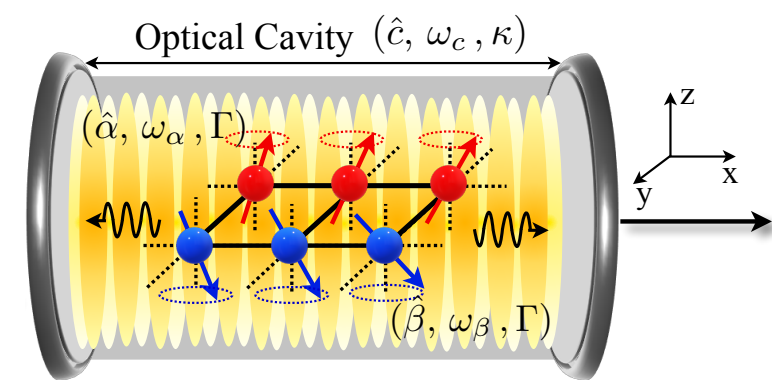
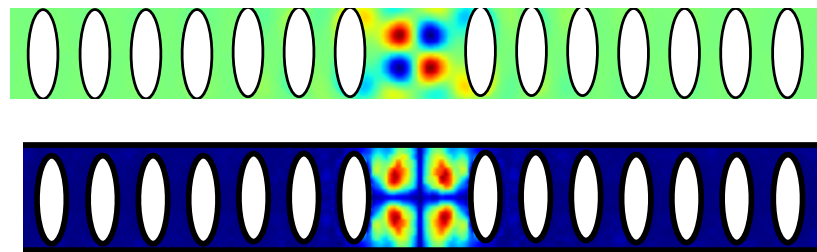
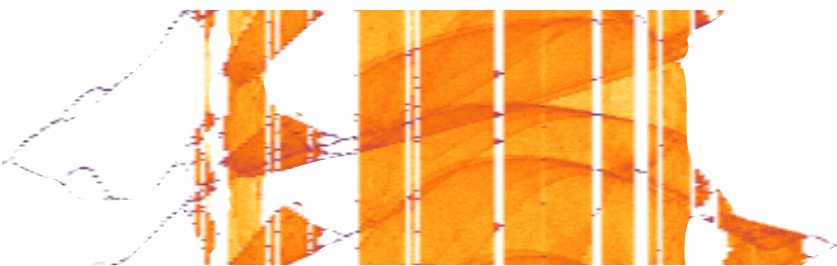


Cavity Optomagnonics



Silvia Viola Kusminskiy

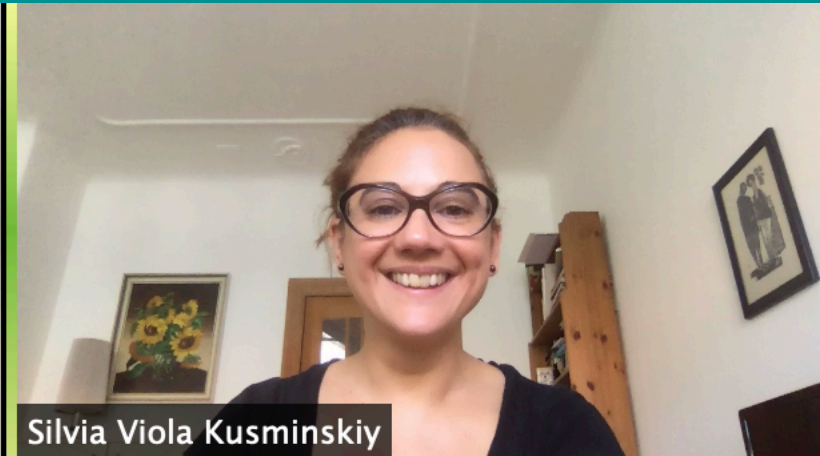
Max Planck Research Group



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Erlangen, Germany

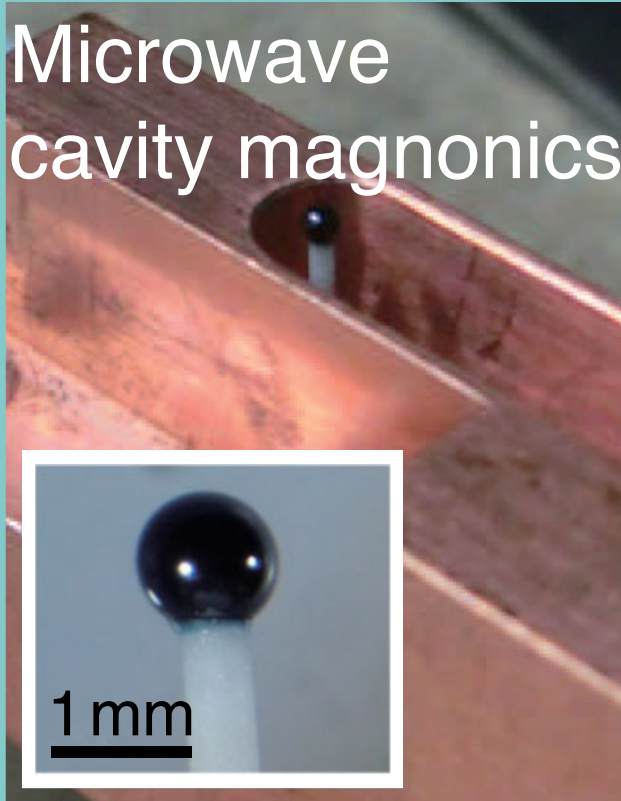
Theory of hybrid quantum systems



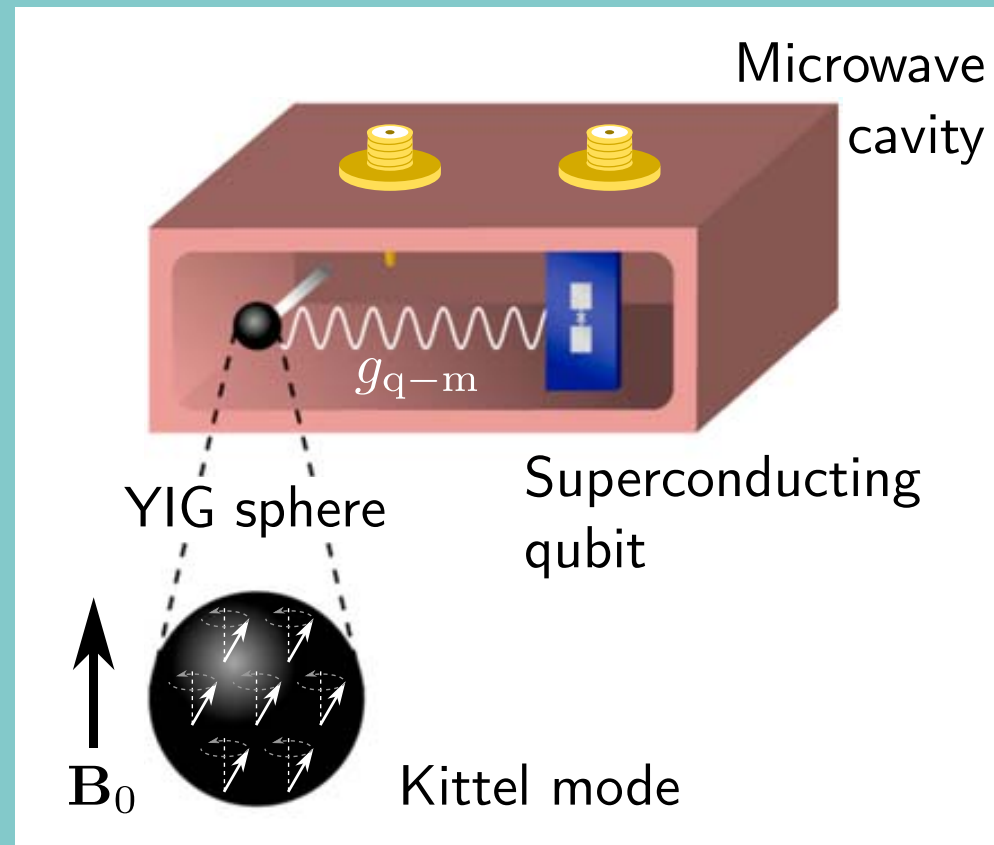
tparvin

Hybrid quantum systems based on magnetic elements

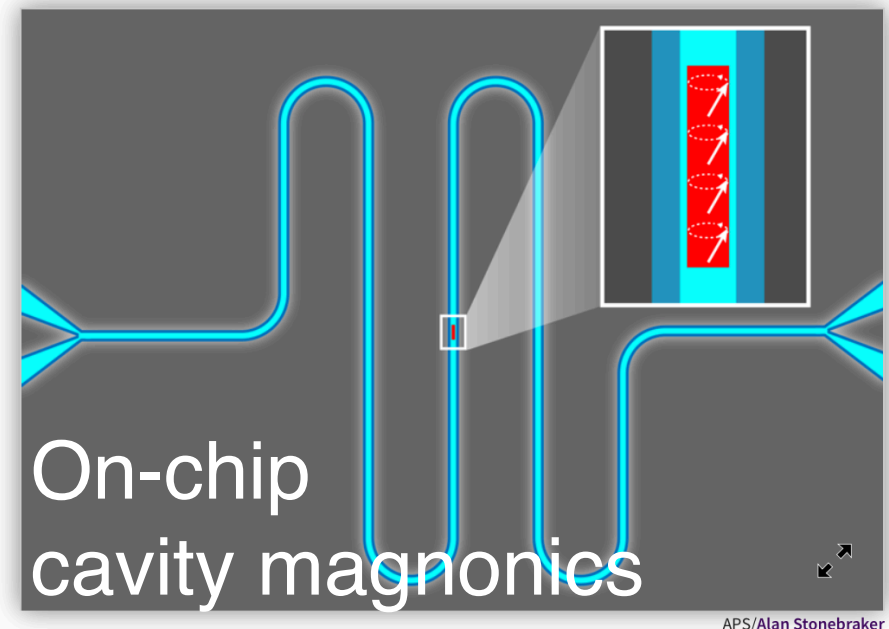
Microwave cavity magnonics



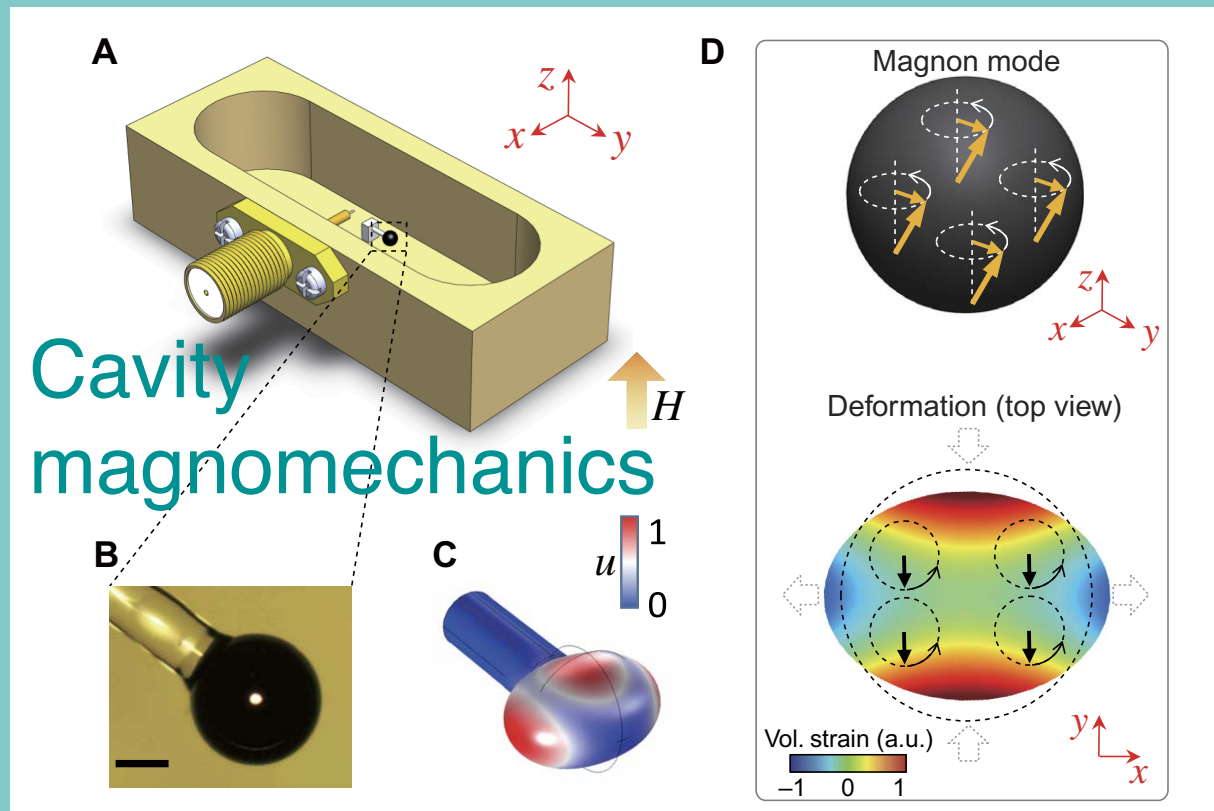
Tabuchi et. al PRL 2014



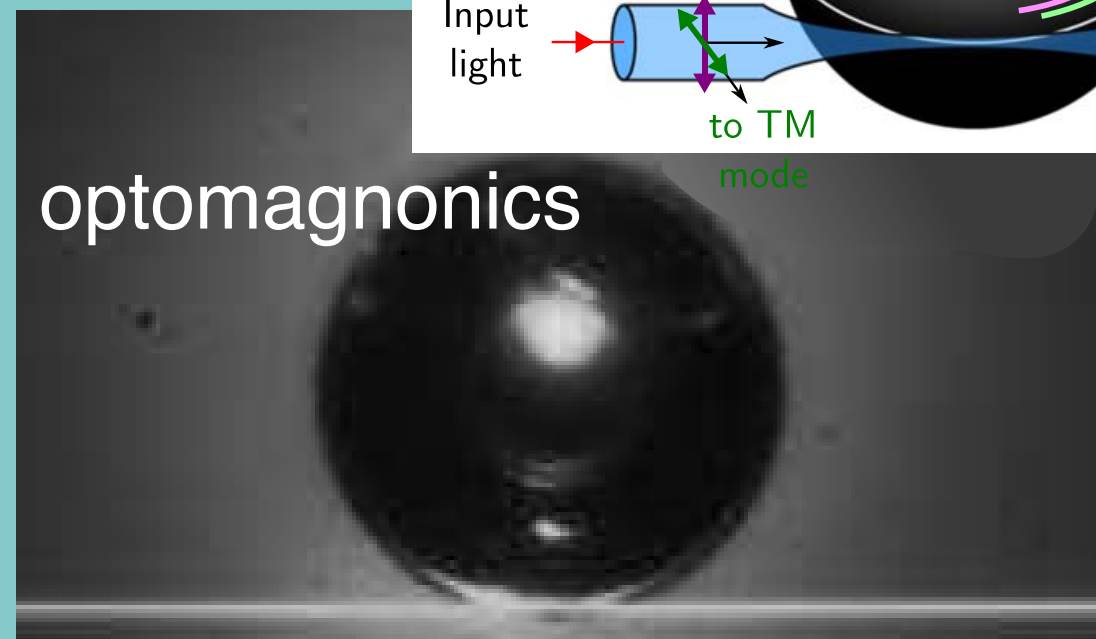
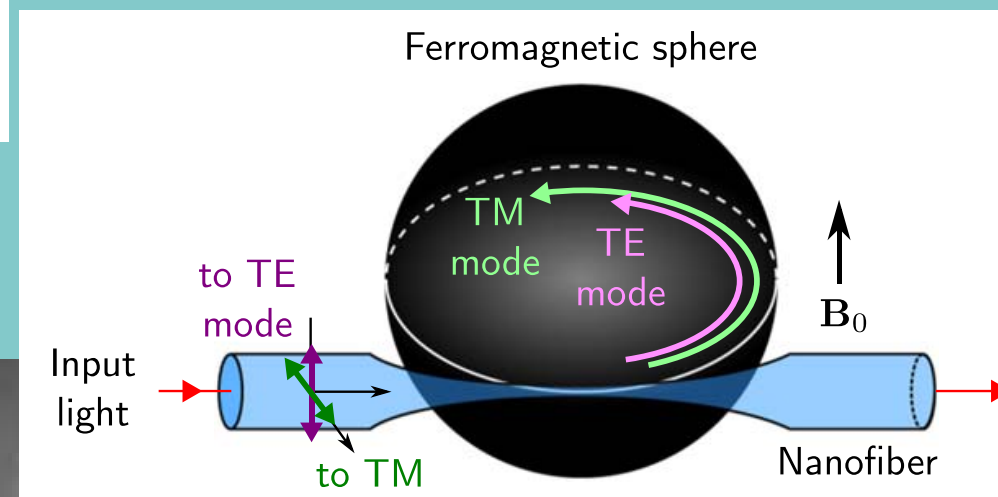
Lachance Quirion et. al Appl. Phys. Express 2019



