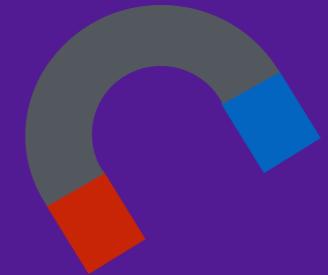




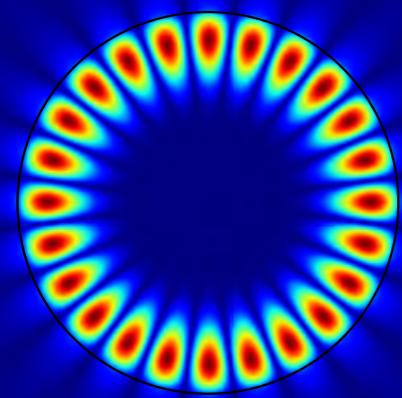
# Cavity Optomagnonics

## nonlinear dynamics and textures

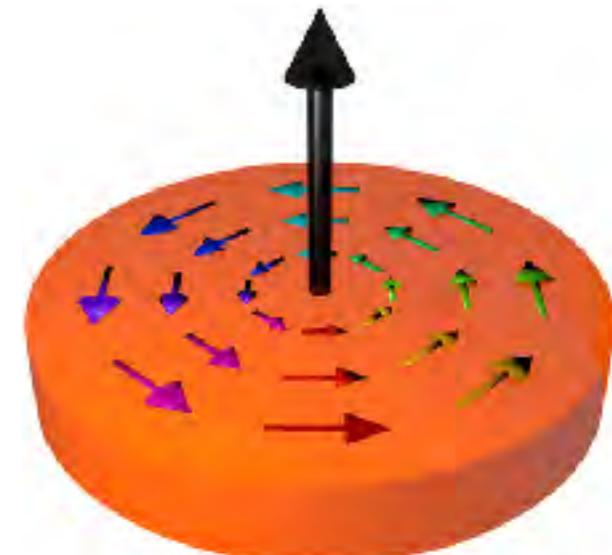


Jasmin Graf, Hannes Pfeifer, Florian Marquardt  
Hong Tang (Yale)

**Silvia Viola Kusminskiy**



MAX PLANCK INSTITUTE  
for the science of light



# New Max Planck Research Group



MAX PLANCK INSTITUTE  
for the science of light



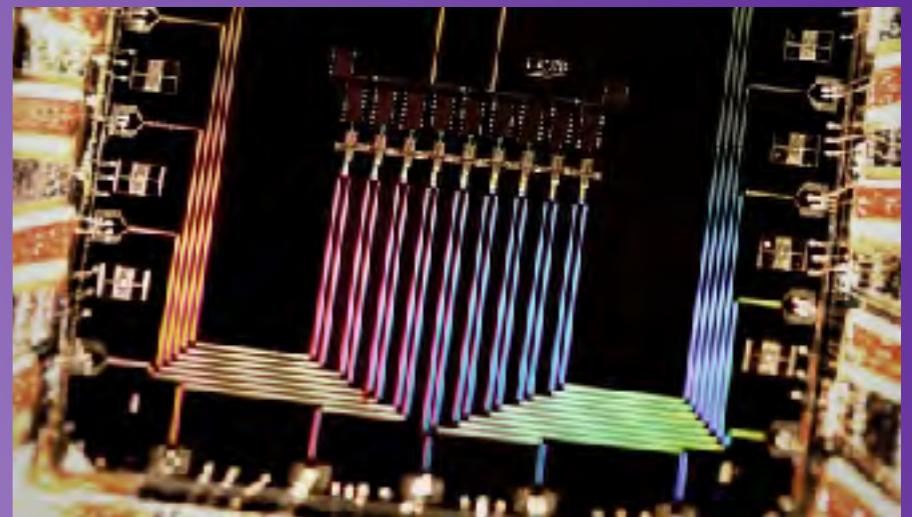
Erlangen, Germany



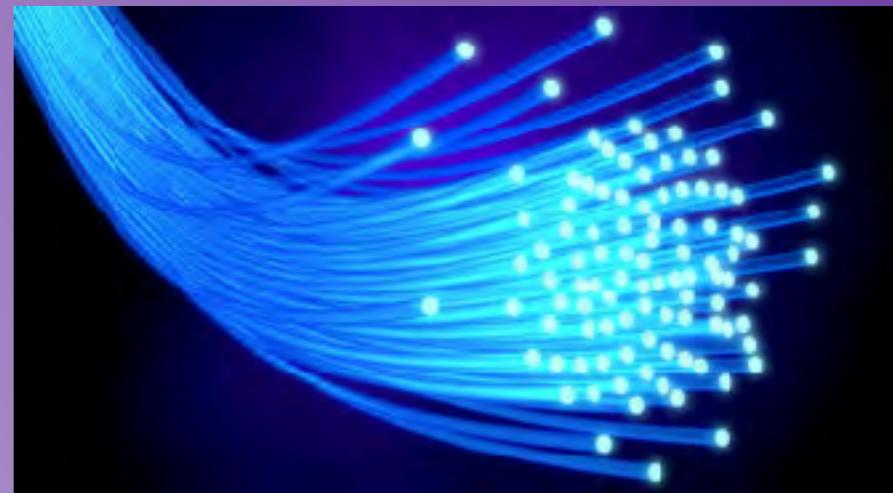
**classical technologies**

# quantum technologies

superconducting quantum circuit



Martinis group  
UCSB and Google (2015)



optical fiber

# classical technologies

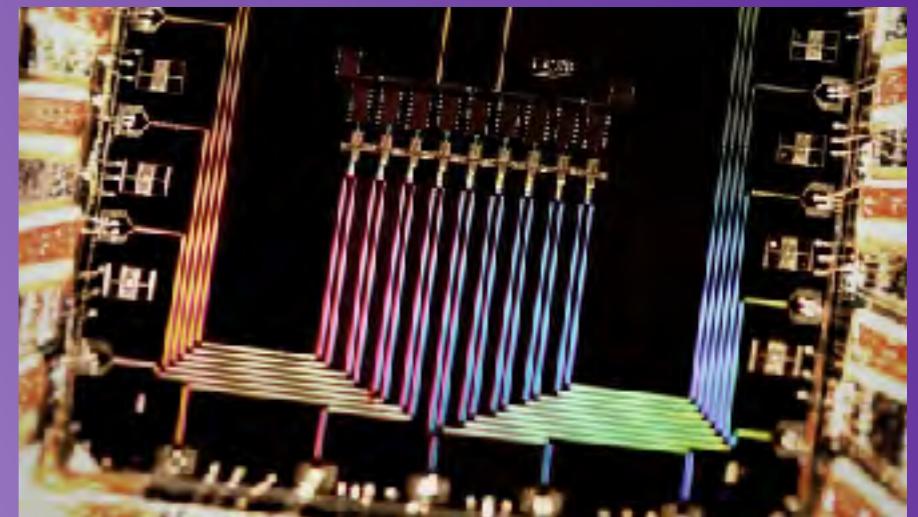
# quantum technologies



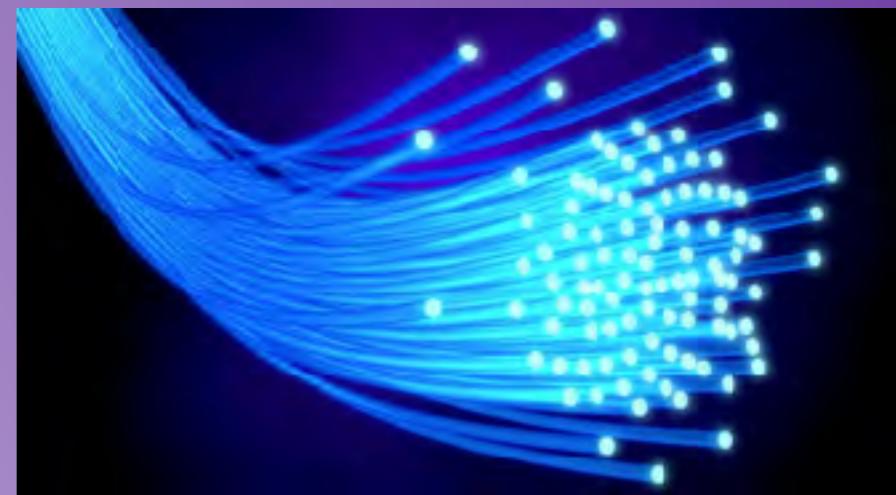
classical technologies

need  
hybrid  
systems

superconducting quantum circuit

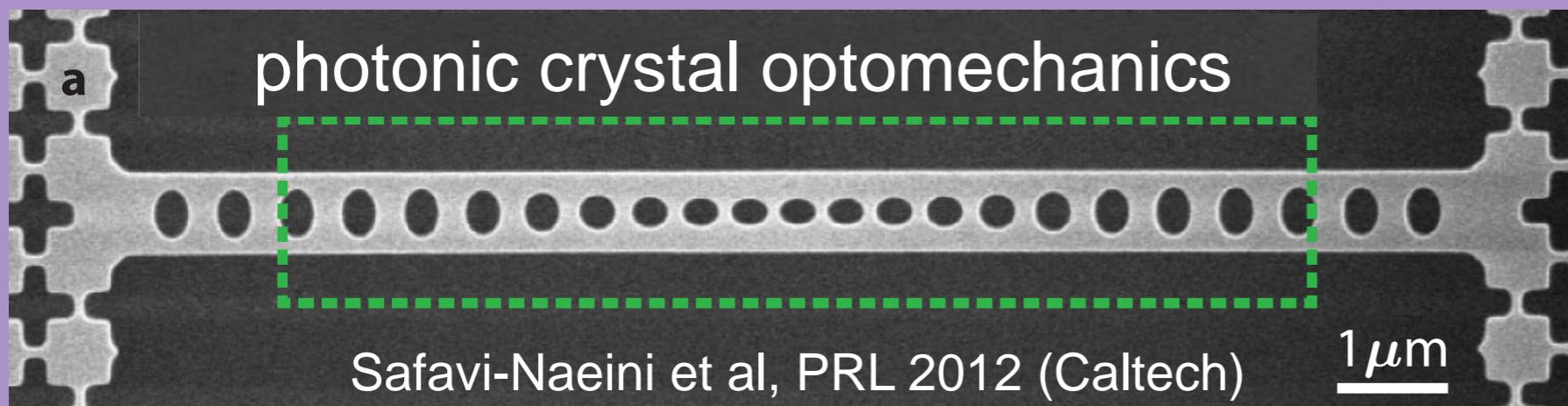


Martinis group  
UCSB and Google (2015)

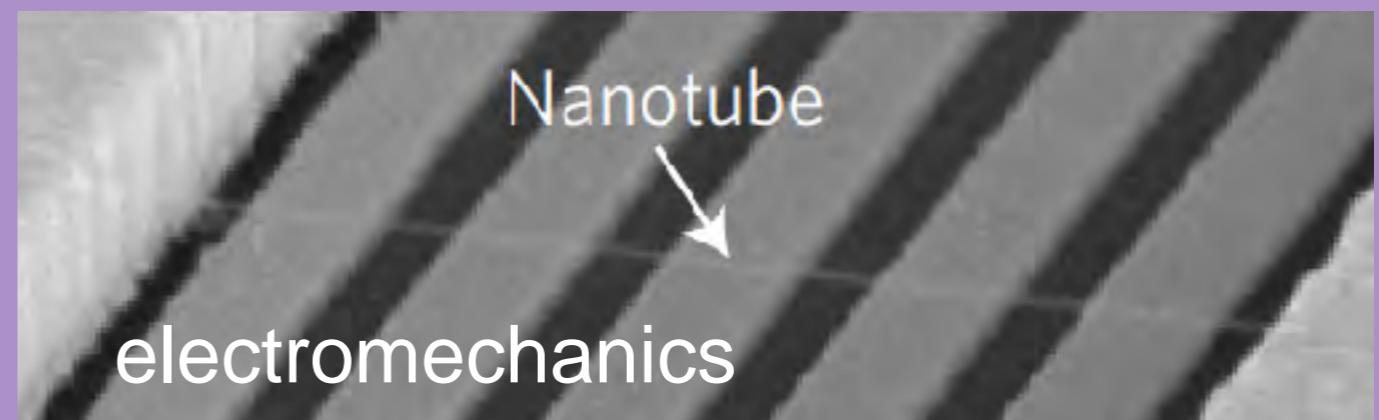
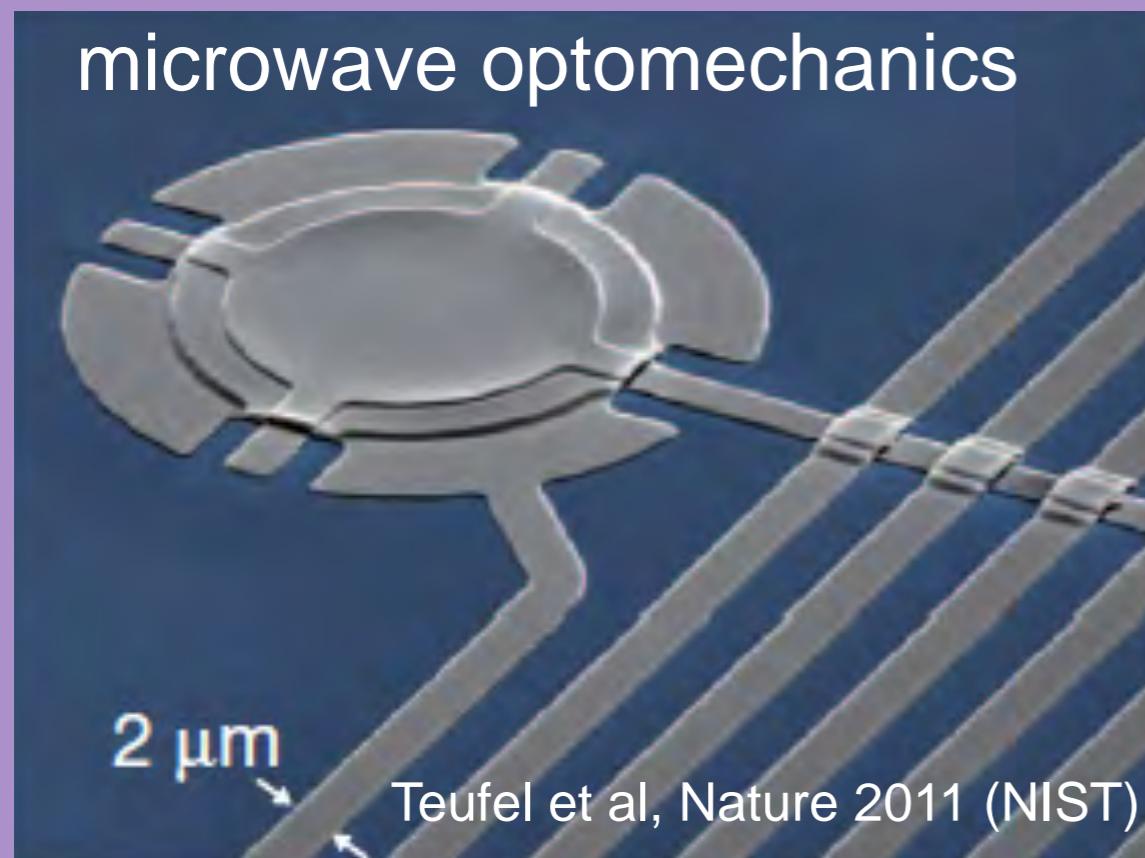


optical fiber

# Hybrid Systems for Quantum Technologies



mesoscopic:  
nano/micro scale  
systems



Benyamini et al, Nature Physics 10, 151 (2014)

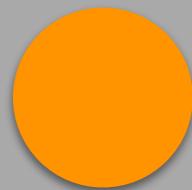


use collective excitations

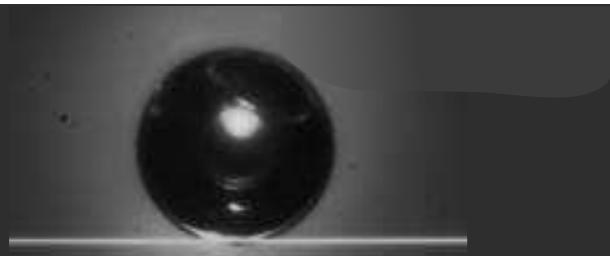
# Optomagnonics



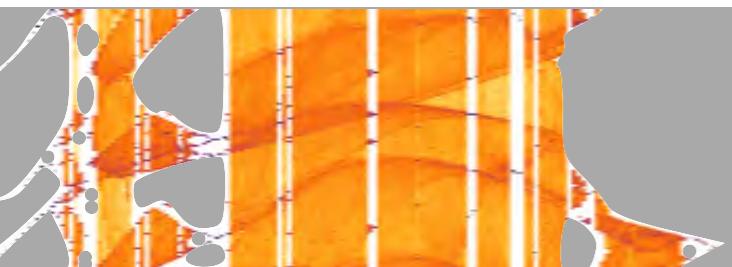
Picture from Tabuchi et al, PRL 113, 083603 (2014)



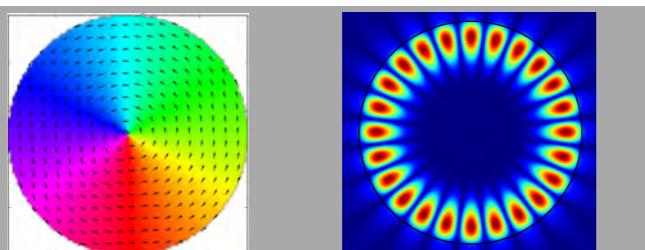
## Introduction and motivation



## Optomagnonic Hamiltonian



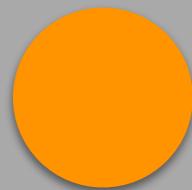
## Optically induced spin dynamics



## Magnetic textures: vortex in a disk



## Summary



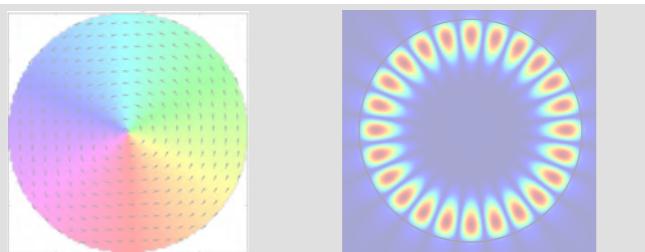
## Introduction and motivation



## Optomagnetic Hamiltonian



## Optically induced spin dynamics



## Magnetic textures: vortex in a disk



## Summary

# Magnonics



elementary magnetic  
excitation  
(quantum of spin wave)

# Magnonics



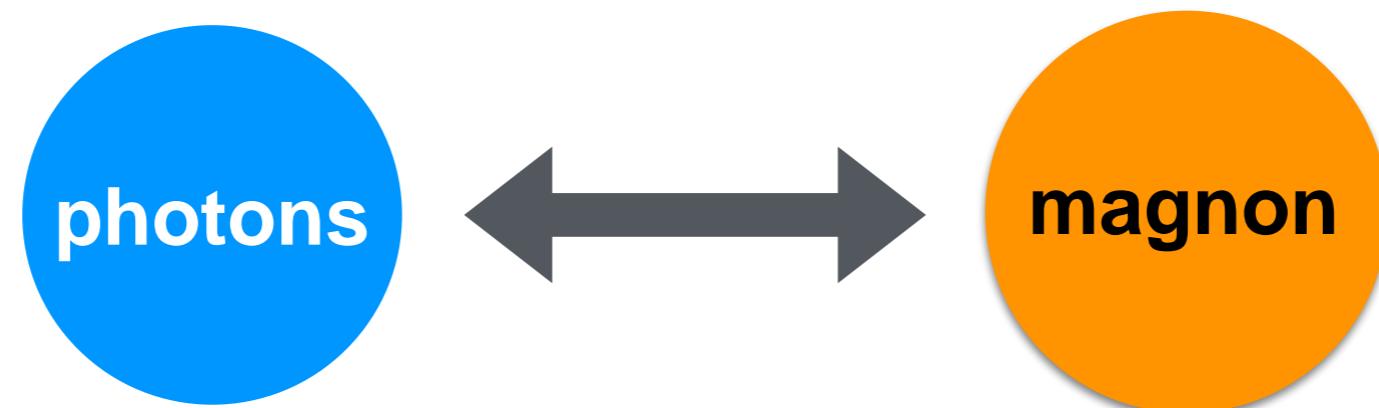
elementary magnetic  
excitation  
(quantum of spin wave)

Robust

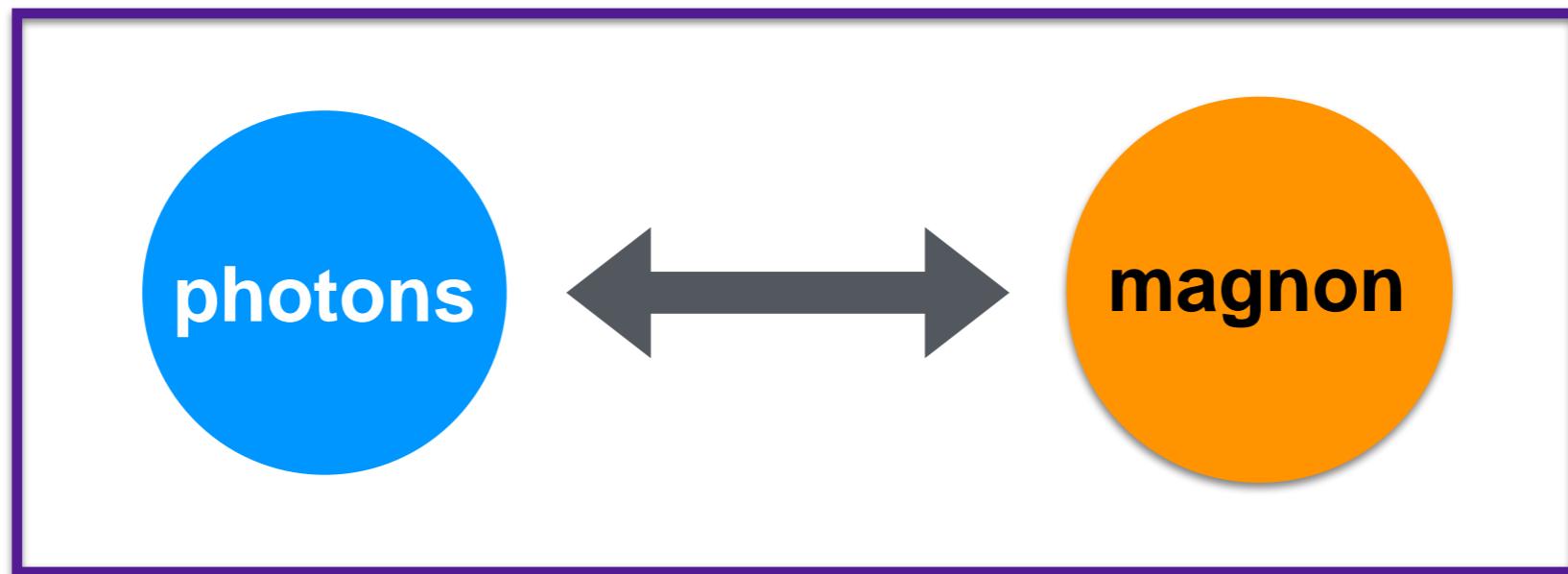
Low Power

Tunable

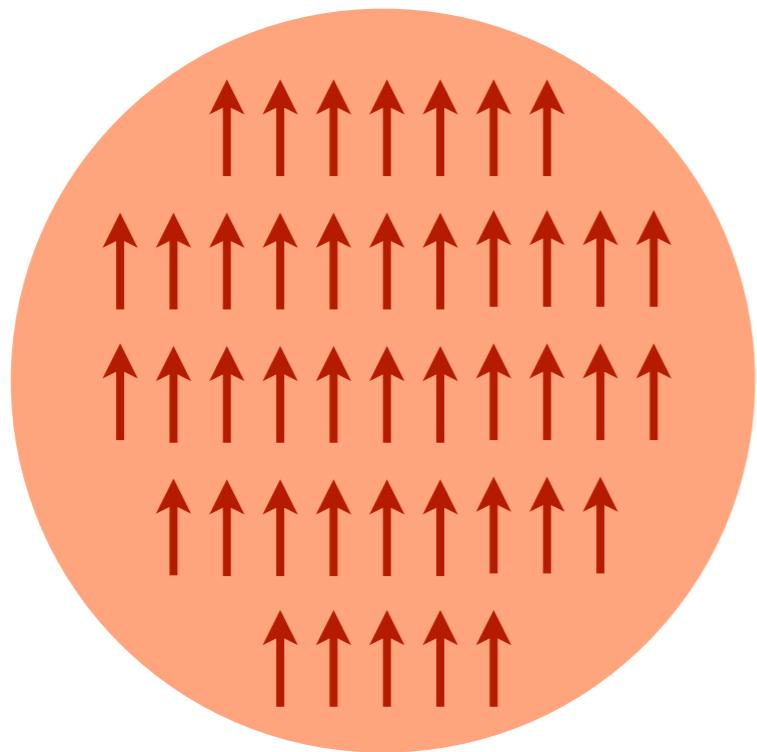
# Optomagnonics



# Cavity Optomagnonics



## Kittel mode



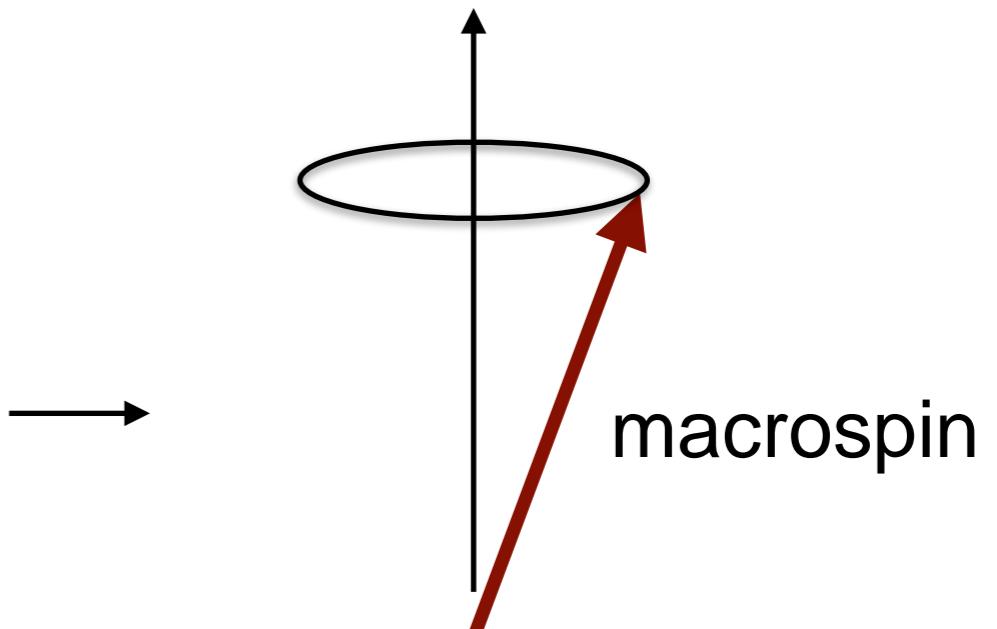
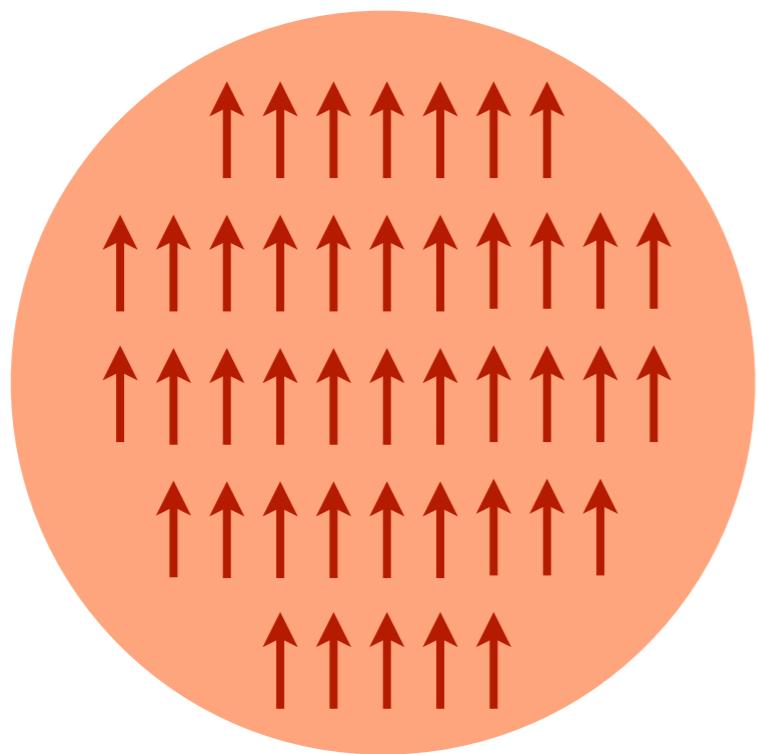
homogeneous  
magnetic mode

$$\mathbf{M}(\mathbf{r}) = \mathbf{M}$$

spin wave with  $k=0$

# Magnonics

## Kittel mode



$$\Omega \propto H$$

homogeneous  
magnetic mode

$$\mathbf{M}(\mathbf{r}) = \mathbf{M}$$

spin wave with  $\mathbf{k} = 0$

tunable precession frequency

$$\Omega \sim \text{GHz}$$

for 30mT

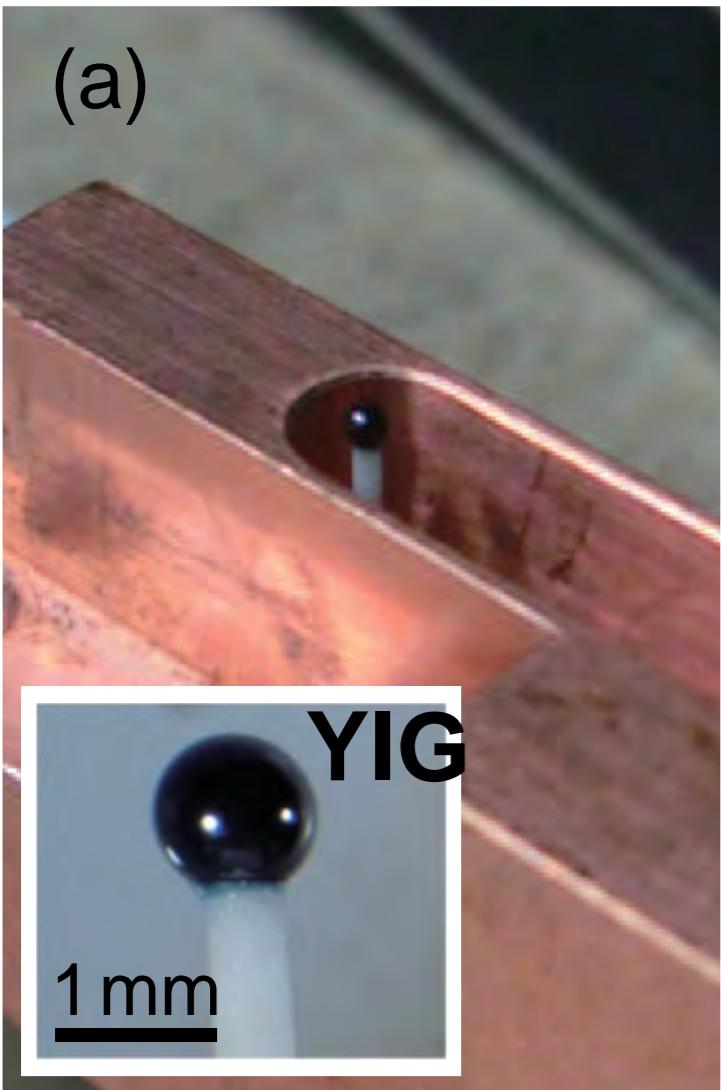
# Microwave Regime

Magnons

Microwaves



Strong coupling demonstrated in 2014



- Tabuchi et. al PRL 113, 083603  
(Nakamura's group, Tokyo)
- Zhang et. al PRL 113, 156401  
(Hong Tang's group, Yale)

