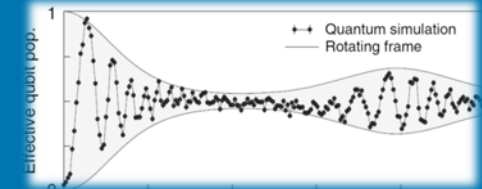
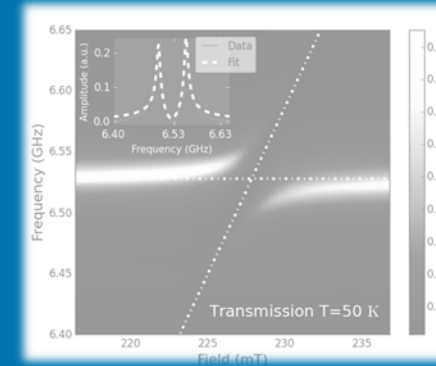


Electro-magnetic and -magnonic cooperativity



May 17th 2018

Martin P. Weides

University of Glasgow, UK

Karlsruhe Institute of Technology (KIT), Germany

Till 2017: Johannes Gutenberg University Mainz (JGU), Germany



1. Analog quantum simulation of ultrastrong coupling

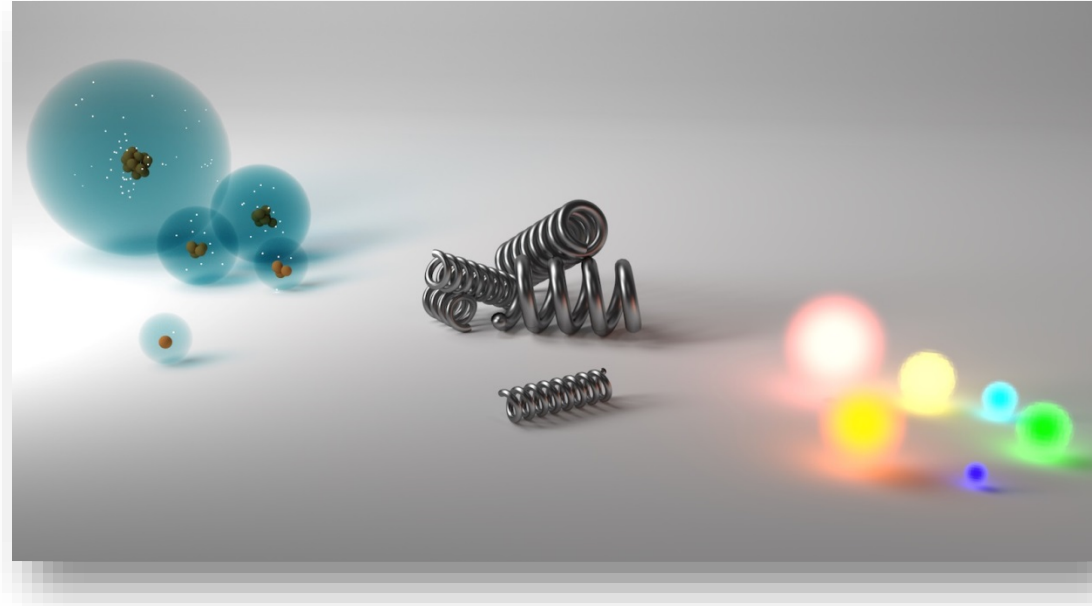
2. Spectroscopic data on YIG

- From RT to mK
- mK data
- Thin film YIG

3. Synchronizing magnons with photons

- Avoided level crossing and linewidth

Quantum Rabi model



QUTIS Solano

- description of fundamental light-matter interaction

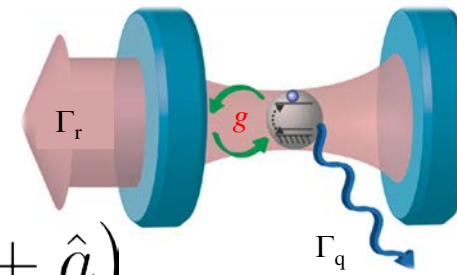
$$\frac{\hat{H}}{\hbar} = \omega_r \hat{a}^\dagger \hat{a} + \frac{\omega_q}{2} \hat{\sigma}_z + g (\hat{\sigma}^+ + \hat{\sigma}^-) (\hat{a}^\dagger + \hat{a})$$

- Ultra/ deep strong coupling regime: $g \approx \omega_r, \omega_q$

Rabi PR **49** (1936); Rabi PR **51** (1937)

WMI 2010, Delft 2016, Waterloo 2017, Tokyo 2017...

Rabi model and coupling regimes



Fundamental light-matter interaction (Rabi)

$$\hat{H}/\hbar = \omega_r \hat{a}^\dagger \hat{a} + \frac{\omega_q}{2} \hat{\sigma}_z + g (\hat{\sigma}^+ + \hat{\sigma}^-) (\hat{a}^\dagger + \hat{a})$$

Creation (annihilation) operator for field mode \hat{a}^\dagger, \hat{a}

Qubit operators $\hat{\sigma}_z |\pm\rangle = \pm |\pm\rangle, \hat{\sigma}^\pm |\pm\rangle = |\mp\rangle, \hat{\sigma}_x = \hat{\sigma}^+ + \hat{\sigma}^-, \hat{\sigma}_y = -i(\hat{\sigma}^+ - \hat{\sigma}^-)$

Coupling strength

- Weak $g \ll \Gamma_r, \Gamma_q, \omega_r, \omega_q$
- Strong $\Gamma_r, \Gamma_q \ll g \ll \omega_r, \omega_q$
- Ultra-strong $\Gamma_r, \Gamma_q, \omega_r/10, \omega_q/10 < g$
- Deep-strong $\Gamma_r, \Gamma_q, \omega_r, \omega_q < g$

Experimental access complexity

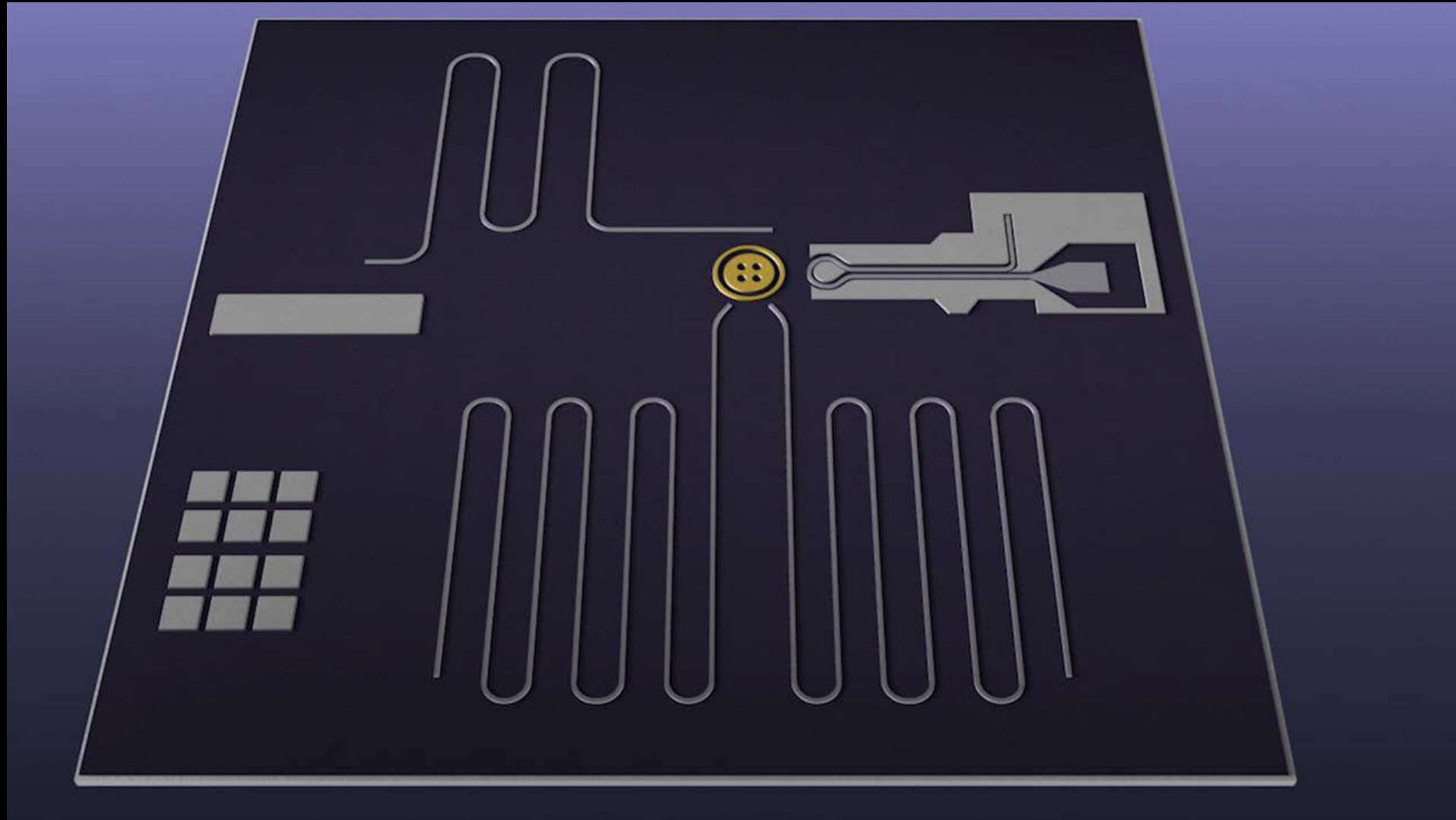
not exactly solvable
(needs 2nd conserved quantity besides energy)

For small coupling ($g \ll \omega_r, \omega_q$) interactions

$$\underbrace{\hat{\sigma}^+ \hat{a}^\dagger, \hat{\sigma}^- \hat{a}}_{\omega_r + \omega_q}, \underbrace{\hat{\sigma}^+ \hat{a}, \hat{\sigma}^- \hat{a}^\dagger}_{|\omega_r - \omega_q|}$$

→ Jaynes-Cummings
$$\hat{H}/\hbar = \omega_r \hat{a}^\dagger \hat{a} + \frac{\omega_q}{2} \hat{\sigma}_z + g (\hat{a}^\dagger \hat{\sigma}^- + \hat{a} \hat{\sigma}^+)$$

From small to ultra / deep - strong coupling



$$|\Psi(t)\rangle = \alpha|R_g g\rangle + \beta|R_e e\rangle$$

Analog quantum simulation of ultra-strong coupling

$$\hat{H}/\hbar = \omega_r \hat{a}^\dagger \hat{a} + \frac{\omega_q}{2} \hat{\sigma}_z + g (\hat{a}^\dagger \hat{\sigma}^- + \hat{a} \hat{\sigma}^+) + \hat{\sigma}_x (\eta_1 \cos \omega_1 t + \eta_2 \cos \omega_2 t)$$

Add two microwave drives

In reference frame rotating with ω_1

$$\hat{H}/\hbar = (\omega_r - \omega_1) \hat{a}^\dagger \hat{a} + \frac{\omega_q - \omega_1}{2} \hat{\sigma}_z + g (\hat{a}^\dagger \hat{\sigma}^- + \hat{a} \hat{\sigma}^+) + \frac{\eta_1}{2} \hat{\sigma}_x + \frac{\eta_2}{2} (\hat{\sigma}^+ e^{i(\omega_1 - \omega_2)t} + \hat{\sigma}^- e^{-i(\omega_1 - \omega_2)t})$$

- interaction picture in $\frac{\eta_1}{2} \hat{\sigma}_x$
- basis change via Hadamard transformation
- constraints: $\omega_1 - \omega_2 = \eta_1$, $\omega_{eff} \equiv \omega_r - \omega_1 \approx \text{MHz}$

→ effective Hamiltonian (ultra-strong /deep-strong)

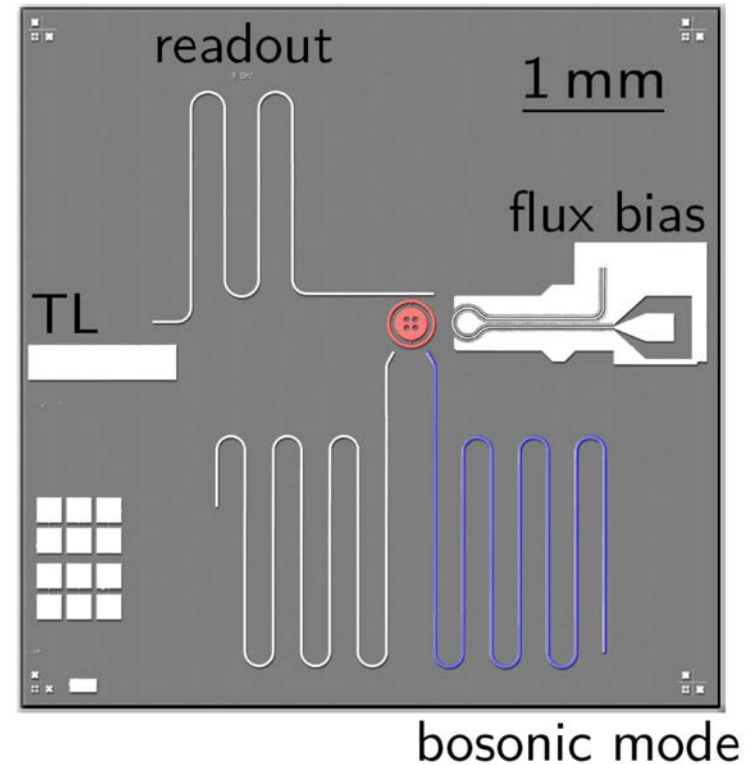
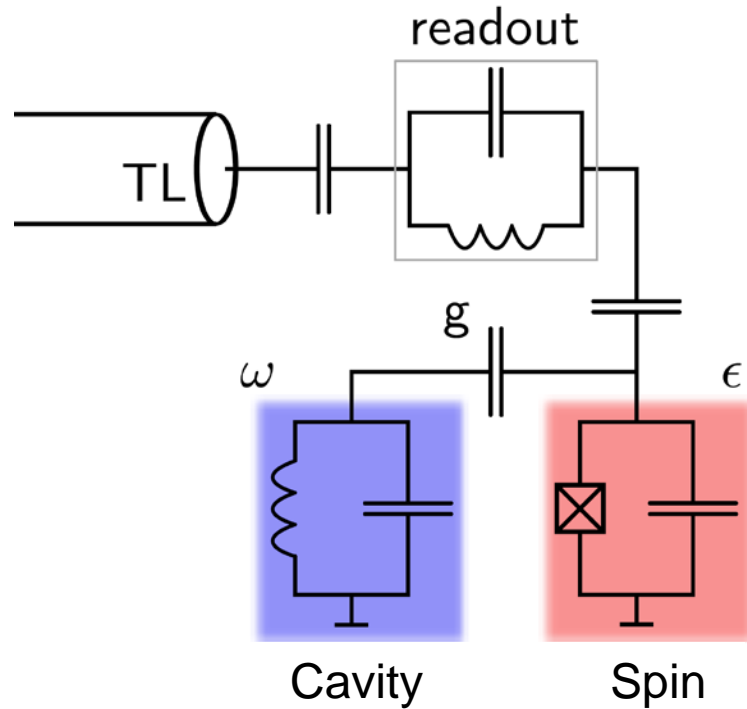
$$\hat{H}_{\text{eff}}/\hbar = \underbrace{\omega_{\text{eff}}}_{\sim \text{MHz}} \hat{a}^\dagger \hat{a} + \underbrace{\frac{\eta_2}{2}}_{\sim \text{MHz}} \frac{\hat{\sigma}_z}{2} + \underbrace{\frac{g}{2}}_{2.5 \text{ MHz}} (\hat{\sigma}^+ + \hat{\sigma}^-) (\hat{a}^\dagger + \hat{a})$$

Ballester PRX 2 (2012)

Ultra-strong coupling in rotating frame!

