

ORBITAL HALL EFFECT IN 2D MATERIALS

TATIANA G. RAPPOPORT

MINHO UNIVERSITY

UNIVERSIDADE FEDERAL DO RIO DE JANEIRO

FCT

Fundação para a Ciência e a Tecnologia



COLLABORATORS



Luis Canonico
UFF



Tarik Cysne
UFF



Roberto Bechara Muniz
UFF

L. M. Canonico, T. G. Rappoport, R. B. Muniz, Phys. Rev. Lett. 122 (2019) 196601.

L. M. Canonico, T. P. Cysne, T. G. Rappoport and R. B. Muniz, Phys. Rev. B 101, 075429 (2020)

L. M. Canonico, T. P. Cysne, A. Molina-Sanchez, R. B. Muniz and T. G. Rappoport
Phys. Rev. B 101, 161409 (2020).



NUMERICAL CALCULATIONS



AIRES FERREIRA
University of York



TATIANA RAPPOPORT
Federal University of Rio de Janeiro



JOÃO M. V. P. LOPES
Universidade do Porto



LUCIAN COVACI
Universiteit Antwerpen



MIŠA ANĐELKOVIĆ
Universiteit Antwerpen



SIMÃO MENESES JOÃO
Universidade do Porto

Open Source

Python Scripts

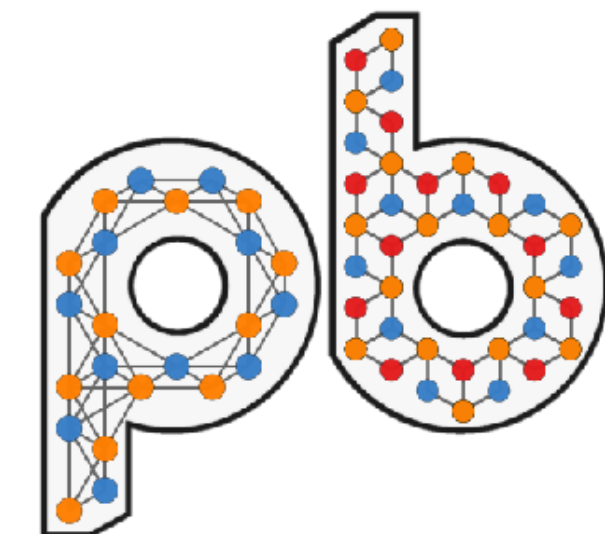
Evaluation of response functions in systems with up to 10^{10} orbitals

<https://quantum-kite.com/>

KITE: high-performance accurate modelling of electronic structure and response functions of large molecules, disordered crystals and heterostructures

R. Soc. open sci. 7, 191809 (2020)

+



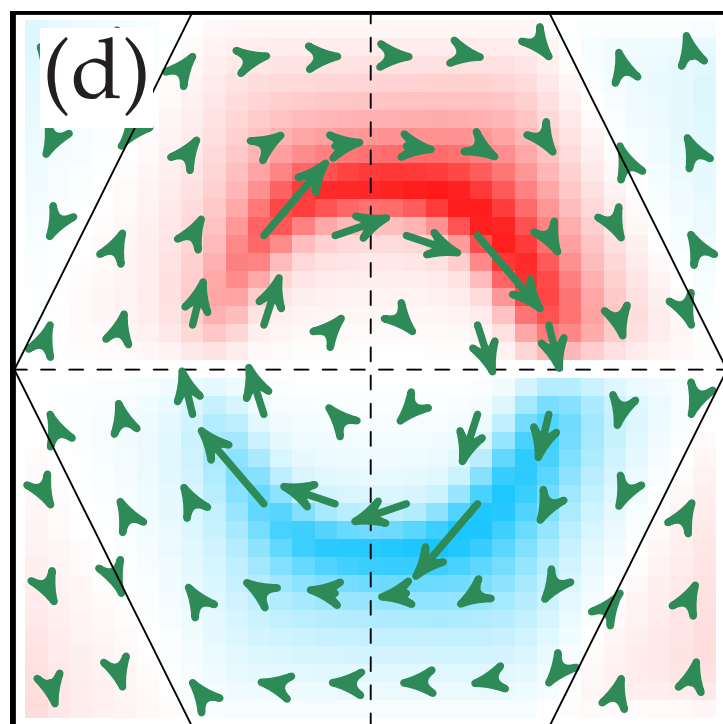
Orbital angular momentum (OAM) can be manipulated like spin

No need of exchange interaction or SOC

Orbital Hall effect

B. A. Bernevig et al. PRL 2005
 H. Kontani et al. PRL 2009
 D. Go et al. PRL 2018 ..

Orbital Rashba effect



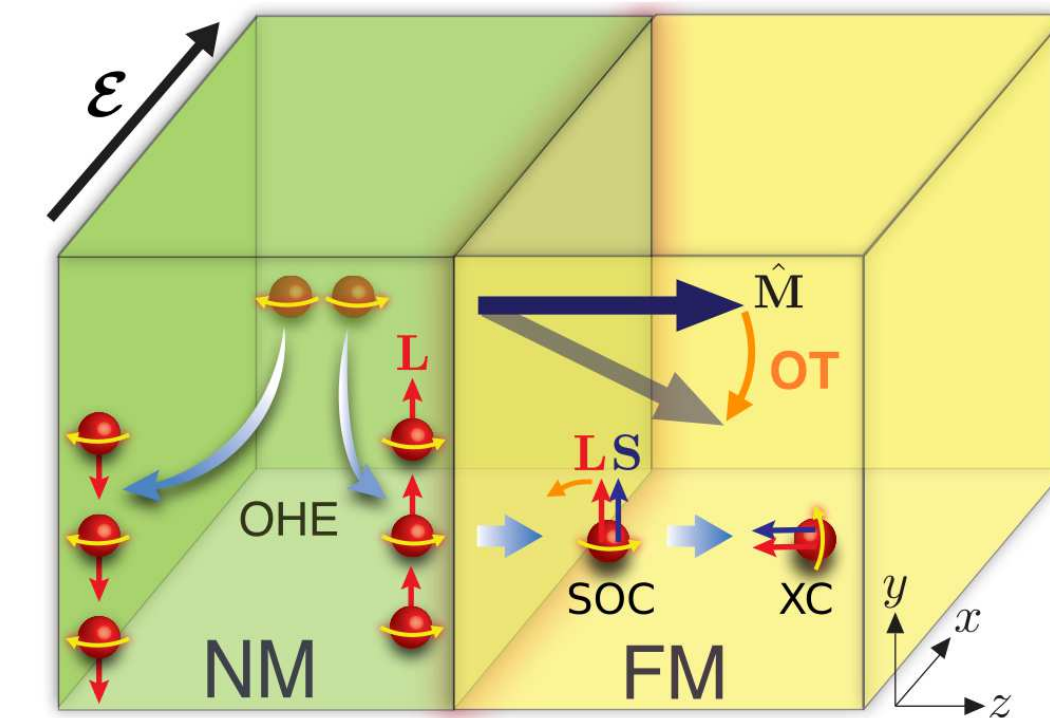
Jin-Hong Park et al PRB 2012
 Sp metals
 D. Go et al. Sci.Rep. 2017
 Tin Telluride monolayers
 Jeongwoo Kim et al, Nature Comm 2019

Orbital Rashba-Edelstein Effect

T. Koretsune, PRB 2012
 T. Yoda et al Nano Letters 2018
 N.Salemi et al. Nature Comm. 2019

Orbital Chern insulators

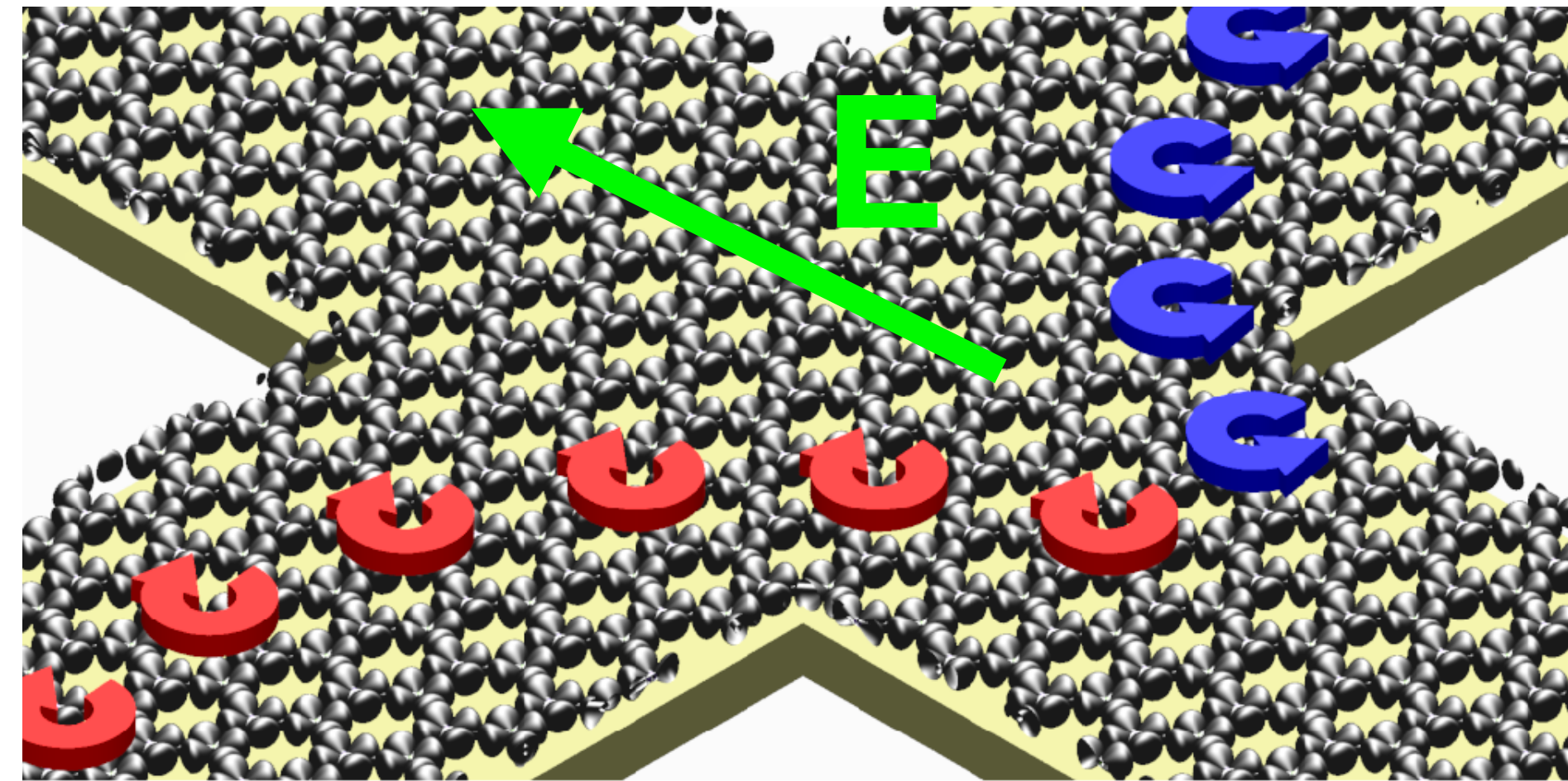
A. L. Sharpe et al. Science 2019
 M. Serlin et al. Science 2019
 G. Chen et al. Nature 2020



Orbital Torque

Xi Chen et al. Nature Comm. 2018
 D. Go et al. Phys. Rev. Research 2020
 Z. C. Zheng et al, PR. Research 2020
 Y. Tazaki et al. ArXiv:2004.09165

Orbital angular momentum (OAM) analogous of the spin Hall effect



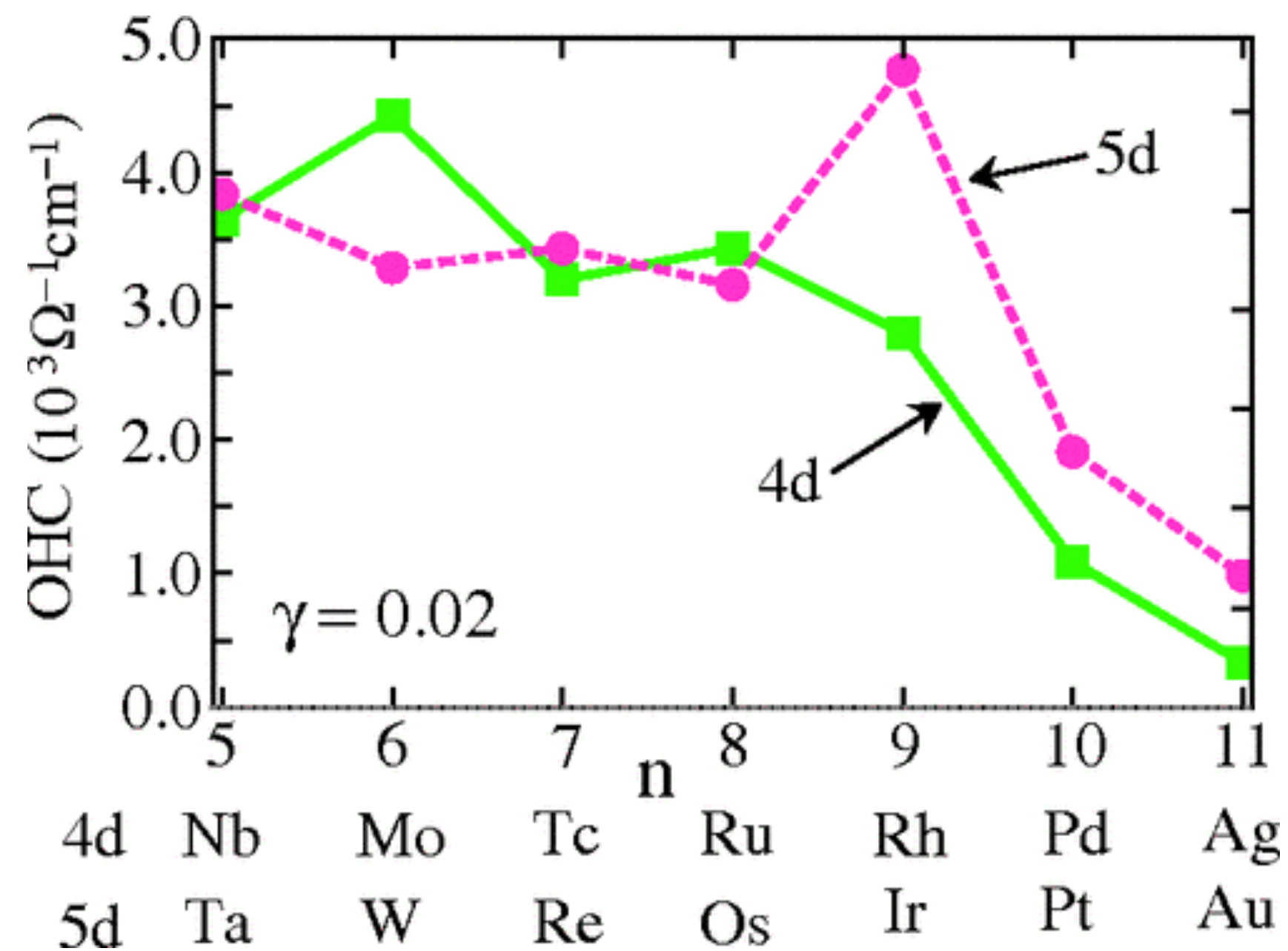
First proposal (for Silicon): B. A. Bernevig, T. L. Hughes, and S-C. Zhang, PRL (2005)

$$\sigma_{\text{OH(SH)}} = \frac{e}{\hbar} \sum_{n \neq m} \int \frac{d^3 k}{(2\pi)^3} (f_{m\mathbf{k}} - f_{n\mathbf{k}}) \Omega_{nm\mathbf{k}}^{X_z},$$

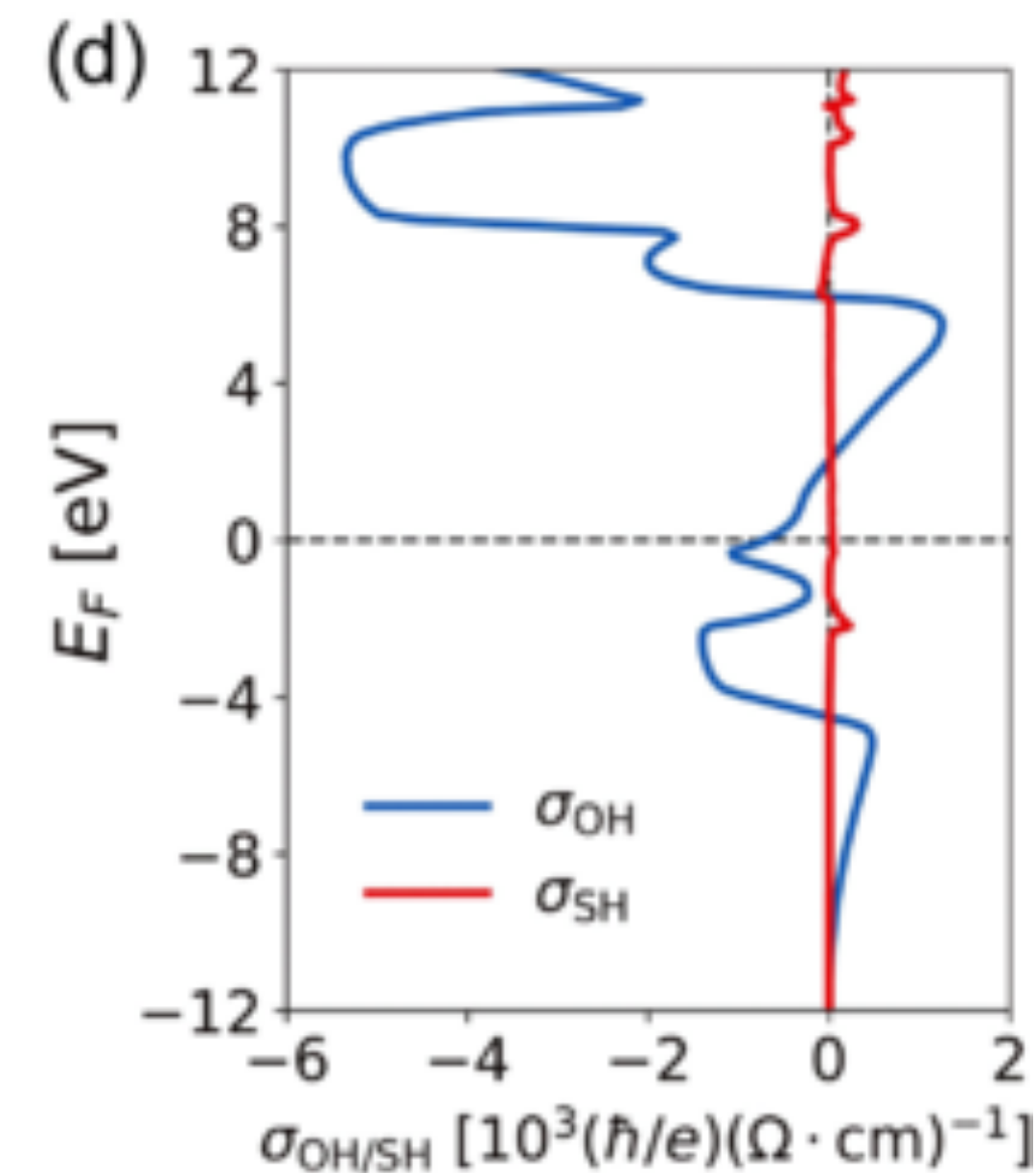
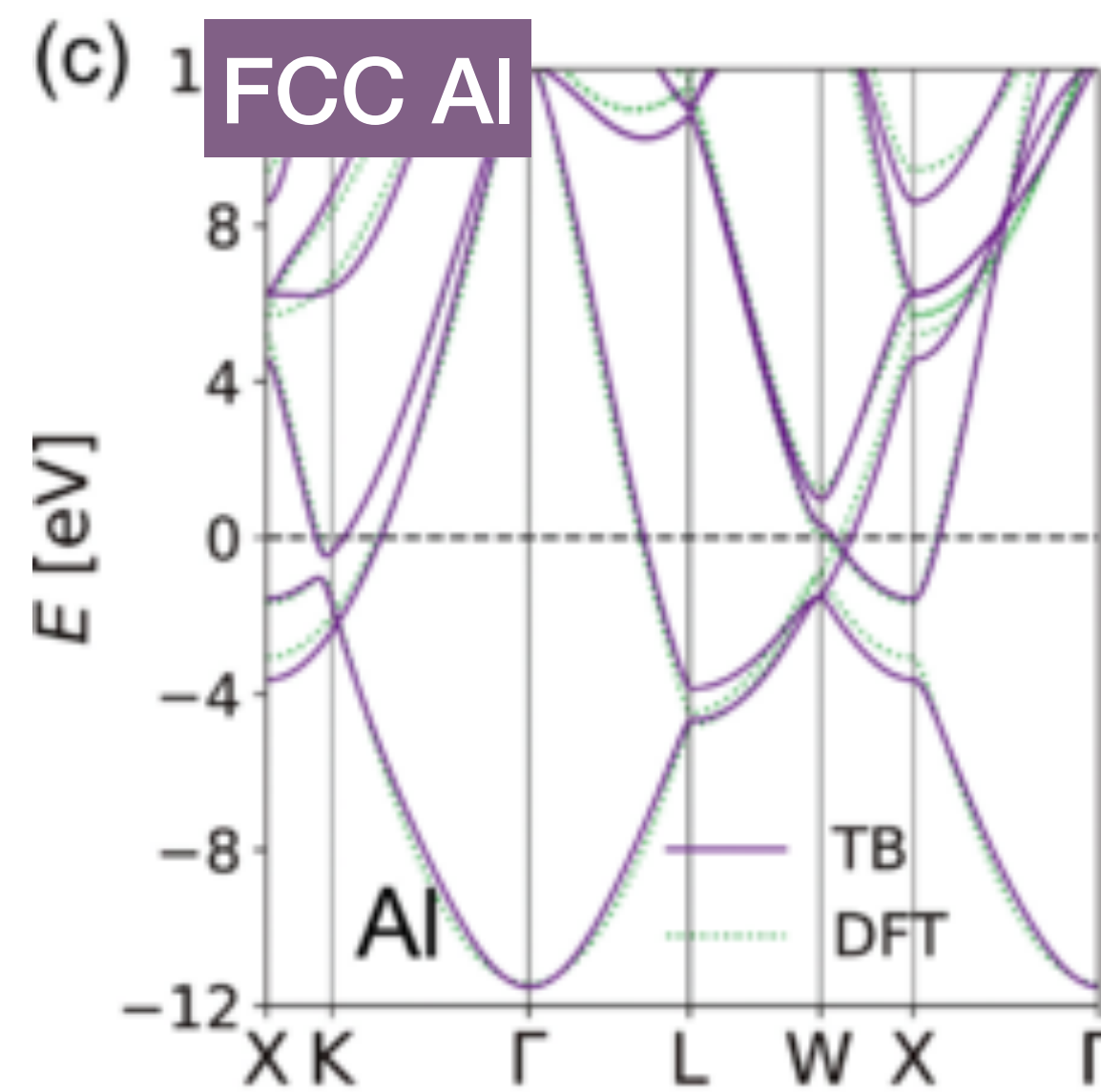
$$\Omega_{nm\mathbf{k}}^{X_z} = \hbar^2 \text{Im} \left[\frac{\langle u_{n\mathbf{k}} | j_y^{X_z} | u_{m\mathbf{k}} \rangle \langle u_{m\mathbf{k}} | v_x | u_{n\mathbf{k}} \rangle}{(E_{n\mathbf{k}} - E_{m\mathbf{k}} + i\eta)^2} \right]$$

$$j_y^{X_z} = (v_y X_z + X_z v_y) / 2$$

$$X_z = L_z(S_z)$$



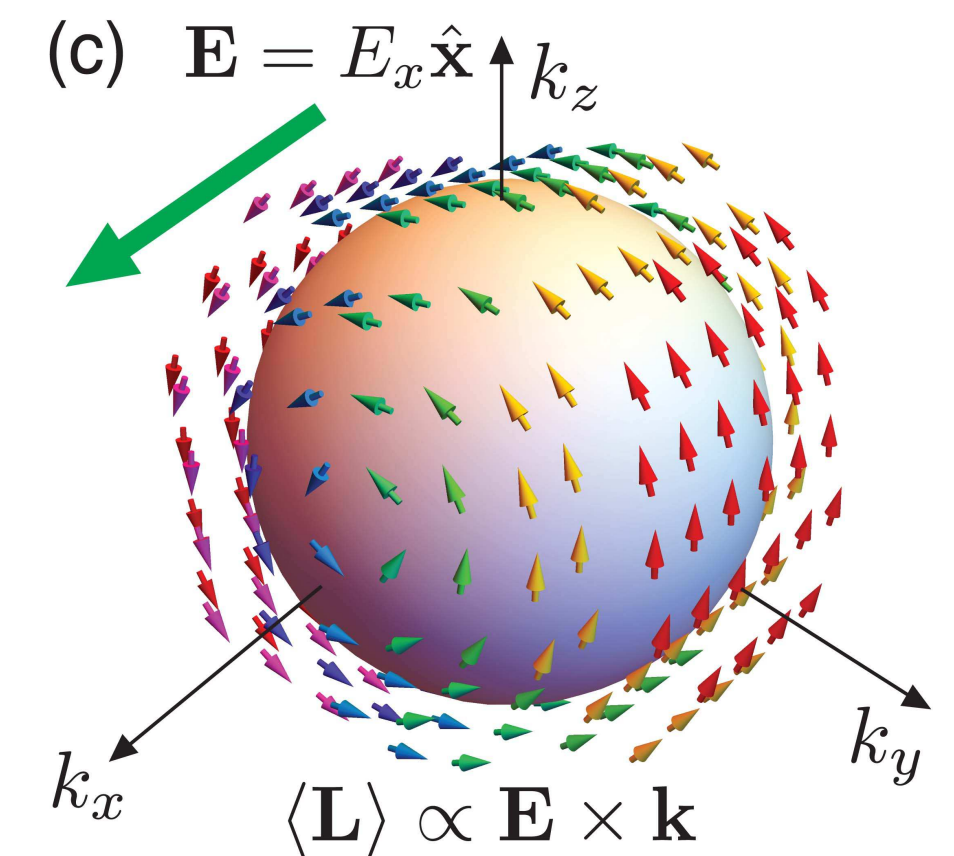
H. Kontani et al. PRL 2009
T. Tanaka et al. PRB 2008