# YIG



# YIG

Yttrium Iron Garnet



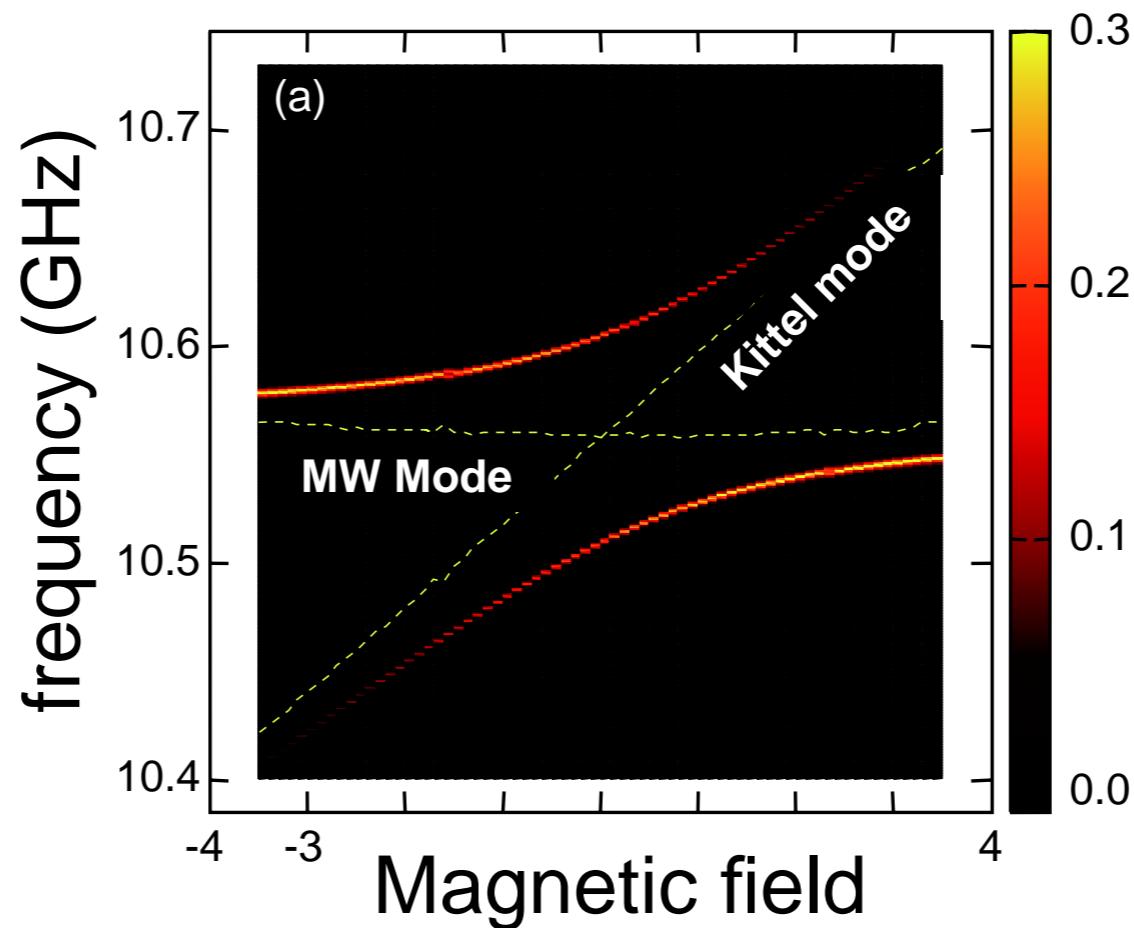
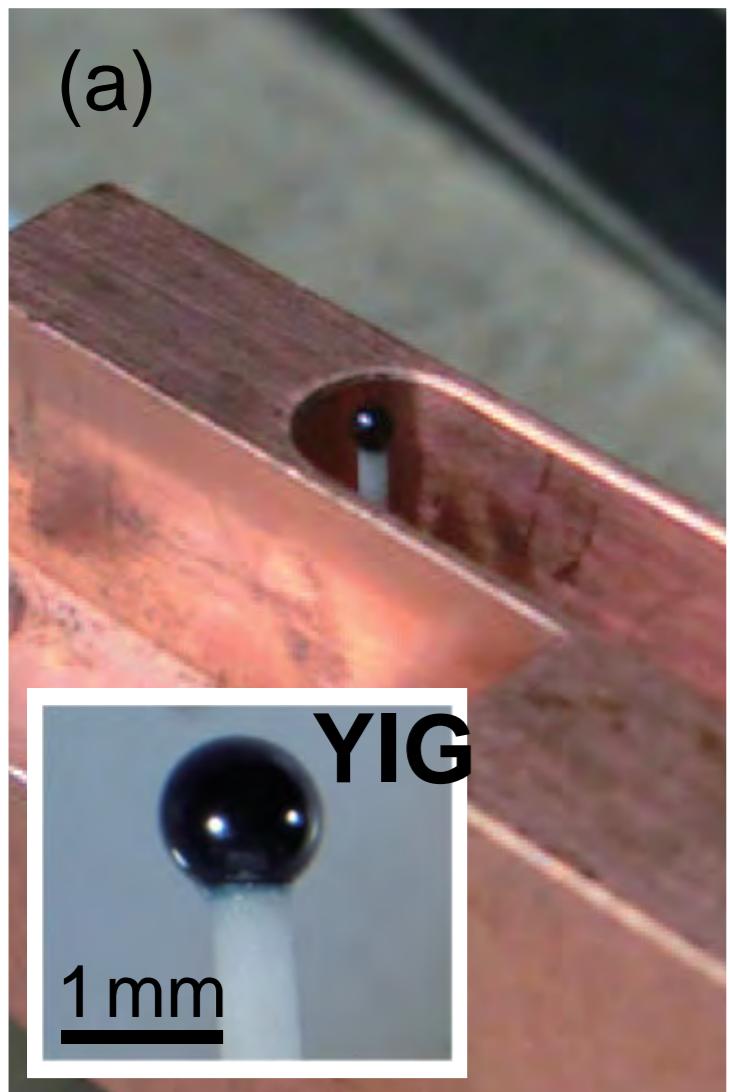
- ferrimagnetic
- insulator
- transparent in the infrared

# Microwave Regime

Magnons

Microwaves

Strong coupling demonstrated in 2014



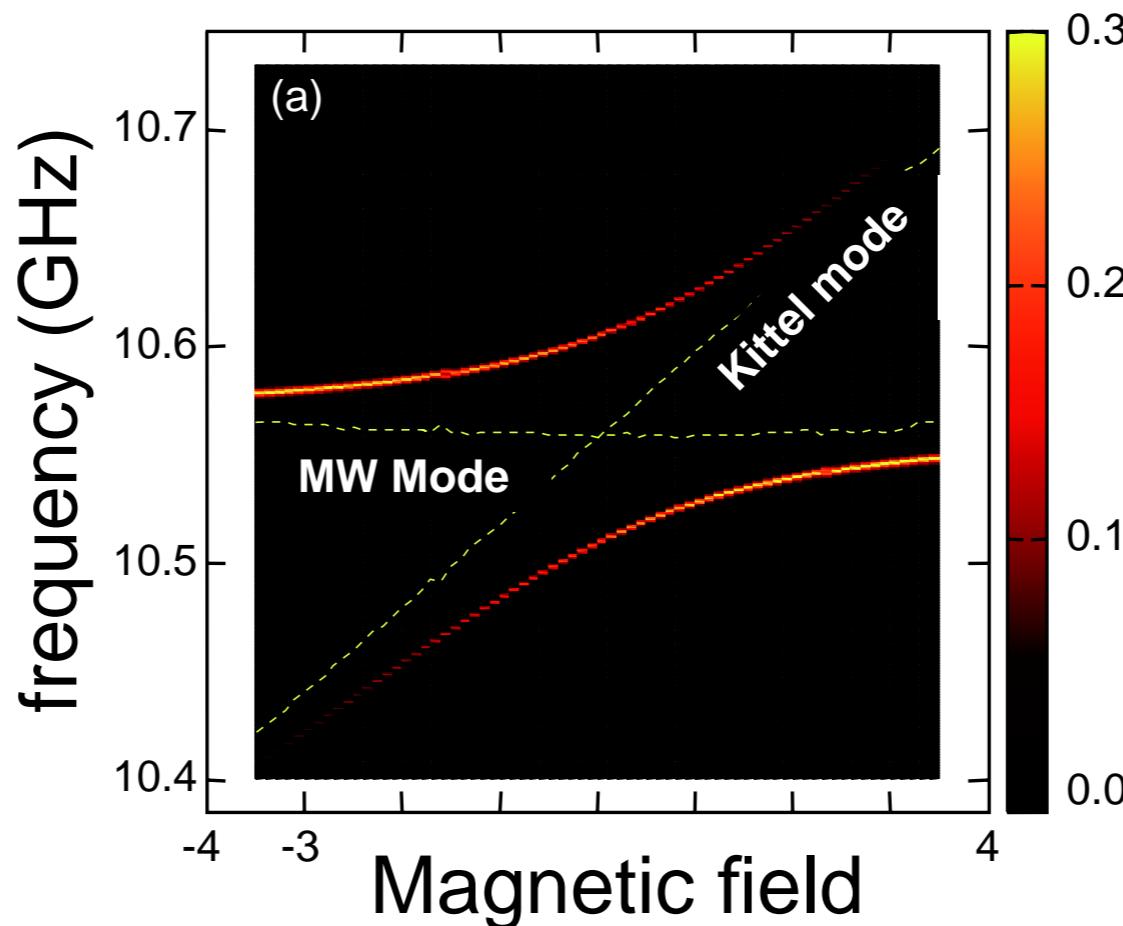
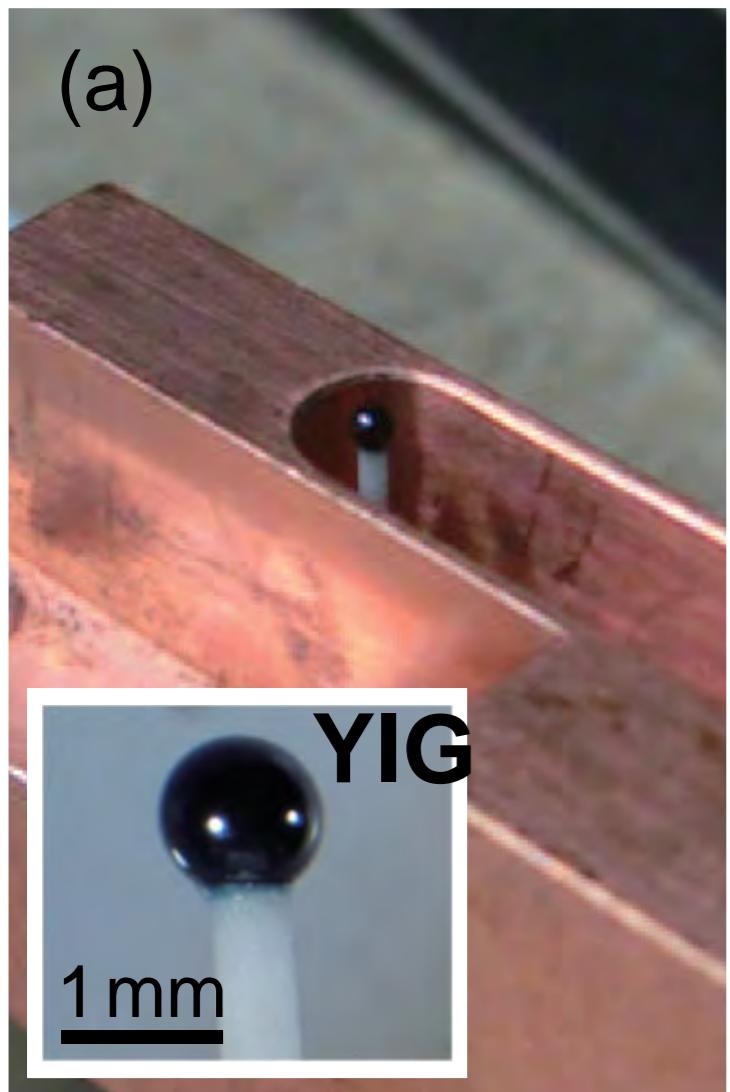
- Tabuchi et. al PRL 113, 083603  
(Nakamura's group, Tokyo)
- Zhang et. al PRL 113, 156401  
(Hong Tang's group, Yale)

# Microwave Regime

Magnons

Microwaves

Strong coupling regime



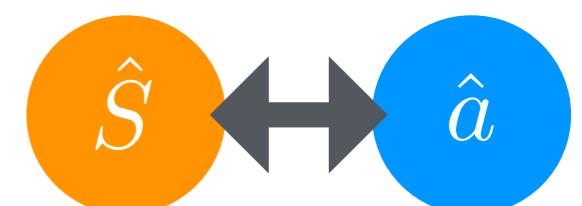
Huebl et. al, PRL 111, 127003 (2013)

Zhang et. al PRL 113, 156401 (2014)

Tabuchi et. al PRL 113, 083603 (2014)

Resonant coupling

$$\hat{S}^+ \hat{a} + \hat{S}^- \hat{a}^\dagger$$

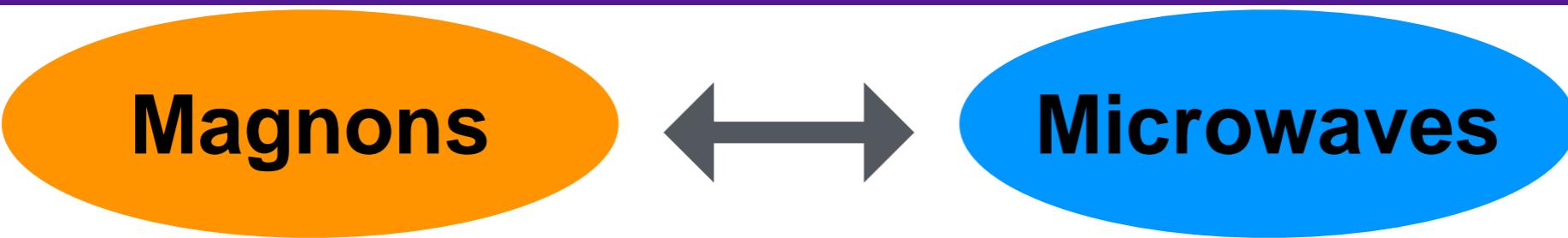


$\sim 50\text{MHz}$

Cooperativity  
 $C = 3 \times 10^3$

Soykal and M. E. Flatte  
PRL 104, 077202 (2010)

# Microwave Regime

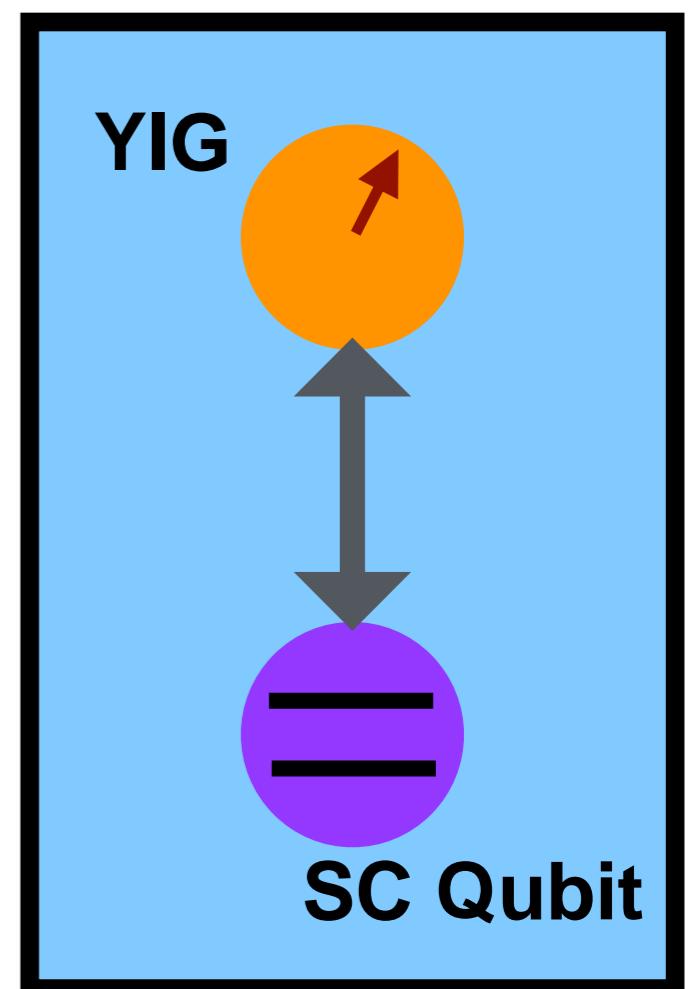


QUANTUM INFORMATION

(Science 2015)

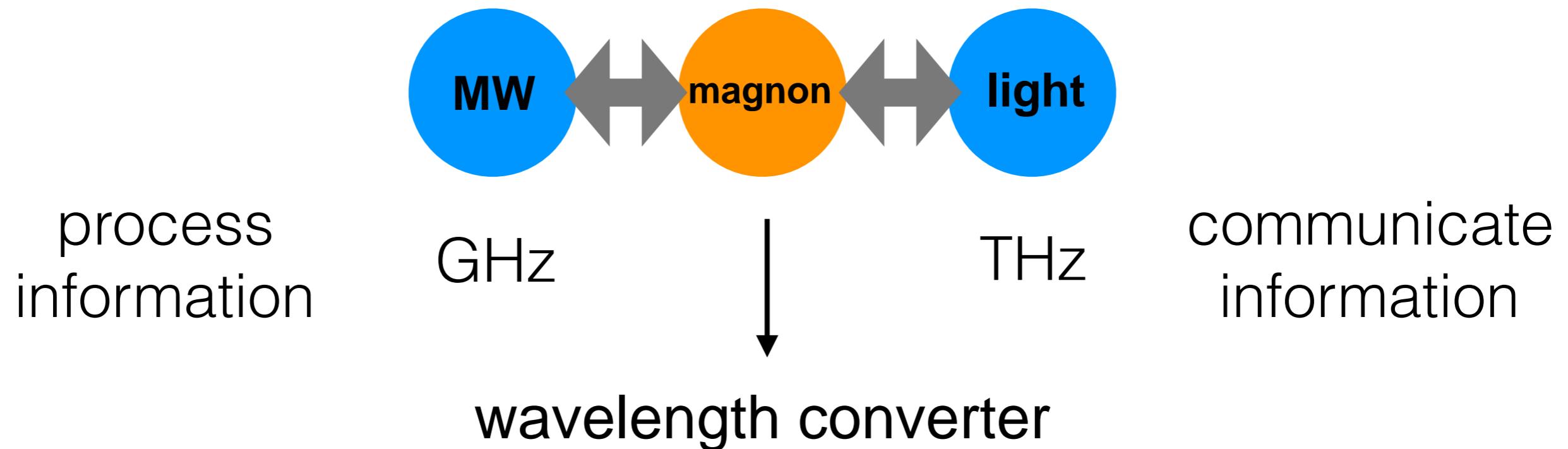
## Coherent coupling between a ferromagnetic magnon and a superconducting qubit

Yutaka Tabuchi,<sup>1,\*</sup> Seiichiro Ishino,<sup>1</sup> Atsushi Noguchi,<sup>1</sup> Toyofumi Ishikawa,<sup>1</sup>  
Rekishu Yamazaki,<sup>1</sup> Koji Usami,<sup>1</sup> Yasunobu Nakamura<sup>1,2</sup>



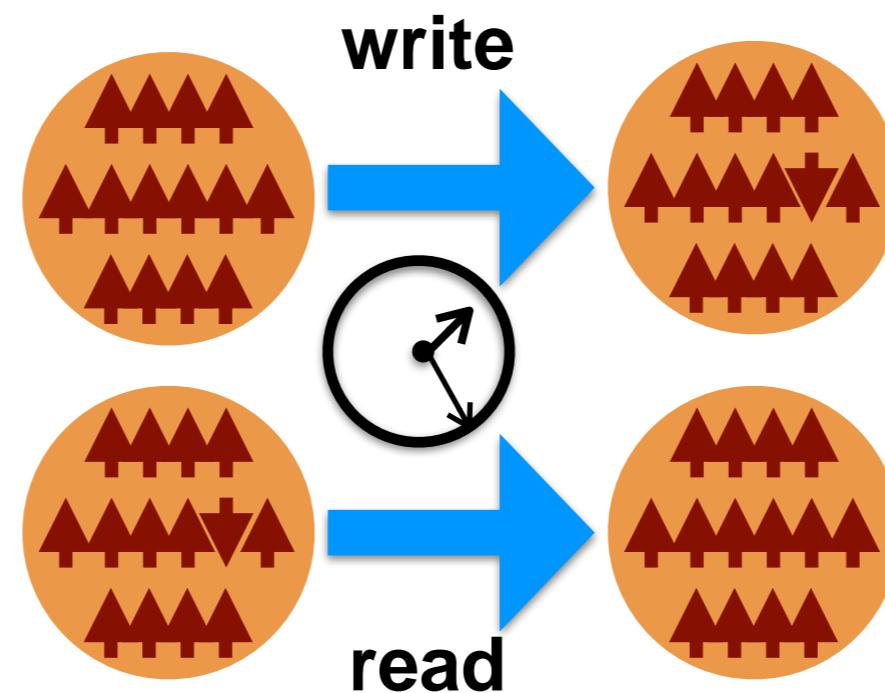
MW Cavity

# Coupling to Optics?



**Motivation:**  
**magnon as a transducer**

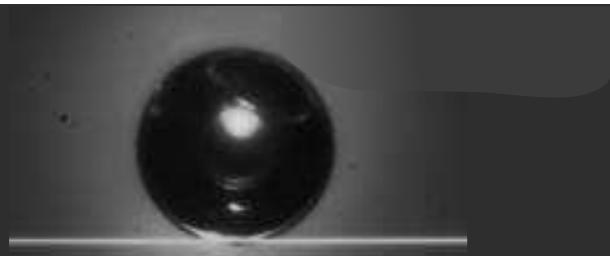
# Coupling to Optics?



