

# Neuromorphic magnon-spintronic networks

Philipp Pirro

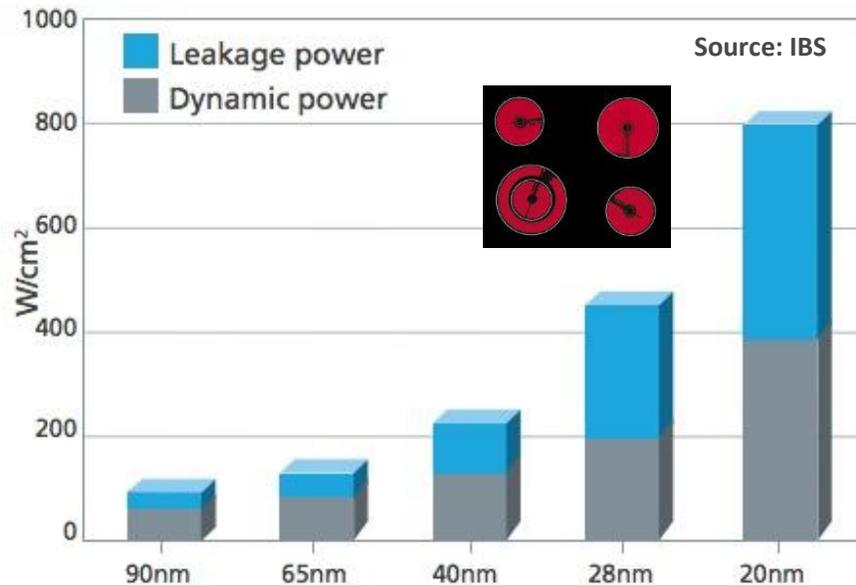
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# Neuromorphic computing

Use of novel ways to compute which are inspired by the astonishing **energy efficiency** of the human brain

Digital Computing  
(CMOS power density)

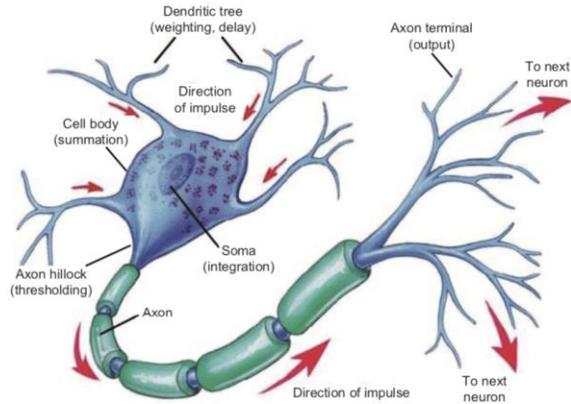


Human Brain

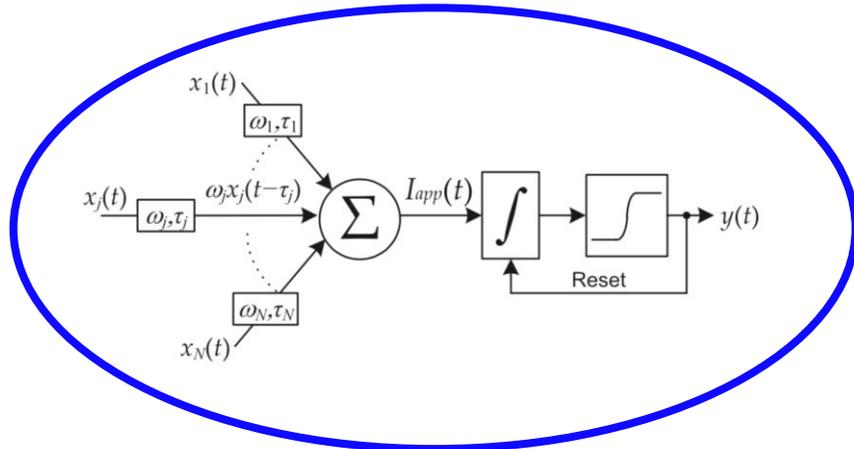


Only 20 W total power consumption ...

# Artificial Neural networks



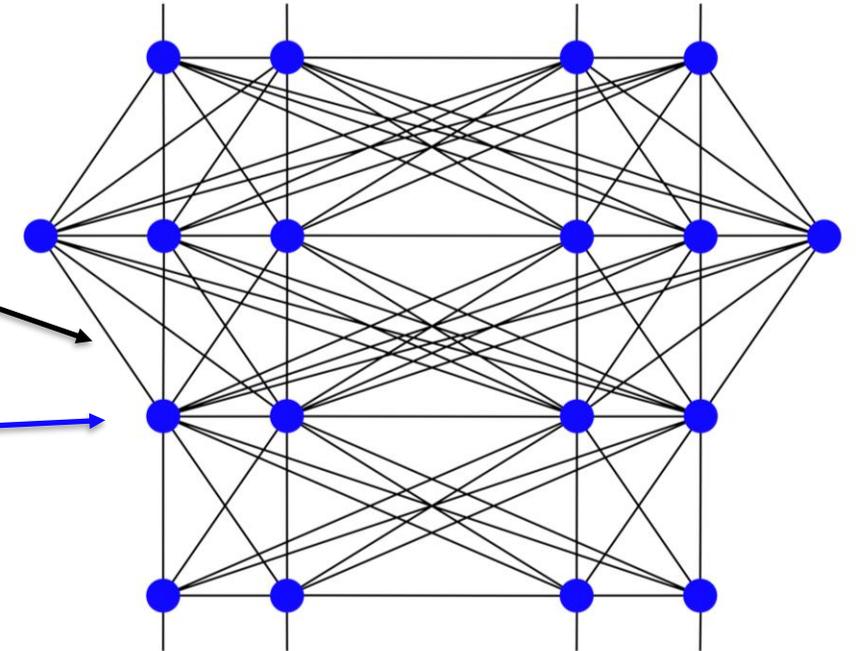
Biological Neuron



Nonlinear Building block:  
„Artificial neuron“

Connections  
„Artificial synapses“

Artificial neural Network



Computation using a highly connected networks  
of nonlinear elements

# Neuromorphic networks

- Inherently **analog processing**  
→ digital systems are rather inefficient, wave-based approaches have a natural advantage
- **Nonlinearity:** every neuron has a build-in nonlinear function
- **Highly interconnected systems:**  
the (energy) efficiency of the connections can be more important than the efficiency of the neurons
- **Reprogramming:** to learn, the strengths of the interconnections (“weights”) between neurons need to be changed

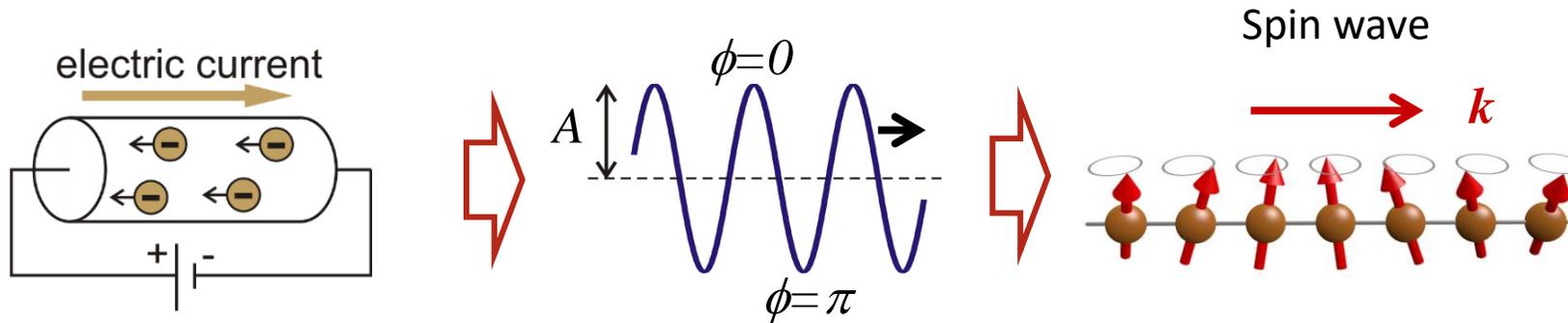
## Human brain:

- About 85 billion neurons connected by about  $10^{14}$  synapses
- **Every neuron has about 1.000-30.000 direct connections to other neurons**
- Total length of the connections: 5.6 million km



- General concept of an all-spintronic network using spintronic auto-oscillators and spin waves
- Neuromorphic computing using spintronic auto-oscillators
- Nano-magnonic building blocks
- Inverse design magnonics
- Coupling of spintronic auto-oscillators and nano-magnonic building blocks

- Use of spin waves (quasi particle: magnon) to transport and process data



Variable

Scalar

Vector

$(A, \phi, f, k)$

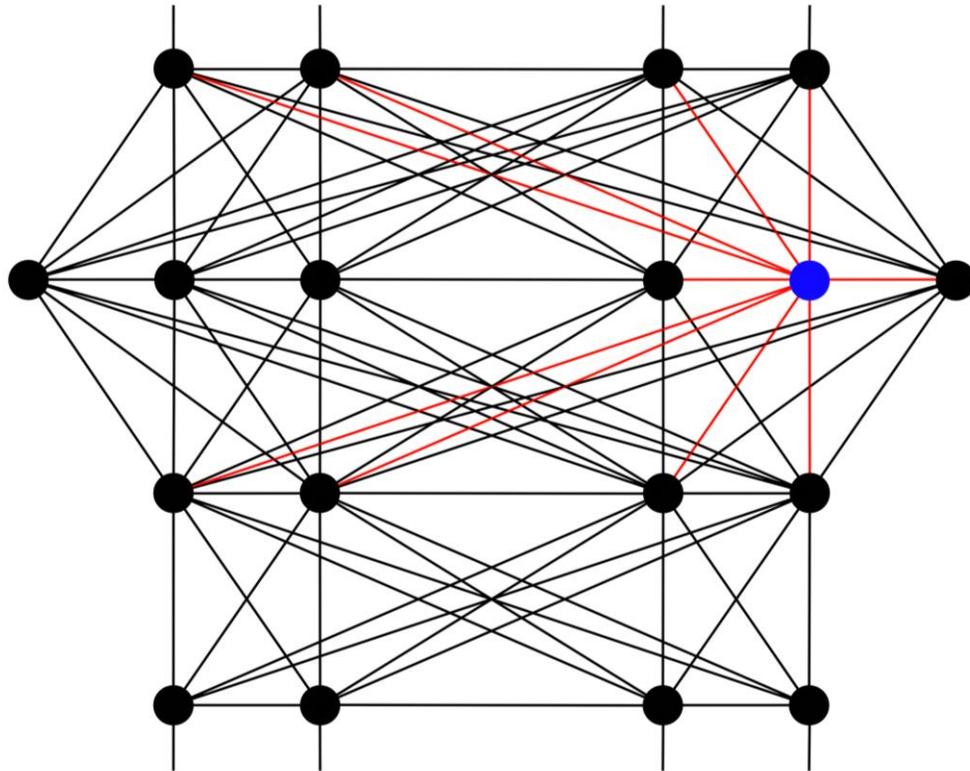
Transport

Driven by **potential gradient**

Driven by **wave propagation**

- Coherent coupling
- Interference effects and logic
- Intrinsic nonlinearity
- Scalability: Nanometer wavelength
- Frequency multiplexing

# Connectivity challenge



Direct physical realization?

## Electrical wiring scheme

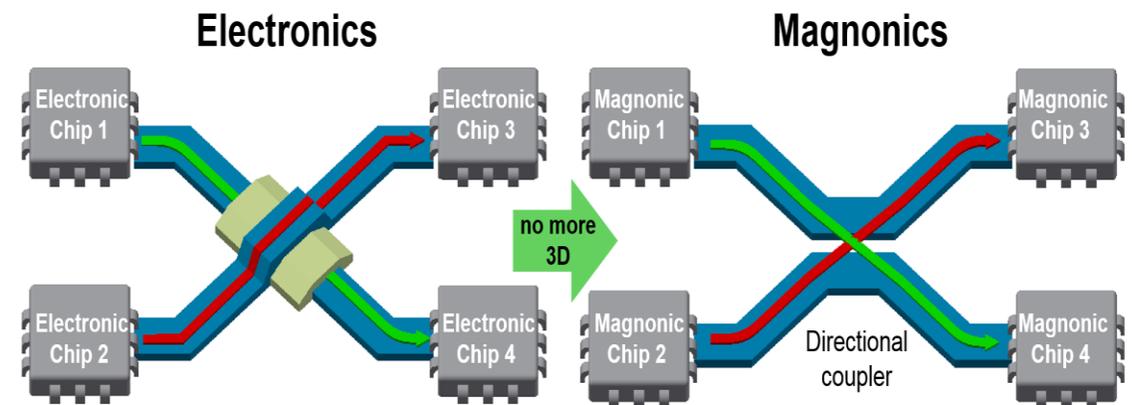
A network with  $N$  neurons needs  $\frac{N(N-1)}{2}$  physical connections to create *all-to-all connectivity*

“Hopfield network”:

J. J. Hopfield, Proc. Natl Acad. Sci. USA 79, 2554 (1982).

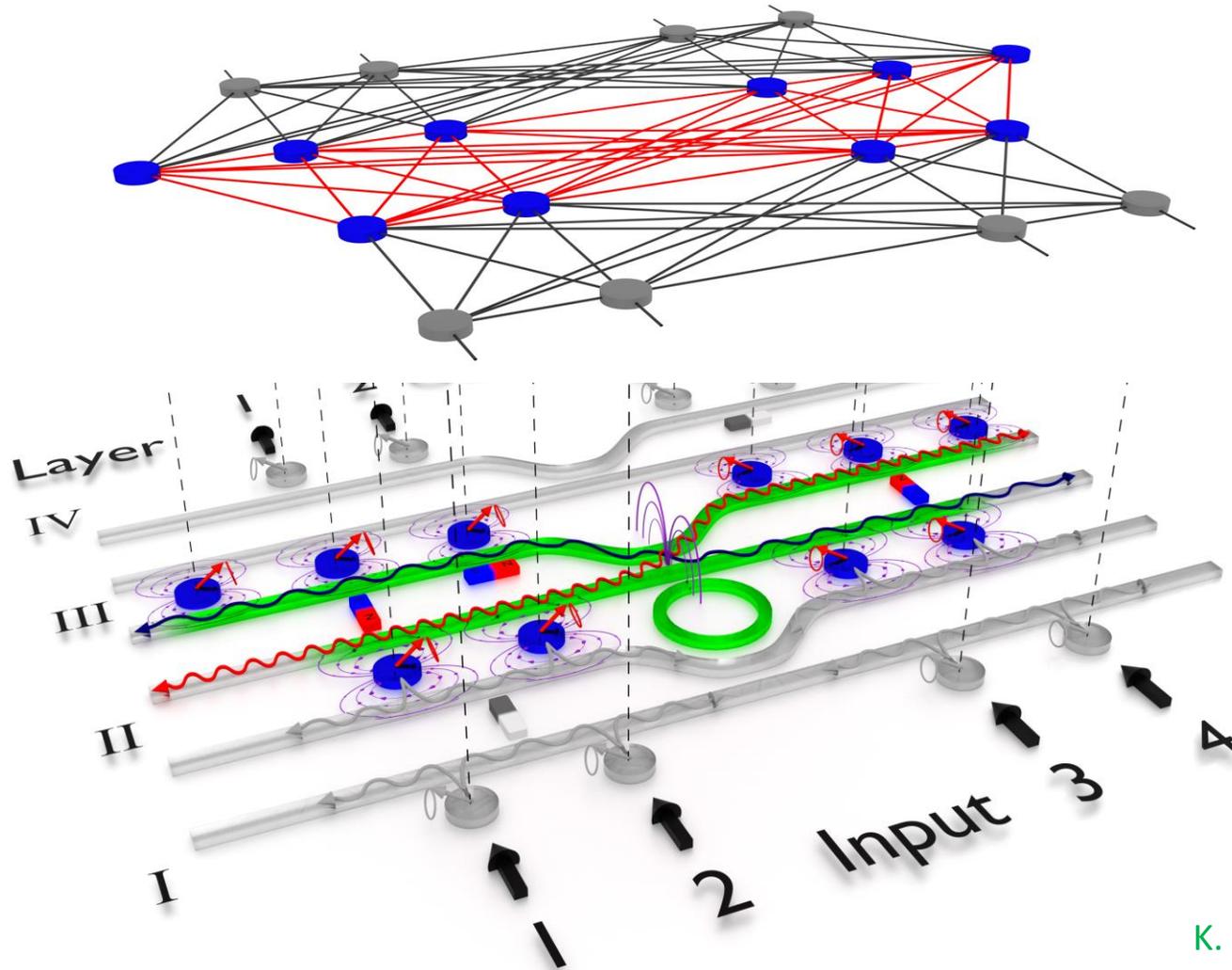
## Connection by waves

Use of **coherent coupling effects** allows to use 2D systems



Additional reduction of physical interconnects by **frequency multiplexing**

# Our concept: all-spintronic approach



## Artificial Neurons: spintronic auto-oscillators (SAO)

Nanoscaled objects with high intrinsic nonlinearity

## Interconnects: coherent spin waves

- Artificial synapses created by ultralow-damping magnonic nano-conduits
- Including coherent coupling effects, interference, spin-wave nonlinearity and frequency multiplexing

## Programming: magnetic memory cells

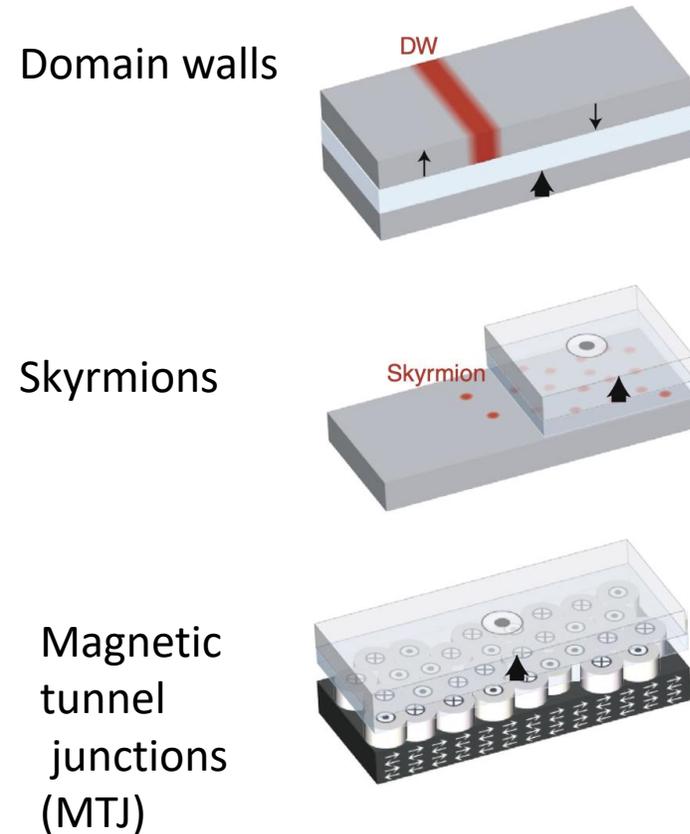
Nanomagnets like those used in MRAM influencing the spin-wave propagation

Not the focus of this talk, but several realizations exist

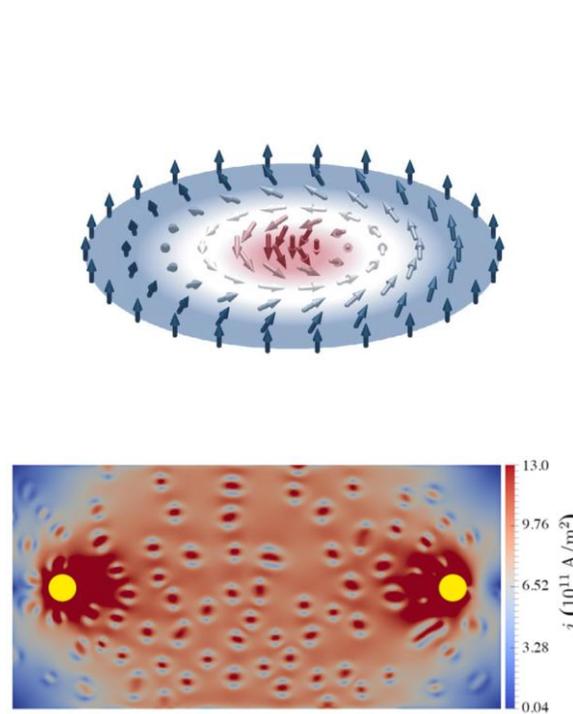
K. Baumgaertl and D. Grundler, "Bistable nanomagnet as programmable phase inverter for spin waves," *Appl Phys Lett*, **118**, 162402, (2021).

