



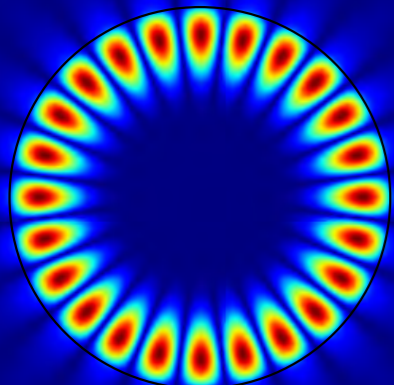
Cavity Optomagnonics

nonlinear dynamics
and textures

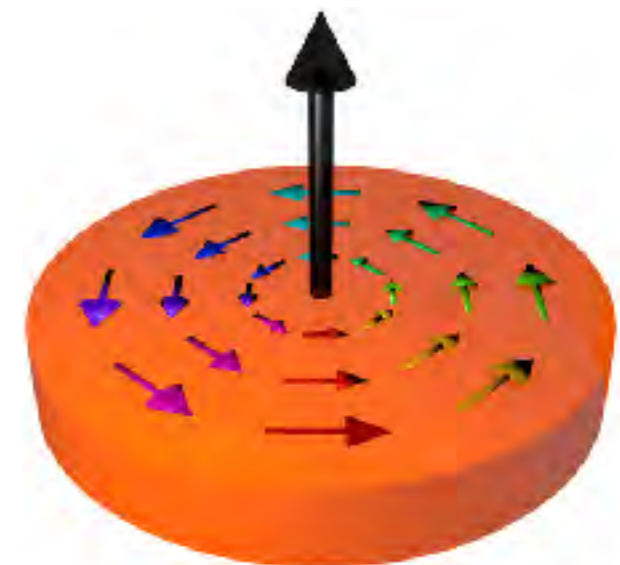


Jasmin Graf, Hannes Pfeifer, Florian Marquardt
Hong Tang (Yale)

Silvia Viola Kusminskiy



MAX PLANCK INSTITUTE
for the science of light



New Max Planck Research Group



MAX PLANCK INSTITUTE
for the science of light

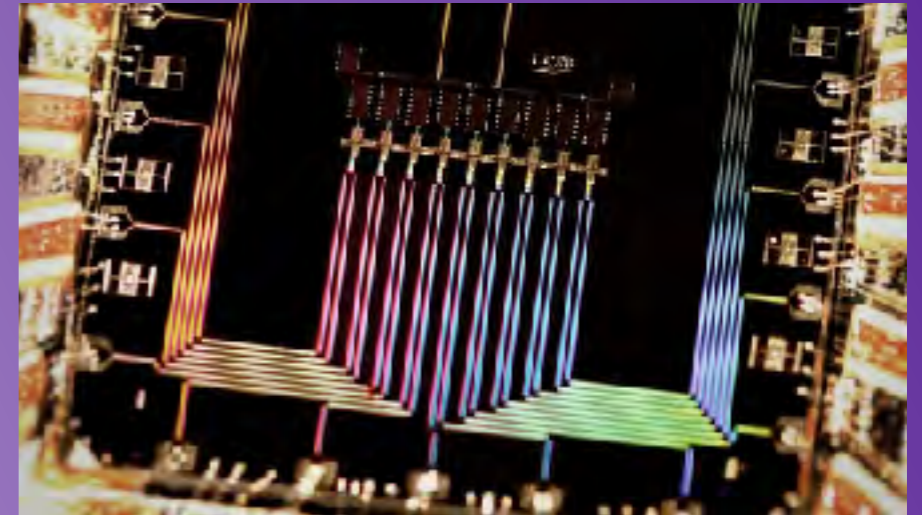
Erlangen, Germany



classical technologies

quantum technologies

superconducting quantum circuit



Martinis group
UCSB and Google (2015)



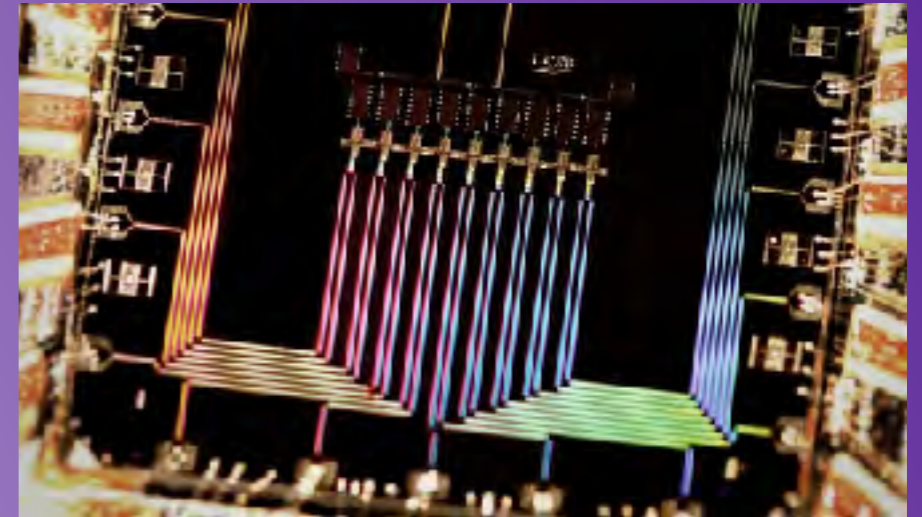
optical fiber



classical technologies

quantum technologies

superconducting quantum circuit



Martinis group
UCSB and Google (2015)

need
hybrid
systems

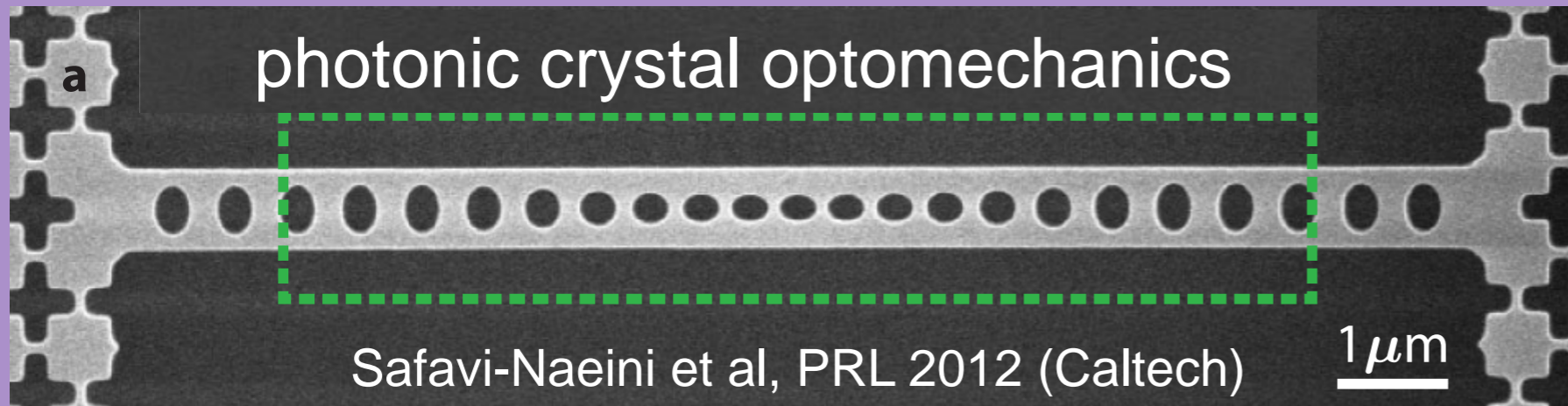


optical fiber

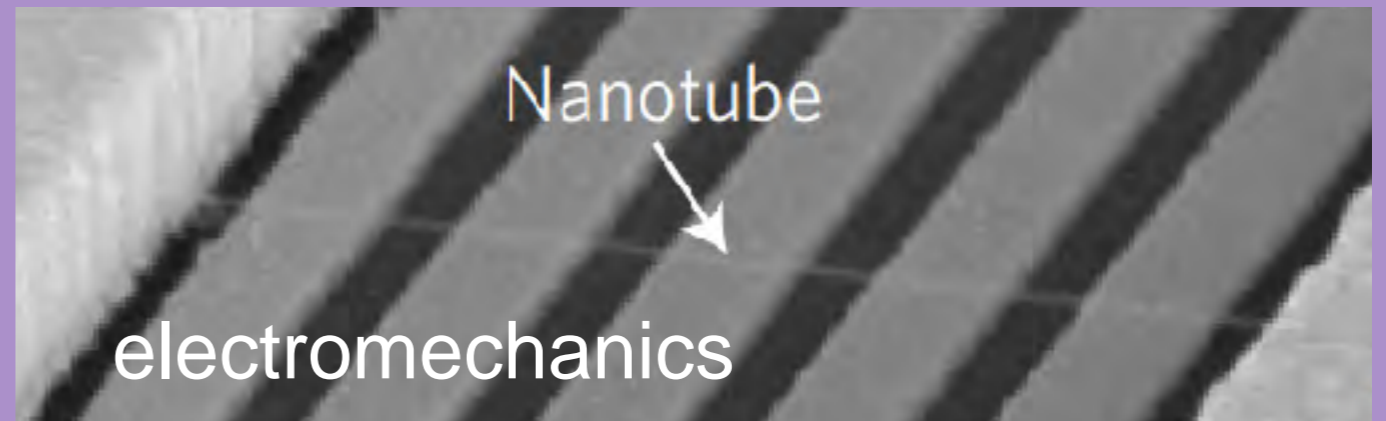
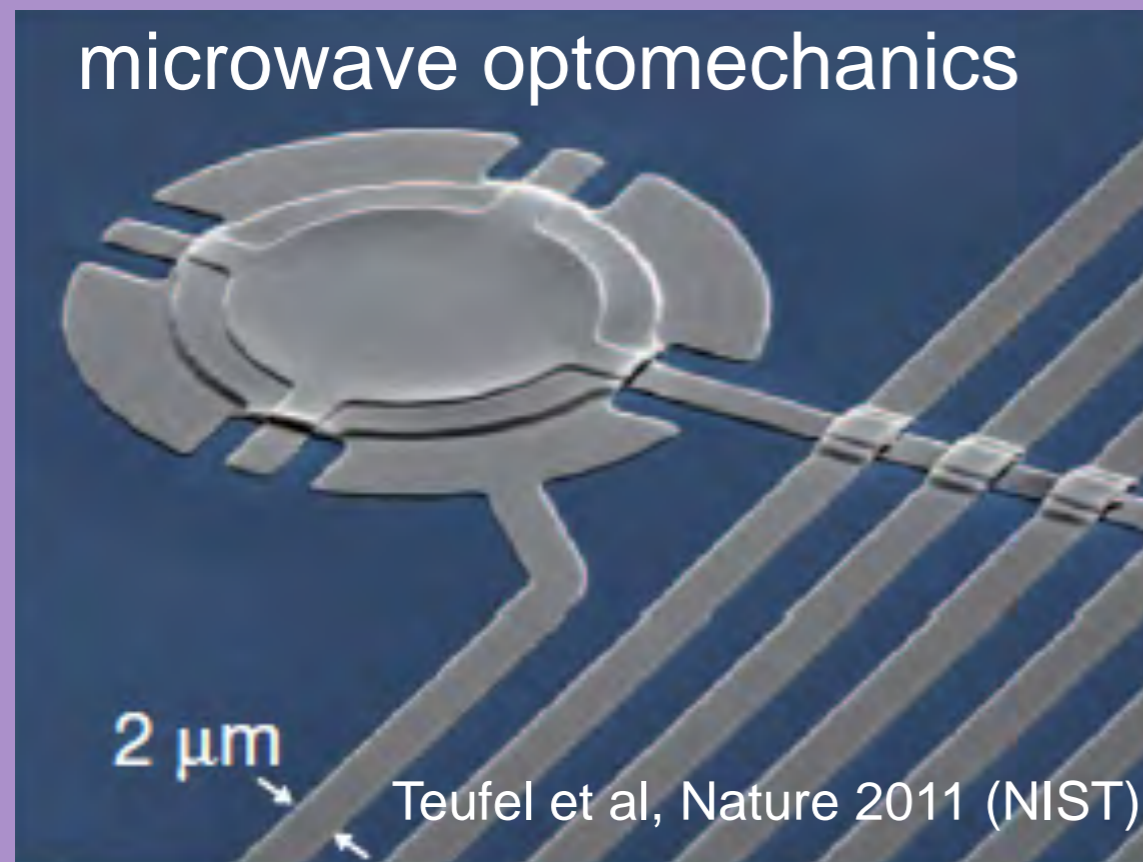


classical technologies

Hybrid Systems for Quantum Technologies



mesoscopic:
nano/micro scale
systems



Benyamini et al, Nature Physics 10, 151 (2014)



Osada et. al PRL 116, 223601 (2016)

use collective excitations

Optomagnonics



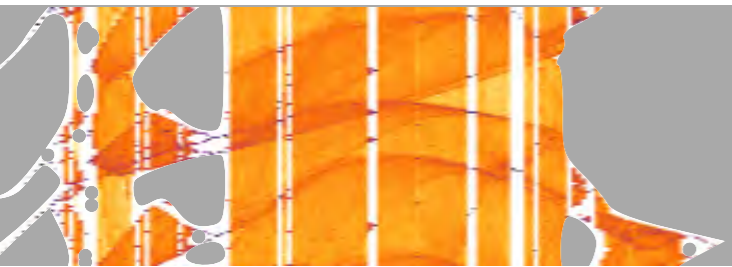
Picture from Tabuchi et al, PRL 113, 083603 (2014)



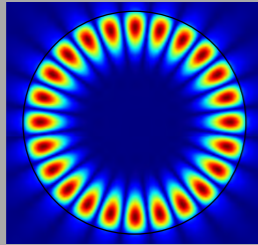
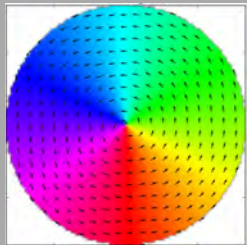
Introduction and motivation



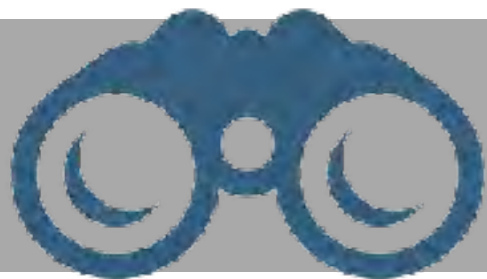
Optomagnonic Hamiltonian



Optically induced spin dynamics



Magnetic textures: vortex in a disk



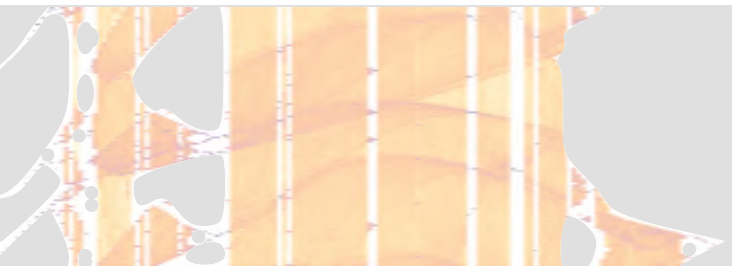
Summary



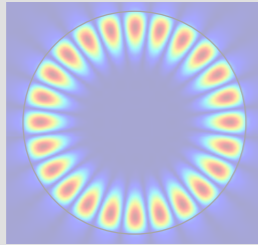
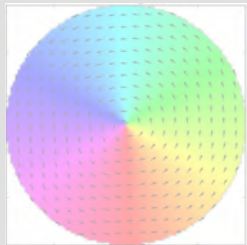
Introduction and motivation



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Summary

Magnonics



magnon

elementary magnetic
excitation
(quantum of spin wave)

Magnonics



magnon

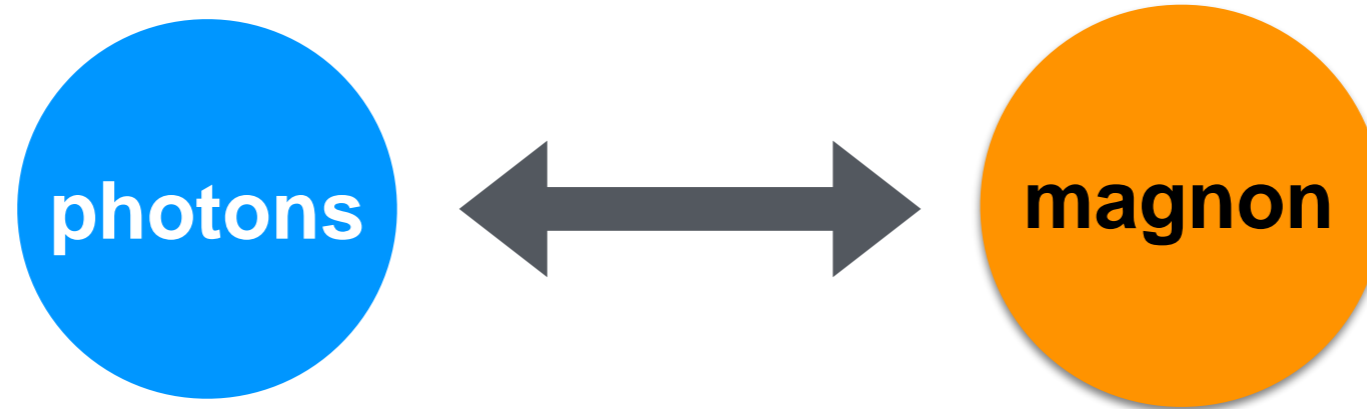
elementary magnetic
excitation
(quantum of spin wave)

Robust

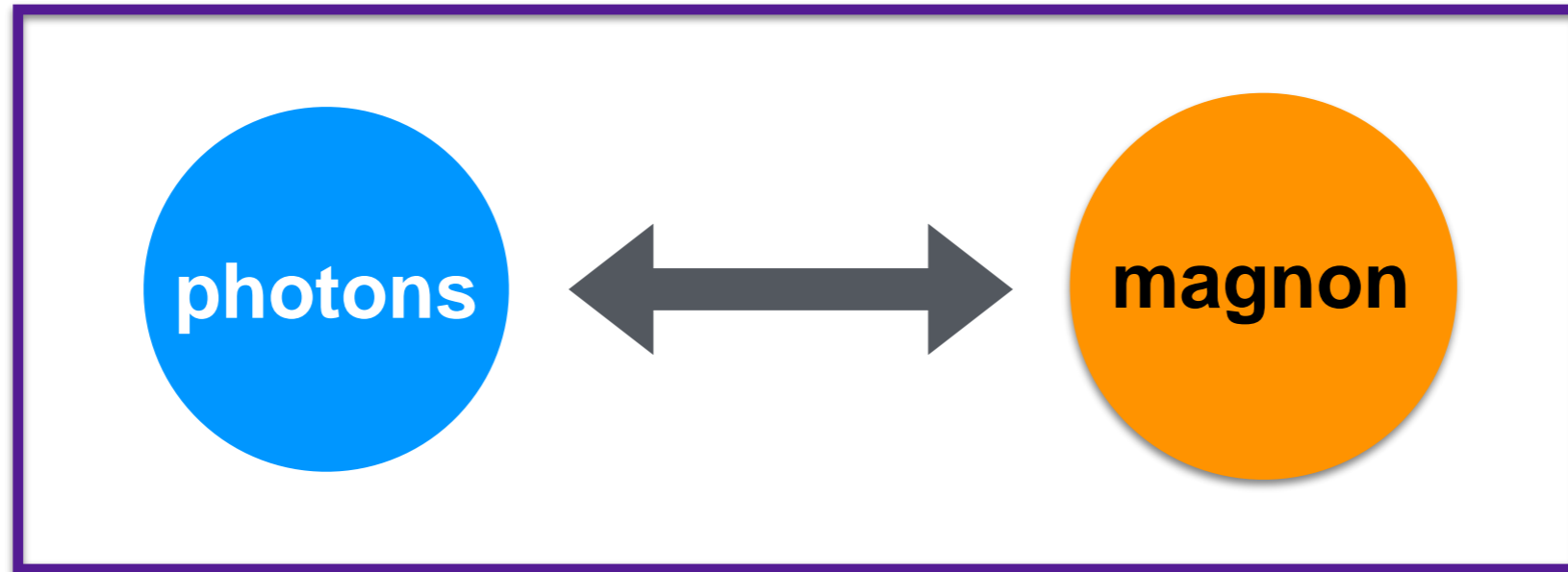
Low Power

Tunable

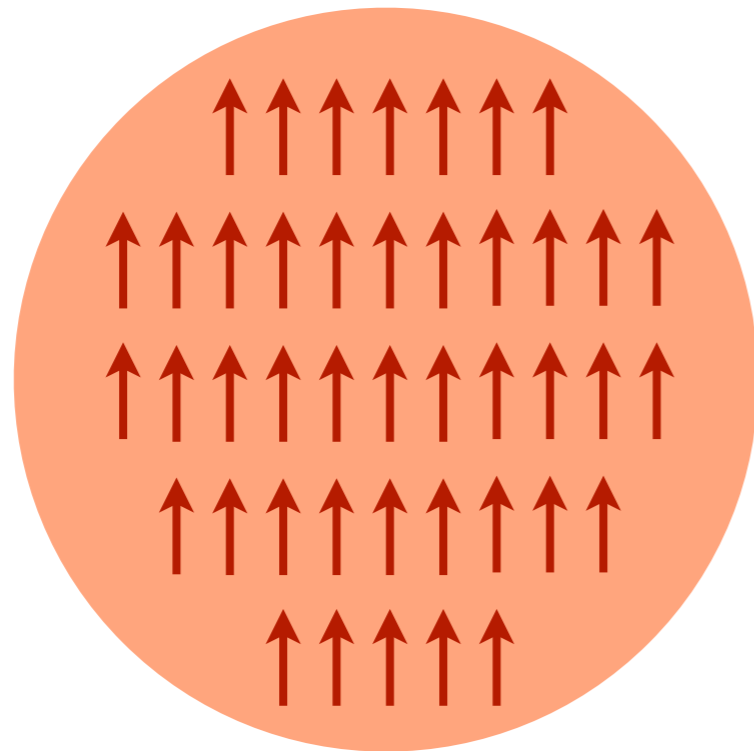
Optomagnonics



Cavity Optomagnonics



Kittel mode



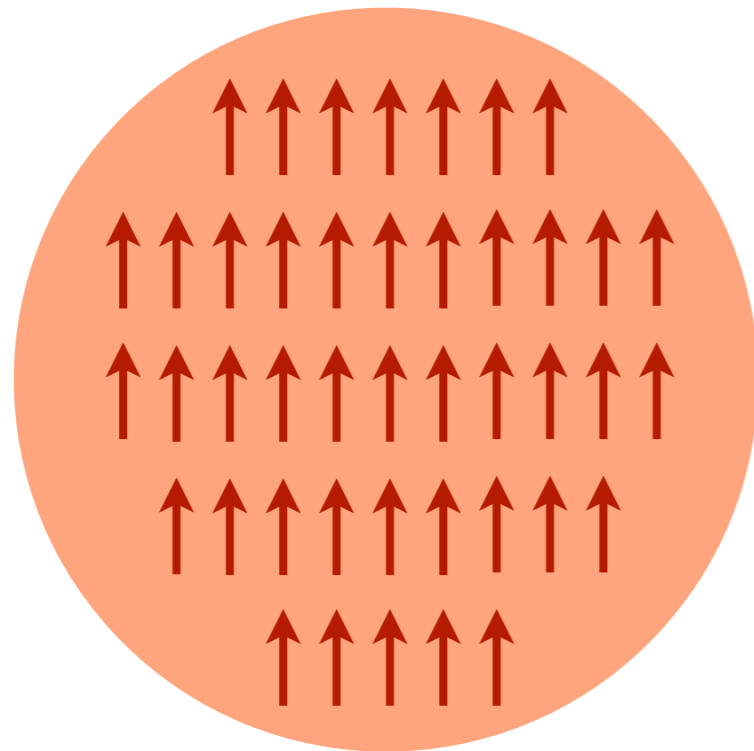
homogeneous
magnetic mode

$$\mathbf{M}(\mathbf{r}) = \mathbf{M}$$

spin wave with $k=0$

Magnonics

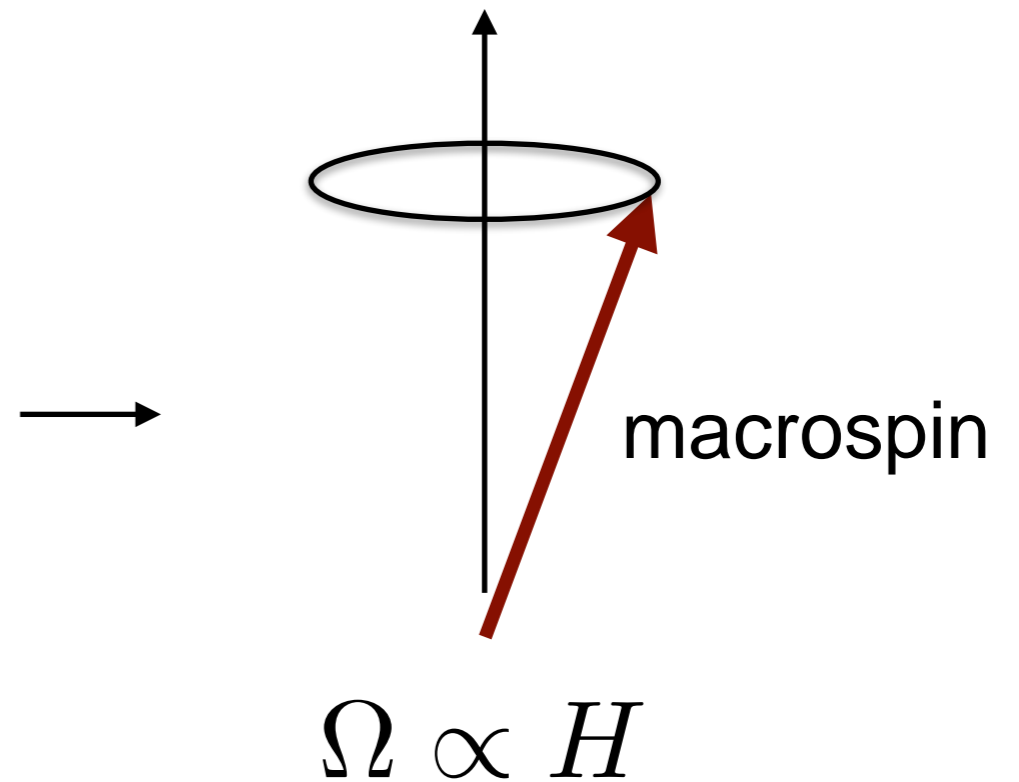
Kittel mode



homogeneous
magnetic mode

$$\mathbf{M}(\mathbf{r}) = \mathbf{M}$$

spin wave with $\mathbf{k} = 0$



tunable precession frequency

$$\Omega \sim \text{GHz}$$

for 30mT

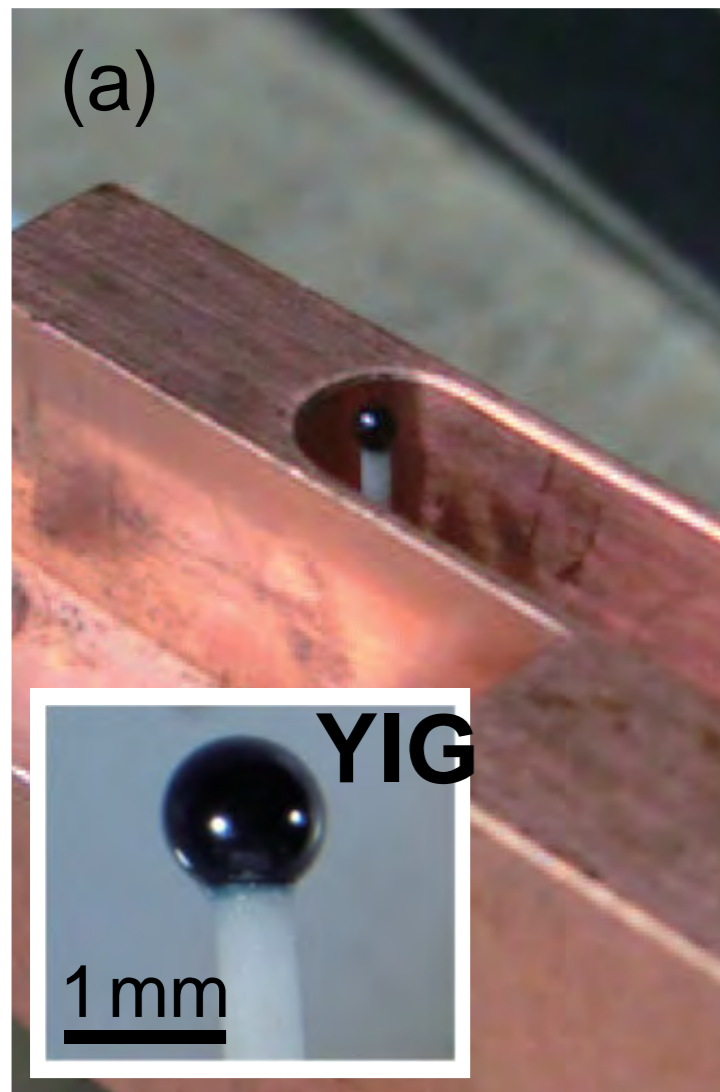
Microwave Regime

Magnons



Microwaves

Strong coupling demonstrated in 2014



- Tabuchi et. al PRL 113, 083603 (Nakamura's group, Tokyo)