D Go, HW Lee arXiv:1903.01085
D Jo, D Go, HW Lee PRB, 2018

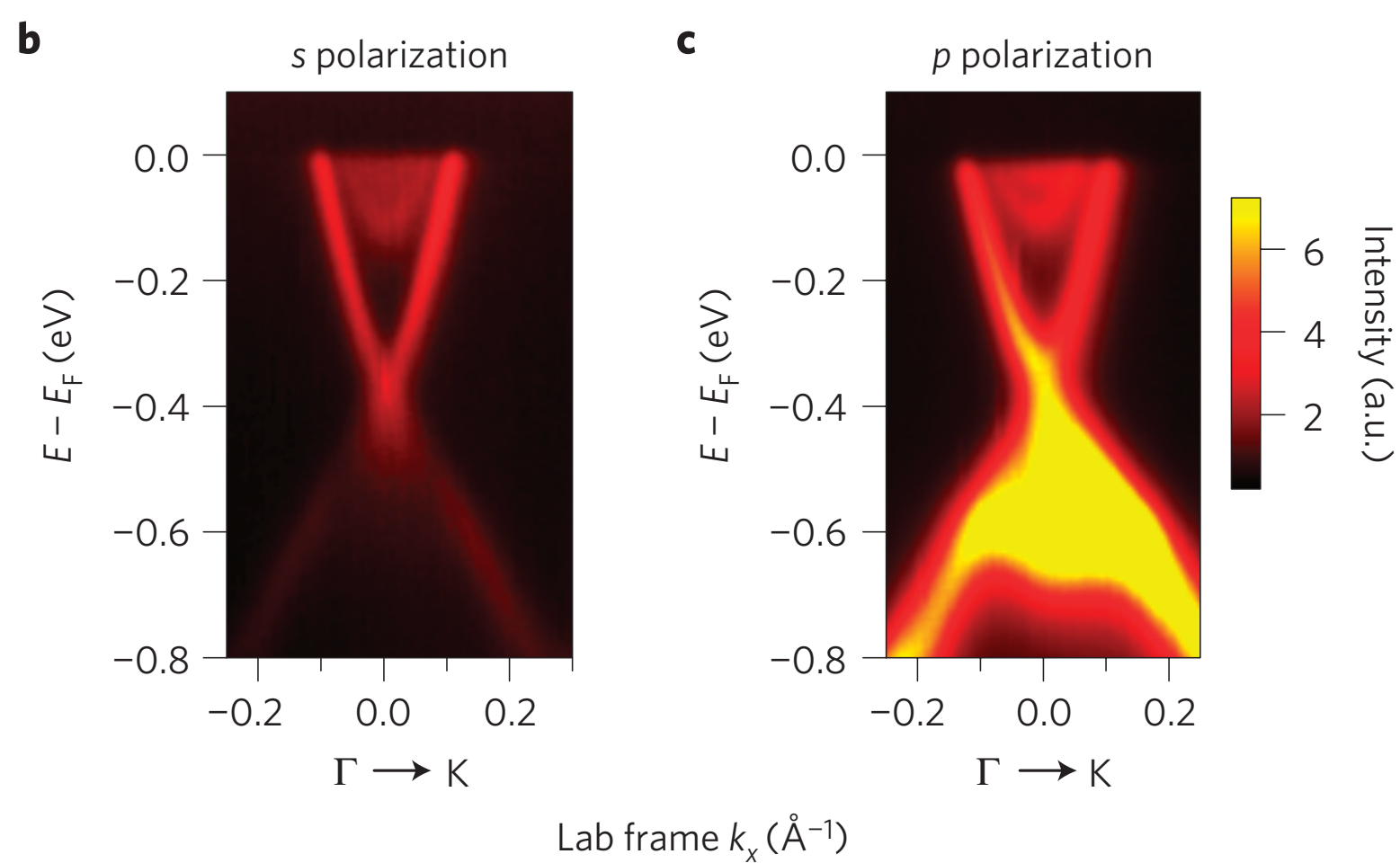
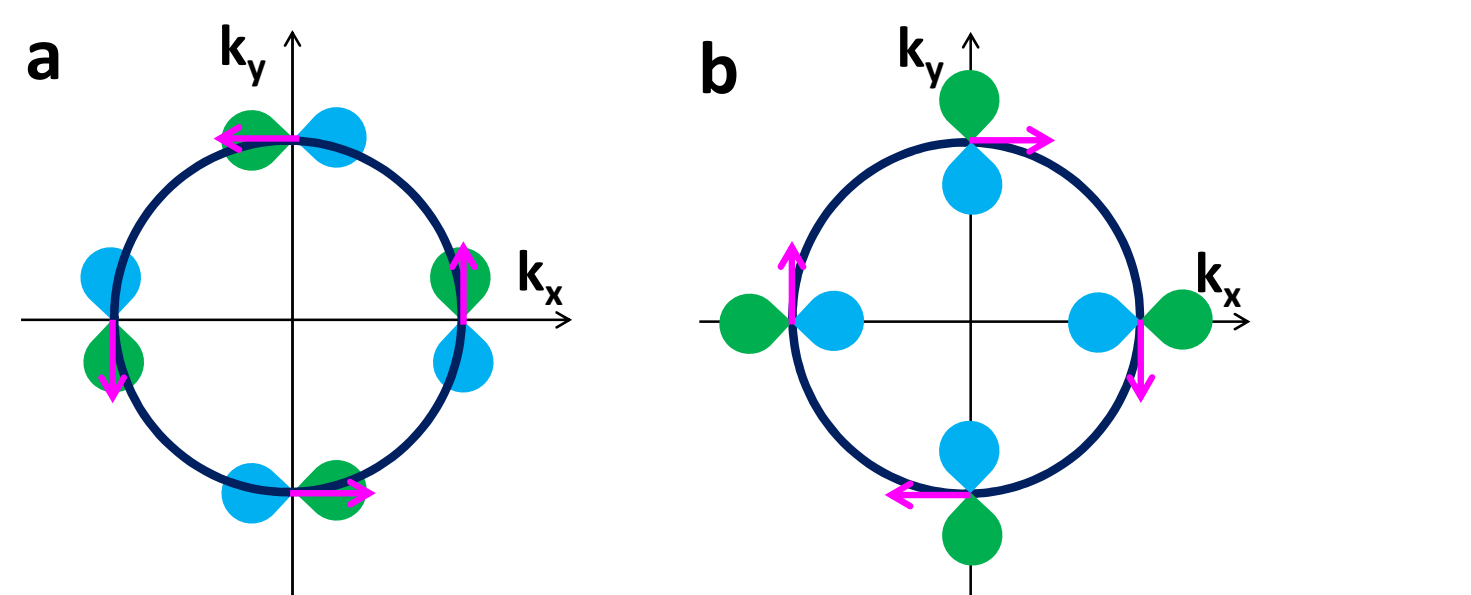
Orbital Texture induce OHE

D Jo, D Go, HW Lee PRL, 2018



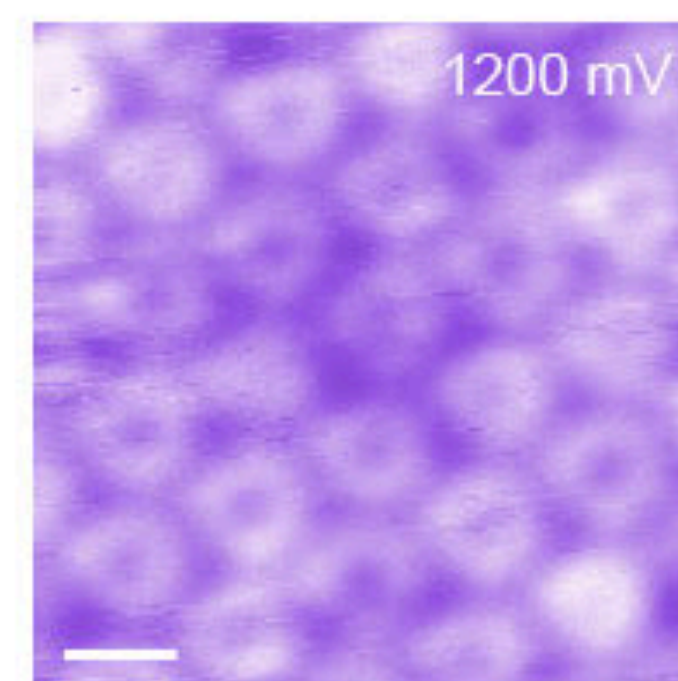
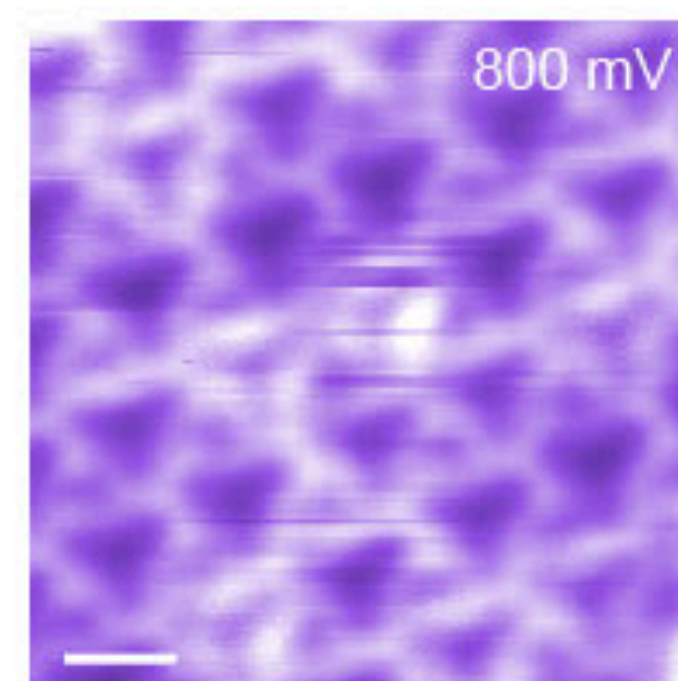
Topological Insulators

H Zhang, CX Liu, SC Zhang PRL 2013
Yue Cao et al Nat. Phys. 2013



1T Ta-based TMD layers

T. Ritschel et al. Nature Phys. 2015
Yi Chen et al Nature Phys. 2019

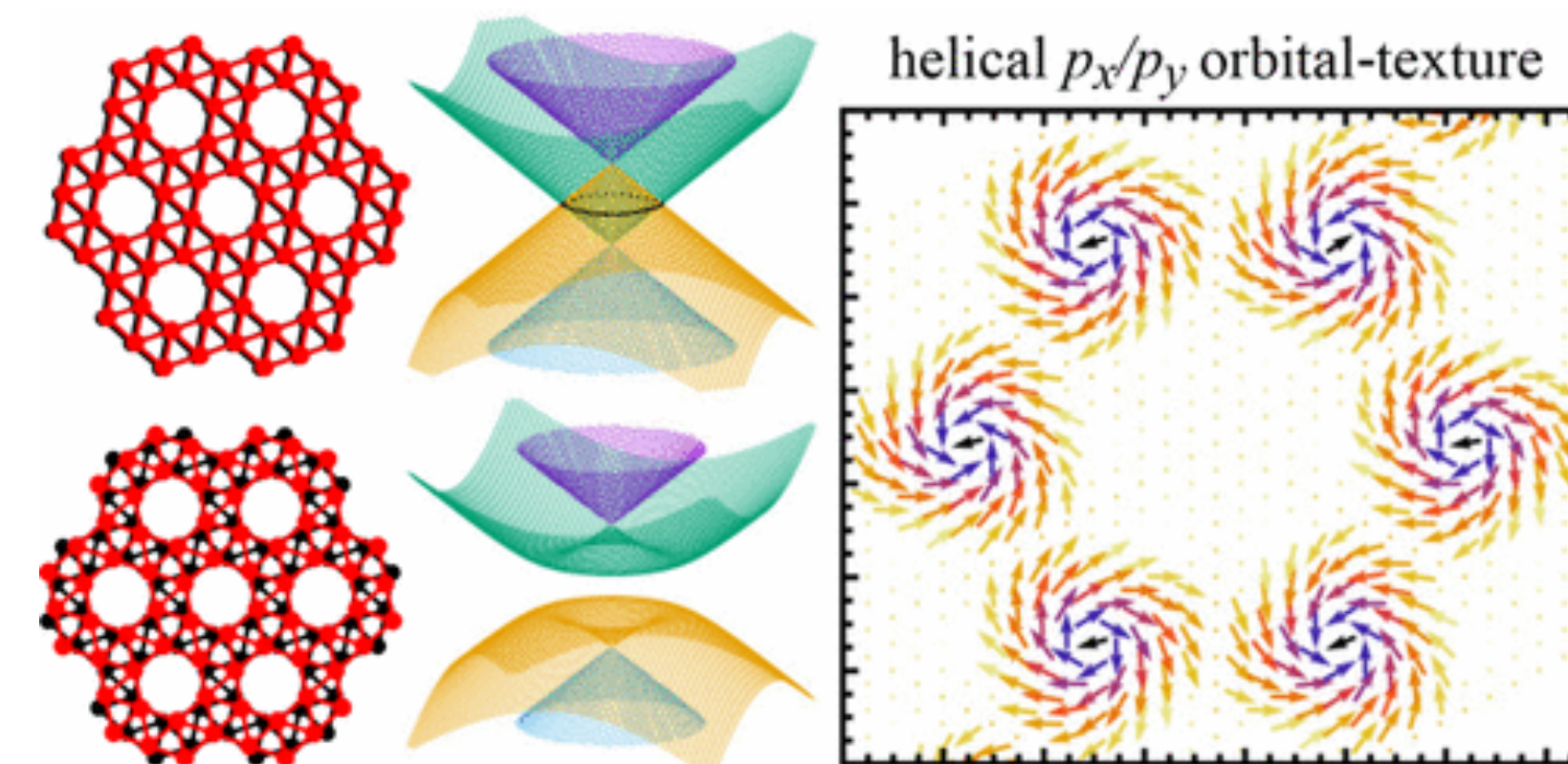


2DEG in Oxides

J.J.Kim et al, Nat. Comm. 2014

Borophene

F. C. de Lima et al., Nanoletters. 2019

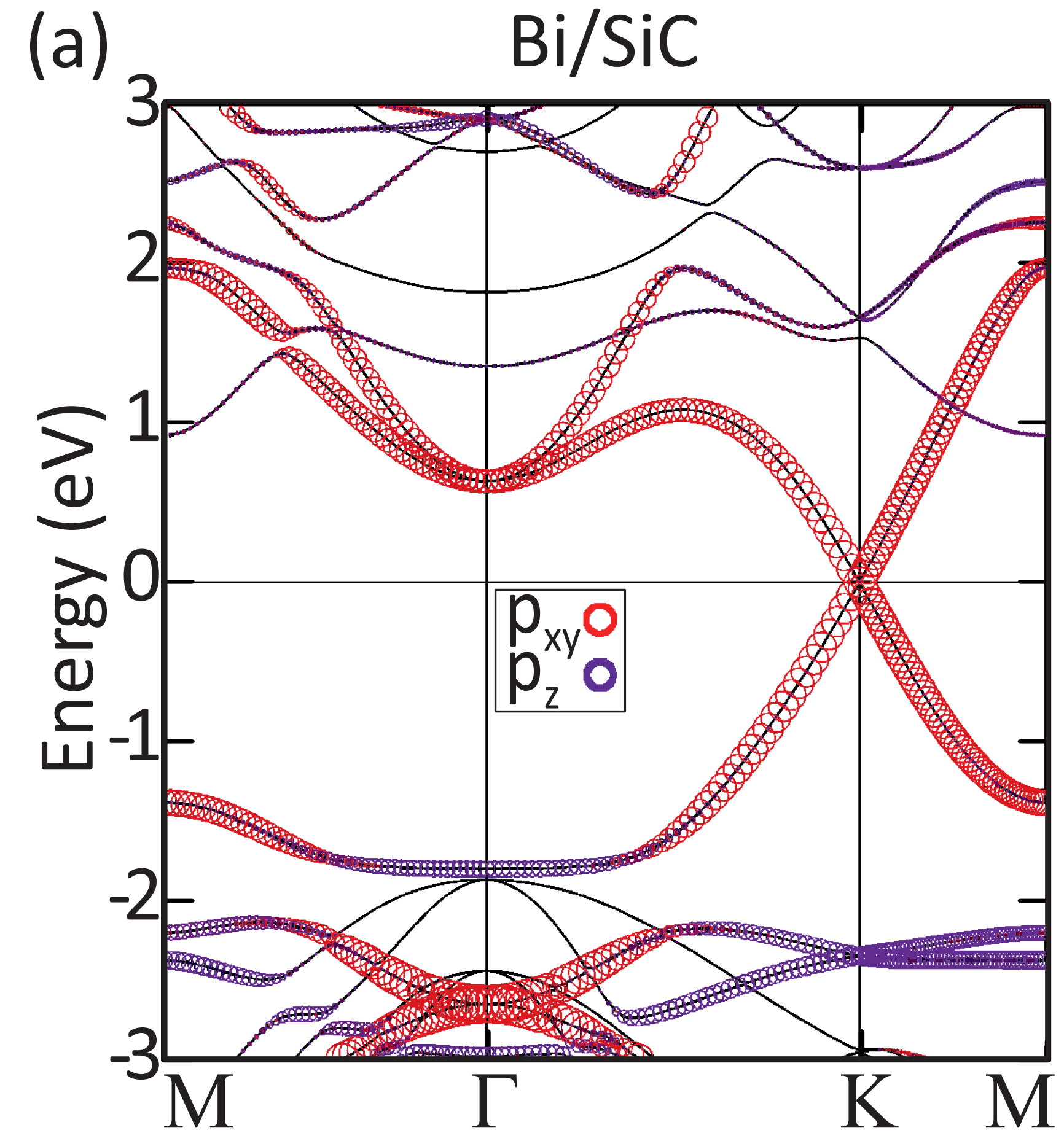
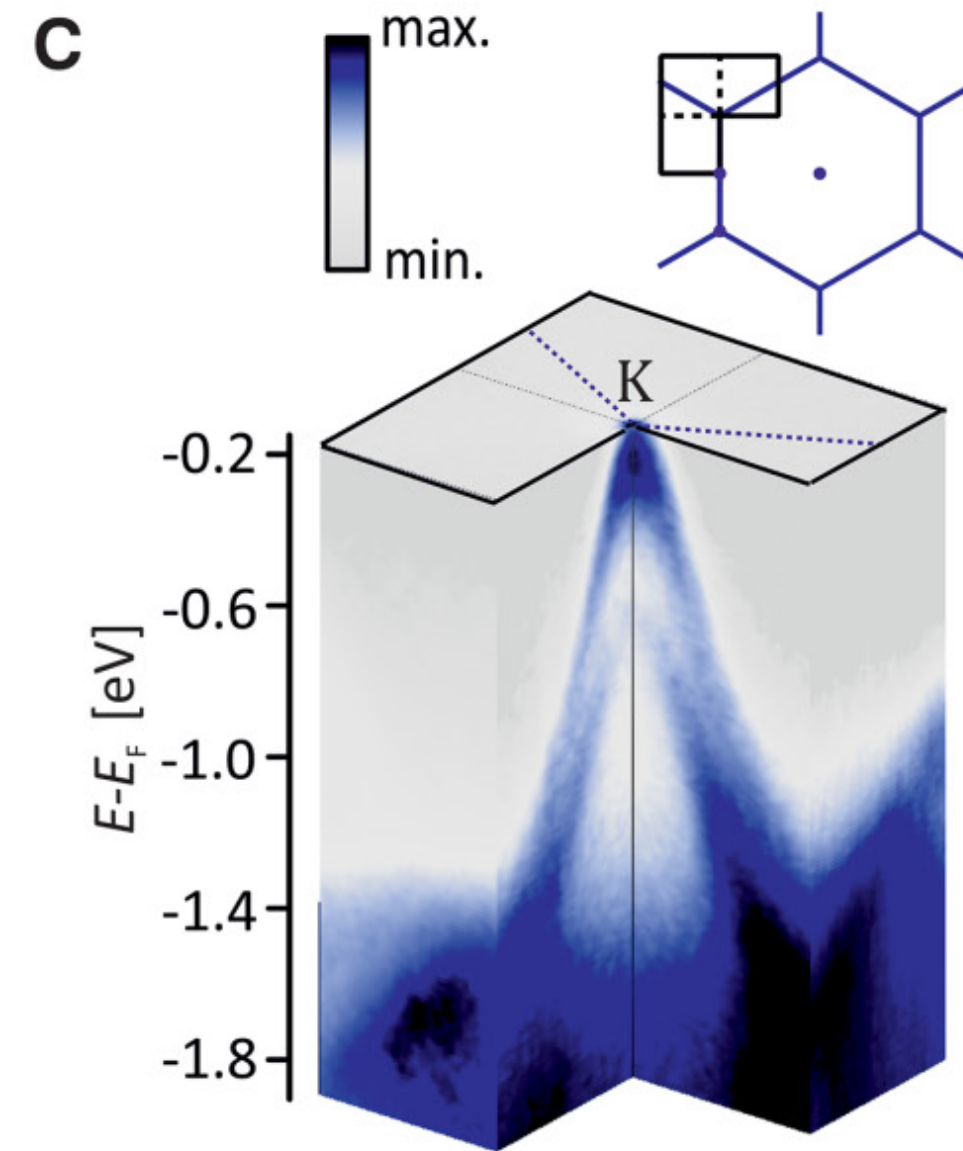
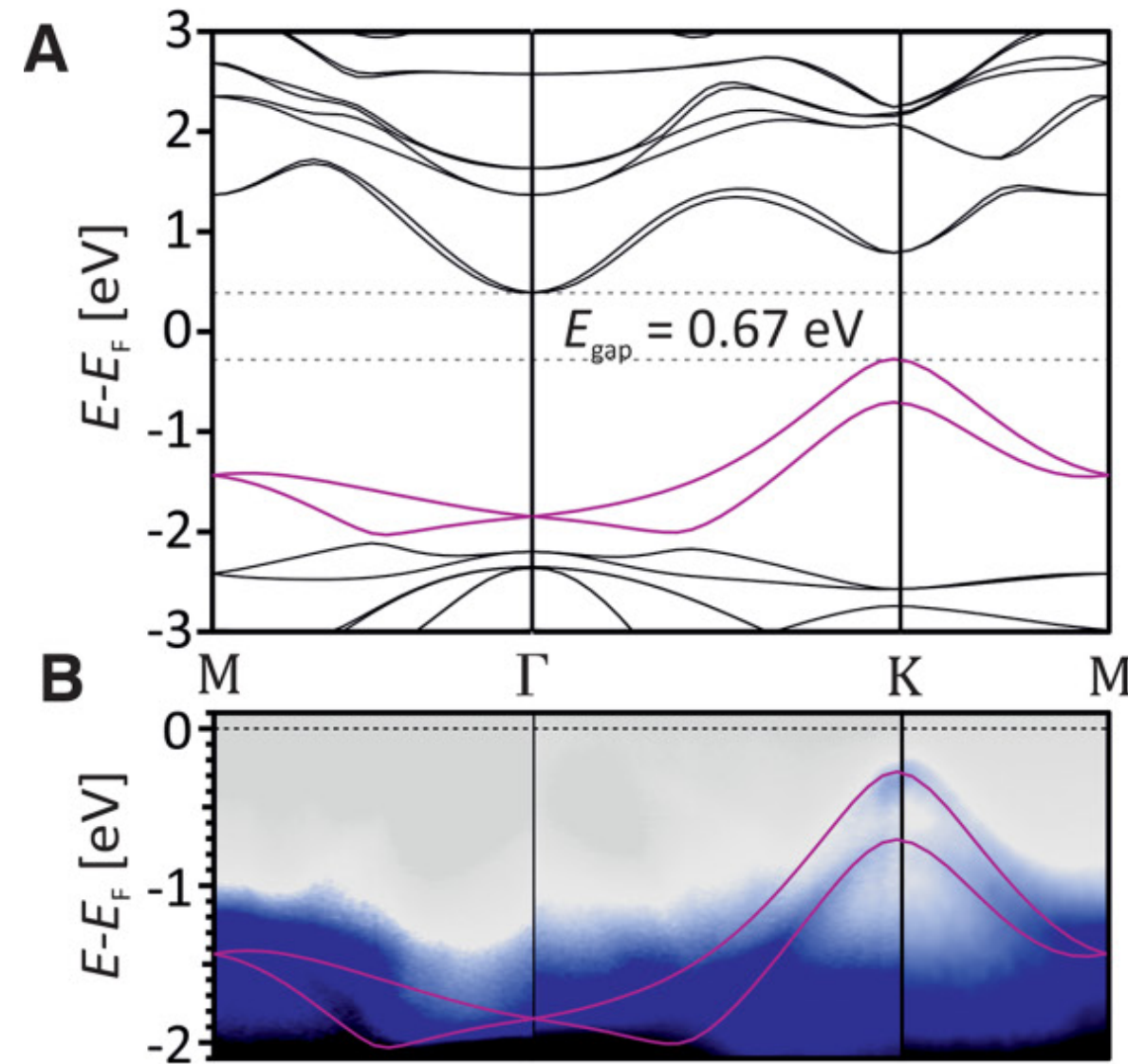
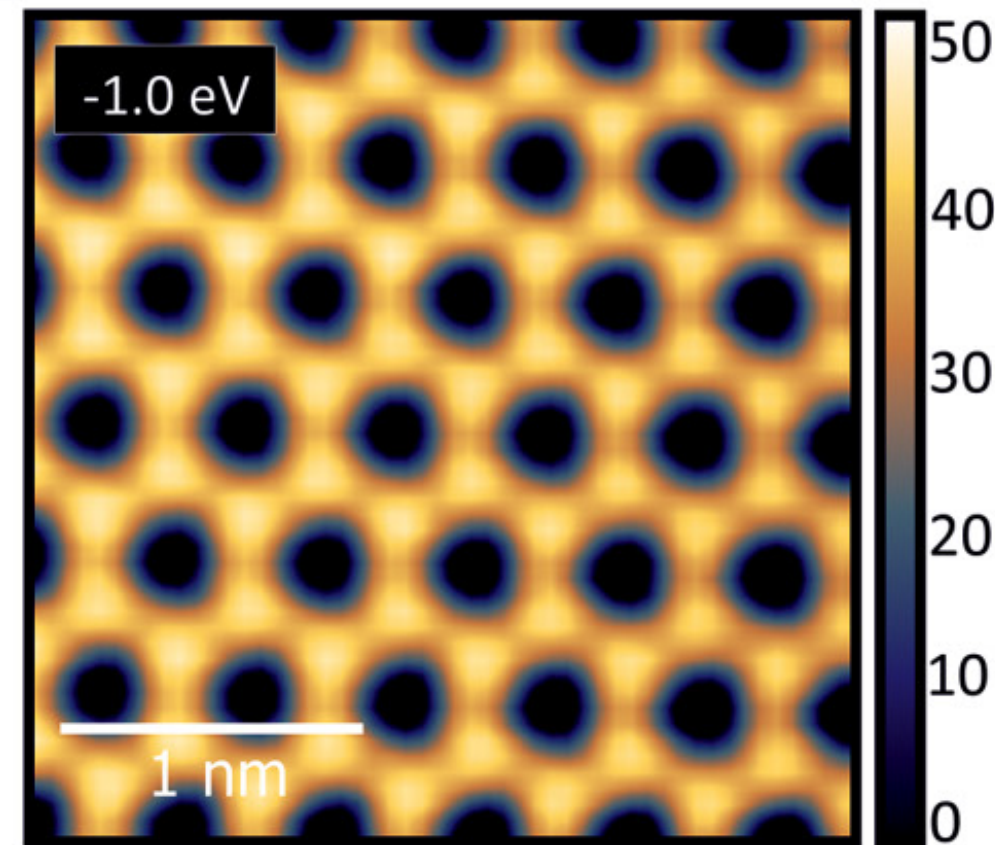


