

NEW DEVELOPMENTS ON CHROMIUM TRIHALIDES 2D FERROMAGNETS

Dr. David Soriano
Radboud University of Nijmegen

2D van der Waals Spin Systems (4 – 7 August 2020)



- What we already know about CrX_3
- Coulomb interactions in CrI_3
- Magnetic polarons in bilayer CrI_3
- Take-home message

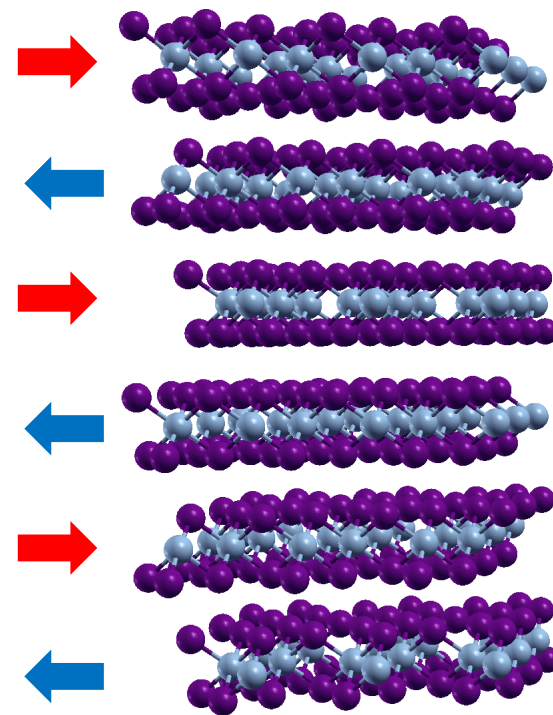
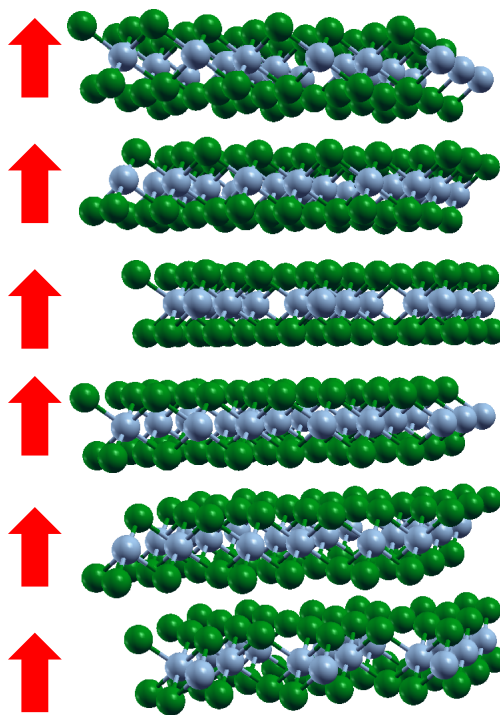
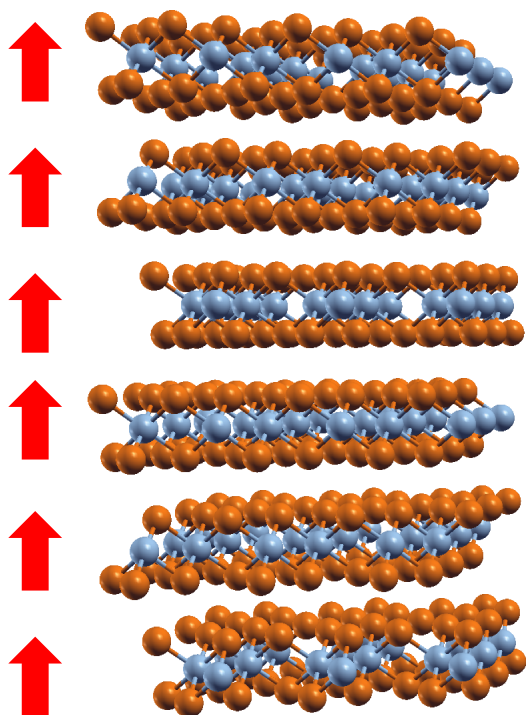
➤ Magnetism in Bulk

Physics. — “*Further experiments with liquid helium. Z. Magnetic researches. XXVIII. Magnetisation of anhydrous CrCl_3 , CoCl_2 and NiCl_2 at very low temperatures.*” By H. R. WOLTJER and H. KAMERLINGH ONNES.

(Communicated at the meeting of May 30, 1925).

§ 1. *Introduction.* In the preceding communication the magnetic anomalies shown by anhydrous CrCl_3 , CoCl_2 and NiCl_2 at the temperatures of liquid hydrogen have been pointed out. It seemed to be important to extend this research to the very low temperatures obtainable with liquid helium. The following questions came to the foreground: as regards CrCl_3 whether the initial susceptibility would increase with decreasing temperature as strongly as in the liquid hydrogen region and whether in strong fields saturation phenomena would appear; for the other substances whether the decrease of the susceptibility with decreasing temperature that seemed to be indicated by the measurements in liquid hydrogen would be continued.

➤ Magnetism in Bulk

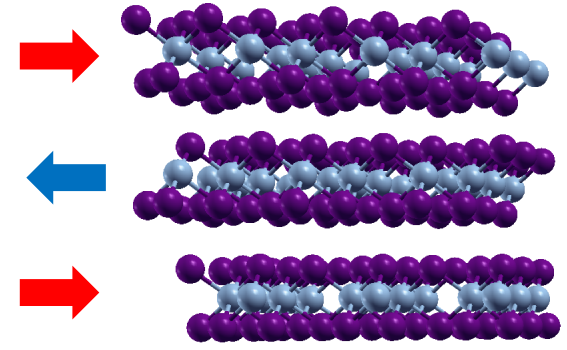
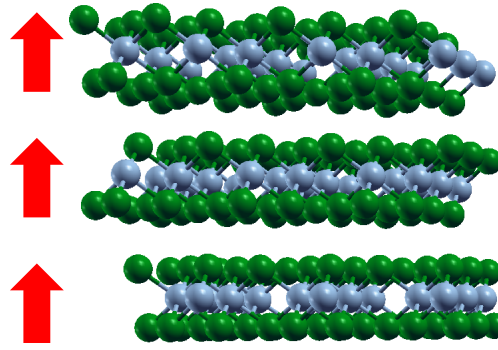
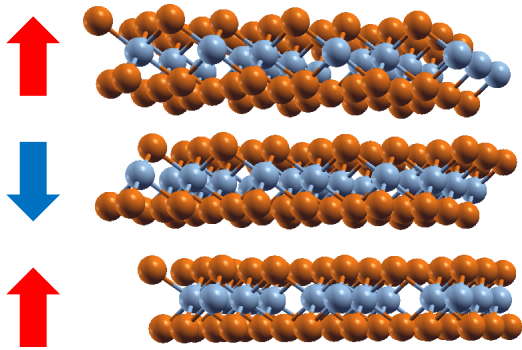


Dillon et al., *Journal of Applied Physics*, **36**, 1259 – 1260 (1965)

Tsubokawa, *Journal of the Physical Society of Japan*, **15**, 1664 – 1668 (1960)

Cable et al., *Journal of Physics and Chemistry of Solids*, **19**, 29 – 34 (1961)

➤ Magnetism in **thin samples**



Huang et al., *Nature*, **546**, 270 – 273 (2017)

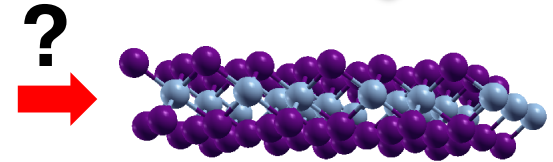
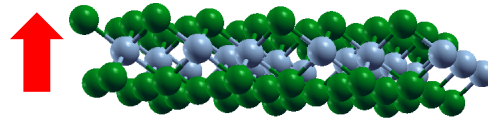
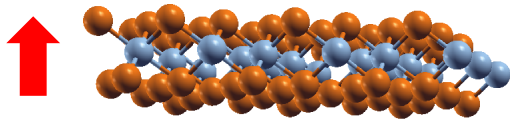
Klein, **DS**, et al., *Science*, **360**, 1218 – 1222 (2018)

Song et al., *Science*, **360**, 1214 – 1218 (2018)

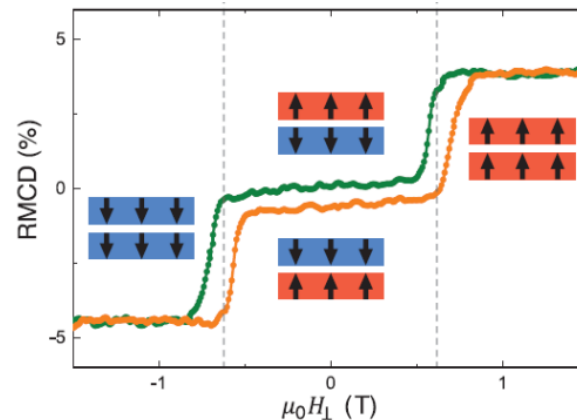
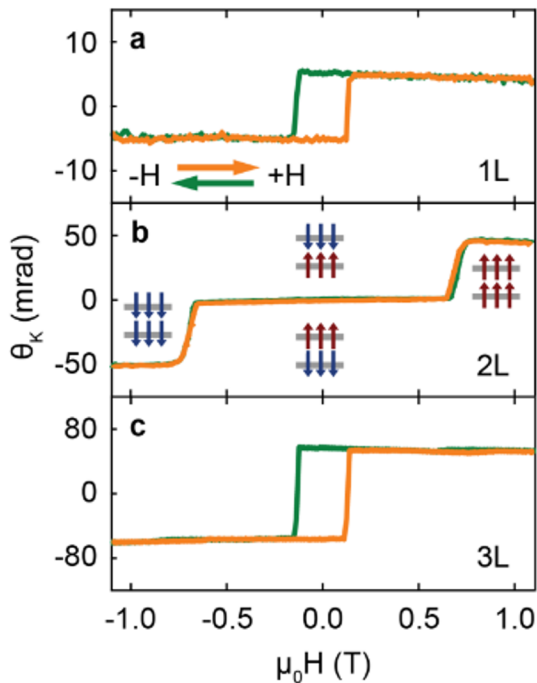
Klein et al., *Nature Physics*, **15**, 1255 – 1260 (2019)

Kim et al., *PNAS*, **116**, 11131 – 11136 (2019)

➤ Magnetism in monolayer



Bedoya-Pinto et al., *arXiv:2006.07605*
(Talk Thursday 9:00)



Huang et al., *Nature*, **546**, 270 – 273 (2017)

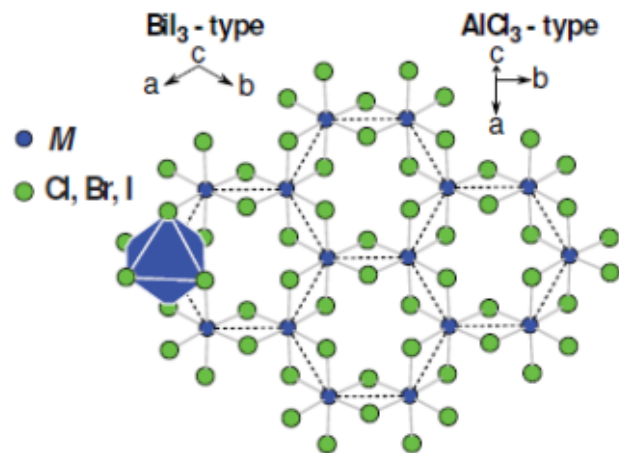
Klein, **DS**, et al., *Science*, **360**, 1218 – 1222 (2018)

Song et al., *Science*, **360**, 1214 – 1218 (2018)

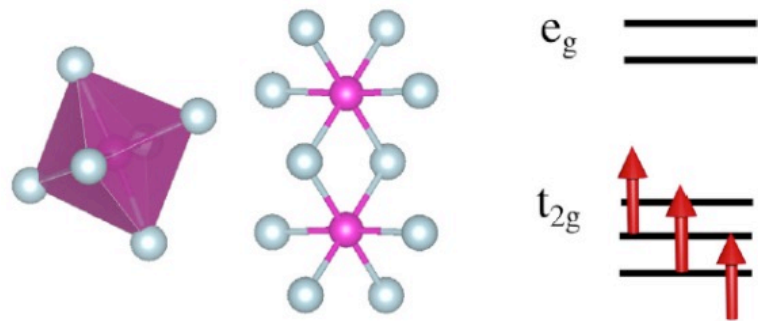
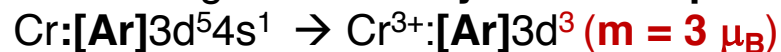
Klein et al., *Nature Physics*, **15**, 1255 – 1260 (2019)

Kim et al., *PNAS*, **116**, 11131 – 11136 (2019)

➤ Magnetism at the microscopic level: DFT



Octahedral ligand field: **Crystal field splitting**

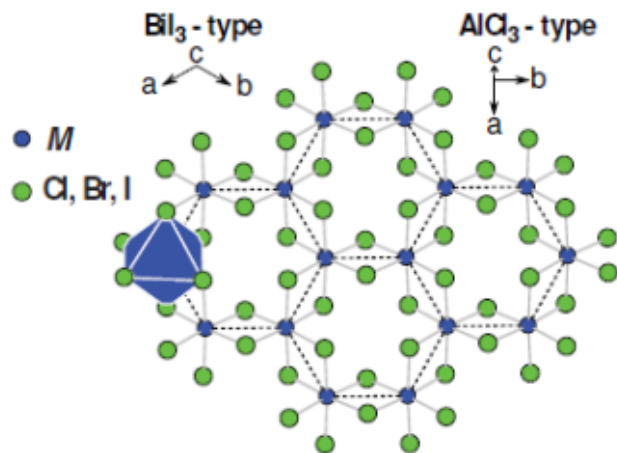


Lado and Fernández-Rossier, *2D Materials* **4** 035002 (2017)

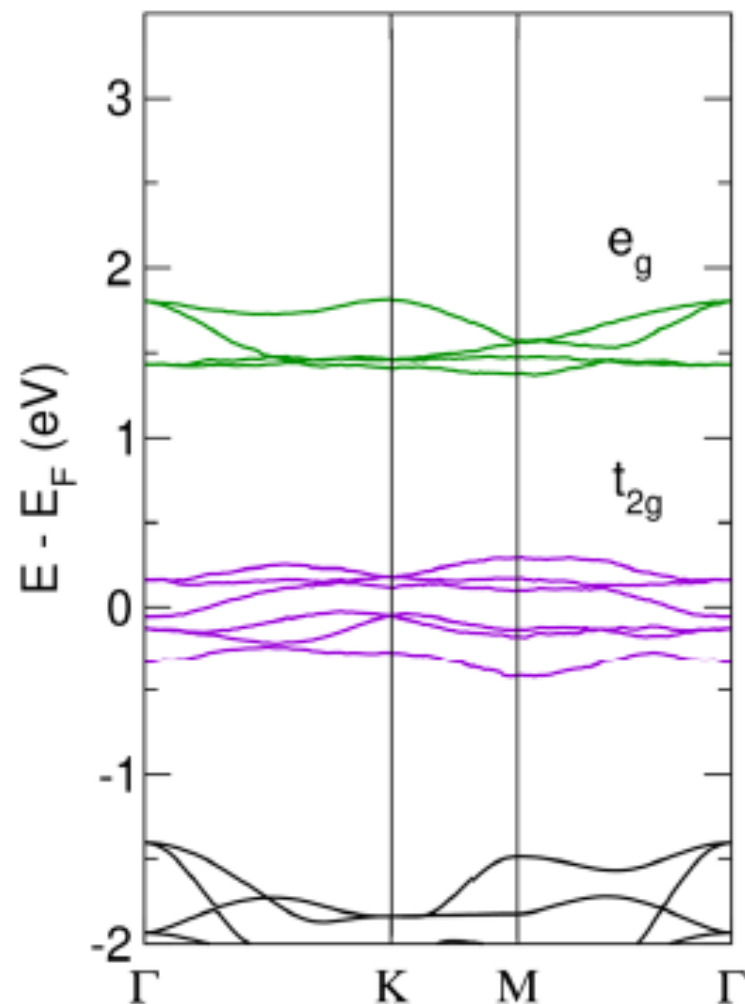
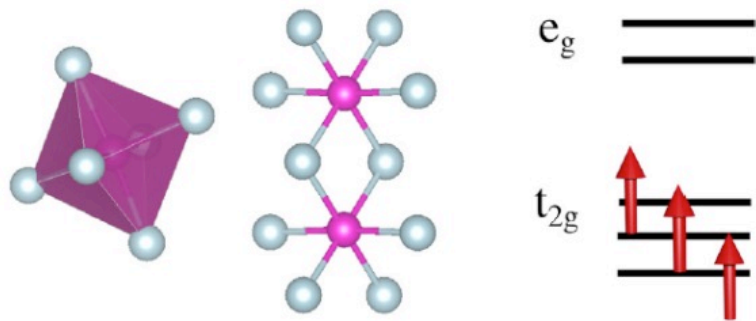
McGuire, *Crystals*, **7**, 121 (2017)