**Motivation:**  
**magnon state as a quantum memory**



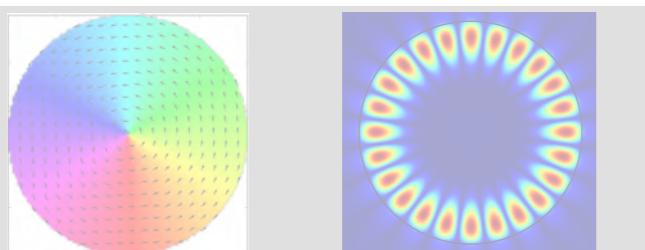
## Introduction and motivation



## Optomagnetic Hamiltonian



## Optically induced spin dynamics



## Magnetic textures: vortex in a disk

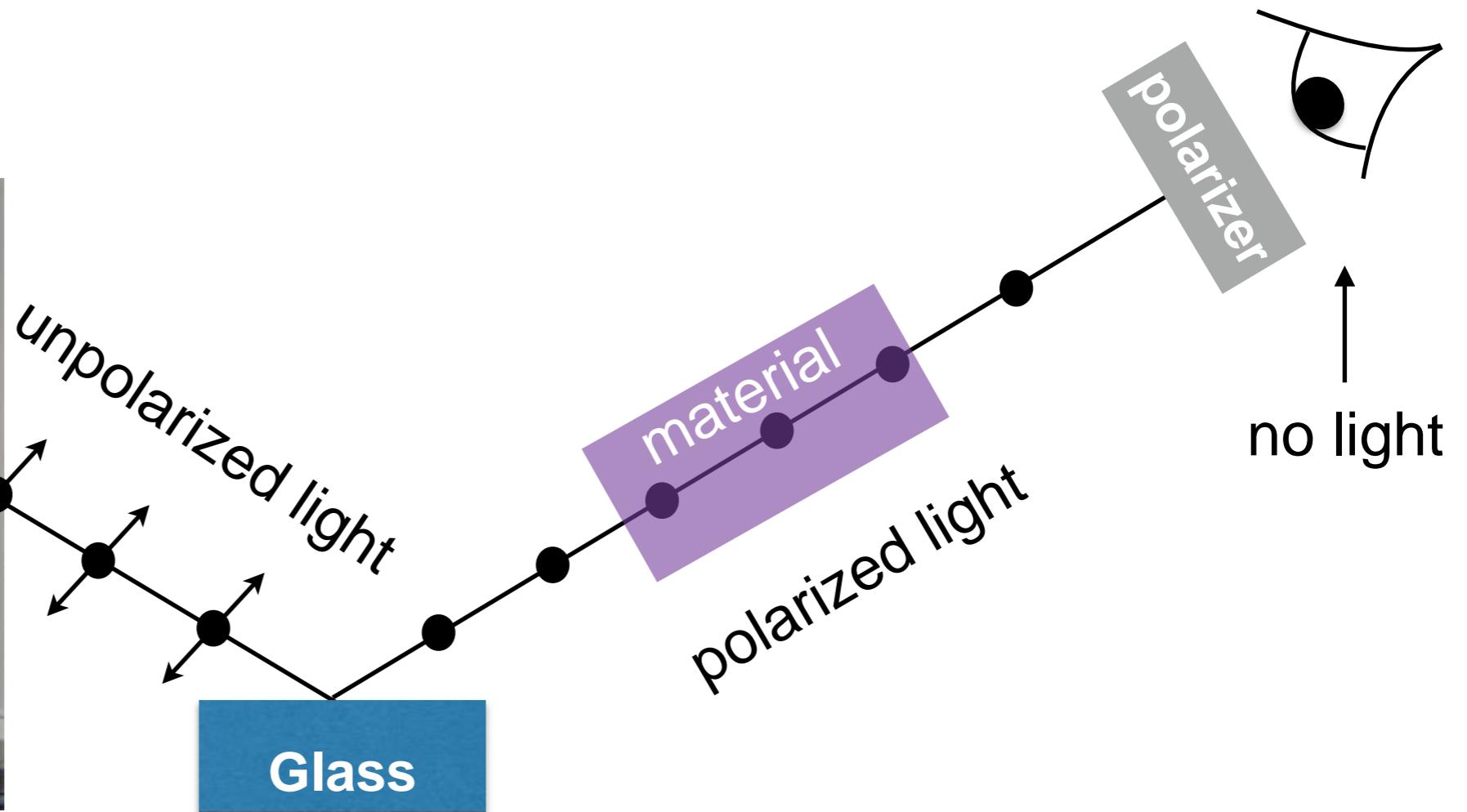


## Summary

# Faraday Effect (1846)



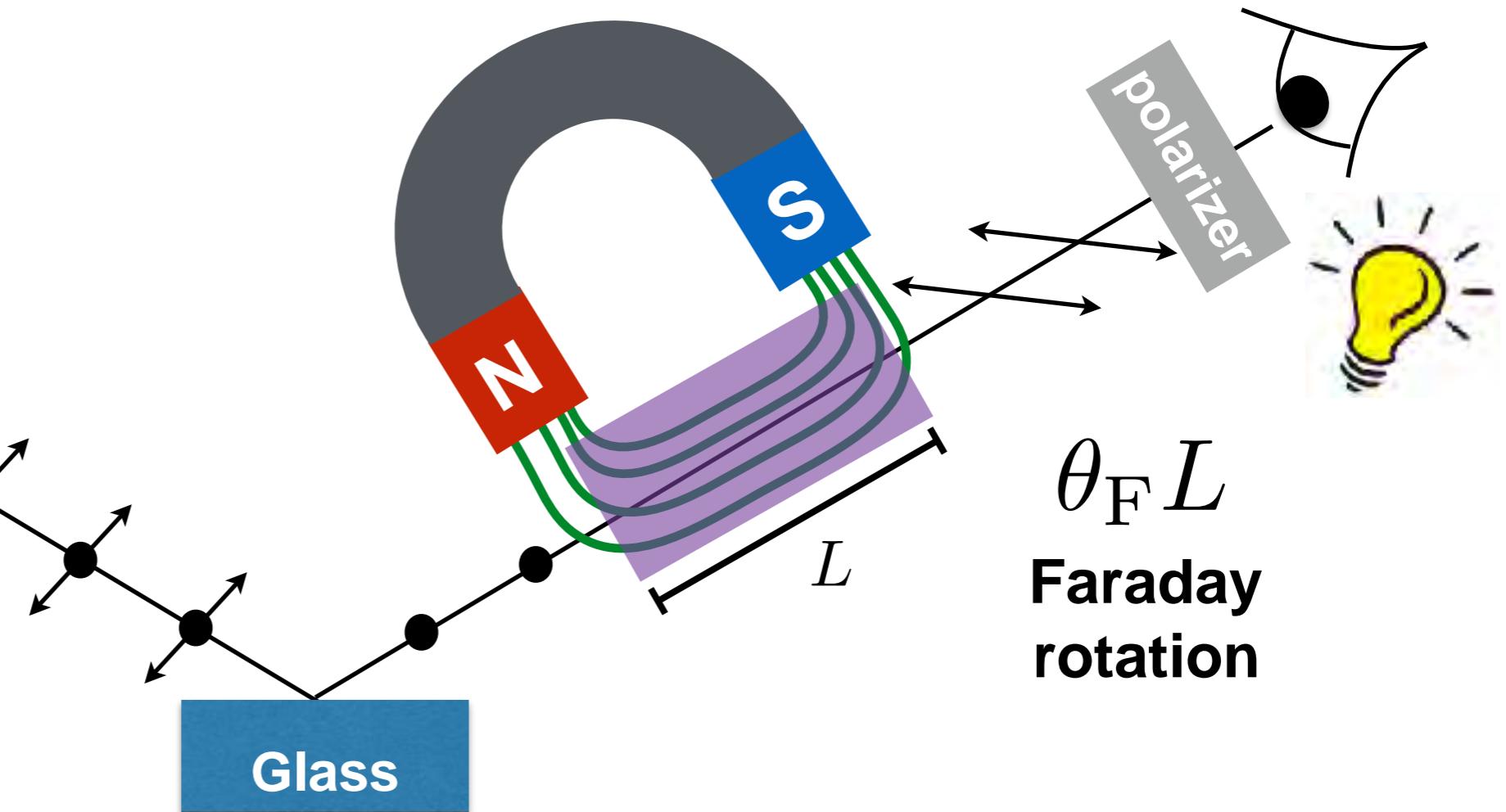
Oil Lamp



# Faraday Effect (1846)



Oil Lamp

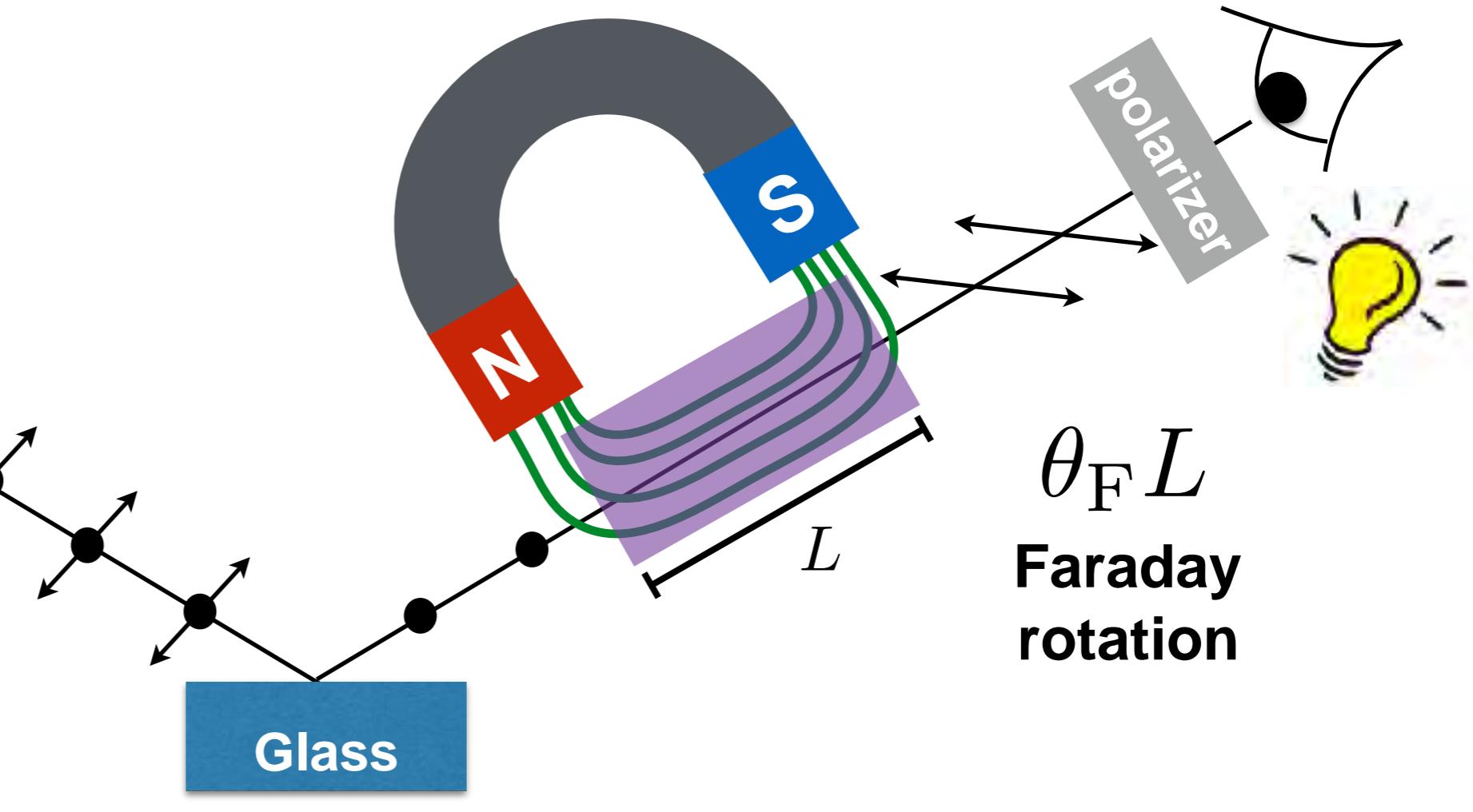


$\theta_F L$   
**Faraday  
rotation**

# Faraday Effect (1846)



Oil Lamp



$\theta_F L$   
Faraday  
rotation

## RELATION OF LIGHT TO THE MAGNETIC FORCE.

15

### ¶ iii. *General considerations.*

2221. Thus is established, I think for the first time\*, a true, direct relation and dependence between light and the magnetic and electric forces; and thus a great

# Coupling to Optics?: Faraday Effect

Faraday  
rotation

$$\bar{U}_{\text{MO}} = \theta_F \sqrt{\frac{\varepsilon}{\varepsilon_0}} \int d\mathbf{r} \left[ \frac{\mathbf{M}(\mathbf{r})}{M_s} \cdot \frac{\varepsilon_0}{2i\omega} [\mathbf{E}^*(\mathbf{r}) \times \mathbf{E}(\mathbf{r})] \right]$$



magnetization  
density

optical  
spin density



# Coupling to Optics?: Faraday Effect

Faraday  
rotation

$$\bar{U}_{\text{MO}} = \theta_F \sqrt{\frac{\varepsilon}{\varepsilon_0}} \int d\mathbf{r} \left[ \frac{\mathbf{M}(\mathbf{r})}{M_s} \cdot \frac{\varepsilon_0}{2i\omega} [\mathbf{E}^*(\mathbf{r}) \times \mathbf{E}(\mathbf{r})] \right]$$

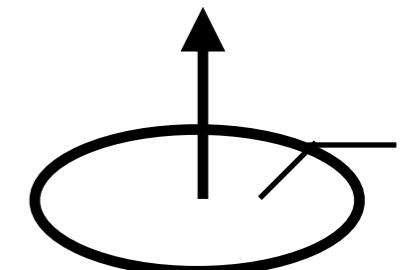


magnetization  
density

optical  
spin density



$\mathbf{E}^* \times \mathbf{E}$



# Coupling to Optics?: Faraday Effect

Faraday  
rotation

$$\bar{U}_{\text{MO}} = \theta_F \sqrt{\frac{\varepsilon}{\varepsilon_0}} \int d\mathbf{r} \left[ \frac{\mathbf{M}(\mathbf{r})}{M_s} \cdot \frac{\varepsilon_0}{2i\omega} [\mathbf{E}^*(\mathbf{r}) \times \mathbf{E}(\mathbf{r})] \right]$$



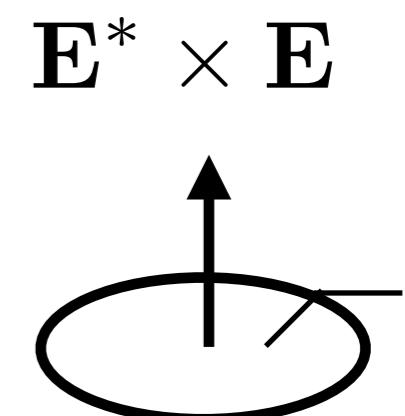
optical  
spin density



magnetization  
density

$$\varepsilon_{ij}(\mathbf{M}) = \varepsilon_0 (\varepsilon \delta_{ij} - i f \epsilon_{ijk} M_k)$$

broken time-reversal symmetry



# Optomagnonic Hamiltonian

$$\bar{U}_{\text{MO}} = \theta_F \sqrt{\frac{\varepsilon}{\varepsilon_0}} \int d\mathbf{r} \left[ \frac{\mathbf{M}(\mathbf{r})}{M_s} \cdot \frac{\varepsilon_0}{2i\omega} [\mathbf{E}^*(\mathbf{r}) \times \mathbf{E}(\mathbf{r})] \right]$$

Quantize:



two-photon process

# Optomagnonic Hamiltonian

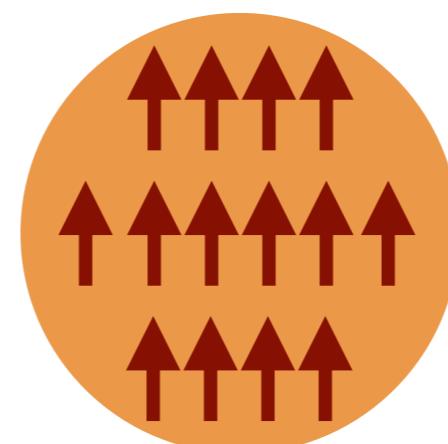
$$\bar{U}_{\text{MO}} = \theta_F \sqrt{\frac{\varepsilon}{\varepsilon_0}} \int d\mathbf{r} \left[ \frac{\mathbf{M}(\mathbf{r})}{M_s} \cdot \frac{\varepsilon_0}{2i\omega} [\mathbf{E}^*(\mathbf{r}) \times \mathbf{E}(\mathbf{r})] \right]$$

Quantize:

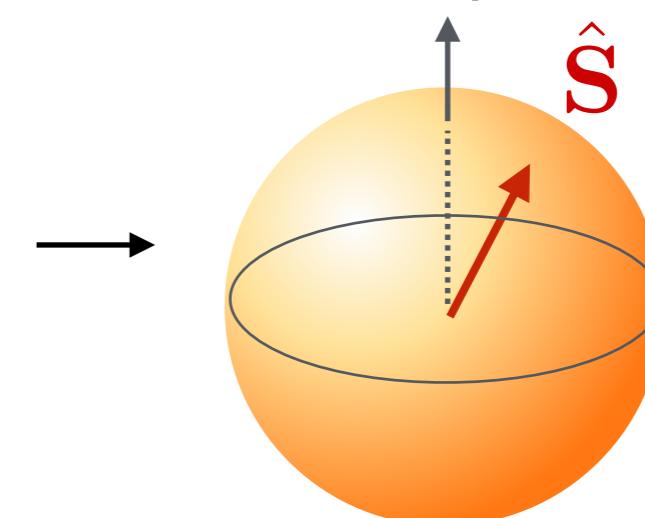
$$\mathbf{M}(\mathbf{r}) = \mathbf{M}$$



Kittel mode



Bloch sphere



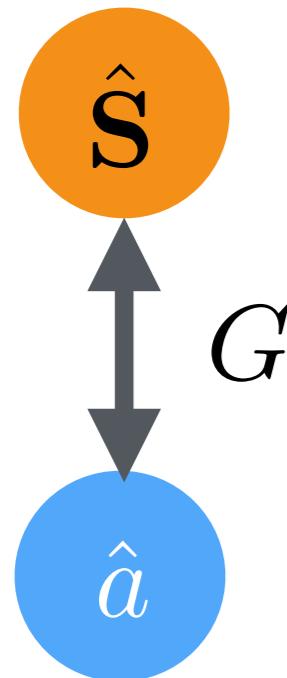
$$\Omega \propto H$$

# Optomagnonic Hamiltonian

Microscopic Hamiltonian

Parametric  
coupling

$$\hat{H}_{MO} = \hbar \sum_{j\beta\gamma} \hat{S}_j^j G_{\beta\gamma}^j \hat{a}_\beta^\dagger \hat{a}_\gamma$$

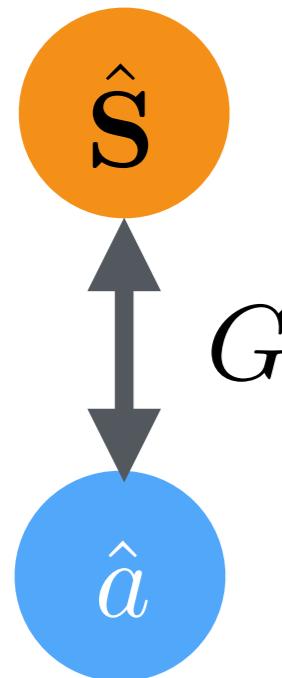


# Optomagnonic Hamiltonian

Microscopic Hamiltonian

Parametric coupling

$$\hat{H}_{MO} = \hbar \sum_{j\beta\gamma} \hat{S}_j G_{\beta\gamma}^j \hat{a}_\beta^\dagger \hat{a}_\gamma$$



Optomagnonic coupling

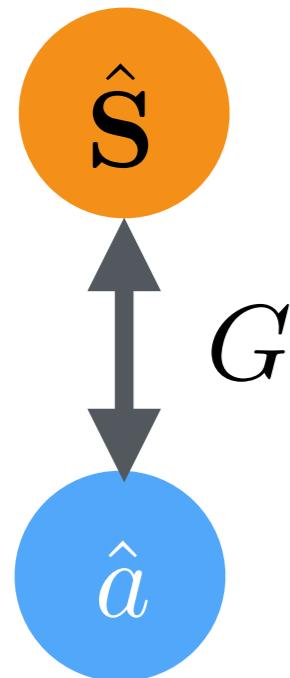
$$G_{\beta\gamma}^j = -i \frac{\theta_F \lambda}{2\pi\hbar S} \frac{\epsilon_0 \epsilon}{2} \epsilon_{jmn} \int d\mathbf{r} E_{\beta m}^*(\mathbf{r}) E_{\gamma n}(\mathbf{r})$$

# Optomagnonic Hamiltonian

Microscopic Hamiltonian

Parametric coupling

$$\hat{H}_{MO} = \hbar \sum_{j\beta\gamma} \hat{S}_j G_{\beta\gamma}^j \hat{a}_\beta^\dagger \hat{a}_\gamma$$



Optomagnonic coupling

$$G_{\beta\gamma}^j = -i \frac{\theta_F \lambda}{2\pi\hbar S} \frac{\epsilon_0 \epsilon}{2} \epsilon_{jmn} \int d\mathbf{r} E_{\beta m}^*(\mathbf{r}) E_{\gamma n}(\mathbf{r})$$

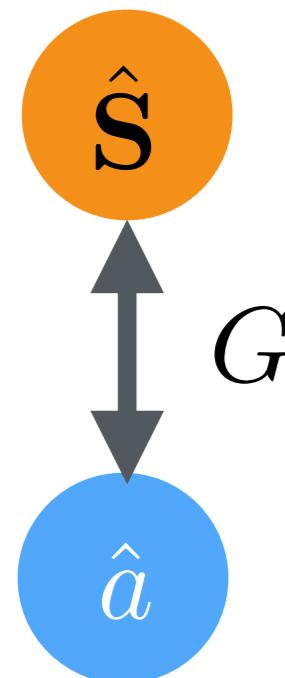
overlap electric field  
mode functions

# Optomagnonic Hamiltonian

Microscopic Hamiltonian

Parametric coupling

$$\hat{H}_{MO} = \hbar \sum_{j\beta\gamma} \hat{S}_j G_{\beta\gamma}^j \hat{a}_\beta^\dagger \hat{a}_\gamma$$



Optomagnonic coupling

$$G_{\beta\gamma}^j = \left( i \frac{\theta_F \lambda}{2\pi\hbar S} \frac{\epsilon_0 \epsilon}{2} \right) \epsilon_{jmn} \int d\mathbf{r} E_{\beta m}^*(\mathbf{r}) E_{\gamma n}(\mathbf{r})$$

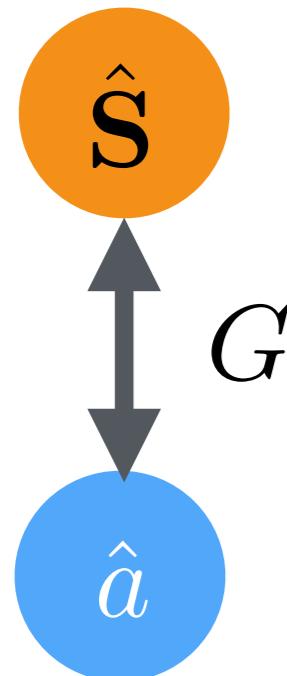
Faraday rotation

# Optomagnonic Hamiltonian

Microscopic Hamiltonian

Parametric coupling

$$\hat{H}_{MO} = \hbar \sum_{j\beta\gamma} \hat{S}_j G_{\beta\gamma}^j \hat{a}_\beta^\dagger \hat{a}_\gamma$$

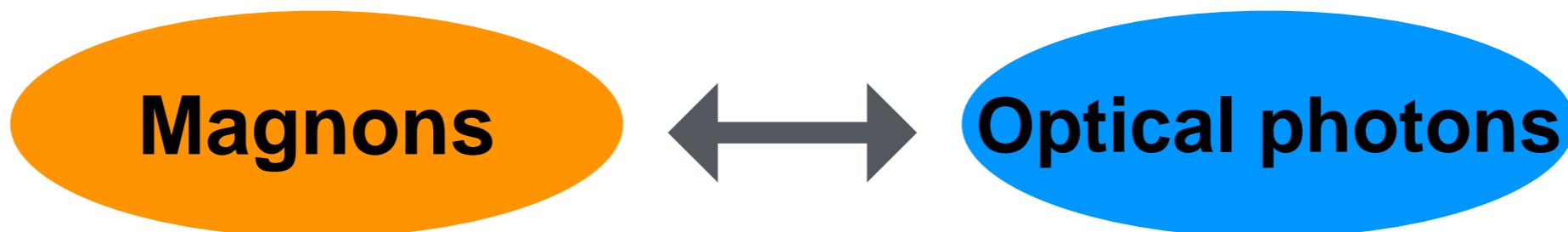


Optomagnonic coupling

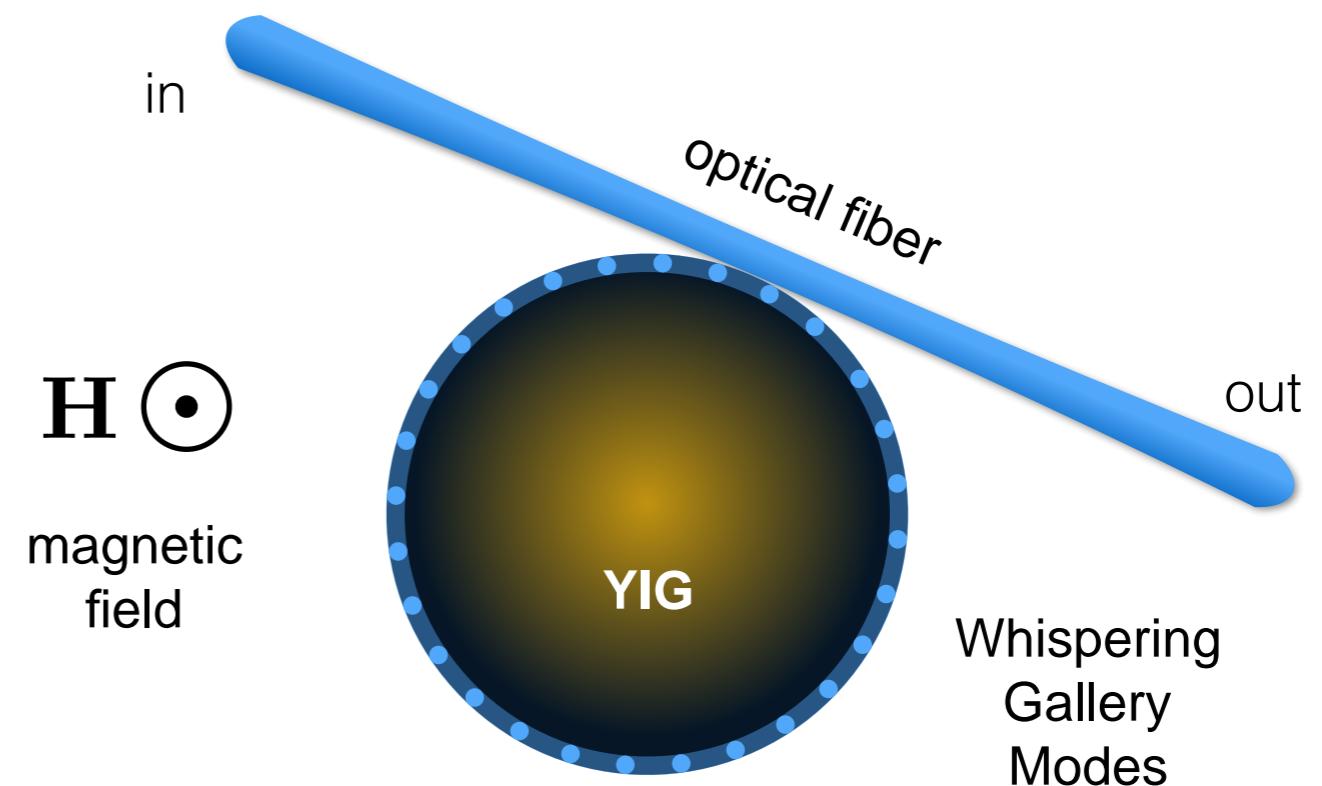
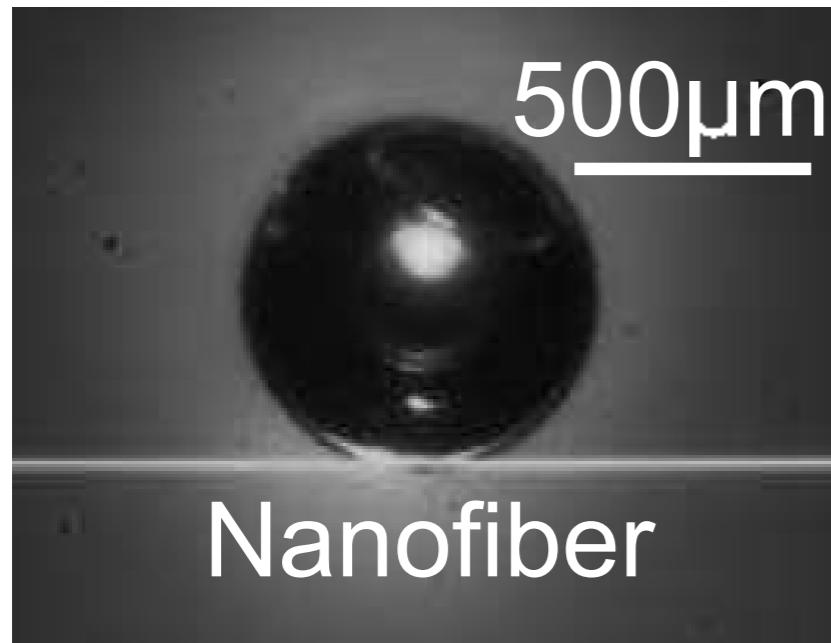
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number of spins

# Cavity Optomagnonics



Coupling demonstrated in 2016

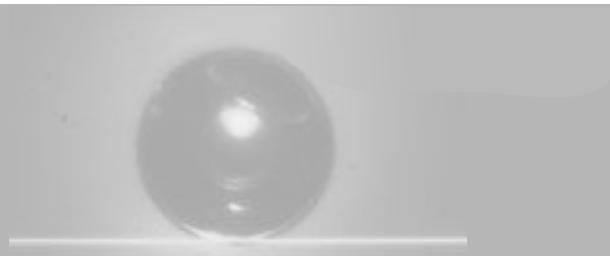


- Osada et. al PRL 116, 223601  
(Nakamura's group, Tokyo)
- Haigh et. al PRL 117, 133602  
(Cambridge Univ / Hitachi)
- Zhang et. al PRL 117, 123605  
(Hong Tang's group, Yale)