OUR MINIMAL MODEL

GENERAL ASPECTS

Epitaxy

SiC Substrate



F. Reis, G. Li, L. Dudy, M. Bauernfeind, S. Glass, W. Hanke, R. Thomale, J. Schäfer, R. Claessen, Science 2017



PX-PY HAMILTONIAN + SOC

$$\mathcal{H} = \sum_{\langle ij \rangle} \sum_{\mu\nu s} t_{ij}^{\mu\nu} p_{i\mu s}^\dagger p_{j\nu s} + \sum_{i\mu s} \epsilon_i p_{i\mu s}^\dagger p_{i\mu s} + \sum_{i\mu s} \mathbf{h}_{\mu s}^z p_{i\mu s}^\dagger p_{i\mu s},$$

$$\lambda_I L_z S_z$$

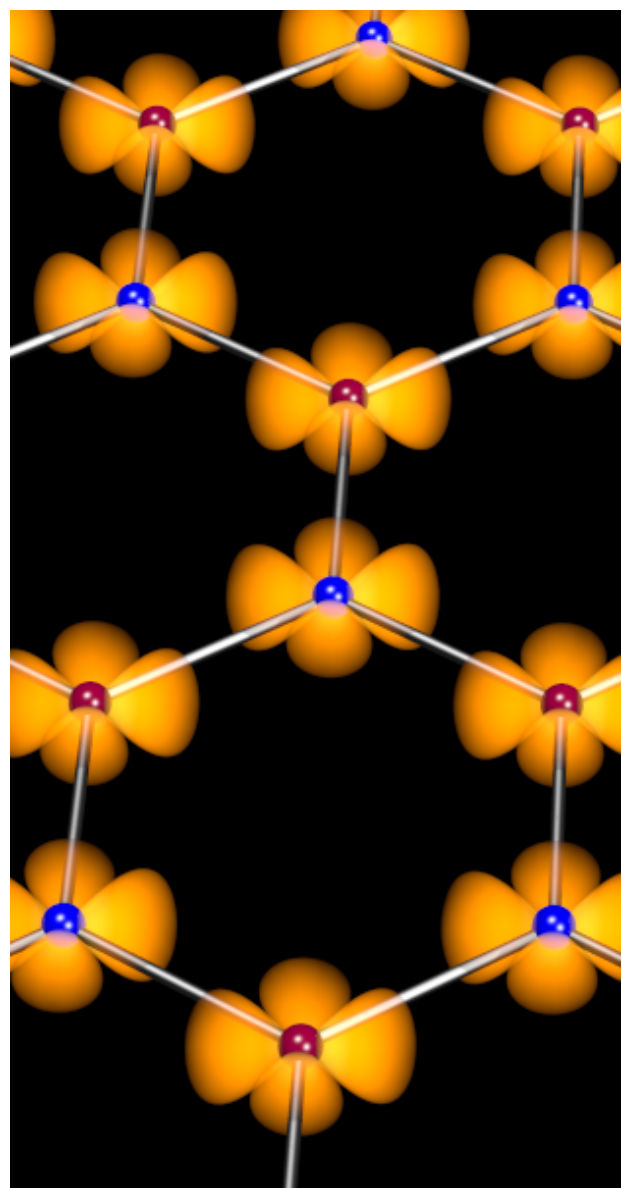
$$h_{\text{ex}} L_z$$

$$\epsilon_i = \pm V_{AB}$$

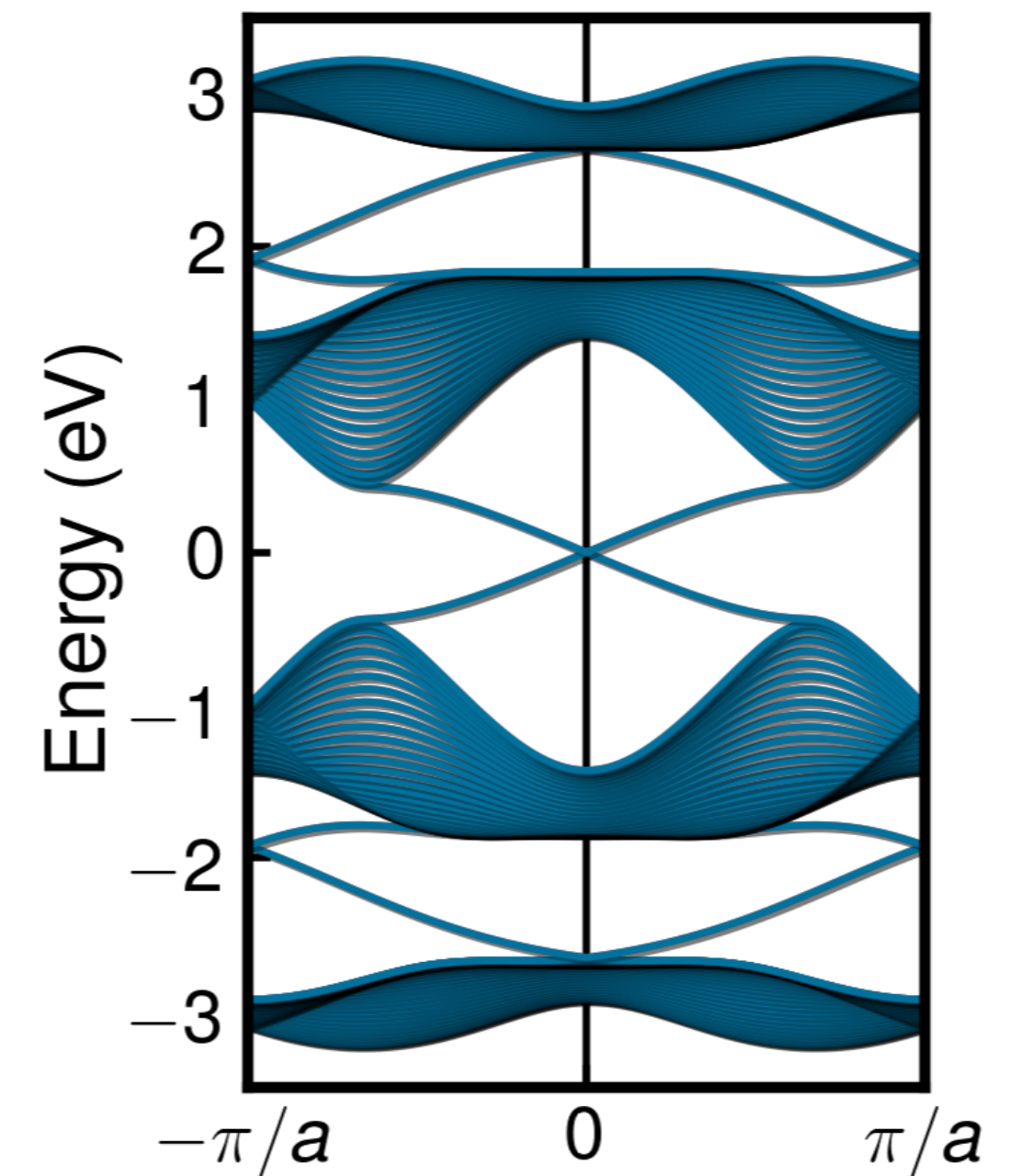
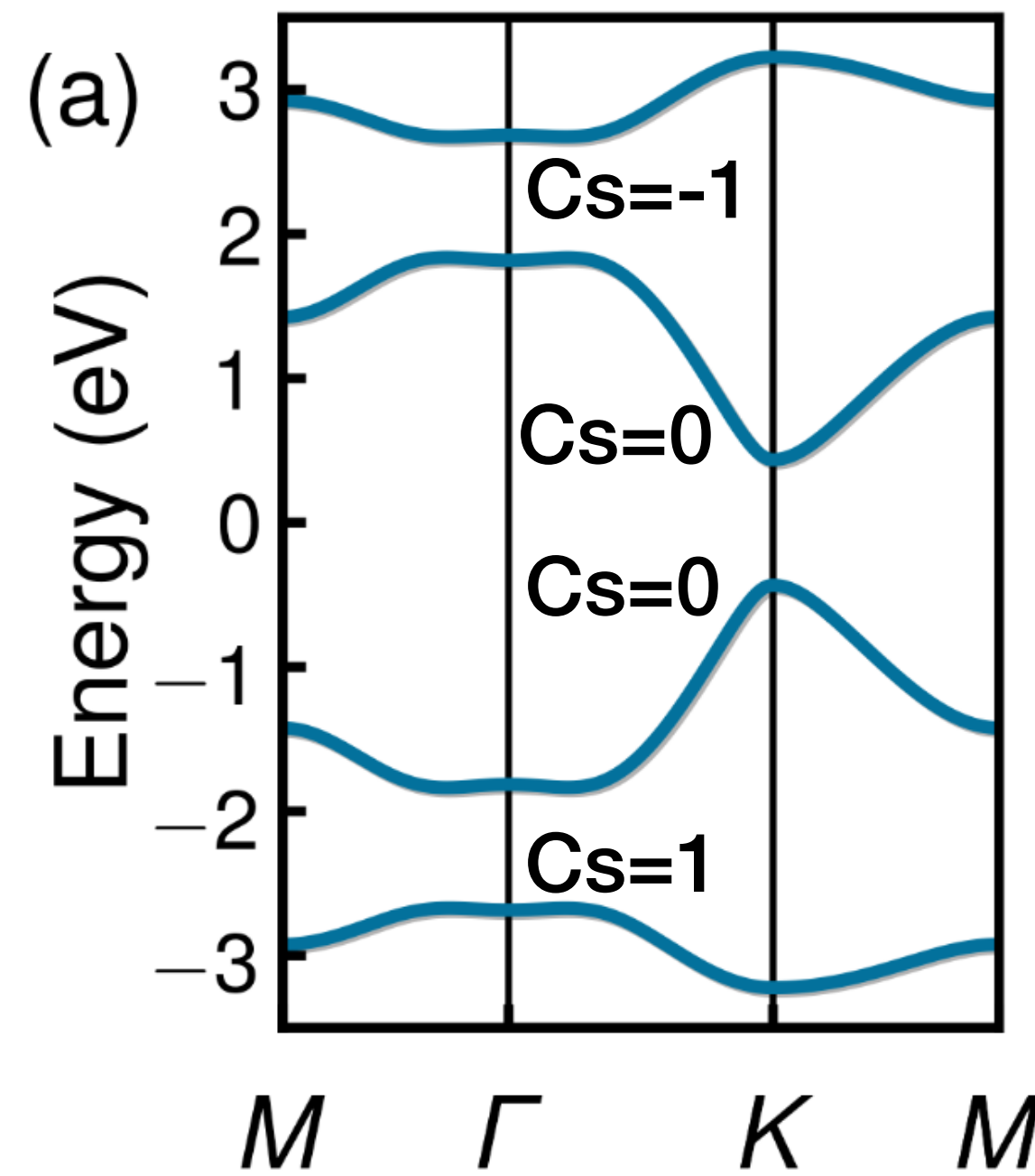
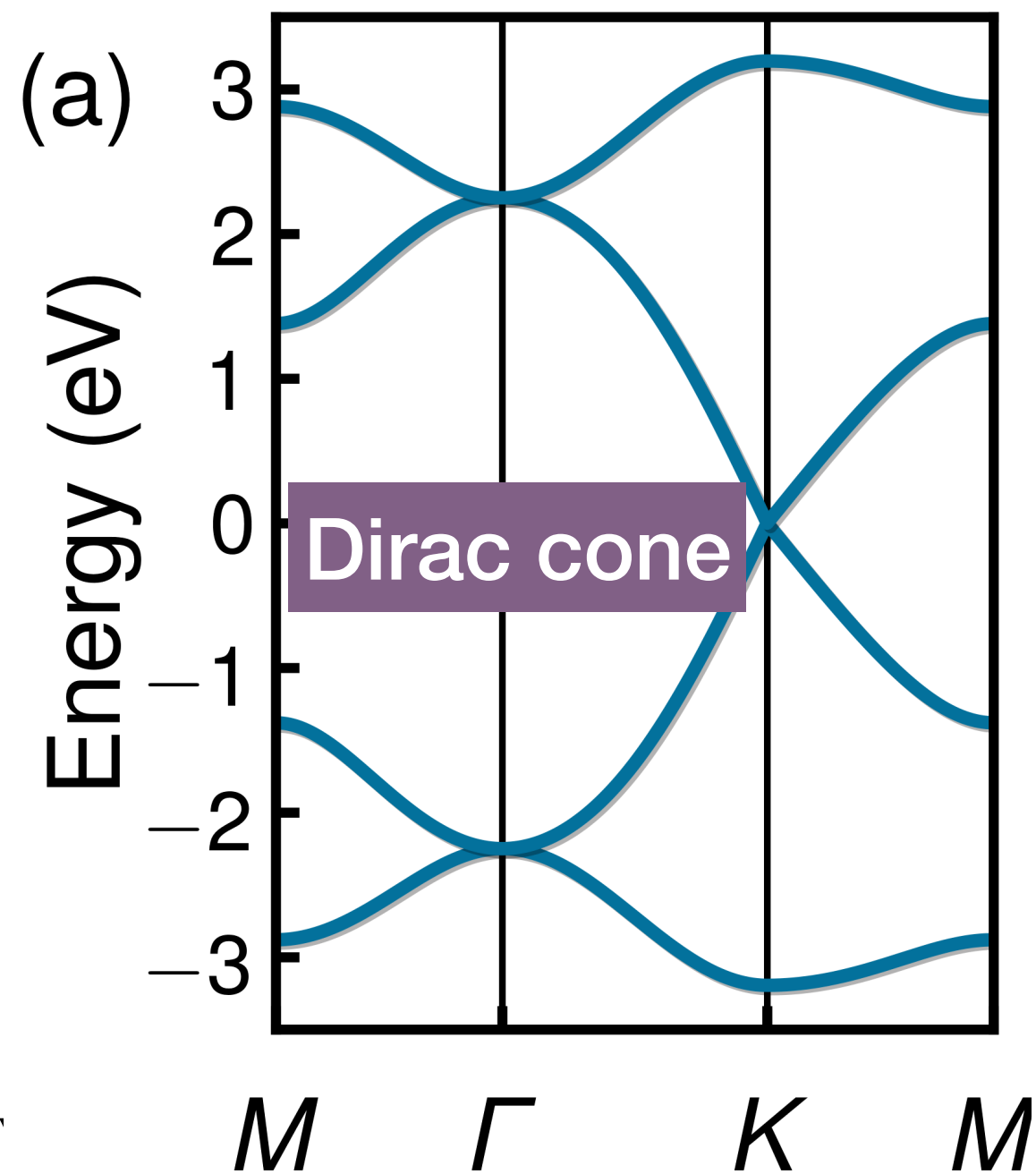
$$p_\mu = p_\pm = \frac{1}{\sqrt{2}}(p_x \pm ip_y)$$

