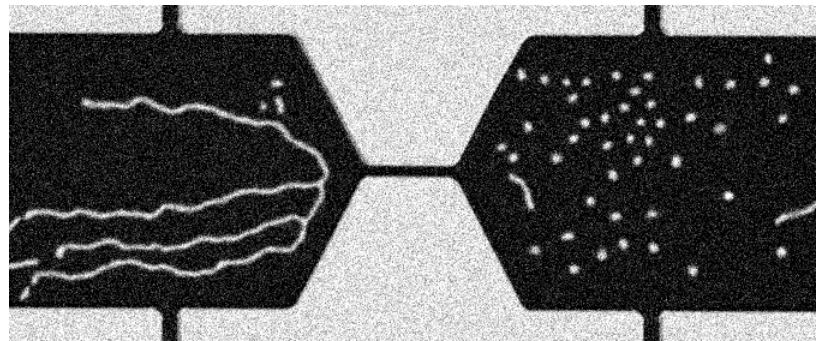
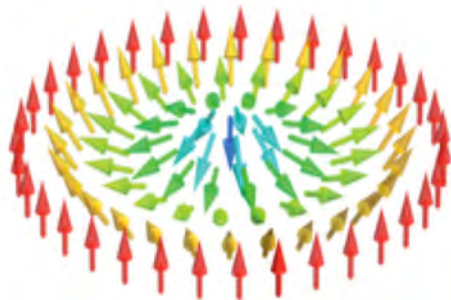


Manipulating Magnetic Skyrmions

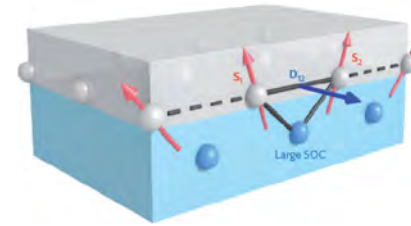


Axel Hoffmann

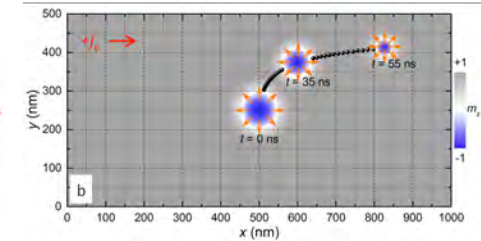
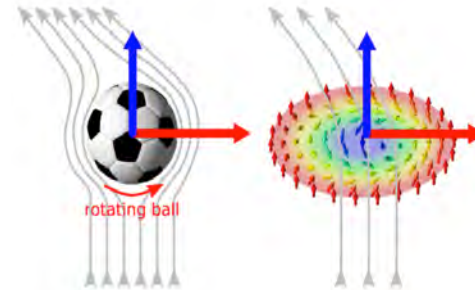
Materials Science Division
Argonne National Laboratory

Outline

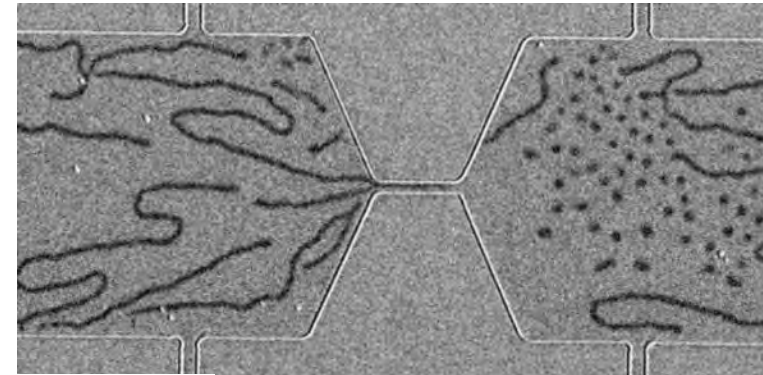
■ Magnetic Skyrmions



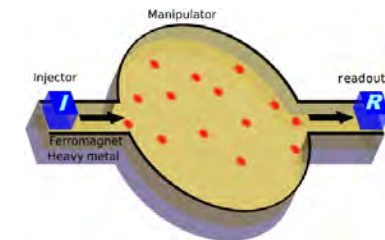
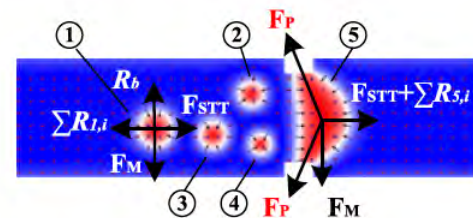
■ Moving Skyrmions



■ Generating Skyrmions



■ Neuromorphic Ideas



■ Conclusions

Journal of Applied Physics: Special Topic



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124 (2018)



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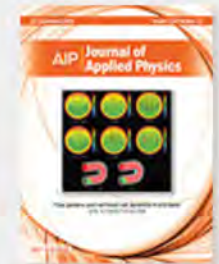
[Issue 9, September 07](#)

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DISPLAY : 20 50 100 all

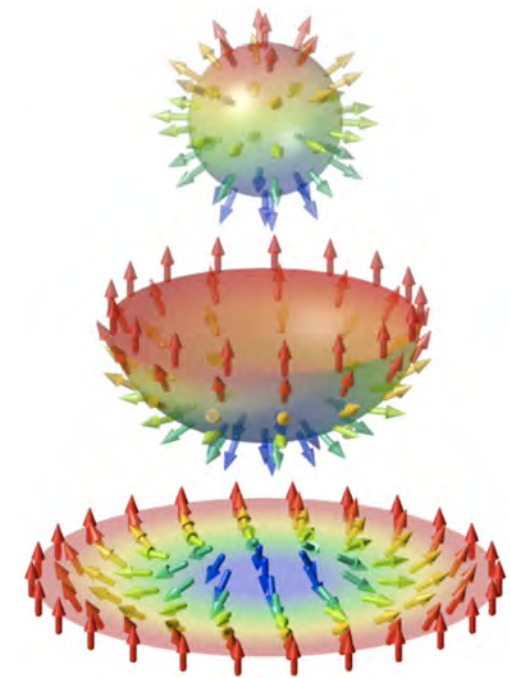
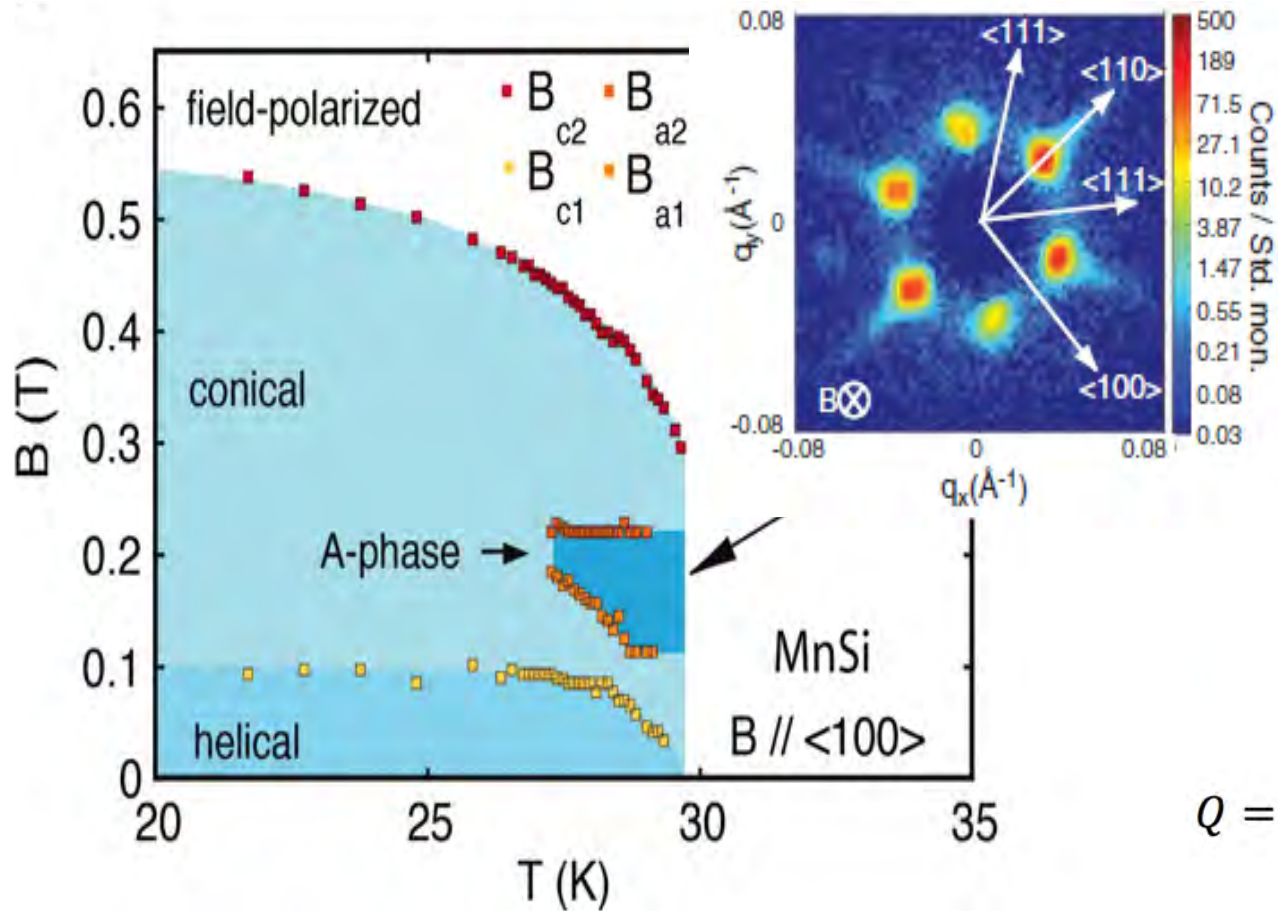
SPECIAL TOPIC: NEW PHYSICS AND MATERIALS FOR NEUROMORPHIC COMPUTATION Perspectives



Magnetic Skyrmions

Recent Review: W. Jiang *et al.*, Phys. Rep. **704**, 1 (2017)

Discovery of Magnetic Skyrmions



Topological Charge

$$Q = \frac{1}{4\pi} \int \mathbf{m} \cdot (\partial_x \mathbf{m} \times \partial_y \mathbf{m}) dx dy$$

$$Q = \pm 1$$

S. Mühlbauer *et al.*, Science **323**, 915 (2009)

Charge Current Manipulation of Skyrmions

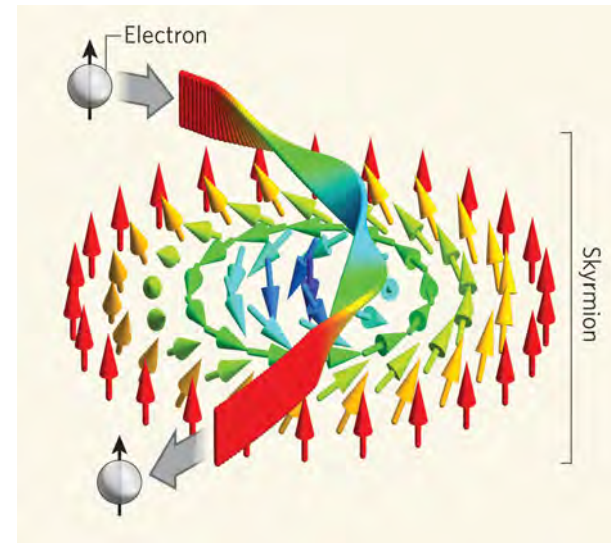
Emergent Magnetic Field

J. Zang *et al.*, Phys. Rev. Lett. **107**, 136804 (2011)

$$h_i = \frac{\hbar c}{2e} \delta_{iz} \mathbf{n} \cdot (\partial_x \mathbf{n} \times \partial_y \mathbf{n}) = \pm \frac{\hbar c}{2e}$$

$$h \approx \frac{\Phi_0}{\pi R^2} \approx \frac{\Phi_0}{\pi a^2} \left(\frac{D}{J}\right)^2$$

$$h \sim 100 \text{ T}$$



Back-action moves skyrmion

➤ Ultralow threshold Current

$$j_c \approx 10^6 \text{ A} \cdot \text{cm}^{-2}$$

Domain Wall

$$j_c \approx 0.2 \text{ A} \cdot \text{cm}^{-2}$$

Skyrmion

Skyrmions are Stabilized by Chiral Interactions

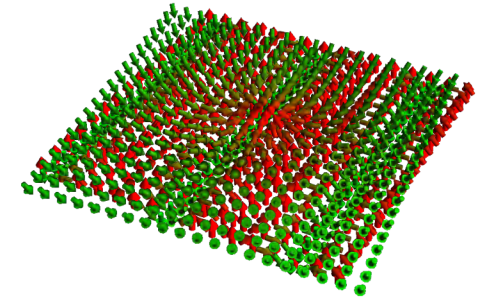
W. Jiang *et al.*, Phys. Rep. **704**, 1 (2017)

$$H = \sum_{\langle ij \rangle} -J \mathbf{S}_i \cdot \mathbf{S}_j + \mathbf{D}_{ij} \cdot (\mathbf{S}_i \times \mathbf{S}_j) - \sum_i \mathbf{B} \cdot \mathbf{S}_i$$

Ferromagnetic

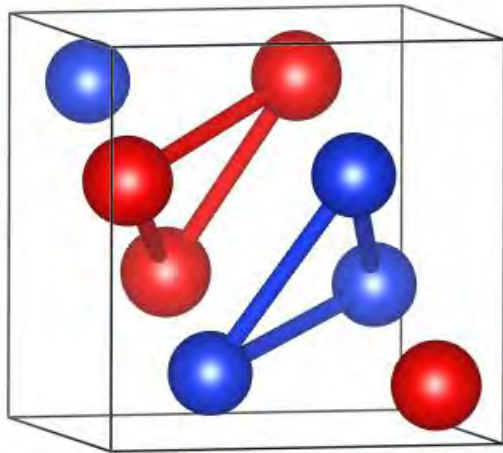
Helical Spiral

Skyrmion



Dzyaloshinskii-Moriya Interaction (DMI) requires Inversion Symmetry Breaking

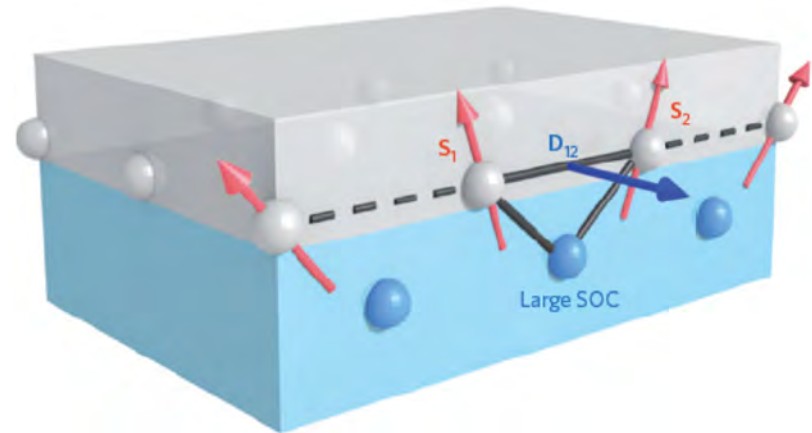
Bulk



e.g., B20 compounds (MnSi, etc.)

Axel Hoffmann, Materials Science Division, Argonne National Laboratory

Multilayers



e.g., Co/Pt, Ni₈₀Fe₂₀/Ta, etc.

hoffmann@anl.gov

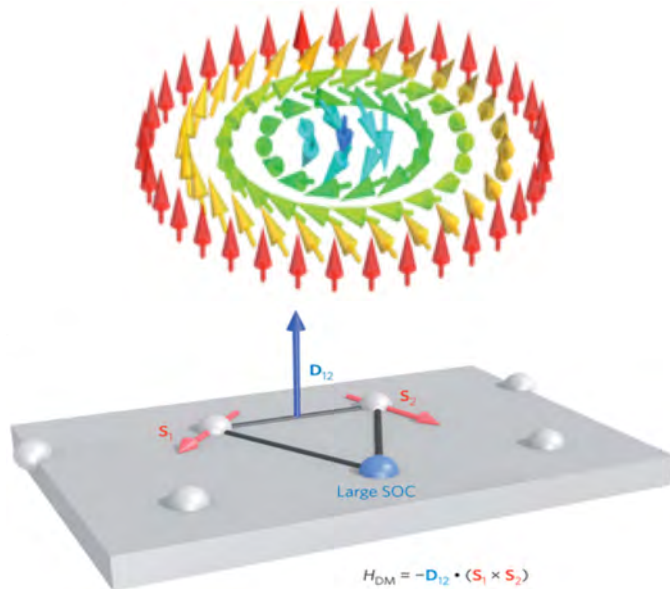


Stabilizing Skyrmions

Broken inversion symmetry leads to Dzyaloshinskii-Moriya Interaction (DMI) $H_{\text{dmi}} = -D_{ij} \cdot (S_i \times S_j)$

Bulk DMI

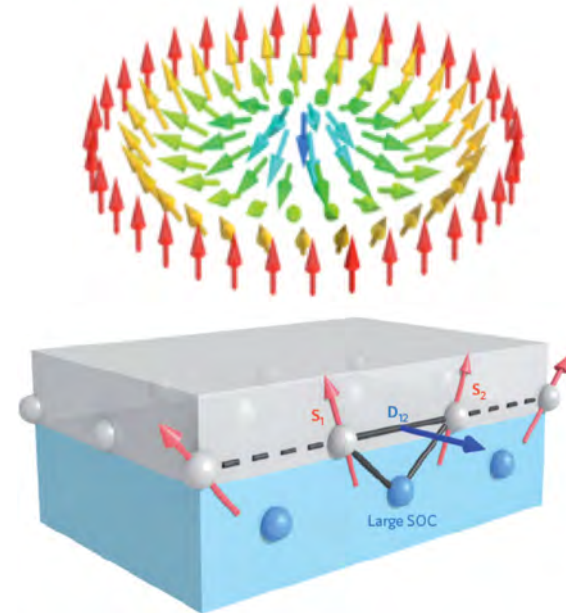
Vortex-like (Bloch)



B20 compound MnSi, FeGe, FeCoSi

Interfacial DMI

Hedgehog (Néel)



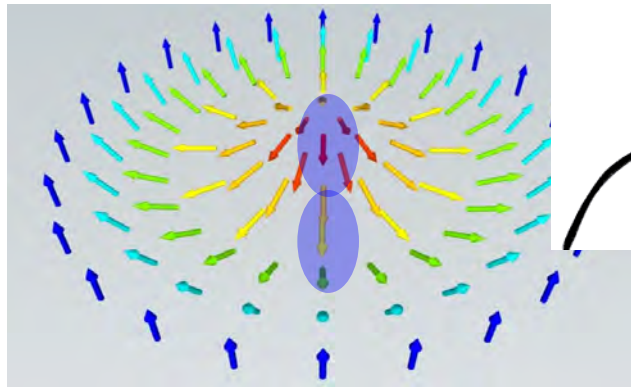
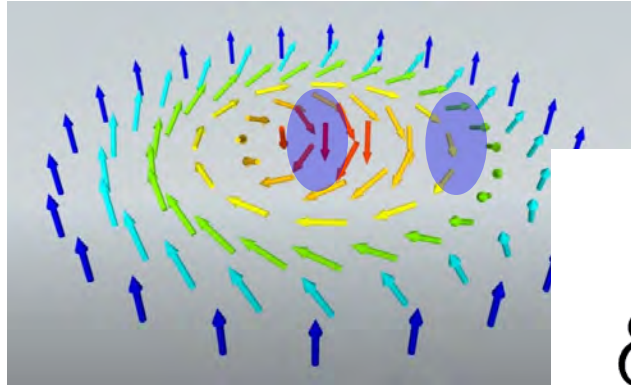
Ta/CoFeB/MgO, Pt/Co/MgO, Ir/Fe/Pd

