

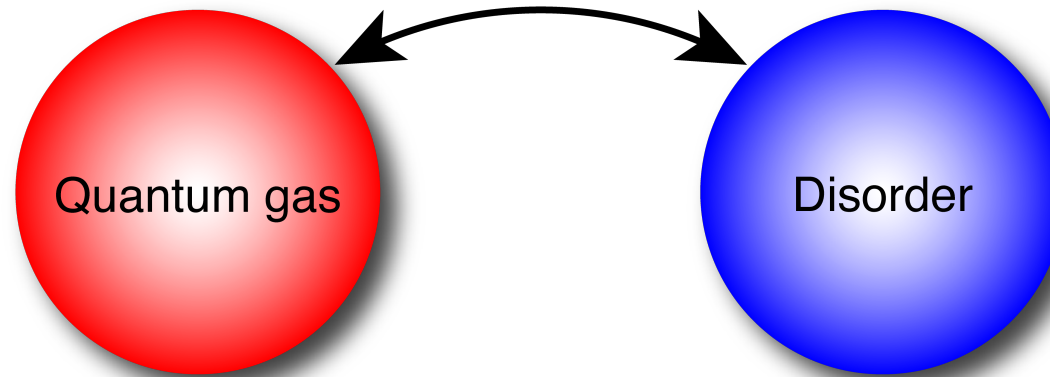
# Nonequilibrium dynamics of quantum gases in time-dependent disorder

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Technische Universität Kaiserslautern

SPICE workshop *Dissipative Phases of Entangled Quantum Matter*  
SFB QuCoLiMa Talk – May 3rd 2021



# Outline



## Noninteracting gases in disorder Anderson localization

J. Billy et al., Nature 453, 891 (2008)  
G. Roati et al., Nature 453, 895 (2008)  
S. Kondov et al., Science 334, 66 (2011)

## Lokalization in interacting lattice systems:

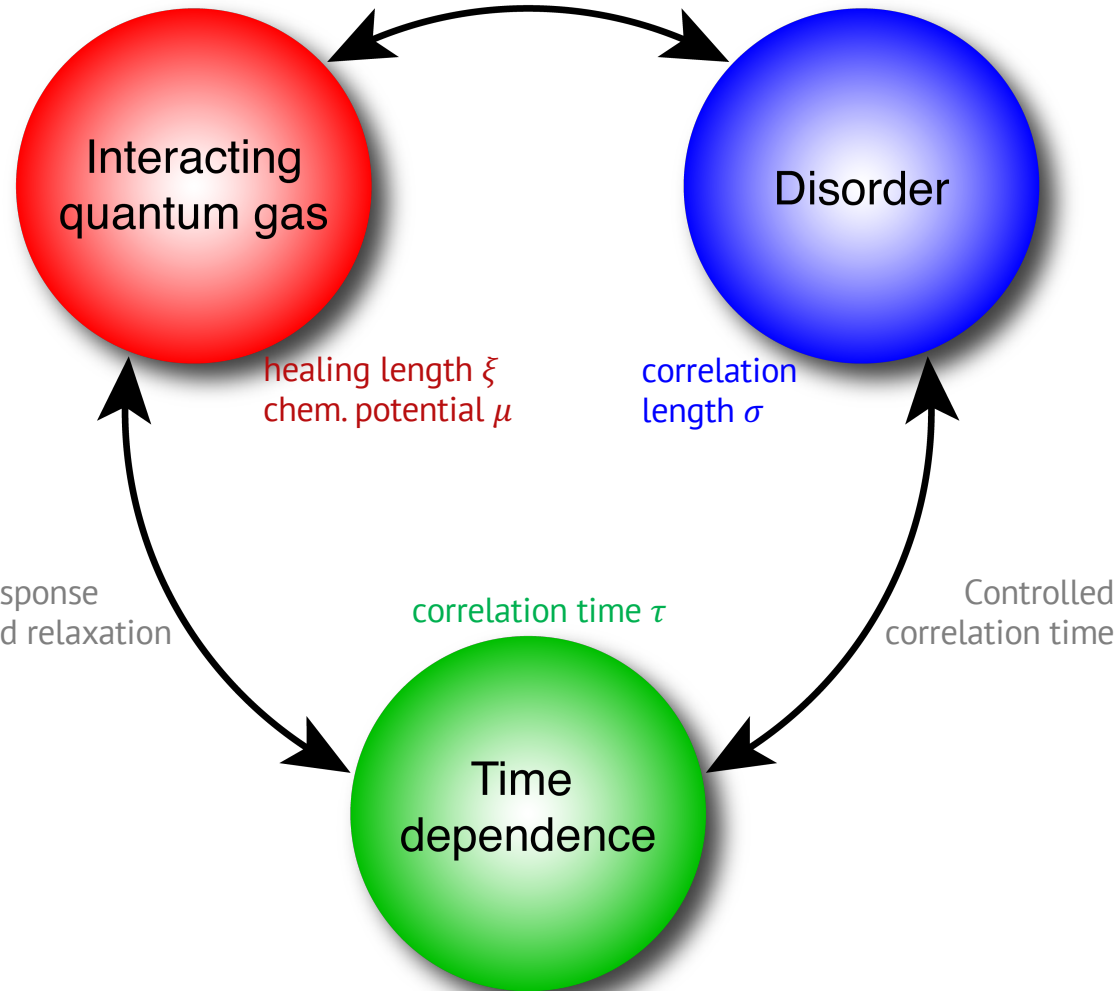
M. Schreiber et al., Science 349, 842 (2015)  
A. Lukin et al., Science 364, 256 (2019)

## Weakly interacting gases:

J. Lye et al., PRL 95, 070401 (2005)  
Y. Chen et al., PRA 77, 033632 (2008)  
D. Dries et al., PRA 82, 033603 (2010)

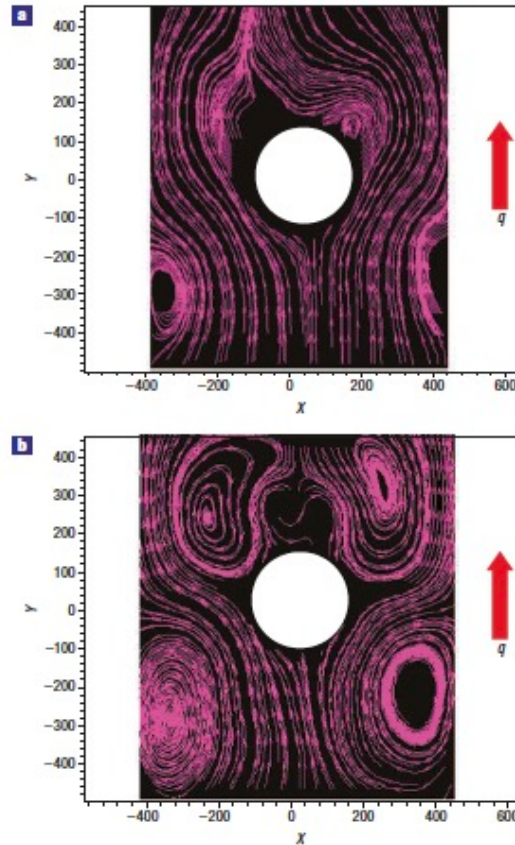
# Outline

Interacting BEC  
BCS superfluid  
Unitary Fermi gas



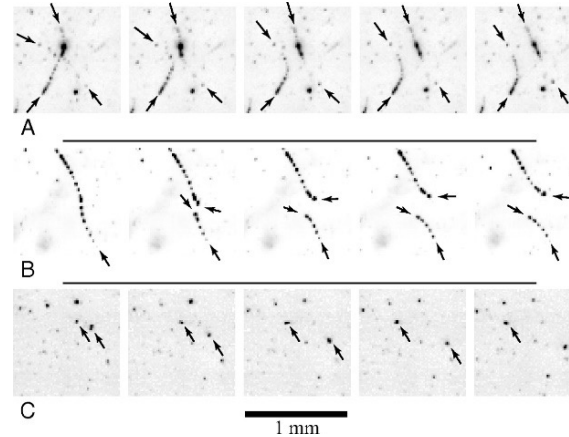
What dominates the response of a quantum system to and relaxation after time-dependent disorder?

## Large-scale turbulence in He-II



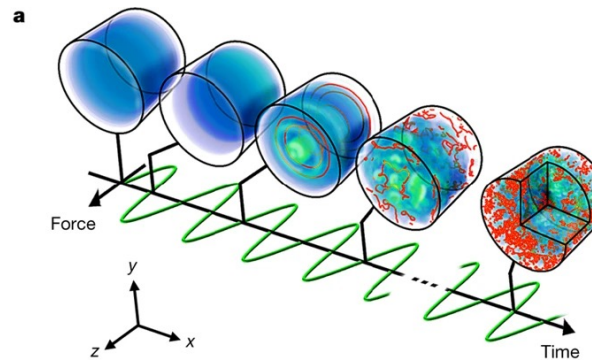
Zhang and Sciver,  
*Nature Phys.* **1**, 36 (2005)

## Reconnecting vortices in He-II



Bewley et al., *PNAS* **105**, 13707 (2008)

## Turbulence in trapped atomic gases

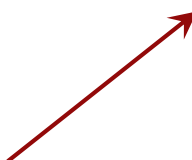


White et al., *PNAS* **111**, 4719 (2014)

Navon et al., *Nature* **539**, 72 (2016)



$$\psi(\vec{r}, t) = \sqrt{n(\vec{r})} \times e^{i\varphi}$$




(Superfluid) amplitude



Quantum phase

What are the contributions of density and phase coherence for quantum dynamics?

What limits the relaxation of a nonequilibrium quantum system?



