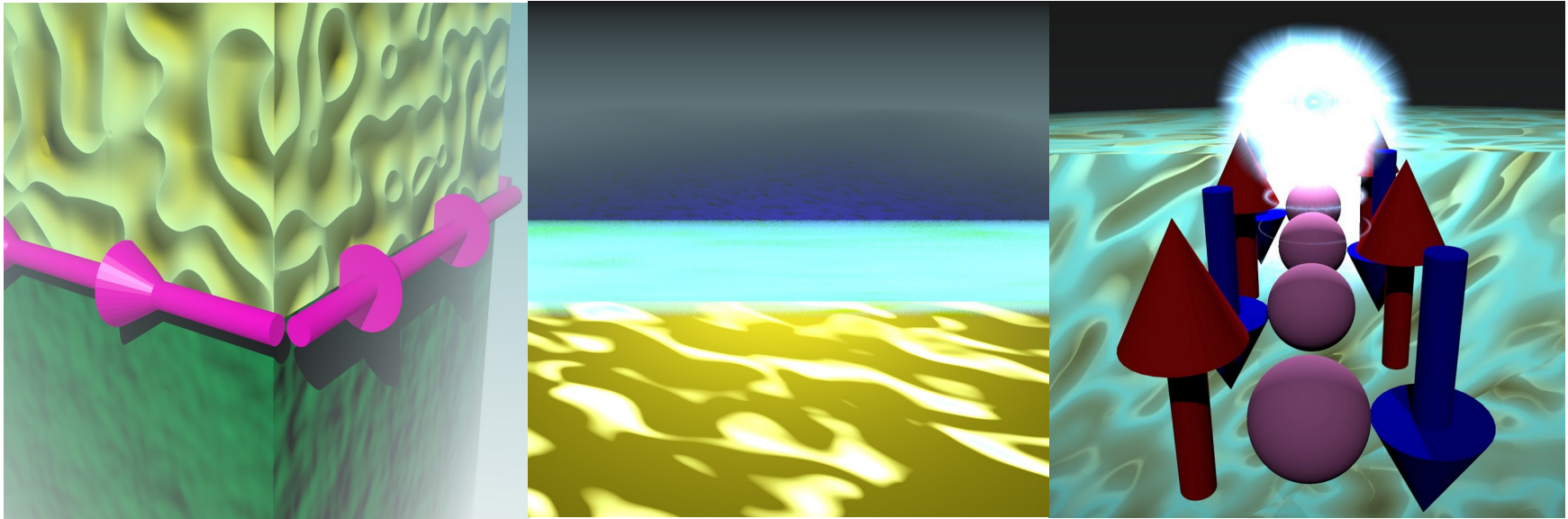


# Solitons and topological superconductivity in antiferromagnet-superconductor interfaces

**Jose Lado**

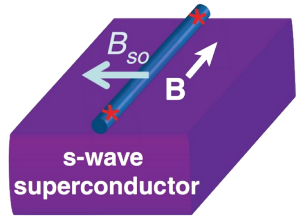
*Department of Applied Physics, Aalto University, Finland*



*Coherent order and transport in spin-active systems: Interplay between magnetism and superconductivity, SPICE, November 17<sup>th</sup> 2020*

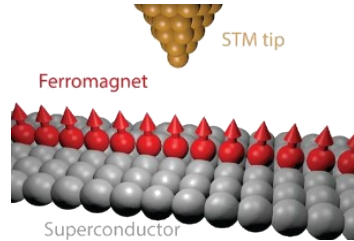
# Platforms for Majorana physics

## Semiconductors



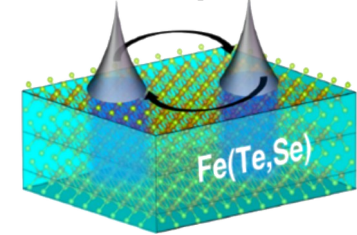
*Science* 336.6084 (2012): 1003-1007

## Ferromagnetic atomic chains



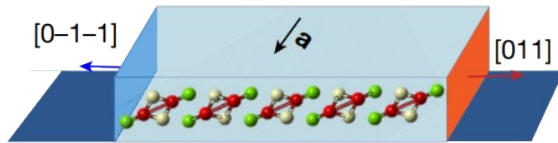
*Science* 346.6209 (2014): 602-607

## Fe-based superconductors



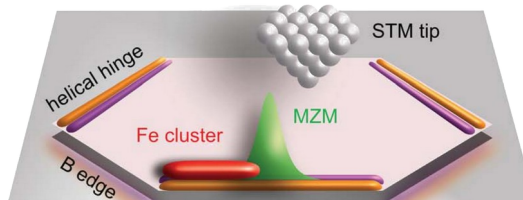
*Science* 362.6412 (2018): 333-335

## Heavy-fermion compounds



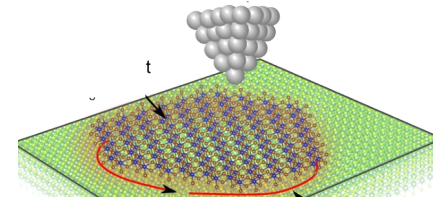
*Nature* 579, 523–527 (2020)

## Topological insulators



*Science* 364.6447 (2019): 1255-1259

## Two-dimensional materials



arXiv:2002.02141 (2020)

New materials open new venues for engineering and controlling Majorana physics 2

# Topological superconductivity with antiferromagnetic insulators

## Build a topological superconductor with

- A conventional (s-wave) superconductor
- An antiferromagnetic insulator

The prize



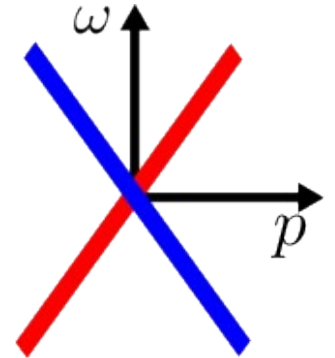
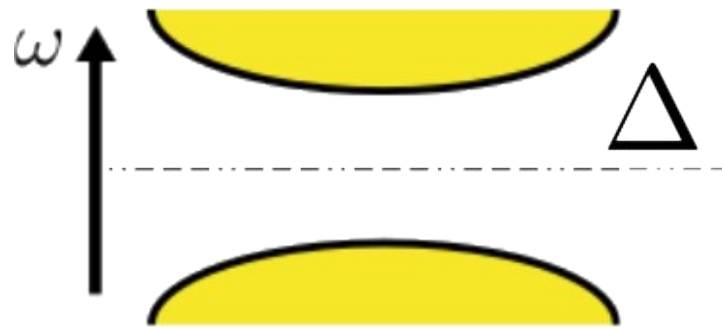
Bringing a new solid state platform to realize artificial topological superconductors

# How to build your own topological superconductor



## Ingredients

- s-wave pairing
- Helical states



**Objective: to realize a spinless superconductor**

$$H = \sum_n t c_{n+1}^\dagger c_n + \Delta c_n c_{n+1} + c.c.$$

# The initial problem

How can we get a topological phase starting from a trivial insulator?



We need to create a “spinless” gapless state out of an insulator



# Behind the scenes

Manfred Sigrist



Phys. Rev. Lett. 121, 037002 (2018)  
Phys. Rev. Research 2, 023347 (2020)

Senna Luntama

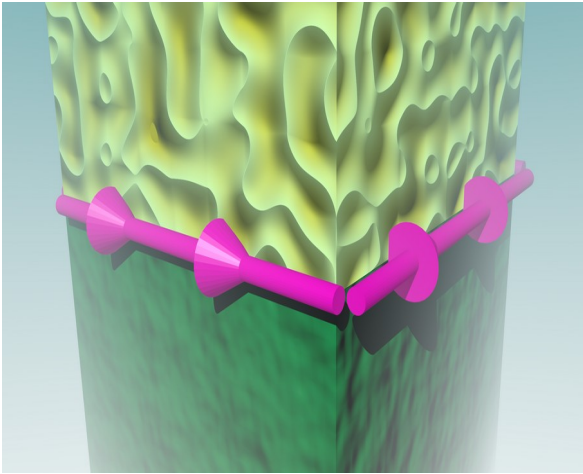


arXiv:2011.06990 (2020)

Päivi Törmä



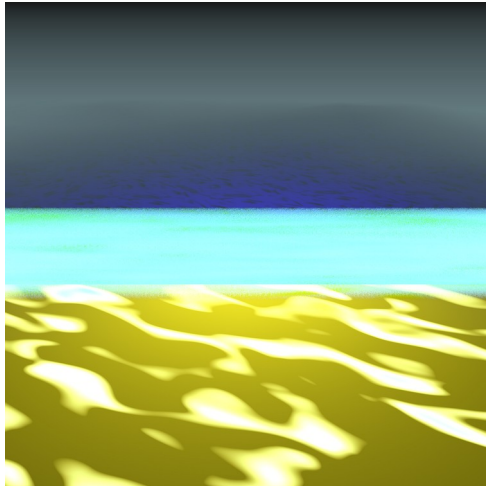
# Today's story



Topological superconductivity (TS)  
in 3D AF insulators

***No interactions***

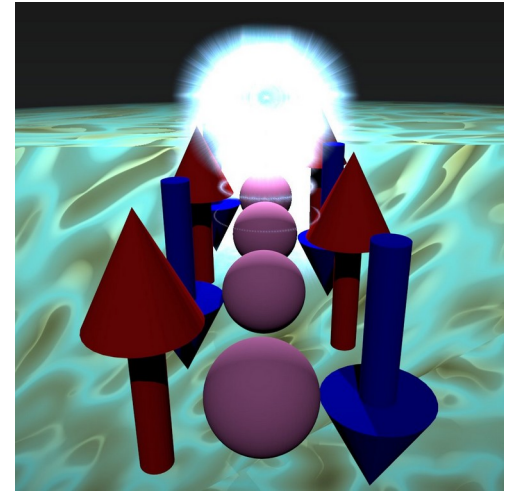
*Phys. Rev. Lett.* 121, 037002 (2018)



Interaction-induced  
TS in 2D AF insulators

***Mean-field interactions***

*arXiv:2011.06990* (2020)