On-site

S_z is a good quantum number

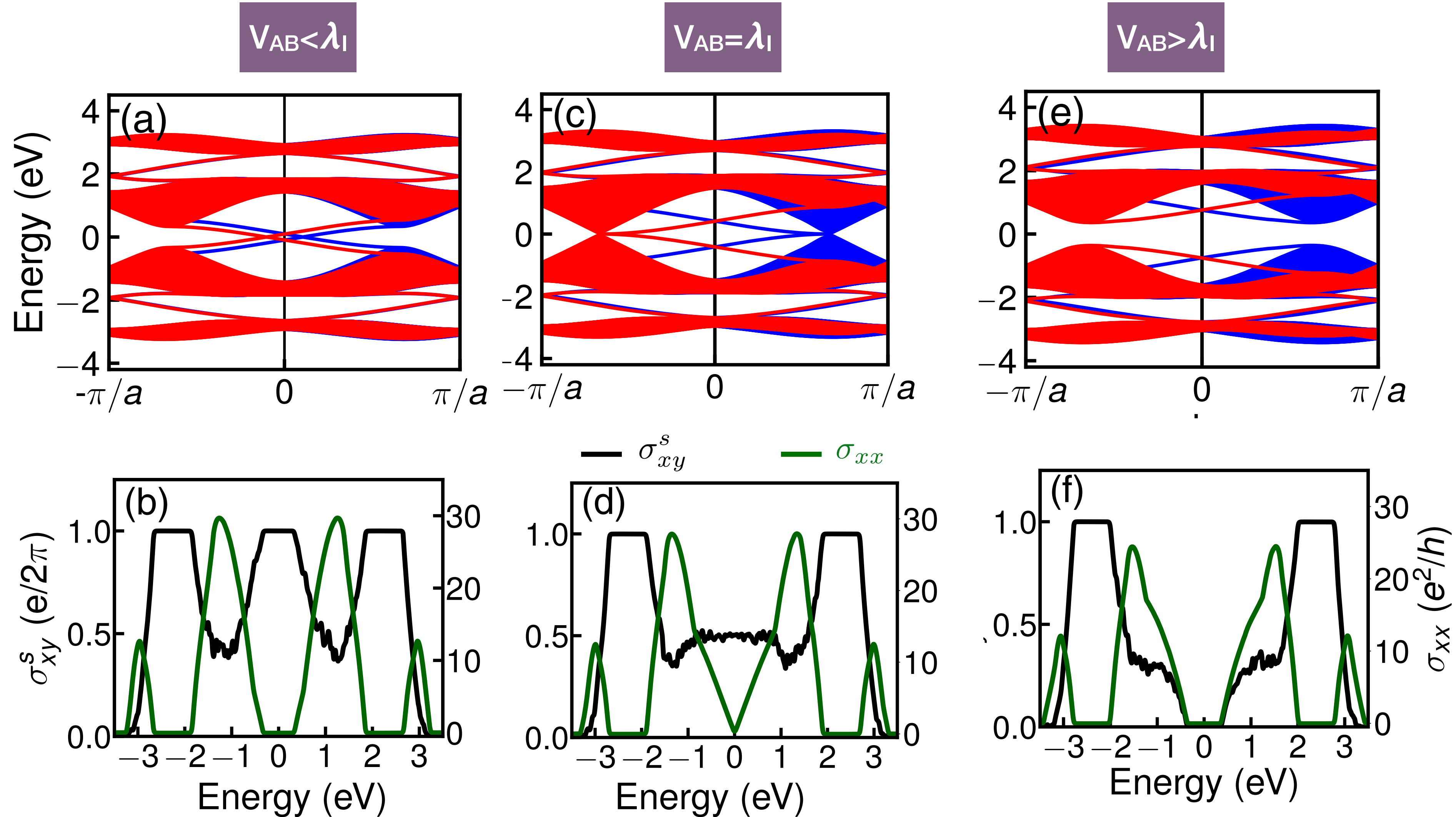


C. Wu, PRL (2008)





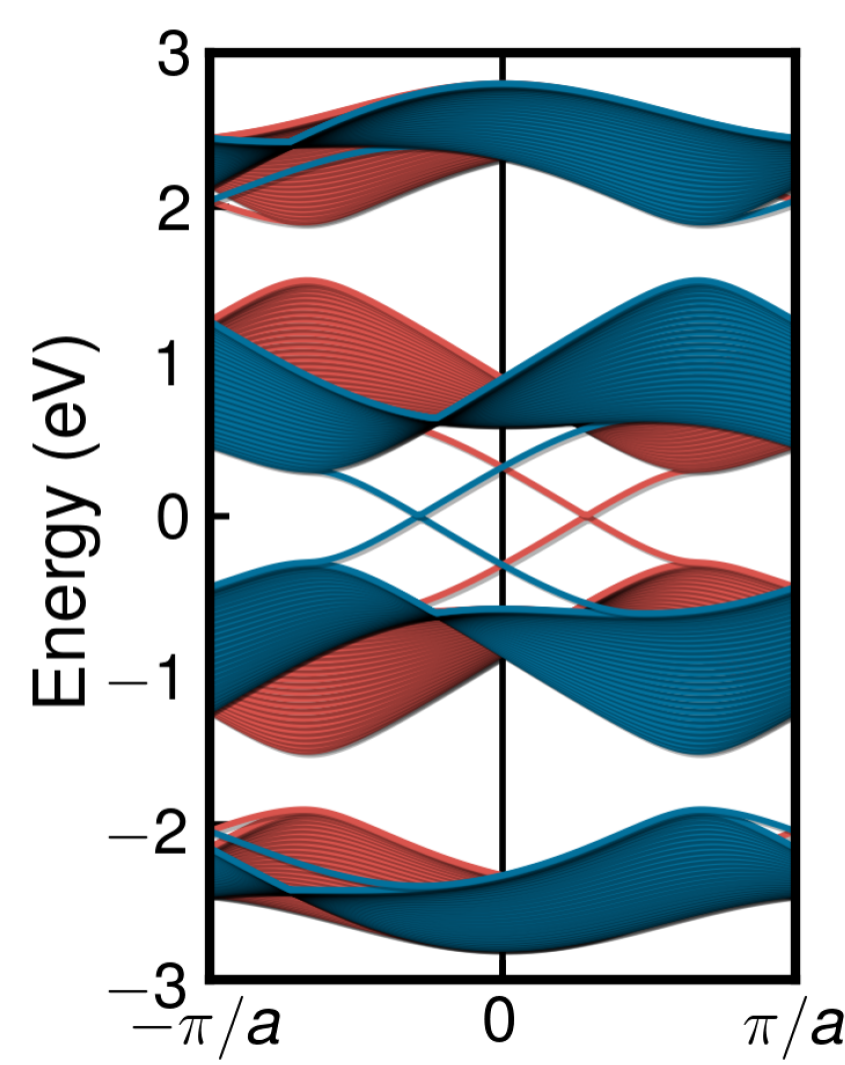
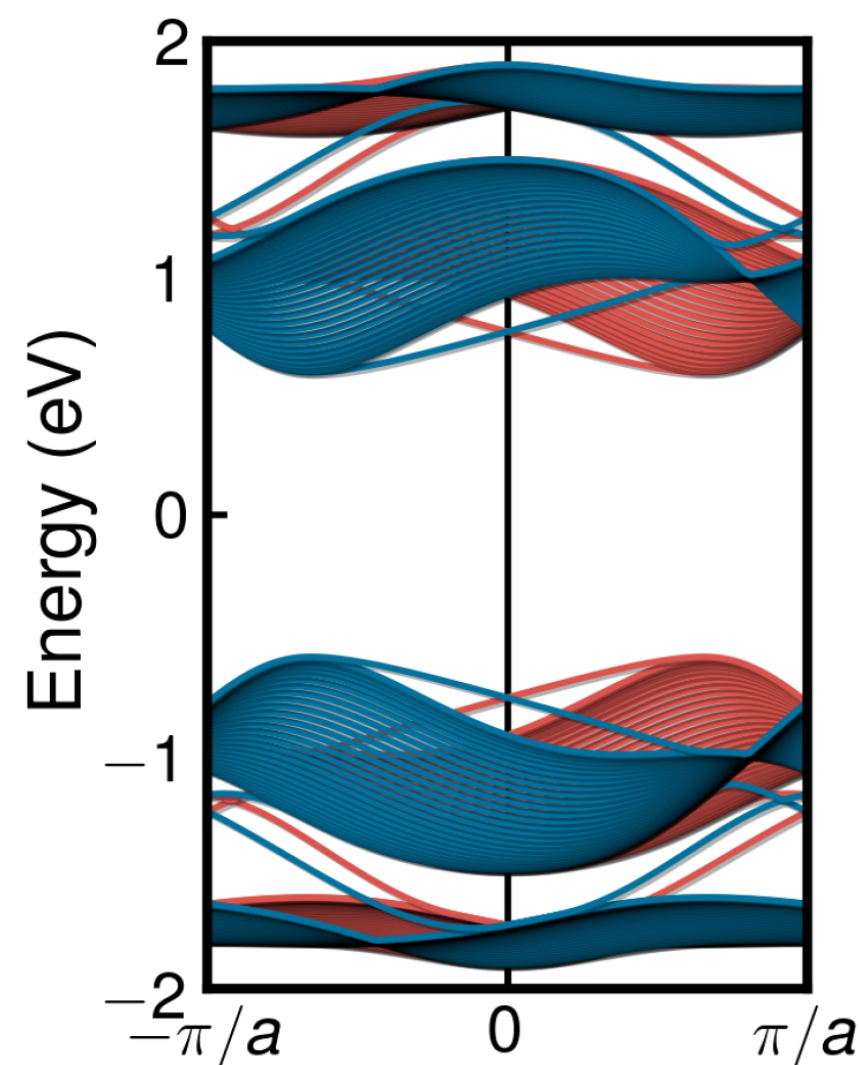
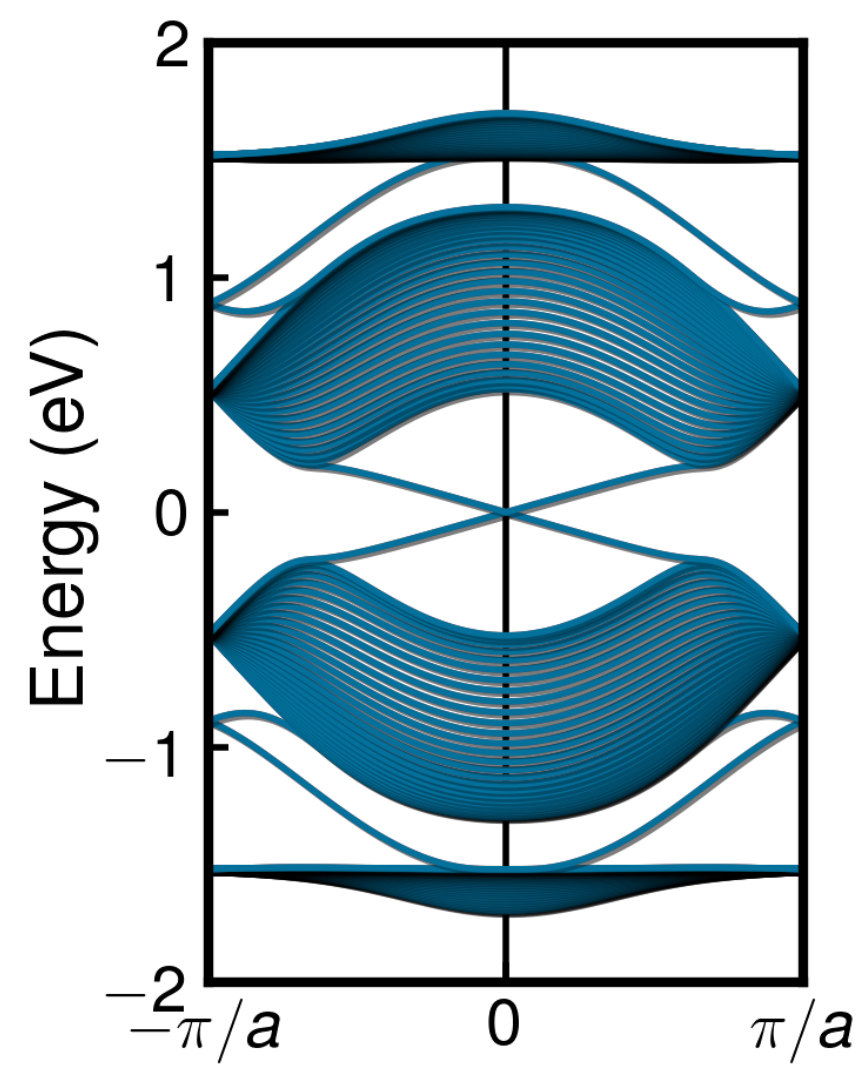
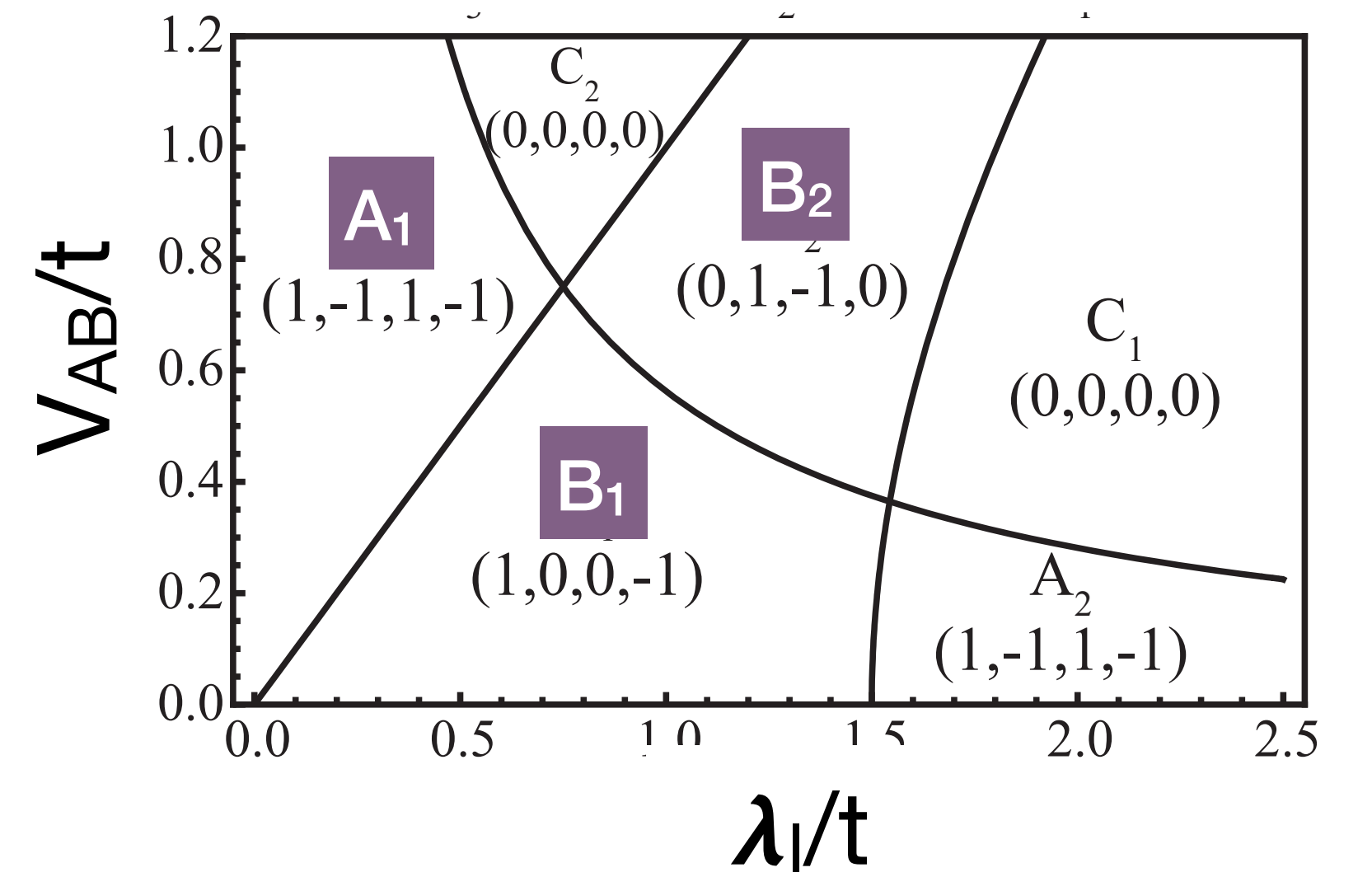
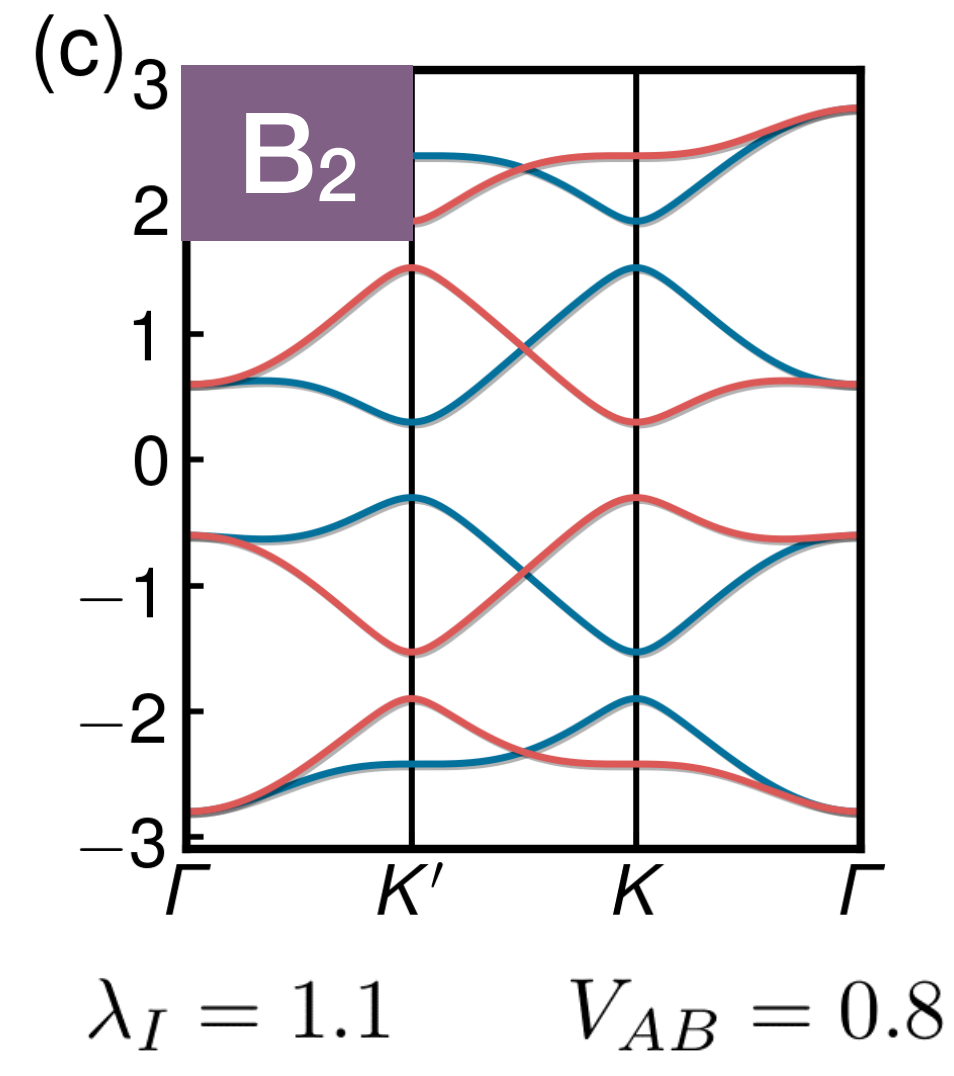
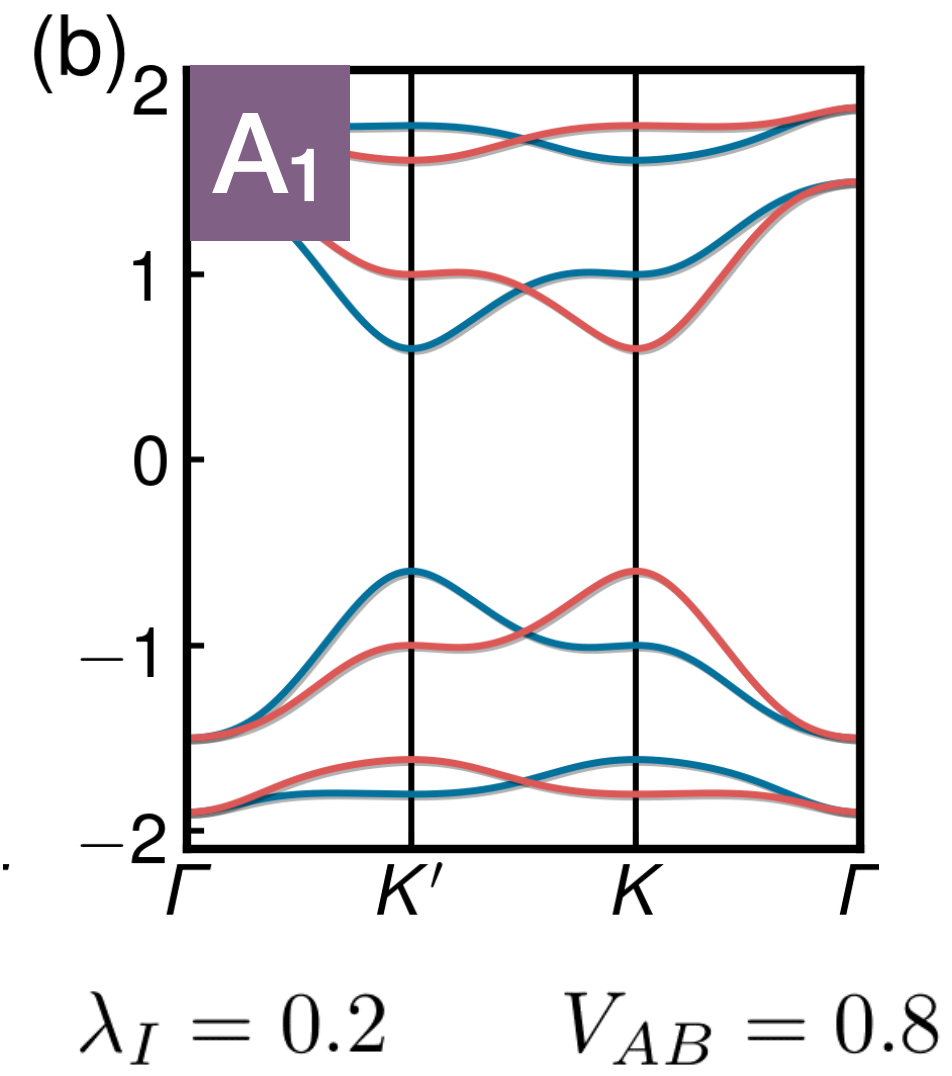
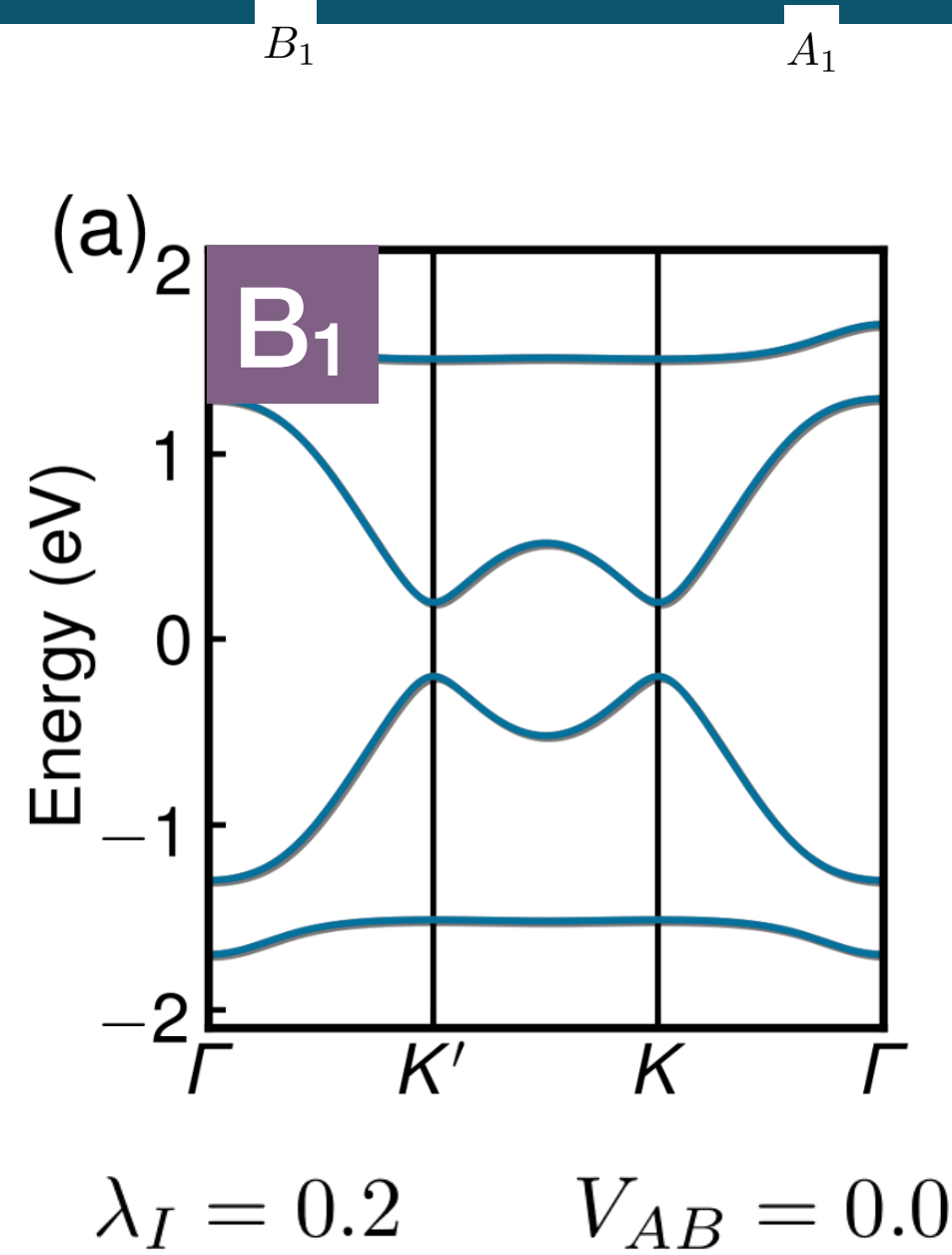
SUBLATTICE SYMMETRY BREAKING



Luis M. Canonico, Tatiana G. Rappoport, R. B. Muniz, Phys. Rev. Lett. 122 (2019) 196601.



P_X-P_Y : TOPOLOGICAL PHASE DIAGRAM



ORBITAL ANGULAR MOMENTUM



P_x - P_y - ORBITAL TEXTURES

Because of the restricted Hilbert space, we define the spinors:

$$l_z = |p_+\rangle\langle p_+| - |p_-\rangle\langle p_-|,$$

$$l_x = |p_+\rangle\langle p_-| + |p_-\rangle\langle p_+|,$$

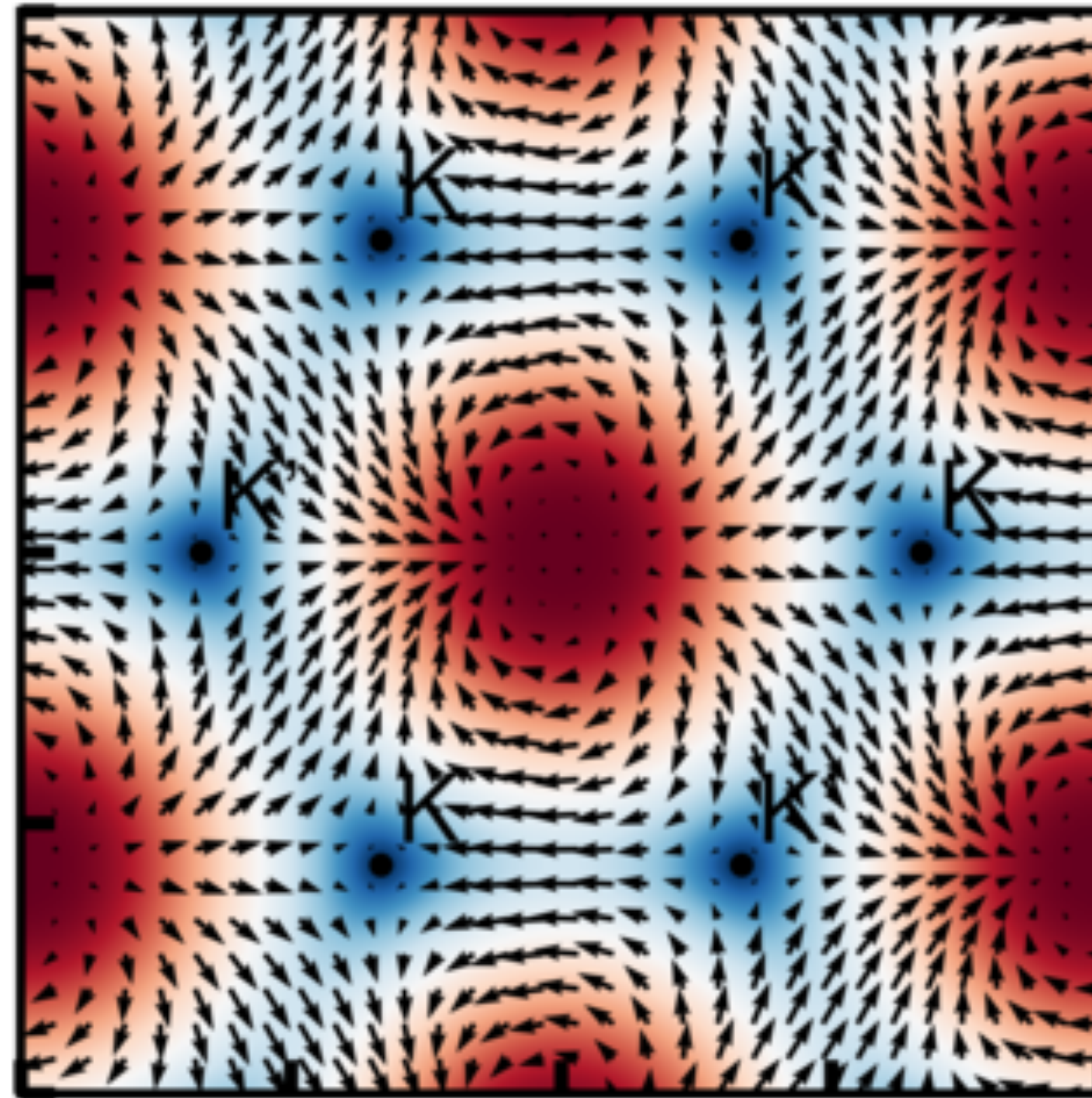
$$l_y = i(|p_-\rangle\langle p_+| - |p_+\rangle\langle p_-|).$$

$$\vec{l}_n(\vec{k}) = \langle l_x \rangle_n(\vec{k})\hat{x} + \langle l_y \rangle_n(\vec{k})\hat{y} + \langle l_z \rangle_n(\vec{k})\hat{z},$$