APS/Alan Stonebraker



Zhang et. al Science Advances 2016



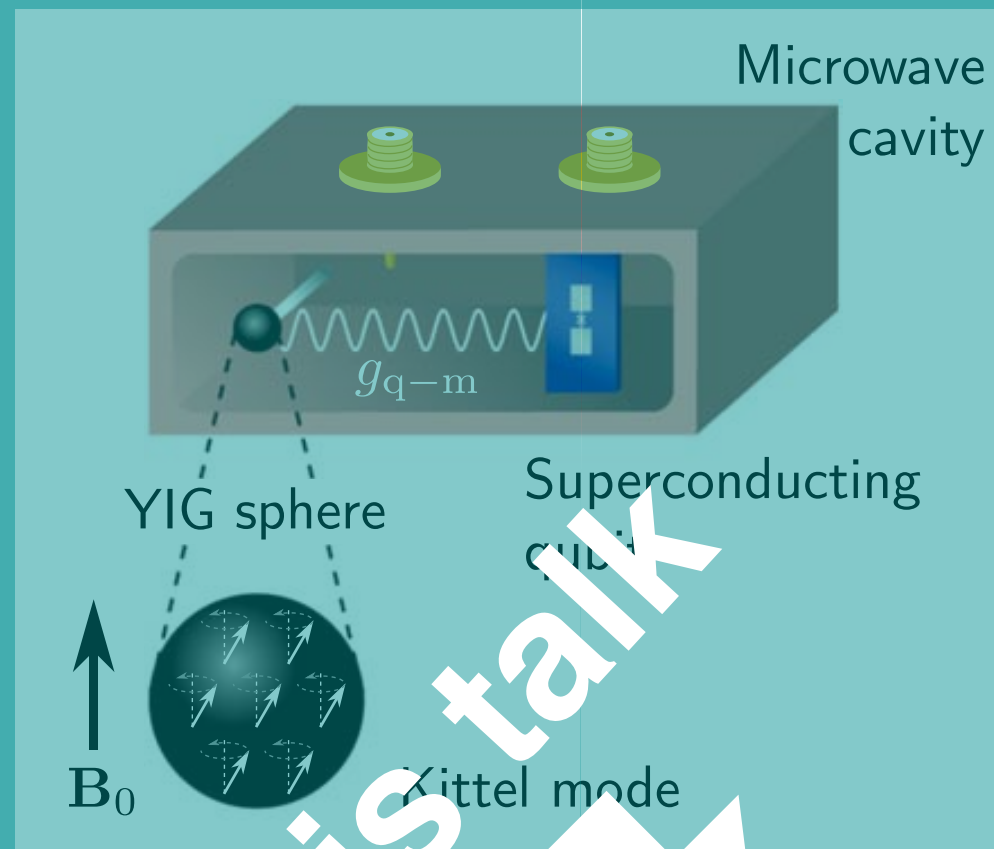
Osada et. al PRL 116 2016

Hybrid quantum systems based on magnetic elements

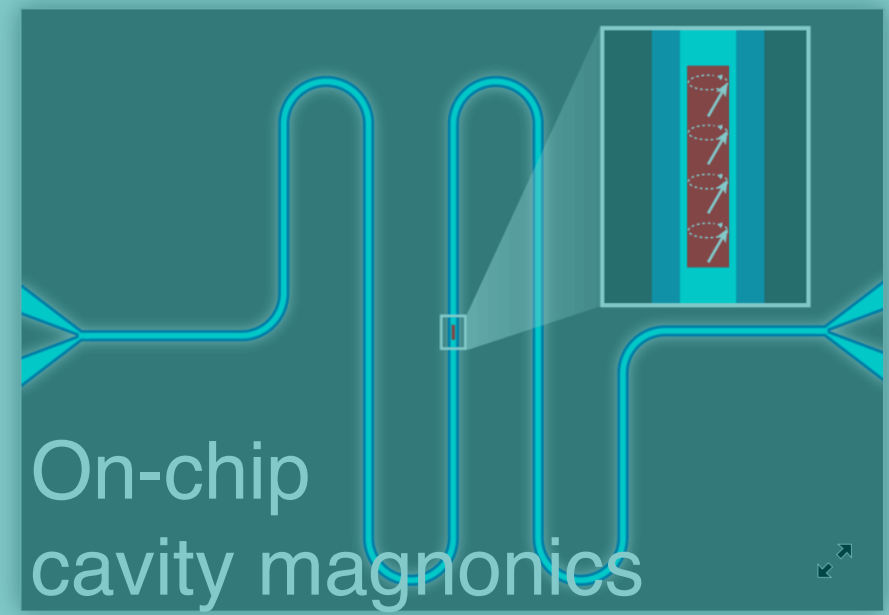
Microwave
cavity magnonics



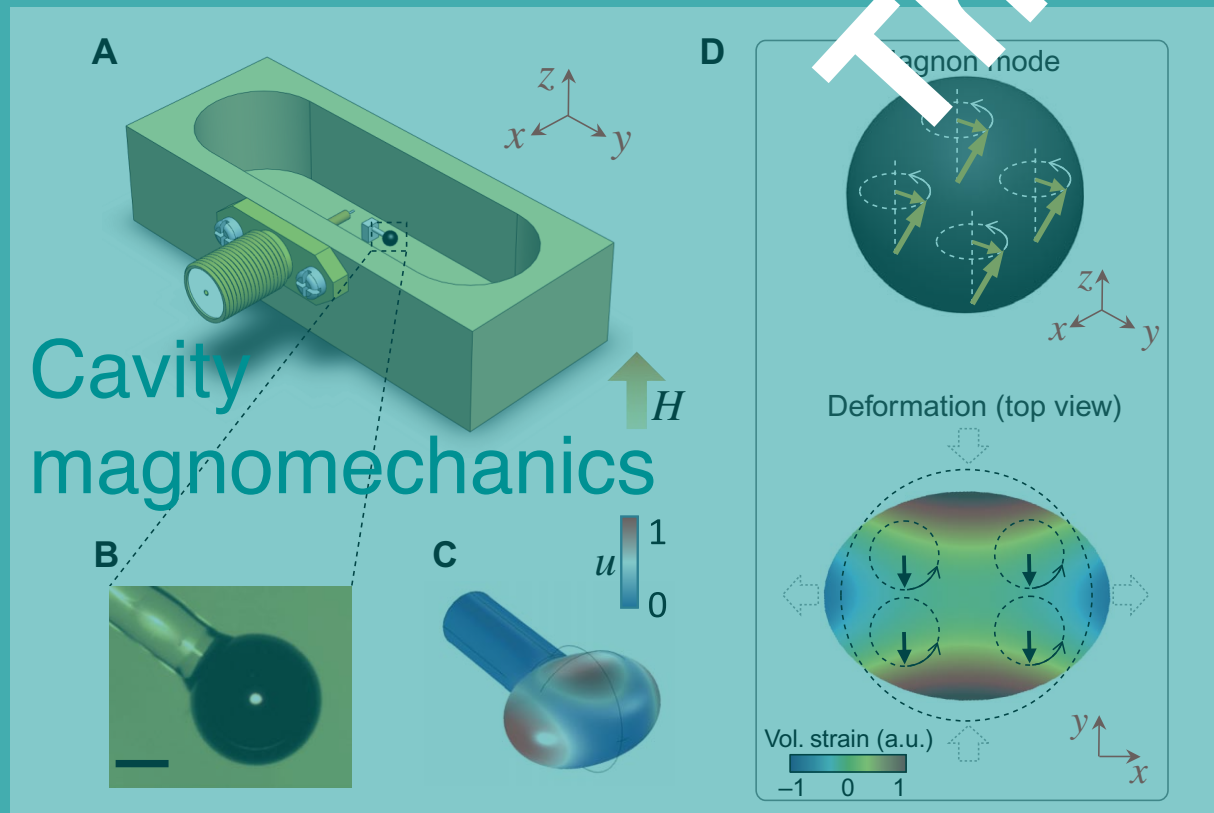
Tabuchi et. al PRL 2014



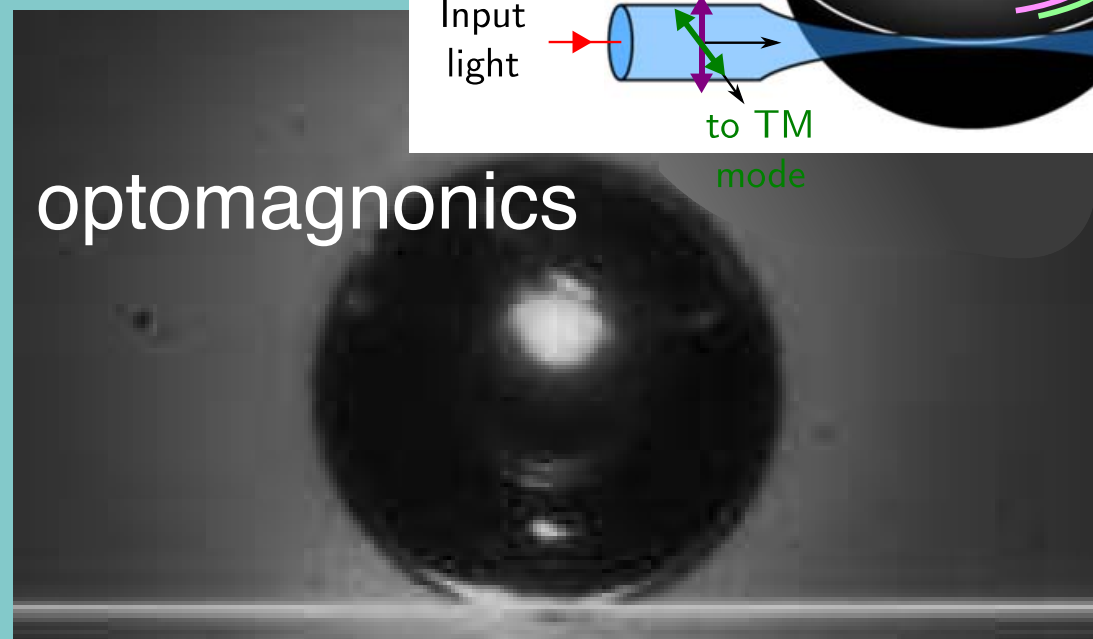
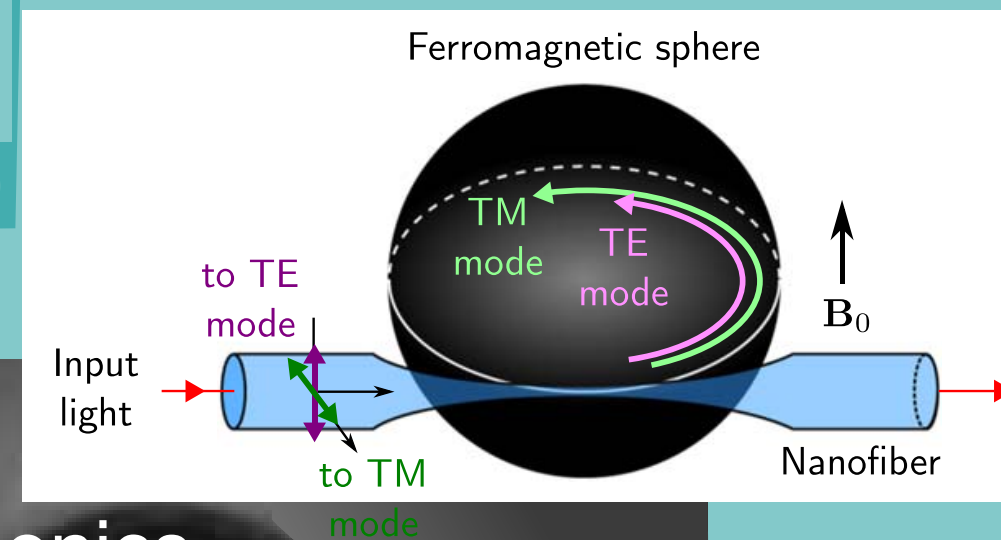
Lachance Quirke et al Appl. Phys. Express 2019



