



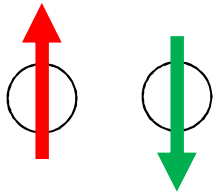
Nano-scale skyrmions and atomic-scale spin textures studied with STM

Kirsten von Bergmann
University of Hamburg

atomic-scale magnetic order: ingredients

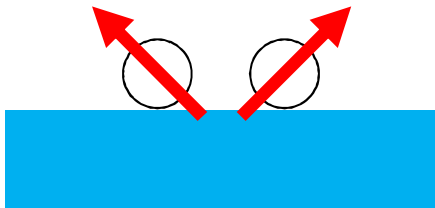
magnetic exchange interaction

$$E = -J (S_1 \cdot S_2)$$

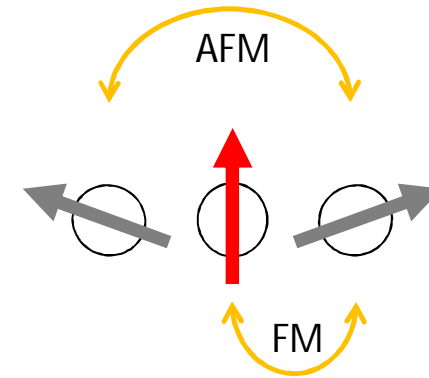


antisymmetric exchange (DMI)
Dzyaloshinskii-Moriya interaction
due to spin-orbit coupling
and broken inversion symmetry

$$E = -D (S_1 \times S_2)$$



exchange frustration

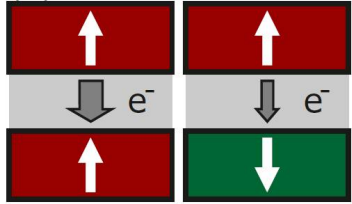


spin-polarized STM

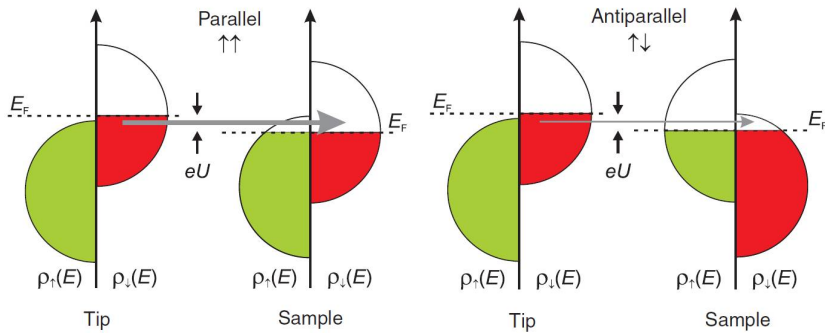
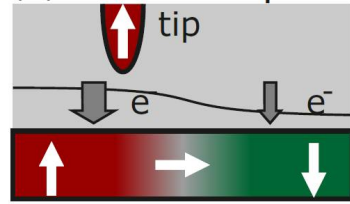
M. Bode, Rep. Prog. Phys. **66**, 523 (2003).
 R. Wiesendanger, Rev. Mod. Phys. **81** 1495 (2009).

TMR-effect
 (tunnel magnetoresistance)
 in STM geometry

(a) GMR/TMR



(b) STM setup



$$I_{SP}(U_0) = I_0 [1 + P_s \cdot P_t \cdot \cos(\vec{M}_s, \vec{M}_t)]$$

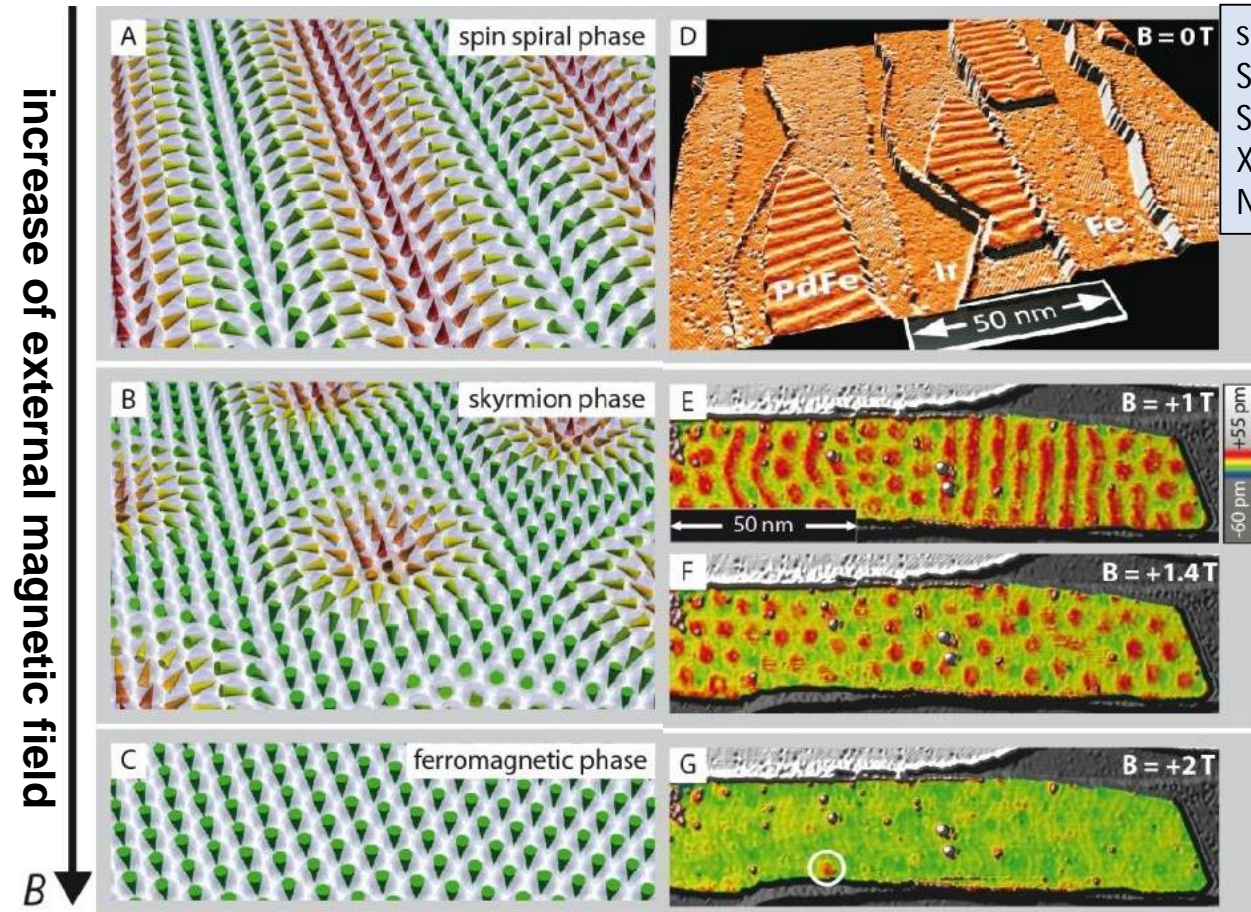
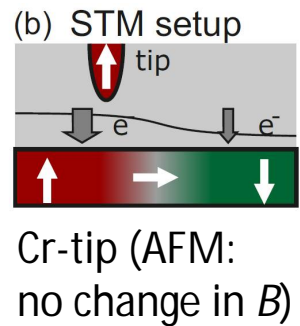
in-situ tip
 and sample
 preparation

STM
 $T = 1.3 - 4.2 \text{ K}$
 $B_{\perp} < 9 \text{ T}$

STM
 $T = 8 - 13 \text{ K}$
 $B_{\perp} < 2.5 \text{ T}$



SP-STM on Pd/Fe/Ir(111)

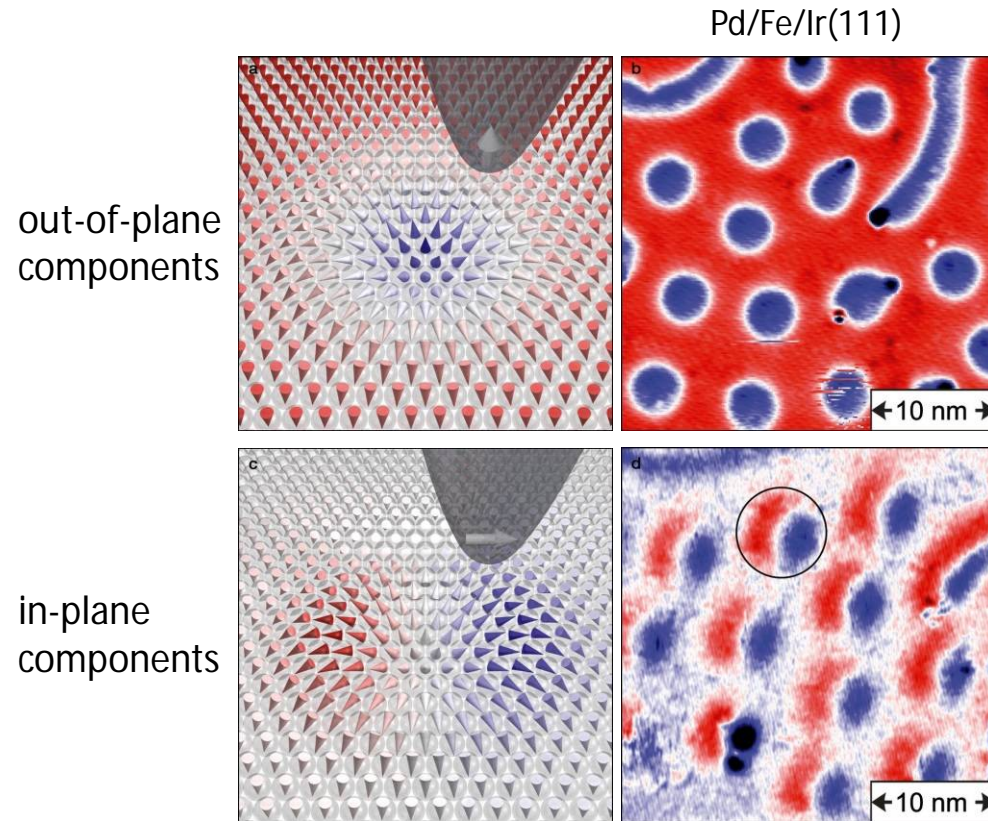


similar to:
 S. Mühlbauer et al.,
 Science **323**, 915 (2009).
 X.Z. Yu et al.,
 Nature **465**, 901 (2010).

spin spiral
 due to
 competition
 of J and D

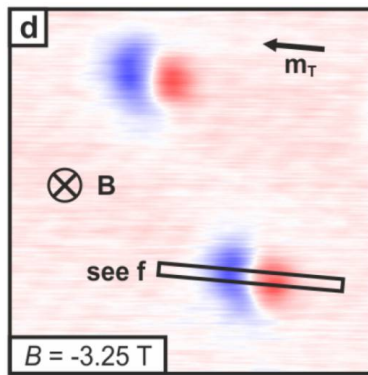
N. Romming, ...KvB et al., Science **341**, 636 (2013).

SP-STM and skyrmions



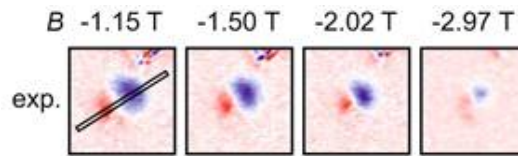
spin structure of an isolated skyrmion

two overlapping 180° domain walls



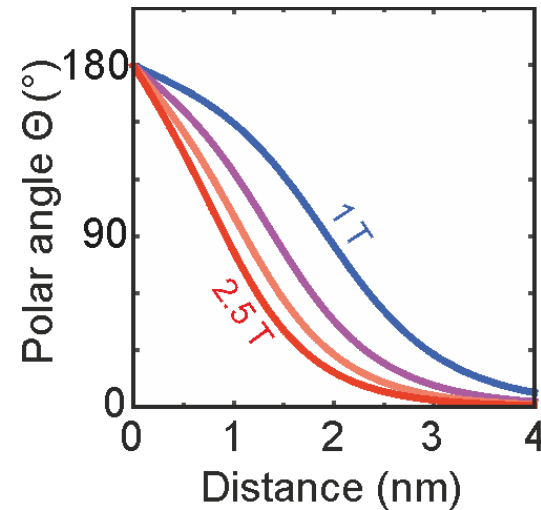
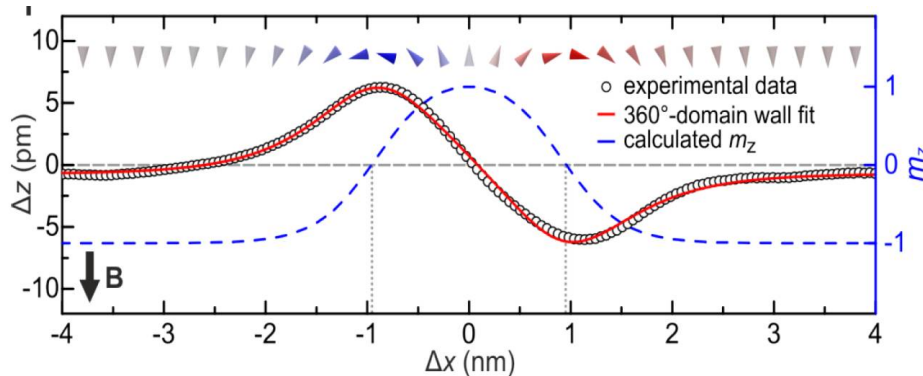
$$\theta(\rho, c, w) = \sum_{+,-} \left[\arcsin \left(\tanh \left(\frac{-\rho \pm c}{w/2} \right) \right) \right]$$