The quantum many-body  
1D limit

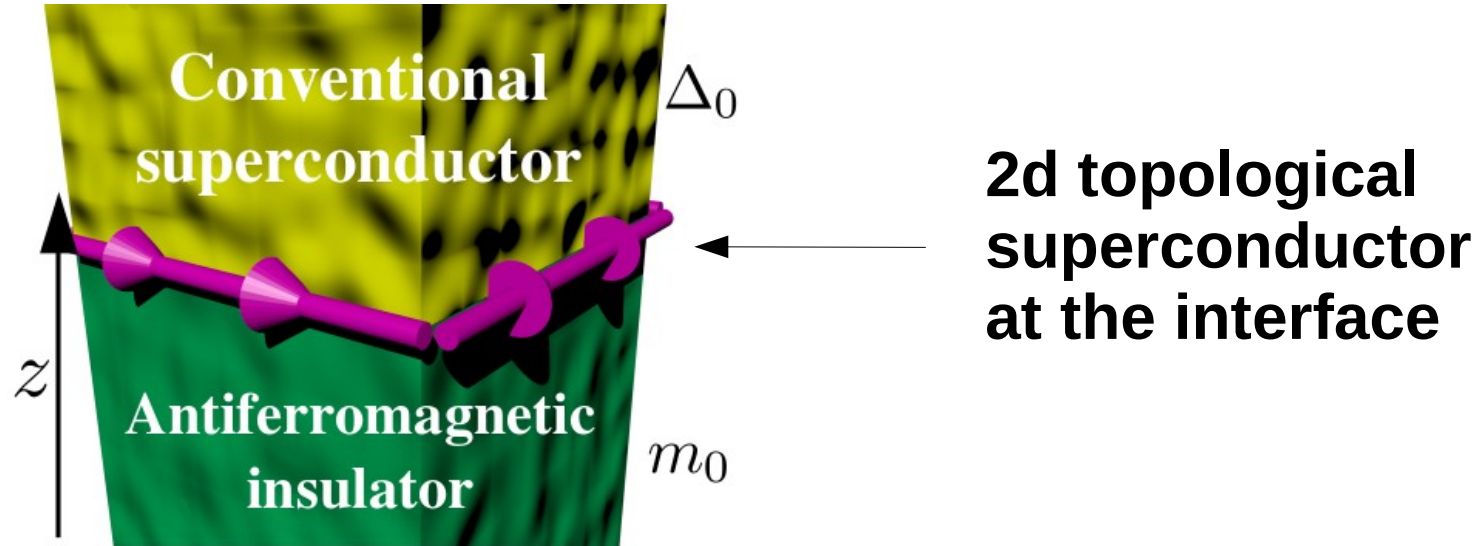
***Purely quantum many-body***

*Phys. Rev. Research* 2, 023347 (2020)

**Creating a 2D topological  
superconductor with a 3D  
antiferromagnetic insulator**



# Heterostructure for 2D TS in a 3D AF insulator



$$\mathcal{H} = \mathcal{H}_{\text{kin}} + \mathcal{H}_{\text{AF}} + \mathcal{H}_{\text{SC}} + \mathcal{H}_{\text{SOC}}$$

Kinetic  
energy

Antiferromagnetism

Superconductivity

Spin-orbit coupling

# Solitonic modes between Dirac AF and SC

Total Hamiltonian, for an antiferromagnet with gaped Dirac points

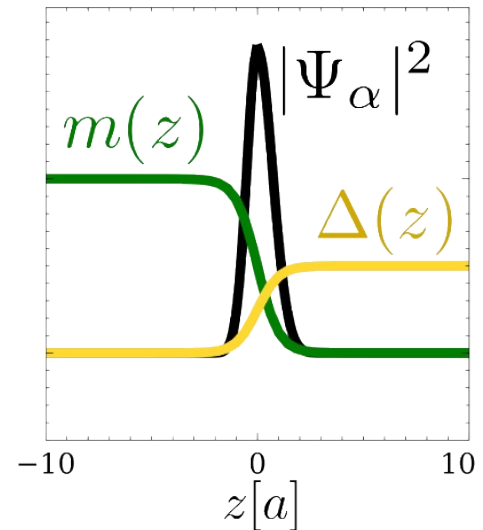
$$\mathcal{H} = \mathcal{H}_{\text{kin}} + \mathcal{H}_{\text{AF}} + \mathcal{H}_{\text{SC}}$$



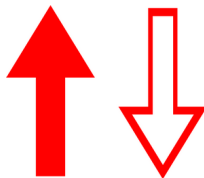
There will be two zero solutions  $\mathcal{H}|\Psi_\alpha\rangle = 0$

*Phys. Rev. X 5, 041042 (2015)*

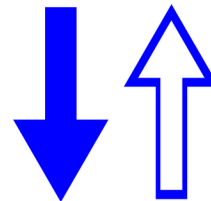
*similar to a Jackiw-Rebbi soliton  
Phys. Rev. D 13, 3398 (1976)*



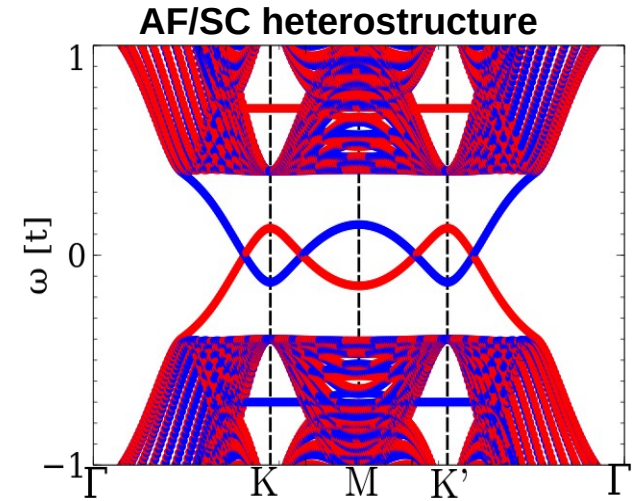
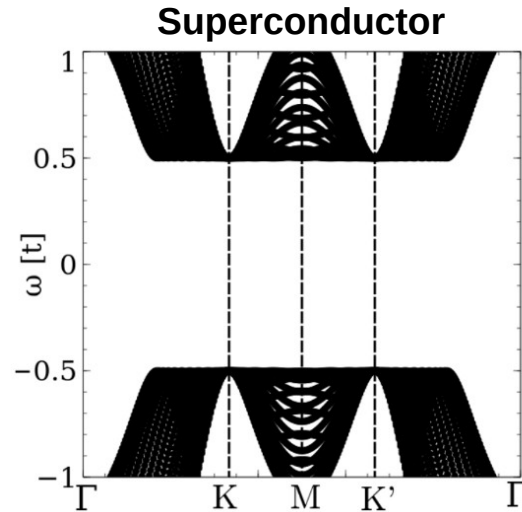
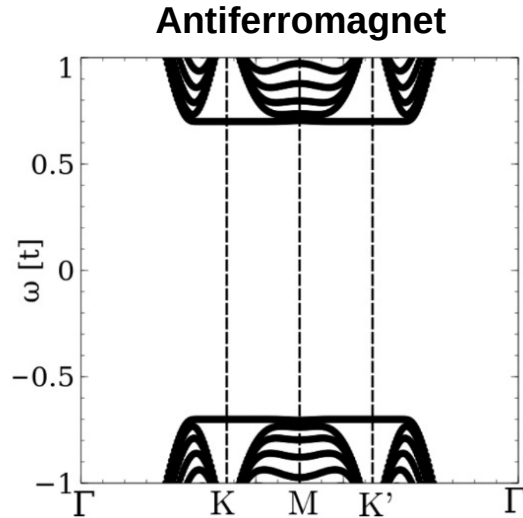
**Sector #1**  
Up electron, down hole



**Sector #2**  
Down electron, up hole



# Emergence of interfacial modes, no spin-orbit coupling

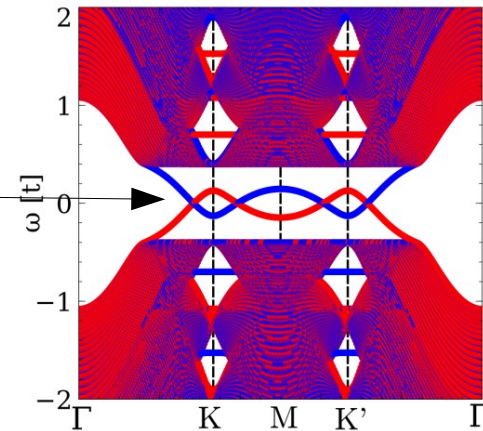
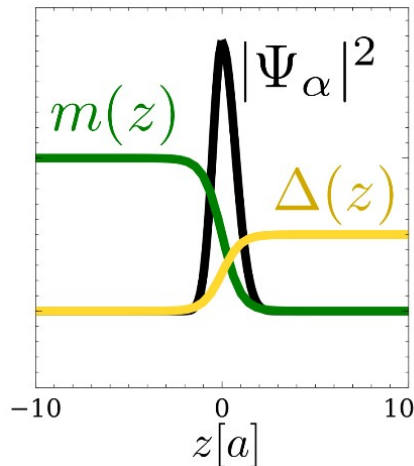
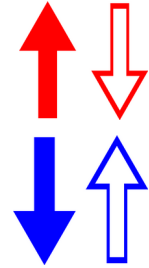