APS/Alan Stonebraker



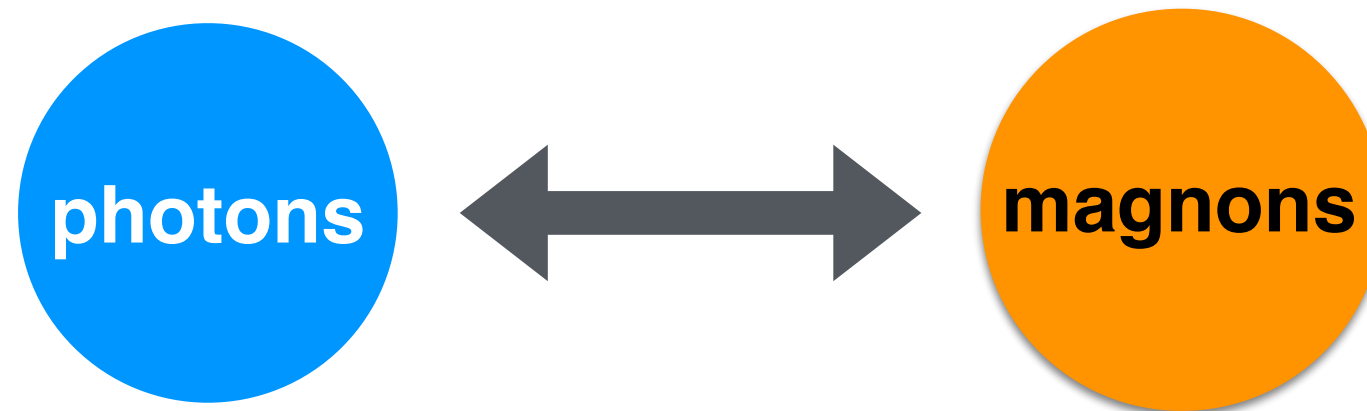
Zhang et. al Science Advances 2016



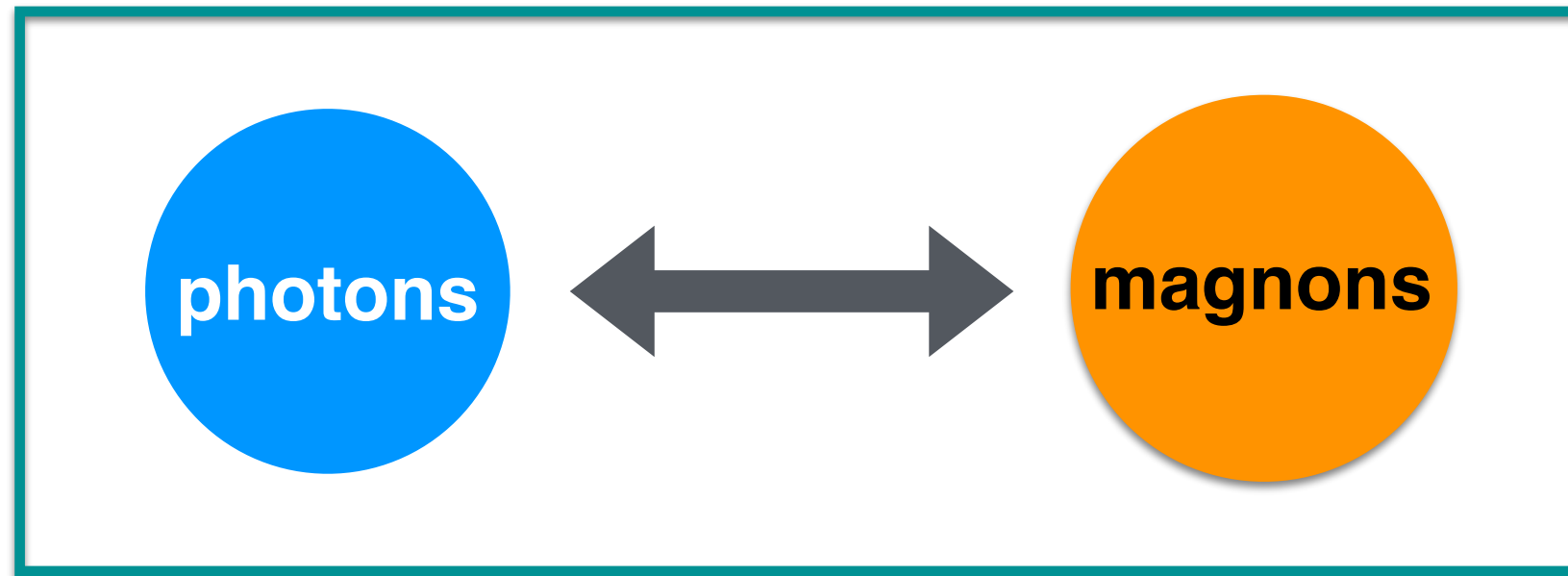
optomagnonics

Osada et. al PRL 116 2016

Optomagnonics

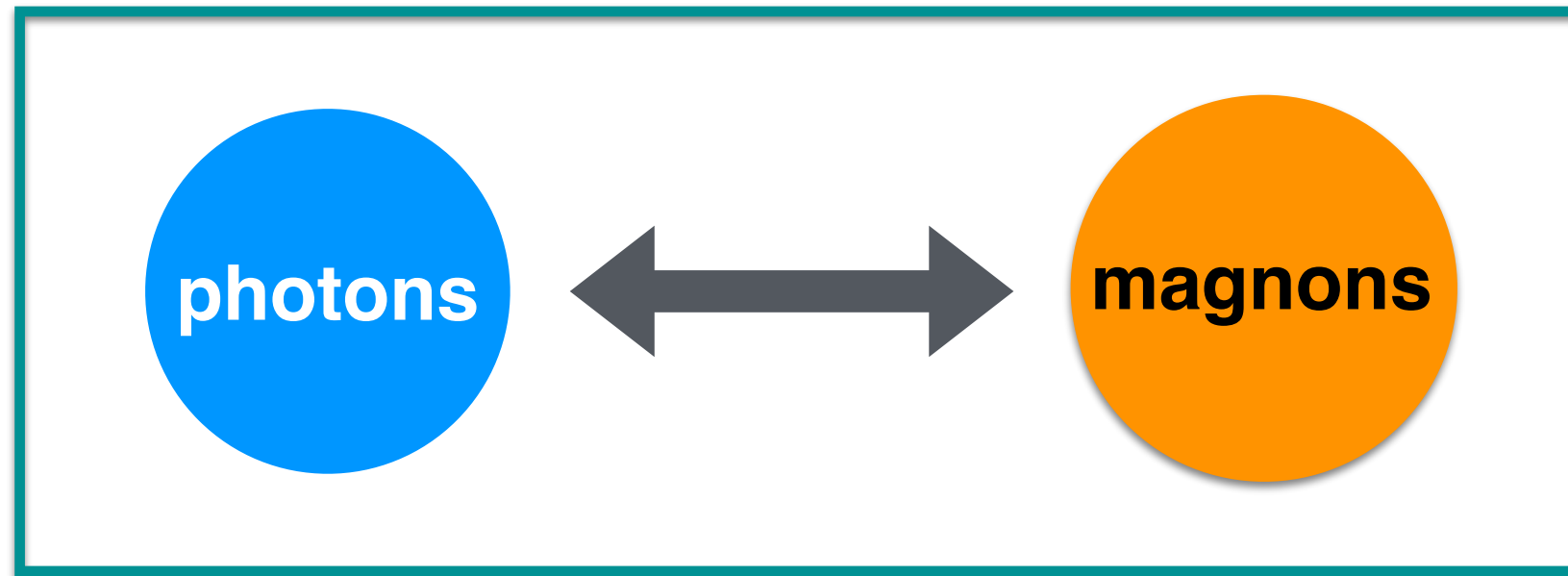


Cavity Optomagnonics



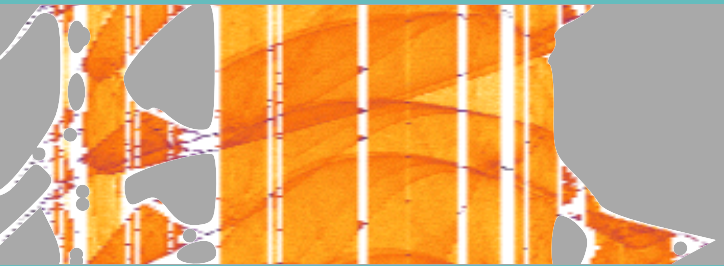
cavity-enhanced spin-photon interaction

Cavity Optomagnonics

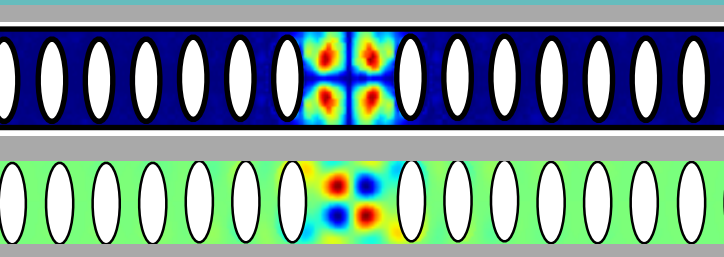


cavity-enhanced spin-photon interaction

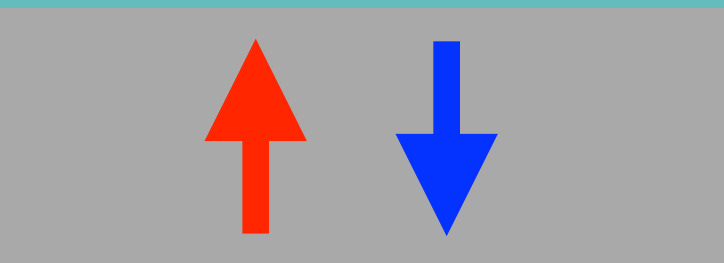
dynamical effects: frequency shifts, induced dissipation...



Optically induced spin dynamics



Optomagnonic crystals

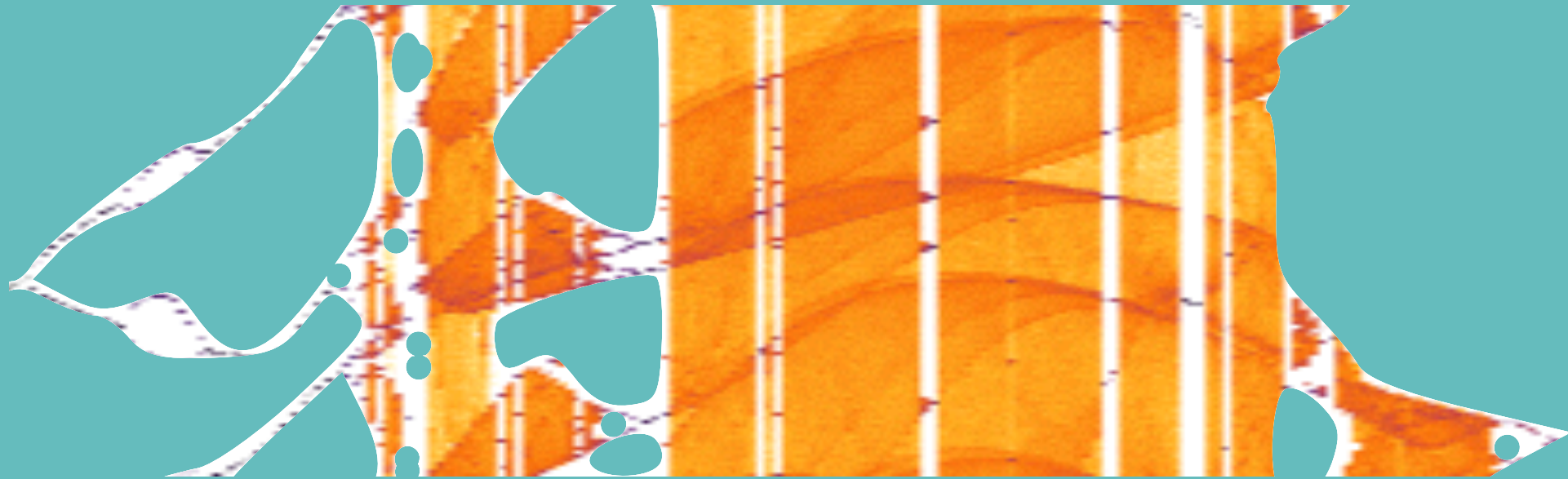


AFM (cavity) optomagnonics



Outlook

Optically induced spin dynamics



SVK, H. X. Tang, and F. Marquardt,
PRA 94, 033821 (2016)



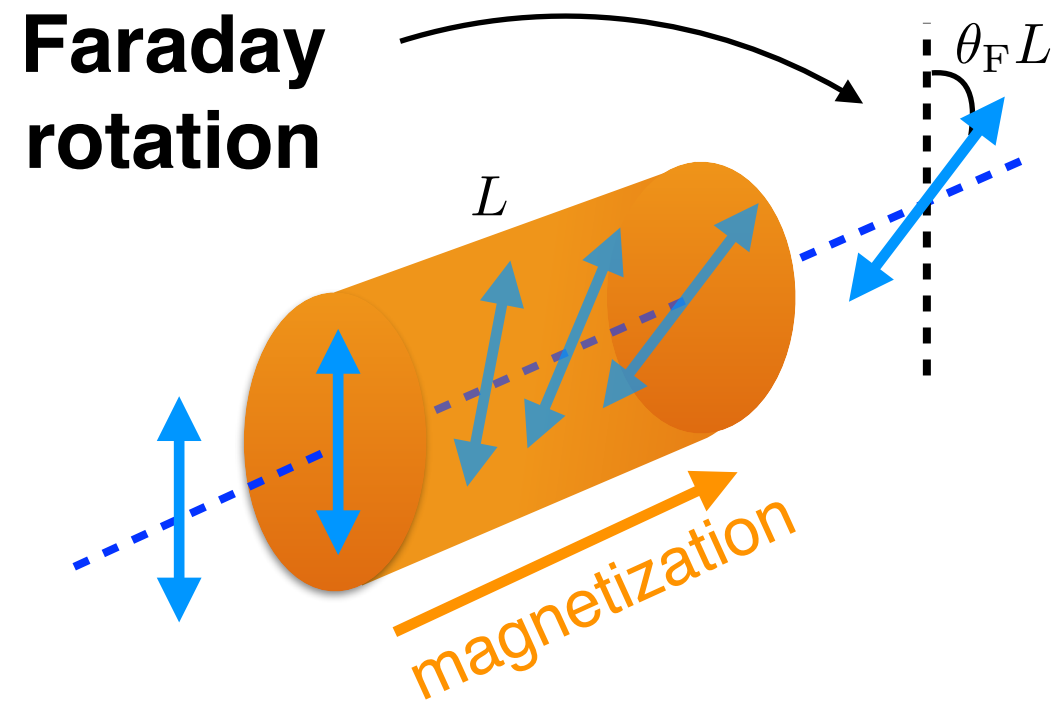
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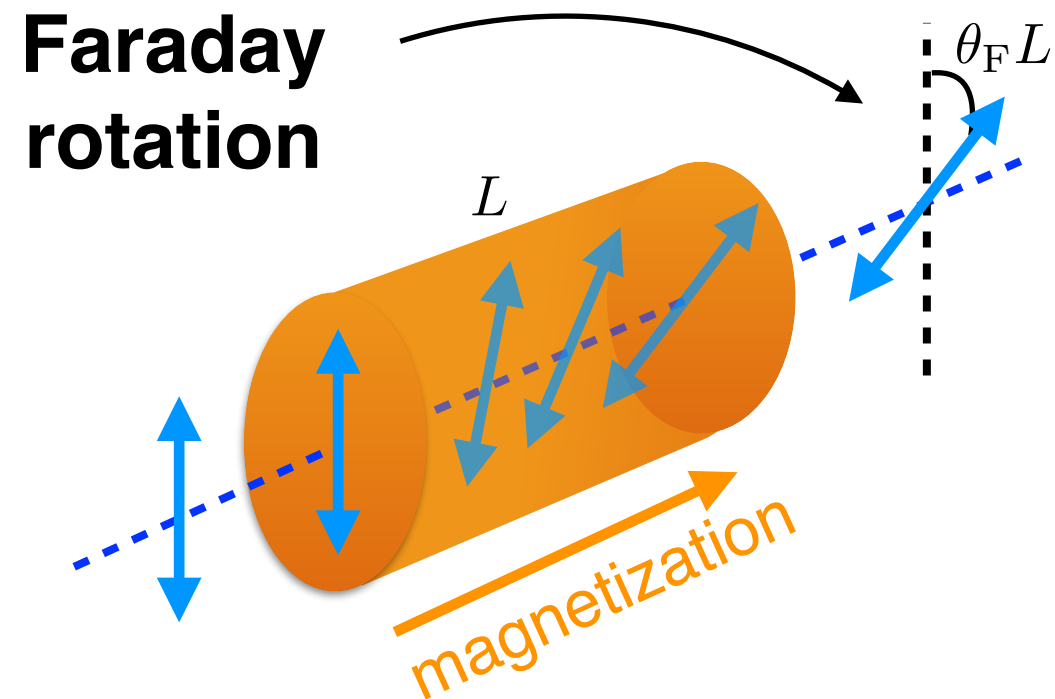
FRIEDRICH-ALEXANDER
UNIVERSITÄT
ERLANGEN-NÜRNBERG



Coupling to Optics?: Faraday Effect



Coupling to Optics?: Faraday Effect



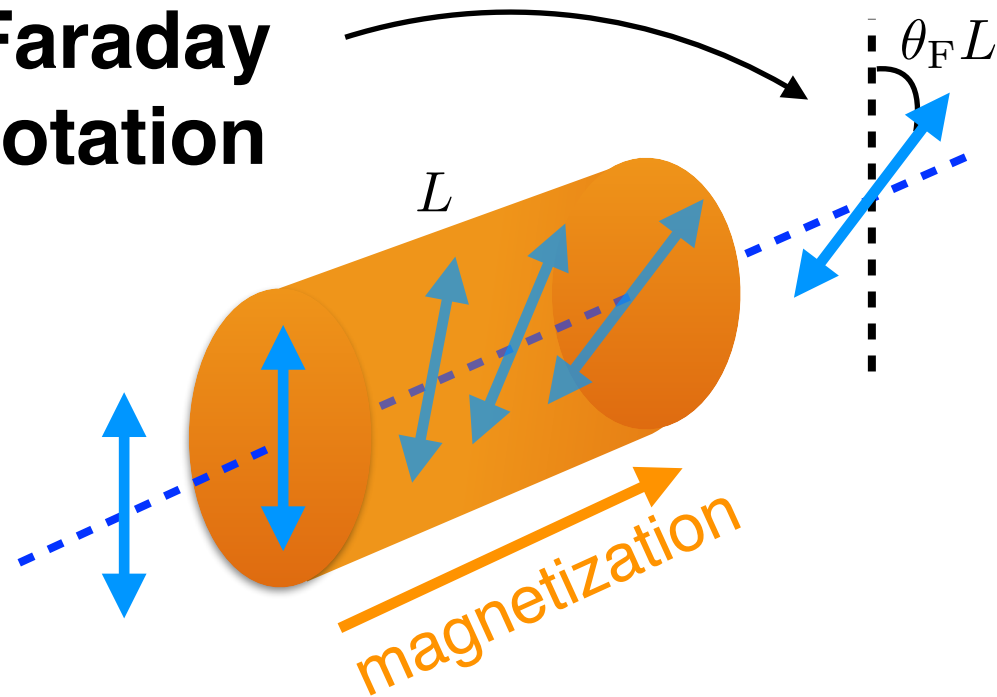
permittivity

$$\varepsilon_{ij}(\mathbf{M}) = \varepsilon_0 (\varepsilon \delta_{ij} - i f \epsilon_{ijk} M_k)$$

broken time-reversal symmetry

Coupling to Optics?: Faraday Effect

Faraday rotation



permittivity

$$\varepsilon_{ij}(\mathbf{M}) = \varepsilon_0 (\varepsilon \delta_{ij} - i f \epsilon_{ijk} M_k)$$

broken time-reversal symmetry

**optical
spin density**



$$\bar{U}_{\text{MO}} = \theta_F \sqrt{\frac{\varepsilon}{\varepsilon_0}} \int d\mathbf{r} \frac{\mathbf{M}(\mathbf{r})}{M_s} \cdot \frac{\varepsilon_0}{2i\omega} [\mathbf{E}^*(\mathbf{r}) \times \mathbf{E}(\mathbf{r})]$$

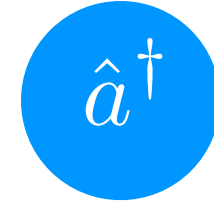
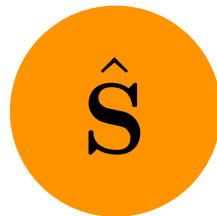


**magnetization
density**

Optomagnonic Hamiltonian

$$\bar{U}_{\text{MO}} = \theta_{\text{F}} \sqrt{\frac{\varepsilon}{\varepsilon_0}} \int d\mathbf{r} \frac{\mathbf{M}(\mathbf{r})}{M_{\text{s}}} \cdot \frac{\varepsilon_0}{2i\omega} [\mathbf{E}^*(\mathbf{r}) \times \mathbf{E}(\mathbf{r})]$$

Quantize:

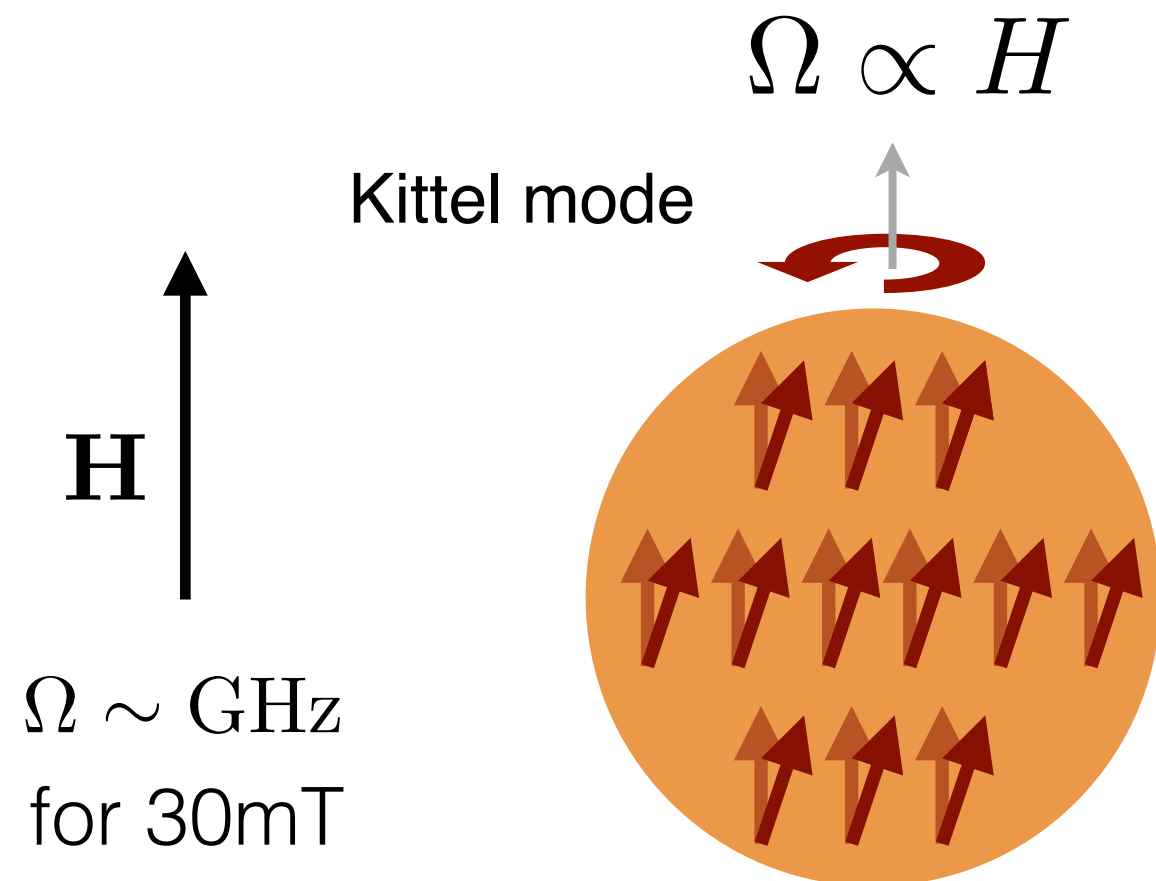
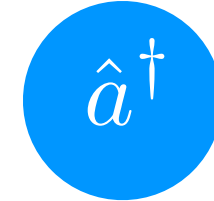


two-photon process

Optomagnonic Hamiltonian: Kittel Mode

$$\bar{U}_{\text{MO}} = \theta_{\text{F}} \sqrt{\frac{\varepsilon}{\varepsilon_0}} \int d\mathbf{r} \frac{\mathbf{M}(\mathbf{r})}{M_{\text{s}}} \cdot \frac{\varepsilon_0}{2i\omega} [\mathbf{E}^*(\mathbf{r}) \times \mathbf{E}(\mathbf{r})]$$