# Further neuromorphic spintronic elements

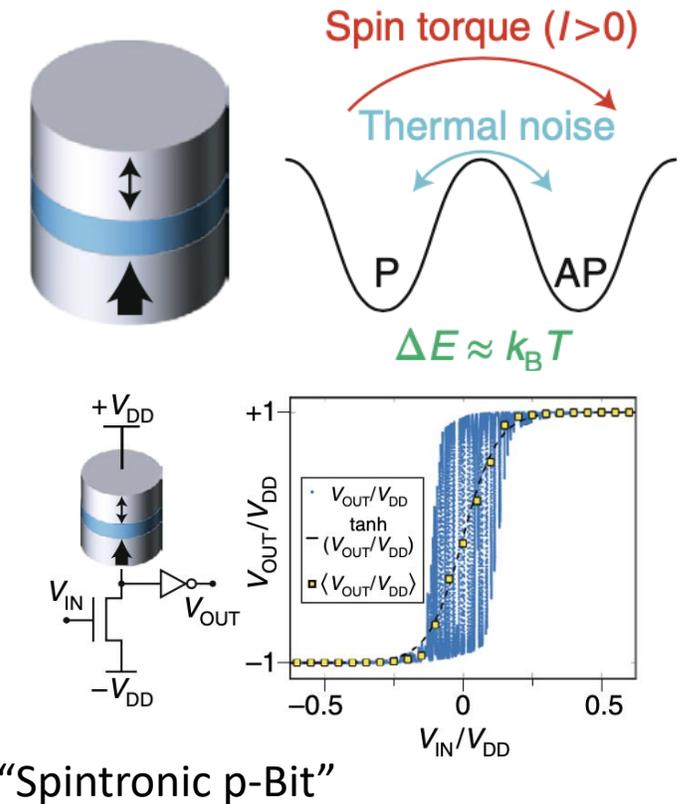
## Spintronic Memristors



## Skymion reservoirs



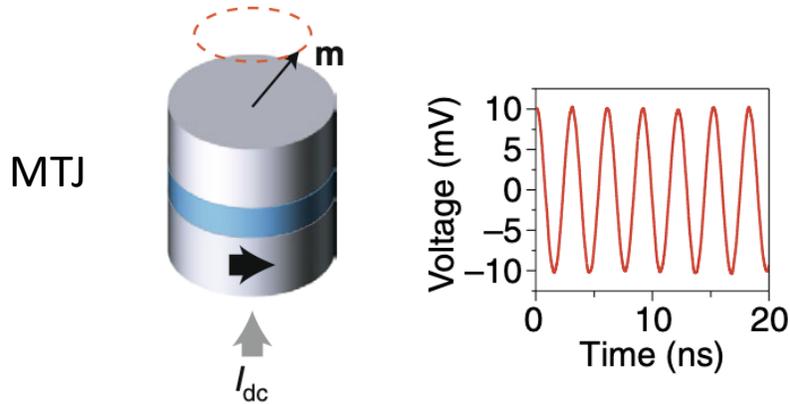
## Stochastic MTJ for probabilistic computing



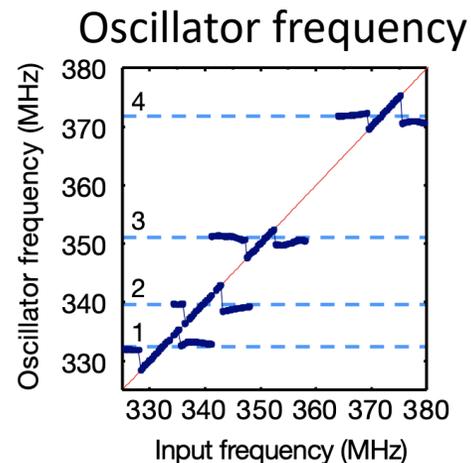
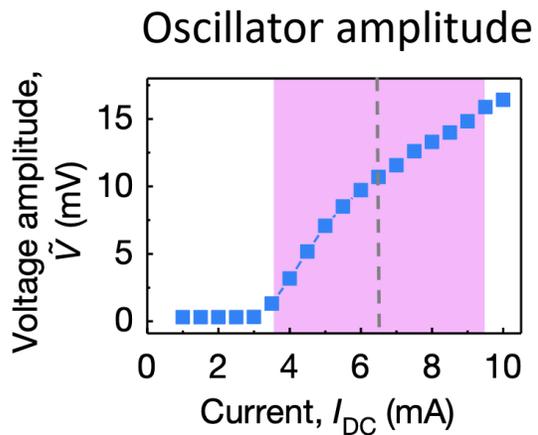
J. Grollier, D. Querlioz, K. Y. Camsari, K. Everschor-Sitte, S. Fukami, and M. D. Stiles, “*Neuromorphic spintronics*,” *Nature Electronics* **3**, 360–370 (2020).

# Spintronic (auto)-oscillators

Example: **Spin torque nano-oscillator (STNO)**



- Converts a DC electronic current in a sustained magnetic auto-oscillation
- Frequency ranges from 0.1 to several tens of GHz
- Both amplitude and frequency of the auto-oscillation depend nonlinearly on injected current, external signals

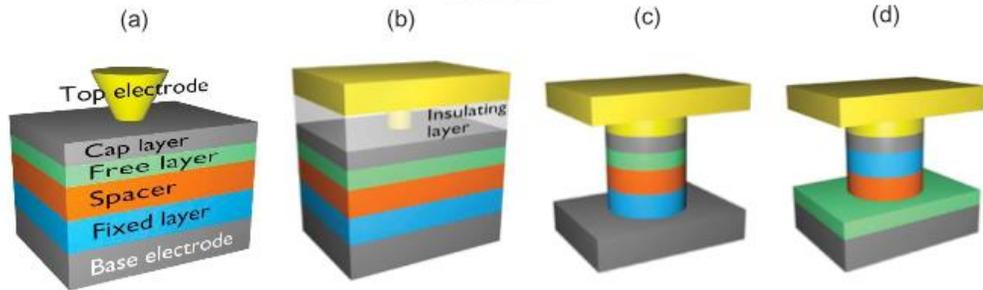


M. Romera, *et al.*, *Nature* **563**, 230–234, (2018).  
J. Torrejon, *et al.*, *Nature* **547** 428–431 (2017).

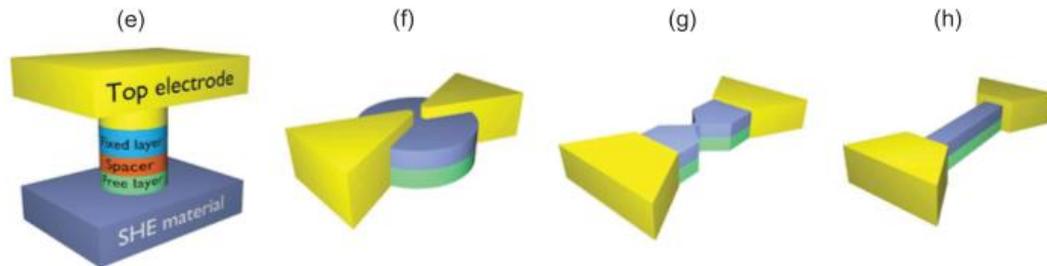
# Different types of spintronic auto-oscillators (SAO)

**Spin-torque nano oscillators (STNO)** based on spin current injected from a fixed magnetic layer

STNOs



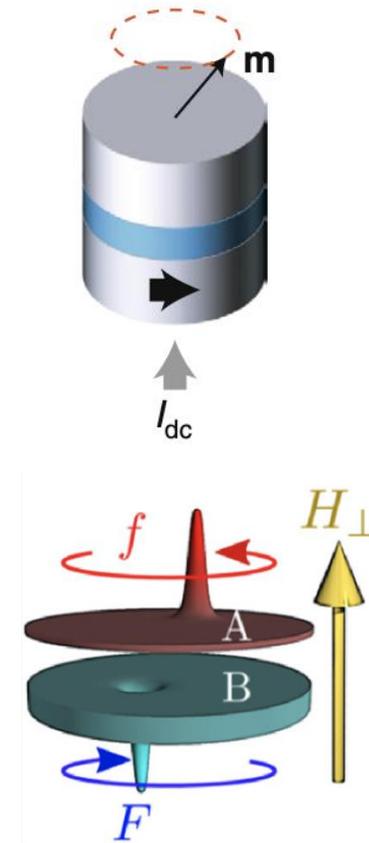
SHNOs



**Spin Hall nano oscillators (SHNO)** based on spin current injected via the Spin Hall effect in an adjacent heavy metal like Pt

T. Chen, *et al.*, *Proc. IEEE*, **104**, 1919–1945 (2016).

Uniformly magnetized oscillators

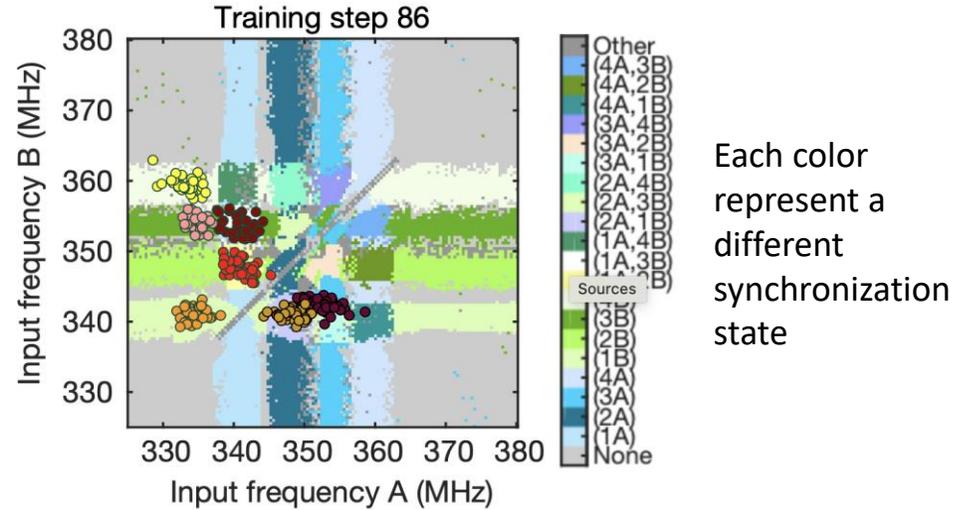
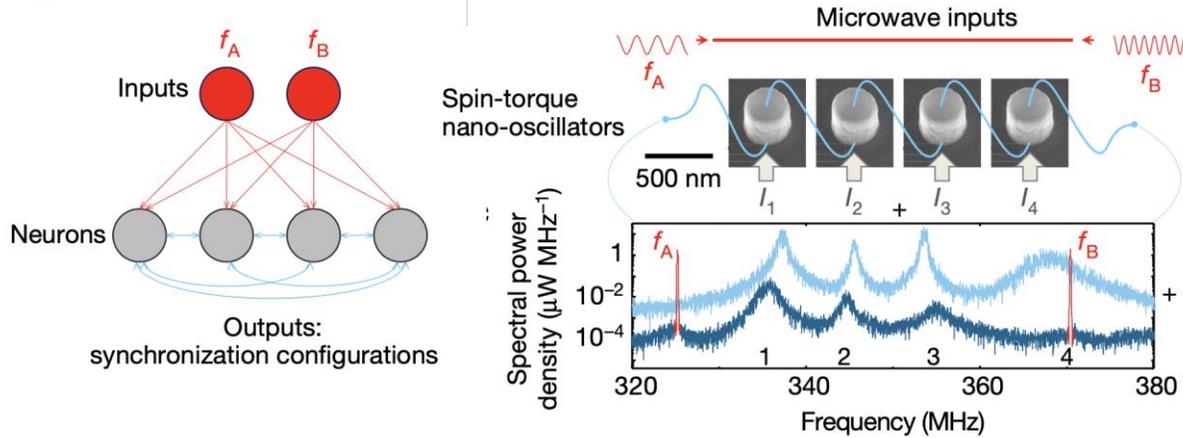


Vortex oscillators

J. Torrejon, *et al.* *Nature*, 547 428–431 (2017).

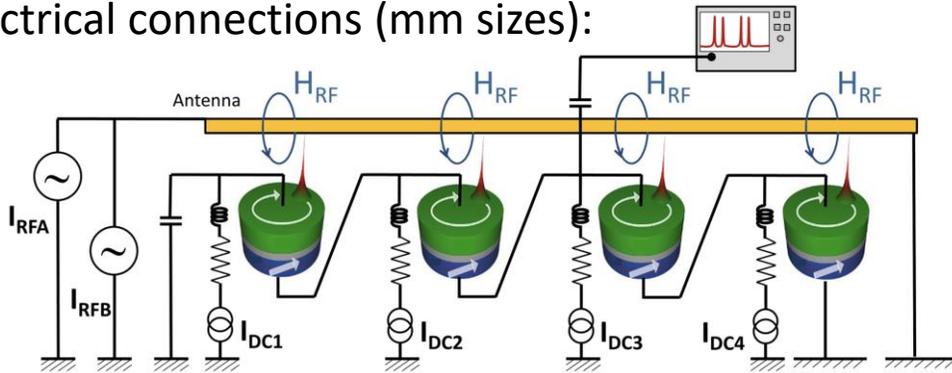
A. Hamadeh, *et al.* *Phys. Rev. Lett.*, 112, 257201 (2014).

# Spintronic auto-oscillators for neuromorphic computing



Each color represent a different synchronization state

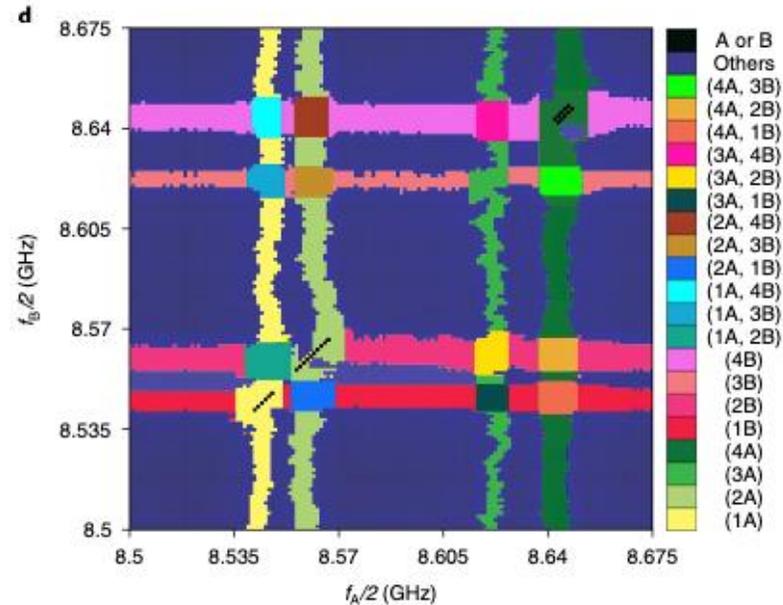
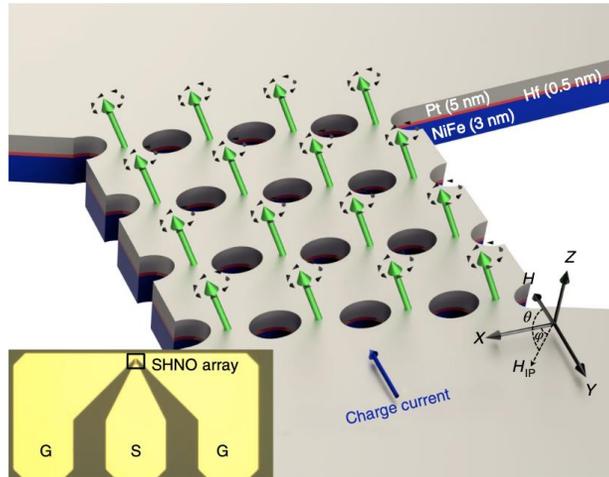
Electrical connections (mm sizes):



- Electrically coupled **SAOs synchronize to external microwave signals** representing the input data
- Training: Oscillator frequencies are tuned electrically by changing the DC current
- After training, vowel is recognized from the synchronization state: which oscillators synchronizes to which input frequency

M. Romera, *et al.*, “Vowel recognition with four coupled spin-torque nano-oscillators,” *Nature* **563**, 230–234, (2018).

Similar approach is possible using Spin Hall Nano Oscillators...



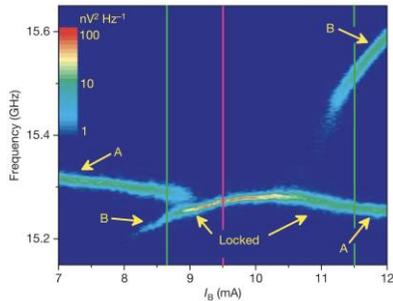
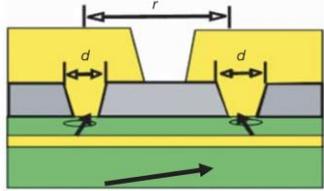
Synchronization map

However, challenge to change the connection between oscillators and to adjust individual oscillators for training...

M. Zahedinejad, *et al.*, *Nature Nanotech.*, **104**, 1–6, (2019).

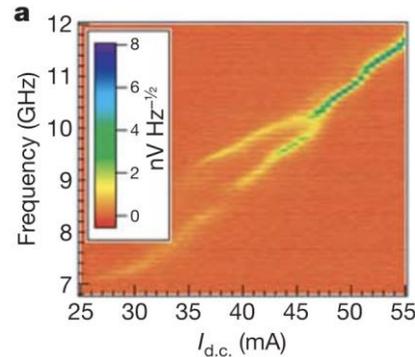
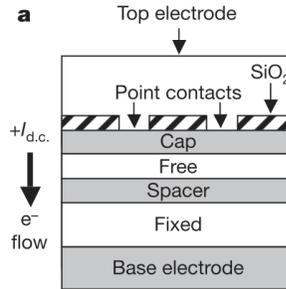
# Spin-wave based synchronization of SAOs

Synchronization for  
max. 500 nm separation



Spin-wave medium:  
5 nm NiFe

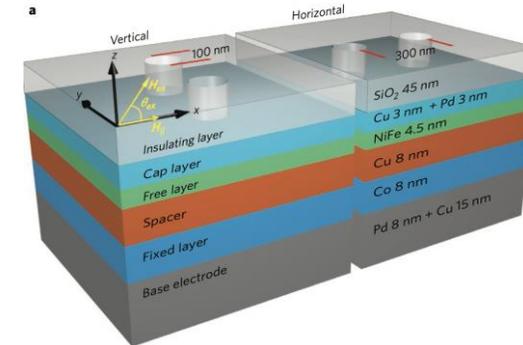
S. Kaka, *et al.*,  
*Nature* **437**, 389–392 (2005).



Spin-wave medium:  
4.5 nm NiFe

F. B. Mancoff, *et al.*,  
*Nature* **437** 393–395, (2005)

Synchronization for  
max. 1000 nm separation



Spin-wave medium:  
4.5 nm NiFe

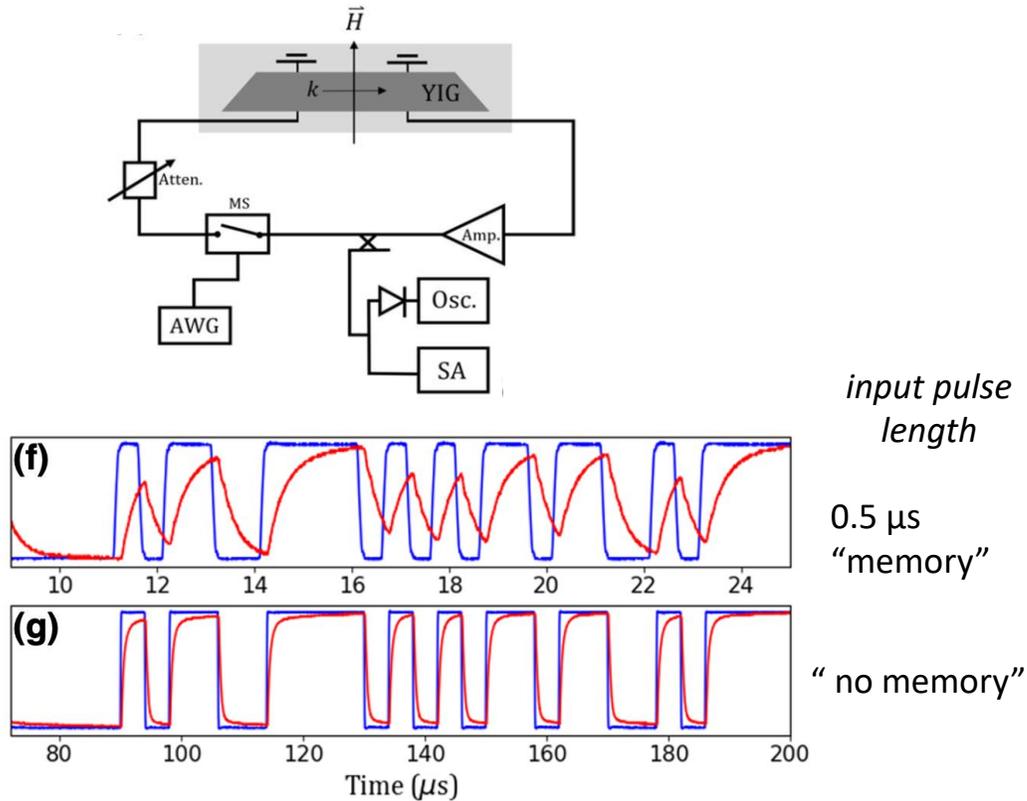
A. Houshang, *et al.*,  
*Nature Nanotech.* **11**, 280–286, (2016).

Systems are optimized for spin-toque effects, no emphasis on the magnonic aspects

- Very **small spin-wave decay length** (material, no dedicated waveguiding), **no interference effects** possible
- Only applicable for closely spaced SAOs with **next-neighbor coupling**, **no change of connections** possible

# Pure magnonic neuromorphic approaches

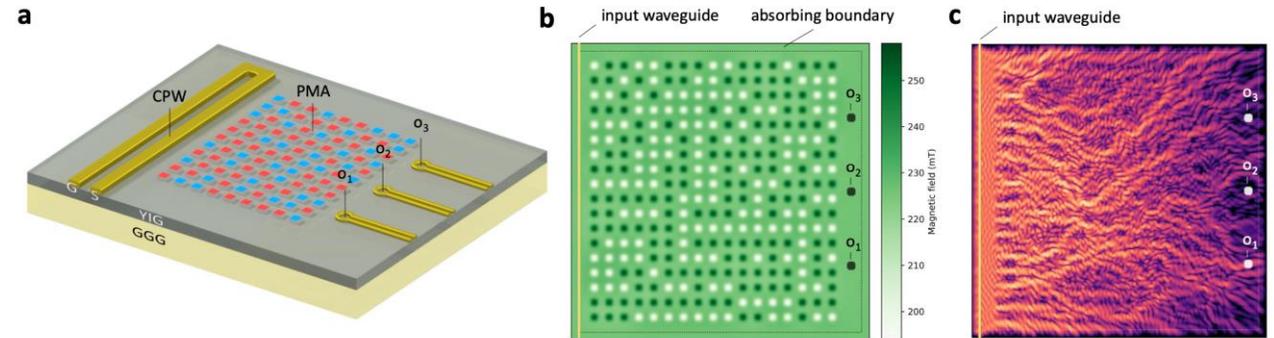
## Spin-wave delay-line active-ring resonator system



S. Watt and M. P. Kostylev, *Phys. Rev. Applied*, 13, 034057 (2020).

- Uses strong **nonlinearity** of the spin-wave system
- Delayed response, fading memory for **reservoir computing**