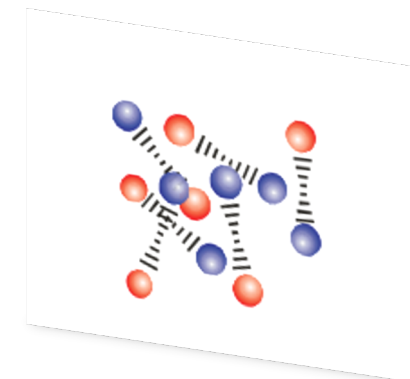
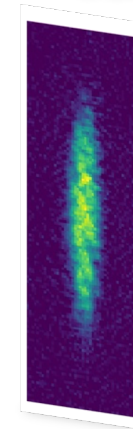
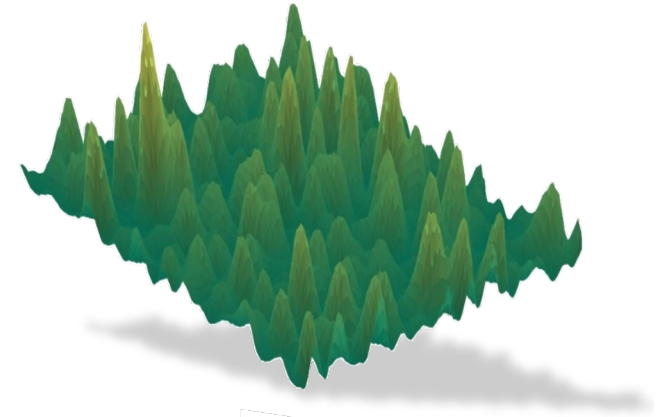
# Outline

Quantum gases along the BEC-BCS crossover in controlled disorder

Probing the role of long-range coherence for quantum dynamics

Response of a BEC and a unitary gas to disorder with dissipation

Quantum gases in dynamical disorder

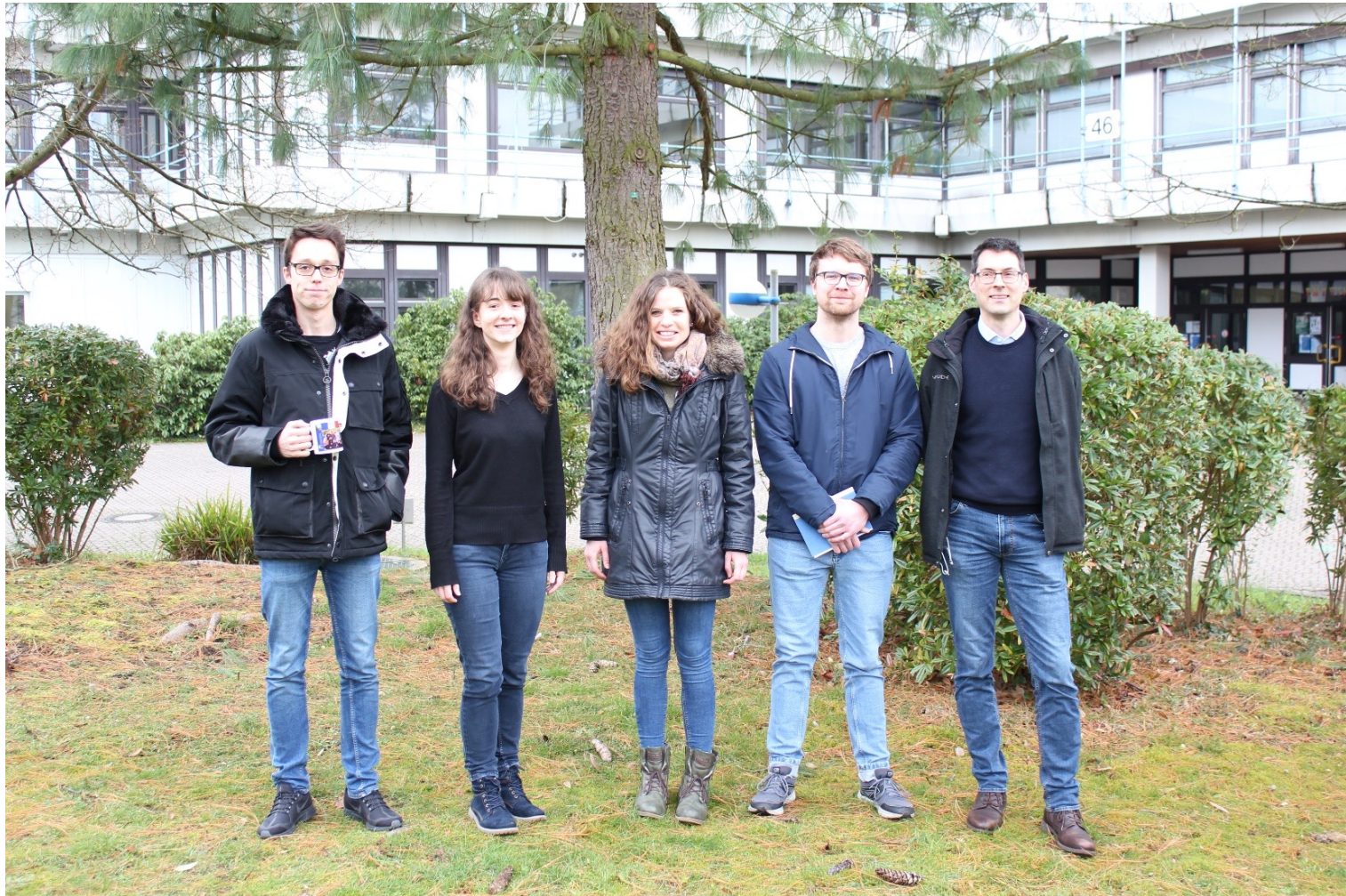


# The Tools –

Quantum gases along the BEC-BCS  
crossover in engineered disorder

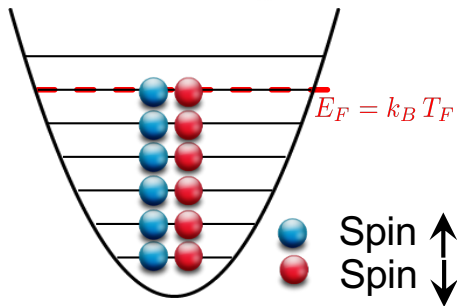
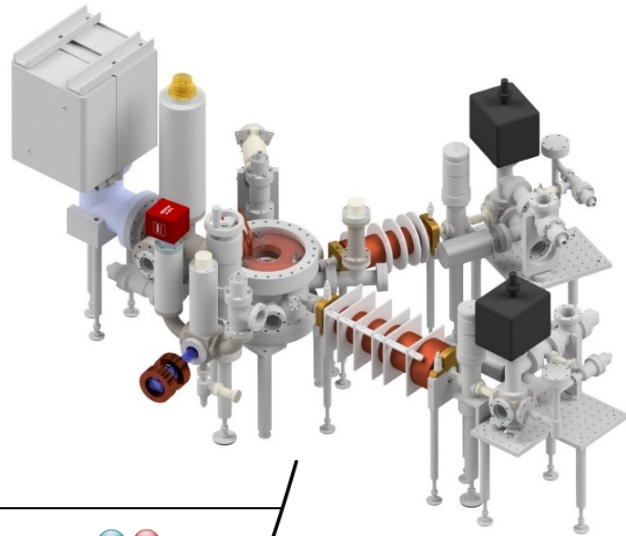


# Fermi Team





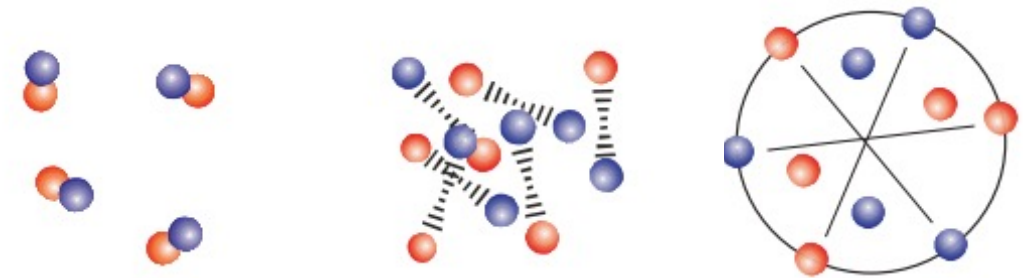
# Degenerate fermionic Li gases



$N = 10^5 \dots 10^6$   $^6\text{Li}$  atoms

$T \approx 100$  nK

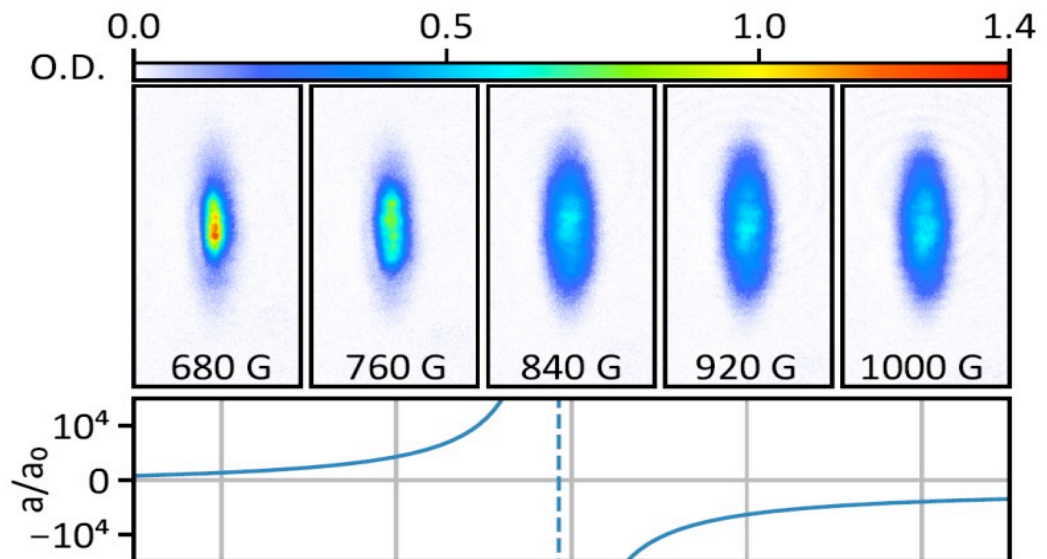
$\frac{N_0}{N} \geq 0.6$  condensate fraction in BEC