# Interface states between AF and SC

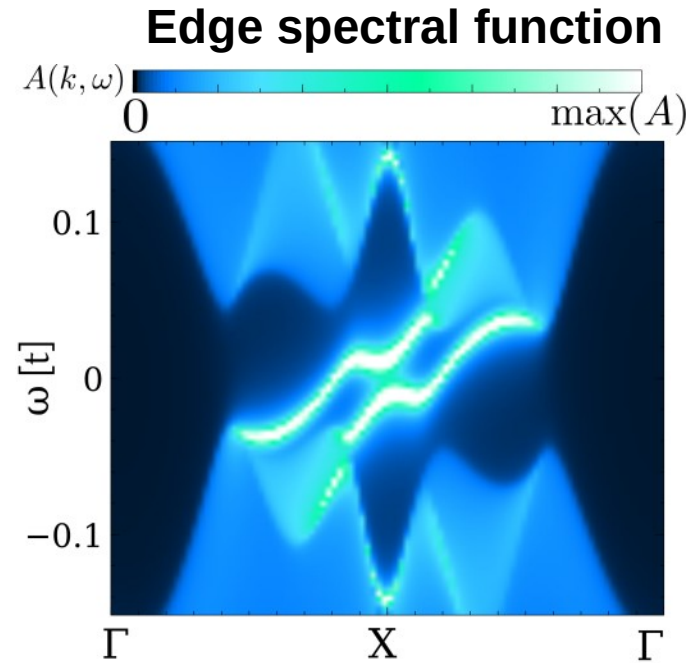
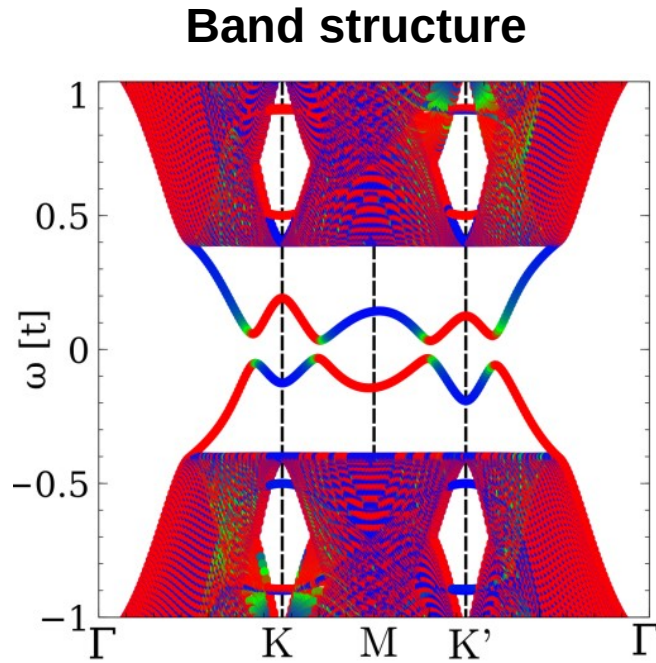
## Superconducting solitonic excitations

$$\Psi_1(z) = g(z) [c_{A, \vec{k}_{\parallel}, \uparrow} - ic_{B, \vec{k}_{\parallel}, \uparrow} - c_{A, -\vec{k}_{\parallel}, \downarrow}^\dagger - ic_{B, -\vec{k}_{\parallel}, \downarrow}^\dagger]$$

$$\Psi_2(z) = g(z) [c_{A, \vec{k}_{\parallel}, \downarrow} + ic_{B, \vec{k}_{\parallel}, \downarrow} - c_{A, -\vec{k}_{\parallel}, \uparrow}^\dagger + ic_{B, -\vec{k}_{\parallel}, \uparrow}^\dagger]$$

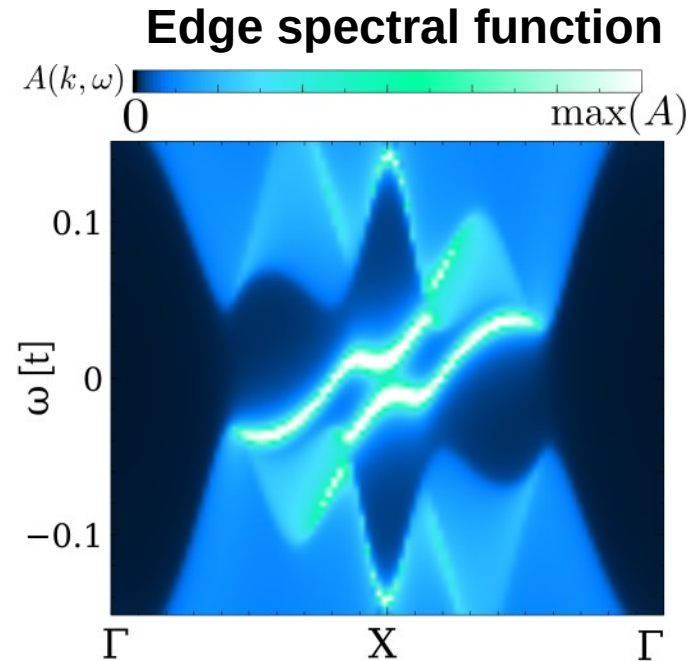
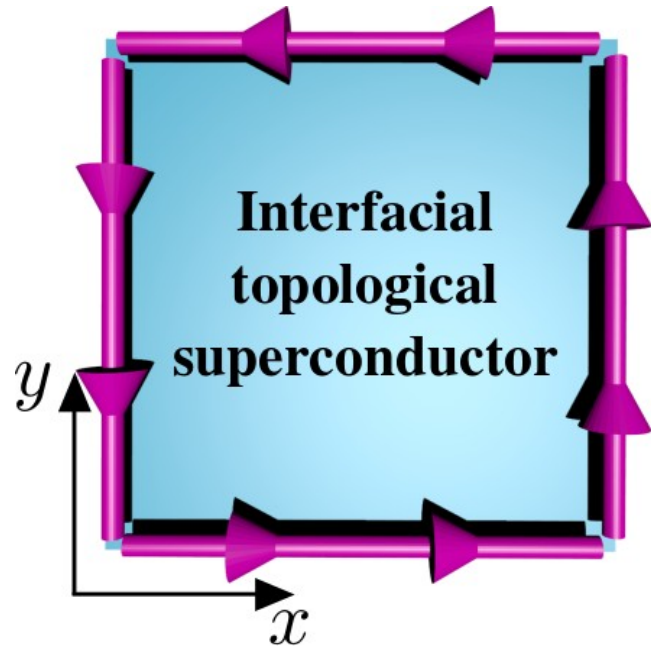


# Topological superconductivity with spin-orbit coupling



**Topological superconductivity showing gapless Majorana modes**

# Adding spin-orbit coupling



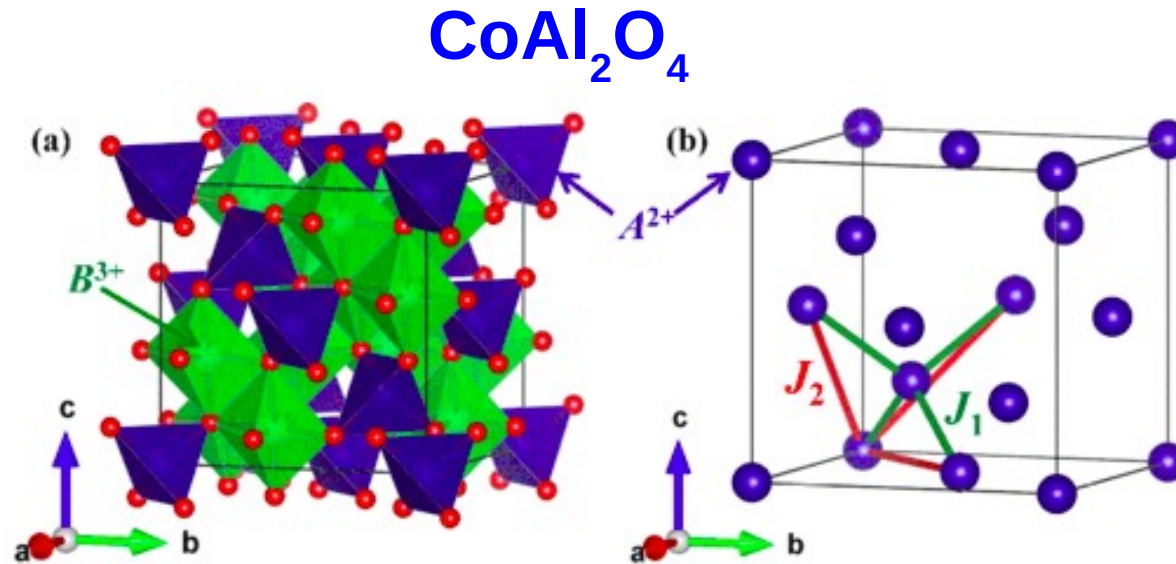
The interface realizes a topological superconductor



# 3D AF material candidates, spinels

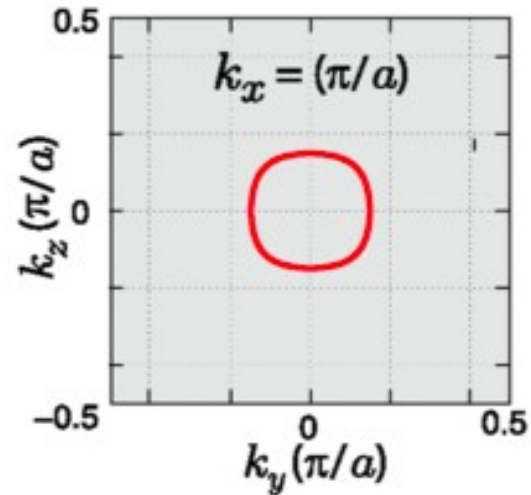
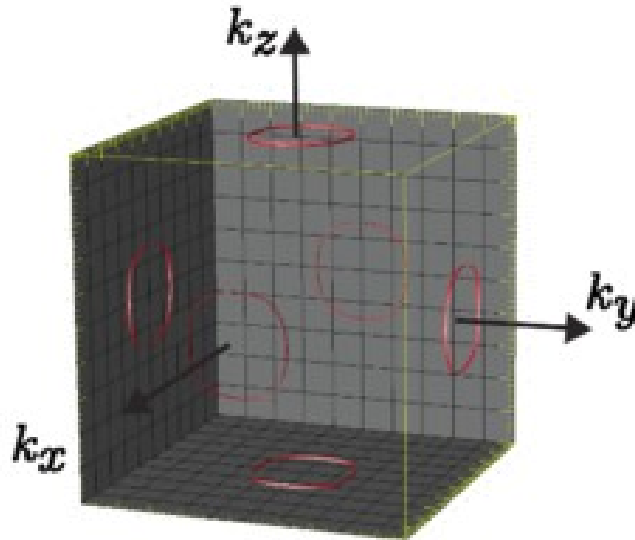
Antiferromagnet forming a diamond lattice