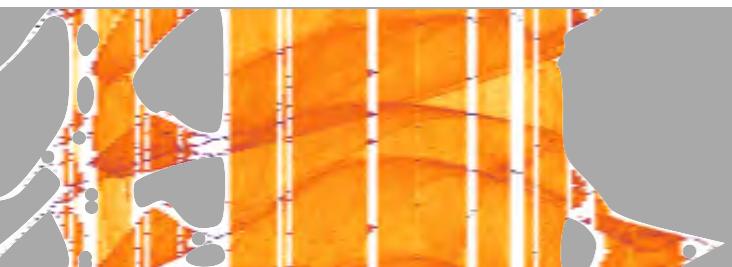
**A cavity enhances the effect**



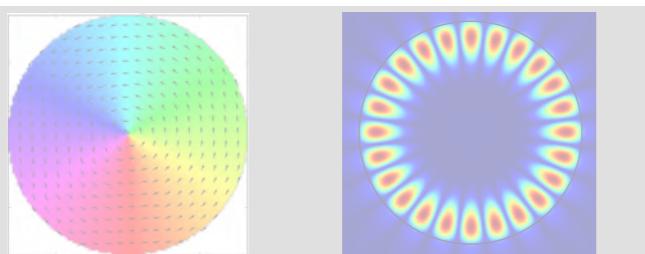
## Introduction and motivation



## Optomagnetic Hamiltonian



## Optically induced spin dynamics



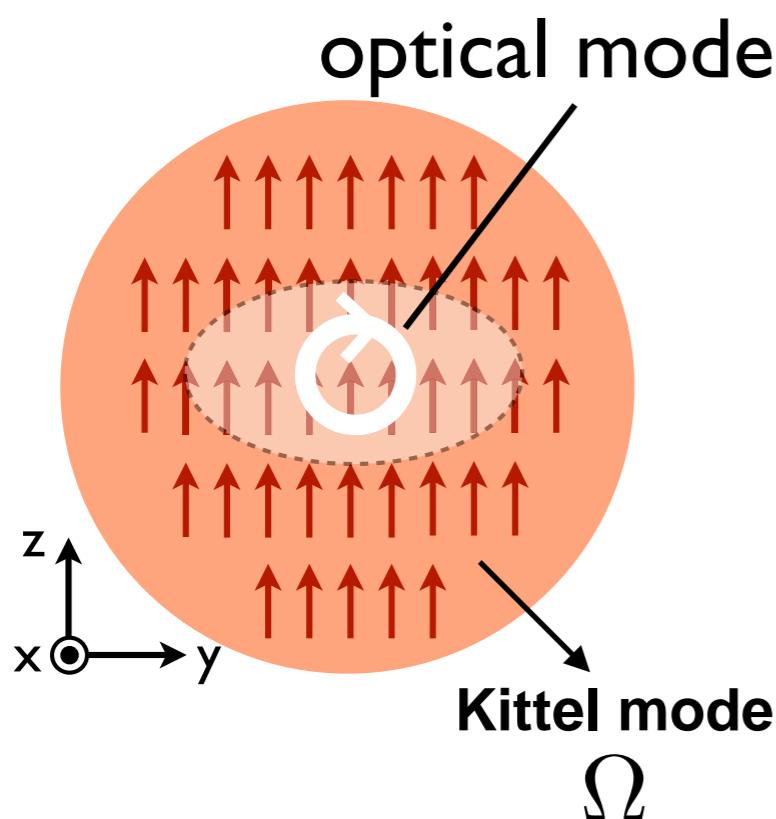
## Magnetic textures: vortex in a disk



## Summary

# Cavity Optomagnonics: one optical mode

$$H = -\hbar\Delta\hat{a}^\dagger\hat{a} - \hbar\Omega\hat{S}_z + \hbar G\hat{S}_x\hat{a}^\dagger\hat{a}$$

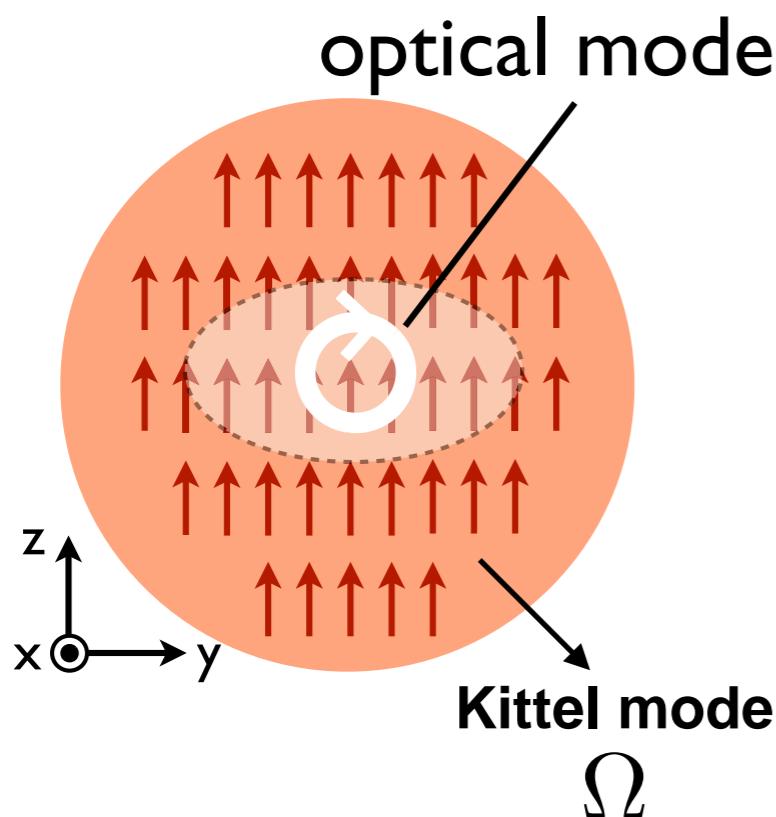


driving laser detuning

$$\Delta = \omega_{las} - \omega_{cav}$$

# Cavity Optomagnonics: one optical mode

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driving laser detuning

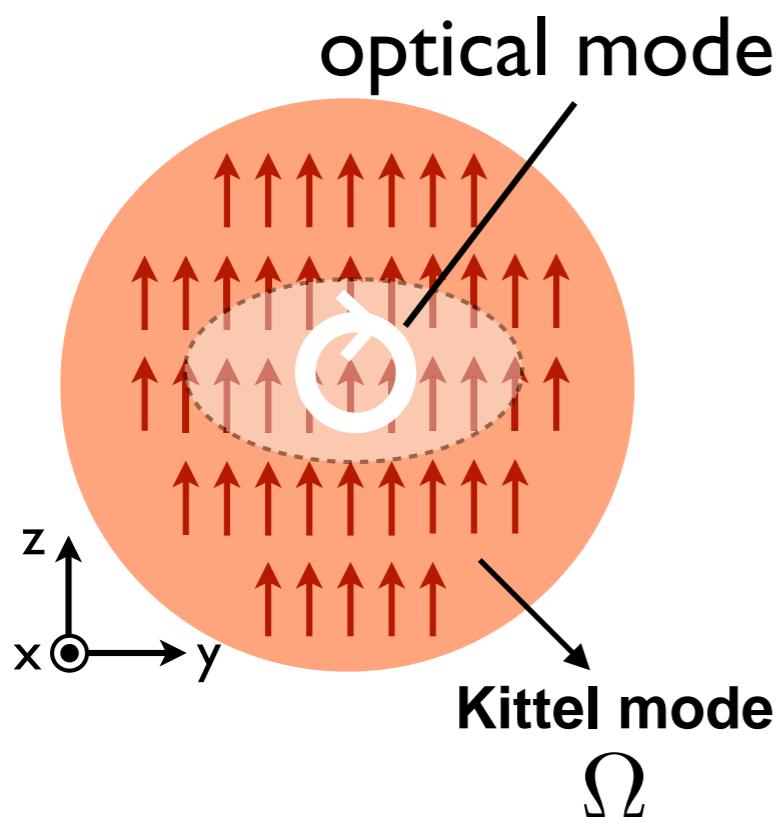
$$\Delta = \omega_{las} - \omega_{cav}$$

$$G = \frac{1}{S} \frac{c \theta_F}{4\sqrt{\epsilon}} \approx 1 \text{Hz}$$

YIG  
 $(1\mu m)^3$

# Cavity Optomagnonics: one optical mode

$$H = -\hbar\Delta\hat{a}^\dagger\hat{a} - \hbar\Omega\hat{S}_z + \hbar G\hat{S}_x\hat{a}^\dagger\hat{a}$$



driving laser detuning

$$\Delta = \omega_{las} - \omega_{cav}$$

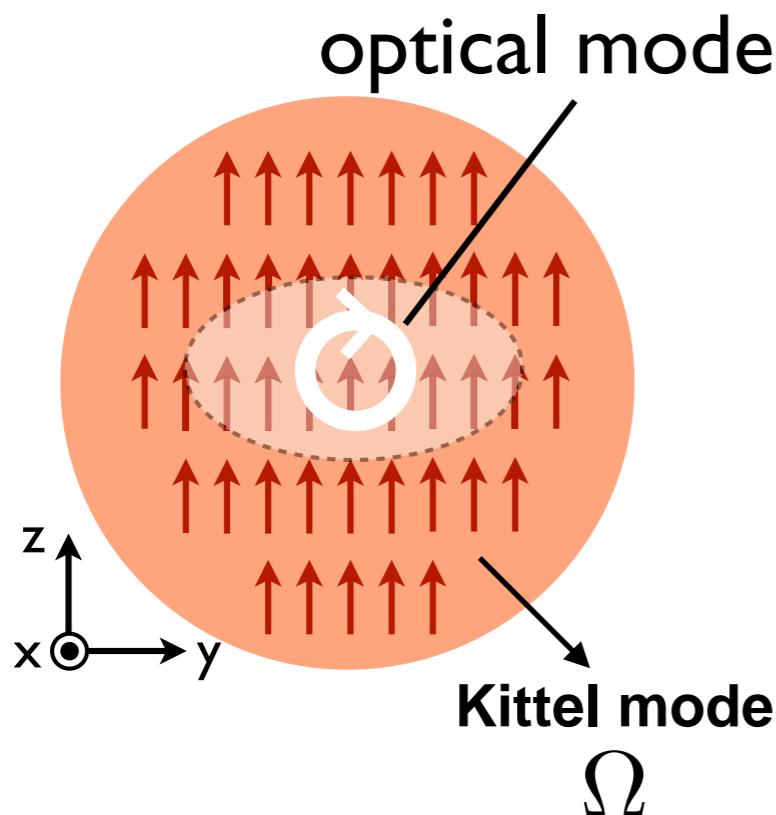
$$G = \frac{1}{S} \frac{c \theta_F}{4\sqrt{\epsilon}} \approx 1 \text{Hz}$$

**Optical magnetic field density**

$$b_{\text{opt}} \sim \frac{10^{-11} \text{T}}{\text{photon}/(\mu\text{m})^3}$$

# Cavity Optomagnonics: one optical mode

$$H = -\hbar\Delta\hat{a}^\dagger\hat{a} - \hbar\Omega\hat{S}_z + \hbar G\hat{S}_x\hat{a}^\dagger\hat{a}$$



driving laser detuning

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**Optical magnetic field density**

$$b_{\text{opt}} \sim \frac{10^{-11}\text{T}}{\text{photon}/(\mu\text{m})^3}$$

**Enhanced by # photons in the cavity!**

# Cavity Optomagnonics: one optical mode

## Classical Equation of Motion

$$\dot{a} = -i (GS_x - \Delta) a - \frac{\kappa}{2} (a - \alpha_{\max})$$
$$\dot{\mathbf{S}} = (G a^* a \mathbf{e}_x - \Omega \mathbf{e}_z) \times \mathbf{S} + \frac{\eta_G}{S} (\dot{\mathbf{S}} \times \mathbf{S})$$

Cavity decay rate

initial light amplitude

# Effective Equation of Motion for the Spin

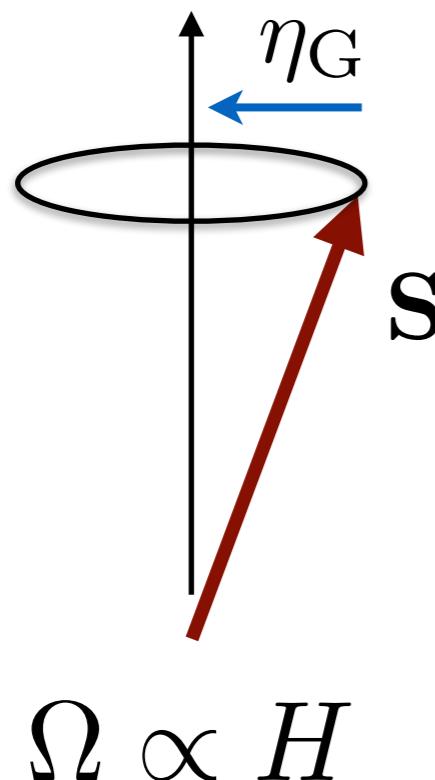
Fast cavity limit: integrate out the light field

$$\dot{\mathbf{S}} = \mathbf{B}_{\text{eff}} \times \mathbf{S} + \frac{\eta_{\text{opt}}}{S} (\dot{S}_x \mathbf{e}_x \times \mathbf{S})$$

**Effective Landau-Lifshitz-Gilbert equation of motion**

# Landau-Lifschitz-Gilbert Equation

Dynamics of the macrospin



$$\dot{\mathbf{S}} = -\Omega \mathbf{e}_z \times \mathbf{S} + \frac{\eta_G}{S} (\dot{\mathbf{S}} \times \mathbf{S})$$

damping constant  
↓  
phenomenological damping term  
(Gilbert damping)

precession frequency

# Effective Equation of Motion for the Spin

Fast cavity limit: integrate out the light field

$$\dot{\mathbf{S}} = \mathbf{B}_{\text{eff}} \times \mathbf{S} + \frac{\eta_{\text{opt}}}{S} (\dot{S}_x \mathbf{e}_x \times \mathbf{S})$$

## Effective Landau-Lifshitz-Gilbert equation of motion

Optically induced

magnetic field  $\mathbf{B}_{\text{eff}}$

dissipation  $\eta_{\text{opt}}$

**non-linear** functions of  $\mathbf{S}$

# Fast Cavity Limit

$$\dot{\mathbf{S}} = \mathbf{B}_{\text{eff}} \times \mathbf{S} + \frac{\eta_{\text{opt}}}{S} \left( \dot{S}_x \mathbf{e}_x \times \mathbf{S} \right)$$

**effective field**

$$\mathbf{B}_{\text{eff}} = -\Omega \mathbf{e}_z + \mathbf{B}_{\text{opt}}$$

$$\mathbf{B}_{\text{opt}} = \frac{G}{[(\frac{\kappa}{2})^2 + (\Delta - GS_x)^2]} \left( \frac{\kappa}{2} \alpha_{\text{max}} \right)^2 \mathbf{e}_x$$

**damping  
can change sign**

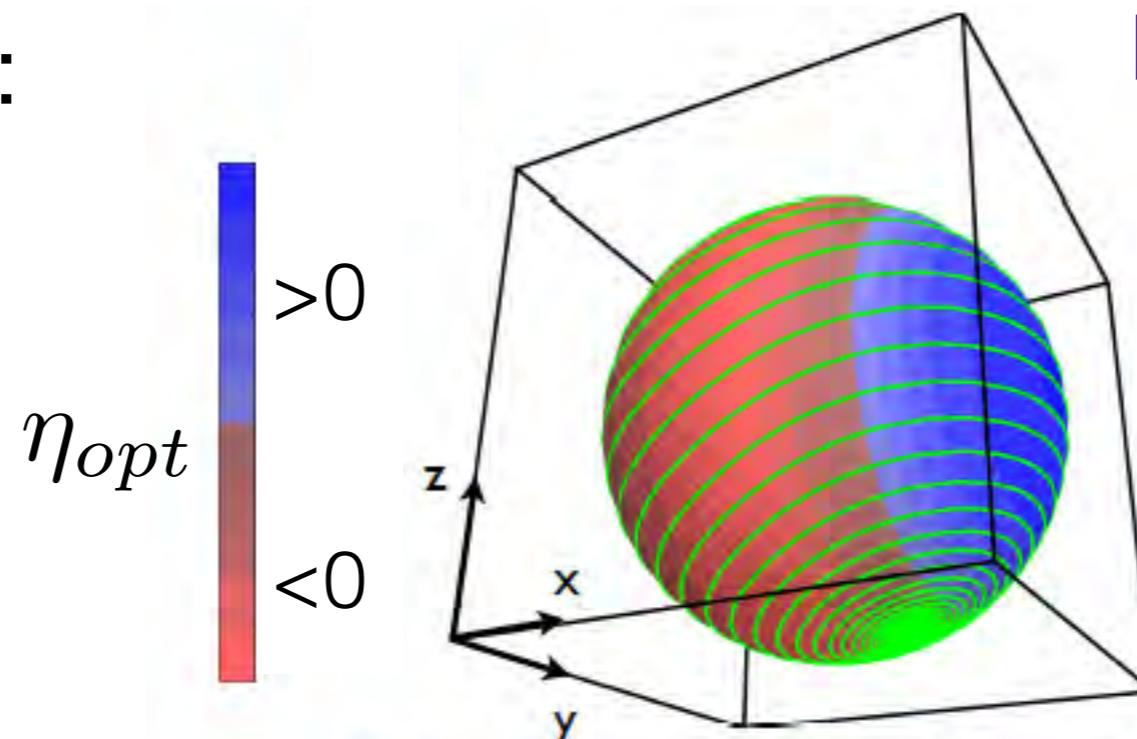
$$\eta_{\text{opt}} = -2G\kappa S |\mathbf{B}_{\text{opt}}| \frac{(\Delta - GS_x)}{[(\frac{\kappa}{2})^2 + (\Delta - GS_x)^2]^2}$$

**tunable by the external laser drive**

# Spin Dynamics: Fast Cavity Limit

Blue detuned case:

dissipation  
changes sign

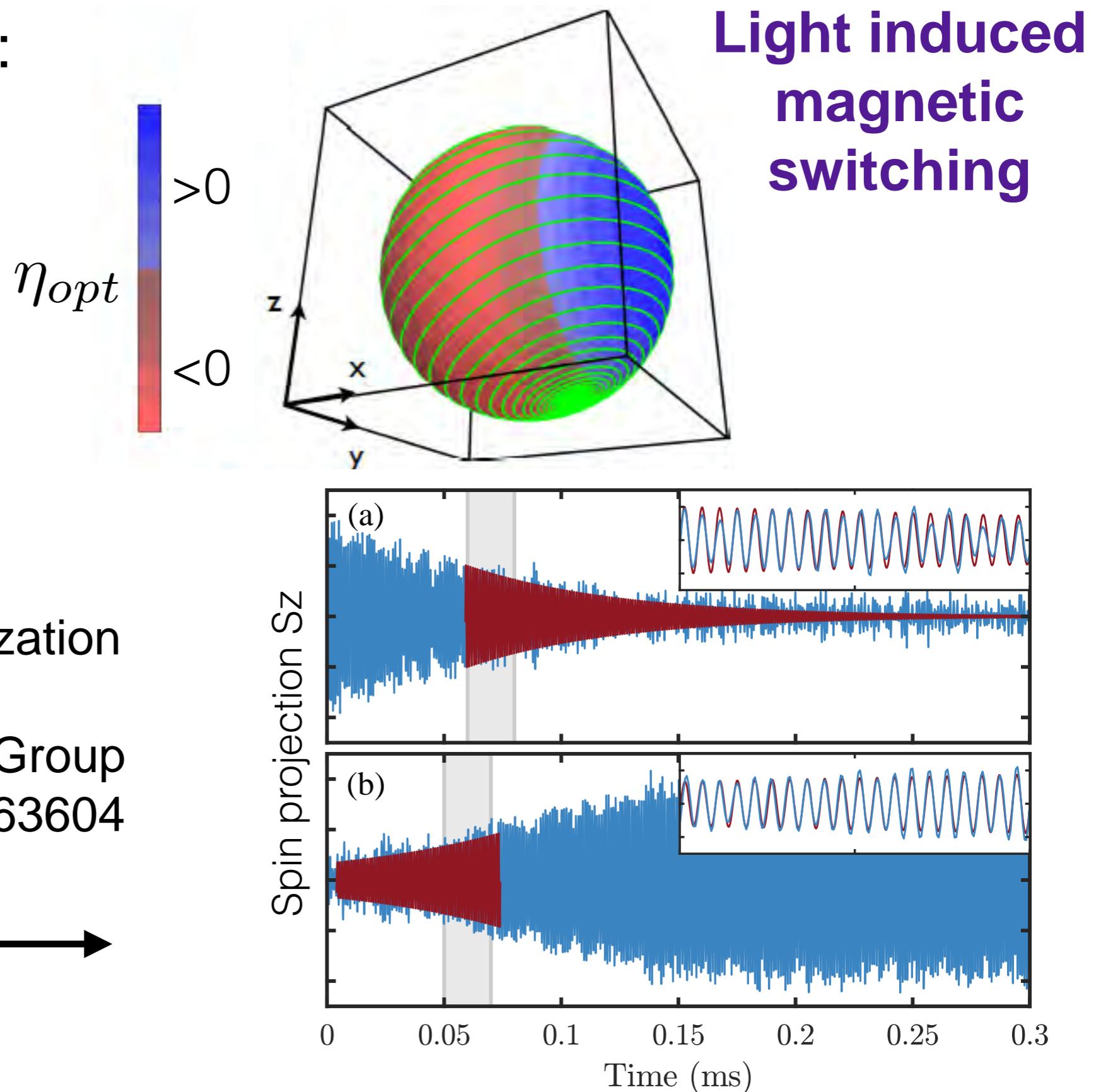


Light induced  
magnetic  
switching

# Spin Dynamics: Fast Cavity Limit

Blue detuned case:

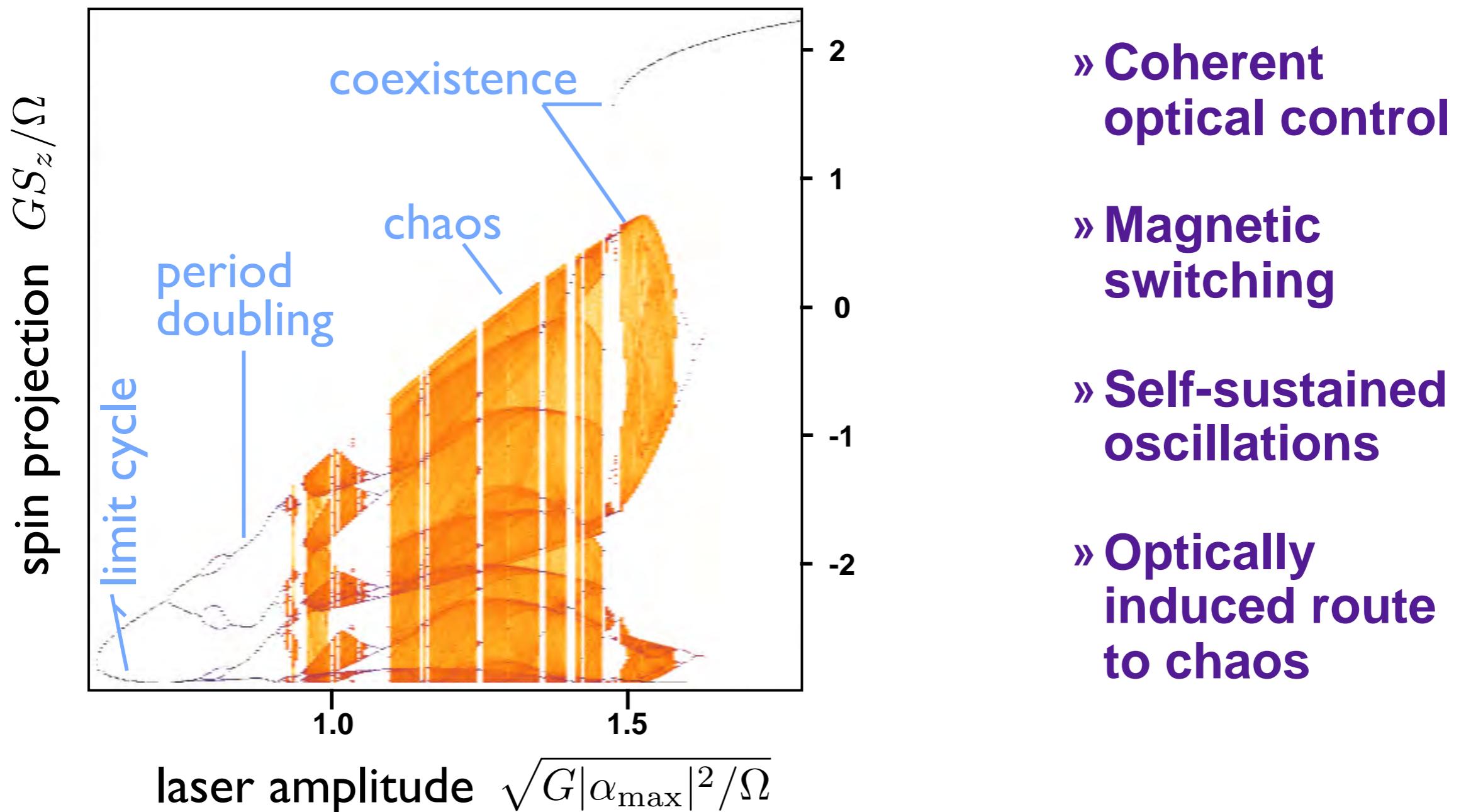
dissipation  
changes sign



See experimental realization  
with cold atoms,  
Dan M. Stamper-Kurn Group  
Phys. Rev. Lett. **118**, 063604  
(2017)



# Full Nonlinear Dynamics





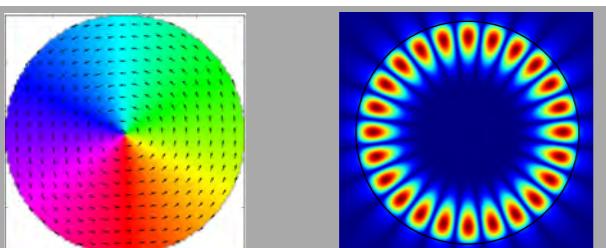
## Introduction and motivation



## Optomagnonic Hamiltonian



## Optically induced spin dynamics



## Magnetic textures: vortex in a disk



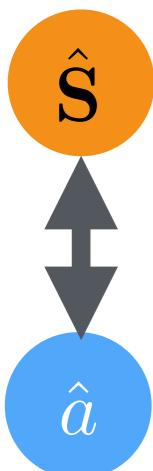
## Summary

But...

## Problem

the state of the art optomagnonic coupling is very small

Coupling per photon  $g_0 \approx 60\text{Hz}$       Cooperativity  $\mathcal{C} \approx 10^{-7}$



(for small oscillations: spin  $\longrightarrow$  harmonic oscillator)

$$\hbar G \hat{S}_x \hat{a}^\dagger \hat{a} \approx \underbrace{\hbar G \sqrt{S/2}}_{g_0} \hat{a}^\dagger \hat{a} (\hat{b} + \hat{b}^\dagger)$$

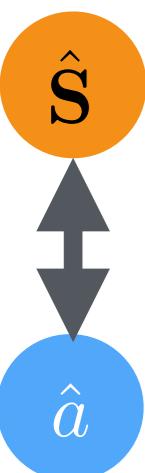
But...

## Problem

the state of the art optomagnonic coupling is too small

Coupling per photon  $g_0 \approx 60\text{Hz}$

Cooperativity  $\mathcal{C} \approx 10^{-7}$



## Some solutions

smaller systems

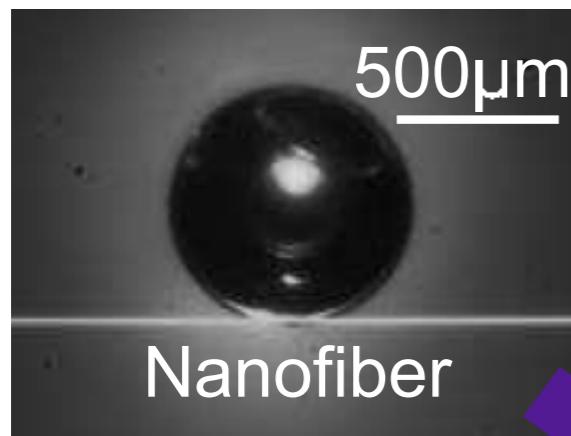
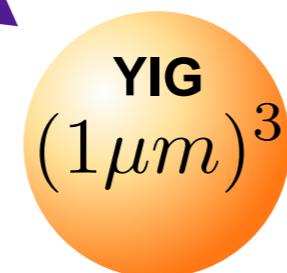
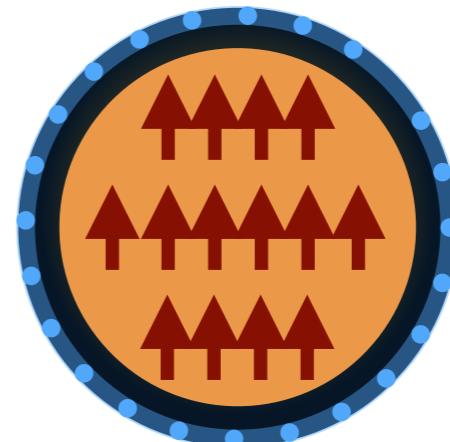


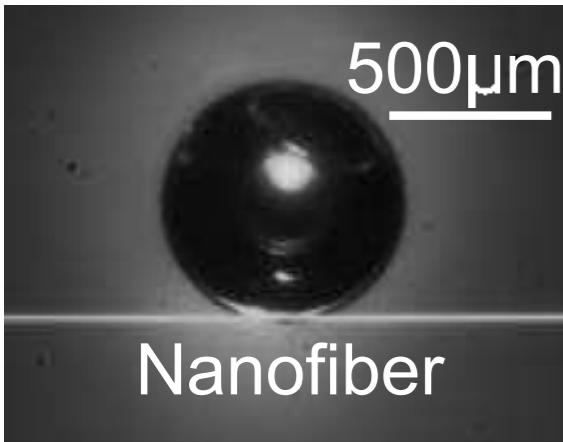
Fig: Osada et. al.  
PRL 116, 223601

better overlap of modes



?