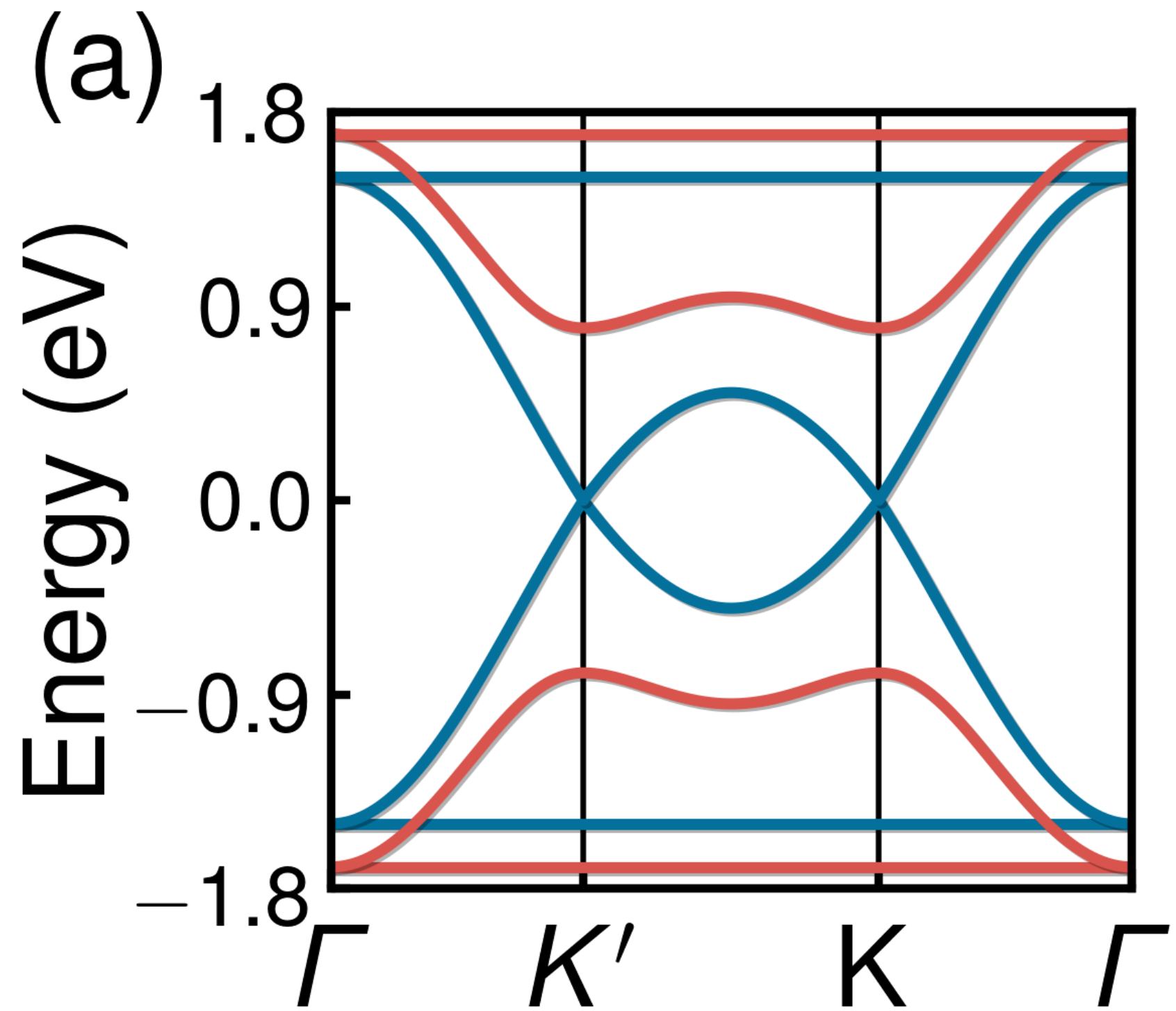
$$\langle l_i \rangle_n(\vec{k}) = \sum_{\sigma=A,B} \langle \psi_n(\vec{k}) | l_i(\sigma) | \psi_n(\vec{k}) \rangle,$$

$$H_D = -\frac{\sqrt{3}\hbar v_F}{2a} (l_x \sigma_x + \tau l_y \sigma_y).$$

$$p_\mu = p_\pm = \frac{1}{\sqrt{2}}(p_x \pm ip_y)$$

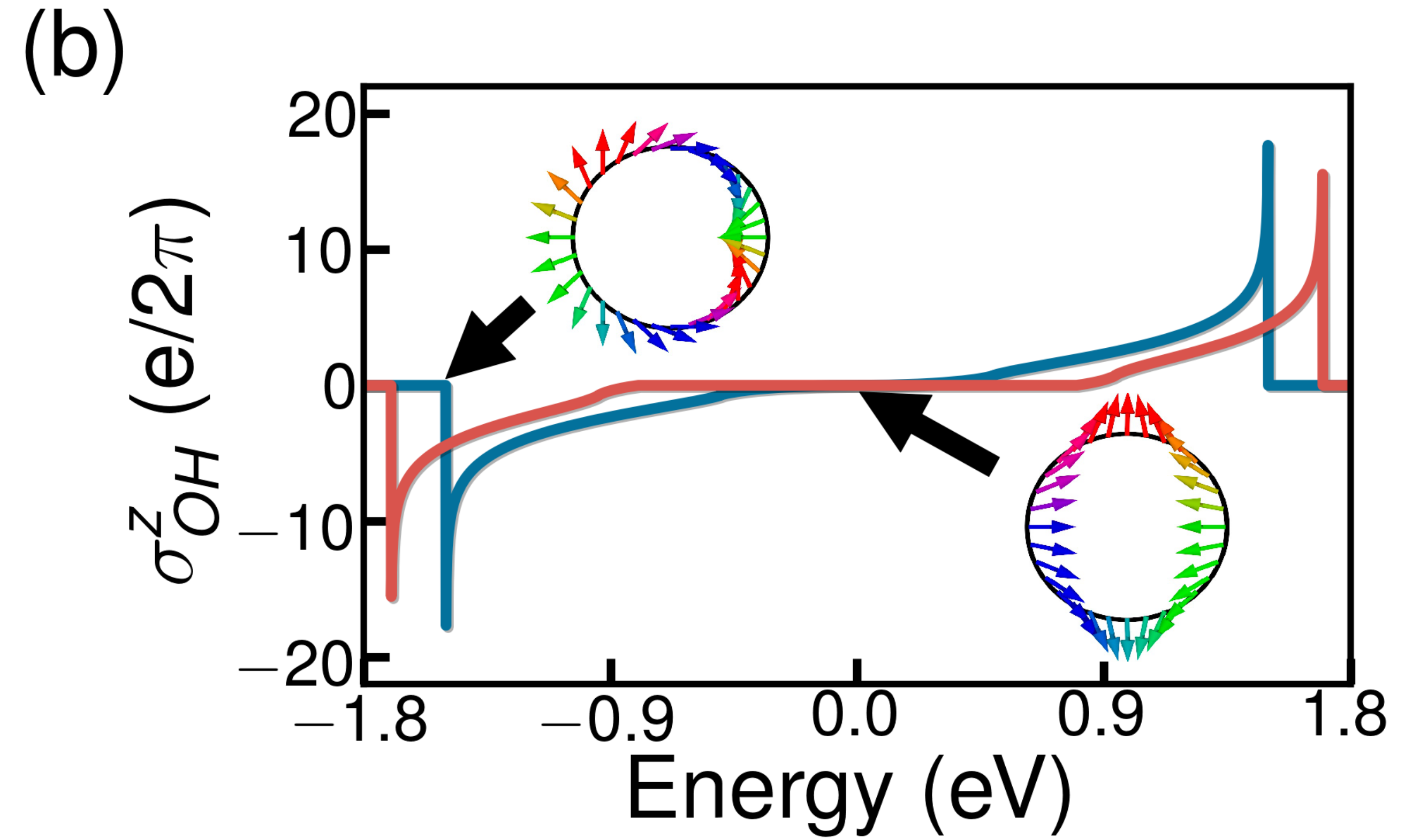


$$\lambda_I = 0$$

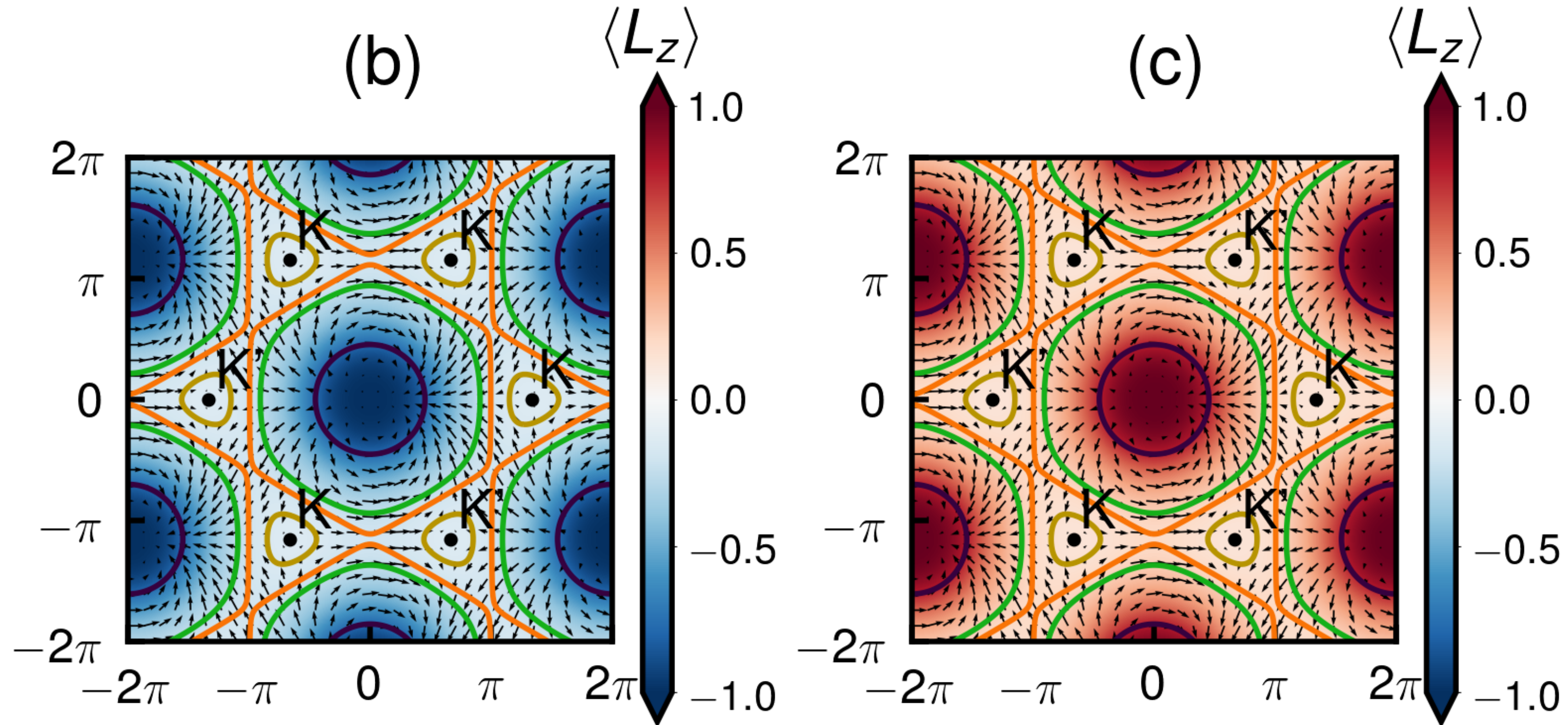


$V_{AB} = 0.0$ $V_{AB} = 0.8$

█ █



J. Sinova et al. PRL 2004

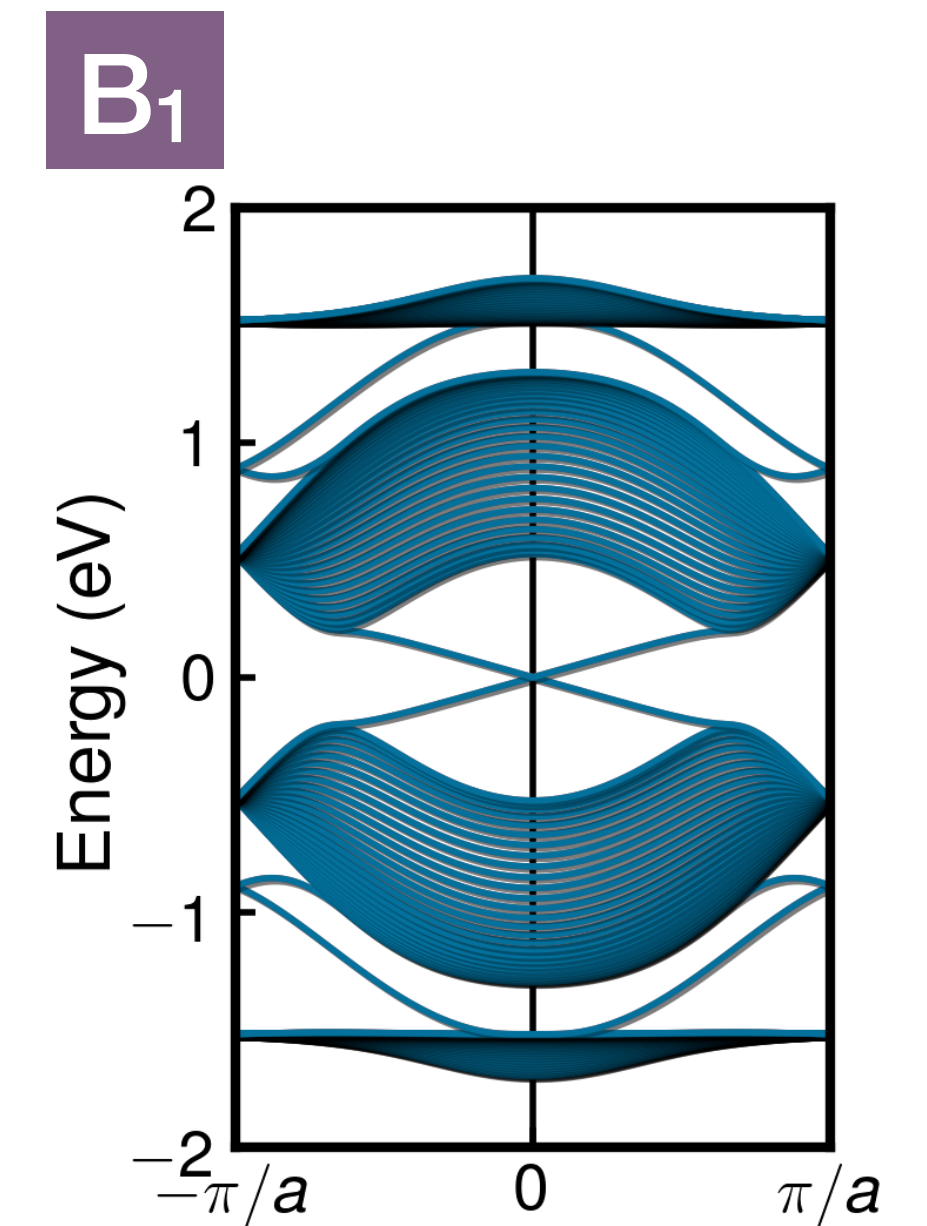
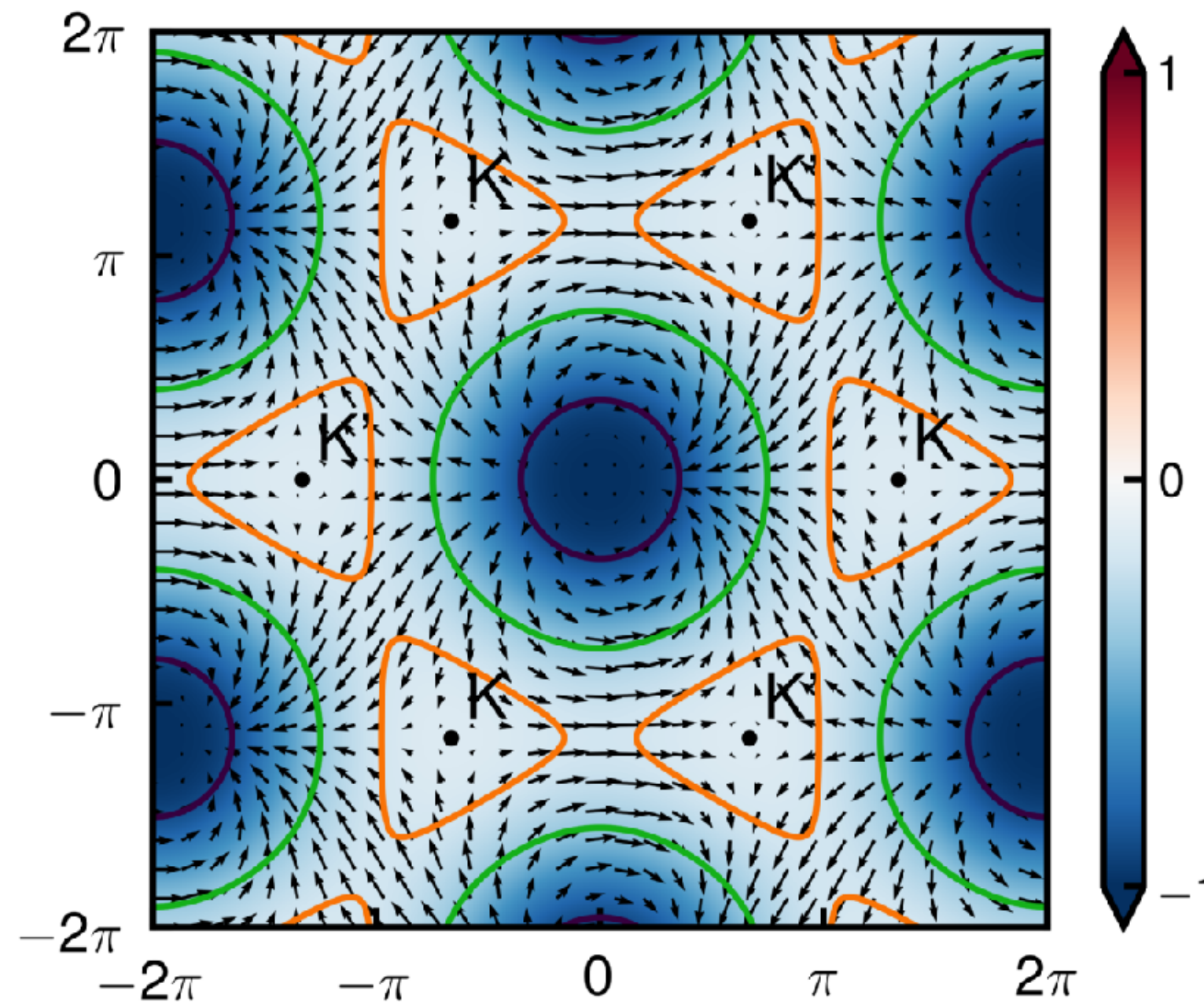
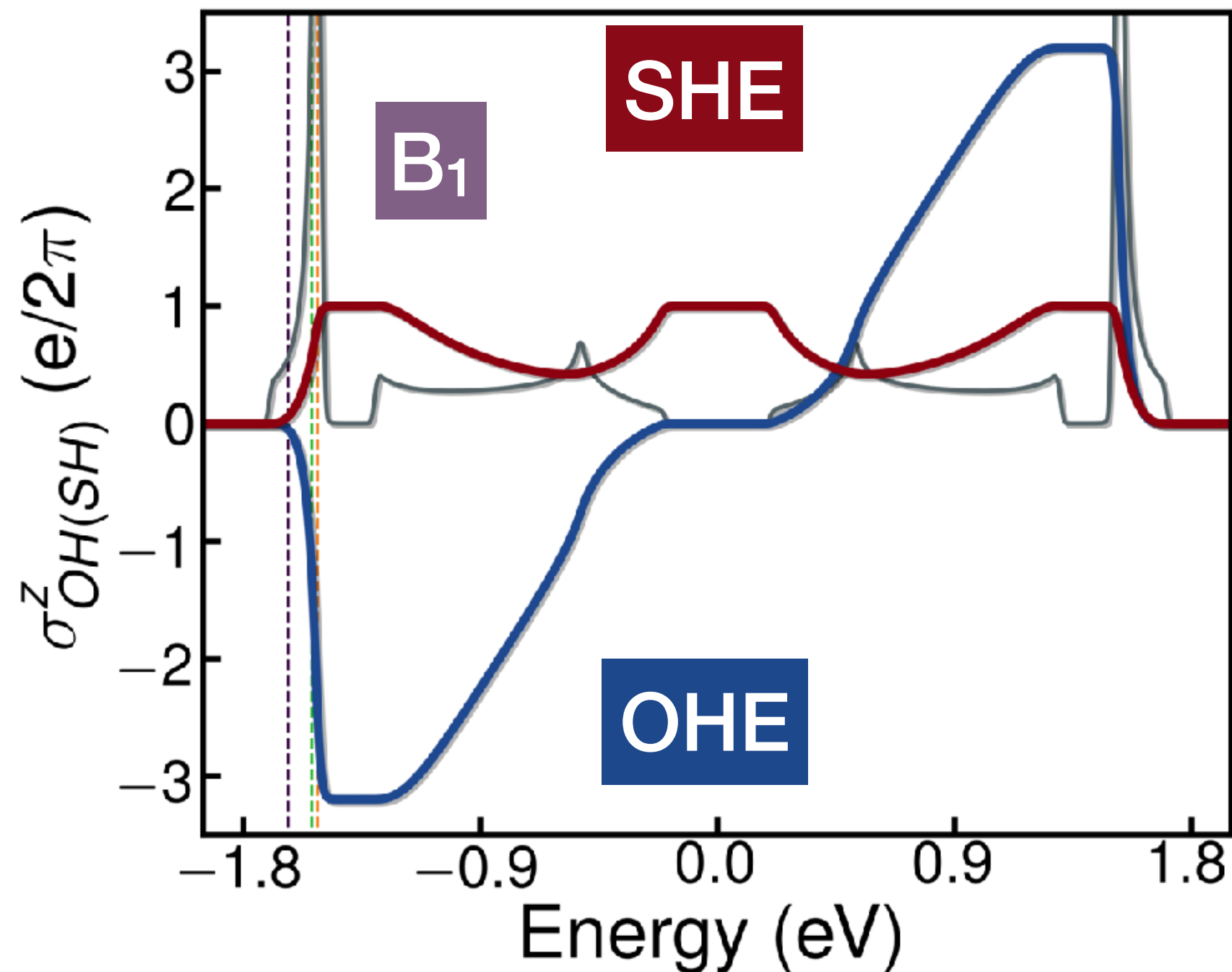
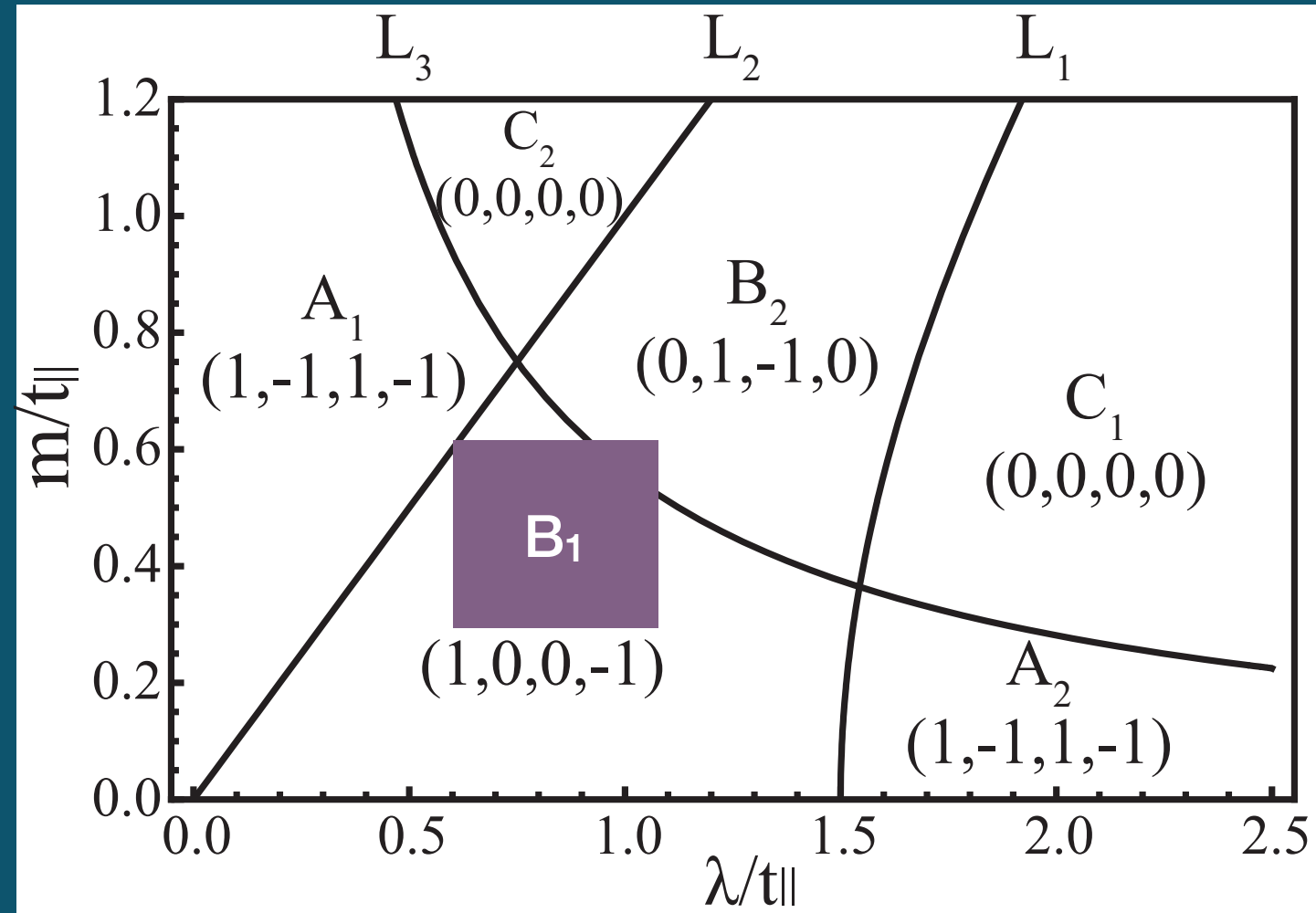