A. Fert *et al.*, Nature Nano. 8, 152 (2013)

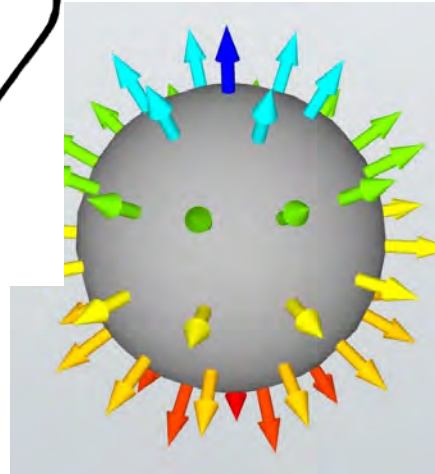
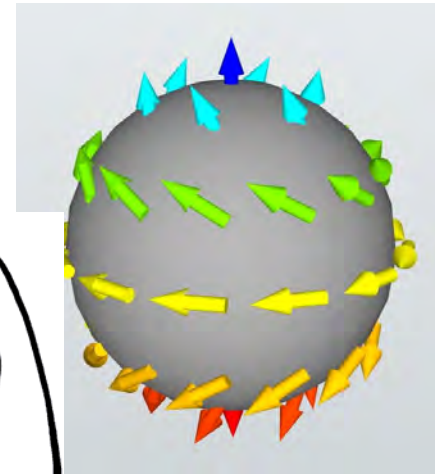
Axel Hoffmann, Materials Science Division, Argonne National Laboratory

hoffmann@anl.gov

Topological Nature of Skyrmions



Wrap



$$\frac{1}{4\pi} \int d^2x n \cdot (\partial_x n \times \partial_y n) = \pm 1$$

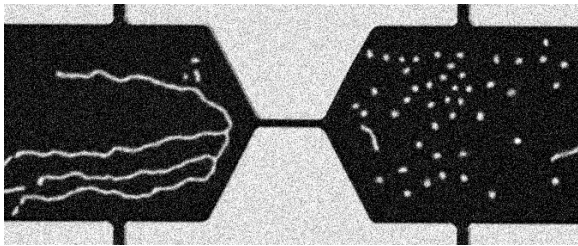
Topological Charge

Courtesy of Jiadong Zang

Skyrmions at Room Temperature

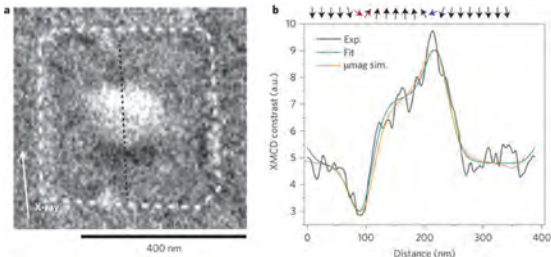
“Single” Layer

TaO_x/CoFeB/Ta: ≈ 1 μm



W. Jiang *et al.*, Science **349**, 283 (2015)

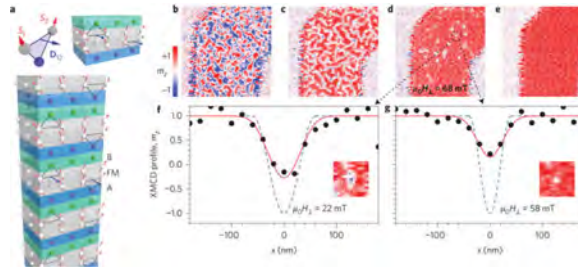
Pt/Co/MgO: ≈ 130 nm



O. Boulle *et al.*,
Nature Nanotechn. **11**, 449 (2016)

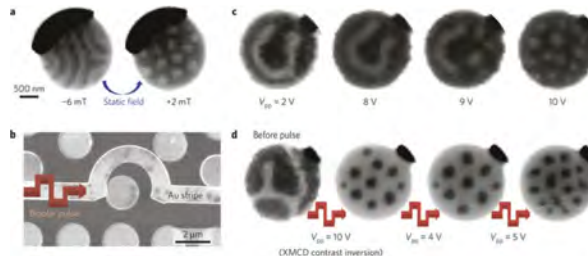
Multilayer

(Ir/Co/Pt)₁₀: ≈ 30–90 nm



C. Moreau-Luchaire *et al.*,
Nature Nanotechn. **11**, 444 (2016)

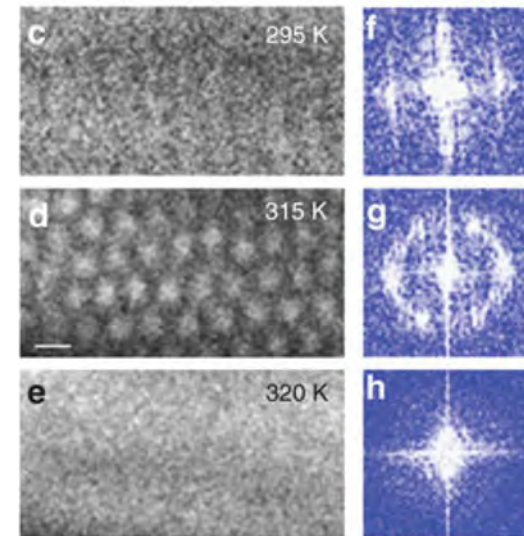
(Pt/Co/Ta)₁₅ and (Pt/CoFeB/MgO)₁₅:
≈ 100 nm



S. Woo *et al.*,
Nature Mater. **15**, 501 (2016)

Bulk

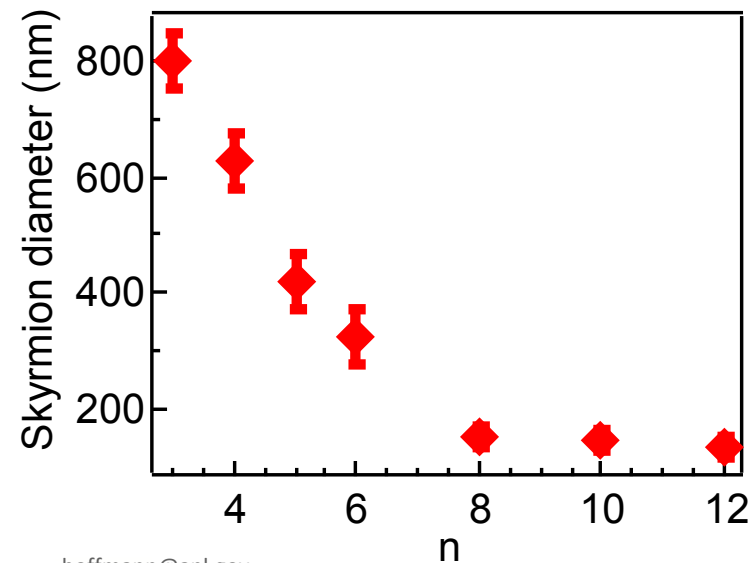
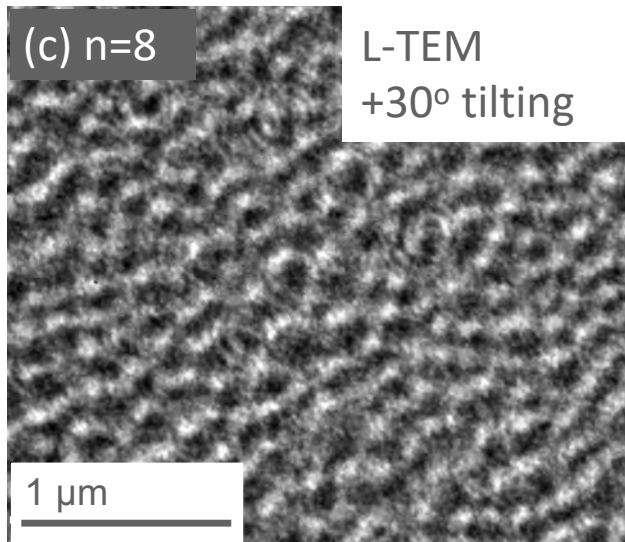
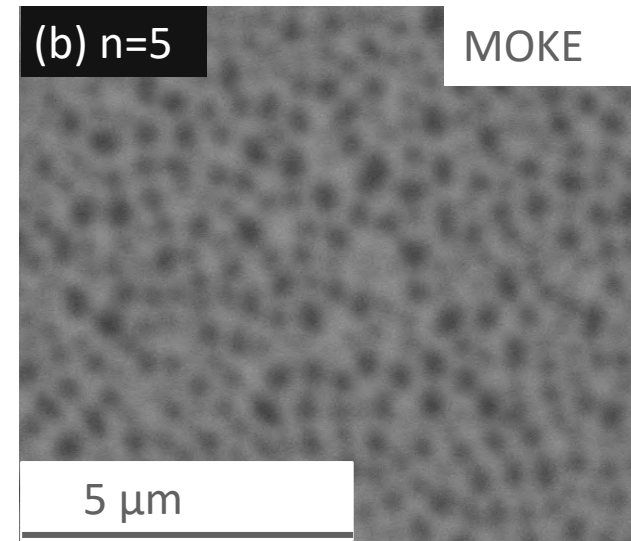
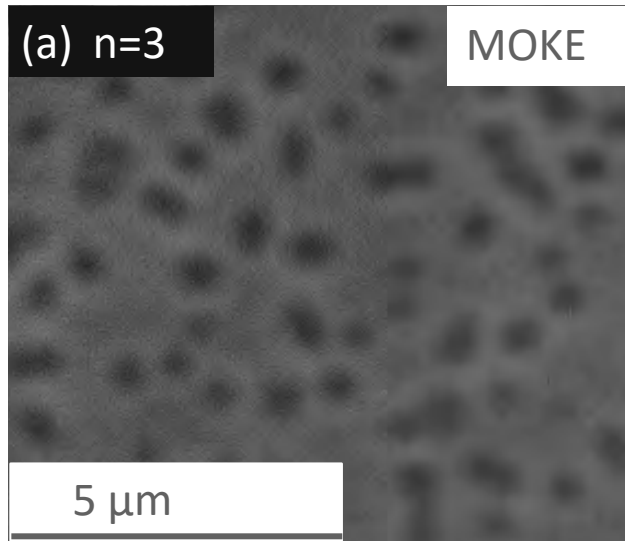
Co₈Zn₉Mn₃:
≈ 115–180 nm



Y. Tokunaga *et al.*,
Nature Comm. **6**, 7638 (2015)

Size Dependence on Number of Multilayers

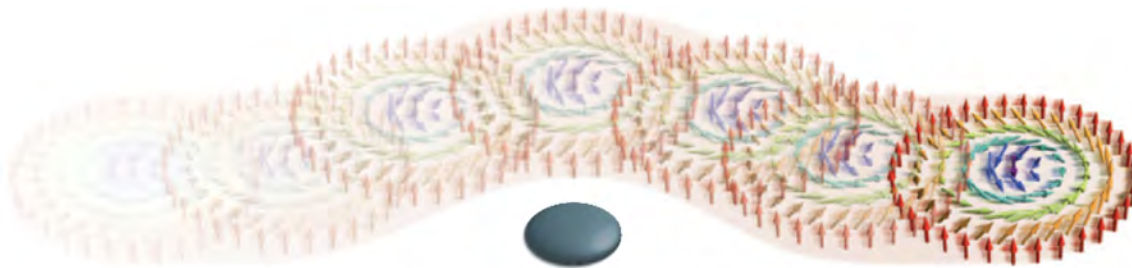
Sample: Ta 2.0nm/ (Pt 1.5 nm/Co 1.0 nm/Ir 1.0 nm) n / Pt 2.0 nm



Moving Skyrmions

Weak Pinning of Skyrmion Motion

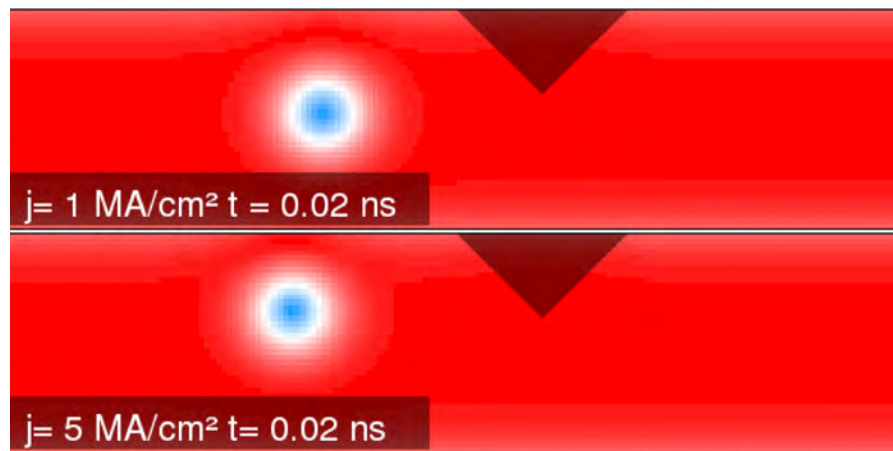
Skyrmions can move around defects



Skyrmion moving around obstacle

A. Rosch,
Nature Nano. 8, 160 (2013)

Micromagnetic Simulations

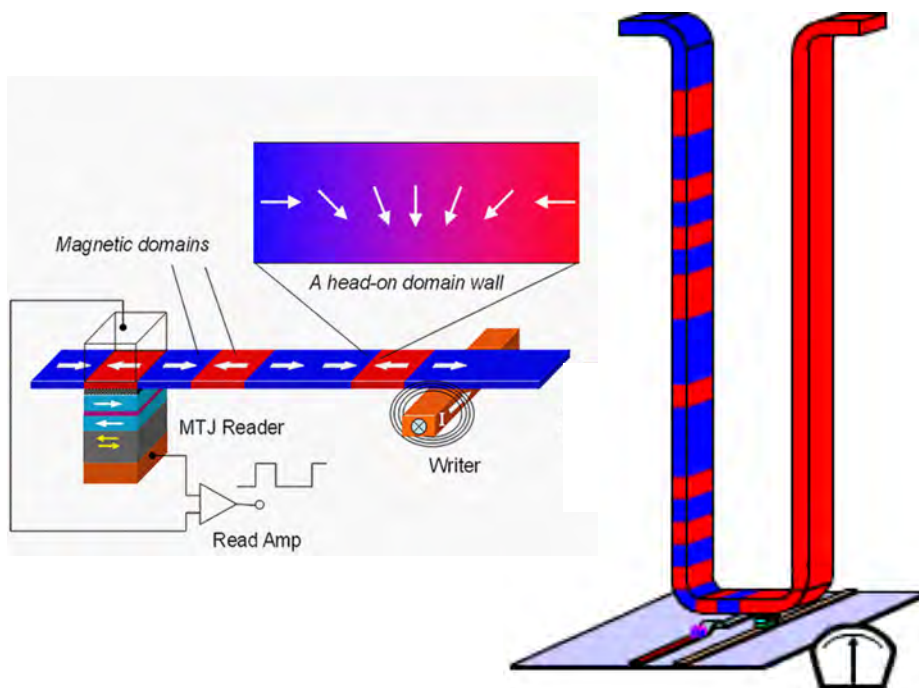


A. Fert *et al.*,
Nature Nano. 8, 152 (2013)

Encoding Information in Spin Textures

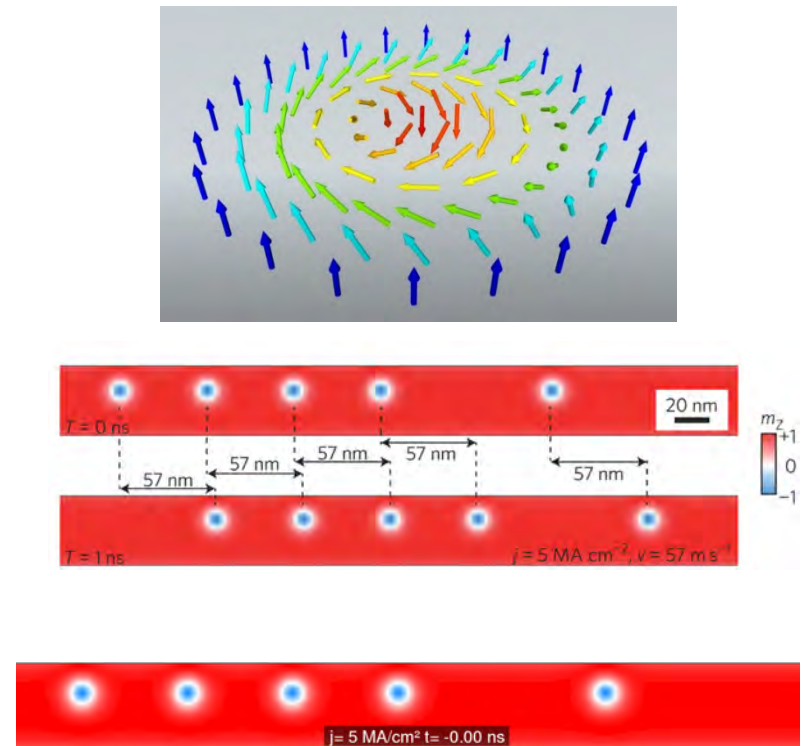
W. Jiang *et al.*, Phys. Rep. **704**, 1 (2017)

Racetrack Memory



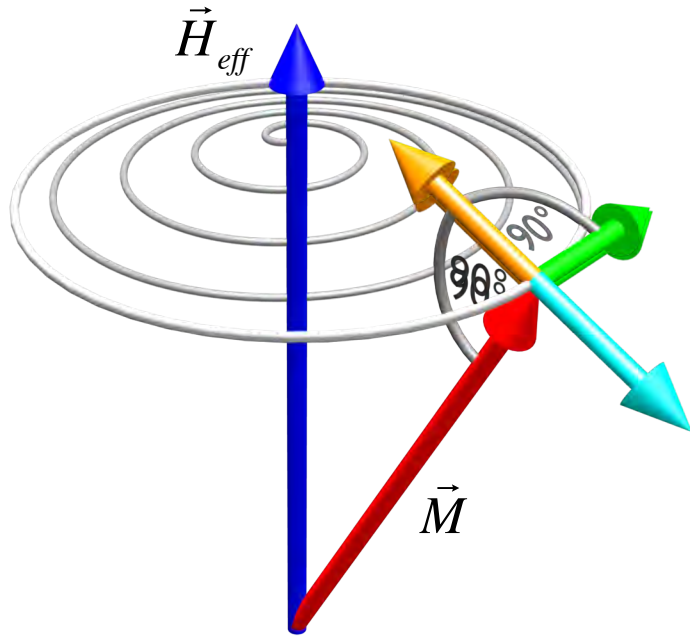
S. S. P. Parkin, M. Hayashi, and L. Thomas,
Science **320**, 190 (2008)

Skyrmions



A. Fert *et al.*, Nature Nano. **8**, 152 (2013)

Magnetization Dynamics with Spin-(Orbit) Torques



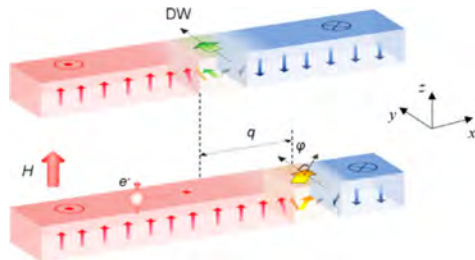
Landau-Lifshitz-Gilbert equation:

$$\frac{d\vec{M}}{dt} = -\gamma \vec{M} \times \vec{H}_{eff} + \frac{\alpha}{M_S} \left(\vec{M} \times \frac{d\vec{M}}{dt} \right) + \frac{\gamma \hbar \vec{J}_S}{2e M_S d_F}$$

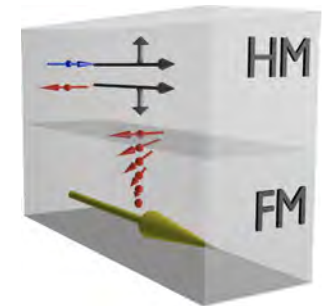
$$\vec{J}_S = \frac{\text{Re}(G_{mix})}{e} \vec{M} \times (\vec{M} \times \vec{\mu}_S) + \frac{\text{Im}(G_{mix})}{e} \vec{M} \times \vec{\mu}_S$$

damping-like

field-like



Spin accumulation generated within magnetic layer or adjacent layer



Thiele Equation

A. A. Thiele, Phys. Rev. Lett. **30**, 230 (1972)

Landau-Lifshitz-Gilbert equation

$$\frac{d\vec{M}}{dt} = -\gamma\vec{M} \times \vec{H}_{eff} + \frac{\alpha}{M_S} \left(\vec{M} \times \frac{d\vec{M}}{dt} \right) + \frac{\gamma\hbar\vec{J}_S}{2eM_S d_F} +$$