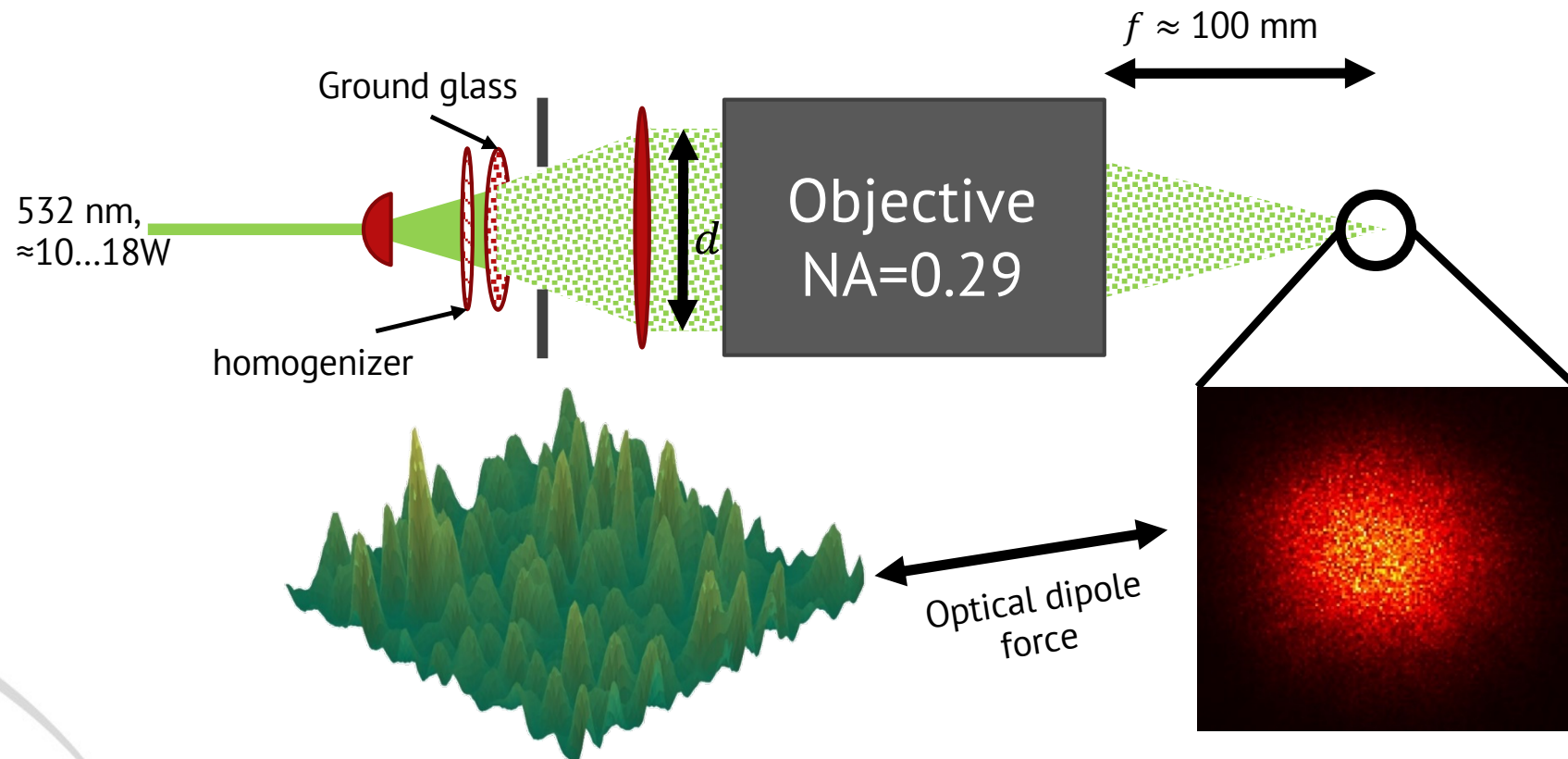
molecular BEC

unitarity

BCS superfluid



# Disordered optical potentials



# Characterization of 3D speckles

- Mean potential depth

$$\langle V_{\text{DIP}} \rangle \sim P/w^2$$

- Correlation length  $\sigma_{\text{trans}} \sim \lambda f/d$

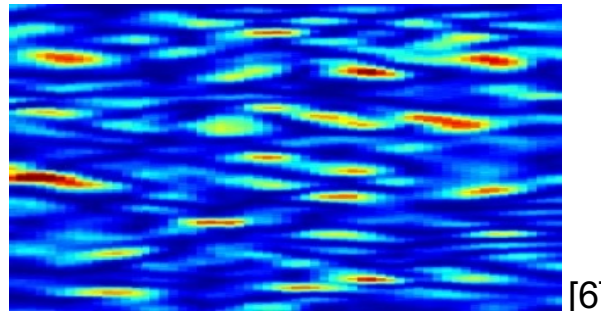
$$C(\vec{\delta r}) = \langle V(\vec{r})V(\vec{r} + \vec{\delta r}) \rangle$$

- anisotropic

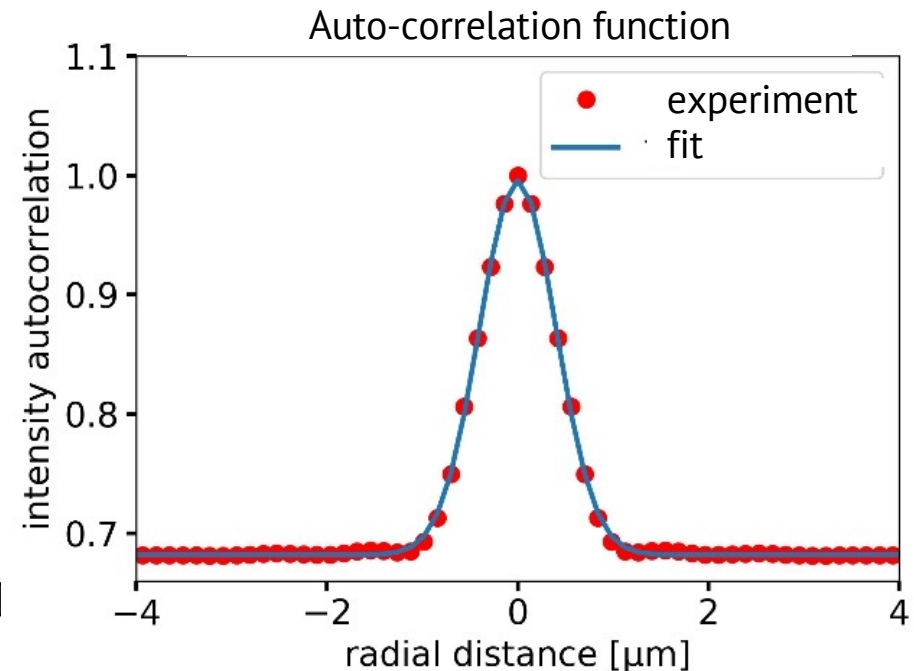
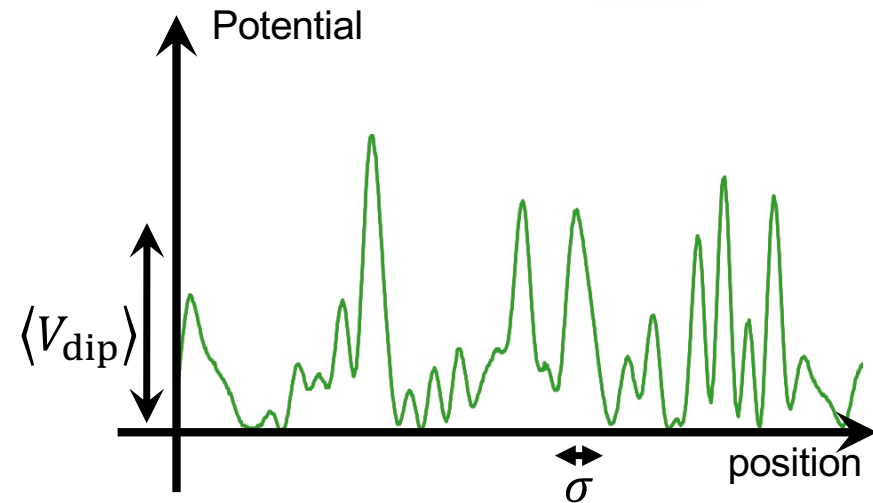
Propagation direction



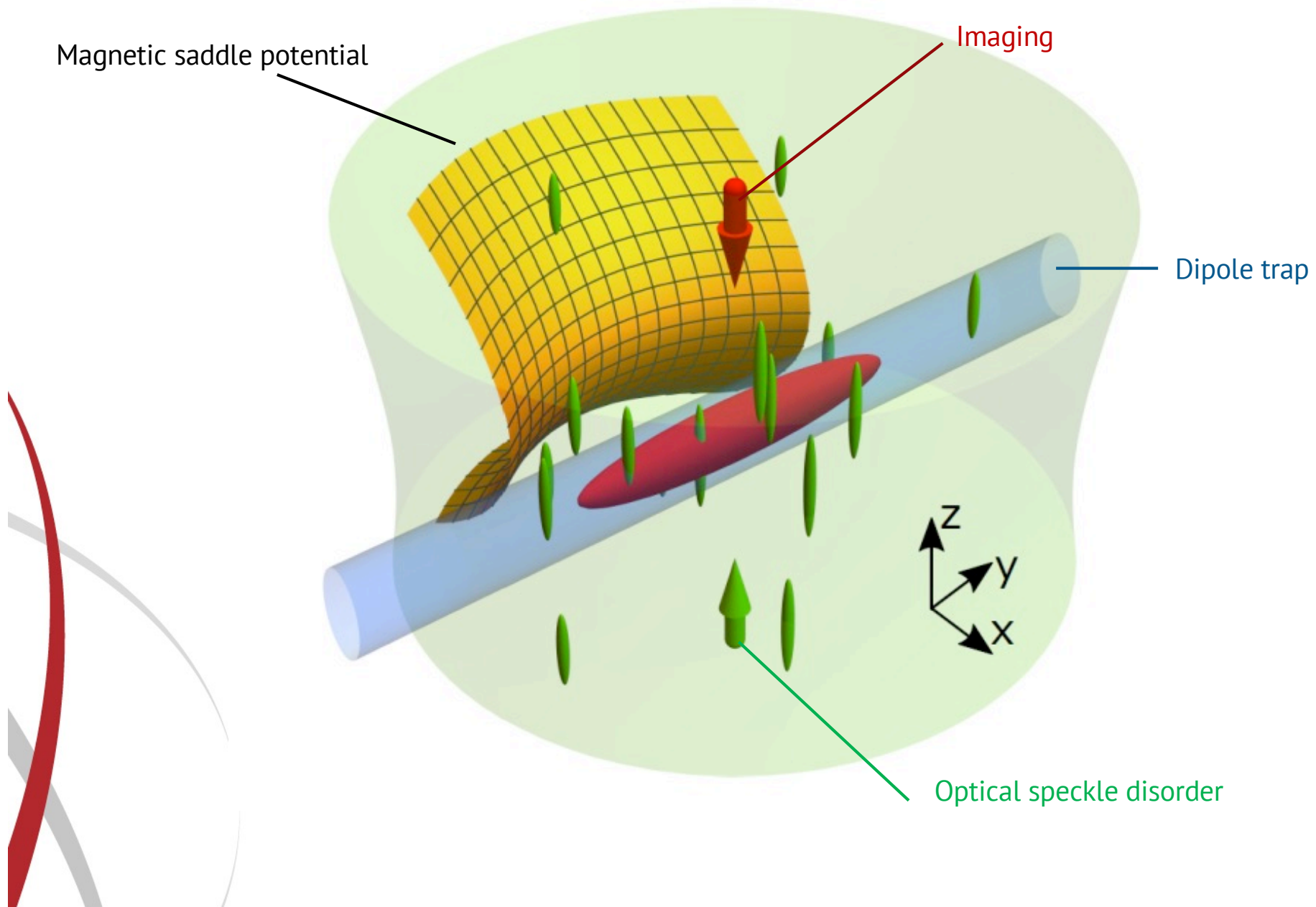
$$\frac{\sigma_{\text{long}}}{\sigma_{\text{trans}}} \approx 6$$