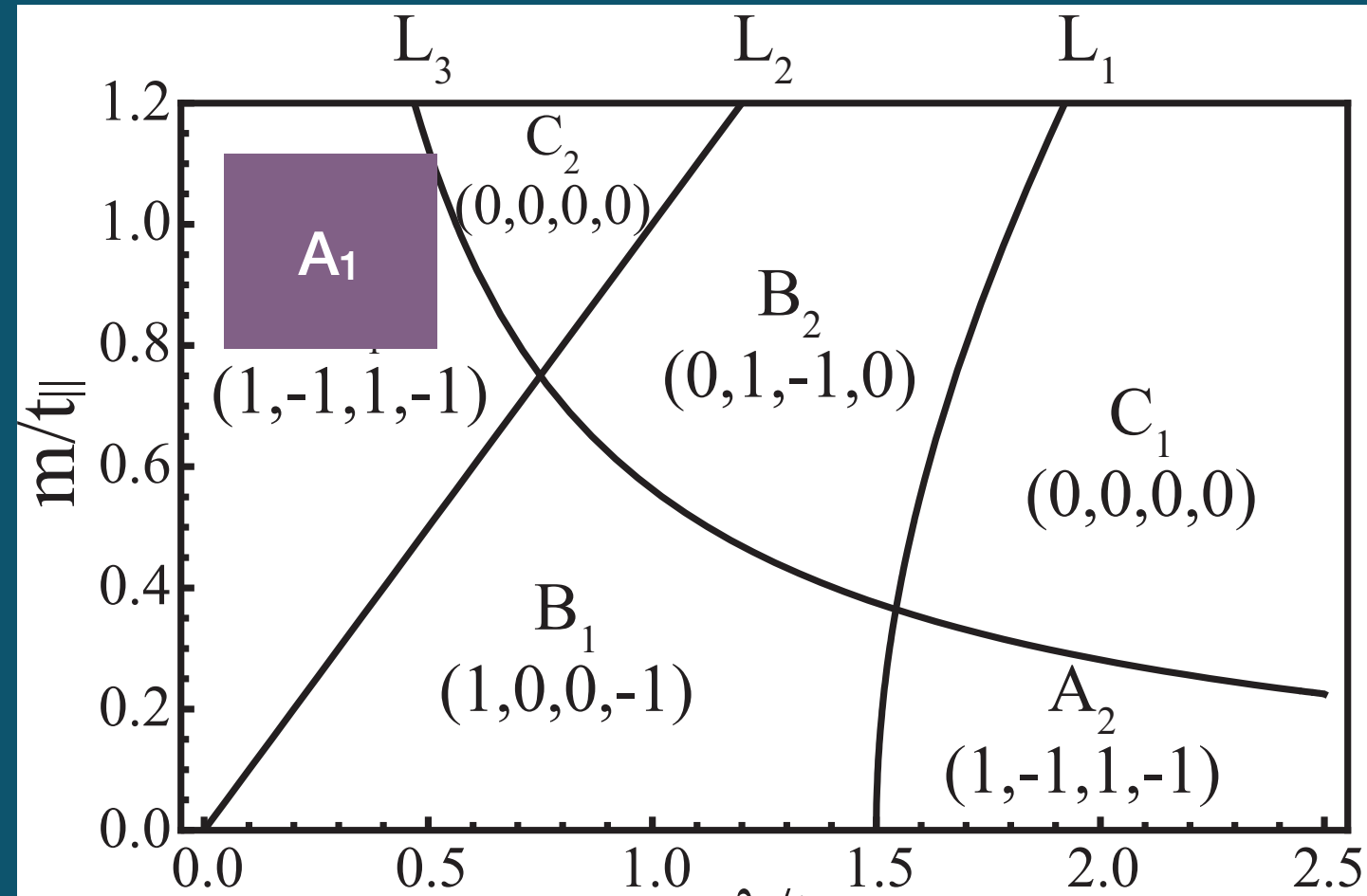
Dresselhaus "SOC"

Degenerate bands: $\Rightarrow \langle l_t^z \rangle = 0$
 In-plane orbital texture survives

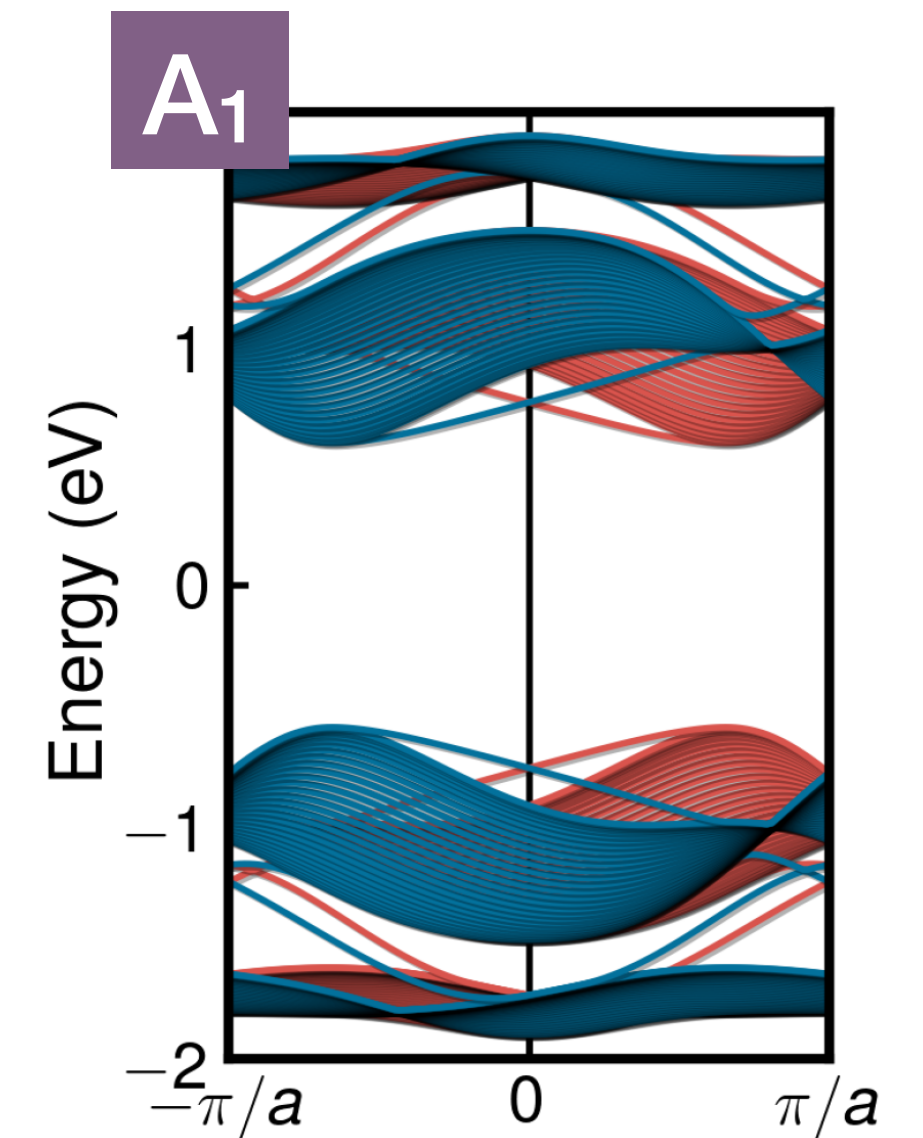
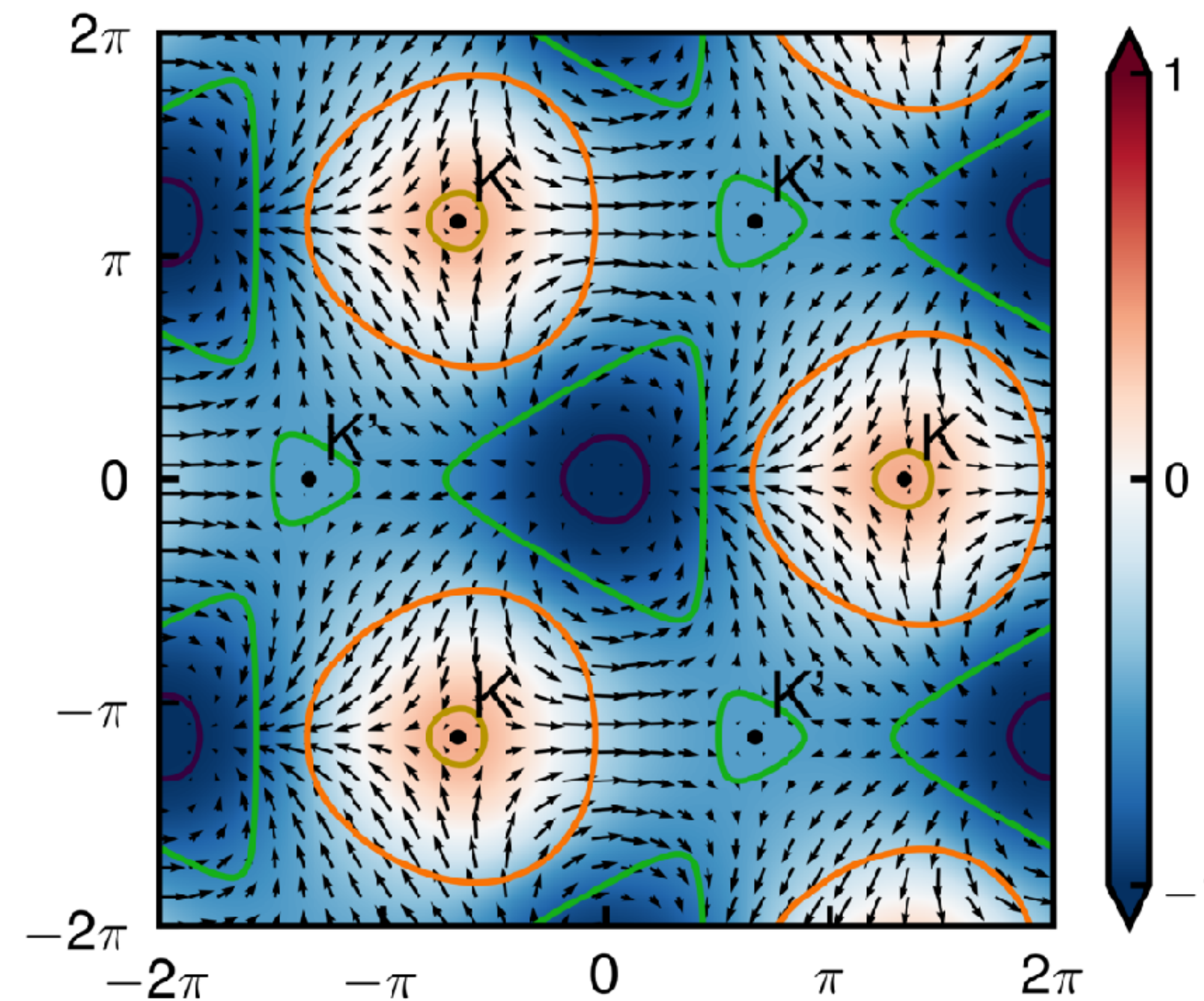
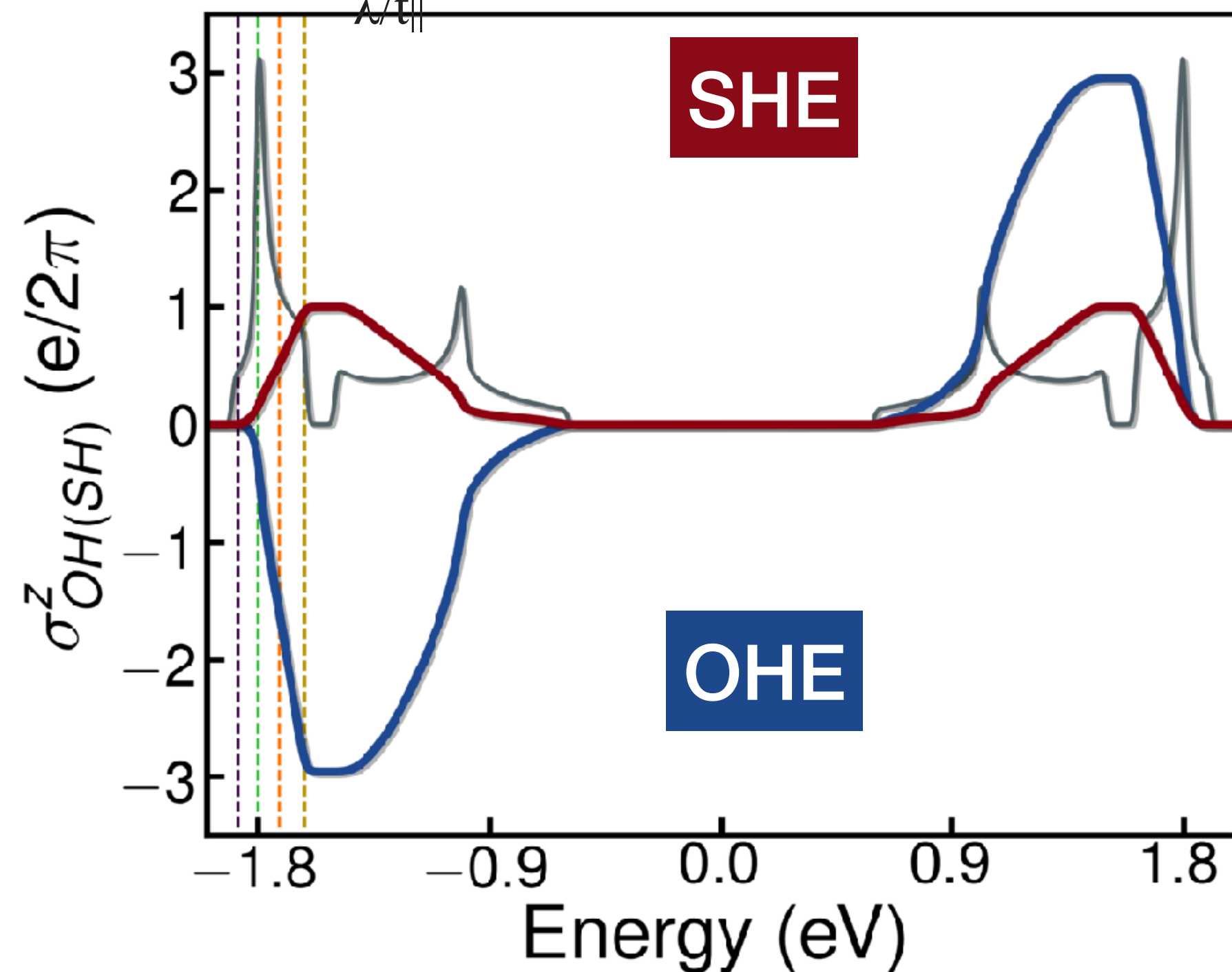
$$H_D = -\frac{\sqrt{3}\hbar v_F}{2a} (\ell_x \sigma_x + \tau \ell_y \sigma_y).$$

B1 with $\lambda_I = 0.2V_{pp\sigma}$ and $V_{AB} = 0$.



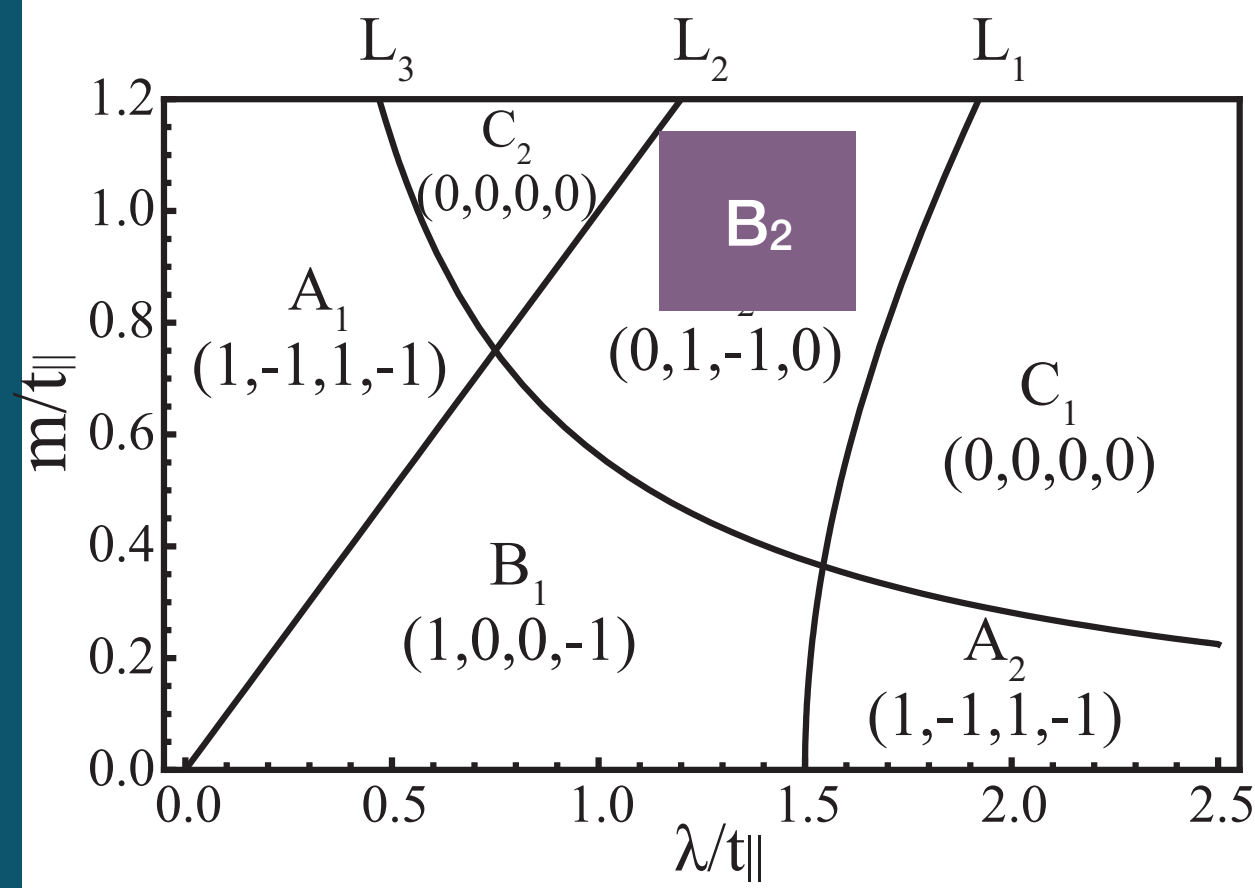


A1 with $\lambda_I = 0.2V_{pp\sigma}$ and $V_{AB} = 0.8V_{pp\sigma}$

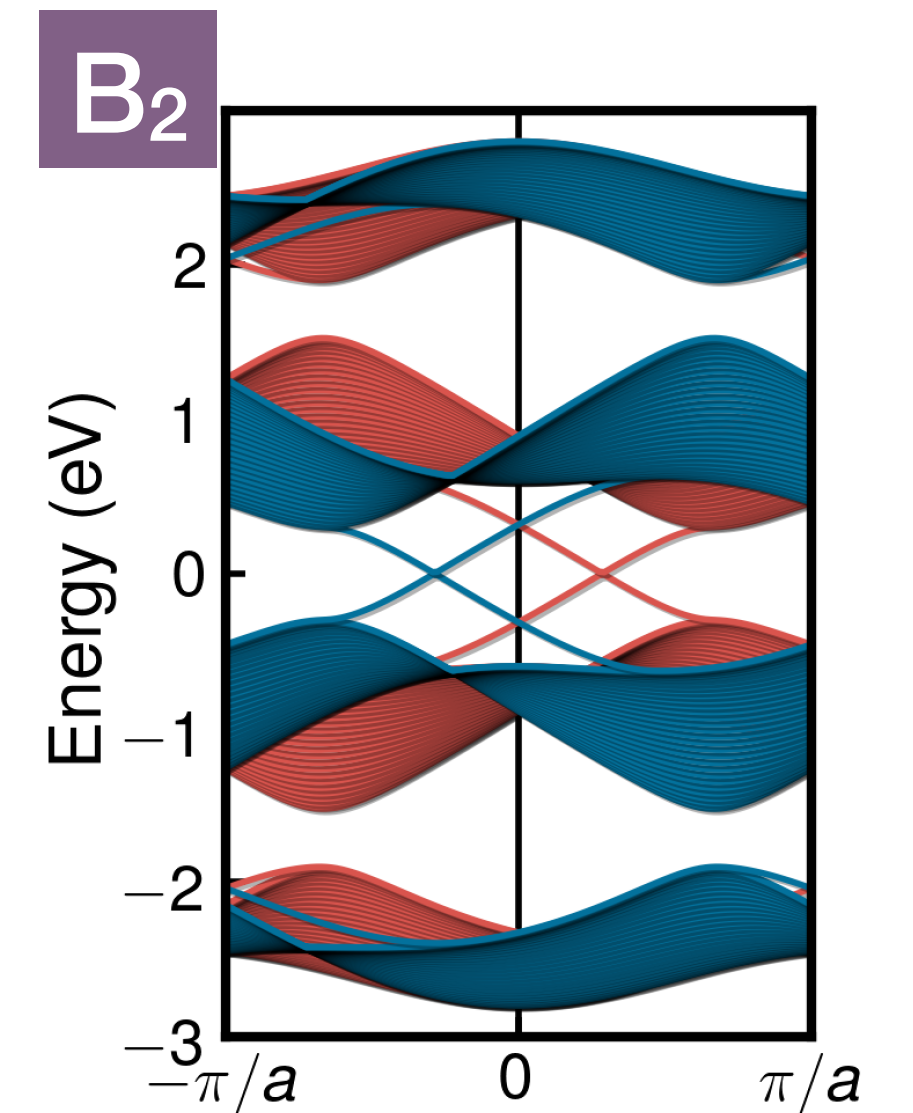
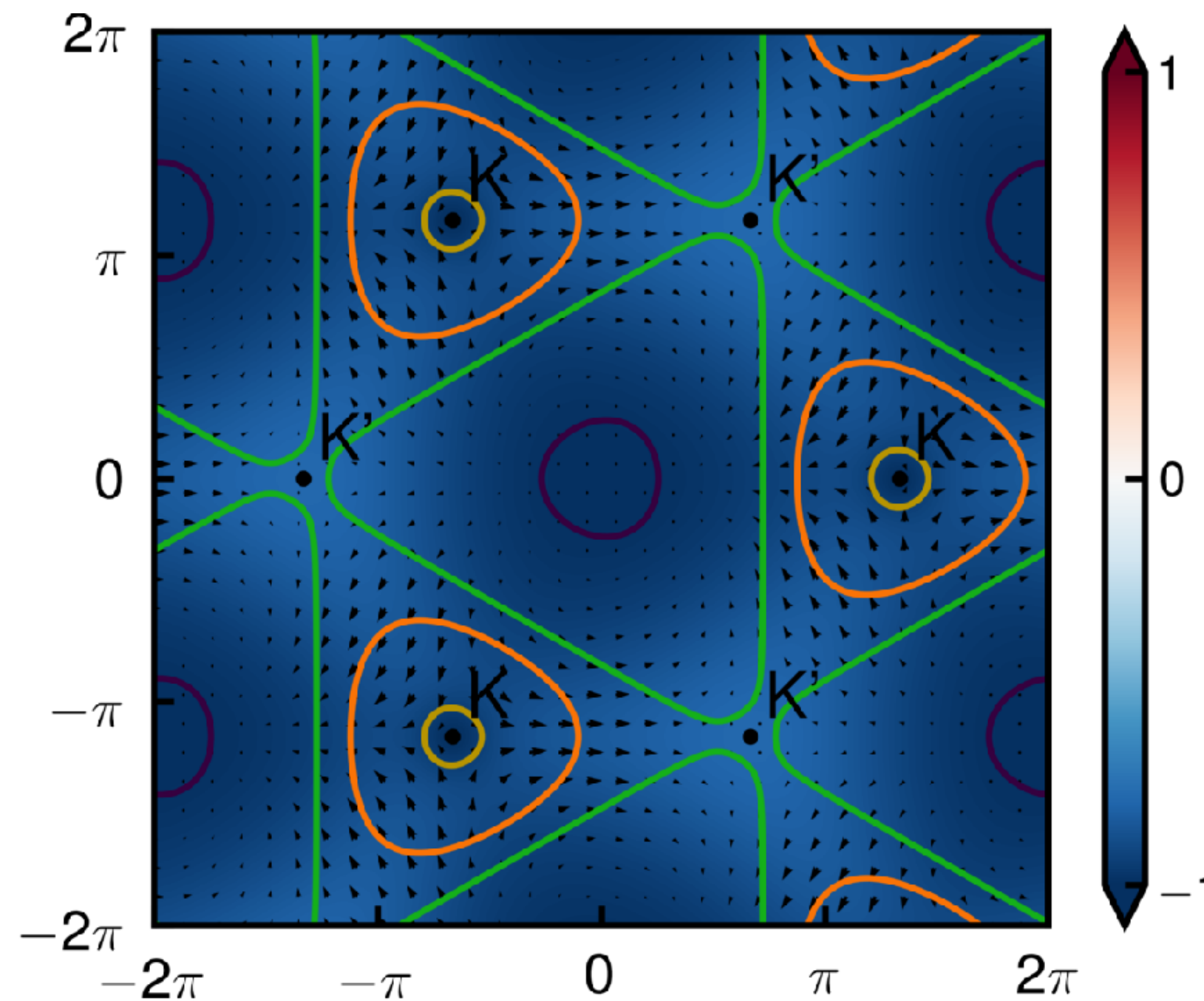
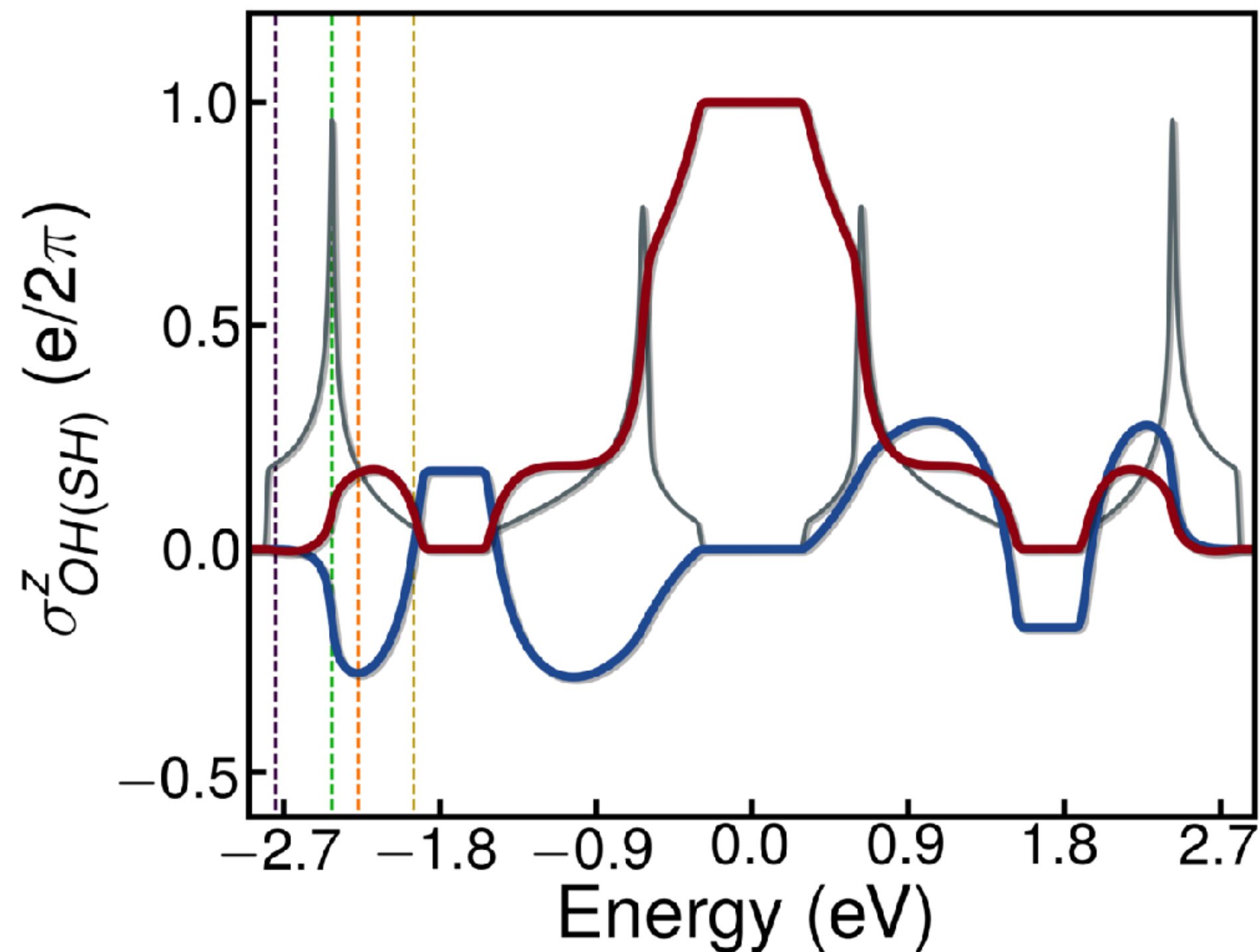