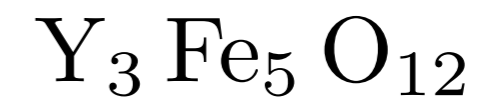
- Zhang et. al PRL 113, 156401 (Hong Tang's group, Yale)

YIG



YIG

Yttrium Iron Garnet



- ferrimagnetic
- insulator
- transparent in the infrared

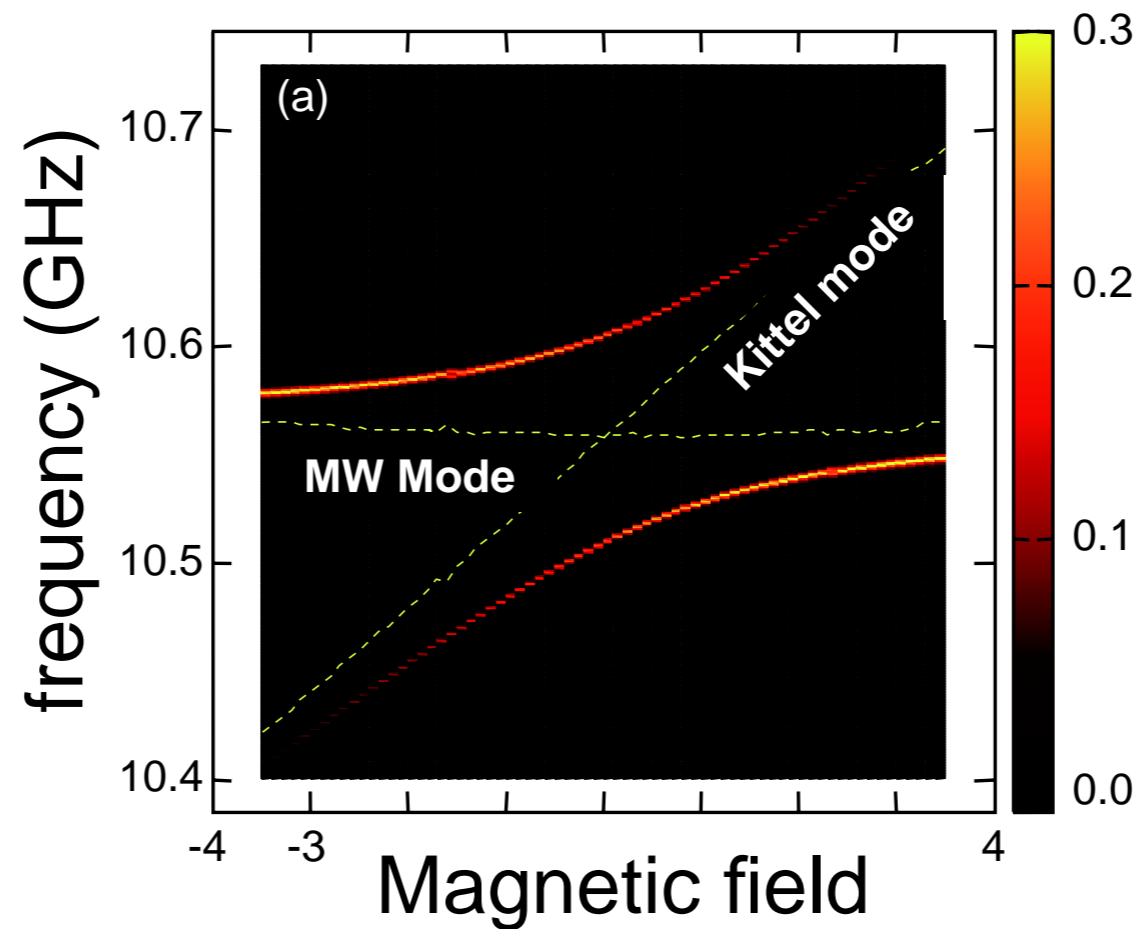
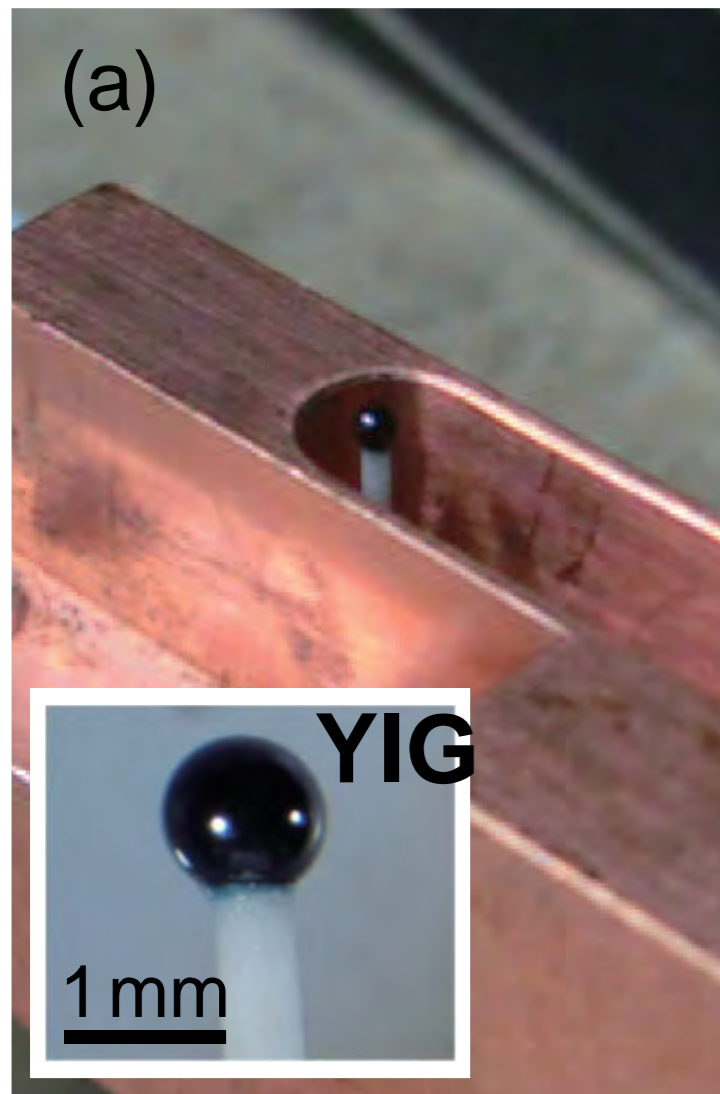
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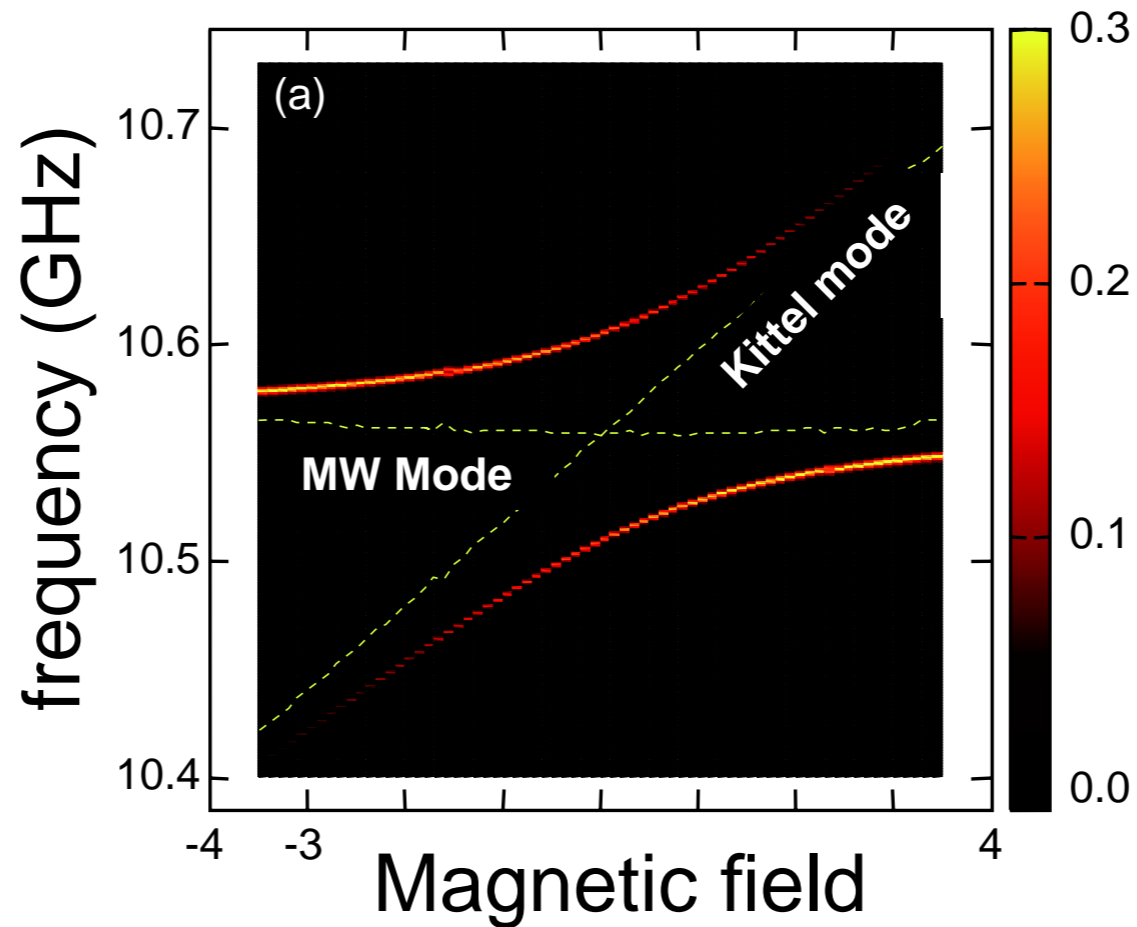
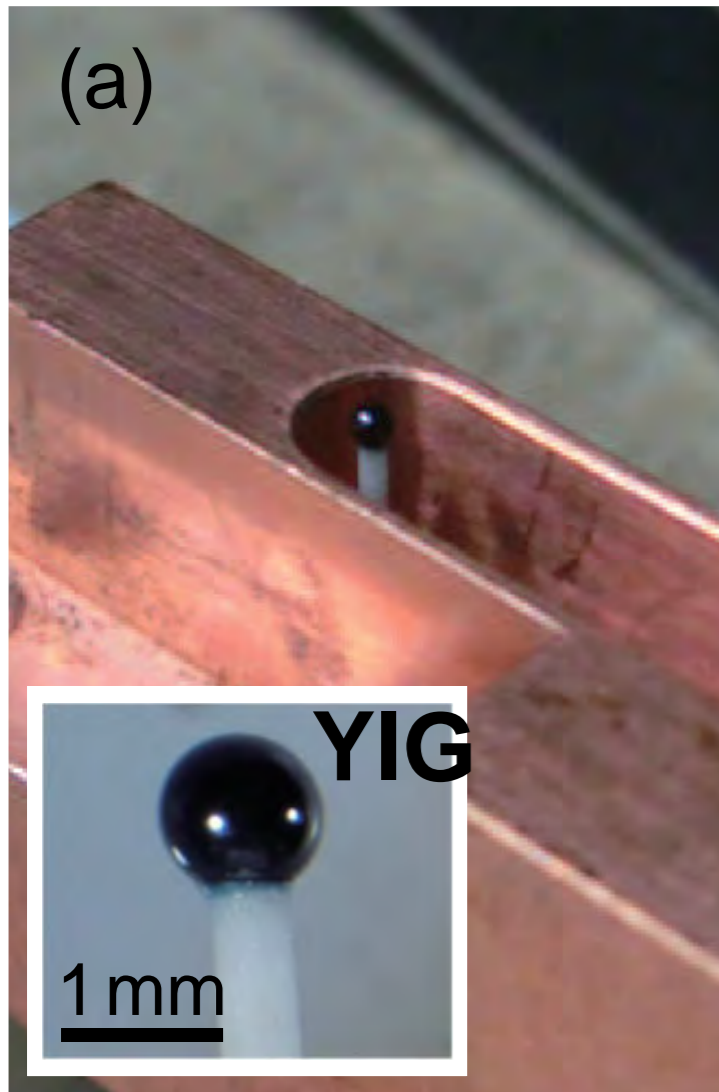
Microwave Regime

Magnons



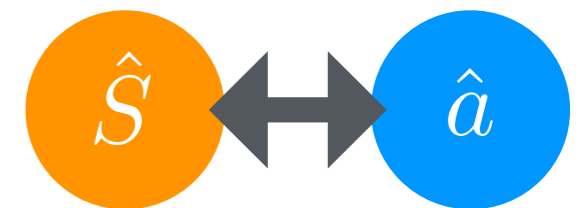
Microwaves

Strong coupling regime



Resonant coupling

$$\hat{S}^+ \hat{a} + \hat{S}^- \hat{a}^\dagger$$



$\sim 50\text{MHz}$

Cooperativity

$$\mathcal{C} = 3 \times 10^3$$

Huebl et. al, PRL 111, 127003 (2013)

Zhang et. al PRL 113, 156401 (2014)

Tabuchi et. al PRL 113, 083603 (2014)

Soykal and M. E. Flatte
PRL 104, 077202 (2010)

Microwave Regime

Magnons



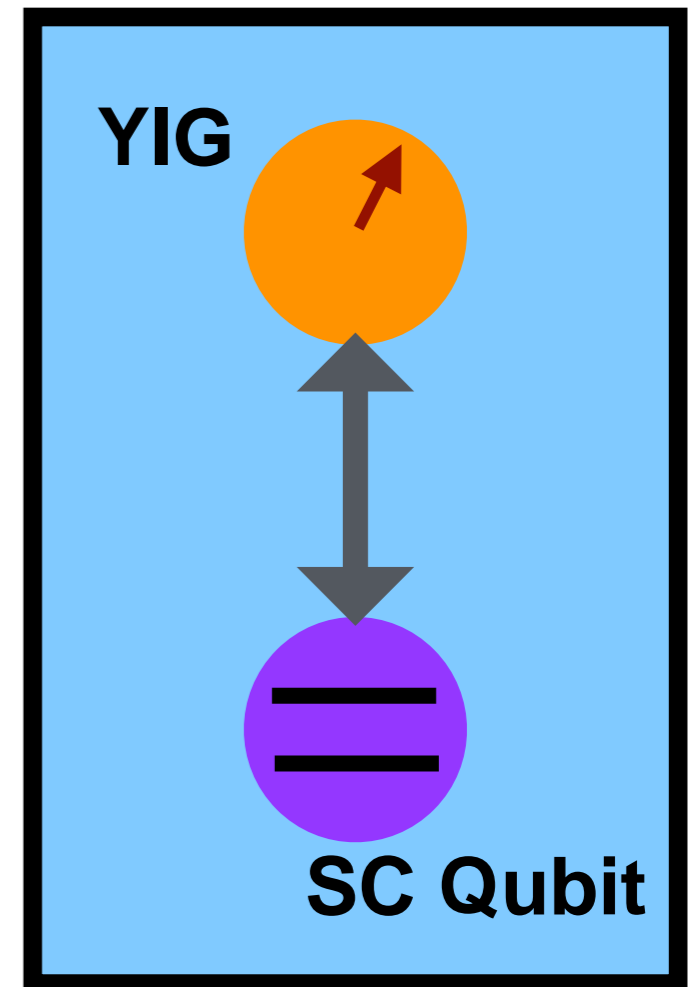
Microwaves

QUANTUM INFORMATION

(Science 2015)

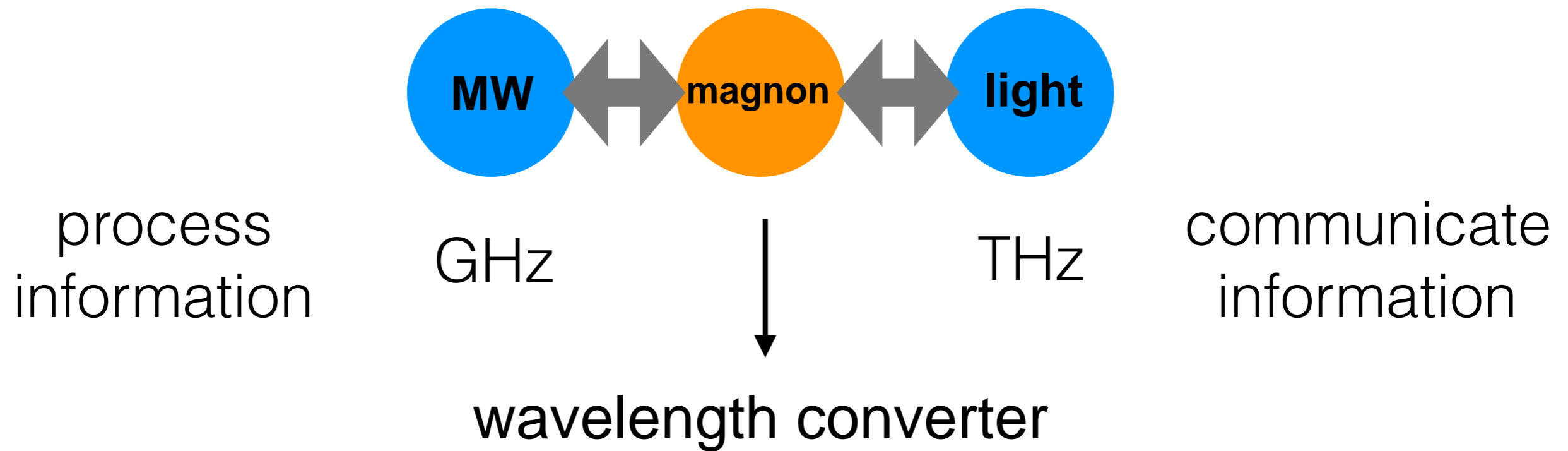
Coherent coupling between a ferromagnetic magnon and a superconducting qubit

Yutaka Tabuchi,^{1*} Seiichiro Ishino,¹ Atsushi Noguchi,¹ Toyofumi Ishikawa,¹
Rekishu Yamazaki,¹ Koji Usami,¹ Yasunobu Nakamura^{1,2}



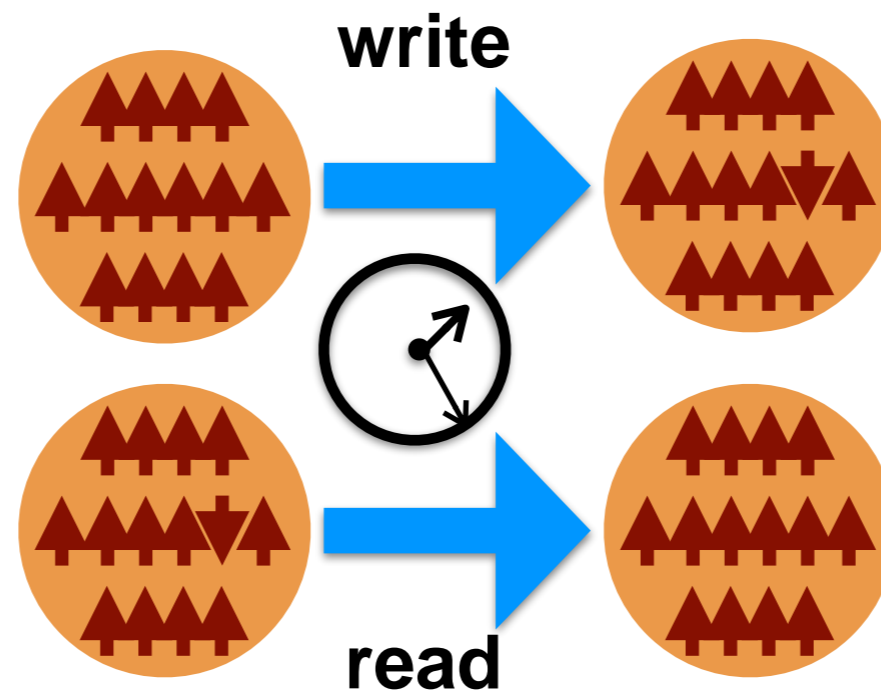
MW Cavity

Coupling to Optics?



**Motivation:
magnon as a transducer**

Coupling to Optics?



Motivation:
magnon state as a quantum memory



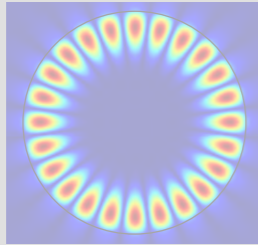
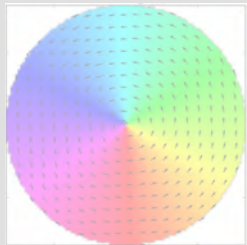
Introduction and motivation



Optomagnonic Hamiltonian



Optically induced spin dynamics



Magnetic textures: vortex in a disk

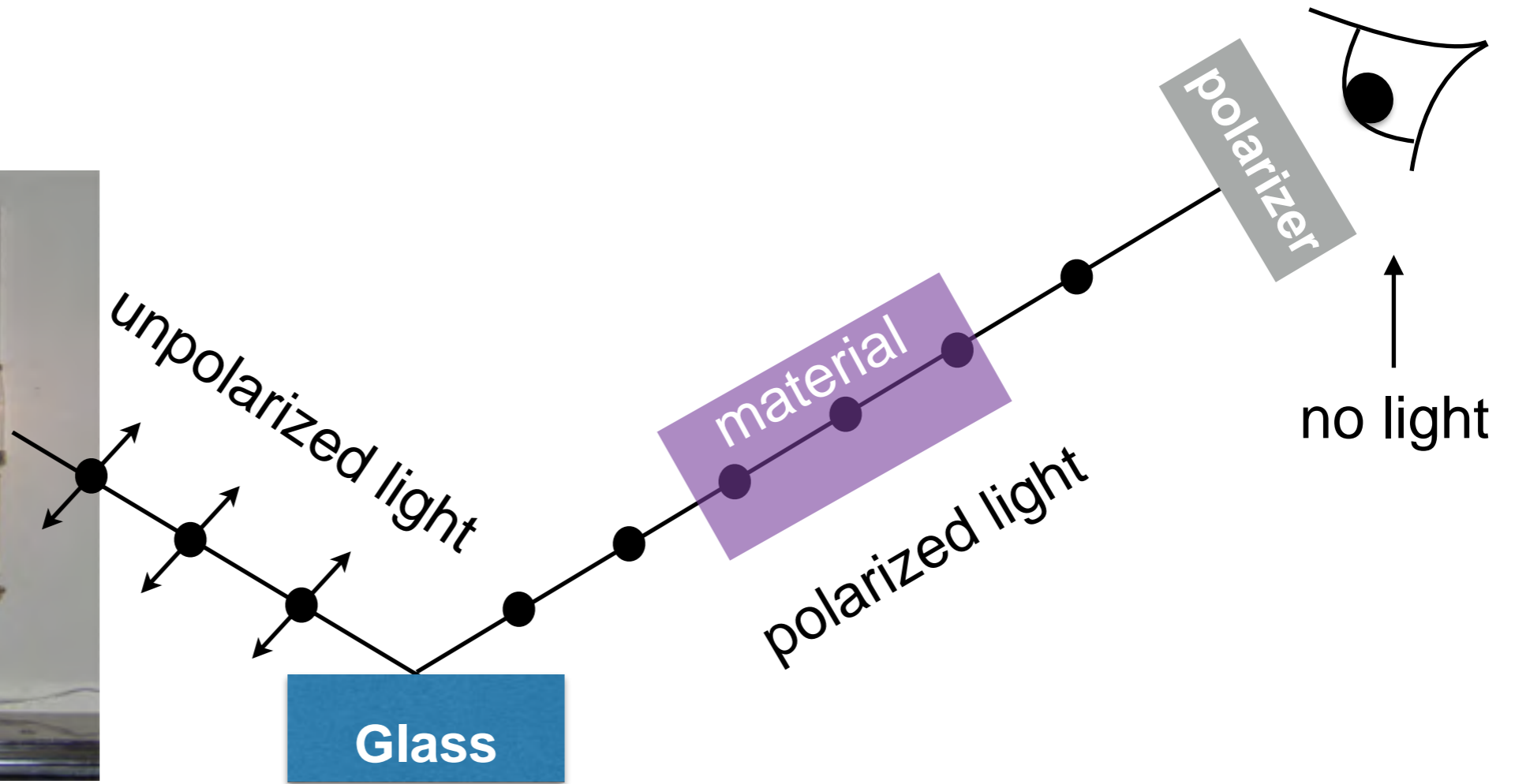


Summary

Faraday Effect (1846)



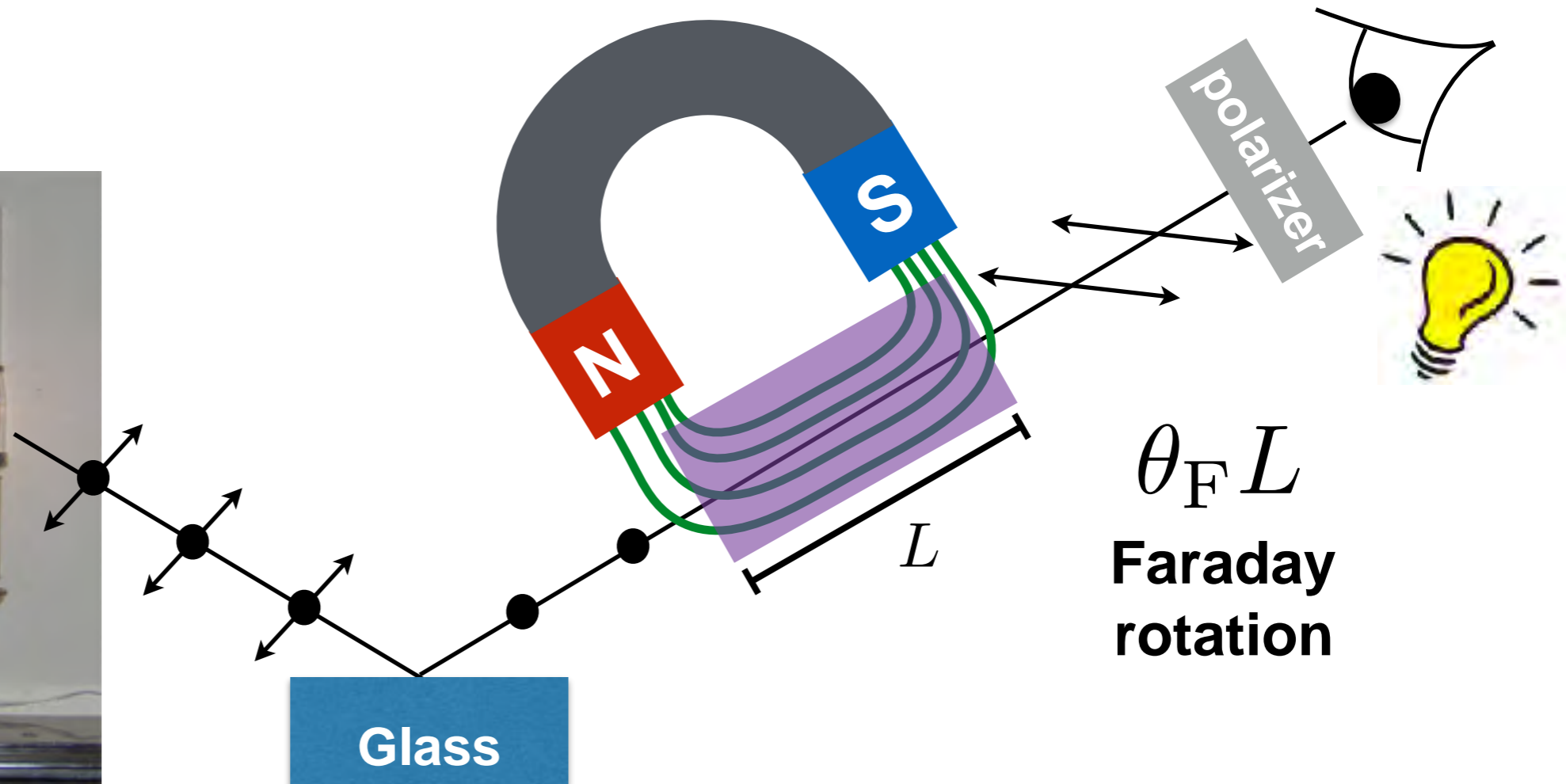
Oil Lamp



Faraday Effect (1846)

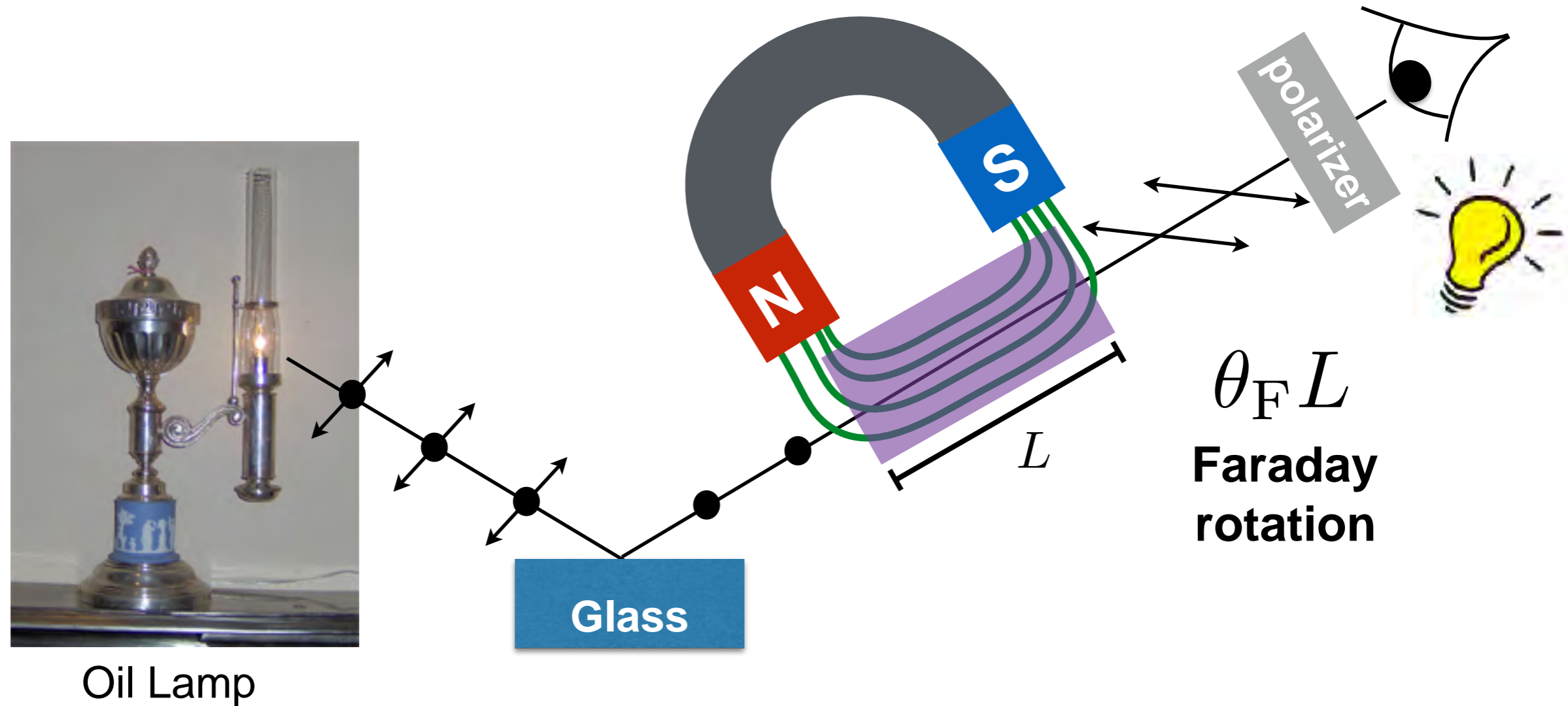


Oil Lamp



$\theta_F L$
Faraday
rotation

Faraday Effect (1846)



RELATION OF LIGHT TO THE MAGNETIC FORCE.