# Optomagnonics beyond the Kittel mode



Optomagnetic coupling demonstrated

- Non-homogeneous magnon mode
- Homogeneous ground state

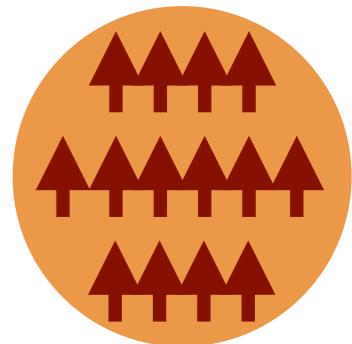
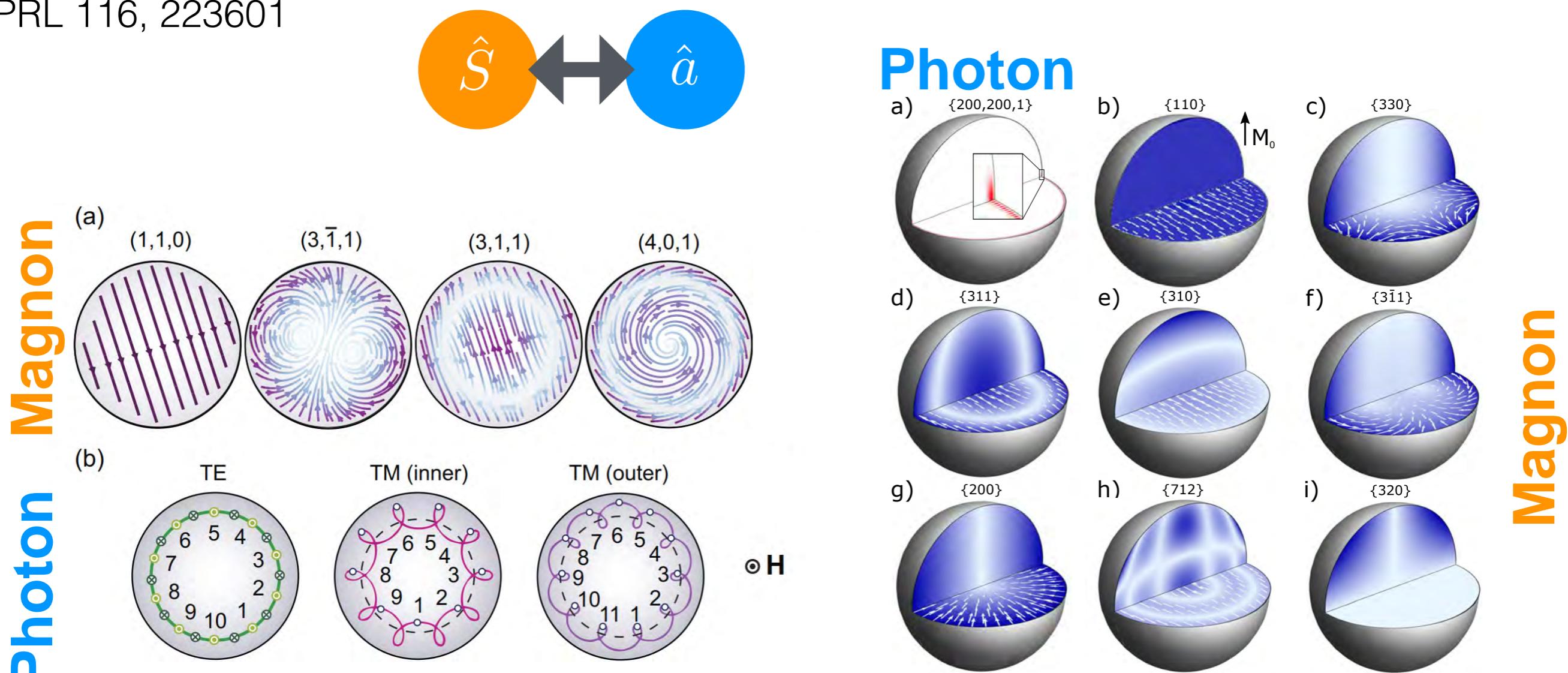
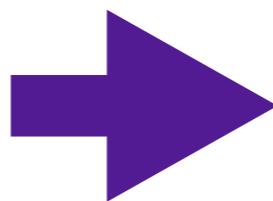


Fig: Osada et. al.  
PRL 116, 223601

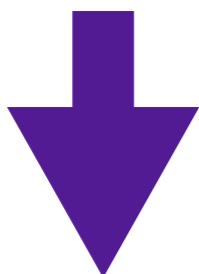
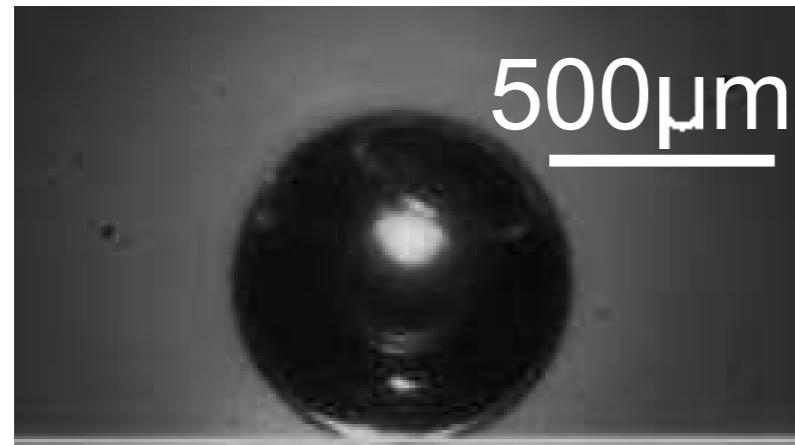


# Magnetic Textures

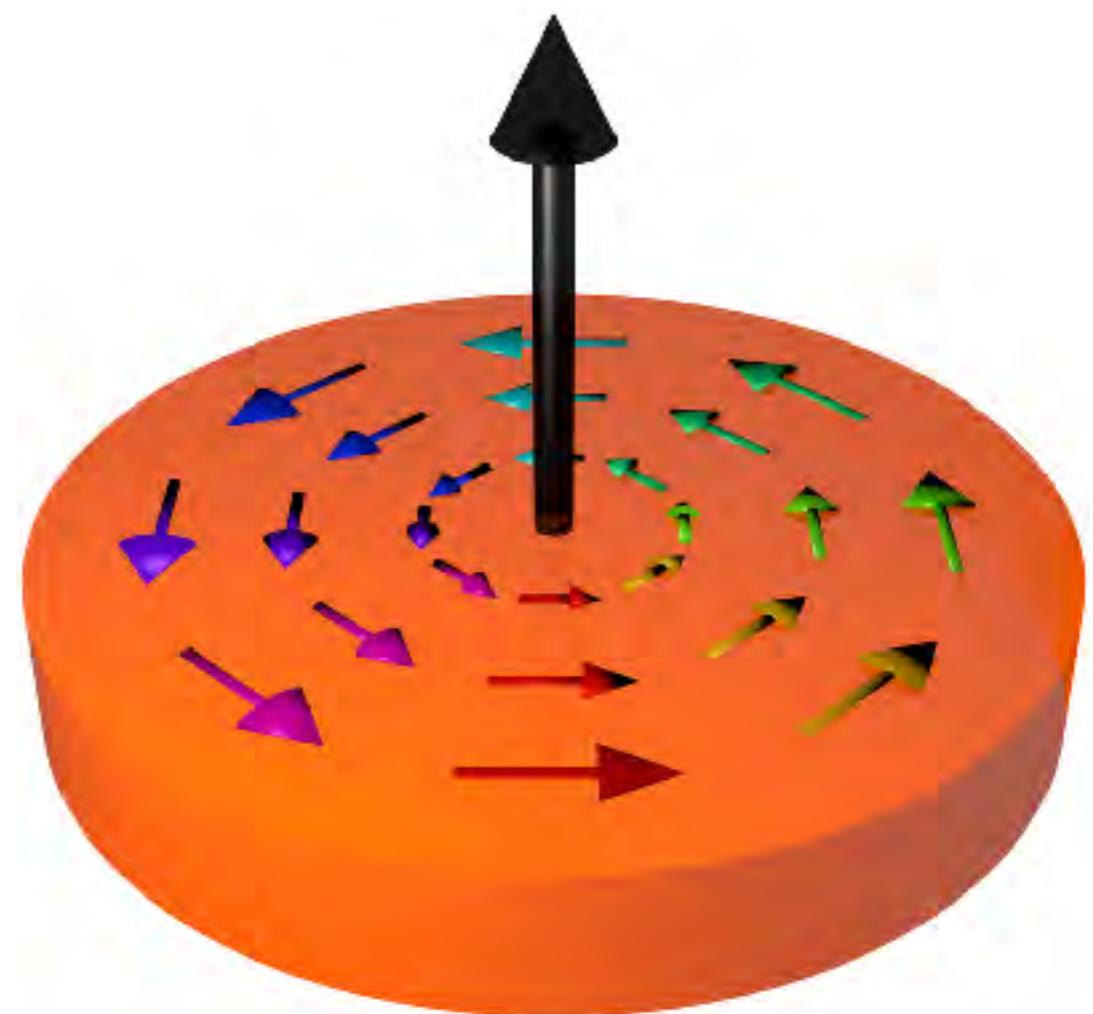
smaller systems



Magnetic textures

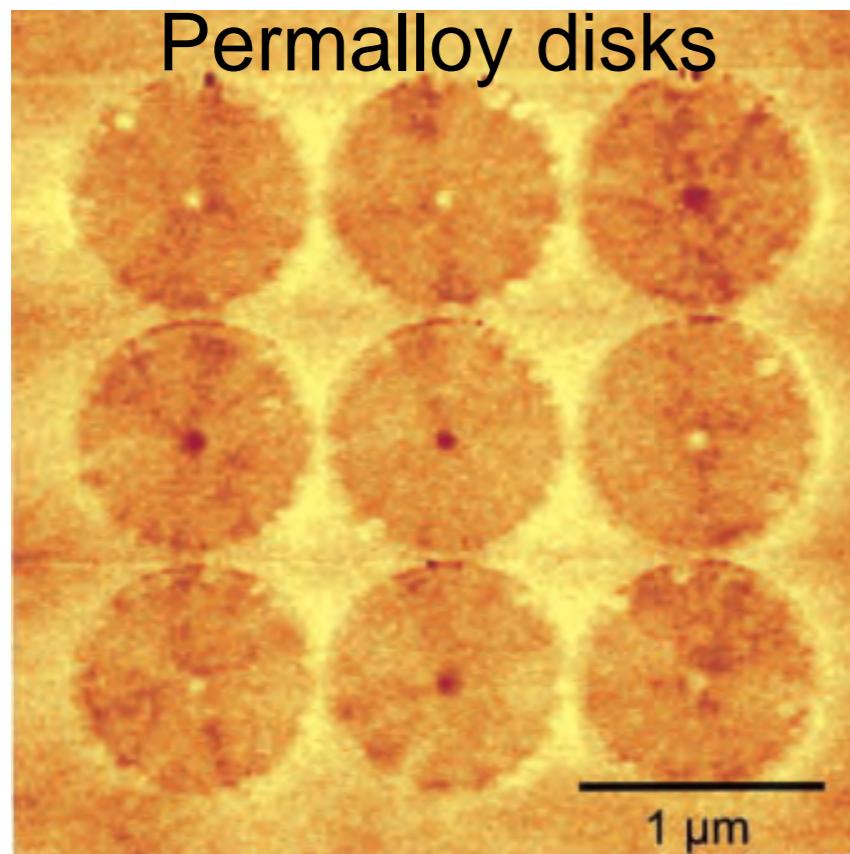


YIG  
 $(1\mu m)^3$

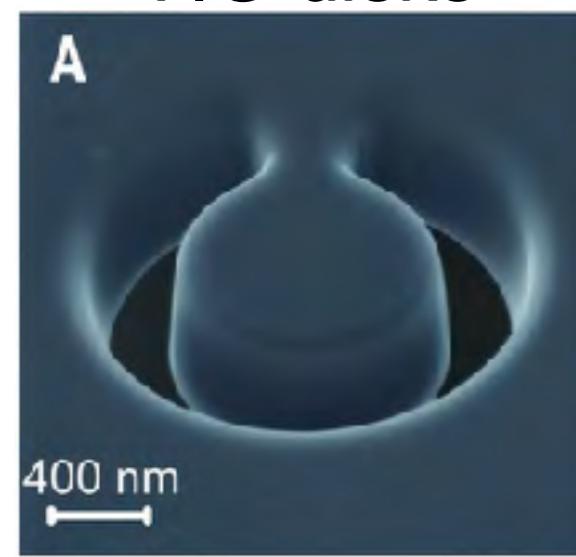


Vortex in a micro disk

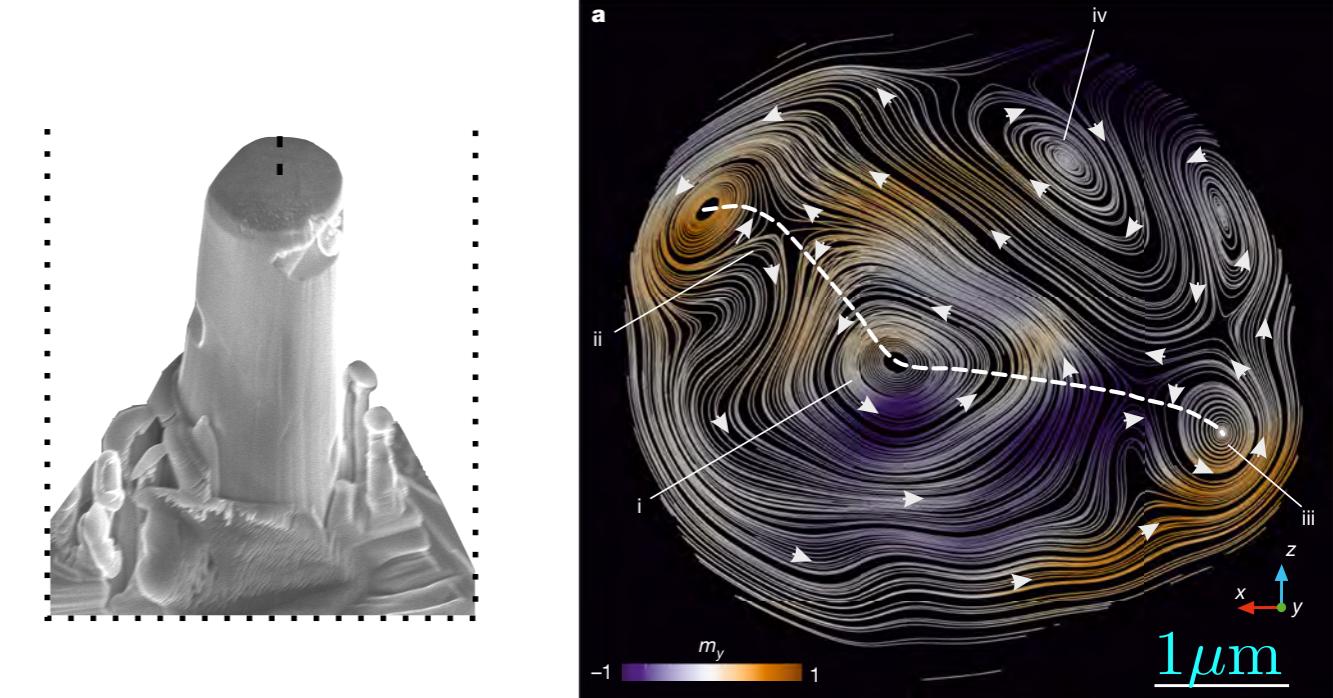
# Magnetic Textures: Vortex in Microdisks



T.Shinjo et al, Science 289, 930 (2000)

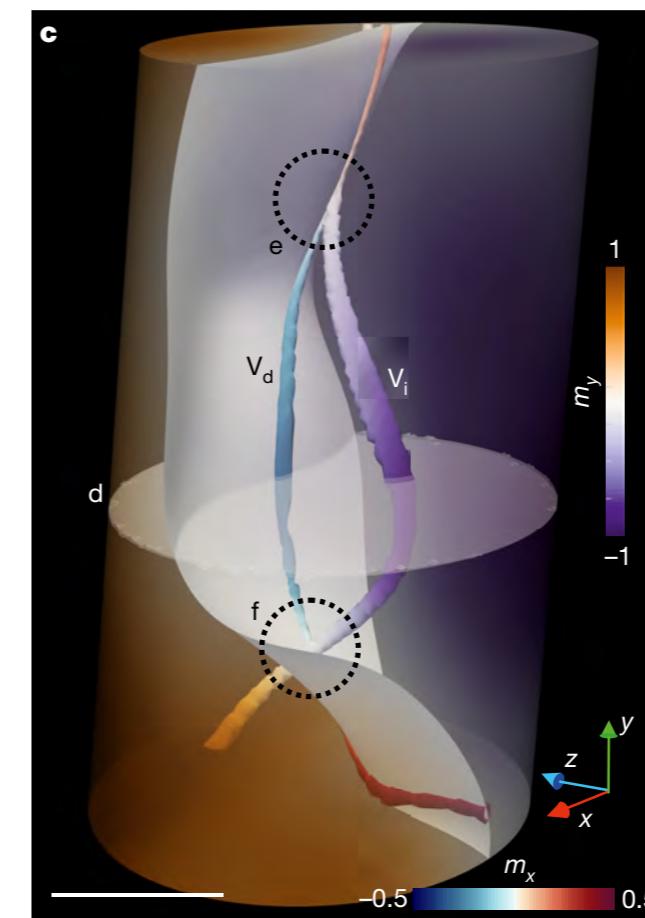


Losby et al, Science 350, 798 (2015)



Cobalt Gadolinium  
pillars

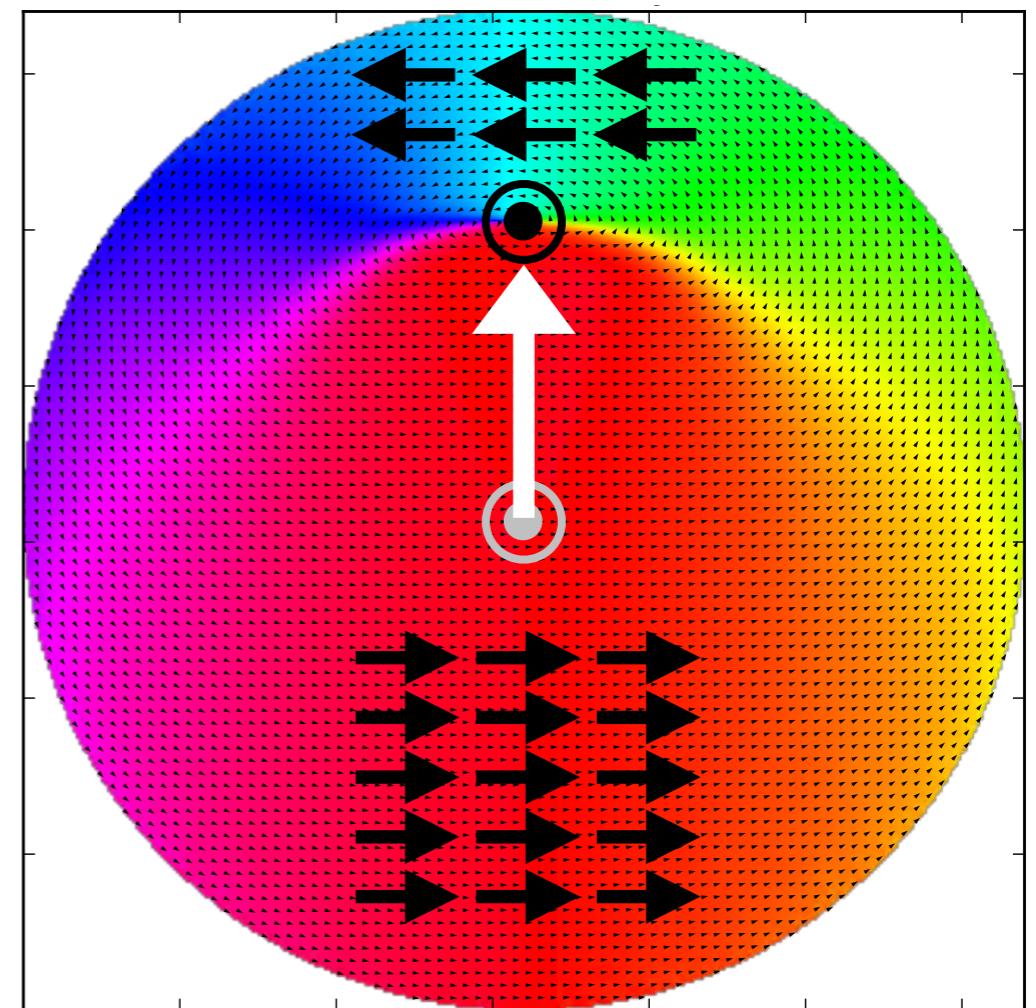
C. Donally et al,  
Nature 547  
328 (2017)