*Antiferromagnetic spinels*



# 3D AF material candidates, Dirac materials

Dirac lines in the absence of spin-orbit coupling and magnetism

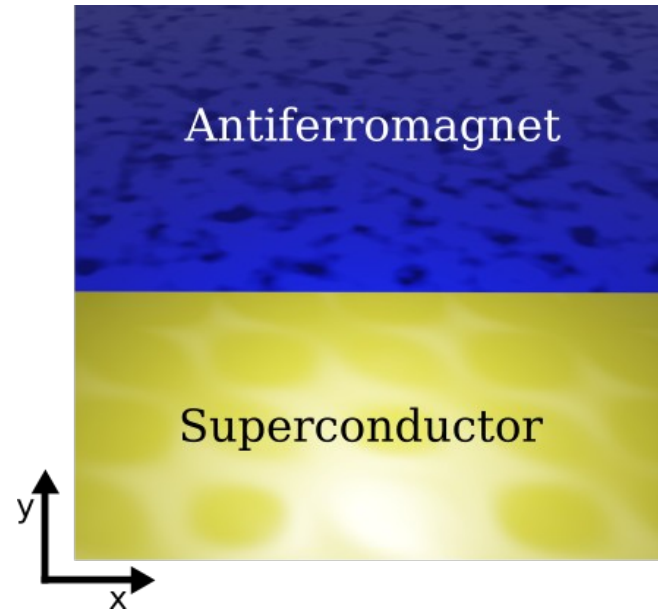


*Phys. Rev. Lett.* 115, 036806 (2015)

Antiferromagnets whose paramagnetic state hosts Dirac lines

**Interaction-induced  
1D topological  
superconductivity in 2D  
antiferromagnets**

# Topological superconductivity driven by interactions



We will focus on a heterostructure between a 2D superconductor and a 2D superconductor

$$\mathcal{H} = \mathcal{H}_{\text{kin}} + \mathcal{H}_{\text{AF}} + \mathcal{H}_{\text{SC}} + \mathcal{H}_{\text{int}}$$

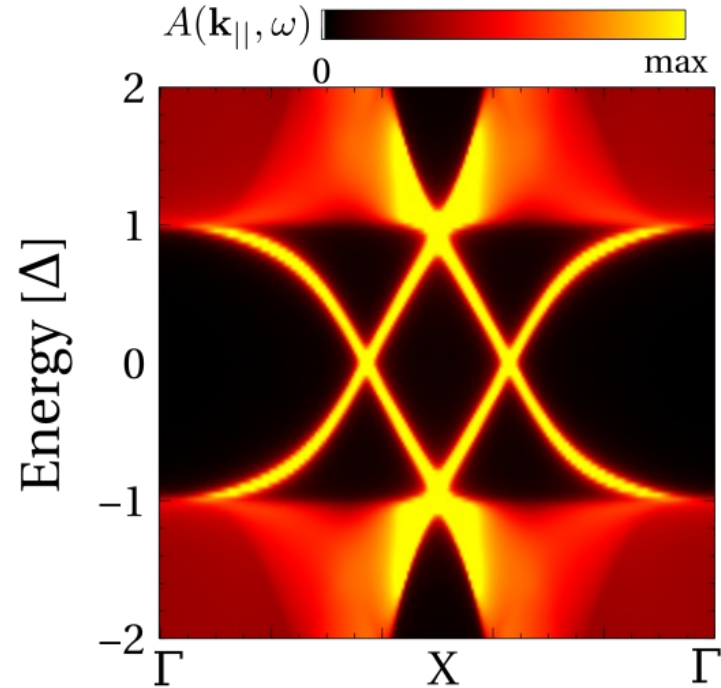
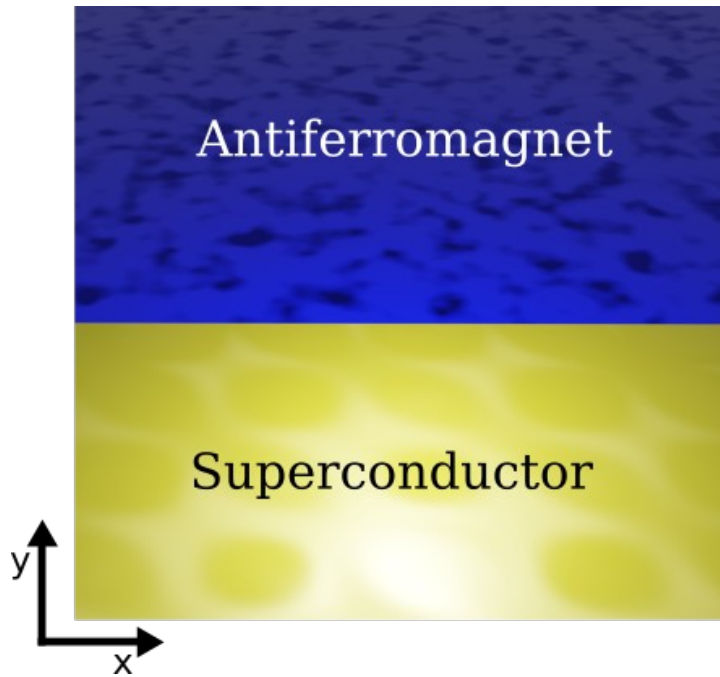
Kinetic energy                  Antiferromagnetism                  Repulsive interactions

Superconductivity

Can we get topological superconductivity just driven by repulsive electronic interactions?

# Interface AF-SC modes

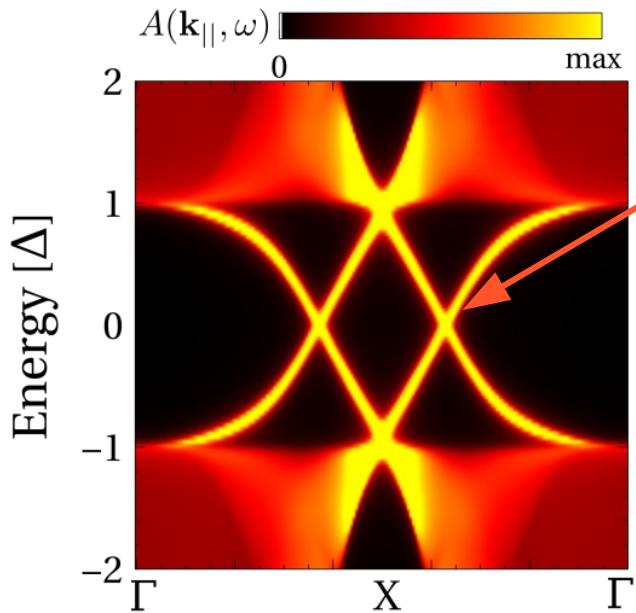
$$\mathcal{H} = \mathcal{H}_{\text{kin}} + \mathcal{H}_{\text{AF}} + \mathcal{H}_{\text{SC}}$$



Gapless zero modes appear at the one-dimensional AF-SC interface

# Interactions in the model

What happens when we now include interactions in whole system?



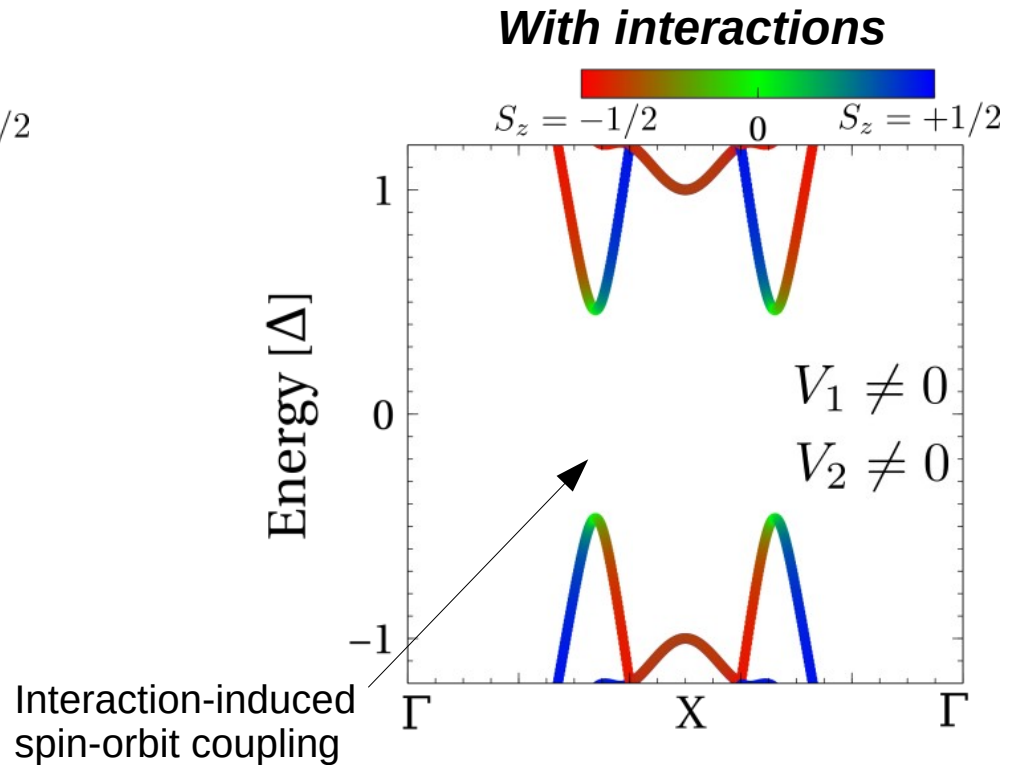
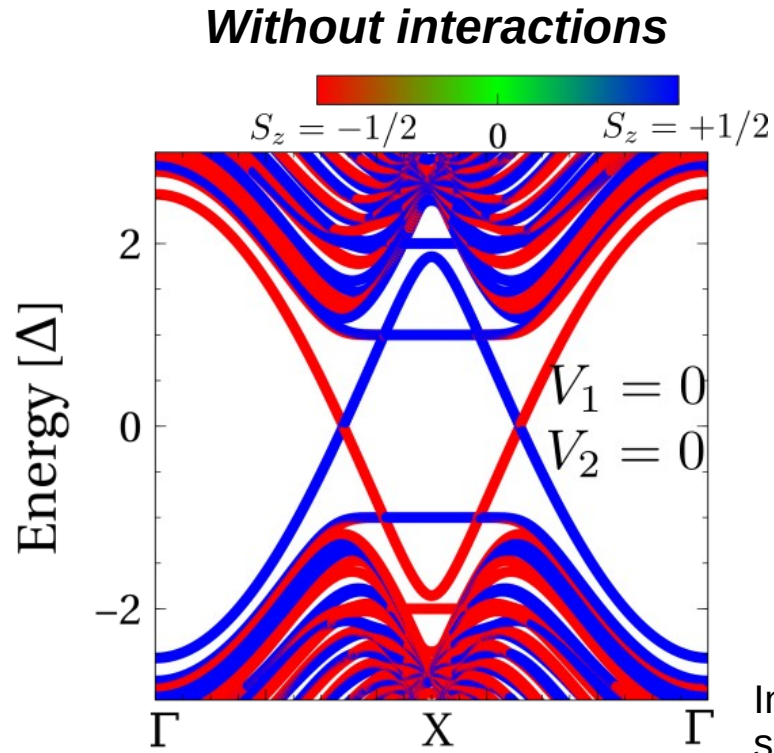
Could there be an interaction-induced gap opening of the interface modes?