DS, Katsnelson and Fernández-Rossier, *Nano Letters* (Review) **10.1021/acs.nanolett.0c02381**

➤ Magnetism at the microscopic level: DFT



Octahedral ligand field: **Crystal field splitting**
 $\text{Cr}:[\text{Ar}]3d^54s^1 \rightarrow \text{Cr}^{3+}:[\text{Ar}]3d^3$ ($m = 3 \mu_B$)

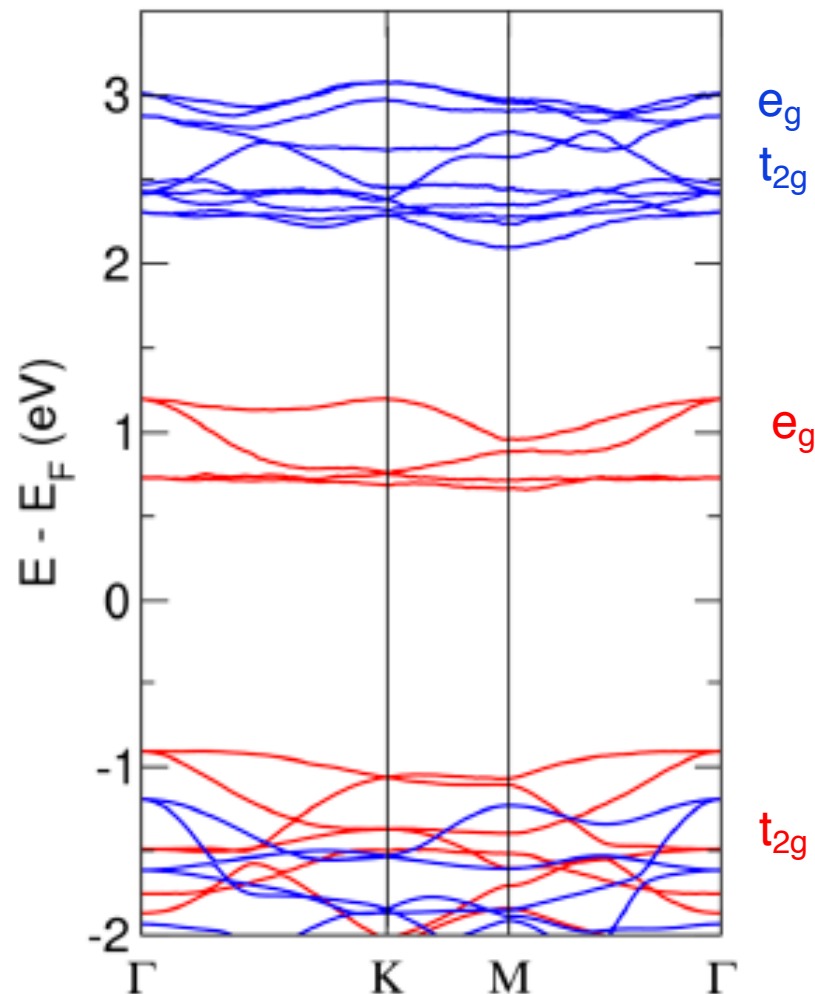
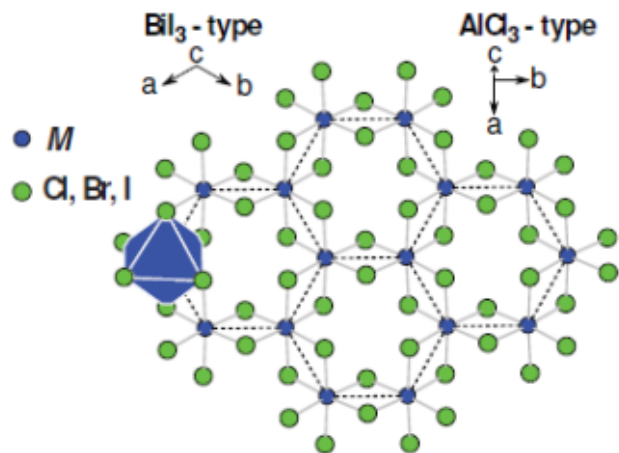


Lado and Fernández-Rossier, *2D Materials* **4** 035002 (2017)

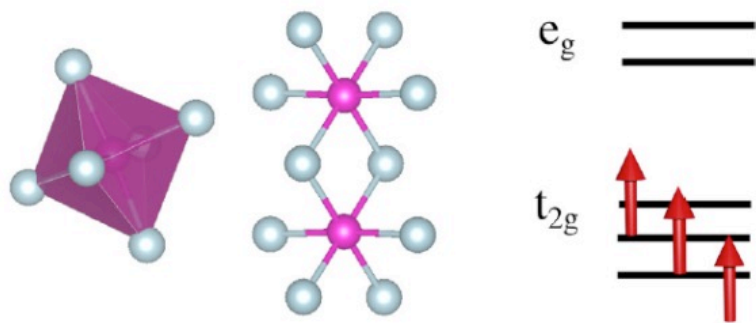
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DS, Katsnelson and Fernández-Rossier, *Nano Letters* (Review) [10.1021/acs.nanolett.0c02381](https://doi.org/10.1021/acs.nanolett.0c02381)

➤ Magnetism at the microscopic level: **DFT+U+J**



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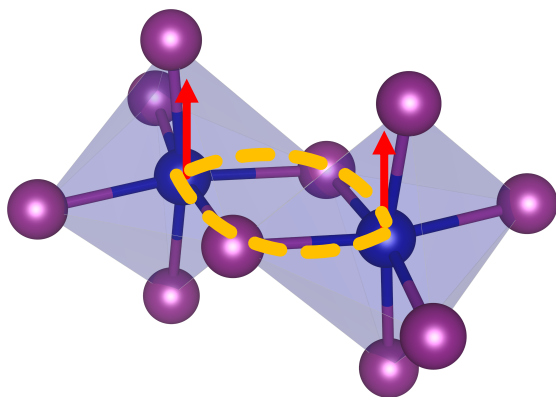
Lado and Fernández-Rossier, *2D Materials* **4** 035002 (2017)

McGuire, *Crystals*, **7**, 121 (2017)

DS, Katsnelson and Fernández-Rossier, *Nano Letters* (Review) [10.1021/acs.nanolett.0c02381](https://doi.org/10.1021/acs.nanolett.0c02381)

➤ Magnetism at the microscopic level: **Intralayer Exchange**

Superexchange (Goodenough-Kanamori)



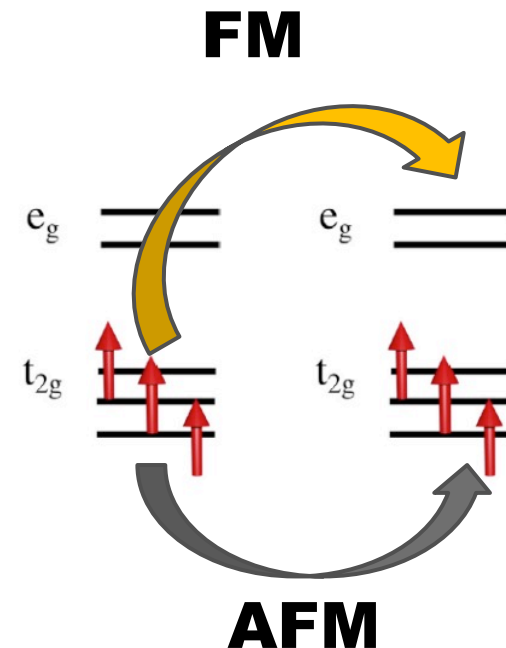
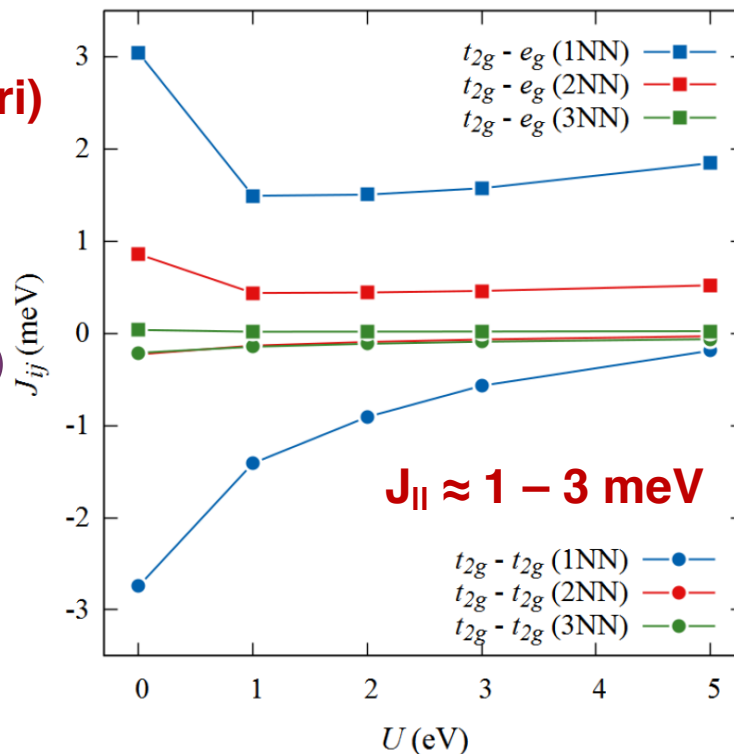
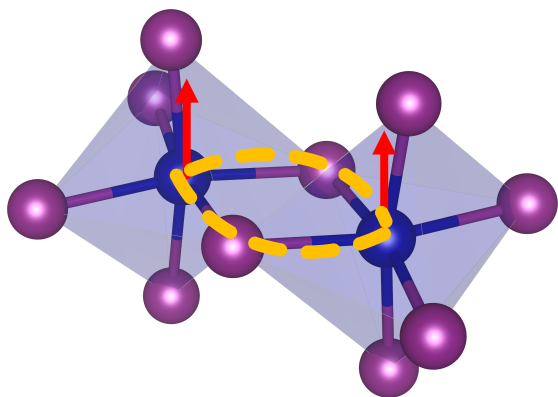
	$d_{\text{Cr-Cr}}(\text{\AA})$	$\alpha(\text{deg})$	$T_{\text{C/N}}(\text{K})$	Type of anisotropy
CrI ₃	4.026	97.5	45 ⁴ (68) ⁵³	Easy axis (z)
CrBr ₃	3.722	94.9	27 ⁵⁴ (37) ⁵⁵	Easy axis (z)
CrCl ₃ [†]	3.491	95.5	10* ⁴⁸ 17** ⁵⁶ (17) ⁵⁷	Easy plane (xy)

Kashin et al., *2D Materials*, **7**, 025036 (2020)

DS, Katsnelson and Fernández-Rossier, *Nano Letters* (Review) [10.1021/acs.nanolett.0c02381](https://doi.org/10.1021/acs.nanolett.0c02381)

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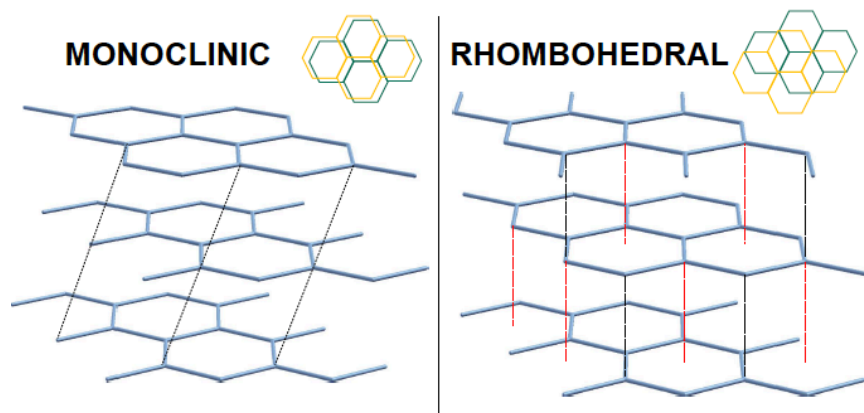
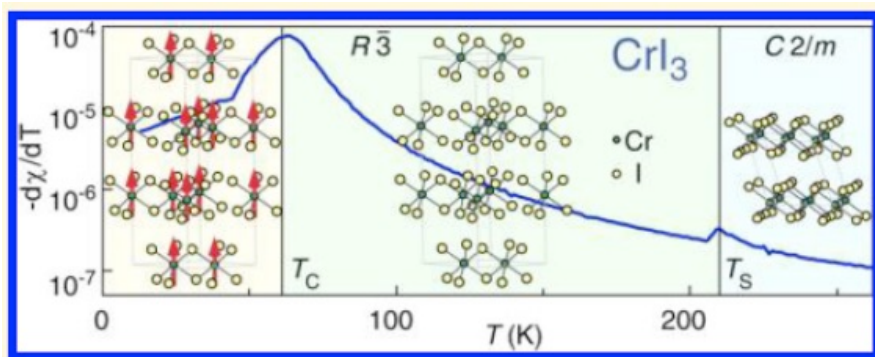
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CrI ₃	4.026	97.5	45^4 (68) ⁵³	Easy axis (z)
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Kashin et al., *2D Materials*, **7**, 025036 (2020)

DS, Katsnelson and Fernández-Rossier, *Nano Letters* (Review) [10.1021/acs.nanolett.0c02381](https://doi.org/10.1021/acs.nanolett.0c02381)

➤ Magnetism at the microscopic level: Interlayer Exchange

$T_S = 210 \text{ K (CrI}_3\text{); 420 K (CrBr}_3\text{); 240 K (CrCl}_3\text{)}$



McGuire et al., *Chem. Mater.*, **27**, 612 – 620 (2015)

Sivadas et al., *Nano Letters*, **18**, 7658 – 7664 (2018)

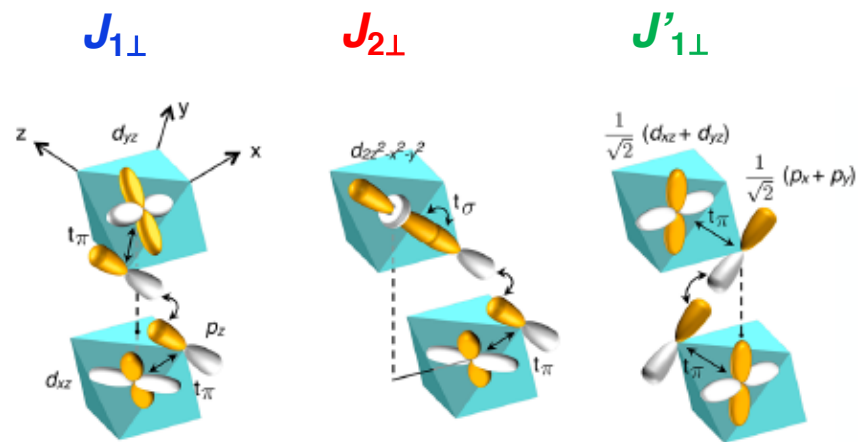
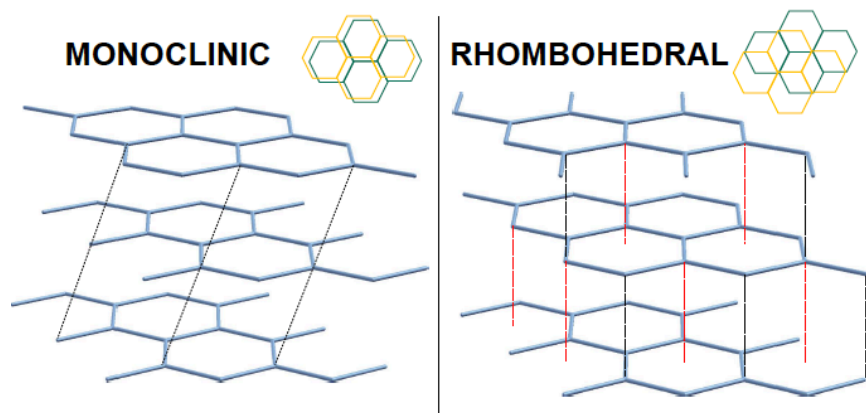
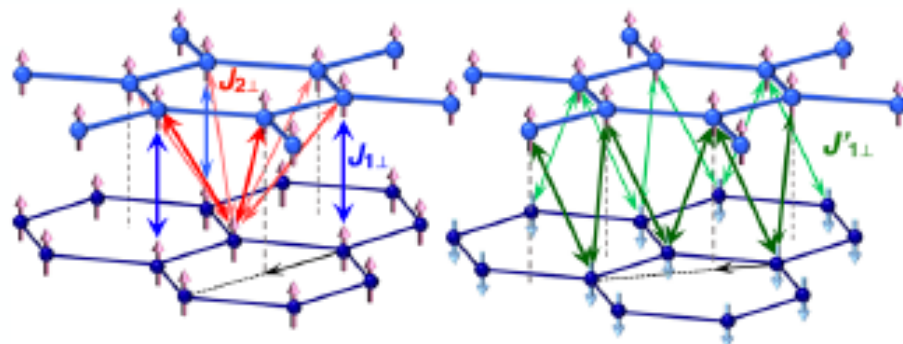
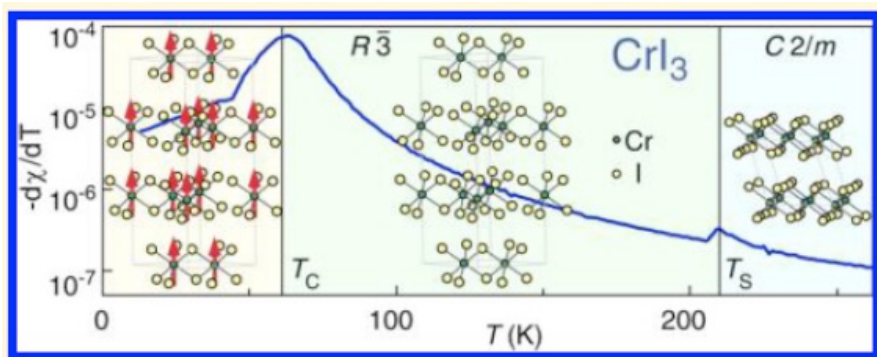
DS, Cardoso and Fernández-Rossier, *Sol. Stat. Comm.*, **299**, 113662 (2019)