# Vortex

- Position tunable by a magnetic field

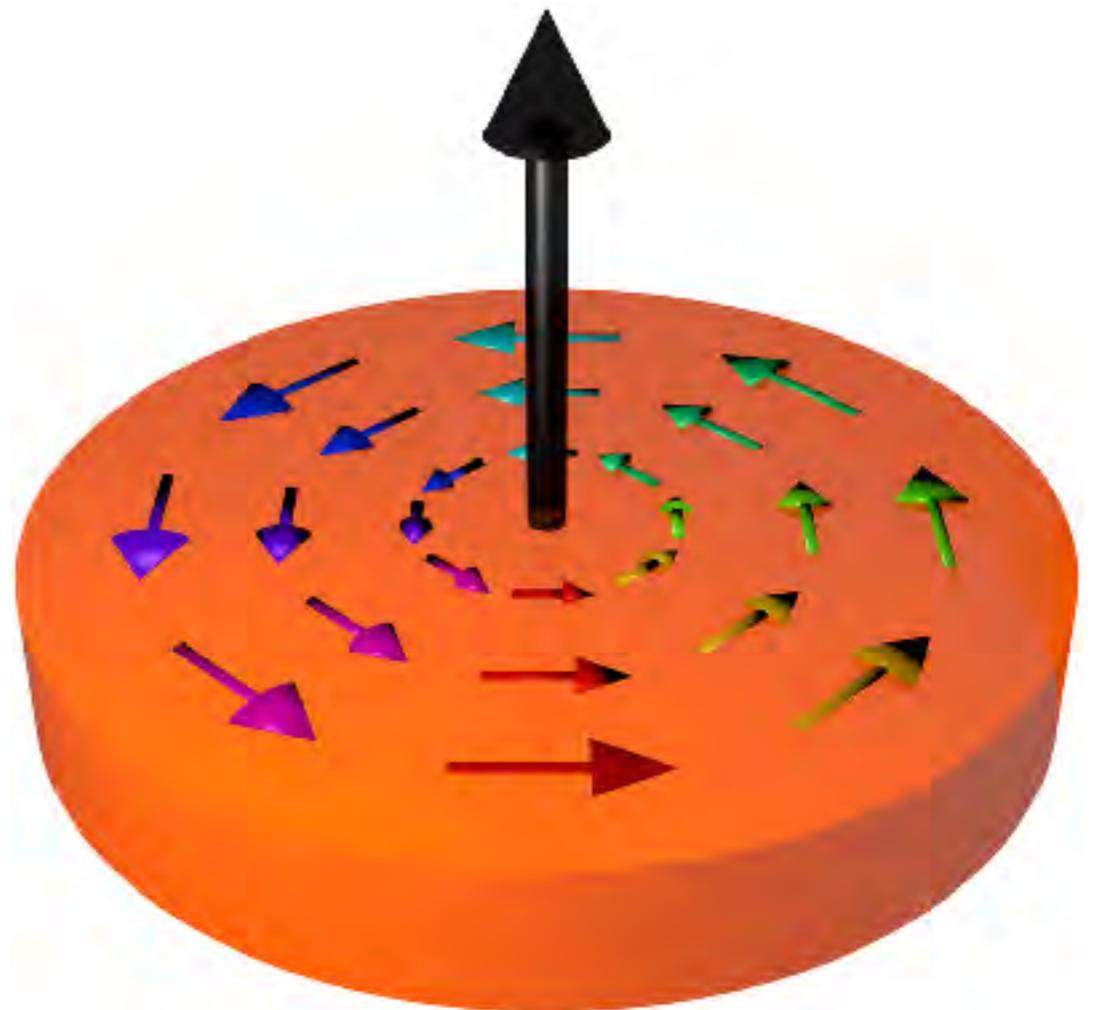
View from above



$B_{\text{ext}}$

# Vortex

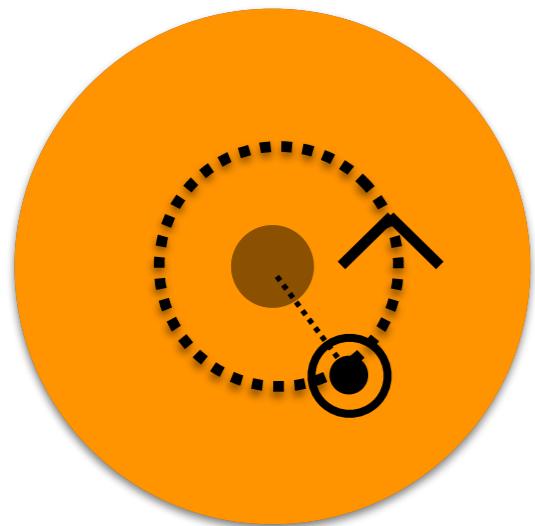
- **Supports localized magnon modes**



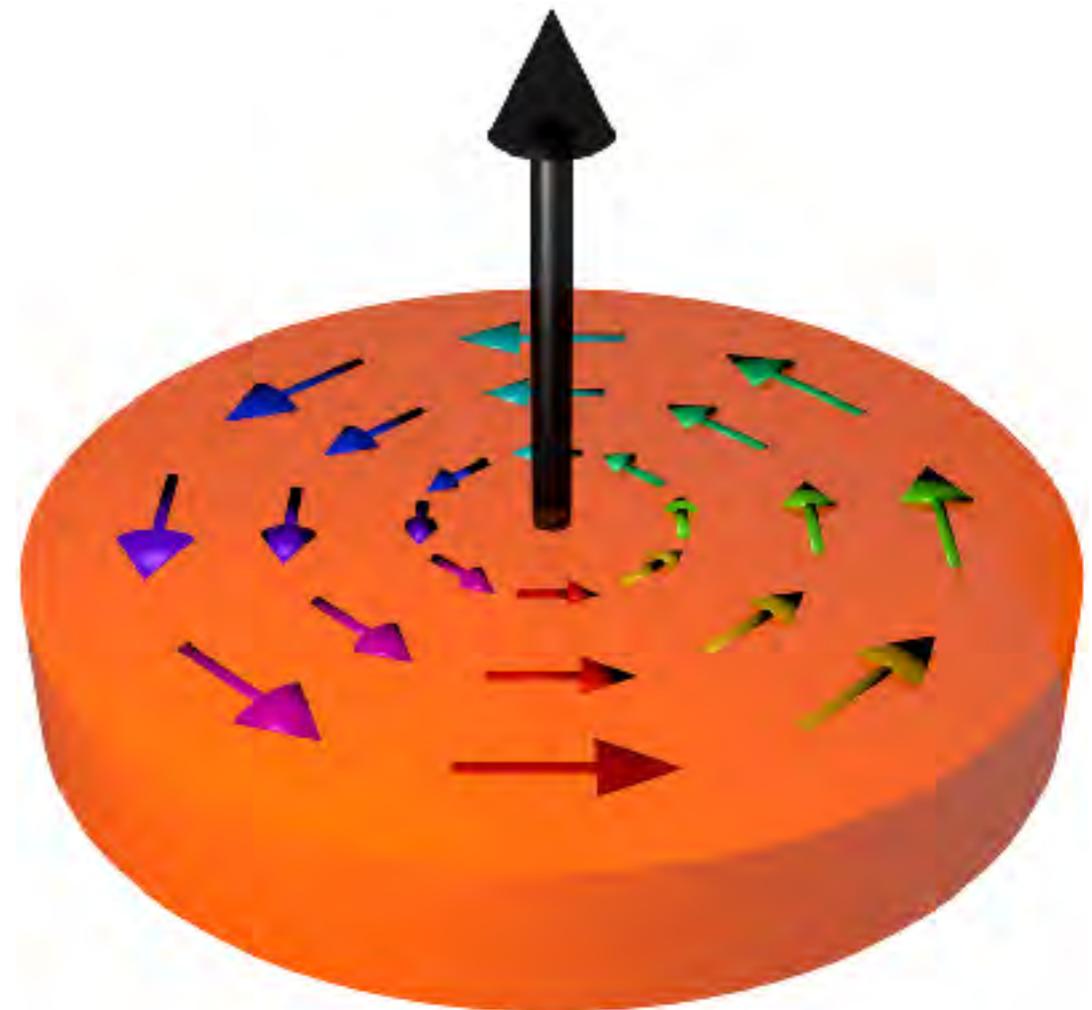
# Vortex

- Supports localized magnon modes

## Gyrotropic mode

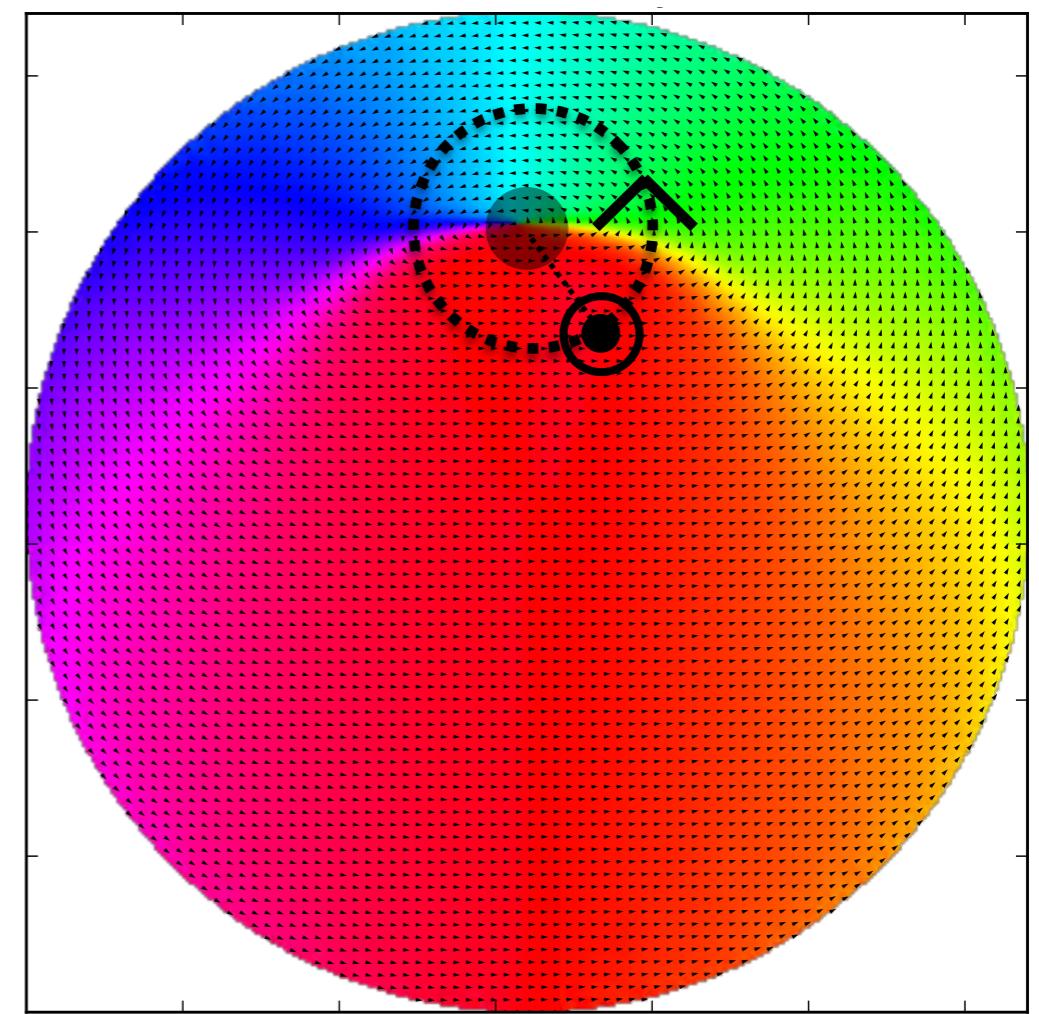
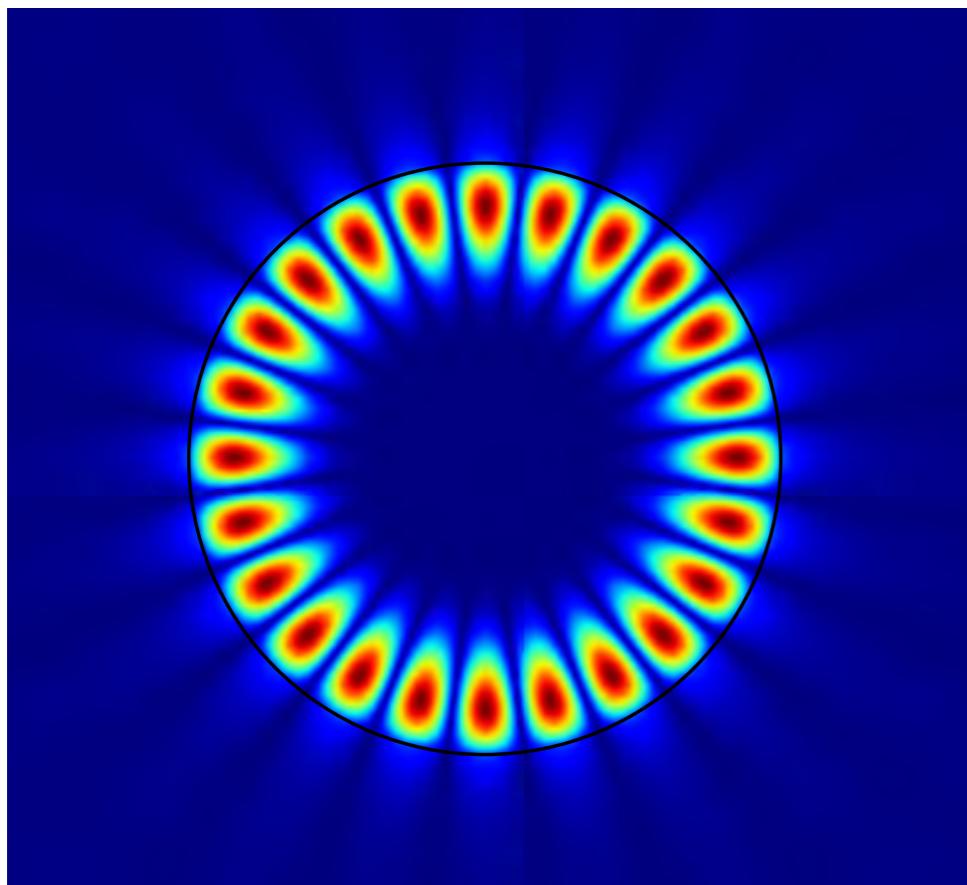


- Sub -GHz
- Gapped



# Vortex

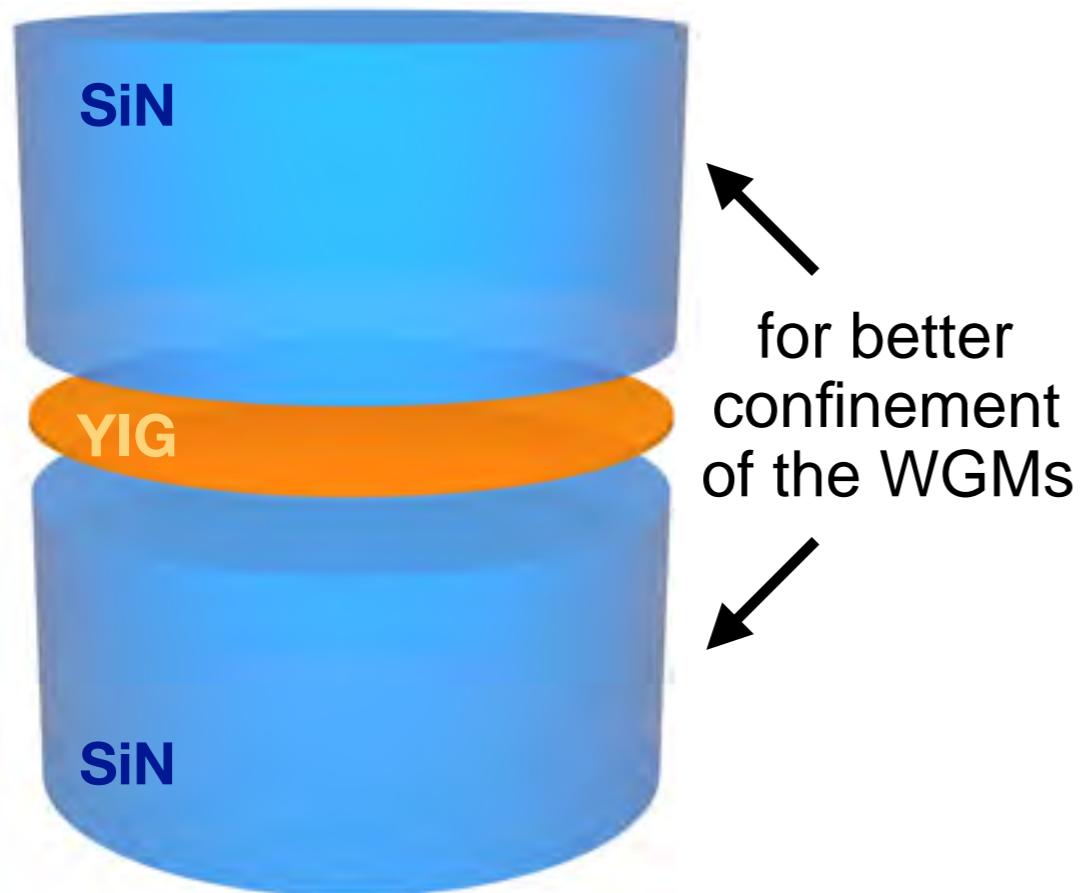
Coupling to optical  
Whispering Gallery Modes?



$\mathbf{B}_{\text{ext}}$

# Setup: two cases

## Thin Disk Heterostructure

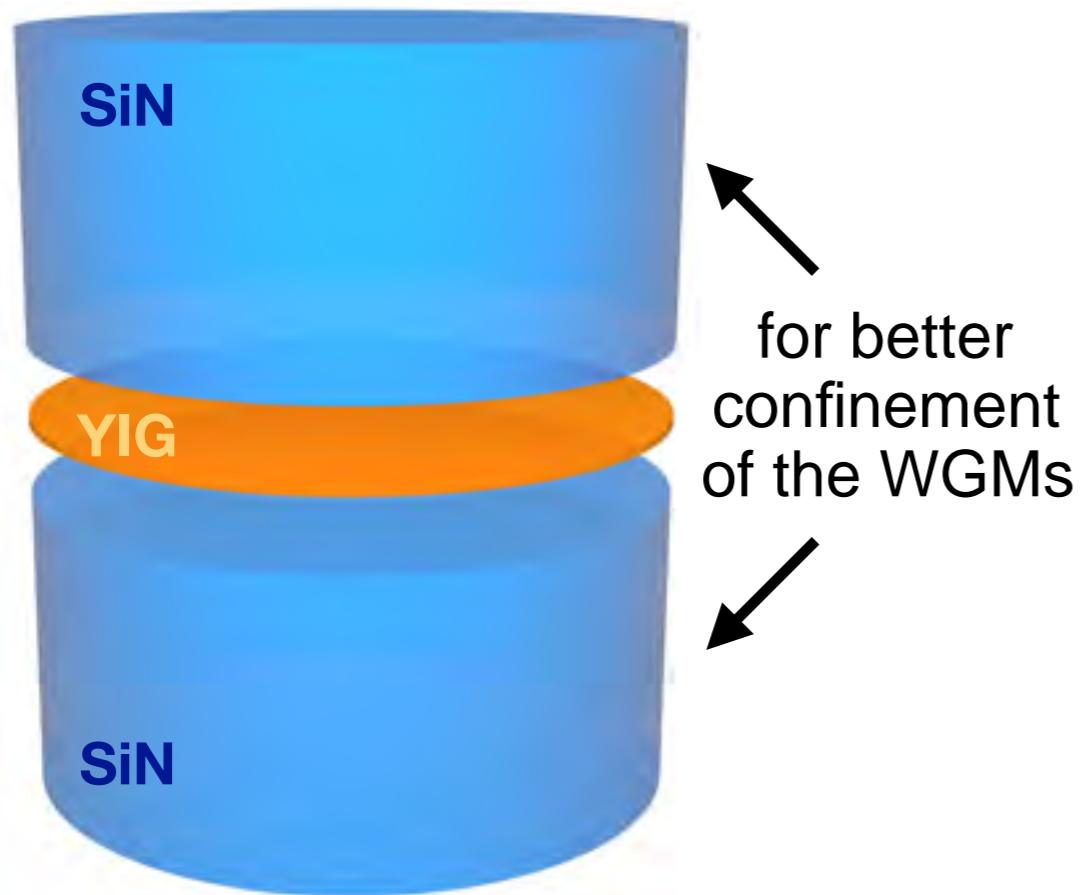


$$h_{\text{YIG}} \sim l_{ex} \sim 10\text{nm}$$

- The magnon modes live in the thin YIG disk
- The optical WGMs live in the whole structure

# Setup: two cases

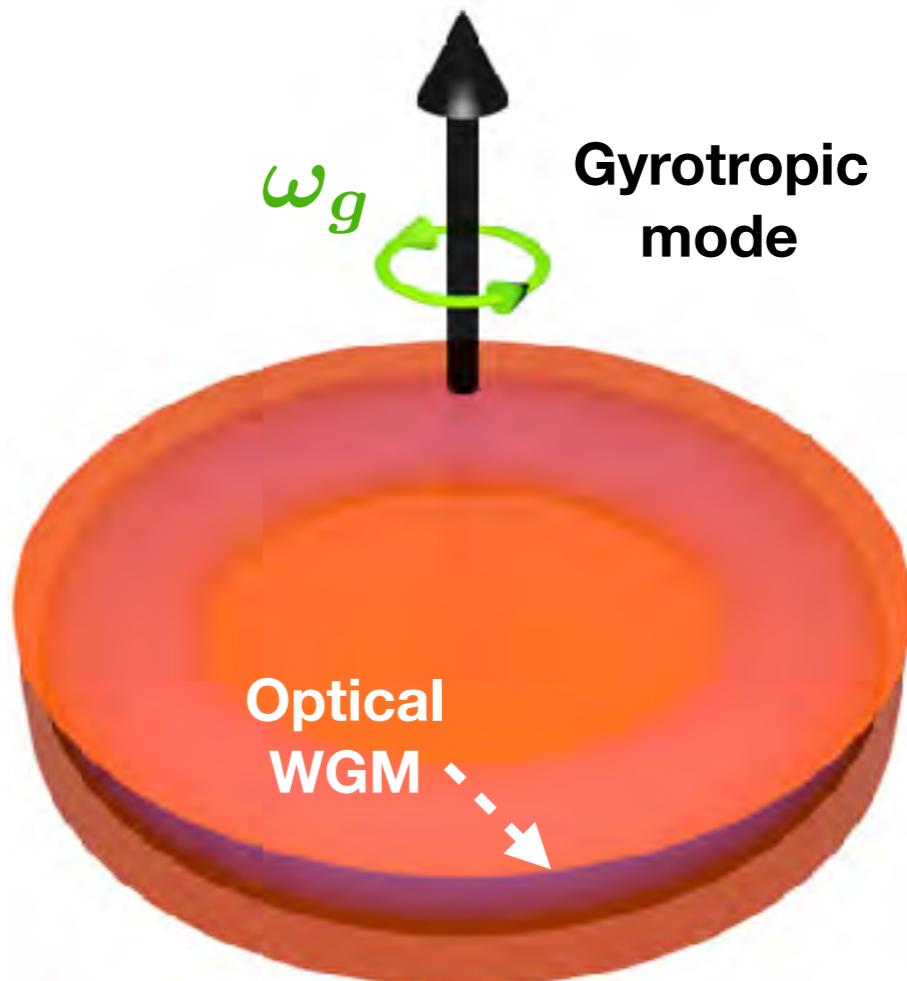
## Thin Disk Heterostructure



$$h_{\text{YIG}} \sim l_{ex} \sim 10\text{nm}$$

- The magnon modes live in the thin YIG disk
- The optical WGMs live in the whole structure

## “Thick” YIG Disk

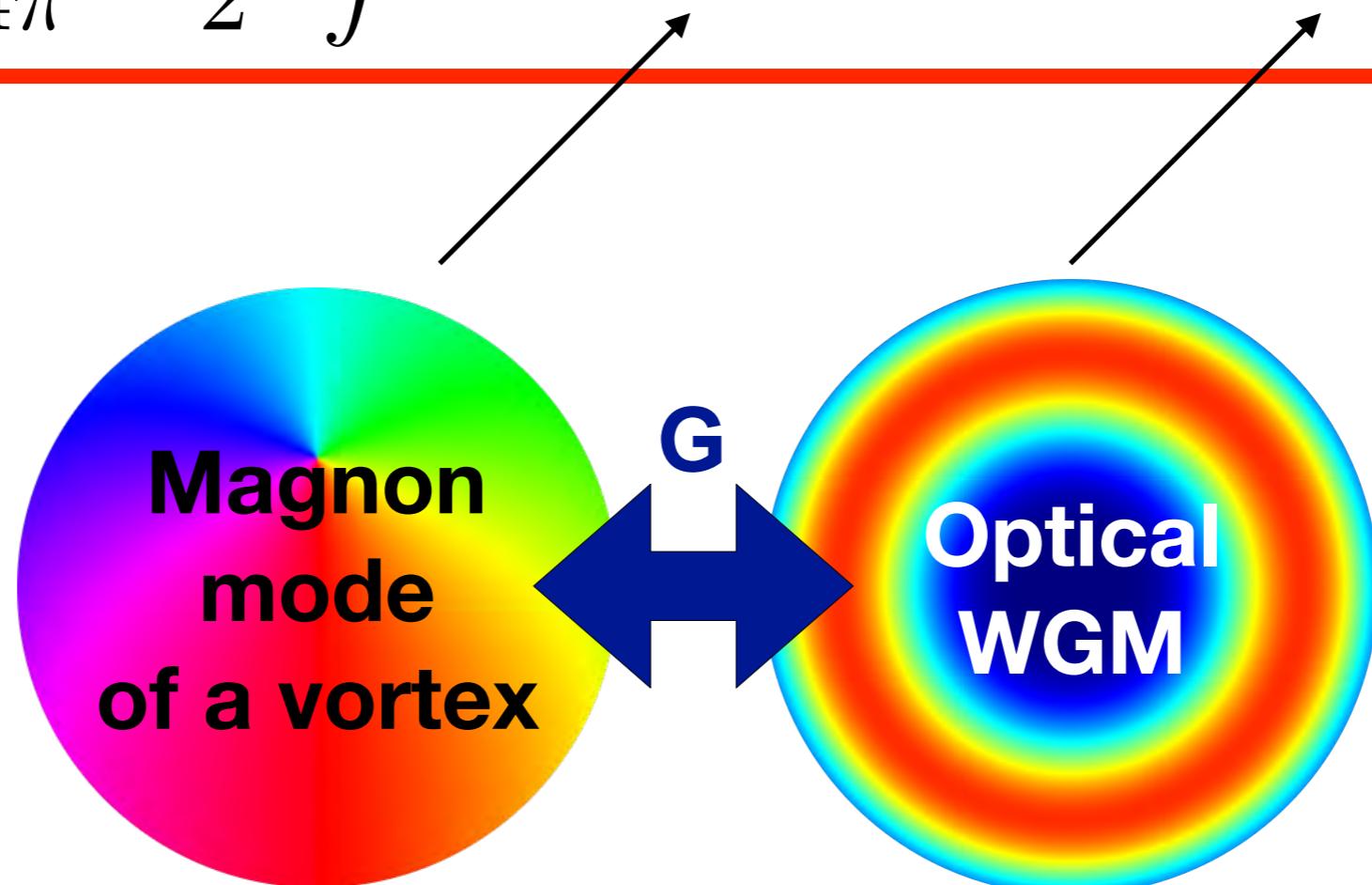


$$h_{\text{YIG}} \sim R_{\text{YIG}} \sim 1\mu\text{m}$$

- YIG disk: magnons + optical cavity
- Magnetic texture: Non-trivial z-dependence

# Optomagnonic Coupling

$$H_c = -i \frac{\theta_F \lambda_n}{4\pi} \frac{\epsilon_0 \epsilon}{2} \int d\mathbf{r} \ m(\mathbf{r}, t) \cdot [\mathbf{E}^*(\mathbf{r}, t) \times \mathbf{E}(\mathbf{r}, t)]$$



Vansteenkiste et. al  
AIP Advances 4,  
107133 (2014)

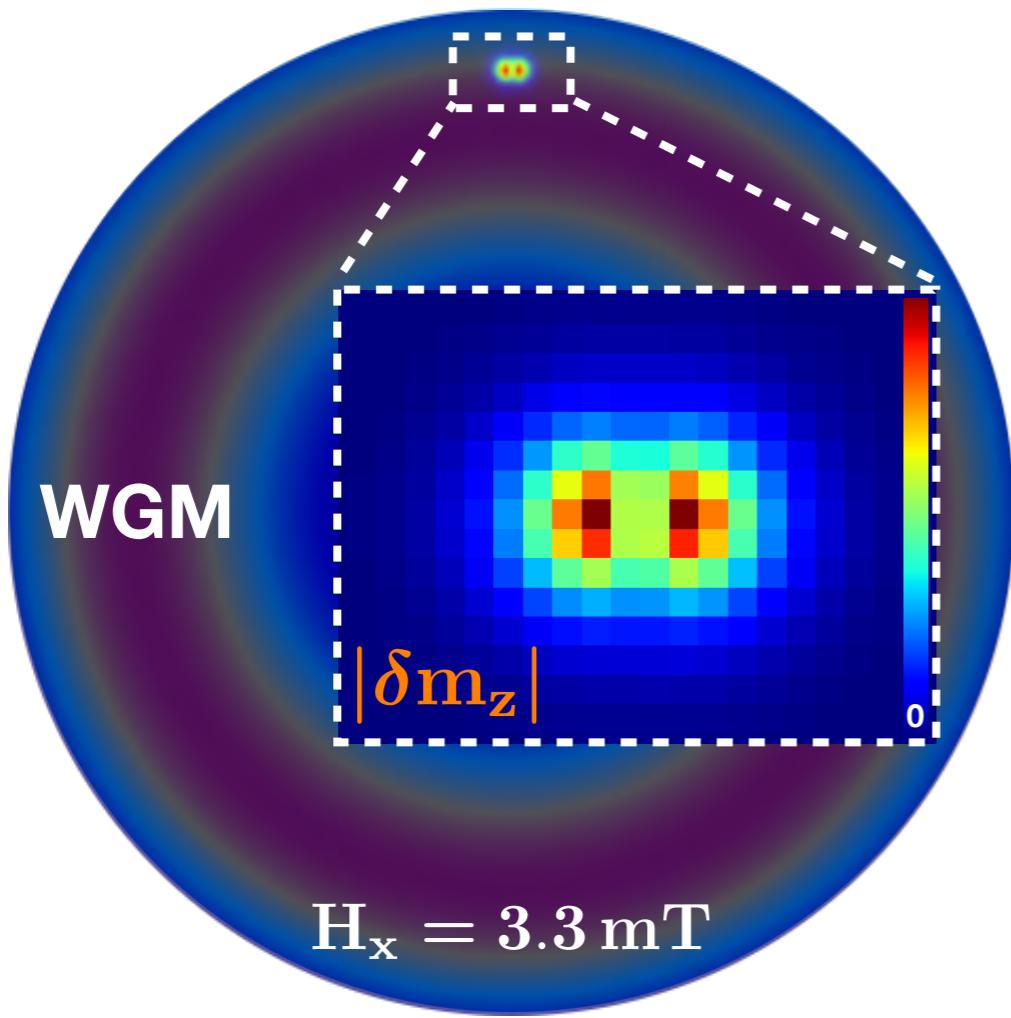
MuMax3

COMSOL

Simulation software

# Vortex in a thin disk: optomagnonic coupling spatial dependence

Magnon and optical  
modes

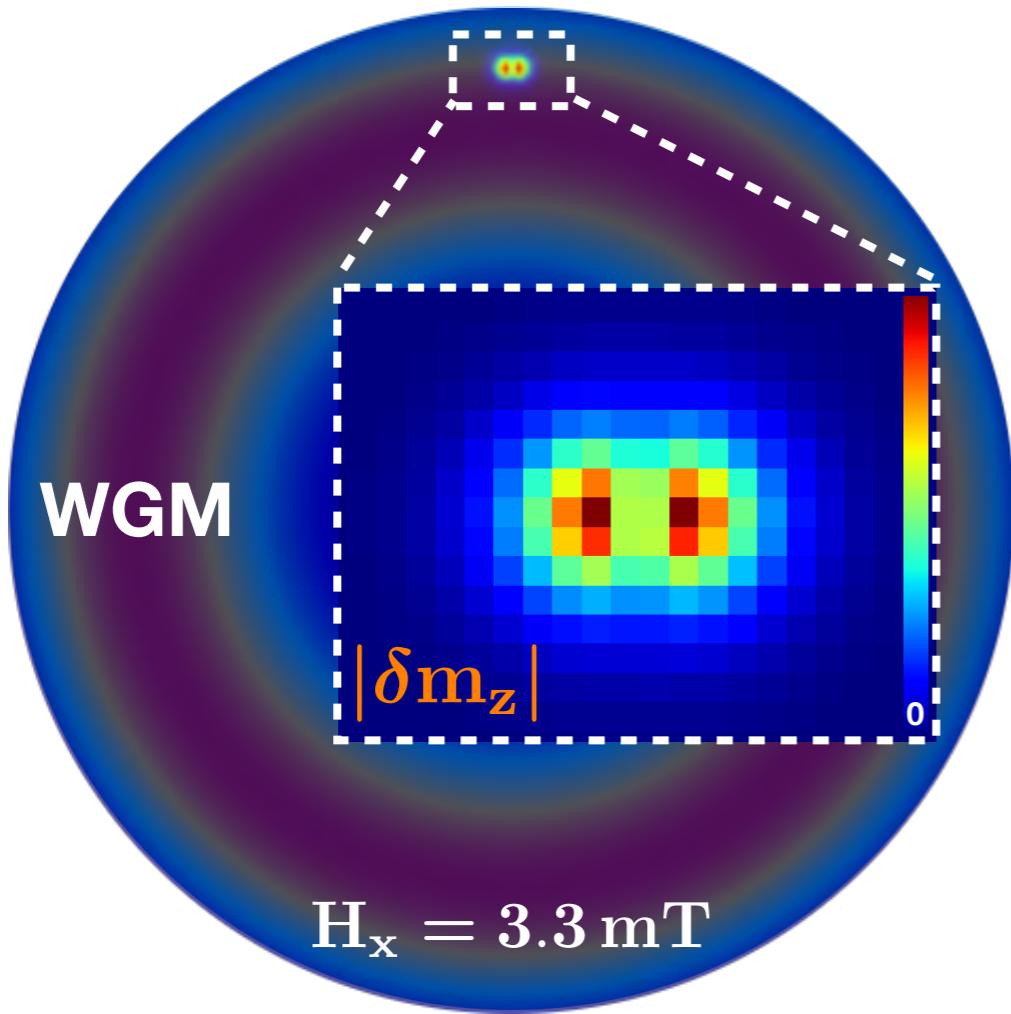


Gyrotropic mode  $\omega_g \approx 30 \text{ MHz}$

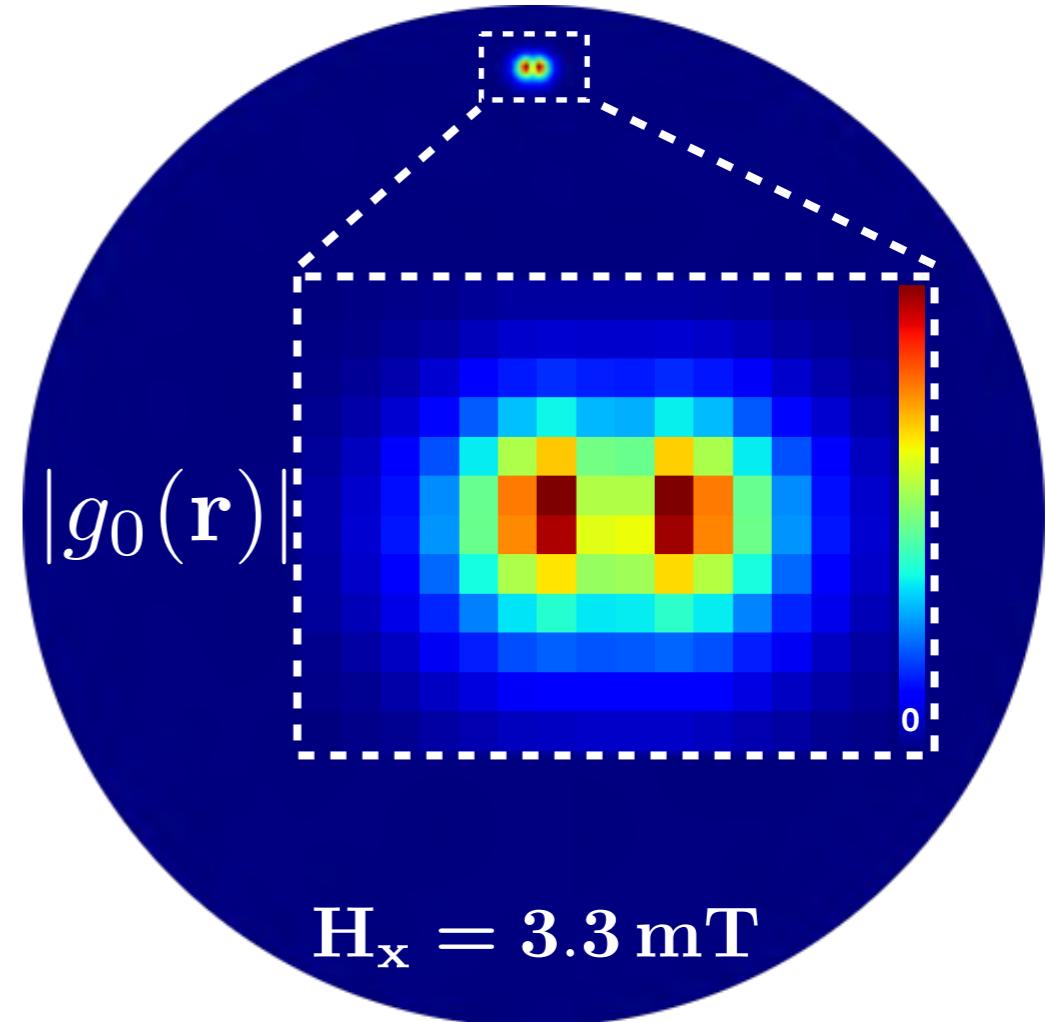
# Vortex in a thin disk: optomagnonic coupling

