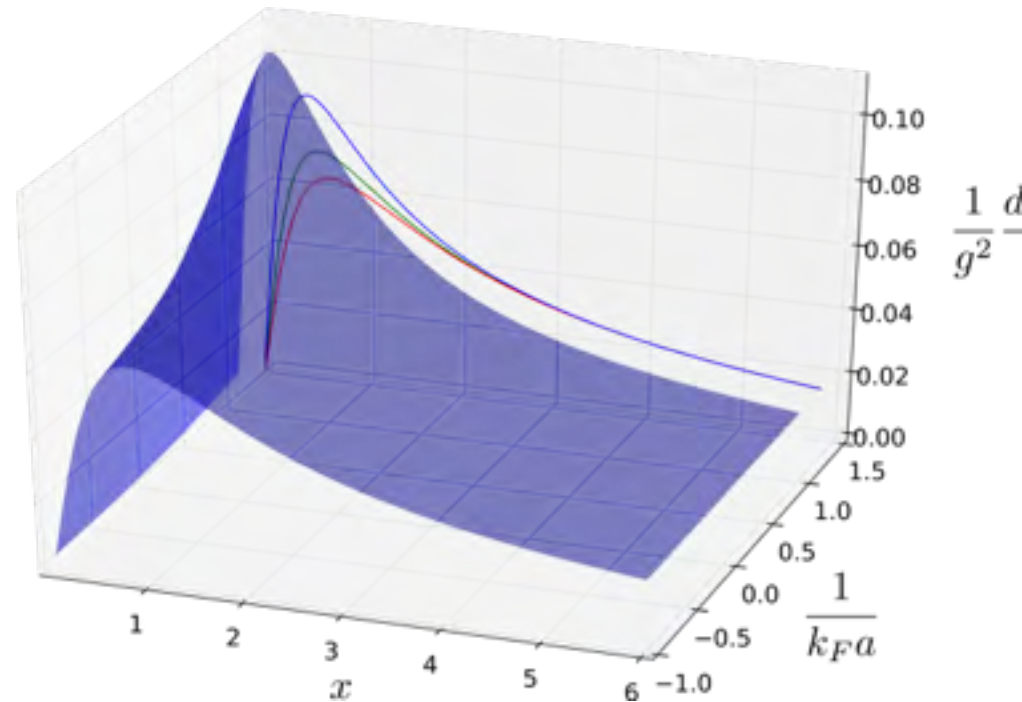
- **Quantum-non demolition** and **continuous** measurement of the number of atoms in a reservoir