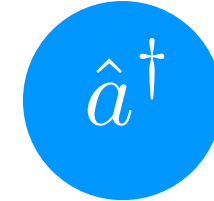
Quantize:



Optomagnonic Hamiltonian: Kittel Mode

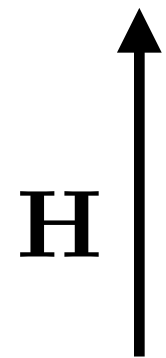
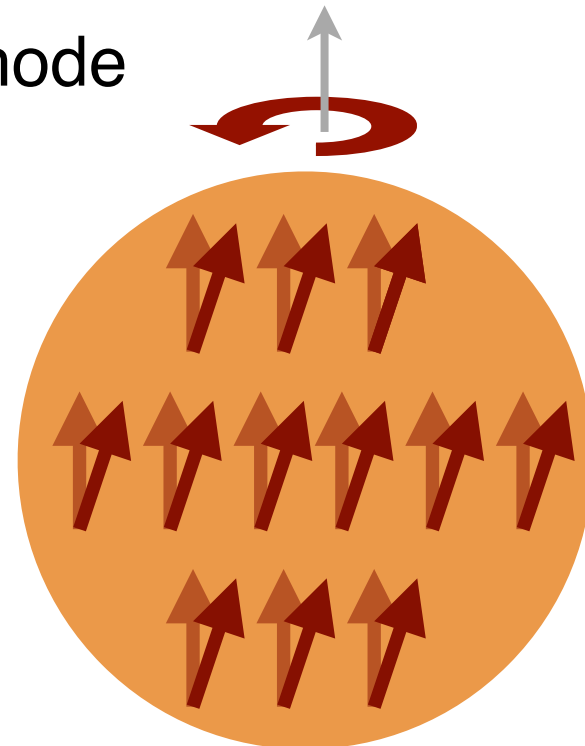
$$\bar{U}_{\text{MO}} = \theta_F \sqrt{\frac{\varepsilon}{\varepsilon_0}} \int d\mathbf{r} \frac{\mathbf{M}(\mathbf{r})}{M_s} \cdot \frac{\varepsilon_0}{2i\omega} [\mathbf{E}^*(\mathbf{r}) \times \mathbf{E}(\mathbf{r})]$$

Quantize:



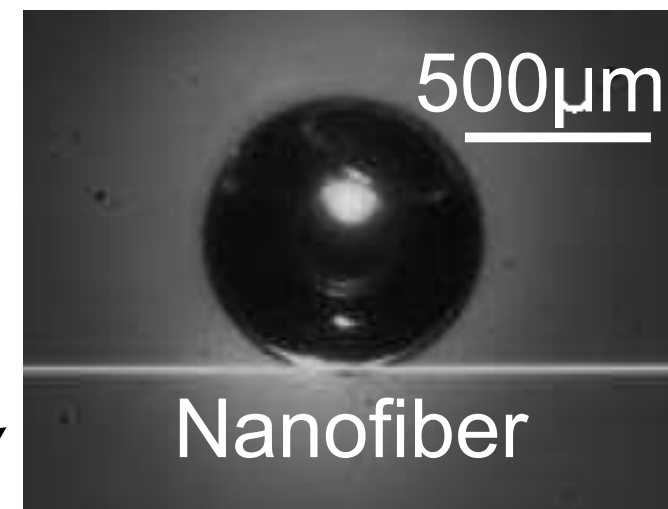
$$\Omega \propto H$$

Kittel mode



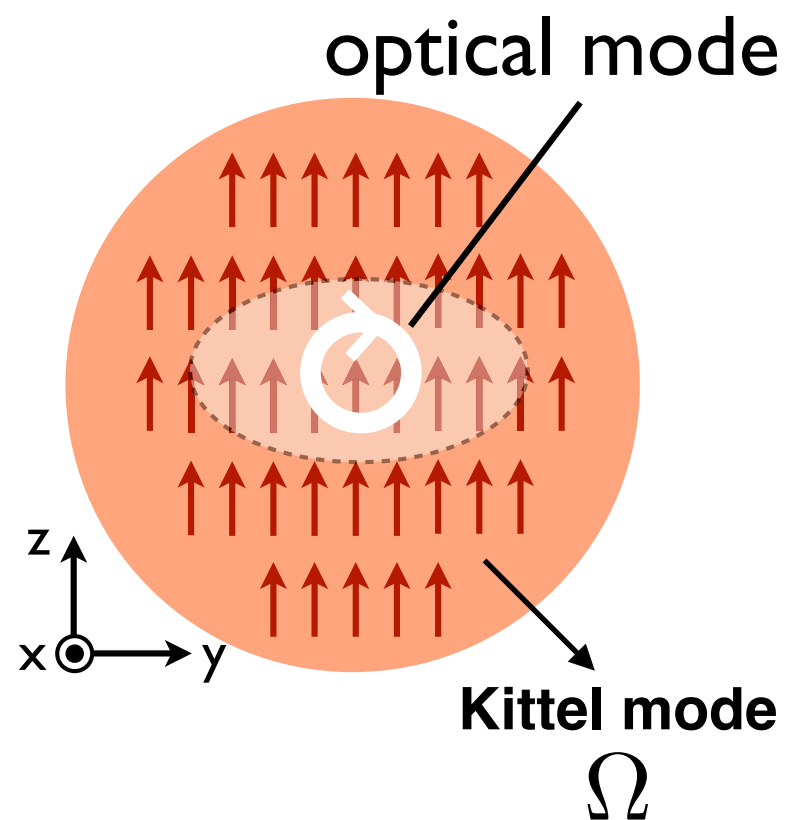
$\Omega \sim \text{GHz}$
for 30mT

Yttrium Iron Garnet (YIG)



- [Osada et. al PRL 116, 223601 \(2016\)](#)
- [Haigh et. al PRL 117, 133602 \(2016\)](#)
- [Zhang et. al PRL 117, 123605 \(2016\)](#)

Cavity Optomagnonics: simple model



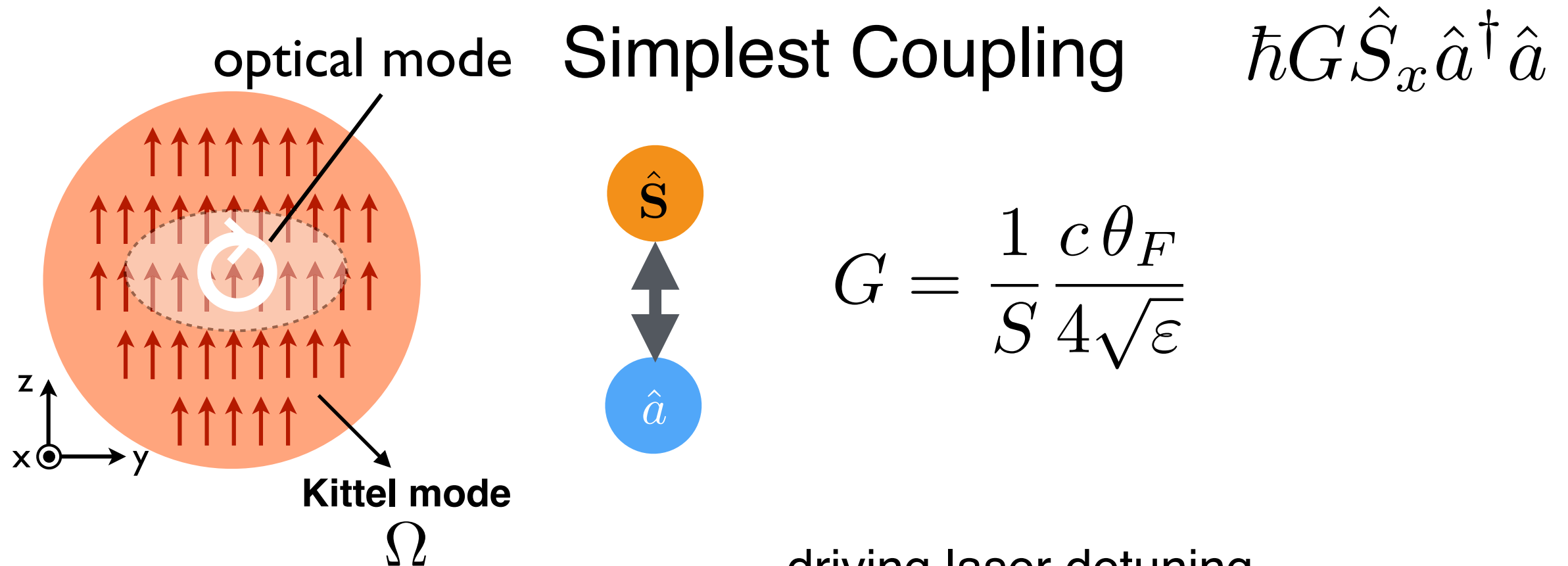
Simplest Coupling



$$G = \frac{1}{S} \frac{c \theta_F}{4\sqrt{\epsilon}}$$

$$\hbar G \hat{S}_x \hat{a}^\dagger \hat{a}$$

Cavity Optomagnonics: simple model



Hamiltonian

$$H = -\hbar \Delta \hat{a}^\dagger \hat{a} - \hbar \Omega \hat{S}_z + \hbar G \hat{S}_x \hat{a}^\dagger \hat{a}$$

in rotating frame

+ magnon and cavity decay rates

Γ

$\mathcal{K}$

Fast Cavity Limit

Fast cavity limit: integrate out the light field

$$\dot{\mathbf{S}} = \mathbf{B}_{\text{eff}} \times \mathbf{S} + \frac{\eta_{\text{opt}}}{S} \left(\dot{S}_x \mathbf{e}_x \times \mathbf{S} \right)$$

Effective Landau-Lifshitz-Gilbert equation of motion

effective field

$$\mathbf{B}_{\text{eff}} = -\Omega \mathbf{e}_z + \mathbf{B}_{\text{opt}} \quad \mathbf{B}_{\text{opt}} = \frac{G}{\left[\left(\frac{\kappa}{2}\right)^2 + (\Delta - GS_x)^2\right]} \left(\frac{\kappa}{2} \alpha_{\text{max}}\right)^2 \mathbf{e}_x$$

frequency shift

damping

can change sign

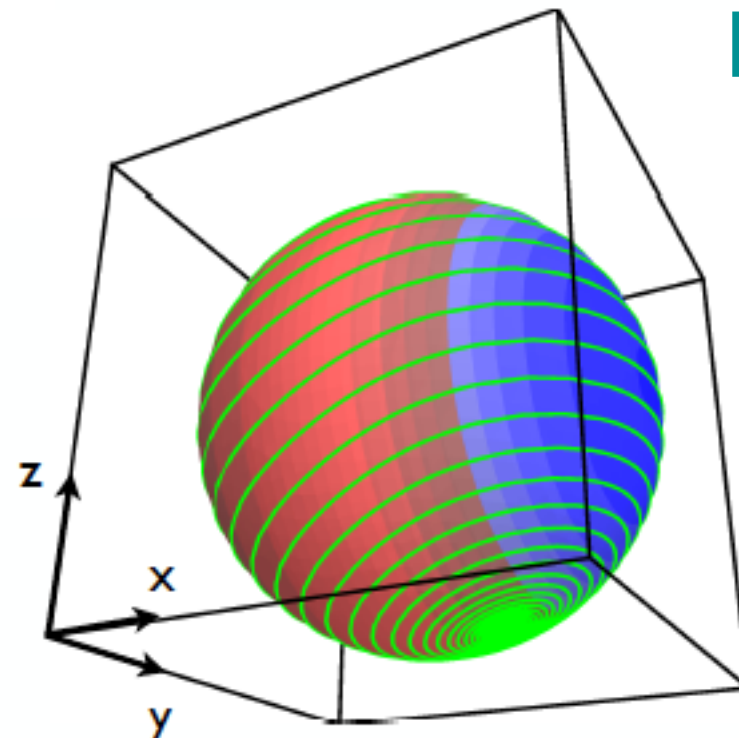
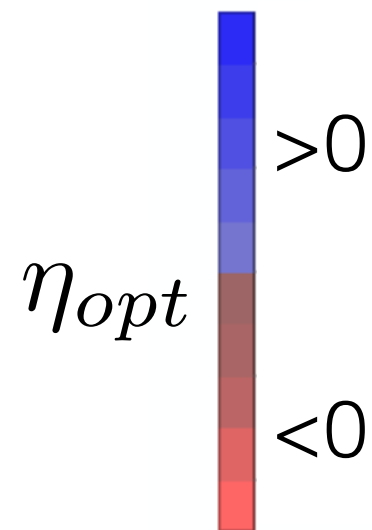
$$\eta_{\text{opt}} = -2G\kappa S |\mathbf{B}_{\text{opt}}| \frac{(\Delta - GS_x)}{\left[\left(\frac{\kappa}{2}\right)^2 + (\Delta - GS_x)^2\right]^2}$$

tunable by the external laser drive

Spin Dynamics: Fast Cavity Limit

Blue detuned case:

dissipation
changes sign

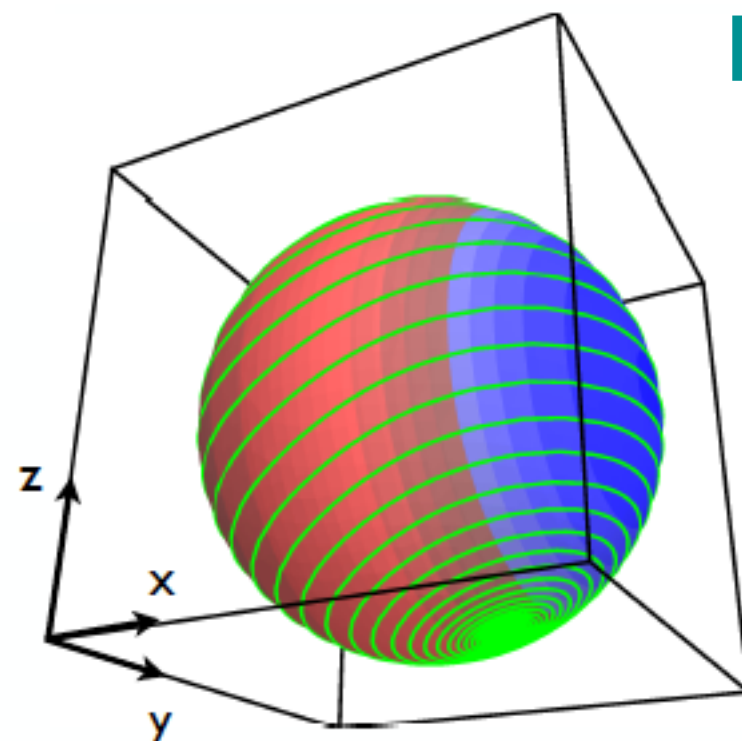
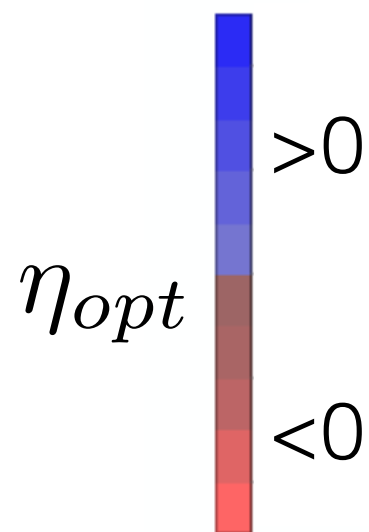