DS, Katsnelson and Fernández-Rossier, *Nano Letters* (Review) **10.1021/acs.nanolett.0c02381**

➤ Magnetism at the microscopic level: Interlayer Exchange

$T_S = 210 \text{ K (CrI}_3\text{); 420 K (CrBr}_3\text{); 240 K (CrCl}_3\text{)}$

Super-superexchange



$J_{\perp} \approx 0.04 \text{ meV}$

McGuire et al., *Chem. Mater.*, **27**, 612 – 620 (2015)

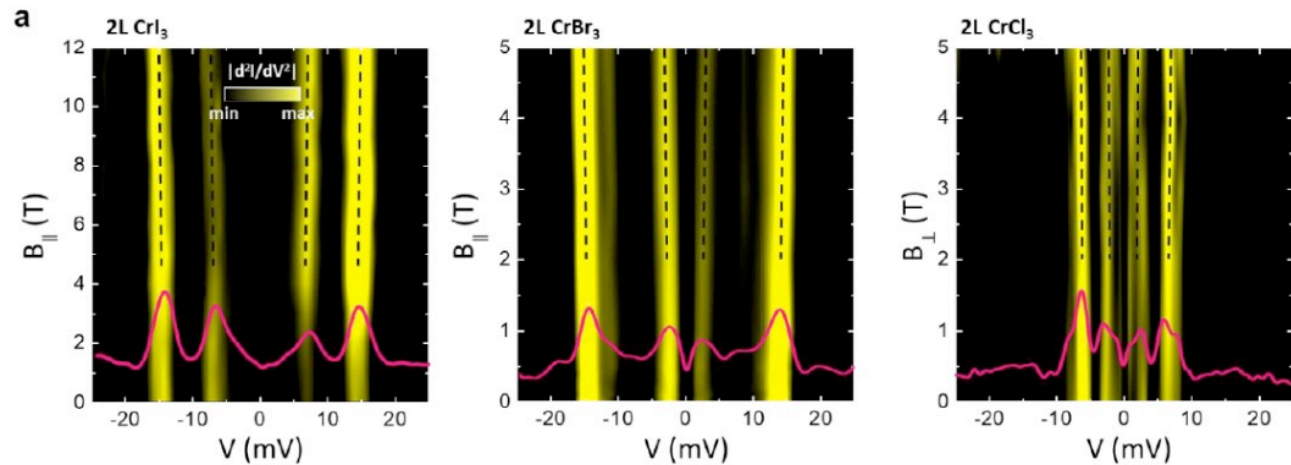
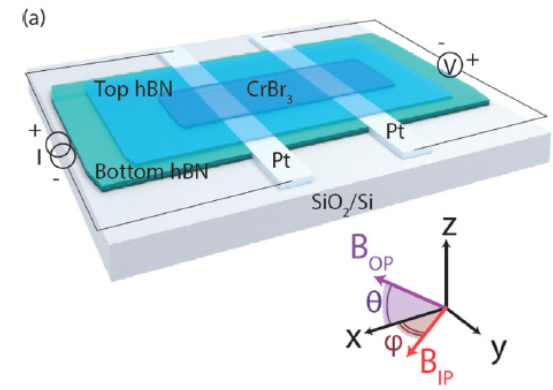
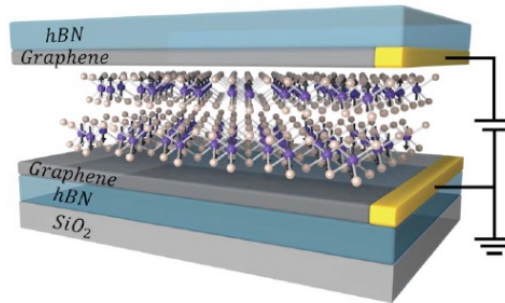
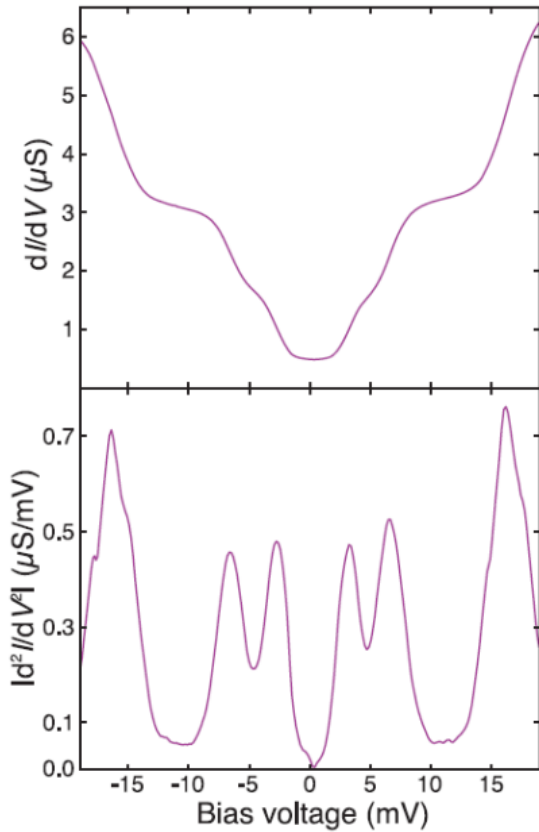
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DS, Katsnelson and Fernández-Rossier, *Nano Letters* (Review) [10.1021/acs.nanolett.0c02381](https://doi.org/10.1021/acs.nanolett.0c02381)

➤ Magnetism at the microscopic level: Spin-Waves

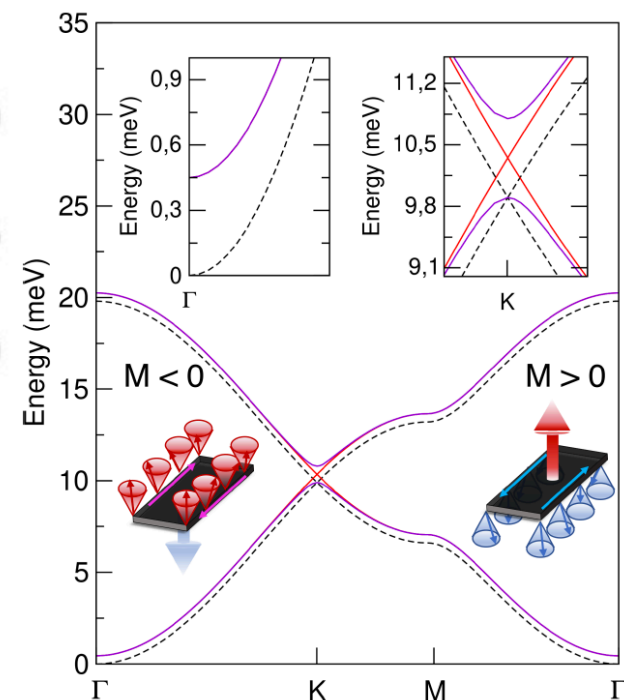
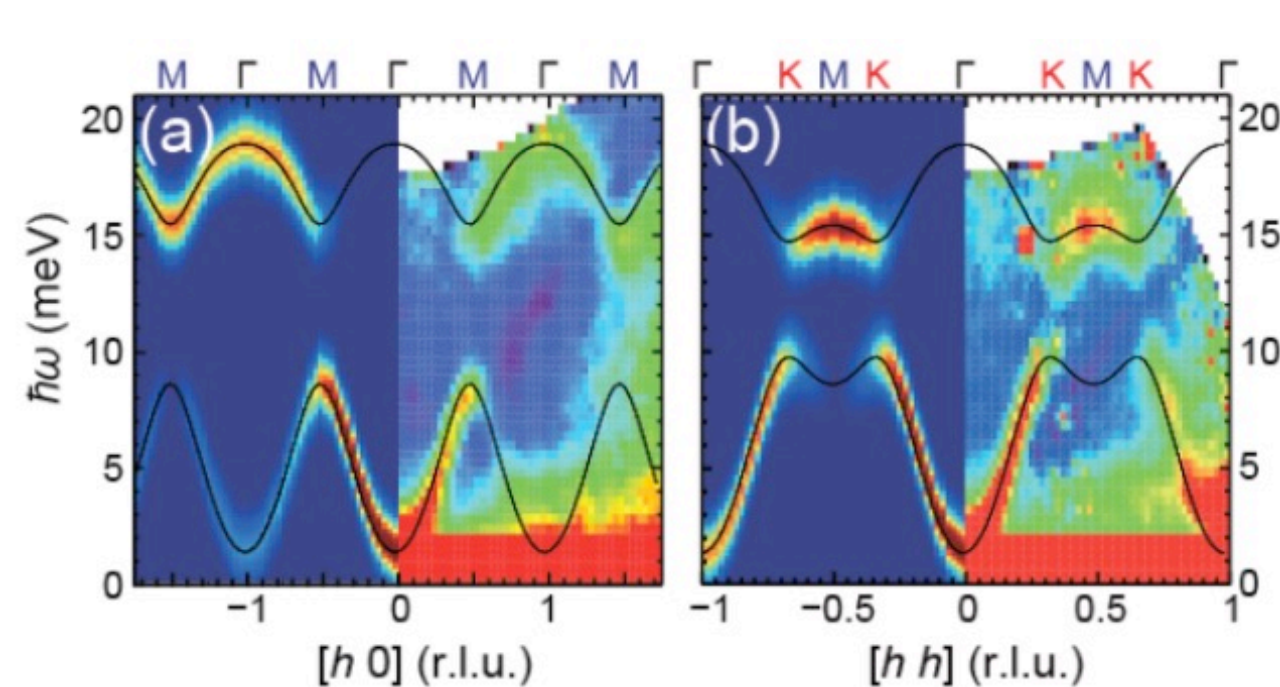
Inelastic Electron Tunneling Spectroscopy (IETS)



Klein, DS, *et al.*, *Science*, **360**, 1218 – 1222 (2018)
 Kim et al., *PNAS*, **116**, 11131 – 11136 (2019)
 Liu et al., *Phys. Rev. B*, **101**, 205407 (2020)

➤ Magnetism at the microscopic level: Spin-Waves

Inelastic Neutron Scattering (INS)



$$\Delta_{\Gamma} = 2AS + 3SJ_z$$

$$\Delta_K \propto K \text{ or } D'$$

A: Single-ion Anisotropy
J_z: Anisotropic Exchange
K: Kitaev interaction
D': 2nd Neighbor DMI

Chen et al., *Phys. Rev. X*, **8**, 041028 (2018)

DS, Katsnelson and Fernández-Rossier, *Nano Letters* (Review) [10.1021/acs.nanolett.0c02381](https://doi.org/10.1021/acs.nanolett.0c02381)

➤ Magnetism at the microscopic level: Anisotropy

	B_{\parallel}^c (T)	B_{\perp}^c (T)	MAE (meV)	J_z (meV)	J_1 (meV)	J_2 (meV)	J_3 (meV)	$K D^1$ (meV)	A (meV)
CrI ₃	6.5 ^{H31,54} [FL] 3.8 ^{H12} [BL]	2.0 ^{E54} [FL]	0.65 ^{T43} [ML] 0.68 ^{T45} [ML]	2.38 ^{E54} [FL]	2.29 ^{E54} [FL]	0.16 ^{E34} [Bulk] 0.56 ^{T64} [ML] 0.4 ^{T46} [ML] 0.63 ^{T45} [ML]	-0.1 ^{E34} [Bulk] 0.001 ^{T64} [ML] -0.15 ^{T45} [ML]	5.2 ^{E35} [Bulk]	0.22 ^{E34} [FL]
		1.8 ^{E12,29} [FL]		0.27 ^{E35} [Bulk]	2.01 ^{E34} [Bulk]			0.08 ^{T66} [ML]	
		0.6 ^{E12} [BL]		0.022 ^{T64} [ML]	0.20 ^{E35} [Bulk]			0.85 ^{T68} [ML]	
		0.85 ^{E29} [BL]		0.09 ^{T43} [ML]	3.24 ^{T64} [ML]			0.3 ^{E34} [Bulk]	
					2.2 ^{T43} [ML]				
					1.44 ^{T67} [ML]				
CrBr ₃	0.4 ^{E54} [FL]	<0.01 ^{E54} [FL]	0.18 ^{T45} [ML]	1.58 ^{E54} [FL]	1.56 ^{E54} [FL]	0.38 ^{T45} [ML]	-0.15 ^{T45} [ML]		
				2.6 ^{T45} [ML]	2.86 ^{T45} [ML]				
CrCl ₃	2.0 ^{E54} [FL]	2.4 ^{E54} [FL]	0.03 ^{T45} [ML]	0.91 ^{E54} [FL]	0.92 ^{E54} [FL]	0.23 ^{T45} [ML]	-0.13 ^{T45} [ML]		
		0.85 ^{E49} [BL]		1.92 ^{T45} [ML]	1.6 ^{E49} [FL]				

Still an open issue!