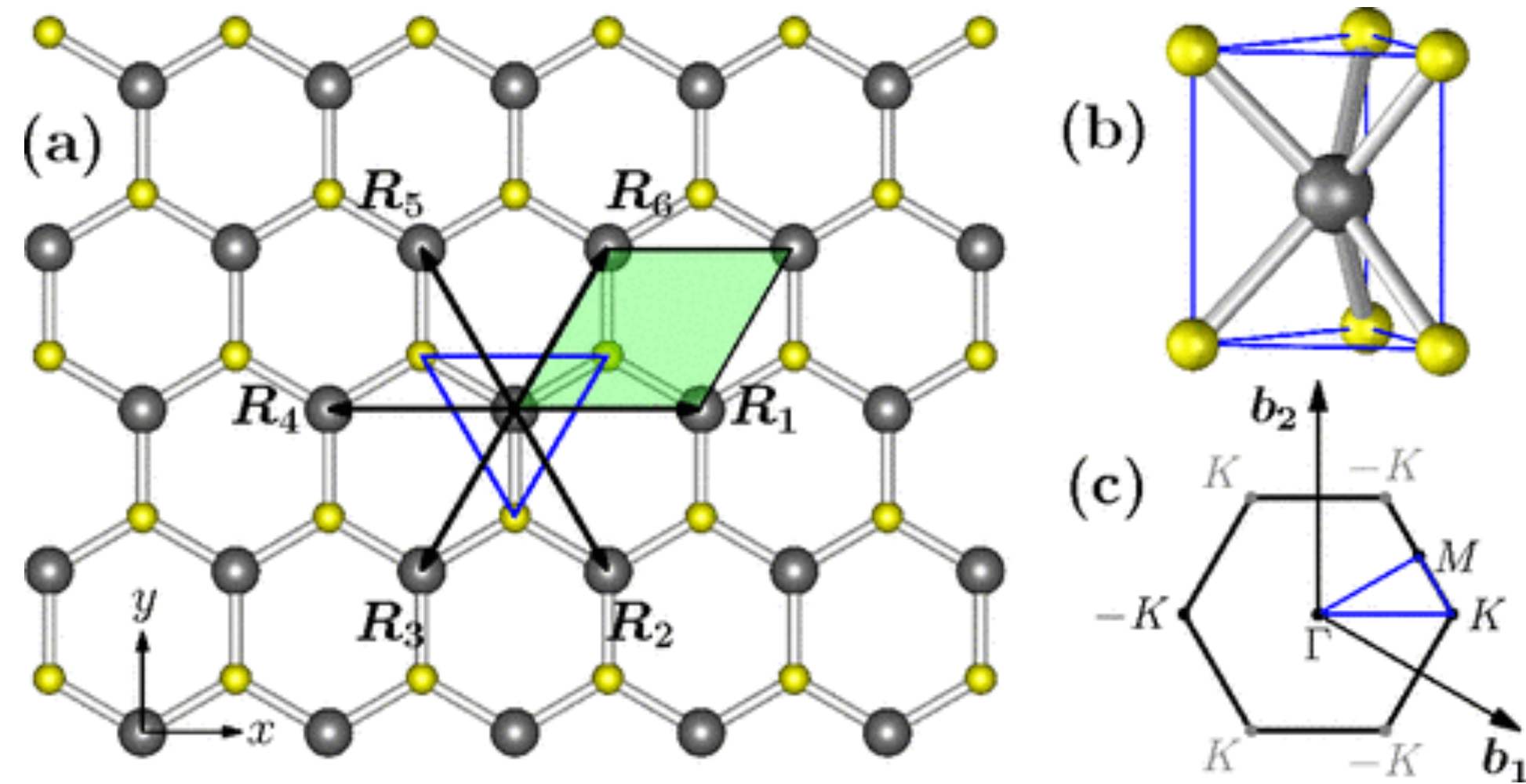
OHE - PHASE B2



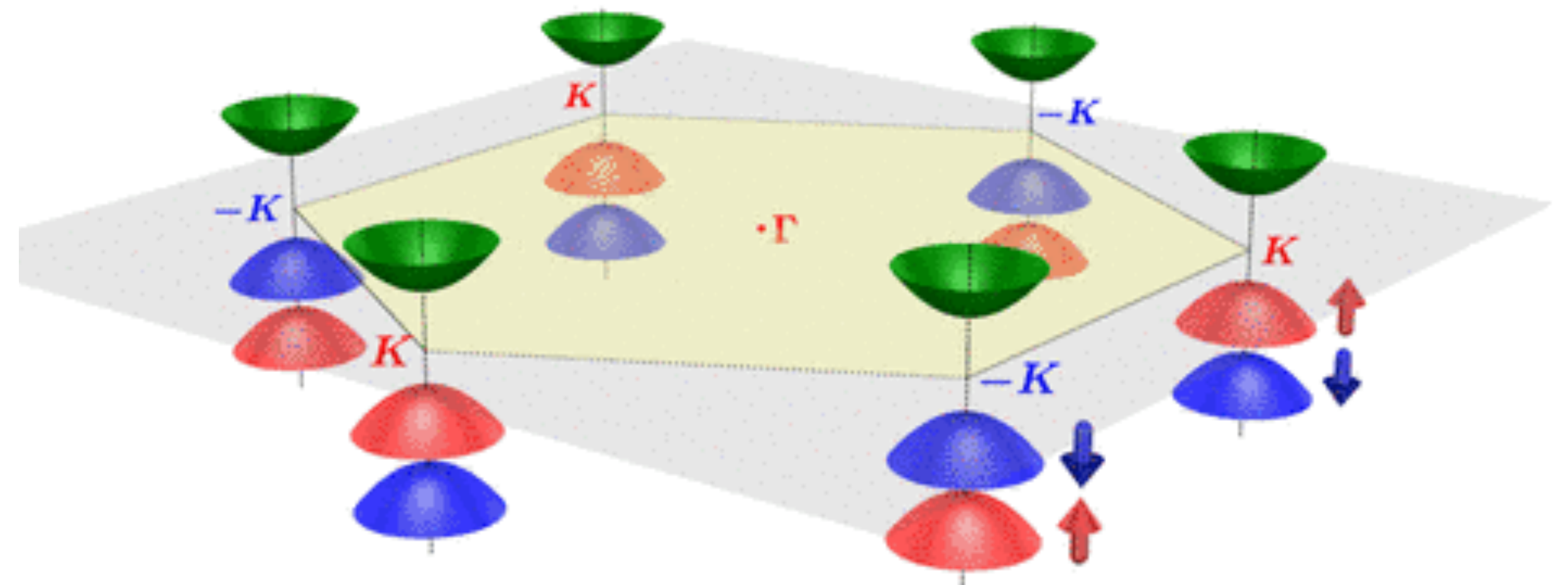
B2 with $\lambda_I = 1.1V_{pp\sigma}$ and $V_{AB} = 0.8V_{pp\sigma}$



OHE IN TMDS



Spin-valley locking

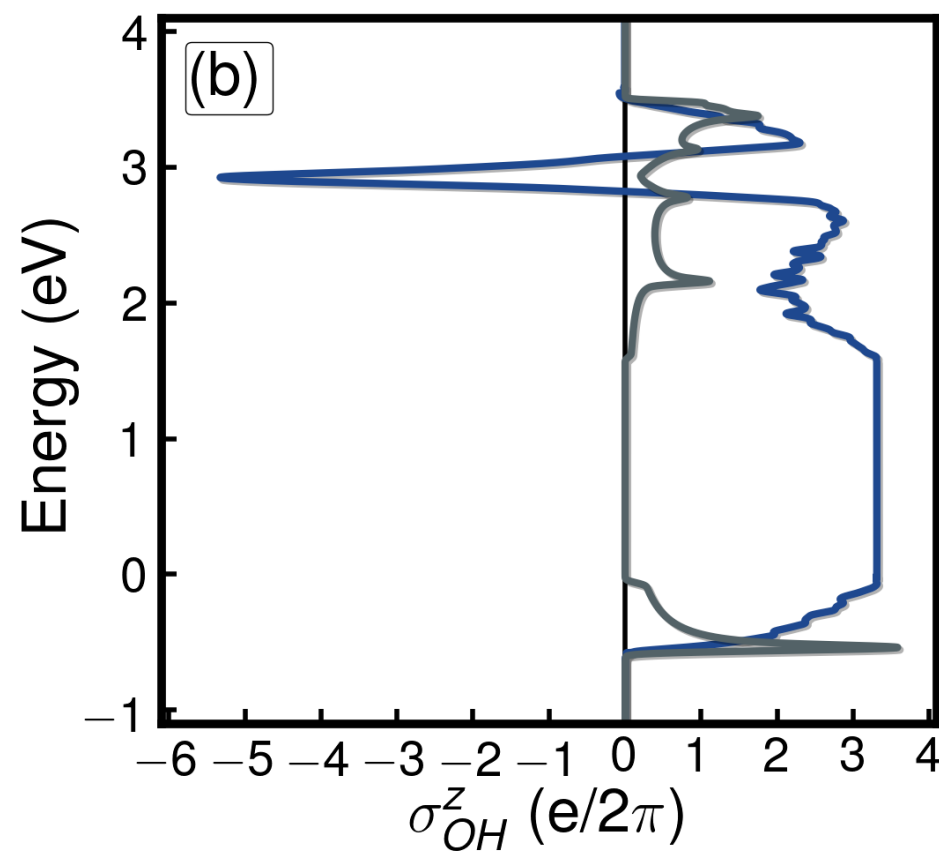
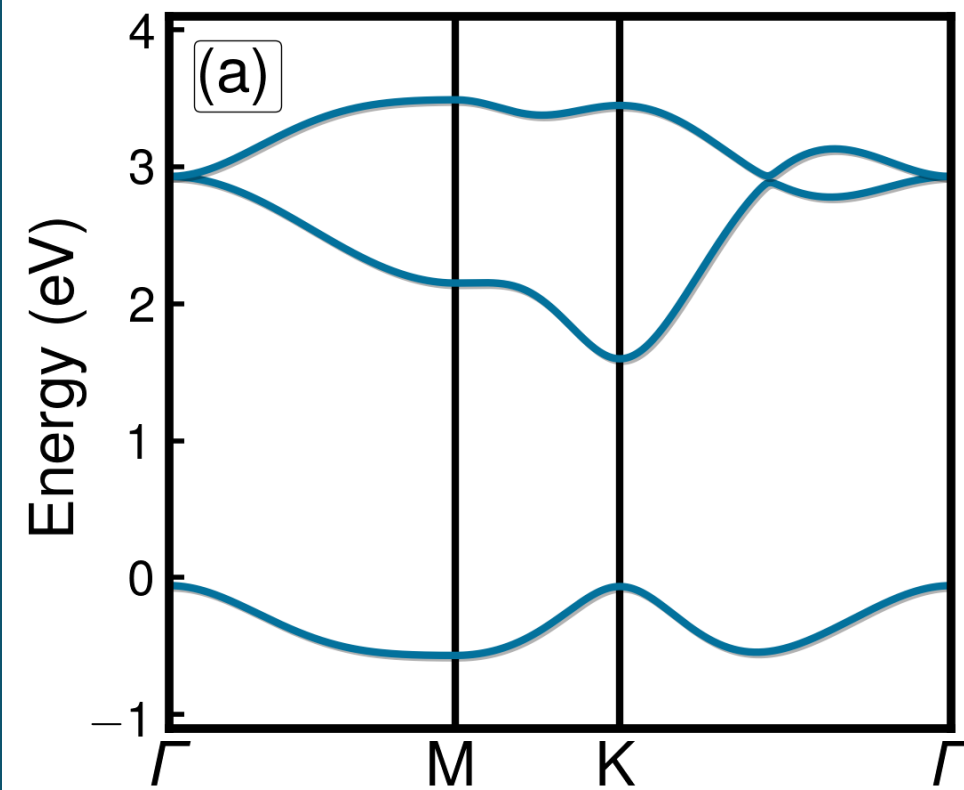


3 bands model based on TM **d** orbitals

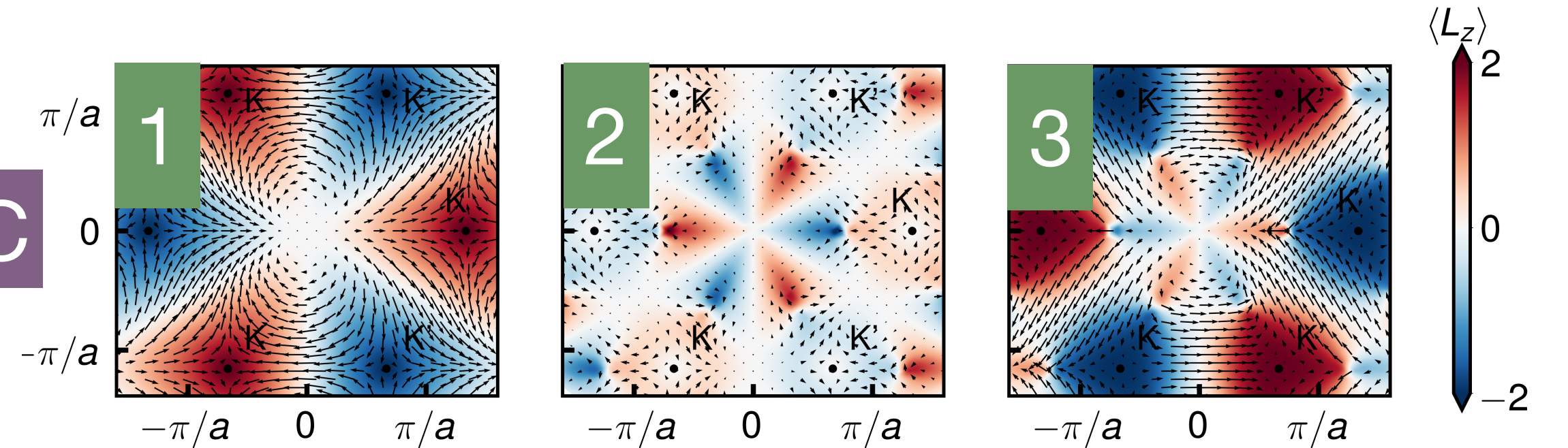
$$d_{z^2}, d_{xy} \text{ and } d_{x^2+y^2}, \quad \mathbf{L}^z = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 2i \\ 0 & -2i & 0 \end{bmatrix}$$

G. B. Liu et al, PRB 2012
Di Xiao, PRL 2012

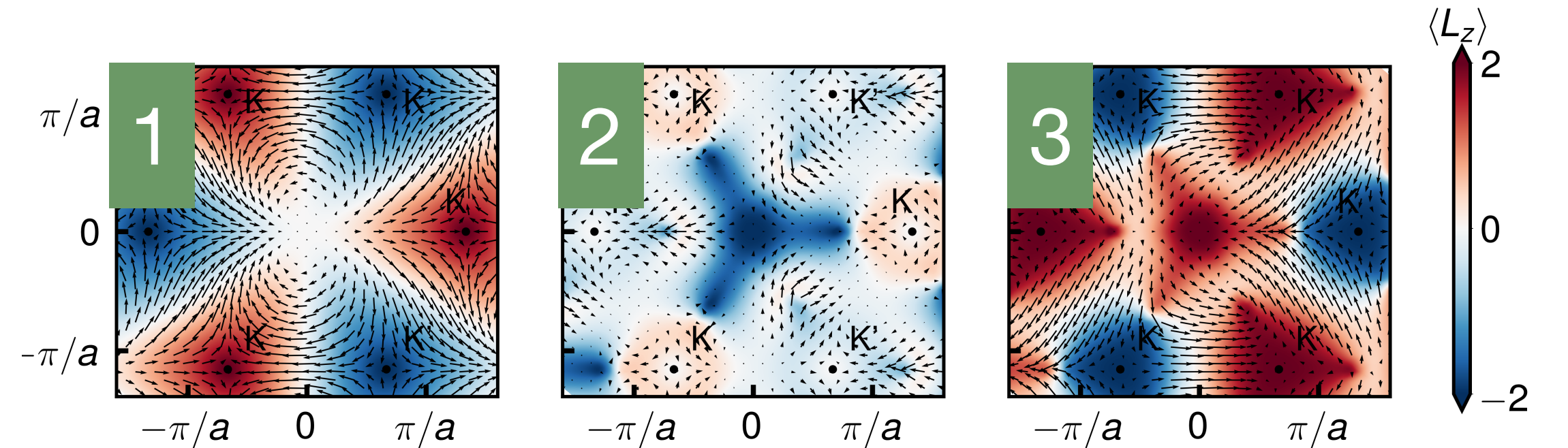
Orbital-Valley locking in the valence band!



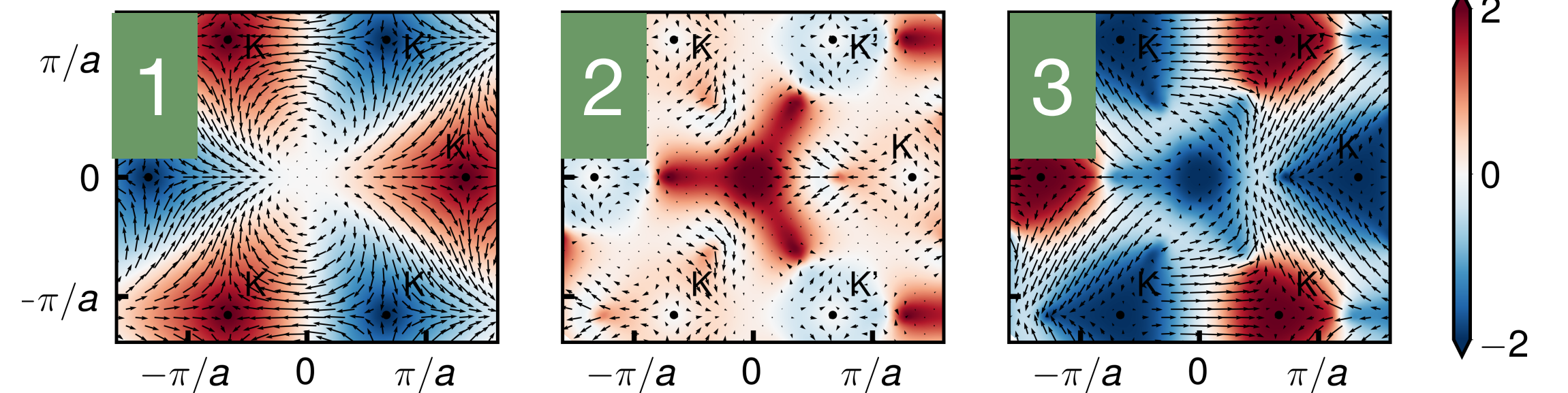
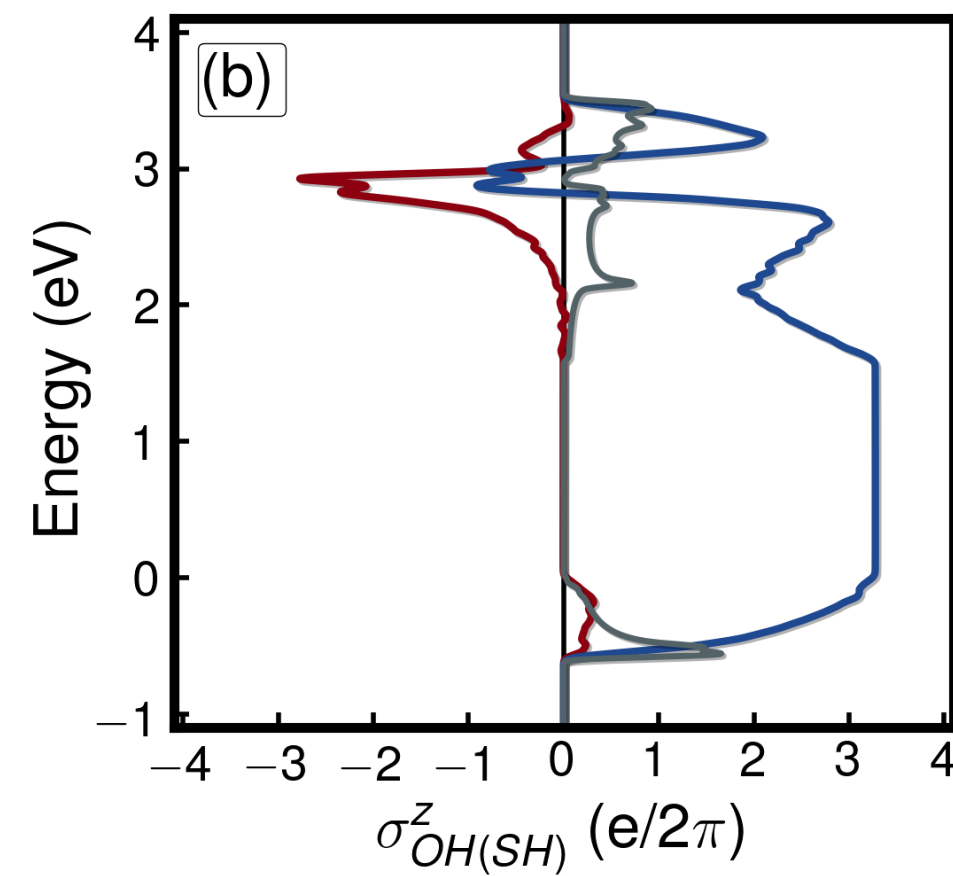
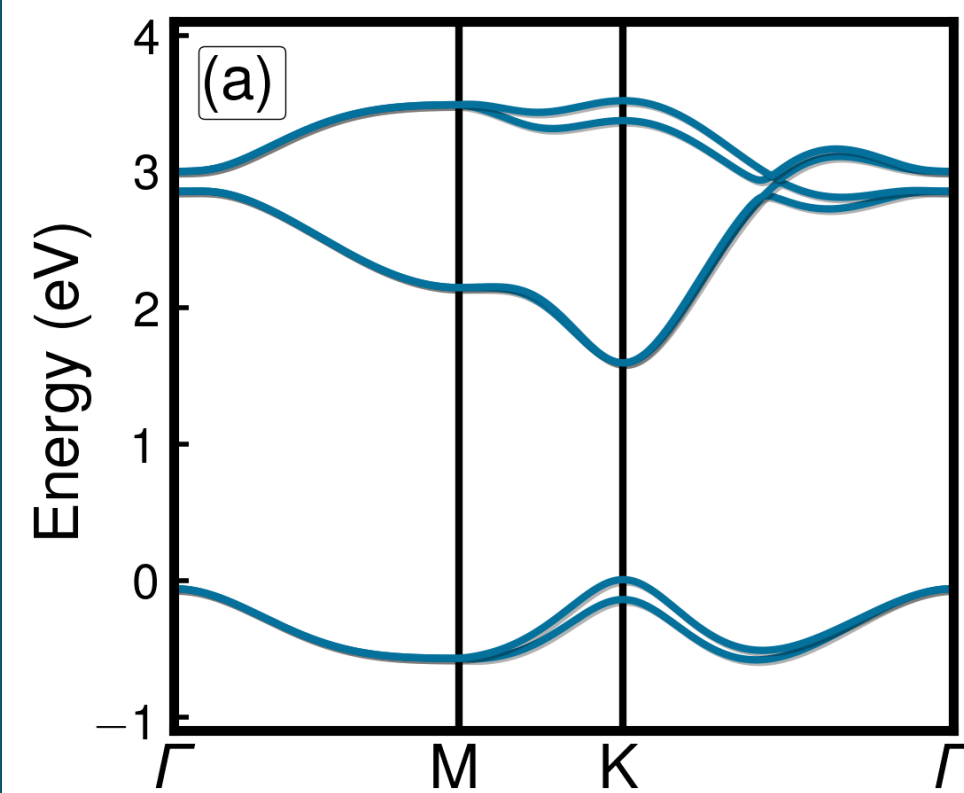
Zero SOC