15

¶ iii. *General considerations.*

2221. Thus is established, I think for the first time*, a true, direct relation and dependence between light and the magnetic and electric forces; and thus a great

Coupling to Optics?: Faraday Effect

Faraday
rotation

$$\bar{U}_{\text{MO}} = \theta_{\text{F}} \sqrt{\frac{\epsilon}{\epsilon_0}} \int d\mathbf{r} \frac{\mathbf{M}(\mathbf{r})}{M_{\text{S}}} \cdot \frac{\epsilon_0}{2i\omega} [\mathbf{E}^*(\mathbf{r}) \times \mathbf{E}(\mathbf{r})]$$

optical
spin density



magnetization
density

Coupling to Optics?: Faraday Effect

Faraday rotation

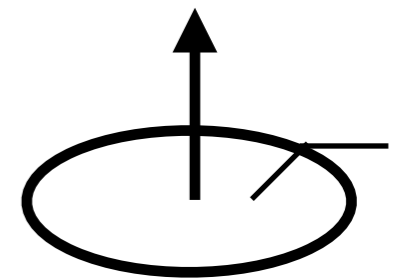
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optical spin density



magnetization density

$\mathbf{E}^* \times \mathbf{E}$



Coupling to Optics?: Faraday Effect

Faraday rotation

optical spin density



$$\bar{U}_{\text{MO}} = \theta_{\text{F}} \sqrt{\frac{\epsilon}{\epsilon_0}} \int d\mathbf{r} \frac{\mathbf{M}(\mathbf{r})}{M_s} \cdot \frac{\epsilon_0}{2i\omega} [\mathbf{E}^*(\mathbf{r}) \times \mathbf{E}(\mathbf{r})]$$

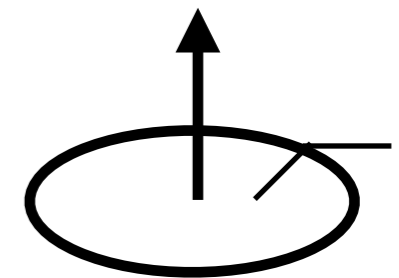


magnetization density

$$\epsilon_{ij}(\mathbf{M}) = \epsilon_0 (\epsilon \delta_{ij} - if \epsilon_{ijk} M_k)$$

broken time-reversal symmetry

$$\mathbf{E}^* \times \mathbf{E}$$



Optomagnonic Hamiltonian

$$\bar{U}_{\text{MO}} = \theta_{\text{F}} \sqrt{\frac{\varepsilon}{\varepsilon_0}} \int d\mathbf{r} \frac{\mathbf{M}(\mathbf{r})}{M_{\text{S}}} \cdot \frac{\varepsilon_0}{2i\omega} [\mathbf{E}^*(\mathbf{r}) \times \mathbf{E}(\mathbf{r})]$$

Quantize:



two-photon process

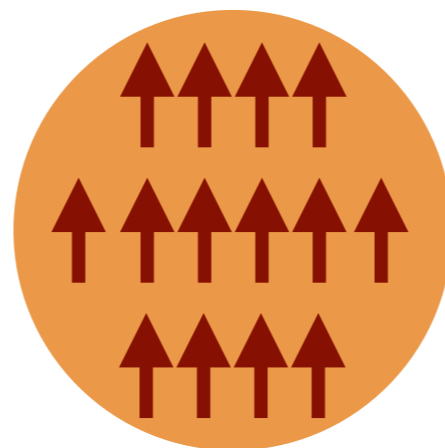
Optomagnonic Hamiltonian

$$\bar{U}_{\text{MO}} = \theta_{\text{F}} \sqrt{\frac{\varepsilon}{\varepsilon_0}} \int d\mathbf{r} \frac{\mathbf{M}(\mathbf{r})}{M_{\text{S}}} \cdot \frac{\varepsilon_0}{2i\omega} [\mathbf{E}^*(\mathbf{r}) \times \mathbf{E}(\mathbf{r})]$$

Quantize:

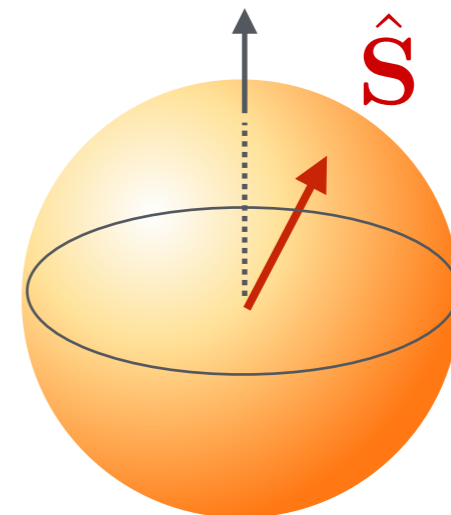


Kittel mode



$$\Omega \propto H$$

Bloch sphere

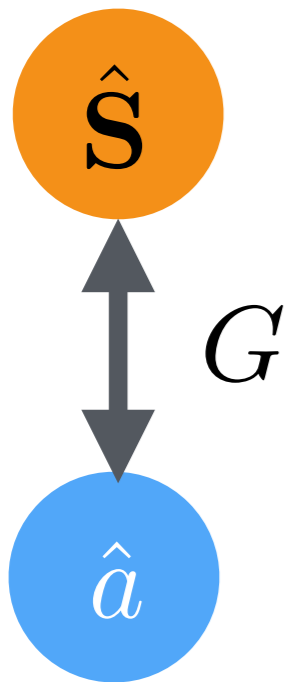


$$\mathbf{M}(\mathbf{r}) = \mathbf{M}$$

Optomagnonic Hamiltonian

Microscopic Hamiltonian

Parametric
coupling



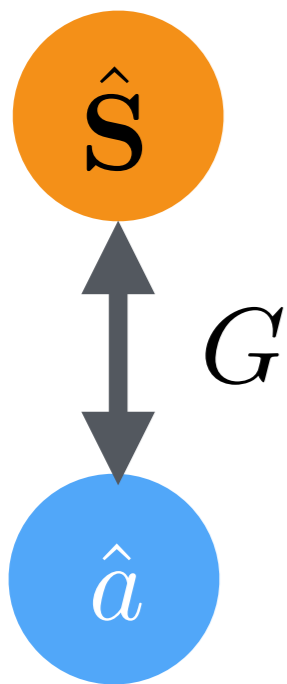
$$\hat{H}_{MO} = \hbar \sum_{j\beta\gamma} \hat{S}_j G_{\beta\gamma}^j \hat{a}_\beta^\dagger \hat{a}_\gamma$$

Optomagnonic Hamiltonian

Microscopic Hamiltonian

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Parametric
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Optomagnonic coupling

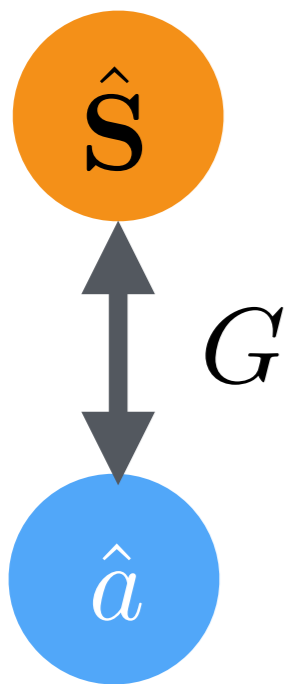
$$G_{\beta\gamma}^j = -i \frac{\theta_F \lambda}{2\pi \hbar S} \frac{\epsilon_0 \epsilon}{2} \epsilon_{jmn} \int d\mathbf{r} E_{\beta m}^*(\mathbf{r}) E_{\gamma n}(\mathbf{r})$$

Optomagnonic Hamiltonian

Microscopic Hamiltonian

$$\hat{H}_{MO} = \hbar \sum_{j\beta\gamma} \hat{S}_j G_{\beta\gamma}^j \hat{a}_\beta^\dagger \hat{a}_\gamma$$

Parametric
coupling



Optomagnonic coupling

$$G_{\beta\gamma}^j = -i \frac{\theta_F \lambda}{2\pi \hbar S} \frac{\epsilon_0 \epsilon}{2} \epsilon_{jmn} \int d\mathbf{r} E_{\beta m}^*(\mathbf{r}) E_{\gamma n}(\mathbf{r})$$

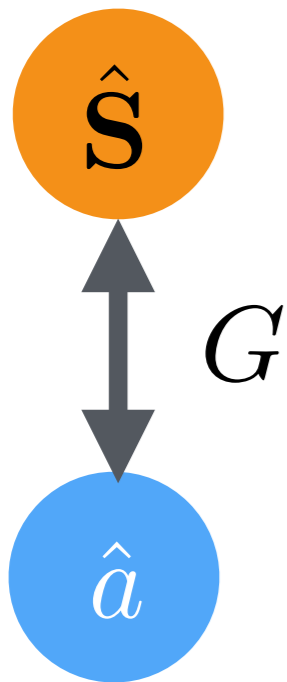
overlap electric field
mode functions

Optomagnonic Hamiltonian

Microscopic Hamiltonian

$$\hat{H}_{MO} = \hbar \sum_{j\beta\gamma} \hat{S}_j G_{\beta\gamma}^j \hat{a}_\beta^\dagger \hat{a}_\gamma$$

Parametric
coupling



Optomagnonic coupling

$$G_{\beta\gamma}^j = \left(i \frac{\theta_F \lambda}{2\pi \hbar S} \frac{\epsilon_0 \epsilon}{2} \epsilon_{jmn} \int d\mathbf{r} E_{\beta m}^*(\mathbf{r}) E_{\gamma n}(\mathbf{r}) \right)$$

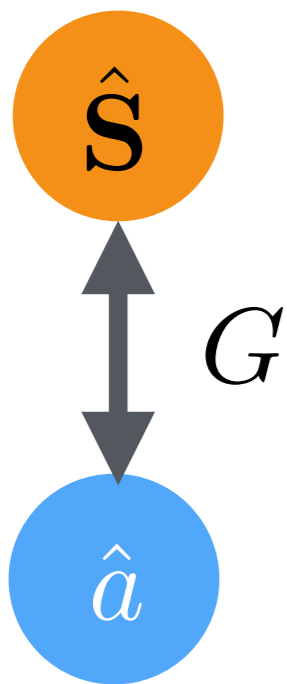
Faraday rotation

Optomagnonic Hamiltonian

Microscopic Hamiltonian

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Parametric
coupling

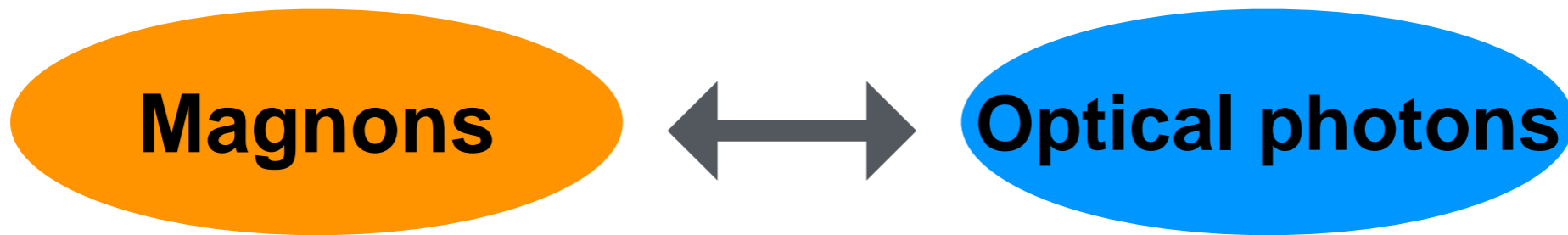


Optomagnonic coupling

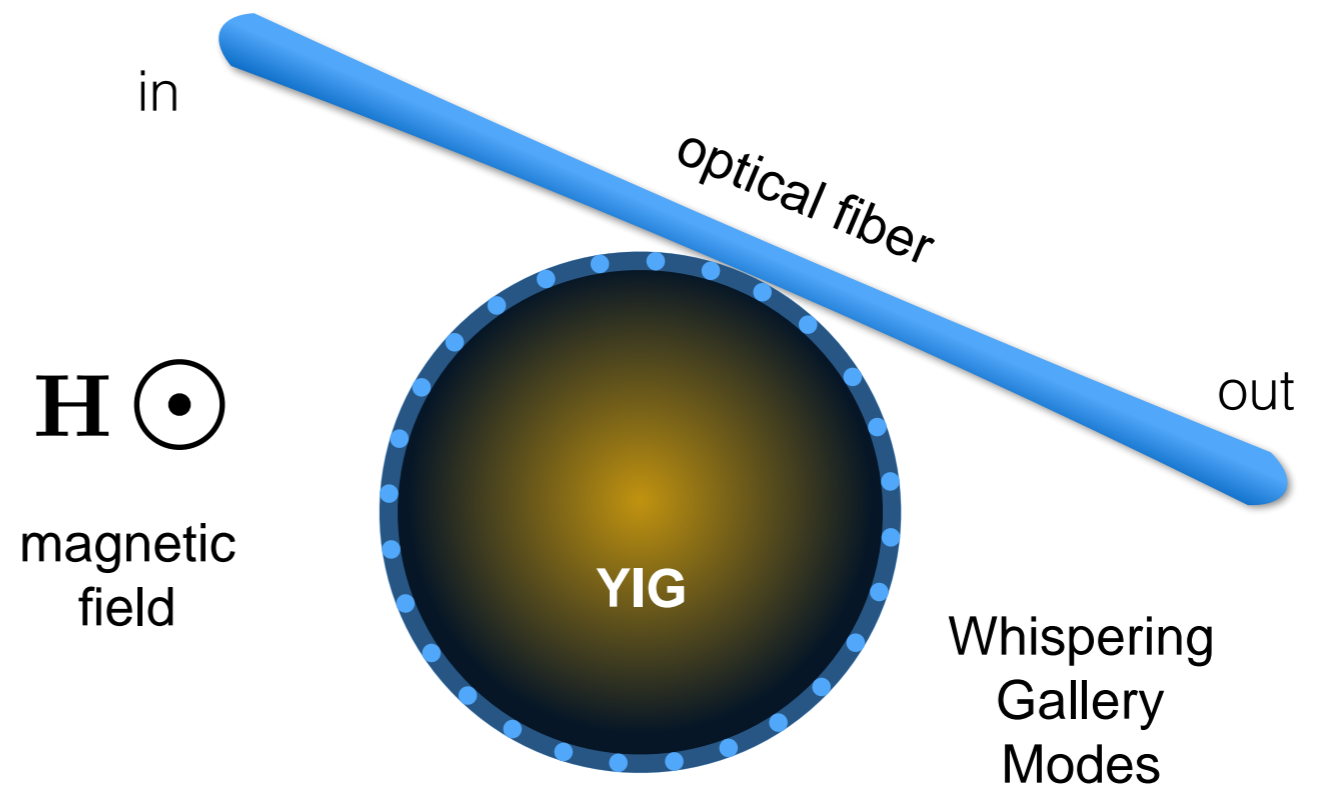
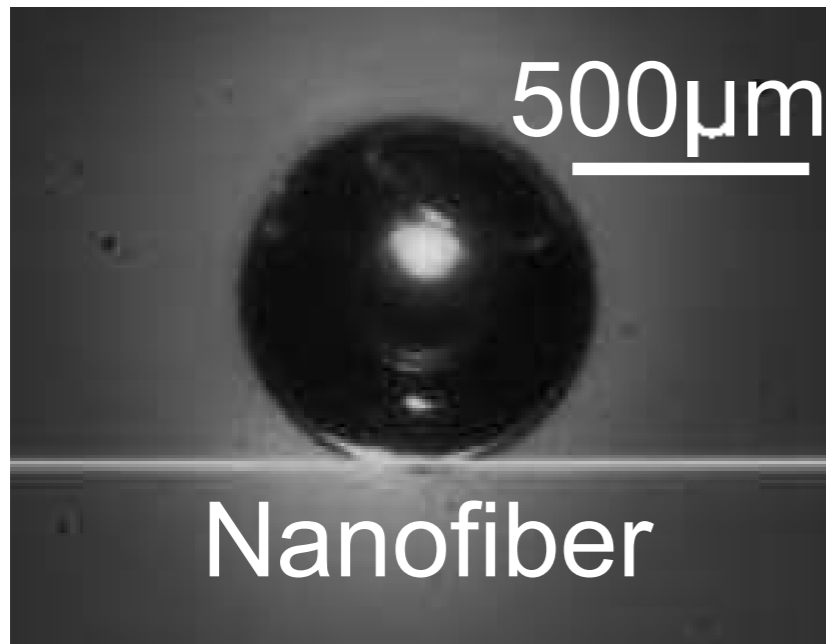
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number of spins

Cavity Optomagnonics



Coupling demonstrated in 2016



A cavity enhances the effect

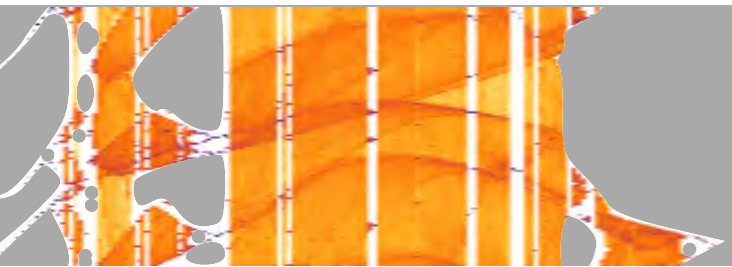
- Osada et. al PRL 116, 223601 (Nakamura's group, Tokyo)
- Haigh et. al PRL 117, 133602 (Cambridge Univ / Hitachi)
- Zhang et. al PRL 117, 123605 (Hong Tang's group, Yale)



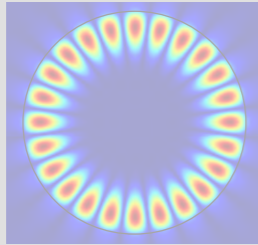
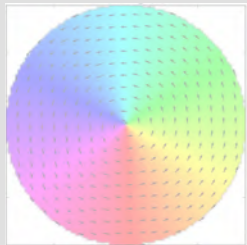
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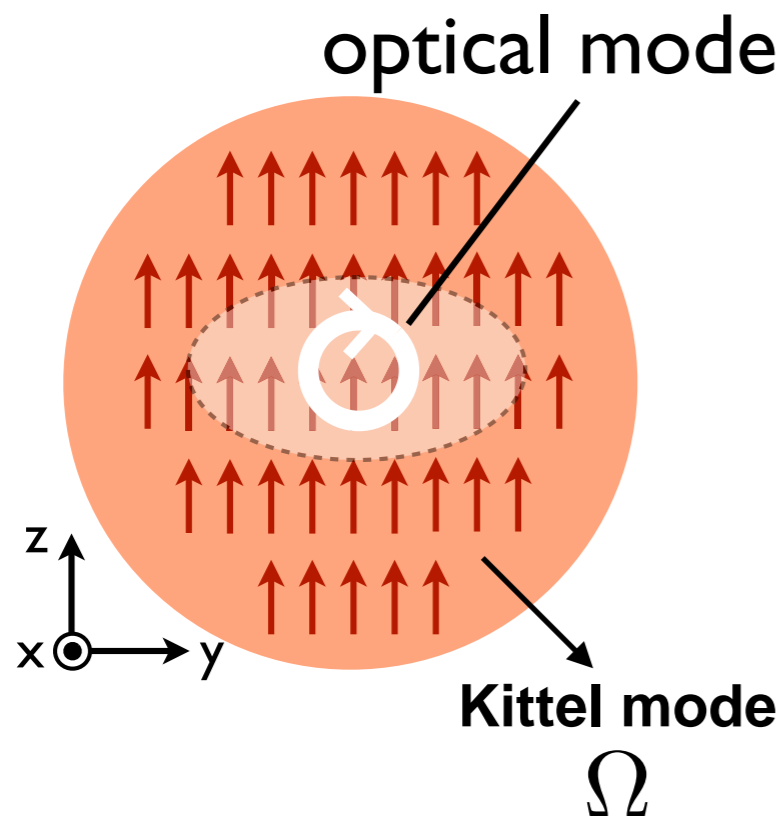
Summary

Cavity Optomagnonics: one optical mode

$$H = -\hbar\Delta\hat{a}^\dagger\hat{a} - \hbar\Omega\hat{S}_z + \hbar G\hat{S}_x\hat{a}^\dagger\hat{a}$$

driving laser detuning

$$\Delta = \omega_{las} - \omega_{cav}$$

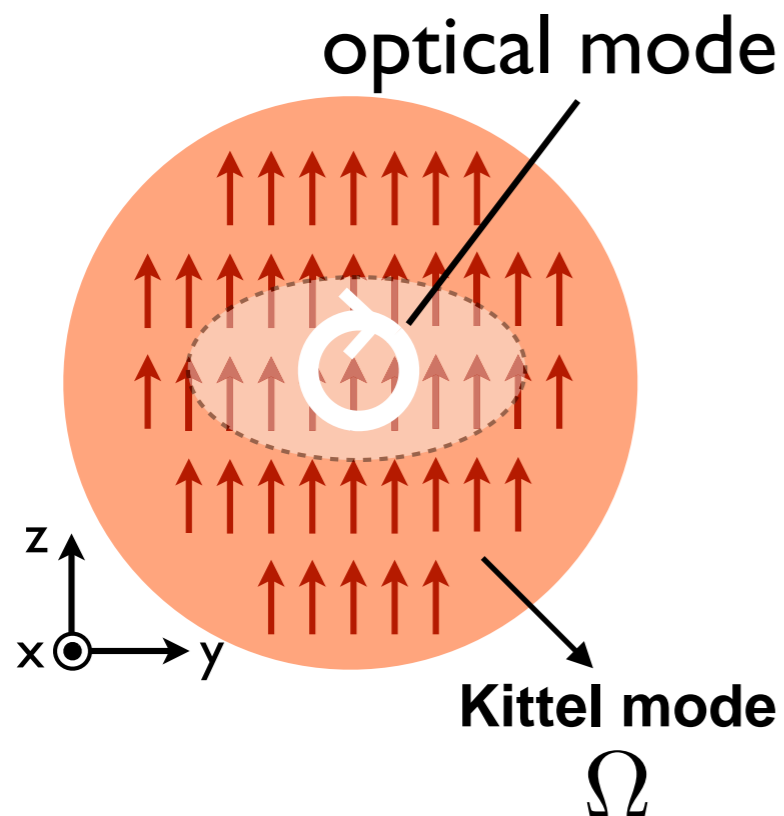


Cavity Optomagnonics: one optical mode

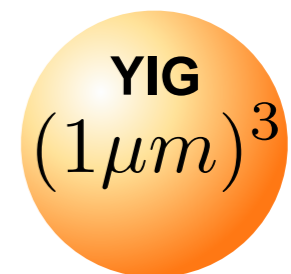
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$$G = \frac{1}{S} \frac{c\theta_F}{4\sqrt{\epsilon}} \approx 1\text{Hz}$$

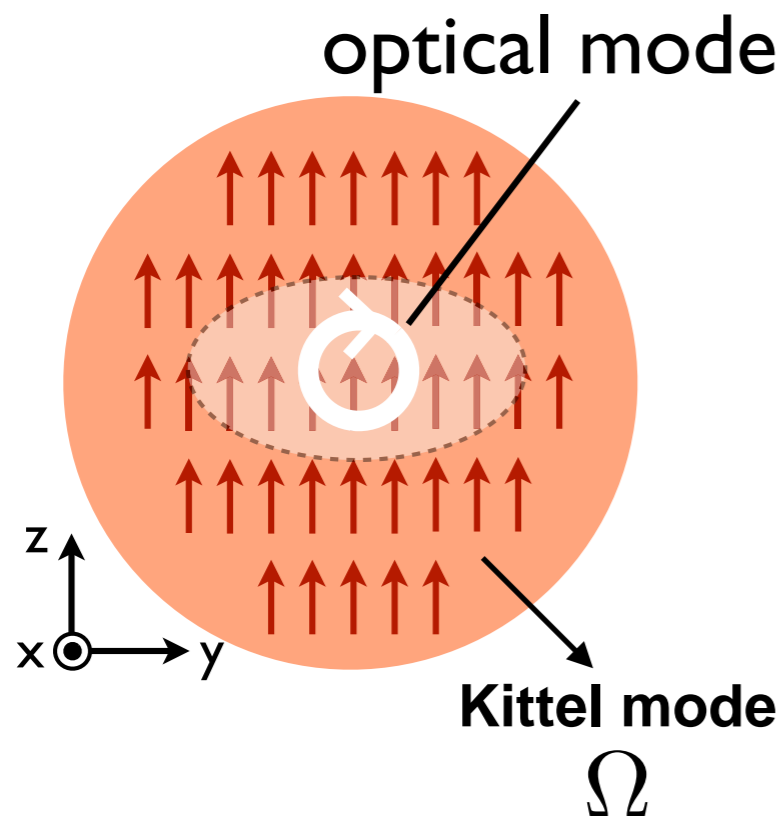


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Optical magnetic field density

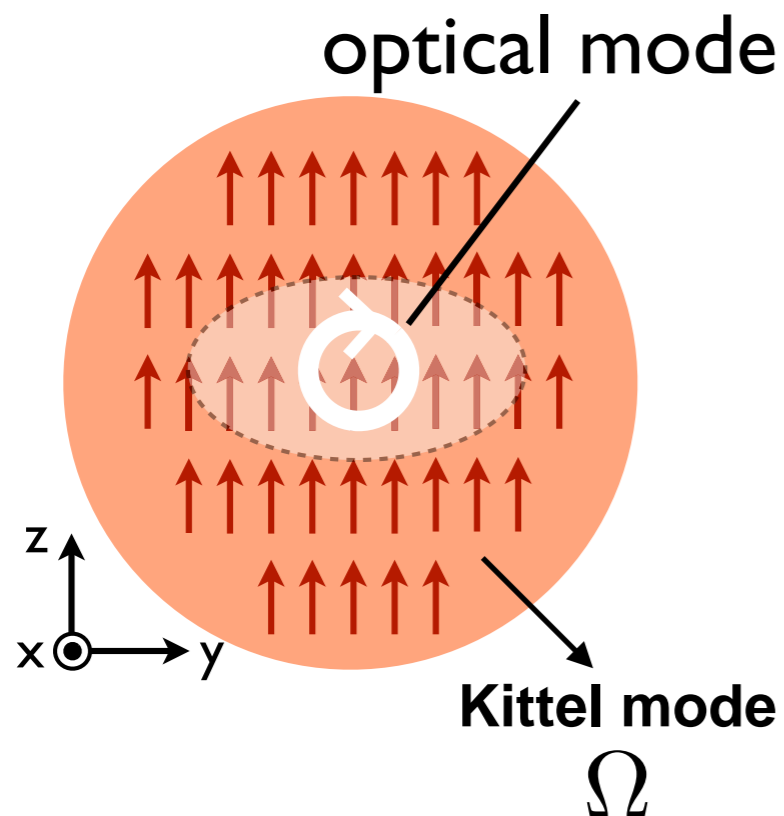
$$b_{\text{opt}} \sim \frac{10^{-11}\text{T}}{\text{photon}/(\mu\text{m})^3}$$

Cavity Optomagnonics: one optical mode

$$H = -\hbar\Delta\hat{a}^\dagger\hat{a} - \hbar\Omega\hat{S}_z + \hbar G\hat{S}_x\hat{a}^\dagger\hat{a}$$

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Optical magnetic field density

$$b_{\text{opt}} \sim \frac{10^{-11}\text{T}}{\text{photon}/(\mu\text{m})^3}$$

Enhanced by # photons in the cavity!