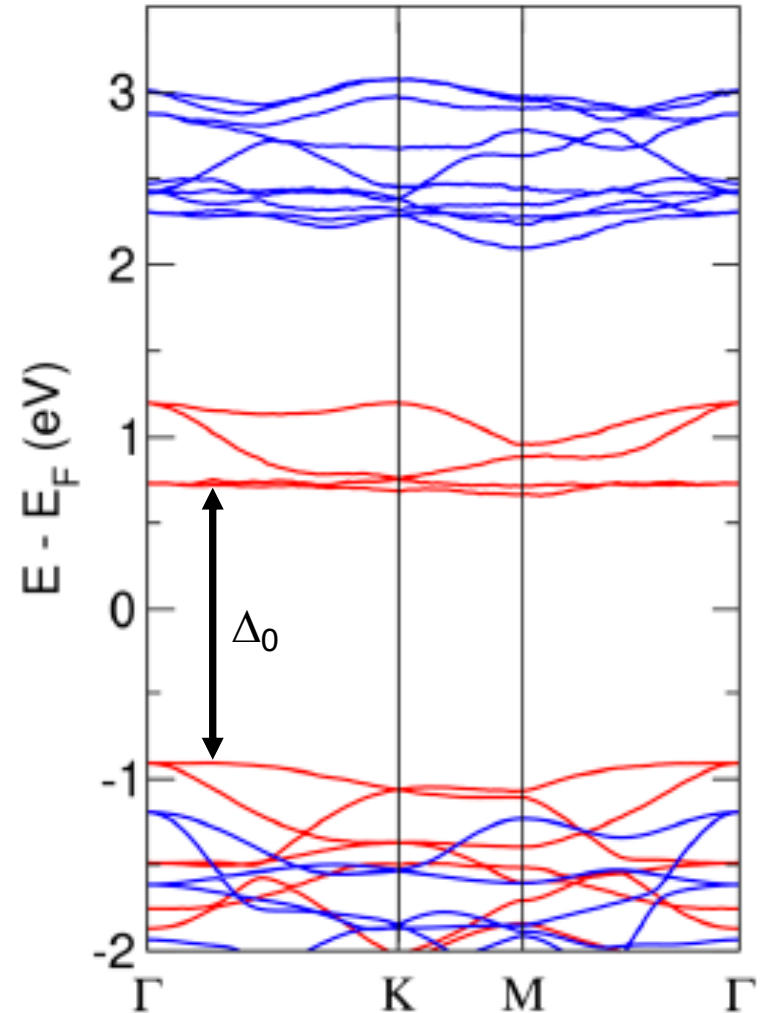
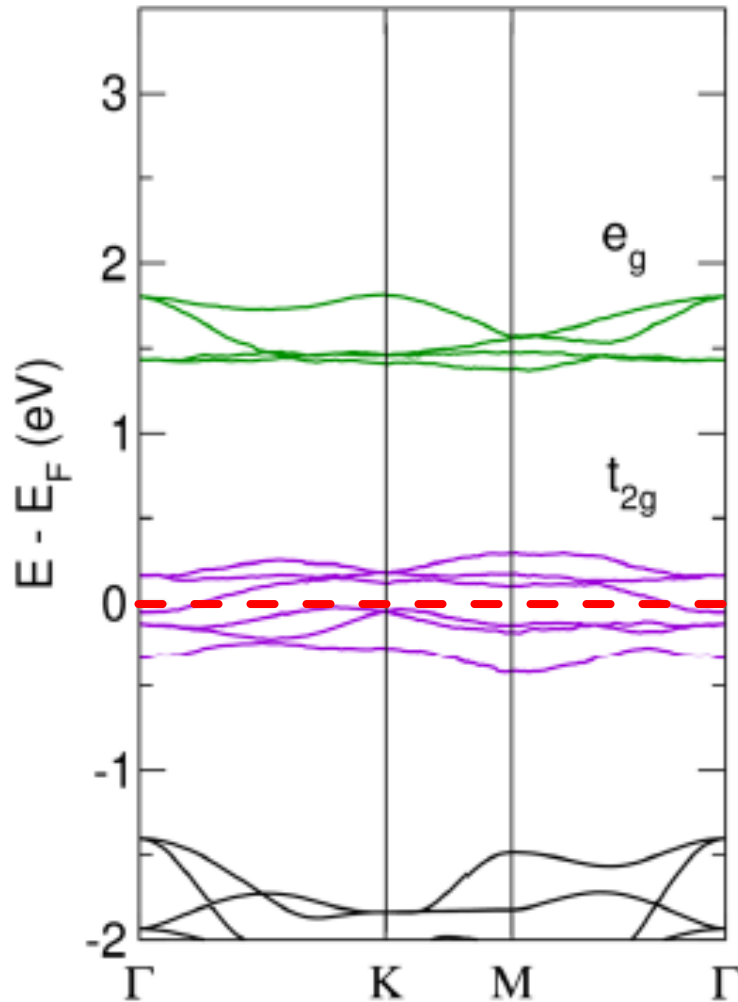
See recent preprint by Ke and Katsnelson (arXiv:2007.14518)

(Poster by Liqin Ke)

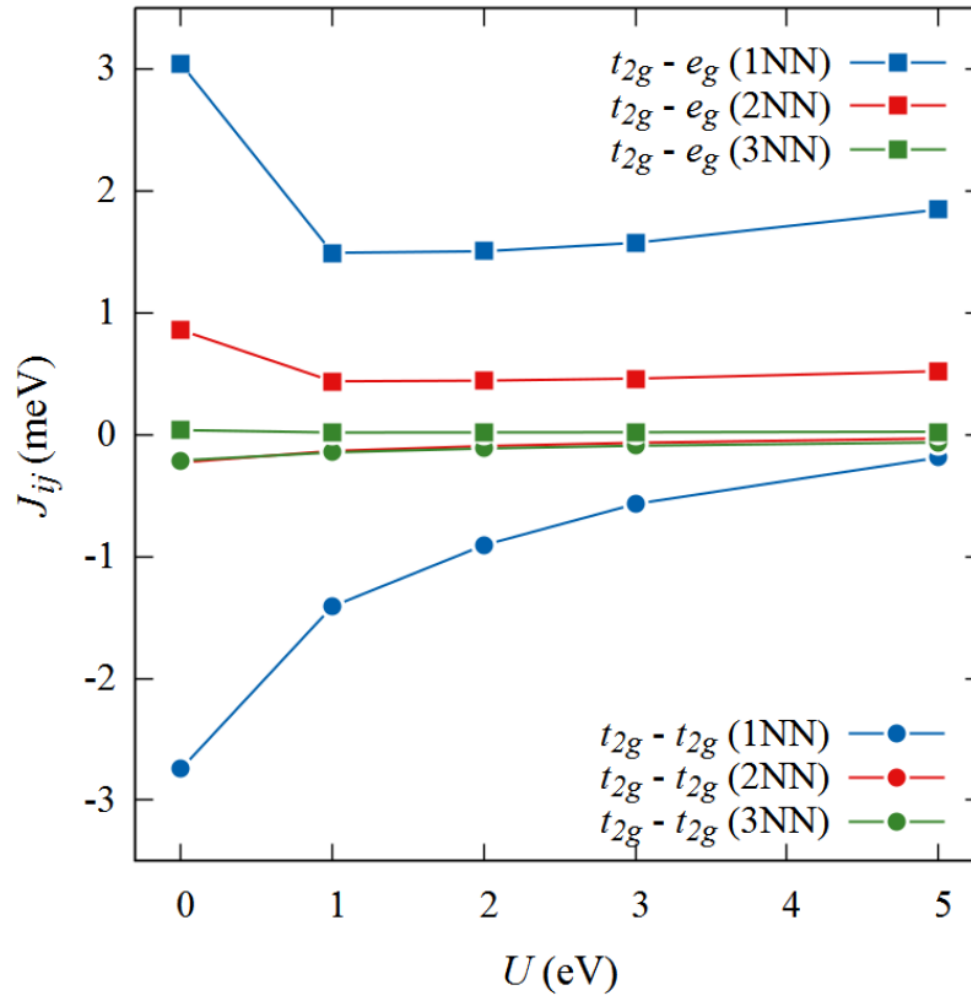
Coulomb Interactions in CrI_3

➤ Strongly correlated materials: **LSDA+U+J**

$U = 3 \text{ eV}; J = 0.5 \text{ eV}$

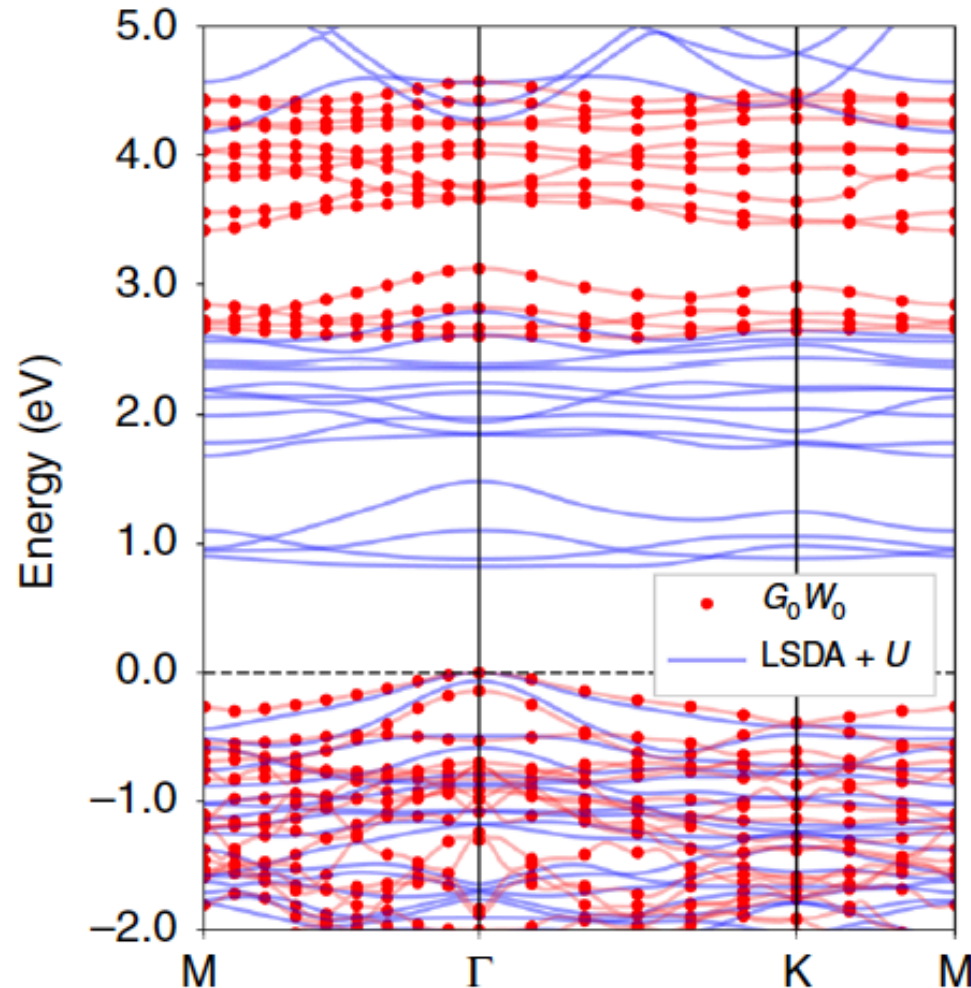


➤ Strongly correlated materials: $J(U)$ dependence



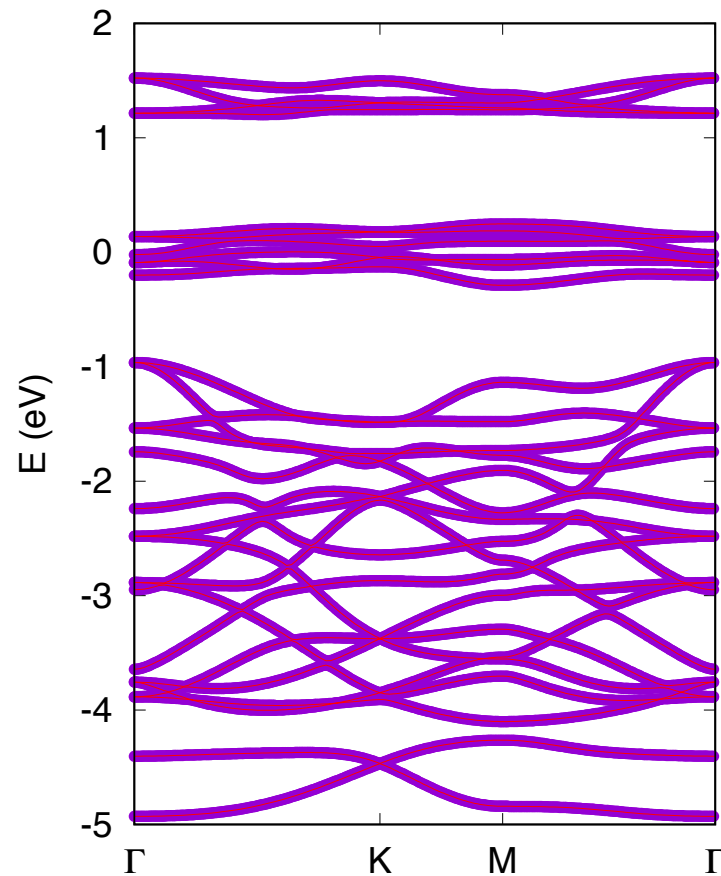
➤ Strongly correlated materials: **GW**

Coulomb and dielectric screening effects are very important



➤ Wannier-Hartree-Fock Approach

Step 1. Calculate the spin-unpolarized Wannier Hamiltonian (H^W) from first-principles (LDA) projected on Cr d -orbitals and I p -orbital



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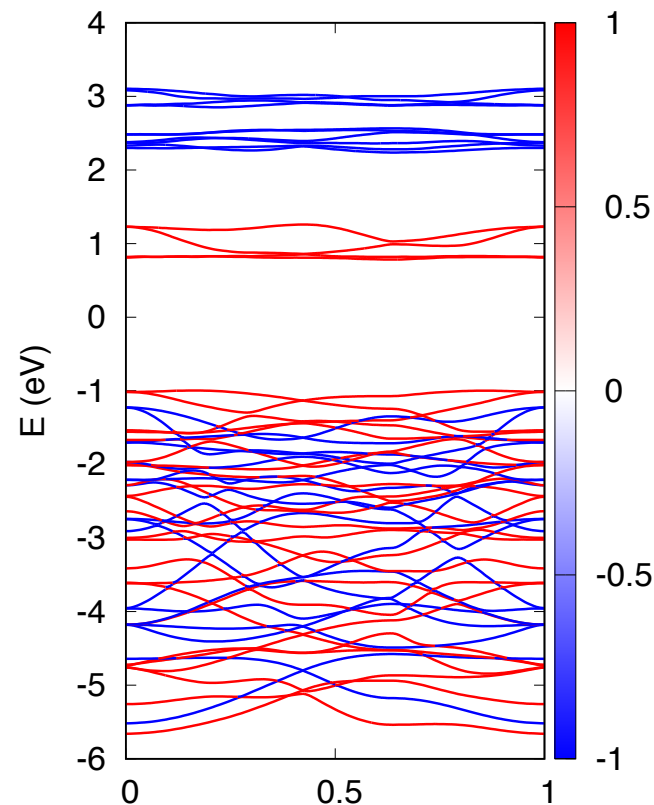
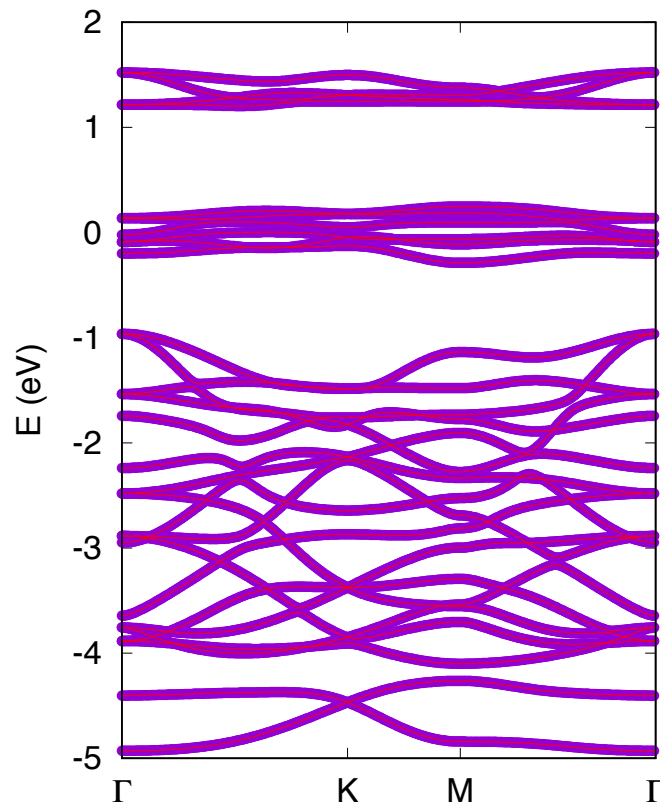
Step 2. Introduce Coulomb interactions using Hartree-Fock (H^{HF}) in the mean-field approximation, and calculate the electronic structure self-consistently

$$\begin{aligned} H^{HF} = & U \sum_m \hat{n}_{m\uparrow} \hat{n}_{m\downarrow} + U' \sum_{m \neq m'} \hat{n}_{m\uparrow} \hat{n}_{m'\downarrow} + \\ & + (U' - J) \sum_{m < m', \sigma} \hat{n}_{m\sigma} \hat{n}_{m'\sigma} + \\ & - J \sum_{m \neq m'} d_{m\uparrow}^\dagger d_{m\downarrow} d_{m'\downarrow}^\dagger d_{m'\uparrow} \end{aligned}$$

➤ Wannier-Hartree-Fock Approach

Step 1. Calculate the spin-unpolarized Wannier Hamiltonian (H^W) from first-principles (LDA) projected on Cr d -orbitals and I p -orbital