[6]



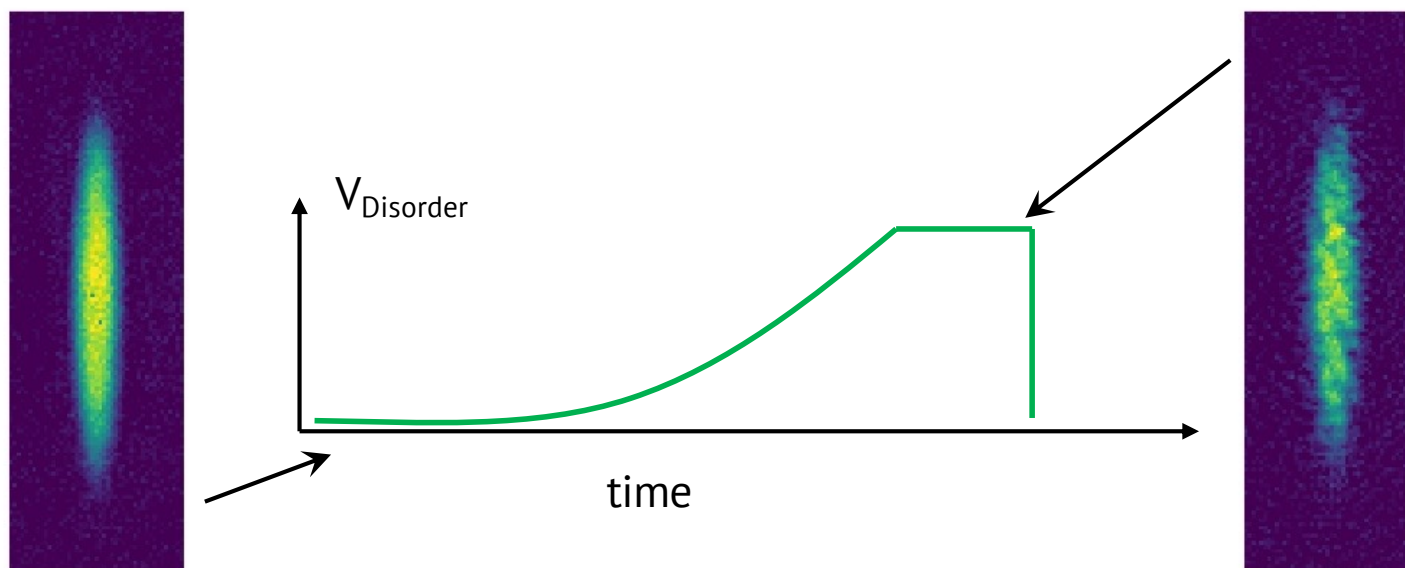
# Experimental Setup



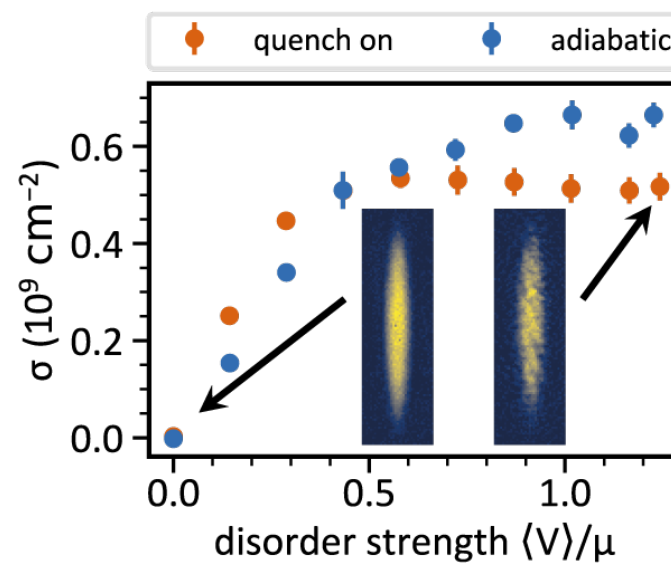
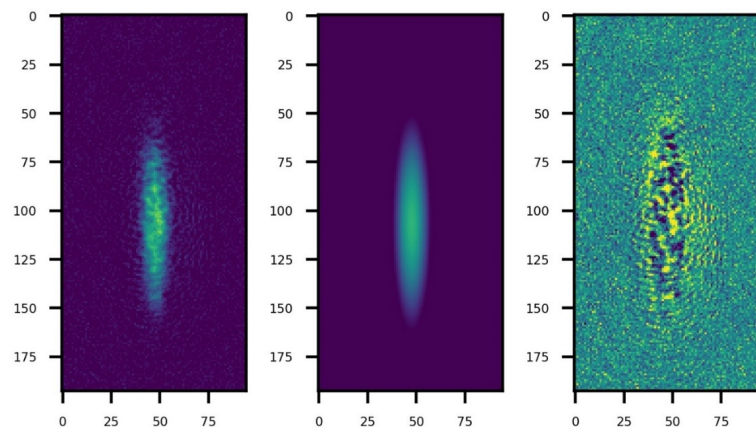


# Molekular BEC response to disorder quenches

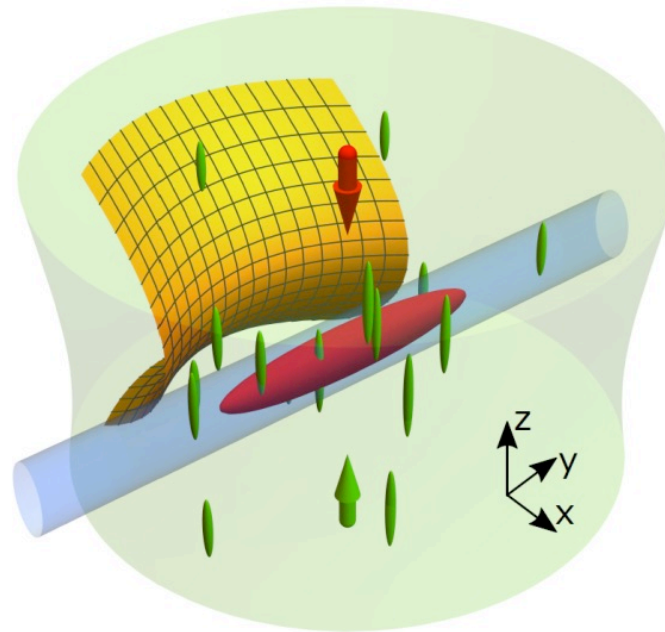
# Density response to disorder



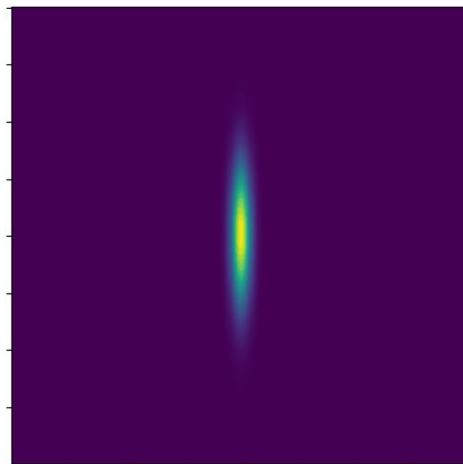
Fluctuations can be quantified:



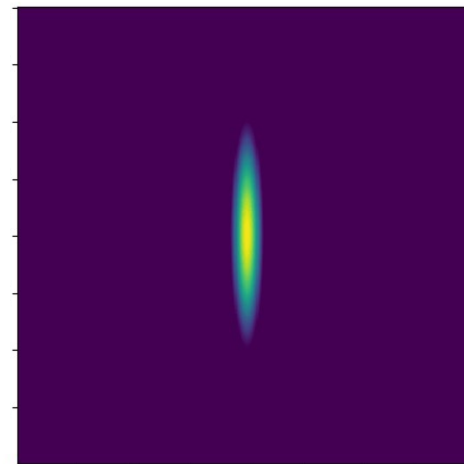
# Hydrodynamic Expansion



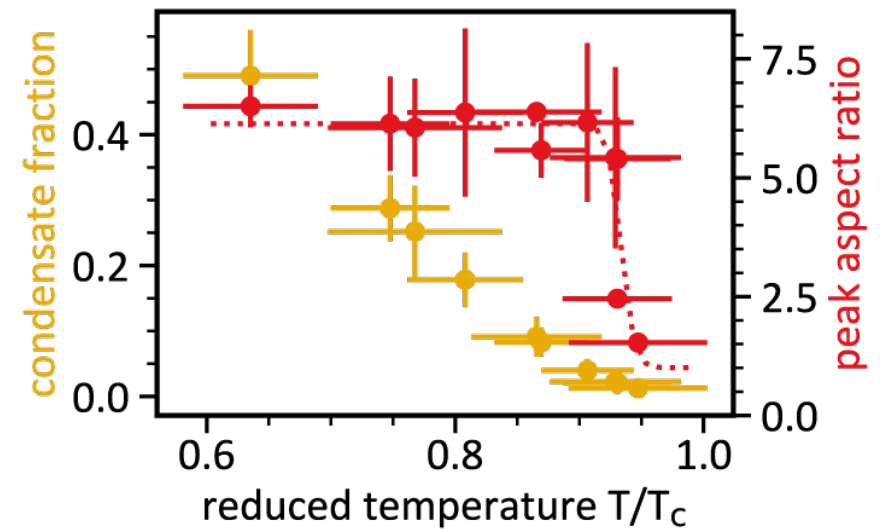
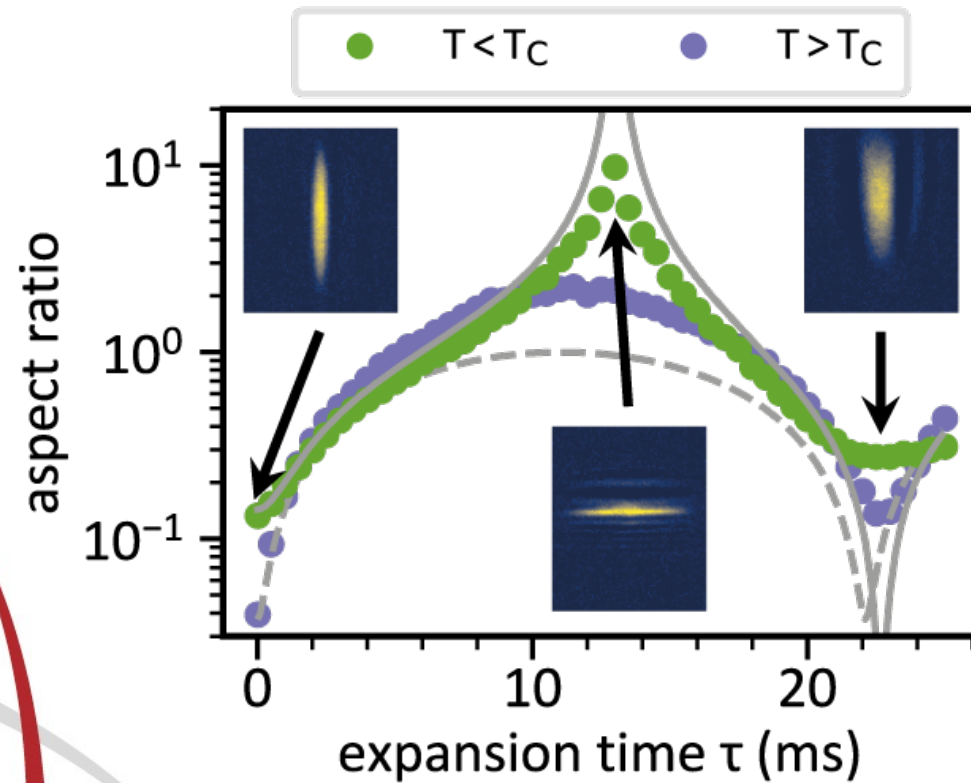
Thermal expansion



Hydrodynamic expansion



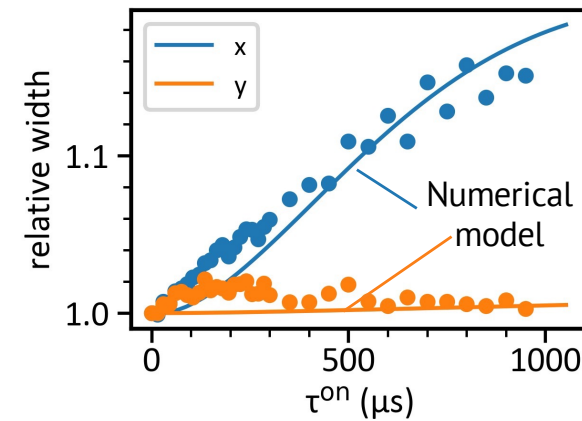
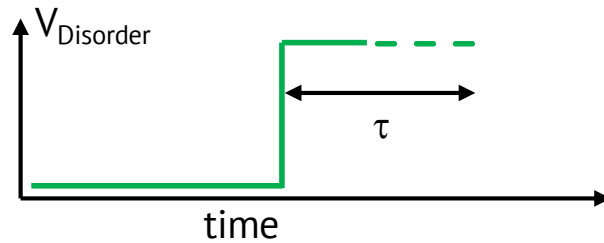
# Hydrodynamic expansion



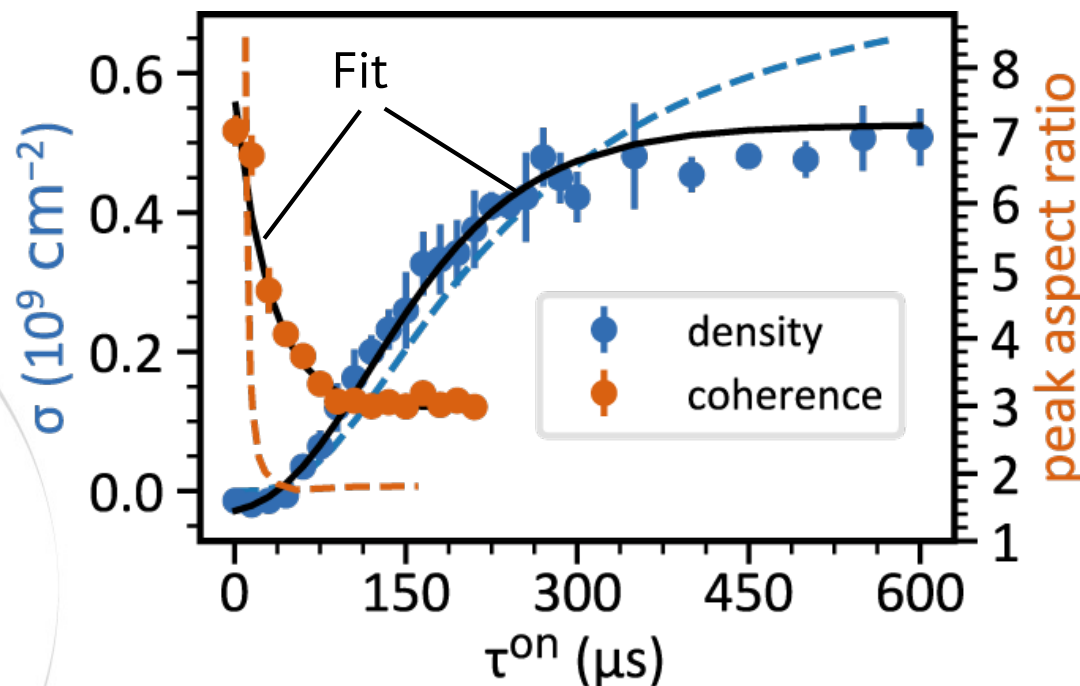
The peak aspect ratio is a measure of long-range coherence.



# Quenching into disorder



What is the **time scale** on which the density and phase coherence respond?



Dashed lines:

-----

3D GPE Simulation



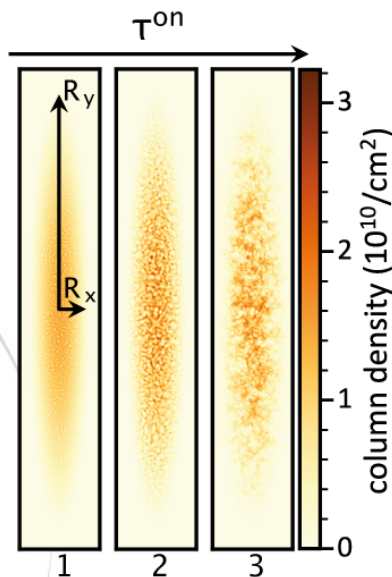
- Split-step Crank-Nicolson approach
- 3D simulation on grid (300,2200,450) with cell size 160 nm
- Speckle shows same statistical properties as in experiment
- Takes optical resolution of speckle and imaging into account
- Assumes  $T = 0$
- 1ms time evolution simulation requires 2 hours of computation time.



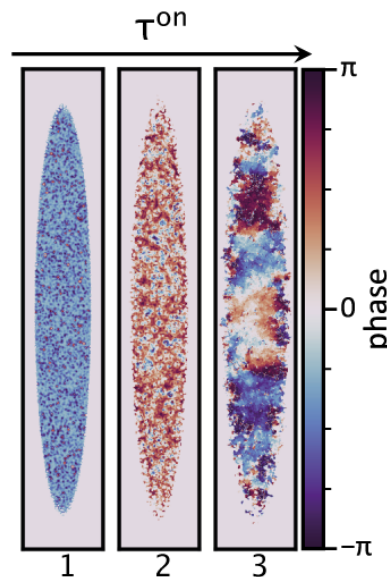
Young et al., *Comput. Phys. Commun.* **220**, 503 (2017)

Muruganam and Adhikari, *Comput. Phys. Commun.* **180**, 1888 (2009)