## spatial dependence

Magnon and optical  
modes

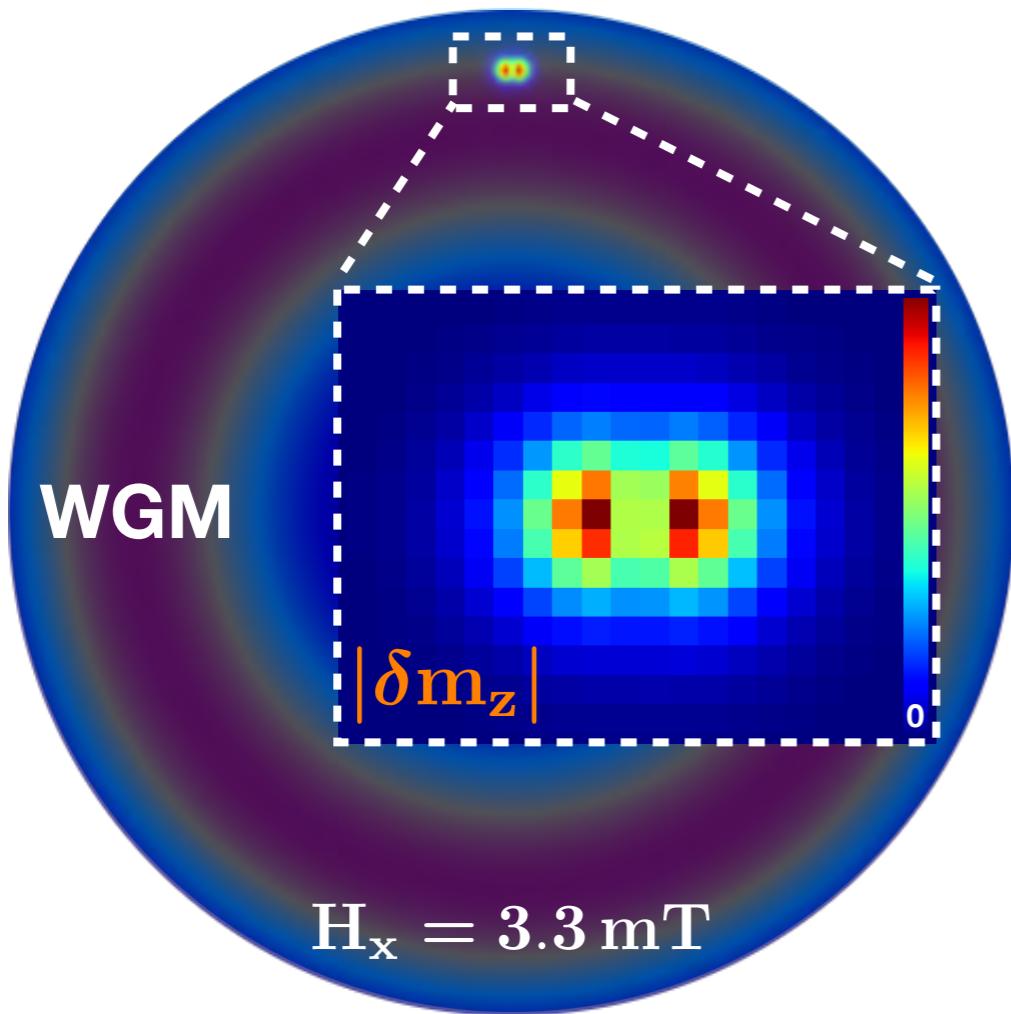


Optomagnonic  
coupling

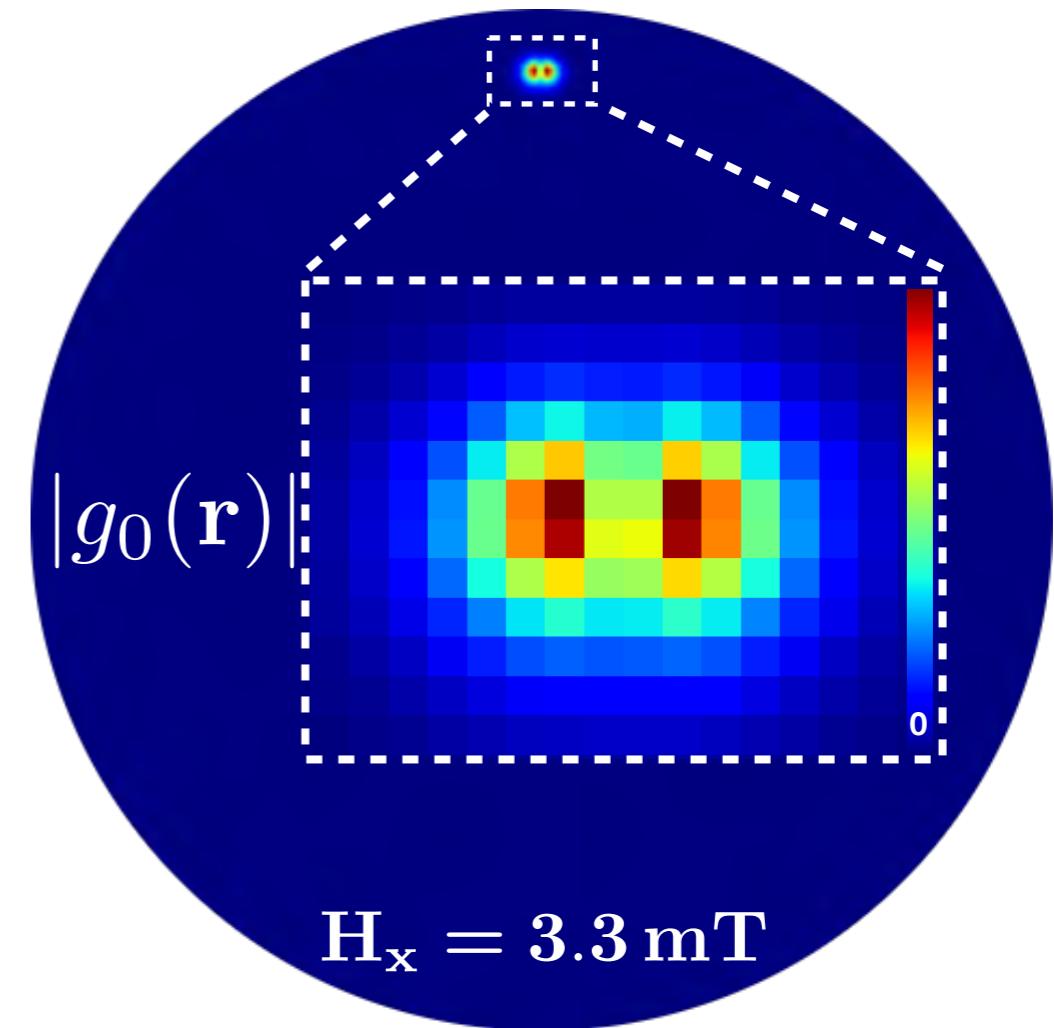


# Vortex in a thin disk: optomagnonic coupling spatial dependence

Magnon and optical  
modes



Optomagnonic  
coupling



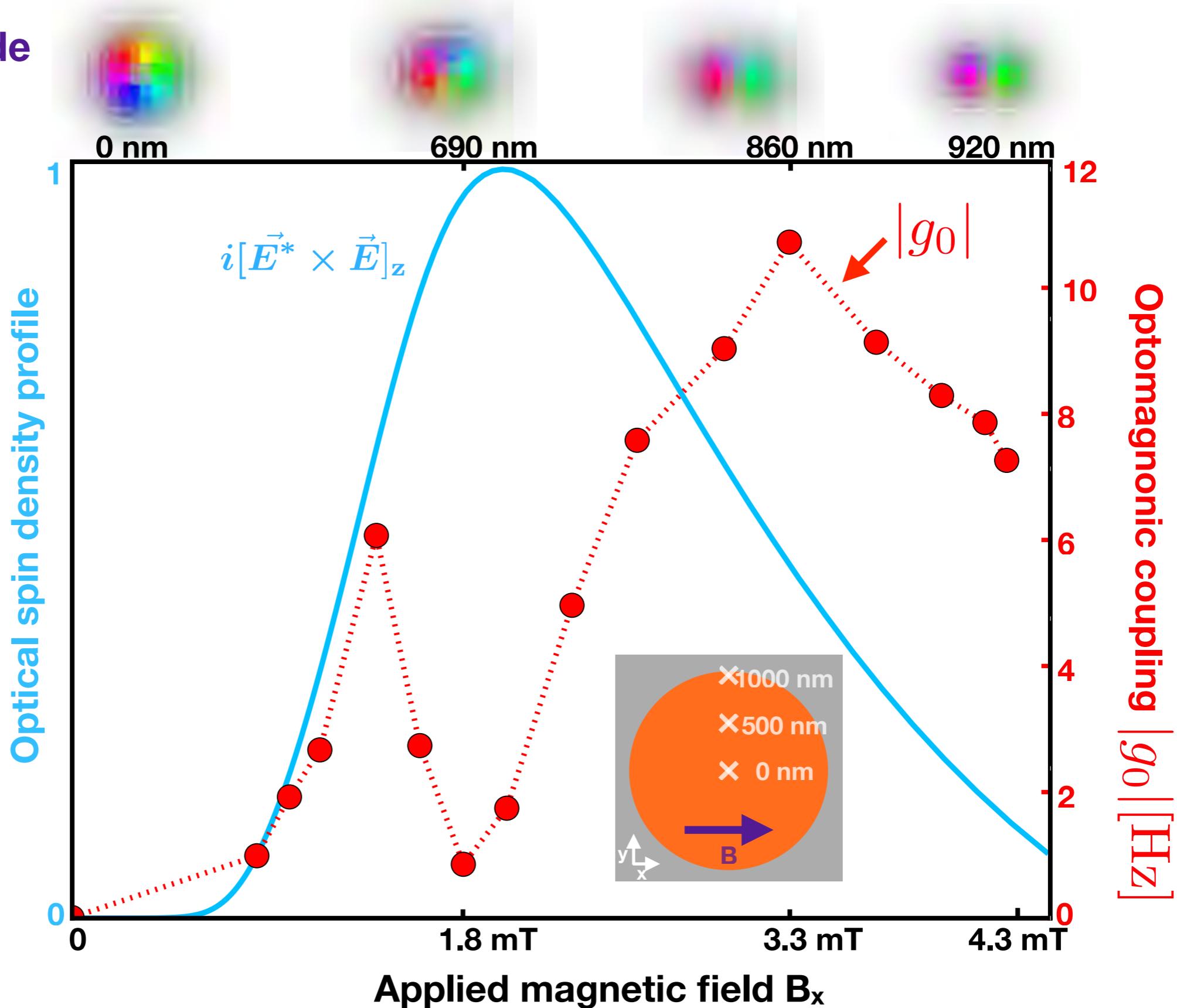
integrate over the  
whole volume

# Thin disk: tuneable coupling via B-field

Gyrotropic mode profile

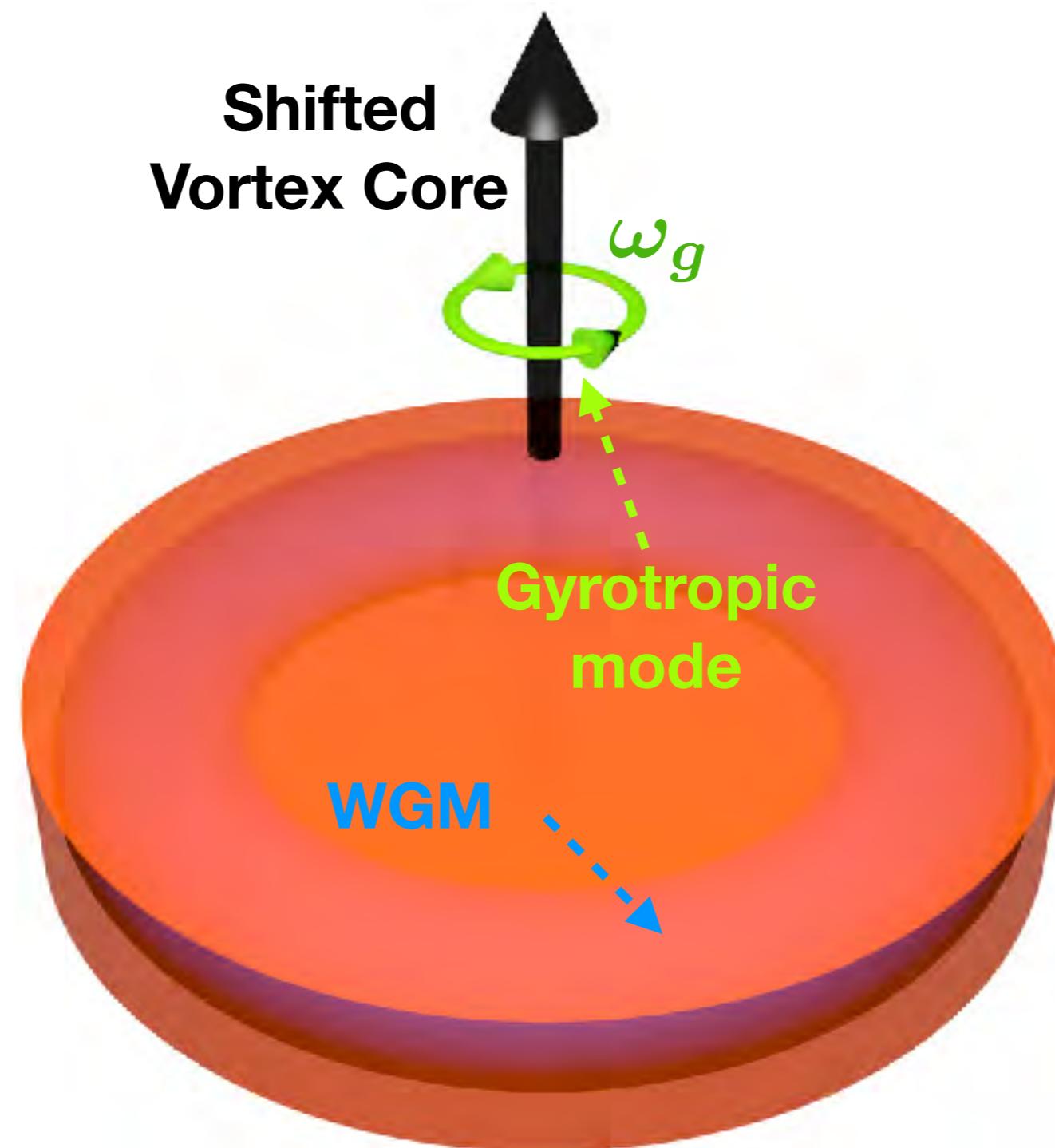
0  $\pi$   $2\pi$

Agrees with analytical approximate solution



# Full YIG microdisk

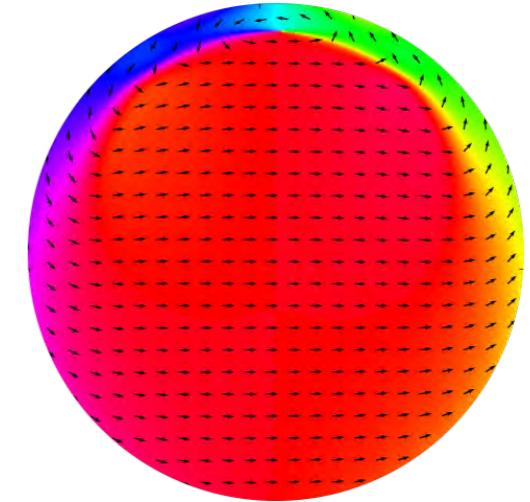
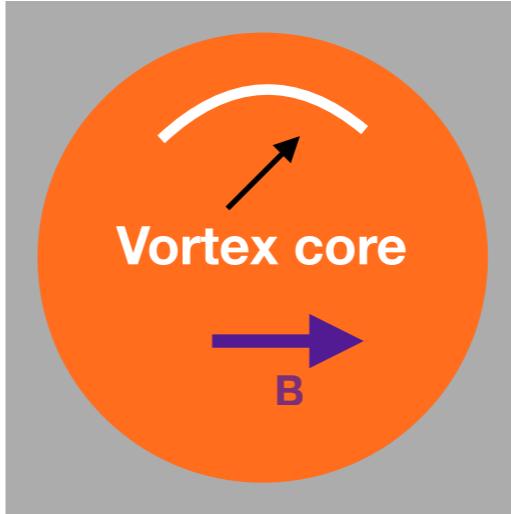
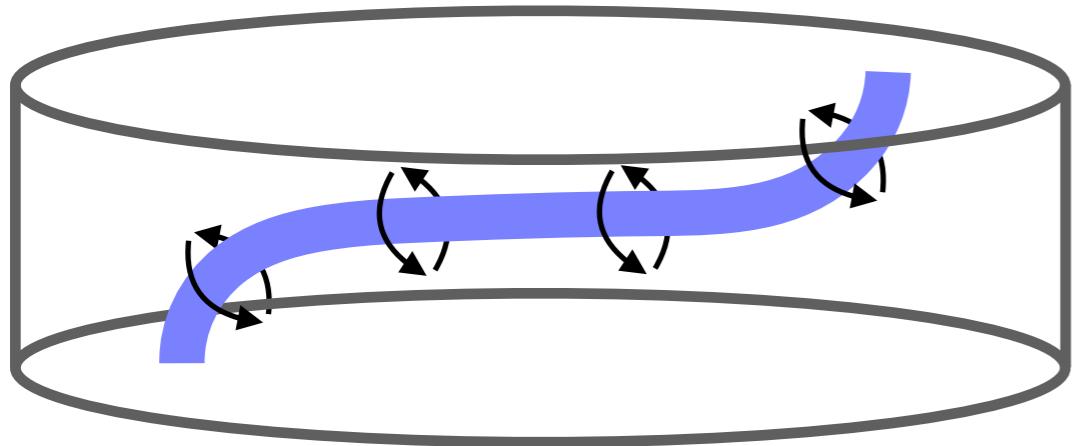
$R = 2\mu\text{m}$   
 $h = 500\text{nm}$



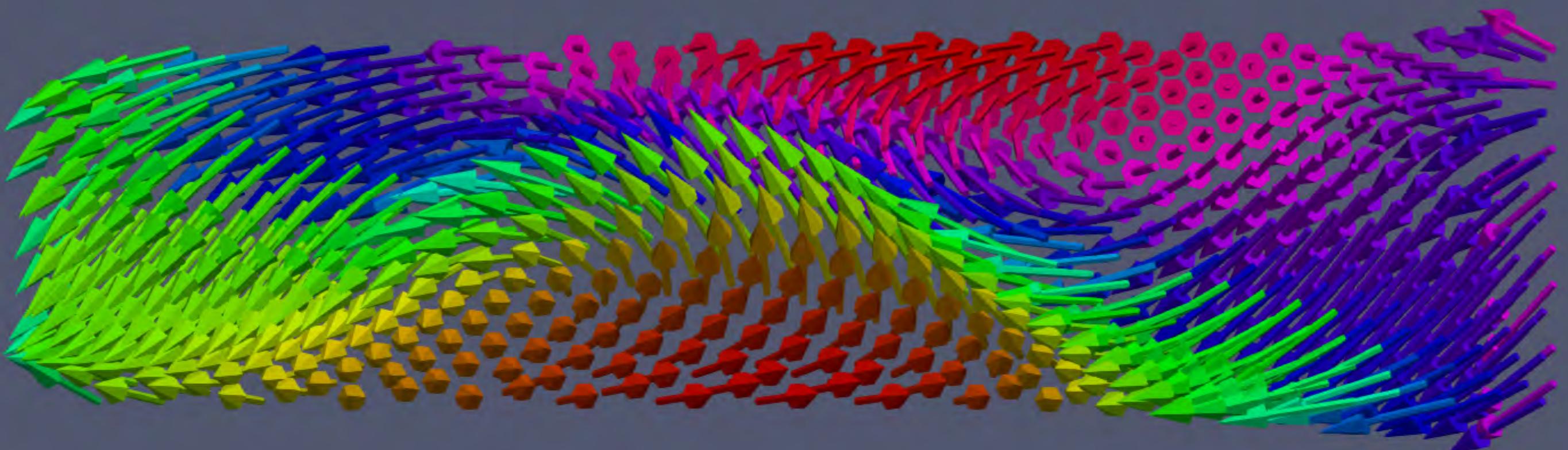
Simple picture of the vortex breaks down:  
Non-trivial z dependence

# Full YIG microdisk

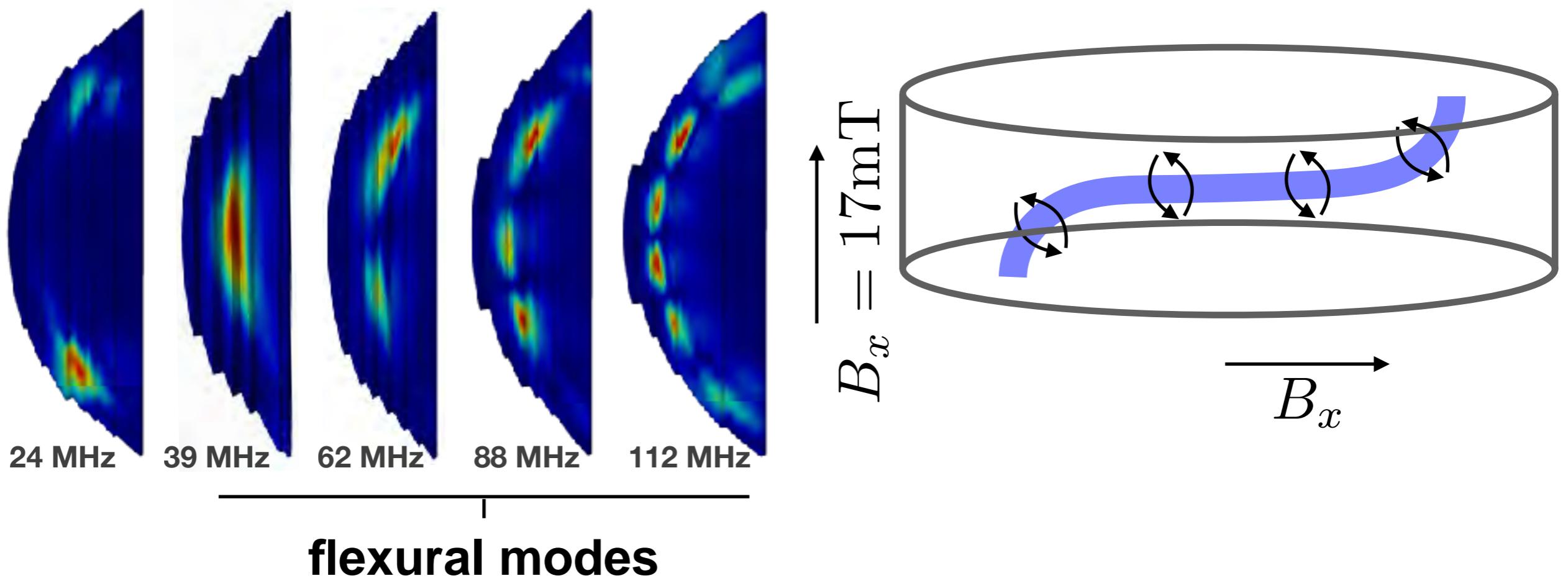
Vortex



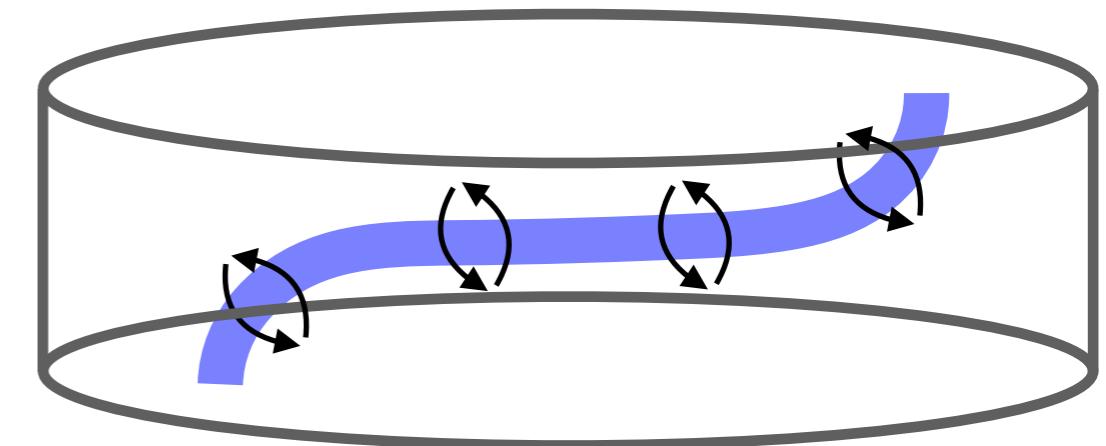
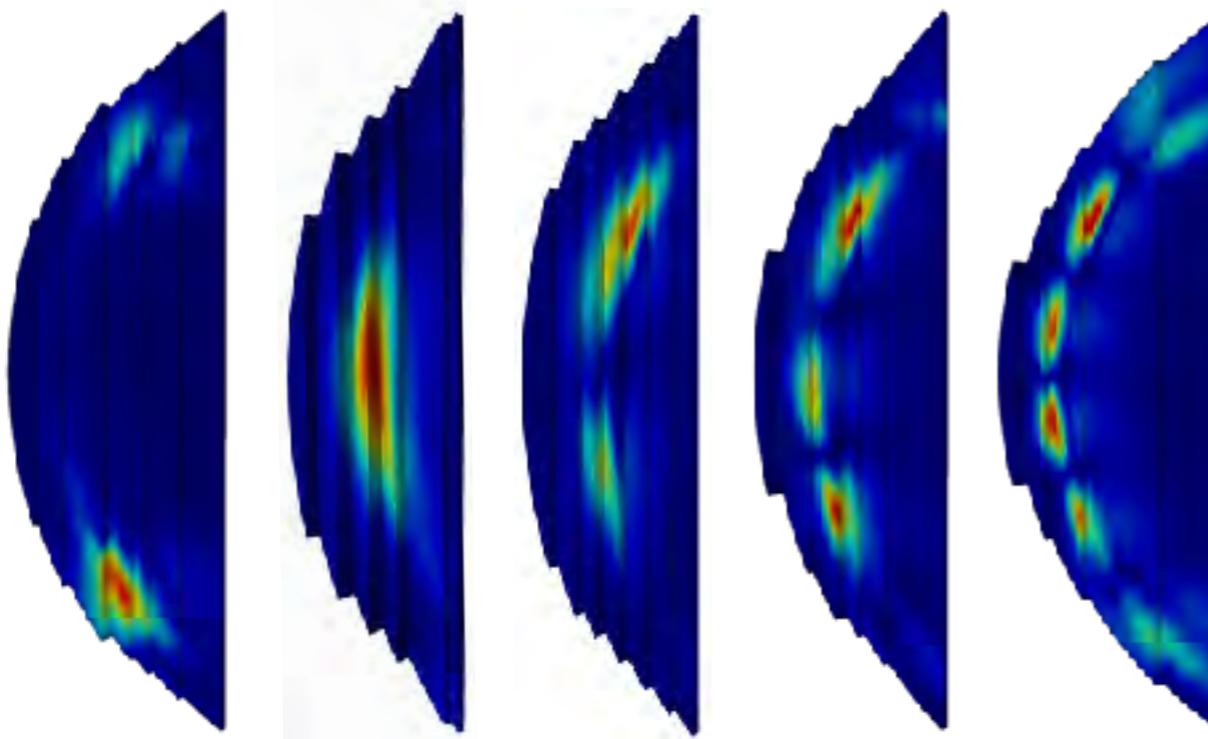
Definitely not 2D!!