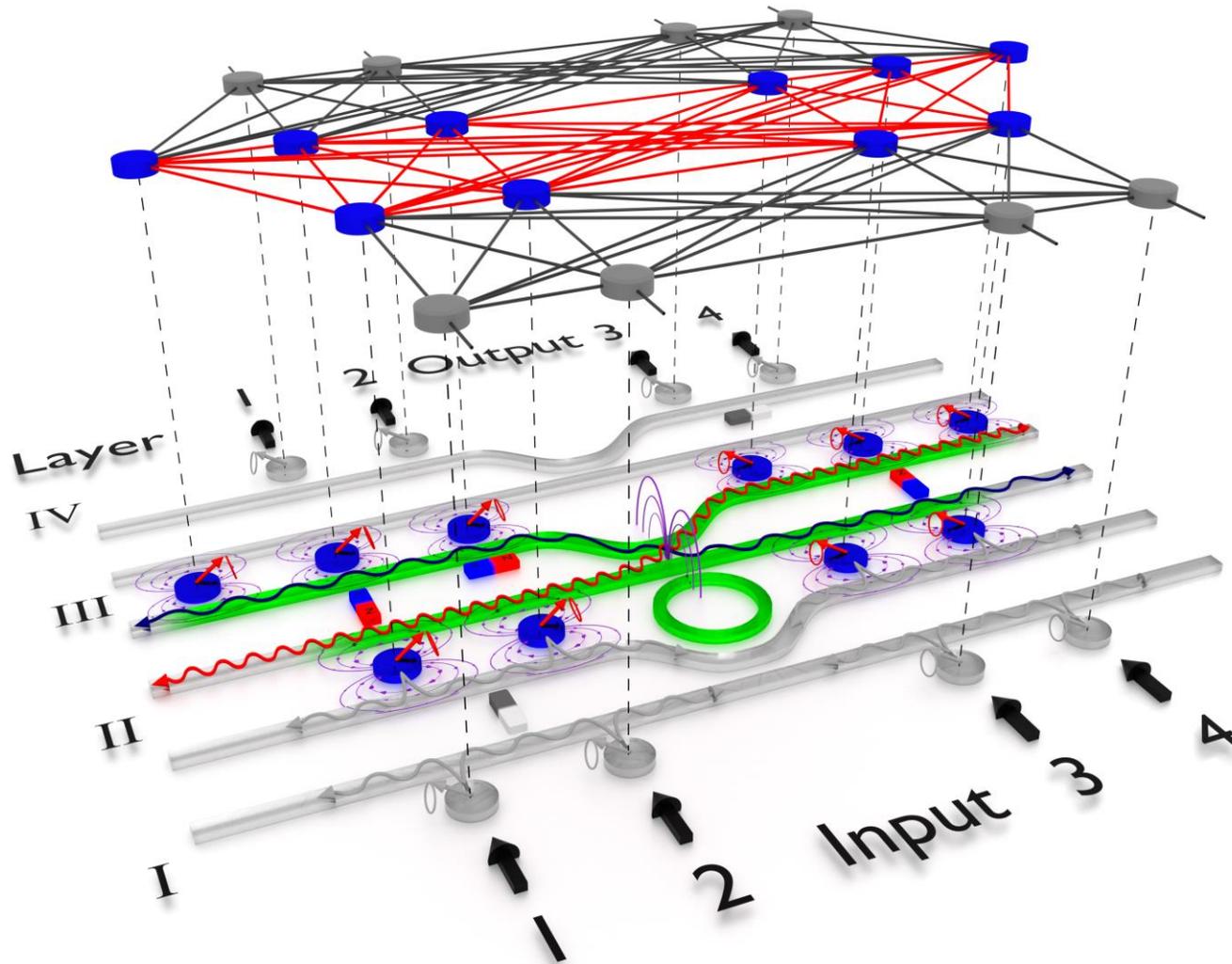
## Trainable magnonic neural network



A. Papp, *et al.*, arXiv: 2012.04594v1 (2020)

- Uses strong **nonlinearity** of the spin-wave system
- Small permanent magnets to train the system for **pattern recognition**

# Our concept



## Artificial Neurons: spintronic auto-oscillators (SAO)

Nanoscaled objects with high intrinsic nonlinearity

## Interconnects: coherent spin waves

- Artificial synapses created by ultralow-damping magnonic nano-conduits
- Including coherent coupling effects, interference, spin-wave nonlinearity and frequency multiplexing

# Theory for SAO coupled by spin waves

Extended Kuramoto model for the coupling of nonlinear oscillators by waves:

$c_n$ : amplitude of oscillator  $n$      $p_n$ : power of oscillator  $n$

$\Omega_{n,m}$ : **coupling strength** between two SAOs

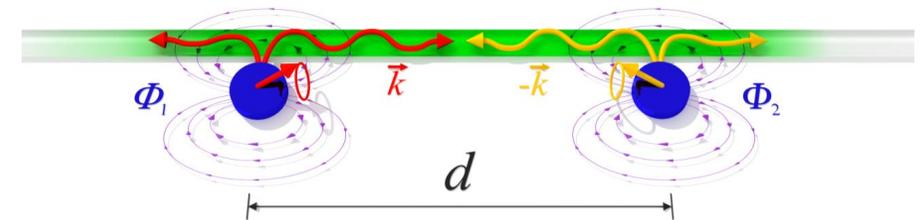
$\beta_{n,m}$ : **coupling phase** between two SAOs

$$\underbrace{\frac{dc_n}{dt} + [i \omega_n(p_n) + \Gamma_{+,n}(p_n) - \Gamma_{-,n}(p_n)] c_n}_{\text{Dynamics of free running oscillator } n} = \underbrace{\sum_m \Omega_{n,m} \cdot e^{i\beta_{n,m}} c_m}_{\text{Coupling of oscillator } n \text{ to other oscillators } m \text{ (via SW)}} + \underbrace{f(t)}_{\text{External force}}$$

$$\Omega_{n,m} \propto \frac{1}{d} e^{-d_{n,m}/\delta} \text{ for unguided spin-waves in an infinite thin film}$$

$$\Omega_{n,m} \propto e^{-d_{n,m}/\delta} \text{ for spin waves guided in a waveguide}$$

$$\beta_{n,m} = k \cdot d \text{ for spin-wave with wave vector } k$$



$\delta$ : exponential spin-wave decay length

A. Slavin and V. Tiberkevich, "Nonlinear Auto-Oscillator Theory of Microwave Generation by Spin-Polarized Current," *IEEE Trans. on Magn.*, **45**, 1875–1918 (2009).

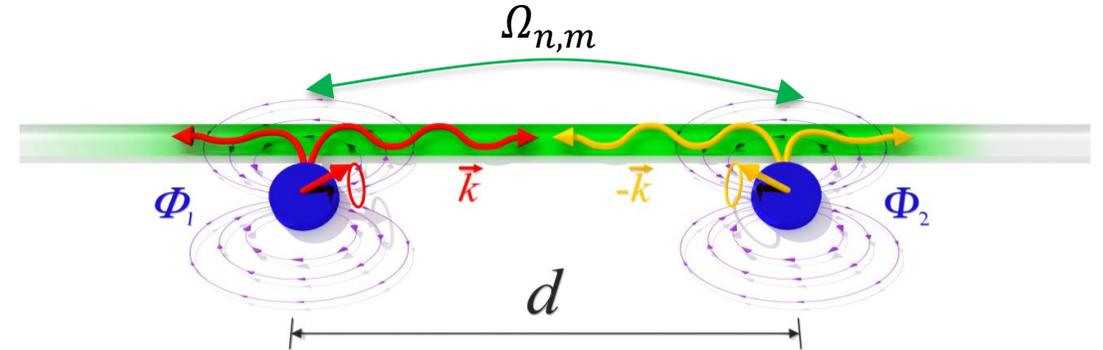
# Increasing connectivity range

High coupling strength also for large distances:

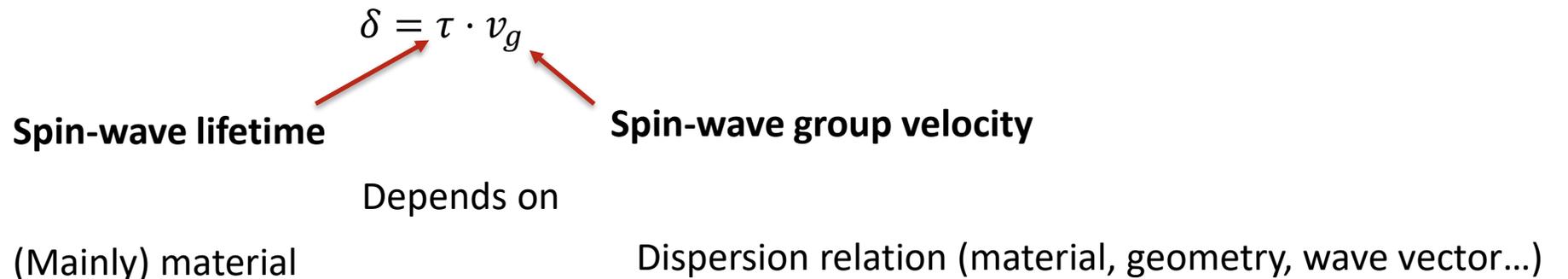
$$\Omega_{n,m} \propto \frac{1}{d} e^{-d_{n,m}/\delta} \text{ for **unguided** spin-waves in an infinite thin film}$$

$$\Omega_{n,m} \propto e^{-d_{n,m}/\delta} \text{ for spin waves guided in a **waveguide**}$$

→ Switching to guided waves removes geometrical decay

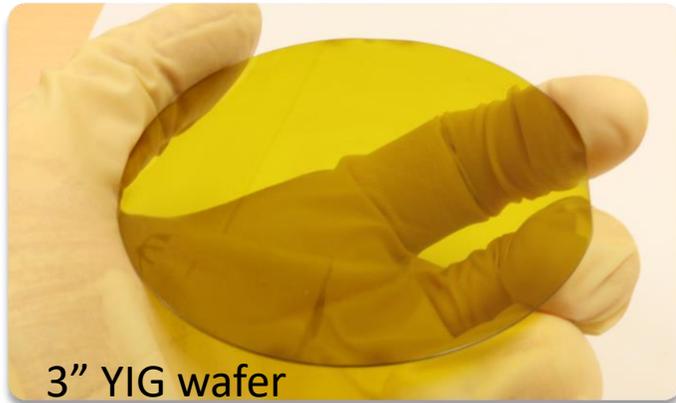


Need to maximize the **spin-wave decay length**  $\delta$  to increase the coupling:



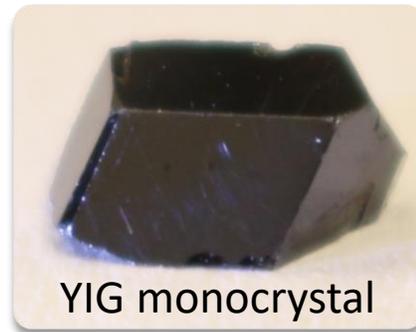
# Yttrium Iron Garnet (YIG, $Y_3Fe_5O_{12}$ )

- ❖ Room temperature ferrimagnet ( $T_C = 560$  K)
- ❖ Low phonon damping
- ❖ Magnon lifetime up to 500 ns !

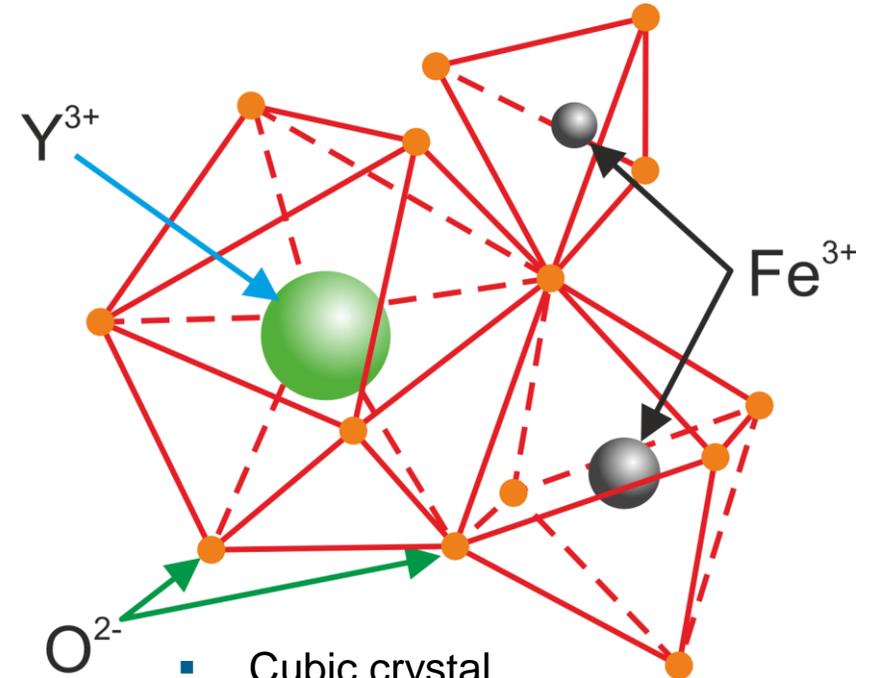


3" YIG wafer

Scientific Research Company  
"Carat", Lviv, Ukraine



YIG monocrystal



- Cubic crystal
- Lattice constant 12.376 Å
- Unit cell – 80 atoms

8 octahedral iron atoms (spin 5/2 up)  
12 tetrahedral iron atoms (spin 5/2 down)

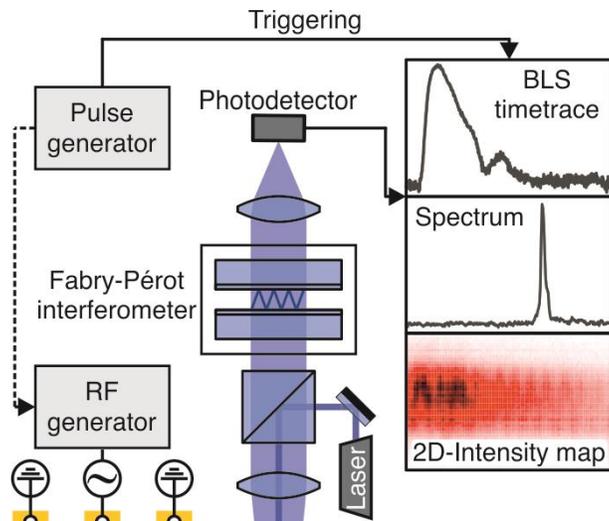


Magnetic moment of a unit cell is  
20 Bohr magnetons  $\mu_B$  at  $T=0$  K

LPE grown YIG films with very low damping down to 10 nm thickness:

C. Dubs, *Phys. Rev. Materials*, 4, 024416, (2020).

# Micro-focused Brillouin Light scattering



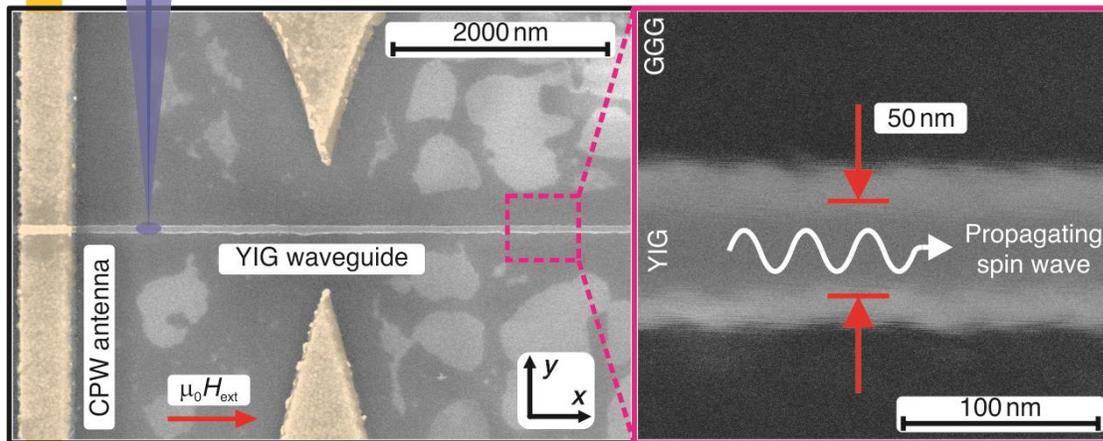
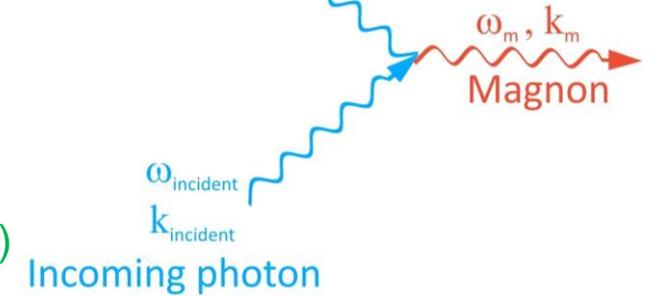
- Laser wavelength 457 nm
- Spot size  $\sim 300$  nm
- Wavevector sensitivity up to  $k_x = 24 \frac{\text{rad}}{\mu\text{m}}$

T. Sebastian *et al.*, *Front. Phys.* 3:35 (2015)

Scattered photon

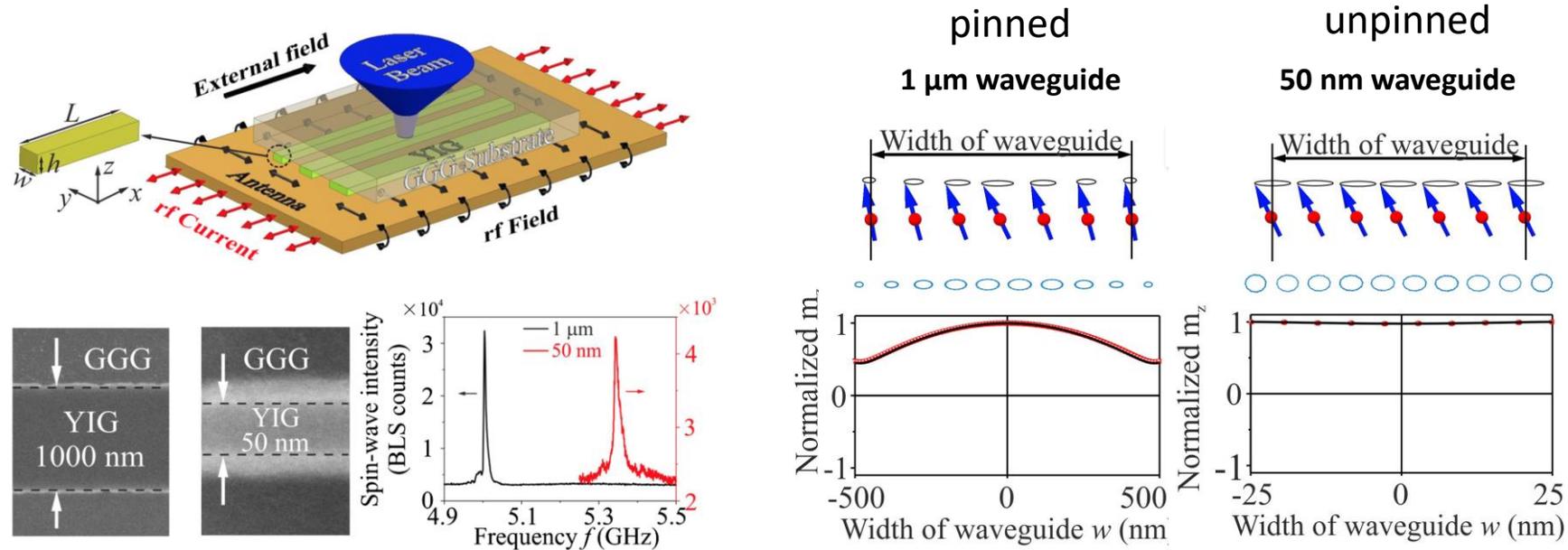
$$\omega_{\text{scattered}} = \omega_{\text{incident}} - \omega_m$$

$$k_{\text{scattered}} = k_{\text{incident}} - k_m$$



B. Heinz, PP *et al.*, *Nano Letters*, **20**, 4220 (2020).

# Spin-wave unpinning on the nanoscale

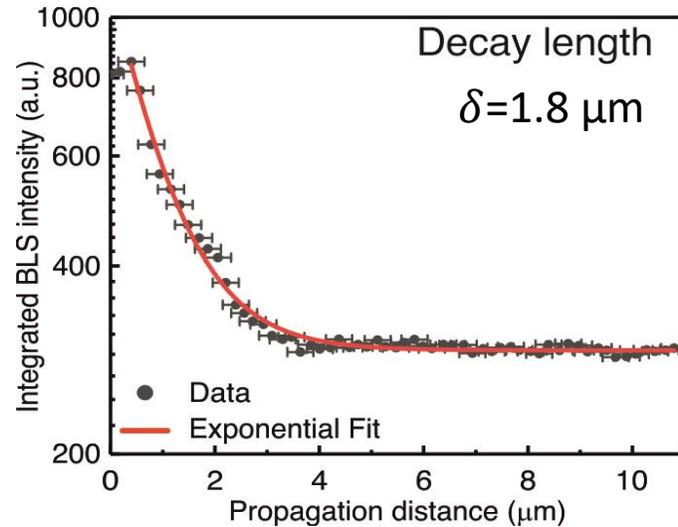


- Increase of the quantized **exchange** energy  $\propto A_{ex} \left( \frac{\pi}{w_{\text{eff}}} \right)^2$  leads to suppression of dipolar pinning of the modes: unpinning for waveguide widths below a critical value  $w_{\text{crit}}$
- **Unpinning increases the dynamic dipolar coupling between nanostructures**  
 → key factor for directional coupler, ring resonator, coupling to spintronic auto-oscillators...