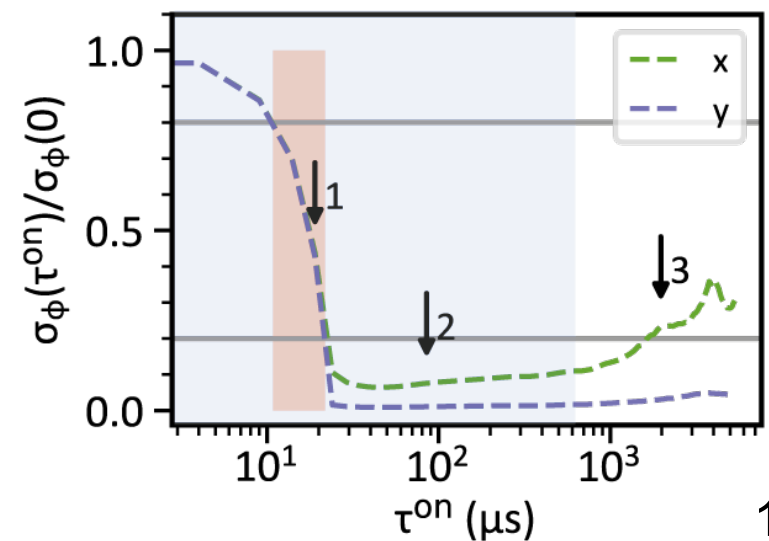
Integrated column density

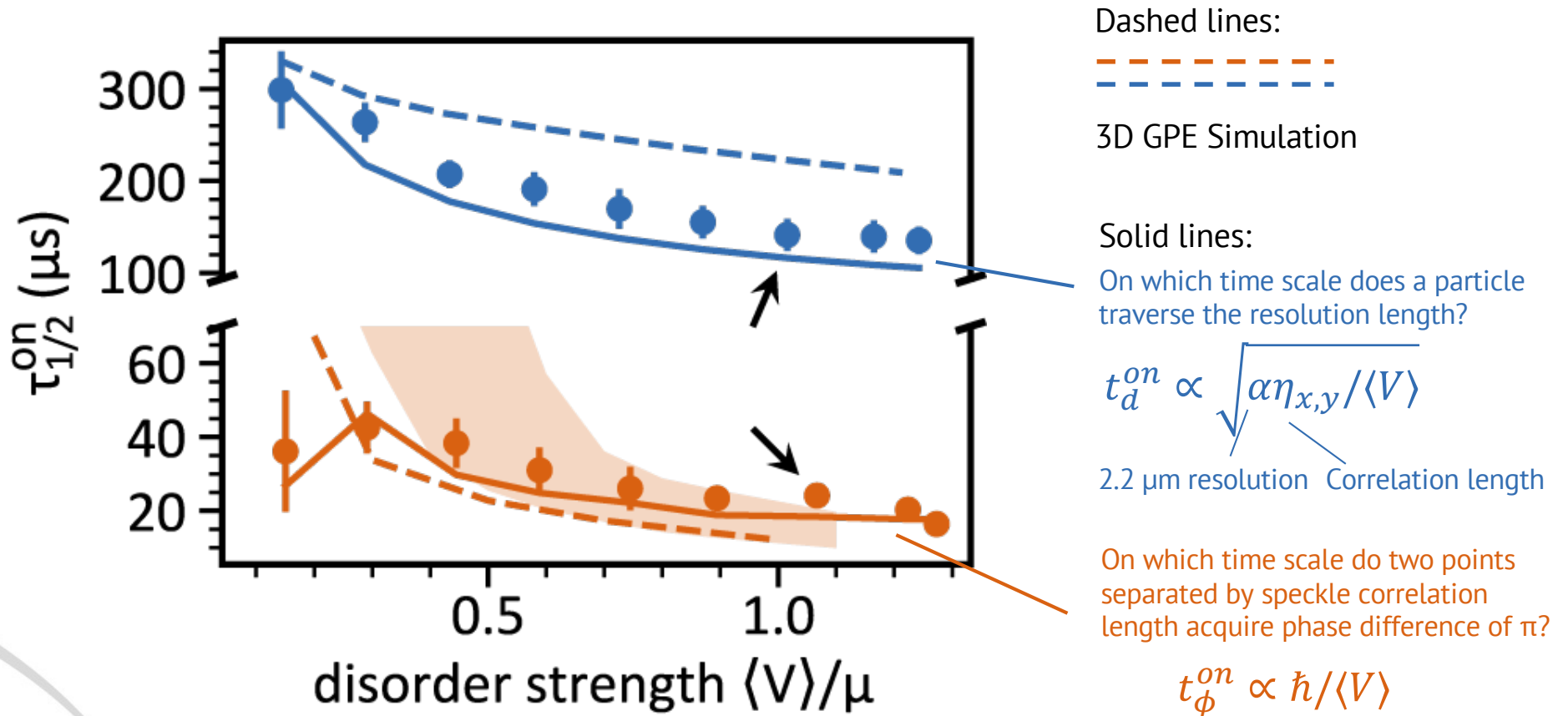


In-plane phase distribution



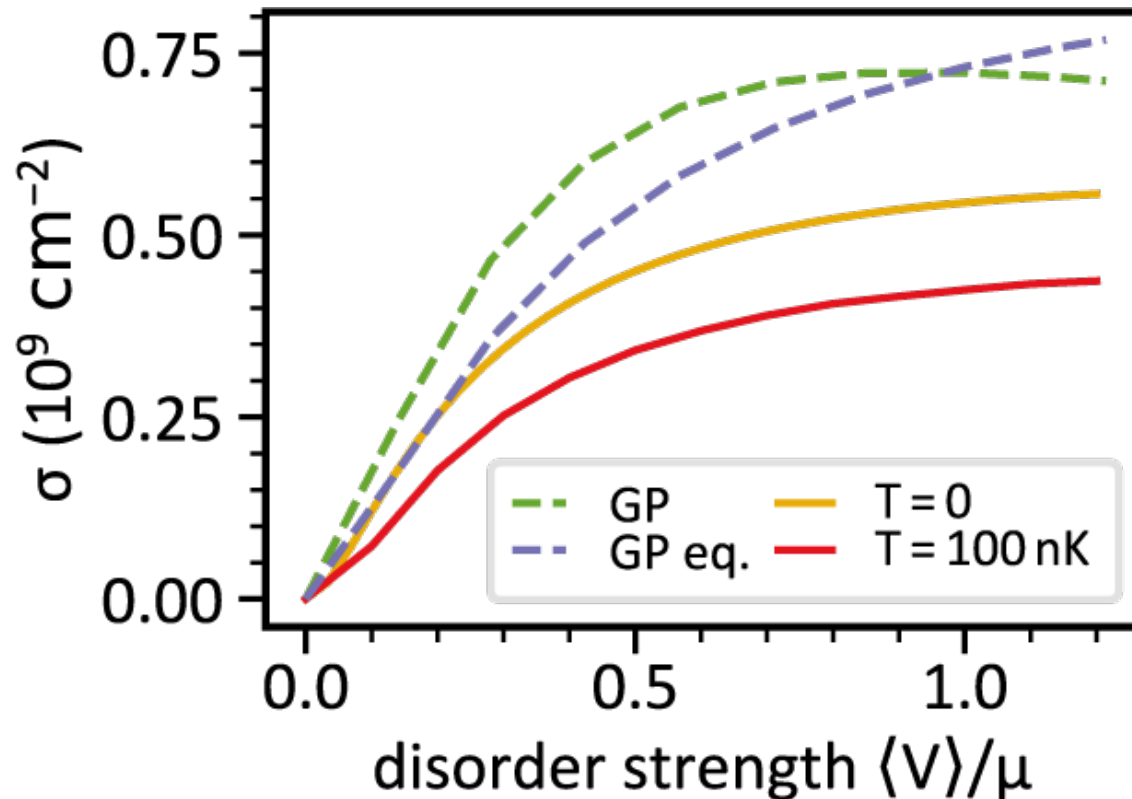
Phase-correlation length  $\sigma_\phi$  of simulated phase distribution





- Density responds **one order of magnitude slower** than quantum hydrodynamics
- Time scale of quantum hydrodynamics can be related to **long-range phase coherence**
- Numerics systematically deviate from experiment.

# Effect of finite temperature



Gross-Pitaevskii  
simulations

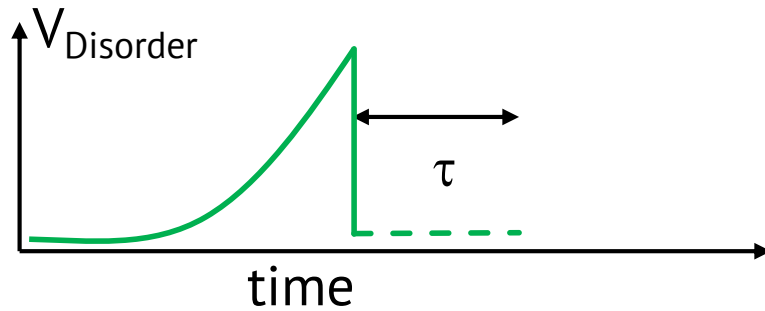
Local-density  
approximation

Local-density approximation breaks down

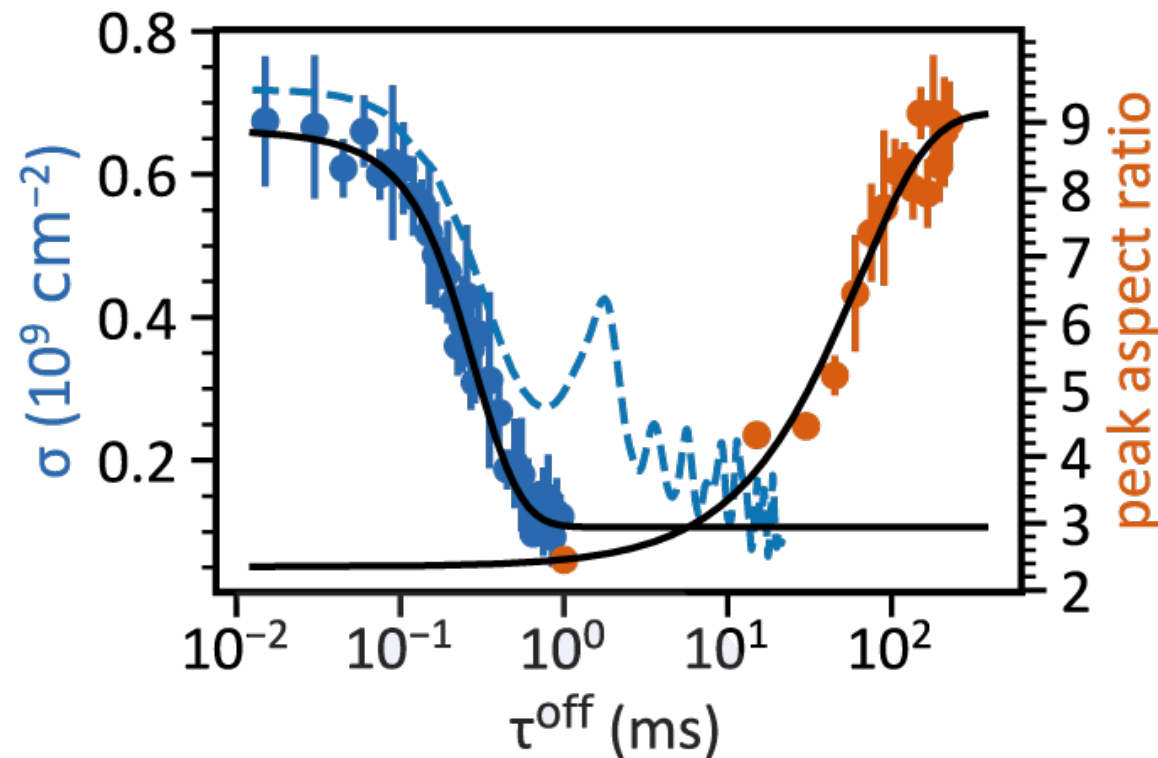
Temperature effects might have a significant impact and lead to the systematic discrepancy with experimental data



