Center for Quantum Spintronics







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Noise







Noise





Current Fluctuations

$\mathbf{E} \left(\mathbf{e}_{c}(t_{2}) \right) = \mathbf{e}_{c}(t_{2}) \left(\mathbf{e}_{c}(t_{2}) \right)$

Thermal fluctuations in reservoirs. Equilibrium fluctuations

Johnson-Nyquist, fluctuation-dissipation theorem





$$\frac{\mathcal{F}_{c}(\omega \rightarrow 0)}{\mathcal{F}_{c}(\omega \rightarrow 0)} = \frac{\partial d^{2} t_{or}}{h} e^{V} \sum T_{n}(1 - T_{n})$$

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Determinism when and . No shot noise.

In general (Lesovik, Buttiker)



Shot Noise and Probability Distribution



Beenakker & Schonenberger, Physics Today (2003)



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Shot Noise and Fractional Charge



Beenakker & Schonenberger, Physics Today (2003)





Noise Driven by Magnetic Resonance







Ferromagnetic Resonance

• Spin-pumping



Silsbee, Janossy, Monod, Hurdequint, Berger





Spin-pumping

$$\mathbf{I}_{s} = \frac{\hbar}{4\pi} g_{\uparrow\downarrow} \mathbf{m} \times \frac{\partial \mathbf{m}}{\partial t}$$

Tserkovnyak, Brataas, Bauer PRL (2002)

 $\mathbf{m}(t) = \mathbf{x}\cos\omega t + \mathbf{y}\sin\omega t$

$$e\mathbf{I}_{s} = \mathbf{z} \left(\frac{\hbar}{2}\right) N_{\perp} \left(\frac{\hbar\omega}{e}\right)$$

Number of transverse waveguide modes







Spin Current Noise

• Isolated ferromagnet

$$\frac{\partial \mathbf{m}}{\partial t} = -\gamma \mathbf{m} \times \left[\mathbf{H}_{\text{eff}} + \mathbf{h}_0(t) \right] + \alpha_0 \mathbf{m} \times \frac{\partial \mathbf{m}}{\partial t}$$

- Ferromagnet in contact with normal metal
 - Spin-pumping enhanced Gilbert damping $\alpha_0 \rightarrow \alpha_0 + \alpha_{sp}$
 - Spin currents fluctuates
 - Spin-transfer torque fluctuates

 $h_0(t) \rightarrow h_0(t) + h_{sp}(t)$

$$h_{sp}(t) = ?$$





Thermal Noise

• Described by a new random field

$$\langle h_{\mathsf{sp},i}(t_1)h_{\mathsf{sp},j}(t_2)\rangle = 2k_BT\frac{\alpha_{\mathsf{sp}}}{\gamma M}\delta_{ij}\delta(t_1-t_2)$$

• Total effective fluctuating field

$$\mathbf{h}(t) = \mathbf{h}_0(t) + \mathbf{h}_{\mathsf{SP}}(t)$$

Enhanced Gilbert damping

$$\alpha = \alpha_0 + \alpha_{sp}$$

• Fluctuation-dissipation theorem is satisfied [PRL (2005)]



Current noise geometrically generated by a driven magnet

Tim Ludwig⁽¹⁾,^{1,2,3} Igor S. Burmistrov,^{3,4} Yuval Gefen,⁵ and Alexander Shnirman^{2,6}

A small metallic ferromagnet tunnel coupled to two normal metal leads





Spin Pumping and Torque Statistics in the Quantum Noise Limit

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(Received 29 September 2016; revised manuscript received 21 March 2017; published 8 June 2017)







Electric Current Noise

- Novel aspect of Ludwig et al.
 - Detects and characterises
 - Ferromagnetic resonance
 - Electron transport in magnetic nanostructure
 - Does not require spin-to-charge conversion such as
 - Spin Hall effect
 - Inverse spin Hall effect



This Work - Generalization in 3 Ways

- I. Arbitrary junctions
 - Ballistic
 - Diffusive
 - Tunnel
- II. Ferromagnets and antiferromagnets
- III. Multi-terminal devices

Noise Driven by Magnetic Resonance





Landauer formalism





Explanation of Electric Current Noise

- Temporal variation in
 - Spin-pumping
 - Spin accumulation
 - Spin filtering





Spin-transfer and spin-pumping

Spin-transfer

Ferromagnet **Normal Metal** Ferromagnet Normal Metal is magnon magnon

Spin-pumping





Spin to Charge Conversion



Spin accumulation in normal metal drives charge current via spin filtering

$$\begin{split} I_c &= I_{\uparrow} + I_{\downarrow} \\ I_c &= (G_{\uparrow} - G_{\downarrow}) \Delta \mu / 2 \end{split}$$





Experimental Consequences

• Low-temperature shot noise when

 $\hbar \omega > k_B T$

• Ferromagnets

 $\omega \sim 100 \text{GHz} \sim 1 K$

• Antiferromagnets

 $\omega \sim 1 \text{THz} \sim 10 K$

- Suppressed contributions also at higher temperatures
- Shot noise depends on drive, thermal noise does not





Current Noise

Current fluctuations

$$P_{\zeta\eta}(t_1, t_2) = \frac{1}{2} \langle \Delta I_{\zeta}(t_1) \Delta I_{\eta}(t_2) + \Delta I_{\eta}(t_2) \Delta I_{\zeta}(t_1) \rangle$$
 Labels lead

• Low-frequency noise

$$p_{\zeta\eta} = \int_0^T \frac{dt}{T} \int_{-\infty}^\infty d\tau P_{\zeta\eta}(t + \tau/2, t - \tau/2)$$