Q. Wang, B. Heinz, PP, et al., *Phys. Rev. Lett.* **122**, 247202 (2019).

# Decay length in 50nm wide YIG waveguides

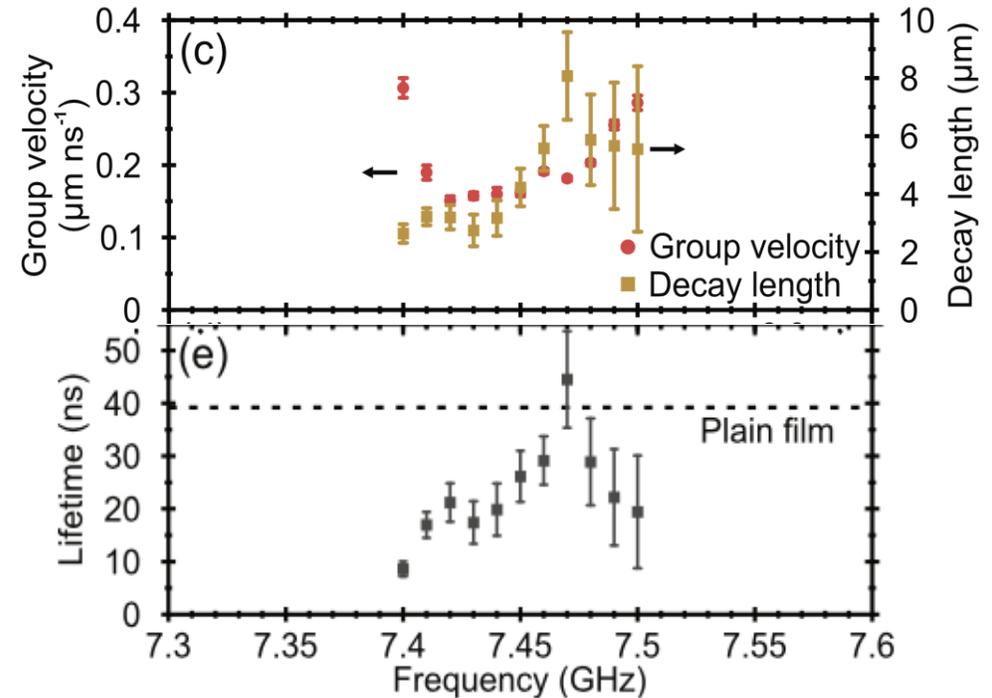
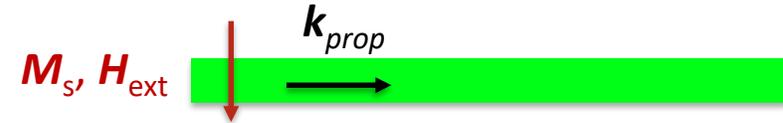
## “Backward Volume Geometry”



- Decrease of exponential decay length  $\delta$  for small width due to drop in group velocity of dipolar spin waves

B. Heinz, PP *et al.*, *Nano Letters*, **20**, 4220 (2020).

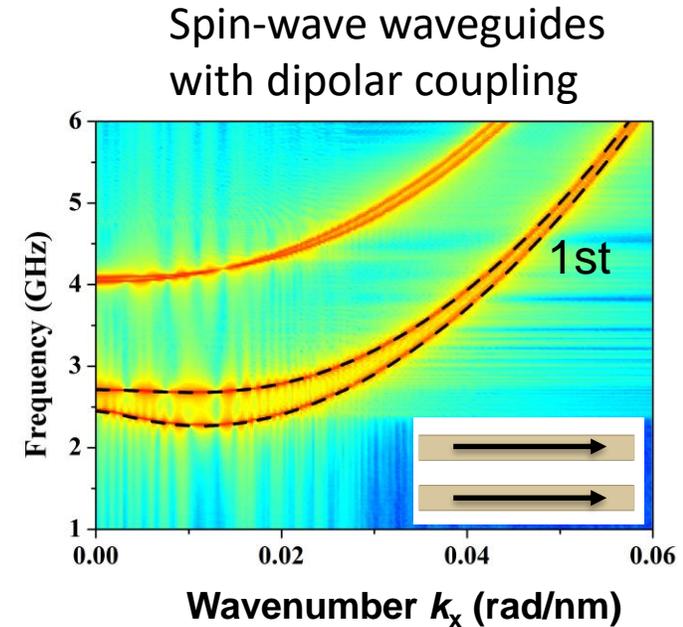
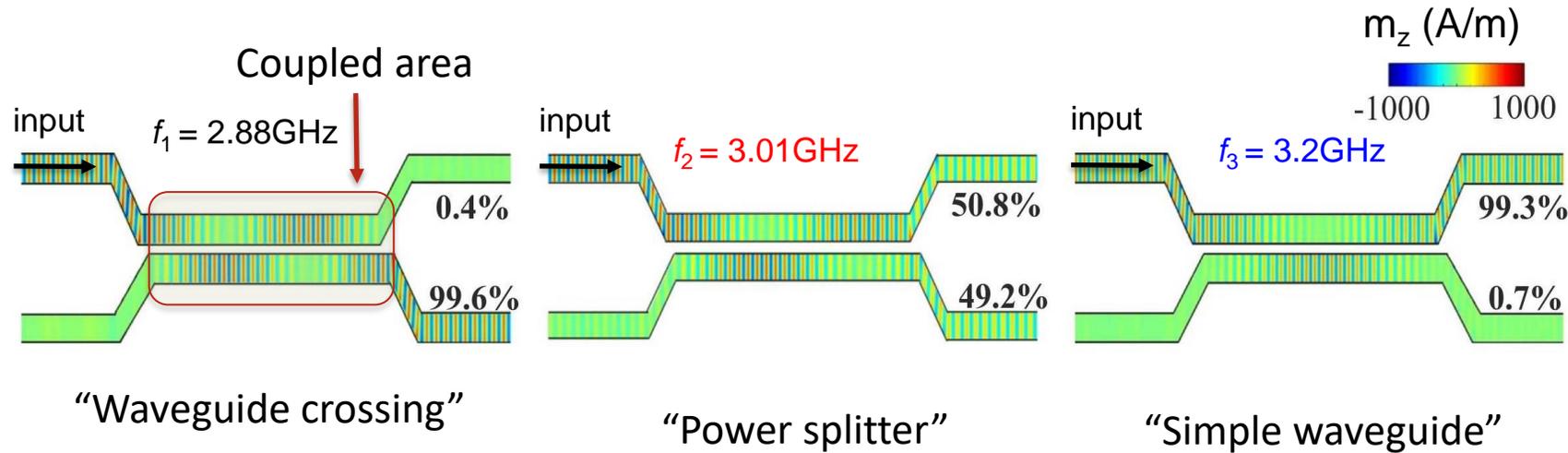
## “Surface wave geometry”



- Long-range spin-wave propagation in transversely magnetized nano-scaled conduits:**  
exponential decay length  $\delta > 5\mu\text{m}$

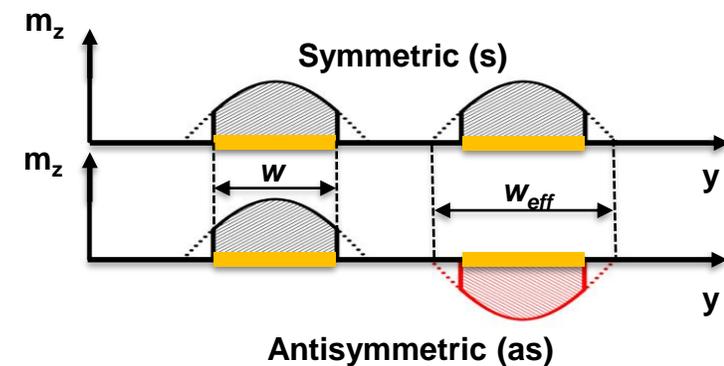
B. Heinz, PP, *et al.*, *APL* **118**, 132406, (2021).

# Spin-wave directional coupler



Coupling length depends on wavelength/frequency and magnetic field

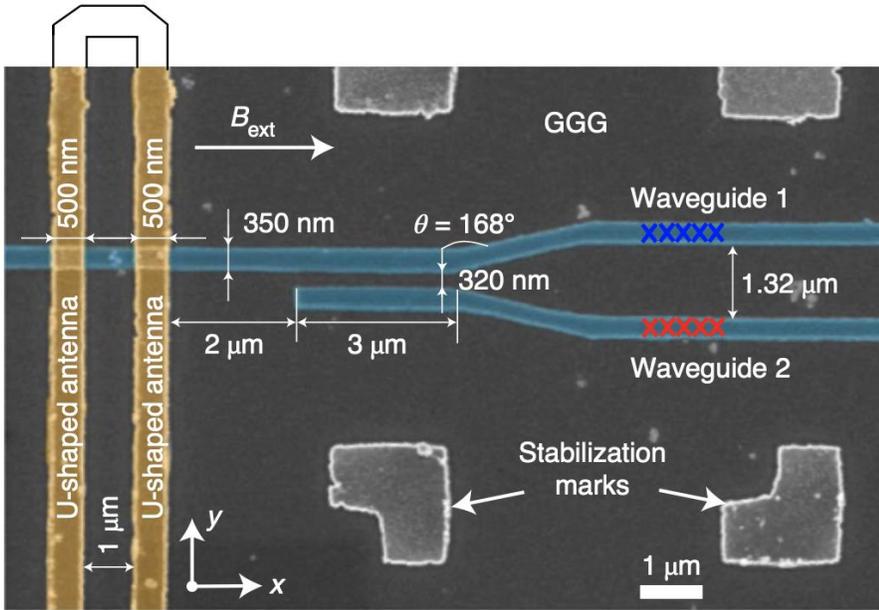
→ Switching of functionality with changing wavelength: crossing, power splitter, simple waveguide



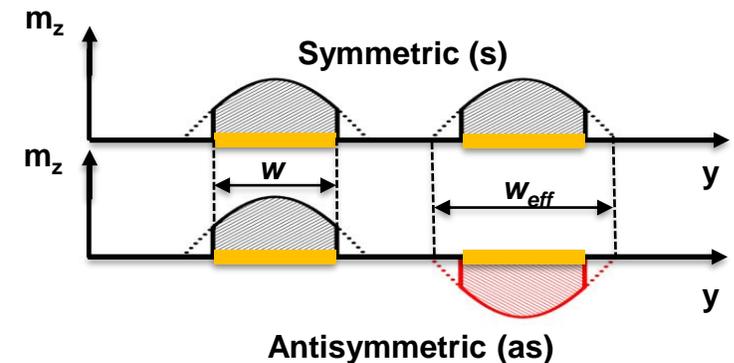
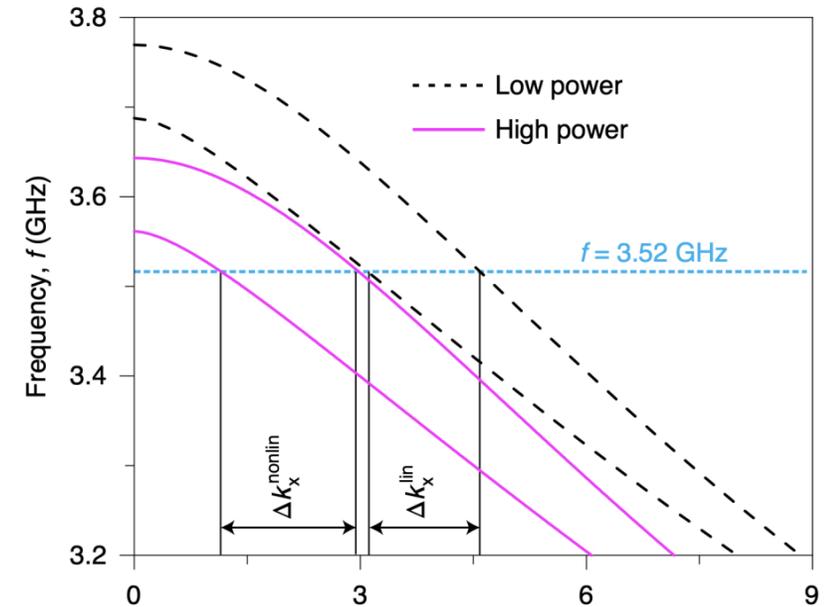
Q. Wang, PP, et al., Science Advances 4, e1701517 (2018)

# Nonlinear spin-wave directional coupler

In contrast to nonlinear SAO, nonlinear spin-wave devices usually work at **fixed frequency**  
employ a **nonlinear change of the wave vector  $k$** :

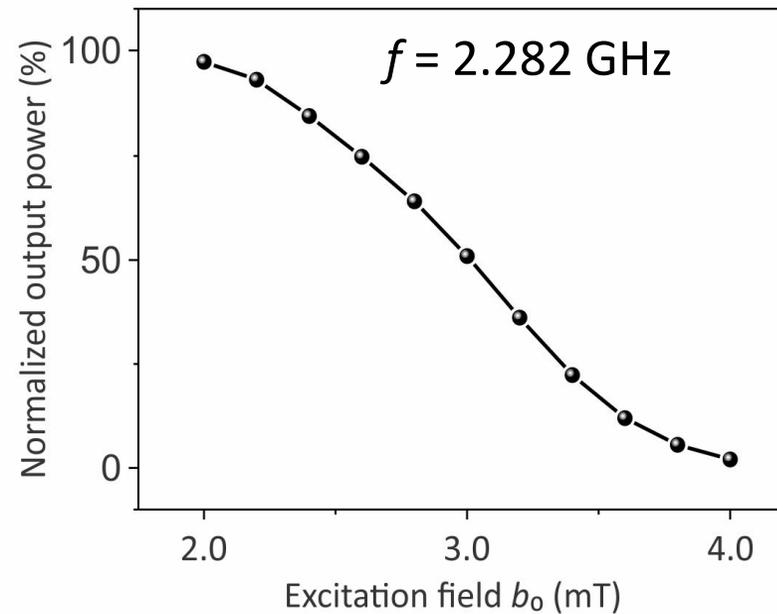
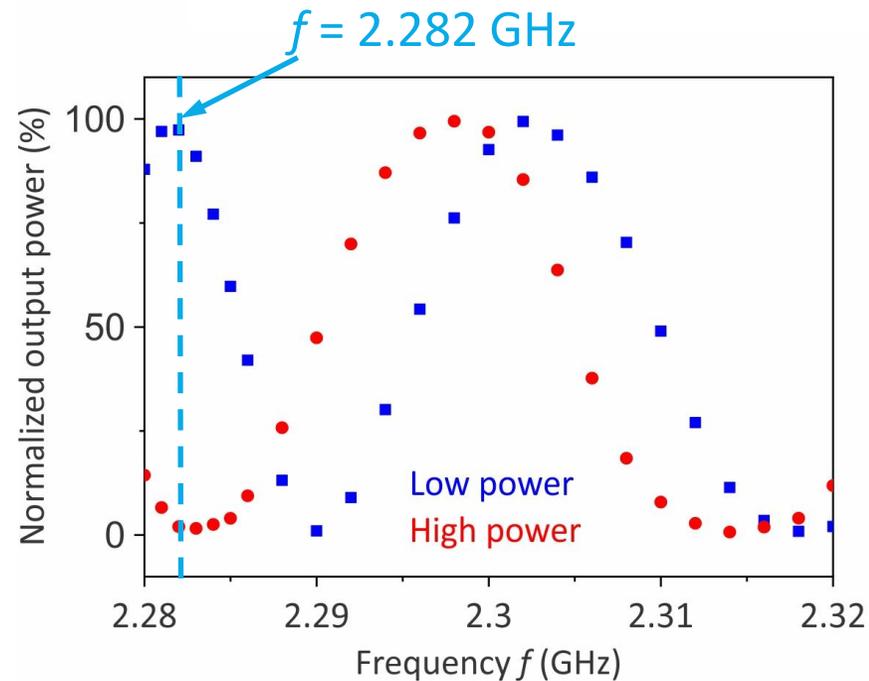
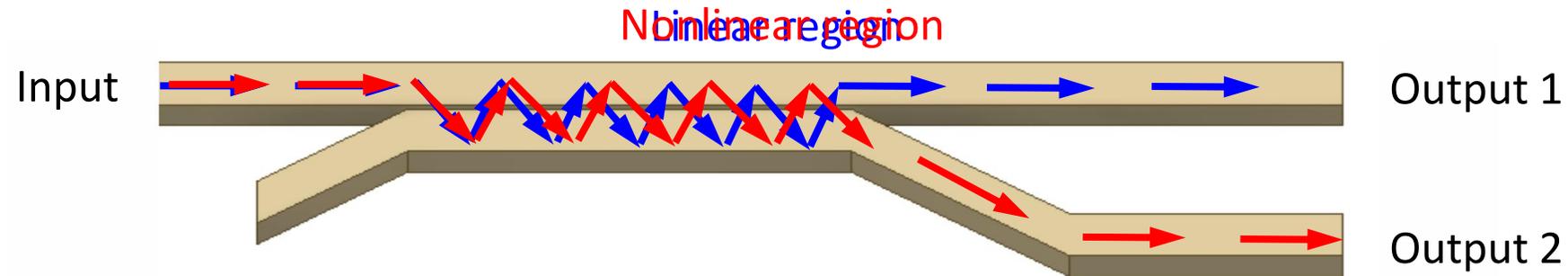


Nanoscaled directional coupler (YIG)



Q. Wang, PP, et al., *Nature Electronics* **3**, 765–774, (2020).

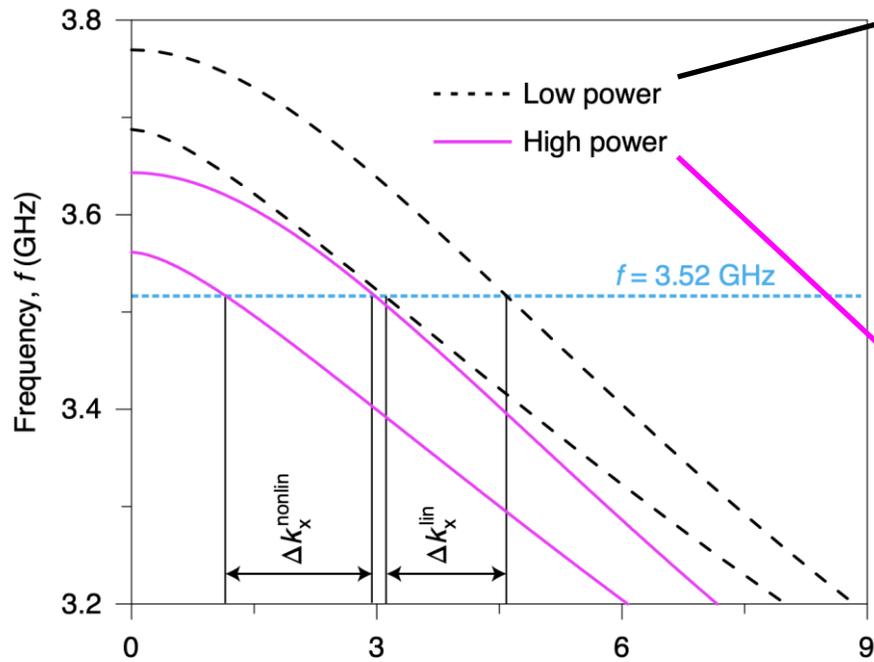
# Nonlinear spin-wave coupler



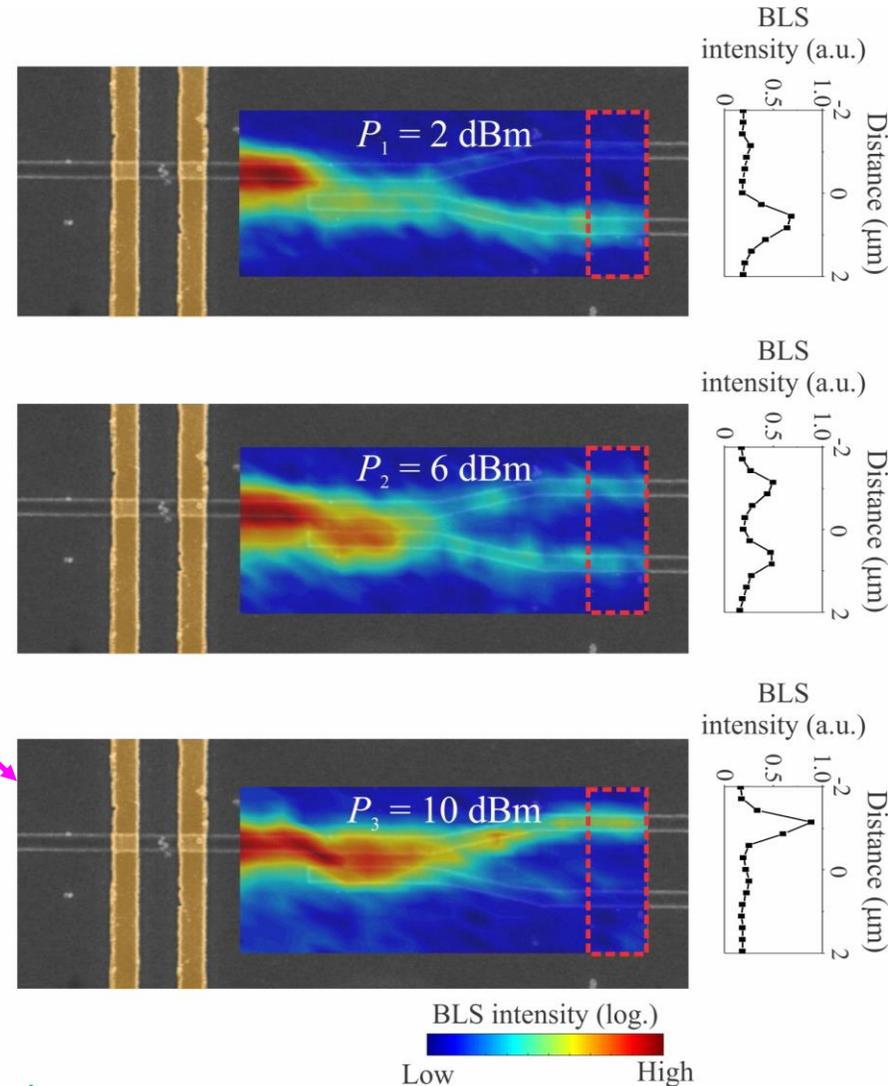
Directional coupler changes the output depending on the input power

Q. Wang, PP, et al., *Nature Electronics* **3**, 765–774, (2020).

# Nonlinear directional coupler: experimental validation



Nonlinear change of the dispersion relation leads to logic functionality

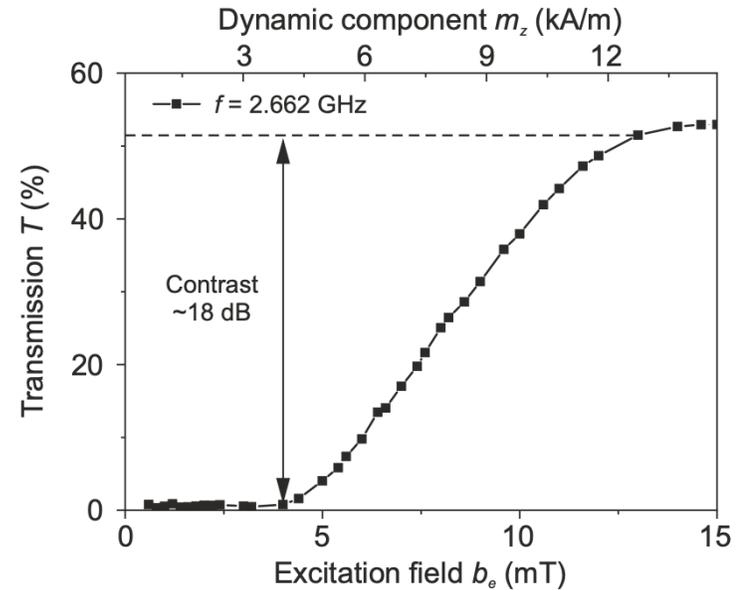
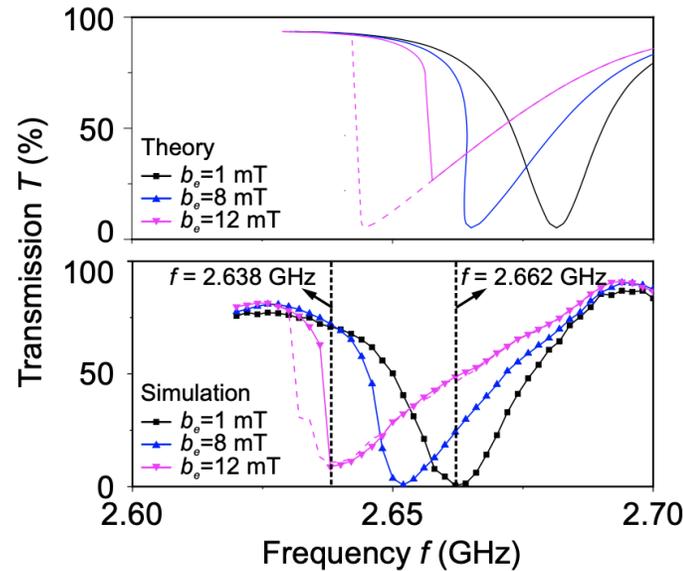
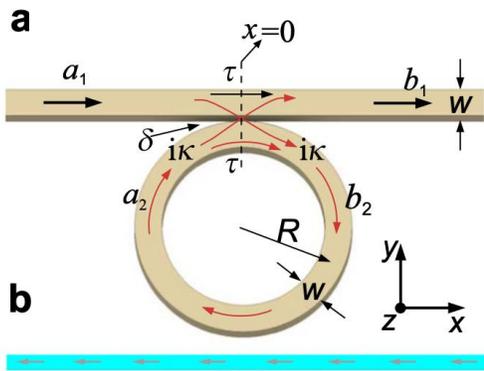
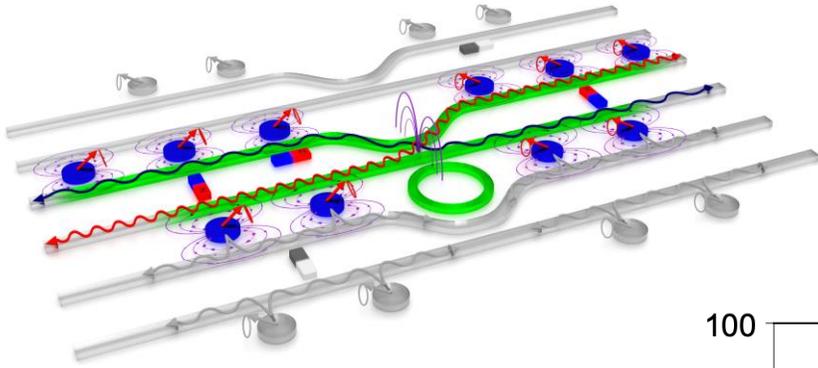


Q. Wang, PP, et al., *Nature Electronics* **3**, 765–774, (2020).

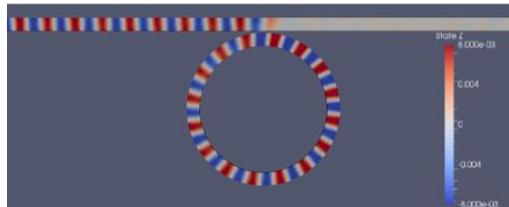
# Nonlinear magnonic ring resonator

Ring resonator:

- Frequency-dependent resonance for wave multiplexing
- Intrinsic spin-wave nonlinearity to create activation function



**Magnonic activation function**



Q. Wang, PP, *et al.*, npj Comput Mater, 6, 453 (2020).

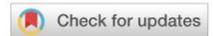
# How to design devices faster?