$$\mathcal{H} = \mathcal{H}_{\text{kin}} + \mathcal{H}_{\text{AF}} + \mathcal{H}_{\text{SC}} + \mathcal{H}_{\text{int}}$$

*We will solve a model with repulsive long-range interactions at the mean-field level*



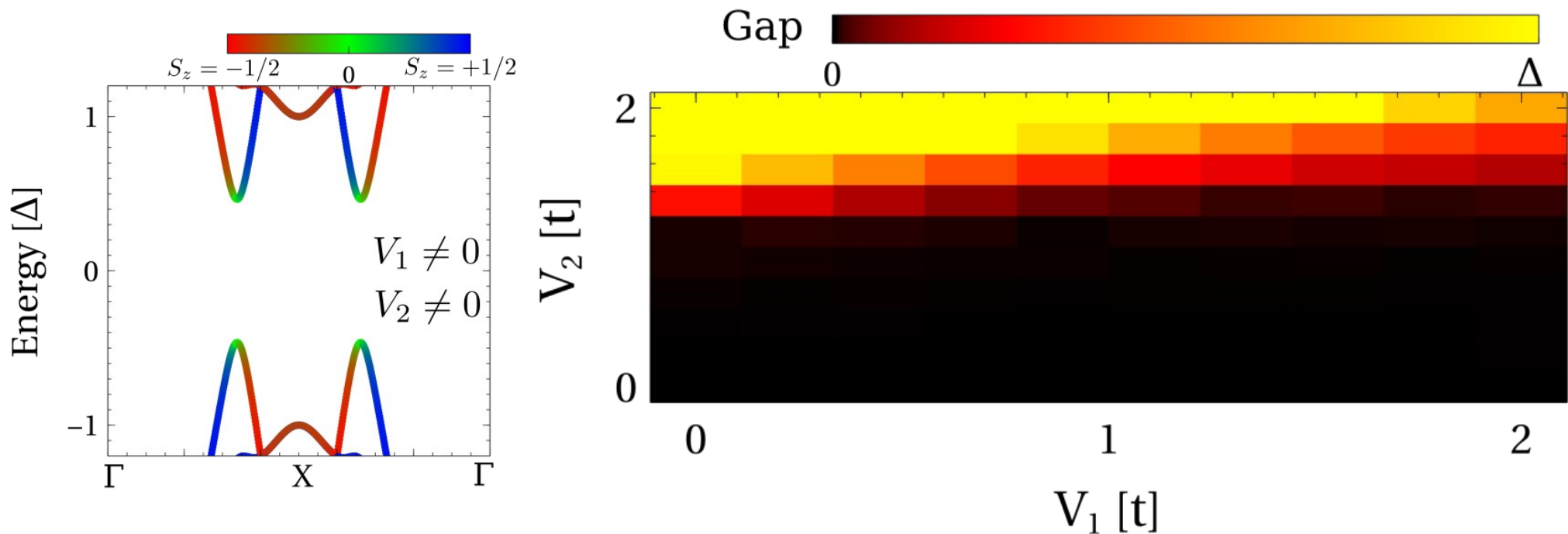
# Impact of interactions



Including repulsive interactions opens up a topological gap in the solitonic modes

# Interaction-induced gap VS interaction strength

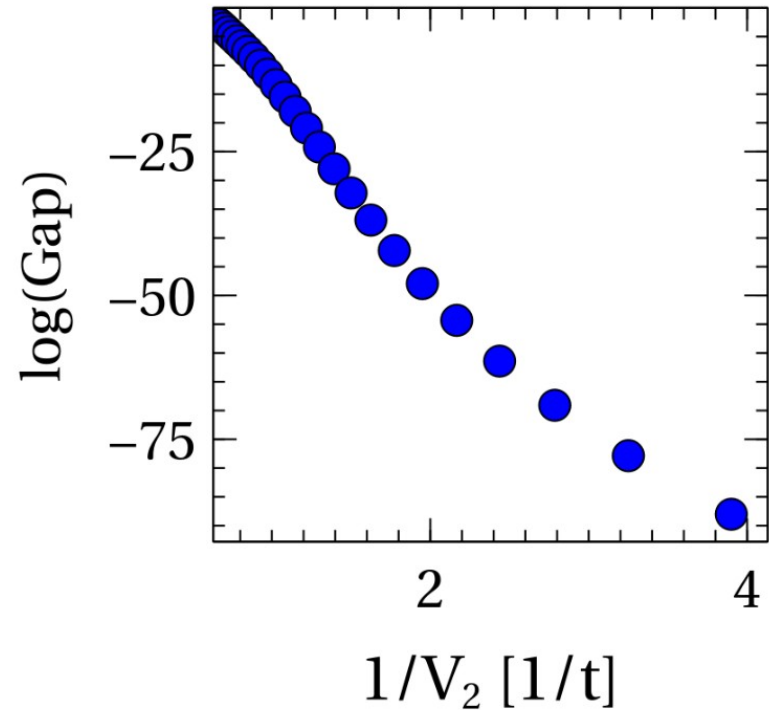
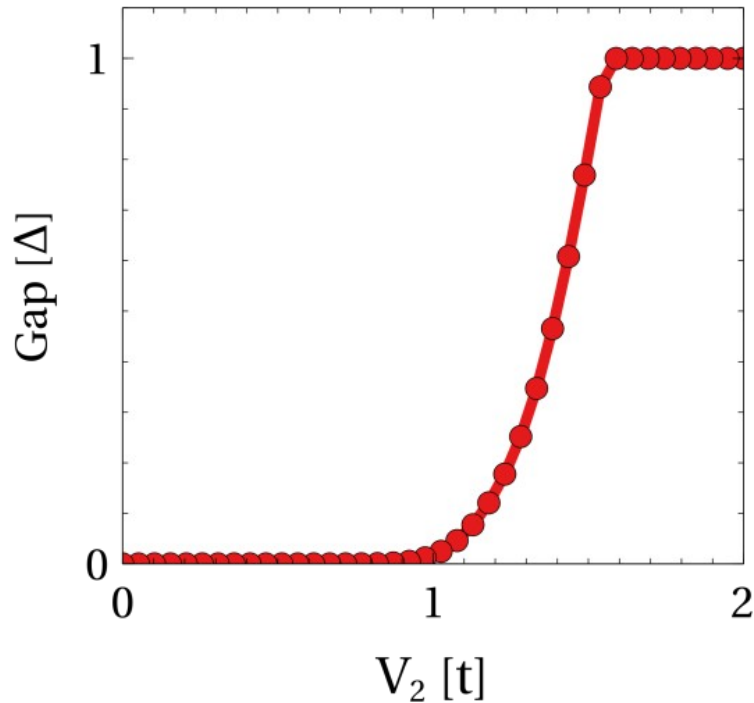
Dependence of the topological gap with respect to first and second neighbor interactions



The interaction-induced gap saturates to  $\Delta$ , the gap of the s-wave superconductor<sub>22</sub>