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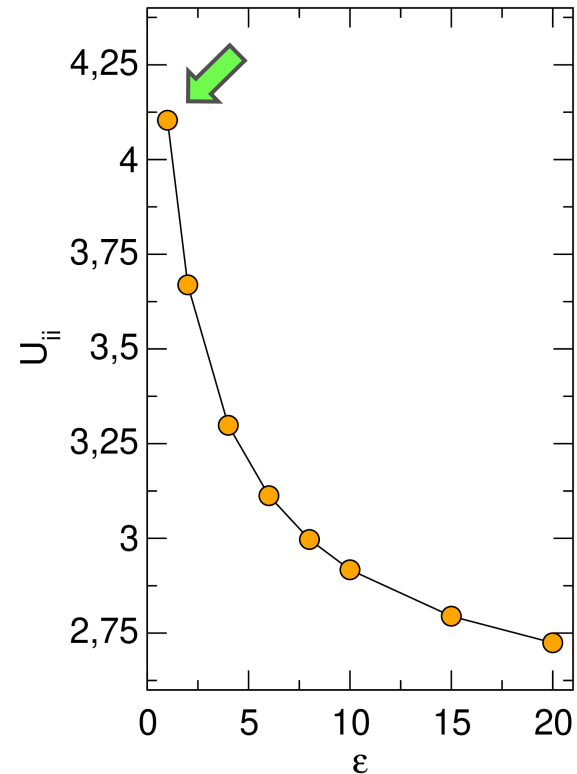
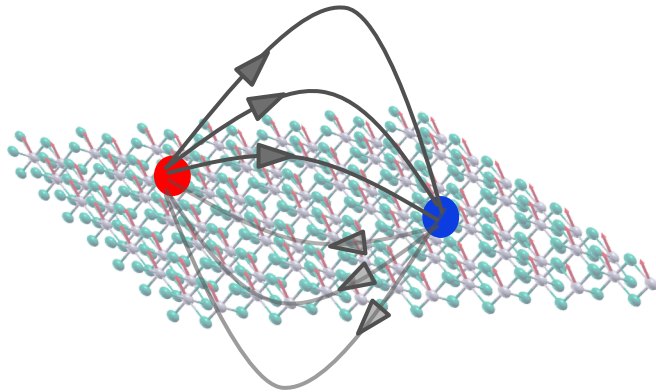
$$\begin{aligned} H^{HF} = & U \sum_m \hat{n}_{m\uparrow} \hat{n}_{m\downarrow} + U' \sum_{m \neq m'} \hat{n}_{m\uparrow} \hat{n}_{m'\downarrow} + \\ & + (U' - J) \sum_{m < m', \sigma} \hat{n}_{m\sigma} \hat{n}_{m'\sigma} + \\ & - J \sum_{m \neq m'} d_{m\uparrow}^\dagger d_{m\downarrow} d_{m'\downarrow}^\dagger d_{m'\uparrow} \end{aligned}$$

Step 3. The orbital-dependent exchange interactions are calculated by means of the magnetic force theorem using the converged total Hamiltonian ($H = H^W + H^{HF}$)

$$J_{kl}^{\alpha\beta} = \frac{1}{4\pi} \int_{-\infty}^{E_F} d\epsilon \text{Im} \left[\Delta_{\alpha\beta} G_{kl}^{\beta\alpha\downarrow}(\epsilon) \Delta_{\beta\alpha} G_{kl}^{\alpha\beta\uparrow}(\epsilon) \right]$$

➤ Wannier-Hartree-Fock Approach: Substrate dielectric screening effects

Van der Waals heterostructure: $\text{hBN/CrI}_3/\text{hBN}$



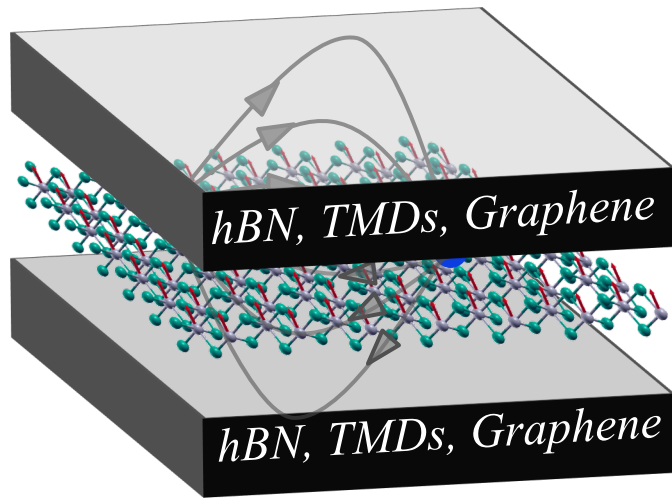
Rösner *et al.*, *Phys. Rev. B*, **92**, 085102 (2015)

Rösner *et al.*, *Nano Letters*, **16**, 2322 – 2327 (2016)

Florian *et al.*, *Nano Letters*, **18**, 2725 – 2732 (2018)

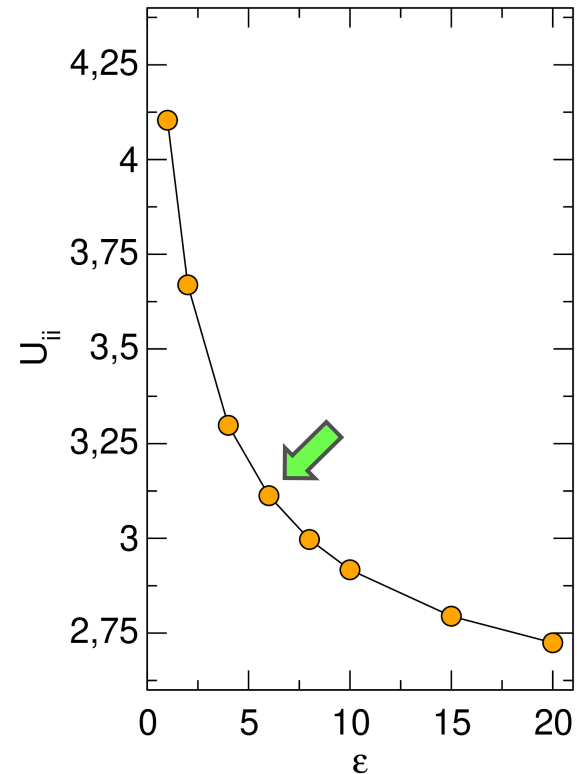
➤ Wannier-Hartree-Fock Approach: Substrate dielectric screening effects

Van der Waals heterostructure: $\text{hBN}/\text{CrI}_3/\text{hBN}$



Dielectric environment

$$U_{ij}^{cRPA} = \varepsilon^{-1} v_{ij}$$



□ Impact on the quasi-particle/excitonic gap

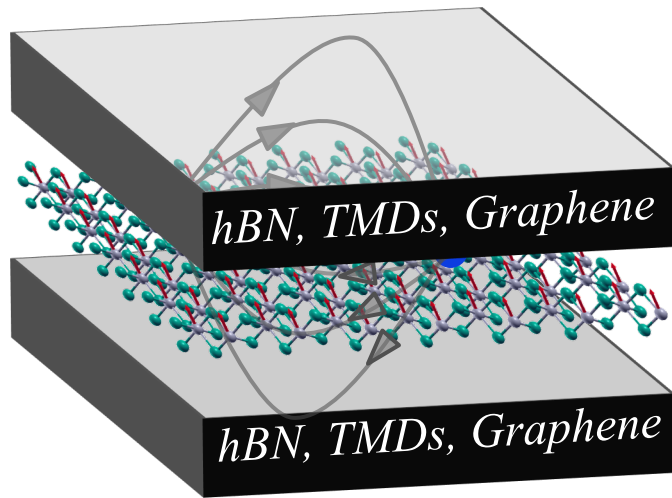
Rösner *et al.*, *Phys. Rev. B*, **92**, 085102 (2015)

Rösner *et al.*, *Nano Letters*, **16**, 2322 – 2327 (2016)

Florian *et al.*, *Nano Letters*, **18**, 2725 – 2732 (2018)

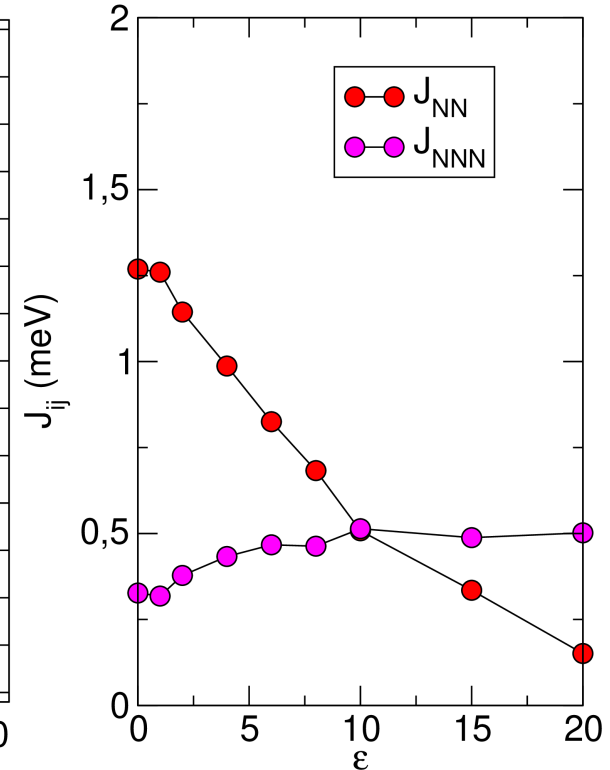
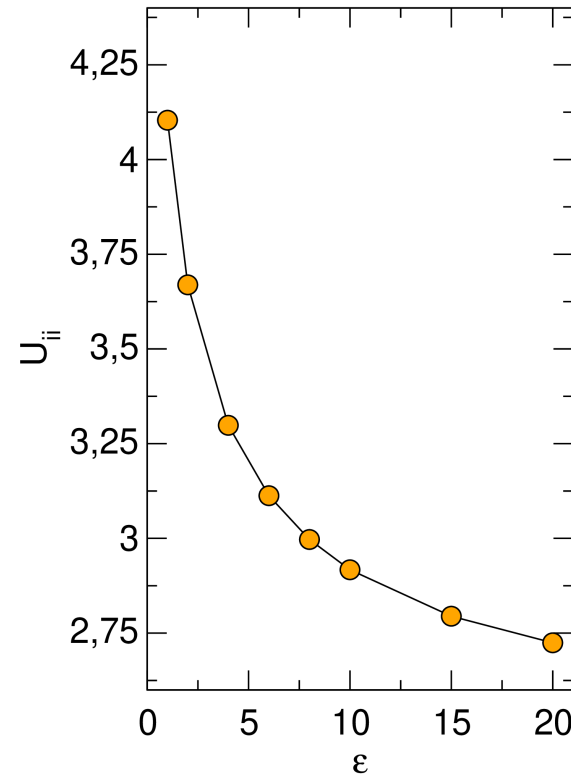
➤ Wannier-Hartree-Fock Approach: Substrate dielectric screening effects

Van der Waals heterostructure: $\text{hBN}/\text{CrI}_3/\text{hBN}$



Dielectric environment

$$U_{ij}^{CRPA} = \varepsilon^{-1} v_{ij}$$



□ Impact on the quasi-particle/excitonic gap

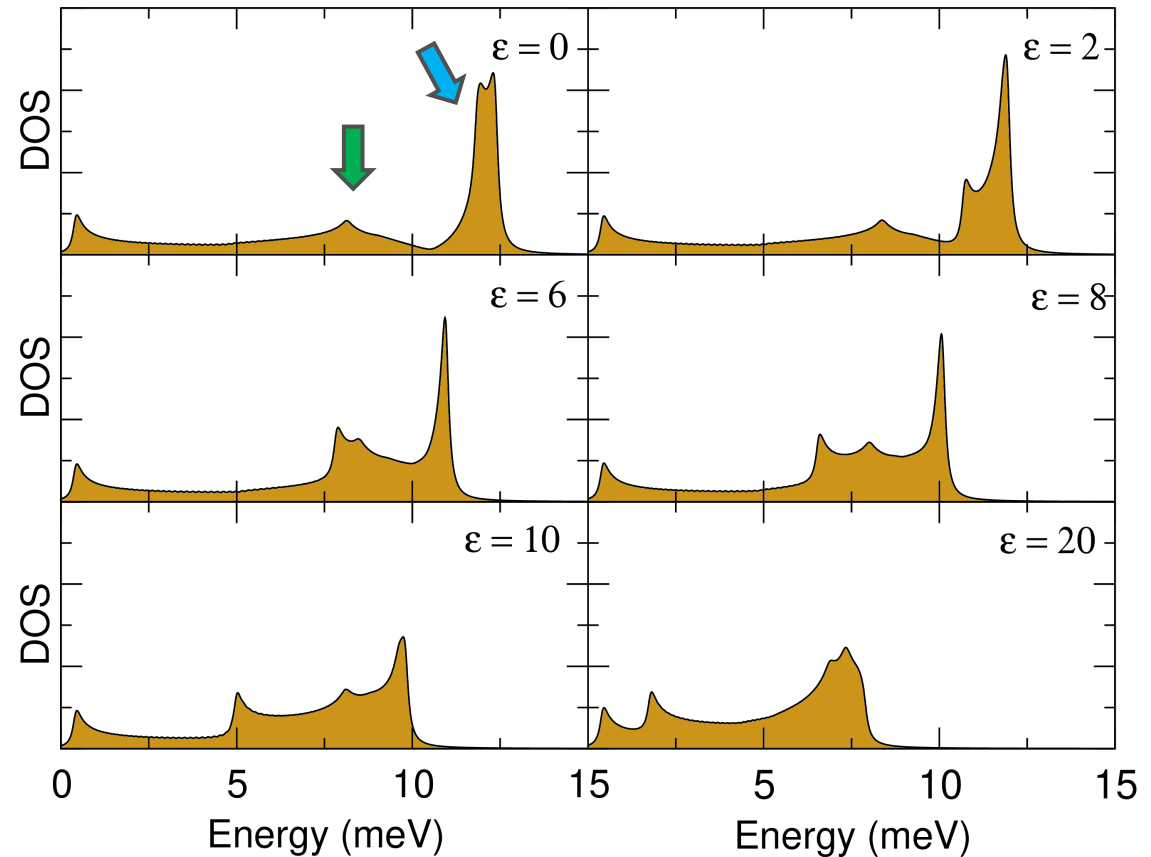
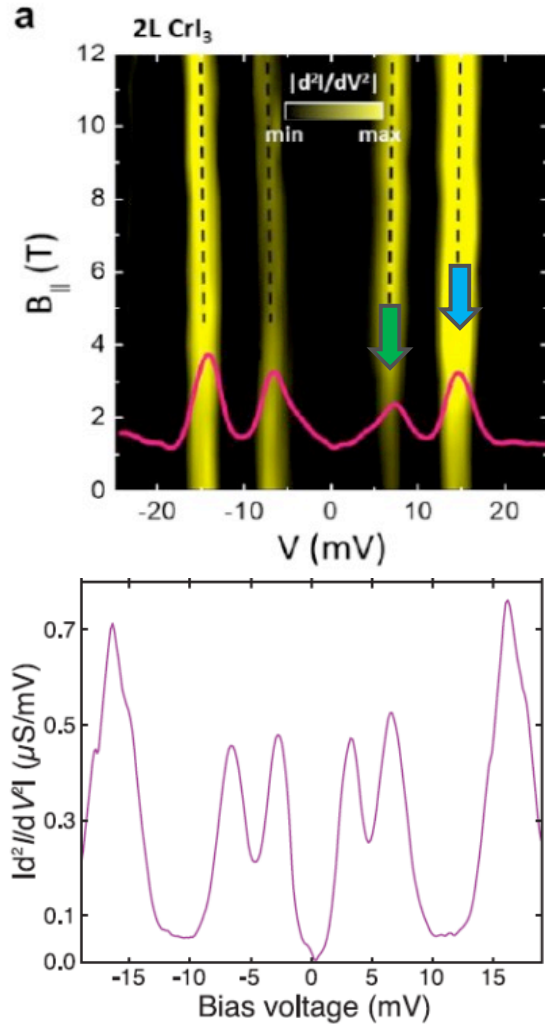
Rösner *et al.*, *Phys. Rev. B*, **92**, 085102 (2015)

Rösner *et al.*, *Nano Letters*, **16**, 2322 – 2327 (2016)

Florian *et al.*, *Nano Letters*, **18**, 2725 – 2732 (2018)