Use automated optimization algorithms to run micromagnetic simulations



ARTICLE



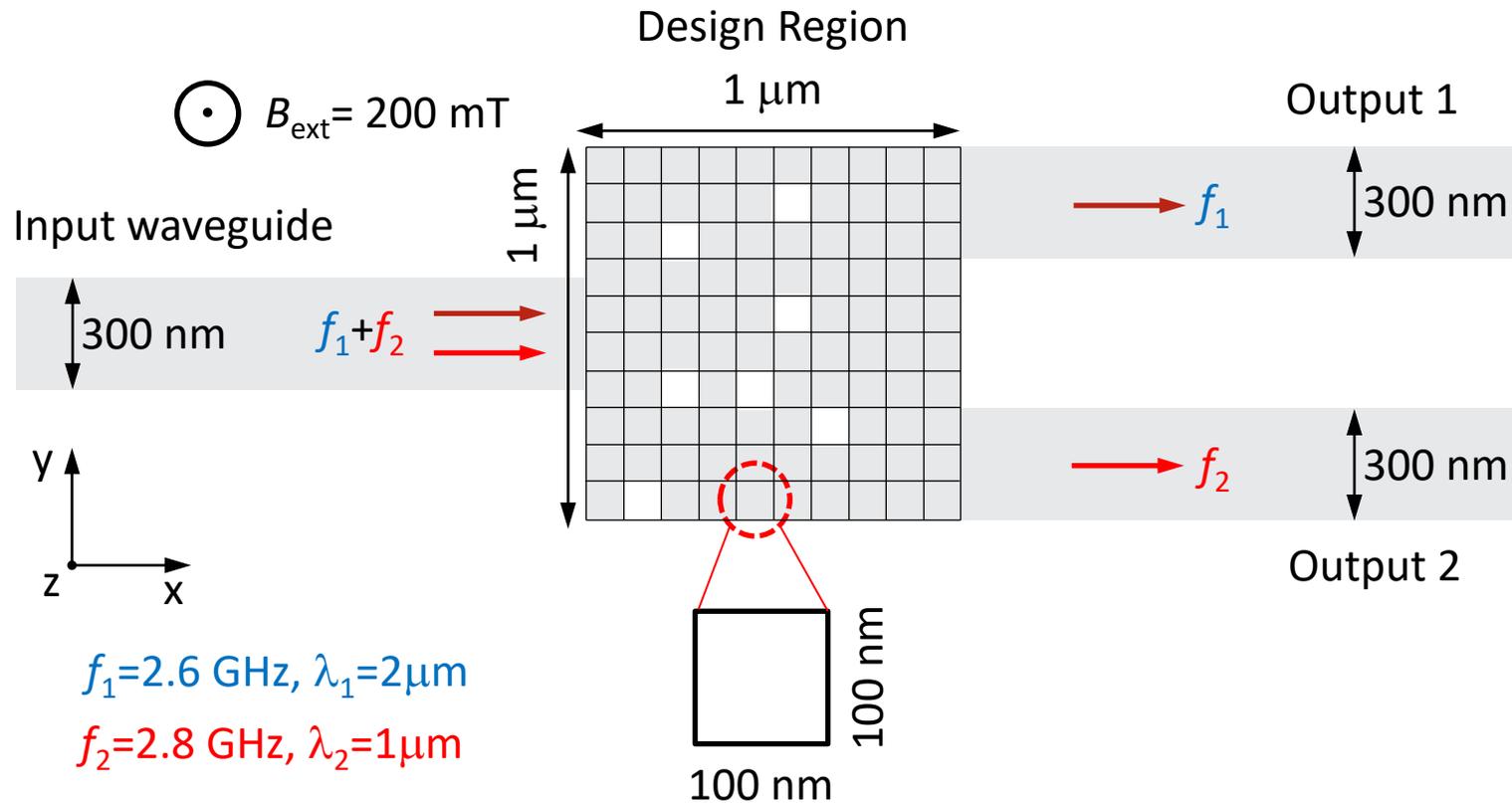
<https://doi.org/10.1038/s41467-021-22897-4>

OPEN

## Inverse-design magnonic devices

Qi Wang <sup>1</sup>✉, Andrii V. Chumak <sup>1</sup> & Philipp Pirro <sup>2</sup>

# Inverse design magnonics



Yttrium Iron Garnet (YIG):

$$M_s = 1.4 \times 10^5 \text{ A/m}$$

$$A = 3.5 \text{ pJ/m}$$

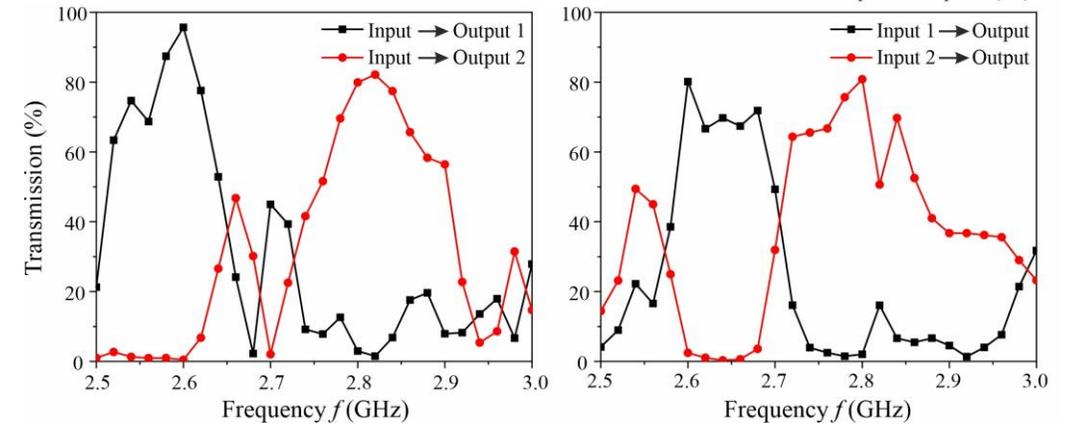
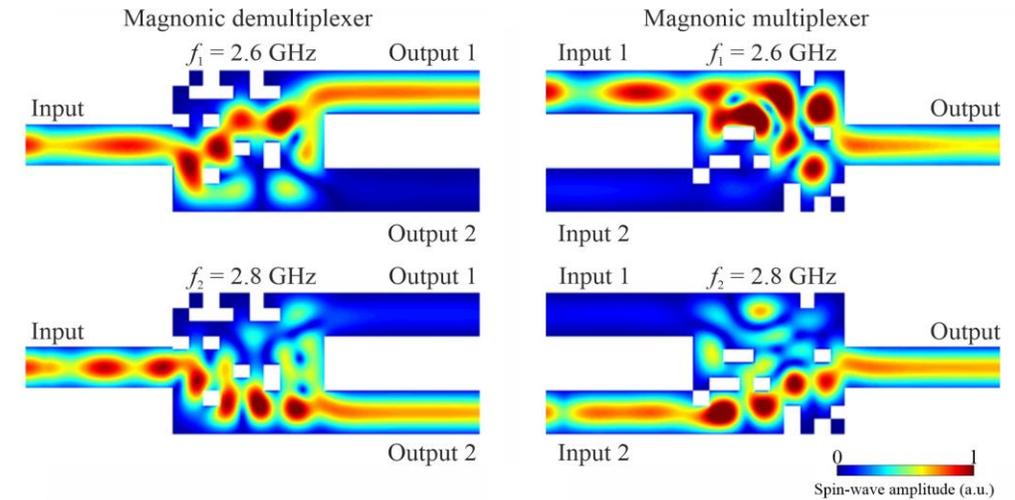
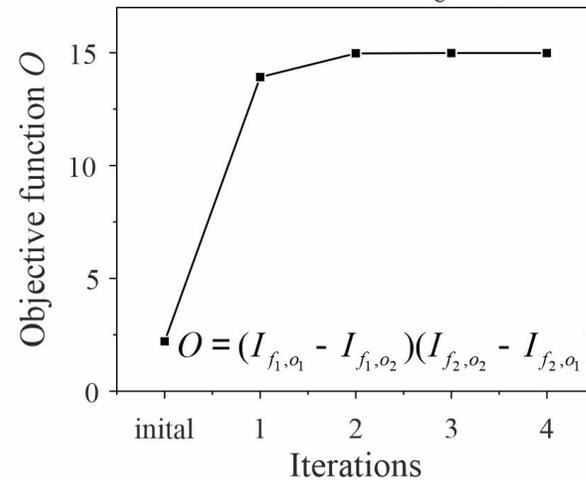
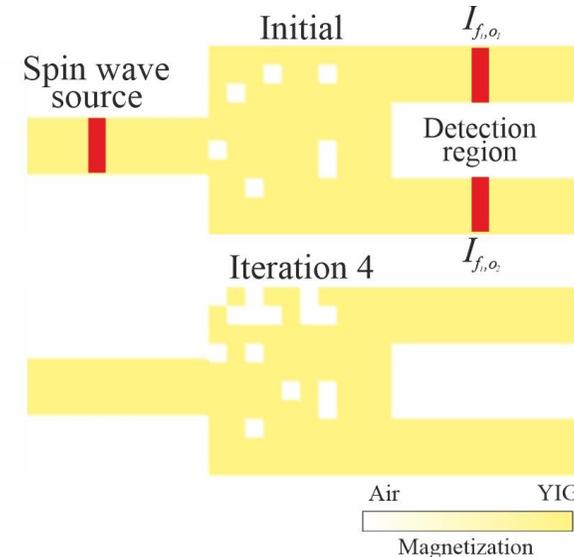
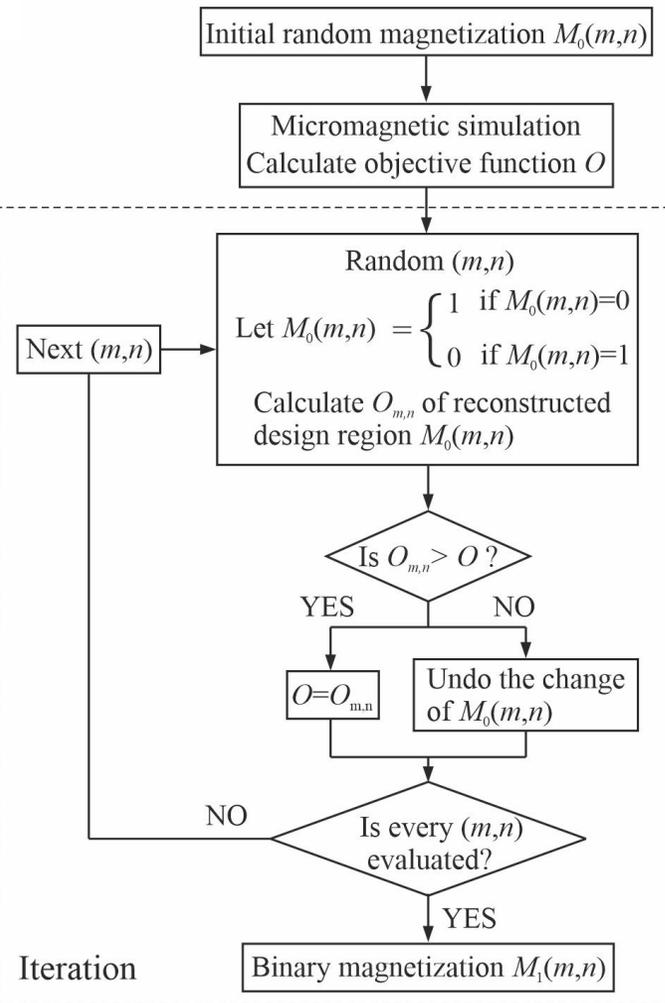
$$\alpha = 2 \times 10^{-4}$$

thickness = 100 nm

Cell size: 20 nm

Q. Wang, A. Chumak, P. Pirro, *Nature Commun.*, **12**, 2636 (2021)

# Inverse design magnonics

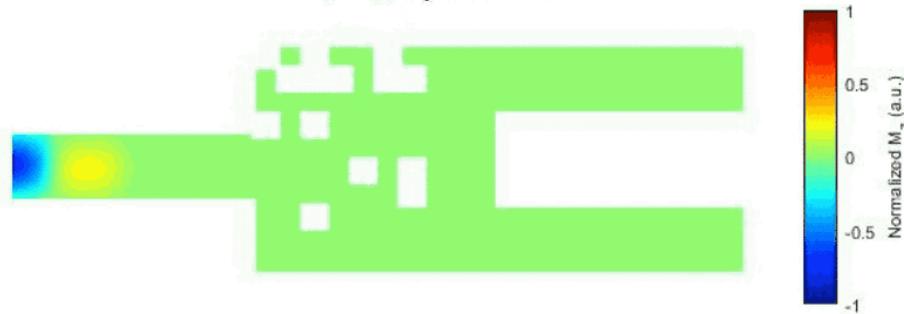


Q. Wang, A. Chumak, P. Pirro, *Nature Commun.*, **12**, 2636 (2021)

# Inverse design magnonics: frequency multiplexer

## Magnonic Demultiplexer

Time= 1 (ns),  $f_1=2.6\text{GHz}$



Time= 1 (ns),  $f_2=2.8\text{GHz}$



## Magnonic Multiplexer

Time= 1 (ns),  $f_1=2.6\text{GHz}$



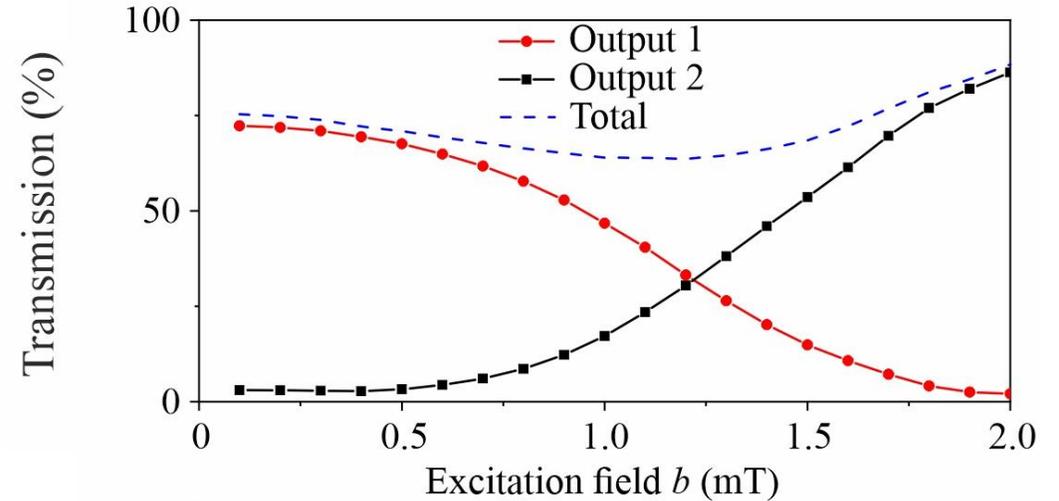
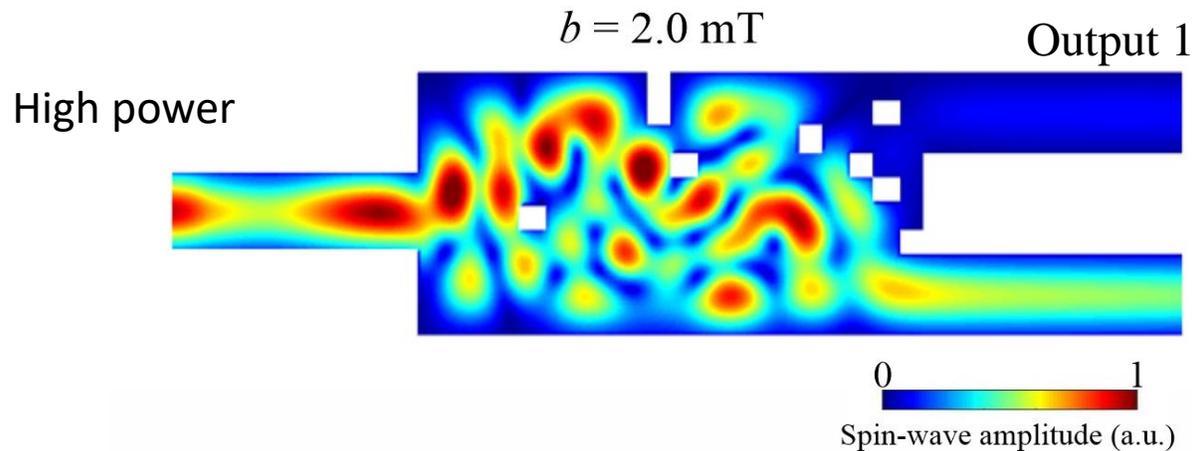
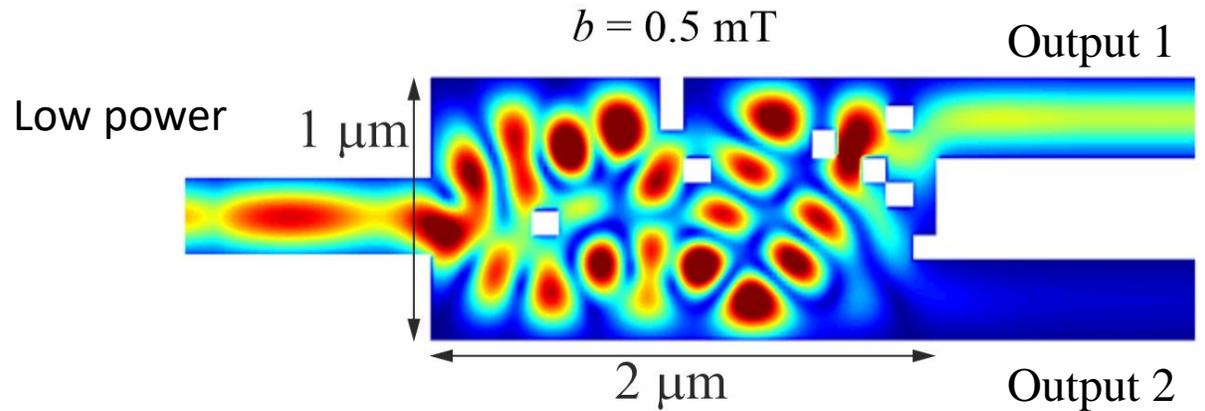
Time= 1 (ns),  $f_2=2.8\text{GHz}$



Q. Wang, A. Chumak, P. Pirro, *Nature Commun.*, **12**, 2636 (2021)

# Inverse design magnonics: nonlinear systems

Objective function:  $O = (I_{low,o_1} - I_{low,o_2})(I_{high,o_2} - I_{high,o_1})$

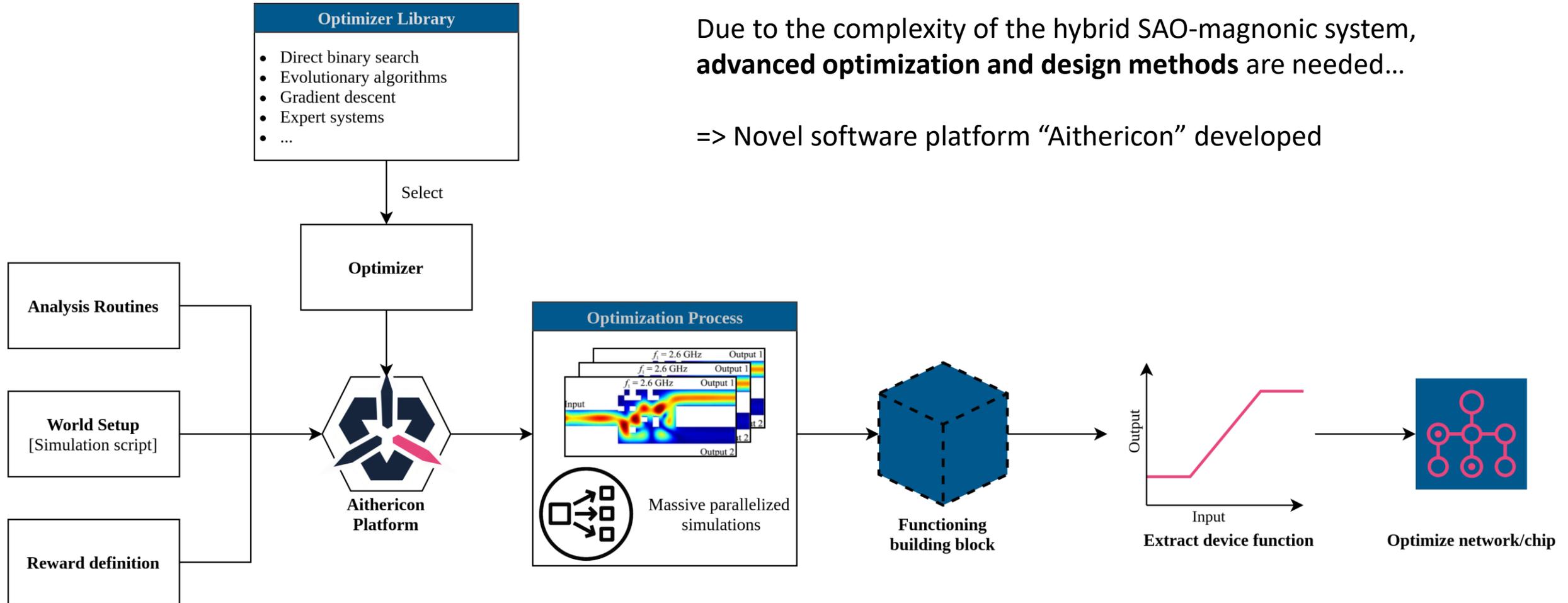


Inverse design magnonics can design linear and nonlinear magnonic devices (almost) completely automatized

# Inverse design: next steps

Due to the complexity of the hybrid SAO-magnonic system, **advanced optimization and design methods** are needed...