**Light induced
magnetic
switching**

Spin Dynamics: Fast Cavity Limit

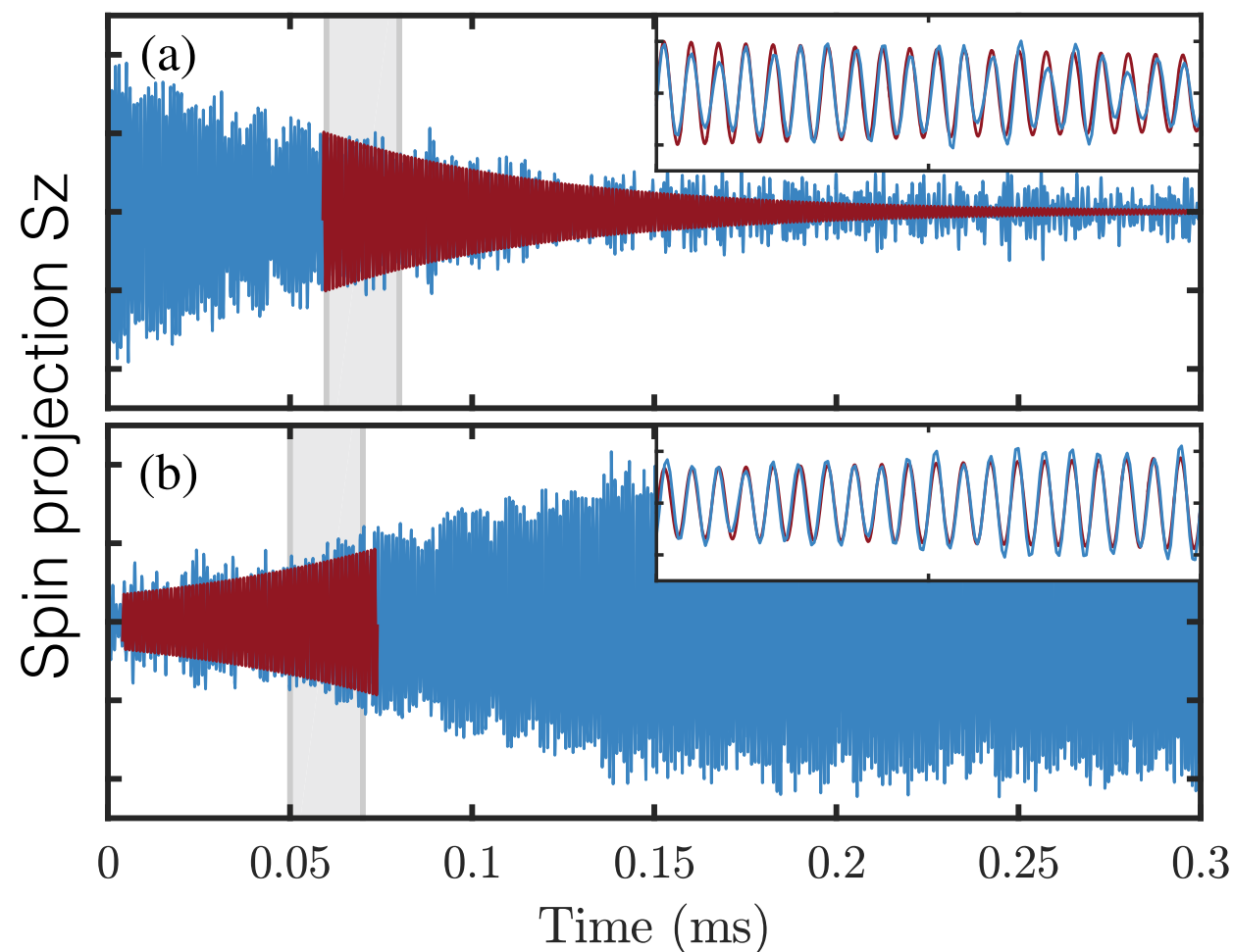
Blue detuned case:

dissipation
changes sign



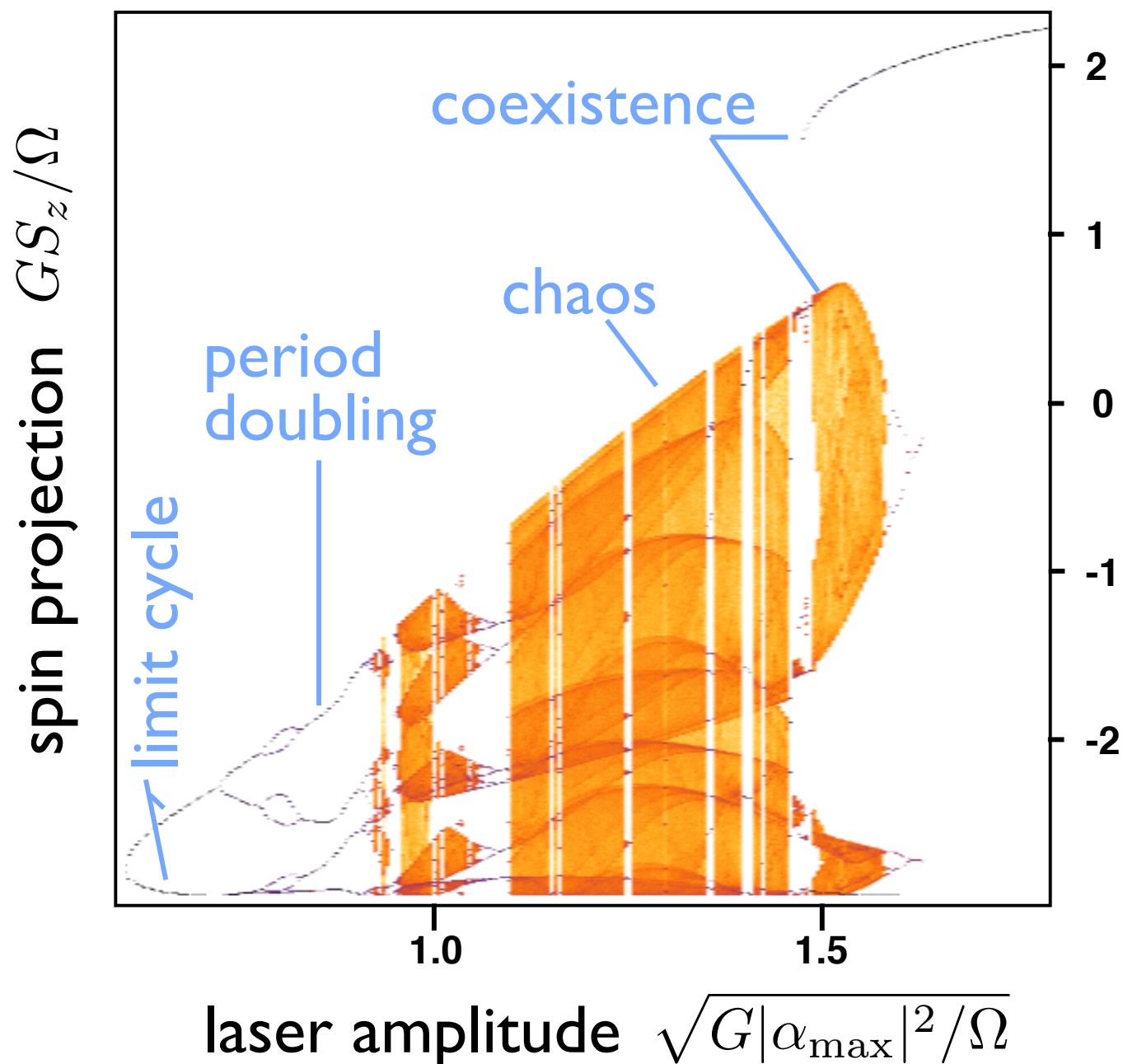
Light induced
magnetic
switching

See experimental realization
with cold atoms,
Dan M. Stamper-Kurn Group
Phys. Rev. Lett. **118**, 063604
(2017)



Optically Induced Spin Dynamics

Classical Dynamics



» **Coherent optical control**

» **Magnetic switching**

» **Self-sustained oscillations**

» **Optically induced route to chaos**

But...

Problem

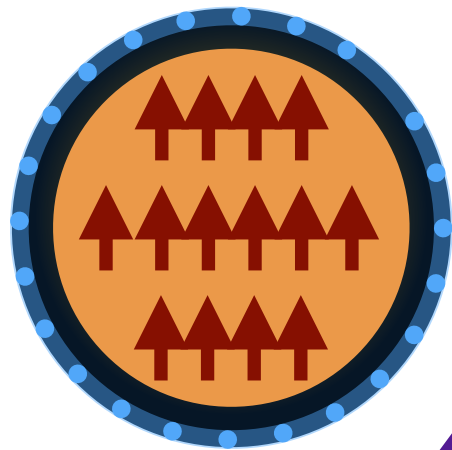
the state of the art optomagnonic coupling is small

**We have shown that the theoretical limit
is much larger**

SVK, H. X. Tang, and F. Marquardt
PRA 94, 033821 (2016)

What we need:

better overlap of modes



?

smaller systems

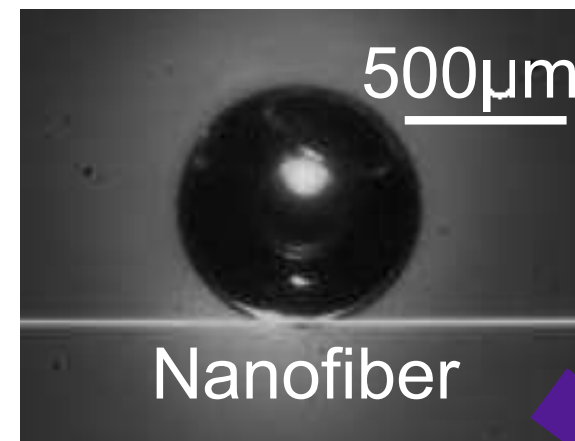
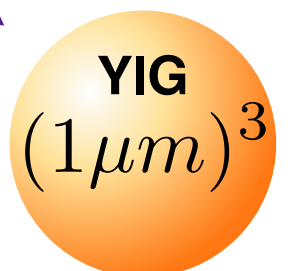
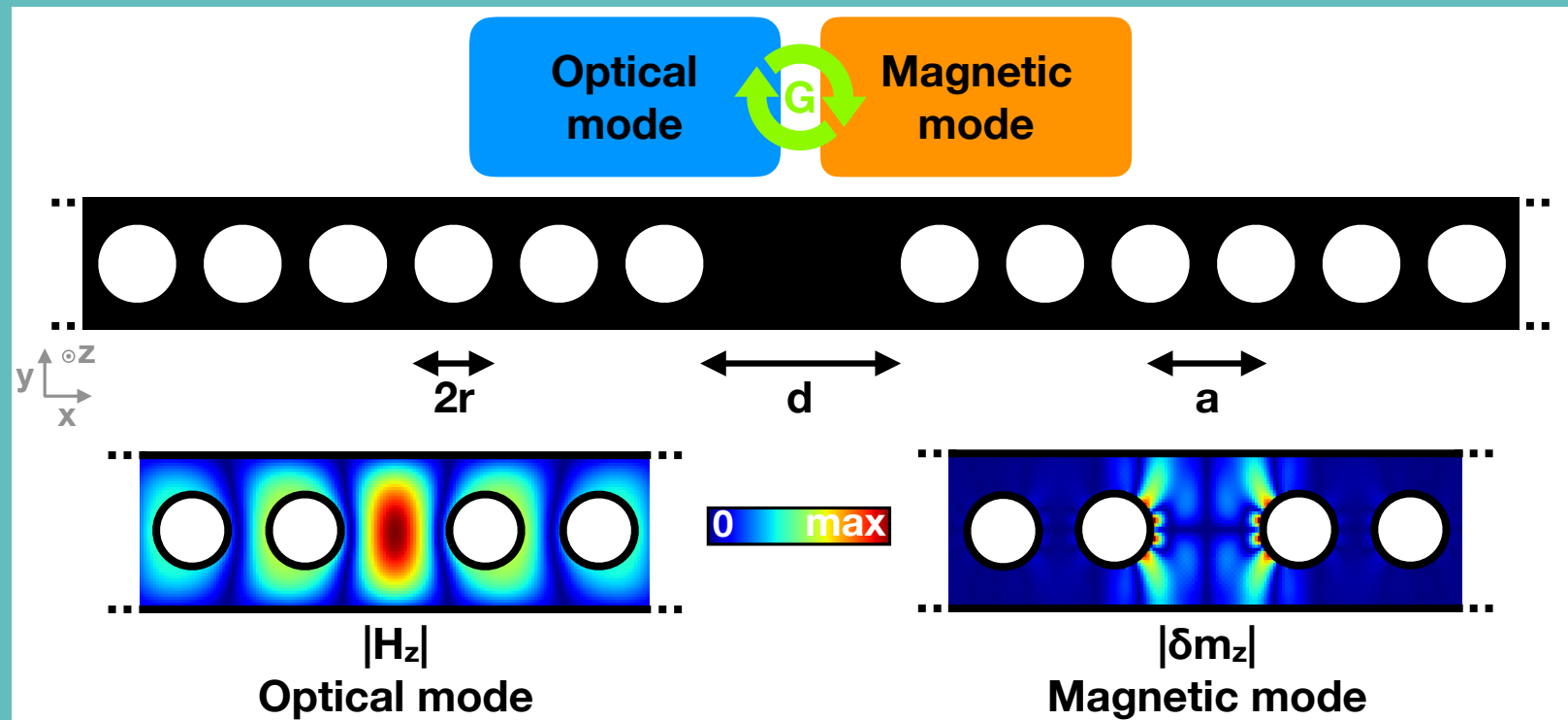


Fig: Osada et. al.
PRL 116, 223601



Optomagnonic Crystals



J. Graf, S. Sharma, H. Huebl, SVK;
Physical Review Research 3, 013277 (2021)



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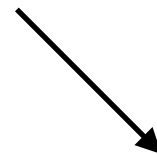
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Optomagnonics beyond the Kittel mode

$$H_{\text{MO}} = -i \frac{\theta_{\text{F}} \lambda_n}{2\pi} \frac{\varepsilon_0 \varepsilon}{2} \int d\mathbf{r} \, \mathbf{m}(\mathbf{r}, t) \cdot [\mathbf{E}^*(\mathbf{r}, t) \times \mathbf{E}(\mathbf{r}, t)]$$

$$\mathbf{m}(\mathbf{r}, t) = \mathbf{m}_0(\mathbf{r}) + \delta\mathbf{m}(\mathbf{r}, t)$$



small

Optomagnonics beyond the Kittel mode

$$H_{\text{MO}} = -i \frac{\theta_F \lambda_n}{2\pi} \frac{\varepsilon_0 \varepsilon}{2} \int d\mathbf{r} \, \mathbf{m}(\mathbf{r}, t) \cdot [\mathbf{E}^*(\mathbf{r}, t) \times \mathbf{E}(\mathbf{r}, t)]$$

$$\mathbf{m}(\mathbf{r}, t) = \mathbf{m}_0(\mathbf{r}) + \delta\mathbf{m}(\mathbf{r}, t)$$

Quantize: Holstein Primakoff to first order

$$\delta\mathbf{m}(\mathbf{r}, t) \rightarrow \frac{1}{2} \sum_{\gamma} \left(\delta\mathbf{m}_{\gamma}(\mathbf{r}) \hat{b}_{\gamma} e^{-i\omega_{\gamma} t} + \delta\mathbf{m}_{\gamma}^*(\mathbf{r}) \hat{b}_{\gamma}^{\dagger} e^{i\omega_{\gamma} t} \right)$$

magnon mode index

mode functions

bosonic operator

Optomagnonics beyond the Kittel mode

$$H_{\text{MO}} = -i \frac{\theta_F \lambda_n}{2\pi} \frac{\varepsilon_0 \varepsilon}{2} \int d\mathbf{r} \, \mathbf{m}(\mathbf{r}, t) \cdot [\mathbf{E}^*(\mathbf{r}, t) \times \mathbf{E}(\mathbf{r}, t)]$$

$$\mathbf{m}(\mathbf{r}, t) = \mathbf{m}_0(\mathbf{r}) + \delta\mathbf{m}(\mathbf{r}, t)$$

Quantize: Holstein Primakoff to first order

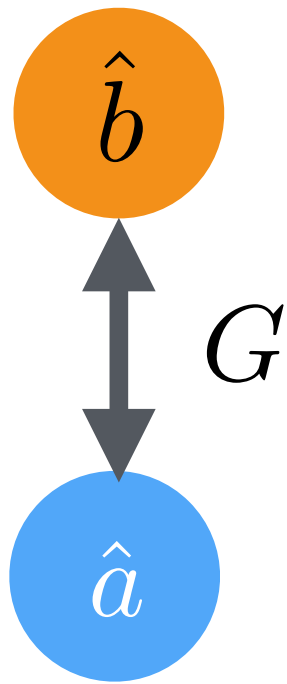
$$\delta\mathbf{m}(\mathbf{r}, t) \rightarrow \frac{1}{2} \sum_{\gamma} \left(\delta\mathbf{m}_{\gamma}(\mathbf{r}) \hat{b}_{\gamma} e^{-i\omega_{\gamma} t} + \delta\mathbf{m}_{\gamma}^*(\mathbf{r}) \hat{b}_{\gamma}^{\dagger} e^{i\omega_{\gamma} t} \right)$$

Quantization of $\mathbf{E}$ optical fields

$$\mathbf{E}^{(*)}(\mathbf{r}, t) \rightarrow \sum_{\beta} \mathbf{E}_{\beta}^{(*)}(\mathbf{r}) \hat{a}_{\beta}^{(\dagger)} e^{-(+)\omega_{\beta} t}$$