Rigid Skyrmion Texture



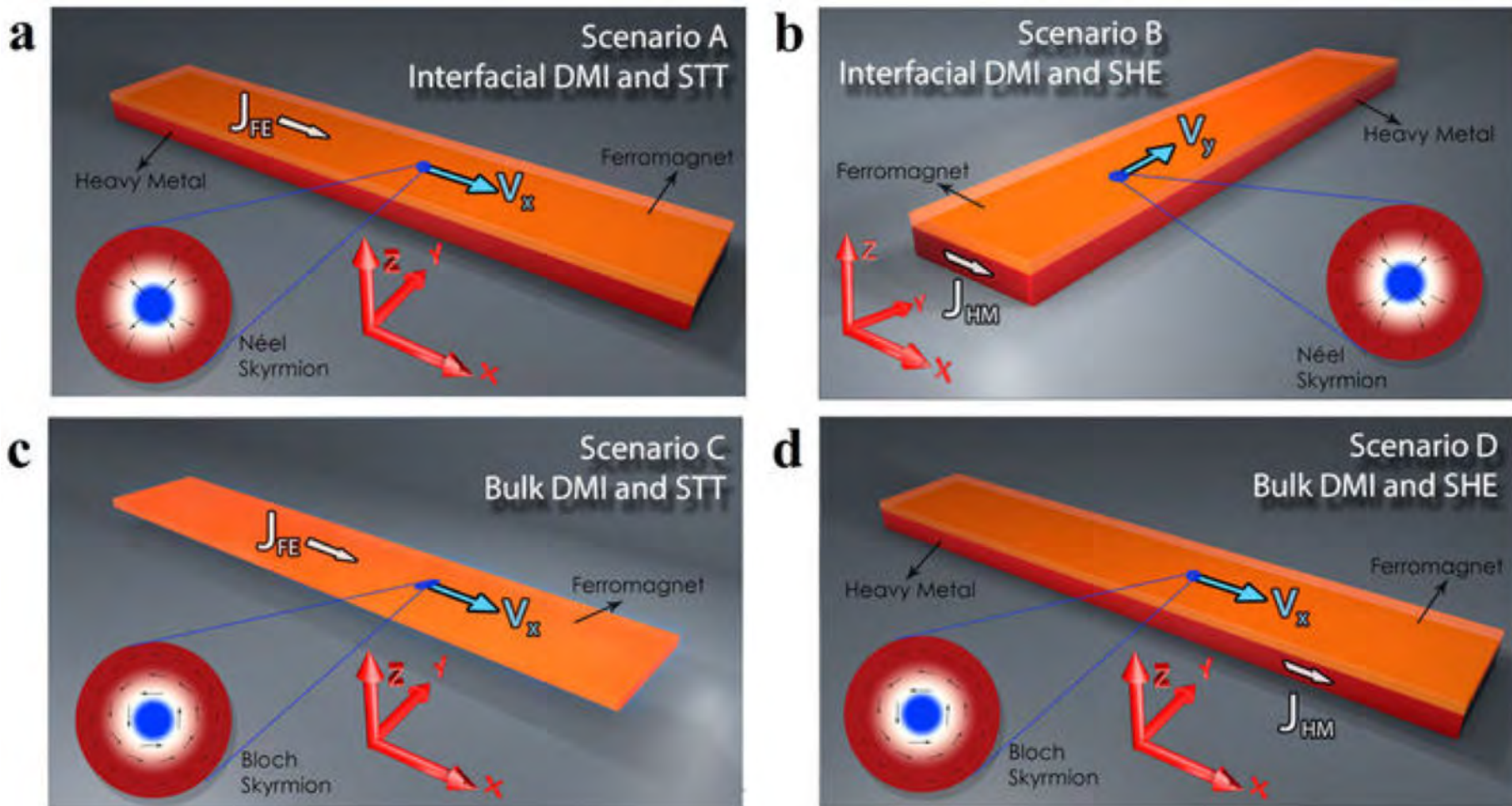
$$G \times v - \alpha D \cdot v + 4\pi \vec{B} J_c = 0$$

$$G = (0, 0, -4\pi Q)$$

$$Q = \frac{1}{4\pi} \int \mathbf{m} \cdot (\partial_x \mathbf{m} \times \partial_y \mathbf{m}) dx dy$$

R. Tomasello *et al.*, Sci. Rep. **4**, 6784 (2014)

Net Force Depends on Skyrmion Structure and Spin Torque Mechanism



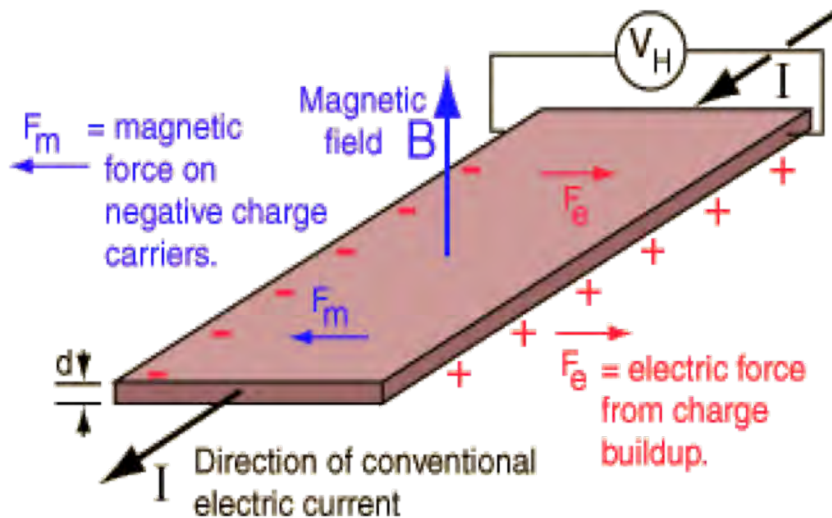
R. Tomasello *et al.*, *Sci. Rep.* **4**, 6784 (2014)

Skyrmion Hall Effect

Classic Hall effect

Electric charge q_e

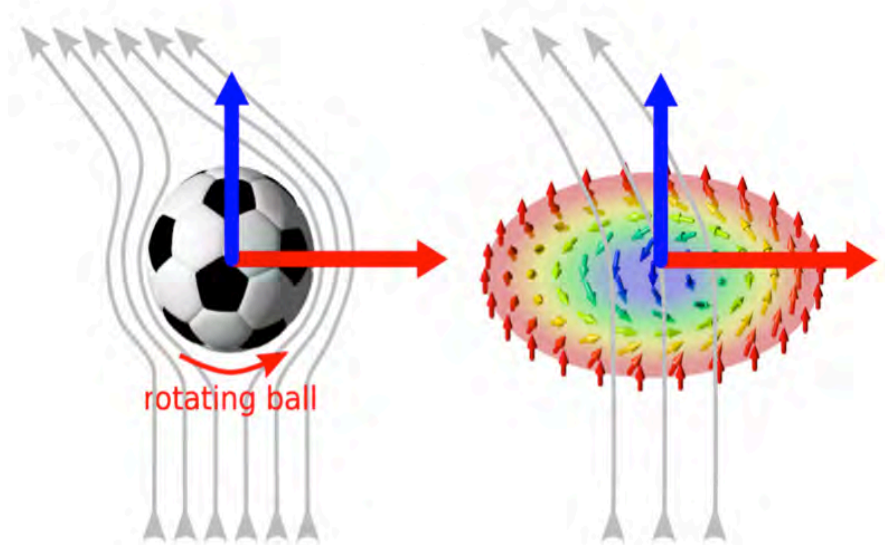
Lorentz force $q_e(\mathbf{v} \times \mathbf{B})$



Skyrmion Hall effect

Topological charge q_t

Magnus force $4\pi q_t(\mathbf{v} \times \mathbf{e}_z)$



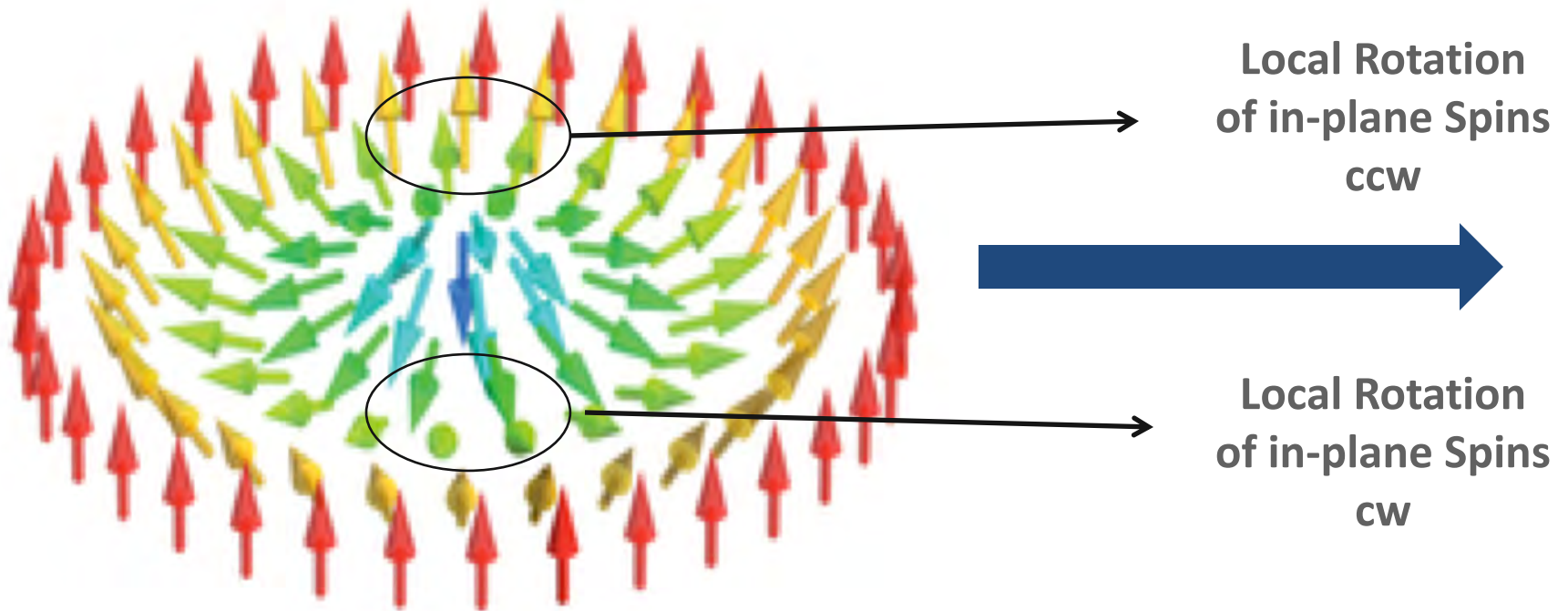
K. Everschor-Sitte and M. Sitte, J. Appl. Phys. **115**, 172602 (2014)

Motion of Rotating Objects

Famous Brazilian Expert: Roberto Carlos



Skyrmion in Motion



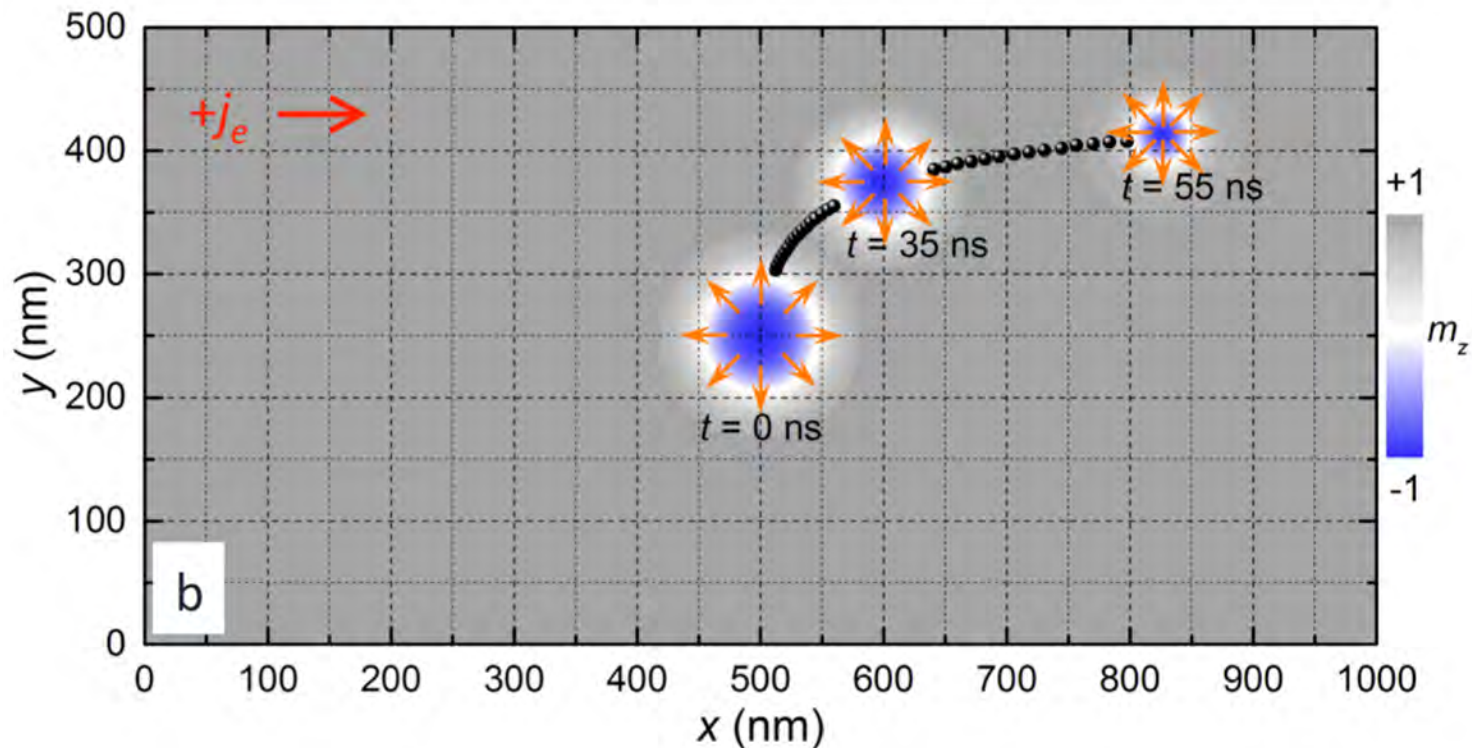
- Different rotation sense on both sides
- Looks like “opposite fields” => magnetic field gradient
- Results in transverse motion

Micromagnetic Simulation

W. Jiang *et al.*,
Nature Phys. **13**, 162 (2017)

Thiele Equation:
$$\mathbf{G} \times \mathbf{v} - \alpha \mathbf{D} \cdot \mathbf{v} + 4\pi \vec{\mathbf{B}} \mathbf{J}_c = 0$$

$$\mathbf{G} = (0, 0, -4\pi Q) \quad Q = \frac{1}{4\pi} \int \mathbf{m} \cdot (\partial_x \mathbf{m} \times \partial_y \mathbf{m}) dx dy$$

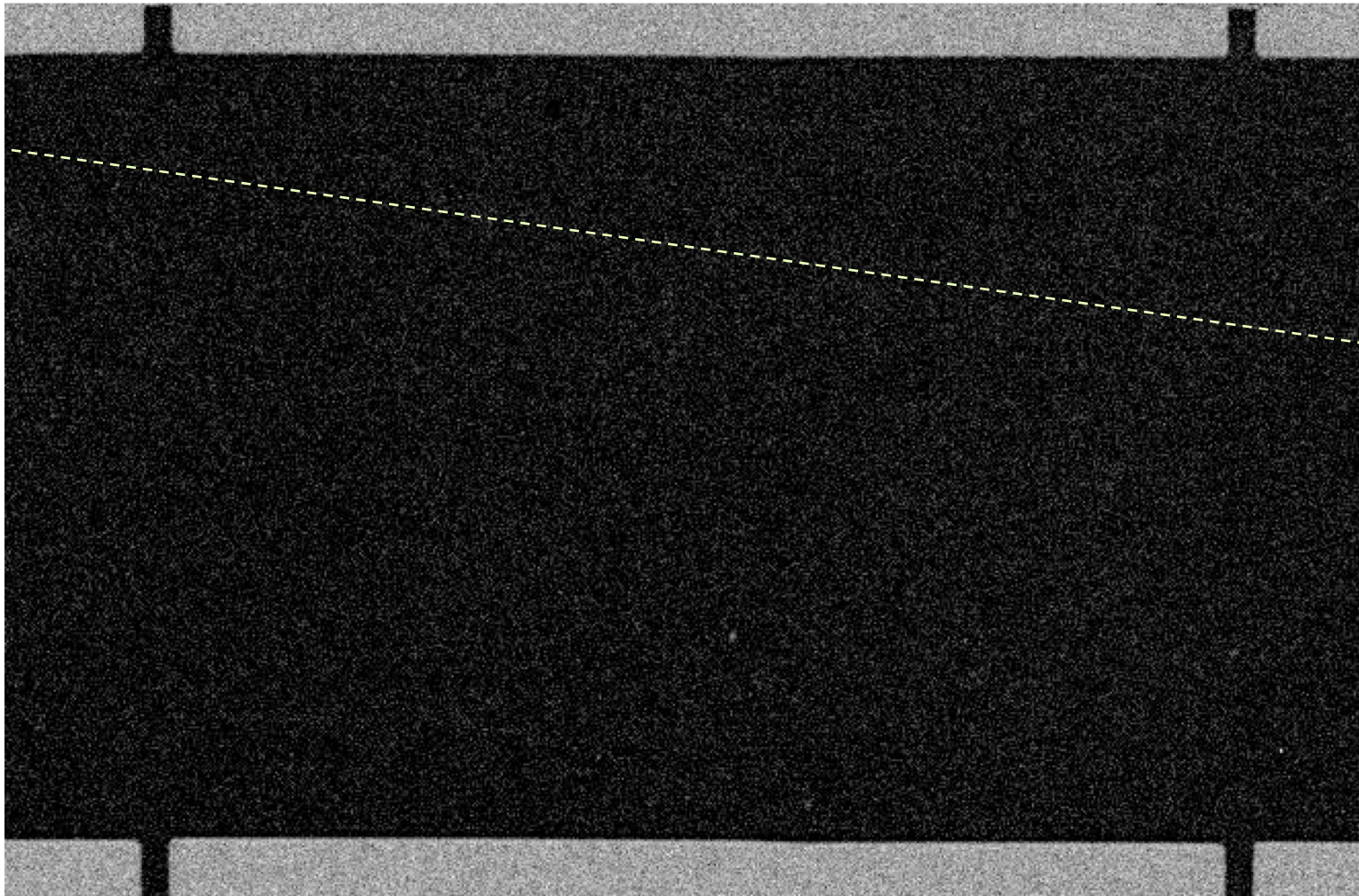


$$\frac{v_y}{v_x} = \frac{1}{\alpha D}$$

Skyrmion Motion with Homogeneous Current

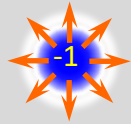
$$j_e = +2.8 \times 10^6 \text{ A/cm}^2$$