ρ position, c center, w width of wall



$$w_0 = 2 \sqrt{\frac{A}{K_{\text{eff}}}}$$

exchange stiffness
effective anisotropy

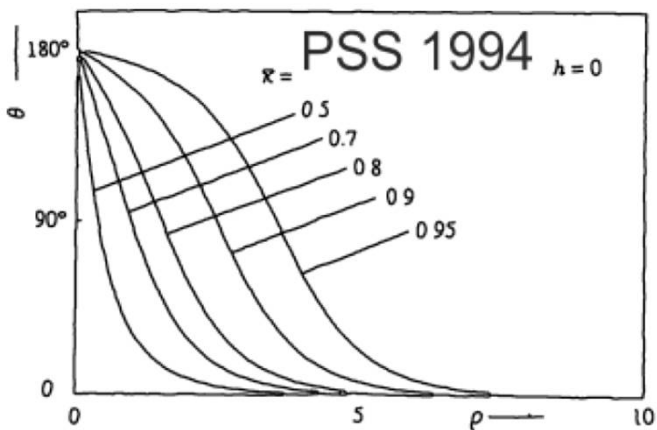


N. Romming, ...KvB et al.,
Phys. Rev. Lett. **114**, 177203 (2015).

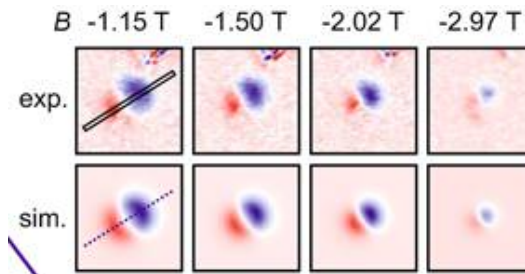
material parameters

$$E(\theta(\rho)) = 2\pi t \int_0^\infty \left[A \left(\left(\frac{d\theta}{d\rho} \right)^2 + \frac{\sin^2 \theta}{\rho^2} \right) - D \left(\frac{d\theta}{d\rho} + \frac{\sin \theta \cos \theta}{\rho} \right) - K \cos^2 \theta - B_z M_S \cos \theta \right] \rho d\rho$$

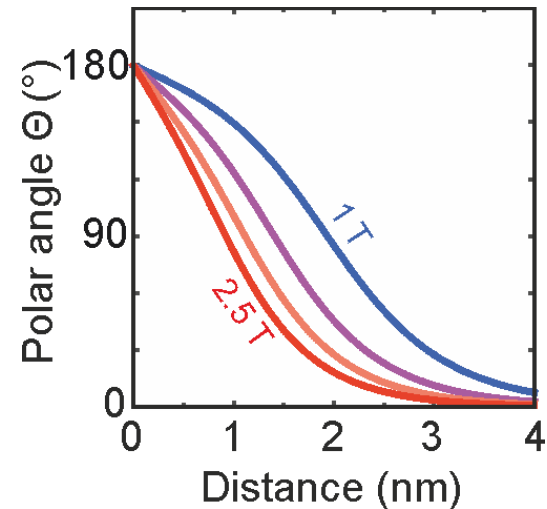
A. Bogdanov, A. Hubert, J. Magn. Magn. Mater. **138**, 255 (1994),
Phys. Status Solidi B **186**, 527 (1994)



$$A = 2.0 \text{ pJ/m} \quad |D| = 3.9 \text{ mJ/m}^2 \quad K = 2.5 \text{ MJ/m}^3 \quad M_S = 1.1 \text{ MA/m}$$

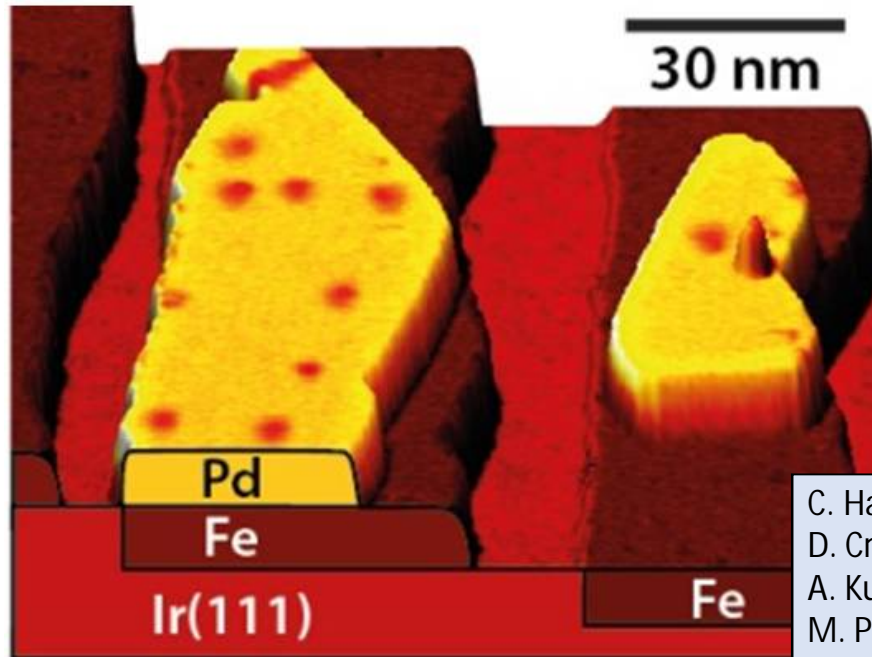
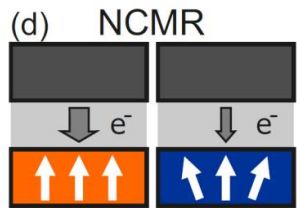
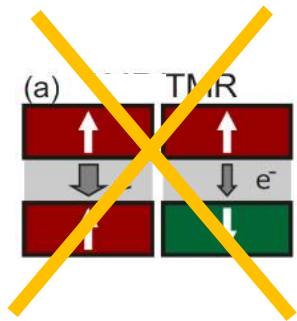


M_S from DFT, also good agreement with the other parameters.
B. Dupe et al., Nat. Commun. **5**, 4030 (2014).
E. Simon et al., Phys. Rev. B **90**, 094410 (2014).



N. Romming, ...KvB et al.,
Phys. Rev. Lett. **114**, 177203 (2015).

STM with non-magnetic tip: electronic properties

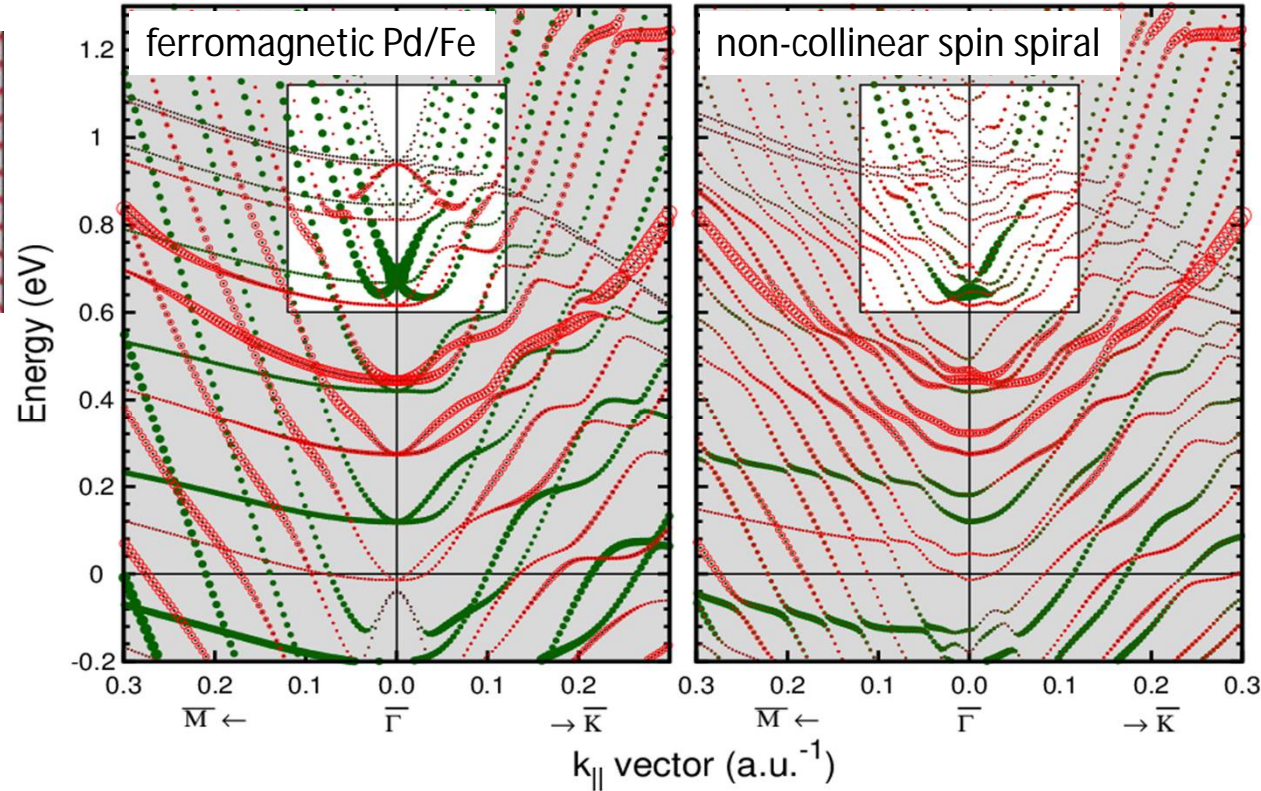
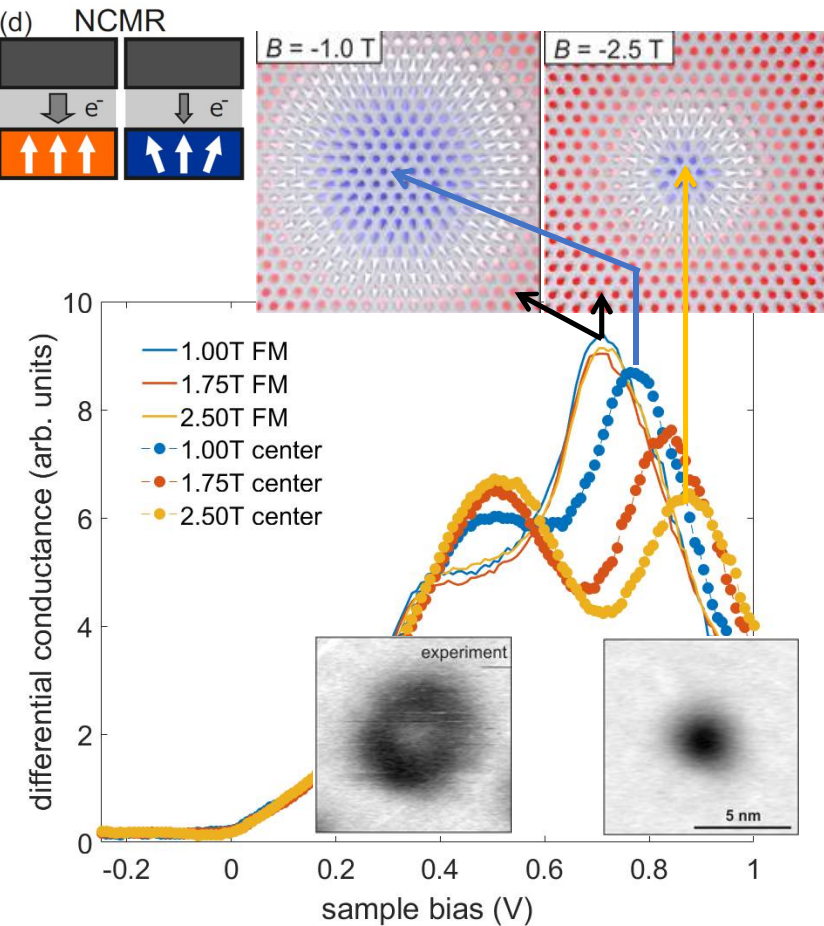


when the magnetic state is non-collinear there is a different electronic structure due to mixing of spin-up and spin-down bands

C. Hanneken, ..., KvB et al., Nature Nano. **10**, 1039 (2015).
D. Crum et al., Nature Commun. **6**, 8541 (2015).
A. Kubetzka, ..., KvB, Phys. Rev. B **95**, 104433 (2017).
M. Perini, ..., KvB, Phys. Rev. Lett. **123**, 237205 (2019).