Optomagnonics beyond the Kittel mode

Coupling Hamiltonian in the spin-wave limit



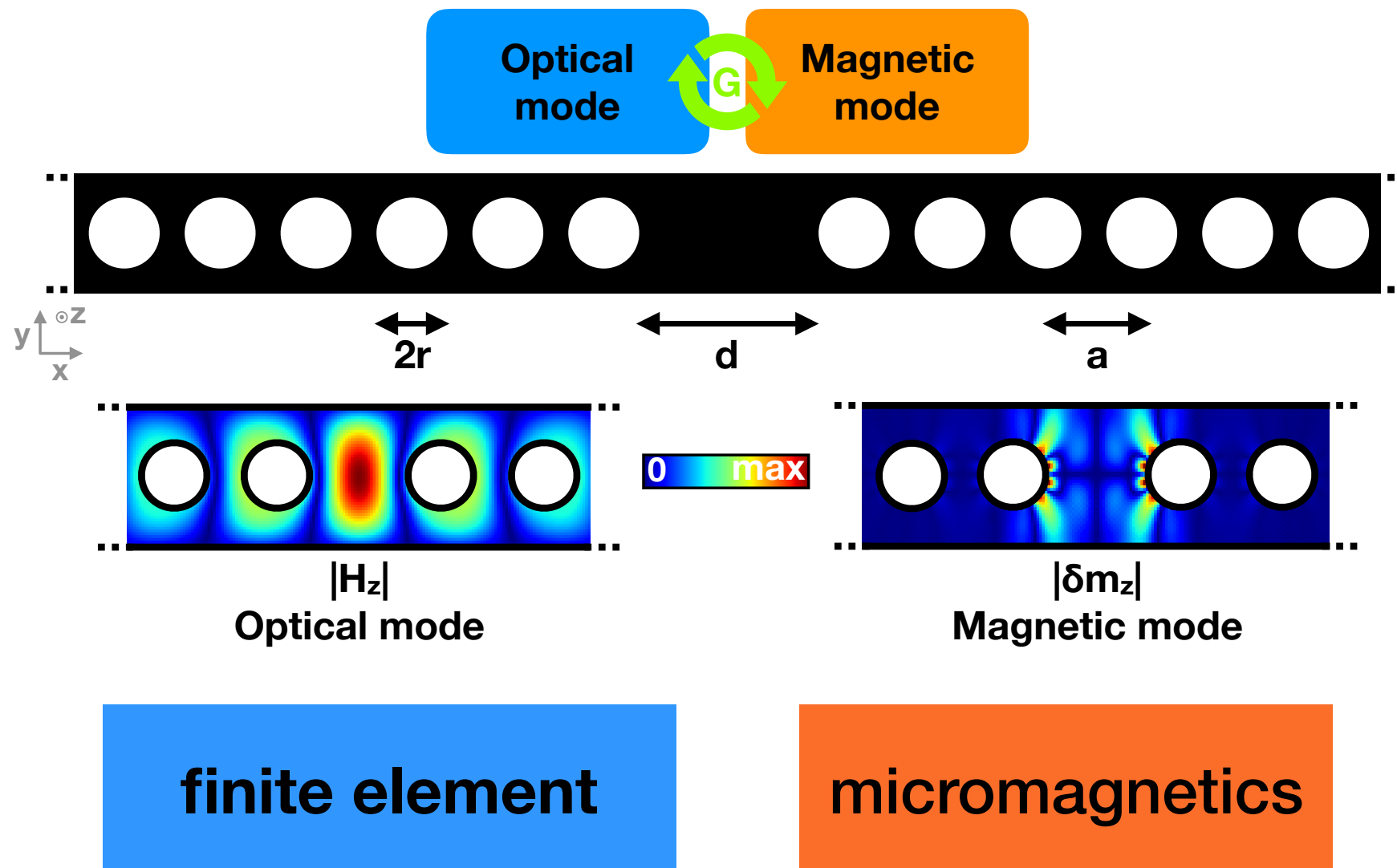
$$\hat{H}_{MO} = \sum_{\alpha\beta\gamma} G_{\alpha\beta\gamma} \hat{a}_{\alpha}^{\dagger} \hat{a}_{\beta} \hat{b}_{\gamma} + \text{h.c.}$$

Optomagnonic coupling

$$G_{\alpha\beta\gamma} = -i \frac{\theta_F \lambda_n}{4\pi} \frac{\varepsilon_0 \varepsilon}{2} \int d\mathbf{r} \, \delta \mathbf{m}_{\gamma}(\mathbf{r}) \cdot [\mathbf{E}_{\alpha}^*(\mathbf{r}) \times \mathbf{E}_{\beta}(\mathbf{r})]$$

Optomagnonic Coupling

$$G_{\alpha\beta\gamma} = -i \frac{\theta_F \lambda_n}{4\pi} \frac{\varepsilon_0 \varepsilon}{2} \int d\mathbf{r} \, \delta \mathbf{m}_\gamma(\mathbf{r}) \cdot [\mathbf{E}_\alpha^*(\mathbf{r}) \times \mathbf{E}_\beta(\mathbf{r})]$$

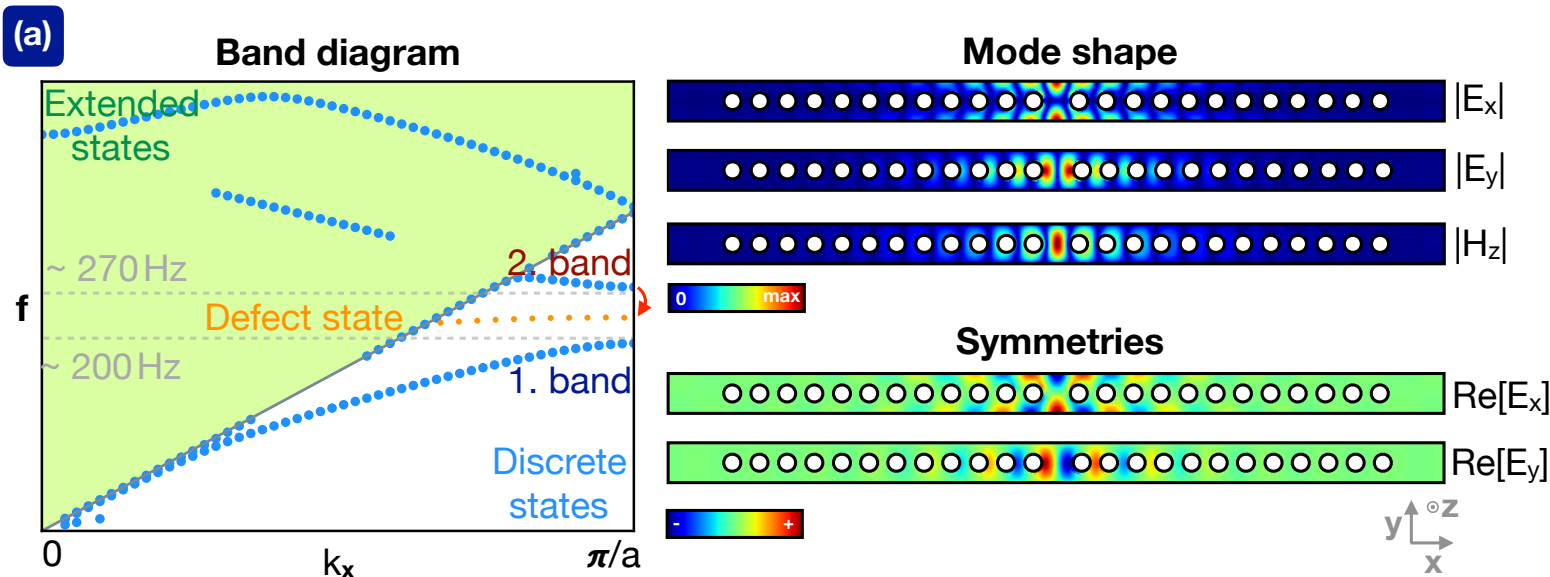


MuMax3

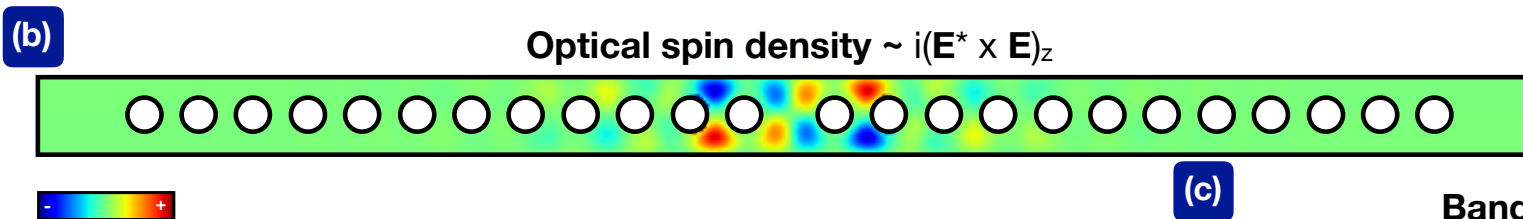
Vansteenkiste et. al
AIP Advances 4,
107133 (2014)

Design: towards optimal mode matching

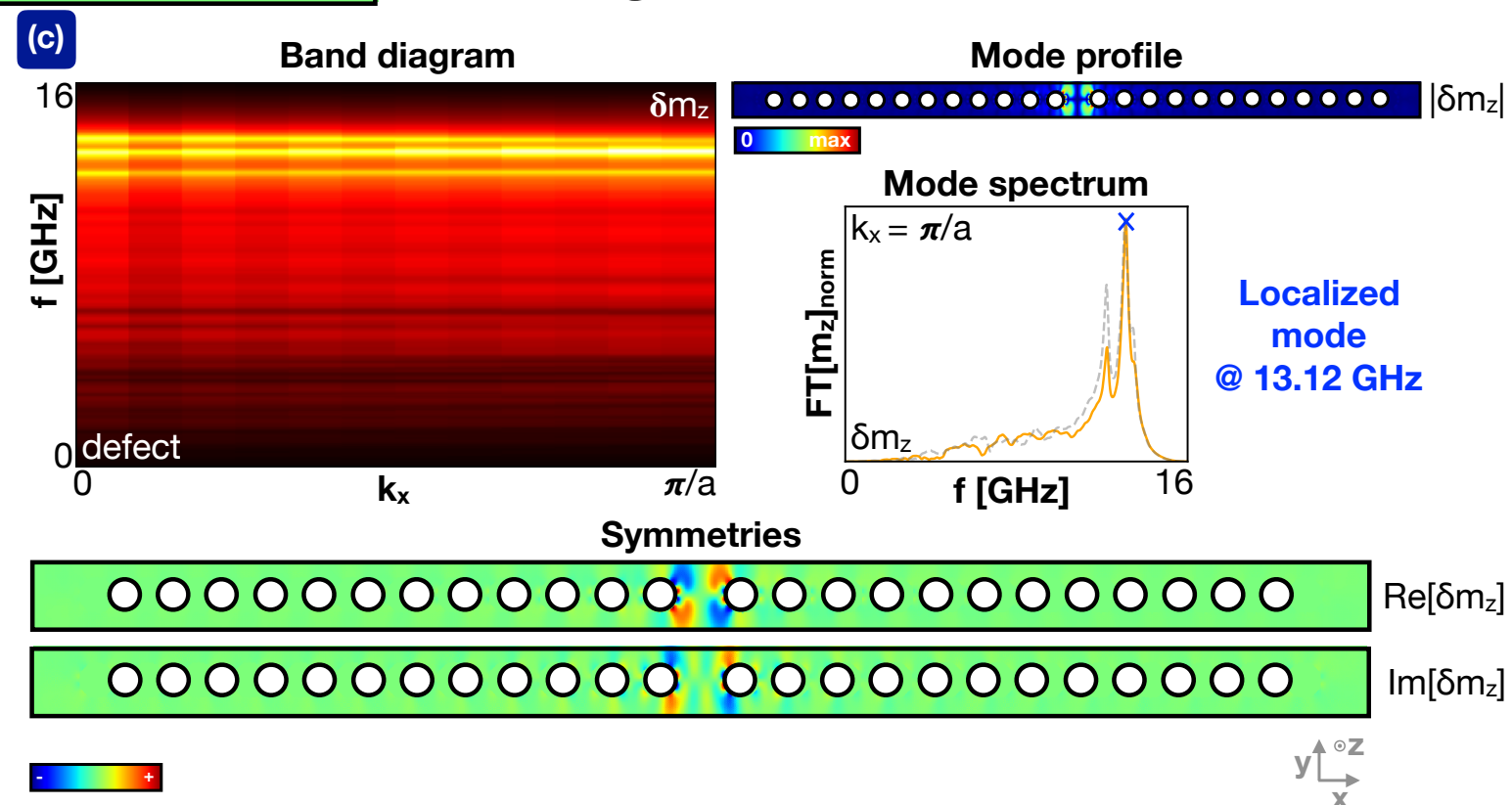
Optics



→ Localized optical mode



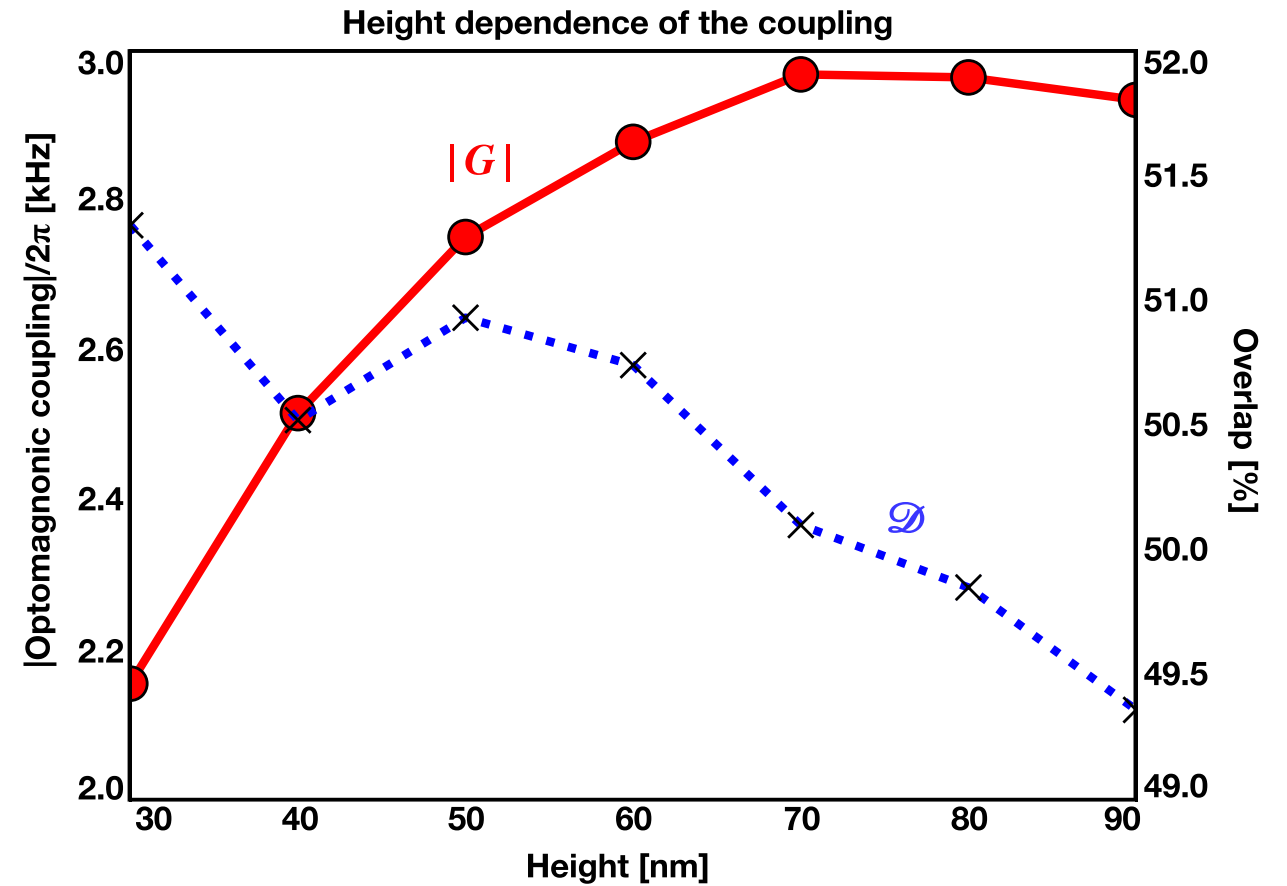
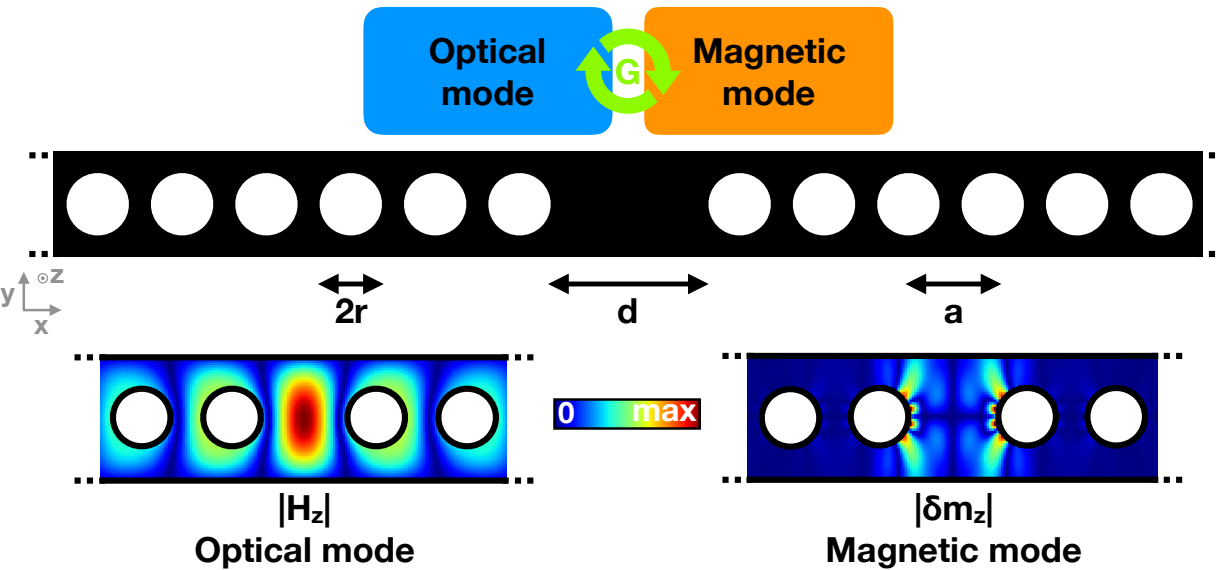
Magnetics