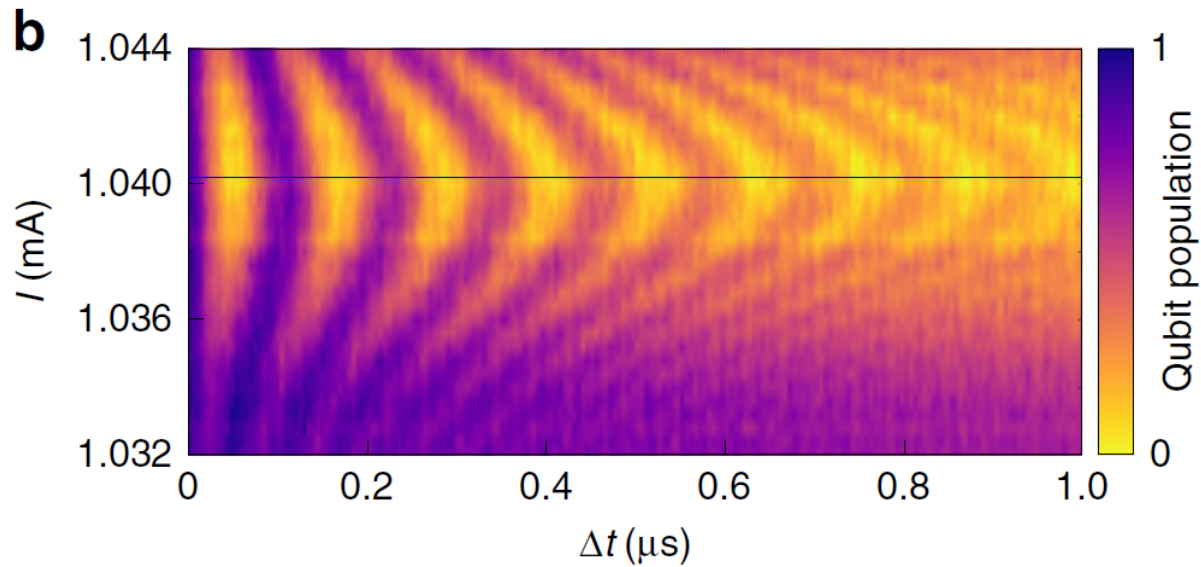
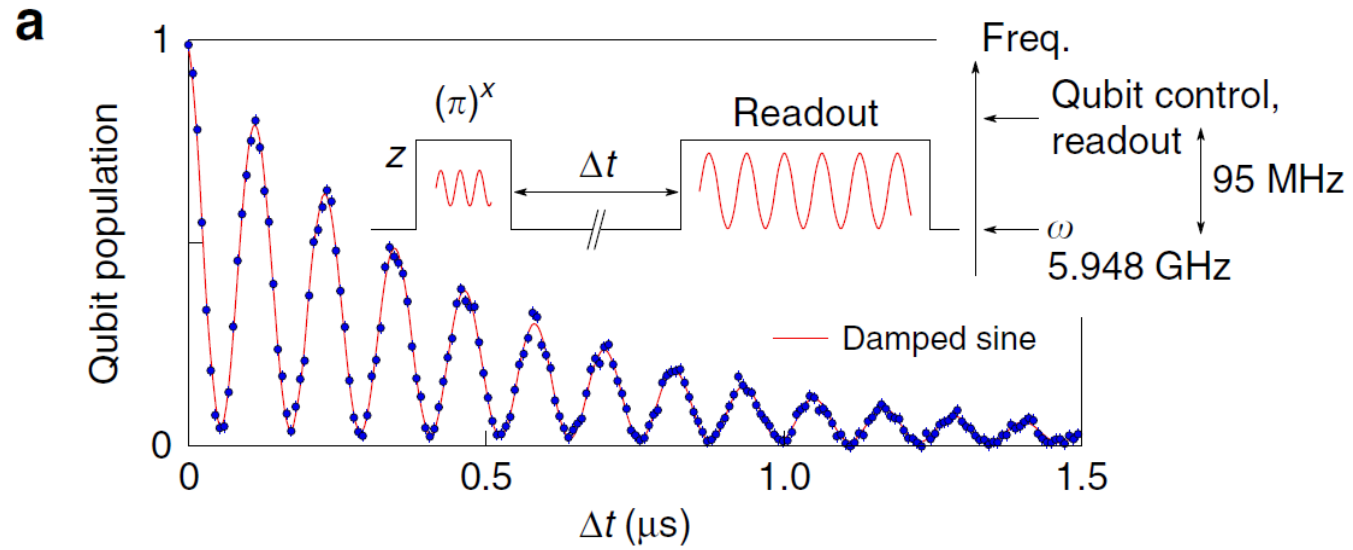
$$\hat{H}_{\text{eff}}/\hbar = \underbrace{\omega_{\text{eff}} \hat{a}^\dagger \hat{a}}_{\sim \text{MHz}} + \underbrace{\frac{\eta_2}{2} \frac{\hat{\sigma}_z}{2}}_{\sim \text{MHz}} + \frac{g}{2} (\hat{\sigma}^+ + \hat{\sigma}^-) (\hat{a}^\dagger + \hat{a})$$

~ MHz
~ MHz
2.5 MHz



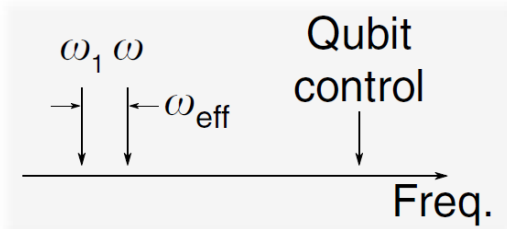
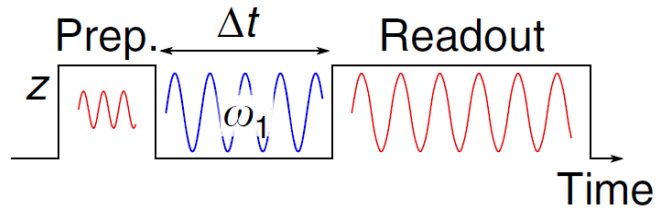
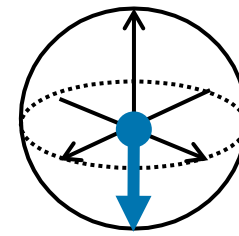
Braumüller *et al.* Nat. Commun. **8**, 779 (2017)

Vacuum Rabi oscillations between qubit and bosonic mode



$$g/2\pi \approx 5 \text{ MHz}$$

Quantum state collapse, idling and revival

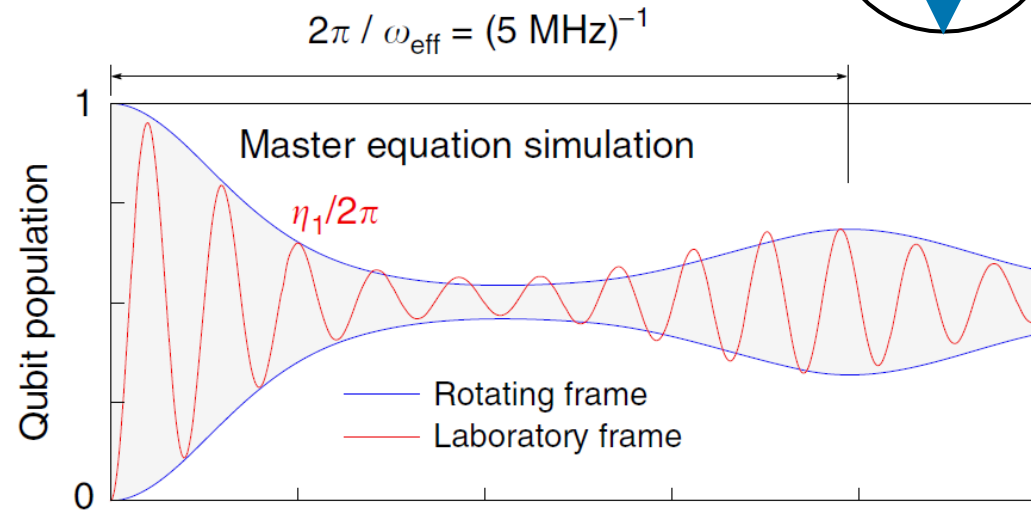


- Non-classical feature
- Hallmark of large coupling

Relative coupling ratio

$$\frac{g}{\omega_{\text{eff}}} \sim 0.6$$

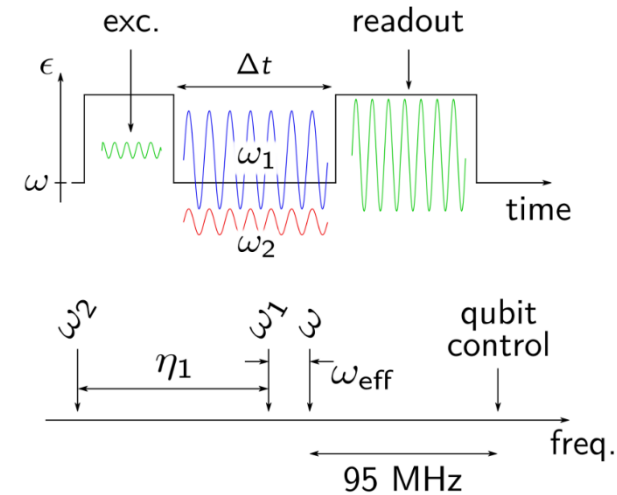
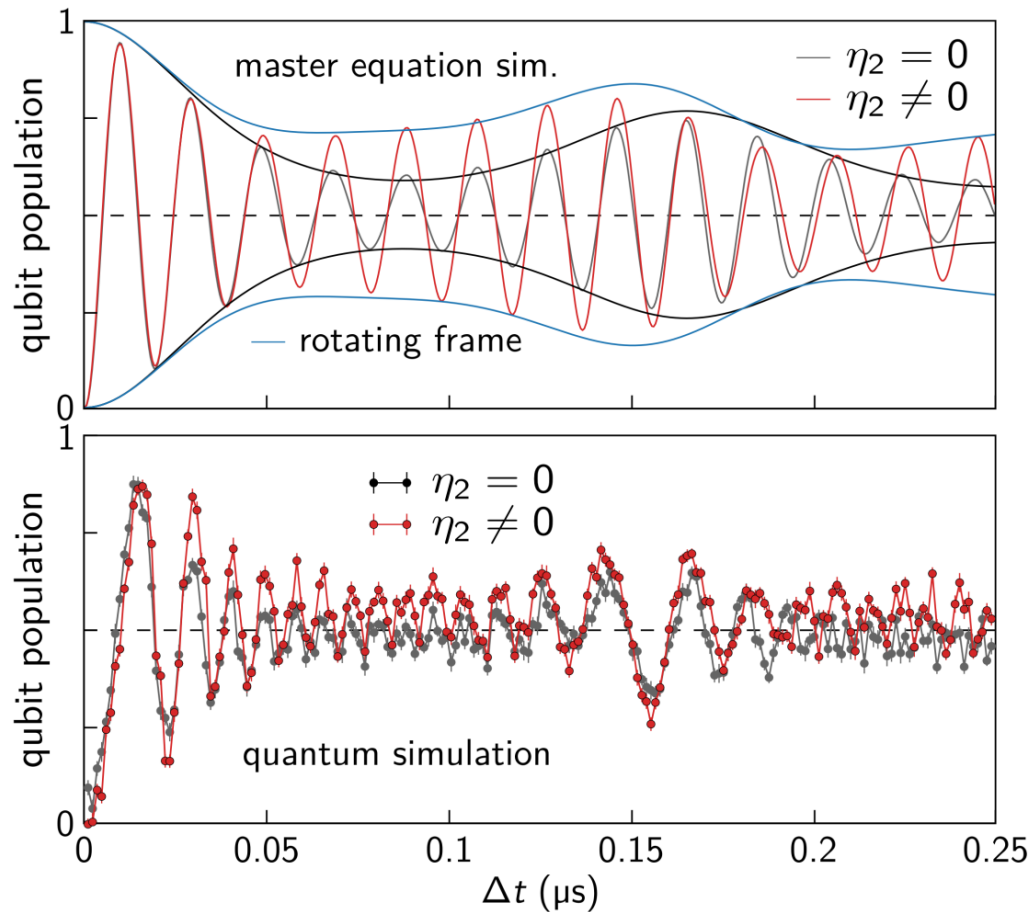
- Ultra-strong coupling



Braumüller *et al.* Nat. Commun. **8**, 779 (2017)

Extend to full quantum Rabi model (i.e. add qubit term)

$$\hat{H}_{\text{eff}}/\hbar = \underbrace{\omega_{\text{eff}} \hat{a}^\dagger \hat{a}}_{6 \text{ MHz}} + \underbrace{\frac{\eta_2}{2} \frac{\hat{\sigma}_z}{2}}_{3 \text{ MHz}} + \underbrace{\frac{g}{2} (\hat{\sigma}^+ + \hat{\sigma}^-)}_{2.5 \text{ MHz}} (\hat{a}^\dagger + \hat{a})$$



- ✓ Main structures captured
- Substructures not \rightarrow ring up dynamics break constrains

Braumüller *et al.* Nat. Commun. **8**, 779 (2017)

Agenda

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2. Spectroscopic data on YIG

- From RT to mK
- mK data
- Thin film YIG

3. Synchronizing magnons with photons

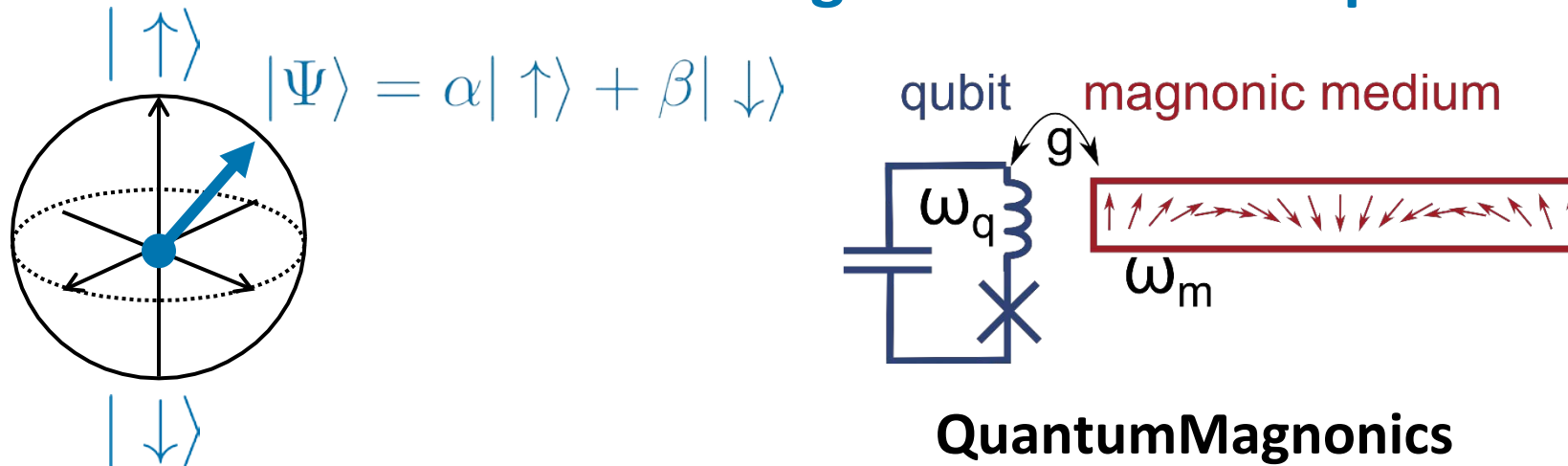
- Avoided level crossing and linewidth

Probing and manipulating single magnons?!

- Quantum ground state ($T=10$ mK)
- Single quanta spectroscopy, coherent coupling
- **How to achieve?**

$$\hbar\omega_m \gg k_B T$$

Extend magnon to artificial spin!