topography colorized with differential conductance signal:
we 'see' the skyrmions also with non-spin-polarized STM tip,
due to the non-collinear magnetoresistance effect

spectroscopy and DFT

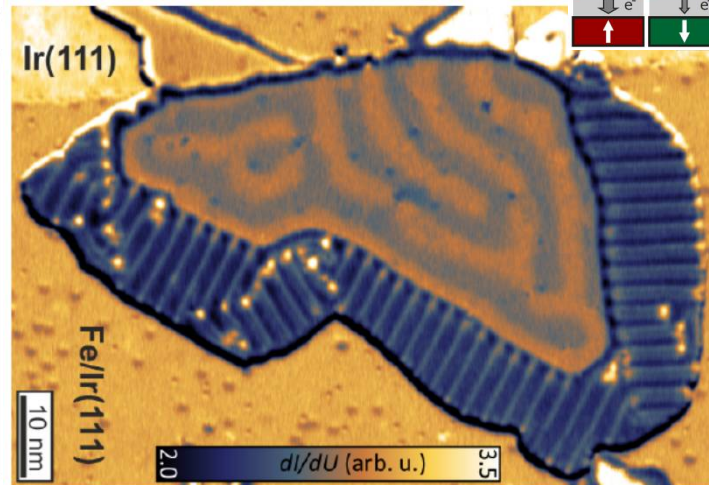
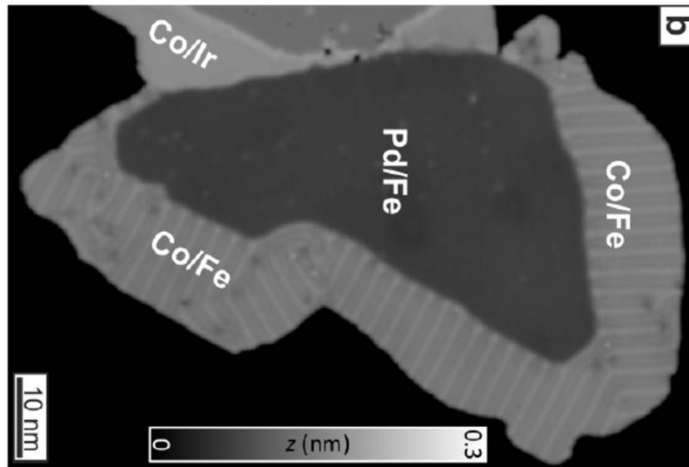
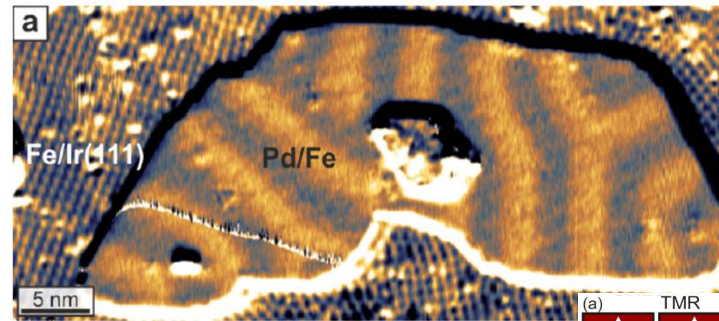
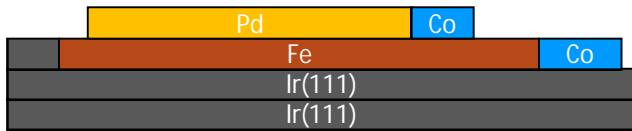


changes of the band structure everywhere in the Brillouin zone !!!
 not limited to tunnel experiments, relevant for all transport (see E_F)

spin spirals in Pd/Fe with modified rim

J. Spethmann, ..., KvB, arXiv:2108.06223

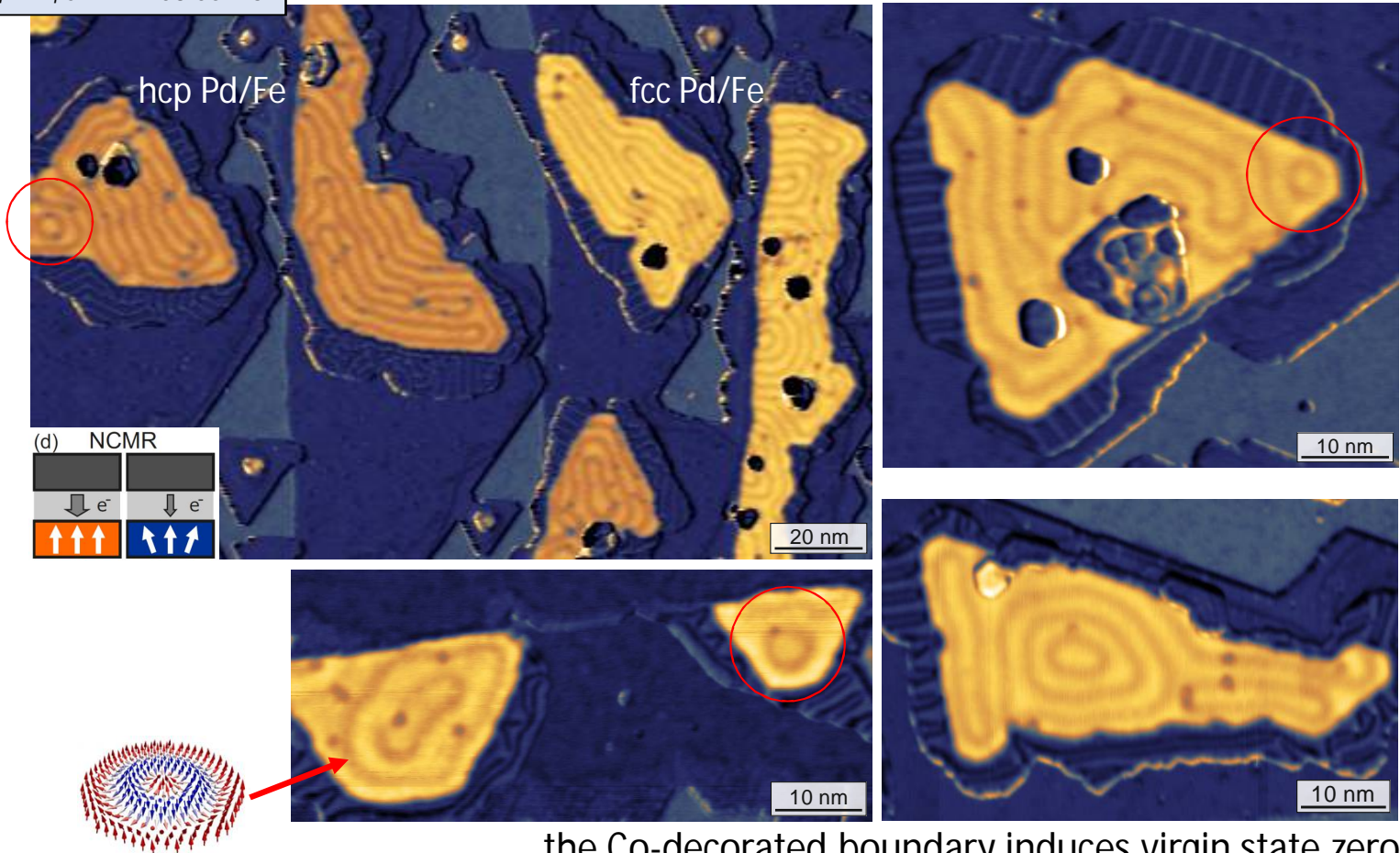
the Co/Fe areas are in-plane



the spin spiral material Pd/Fe is surrounded by Co/Fe (in-plane);
now the spirals orient differently with respect to the island boundary

virgin state: Co/Fe next to Pd/Fe/Ir(111)

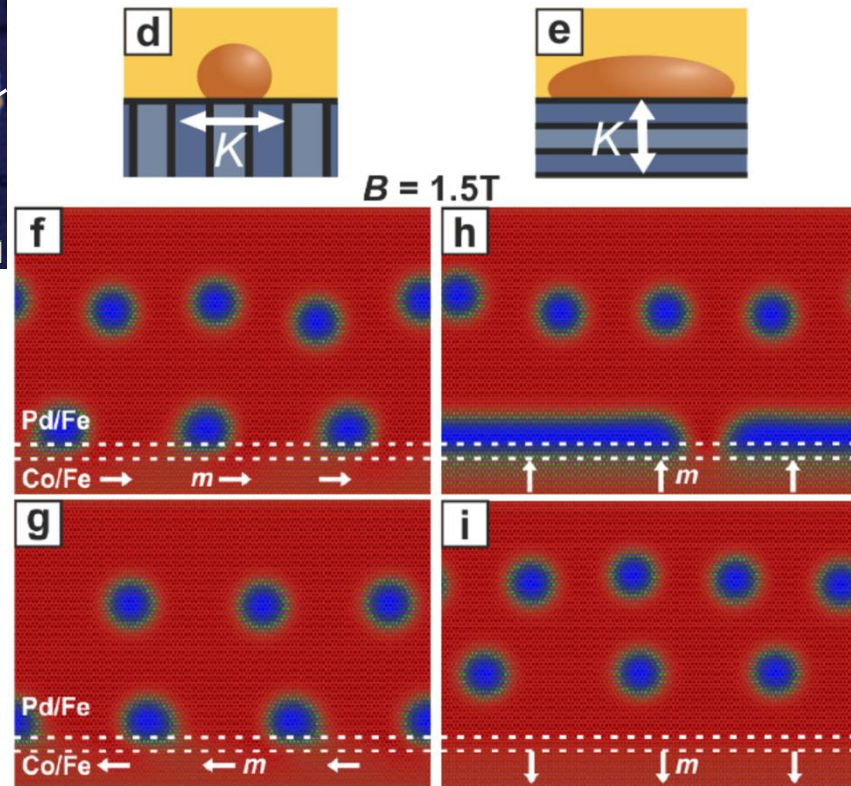
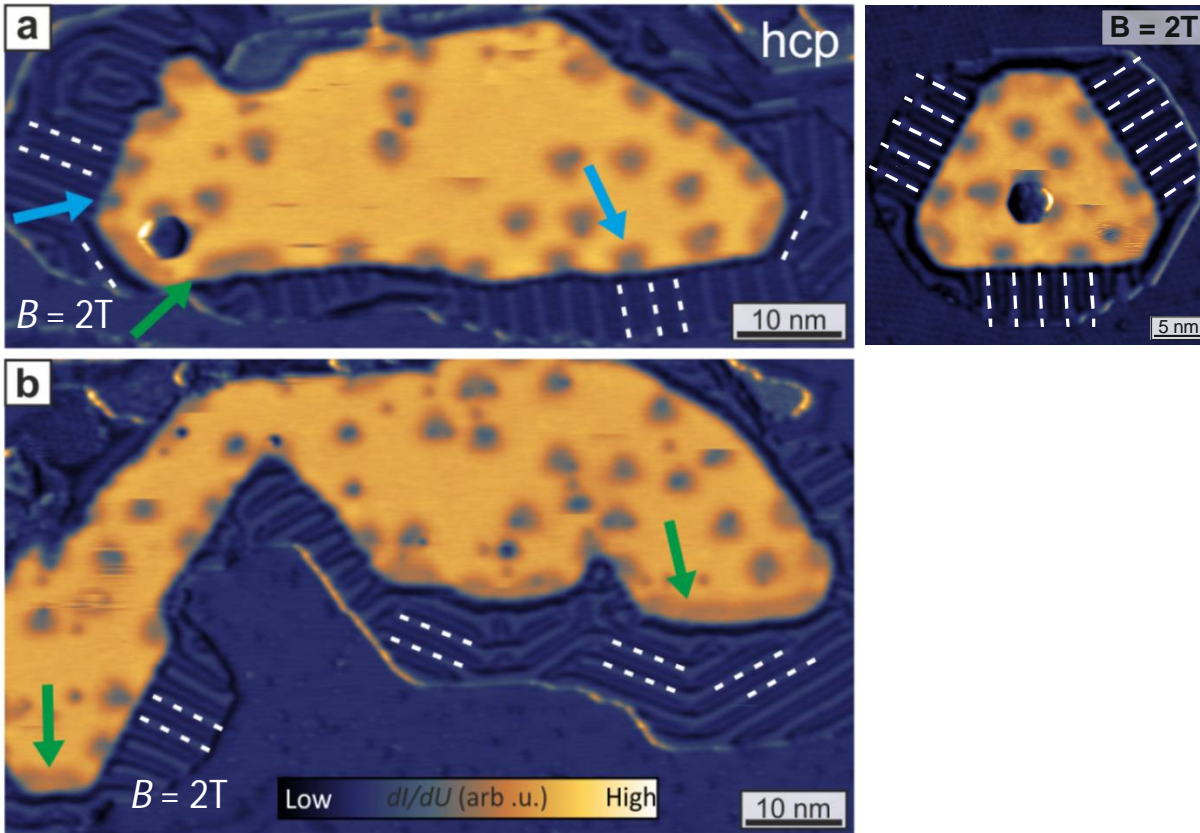
J. Spethmann, ..., KvB, arXiv:2108.06223



the Co-decorated boundary induces virgin state zero-field skyrmions, target states (skyrmionium), multi- π states

skyrmions at the edge

J. Spethmann, ..., KvB, arXiv:2108.06223



boundary magnetization direction leads to either localized or stripped-out skyrmions