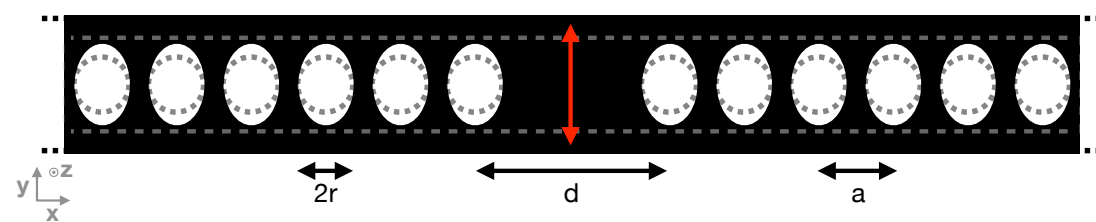
← Localized magnon mode

Match symmetries of magnon mode and optical spin density

Design: towards optimal mode matching

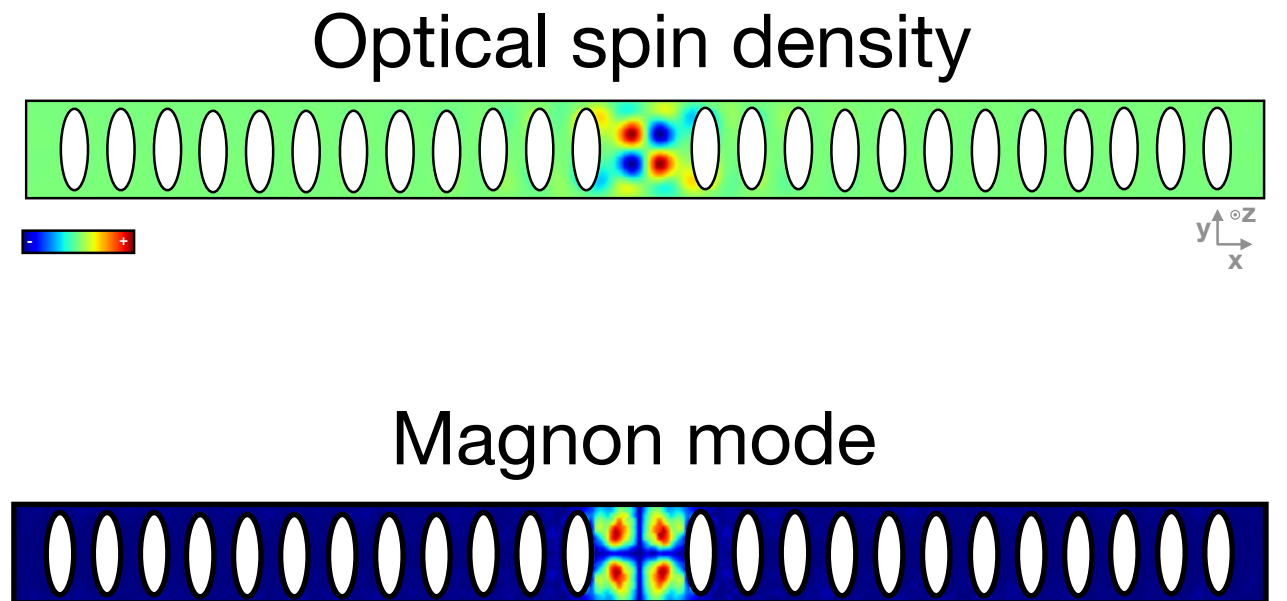


Optimization

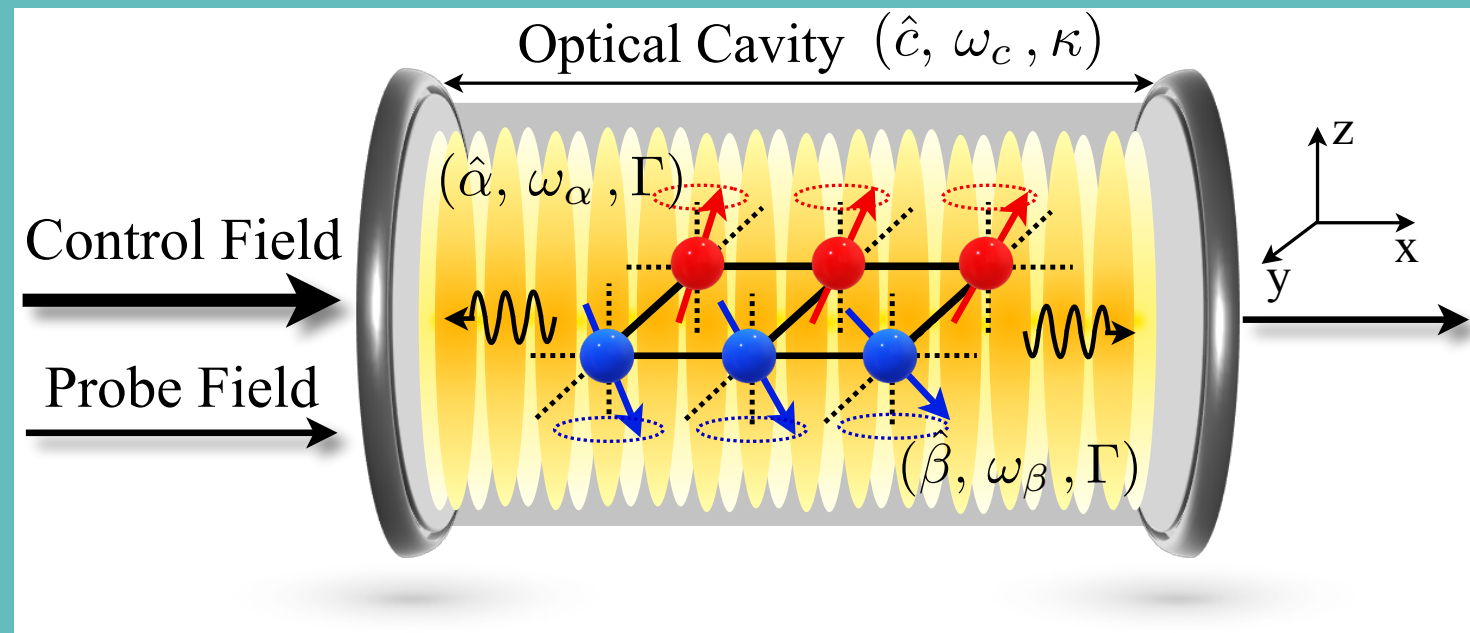


- One order of magnitude gain in coupling
- **However very lossy optical mode**

further work needed



Cavity Optomagnonics with Antiferromagnets



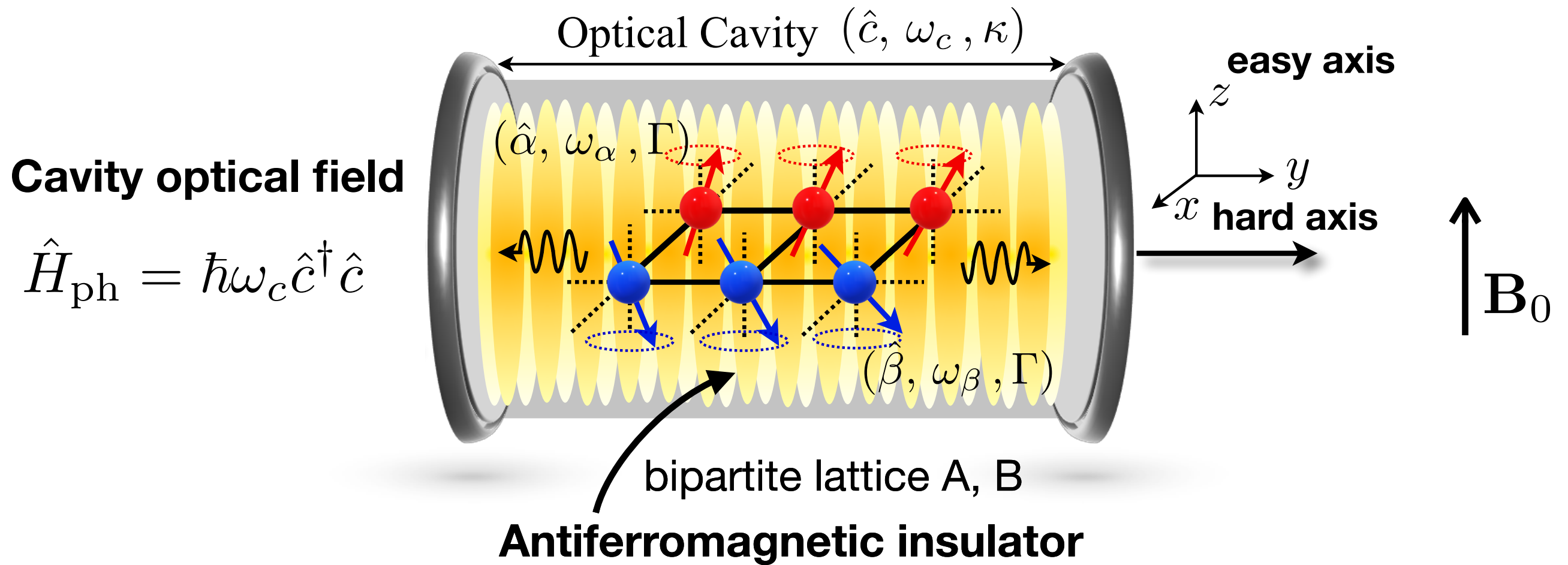
T.S. Parvini, V.A.S.V. Bittencourt, SVK
Phys. Rev. Res. 2, 022027(R) (2020)



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Cavity optomagnonics with AFMs



easy axis anisotropy

$$\hat{H}_{\text{AFM}} = \hbar \sum_{\langle i \neq j \rangle} J \hat{\mathbf{S}}^i \cdot \hat{\mathbf{S}}^j + \hbar |\gamma| \mathbf{B}_0 \cdot \sum_i \hat{\mathbf{S}}^i - \frac{\hbar K_{\parallel}}{2} \sum_i \left(\hat{S}_z^i \right)^2 + \frac{\hbar K_{\perp}}{2} \sum_i \left(\hat{S}_x^i \right)^2$$

hard axis anisotropy

AFMs: Optomagnonic coupling

Fleury
& Loudon
1968

$$\rightarrow \hat{H}_{\text{int}} = \sum_{\mu, \nu, \mathbf{R}} E_1^\mu E_2^\nu \chi^{\mu\nu}(\mathbf{R})$$

permittivity correction

$$\chi^{\mu\nu}(\mathbf{R}) = \sum_{\gamma} K_{\mu\nu\gamma}(\mathbf{R}) S_{\mathbf{R}}^{\gamma}$$

$$\hat{\mathcal{H}}_{\text{OM}} = -\hbar G \hat{c}^\dagger \hat{c} (g_\alpha \hat{a}^\dagger + g_\beta \hat{b}^\dagger + \text{h.c.})$$

photon two magnon branches

$$g_{\alpha(\beta)} = \left(u_{\alpha(\beta)}^+ + v_{\alpha(\beta)}^+ \right) + K \left(u_{\alpha(\beta)}^- + v_{\alpha(\beta)}^- \right)$$

Bogoliubov transformation
coefficients:

from sublattice to collective modes

AFMs: Optomagnonic coupling

$$\hat{\mathcal{H}}_{\text{OM}} = -\hbar G \hat{c}^\dagger \hat{c} (g_\alpha \hat{a}^\dagger + g_\beta \hat{\beta}^\dagger + \text{h.c.})$$

Bogoliubov Factor

$$g_{\alpha(\beta)} = \left(u_{\alpha(\beta)}^+ + v_{\alpha(\beta)}^+ \right) + K \left(u_{\alpha(\beta)}^- + v_{\alpha(\beta)}^- \right)$$

Bogoliubov transformation
coefficients:

from sublattice to collective modes

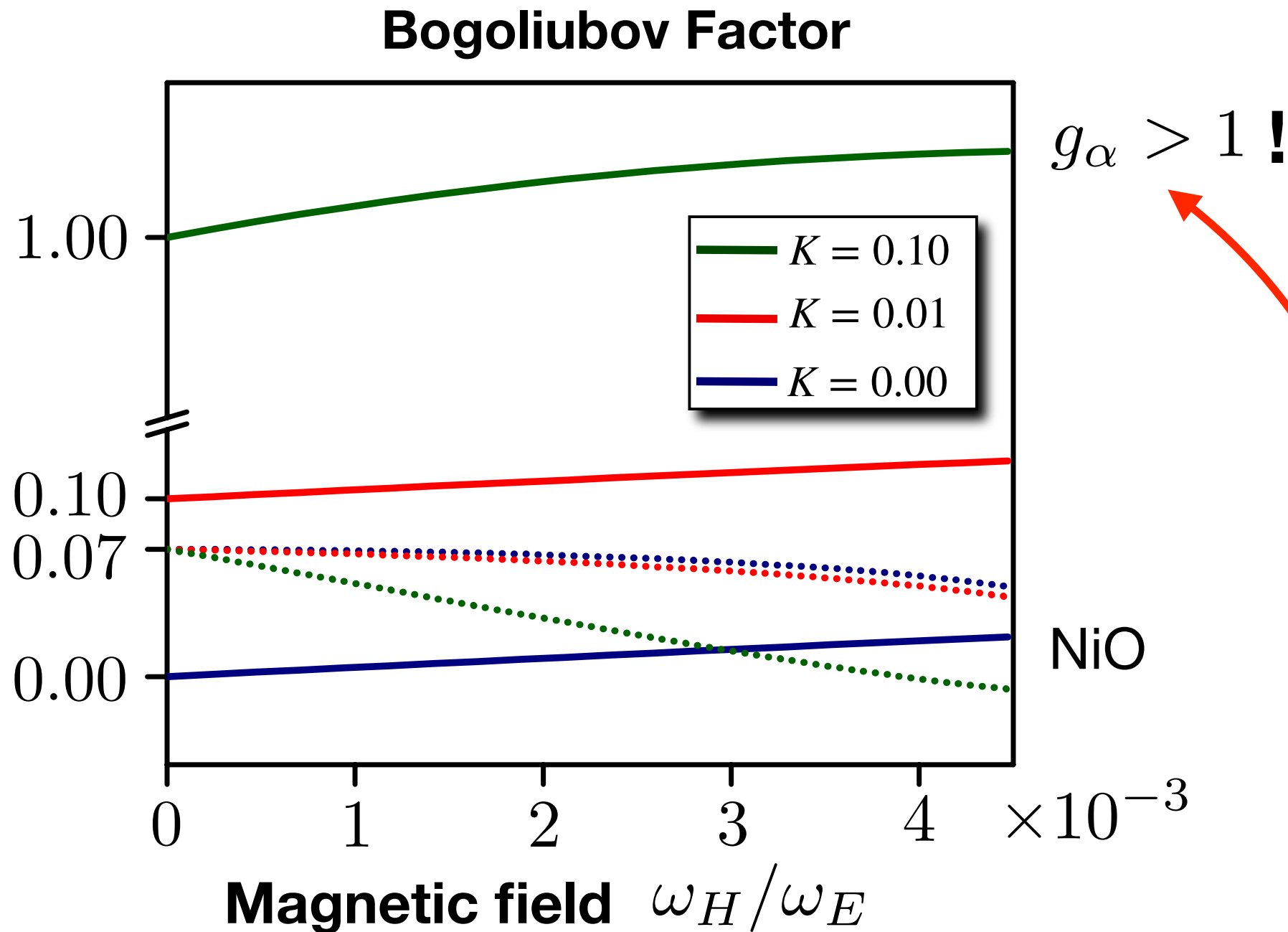
$$K = \frac{K_-}{K_+} \approx 0.01 \quad \begin{array}{l} \text{MnF}_2 \\ \text{FeF}_2 \end{array}$$

characterizes magneto-optical
asymmetry between sublattices

Example: hard-axis dominated AFM

$$\omega_{\perp} > \omega_{\parallel}$$

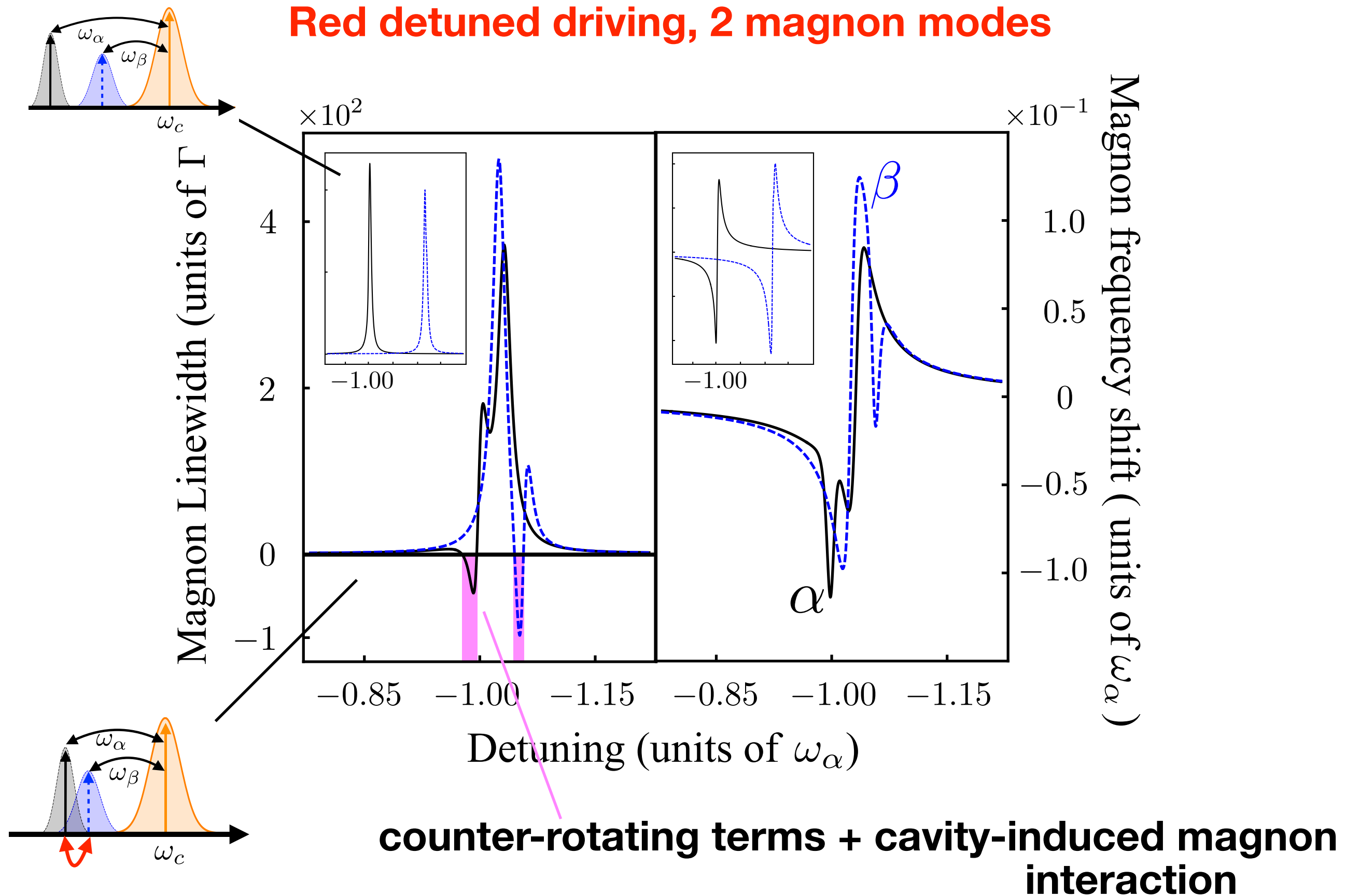
$$\omega_{\parallel}/\omega_E = 1.3 \times 10^{-5} \quad \omega_{\perp}/\omega_E = 7.6 \times 10^{-4}$$



**Enhancement factor possible
for larger magneto-optical anisotropy**

Dynamical response: strong coupling regime

Red detuned driving, 2 magnon modes



Two-magnon processes?