W. Jiang *et al.*,
Nature Phys. **13**, 162 (2017)

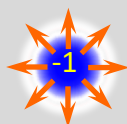
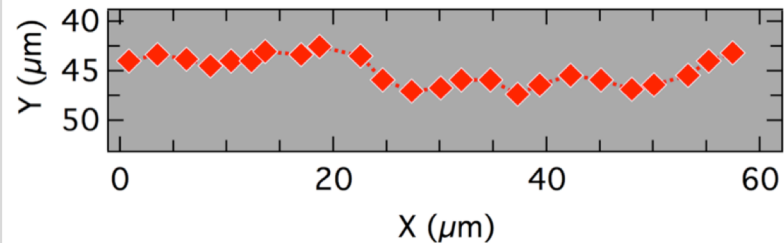
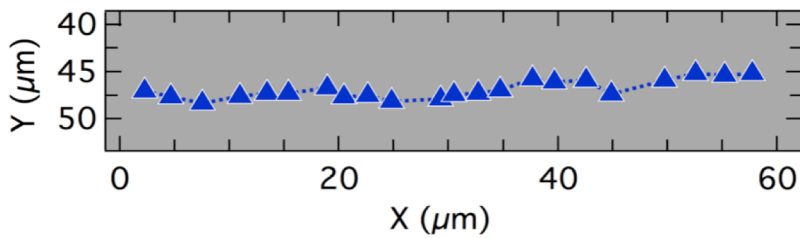
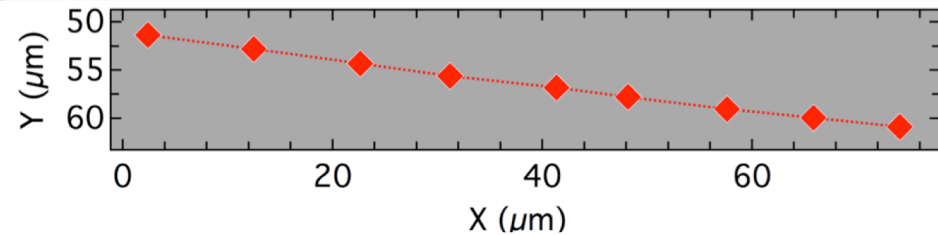
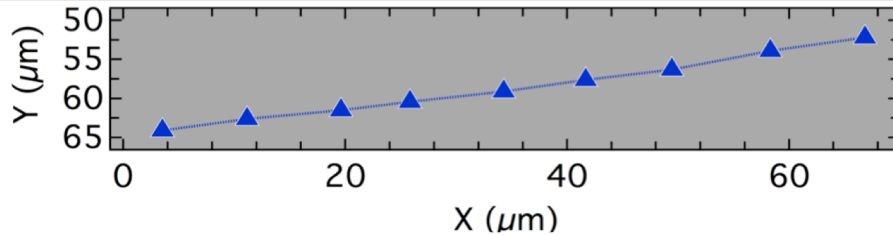
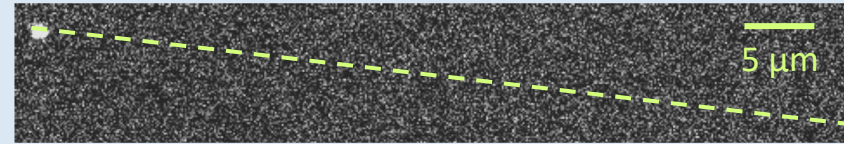
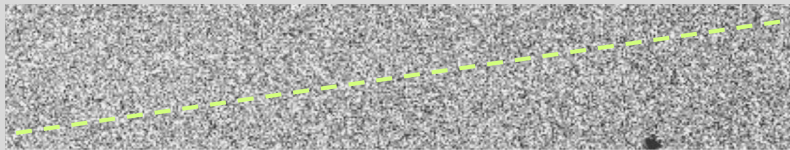
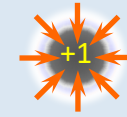


Current Dependence of Motion

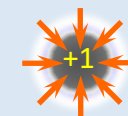
W. Jiang *et al.*,
Nature Phys. **13**, 162 (2017)



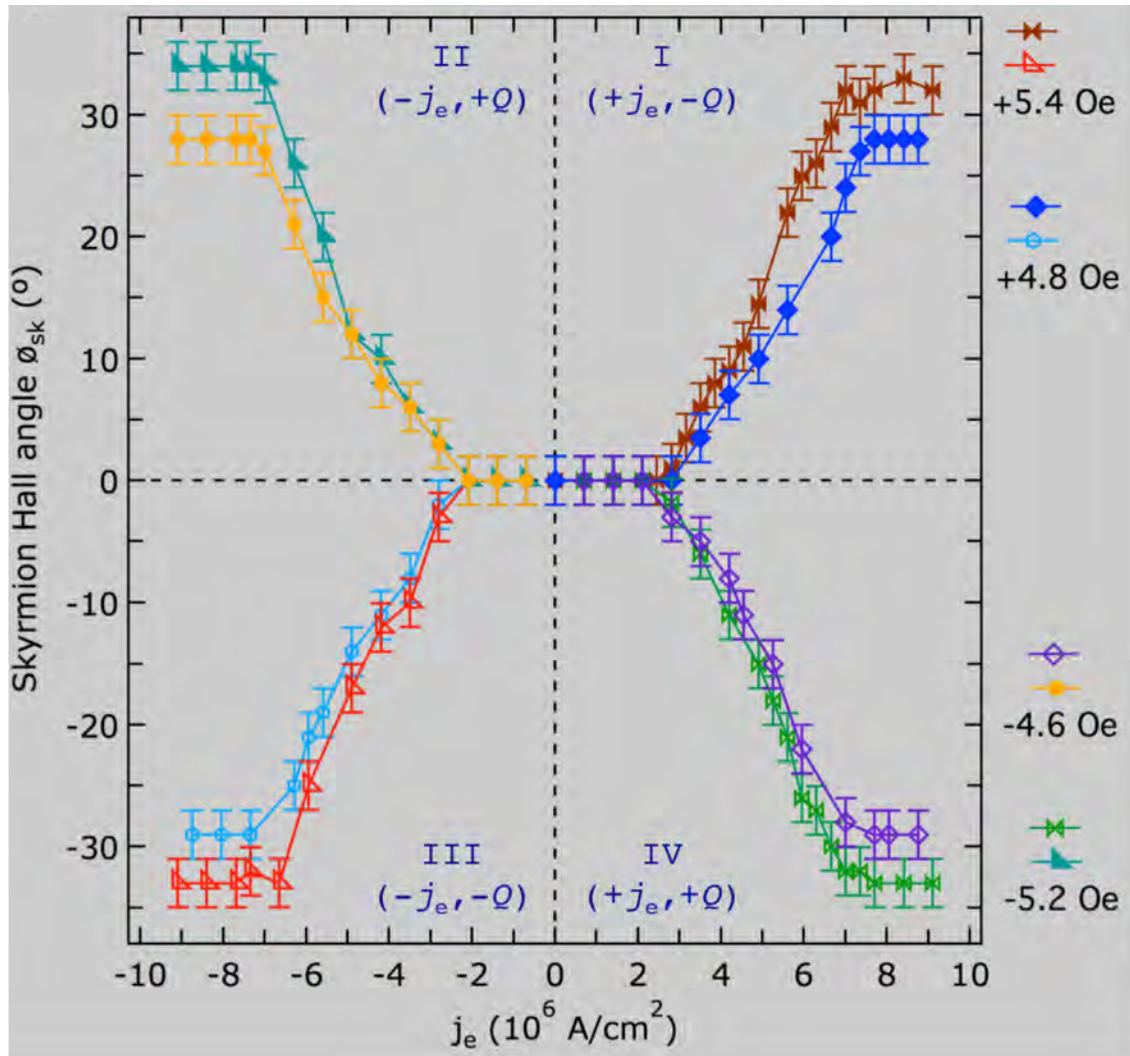
$$j_e = +2.8 \times 10^6 \text{ A/cm}^2 \rightarrow$$



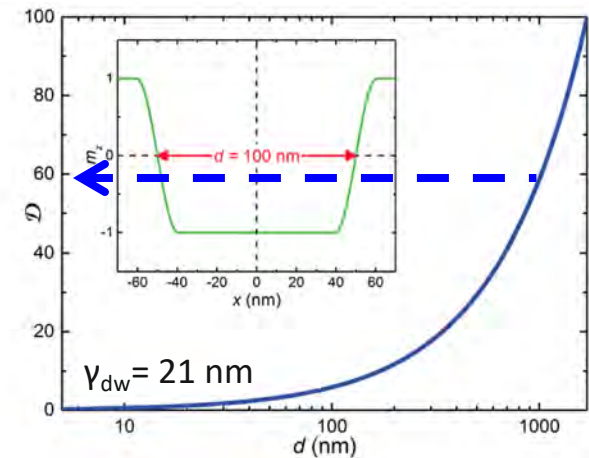
$$j_e = +1.3 \times 10^6 \text{ A/cm}^2 \rightarrow$$



Drive dependent Skyrmion Hall angle



$$D = \frac{\pi^2 d}{8\gamma_{dw}}$$



$$\frac{v_y}{v_x} = \frac{1}{\alpha D} \approx \mathbf{0.83}$$

$$\Phi_{sk} \approx \mathbf{40^\circ}$$

W. Jiang *et al.*,
Nature Phys. **13**, 162 (2017)

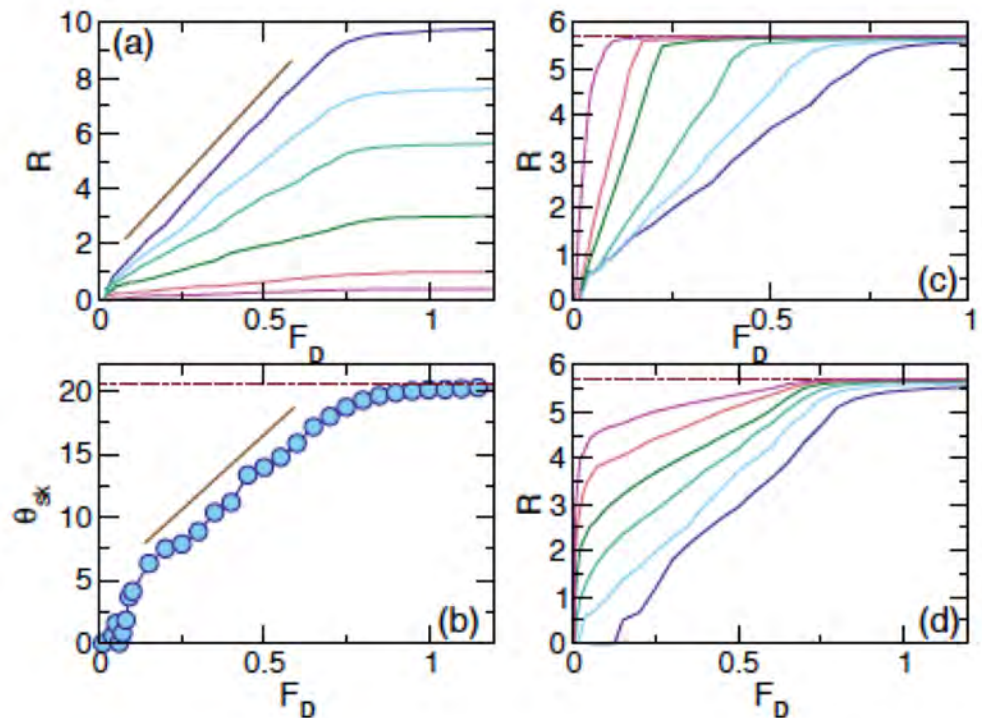
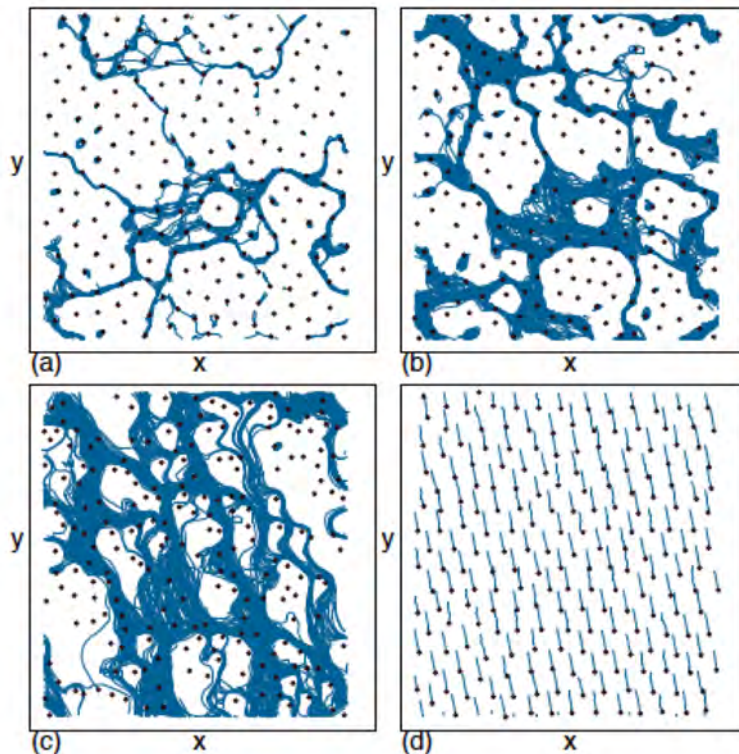
Numerical Simulations

Noise fluctuations and drive dependence of the skyrmion Hall effect in disordered systems

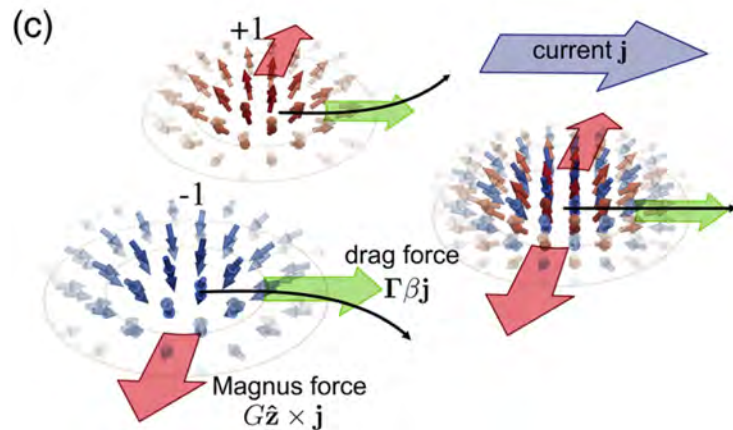
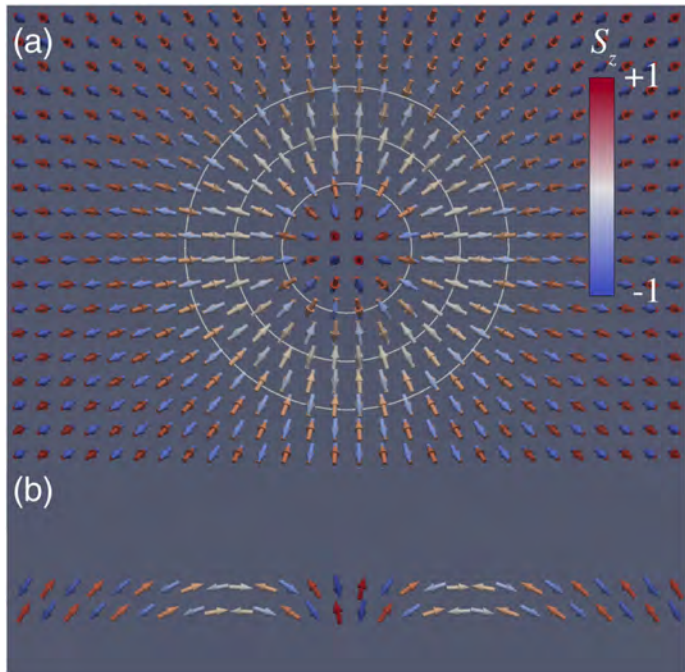
C Reichardt and C J Olson Reichardt

Theoretical Division and Center for Nonlinear Studies, Los Alamos National Laboratory, Los Alamos, NM 87545, USA

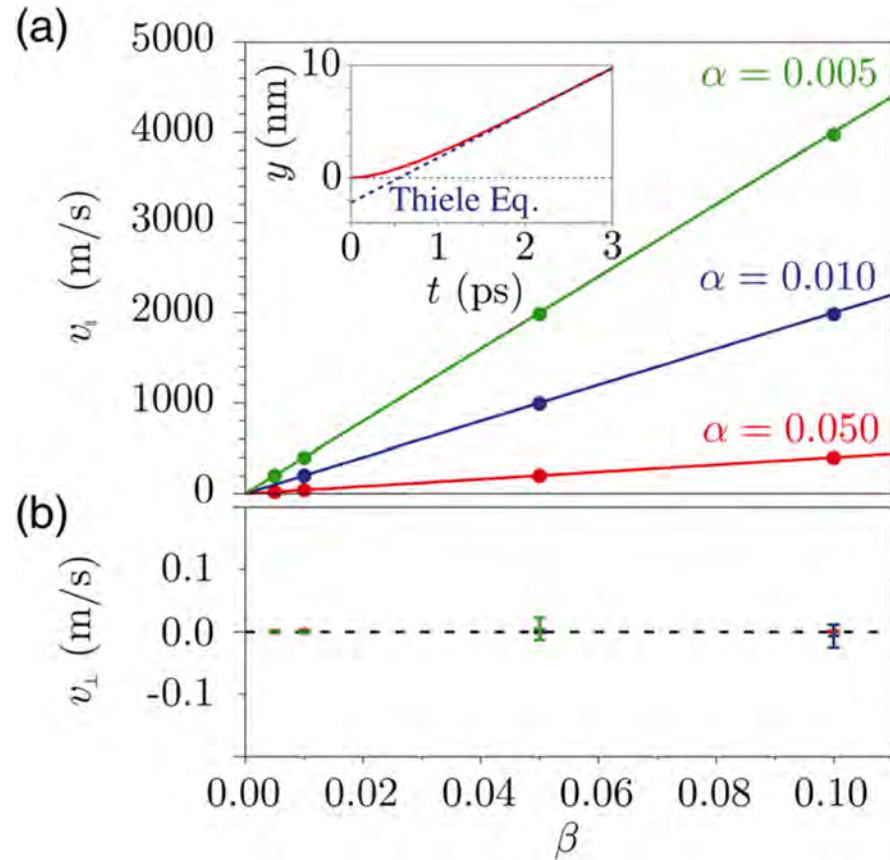
New J. Phys. **18**, 095005 (2016)



Antiferromagnetic Skyrmions



Avoid Skyrmion Hall Effect
No transverse velocity!