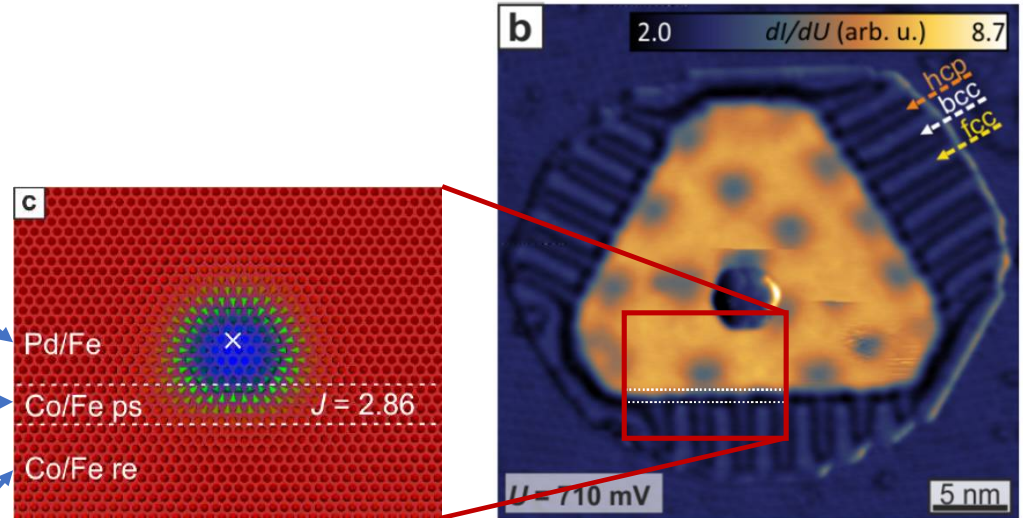
LLG atomistic simulations

J. Spethmann, ..., KvB, arXiv:2108.06223

Pd/Fe: exp. determined parameters
 $J = 2.86$, $D = 0.76$, $K_z = 0.4$ meV/atom

pseudomorphic transition regime:
 $J = J$, $D = D$, $K_z = -0.25$

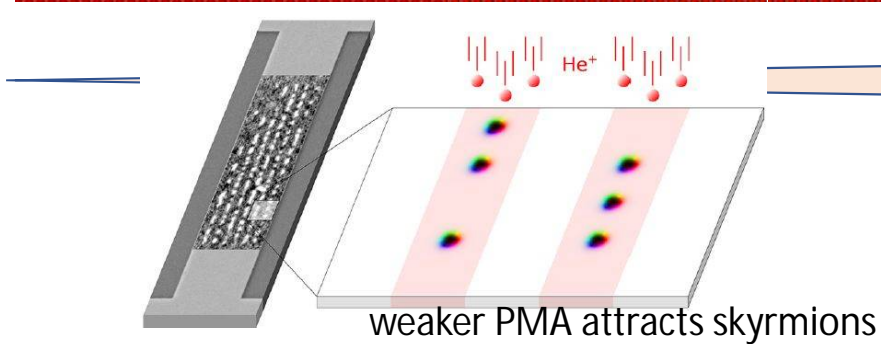
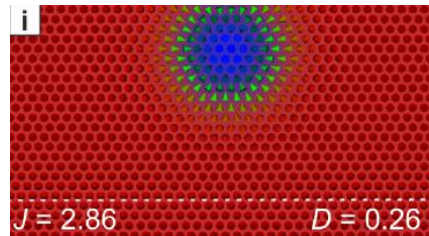
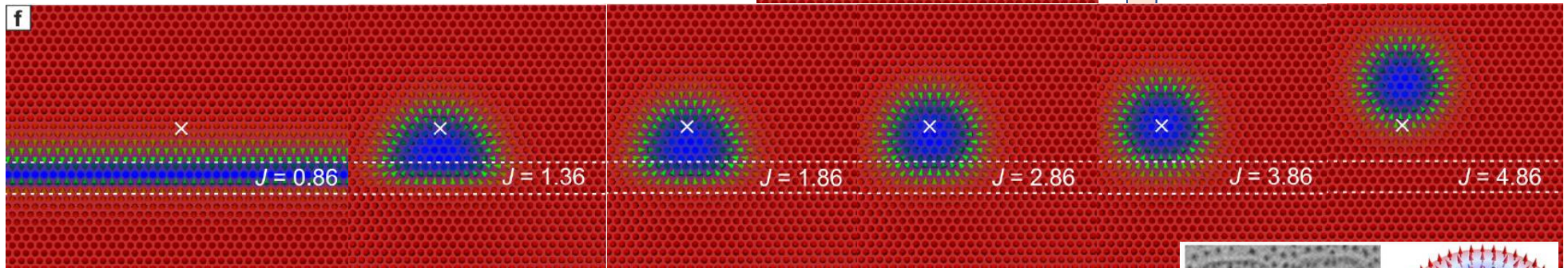
uniaxial reconstruction: random parameters
 $J = 7.86$ (to mimic larger magnetic moment)
 $D = D$, $K_x = 0.65$, $K_z = 0.4$



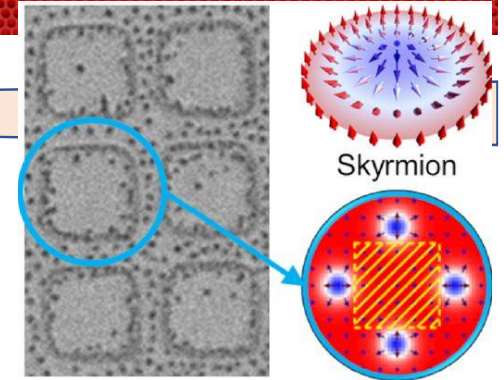
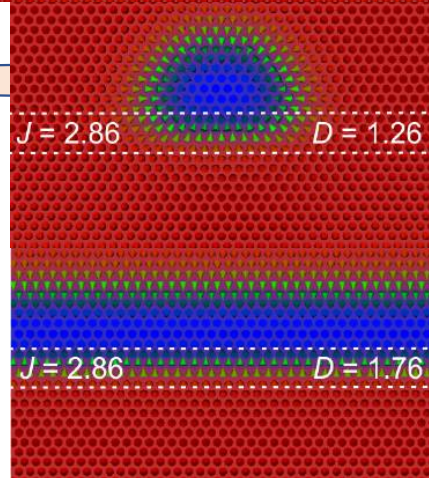
LLG atomistic simulations

J. Spethmann, ..., KvB, arXiv:2108.06223

skyrmions can be pinned/repelled at the edges, depending on material parameters J, D, K



R. Juge et al., Nano Lett. **21**, 2989 (2021).

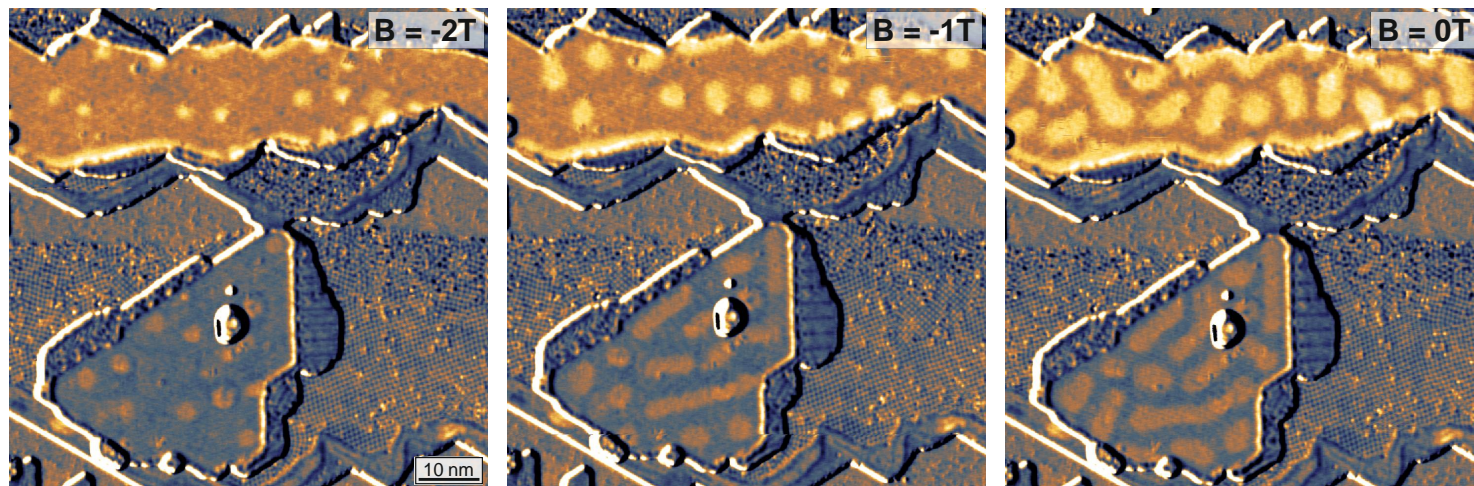


K. Ohara et al., Nano Lett. **21**, 4320 (2021).

higher PMA repels skyrmions

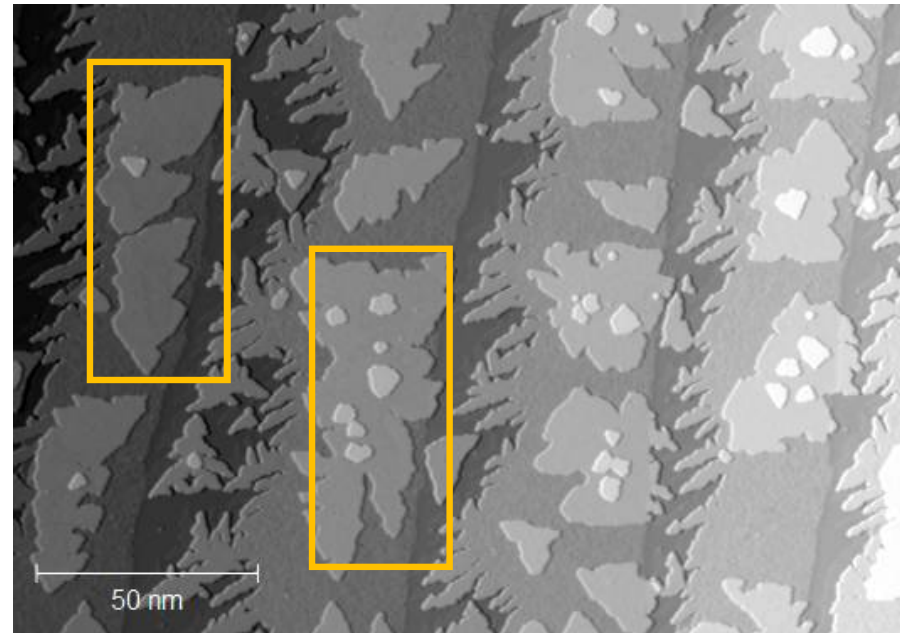
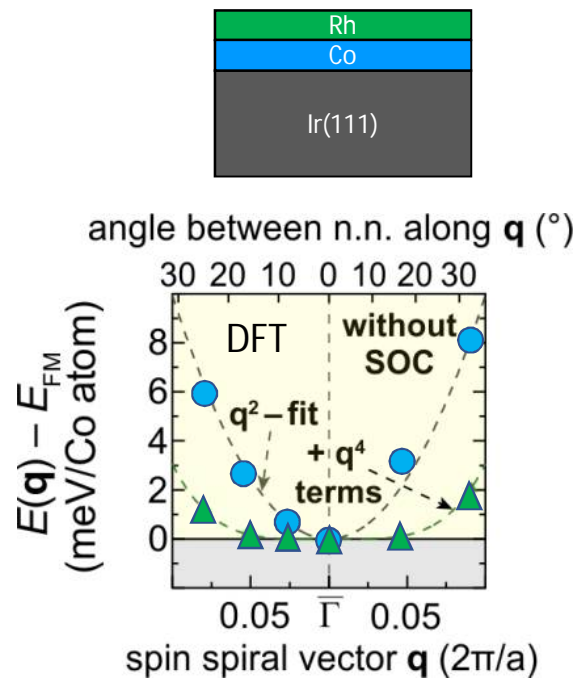
remanent zero-field skyrmions

J. Spethmann, ..., KvB, arXiv:2108.06223

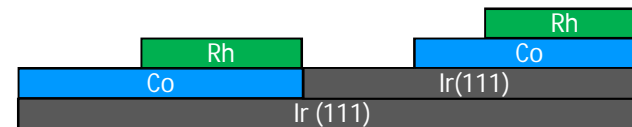


in the remanent state Pd/Fe islands with a Co/Fe rim exhibit many zero-field skyrmions