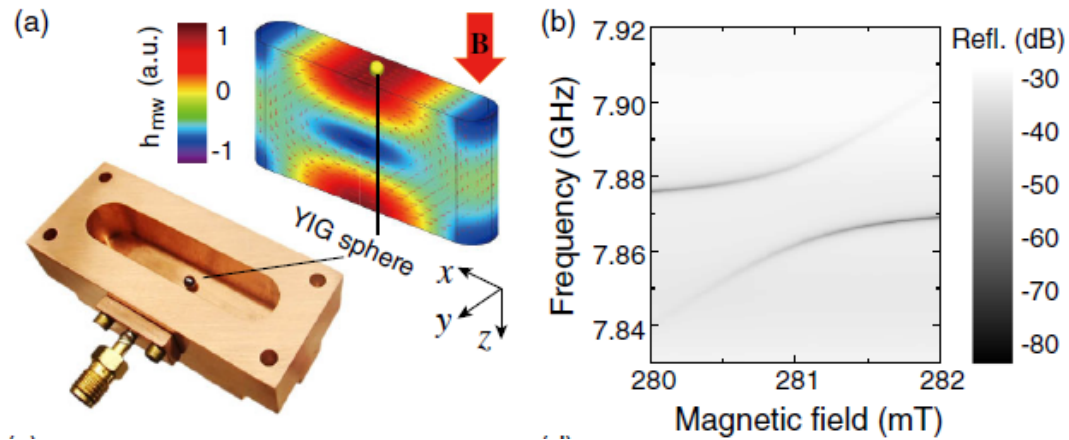
QuantumMagnonics

► Access magnon lifetime and coherence via coherent coupling

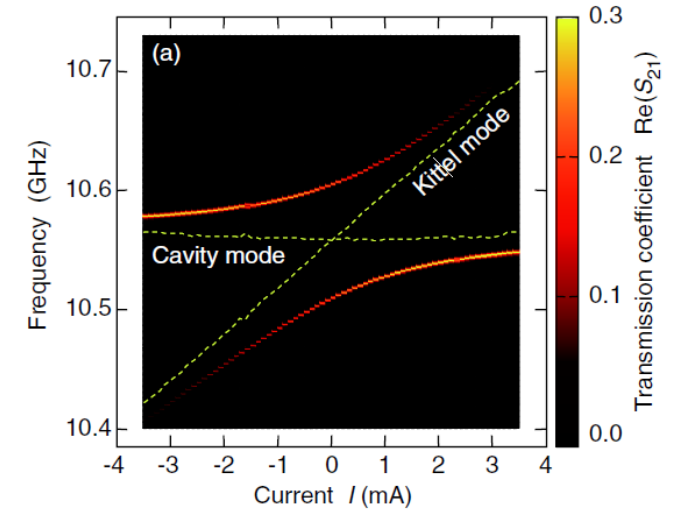
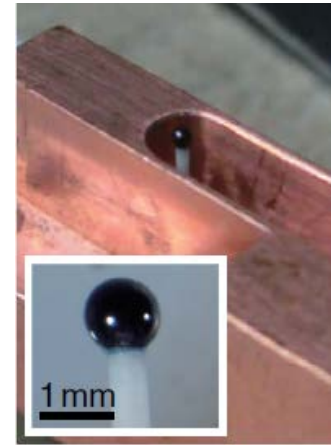
Single magnon creation and detection

Quantum-resolved broadband noise spectroscopy

From room temperature to milliKelvin



X. Zhang *et al.*, *Phys. Rev. Lett.* **113**, 156401 (2014)

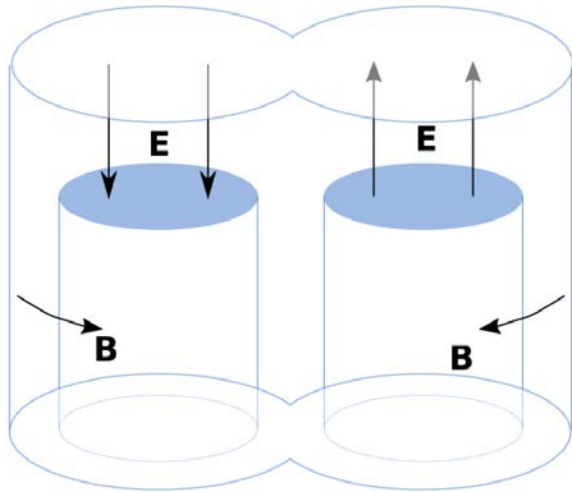


Y. Tabuchi *et al.*, *Phys. Rev. Lett.* **113**, 083603 (2014)

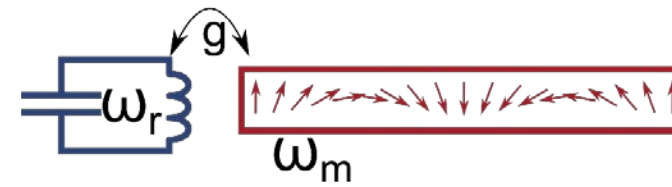
Temperature dependence of hybridized cavity magnon system?

Study from 290 K down to 10mK

3d split ring resonator



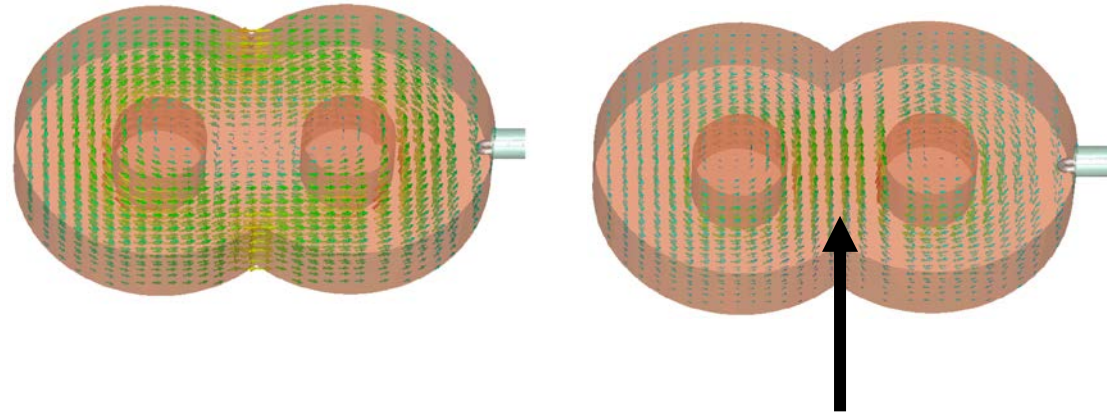
resonator magnonic medium



Magnetic field distribution

Parallel

Antiparallel



Magnetic sphere (YIG)
placed in center

Reentrant cavity: M. Goryachev *et al.*, *Phys. Rev. Appl.*, **2**, 054002 (2014)

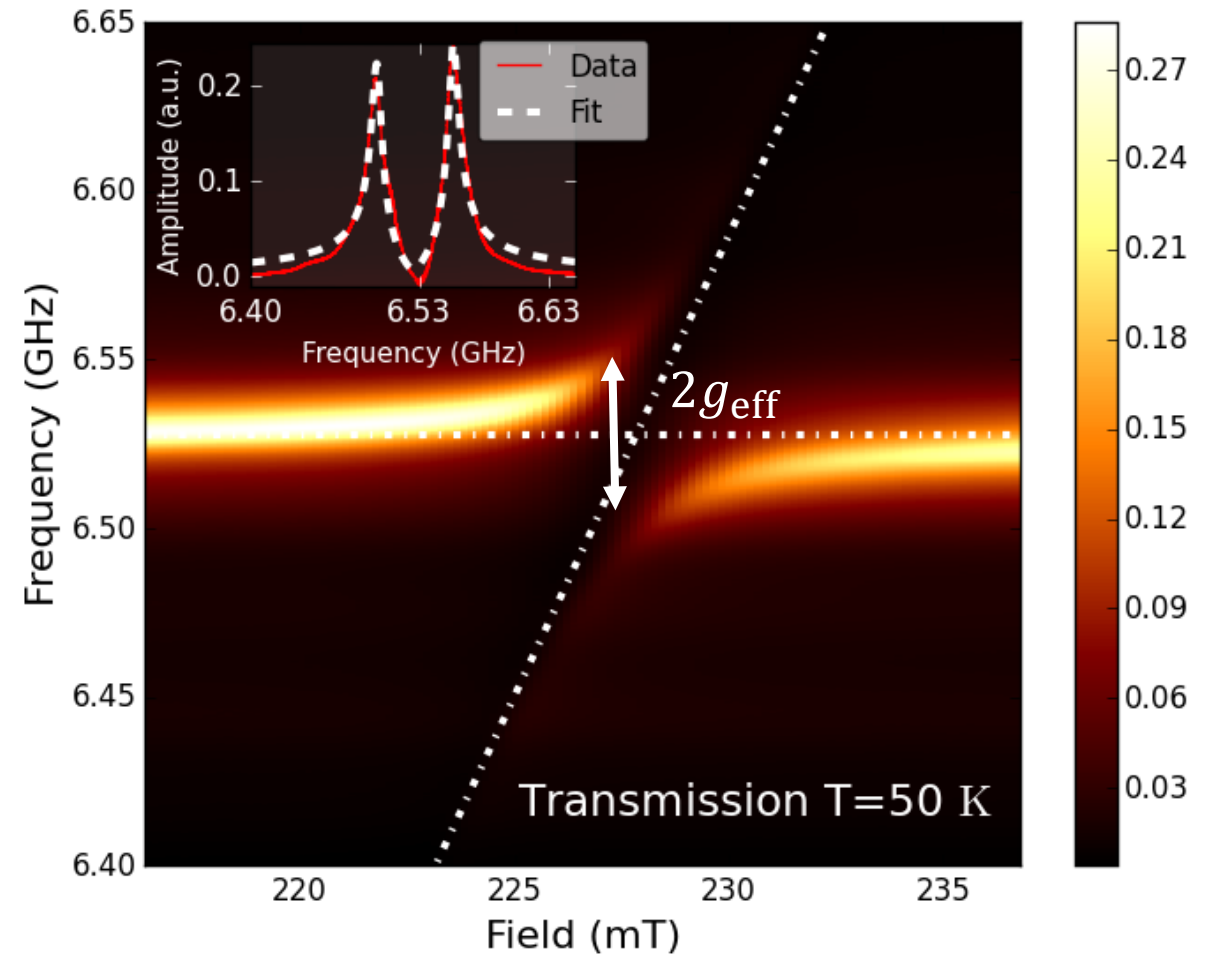
Avoided crossing: Spectrum

Consider coupling to Kittel mode only

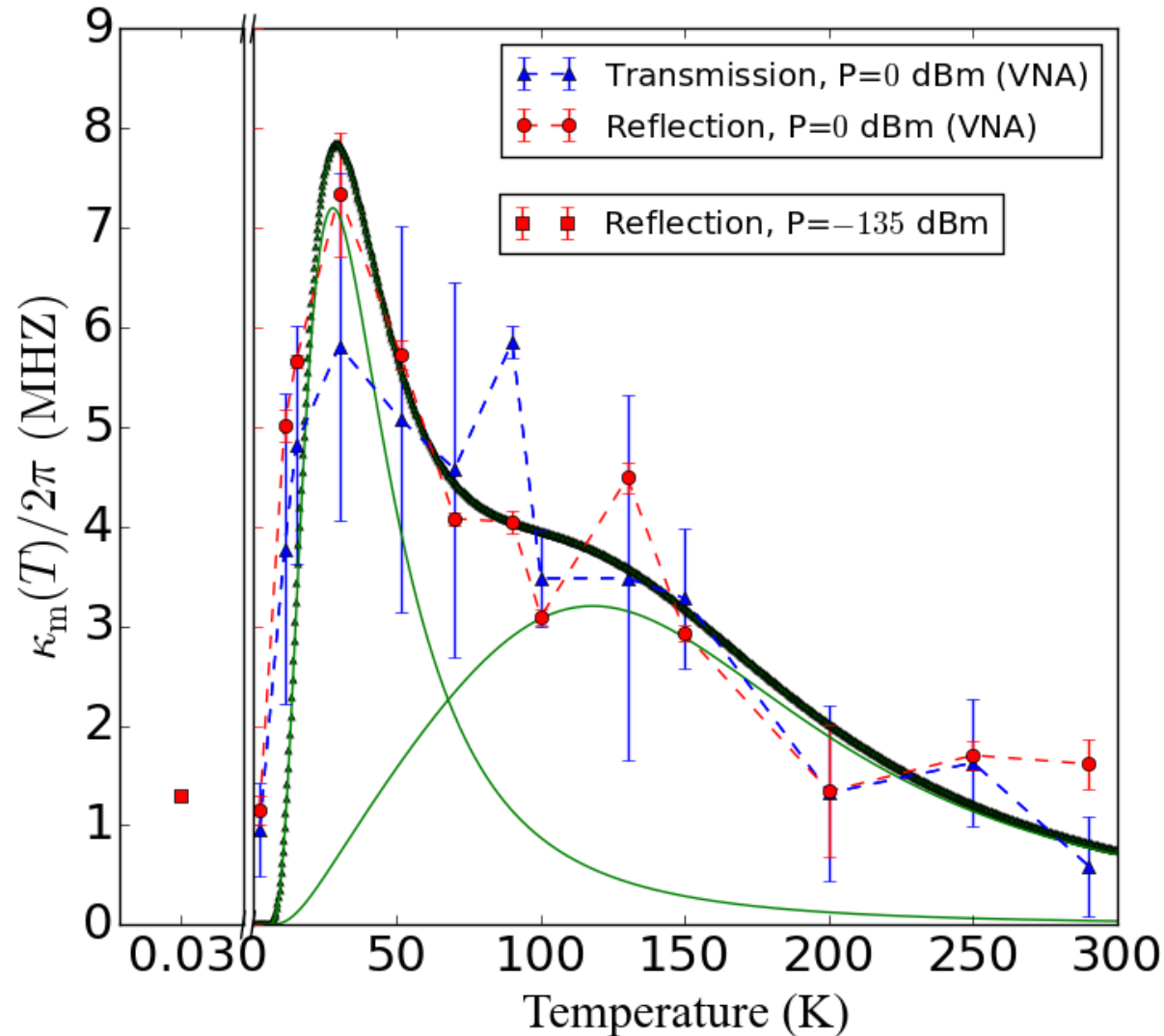
- **Cavity:** field independent
- **YIG:** field dependent

Sphere: $\omega_{\text{res}} = \gamma \mu_0 \overrightarrow{H_{\text{eff}}}$

- **At resonance:** $\omega_{\text{res}} = \omega_r = \omega_m$



Magnon linewidth $\kappa_m(T)$ (T)



Rare earth impurity scattering

- Dominant peak at 43 K
- ‚Broad shoulder‘ at 90 K
- Offset of ~ 1 MHz from intrinsic damping & surface scattering



Model well the temperature behaviour of our system

Boventer *et al.* Phys. Rev. B **97**, 184420

Approaching the quantum regime

- Excitation energy:

$$\hbar\omega \gg k_B T$$

$$T = 50 \text{ mK} \Leftrightarrow \omega/2\pi = 1 \text{ GHz}$$

- Excitation power:

$$\langle n \rangle \approx 1$$

- Non-linear system, anharmonic level structure

Coherent limitations and quantum applications?

Experimental setup

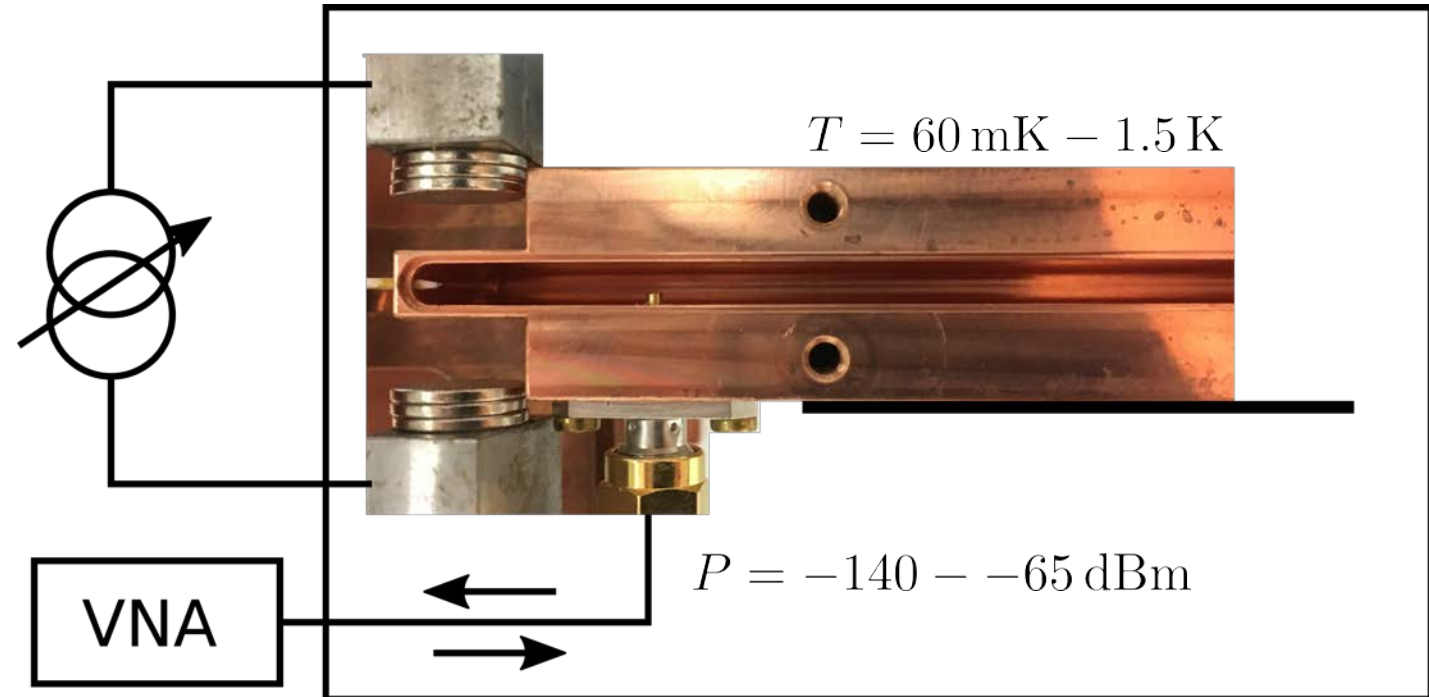
- Yttrium iron garnet ($\text{Y}_3\text{Fe}_5\text{O}_{12}$, YIG) sphere,