# Topological superconductivity without a critical interaction

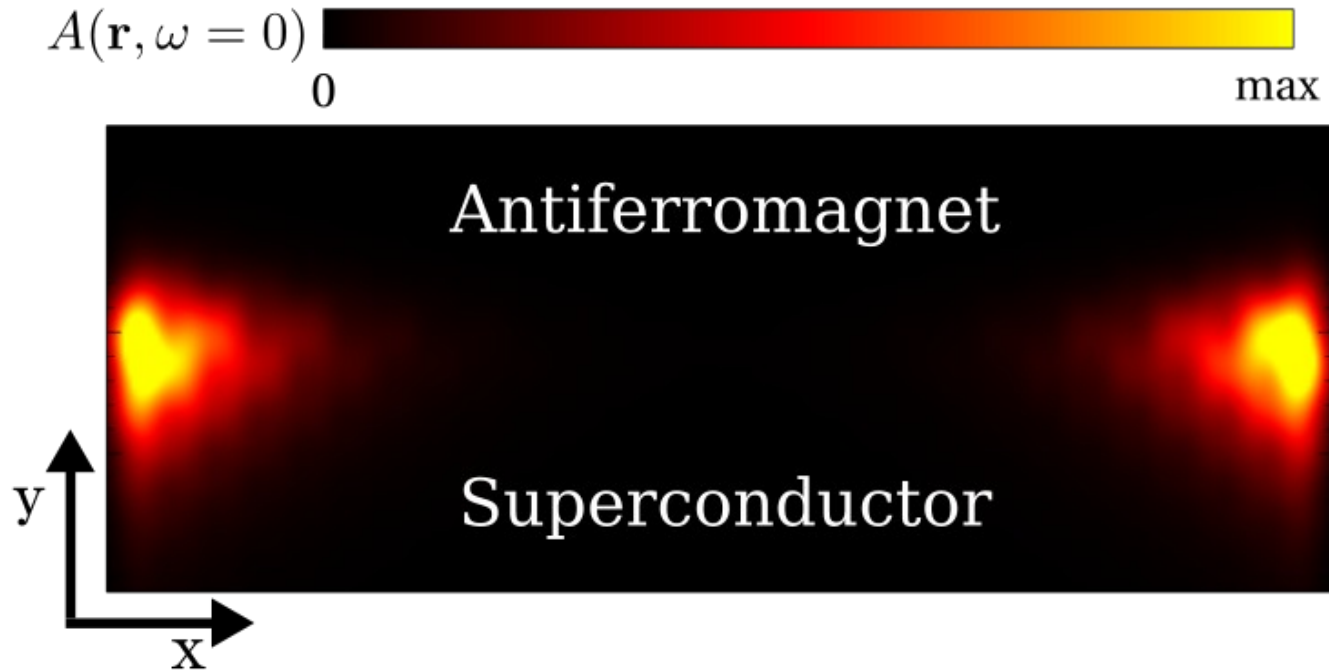
Topological gap VS interaction strength



A topological gap opens up for arbitrarily small interactions

# Majorana zero modes

Spectral function at zero energy, featuring Majorana edge modes



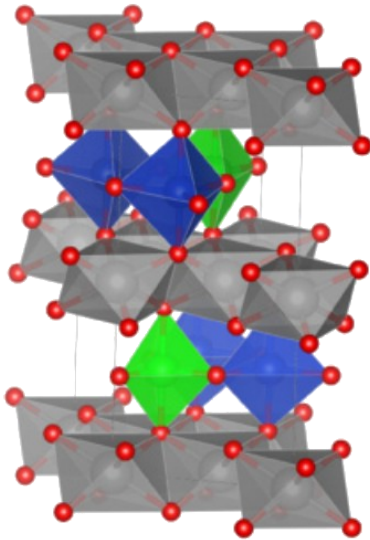
Majorana zero modes emerge at the edge due to electronic interactions

# AF material candidates

## Antiferromagnetic honeycomb oxides

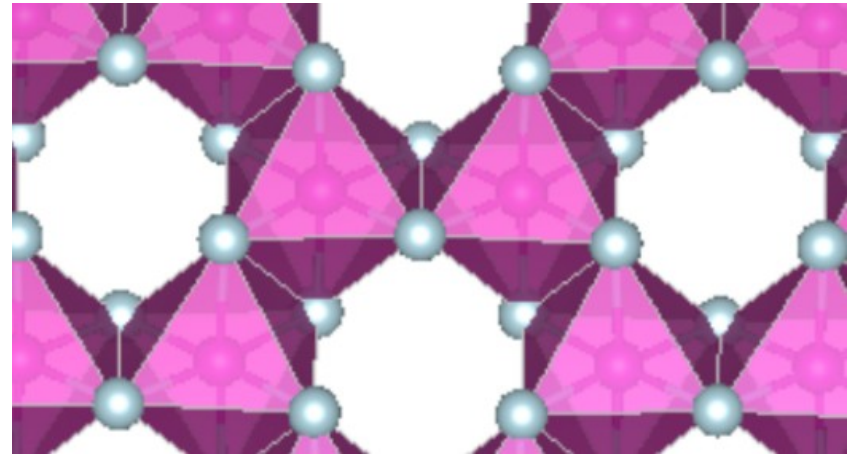
$\text{InCu}_{2/3}\text{V}_{1/3}\text{O}_3$  *Phys. Rev. B* 78, 024420 (2008)

$\beta\text{-Cu}_2\text{V}_2\text{O}_7$  *Phys. Rev. B* 82, 144416 (2010)



## 2D van der Waals materials (strained)

*Phys. Rev. B* 98, 144411 (2018)



# Many-body excitations in quantum antiferromagnet- superconductor junctions



# Diving into the quantum many-body regime

Stagger antiferromagnet (mean-field solution)

$$\mathcal{H} = \mathcal{H}_{\text{kin}} + \mathcal{H}_{\text{AF}} \quad |GS\rangle = |\uparrow\downarrow\rangle$$

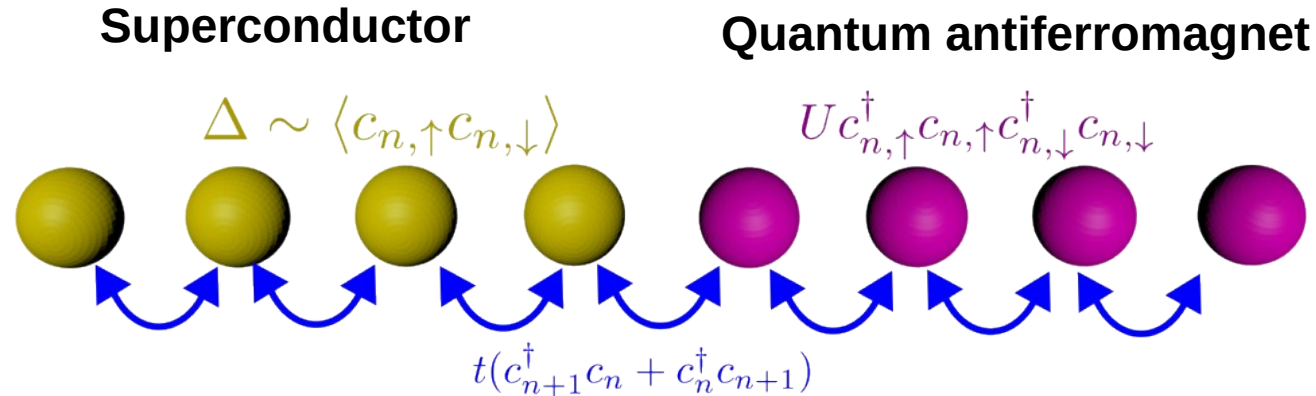
Quantum antiferromagnet (many-body solution)

$$\mathcal{H} = \mathcal{H}_{\text{kin}} + \mathcal{H}_{\text{U}} \quad |GS\rangle = |\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle$$

Hubbard interaction  $\mathcal{H}_{\text{U}} = \sum_n U c_{n,\uparrow}^\dagger c_{n,\uparrow} c_{n,\downarrow}^\dagger c_{n,\downarrow}$

What happens at interfaces between a quantum many-body 1D antiferromagnet and a superconductor?

# Superconductor-quantum antiferromagnet junction



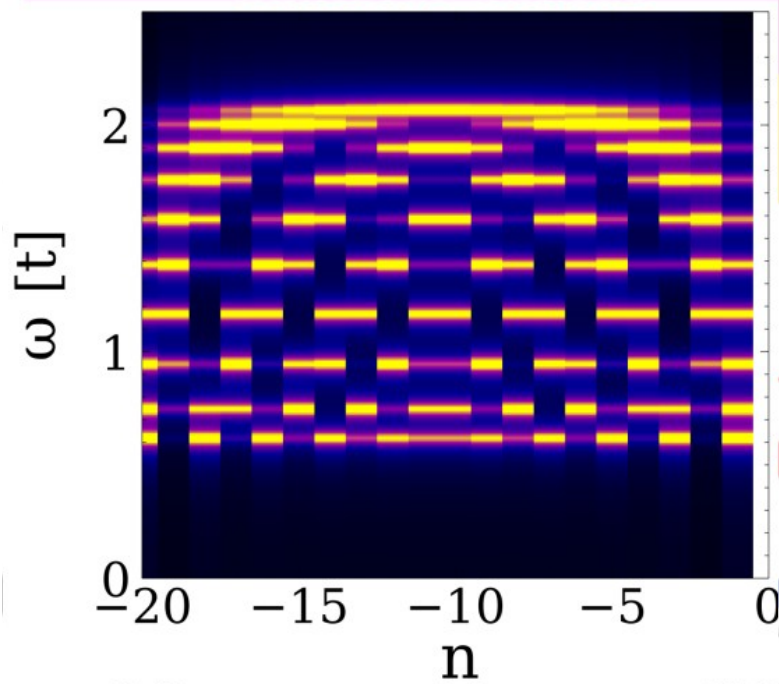
$$\mathcal{H} = \mathcal{H}_{\text{kin}} + \mathcal{H}_{\text{SC}} + \mathcal{H}_{\text{int}}$$

We will solve the interacting model exactly using the tensor network formalism

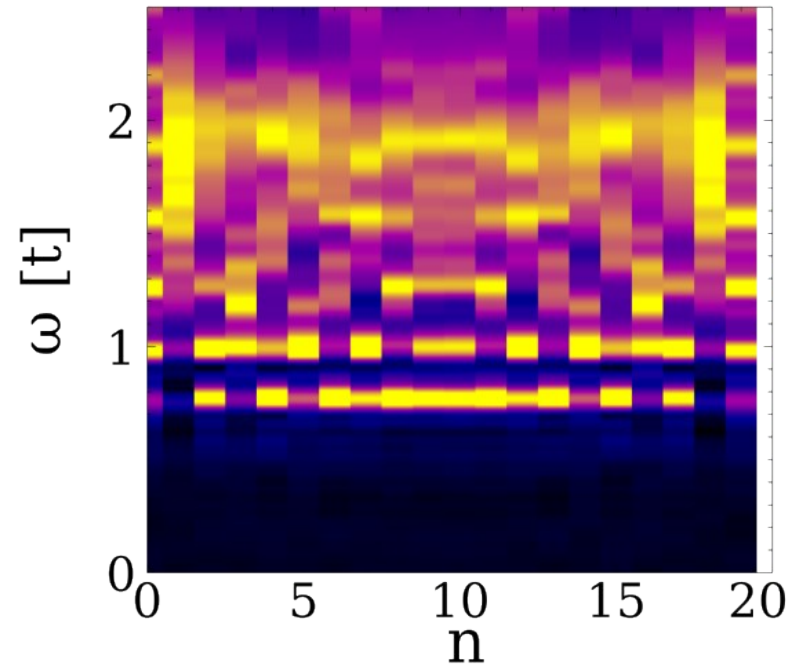
The ground state does not break time-reversal symmetry