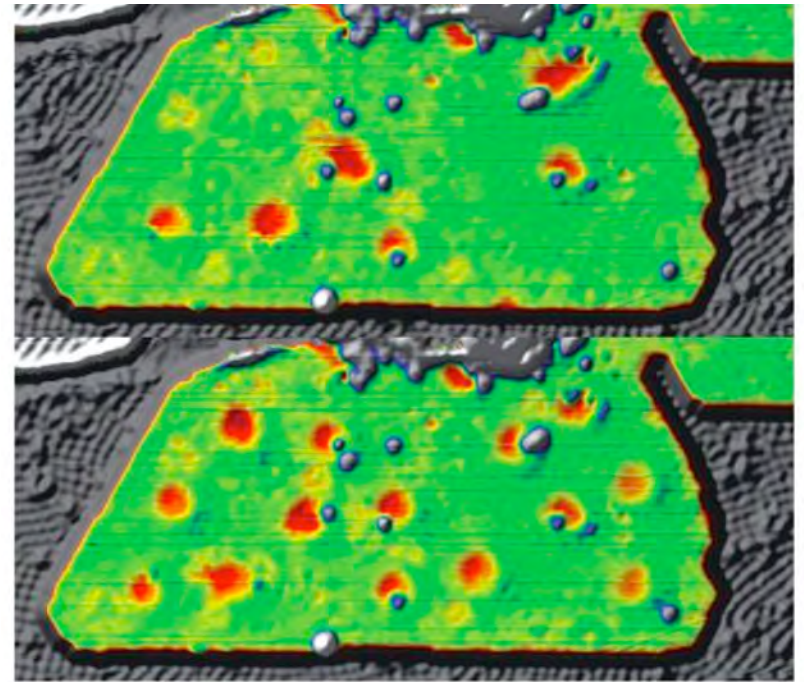
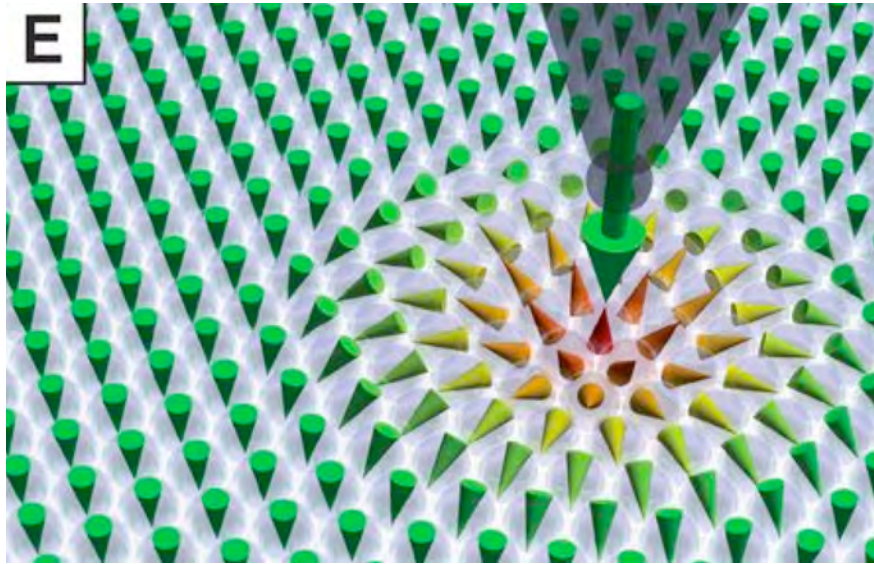


J. Barker and O. A. Tretiakov,
Phys. Rev. Lett. **116**, 147203 (2016)

Generating Skyrmions

Generating Individual Skyrmions

Using spin-polarized scanning tunneling microscope

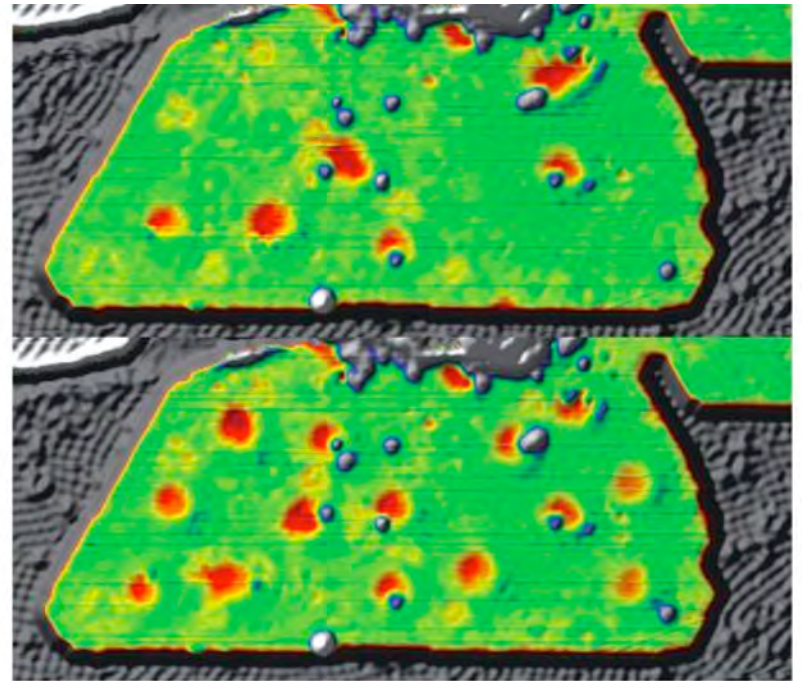
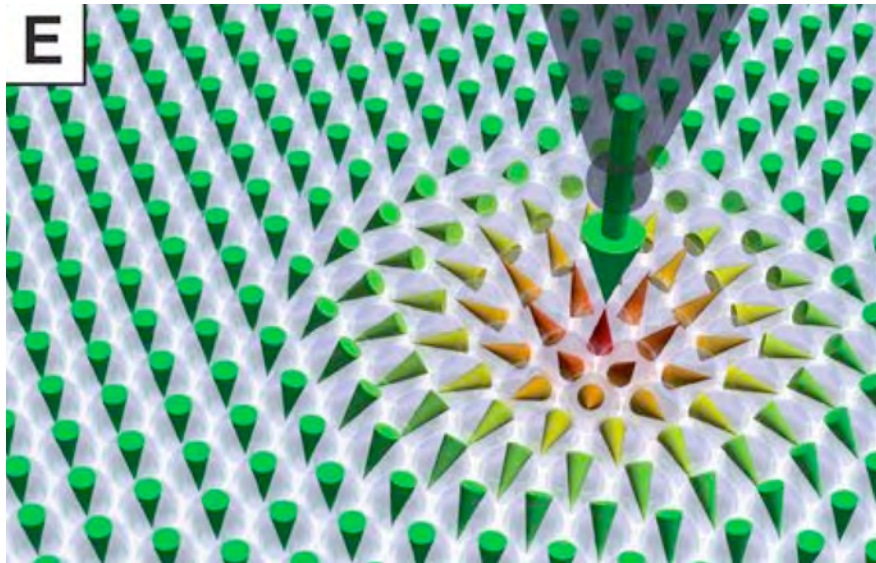


N. Romming, et al., Science **341**, 636 (2013)

Spin-transfer torque switches skyrmion core reversibly

Generating Individual Skyrmions

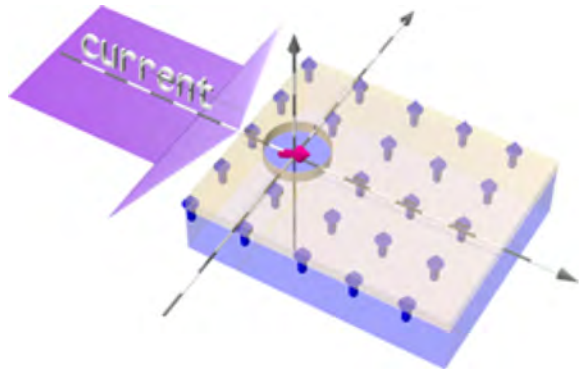
Using spin-polarized scanning tunneling microscope



Applied Goal:

Use **Topological Charge** instead of **Electronic Charge** in
Information Technologies

Inhomogeneities may Nucleate Skyrmions

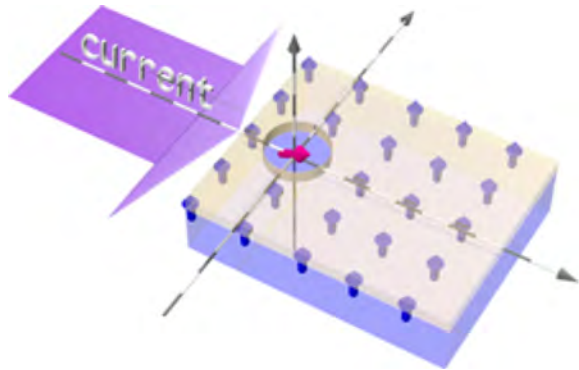


Without DMI:
Nucleation of skyrmion/anti-skyrmion pair

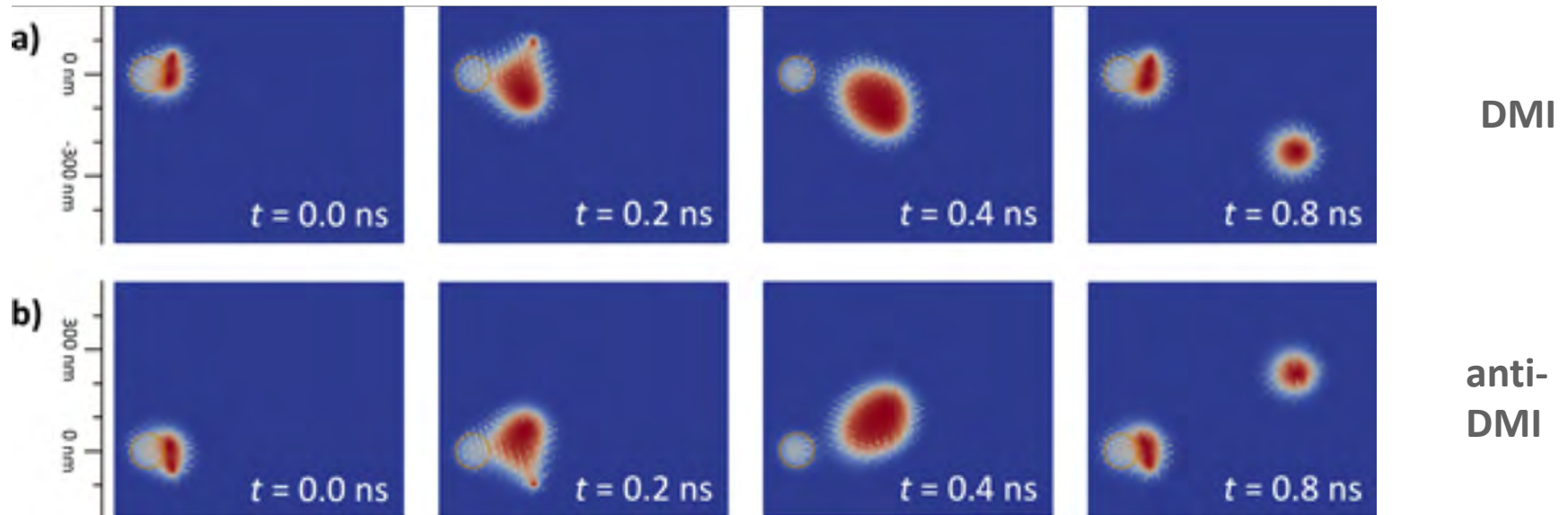


K. Everschor-Sitte, et al., New J. Phys. **19**, 092001 (2017)

Inhomogeneities may Nucleate Skyrmions



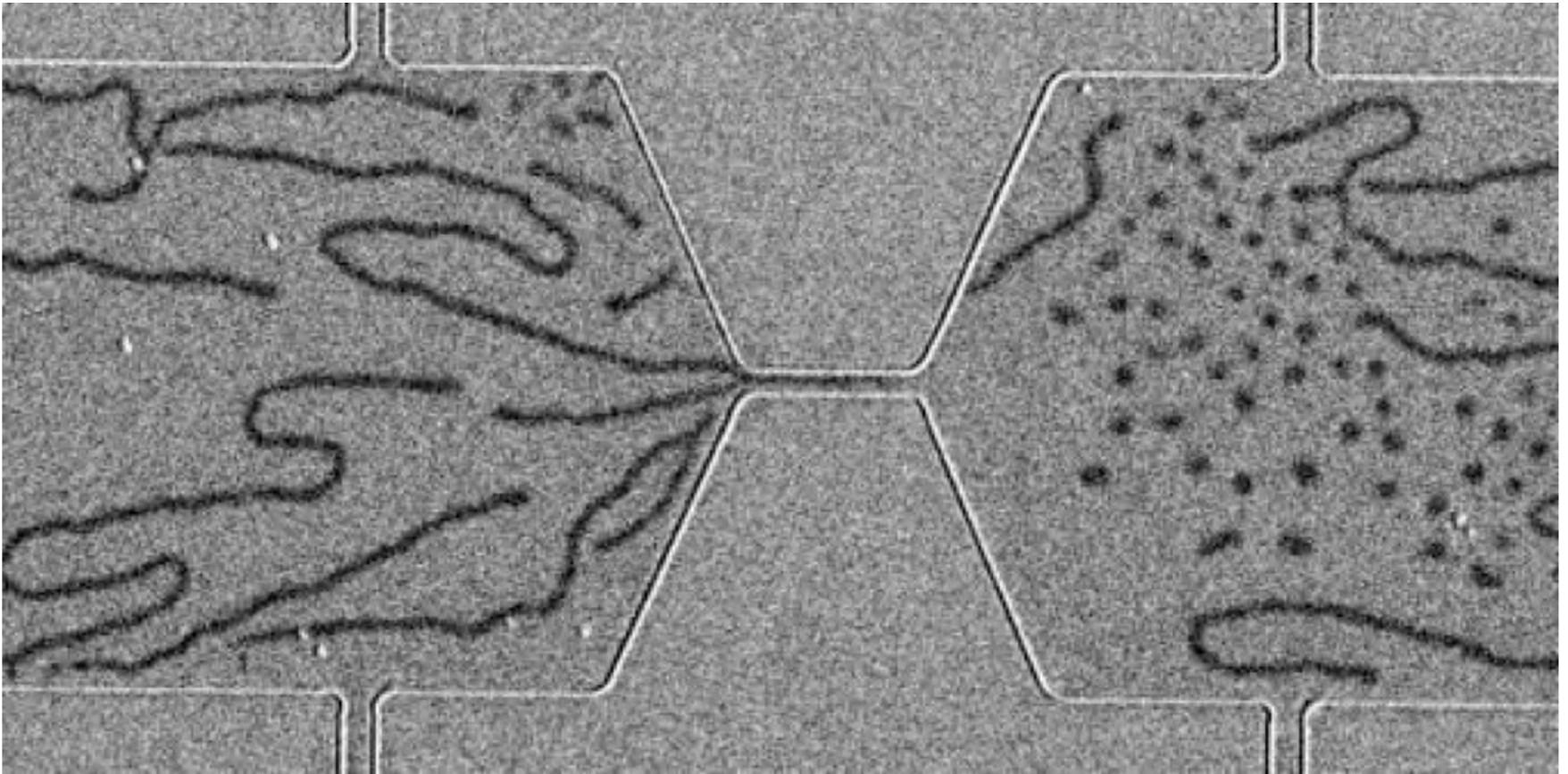
With DMI or anti-DMI:
Stabilize only one of the two pair-partners



K. Everschor-Sitte, et al., New J. Phys. **19**, 092001 (2017)

Skyrmion Generation from Inhomogeneous Current

$B_{\perp} = +0.46$ mT, DC current $J_e = + 6.8 \times 10^4$ A/cm²
TaO_x/CoFeB/Ta



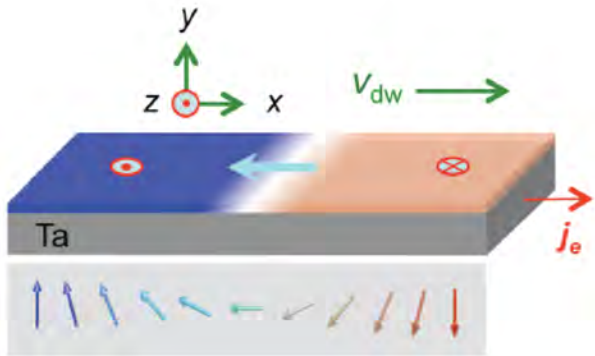
W. Jiang *et al.*, Science **349**, 283 (2015)

Axel Hoffmann, Materials Science Division, Argonne National Laboratory

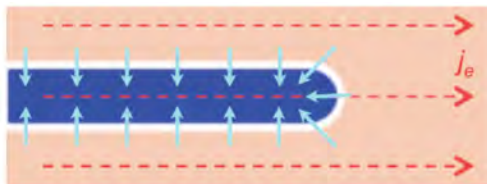
hoffmann@anl.gov



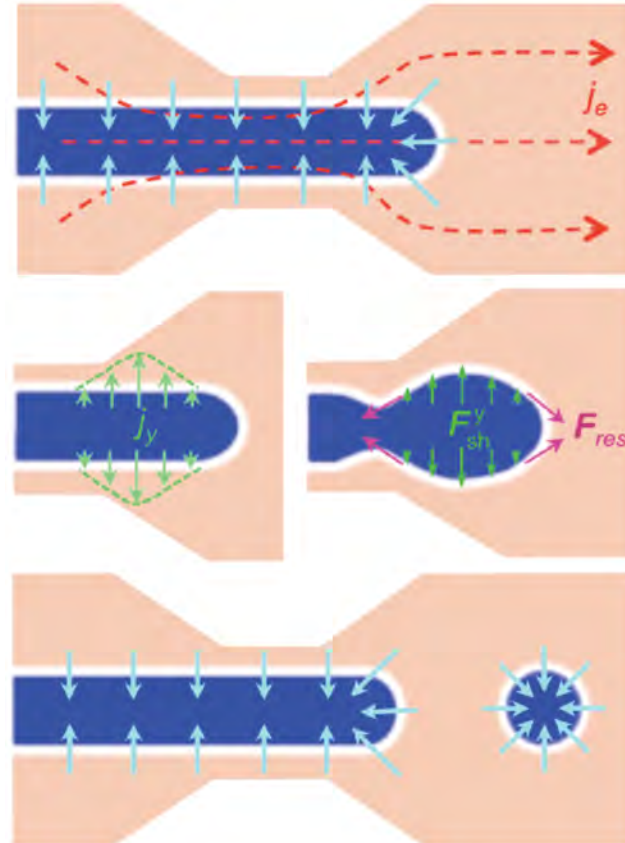
Inhomogeneous Chiral Spin Orbit Torques



Stripe Domain with Homogeneous Current



Stripe Domain with Inhomogeneous Current

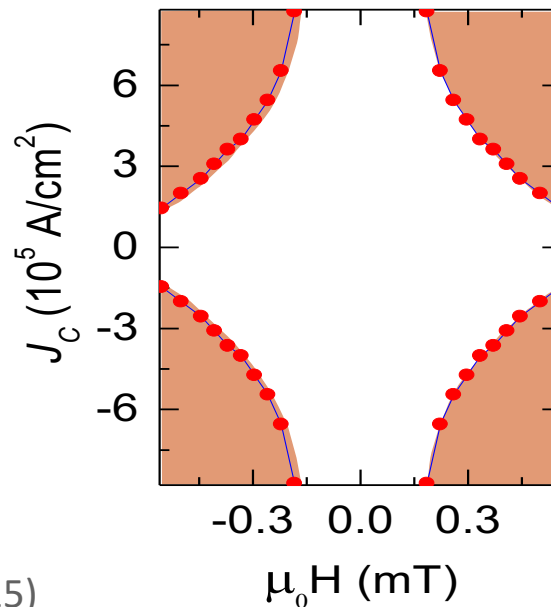
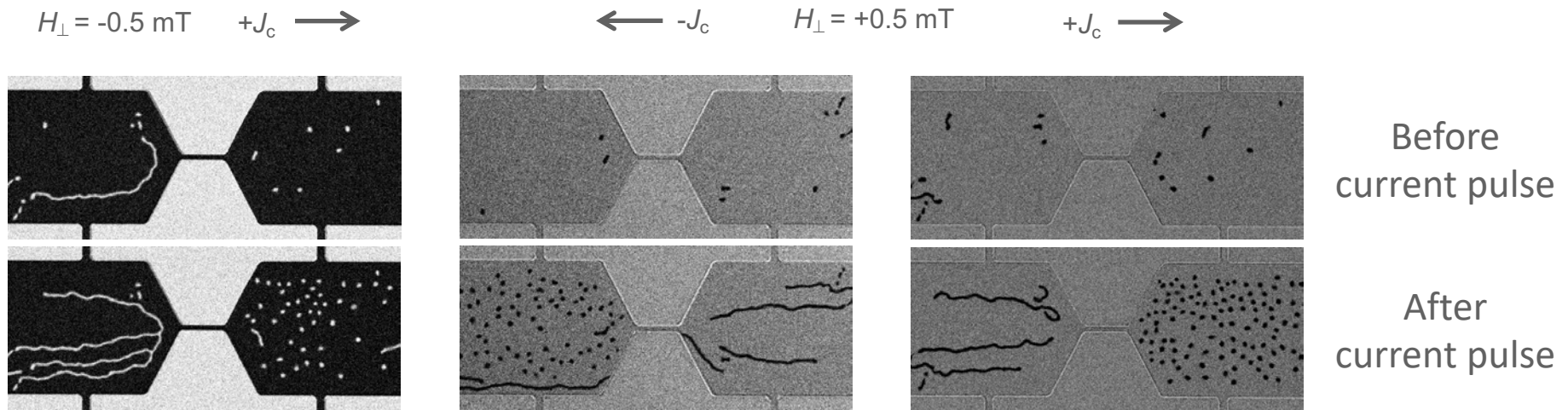