$$\varnothing = 0.5 \text{ mm}$$

- 3d copper cavity resonator

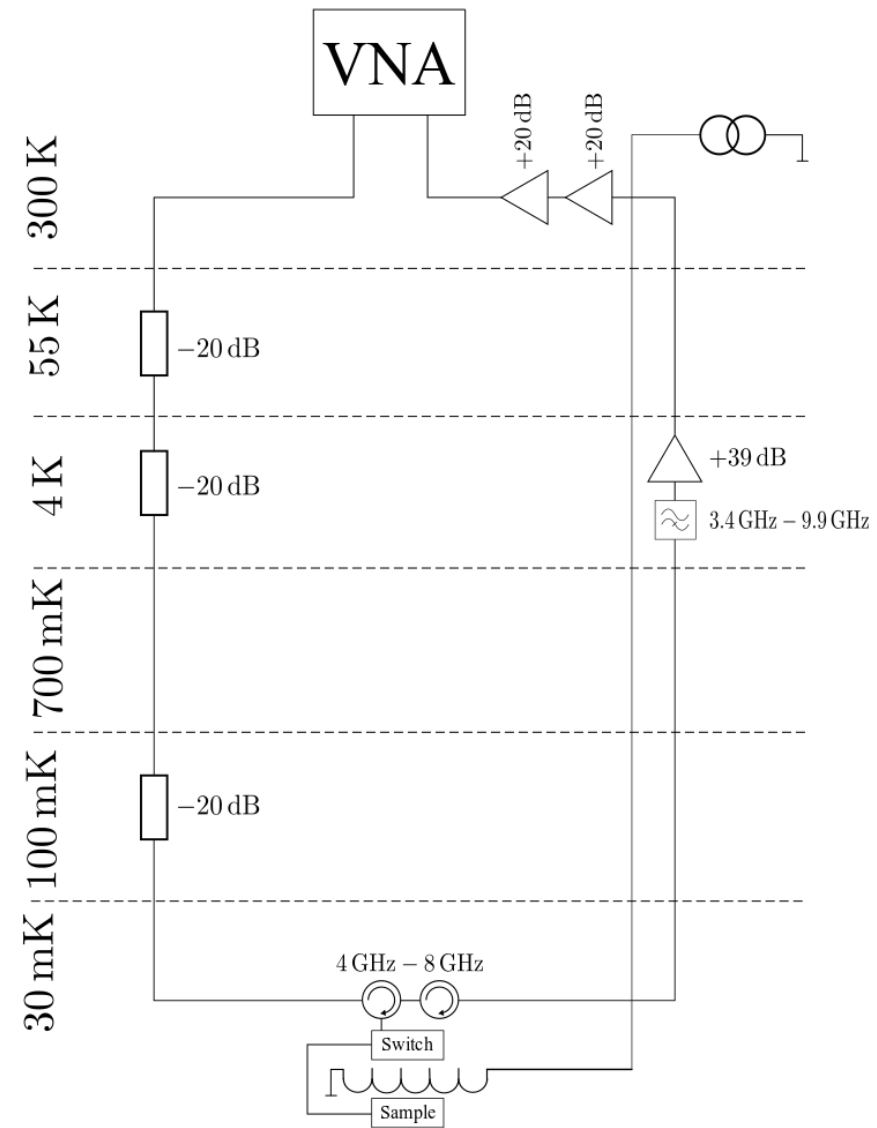
$$\omega_{\text{TE}_{102}}/2\pi = 5.24 \text{ GHz}$$

- Static magnetic field:
tune magnon frequency

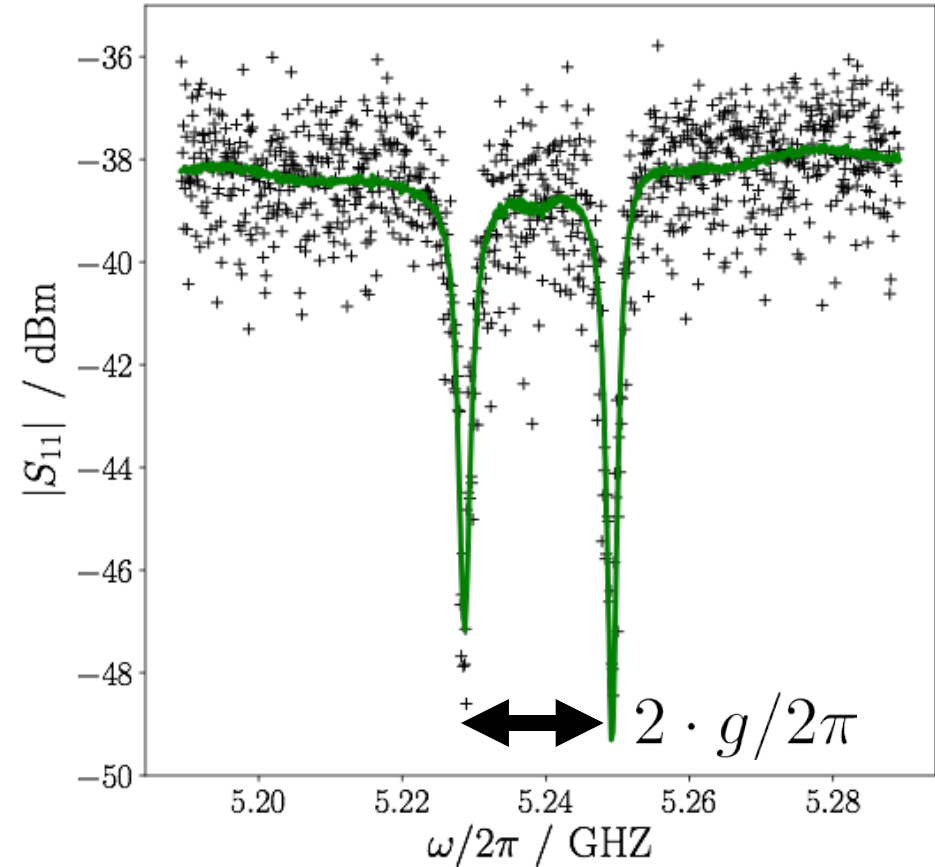
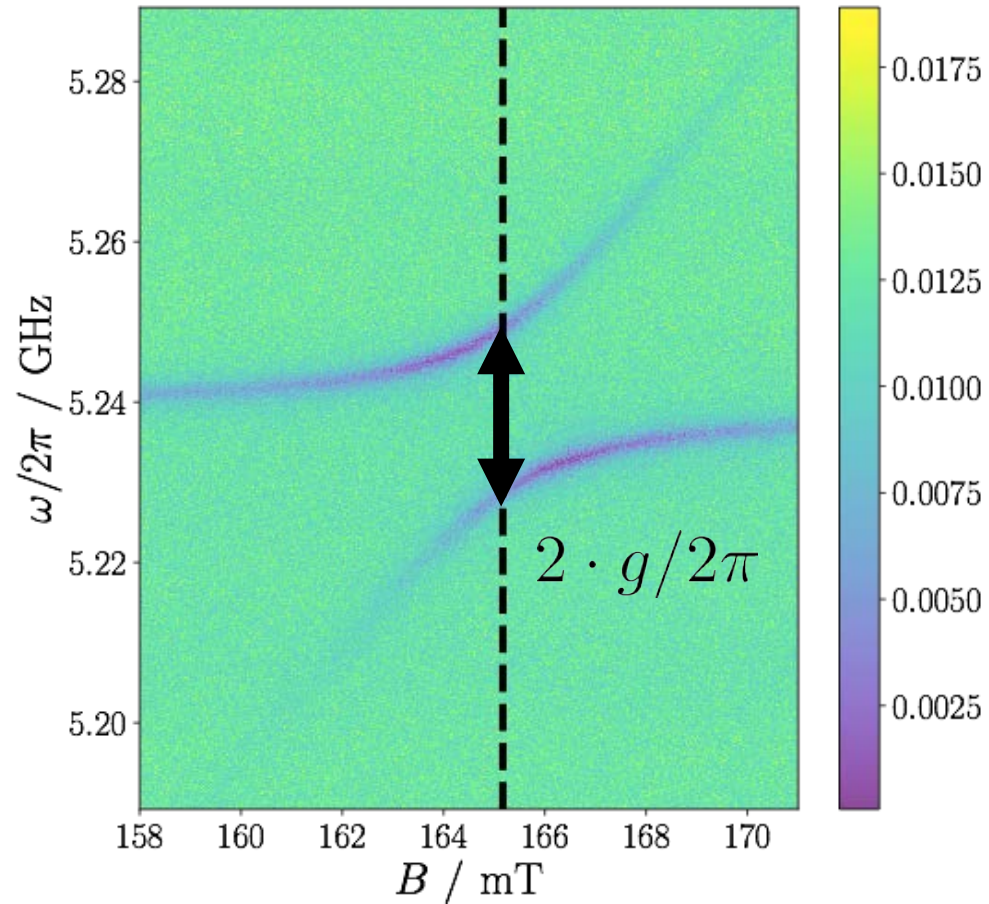


- $$S_{11}(\omega) = -1 + \frac{2\kappa_e}{i(\omega_r - \omega) + \kappa_l + \frac{g^2}{i(\omega_m - \omega) + \kappa_m}}$$