Cavity Optomagnonics: one optical mode

Classical Equation of Motion

Cavity decay rate

initial light amplitude

$$\dot{a} = -i(GS_x - \Delta)a - \frac{\kappa}{2}(a - \alpha_{\max})$$
$$\dot{\mathbf{S}} = (Ga^*a \mathbf{e}_x - \Omega \mathbf{e}_z) \times \mathbf{S} + \frac{\eta_G}{S}(\dot{\mathbf{S}} \times \mathbf{S})$$

Effective Equation of Motion for the Spin

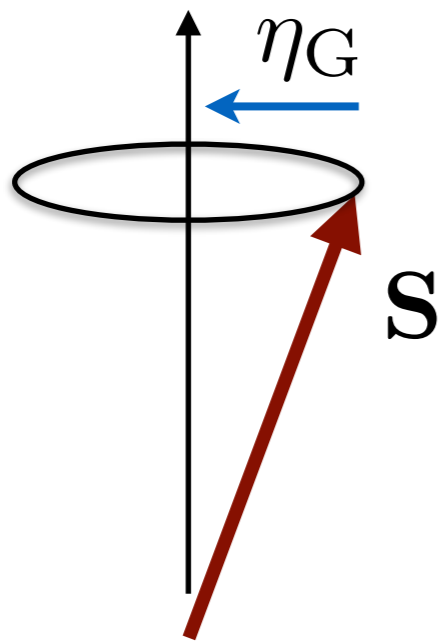
Fast cavity limit: integrate out the light field

$$\dot{\mathbf{S}} = \mathbf{B}_{\text{eff}} \times \mathbf{S} + \frac{\eta_{\text{opt}}}{S} \left(\dot{S}_x \mathbf{e}_x \times \mathbf{S} \right)$$

Effective Landau-Lifshitz-Gilbert equation of motion

Landau-Lifschitz-Gilbert Equation

Dynamics of the macrospin



$$\Omega \propto H$$

precession frequency

$$\dot{\mathbf{S}} = -\Omega \mathbf{e}_z \times \mathbf{S} + \frac{\eta_G}{S} \left(\dot{\mathbf{S}} \times \mathbf{S} \right)$$

↓

phenomenological damping term
(Gilbert damping)

Effective Equation of Motion for the Spin

Fast cavity limit: integrate out the light field

$$\dot{\mathbf{S}} = \mathbf{B}_{\text{eff}} \times \mathbf{S} + \frac{\eta_{\text{opt}}}{S} \left(\dot{S}_x \mathbf{e}_x \times \mathbf{S} \right)$$

Effective Landau-Lifshitz-Gilbert equation of motion

Optically induced	magnetic field	\mathbf{B}_{eff}
	dissipation	η_{opt}

non-linear functions of \mathbf{S}

Fast Cavity Limit

$$\dot{\mathbf{S}} = \mathbf{B}_{\text{eff}} \times \mathbf{S} + \frac{\eta_{\text{opt}}}{S} \left(\dot{S}_x \mathbf{e}_x \times \mathbf{S} \right)$$

effective field

$$\mathbf{B}_{\text{eff}} = -\Omega \mathbf{e}_z + \mathbf{B}_{\text{opt}}$$

$$\mathbf{B}_{\text{opt}} = \frac{G}{\left[\left(\frac{\kappa}{2} \right)^2 + (\Delta - GS_x)^2 \right]} \left(\frac{\kappa}{2} \alpha_{\text{max}} \right)^2 \mathbf{e}_x$$

**damping
can change sign**

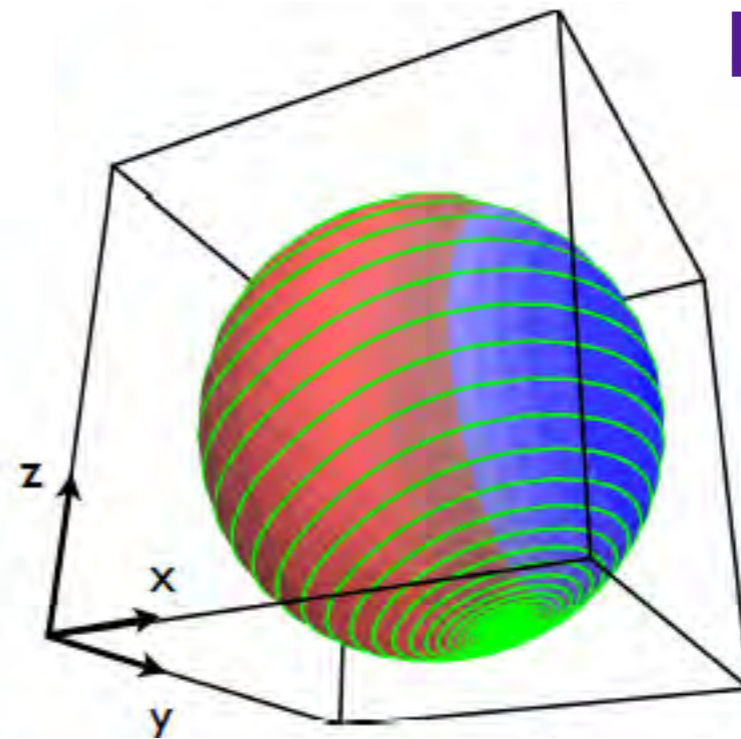
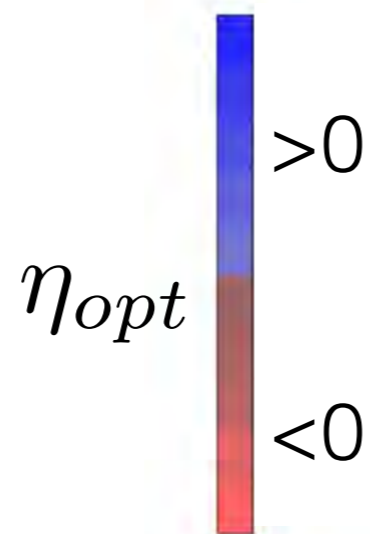
$$\eta_{\text{opt}} = -2G\kappa S |\mathbf{B}_{\text{opt}}| \frac{(\Delta - GS_x)}{\left[\left(\frac{\kappa}{2} \right)^2 + (\Delta - GS_x)^2 \right]^2}$$

tunable by the external laser drive

Spin Dynamics: Fast Cavity Limit

Blue detuned case:

dissipation
changes sign

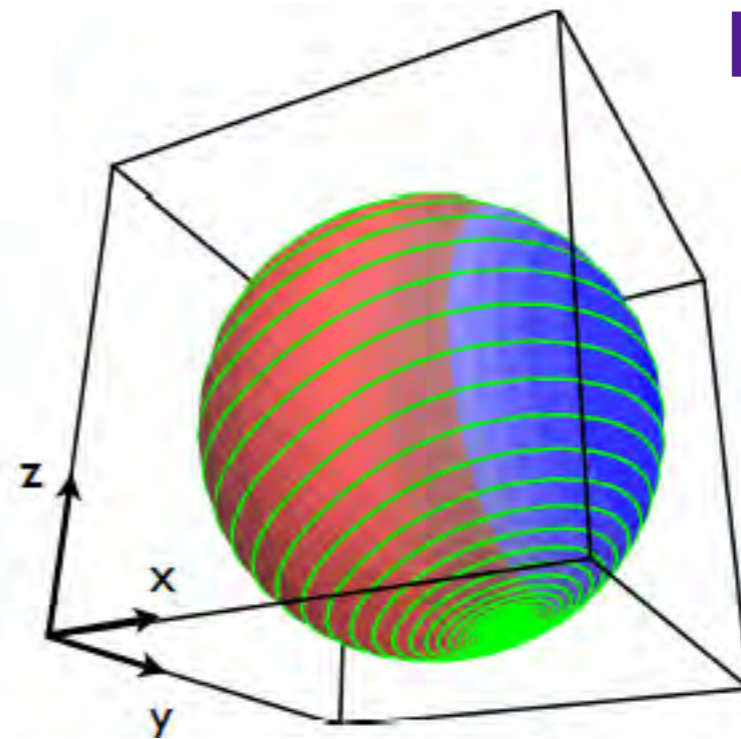
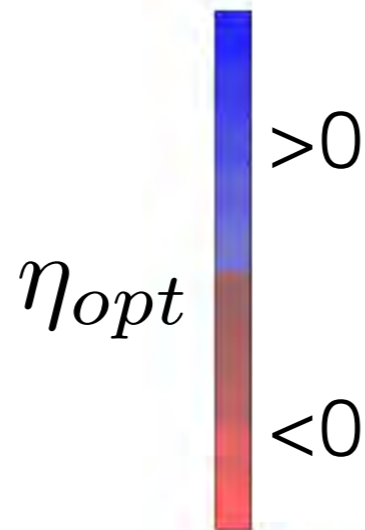


**Light induced
magnetic
switching**

Spin Dynamics: Fast Cavity Limit

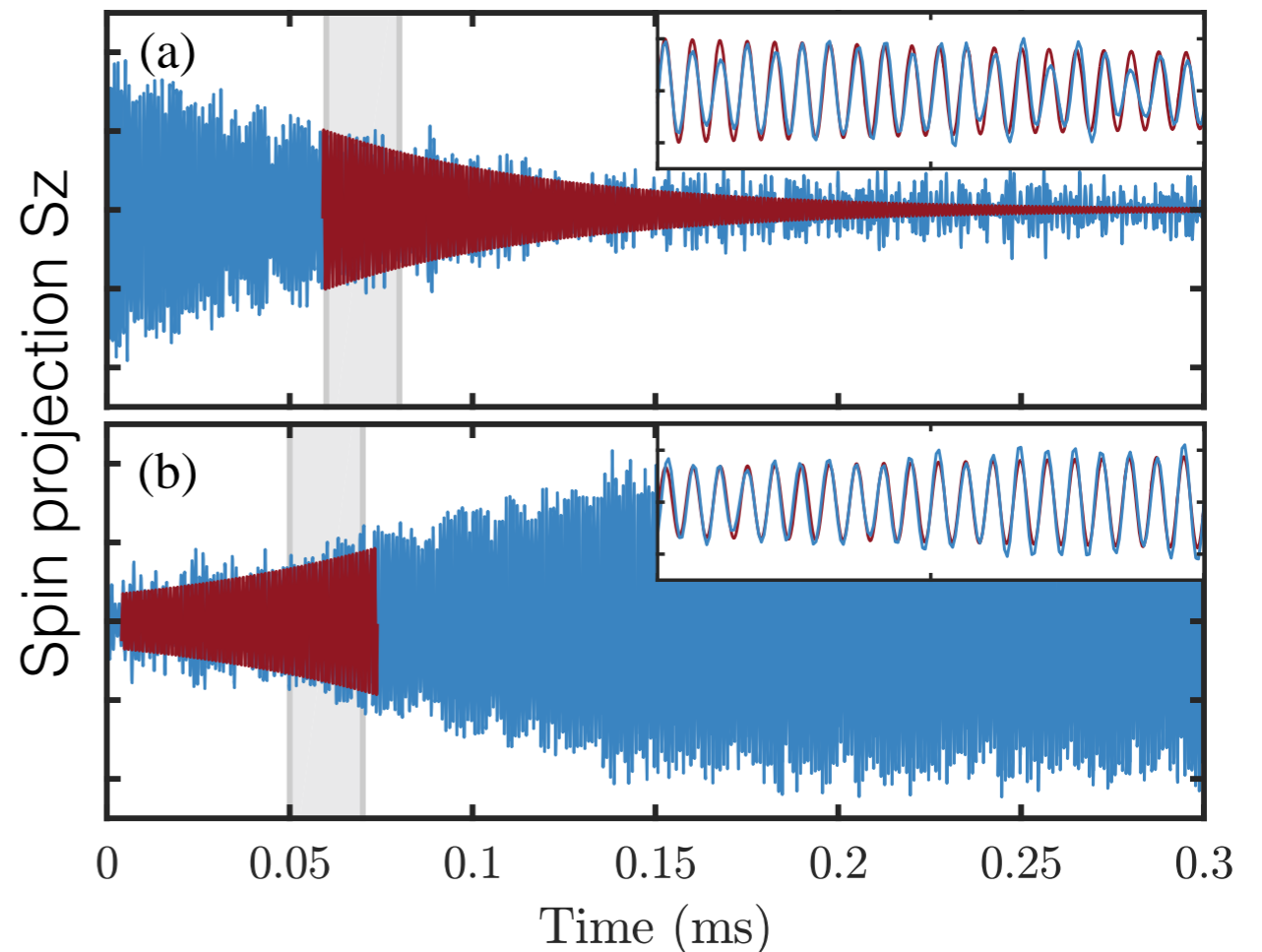
Blue detuned case:

dissipation
changes sign

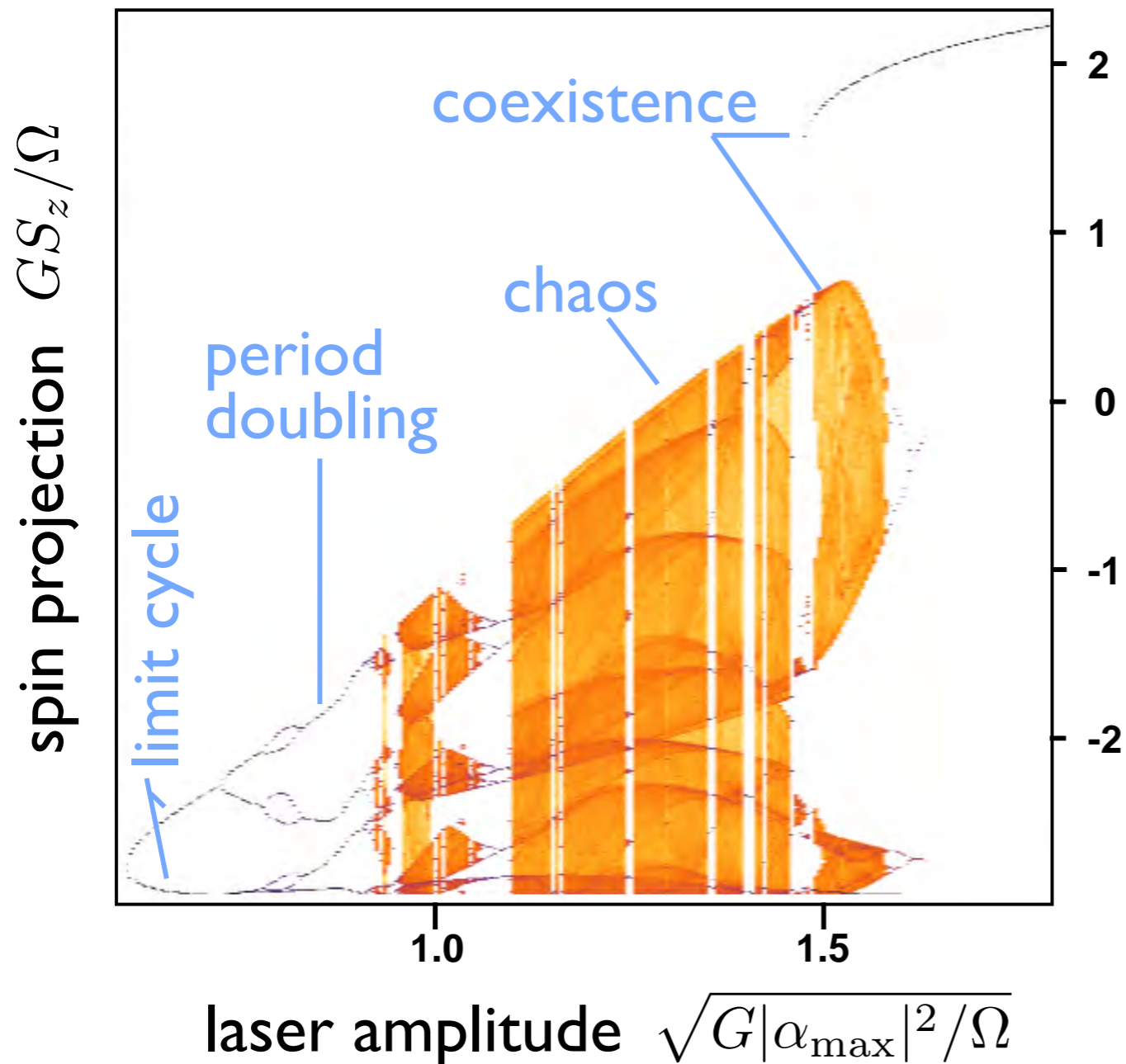


Light induced
magnetic
switching

See experimental realization
with cold atoms,
Dan M. Stamper-Kurn Group
Phys. Rev. Lett. **118**, 063604
(2017)



Full Nonlinear Dynamics



» Coherent optical control

» Magnetic switching

» Self-sustained oscillations

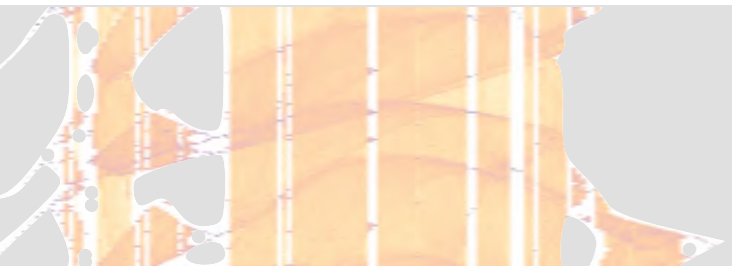
» Optically induced route to chaos



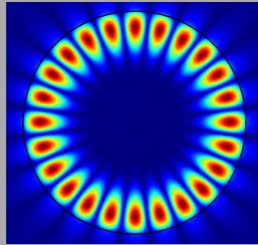
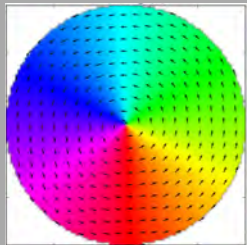
Introduction and motivation



Optomagnonic Hamiltonian



Optically induced spin dynamics



Magnetic textures: vortex in a disk



Summary

But...

Problem

the state of the art optomagnonic coupling is very small

Coupling per photon $g_0 \approx 60\text{Hz}$ Cooperativity $\mathcal{C} \approx 10^{-7}$

(for small oscillations: spin \longrightarrow harmonic oscillator)

$$\hbar G \hat{S}_x \hat{a}^\dagger \hat{a} \approx \underbrace{\hbar G \sqrt{S/2}}_{g_0} \hat{a}^\dagger \hat{a} (\hat{b} + \hat{b}^\dagger)$$

But...

Problem

the state of the art optomagnonic coupling is too small

Coupling per photon $g_0 \approx 60\text{Hz}$ Cooperativity $\mathcal{C} \approx 10^{-7}$



Some solutions

smaller systems

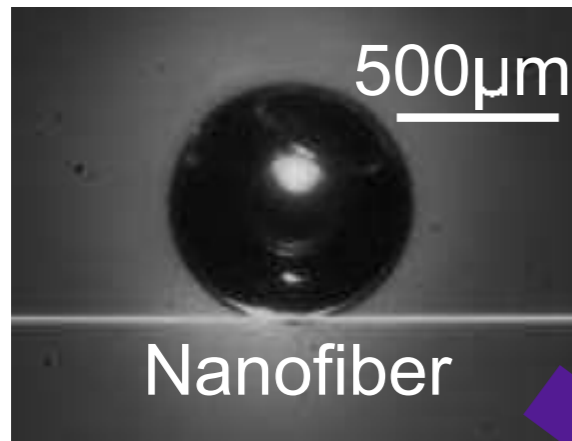
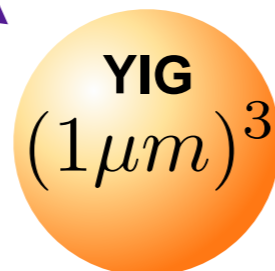
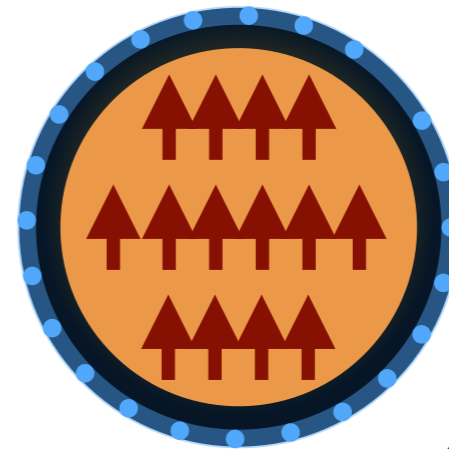


Fig: Osada et. al.
PRL 116, 223601



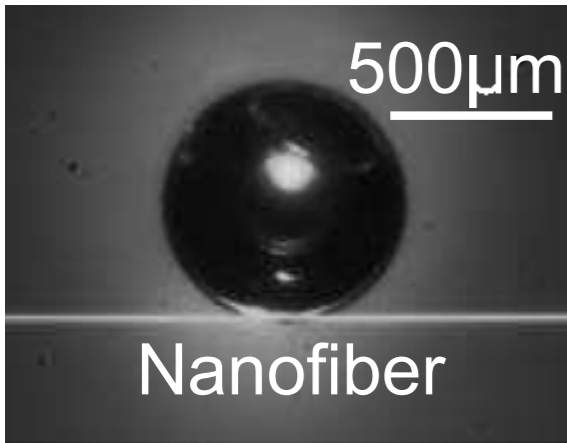
better overlap of modes



?

A purple arrow points from the circular diagram to a large black question mark.

Optomagnonics beyond the Kittel mode



Optomagnonic coupling demonstrated

- Non-homogeneous magnon mode
- Homogeneous ground state

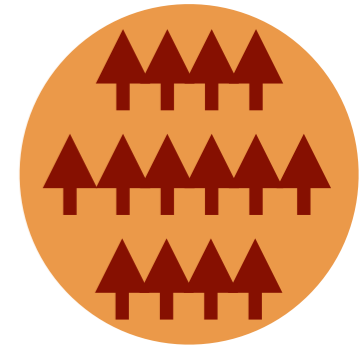
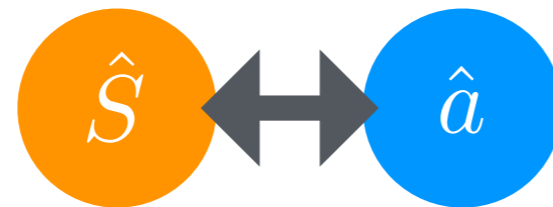
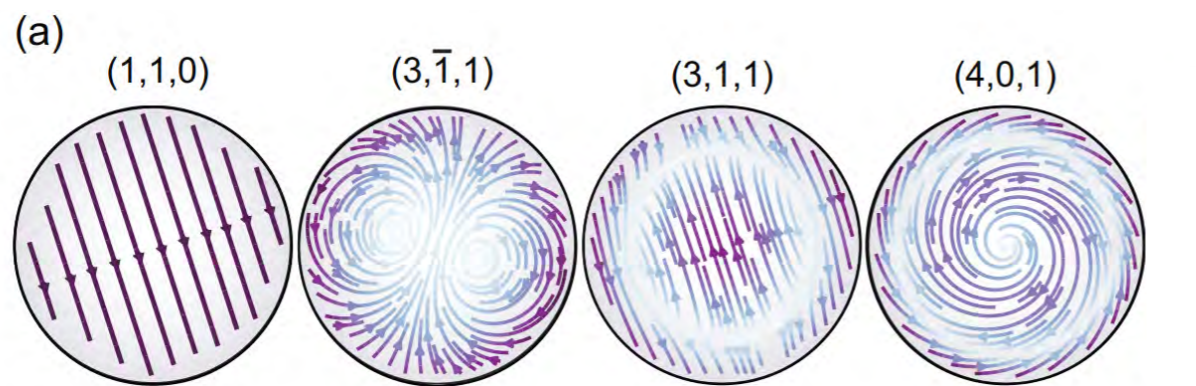