=> Novel software platform “Aithericon” developed

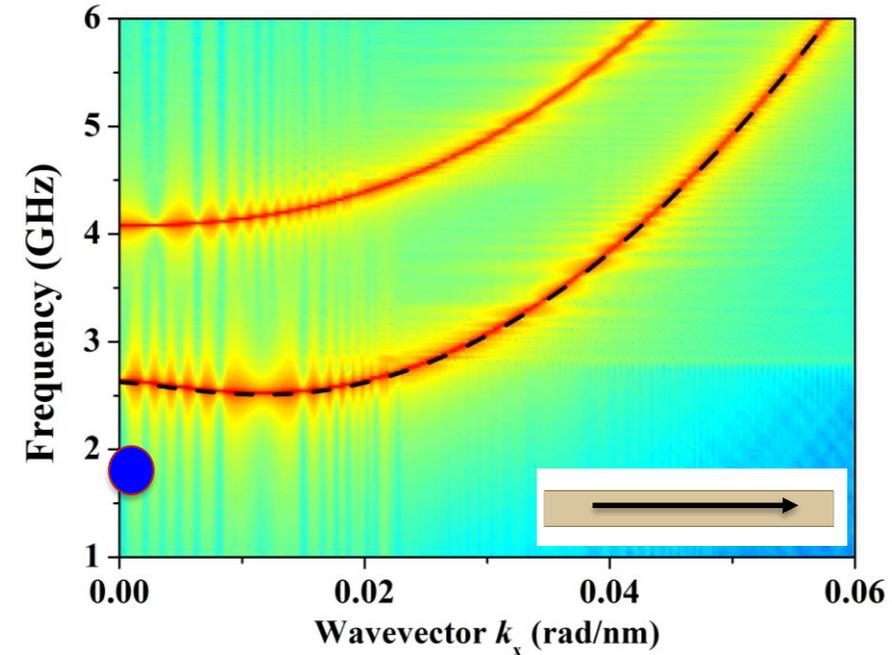


<https://aithericon.com>

# Matching the SAO and the magnonic system

- Frequency mismatch:** large precession amplitudes of SAO  
 → associated nonlinear frequency shift: SAO are not well matched in their frequency to the spin-wave system in the same structure.
- Materials, film thicknesses and geometries **cannot be optimized for both systems simultaneously**

→ **Create a hybrid system with tunable coupling**



YIG spin-wave waveguide (100nm width):  
 spin-wave dispersion relation and frequency of  
 an auto-oscillation (blue dot)  
 induced, e.g., by Spin Hall effects

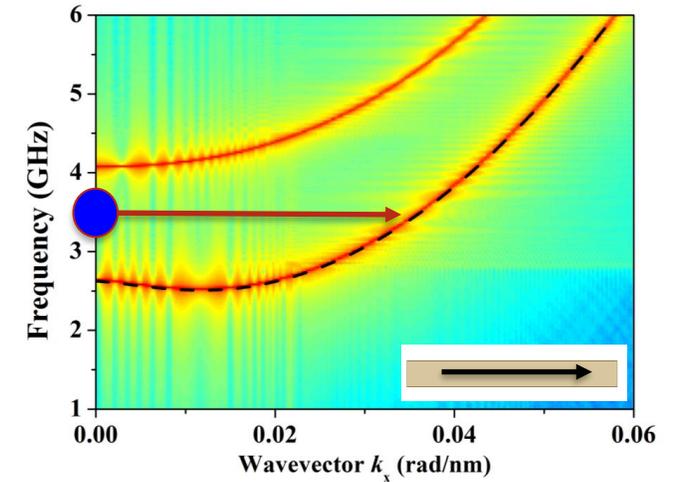
# Matching the SAO and the magnonic system

→ Create a hybrid system with tunable coupling

Example: NiFe-base auto-oscillator coupled to a YIG nanowaveguide

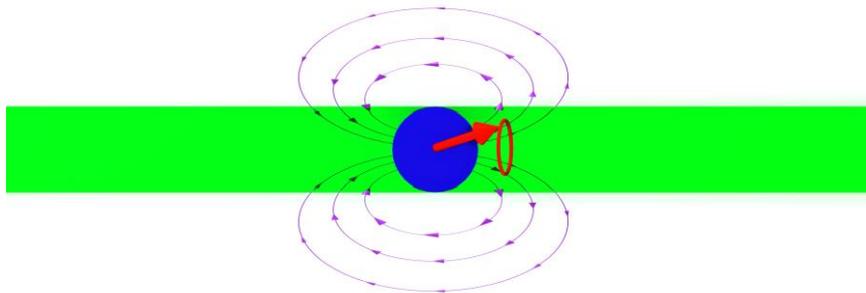
$$M_s = 800 \text{ kA/m}$$

$$M_s = 140 \text{ kA/m}$$



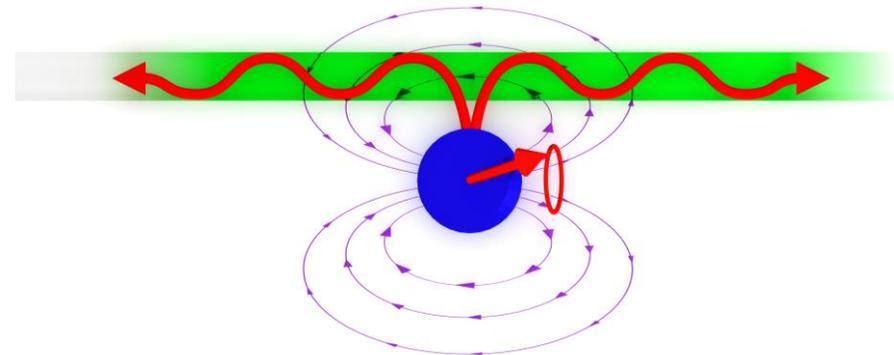
→ Very different  $M_s$  lead to very different ferromagnetic resonance frequencies allow for easier matching

“SAO on waveguide”



Strong coupling, low tunability

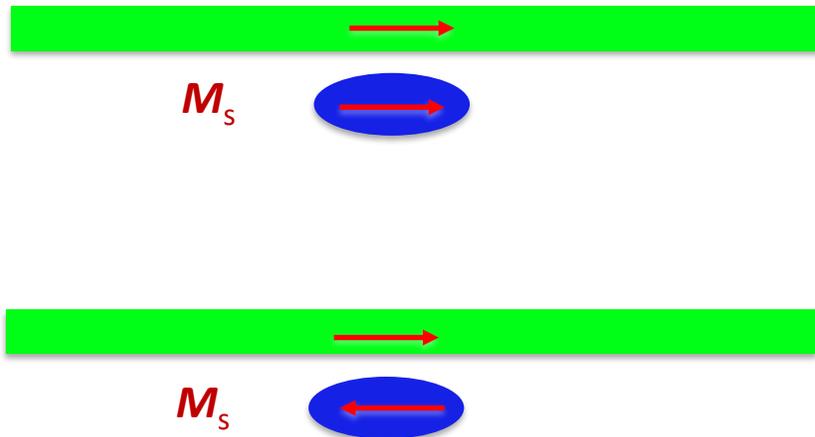
“SAO beside waveguide”



Weaker coupling, tunability by gap

# Tuning the coupling and SAO frequency

- **Dipolar coupling:** excitation strength of spin waves depends on the
  - Gap between SAO and waveguide,
  - SAO size and excited spin-wave wavelength
  - Relative orientation of the SAO and the spin-wave waveguide
- Spin-wave excitation is a radiation loss mechanism for the SAO: it **increases the threshold current** and **changes the auto-oscillation frequency**.



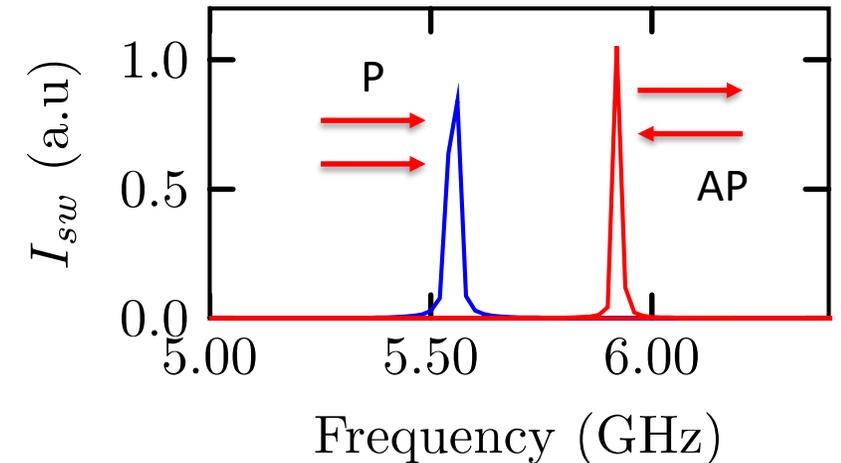
## Parallel $M_s$

- **weak dipolar coupling**
- low spin-wave emission amplitude
- high SAO amplitude
- high (negative) nonlinear shift

## Antiparallel $M_s$

- **strong dipolar coupling**
- high spin-wave emission amplitude
- low SAO amplitude
- small (negative) nonlinear shift

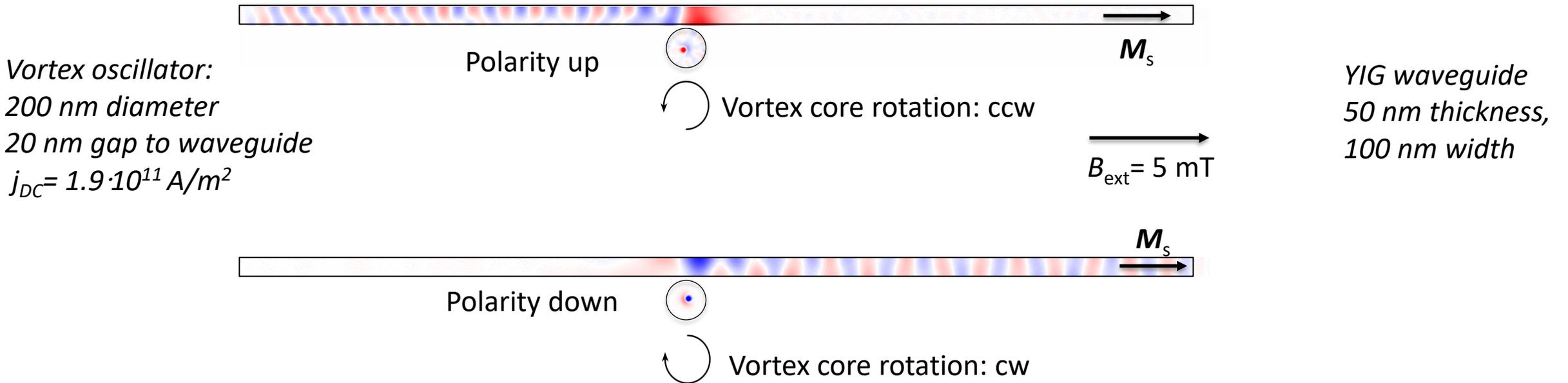
SWs emitted from a NiFe SHNO, into a 5 nm thick YIG waveguide



$$j_{DC} = 1.9 \cdot 10^{11} \text{ A/m}^2, B_{ext} = 10 \text{ mT}$$

# Tuning the spin-wave emission

- Uniform oscillators emit reciprocally, but **vortex oscillators** have a particular rich reconfigurability since the spin-wave emission depends on the **chirality** and the **polarity** of the oscillator.

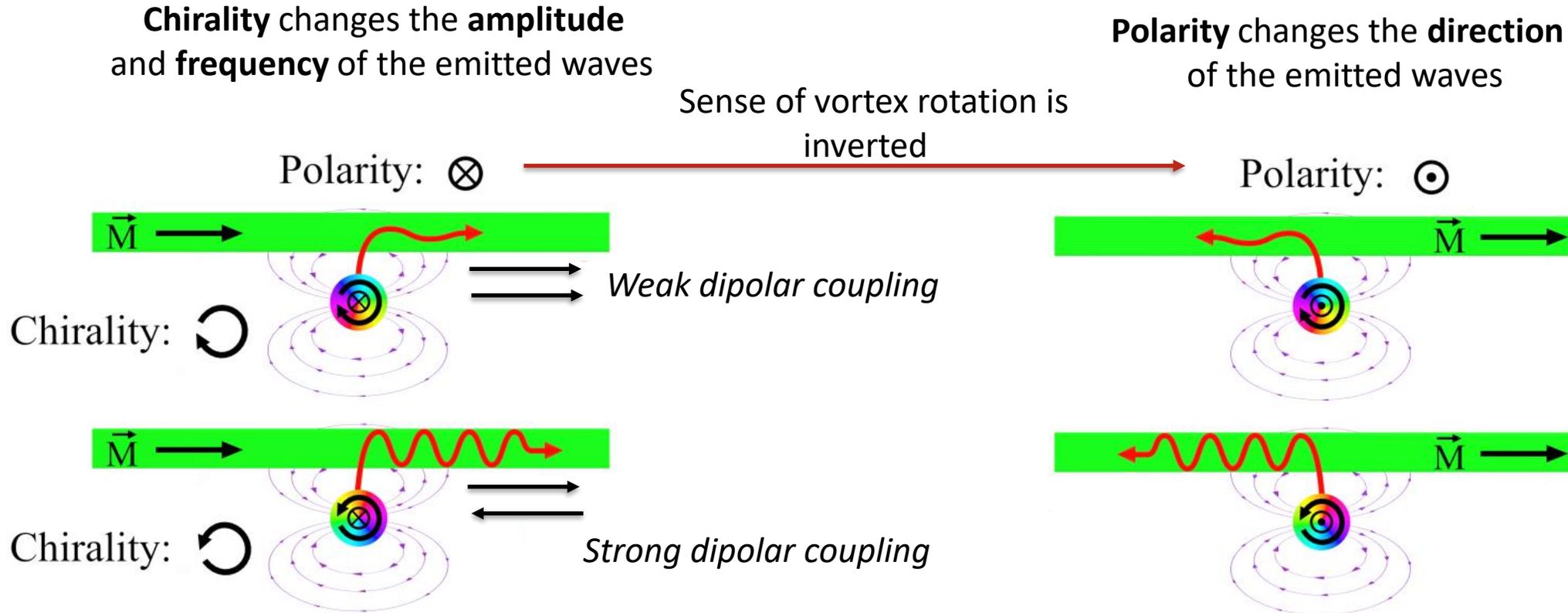


- Non-reciprocal emission** into a completely reciprocal magnonic system (Backward-Volume geometry) due to the **interplay of the different in-plane and out-of-plane components of the dynamic fields** created by the vortex

→ Enables directionality in a network, can be tuned by the ellipticity of the oscillator

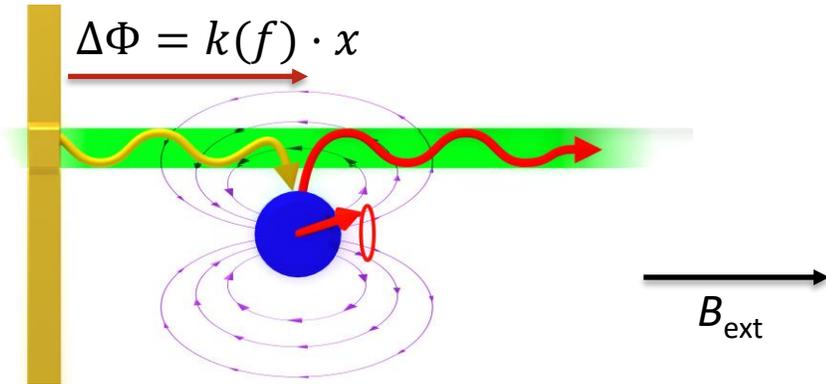
# Tuning the spin-wave emission

- Summary: Vortex oscillator coupled to a Backward Volume spin-wave waveguide



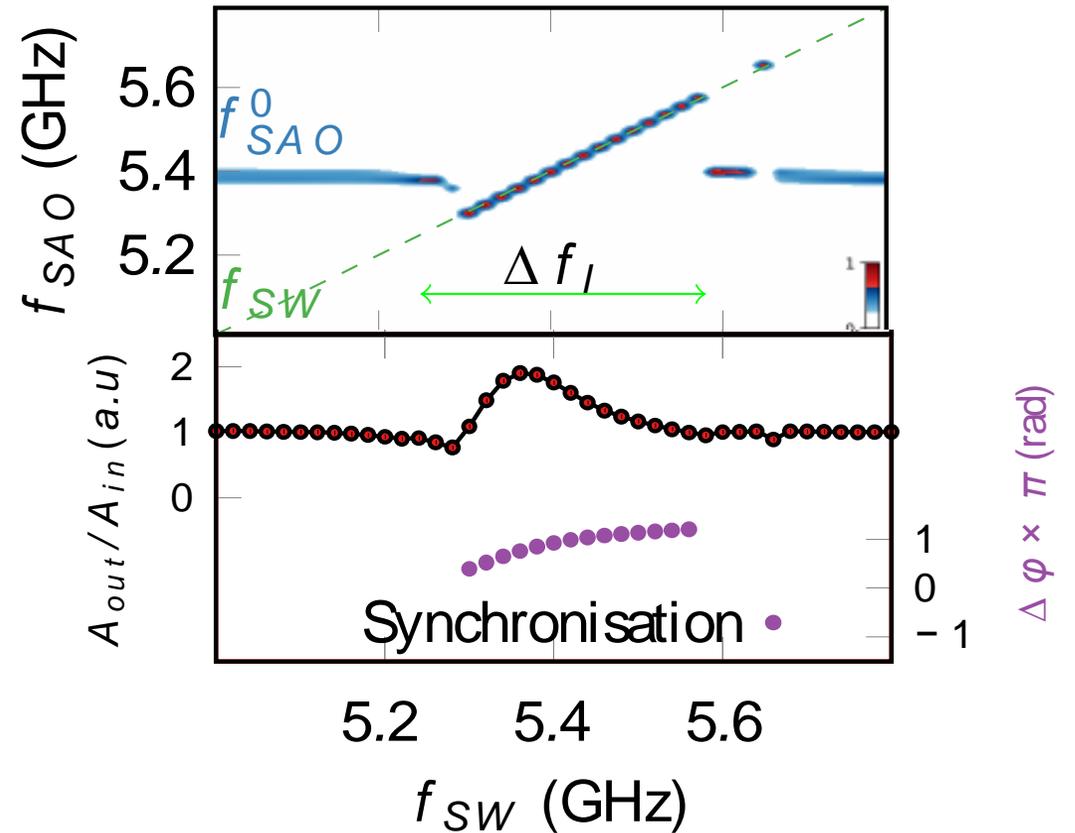
# Synchronization to a magnonic signal

- Inverse process to the emission of spin waves: SAO synchronizes to magnonic signal in the waveguide:



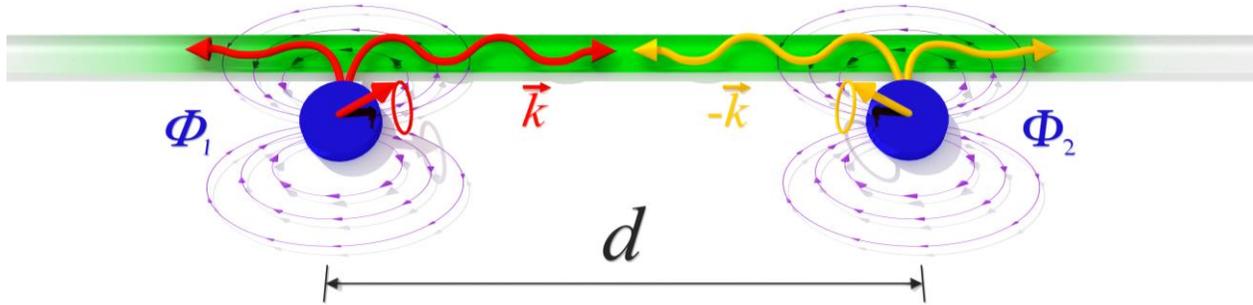
- SAO synchronizes to the magnonic input signal ✓
- Phase of the SAO depends on the spin-wave wavelength ✓
- Amplification depends on spin-wave frequency, can be enhanced by frequency selective elements

Elliptical NiFe SHNO (80x40x5 nm)  
coupled to a 10 nm thick, 100nm wide YIG waveguide



$j_{\text{DC}} = 1.9 \cdot 10^{11} \text{ A/m}^2$ ,  $B_{\text{ext}} = 50 \text{ mT}$ , distance  $x = 1280 \text{ nm}$

# Synchronization of SAO via spin waves



Two elliptical NiFe SHNO (80x40x5 nm), distance  $d=2 \mu\text{m}$  coupled to a 10 nm thick, 100 nm wide YIG waveguide,

**Most efficient synchronization:**

$$\beta = k(f) \cdot d = \arctan(\nu) + l \cdot \pi,$$

$$l \in 0, 1, 2 \dots$$

$\nu$ : normalized nonlinear frequency shift of the oscillators

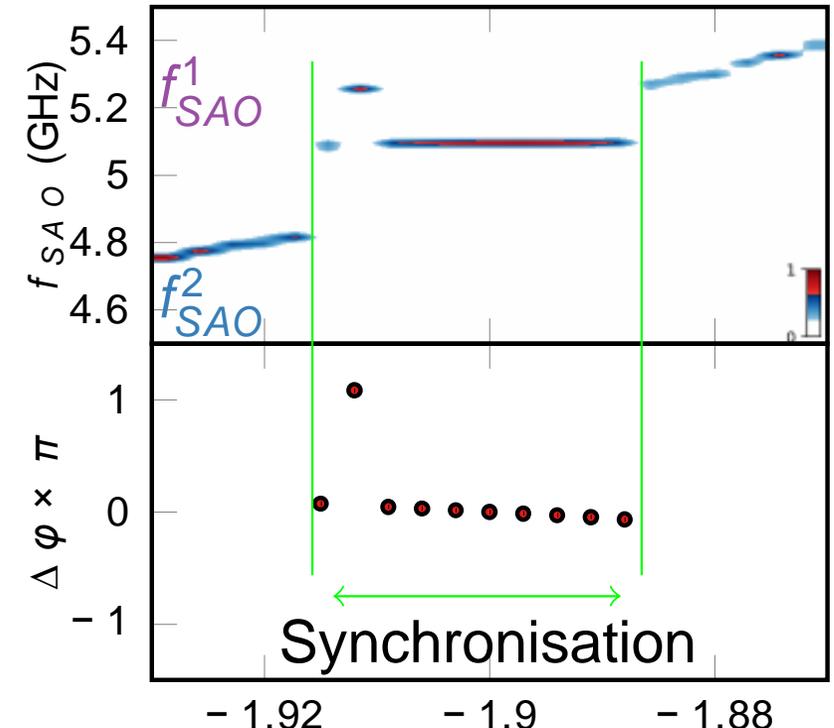
**Two possibilities for the phase difference between oscillators:**

$$\Delta\Phi = \arcsin(\delta\omega/\Delta_2) \text{ or } \Delta\Phi = \pi - \arcsin(\delta\omega/\Delta_2)$$

$\delta\omega$ : frequency mismatch to the free running oscillator

$\Delta_2$ : synchronization bandwidth

Stable solution depends on  $\beta$  and  $\nu$



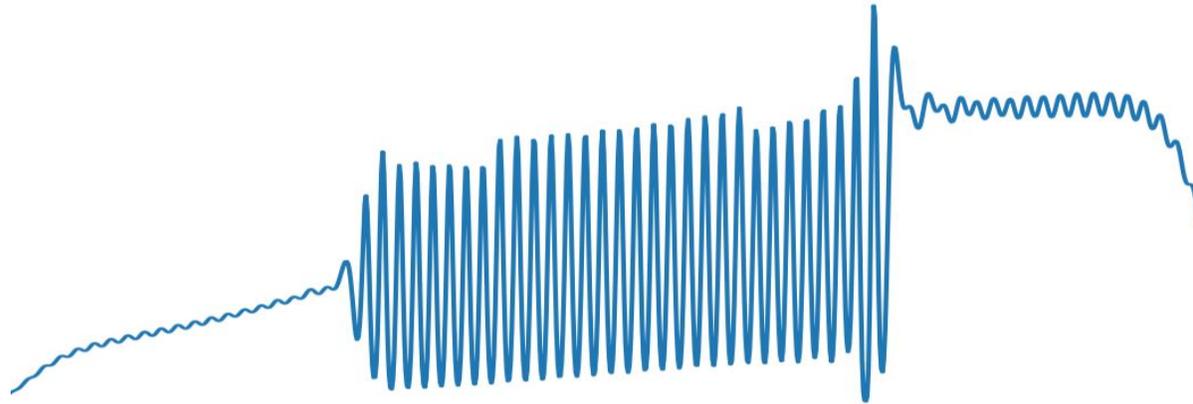
Current density ( $\times 10^{11}$ ) in  $\text{A}/\text{m}^2$  in SAO 2

Synchronization for larger distances  $d$  achievable without further optimization.