Cryogenic wiring

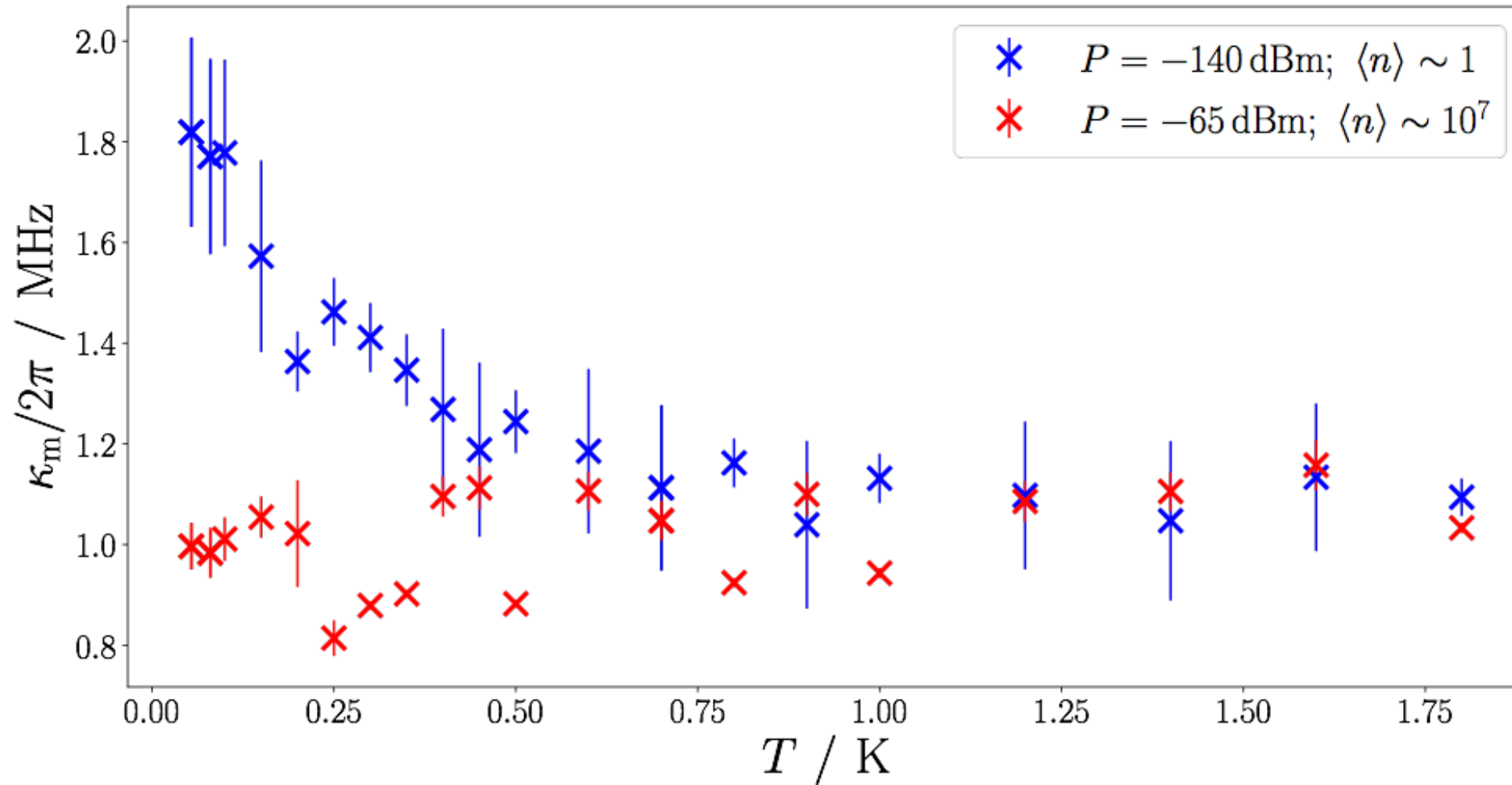


Spectroscopic measurement; 60 mK, -140 dBm

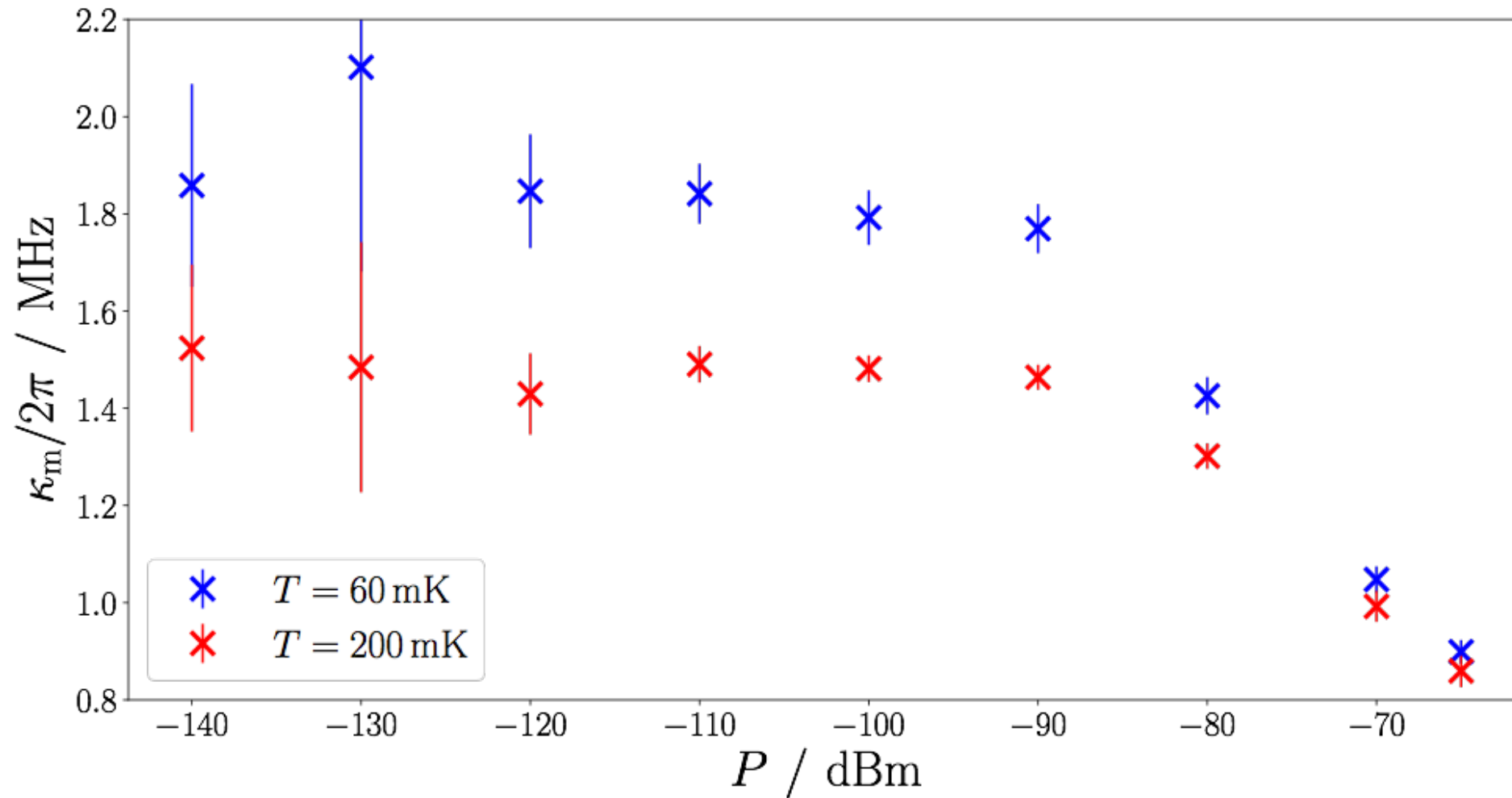


Magnon - photon coupling: $g/2\pi \approx 10.5 \text{ MHz}$

Magnon linewidth: temperature dependence



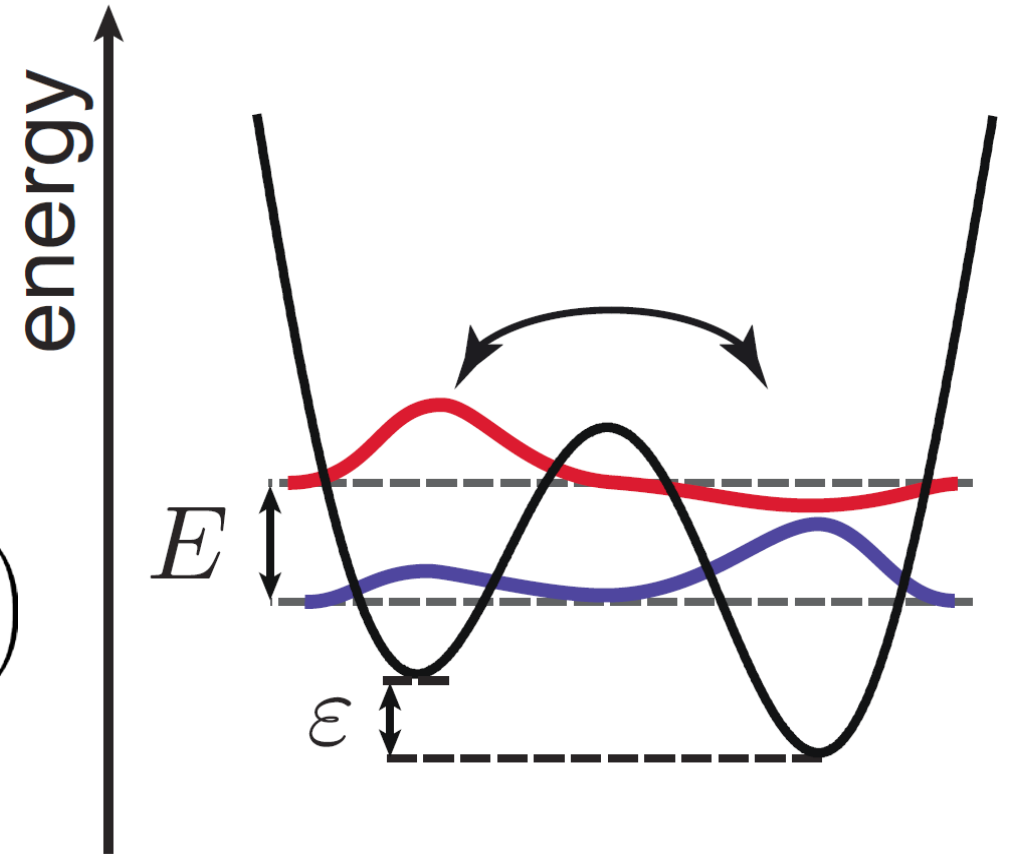
Magnon linewidth: power dependence



Two-Level system (TLS) model

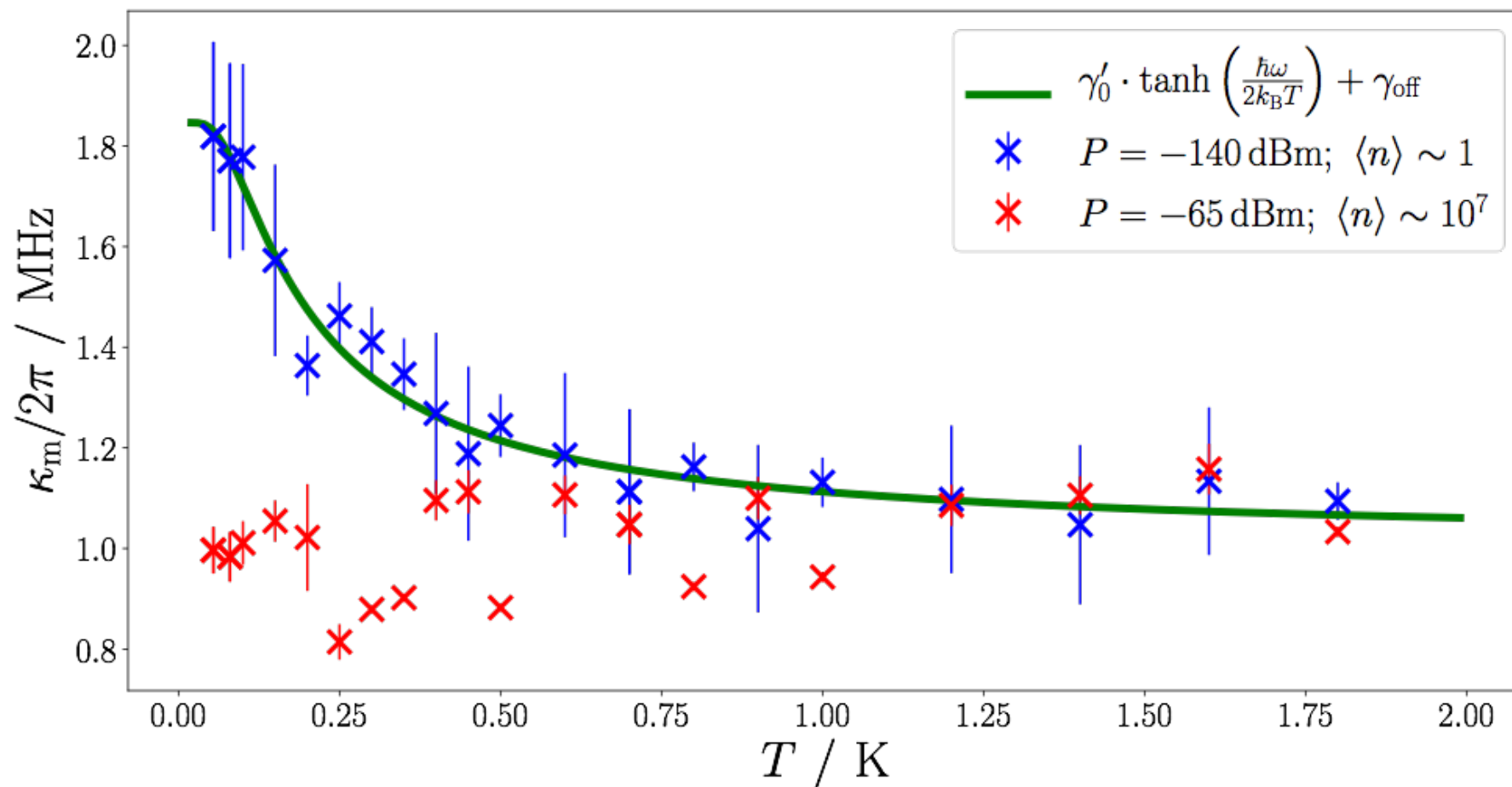
- Bistable energy level
- Loss of excitation

$$\gamma_{\text{TLS}} = \underbrace{\gamma_0 \cdot \frac{1}{\sqrt{1 + \frac{P_{\text{in}}}{P_c}}}}_{\gamma'_0} \cdot \tanh\left(\frac{\hbar\omega}{2k_B T}\right)$$



Y. Tabuchi *et al.*, *Phys. Rev. Lett.* **113**, 083603 (2014)

Magnon linewidth below 1.5 K

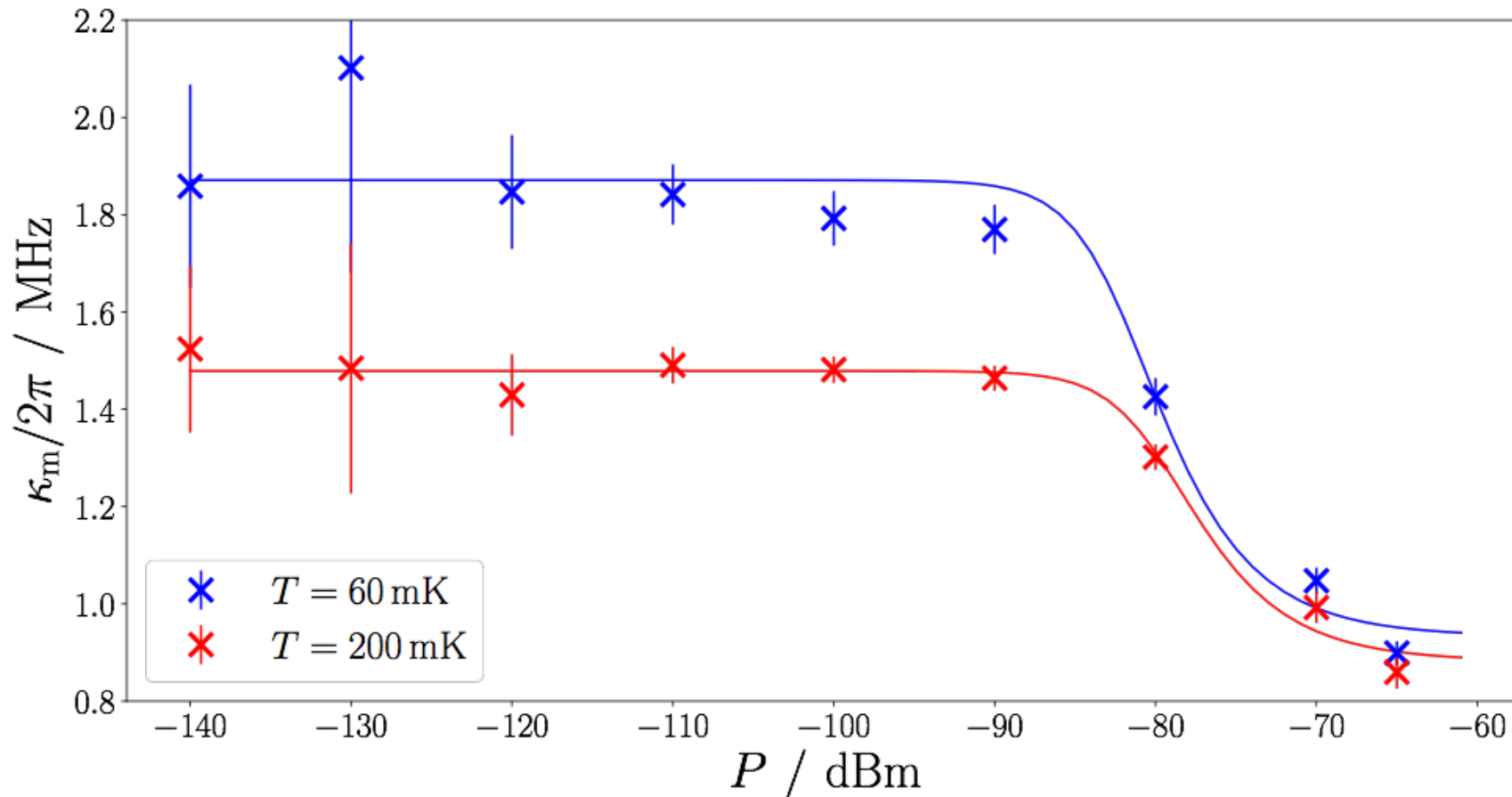


Fit to TLS model:

$$\gamma'_0 = 0.84 \text{ MHz}, \quad \gamma_{\text{off}} = 1.01 \text{ MHz}$$

Magnon linewidth below 1.5 K

$$\gamma_{\text{TLS}} = \gamma_0 \cdot \tanh\left(\frac{\hbar\omega}{2k_{\text{B}}T}\right) \cdot \frac{1}{\sqrt{1 + \frac{P_{\text{in}}}{P_c}}} + \gamma_{\text{off}}$$

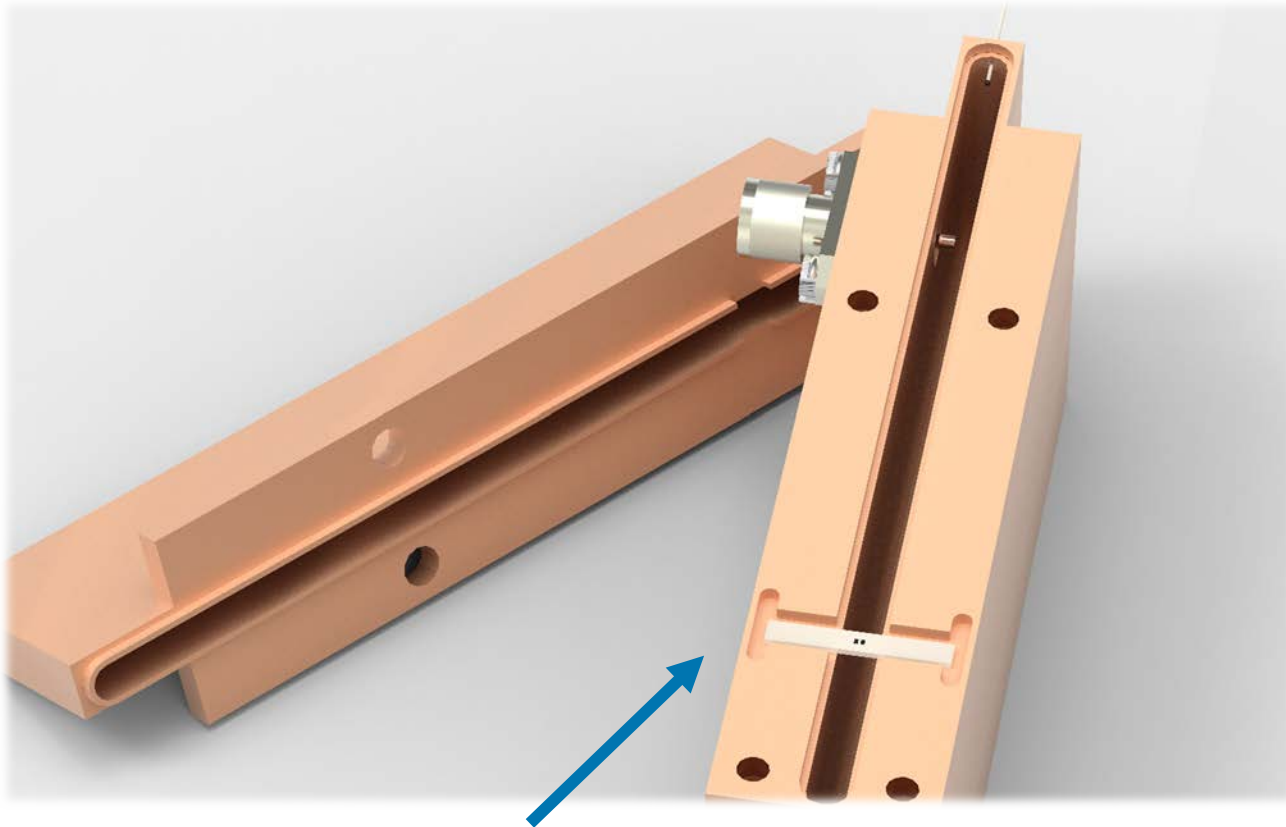


$$\gamma_0 = 1.02 \pm 0.15 \text{ MHz}$$

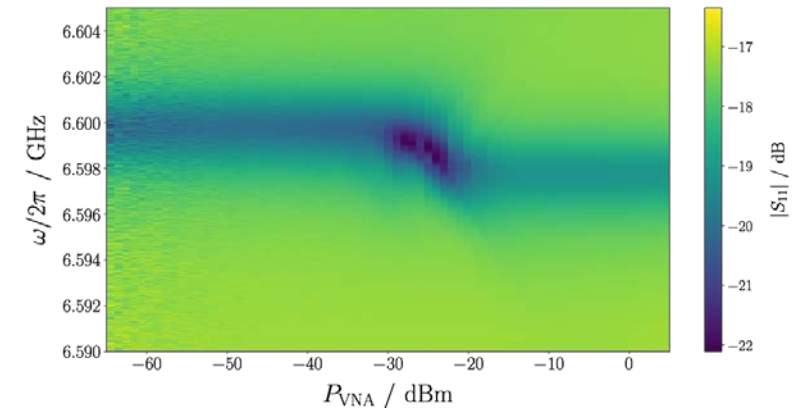
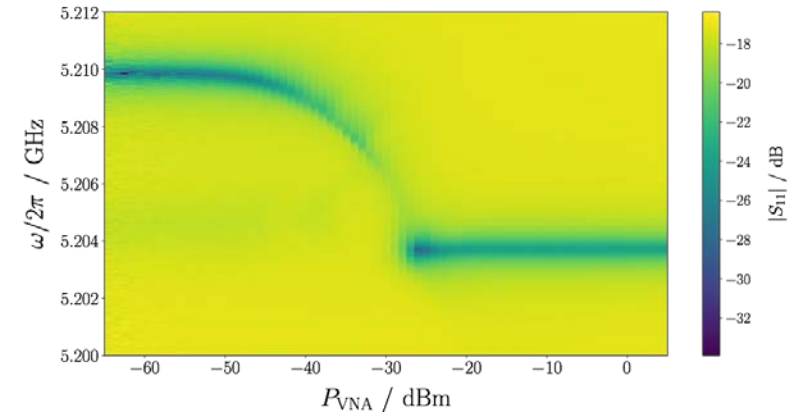
$$P_c = -80.98 \pm 6.33 \text{ dBm}$$

$$\gamma_{\text{off}} = 0.91 \pm 0.11 \text{ MHz}$$

Fresh data: qubit coupled to YIG

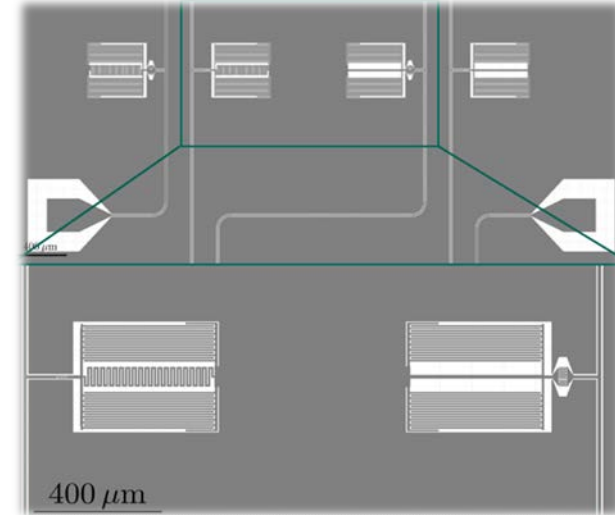
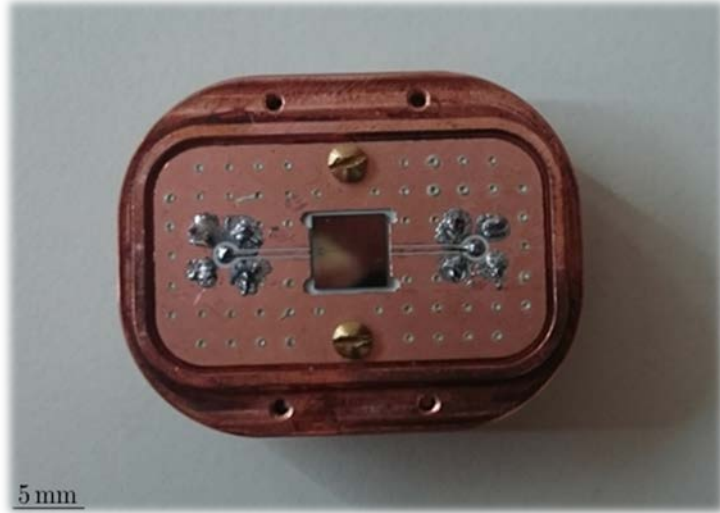