1. Is it possible ?
2. Where is the noise floor ?

# Quantum non-demolition measurement

- Energy absorption rate due to measurement

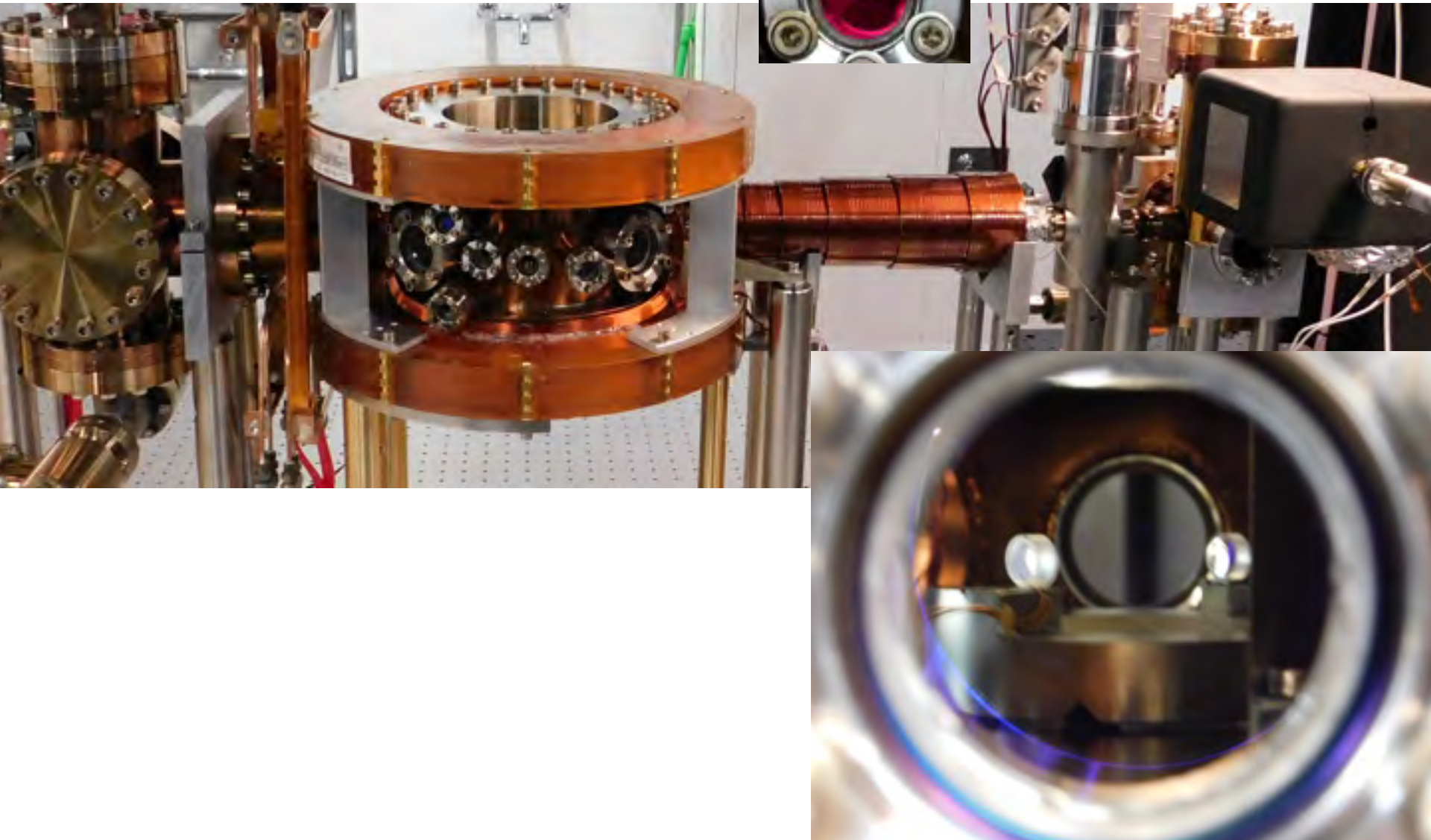
*For low enough bandwidth:  
QND regime reached  
regardless of interactions*



# Quantum limit to current measurement

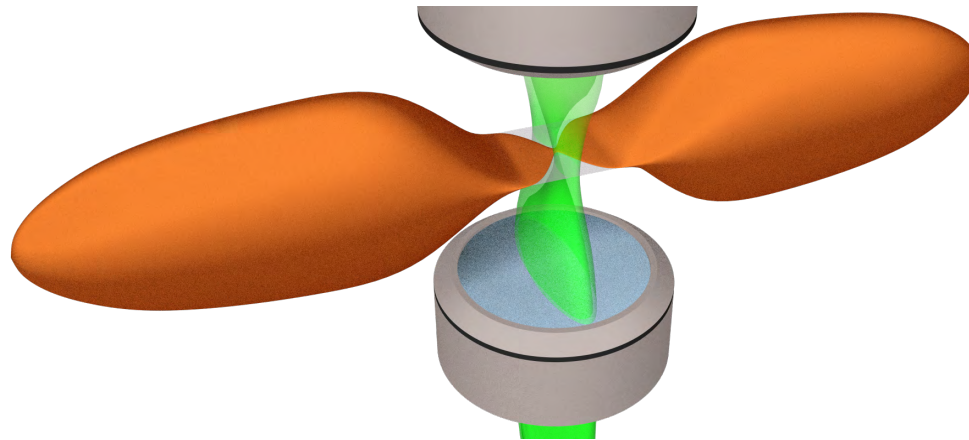
- Measuring  $N$  induces back action on the conjugate variable

# Experimental setup



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