• Two contributions, thermal noise (th) and shot noise (sn)

$$p_{\zeta\eta} = p_{\zeta\eta}^{(\mathsf{th})} + p_{\zeta\eta}^{(\mathsf{sn})}$$





Johnson-Nyquist Noise

• Thermal noise contribution

$$p_{\zeta\eta}^{(\mathsf{th})} = (G_{\zeta\eta} + G_{\eta\zeta})k_B T$$

Conductance matrices

$$G_{\zeta\eta} = \frac{e^2}{h} \operatorname{Tr}_{\mathsf{O}} \left[\delta_{\zeta\eta} - S_{\eta\zeta}^{\uparrow\dagger} S_{\zeta\eta}^{\uparrow} \right] + \frac{e^2}{h} \operatorname{Tr}_{\mathsf{O}} \left[\delta_{\zeta\eta} - S_{\eta\zeta}^{\downarrow\dagger} S_{\zeta\eta}^{\downarrow} \right]$$

scattering matrices for spin-up and spin-down electrons

• Two-terminals, single mode

$$G = \frac{e^2}{h} \left(T^{\uparrow} + T^{\downarrow} \right)$$











• Main new result

$$p_{\zeta\eta}^{(\mathsf{Sn})} = \frac{A_{\zeta\eta} + A_{\eta\zeta}}{8} \left[\hbar\omega \coth \frac{\hbar\omega}{2k_BT} - 2k_BT \right] D(\omega)$$

• Shot noise coefficients

$$A_{\zeta\eta} = \frac{e^2}{h} \operatorname{Tr}_{\mathsf{O}} \left[\delta_{\zeta\eta} - \sum_{\alpha\beta} S^{\uparrow}_{\zeta\alpha} S^{\downarrow\dagger}_{\alpha\eta} S^{\downarrow\dagger}_{\eta\beta} S^{\uparrow\dagger}_{\beta\zeta} \right] + \frac{e^2}{h} \operatorname{Tr}_{\mathsf{O}} \left[\delta_{\zeta\eta} - \sum_{\alpha\beta} S^{\downarrow}_{\zeta\alpha} S^{\uparrow\dagger}_{\alpha\eta} S^{\uparrow}_{\eta\beta} S^{\downarrow\dagger}_{\beta\zeta} \right]$$

• Spin-dynamics factor

$$D(\omega) = \sum_{i} n_{i+} n_{i-} = \sum_{ijk} \chi_{ij+} \chi_{ik-} H_{j+} H_{k-}.$$

out-of-equilibrium deviation of order parameter





• Low-temperature

$$p_{\zeta\eta}^{(\mathrm{Sn})} \approx \frac{A_{\zeta\eta} + A_{\eta\zeta}}{8} |\hbar\omega| D(\omega)$$

• High-temperature

$$p_{\zeta\eta}^{(\mathrm{Sn})} \approx \frac{A_{\zeta\eta} + A_{\eta\zeta}}{8} \frac{\left(\hbar\omega\right)^2}{6k_B T} D(\omega)$$



Spin-dynamics Factor - Ferromagnet



$$D_F(\omega = \omega_A) = \frac{\omega_{H_\perp}^2}{2\alpha^2 \omega_A^2}$$



Qu

Spin

Spin-dynamics Factor - Antiferromagnet



$$D_{AFM}(\omega = \omega_r) = \frac{\omega_{H_\perp}^2}{8\alpha^2 \omega_E^2}$$



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Shot Noise Coefficients

• Many-terminal expression

$$A_{\zeta\eta} = \frac{e^2}{h} \operatorname{Tr}_{\mathsf{O}} \left[\delta_{\zeta\eta} - \sum_{\alpha\beta} S_{\zeta\alpha}^{\uparrow} S_{\alpha\eta}^{\downarrow\dagger} S_{\beta\zeta}^{\uparrow\dagger} \right] + \frac{e^2}{h} \operatorname{Tr}_{\mathsf{O}} \left[\delta_{\zeta\eta} - \sum_{\alpha\beta} S_{\zeta\alpha}^{\downarrow} S_{\alpha\eta}^{\uparrow\dagger} S_{\beta\zeta}^{\uparrow\dagger} \right]$$

• Two-terminal expression

$$A_{ll} = \frac{2e^2}{h} \operatorname{Tr}_{\mathbf{O}} \left[1 - (r_{ll}^{\uparrow} r_{ll}^{\downarrow\dagger} + t_{ll}^{\uparrow} t_{rl}^{\downarrow\dagger}) (r_{ll}^{\downarrow} r_{ll}^{\uparrow\dagger} + t_{ll}^{\downarrow} t_{rl}^{\uparrow\dagger}) \right]$$





Shot Noise Coefficients

• Ballistic junctions

$$A_{ll}^{(F)} = \frac{2e^2}{h} PN \qquad P = \frac{G_{\uparrow} - G_{\downarrow}}{G_{\uparrow} + G_{\downarrow}} \qquad \qquad A_{ll}^{(AF)} = 0$$

• Disordered junctions

$$\langle A_{ll}^{(F)} \rangle = 2 \left(G_{\uparrow} + G_{\downarrow} - 2 \frac{G_{\uparrow} G_{\downarrow}}{G_{sh}} \right) \qquad \qquad \langle A_{ll}^{(AF)} \rangle = 2G \left(1 - \frac{G}{2G_{sh}} \right)$$

 $\langle A_{ll}^{(F)}\rangle\approx \langle A_{ll}^{(AF)}\rangle\approx 2G$



Conclusion

- General expression noise driven by magnetic resonance
- Characterizes and detects
 - Magnetic resonance
 - Electron transport
- Thermal and shot noise contributions
- Shot noise attains its maximum at magnetic resonance
- Shot noise coefficients differ for various junctions
- Brataas, PRB 102, 054440 (2020)