Rh/Co/Ir(111) – metastable zero-field skyrmions

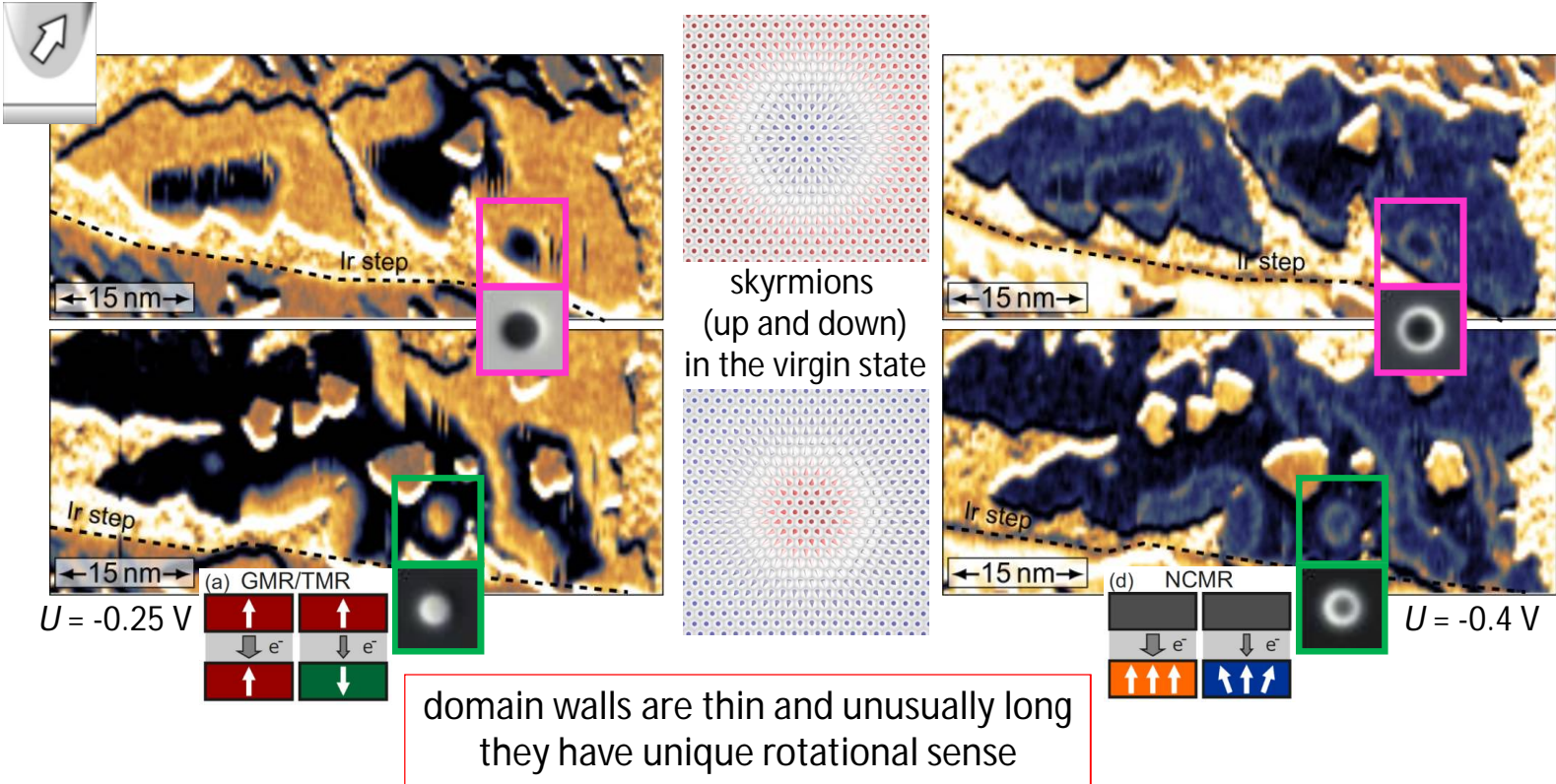


Rh/Co has a ferromagnetic ground state
 strong exchange frustration
 small energy cost for spin rotation up to $\sim 15^\circ$



S. Meyer, ..., KvB, S. Heinze, Nature Commun. **10**, 3823 (2019).
 M. Perini, ..., KvB, Phys. Rev. Lett. **123**, 237205 (2019).

skyrmions in hcp-Rh/Co/Ir(111)



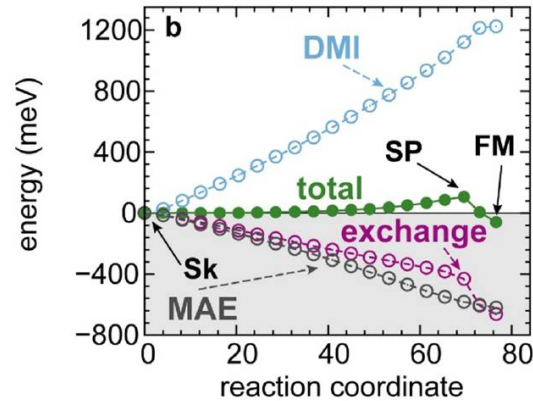
wall width w of 180° domain wall: $\cos \theta = \tanh\left(\frac{x}{w/2}\right)$
 skyrmion diameter ($m_z = 0$) d

upper sk: $d = 4.3$ nm, $w = 0.9$ nm
 lower sk: $d = 3.5$ nm, $w = 1.0$ nm

Energy barrier calculations with GNEB

GNEB = geodesic nudged elastic band

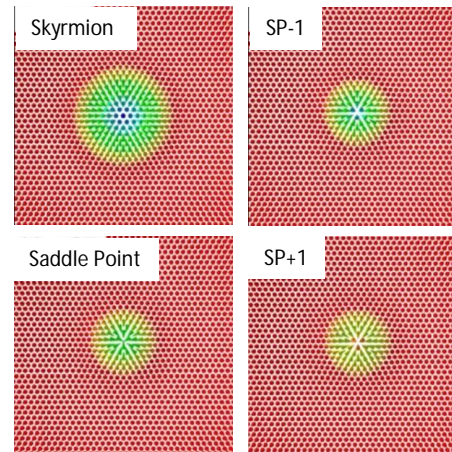
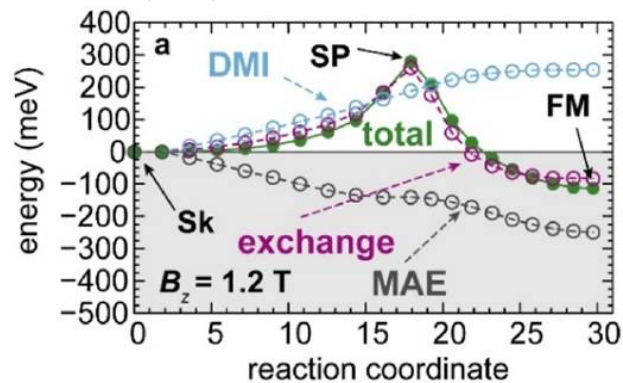
effective model



Typical collapse mechanism: shrinking

P.F. Bessarab et al., *Comp. Phys. Comm.* **196**, 335 (2015).
S. Rohart et al., *Phys. Rev. B* **93**, 214412 (2016).

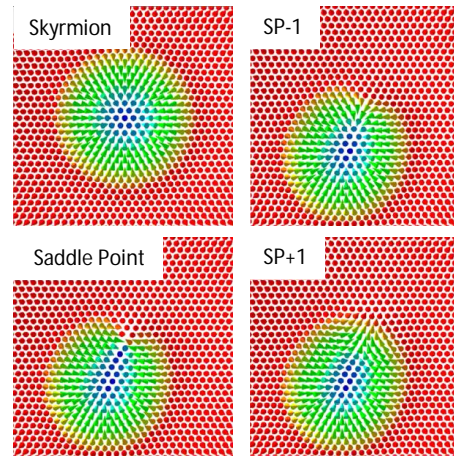
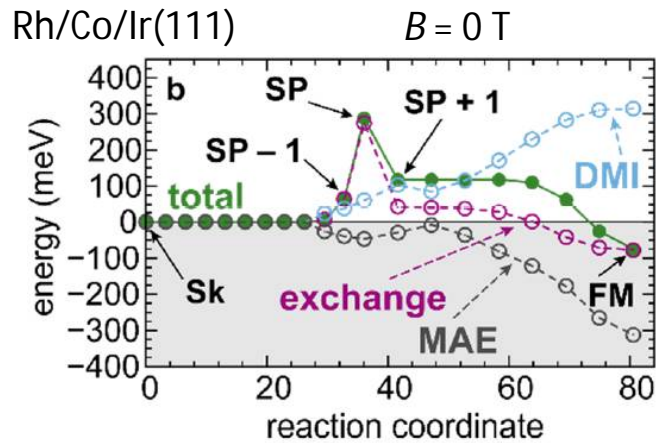
Rh/Co/Ir(111)



exchange frustration
enhances skyrmion stability

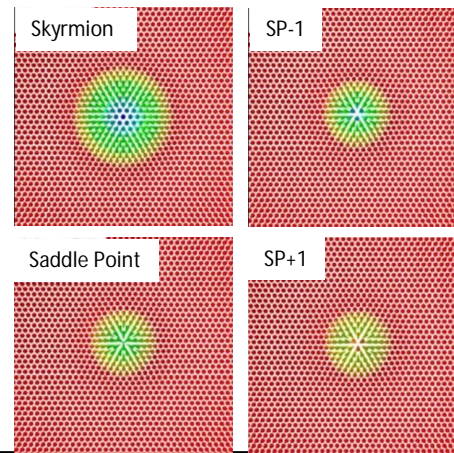
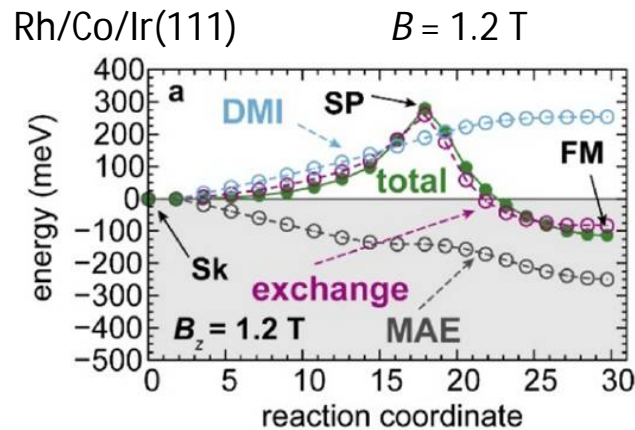
S. von Malottki et al.,
Sci. Rep. **7**, 12299 (2017).

isolated zero-field skyrmion due to exch. frustration



this chimera collapse also in canted fields for Pd/Fe

F. Muckel et al.,
Nature Phys. **17**,
395 (2021).

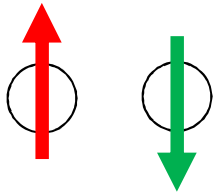


isolated zero-field
magnetic skyrmions
due to strong
exchange frustration

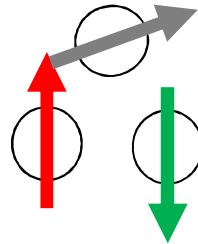
atomic-scale magnetic order: ingredients

magnetic exchange interaction

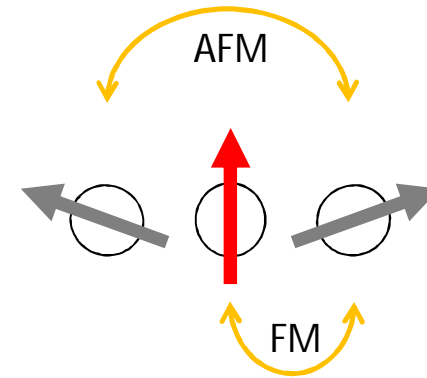
$$E = -J (S_1 \cdot S_2)$$



geometric frustration

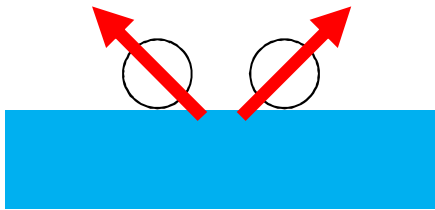


exchange frustration



antisymmetric exchange (DMI)
Dzyaloshinskii-Moriya interaction
due to spin-orbit coupling
and broken inversion symmetry

$$E = -D (S_1 \times S_2)$$



higher-order interactions

$$H_{\text{HO}} = - \sum_{\langle ij \rangle} B (\mathbf{m}_i \mathbf{m}_j)^2 - 2 \sum_{\langle ijk \rangle} Y_3 [(\mathbf{m}_i \mathbf{m}_j)(\mathbf{m}_j \mathbf{m}_k) + (\mathbf{m}_j \mathbf{m}_k)(\mathbf{m}_k \mathbf{m}_i) + (\mathbf{m}_k \mathbf{m}_i)(\mathbf{m}_i \mathbf{m}_j)] - \sum_{\langle ijkl \rangle} K_4 [(\mathbf{m}_i \mathbf{m}_j)(\mathbf{m}_k \mathbf{m}_l) + (\mathbf{m}_i \mathbf{m}_l)(\mathbf{m}_j \mathbf{m}_k) - (\mathbf{m}_i \mathbf{m}_k)(\mathbf{m}_j \mathbf{m}_l)]$$

atomic-scale magnetic order

hexagonal monolayer:

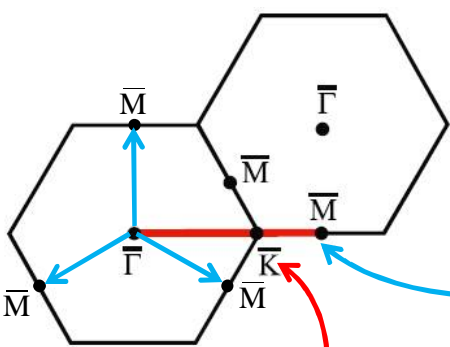
afm nearest neighbor interaction J_1

competition afm J_1 and afm J_2

→ Néel state (120° coplanar)

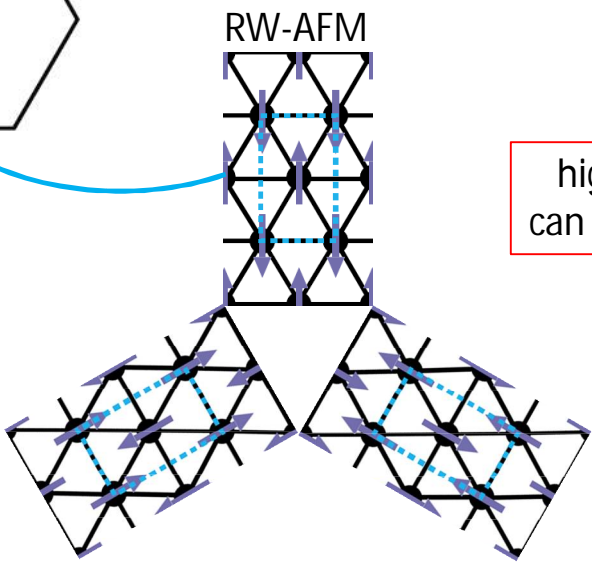
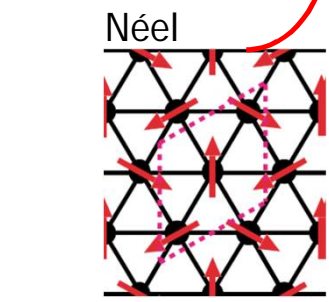
→ RW-AFM (180° collinear)