- So far we have used one-magnon Fleury-Loudon processes
- In AFMs, two-magnon processes are usually dominant

$$\hat{H}_{\text{int}} = \sum_{\mu, \nu, \mathbf{R}} E_1^\mu E_2^\nu \chi^{\mu\nu}(\mathbf{R})$$

$$\chi^{\mu\nu}(\mathbf{R}) = \sum_{\gamma} K_{\mu\nu\gamma}(\mathbf{R}) S_{\mathbf{R}}^\gamma + \sum_{\gamma, \delta} G_{\mu\nu\gamma\delta}(\mathbf{R}) S_{\mathbf{R}}^\gamma S_{\mathbf{R}}^\delta + \sum_{\gamma, \delta, \mathbf{r}} L_{\mu\nu\gamma\delta}(\mathbf{R}, \mathbf{r}) S_{\mathbf{R}}^\gamma S_{\mathbf{R}+\mathbf{r}}^\delta$$

$$\Xi_{\lambda_1 \lambda_2}^{\alpha\beta} = (\hat{\mathbf{e}}_{\lambda_1}^*)^\alpha \hat{\mathbf{e}}_{\lambda_2}^\beta + (\hat{\mathbf{e}}_{\lambda_1}^*)^\beta \hat{\mathbf{e}}_{\lambda_2}^\alpha$$

photons

polarization dependence

$$\begin{aligned} \left[\hat{\mathcal{H}}_R \right]_{\lambda_1 \lambda_2} &= \frac{\hbar S}{2\epsilon_0 V} C \sum_{\mathbf{k}} \sum_{\omega_1, \omega_2} \sqrt{\omega_1 \omega_2} \left\{ \hat{c}_1^\dagger \hat{c}_2 \Xi_{\lambda_1 \lambda_2}^{xy} + \hat{c}_1 \hat{c}_2^\dagger [\Xi_{\lambda_1 \lambda_2}^{xy}]^* \right\} \times \\ &\times \left\{ 2u_{\mathbf{k}} v_{\mathbf{k}} \left(\hat{\alpha}_{\mathbf{k}}^\dagger \hat{\alpha}_{\mathbf{k}} + \hat{\beta}_{-\mathbf{k}}^\dagger \hat{\beta}_{-\mathbf{k}} + 1 \right) + (u_{\mathbf{k}}^2 + v_{\mathbf{k}}^2) \left(\hat{\alpha}_{\mathbf{k}} \hat{\beta}_{-\mathbf{k}} + \hat{\alpha}_{\mathbf{k}}^\dagger \hat{\beta}_{-\mathbf{k}}^\dagger \right) \right\} \end{aligned}$$

magnon pairs

Two-magnon processes + cavity?

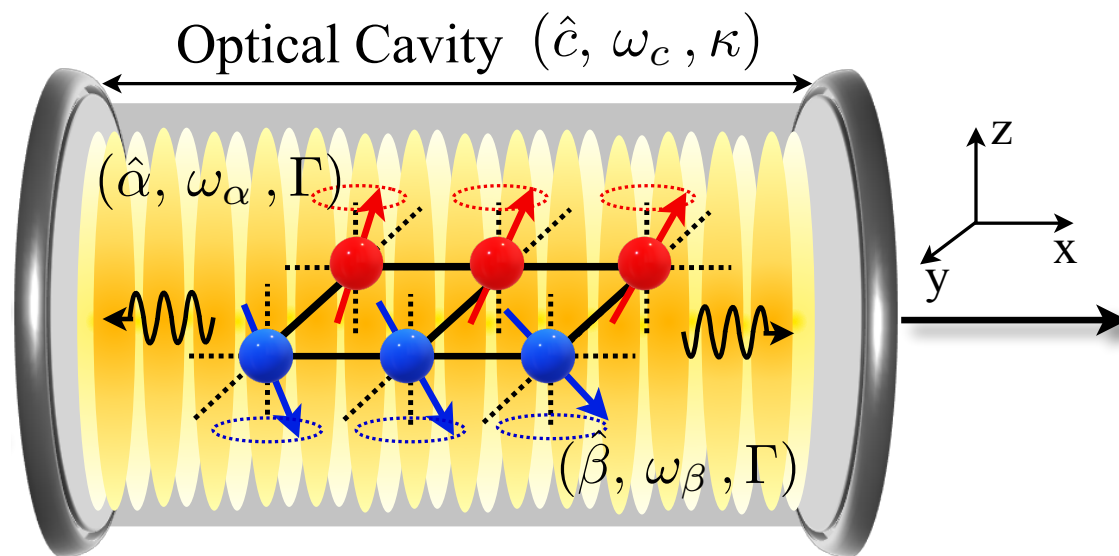
$$\Xi_{\lambda_1 \lambda_2}^{\alpha \beta} = (\hat{\mathbf{e}}_{\lambda_1}^*)^\alpha \hat{\mathbf{e}}_{\lambda_2}^\beta + (\hat{\mathbf{e}}_{\lambda_1}^*)^\beta \hat{\mathbf{e}}_{\lambda_2}^\alpha$$

polarization dependence

photons

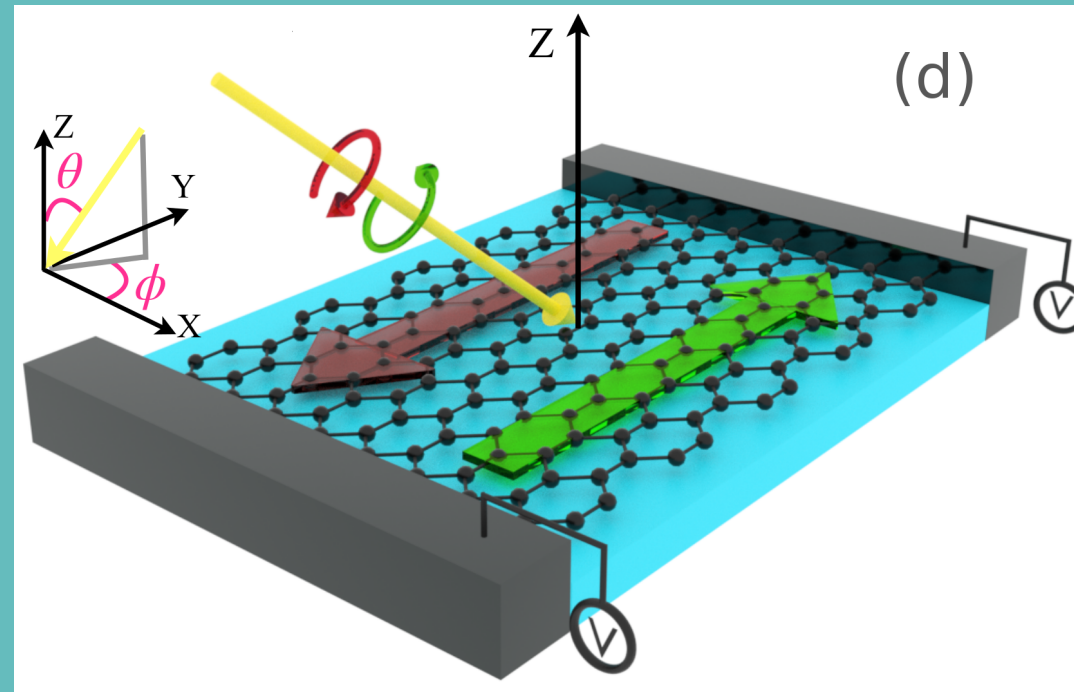
$$\begin{aligned} \left[\hat{\mathcal{H}}_R \right]_{\lambda_1 \lambda_2} &= \frac{\hbar S}{2\epsilon_0 V} C \sum_{\mathbf{k}} \sum_{\omega_1, \omega_2} \sqrt{\omega_1 \omega_2} \left\{ \hat{c}_1^\dagger \hat{c}_2 \Xi_{\lambda_1 \lambda_2}^{xy} + \hat{c}_1 \hat{c}_2^\dagger [\Xi_{\lambda_1 \lambda_2}^{xy}]^* \right\} \times \\ &\times \left\{ 2u_{\mathbf{k}} v_{\mathbf{k}} \left(\hat{\alpha}_{\mathbf{k}}^\dagger \hat{\alpha}_{\mathbf{k}} + \hat{\beta}_{-\mathbf{k}}^\dagger \hat{\beta}_{-\mathbf{k}} + 1 \right) + (u_{\mathbf{k}}^2 + v_{\mathbf{k}}^2) \left(\hat{\alpha}_{\mathbf{k}} \hat{\beta}_{-\mathbf{k}} + \hat{\alpha}_{\mathbf{k}}^\dagger \hat{\beta}_{-\mathbf{k}}^\dagger \right) \right\} \end{aligned}$$

magnon pairs



Coming soon!

All-Optical Generation of Antiferromagnetic Magnon Currents via the Magnon Circular Photogalvanic Effect



E.V. Böstrom, T.S. Parvini, J.W. McIver, A. Rubio, SVK, M.A. Sentef,
arXiv:2104.10914 (2021)



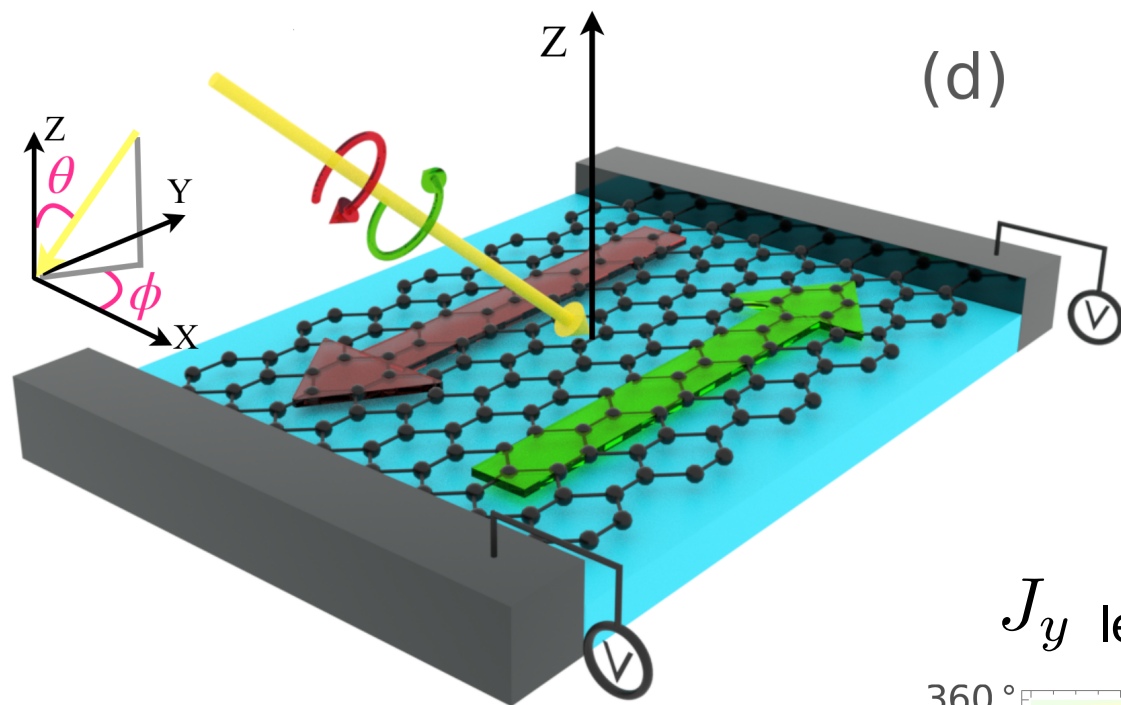
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Magnon circular photogalvanic effect in 2D AFMs

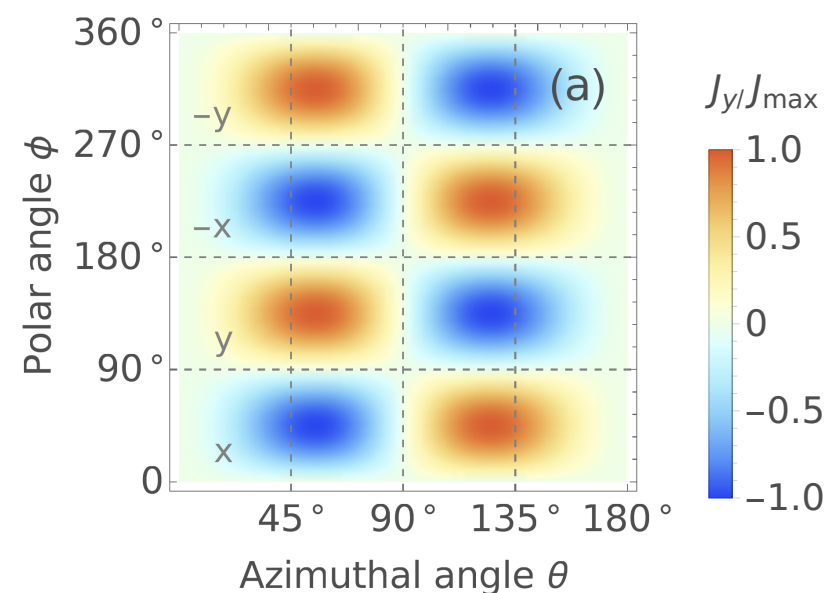
- Directed magnon currents via stimulated two-magnon Raman scattering
- Current controlled by polarization and angle of incidence of light
- Measurable by Inverse Spin Hall Effect



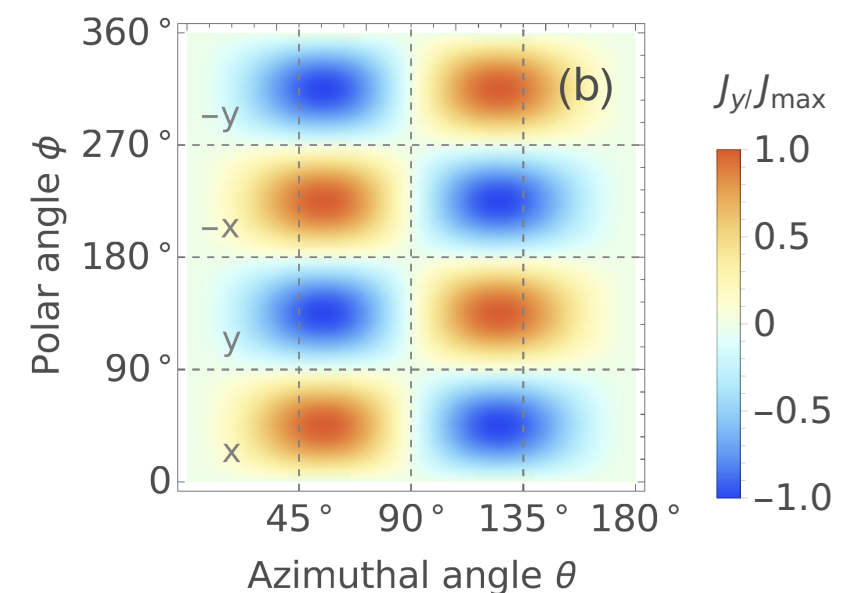
optical susceptibility

$$\langle \mathbf{J} \rangle = \zeta \text{Im}(\sigma) \cos \theta \sin^2 \theta (\sin 2\phi \hat{\mathbf{e}}_y - \cos 2\phi \hat{\mathbf{e}}_x)$$

J_y left-handed light



J_y right-handed light





Outlook

- Cavity-induced dynamical effects can be cast in the form of a LLG equation of motion for the spin with effective magnetic fields and optically induced “Gilbert” damping
- Design of optomagnonic systems in the optical regime shows promise for improved coupling values
- AFMs can present rich new physics: tunable optomagnonic coupling, dark-to-bright transition, cavity-induce magnon interaction
- All-optical generation of magnon currents in 2D by stimulated Raman scattering (2-magnon processes)