Transmon qubit



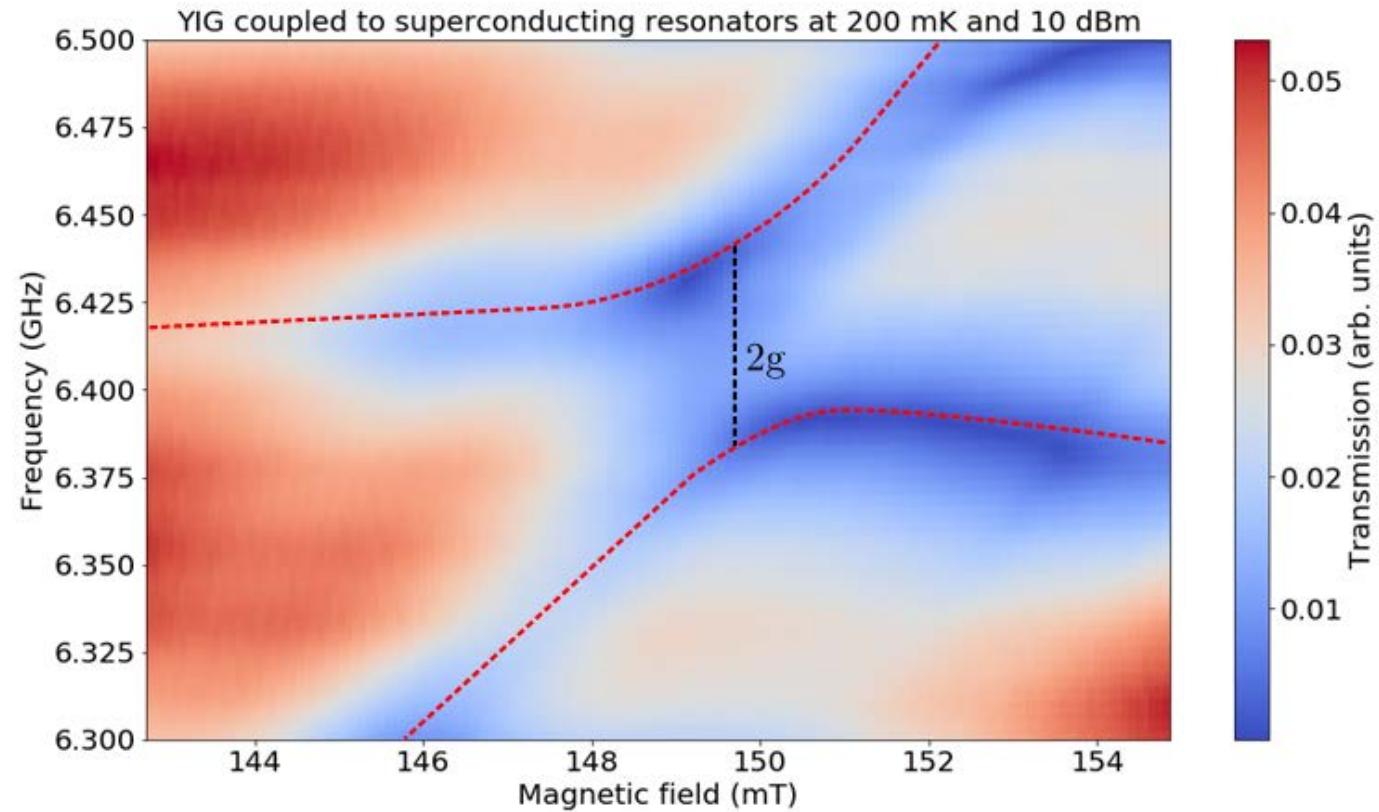
→ (de) couple from qubit

Go thin film

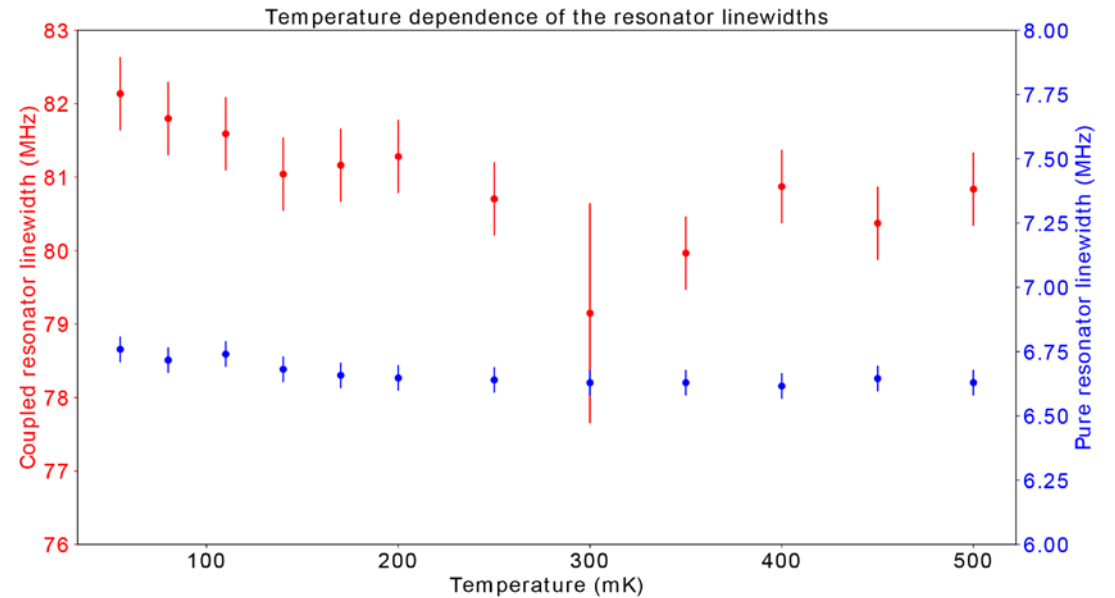
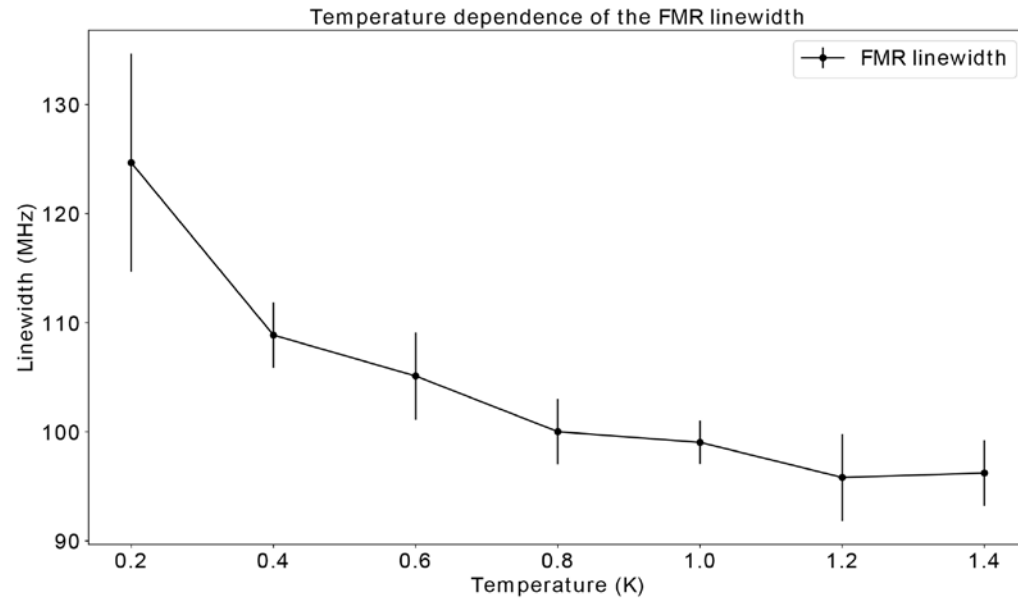


- Sputtered NbN (150 nm) on Si substrate
 - Frequency division mux'ed lumped element resonators
 - Flip-chip: 310nm YIG/GGG (Carsten Dubs, Innovent, LPE) face-down on (some) resonators and transmission line
- Resonator loss, YIG loss and coupling g

Measurement results: at cryogenic temperatures



Thin film YIG on NbN transmission line / resonator



- YIG resonance strongly damped
- Superconducting resonator strongly damped
- ➔ Weak coupling. Keep sampling different magnets....

Agenda

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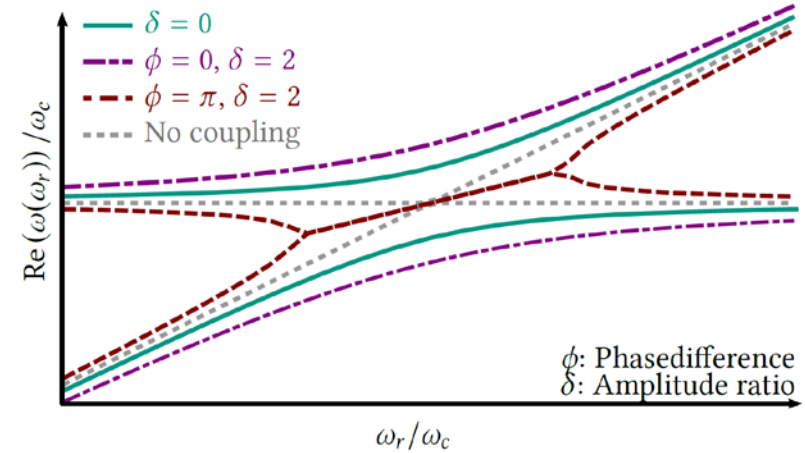
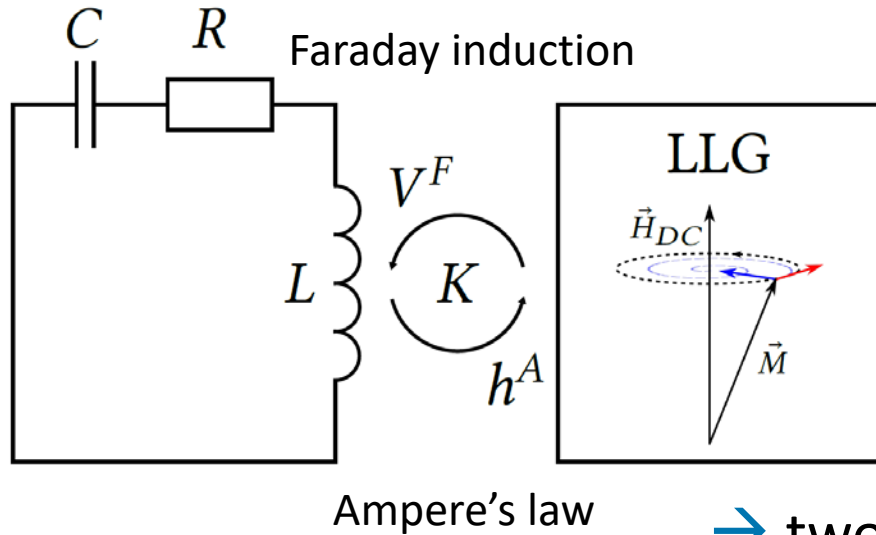
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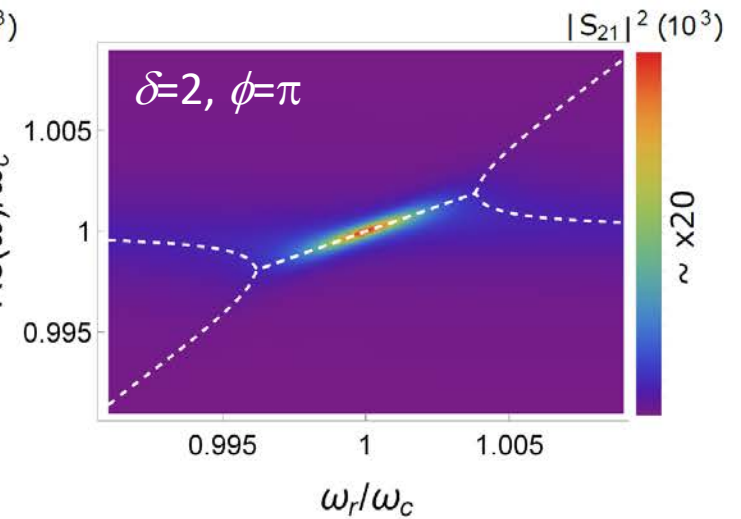
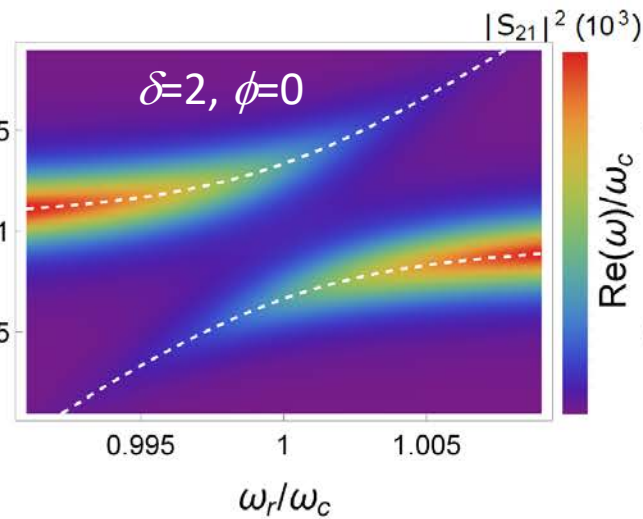
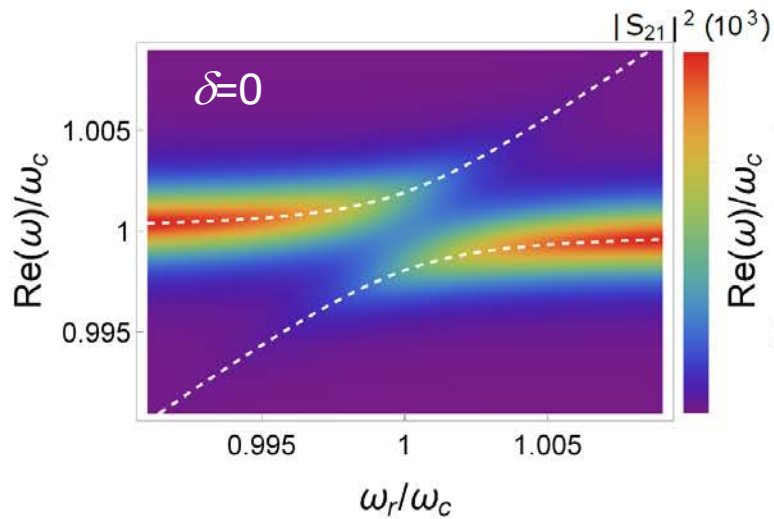
3. Synchronizing magnons with photons