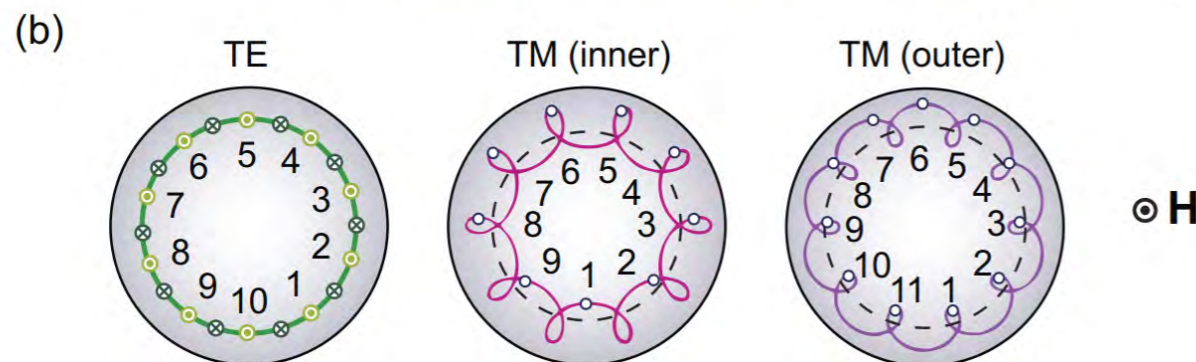
Fig: Osada et. al.
PRL 116, 223601



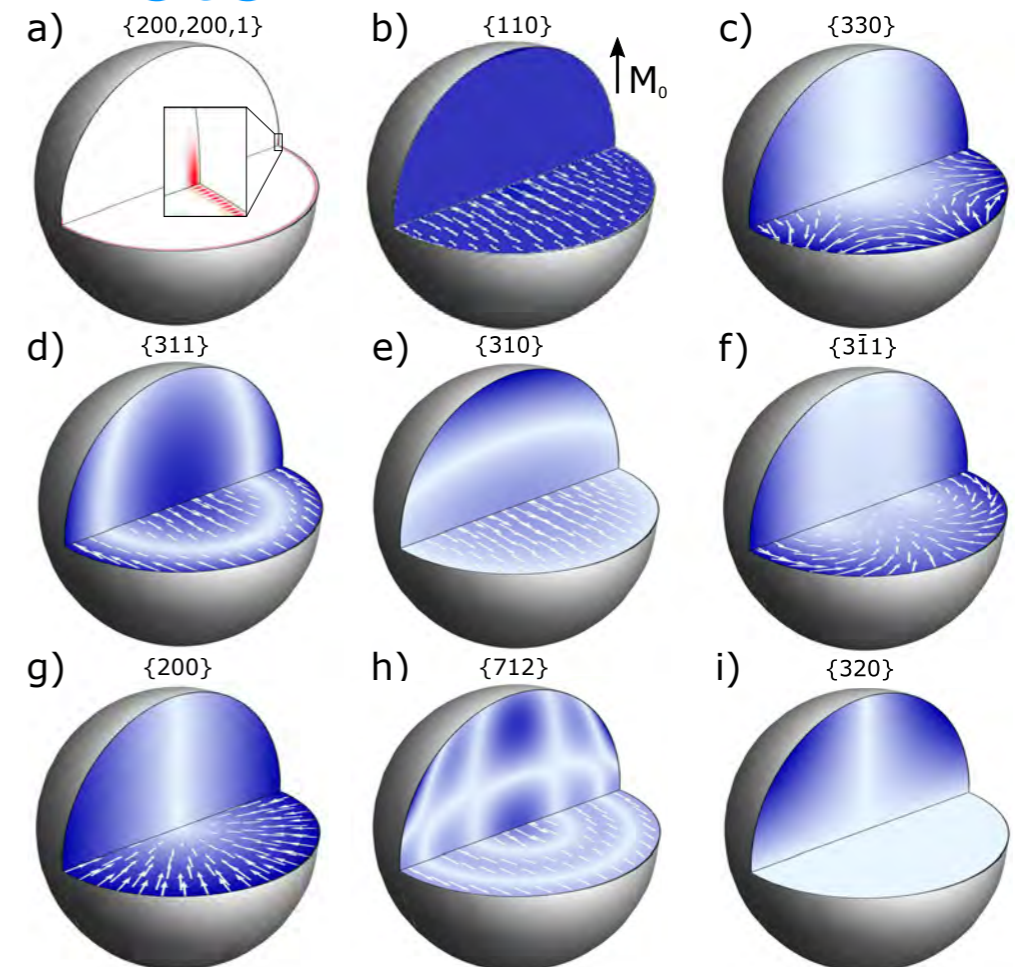
Magnon



Photon



Photon



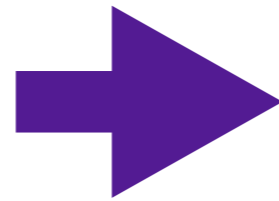
Magnon

A. Osada et al, PRL 120, 123602 (2018)

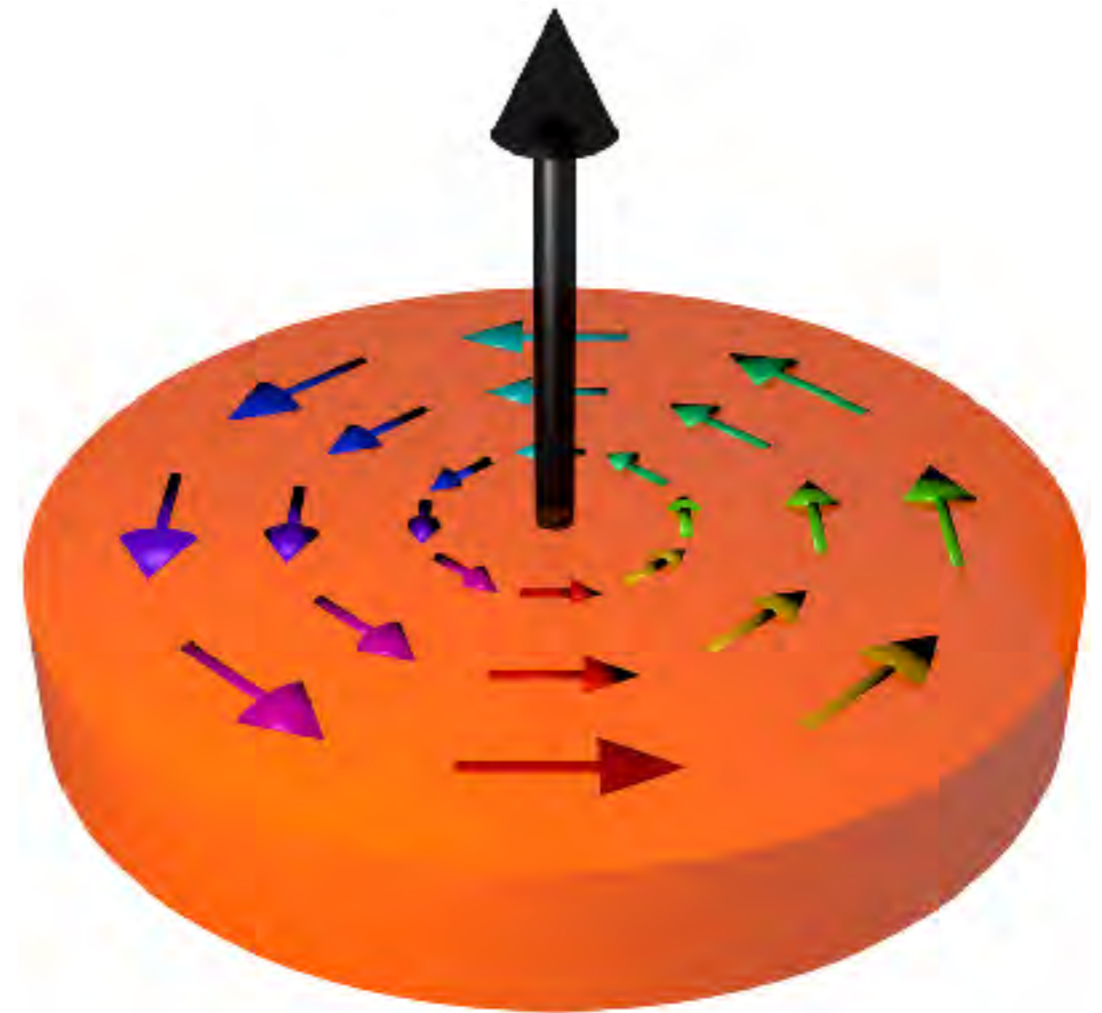
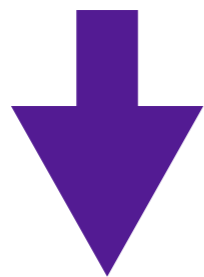
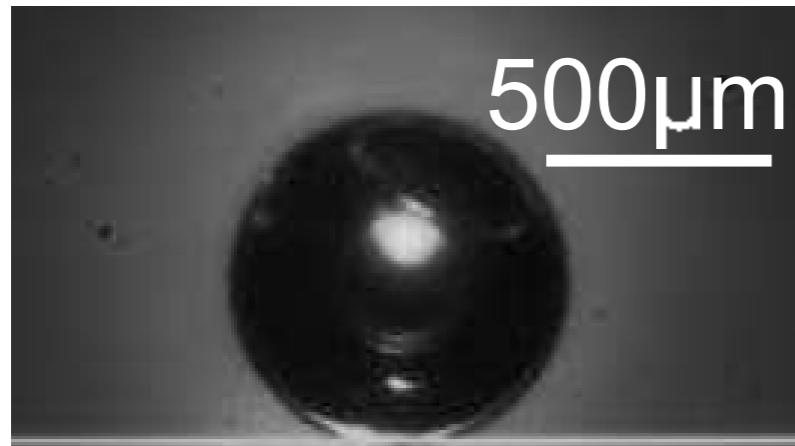
J.A. Haigh et al, Arxiv:1804.00965v1 (2018)

Magnetic Textures

smaller systems

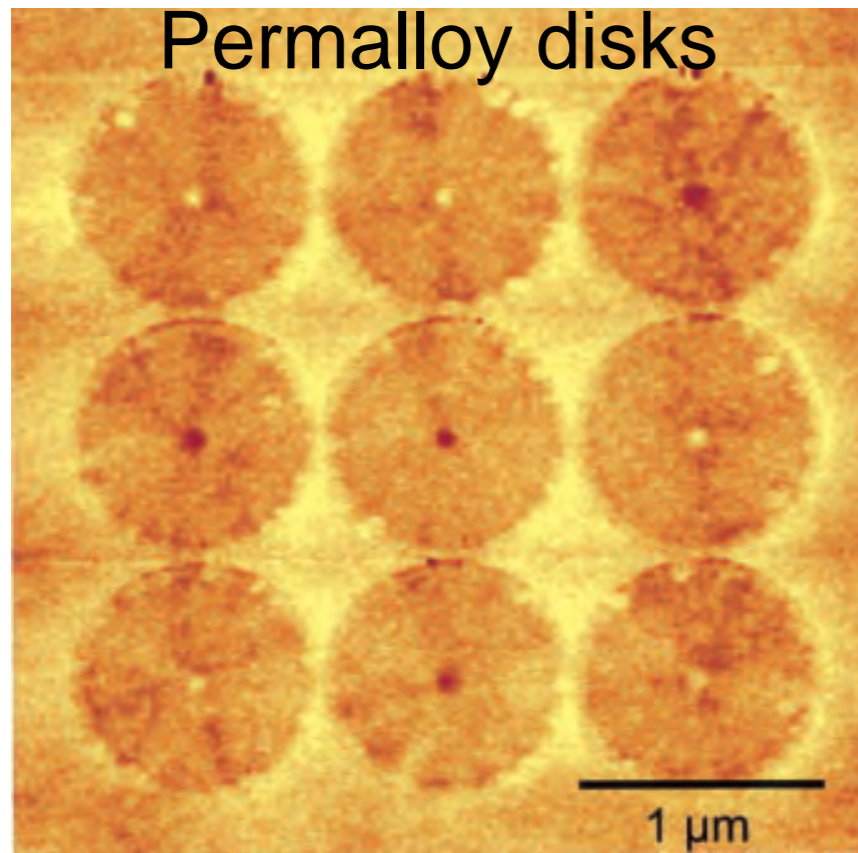


Magnetic textures

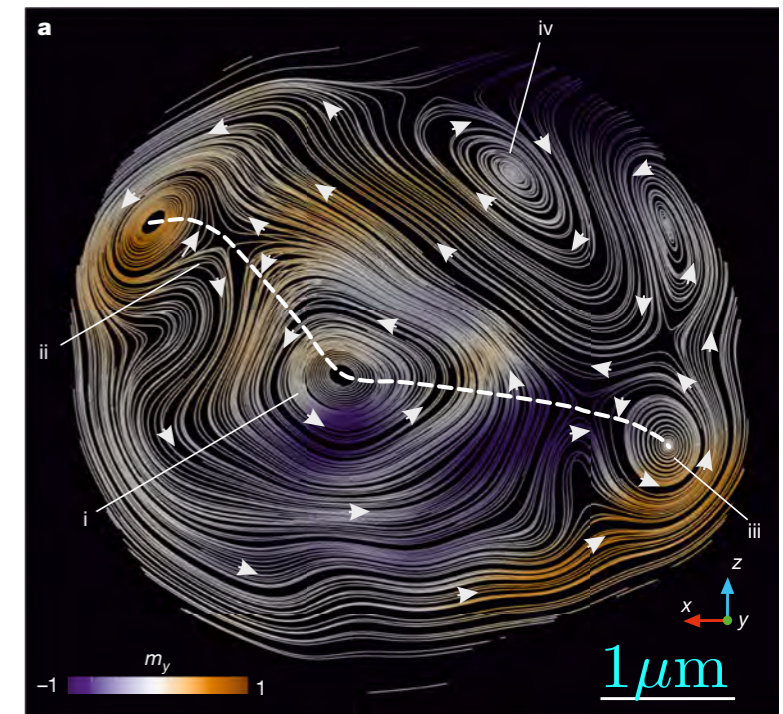
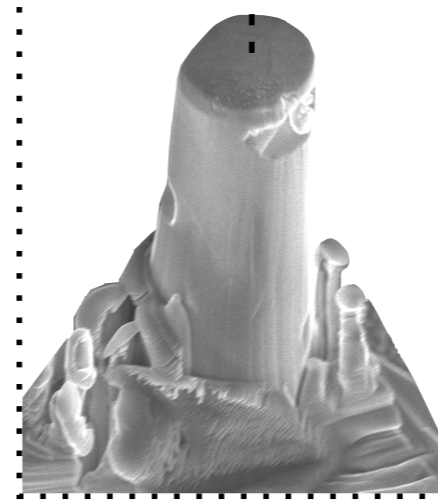


Vortex in a micro disk

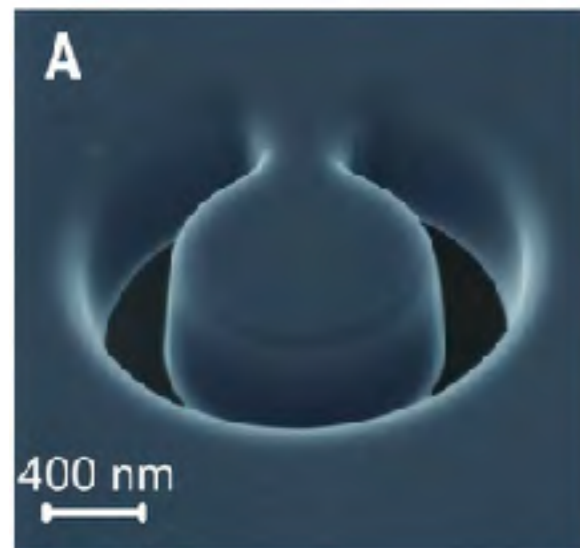
Magnetic Textures: Vortex in Microdisks



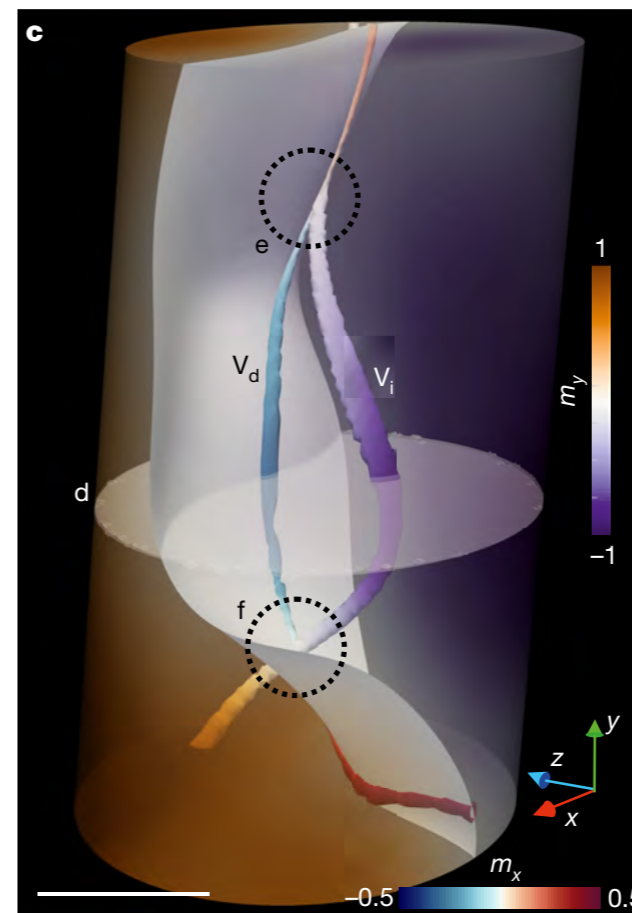
T. Shinjo et al, Science 289, 930 (2000)



YIG disks



Losby et al, Science 350, 798 (2015)



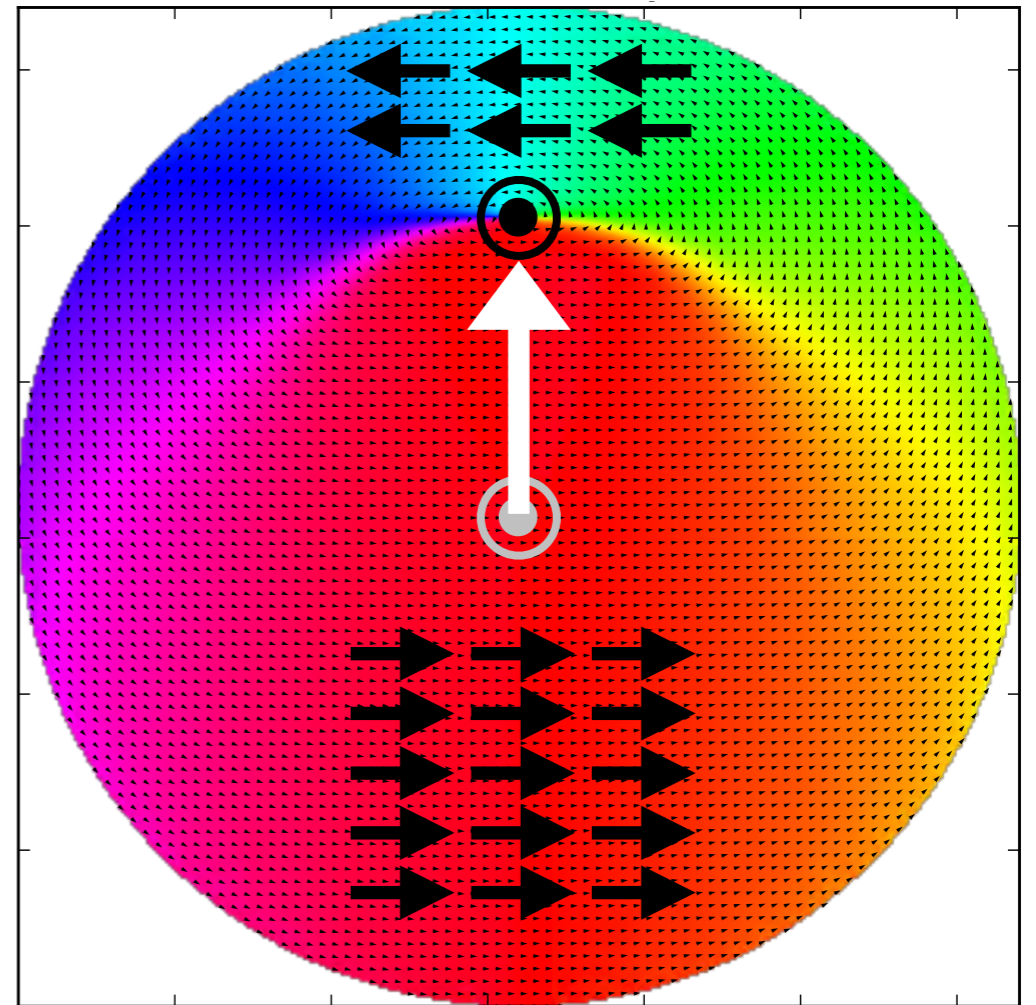
Cobalt Gadolinium pillars

C. Donally et al,
Nature 547
328 (2017)

Vortex

- **Position tunable by a magnetic field**

View from above

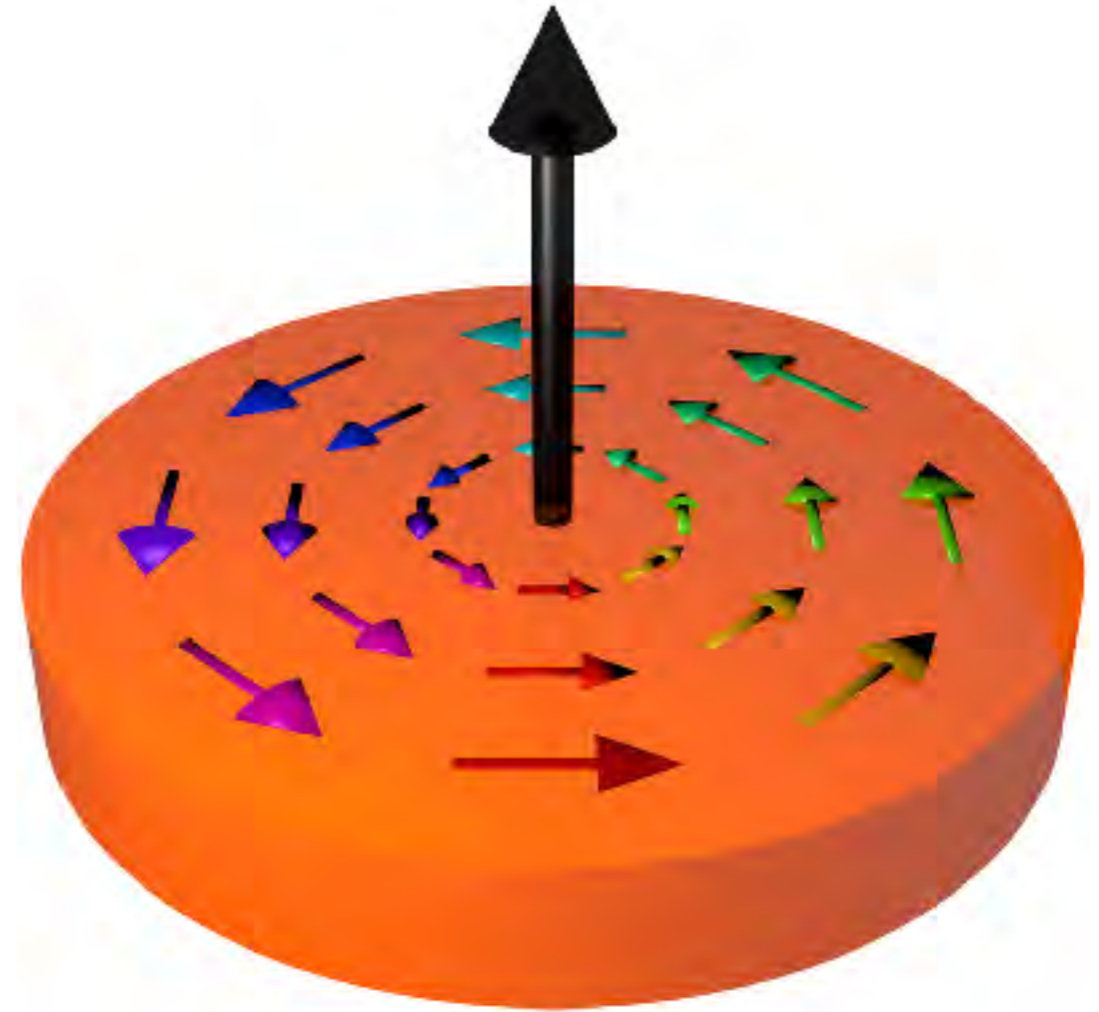


\mathbf{B}_{ext}



Vortex

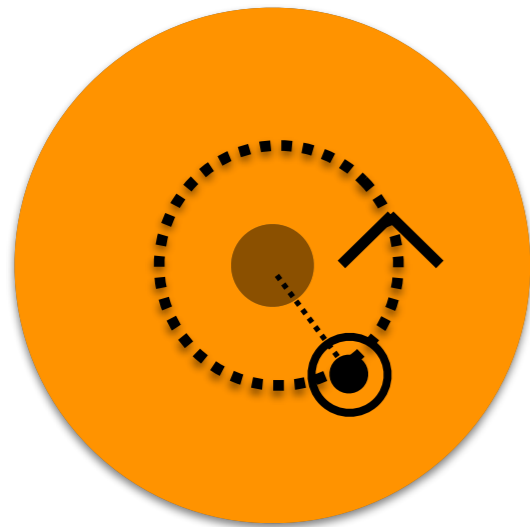
- **Supports localized magnon modes**



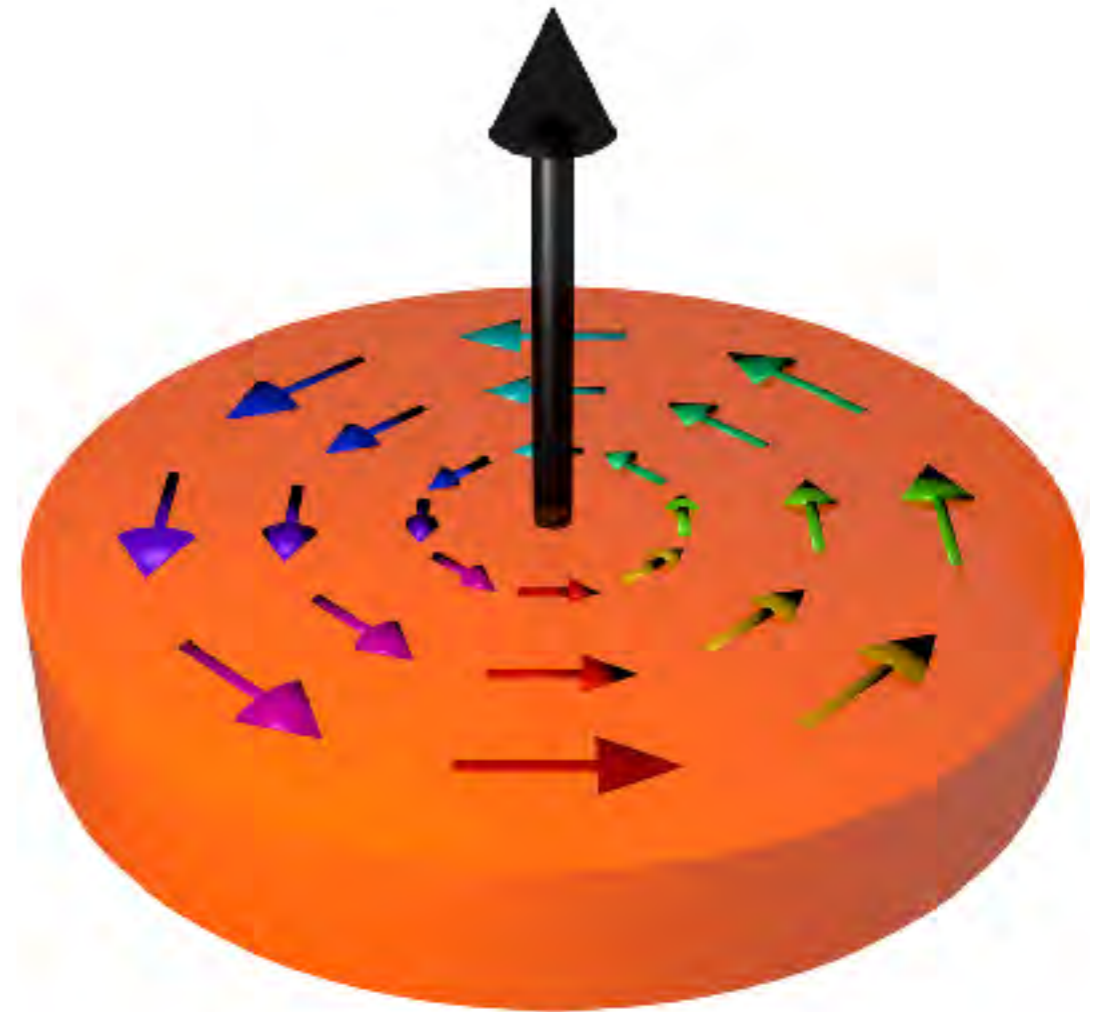
Vortex

- Supports localized magnon modes

Gyrotropic mode

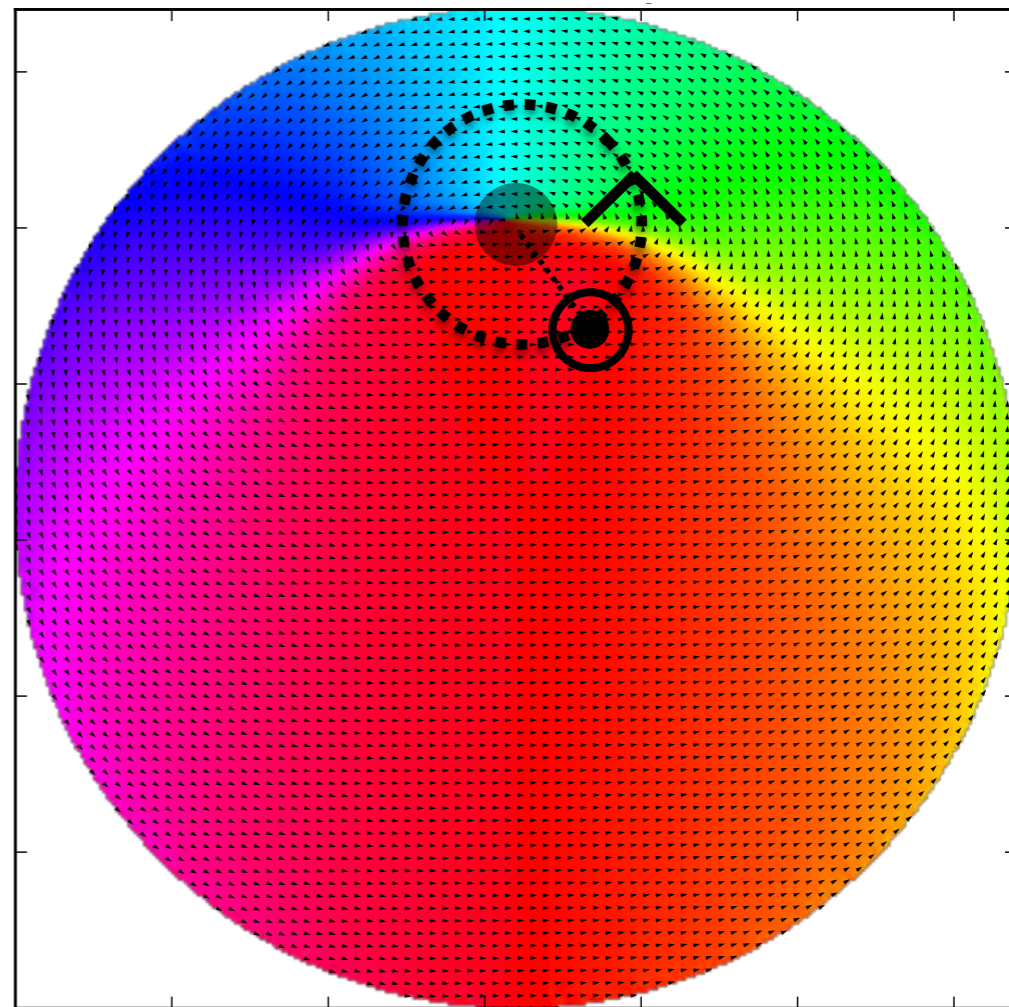
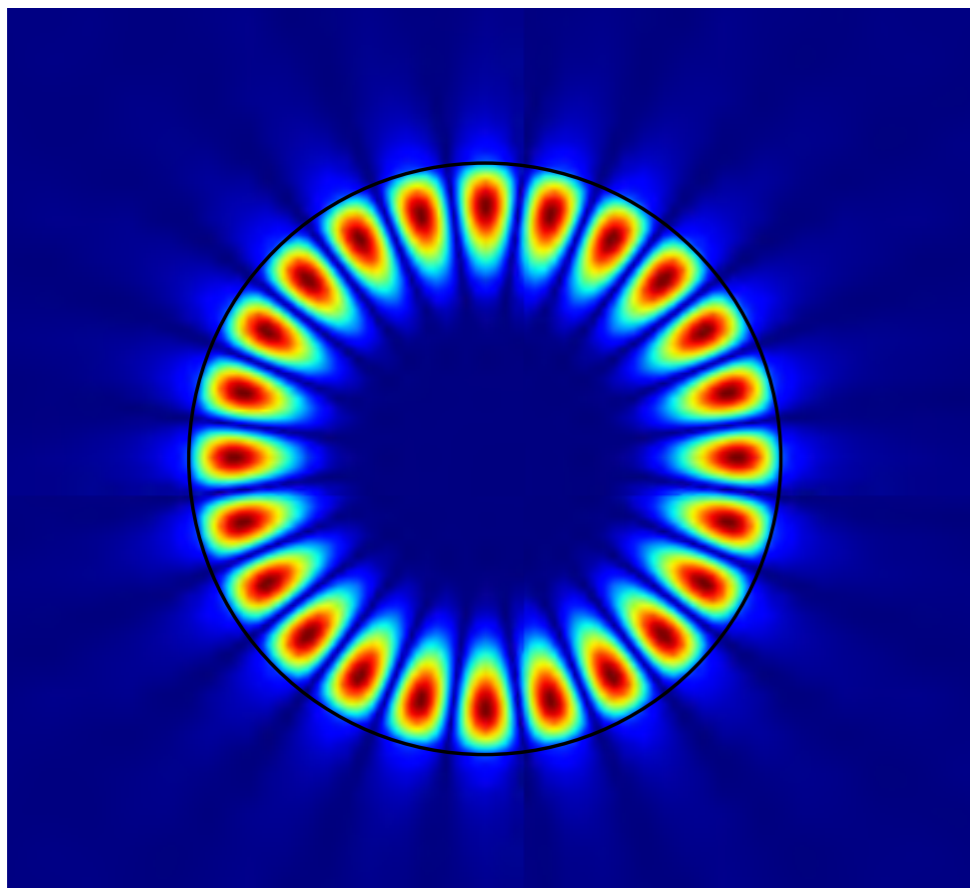


- Sub -GHz
- Gapped



Vortex

Coupling to optical
Whispering Gallery Modes?