➤ Wannier-Hartree-Fock Approach: Spin-wave spectrum

Impact of dielectric environment on the spin-wave dispersion



➤ Wannier-Hartree-Fock Approach: **Conclusions**

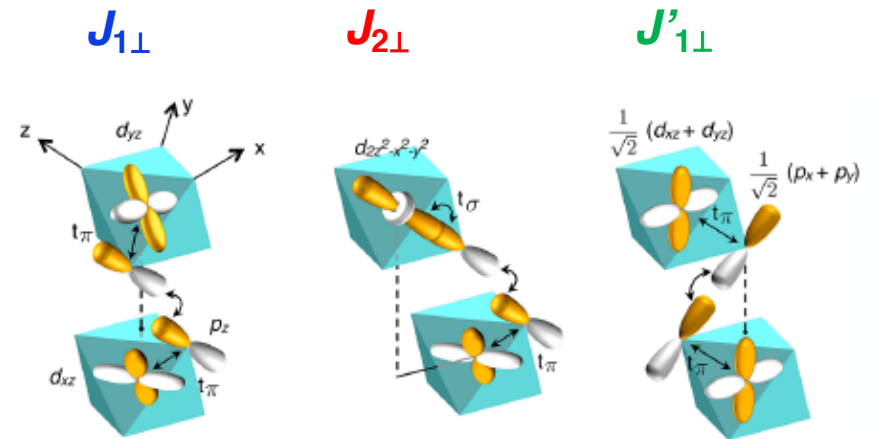
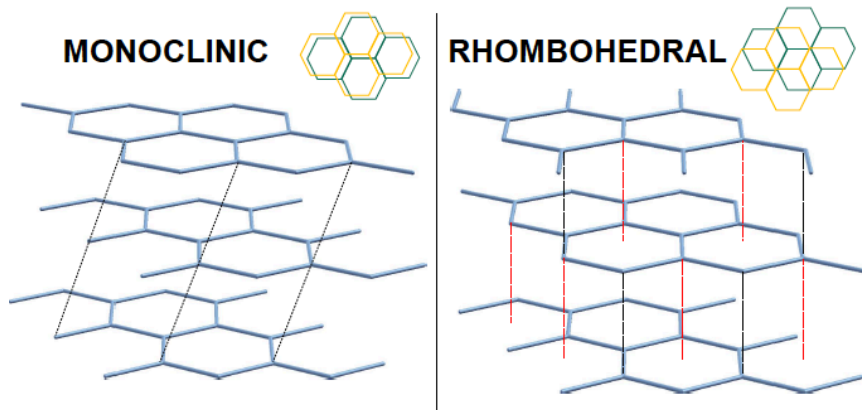
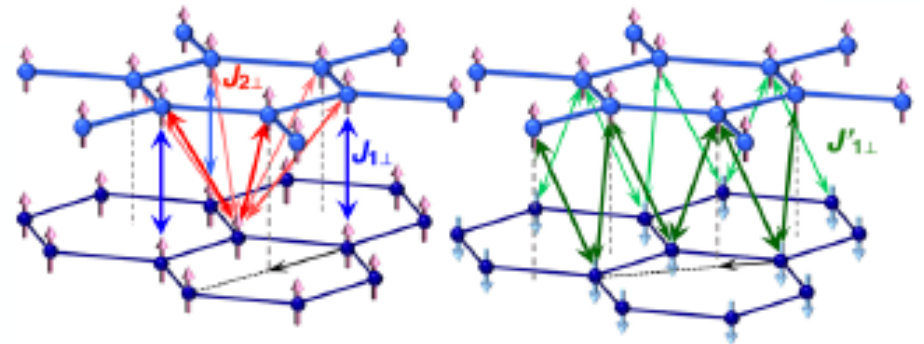
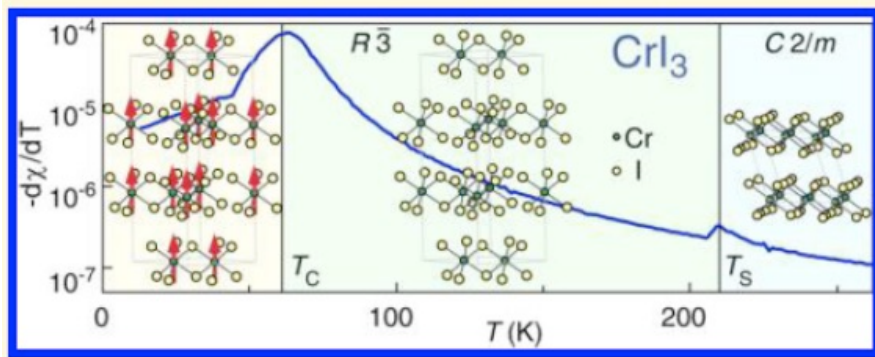
Coulomb and substrate dielectric screening effects impact the magnon spectrum of Chromium Trihalides

We have developed a new computational tool to study Coulomb interactions in CrX_3 combining Wannier-HF and the magnetic force theorem (MFT)

Magnetic Polarons in Bilayer CrI₃

➤ Magnetism at the microscopic level: Interlayer Exchange

$T_S = 210 \text{ K (CrI}_3\text{); 420 K (CrBr}_3\text{); 240 K (CrCl}_3\text{)}$



$J_{\perp} \approx 0.04 \text{ meV}$

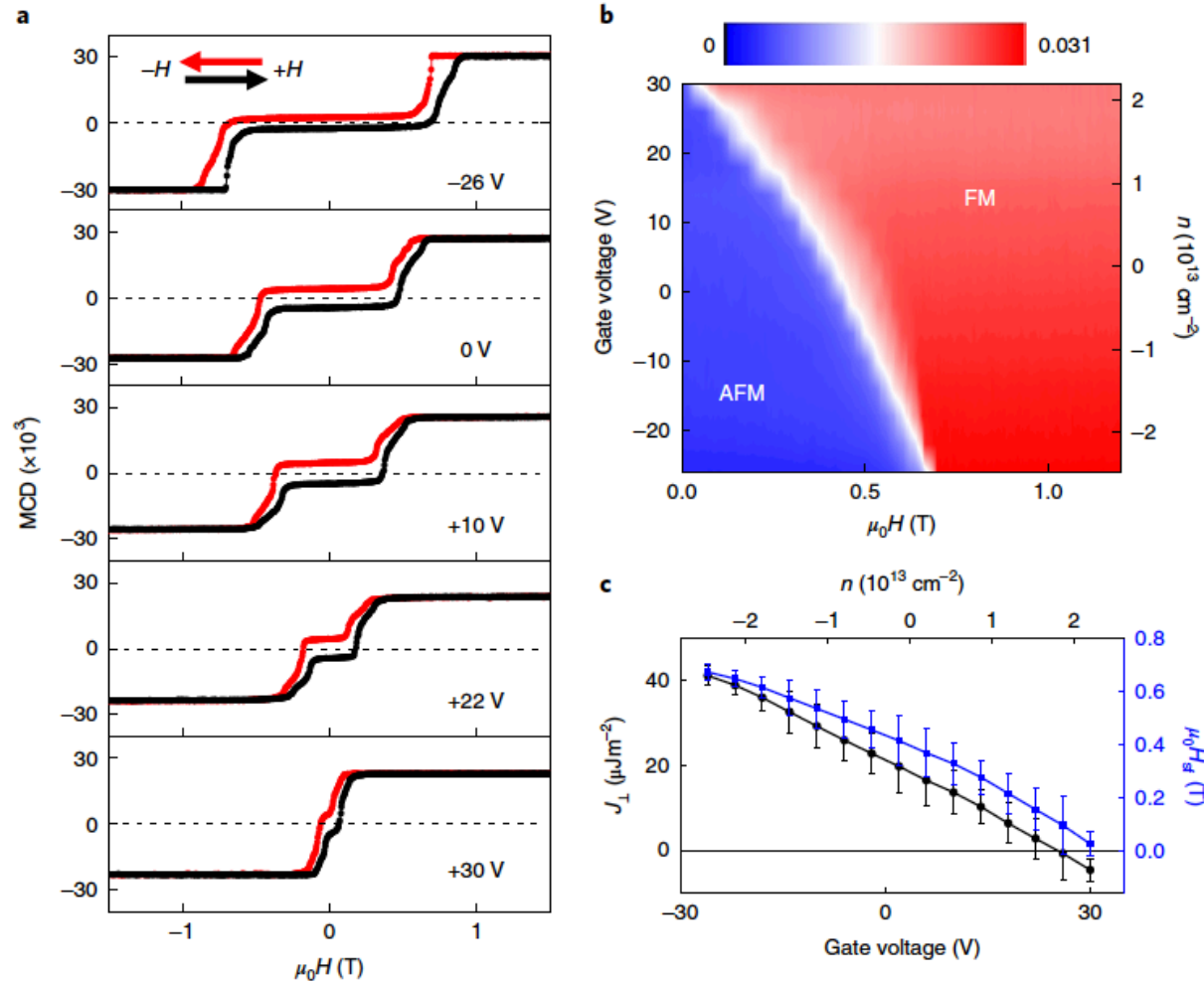
McGuire et al., *Chem. Mater.*, **27**, 612 – 620 (2015)

Sivadas et al., *Nano Letters*, **18**, 7658 – 7664 (2018)

DS, Cardoso and Fernández-Rossier, *Sol. Stat. Comm.*, **299**, 113662 (2019)

DS, Katsnelson and Fernández-Rossier, *Nano Letters* (Mini-Review - Accepted)

➤ Electric field control of interlayer magnetism

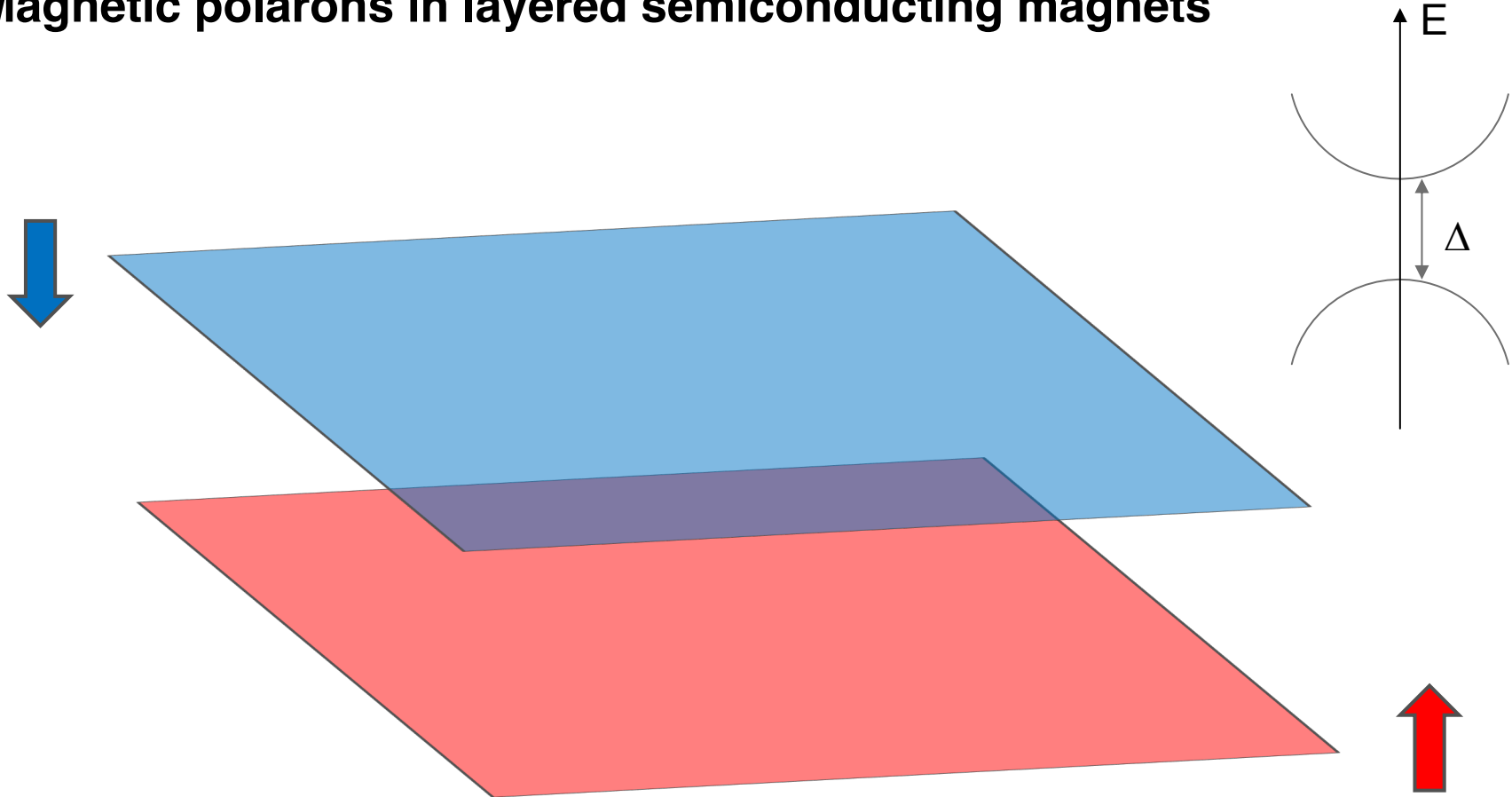


Jiang et al., *Nature Nanotechnology*, **13**, 549 – 553 (2018)

Jiang et al., *Nature Materials*, **17**, 406 – 410 (2018)

Huang et al., *Nature Nanotechnology*, **13**, 544 - 548 (2019)

➤ Magnetic polarons in layered semiconducting magnets

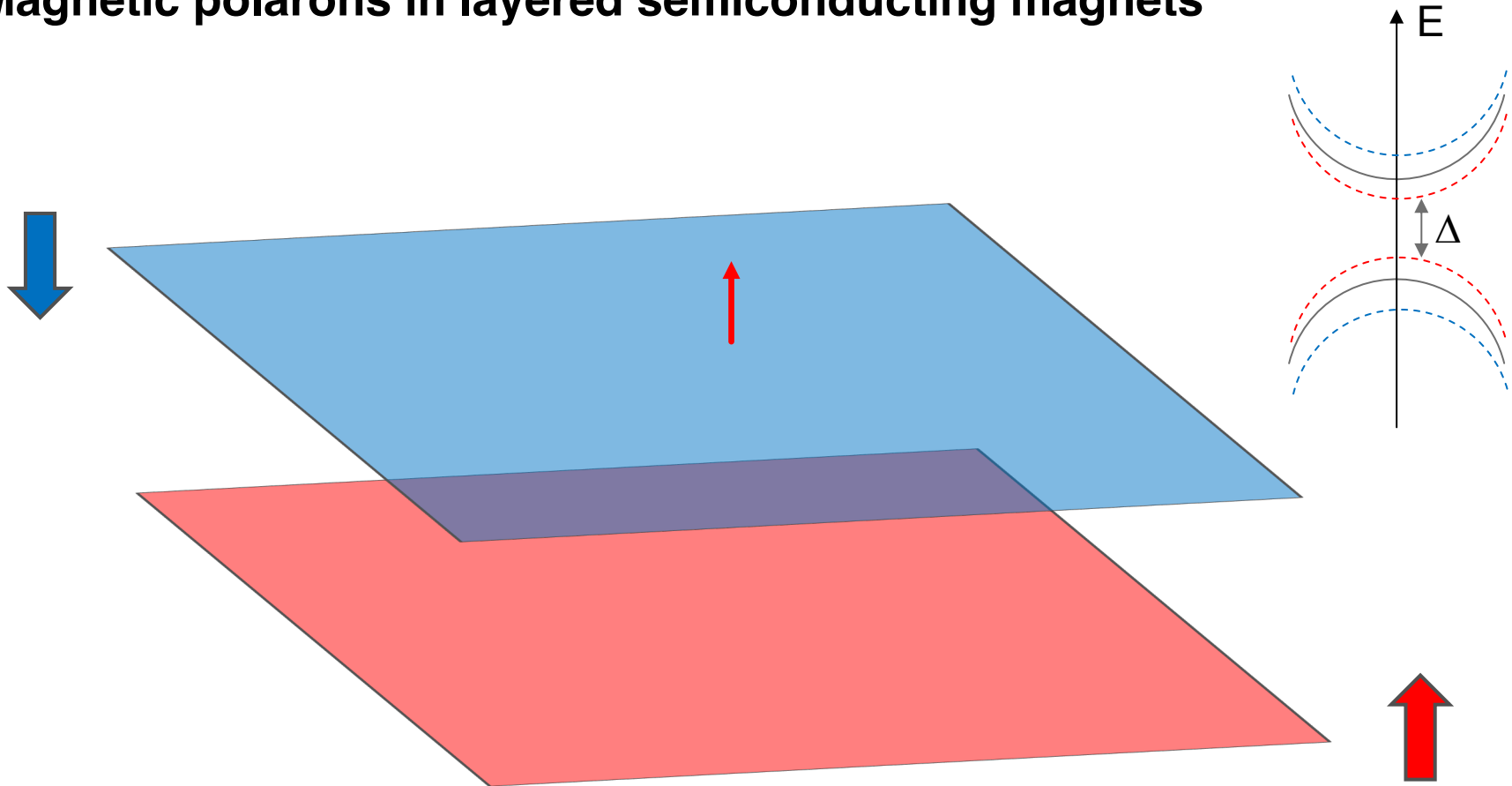


Auslander and Katsnelson, *J. Magn. Magn. Mater.*, **24**, 117 (1981)

Vischer, *Phys. Rev. B*, **10**, 943 (1974)

Mott, *Metal-Insulator Transitions*, Taylor & Francis, London (1974)