SOC

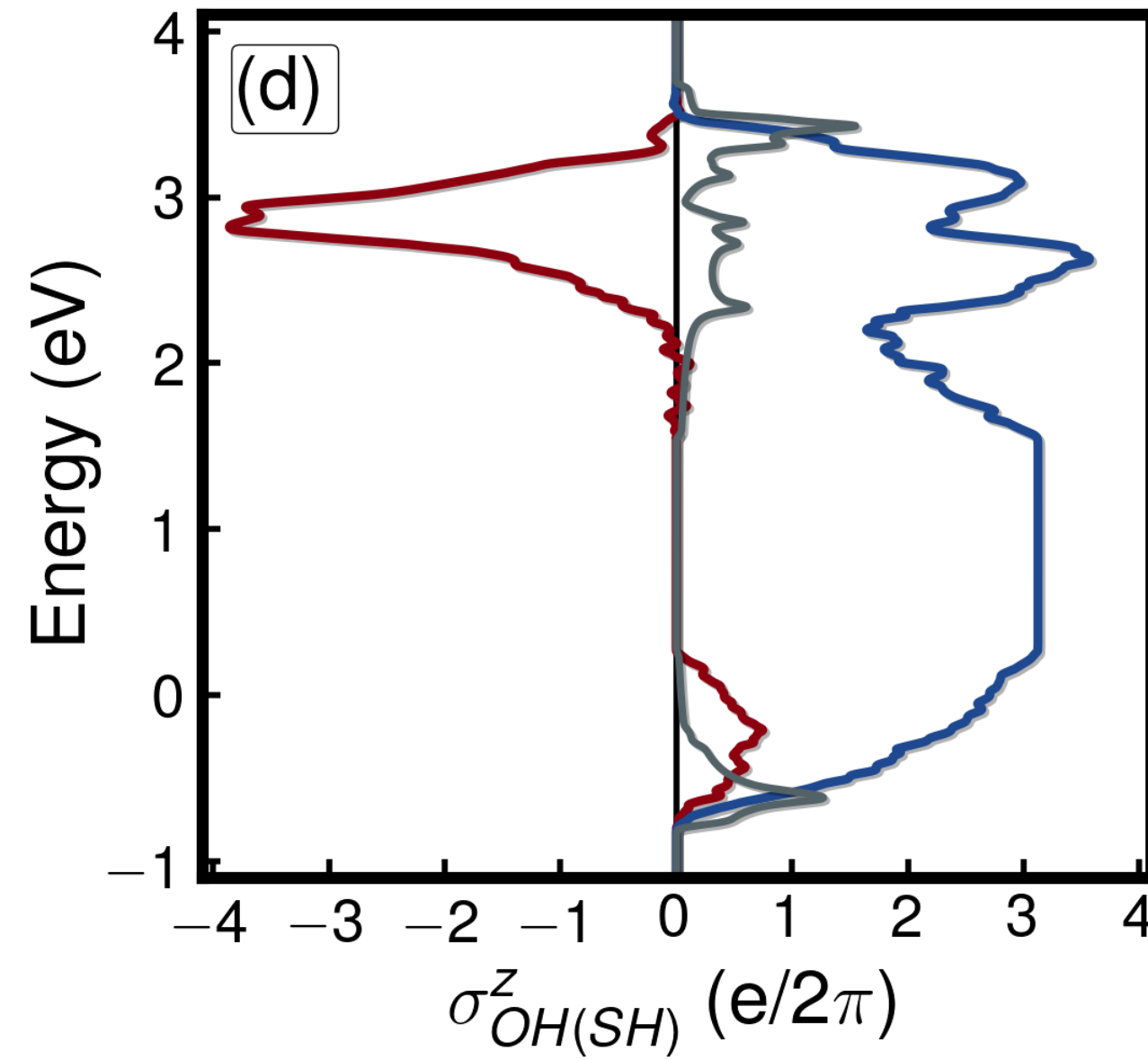
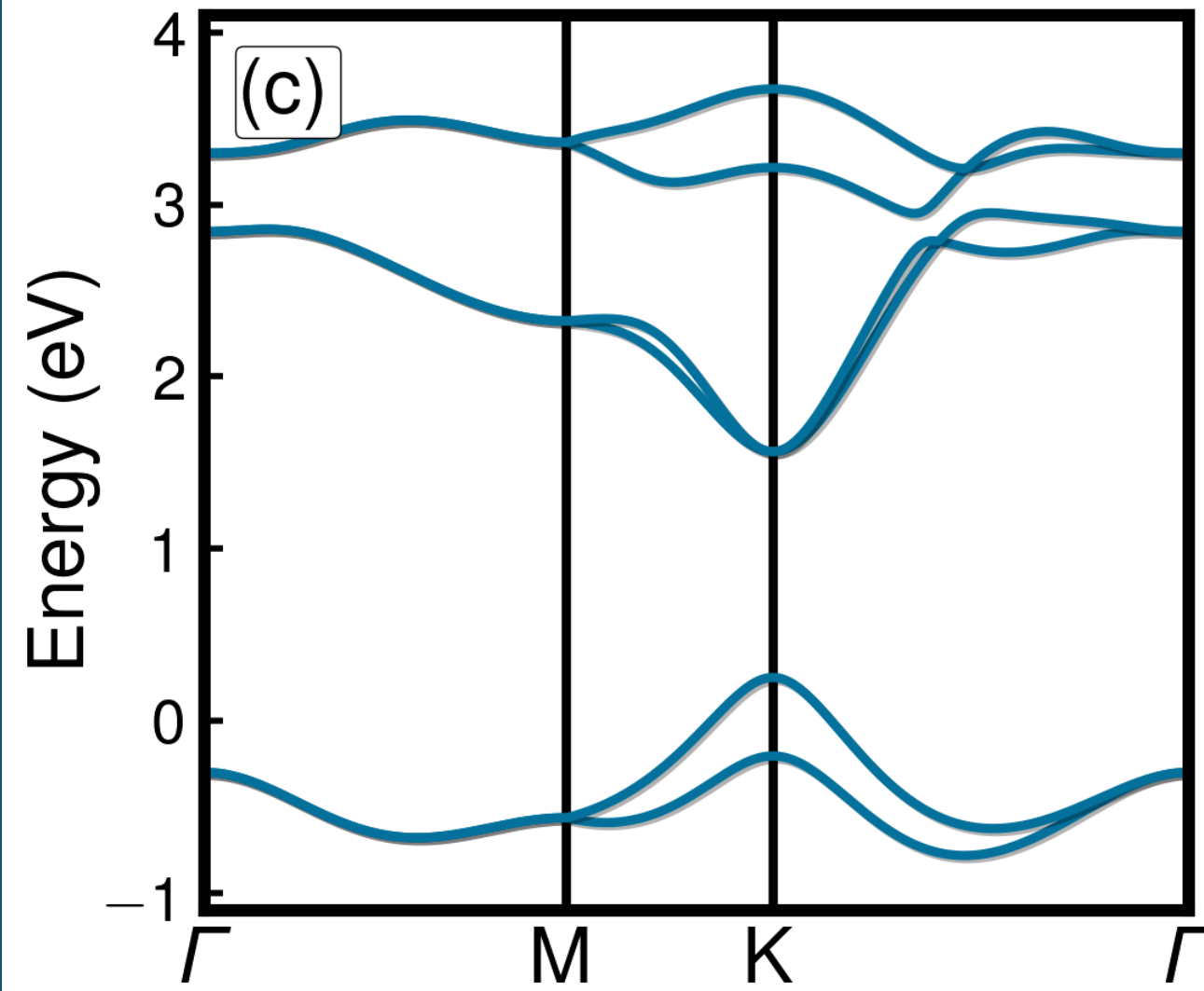


SOC





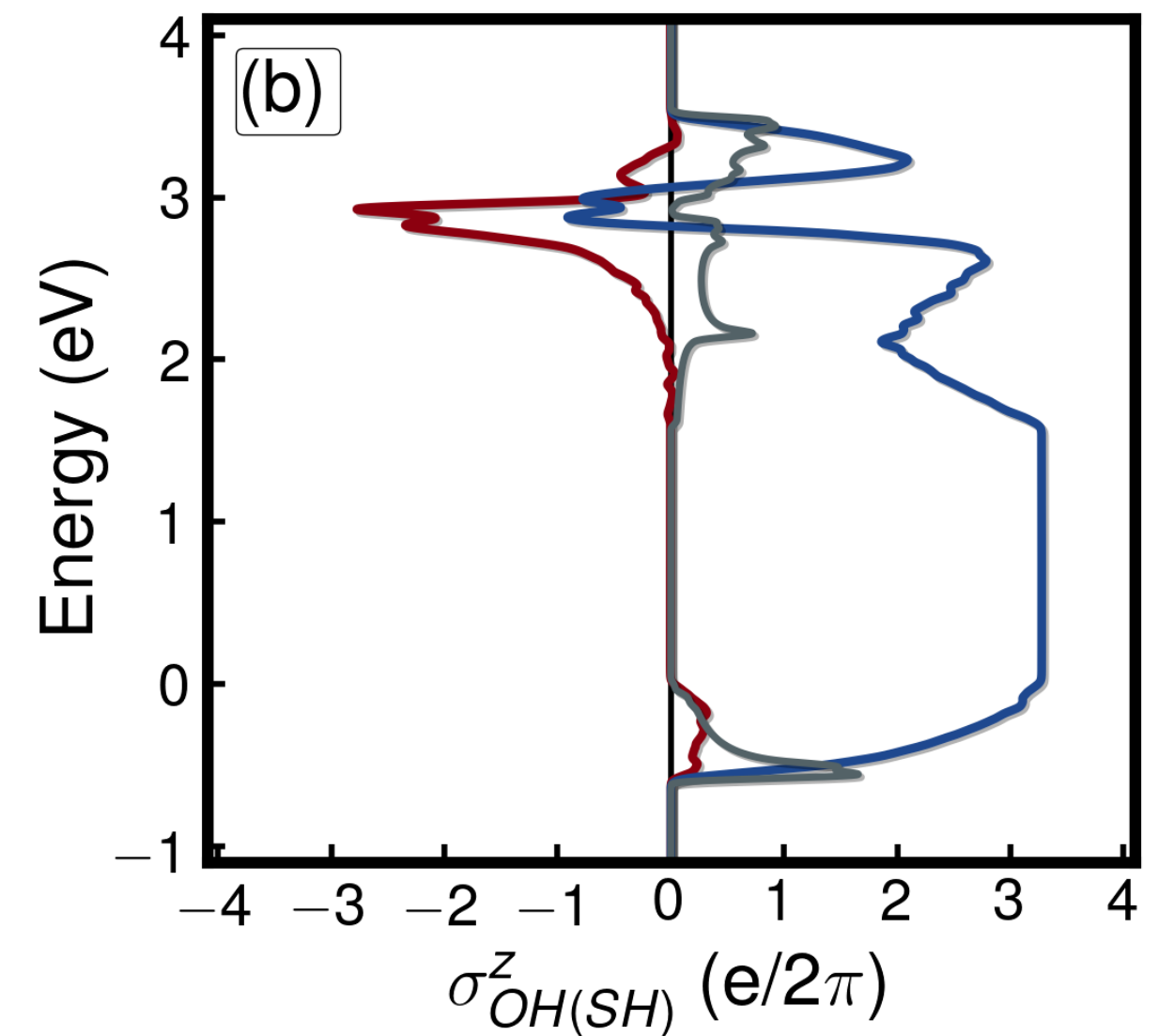
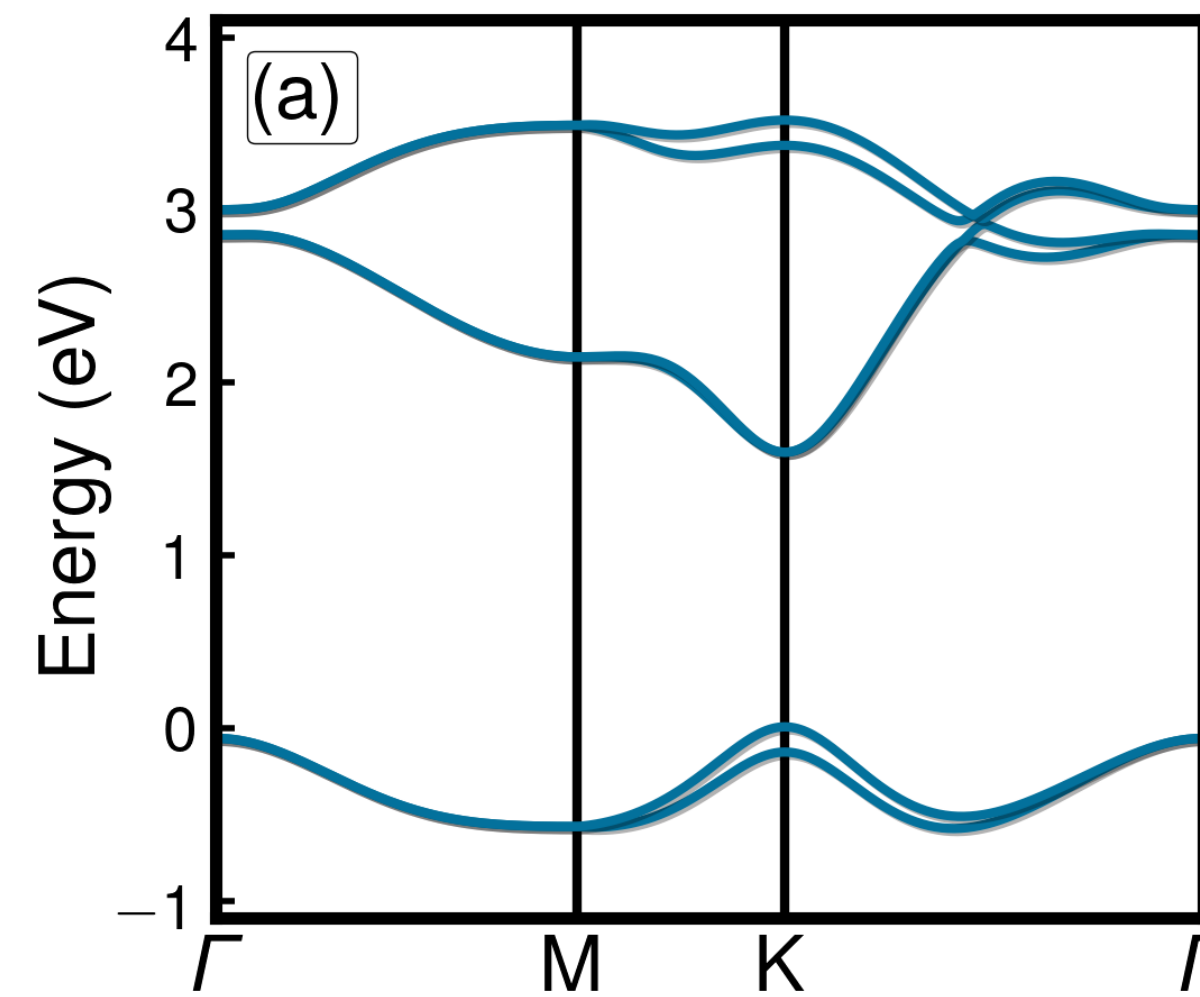
OHE IN TRANSITION METAL DICHALCOGENIDES(1H)



WSe₂

— DOS — OHC — SHC

MoS₂



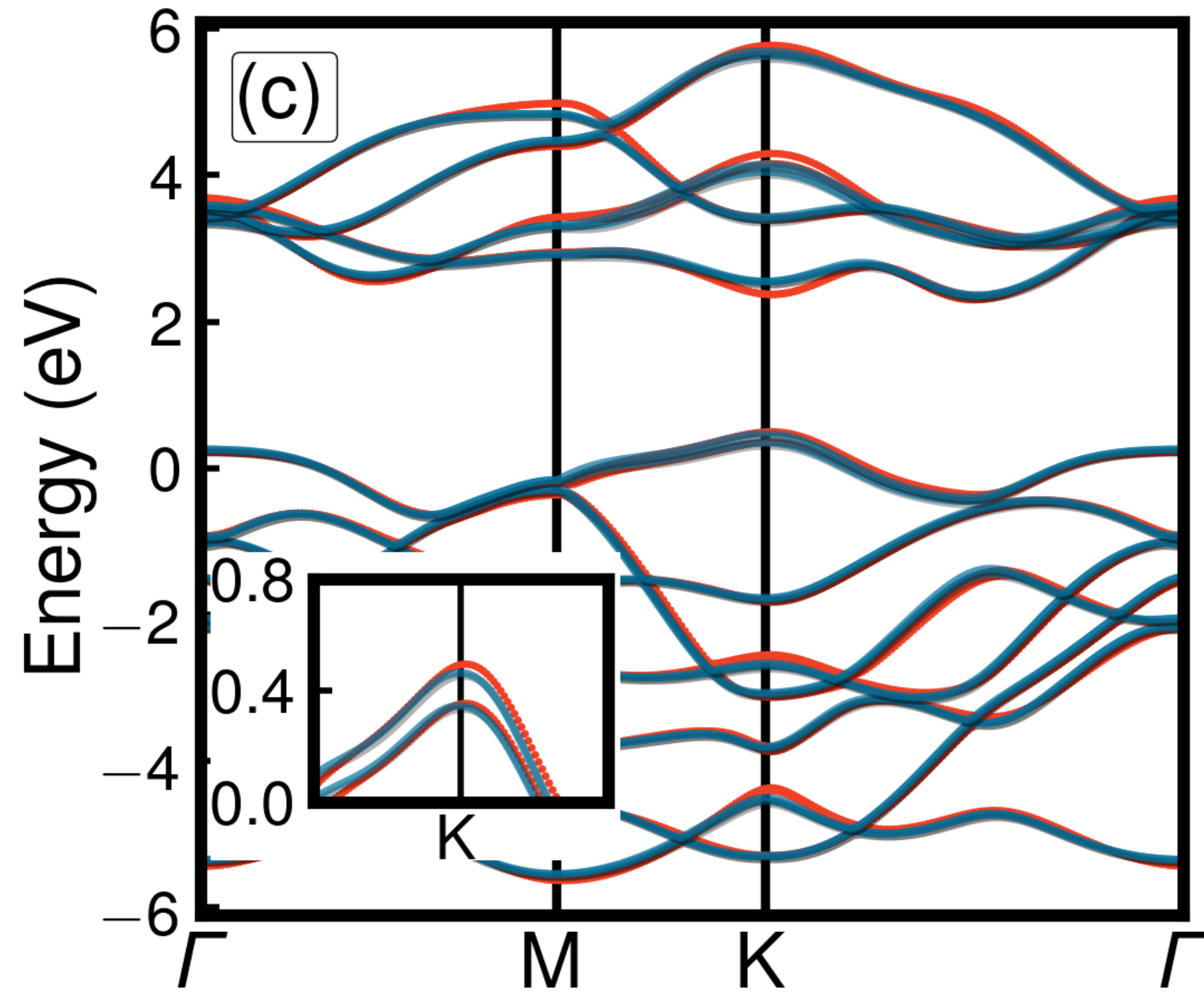
Chalcogen atoms

s , p_x , p_y and p_z

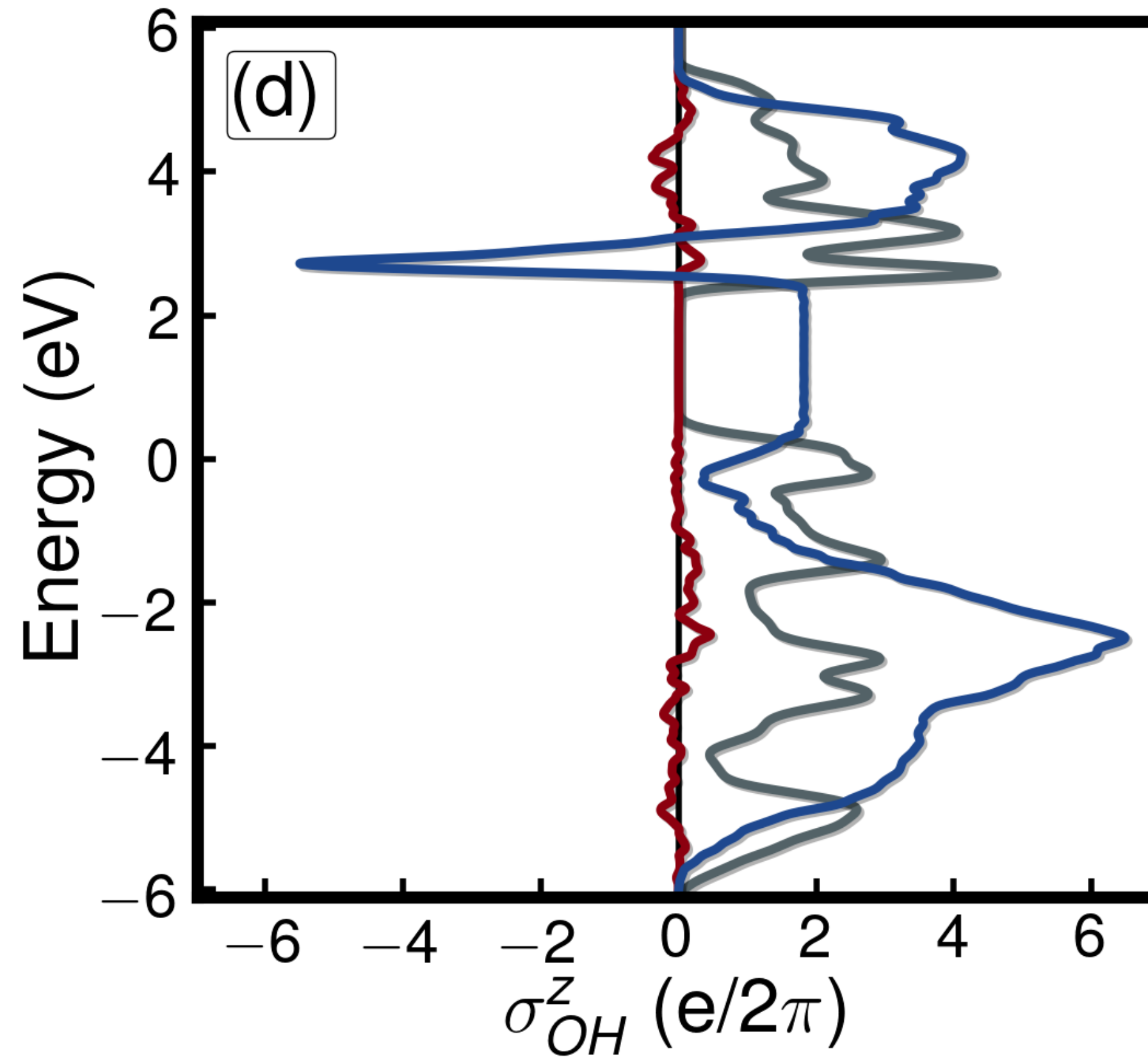
TM atoms

d_{xy} , d_{xz} , d_{yz} , $d_{x^2-y^2}$ and d_{z^2}

MoS₂



..... DFT ——— TB



— DOS — OHC — SHC

$L = 768 \times 768$
 $M = 768$
 $R = 10$

Wannier90

$t_{cutoff} = 0.0125 \times |t_{max}|$



CONCLUSIONS/ PERSPECTIVES

- Metallic multi-orbital 2D materials can host large OHE in the **absence** of SOC
- Trivial multi-orbital 2D insulators can host OHE
 - Non-quantized orbital Hall plateaus
- TMDs present sizeable orbital Hall plateaus
- OHE can be used for example, for orbital torque transfer
- OHE widens the pool of materials that can be used for spin-orbitronics.



**THANK YOU FOR
YOUR ATTENTION**