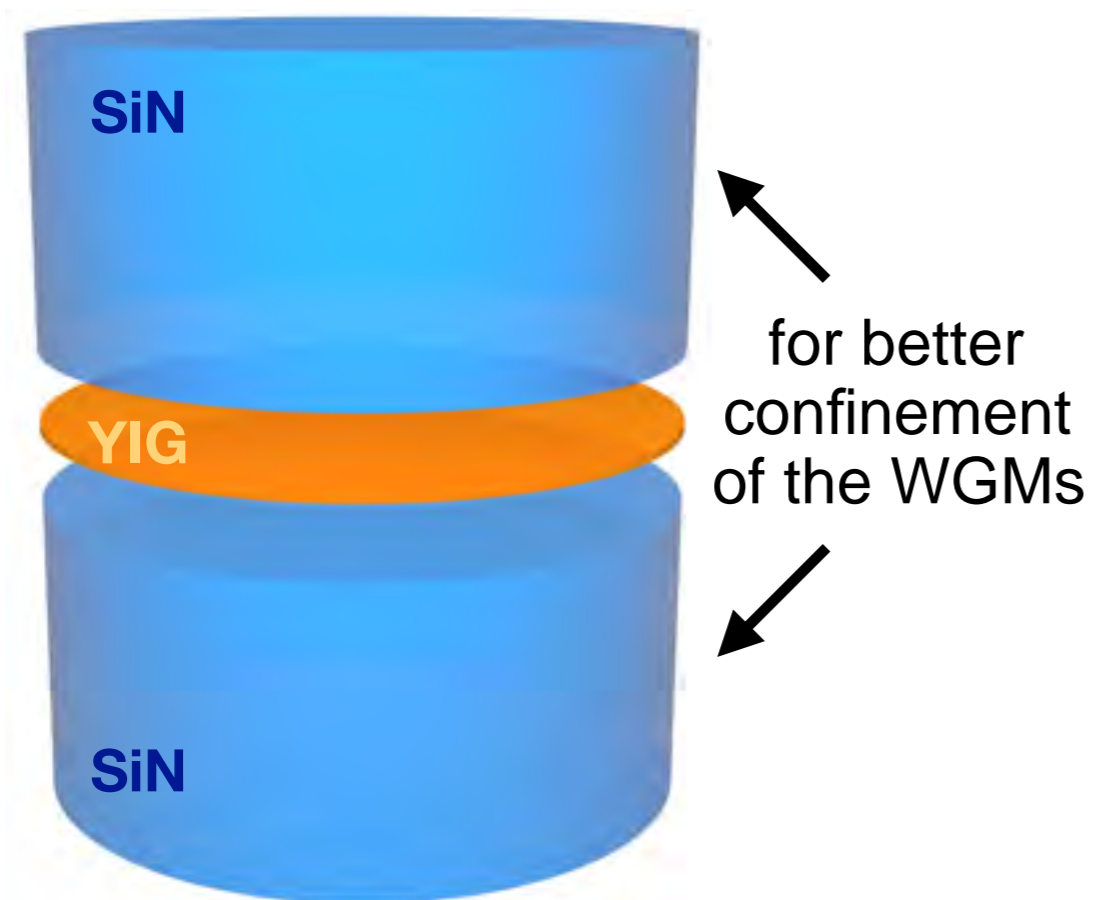


\mathbf{B}_{ext}



Setup: two cases

Thin Disk Heterostructure

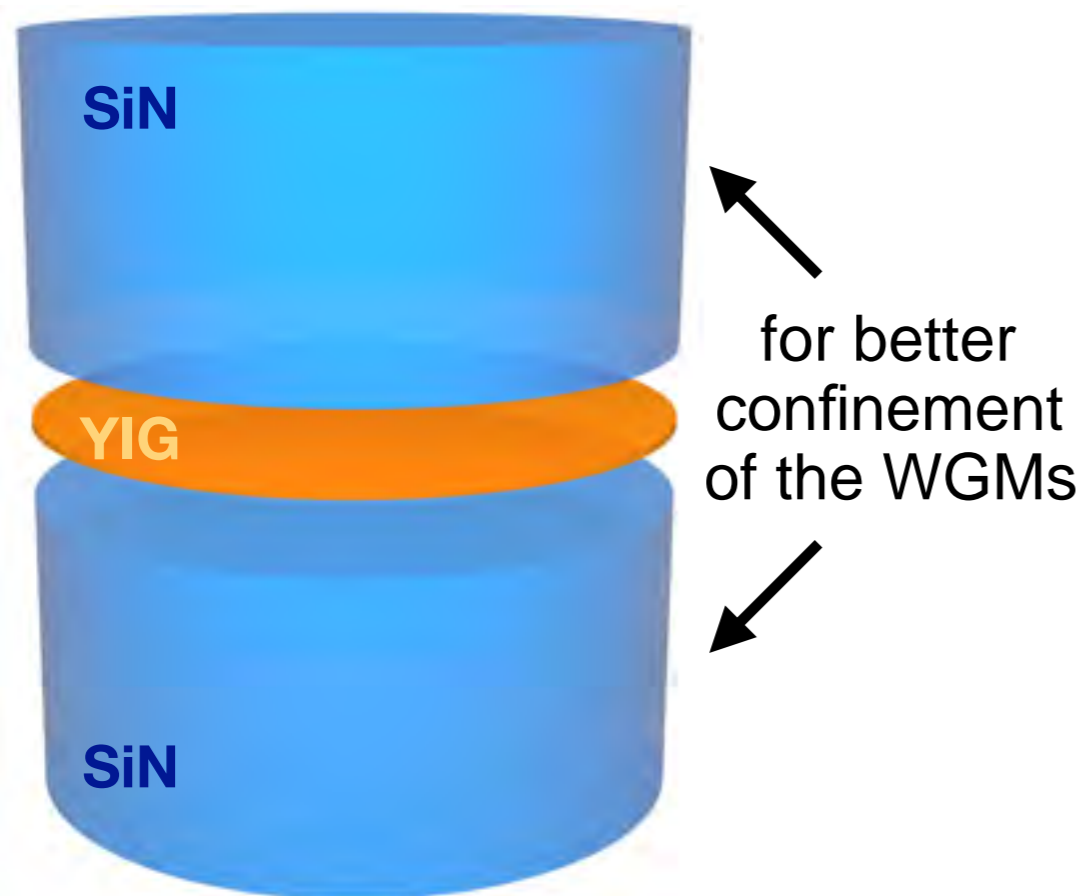


$$h_{\text{YIG}} \sim l_{ex} \sim 10\text{nm}$$

- The magnon modes live in the thin YIG disk
- The optical WGMs live in the whole structure

Setup: two cases

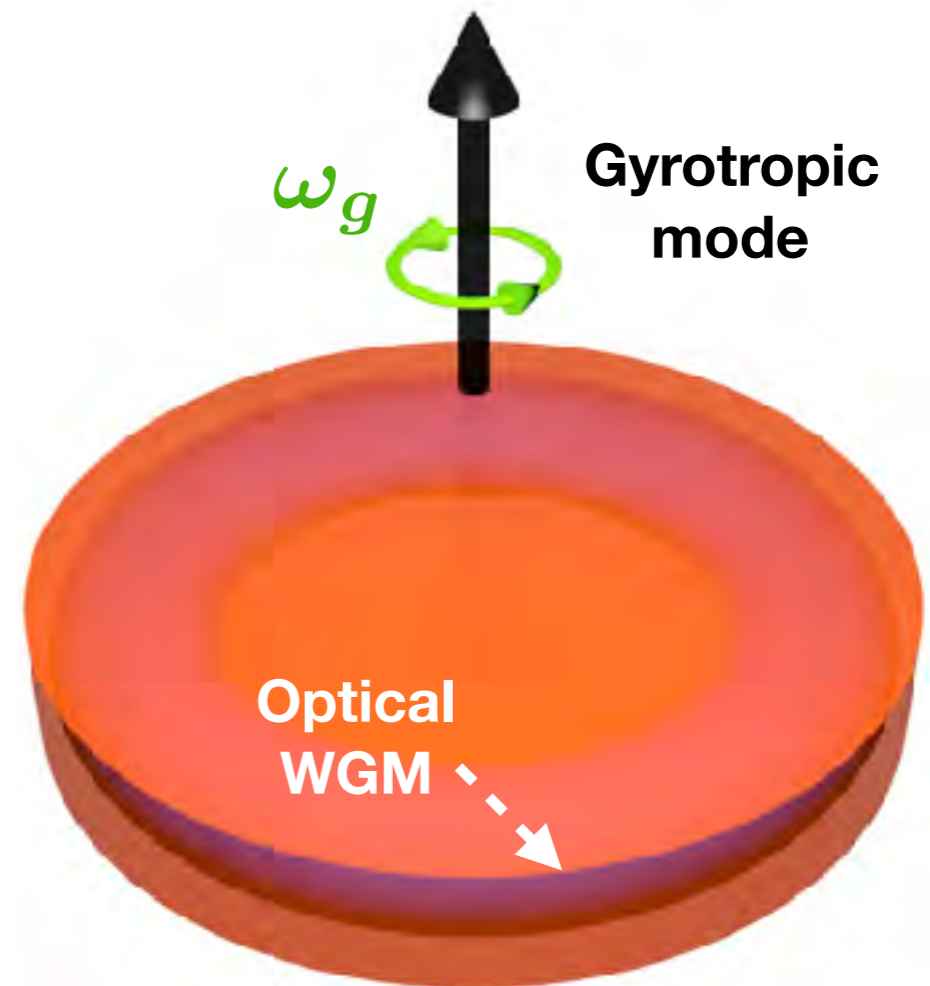
Thin Disk Heterostructure



$$h_{\text{YIG}} \sim l_{ex} \sim 10\text{nm}$$

- The magnon modes live in the thin YIG disk
- The optical WGMs live in the whole structure

“Thick” YIG Disk

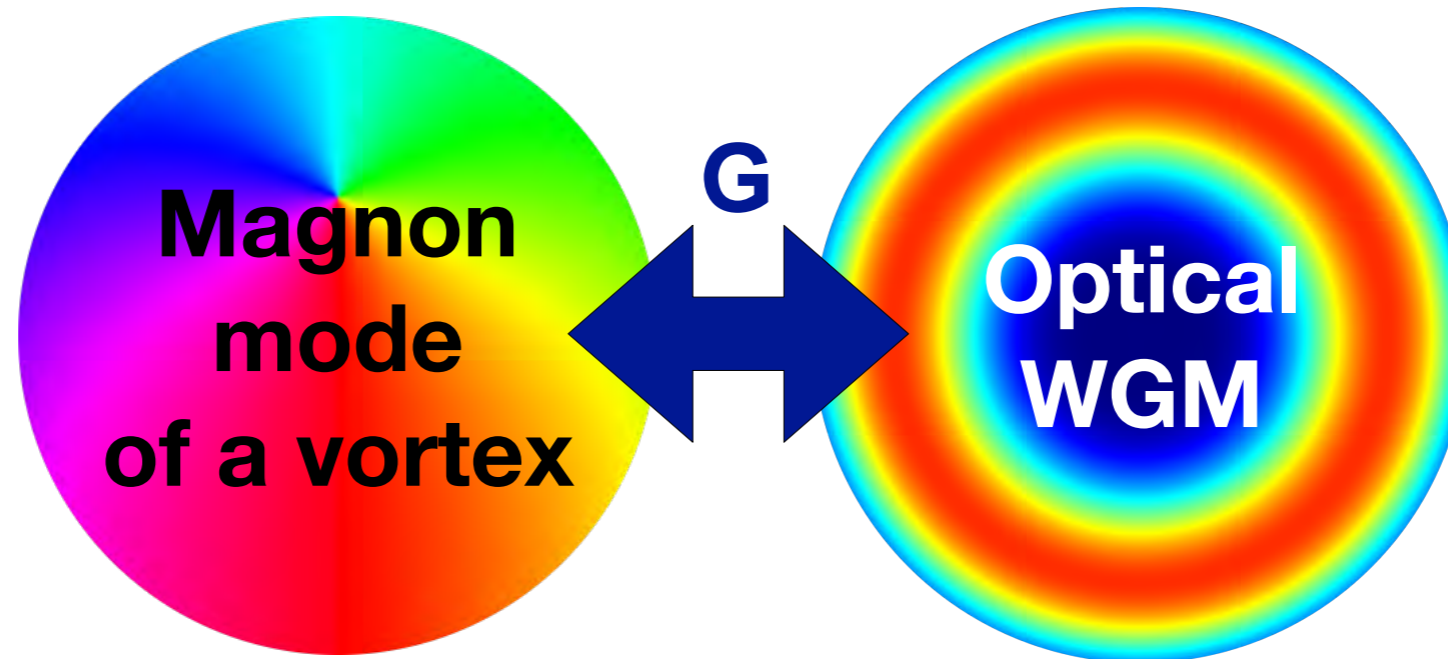


$$h_{\text{YIG}} \sim R_{\text{YIG}} \sim 1\mu\text{m}$$

- YIG disk: magnons + optical cavity
- Magnetic texture: Non-trivial z-dependence

Optomagnonic Coupling

$$H_c = -i \frac{\theta_F \lambda_n \varepsilon_0 \varepsilon}{4\pi} \int d\mathbf{r} \mathbf{m}(\mathbf{r}, t) \cdot [\mathbf{E}^*(\mathbf{r}, t) \times \mathbf{E}(\mathbf{r}, t)]$$



Vansteenkiste et. al
AIP Advances 4,
107133 (2014)

MuMax3

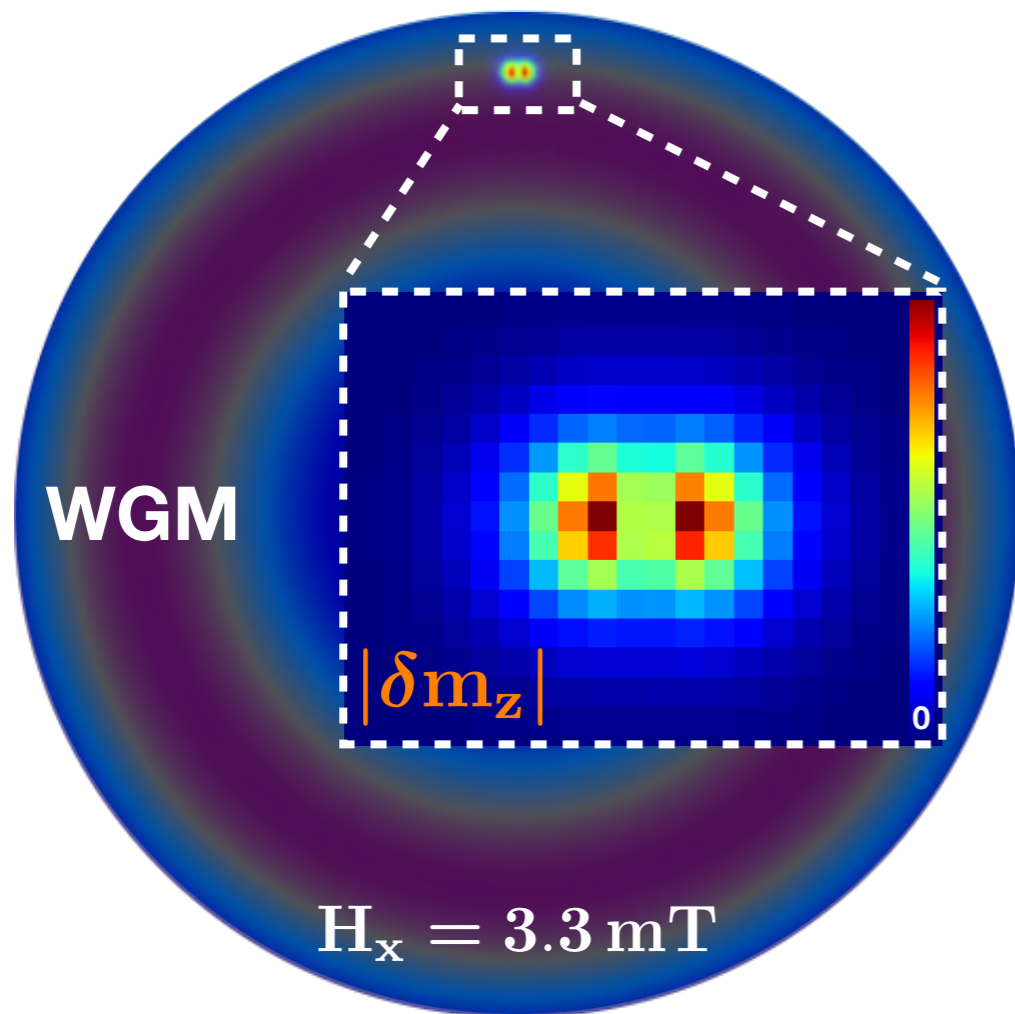
COMSOL

Simulation software

Vortex in a thin disk: optomagnonic coupling

spatial dependence

Magnon and optical modes

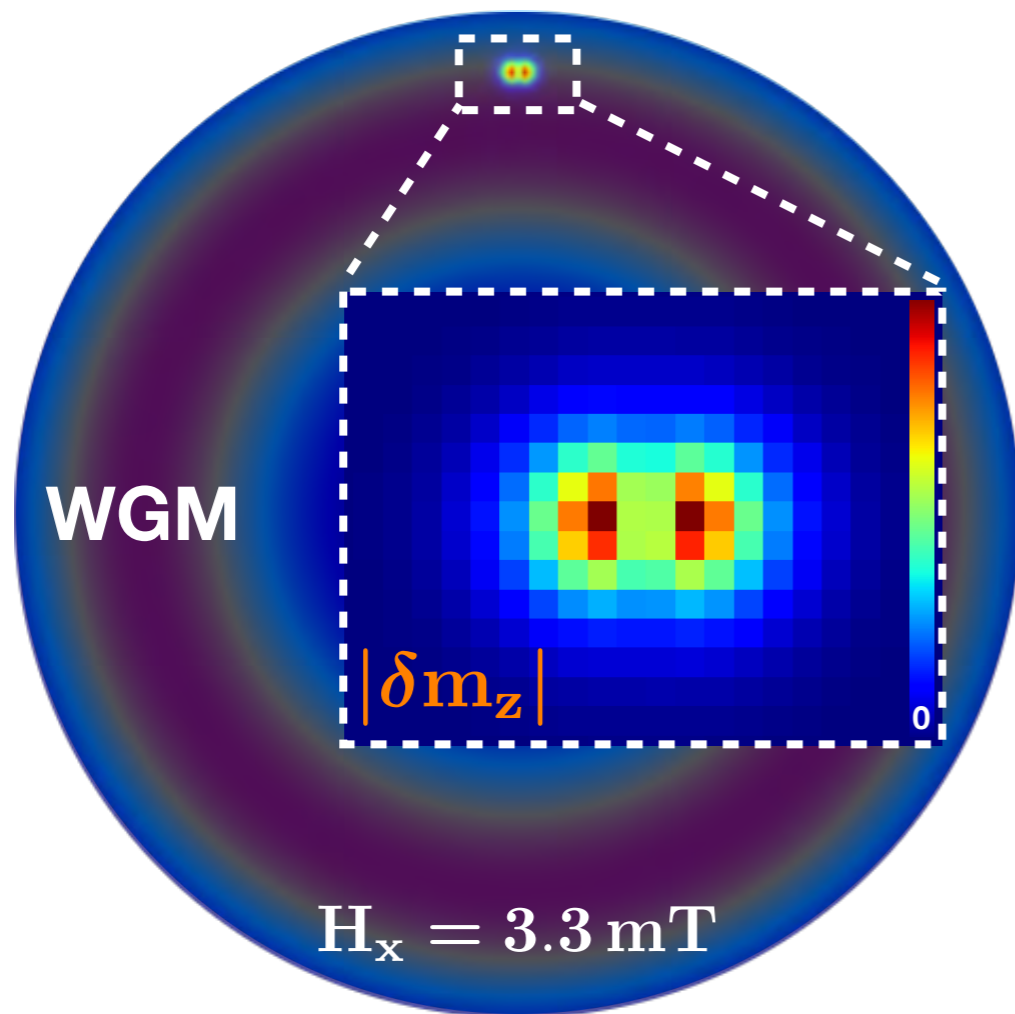


Gyrotropic mode $\omega_g \approx 30 \text{ MHz}$

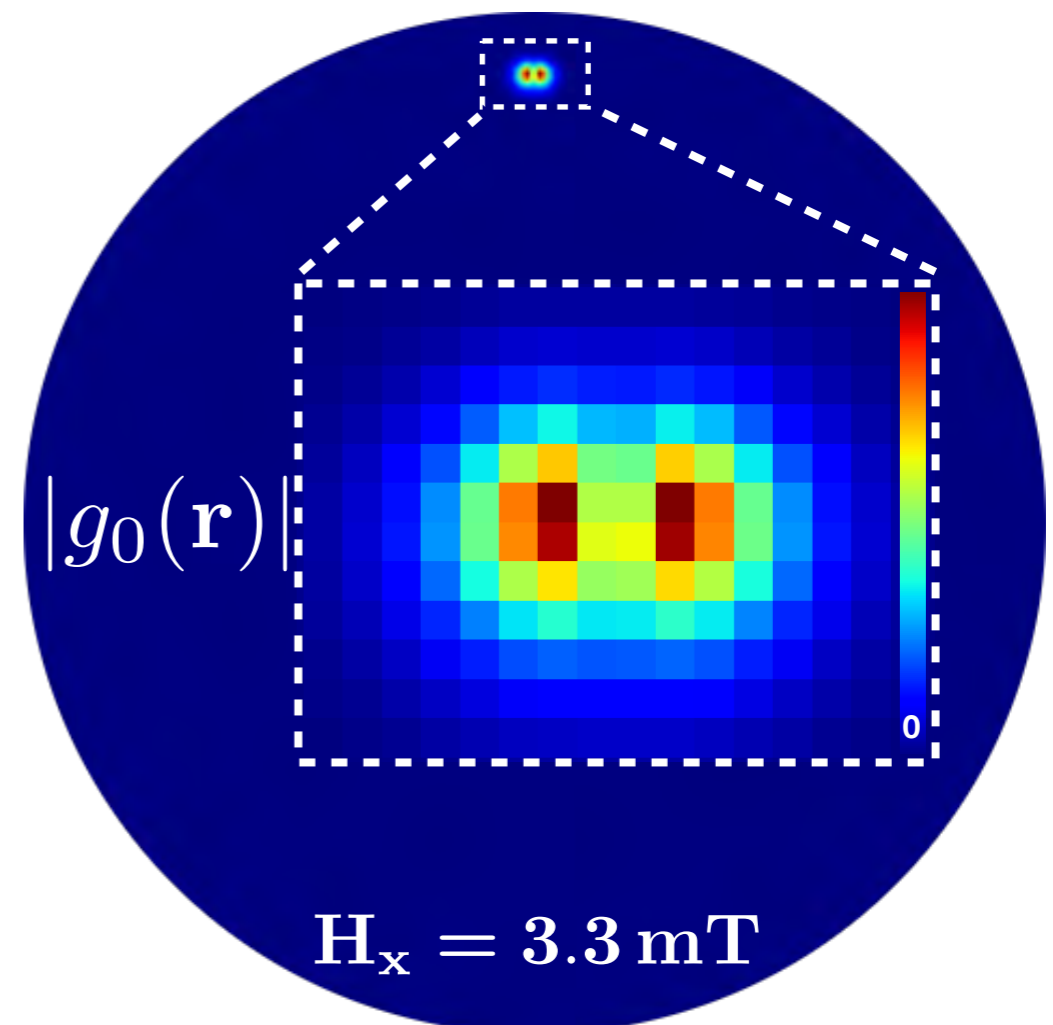
Vortex in a thin disk: optomagnonic coupling