➤ Magnetic polarons in layered semiconducting magnets

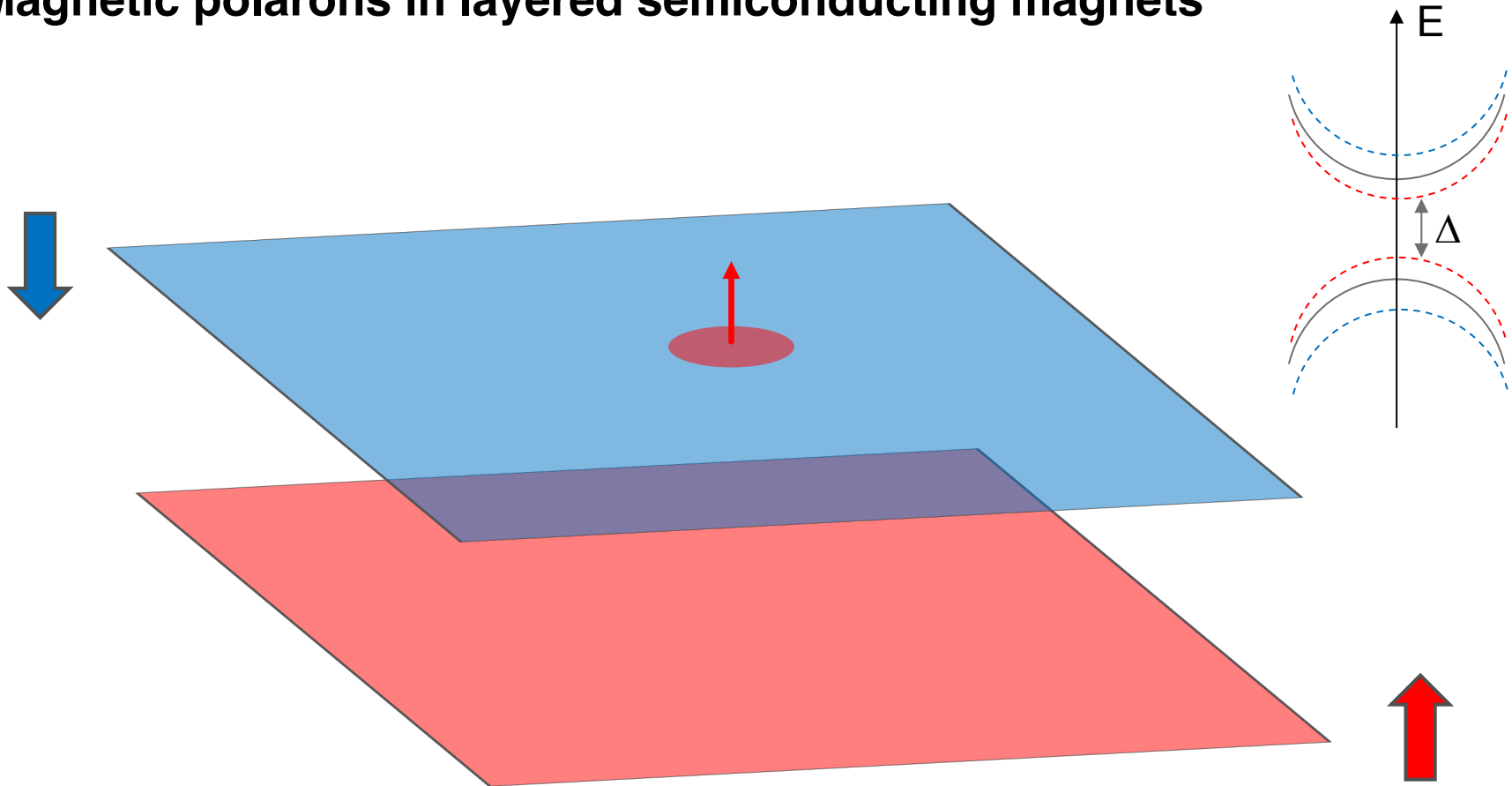


Auslander and Katsnelson, *J. Magn. Magn. Mater.*, **24**, 117 (1981)

Vischer, *Phys. Rev. B*, **10**, 943 (1974)

Mott, *Metal-Insulator Transitions*, Taylor & Francis, London (1974)

➤ Magnetic polarons in layered semiconducting magnets

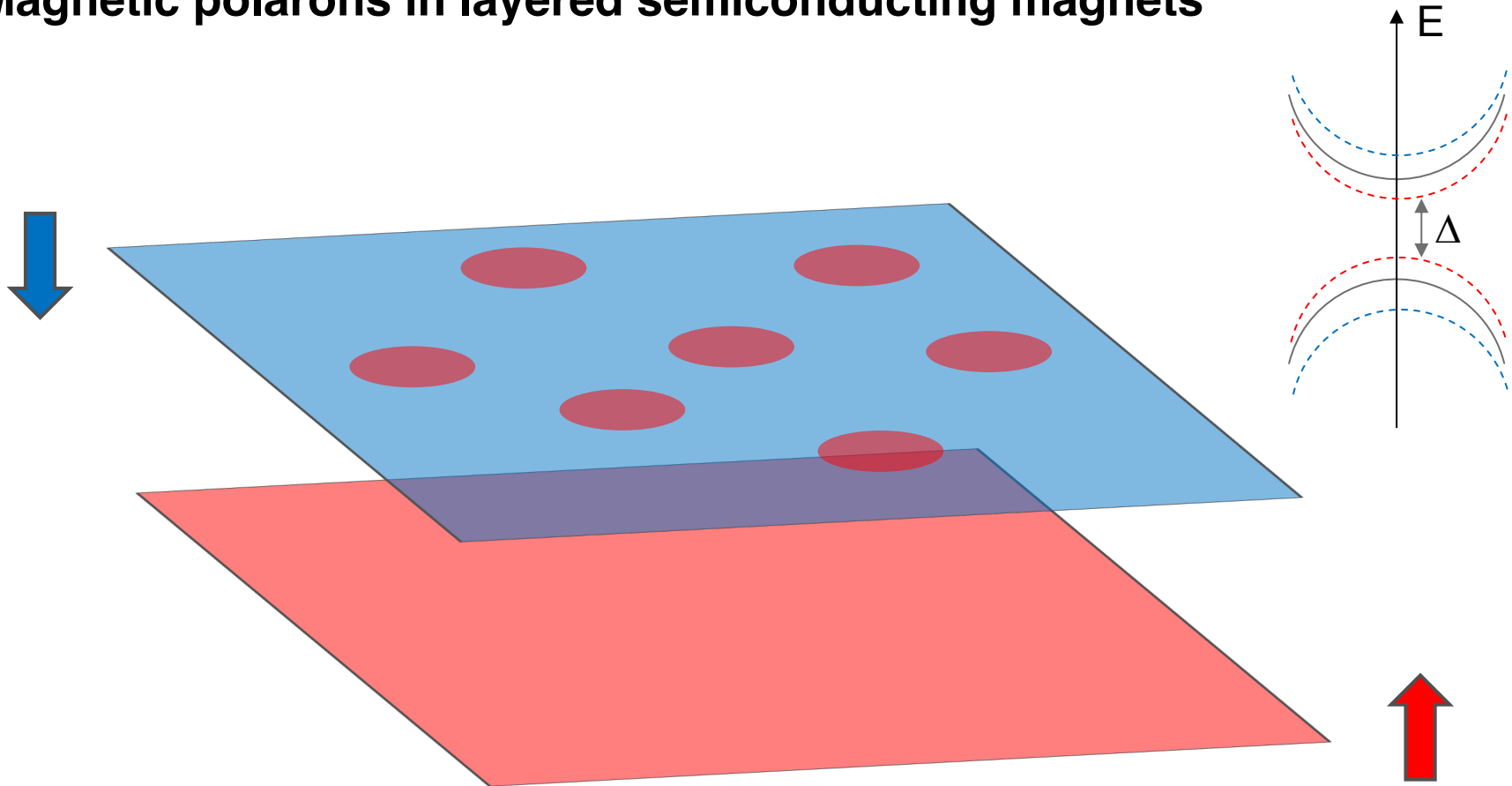


Auslander and Katsnelson, *J. Magn. Magn. Mater.*, **24**, 117 (1981)

Vischer, *Phys. Rev. B*, **10**, 943 (1974)

Mott, *Metal-Insulator Transitions*, Taylor & Francis, London (1974)

➤ Magnetic polarons in layered semiconducting magnets

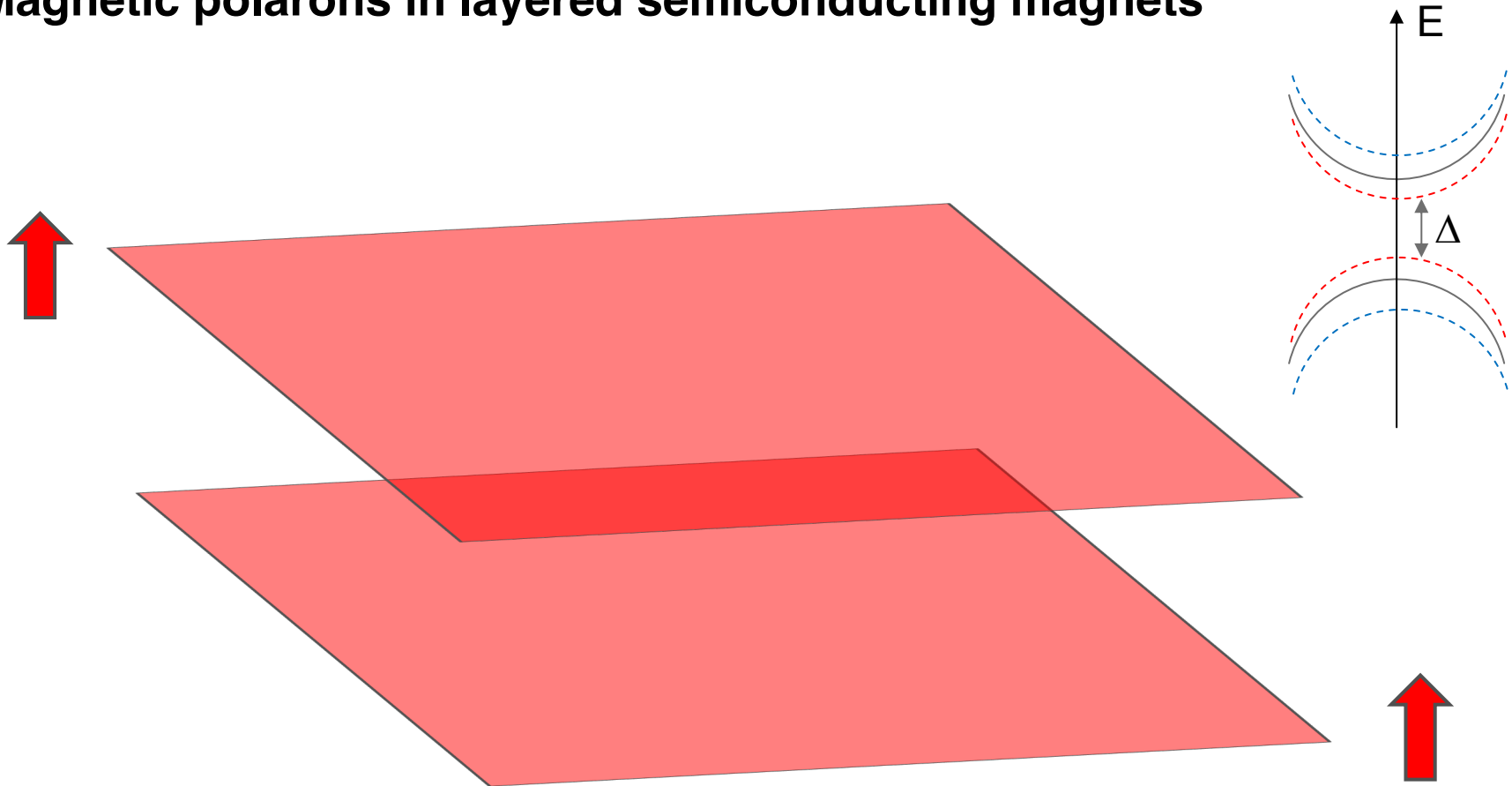


Auslander and Katsnelson, *J. Magn. Magn. Mater.*, **24**, 117 (1981)

Vischer, *Phys. Rev. B*, **10**, 943 (1974)

Mott, *Metal-Insulator Transitions*, Taylor & Francis, London (1974)

➤ Magnetic polarons in layered semiconducting magnets



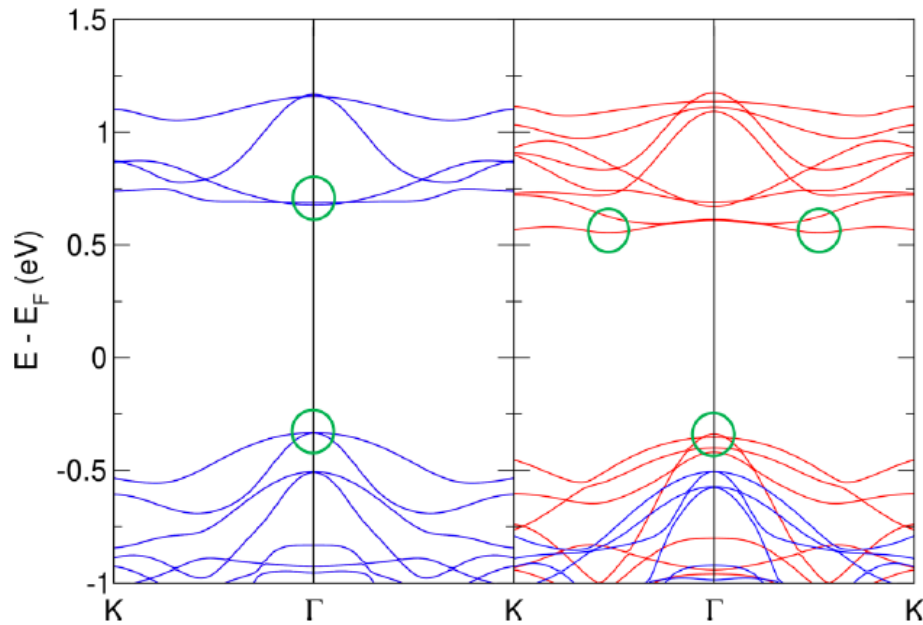
Auslander and Katsnelson, *J. Magn. Magn. Mater.*, **24**, 117 (1981)

Vischer, *Phys. Rev. B*, **10**, 943 (1974)

Mott, *Metal-Insulator Transitions*, Taylor & Francis, London (1974)

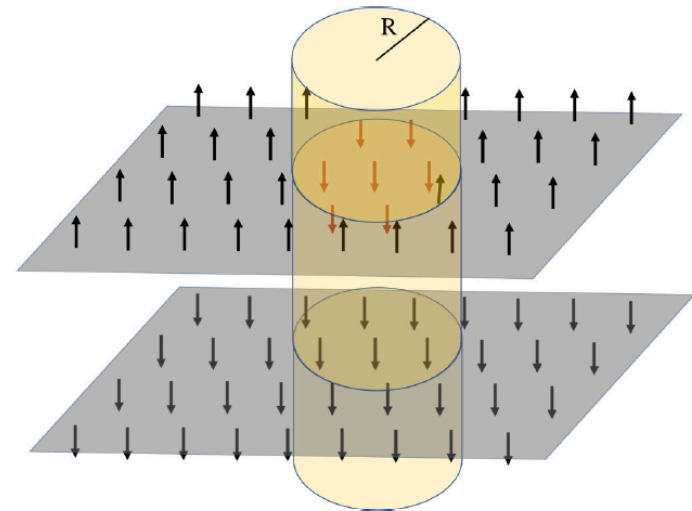
➤ Magnetic polarons in bilayer CrI₃

Formation energy of a magnetic polaron



	VBMax (eV)	CBMin (eV)	m_h^*/m_e	m_e^*/m_e
AFM	-0.333	0.678	0.15	0.18
FM	-0.339	0.555	0.02	0.11

