### Long-Range Phonon Spin Transport

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Phys. Rev. B 101, 104402 (2020); Phys. Rev. Lett. 124, 117201 (2020)

#### **Long-term motivation**



See e.g. Sonin (2010)

## Non-local spin transport in metals/semi-conductors





electron spin accumulation:  $\mu_s \propto e^{-x/\ell_s}$ 

non-local resistance: 
$$R_{
m NL}\sim rac{V_{
m NL}}{I_{
m INJ}}\propto e^{-L/\ell_s}$$

spin-diffusion length:  $\ell_s \sim \mathrm{nm} - \mu \mathrm{m}$ 

From Wei Han et al., JMMM **324**, 369 (2012)

Cornelissen, ..., RD, et al., Nature Physics 11, 1022 (2015); for AFMs: Lebrun, ..., RD, et al., Nature 561, 222 (2018)

### Non-local spin transport though magnetic insulators



magnon spin accumulation:  $\mu_m \propto e^{-x/\ell_m}$ 

non-local resistance:  $R_{\rm NL} \sim V/I \propto e^{-L/\ell_m}$ 

magnon spin diffusion length:  $\ell_m \sim 10~\mu{\rm m}~$  YIG @ room T

#### **General view**



- Electrons (100's nm)
- Magnons (10's μm)
- This talk: phonons (mm's)



### Collaborators



#### Andreas Rueckriegel (Utrecht -> Frankfurt) Simon Streib (Uppsala) Gerrit Bauer (Sendai, Groningen)



Andreas









European Research Council

Phonon spin

 Role of phonons in Einstein-de Haaslike effects

Phonon spin

 Role of phonons in Einstein-de Haaslike effects

## Circularly-polarized phonons carry spin angular momentum

#### PHONON SPIN

S. V. Vonsovskii and M. S Svirskii

Institute of Metal Physics, Academy of Sciences, USSR, Sverdlovsk; Chelyabinsk Pedagogical Institute Translated from Fizika Tverdogo Tela, Vol. 3, No. 7, pp. 2160-2165, July, 1961 Original article submitted March 18, 1961



Vonsovskii, Svirskii (1962), Levine (1962); Zhang, Niu (2014); Picture above: Garanin, Chudnovsky (2015), Nakane, Kohno (2018), Streib, Keshtgar, Bauer (2018), Juraschek, Spaldin (2019).

## Experimental detection phonon spin (I)



dispersion relation:



Holanda et al, Nat. Phys (2018)

## Experimental detection phonon spin (II)

#### set-up:

#### magnon-phonon conversion:





- d С 5 x = 0.25 Lx = 0x = 0.5 Lf (GHz) f(GHz) f (GHz) m 3 3 2 L 10<sup>1</sup> 10<sup>3</sup> 10<sup>4</sup>  $10^{3}$ 10<sup>2</sup> 10<sup>3</sup>  $10^{2}$ 10<sup>5</sup> 10<sup>1</sup>  $10^{2}$ 10<sup>4</sup> 10<sup>5</sup> 10<sup>1</sup> 10<sup>4</sup> 10<sup>5</sup> k (cm<sup>-1</sup>)  $k \,({\rm cm}^{-1})$ k (cm<sup>-1</sup> 0.8 f H (kOe) 0.  $H_0 = 0.240 \text{ kOe}$ 0.4 0.2 └ 0.0 0.2 0.4 0.6 0.8 1.0 x/L<sub>x</sub>
- Excitation of magnon (spin  $\approx \hbar$  ) Conversion to phonon Measurement of phonon polarization

Holanda et al, Nat. Phys (2018)

Phonon spin

 Role of phonons in Einstein-de Haaslike effects

- Phonon spin
- Role of phonons in Einstein-de Haaslike effects

Einstein, de Haas (1915); picture from Matsuo et al. (2015); modern experiments: detection of compensation point via Barnett effect & spin Seebeck mechanical force (Saitoh group, 2019); classical theory: Assmann/Novak (2019); see also Mentink et al. (2019).

#### **Einstein-de Haas effect**



conservation of energy:  $\mu_0 M_s BV \gg \Omega^2/I$  because  $I \propto V^{5/3}$  $\longrightarrow$  Need reservoir = phonons & their spin!  $\Omega \propto V^{-2/3}$ 

### Microscopic theory of Einstein-de Haas-like effects

- Starting point: rotation-invariant Hamiltonian for magnetic insulator
- Split mechanical motion into global rotation & translation + phonons
- Coupled Heisenberg equations for spins, lattice and global rotations
- Approximate as quantum-kinetic theory for magnons and phonons, coupled to magnetization dynamics and global rotation
- Solve by making ansatz in terms of phonon temperature & drift velocity: magnon temperature and chemical potential:

 $\begin{array}{c} \delta T_{\perp}(t), \delta T_{\parallel}(t), v(t) \\ \delta T_{m}(t), \mu(t) \end{array}$ 

• From this, compute change in spin density, phonon spin density and global rotation:  $\delta s(t), \delta l(t), \Omega^{z}(t)$  Phys. Rev. B 101, 104402 (2020)

### **Results (I)**



- Initial condition: heating due to laser pulse, angular momentum conserved
- Magnons and longitudinal phonons equilibrate first
- Phonon spin and global rotation compensate for decrease in magnetization

See Schneider et al., Nature Nano. (2020), for a similar scenario to achieve BEC

### **Results (II)**



- Initial condition: parallel pumping, angular momentum conserved
- Magnons and longitudinal phonons equilibrate first
- Phonon spin and global rotation result due to equilibration with magnons
- Phonon spin large, global rotation changes sign

### **Results (III)**



- Initial condition: (optical) spin injection into phonons
- Magnons and longitudinal phonons equilibrate first
- Magnon spin hardly changes, phonons and global rotation dominate

- Phonon spin
- Role of phonons in Einstein-de Haaslike effects

#### Phonon spin

 Role of phonons in Einstein-de Haaslike effects – conclusion: phonons & their spin important, but what can we do with them?

Phonon spin

 Role of phonons in Einstein-de Haaslike effects – conclusion: phonons & their spin important, but what can we do with them?





- Incoherently driven magnetic reservoirs
- Non-magnetic insulator
- Spin transfer due to magnetoelastic interactions
- Theorical approach: coupled stochastic equations for magnetic and lattice dynamics

## Spin-conductance & resonance condition



for small bias:

$$I_{L \to R} = \sigma(\mu_R - \mu_L)$$

resonance condition

 $L/(\tilde{\lambda}/2) + 2d/(\lambda/2) = \text{integer}$ 



- YIG and GGG parameters
- Decay length ~ 1 mm

## Phonon spin accumulation & spin current



- Same order of magnitude as spin density related to magnetization
- (Quasi-)equilibrium phonon spin accumulation and phonon spin currents

## Experiments in coherent regime



#### FMR experiment, coherent coupling

An et al. Phys. Rev. B (2020), motivated by Streib et al. (2018)

### Conclusion



- Electrons (100's nm); limited by spin-orbit and disorder
- Magnons (10's μm); limited by magnetic quality
- This talk: phonons (mm's); limited by acoustic quality
  Experiments?!

#### **Long-term motivation**



# Superfluid transport of angular momentum without magnetization



Sonin (2010)

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  Experiments?!