spatial dependence

Magnon and optical modes



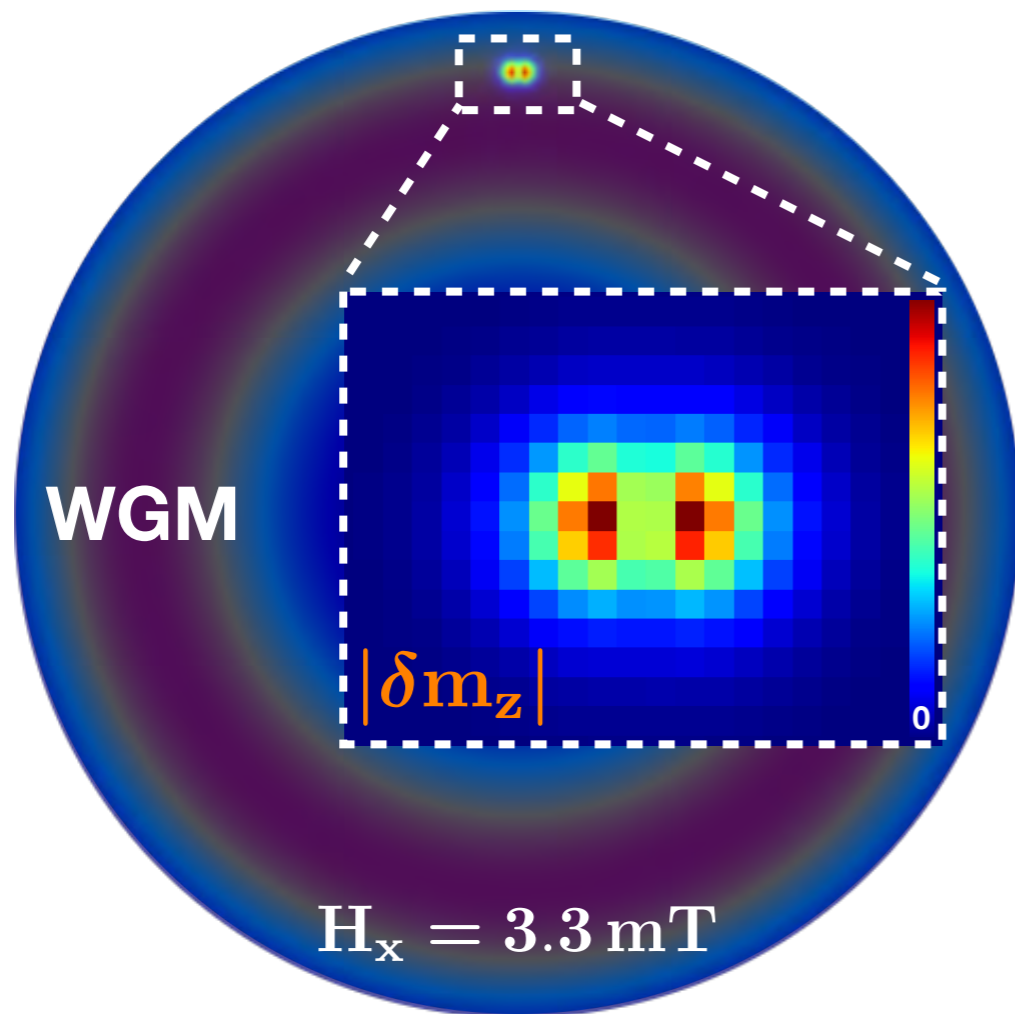
Optomagnonic coupling



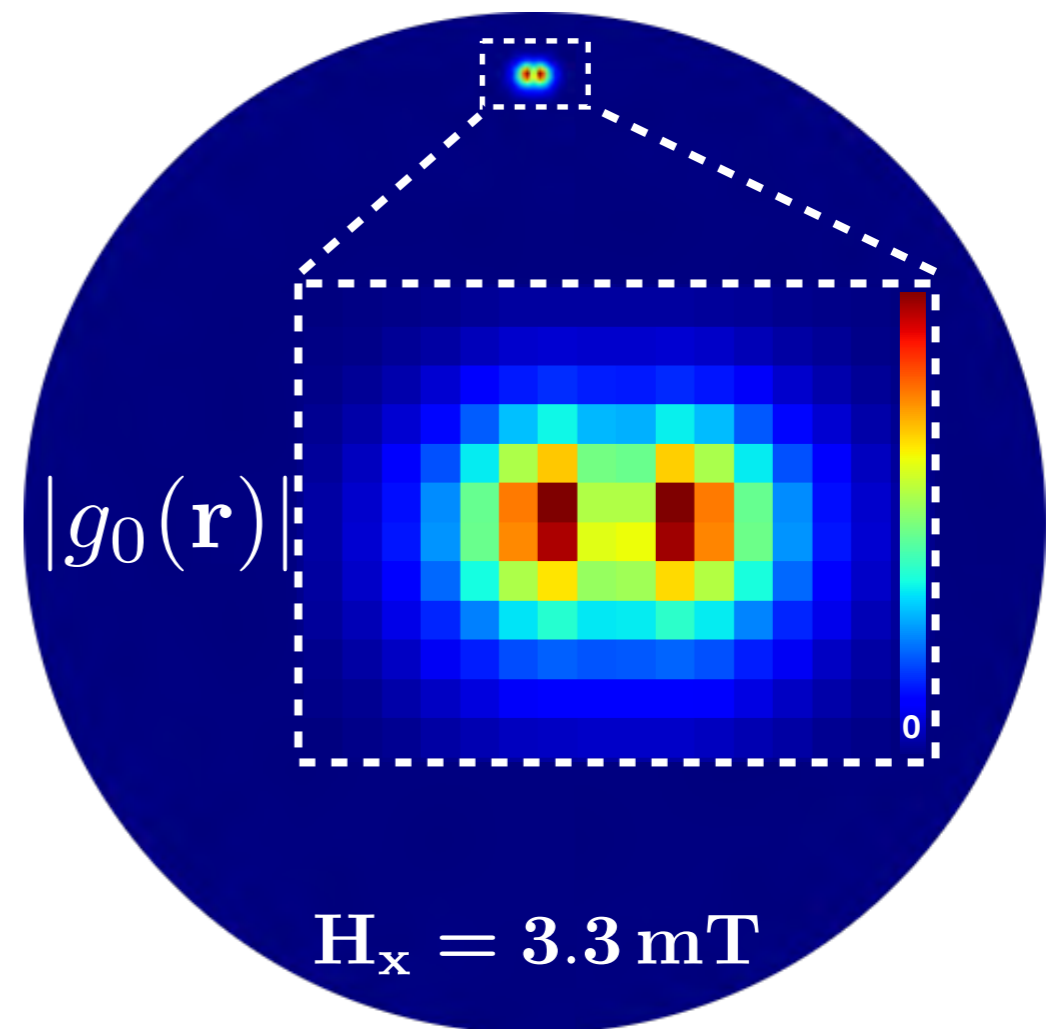
Vortex in a thin disk: optomagnonic coupling

spatial dependence

Magnon and optical modes



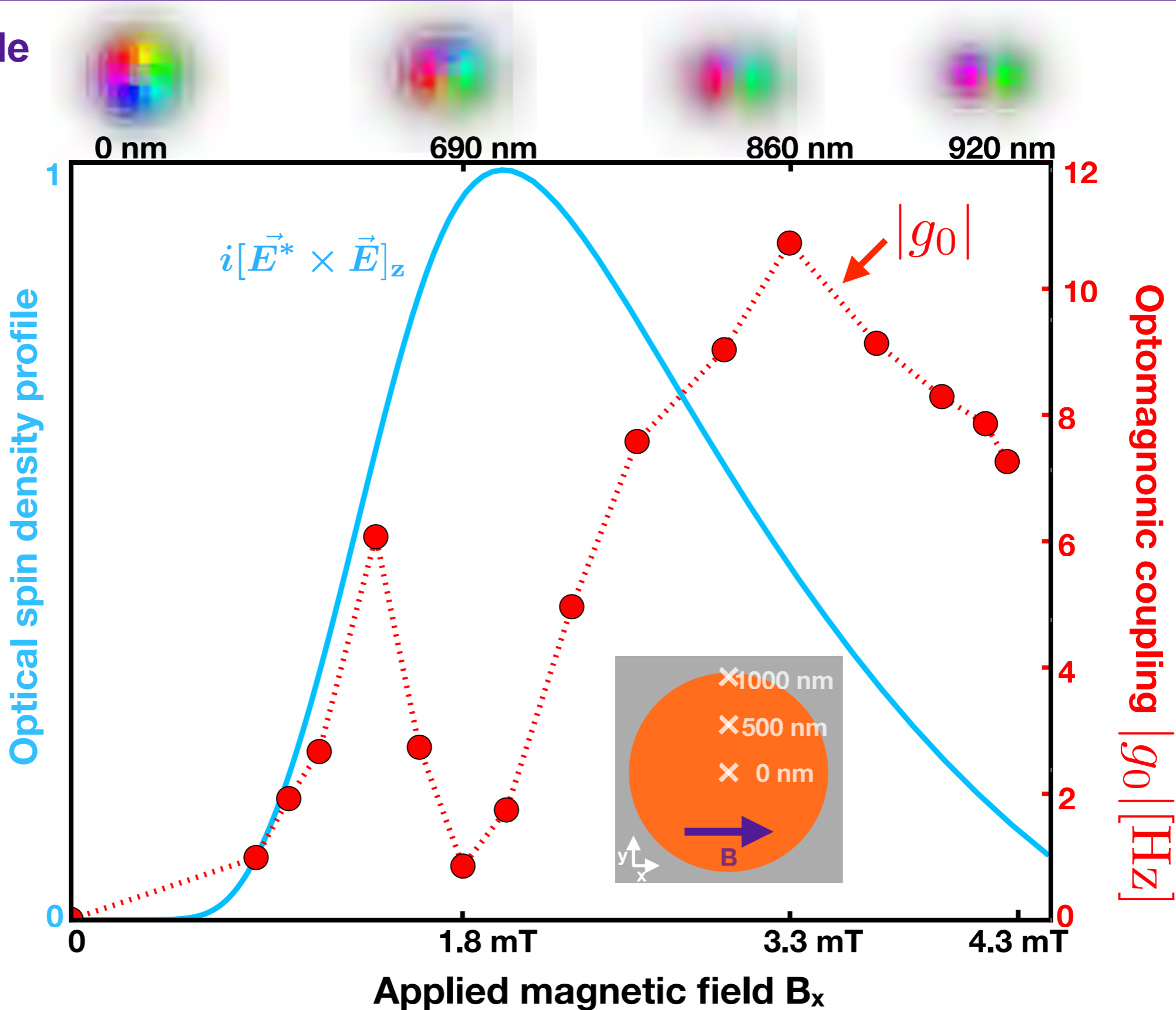
Optomagnonic coupling



integrate over the whole volume

Thin disk: tuneable coupling via B-field

Gyrotropic mode profile

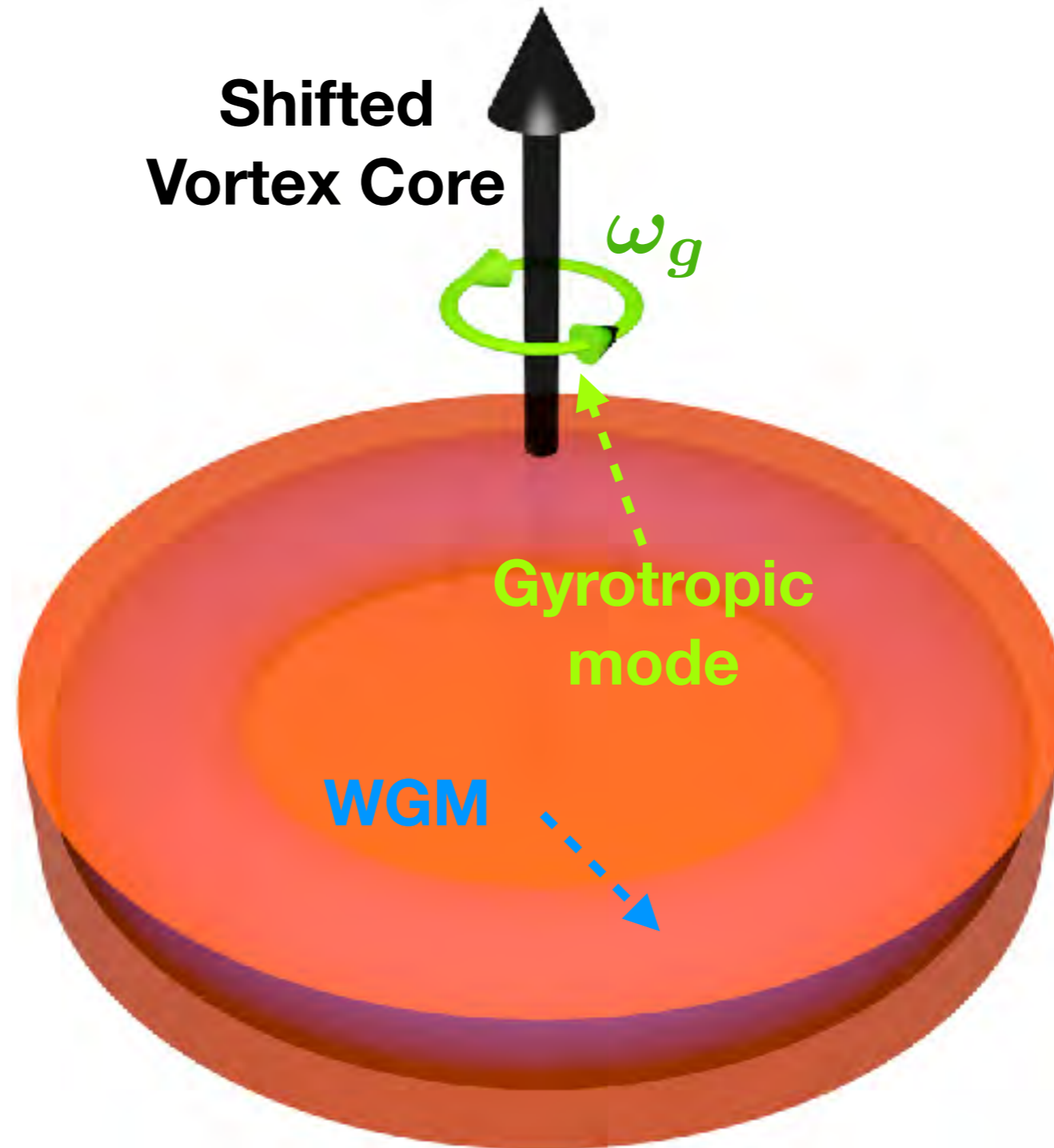


Agrees with analytical approximate solution

Full YIG microdisk

$$R = 2\mu\text{m}$$

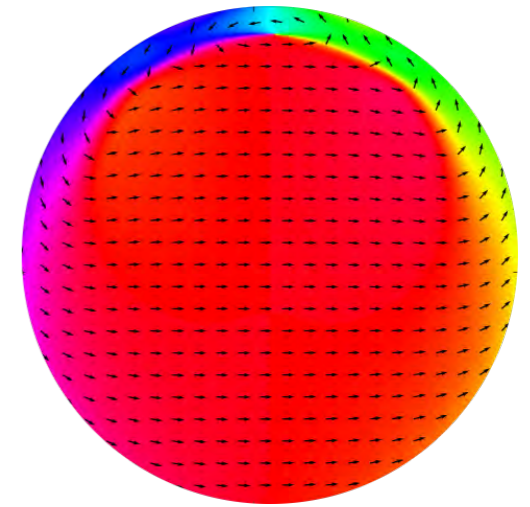
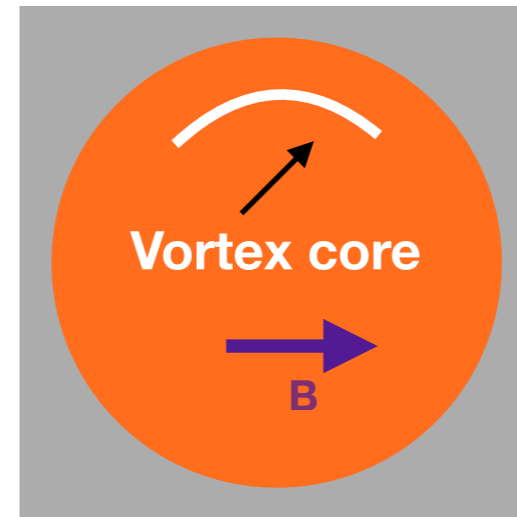
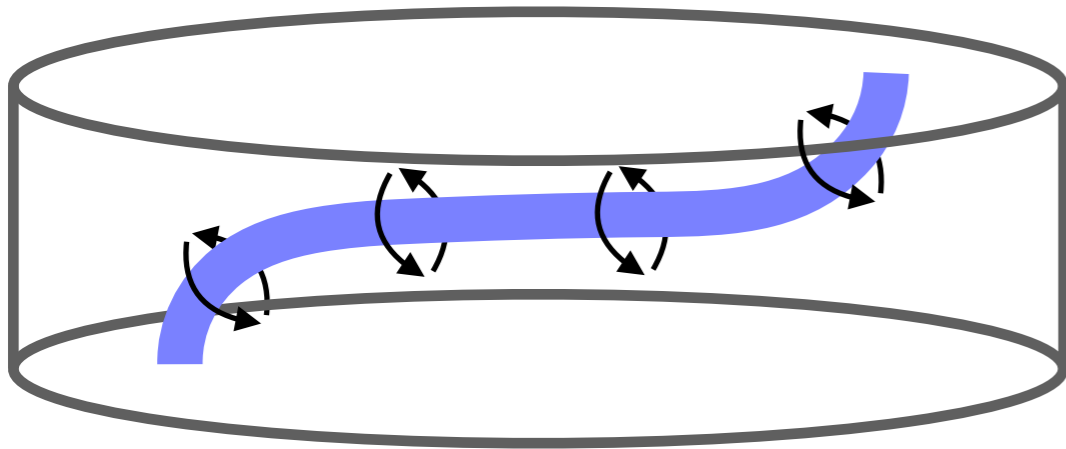
$$h = 500\text{nm}$$



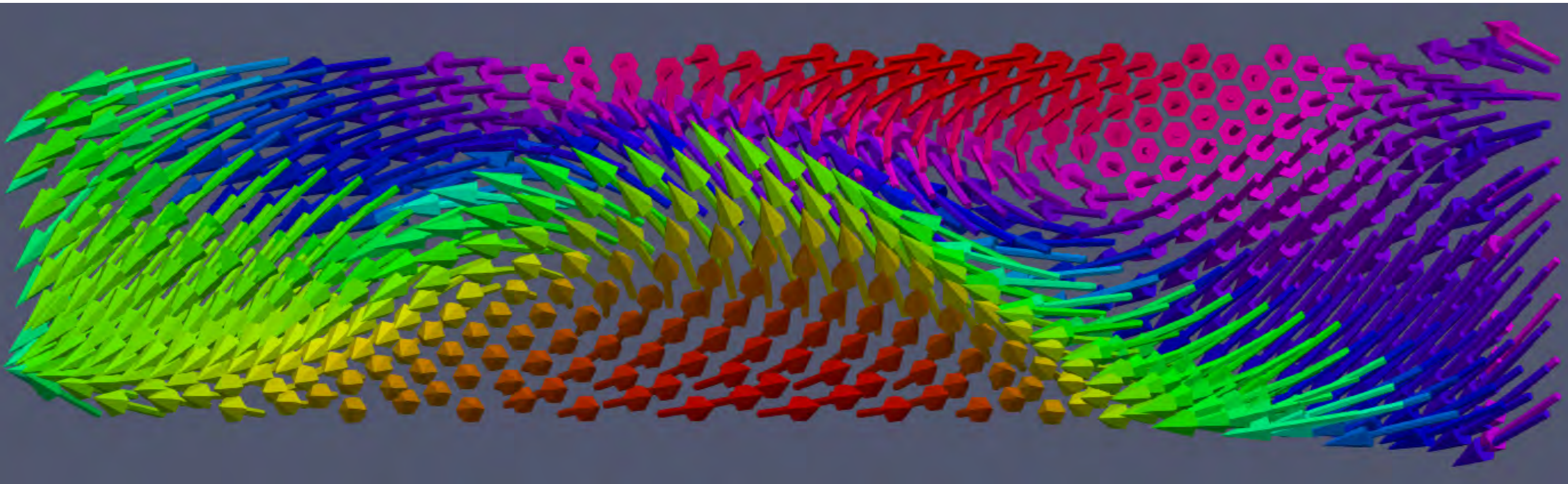
Simple picture of the vortex breaks down:
Non-trivial z dependence

Full YIG microdisk

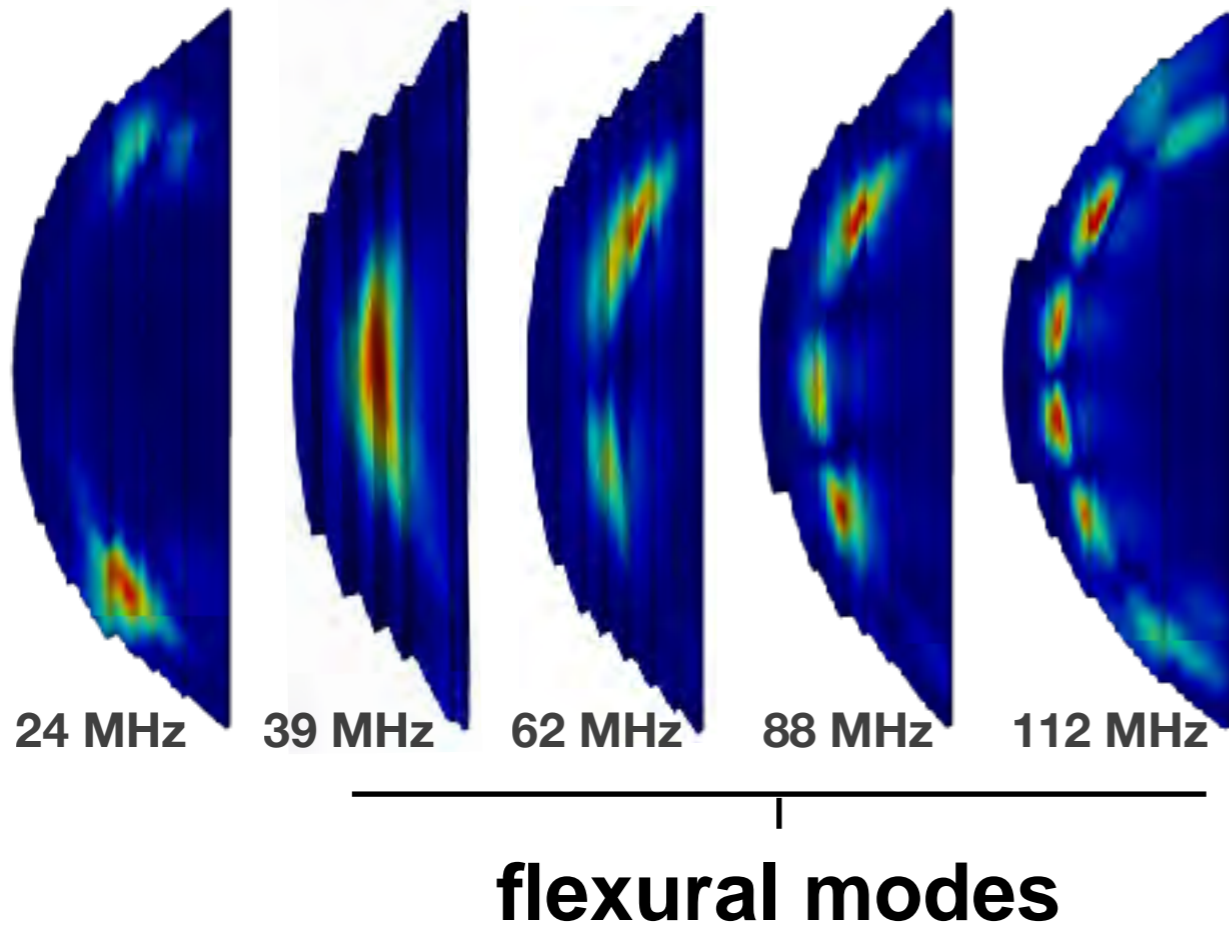
Vortex



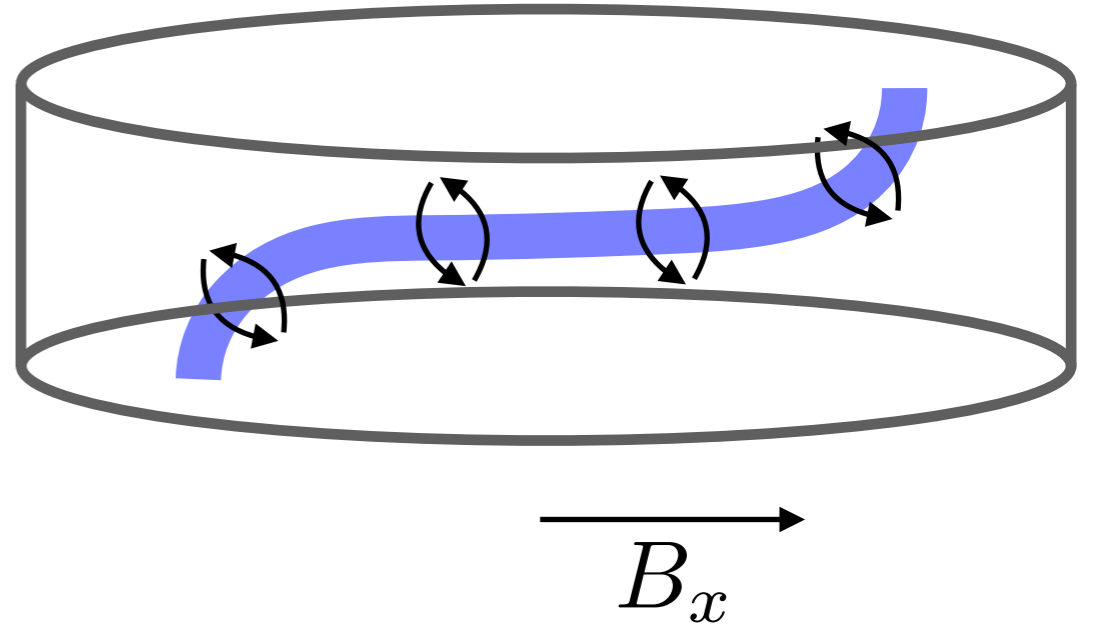
Definitely not 2D!!