W. Jiang *et al.*, Science **349**, 283 (2015)

Axel Hoffmann, Materials Science Division, Argonne National Laboratory

hoffmann@anl.gov

Skyrmion Generation Phase Diagram

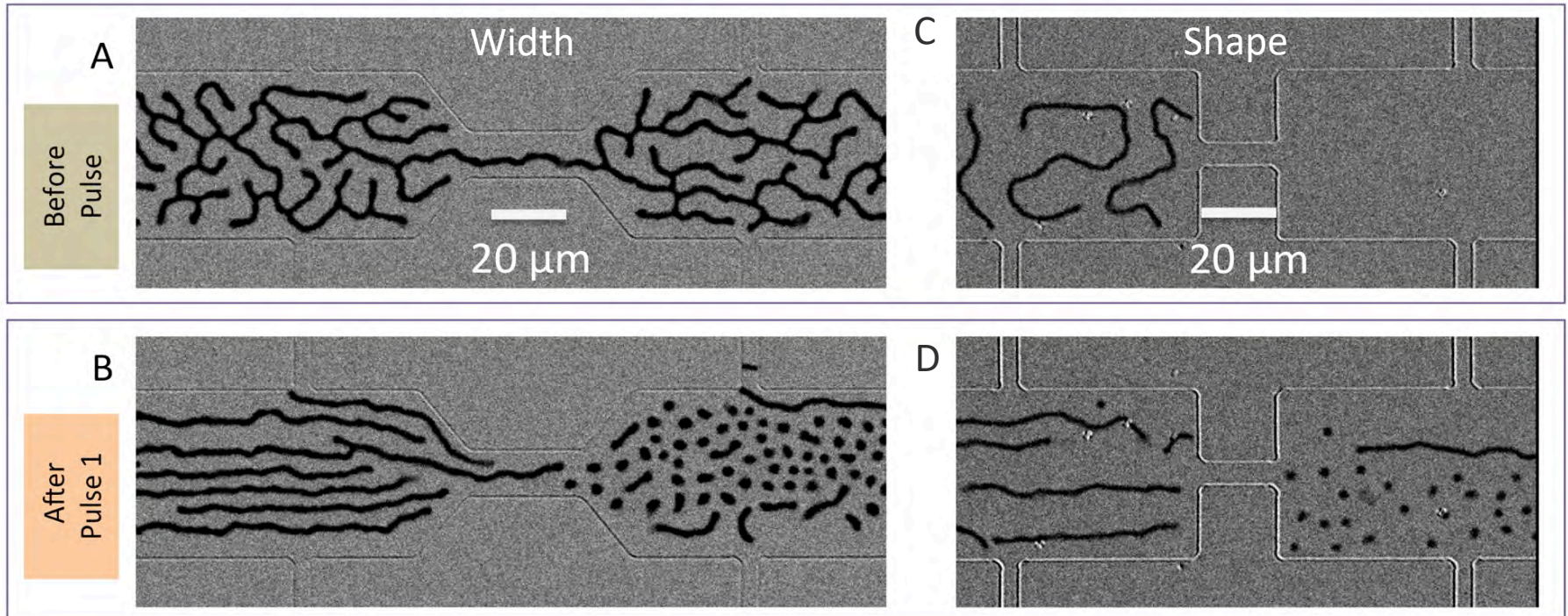


W. Jiang *et al.*, Science **349**, 283 (2015)

Axel Hoffmann, Materials Science Division, Argonne National Laboratory

hoffmann@anl.gov

Different Geometries



Skyrmion generation is robust
Spatially divergent currents are the key

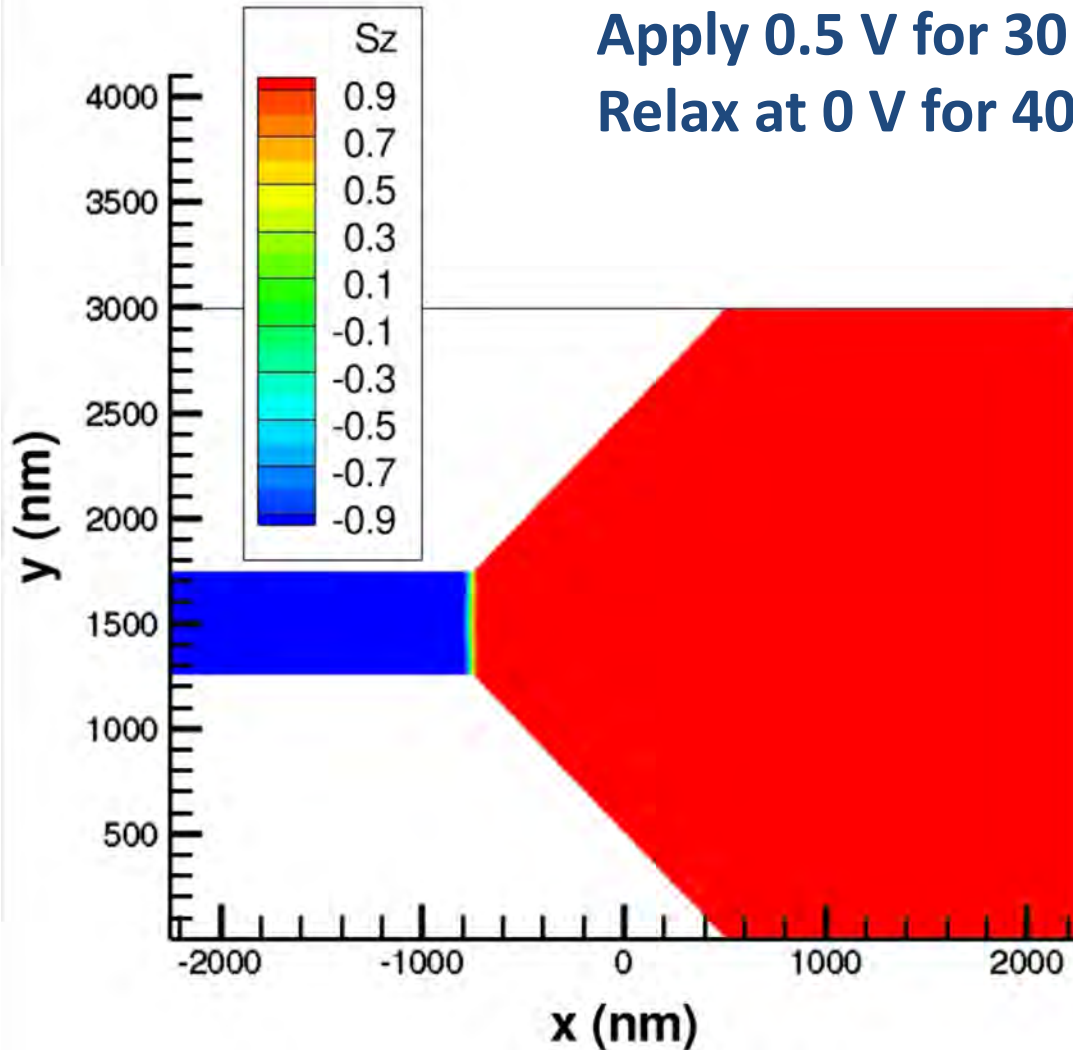
W. Jiang *et al.*, *Science* **349**, 283 (2015)

Axel Hoffmann, Materials Science Division, Argonne National Laboratory

hoffmann@anl.gov



Micromagnetic Simulation of Transformation

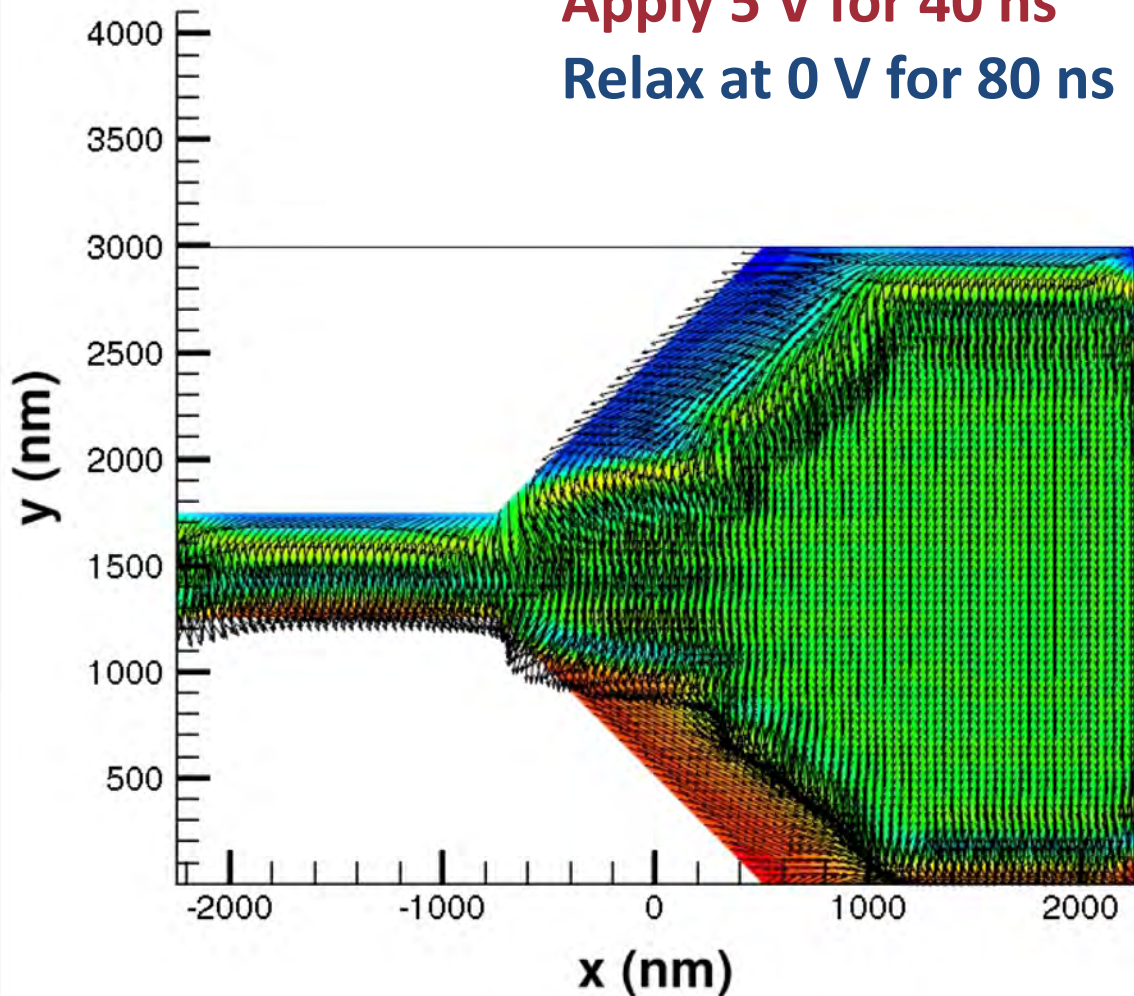


$H = 5$ Oe
 $M_s = 650$ emu/cm³
 $H_a = 8868$ Oe
 $A = 3$ μ erg/cm
 $DMI = 0.5$ erg/cm²
 $\alpha = 0.02$
 $\sigma_{Ta} = 0.83$ MS
 $\theta_{sh} = 10\%$

O. Heinonen *et al.*,
Phys. Rev. B **93**, 094407 (2016)

Micromagnetic Simulation of Transformation

Apply 5 V for 40 ns
Relax at 0 V for 80 ns

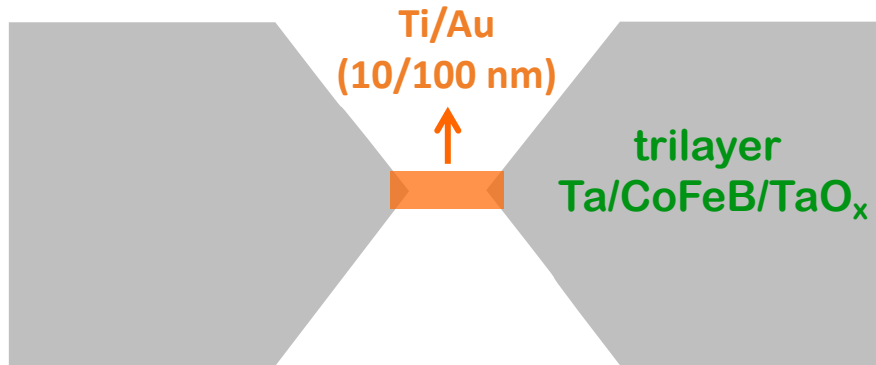


$H = 5 \text{ Oe}$
 $M_s = 650 \text{ emu/cm}^3$
 $H_a = 8868 \text{ Oe}$
 $A = 3 \text{ } \mu\text{erg/cm}$
 $\text{DMI} = 0.5 \text{ erg/cm}^2$
 $\alpha = 0.02$
 $\sigma_{\text{Ta}} = 0.83 \text{ MS}$
 $\theta_{\text{sh}} = 10\%$

**Two distinct
mechanisms for
skyrmion
generation!**

O. Heinonen *et al.*,
Phys. Rev. B **93**, 094407 (2016)

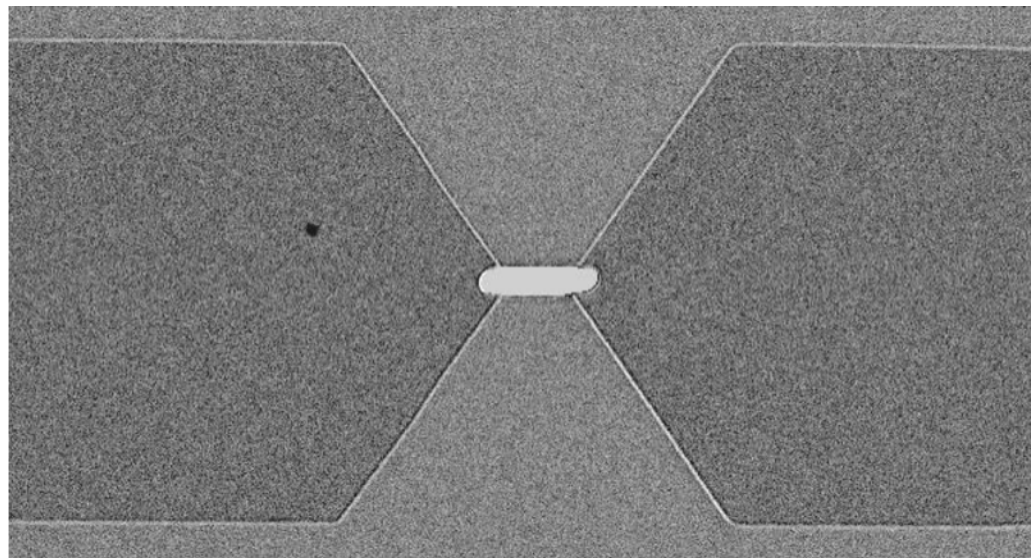
Creation of Skyrmions via Nonmagnetic Contacts



No stripe domains through
No heat involved
Only divergence of current

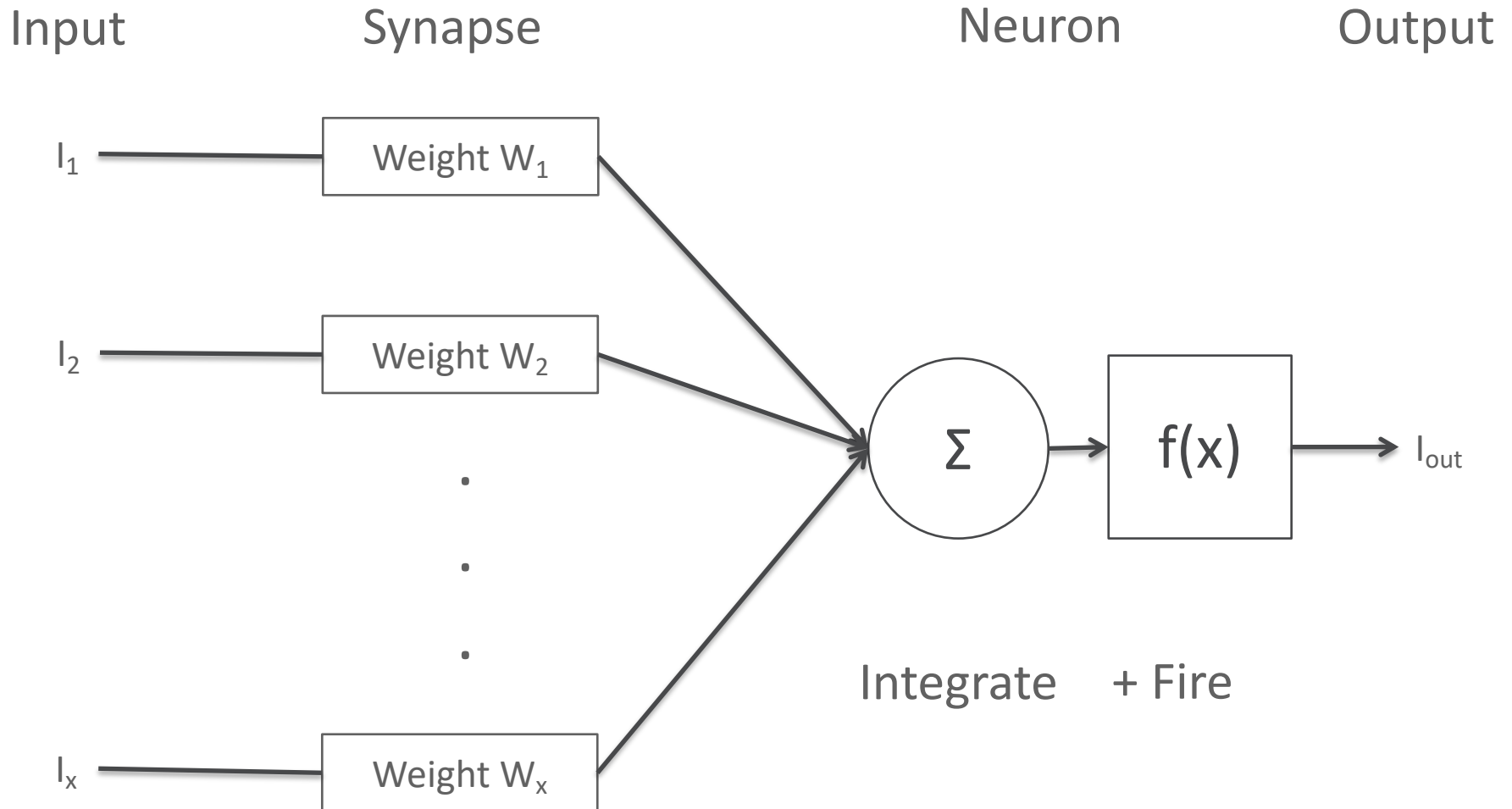
Requires Larger Currents

Pulse current: 15 V of duration 1 ms at 1 Hz

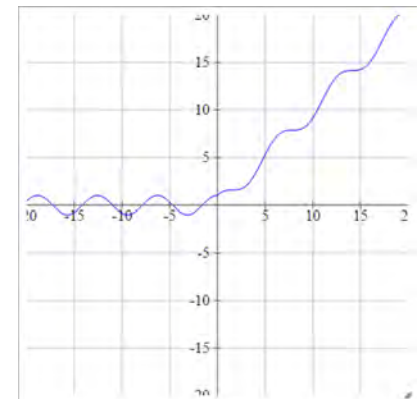
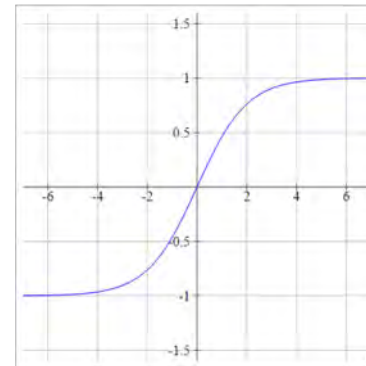
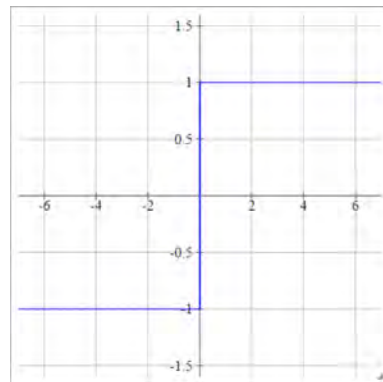
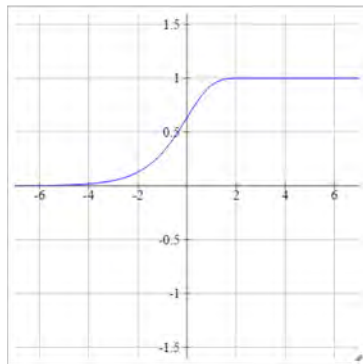
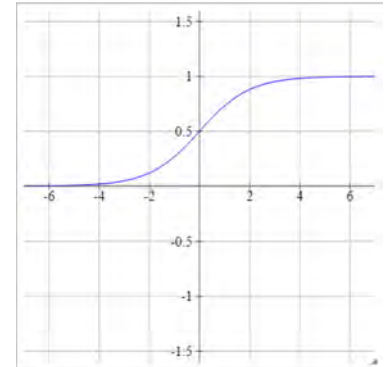
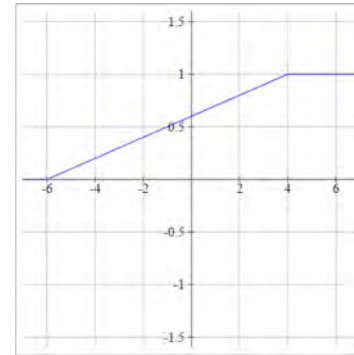
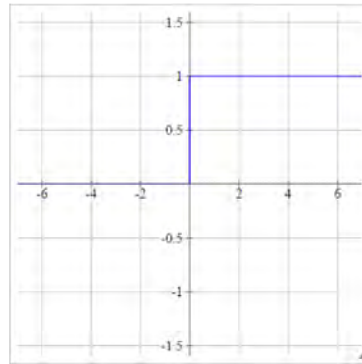
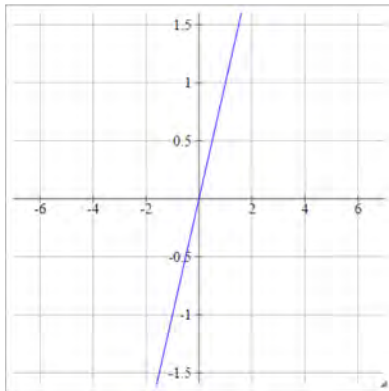