- Avoided level crossing and linewidth

Synchronized spin-photon coupling in a microwave cavity

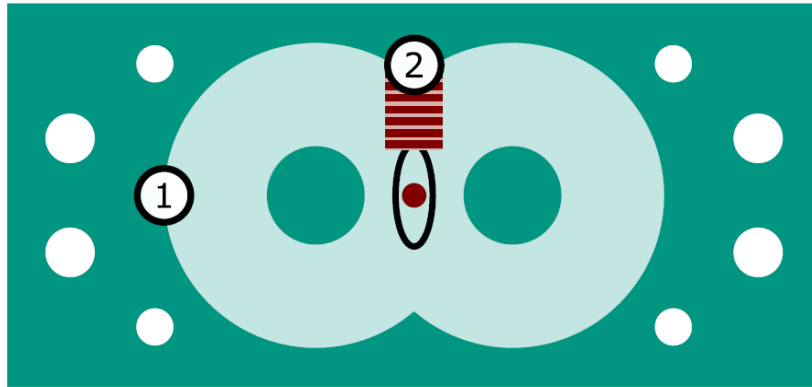


→ two time dependent magnetic fields on M

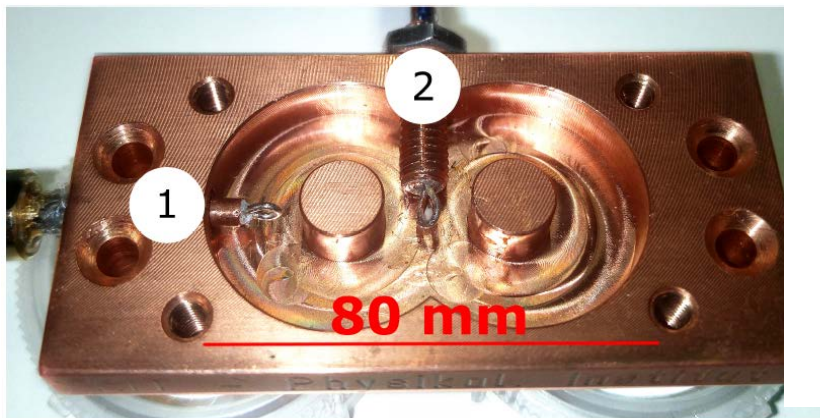


Grigoryan *et al.* arXiv:1702.07110v2

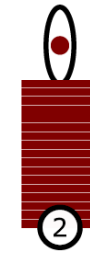
3dimensional approach



- ① Resonator Port
- ② Transmission line
- YIG sphere



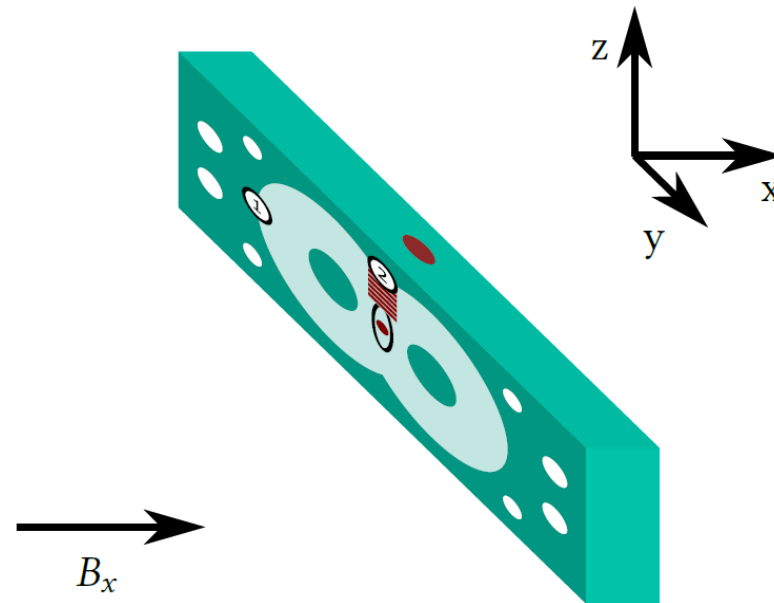
Top view



Side view



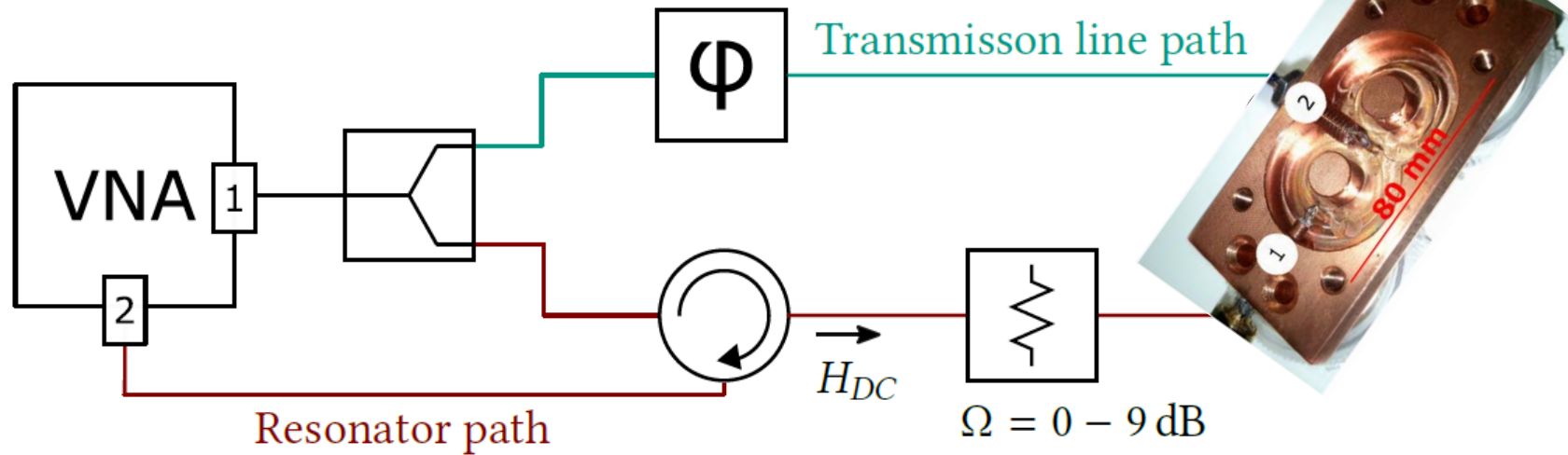
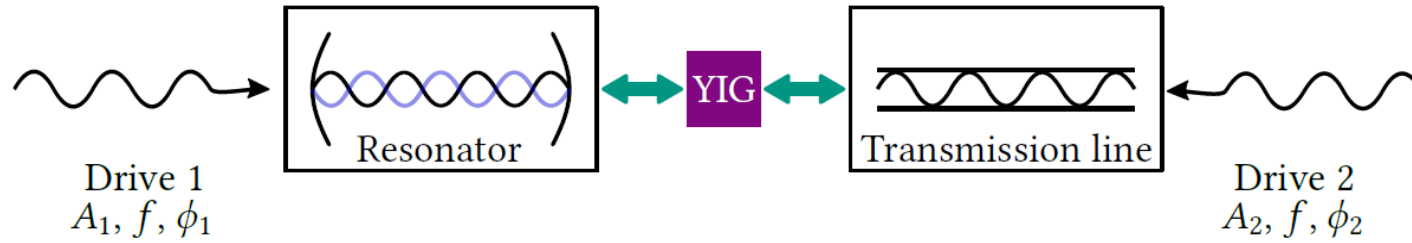
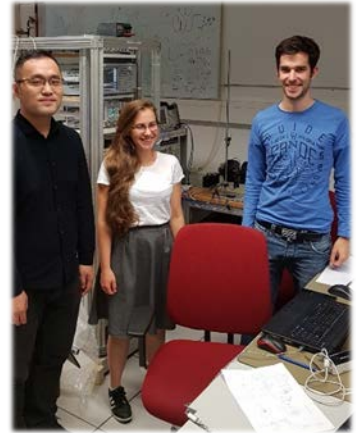
● YIG sphere mounted on BeO along [110] crystal direction



C. Dörflinger MA thesis 2018

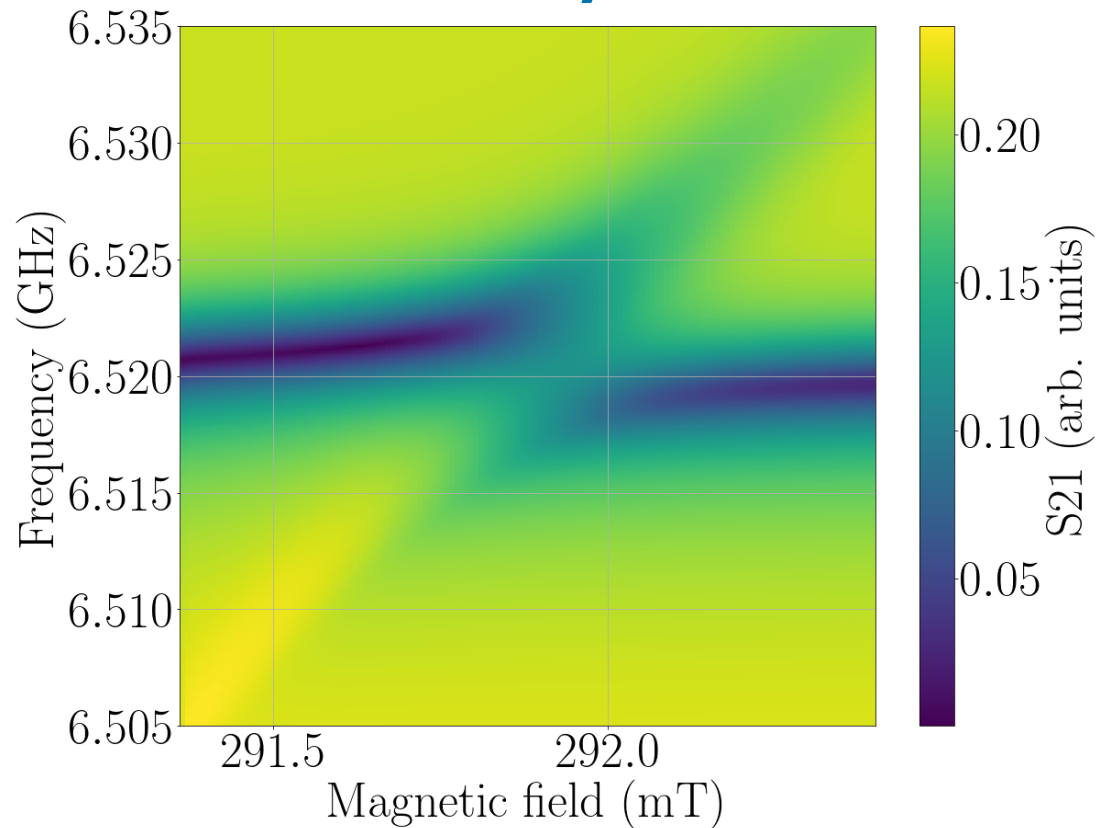
Experimental setup

Isabelle Boventer
Tim Wolz
Christine Dörflinger (missing)
Bimu Yao (Hu group)