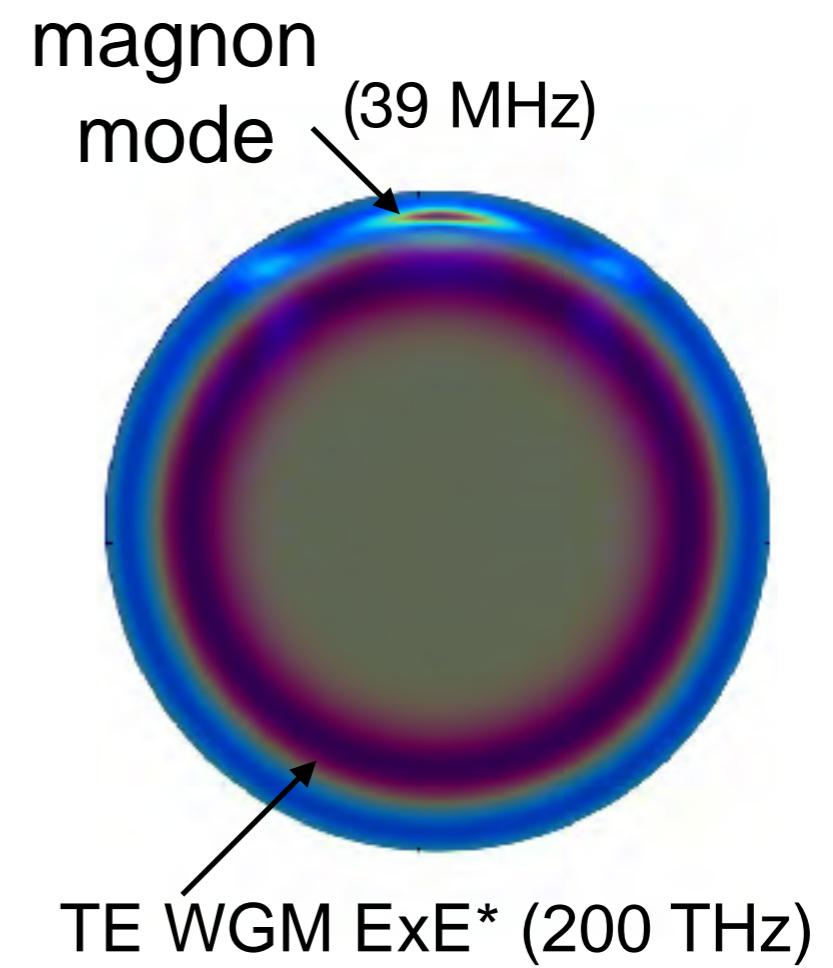
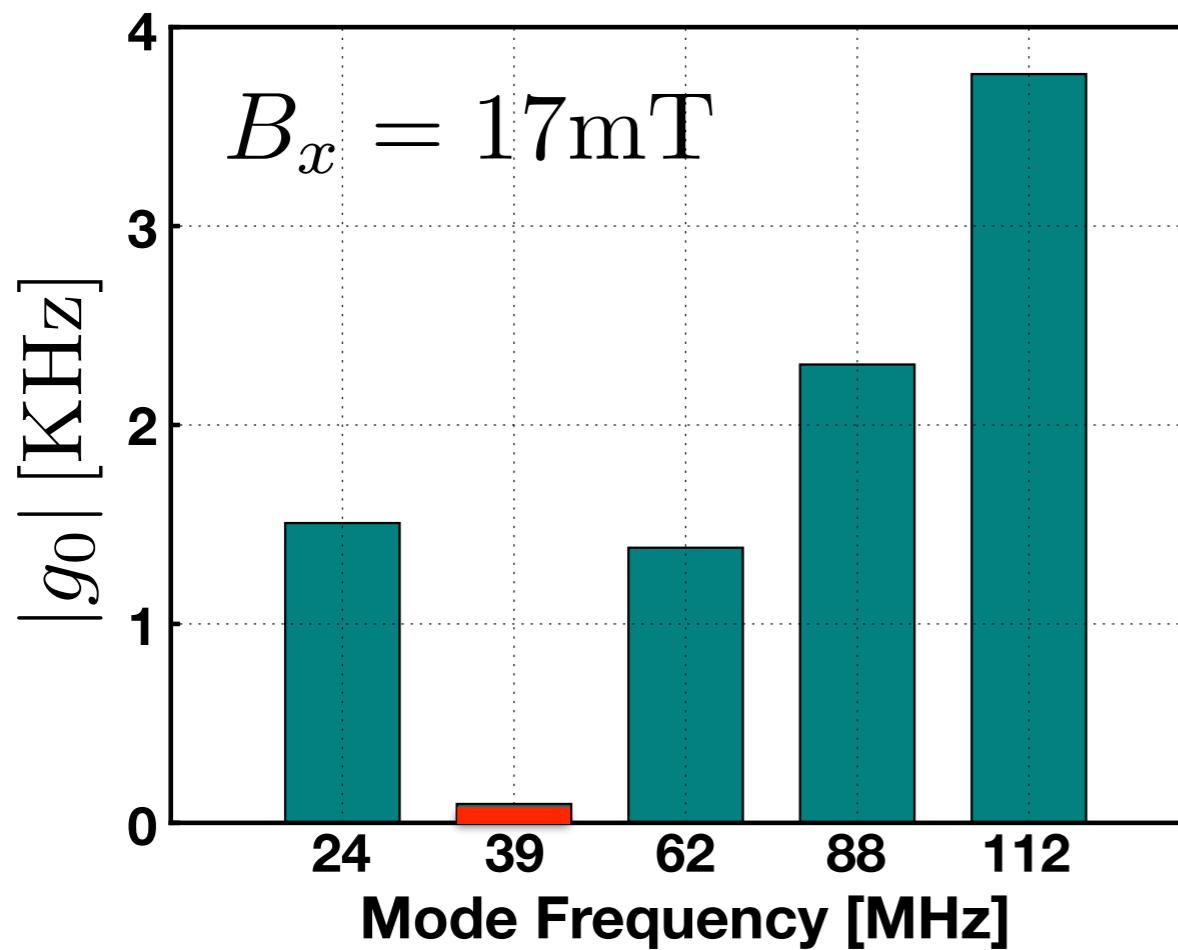
# Full YIG microdisk



# Full YIG microdisk

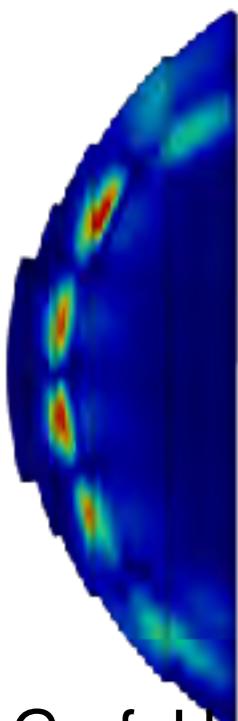
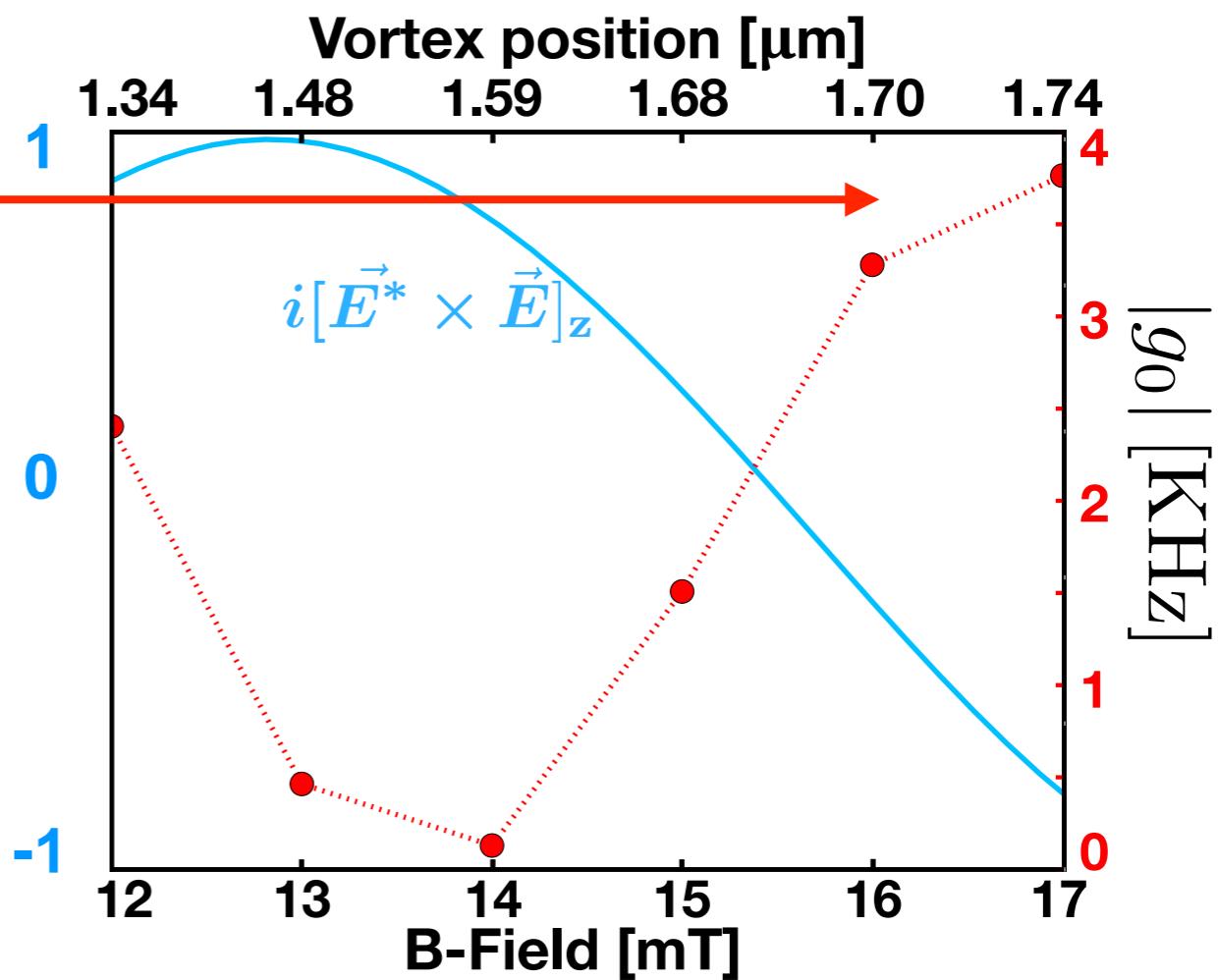
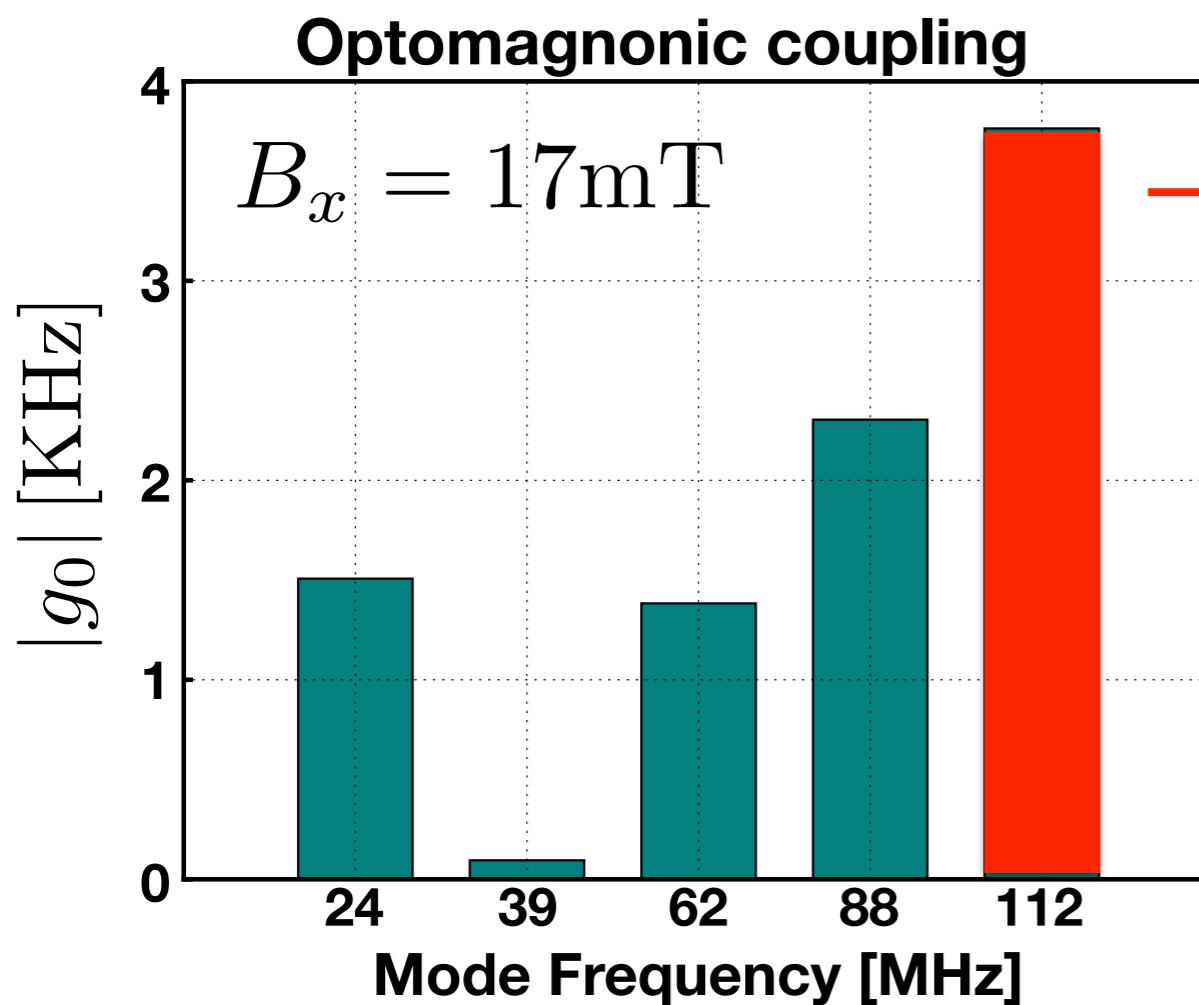


Optomagnonic coupling

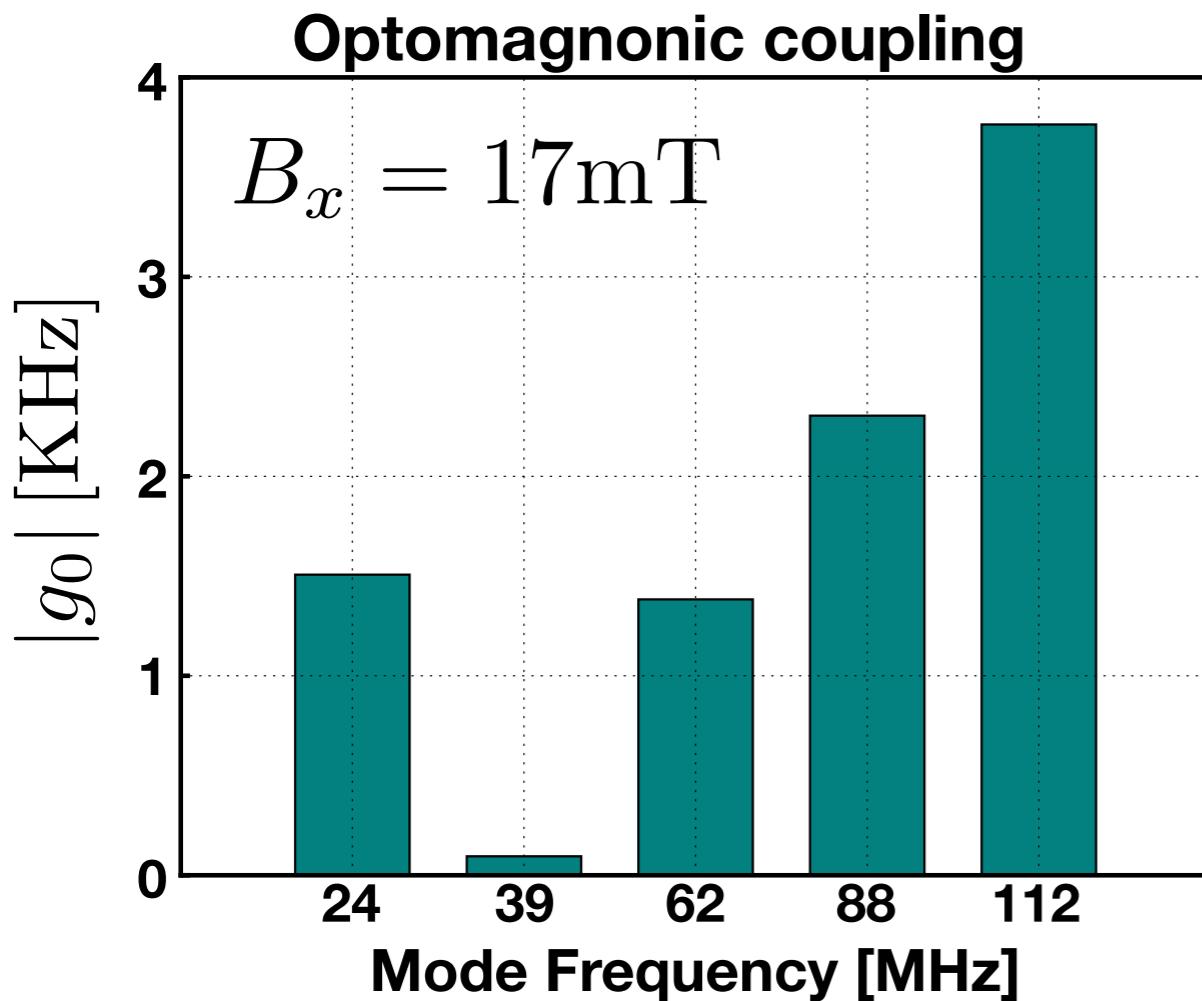


magnon mode (39 MHz)

# Full YIG microdisk



# Full YIG microdisk



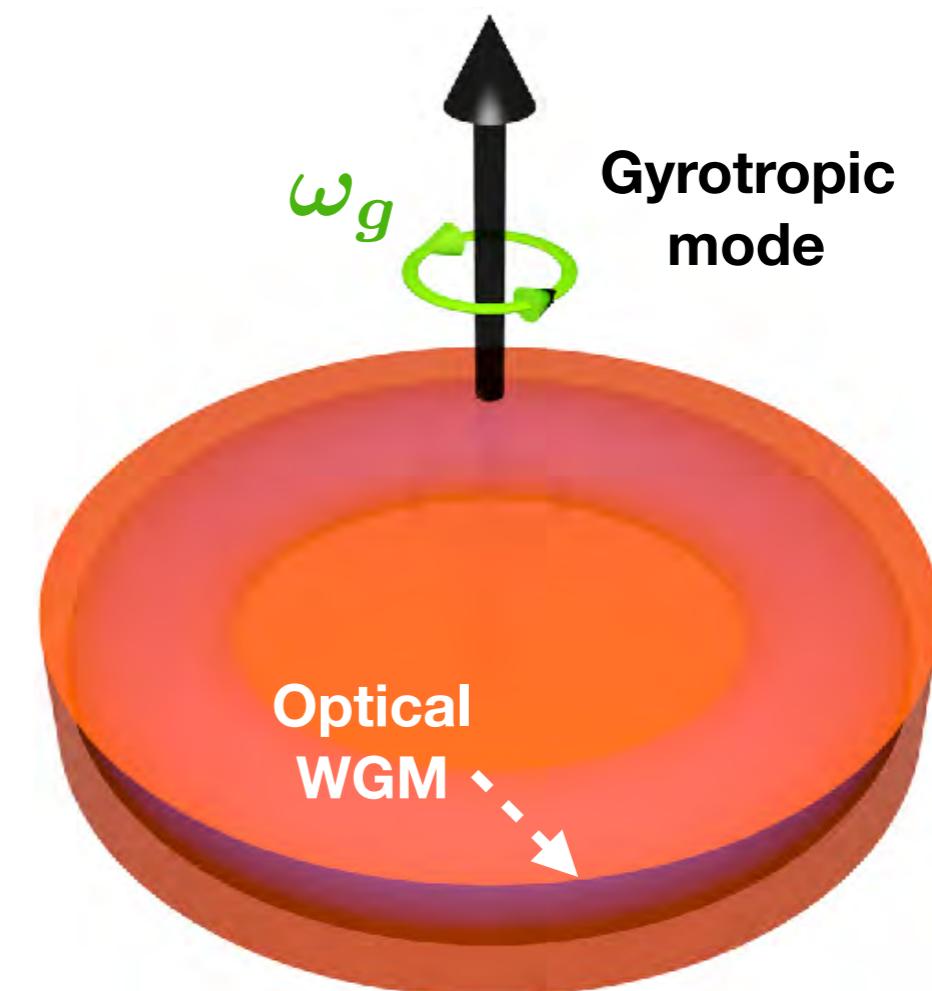
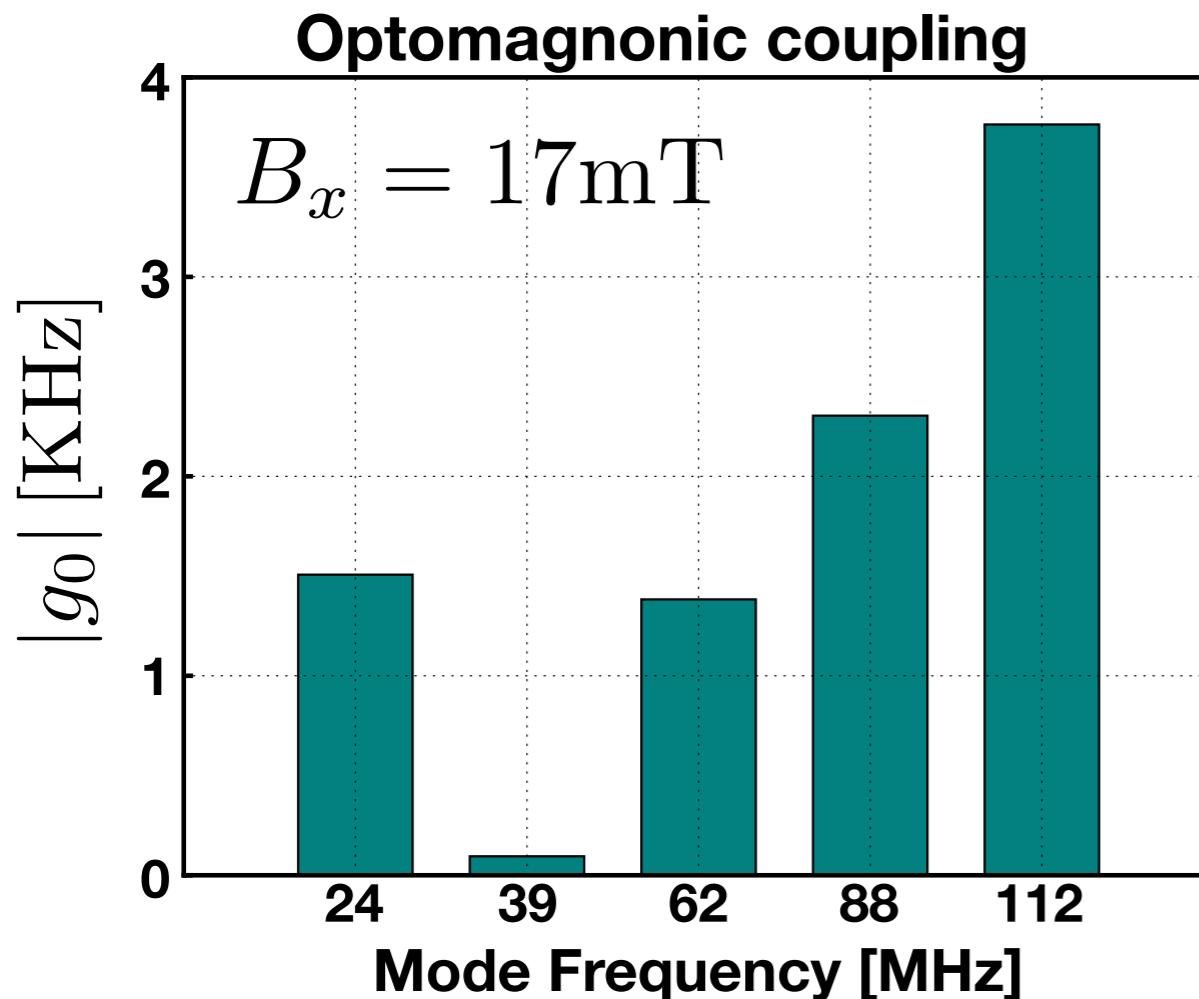
Single photon  
Cooperativity:

$$\mathcal{C}_0 = 4 \frac{g_0^2}{\Gamma \kappa} \approx 10^{-7}$$

Cooperativity at  
maximum photon  
density:

$$\mathcal{C} = 4n_{\text{ph}} \frac{g_0^2}{\Gamma \kappa} \approx 10^{-2}$$

# Full YIG microdisk



- Promising values for coupling - other modes?
- Tuneable coupling by an external magnetic field
- Coupled dynamics of the system?



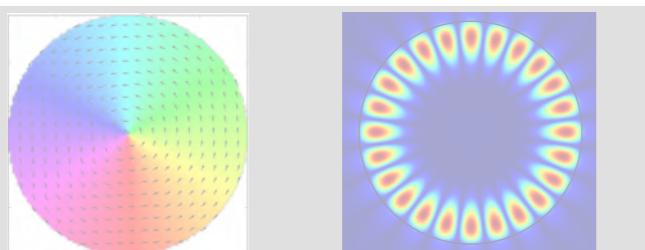
## Introduction and motivation



## Optomagnetic Hamiltonian



## Optically induced spin dynamics



## Magnetic textures: vortex in a disk

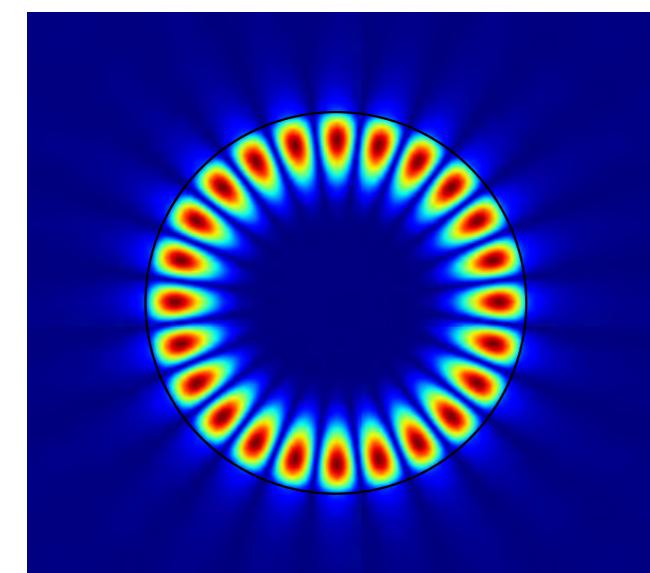
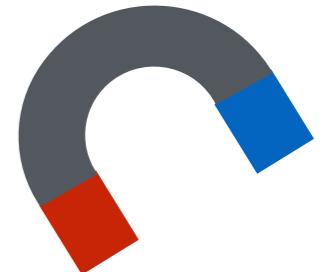


## Summary

# Summary



- Light-induced nonlinear spin dynamics (Kittel mode)
- First time optomagnonics with magnetic textures
- Coupling to magnetic vortex modes
- Promising values of coupling by engineering



MAX PLANCK INSTITUTE  
for the science of light