A. Slavin and V. Tiberkevich, *IEEE Trans. on Magn.*, **45**, 1875–1918 (2009).

# Synchronization patterns

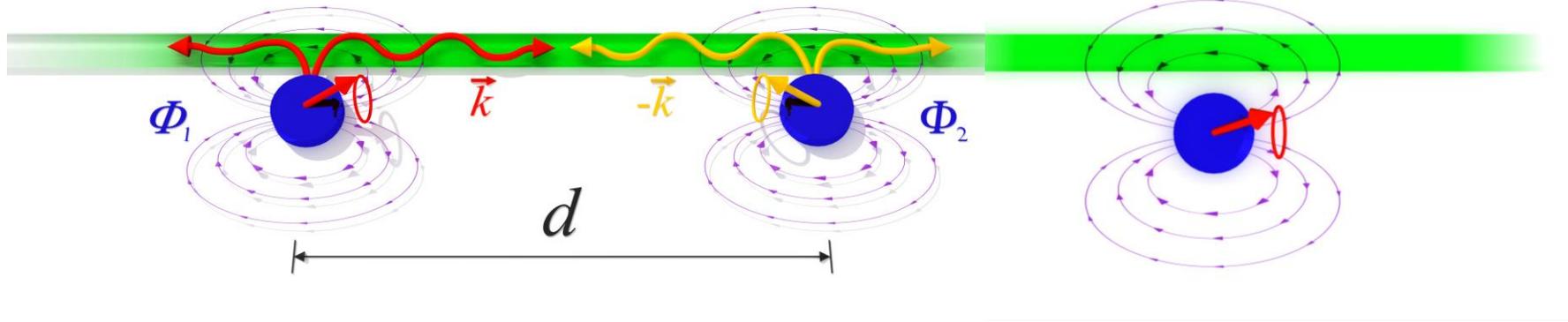
- If synchronization is reached, the resulting interference pattern depends on the realized wavelength, the relative phase- and spatial difference of the oscillators:



## Spin-wave intensity (time averaged)

In this case (uniform SHNO), the non-synchronized system is completely reciprocal (emission of spin waves etc).

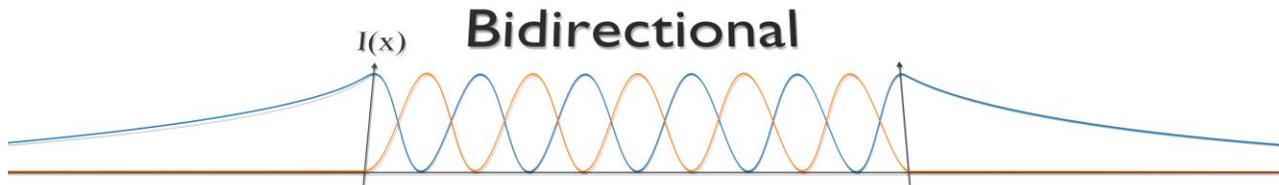
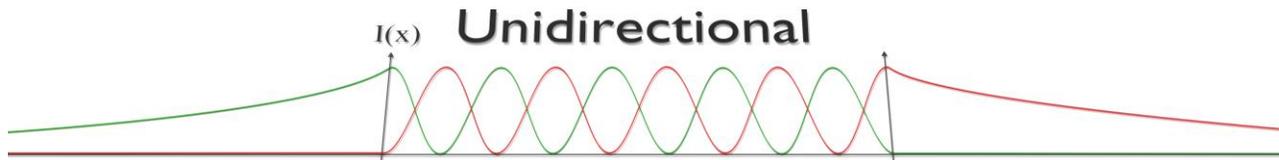
Where does the non-reciprocity come from?



# Synchronization patterns

- If synchronization is reached, the resulting interference pattern depends on the realized wavelength, the relative phase- and spatial difference of the oscillators:

Spin-wave intensity (time averaged)

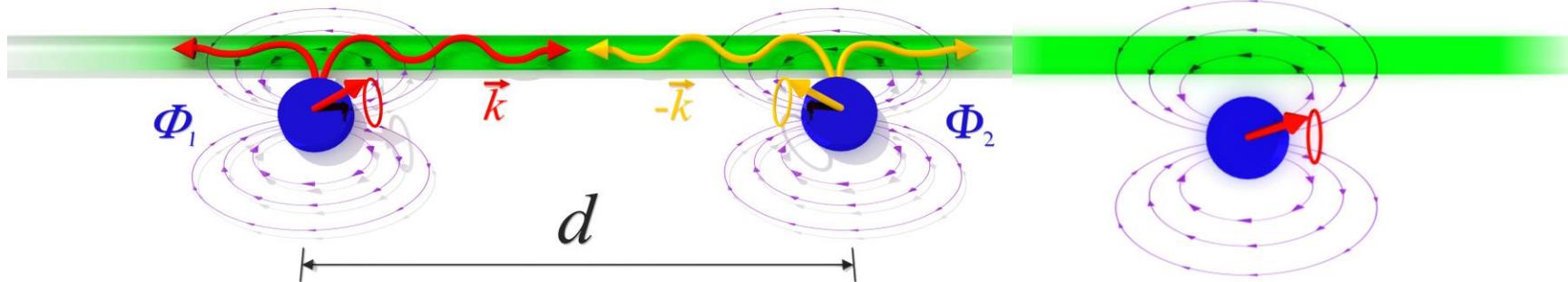


$$d = \lambda(f_{Osci}) \cdot \left( n + \frac{1}{4} \right)$$

$$\Delta\Phi = \Phi_1 - \Phi_2 = \pm\pi/2$$

$$d = \lambda(f_{Osci}) \cdot \left( n + \frac{1}{2} \right)$$

$$\Delta\Phi = \Phi_1 - \Phi_2 = \pi, 0$$

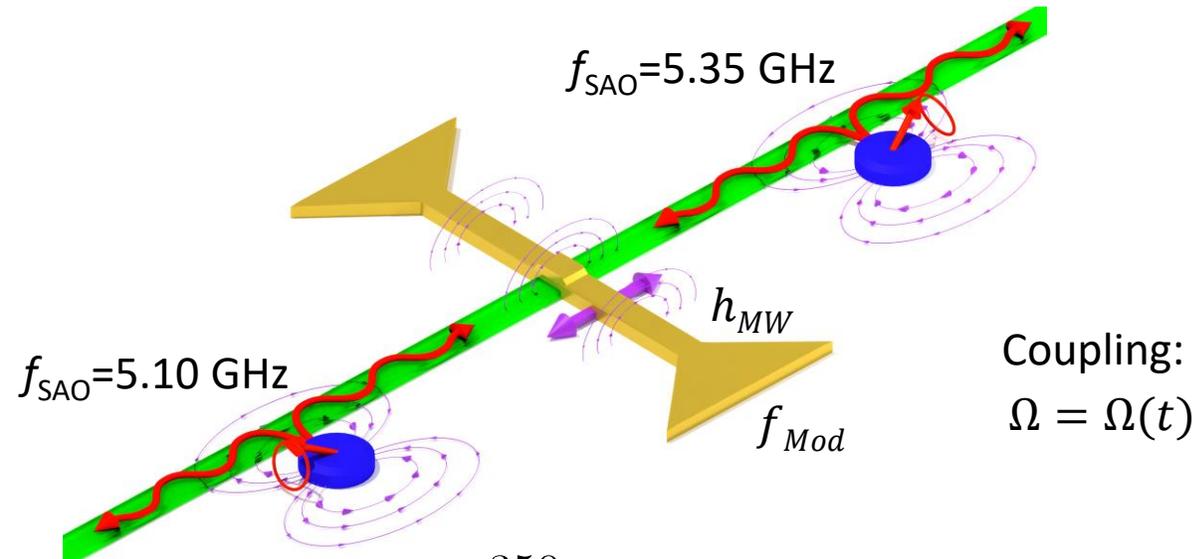
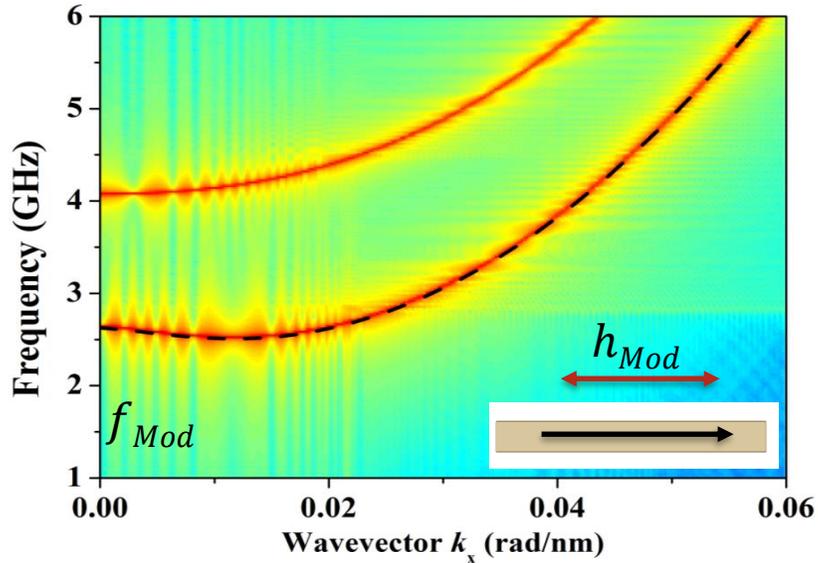


Transition to the **synchronized state**:

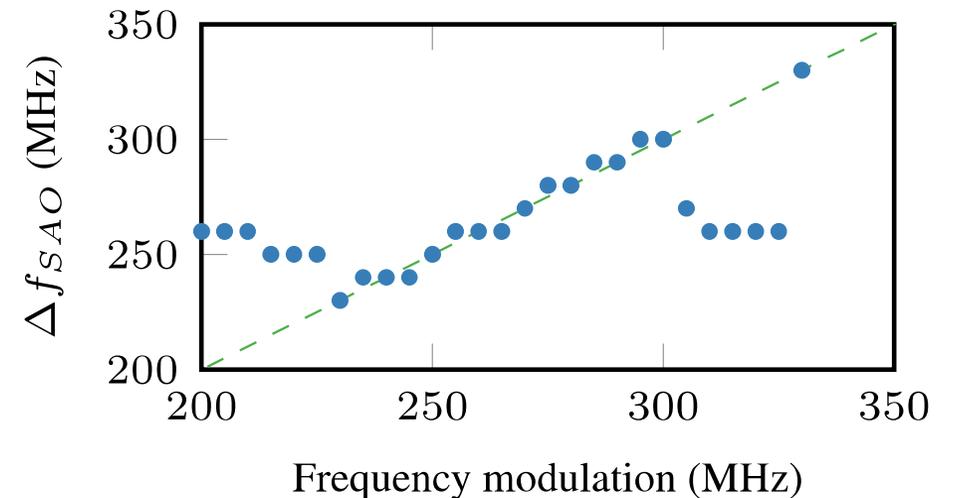
**phase transition** with **ordering parameter  $\Delta\Phi$**  which **decides on the intensity pattern** outside the oscillator pair  
 → defines the direction in which an initial **synchronization spreads through the network**

# Time-modulation of the spin-wave coupling

What happens if we time-modulate the connecting spin-wave band structure with a frequency below the magnon gap?

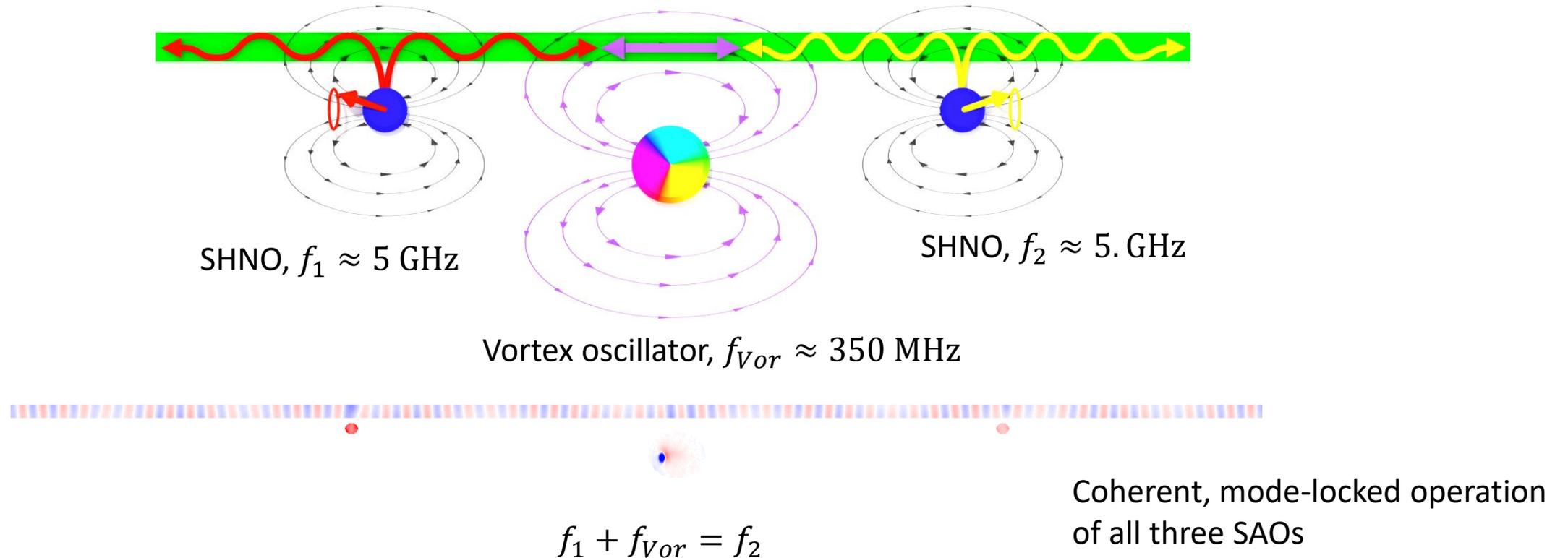


- Modulation of the spin waves leads to **coherent mode-locking** of SAOs running at different  $f_{SAO}$
- Spin waves pulses** develop whose duration decreases if more SAOs are locked with different  $f_{SAO}$



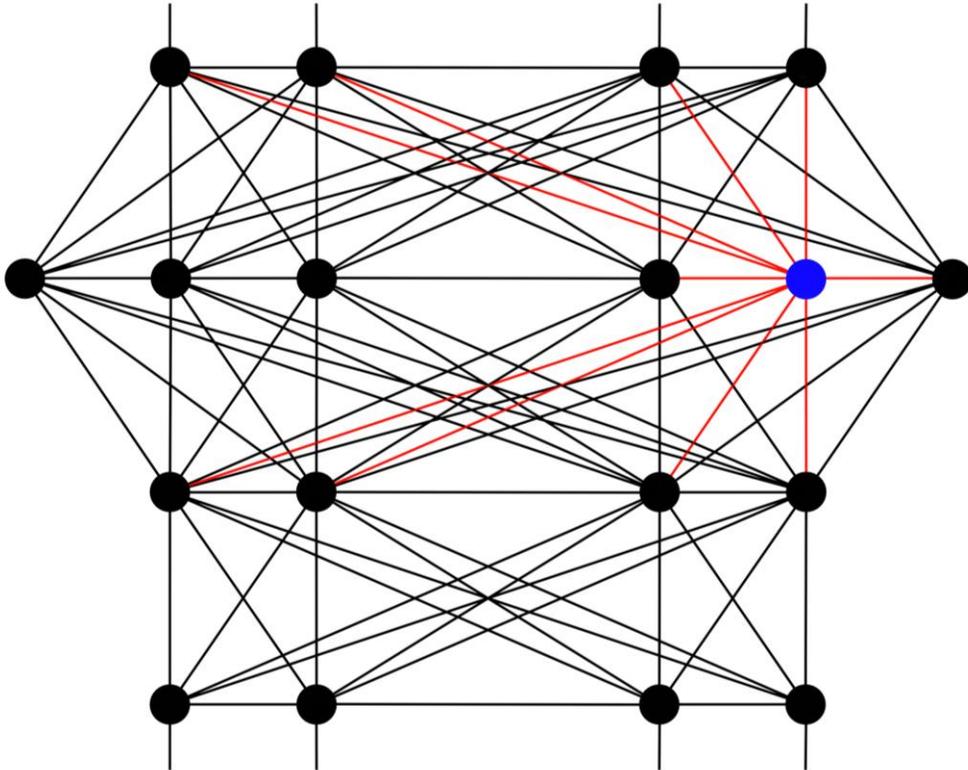
# Time-modulation of the spin-wave band structure

Modulation of the spin-wave band structure can **couple very different oscillator types**:



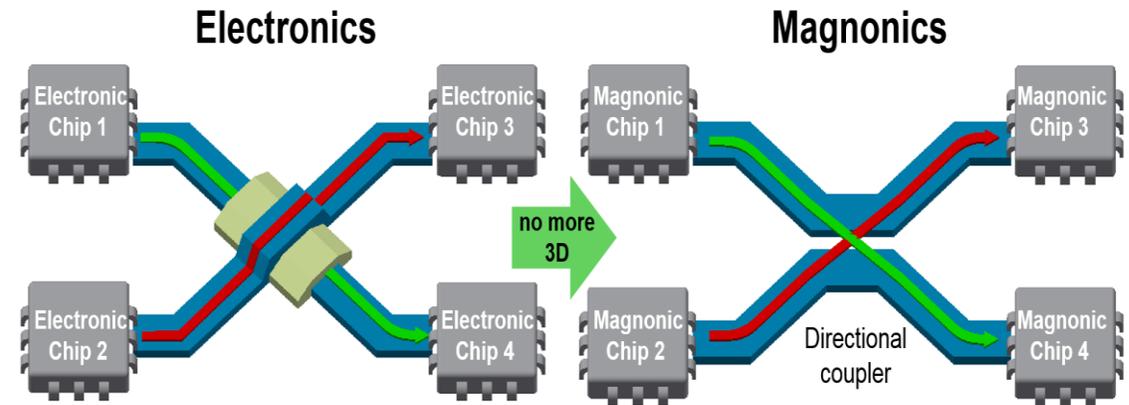
→ There are plenty of coherent phenomena for coupled SAO which go beyond simple synchronization.