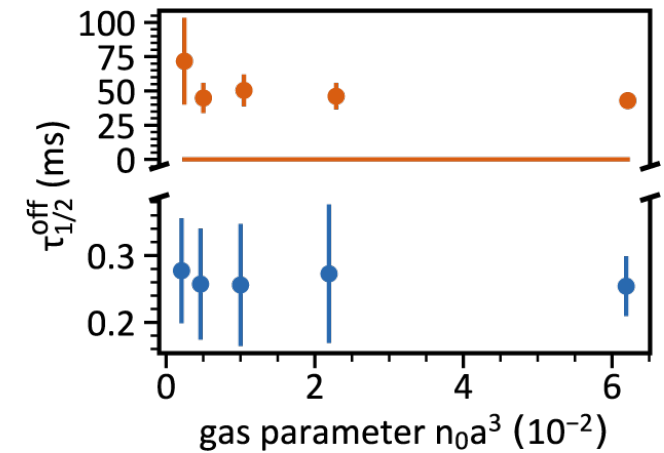
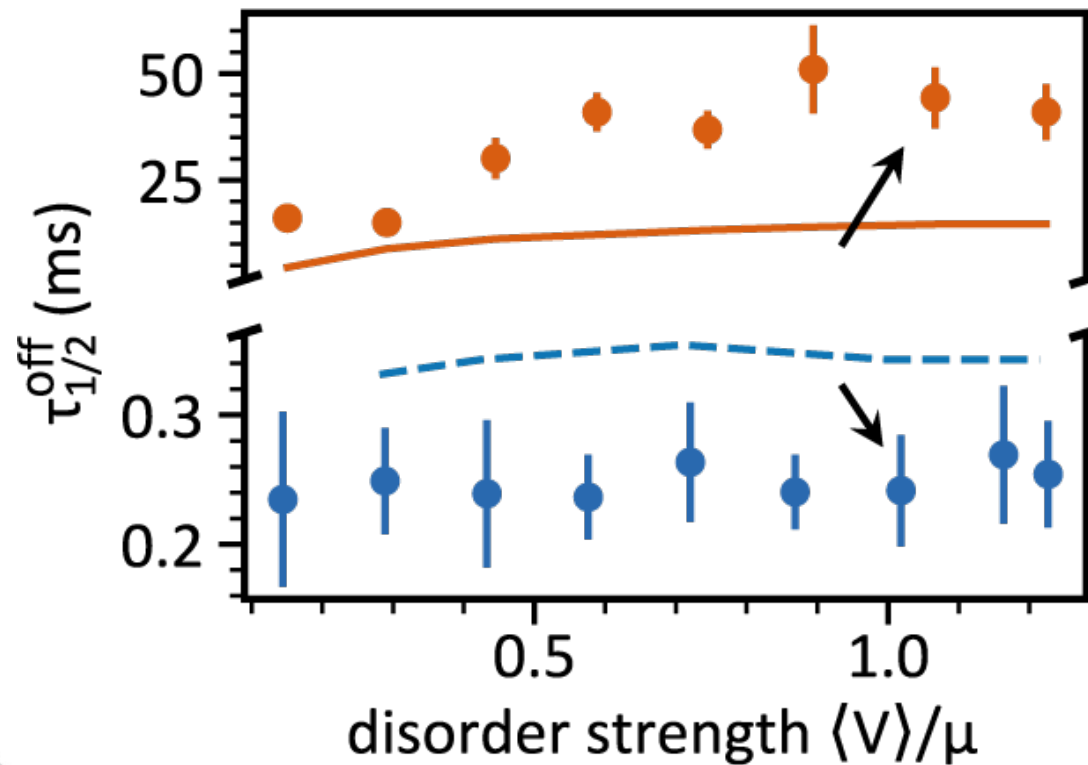
# Quenching out of disorder



What is the **time scale** on which the density and phase coherence respond/relax?



# Quenching out of disorder



Long-range phase coherence needs two orders of magnitude longer to relax compared to the density.

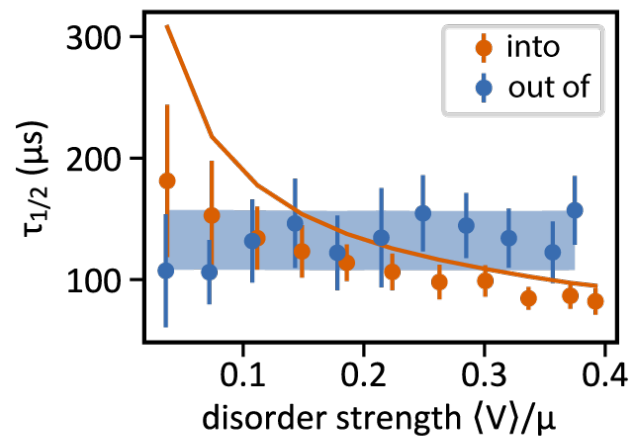
The measured time scale is longer than all time scales in the problem.

Phase excitations are long lived, maybe topologically protected.

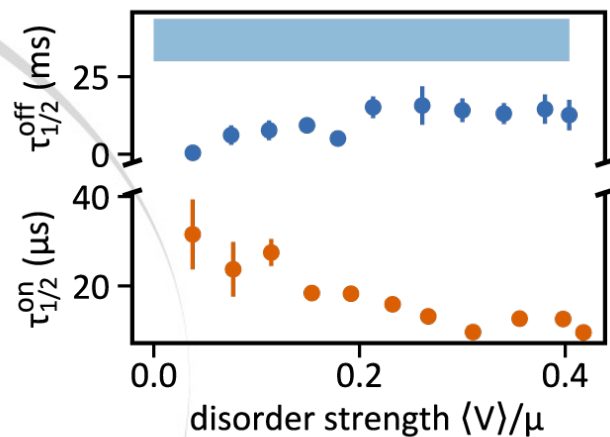
# Toward responses of a unitary gas with dissipation

# Disorder quenches at unitarity

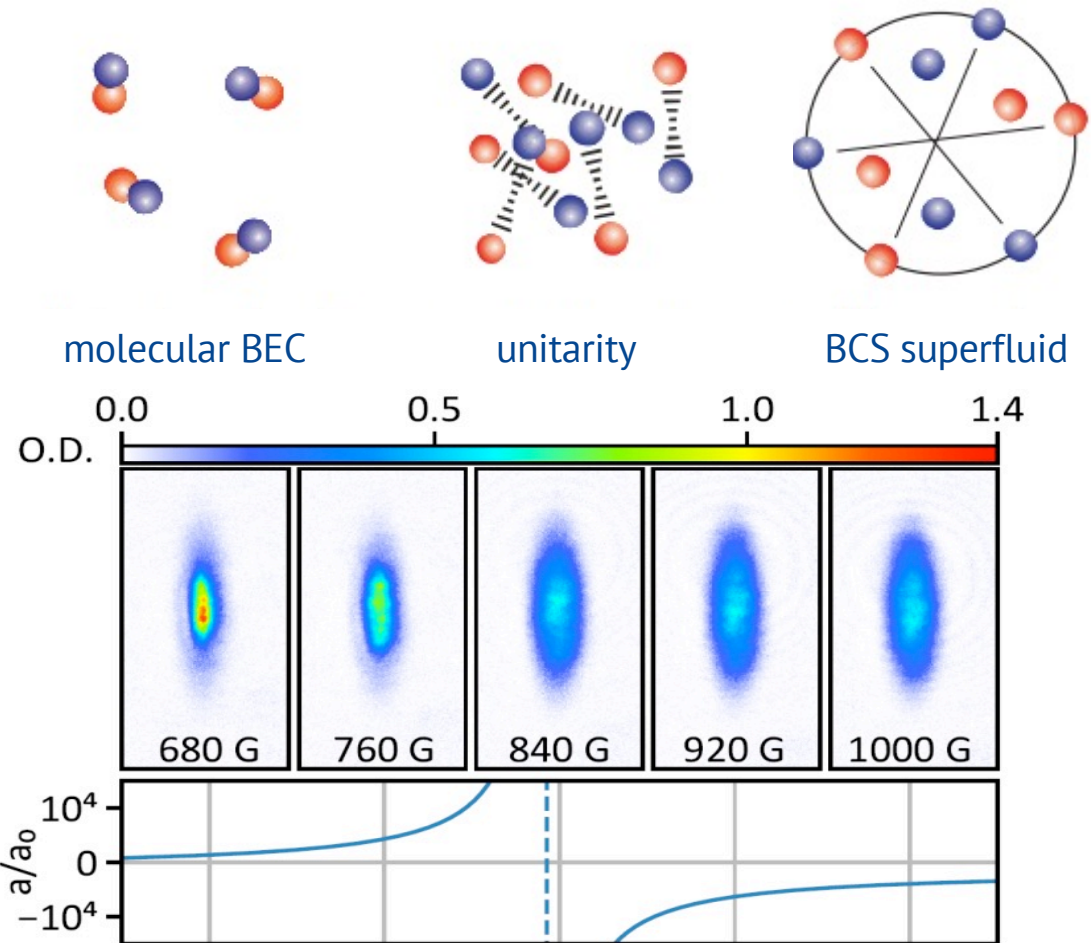
Density response @ unitarity



Phase-coherence response @ unitarity



(Data unpublished)



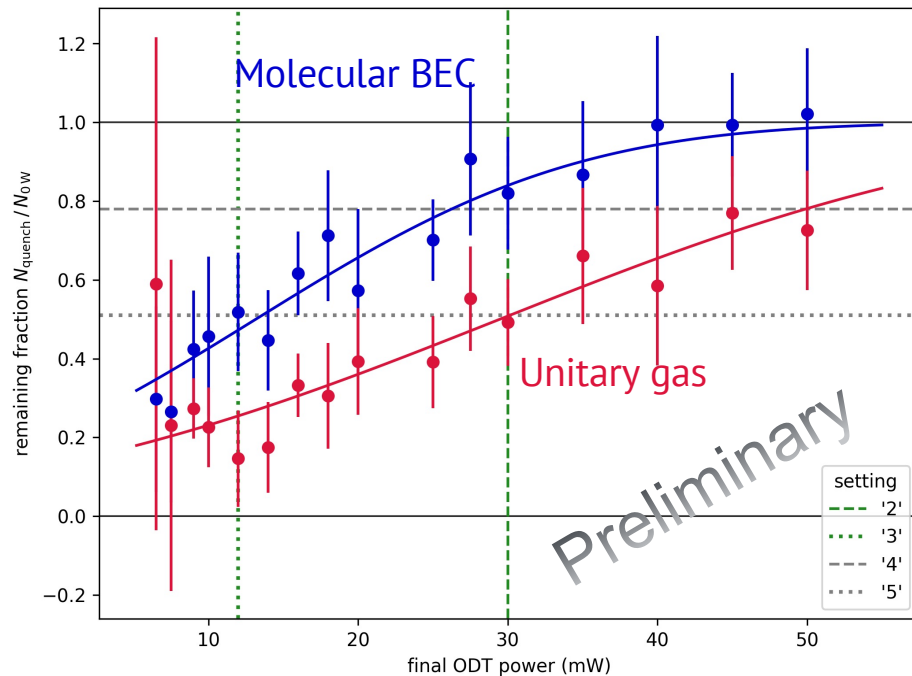
Quenches **into** disorder show comparable time scales.