1-q state superposition multi-q state

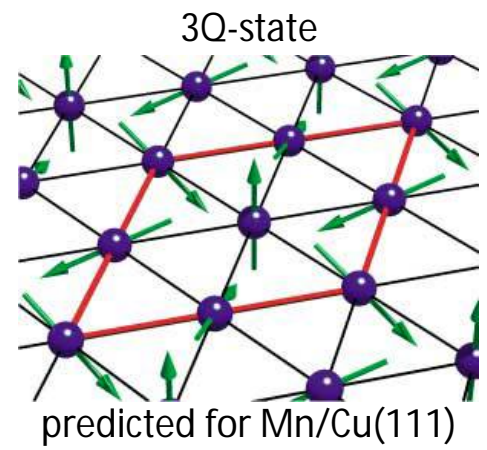


uniaxial
3 rotational domains

2-dimensionally modulated
3-dimensional spin structure

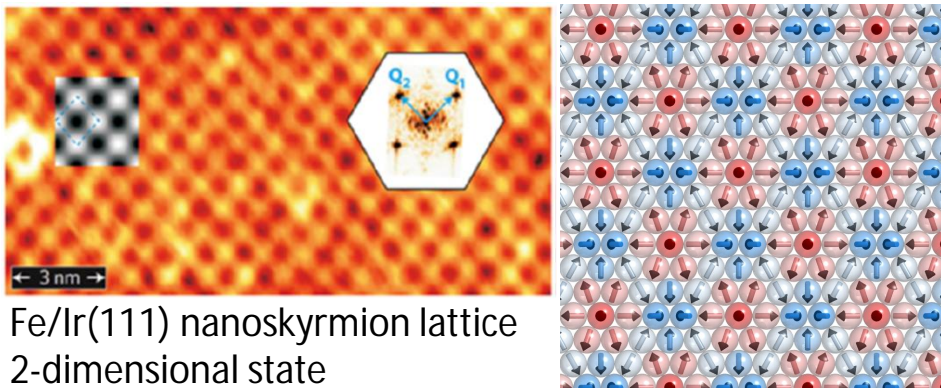


higher-order interactions
can favor one over the other



predicted for Mn/Cu(111)
P. Kurz, et al.,
Phys. Rev. Lett. **86**, 1106 (2001).

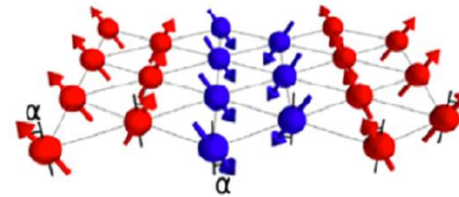
higher-order interactions



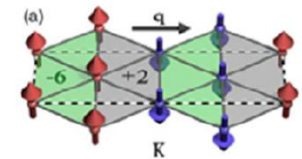
Fe/Ir(111) nanoskymion lattice
2-dimensional state

KvB, S. Heinze et al., Phys. Rev. Lett. **96**, 167203 (2006).
S. Heinze, KvB et al., Nature Phys. **7**, 718 (2011).

Rh/Fe/Ir(111) canted uudd

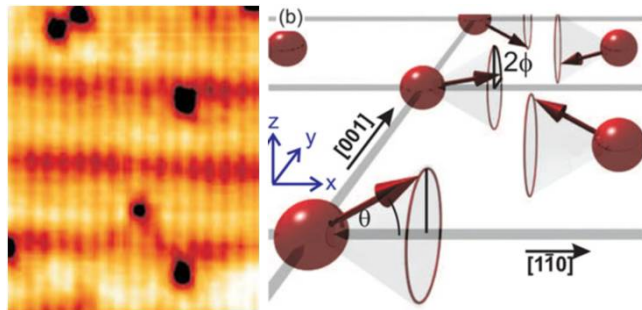


Fe/Rh(111): uudd



N. Romming, ..., KvB, Phys. Rev. Lett. **120**, 207201 (2018).
A. Krönlein et. al, Phys. Rev. Lett. **120**, 207202 (2018).

Mn-DL/W(110)
conical
antiferromag
spin spiral



Y. Yoshida, ..., KvB et al, Phys. Rev. Lett. **108**, 087205 (2012).

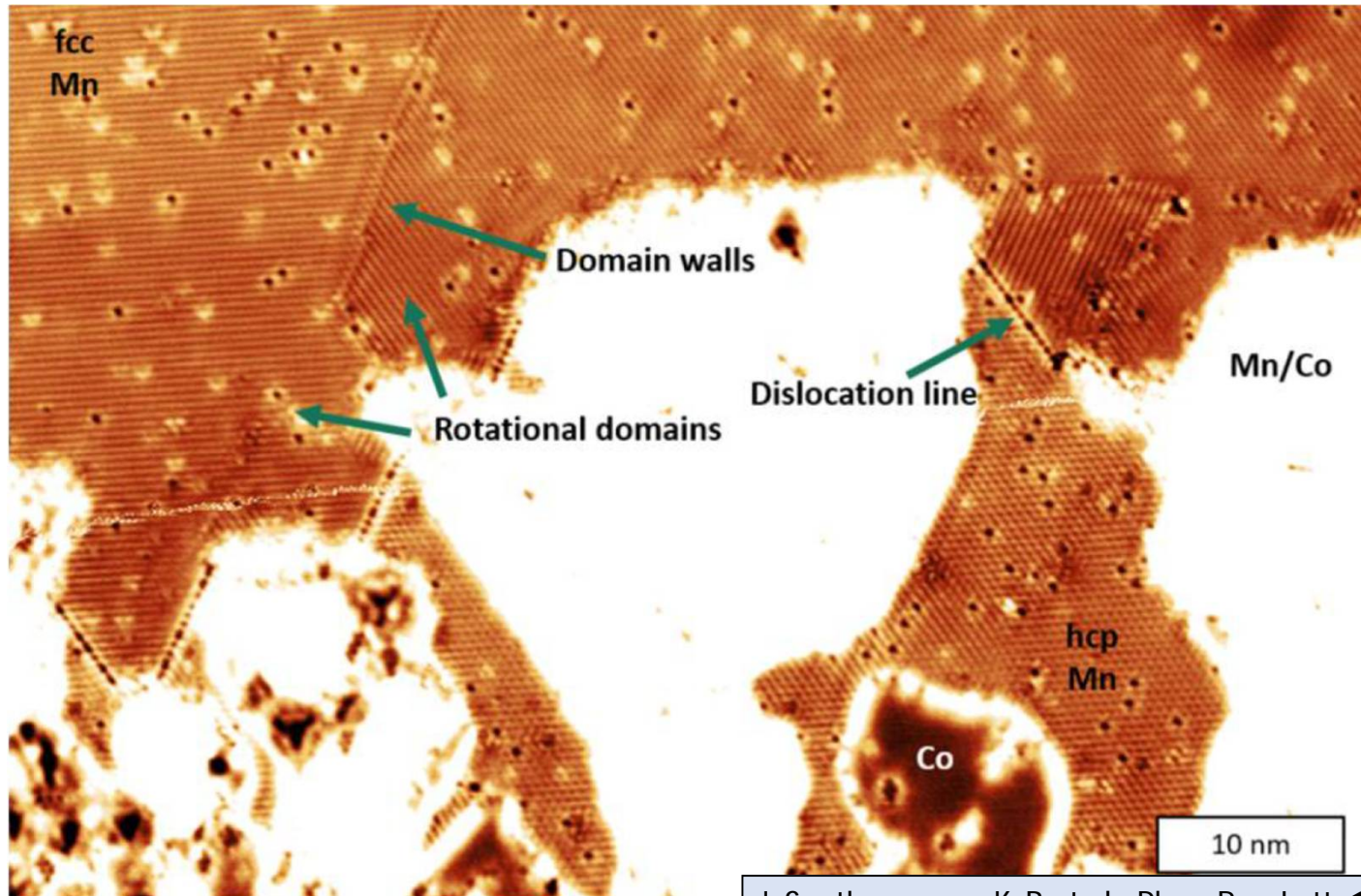
More theoretical investigations,
including further phenomena and impact on transport

P. Ferriani et al, Phys. Rev. Lett. **99**, 187203 (2007).
A. Al-Zubi et al., Phys. Status Solidi B **248**, 2242 (2011).
M. Hoffmann et al, Phys. Rev. B **92**, 020401 (2015).
F.R. Lux et al, Communications Physics **1**, 60 (2018)
M. Hoffmann and S. Blügel, Phys. Rev. B **101**, 024418 (2020).
S. Grytsiuk et al, Nature Commun. **11**, 1 (2020).
S. Paul et al, Nature Commun. **11**, 4756 (2020).

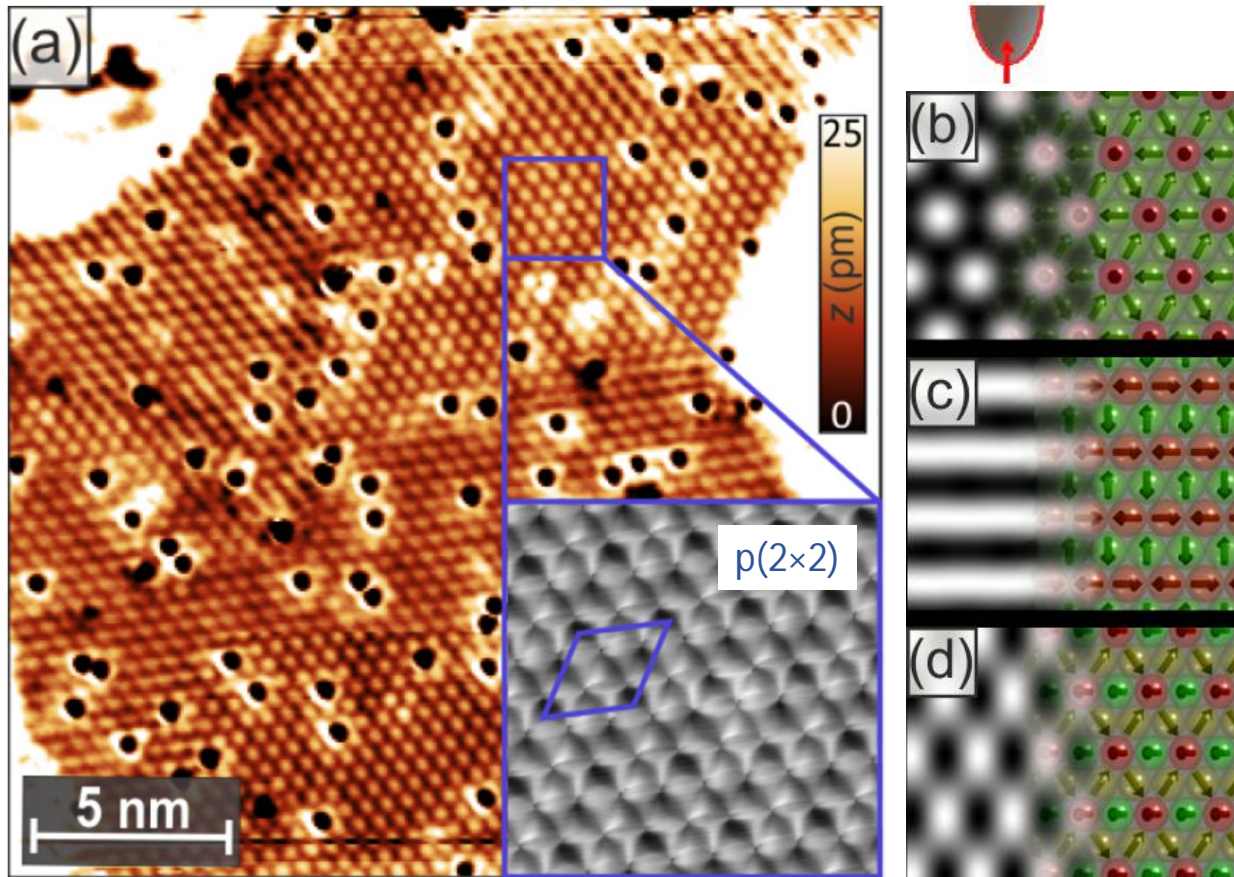
.....