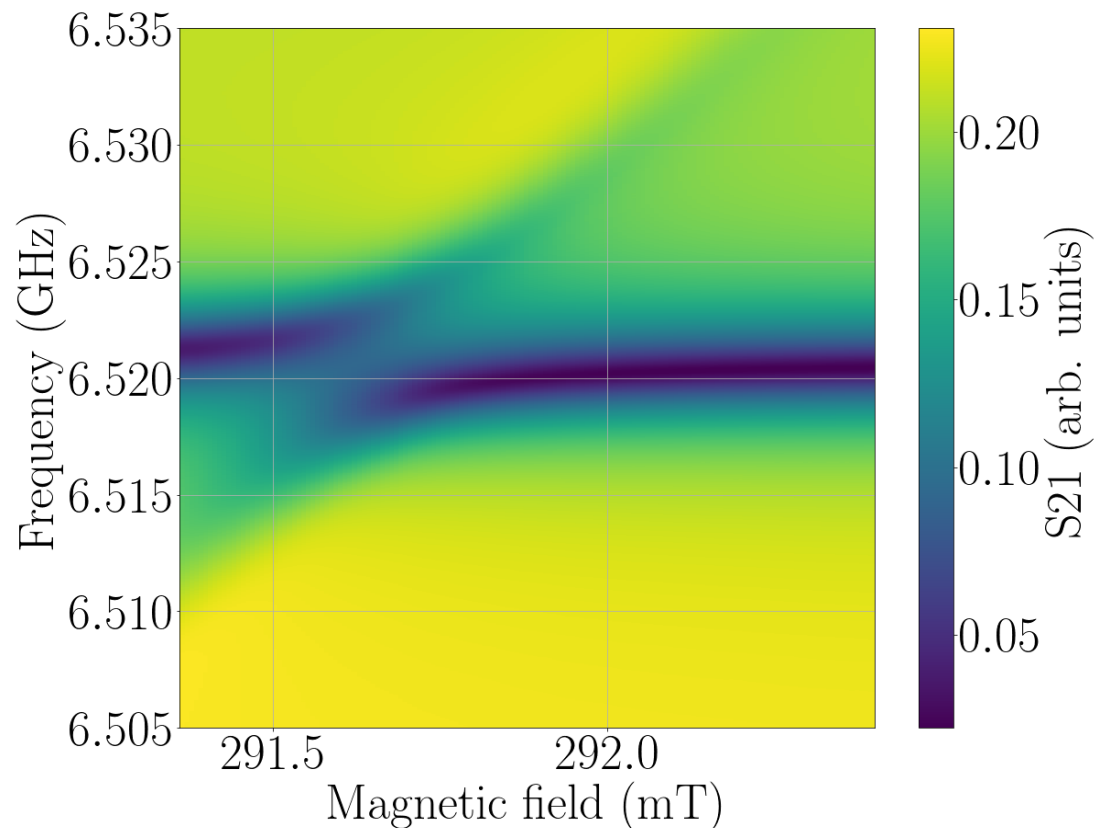


C. Dörflinger MA thesis 2018

Raw data for 3d cavity



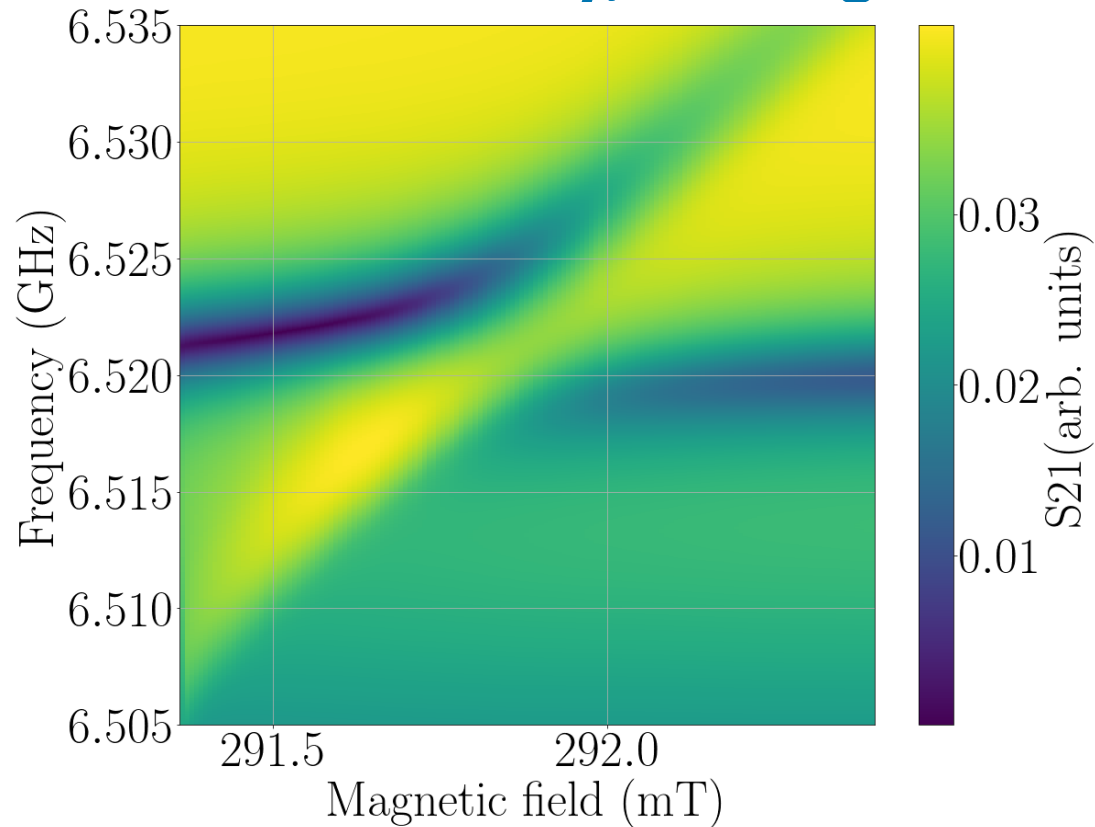
$\phi=0^\circ, \Omega=0\text{dB}$



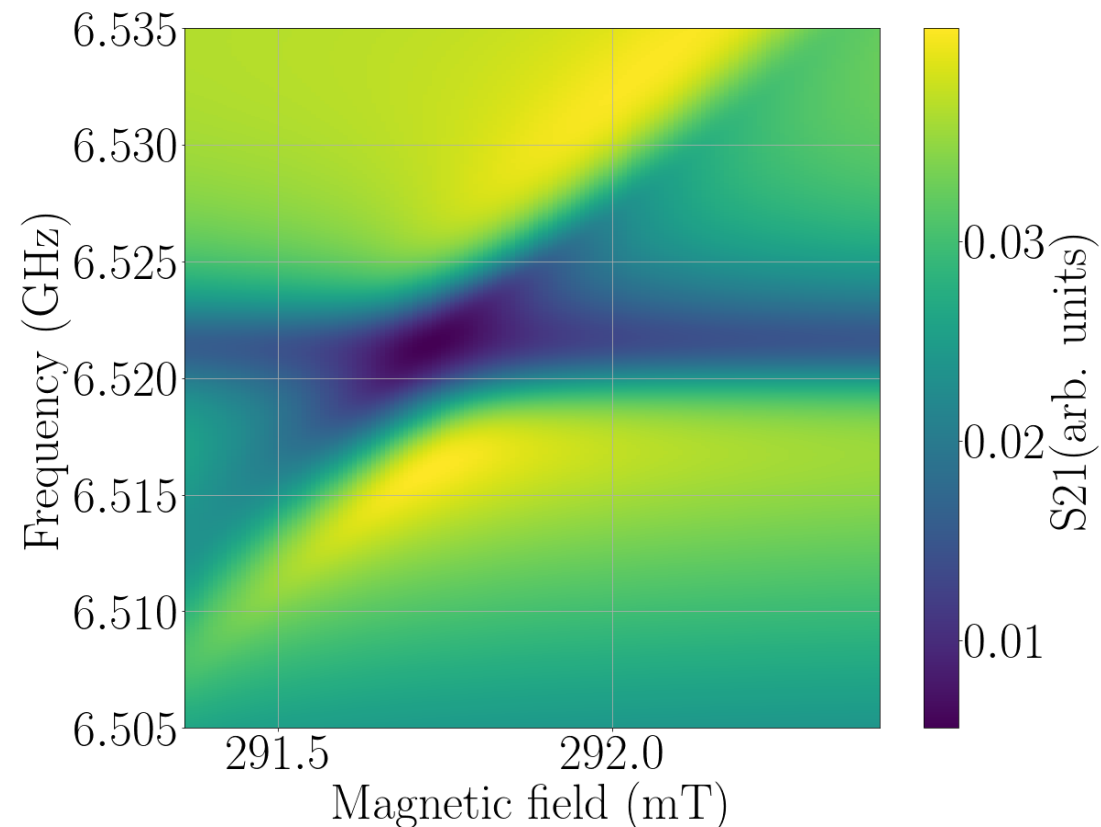
$\phi=180^\circ, \Omega=0\text{dB}$

C. Dörflinger MA thesis 2018

Raw data for 3d cavity, 9dB higher YIG drive



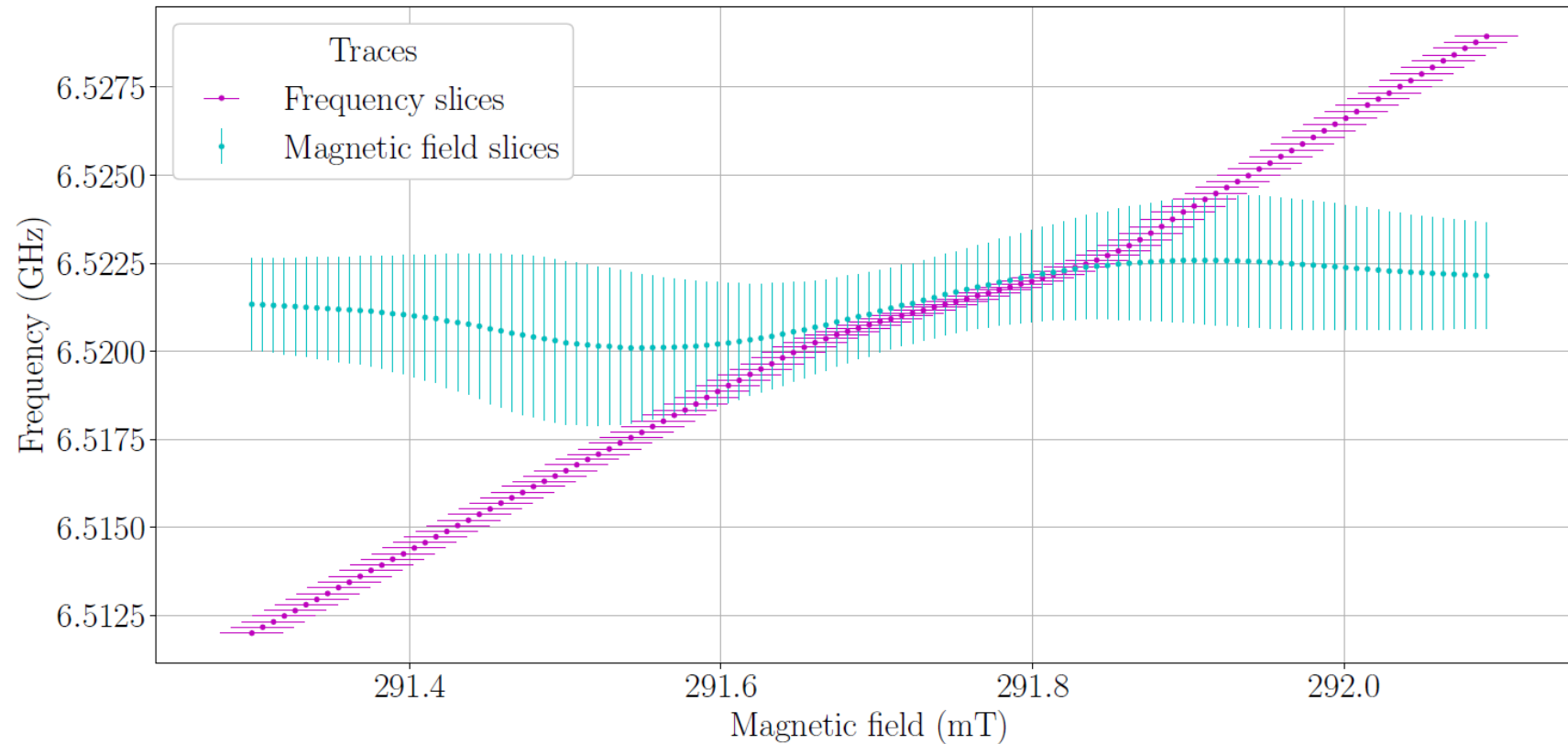
$\phi=0^\circ, \Omega=9\text{dB}$



$\phi=180^\circ, \Omega=9\text{dB}$

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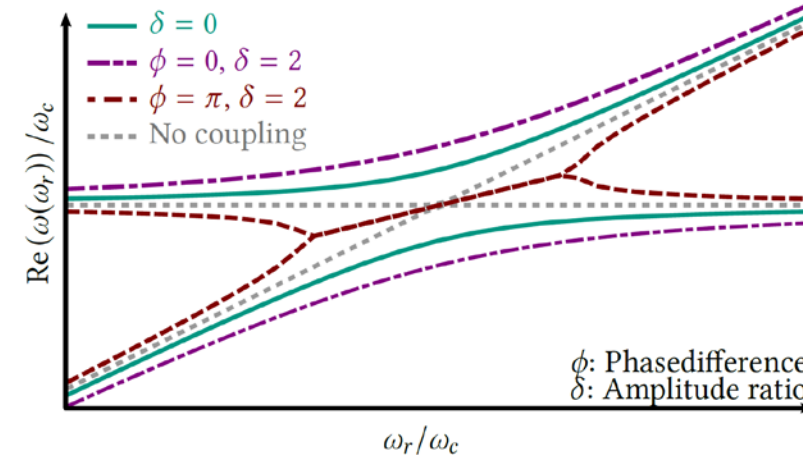
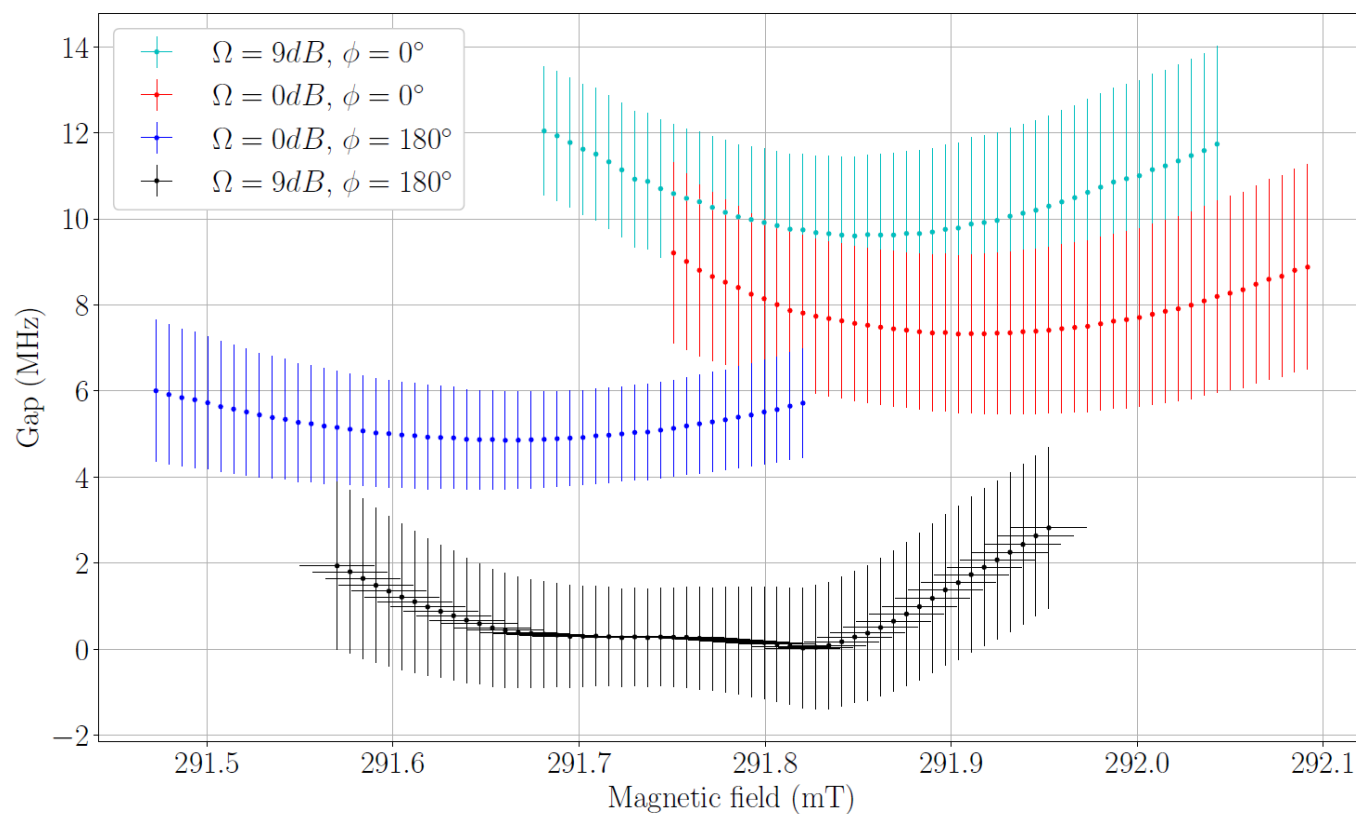
Cavity and Magnon frequencies



→ Synchronization appears

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Dispersion data of polariton modes



- Avoided level gap set by phase and relative amplitude

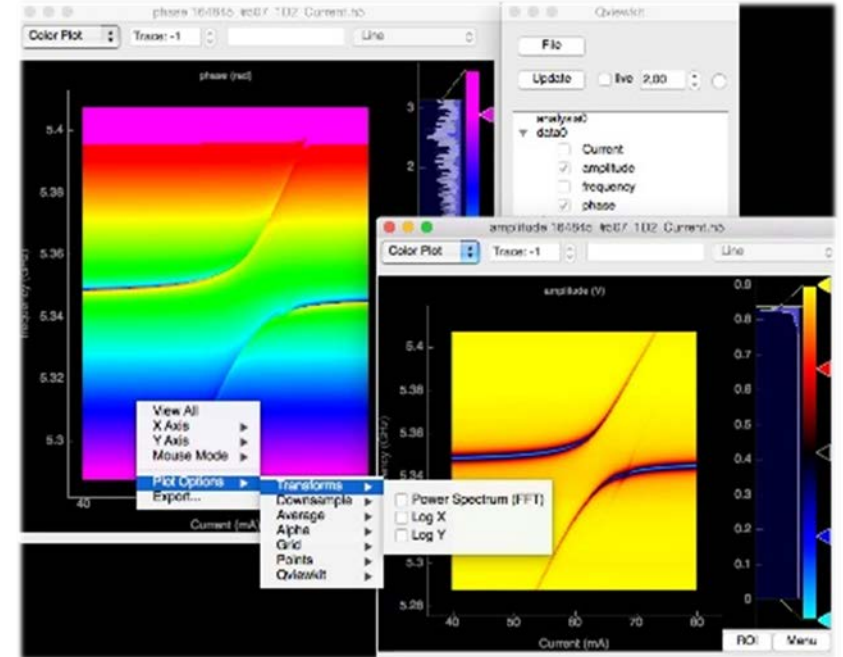
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QKIT software

Open-source software QKIT

<https://github.com/qkitgroup/qkit>

- Python notebooks
- hdf5 data storage
- Instrument drivers, fitting classes
- Flexible data viewer
- Live plotting of measurement data
- Incl. circle fit (Probst *et al.*, Rev. Sci. Instr. 2015)



git.io/qkit



www.phi.kit.edu/weides/

www.gla.ac.uk/schools/engineering/staff/martinweides/

Jochen Braumüller
Christine Dörflinger
Stefan Letzelter
Marco Pfirrmann
Tomislav Piskor
Lucas Radtke
Steffen Schlör
Andre Schneider
Alex Stehli
Tim Wolz
Ping Yang



Alexey Ustinov



JOHANNES GUTENBERG
UNIVERSITÄT MAINZ

@JGU Mainz

Isabelle Boverter

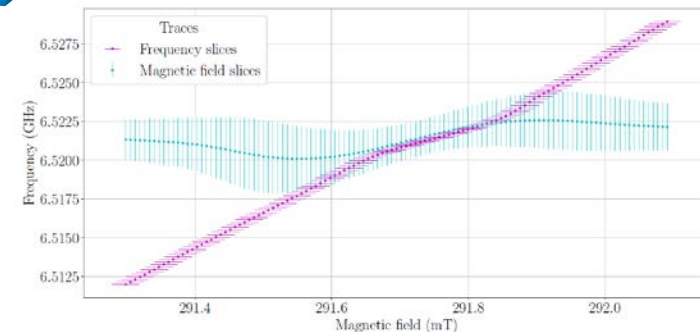
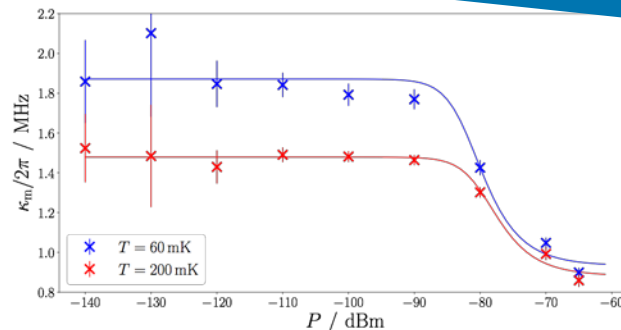
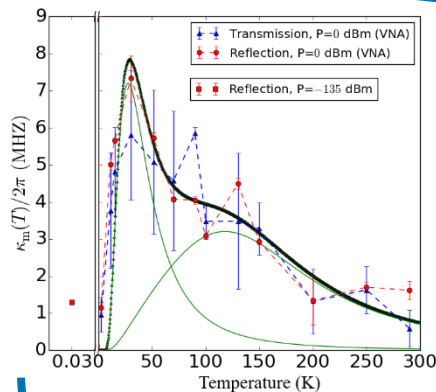
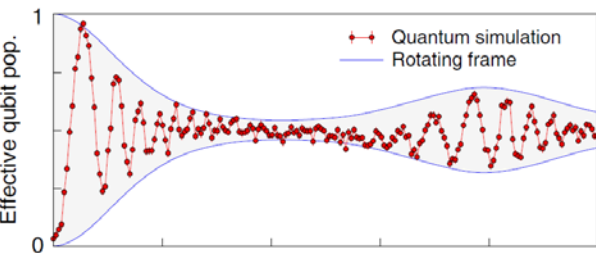
Mathias Kläui



Summary



- Analog simulation of ultra-strong coupling dynamics
- YIG sphere – cavity from 300K to 10mK
 - Power and temperature sweeps indicate additional loss at mK
- Thin film YIG/GGG strongly damped (resonator and FM)
- Controlled synchronization of spin-photon coupling demonstrated
- In progress
 - Coherent coupling to qubit



M. Kläui's talk this afternoon