For quenches **out of** disorder, long-range coherence is established faster.



# Disorder quenches with dissipation

Adjust the trap such that atoms are removed by repulsive disorder speckle.



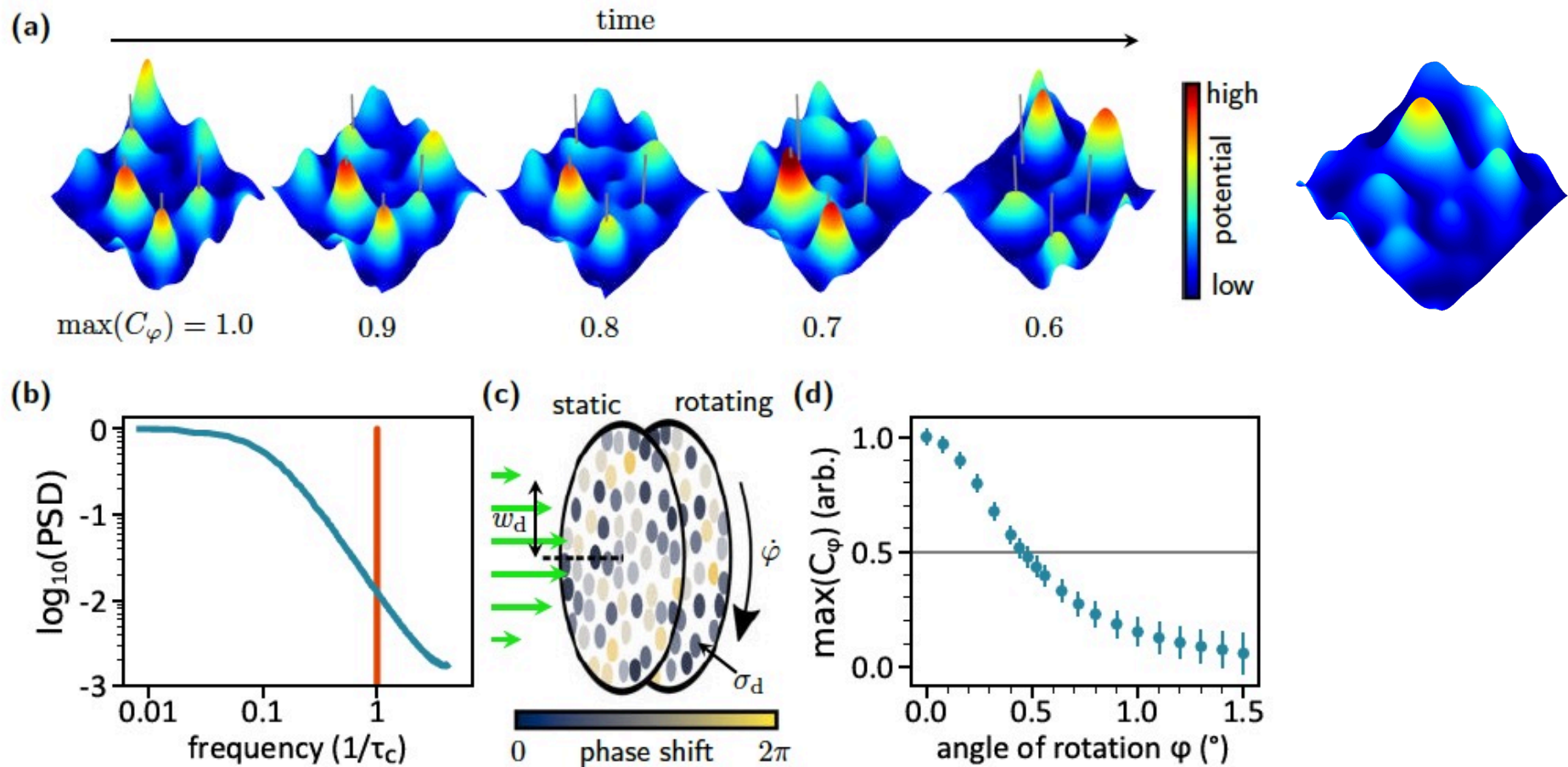
Which system will relax faster and re-establish quantum properties?

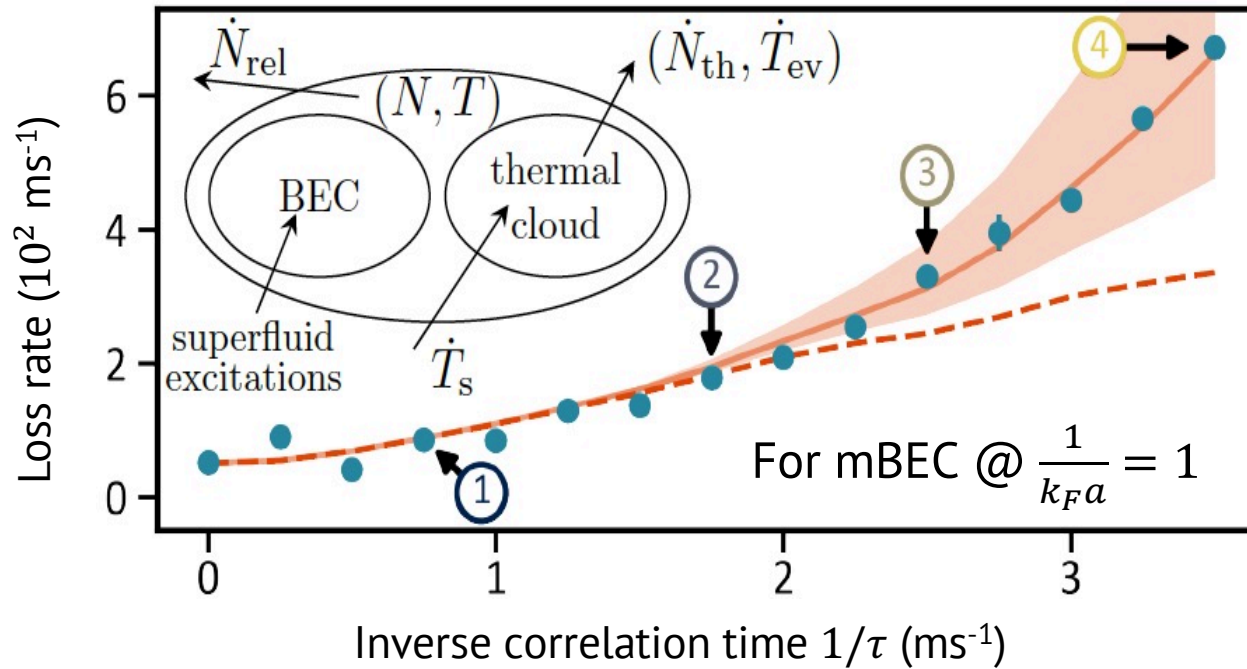
Preliminary observations (work in progress):

- The time scales of density response are not affected by dissipation, neither for quench into nor out of.
- The time scales for quench into disorder **are not affected by dissipation**, neither in BEC nor unitary regime, for phase-coherence response.
- The relaxation to long-range **phase coherence of a unitary gas is unaffected** by dissipation, a **mBEC needs much longer to establish phase coherence** (up to one order of magnitude) -> re-condensation?

# Dynamics in time-dependent disorder potentials

# Tuning correlation times





Cf. Effect on localization: J. Marino's group: Phys. Rev. B **98**, 054302

B. Nagler, S. Hiebel, S. Barbosa, J. Koch, and A. Widera  
preprint, arXiv:2007.11523

# Summary

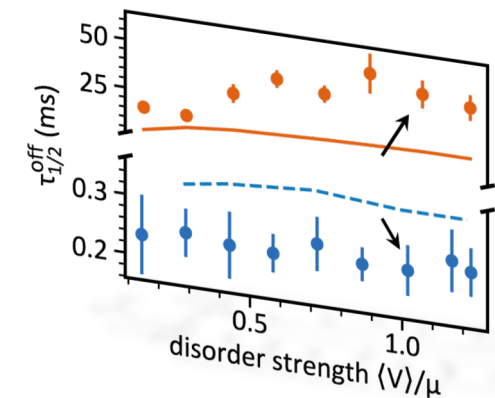
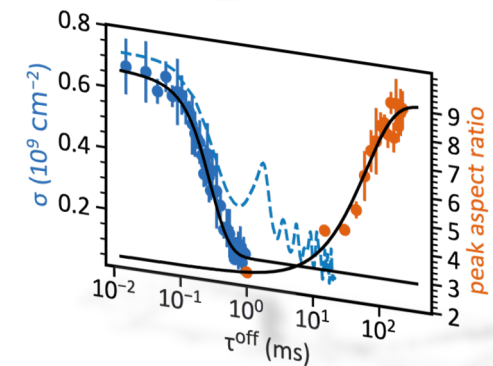
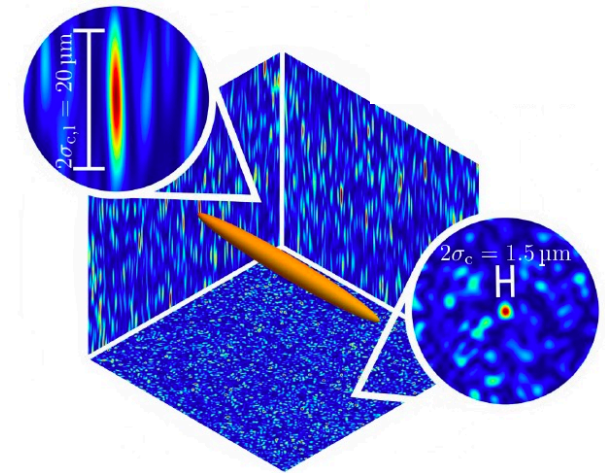
Density and phase-coherence response can be unravelled after disorder quenches

Phase coherence dominates the quantum dynamics: it breaks down faster and revives slower than density

At unitarity, coherent dynamics is re-established much faster...

... even when dissipation is strong.

BEC needs increased times to establish coherent dynamics





# The team