Skymions meet Neuromorphic

Basic Neuromorphic Concept



Possible Transfer Functions



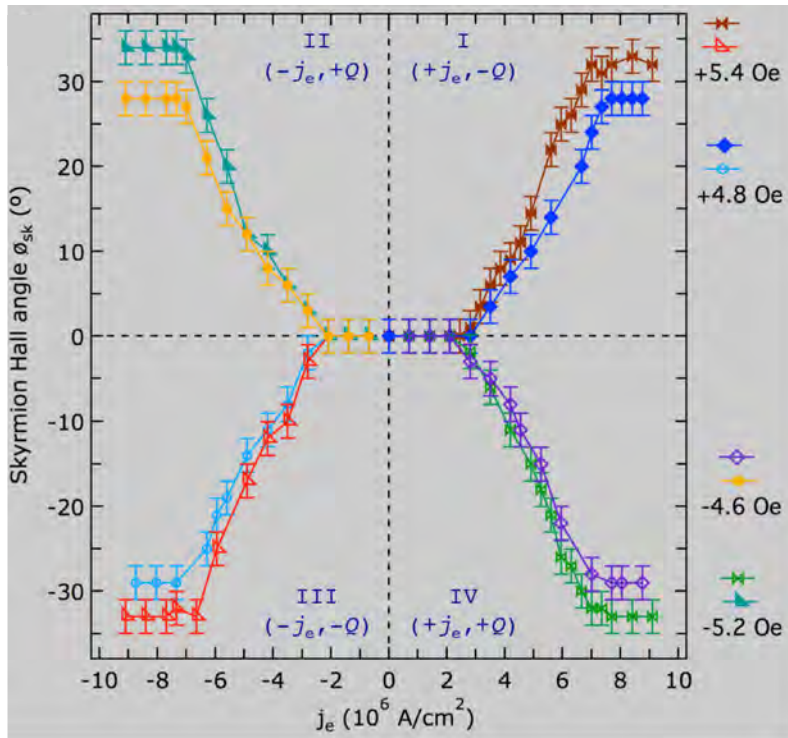
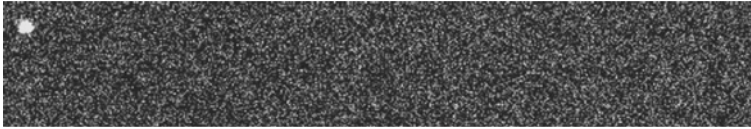
<https://stats.stackexchange.com/questions/115258/comprehensive-list-of-activation-functions-in-neural-networks-with-pros-cons>

Neural network algorithms adjust weights of synapses AND transfer function during training!

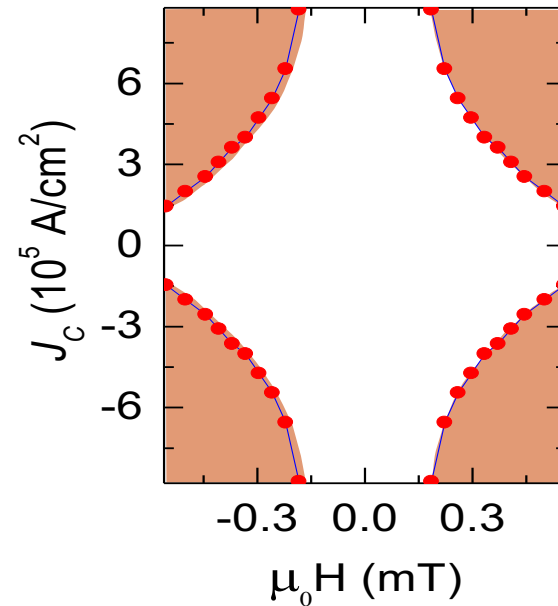
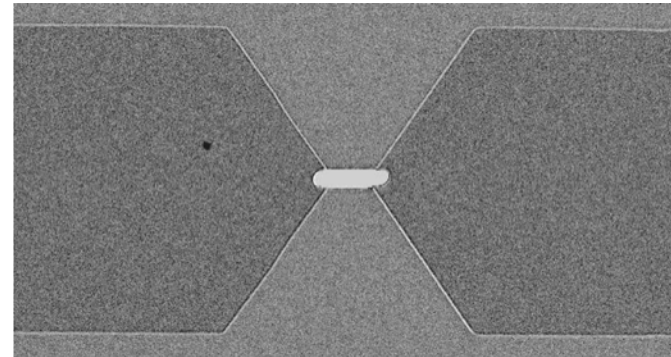
What nonlinear behavior can be used with skyrmions?

Nonlinear Phenomena

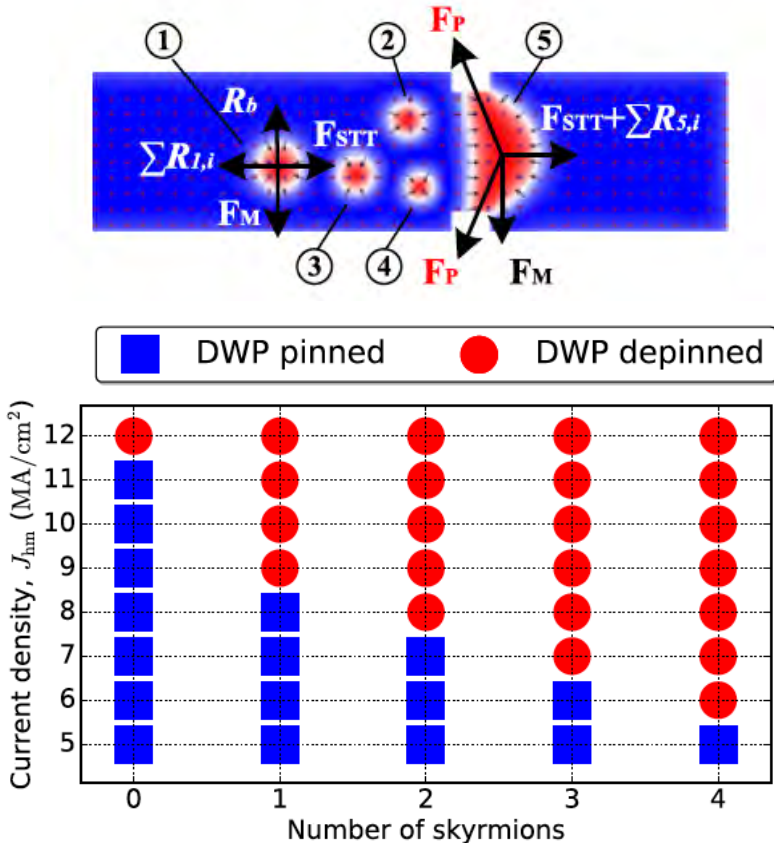
Transverse Motion



Generation and Depinning

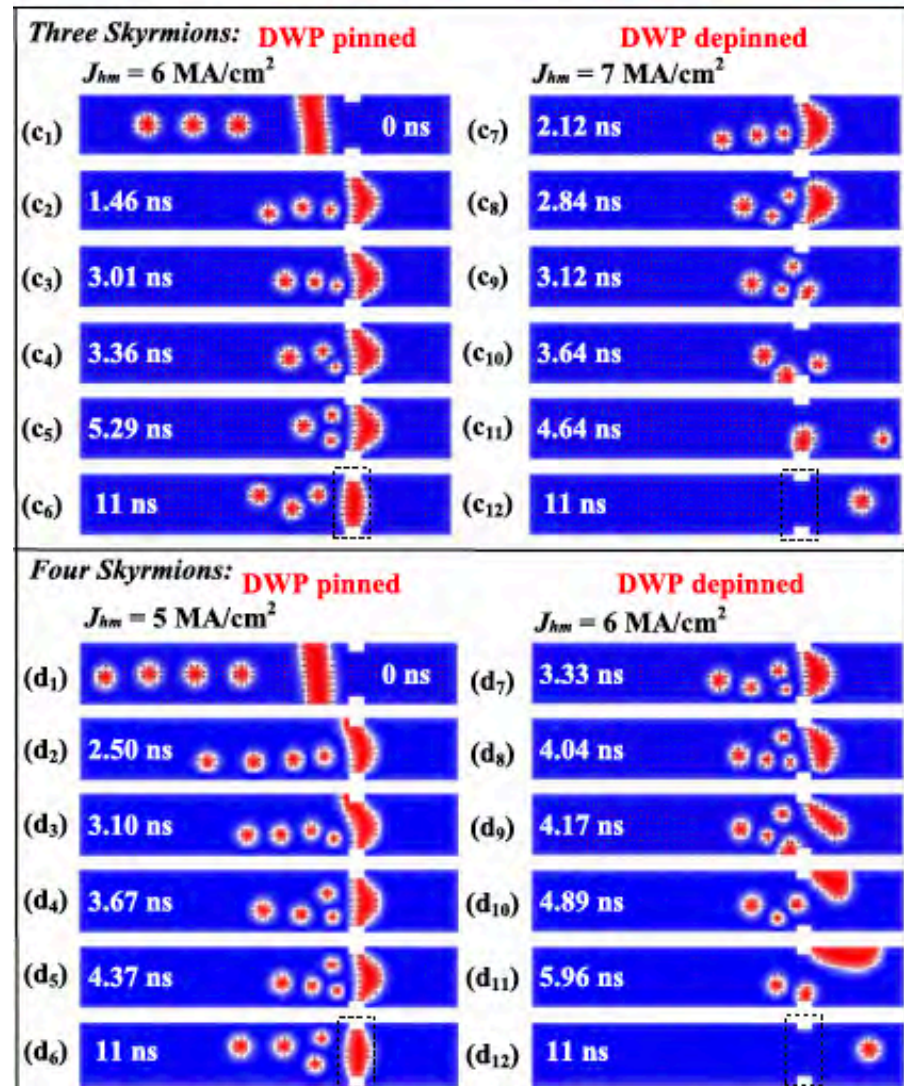


Depinning due to skyrmion accumulation



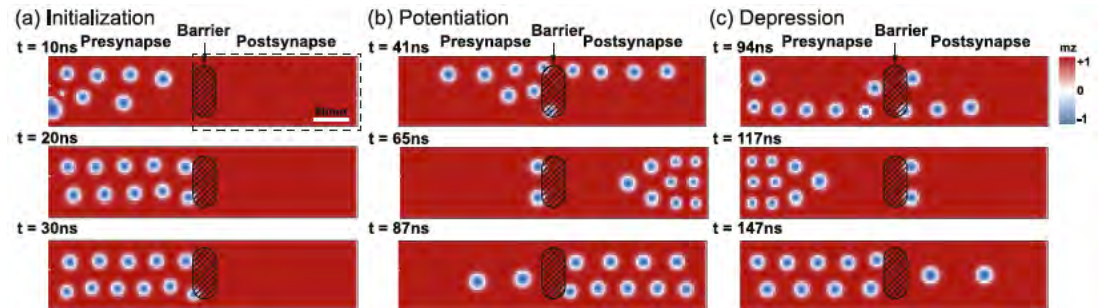
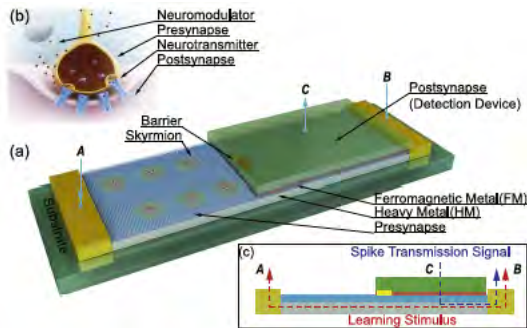
Tunable Transfer Function!

Z. He, S. Angizi, and D. Fan
 IEEE Magn. Lett. **8**, 4305705 (2017)

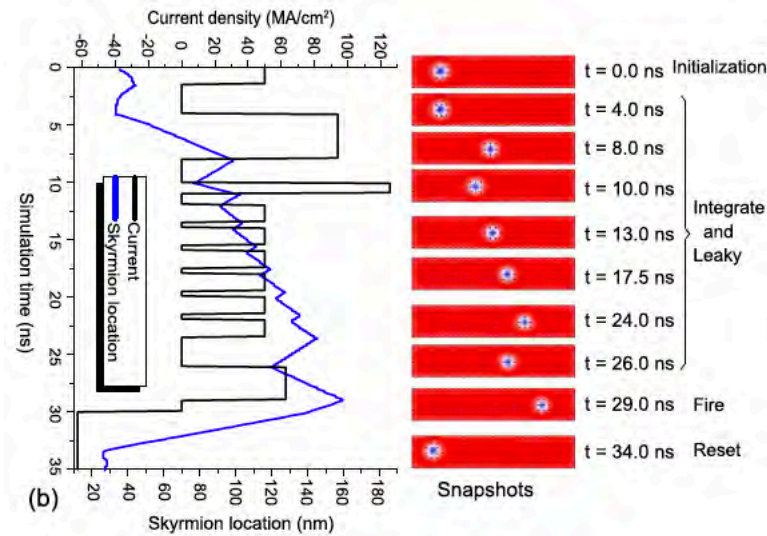
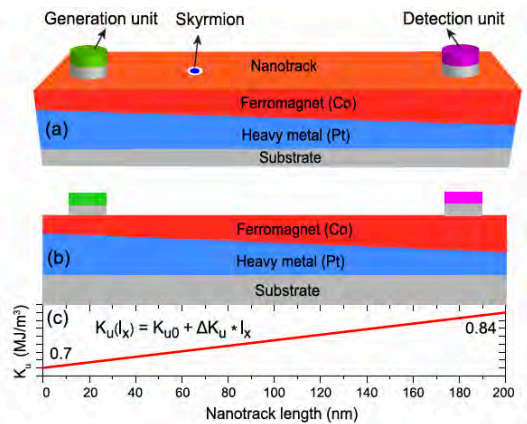


More complex ideas along these lines

Modulating DMI or anisotropy locally

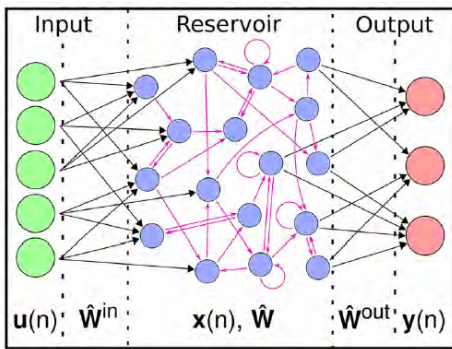


Y.Huang, *et al.*, *Nanotechn.* **28**, 08LT02 (2017)



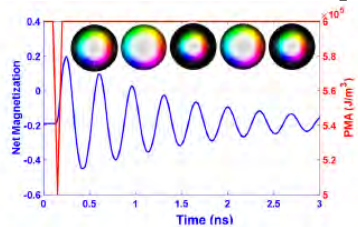
S. Li, *et al.*, *Nanotechn.* **28**, 31LT01 (2017)

Reservoir Computing

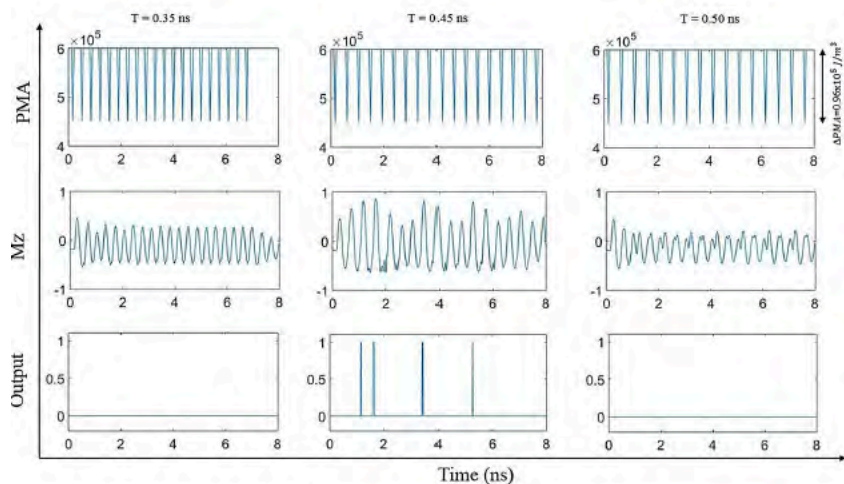


G.Bourianoff *et al.*, AIP Adv. **8**, 055602 (2018)

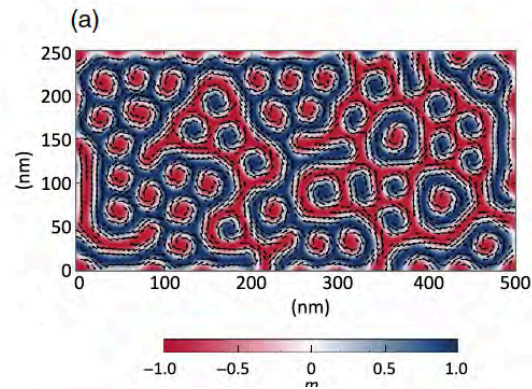
Dynamics



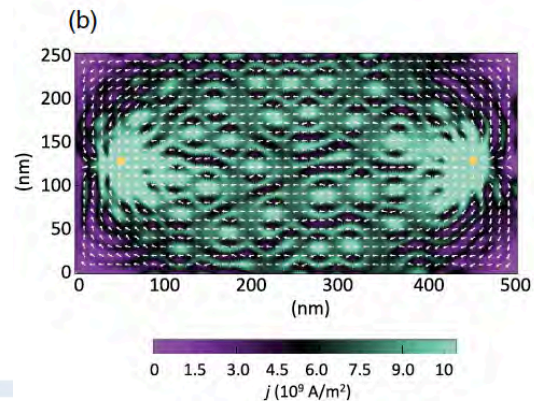
Md.Ali Azam *et al.*,
J. Appl. Phys **124**,
152122 (2018)