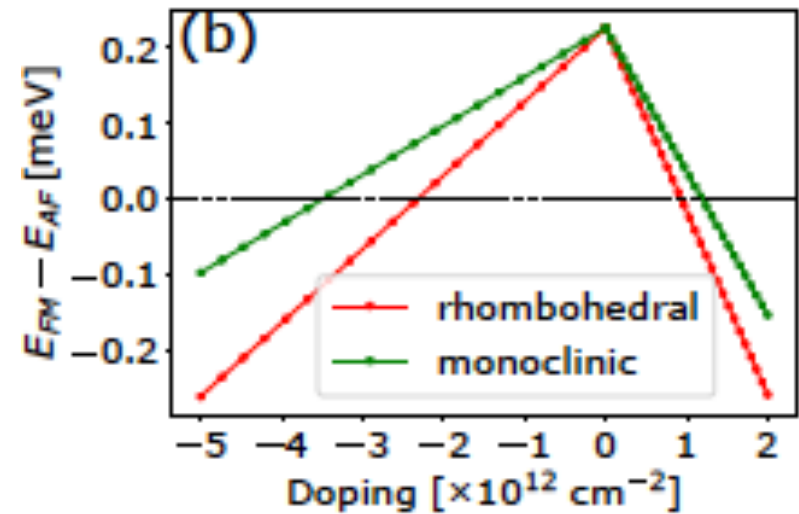
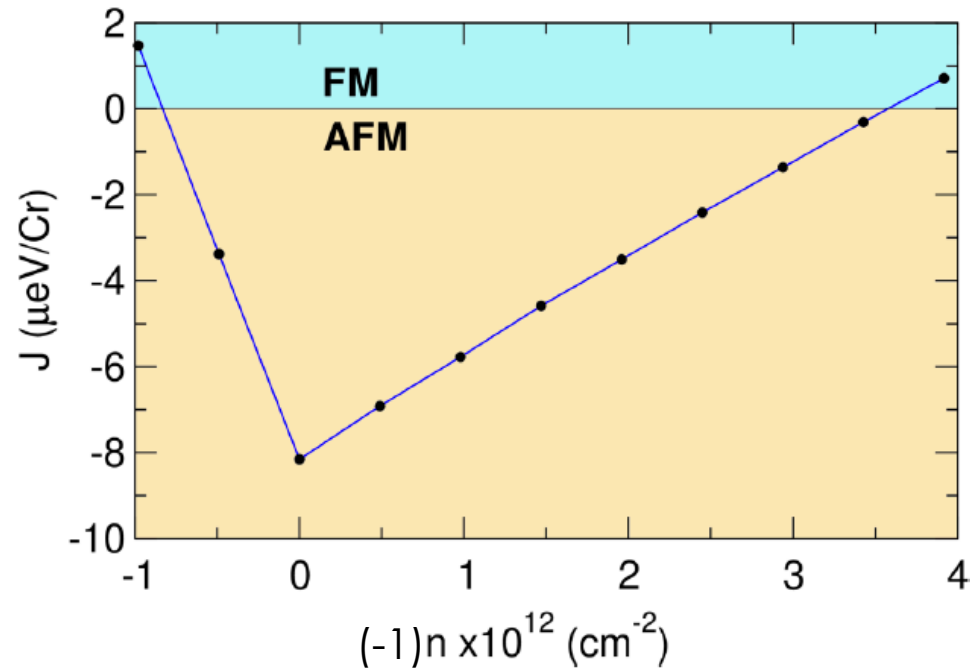
$$\mathcal{E}(R) = -\Delta + \frac{\hbar^2 z_0^2}{2m^*R^2} + J \frac{\pi R^2}{S_0}$$



$$\mathcal{E}_e = -91.3 \text{ meV and } \mathcal{E}_h = 67.9 \text{ meV}$$

➤ Magnetic polarons in bilayer CrI_3

DFT calculations



DS and Katsnelson, *Phys. Rev. B*, **101**, 041402(R) (2020)

Lei et al., [arXiv:1902.06418](https://arxiv.org/abs/1902.06418)

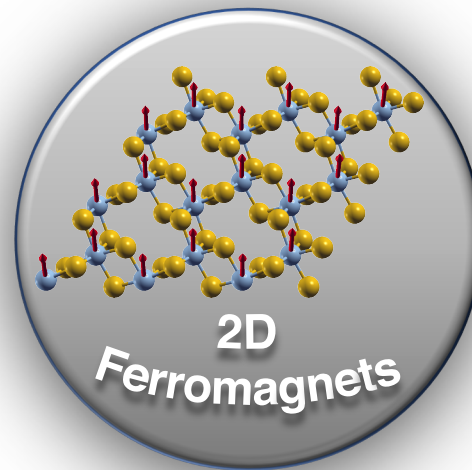
➤ Magnetic polarons in bilayer CrI₃: **Conclusions**

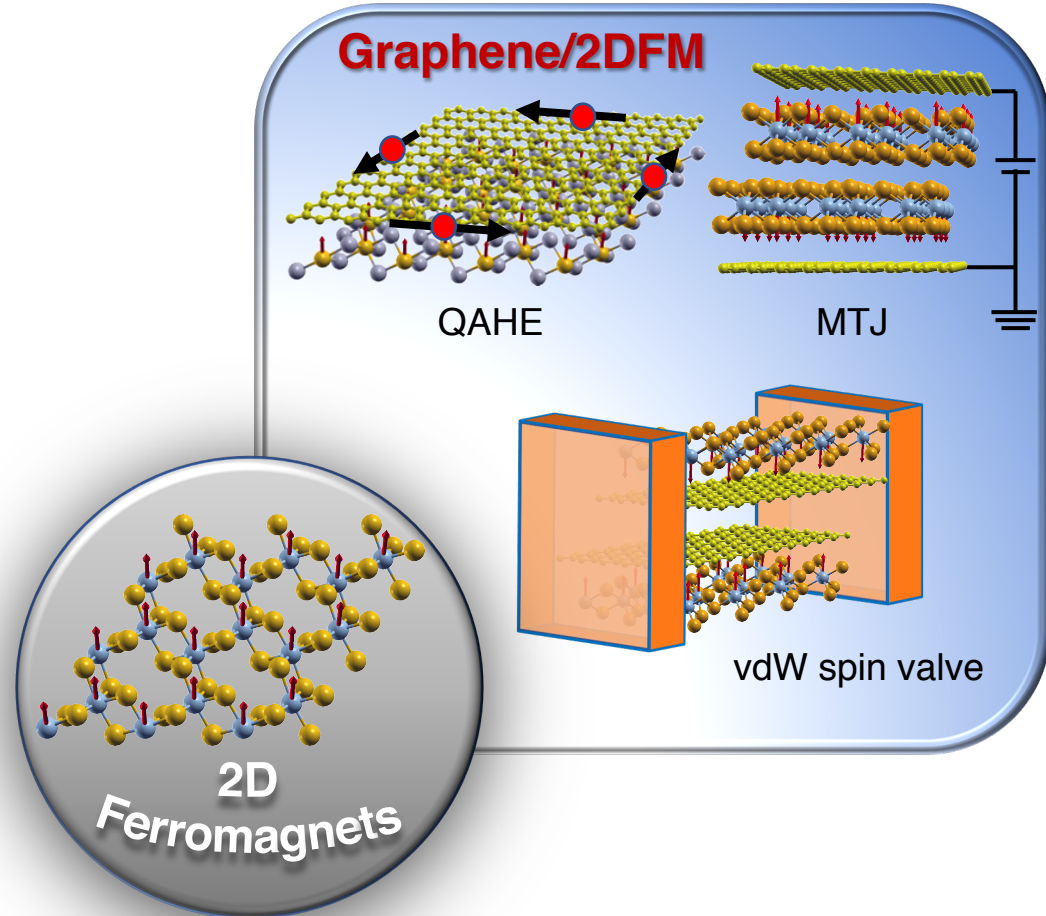
Electric field modulation of interlayer magnetism is driven by magnetic polarons in bilayer CrI₃

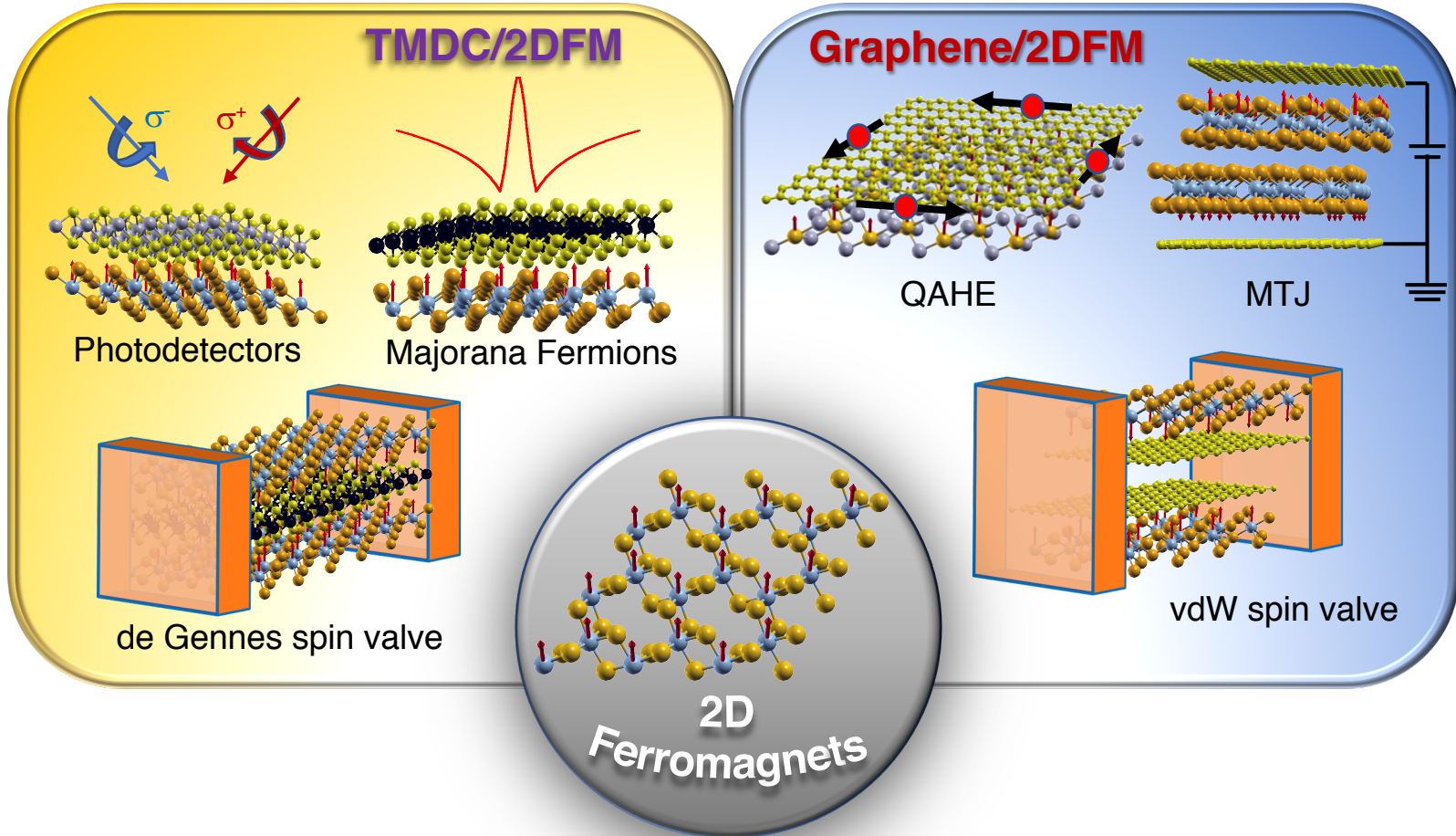
The formation of magnetic polarons is only allowed for electron doping which facilitates the antiferro-to-ferro phase transition

Still several open issues

- Origin of magnetic anisotropy (single-ion, Kitaev, 2nd neighbor DMI, etc.)
- Role of van der Waals interactions in interlayer exchange (different results with different functionals)
- Effect of substrates on the magnetic and electronic properties of CrX_3
- Moiré magnets (Hejazi et al., *PNAS*, **117**, 10721 – 10726 (2020))
- Magneto-optical properties







TMDC/2DFM

Photodetectors

Majorana Fermions

de Gennes spin valve

The TMDC/2DFM section features a yellow background. At the top, it shows two circular diagrams with arrows representing spin states σ^- and σ^+ . Below these are two 3D ball-and-stick models of layered structures. The first model shows a transition metal dichalcogenide (TMDC) structure with red arrows indicating spin. The second model shows a 2D ferromagnetic (2DFM) structure with a red line graph above it. At the bottom, a 3D diagram shows two orange blocks representing electrodes, with a layered structure between them labeled 'de Gennes spin valve'.

Graphene/2DFM

QAHE

MTJ

vdW spin valve

The Graphene/2DFM section features a blue background. At the top, it shows a 3D model of a graphene layer with red dots and black arrows, labeled 'QAHE'. To the right, a diagram shows a magnetic tunnel junction (MTJ) with a battery symbol and ground, labeled 'MTJ'. At the bottom, a 3D diagram shows two orange blocks representing electrodes, with a layered structure between them labeled 'vdW spin valve'.

2D Ferromagnets

A central circular inset shows a 3D ball-and-stick model of a 2D ferromagnetic structure with red arrows indicating spin.

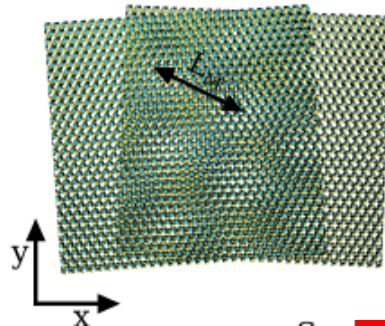
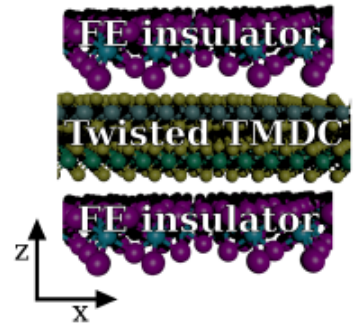
Kang WANG Talk this afternoon 16:20

Moiré
Ferromagnets

Skyrmions in
the Moiré

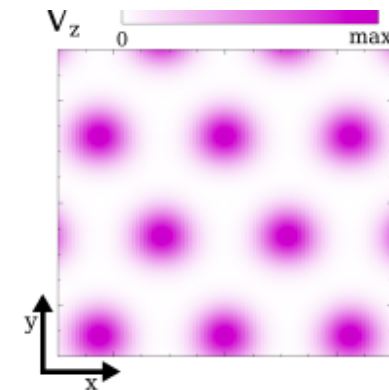
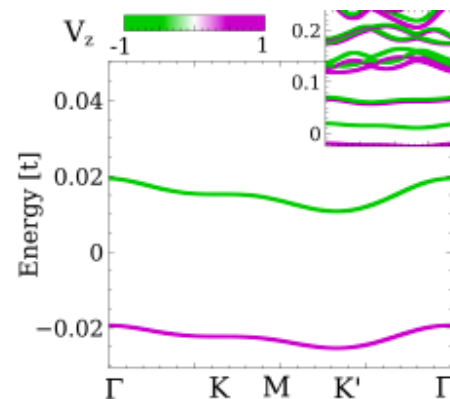
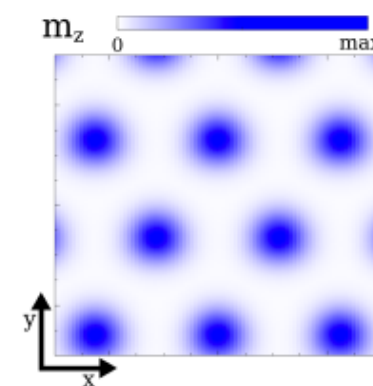
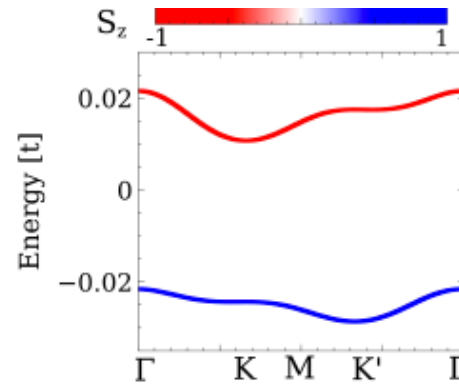
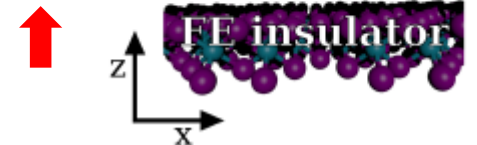
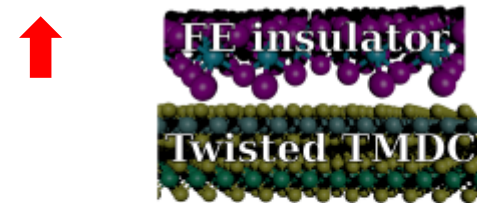
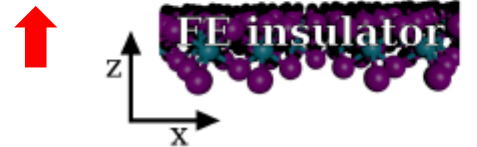
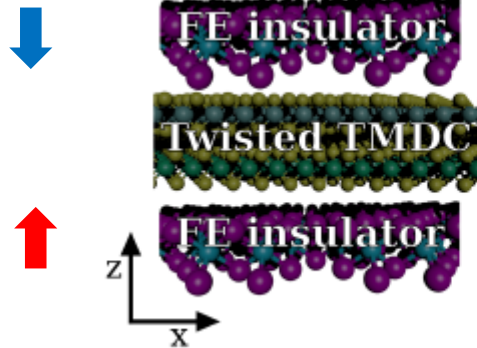
The bottom section features a grey background. On the left, a 3D diagram shows a Moiré pattern of red dots, labeled 'Moiré Ferromagnets'. On the right, a 3D diagram shows a Moiré pattern with colorful circular structures, labeled 'Skyrmions in the Moiré'. At the top right, the text 'Kang WANG Talk this afternoon 16:20' is displayed.

➤ Exchange proximity effects in twisted TMDs



DS and Lado, *J. Phys. D: Appl. Phys.*
<https://doi.org/10.1088/1361-6463/abaa15>

For the coffe break!



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Rösner**



**Dr. Alexander
Rudenko**



**Prof. Joaquín
Fernández
Rossier**



Dr. José Lado

Thank You!



Acknowledgments