Mn monolayer on Re(0001)

fcc-Mn in SP-STM:
stripes along the
close-packed
atomic rows,
every other row
→ RW-AFM



hcp-Mn/Re(0001): the 3Q-state



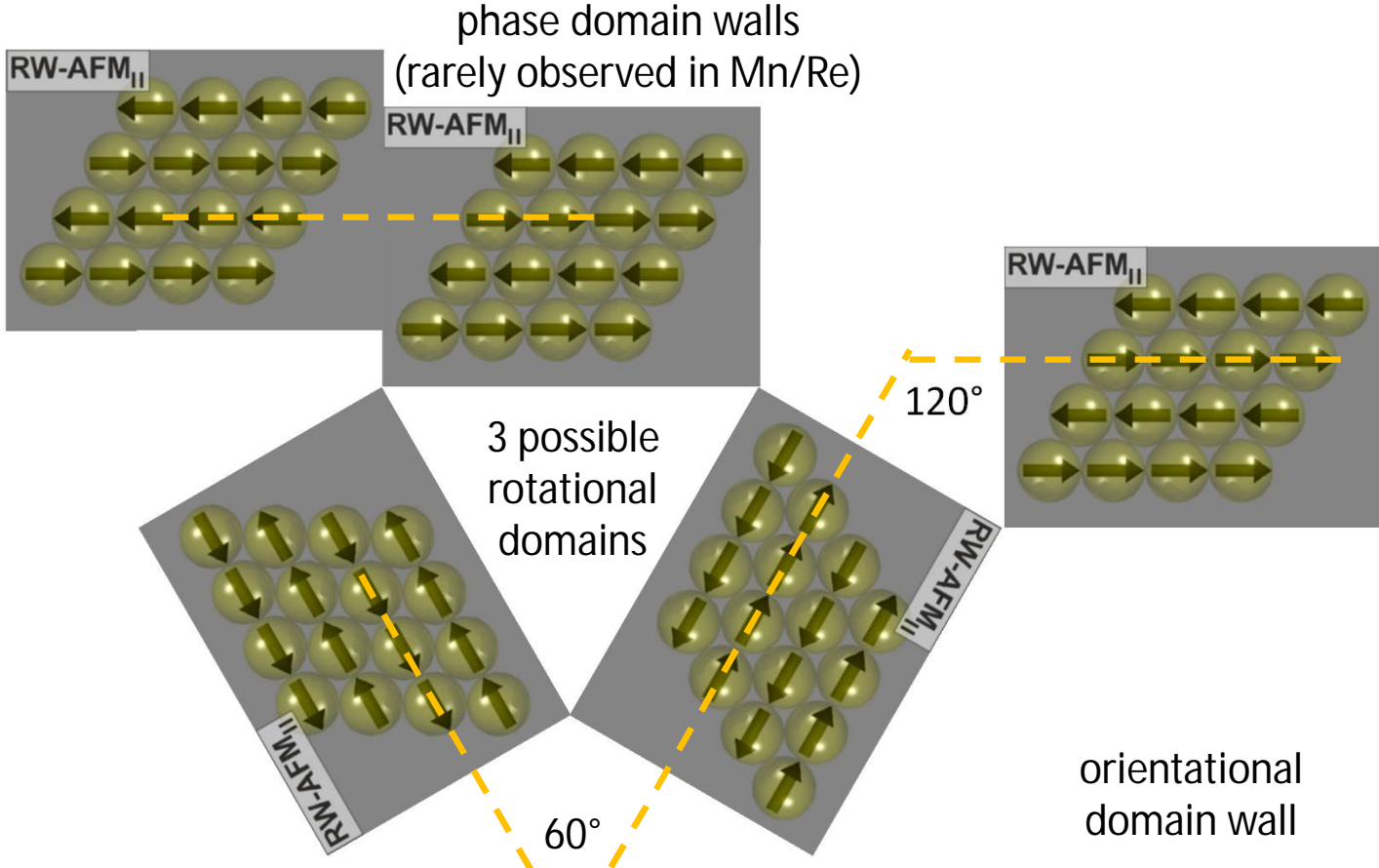
areas of hexagonal $p(2 \times 2)$ pattern
 \rightarrow 3Q state
 (superposition of 3 rotational domains of the RW-AFM state due to higher-order interactions)

HOI

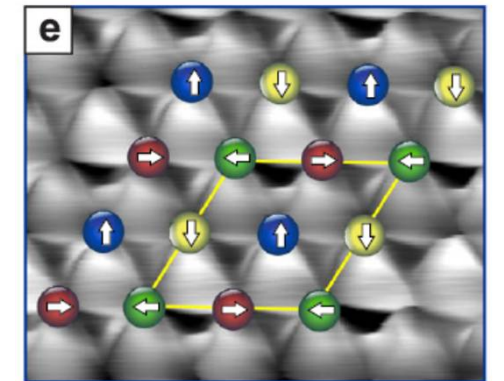
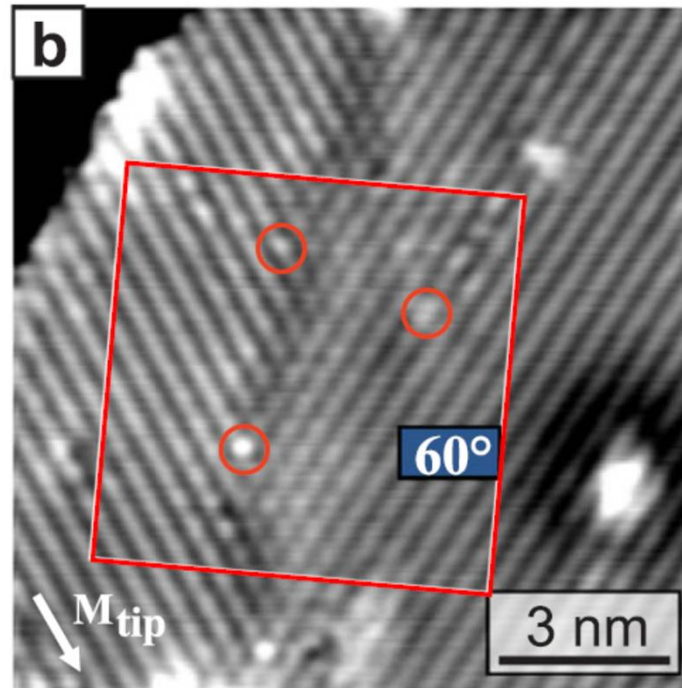
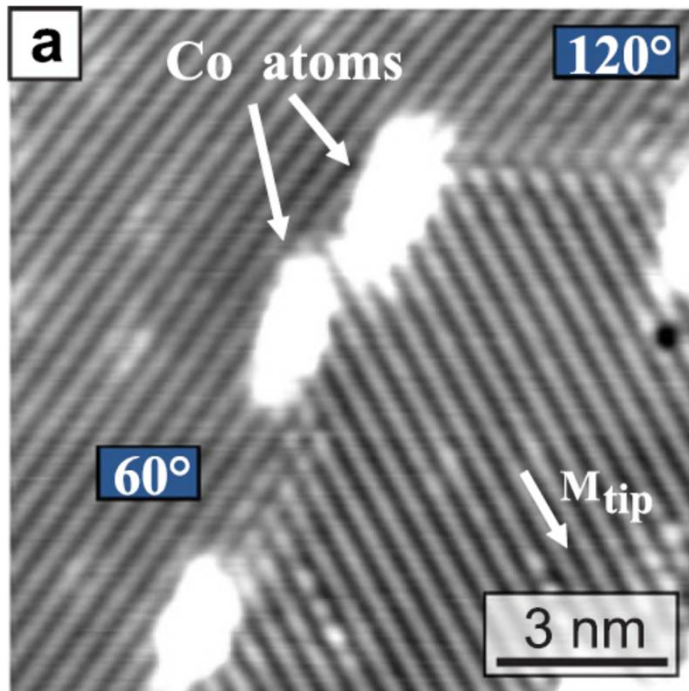
... looks slightly different in different sample areas, it must couple to the lattice ...

S. Haldar et al, arXiv.2106.08622

RW-AFM domain walls



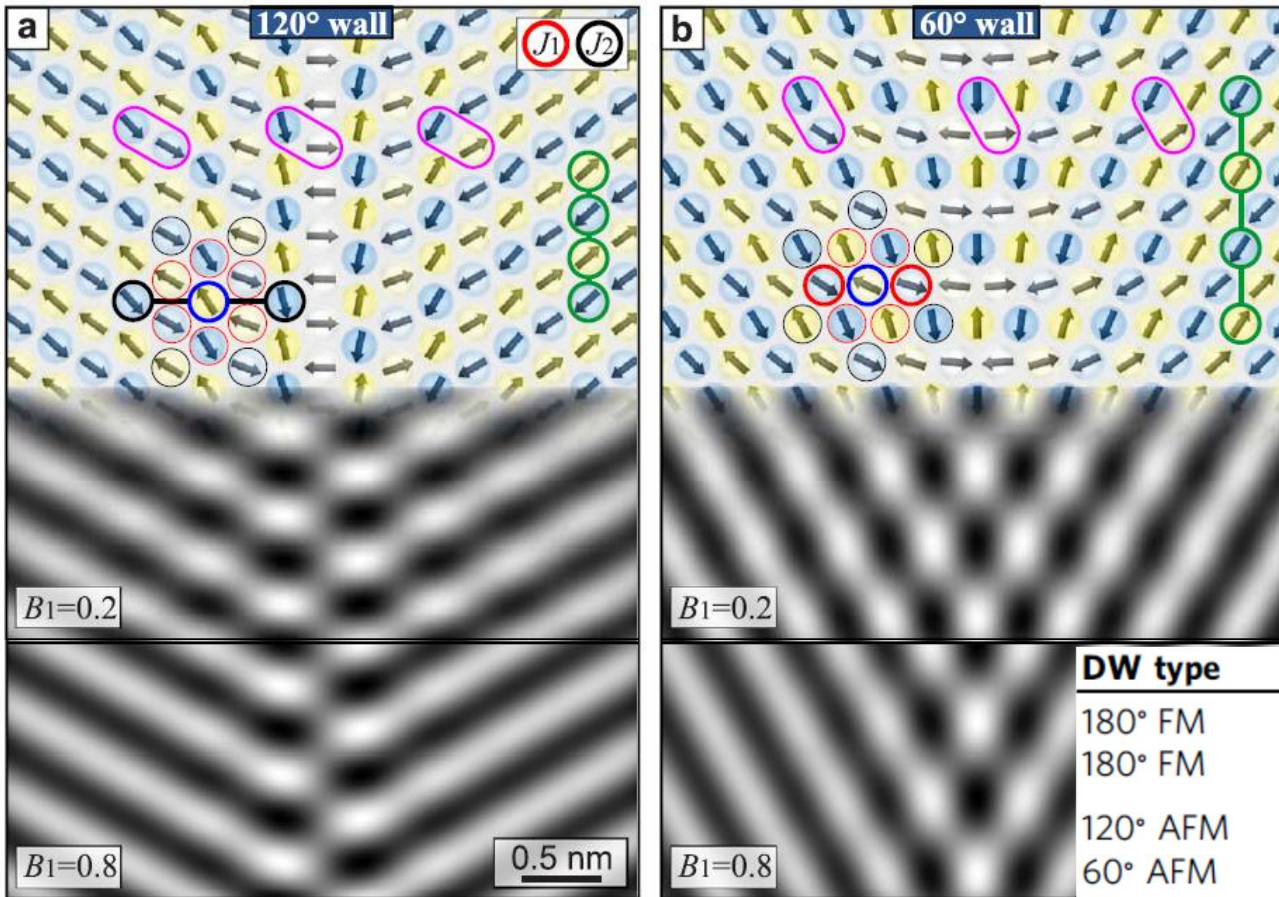
RW-AFM domain walls



p(2×2) superstructure within the domain wall (magnetic atom manipulation imaging)

→ not a coherent rotation of the sublattices but a superposition wall

superposition domain walls



$$H = -J_1(\mathbf{S}_i \cdot \mathbf{S}_j) - J_2(\mathbf{S}_i \cdot \mathbf{S}_j) - K(S_z)^2 - J_{ASE}(\mathbf{S}_i \cdot \mathbf{d}_{ij})(\mathbf{S}_j \cdot \mathbf{d}_{ij}) - B_1(\mathbf{S}_i \cdot \mathbf{S}_j)^2$$

a set of simplified DFT parameters (in meV/atom)
 $J_1 = -25$, $J_2 = -5$, $J_{ASE} = +0.025$, $K = -1$, and B_1

analytical formulas for these superposition domain walls: HOIs determine width and E

| DW type | Model | Width | Energy |
|----------|-------------------------|--------------------------------|---|
| 180° FM | A, K (continuum) | $2\sqrt{A/K}$ | $4\sqrt{AK}$ |
| 180° FM | $J_1 > 0, K > 0$ | $2a\sqrt{\frac{3}{2}J_1/K}$ | $\frac{4}{a}\sqrt{2J_1K}$ |
| 120° AFM | $J_1, J_2 < 0, B_1 > 0$ | $\frac{a}{2}\sqrt{3 J_2 /B_1}$ | $\frac{8}{a}\sqrt{ J_2 B_1}$ |
| 60° AFM | $J_1, J_2 < 0, B_1 > 0$ | $\frac{a}{2}\sqrt{ J_1 /B_1}$ | $\frac{8}{a}\sqrt{\frac{1}{3} J_1 B_1}$ |