# Many-body spectral function

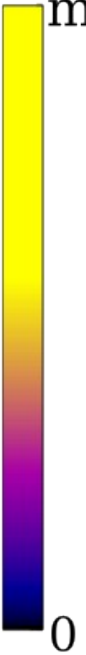
DOS in the superconductor



DOS in the quantum antiferromagnet



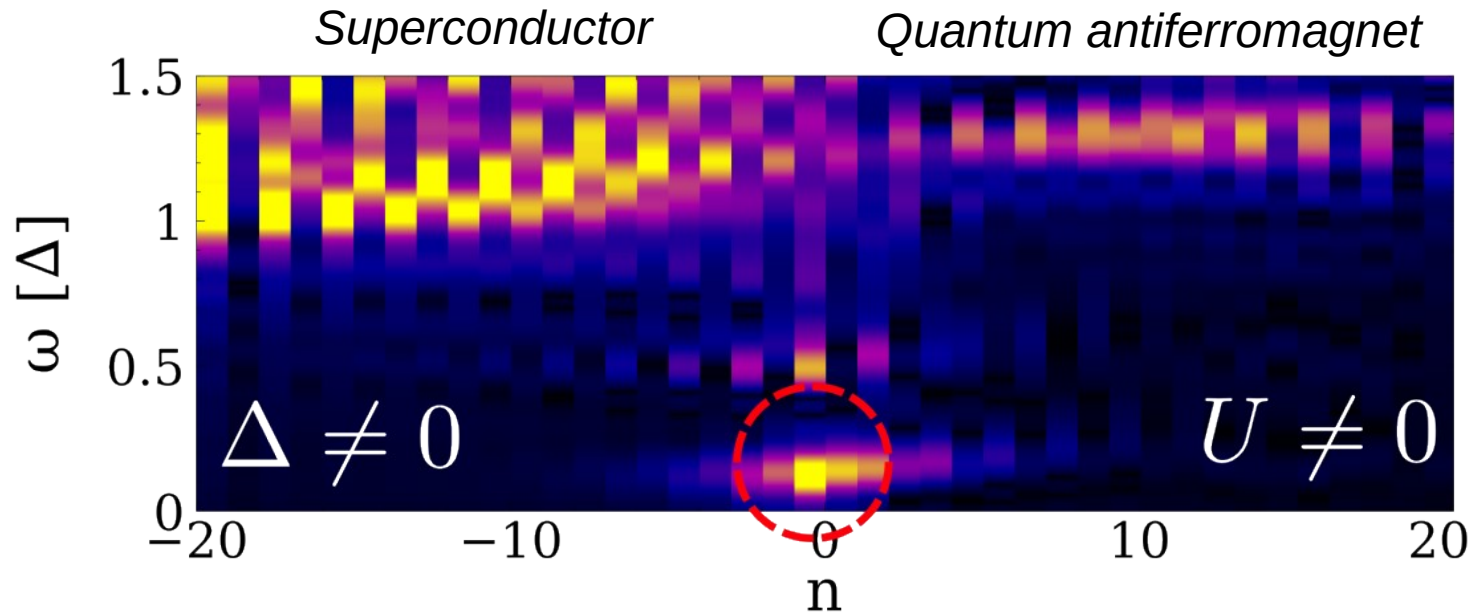
$A(\omega, n)$   
max



Both systems show an electronic gap when decoupled

# In-gap modes at the SC-quantum AF interface

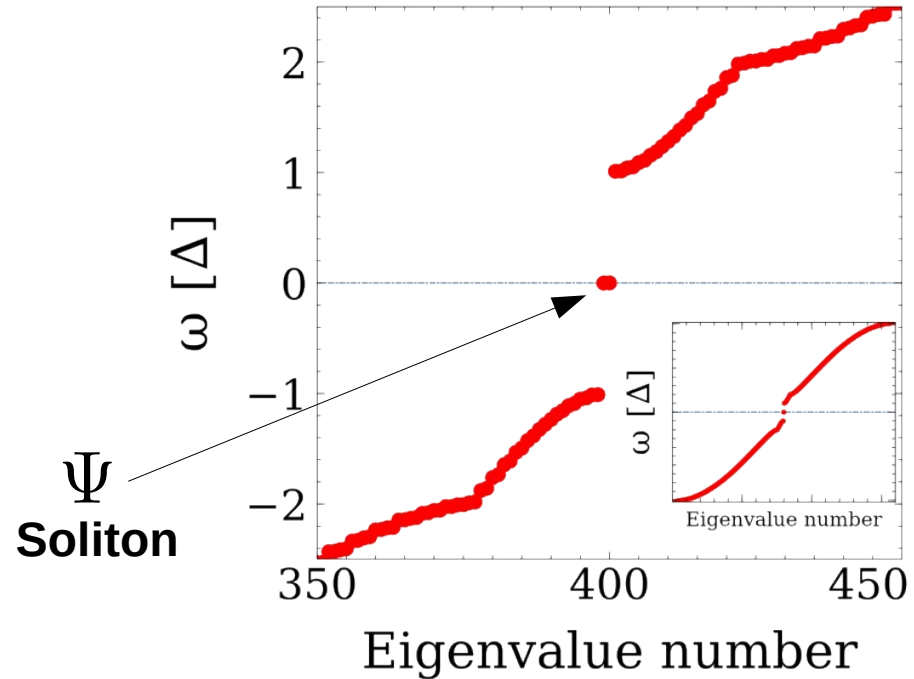
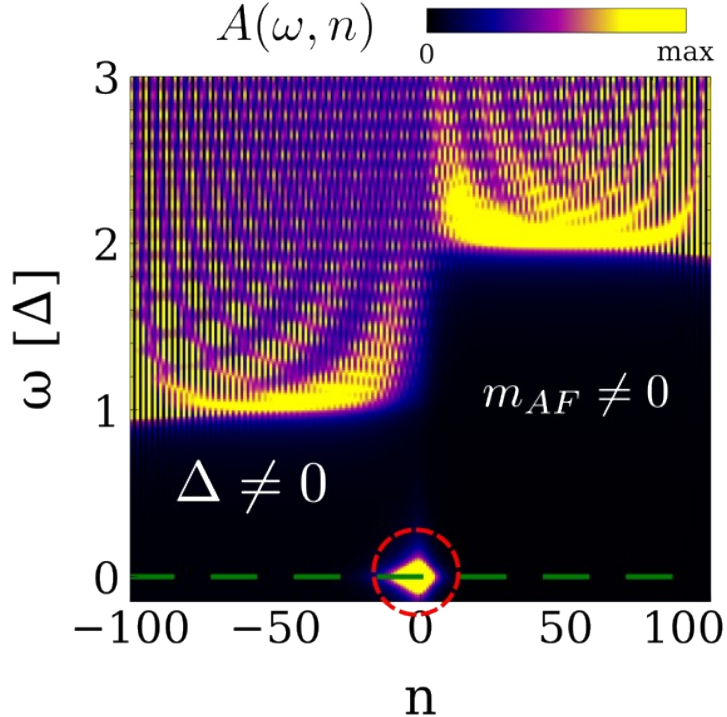
Superconductor-quantum antiferromagnet junction



**Solitonic in-gap modes appear between the superconductor and the quantum antiferromagnet**

# Back to single-particle solitonic zero modes

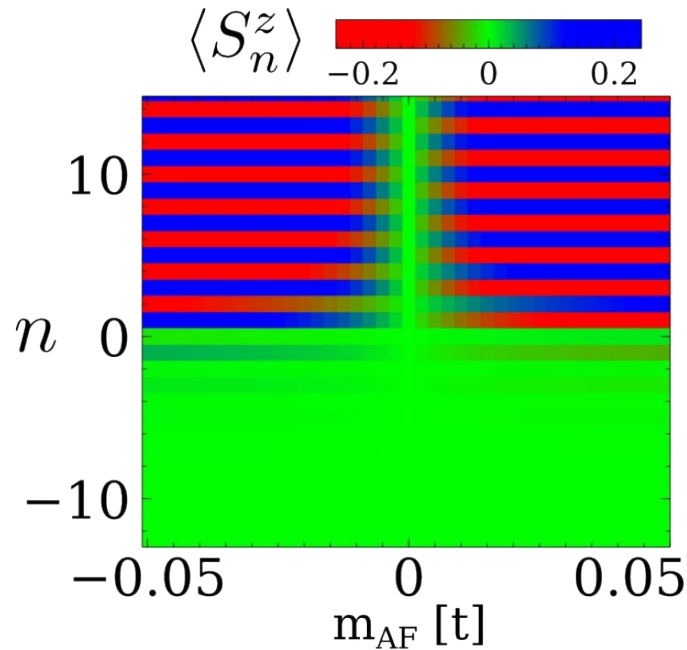
$\mathcal{H} = \mathcal{H}_{\text{kin}} + \mathcal{H}_{\text{SC}} + \mathcal{H}_{\text{AF}}$  Single particle limit (stagger magnetization and no interactions)



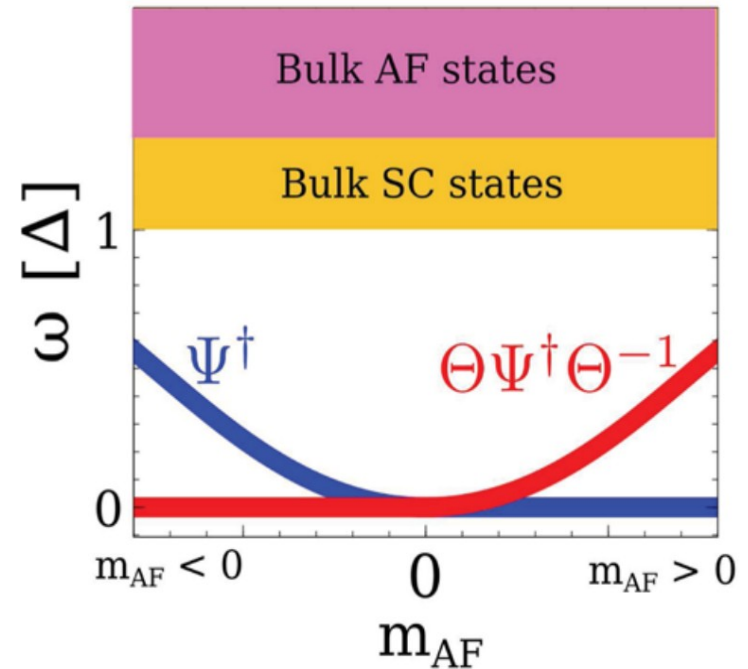
How are these modes connected to the many-body in-gap mode from before?