# Last but not least: connectivity challenge



## Connection by waves

Use of **coherent coupling effects** allows to use 2D systems

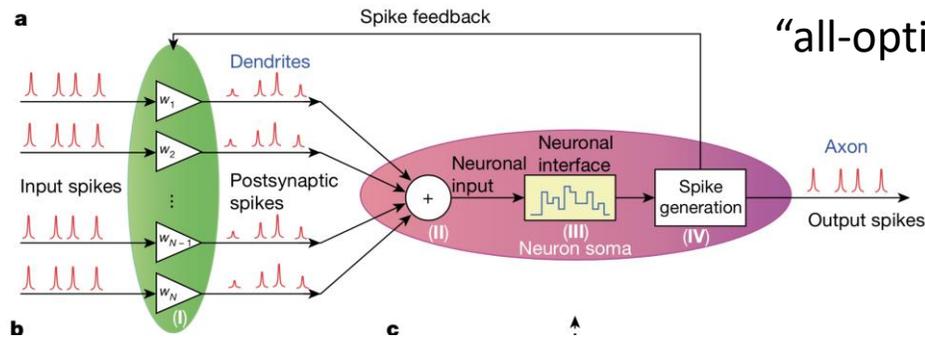


Additional reduction of physical interconnects by **frequency multiplexing**

## All-optical spiking neurosynaptic networks with self-learning capabilities

J. Feldmann<sup>1</sup>, N. Youngblood<sup>2</sup>, C. D. Wright<sup>3</sup>, H. Bhaskaran<sup>2</sup> & W. H. P. Pernice<sup>1\*</sup>

J. Feldmann, *et al.*,  
*Nature* **569**, 208–214 (2019).

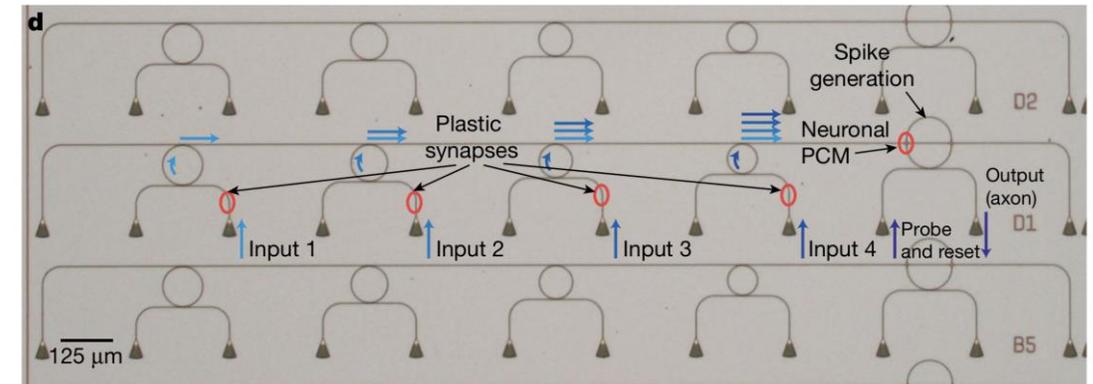


"all-optical neuron"

**Perform in the optical domain:**  
pattern recognition,  
supervised and unsupervised learning

### Main ingredients:

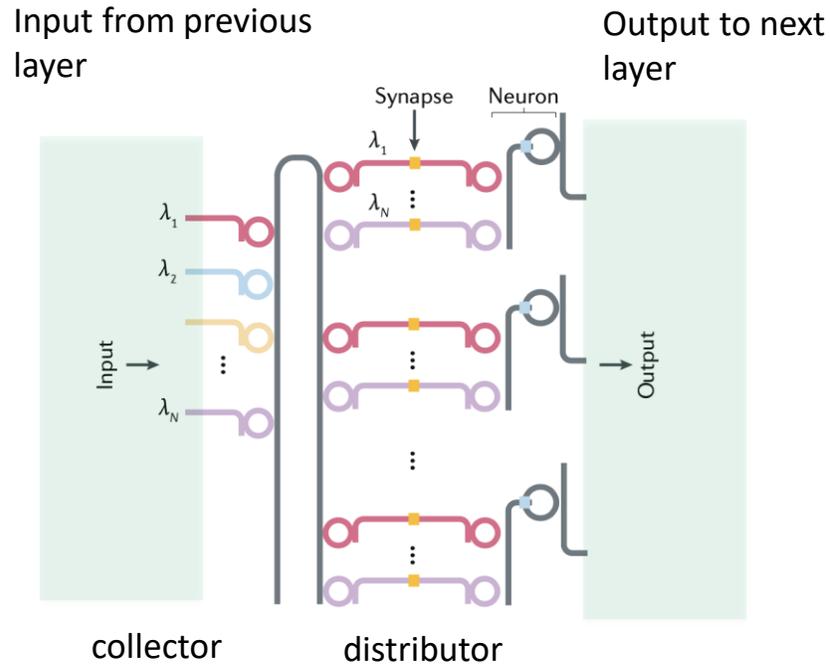
- Photonic ring resonators
- Nonlinear functionality (phase change material)
- **Multiplexing und Demultiplexing**
- Embedded memory (phase change material)



Main problem in optics:  
scalability of the individual elements

# Frequency-division multiplexing

## Photonic neural network using $N$ different frequencies/wavelengths



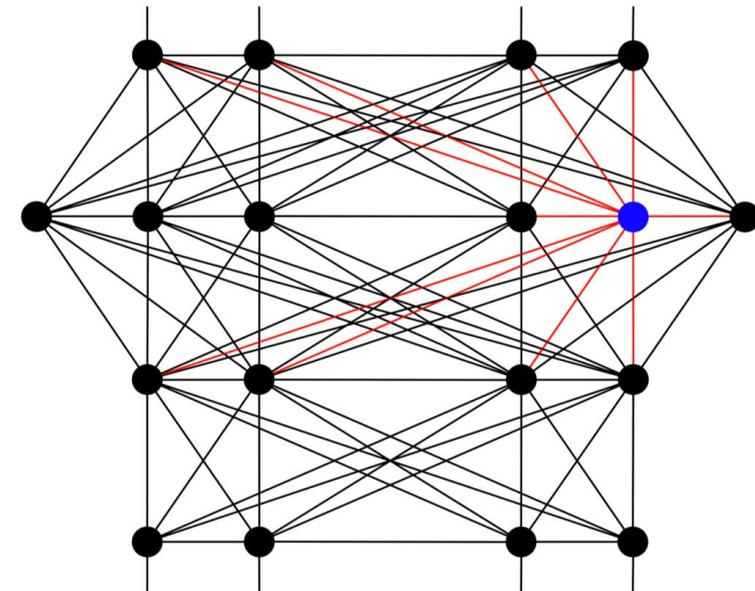
The use of frequency-dependent elements creates an *all-to-all connection* of neurons in a 2D structure using a *linear scaling* number of connecting elements.

J. Feldmann, *et al.*, *Nature* **569**, 208–214 (2019).

D. Marković, *et al.*, *Nat. Rev. Phys.* **2**, 499–510, (2020).

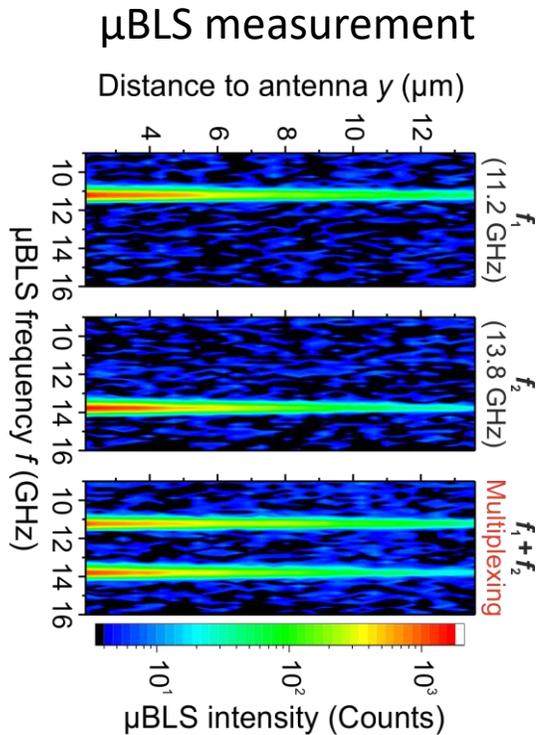
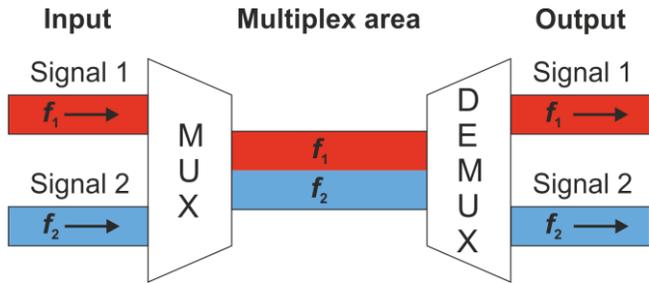
## Wiring scheme

needs  $\frac{N(N-1)}{2}$  physical connections to create *all-to-all connectivity*

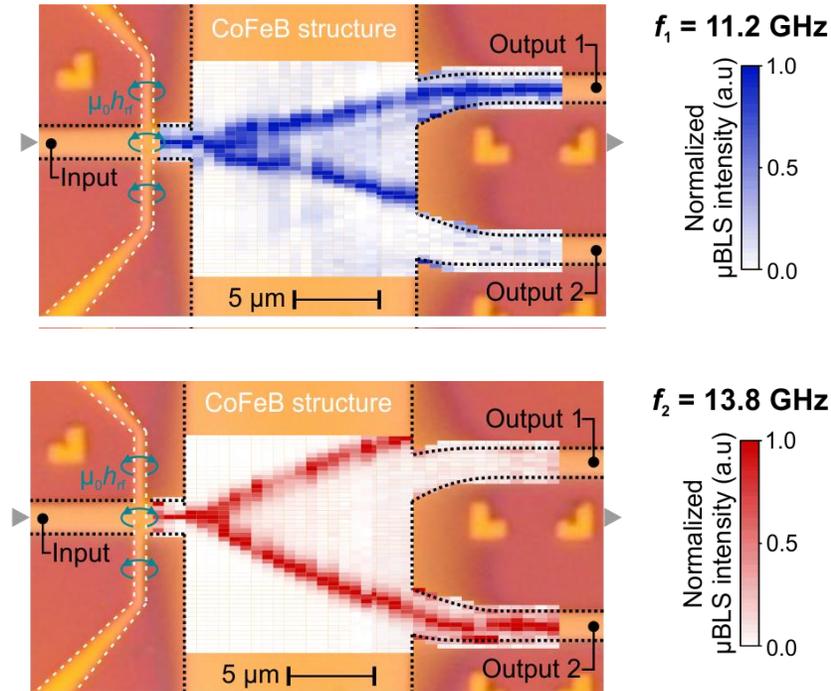


# Frequency-division multiplexing (FDM) for spin-waves

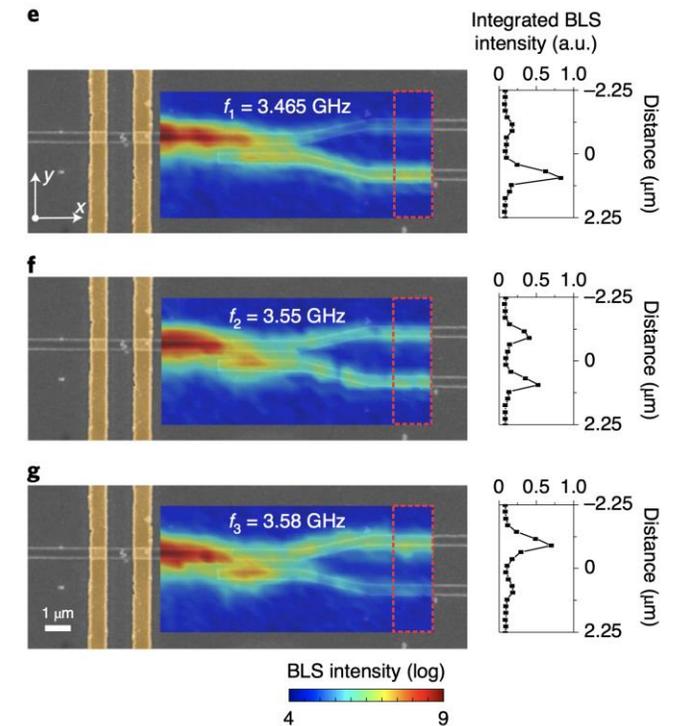
“Several spin-wave frequencies in the same device”



## Caustic-based demultiplexer



## Coupler-based demultiplexer

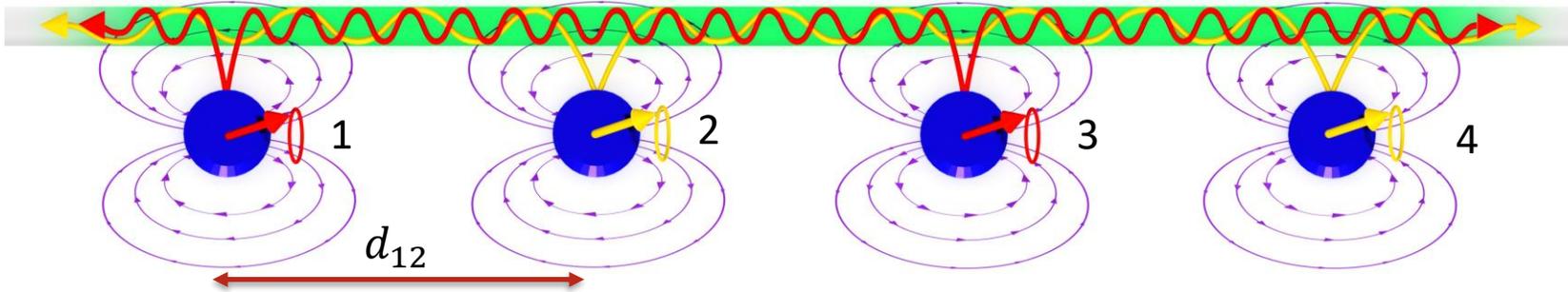


F. Heussner, PP, et al., *Phys. Status Solidi RRL*, **7**, 1800409 (2018).  
F. Heussner, PP, et al., *Phys. Status Solidi RRL*, **14**, 1900695 (2020).

Q. Wang, PP, et al., *Nature Electronics* **3**, 765–774, (2020).

# Synchronization of SAO via frequency multiplexing

Four individual SAOs coupled to the same waveguide:



**How will they synchronize?**

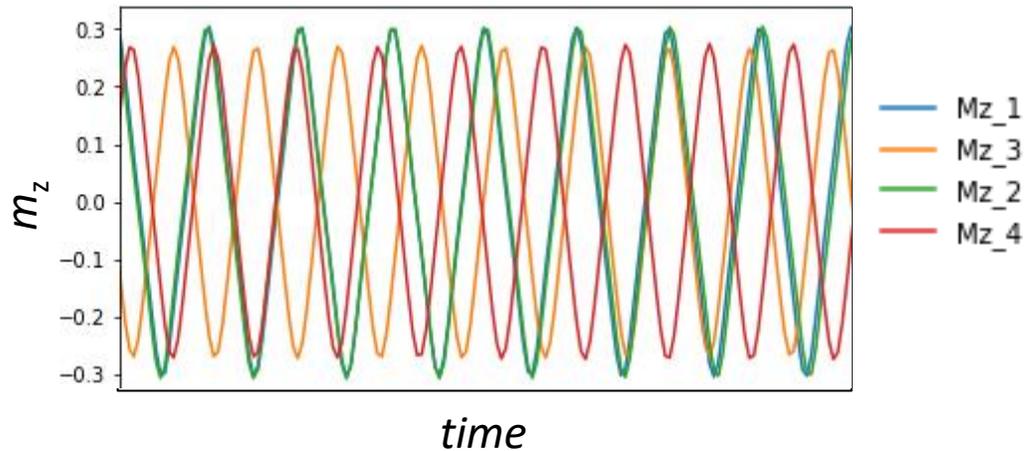
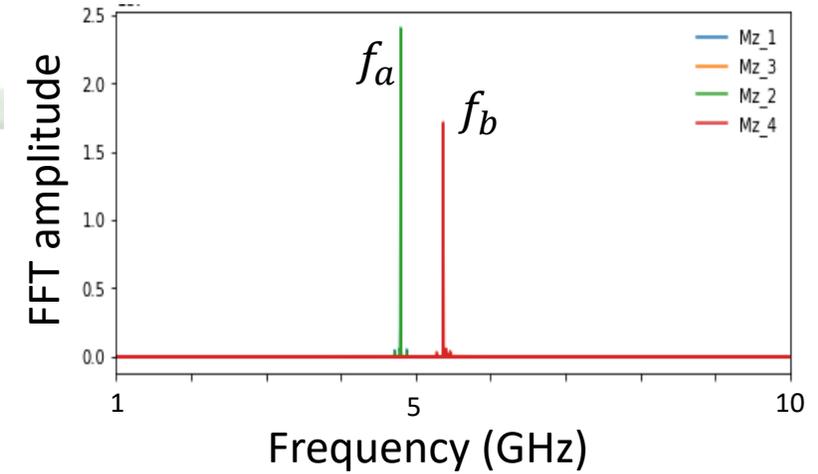
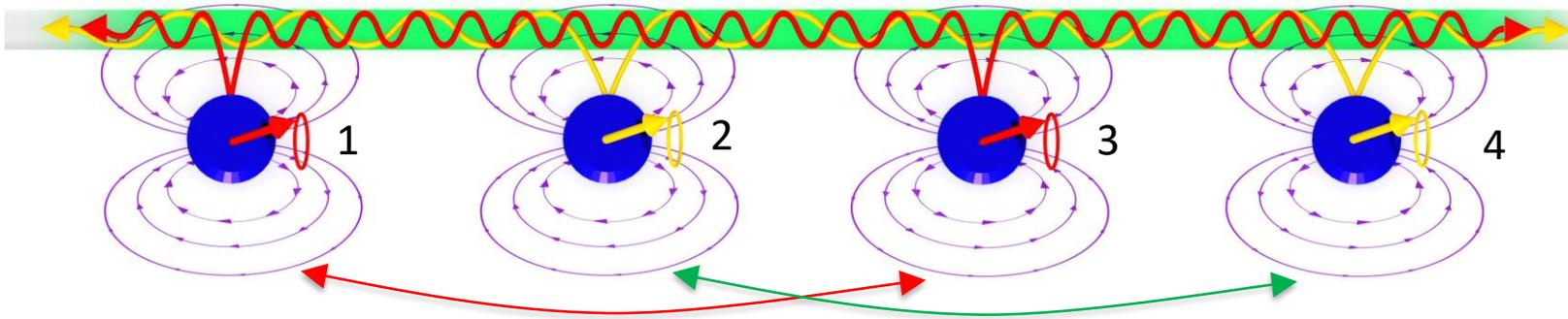
Most efficient synchronization:

$$k(f) \cdot d_{mn} = \arctan(\nu) + l \cdot \pi, l \in 0, 1, 2 \dots$$

This condition might be fulfilled for a distant oscillator, whereas it is not fulfilled for the next neighbor....

# Synchronization of SAO via frequency multiplexing

Four different SAOs coupled to the same waveguide:



SAO 1 and SAO 3 synchronize in phase with  $f_a$ ,  
SAO 2 and SAO 4 synchronize out-of-phase with  $f_b$

Four different SAO coupled by a single magnetic nanowire forming two synchronization clusters.

Additional effect: **nonlinear magnon interaction** seems to mode-lock the clusters  
→ Spin-wave pulses develop, network starts to spike with shorter pulses if more clusters are involved

# Many thanks to...

*Development of the hybrid magnon-spintronic network:*

**Abbass Hamadeh** (Georg Forster stipend of the Humboldt foundation) , Milan Enders, David Breitbach, Morteza Mohseni

*Development the nano-waveguides:*

Björn Heinz, Michael Schneider, Martin Kewenig, Qi Wang, Morteza Mohseni, Thomas Brächer,...,  
Carsten Dubs (Innovent e.v., Jena), Andrii Chumak (University of Vienna)

*Development of magnonic elements and the inverse design magnonics:*

**Qi Wang**, Andrii Chumak (University of Vienna)

*General support:*

Burkard Hillebrands



DFG

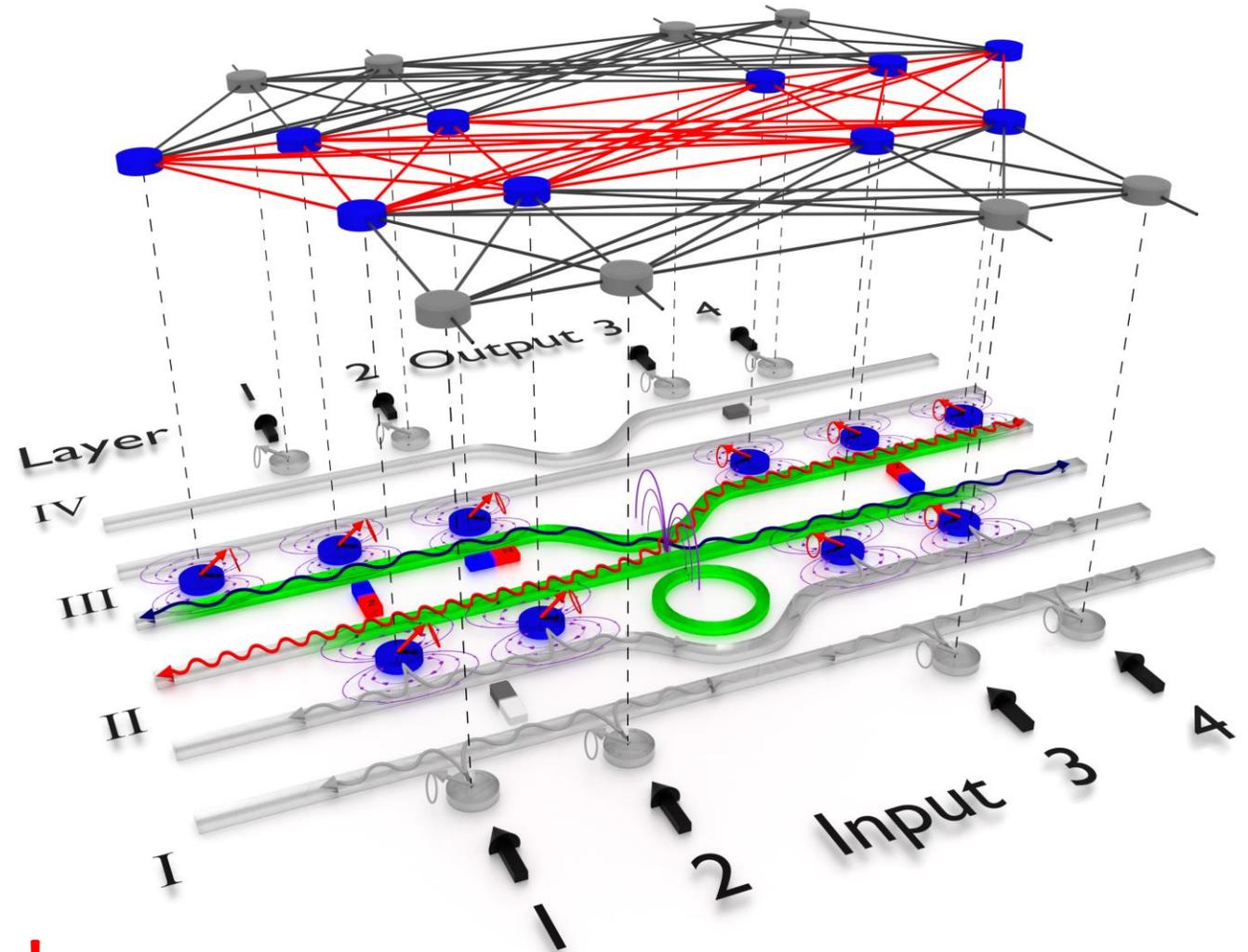


**SPIN+X**  
SFB/TRR 173  
Kaiserslautern • Mainz



# Conclusions

- Proposition of an **all-spintronic neural network** based on **spintronic auto-oscillators** as artificial neurons connect by **spin-waves in nano-waveguides** acting as artificial synapses
- **Oscillators** can be efficiently coupled to ultralow damping magnonic structures and **synchronize over large distances**
- Manipulation of the connecting spin waves allows to **modify the synchronization properties**, create phase-locked states...
- **Frequency-multiplexing** in the spin-wave domain allows to reduce the number of physical interconnects in a scalable and efficient way



**Thank you for your attention!**