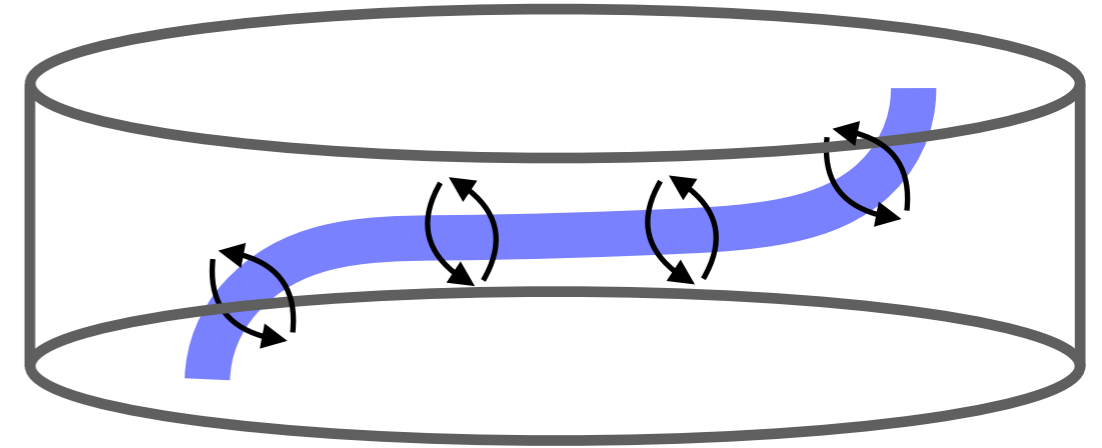
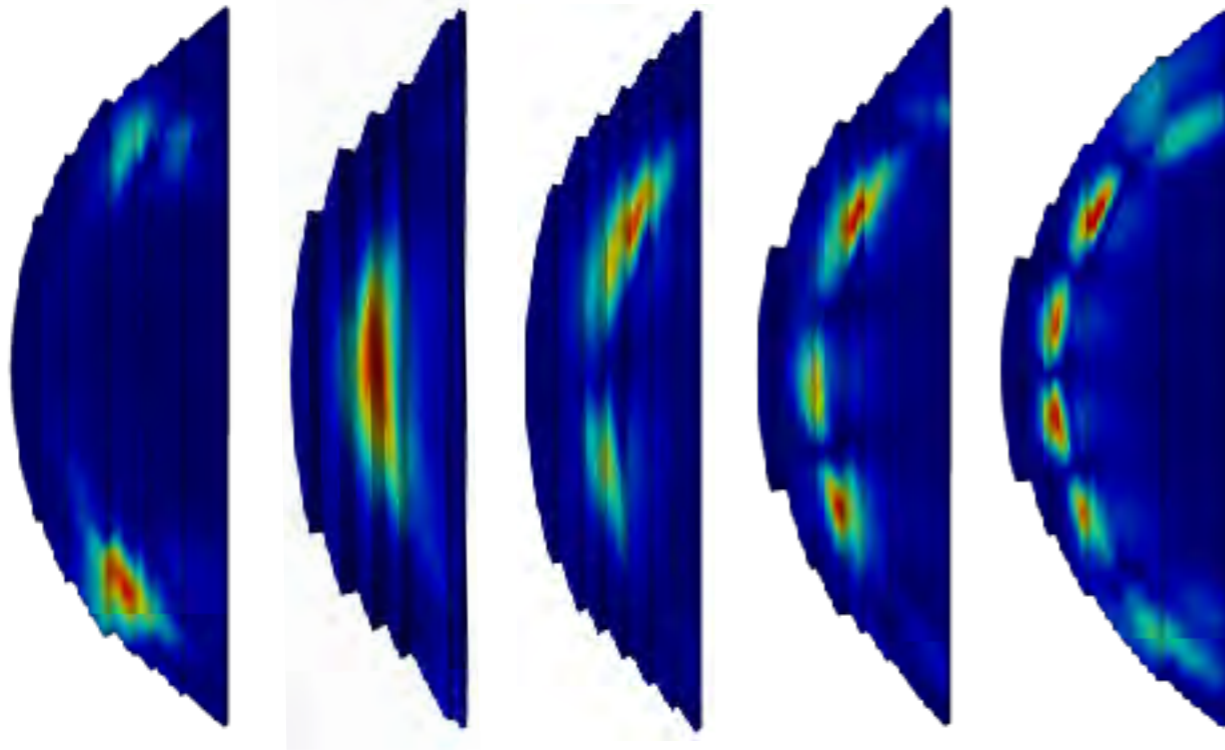
Full YIG microdisk



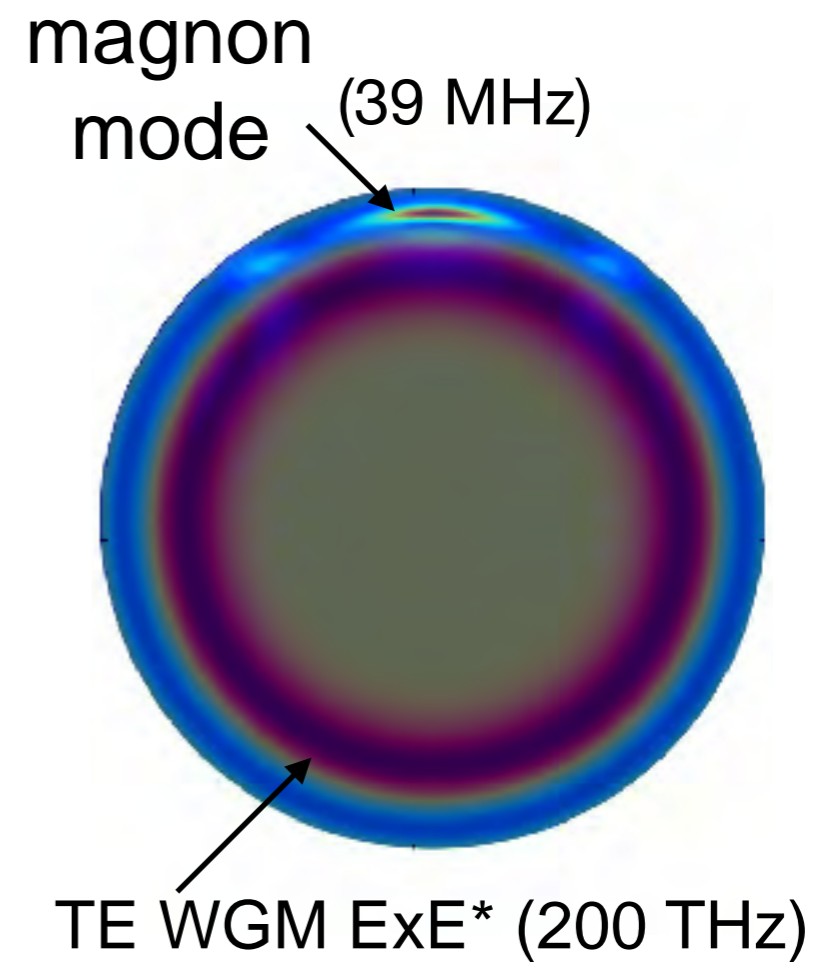
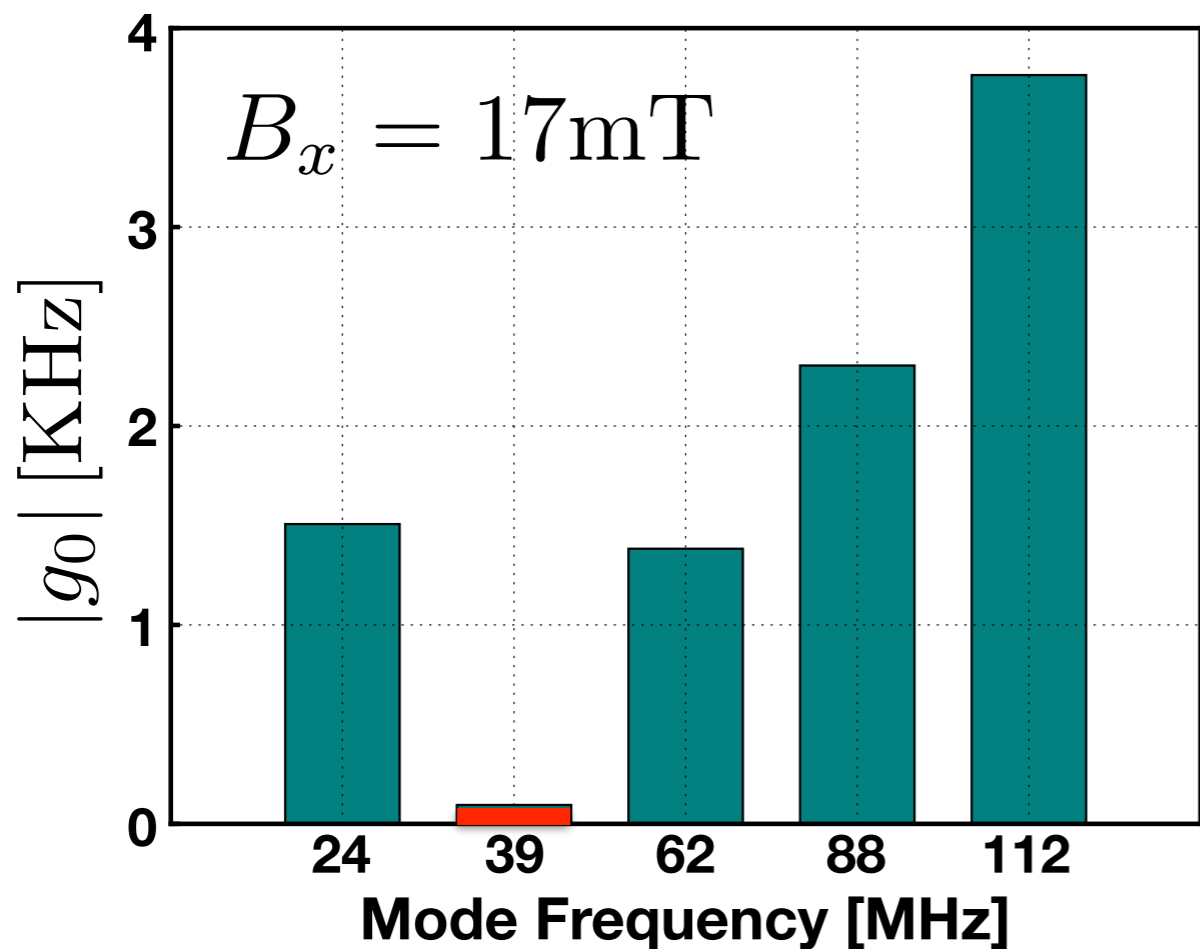
$B_x = 17\text{mT}$



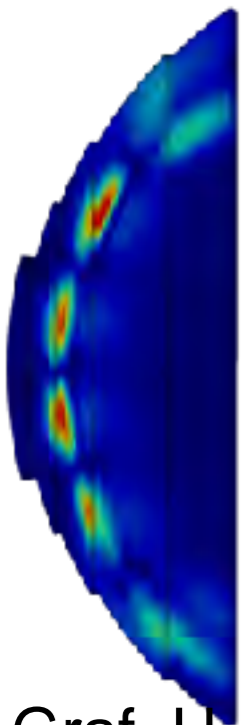
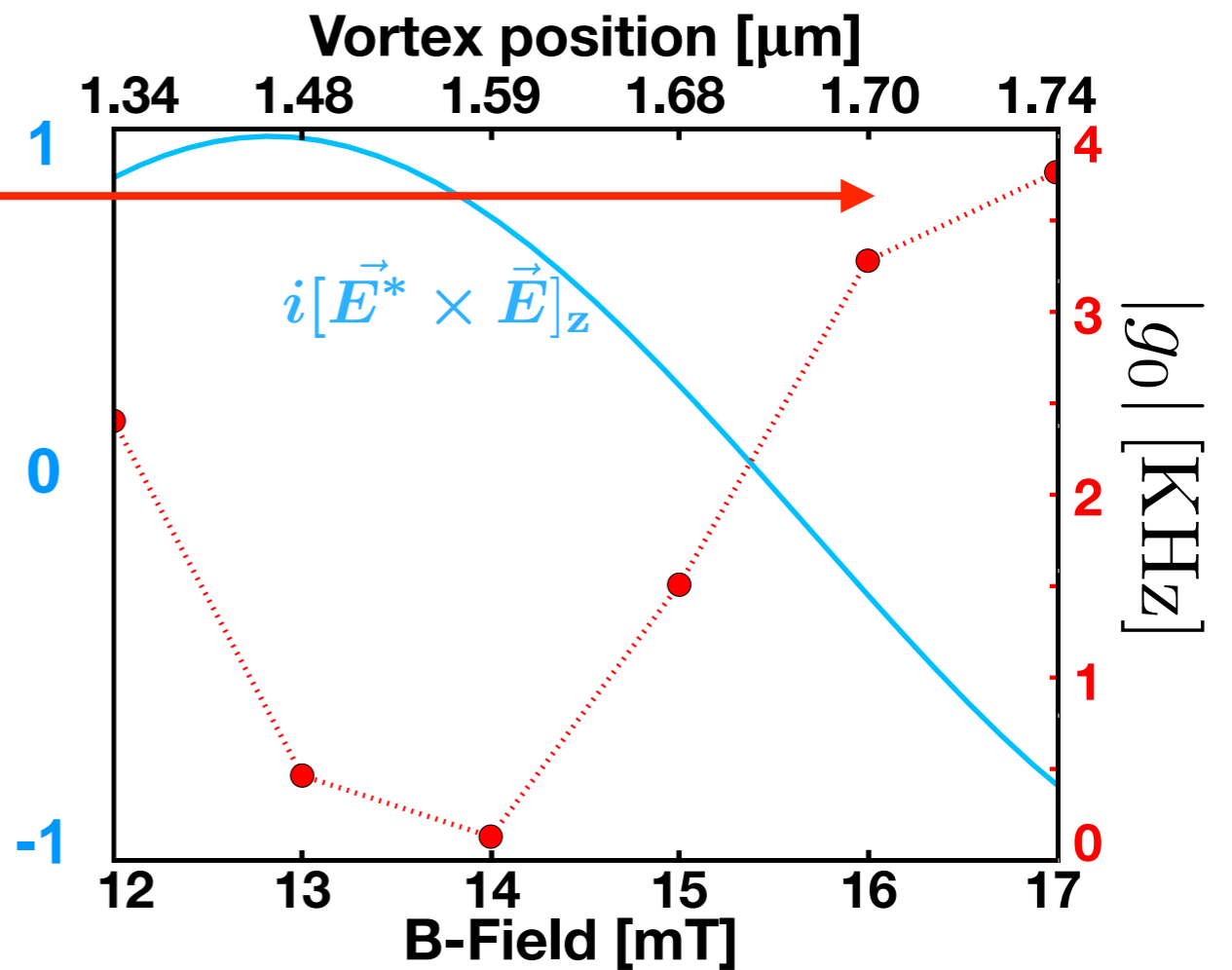
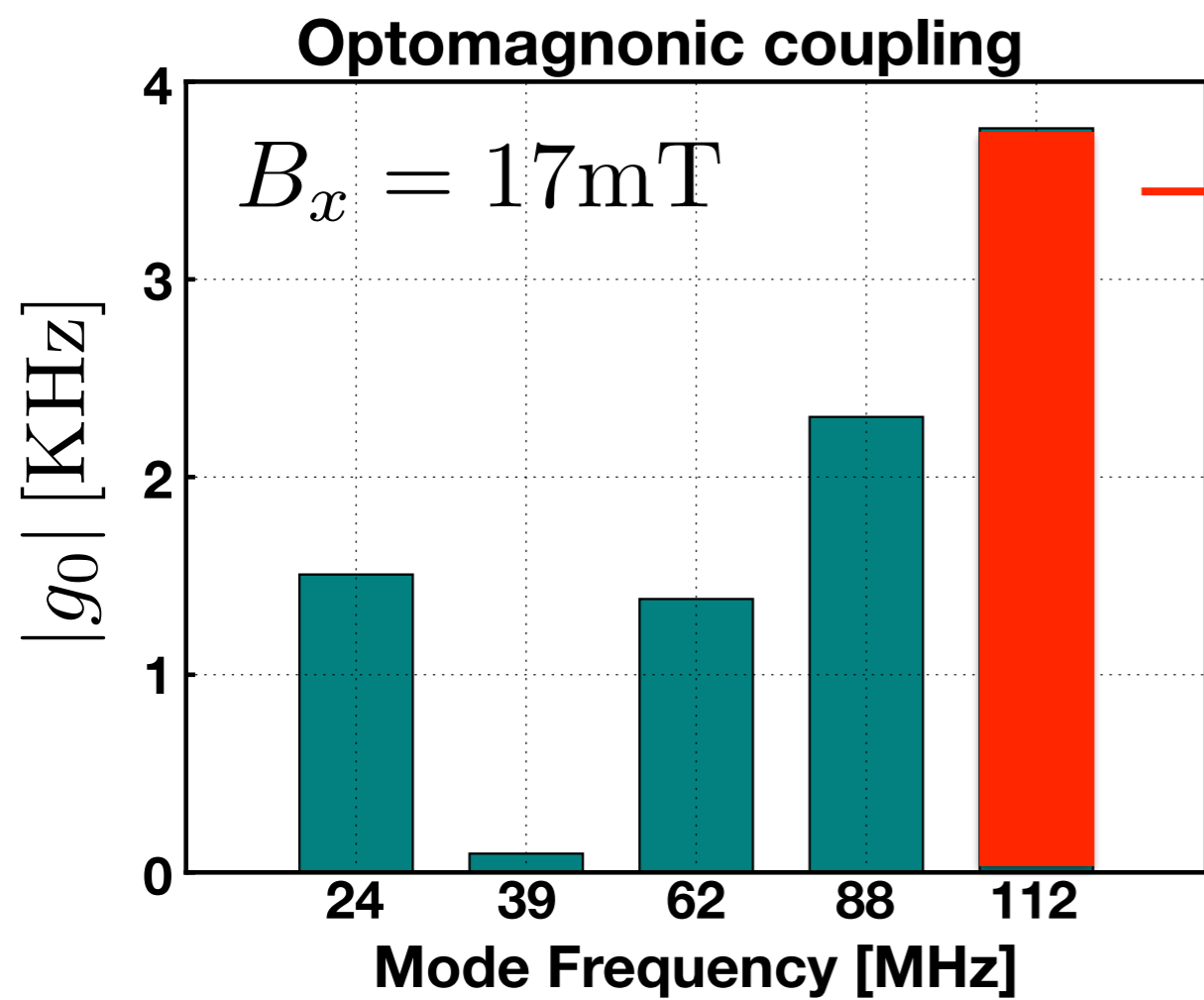
Full YIG microdisk



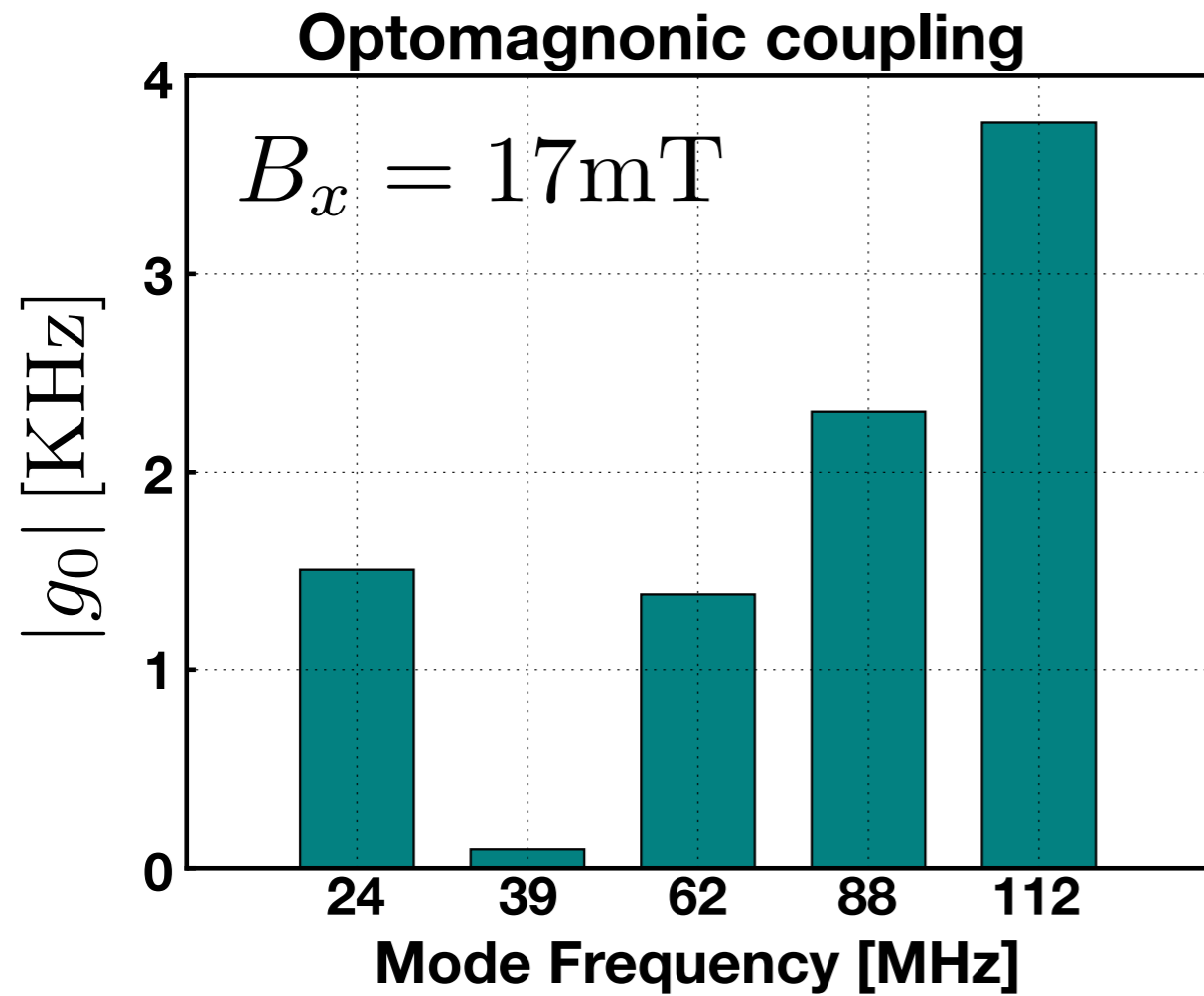
Optomagnonic coupling



Full YIG microdisk



Full YIG microdisk



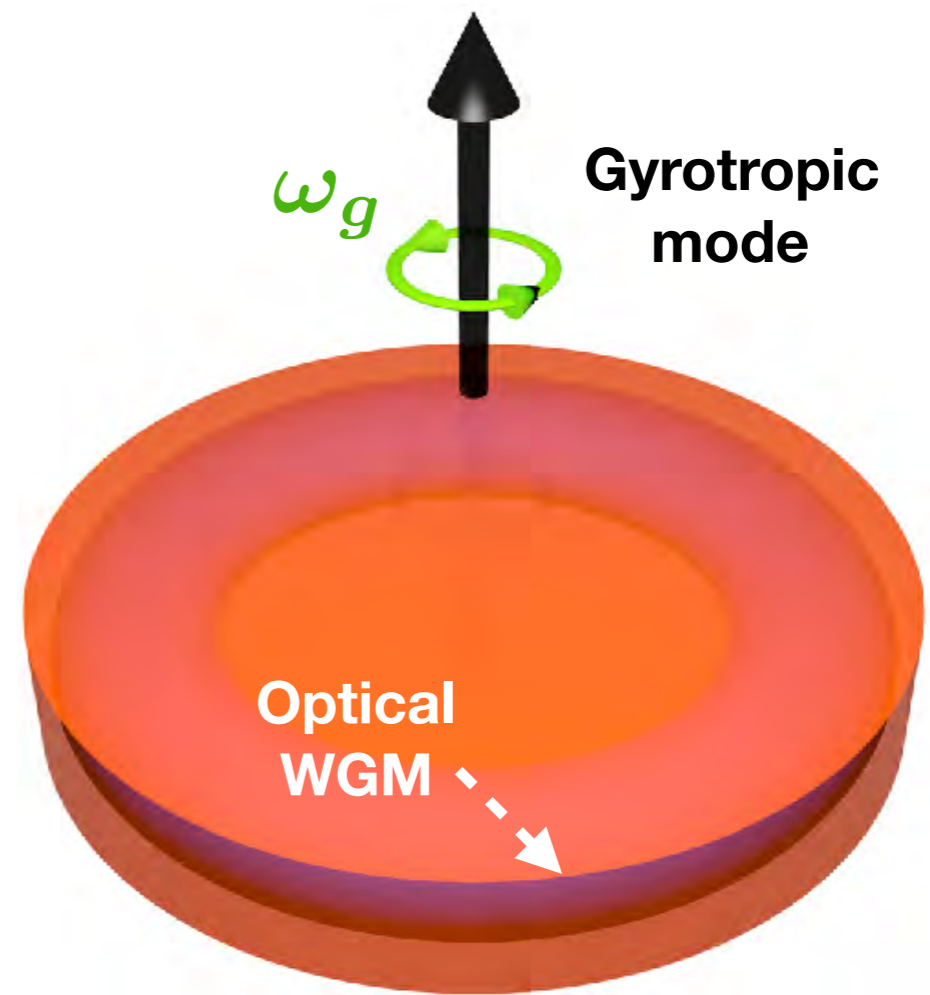
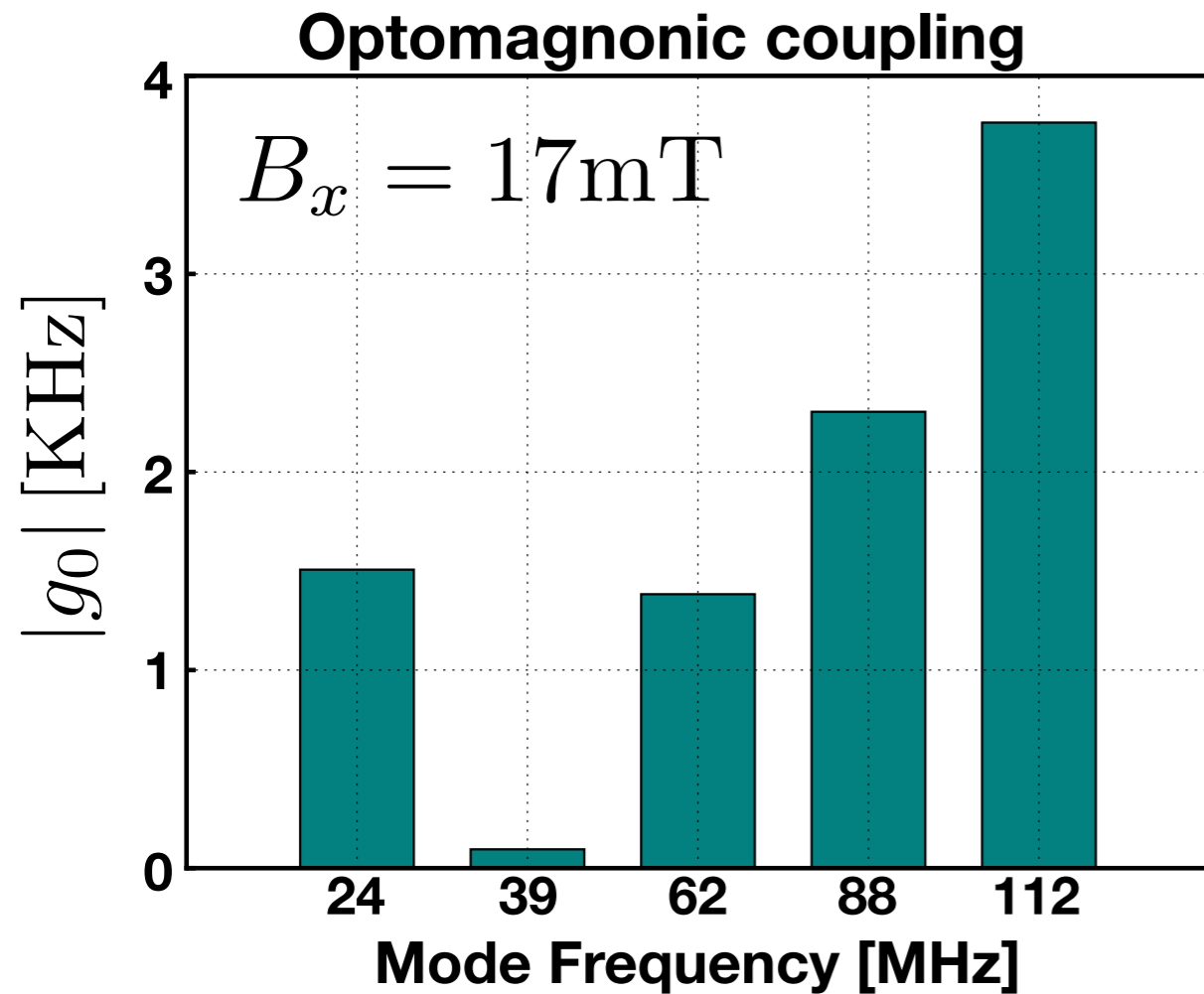
Single photon
Cooperativity:

$$\mathcal{C}_0 = 4 \frac{g_0^2}{\Gamma \kappa} \approx 10^{-7}$$

Cooperativity at
maximum photon
density:

$$\mathcal{C} = 4 n_{\text{ph}} \frac{g_0^2}{\Gamma \kappa} \approx 10^{-2}$$

Full YIG microdisk



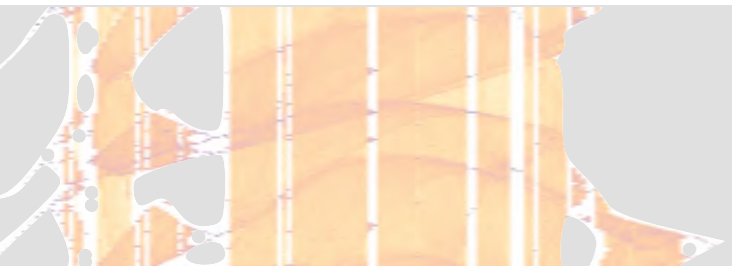
- Promising values for coupling - other modes?
- Tuneable coupling by an external magnetic field
- Coupled dynamics of the system?



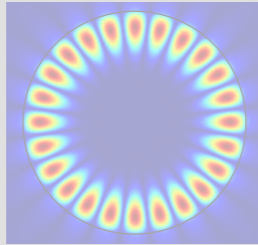
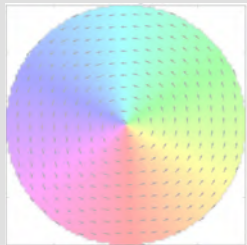
Introduction and motivation



Optomagnonic Hamiltonian



Optically induced spin dynamics




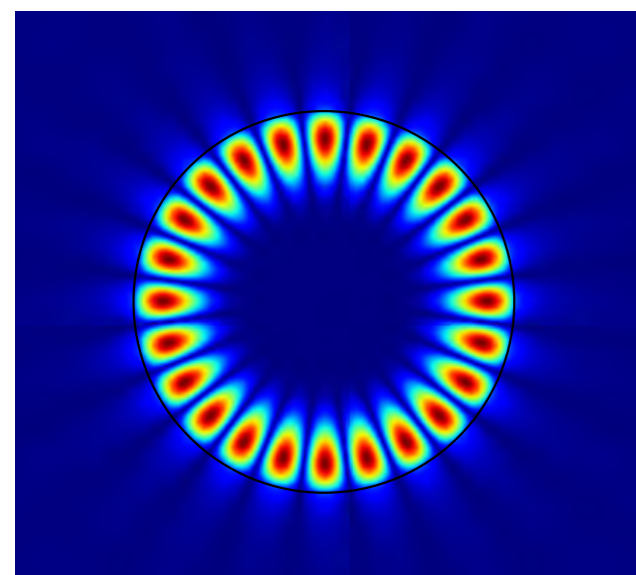
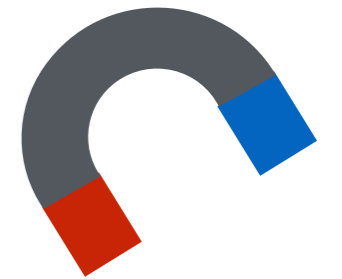
Magnetic textures: vortex in a disk



Summary

Summary

-  Light-induced nonlinear spin dynamics (Kittel mode)
- First time optomagnonics with magnetic textures
- Coupling to magnetic vortex modes
- Promising values of coupling by engineering



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for the science of light