Complex Spin Textures



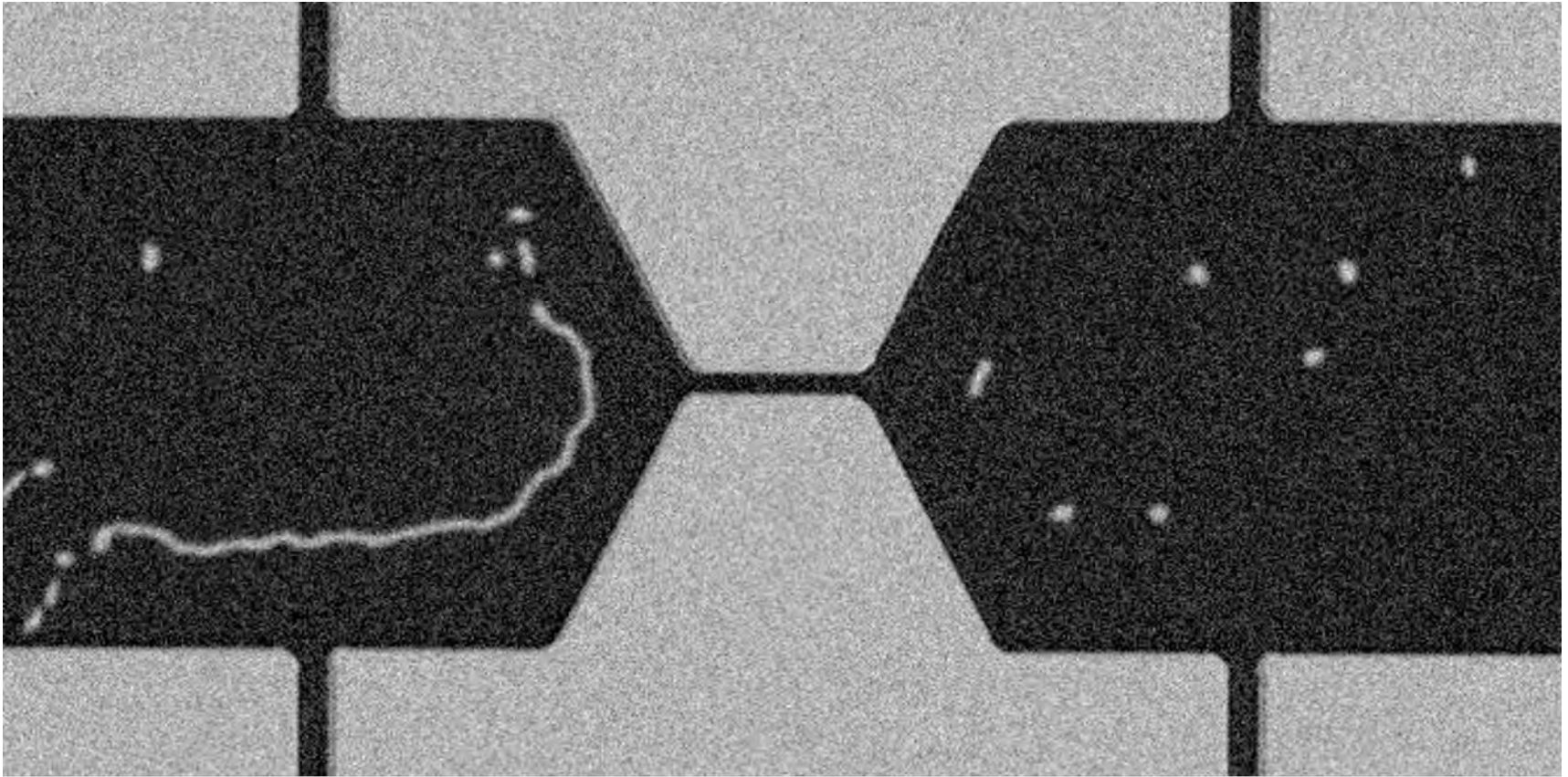
D.Prychynenko *et al.*,
Phys Rev. Appl. **9**,
014034 (2018)



Stochastic Behavior

$$H_{\perp} = -0.5 \text{ mT}$$

$$+ J_c \longrightarrow$$



W. Jiang *et al.*, *Science* **349**, 283 (2015)

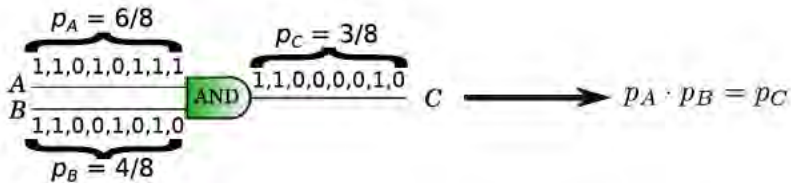
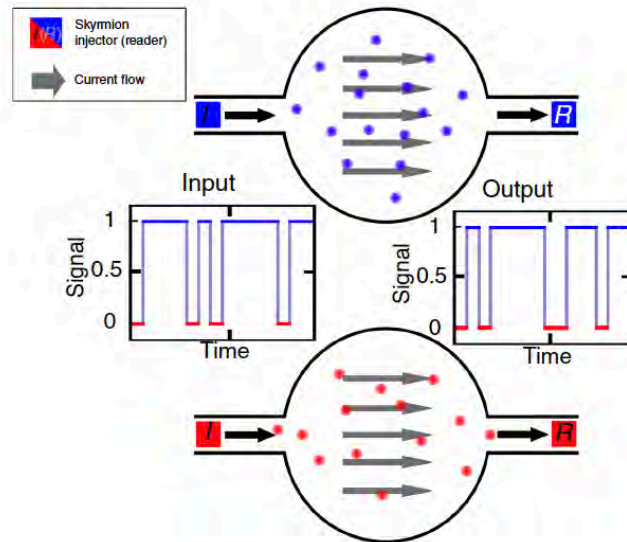
Axel Hoffmann, Materials Science Division, Argonne National Laboratory

hoffmann@anl.gov



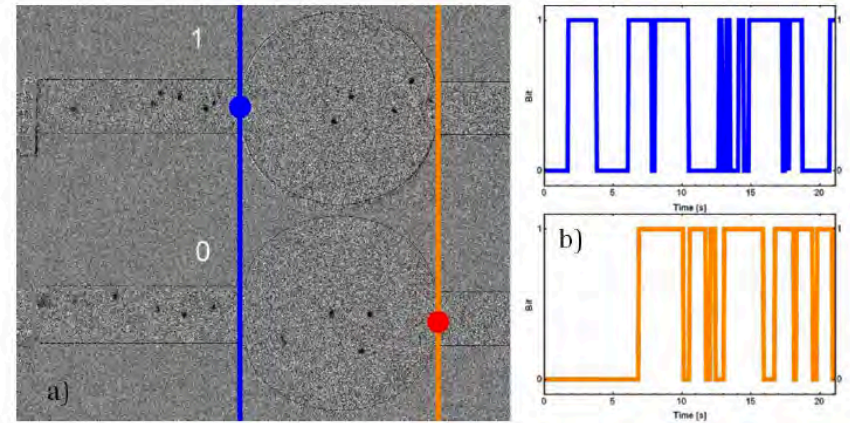
Skyrmion Reshuffler

Theoretical Concept



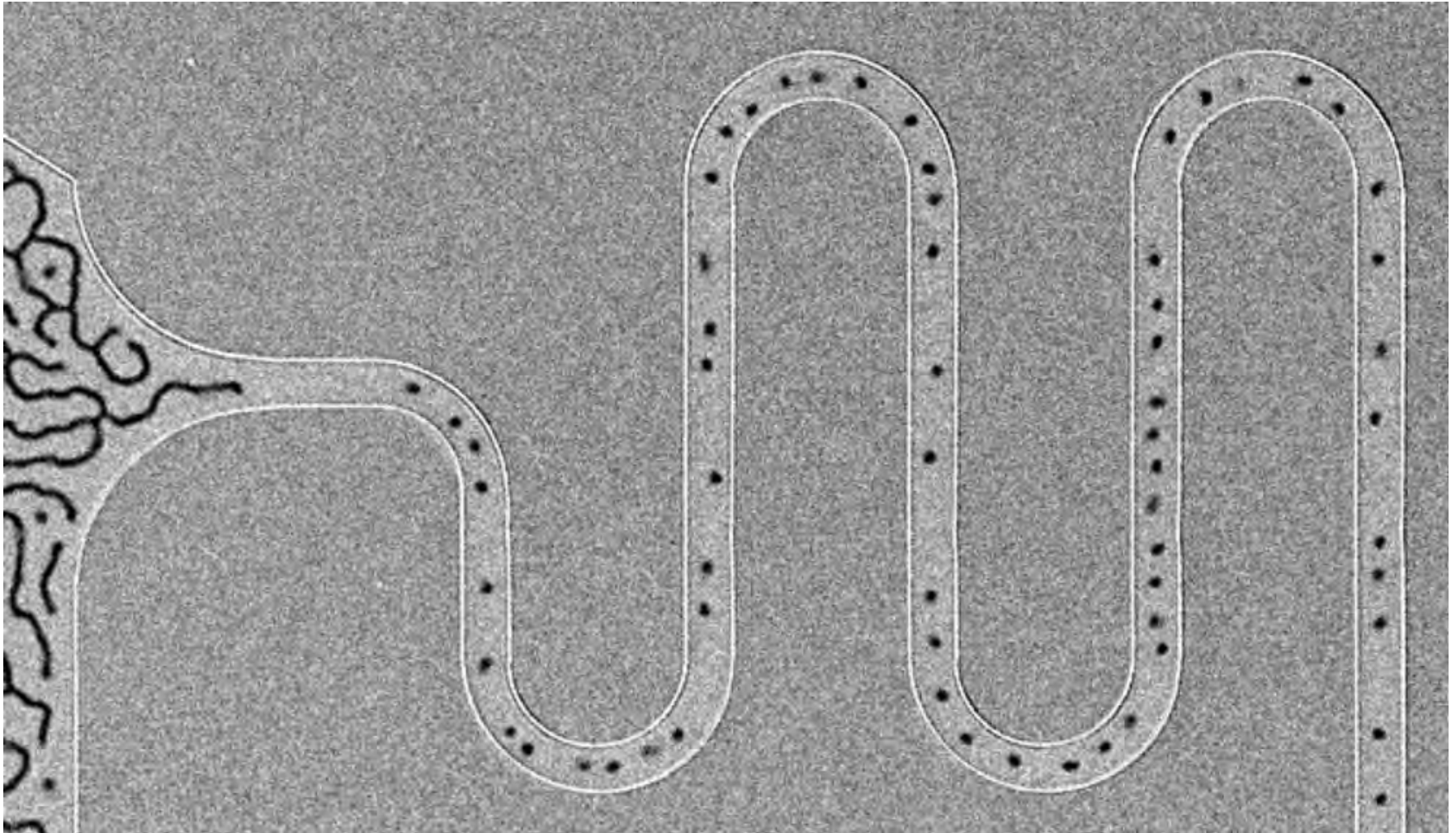
D. Pinna *et al.*, Phys. Rev. Appl. **9**, 064018 (2018)

Experimental Demonstration

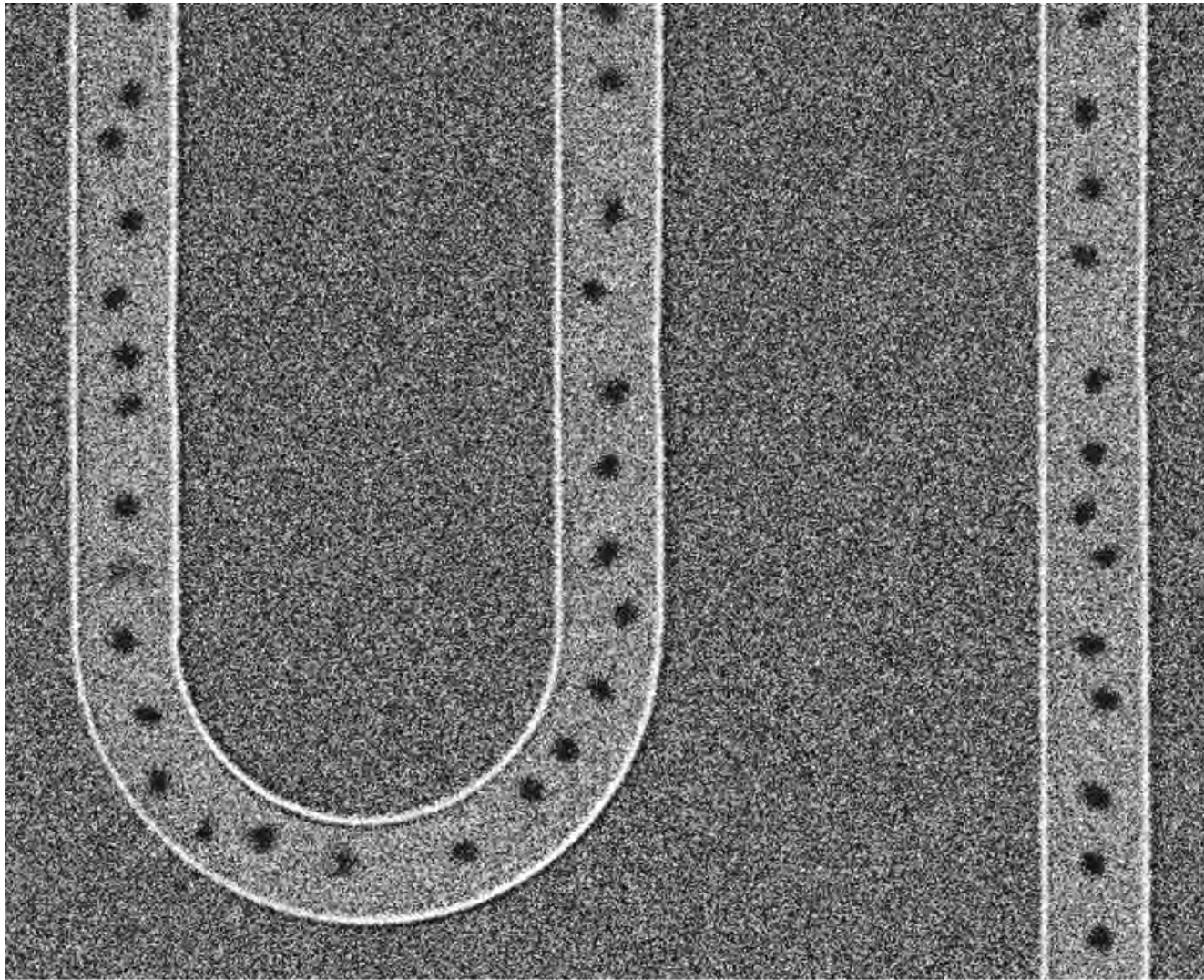


J. Závorka *et al.*, arXiv: 1805.05924

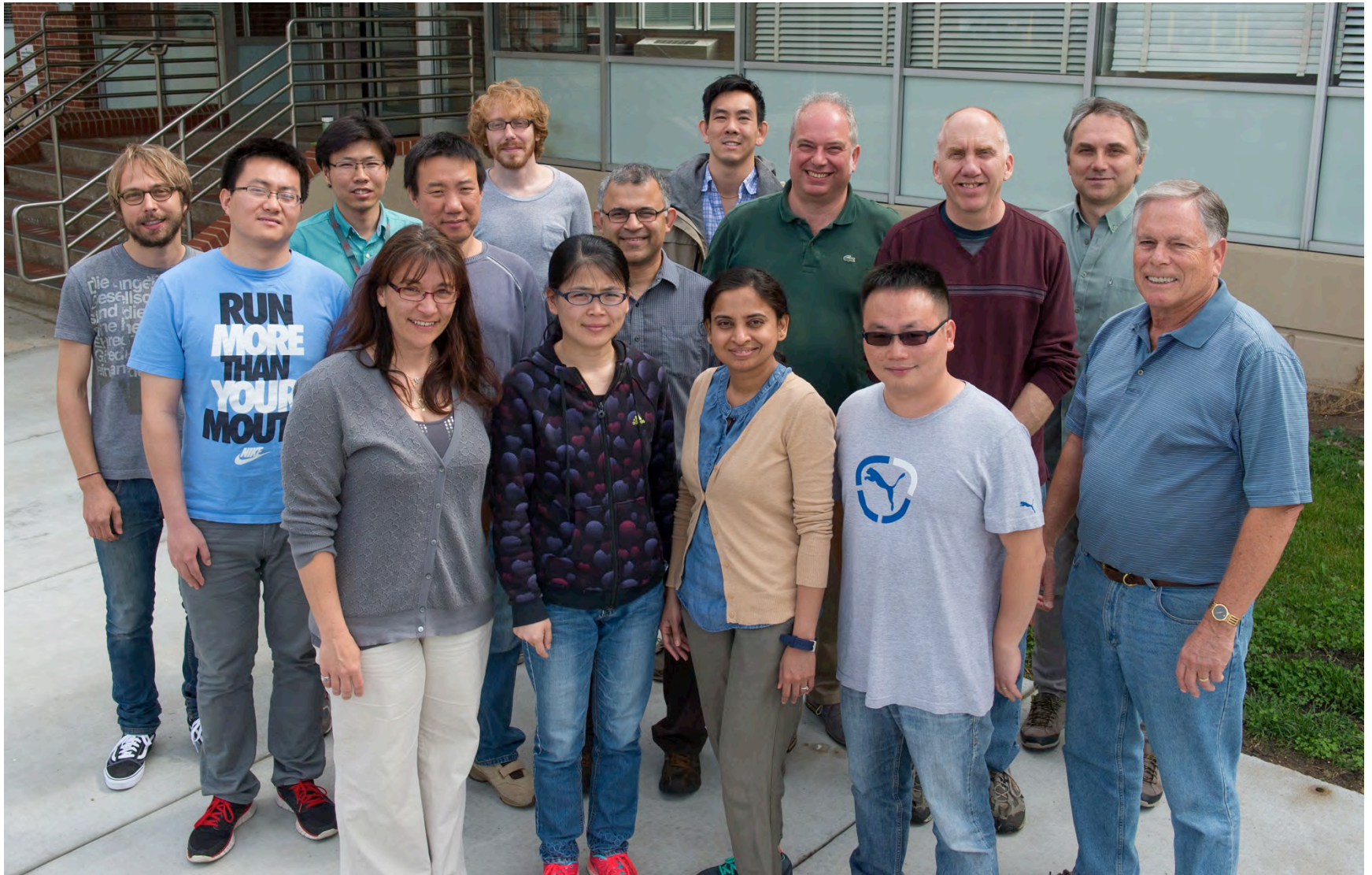
Just the Beginning of the Fun!



Just the Beginning of the Fun!



Magnetic Films Group at Argonne



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John E. Pearson, Frank. Y. Fradin, Olle Heinonen, Suzanne G. E. te Velthuis
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The University of Hong Kong

Xiao Wang and Xuemei Cheng
Bryn Mawr College

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DOE-BES Materials Science and Engineering Division



Conclusions

■ Magnetic Skyrmions

- Use interfacial interactions to stabilize them at room-temperature

■ Motion of Skyrmions

- Spin-orbit torques provide very efficient driving force
- Topological charge gives rise to strong gyroscopic forces: skyrmion Hall effect

■ Generating Skyrmions

- Inhomogeneities in spin textures or driving force can nucleate new skyrmions

■ Skyrmions for Neuromorphic Computing

- Can exhibit threshold and non-linear behavior
- Stochastic motion