superposition walls in other systems

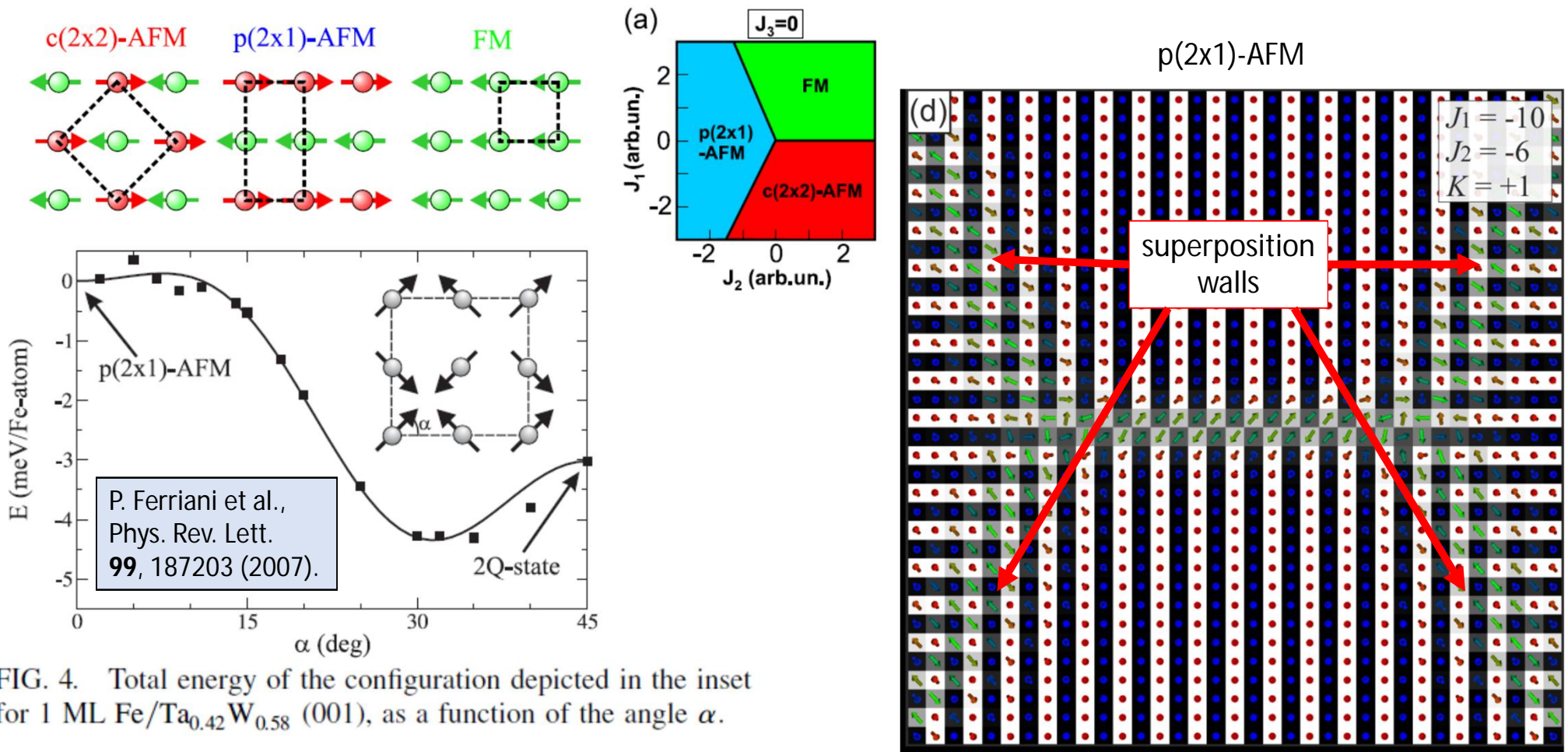
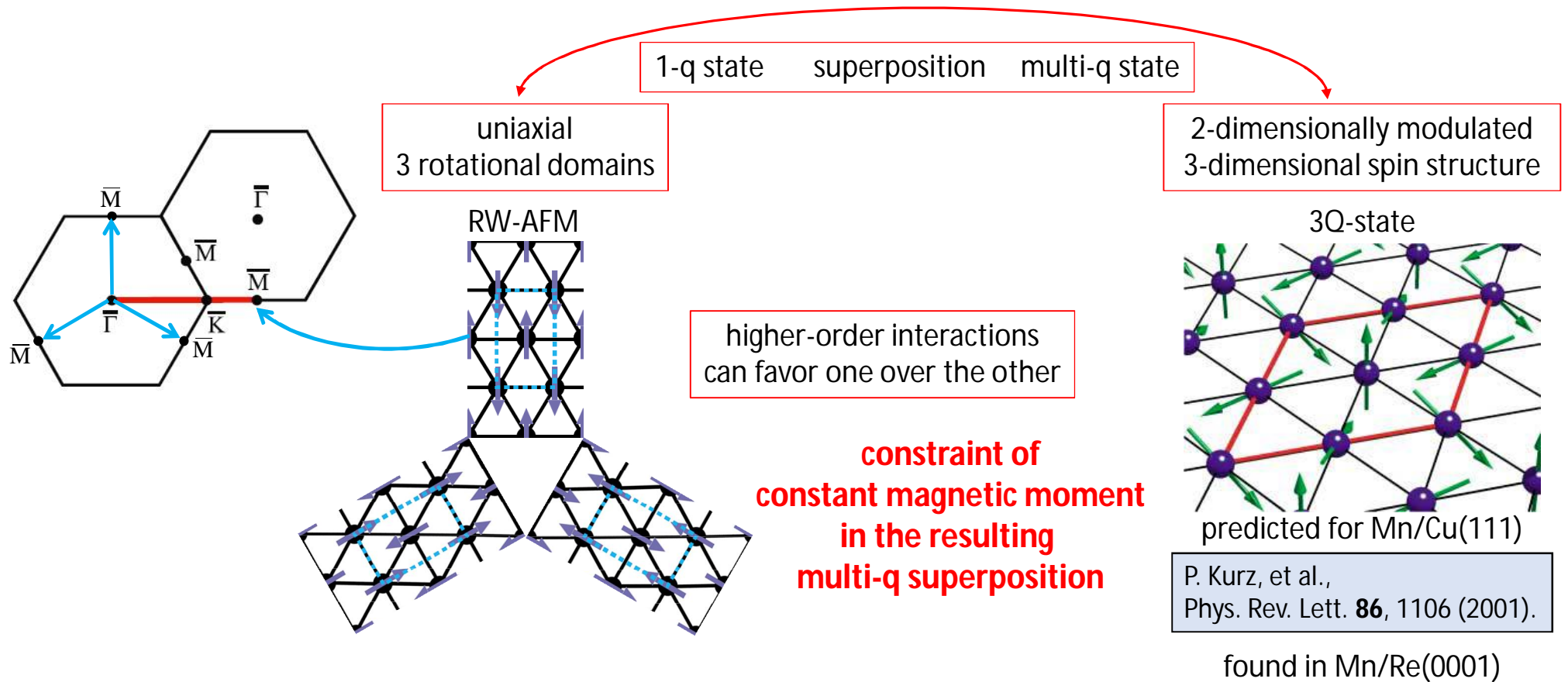


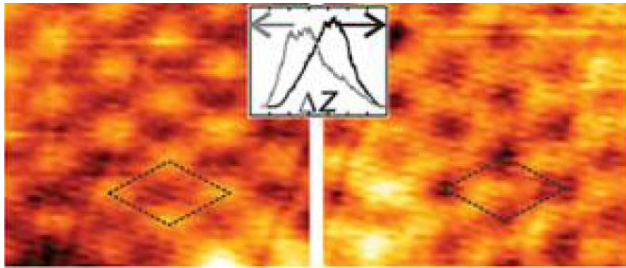
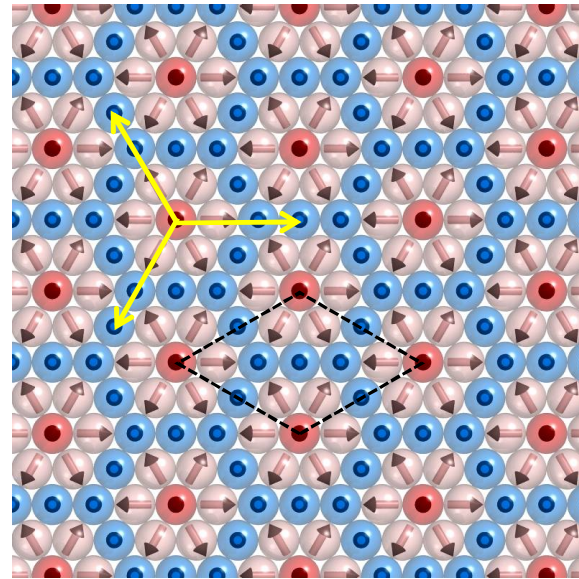
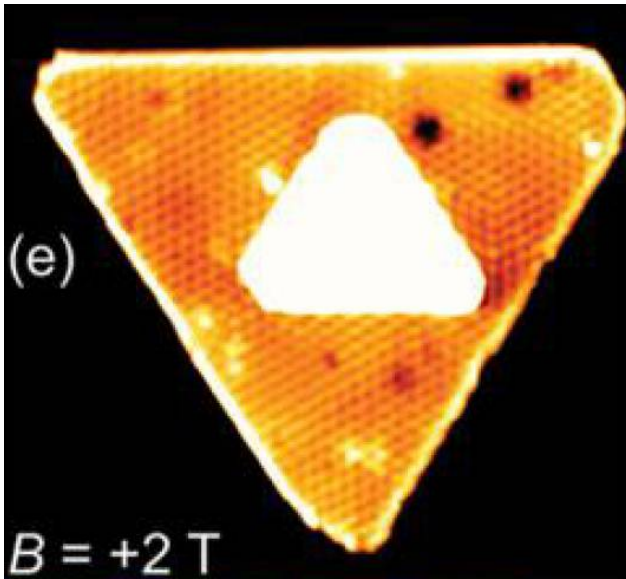
FIG. 4. Total energy of the configuration depicted in the inset for 1 ML Fe/Ta_{0.42}W_{0.58} (001), as a function of the angle α .

single-q to multi-q



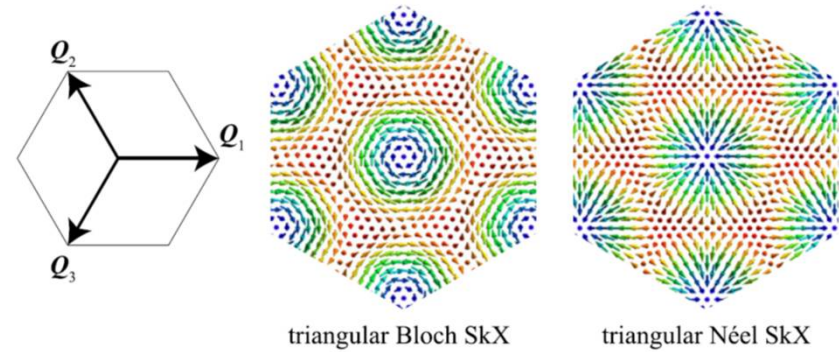
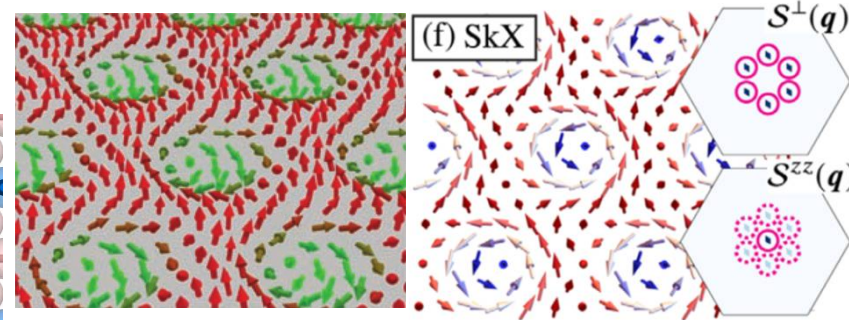
larger magnetic unit cells ?

constraint of constant magnetic moment usually not possible



after the superposition we adjust the Fe magnetic moment to be constant (large intra-atomic exchange)

KvB, et. al, Nano Lett. **15**, 3280 (2015).



S. Mühlbauer et al., Science **323**, 915 (2009).
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summary

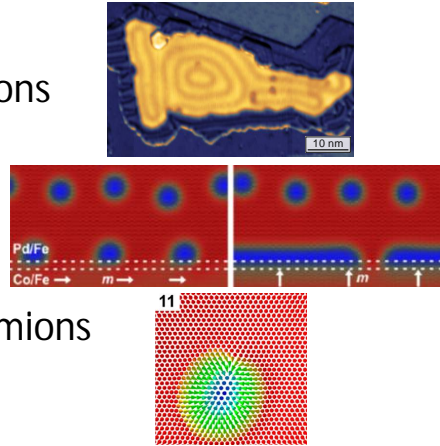
nano-scale skyrmions

SP-STM and NCMR-imaging useful to characterize skyrmions
the rim can be utilized to modify the spin texture
zero-field skyrmions, target states, multi- π
localized or stripped-out skyrmions at the boundary

J. Spethmann, ..., KvB, arXiv:2108.06223

frustrated exchange can stabilize isolated virgin state skyrmions

S. Meyer, ..., KvB, S. Heinze, Nature Commun. **10**, 3823 (2019).
M. Perini, ..., KvB, Phys. Rev. Lett. **123**, 237205 (2019).



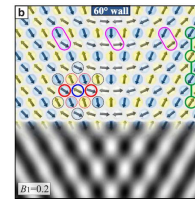
higher-order interactions

HOIs can couple the RW-AFM on a hexagonal lattice to form the 3Q state
HOIs can lead to superposition walls between afm rotational domain walls
HOIs have a direct impact on the width and energy of superposition walls

J. Spethmann, ... KvB et al., Phys. Rev. Lett. **124**, 227203 (2020).
J. Spethmann, ... KvB et al., Nature Commun. **12**, 3488 (2021).

experimental screening is ... interesting ... always good for a surprise

Fe/Ir and Fe/Rh interfaces seem to promote atomic-scale magnetic order induced by HOIs
several square/hexagonal magnetic states (multi-q?) of different size have been identified



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Jonas Spethmann
Marco Perini
Roland Wiesendanger
Stefan Heinze + group
(Theory, Univ. Kiel)

Deutsche Forschungsgemeinschaft 
DFG 
Funded by the Horizon2020 Framework Programme of the European Union

402843438, 418425860
EU-FET-OPEN: MagicSky