# From many-body to the single-particle symmetry broken state

$$\mathcal{H} = \mathcal{H}_{\text{kin}} + \mathcal{H}_{\text{SC}} + \mathcal{H}_{\text{AF}} + \mathcal{H}_{\text{int}}$$

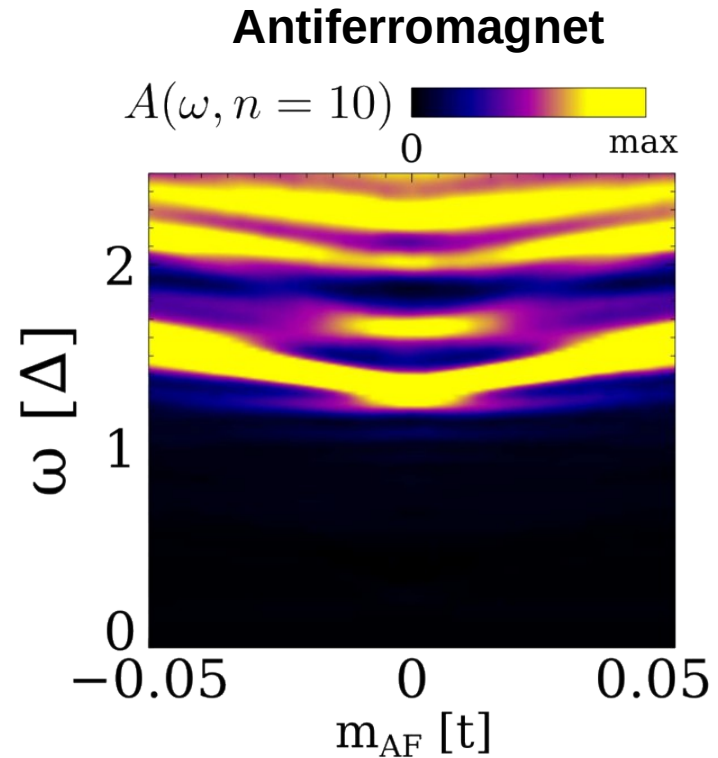
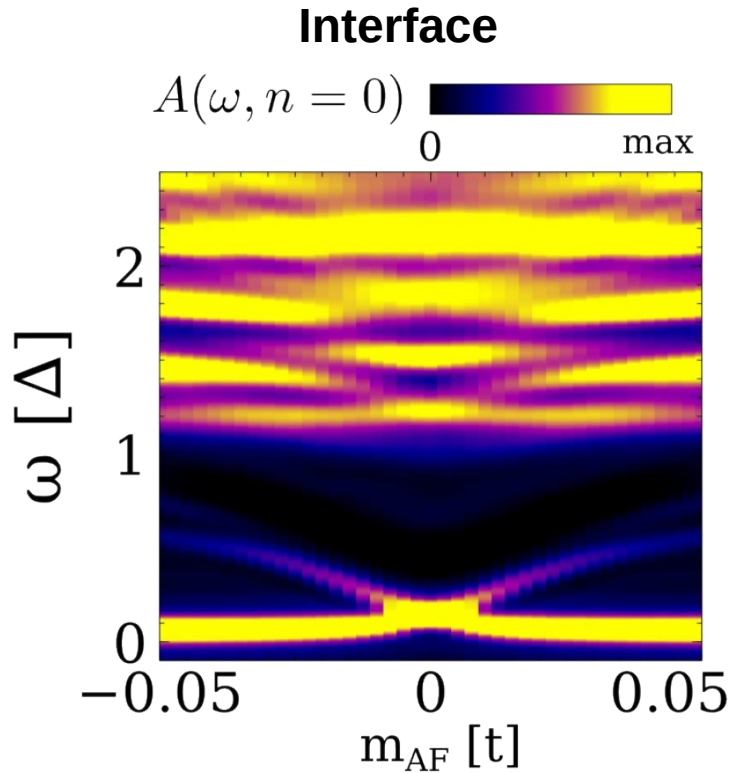


Sketch of the charge excitations



Switching on a magnetization pushes the interacting model to the symmetry broken state 32

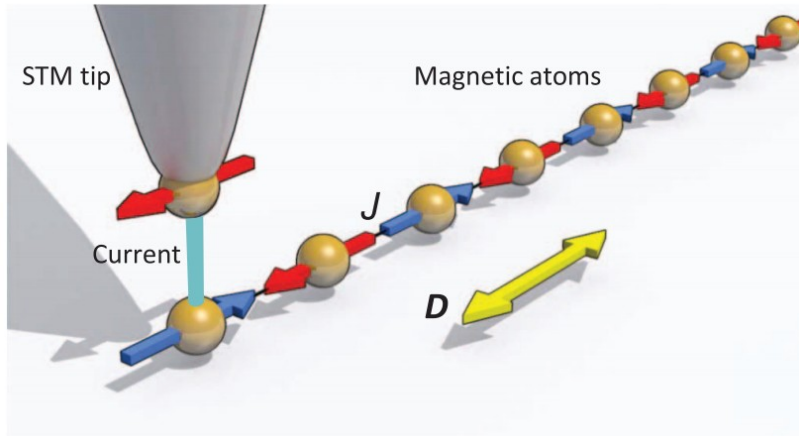
# From many-body to symmetry broken



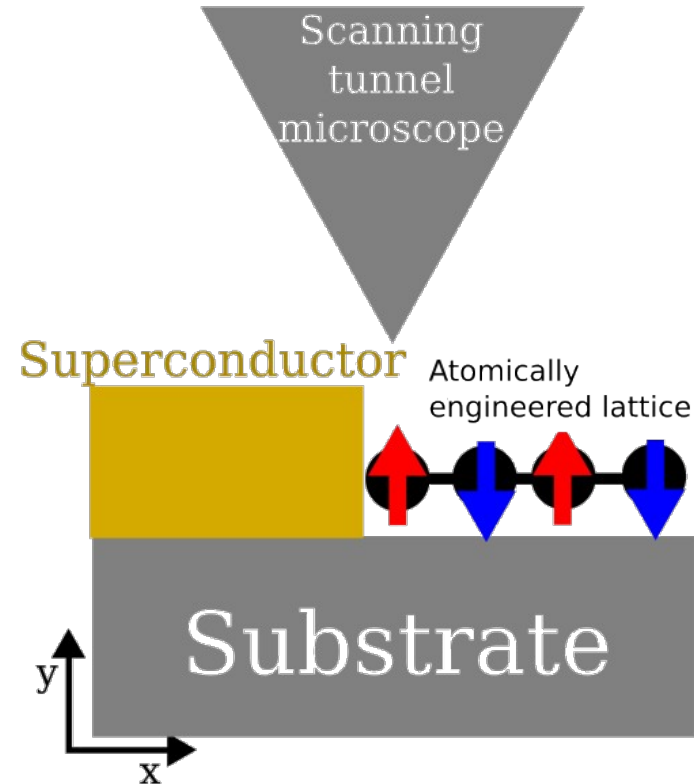
The solitonic single-particle mode transforms into the many-body in-gap mode 33



# Experimental realization with atomically engineered lattices

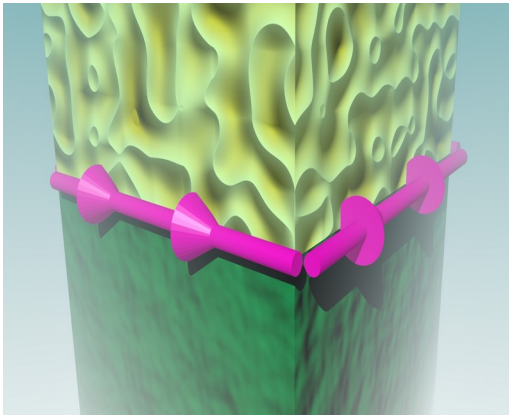


*Science* 335.6065 (2012): 196-199  
*Nature Physics* 12, 656–660 (2016)  
*Rev. Mod. Phys.* 91, 041001 (2019)

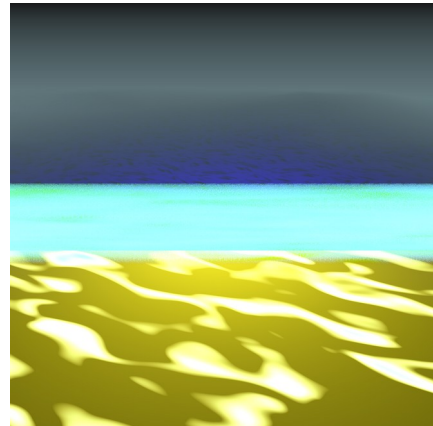


# Take home

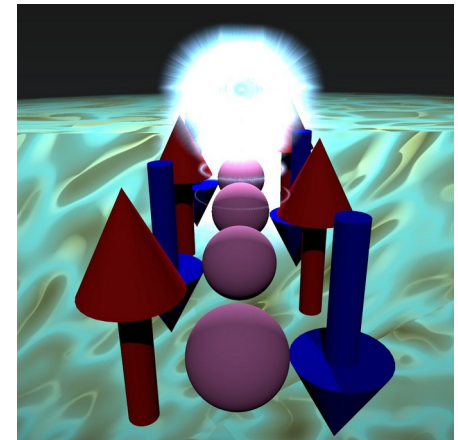
**Antiferromagnet-superconductor junctions provide a powerful platform to engineer solitons, unconventional superconductors and robust many-body excitations.**



Phys. Rev. Lett. 121, 037002 (2018)



arXiv:2011.06990 (2020)



Phys. Rev. Research 2, 023347 (2020)

# Thank you!