

# Emergent states of interacting electrons on triangular lattices

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## Spin liquid

- 1. Quantum spin liquid** -  $\kappa$ -(ET)<sub>2</sub>Cu<sub>2</sub>(CN)<sub>3</sub>
    - present status of experiments
  - 2. Doped quantum spin liquid** -  $\kappa$ -(ET)<sub>4</sub>Hg<sub>2.89</sub>Hg<sub>8</sub> -
    - non-FL to FL crossover
    - quantum critical phase
    - BEC-BCS crossover
    - reduced superfluid density
    - preformed pairs & pairing symmetry
- PR X 12\_011016 (2022)  
arXiv:2201.10714  
arXiv:2202.06032  
arXiv:2205.03682

## Charge glass

- 3. Quantum charge glass** -  $\theta$ -(ET)<sub>2</sub>X -
    - classical manifestations (slow dynamics, aging, short-range order)
    - anomalously high crystallization speed
    - classical to quantum crossover
- arXiv:2201.04855  
arXiv:2205.10795

Today's talk is based on collaboration with

K. Miyagawa, Kagawa, Shimizu, Kurosaki, Furukawa, H. Oike, M. Urai, Y. Suzuki,  
K. Wakamatsu, Y. Ueno, T. Fujii, J. Ibuka, T. Sato, H. Murase (U Tokyo)

G, Saito, M. Maesato (Kyoto U.)

T. Sasaki, S. Iguchi, M. Saito (Tohoku U., IMR)

R. Kato (RIKEN)

H. Taniguchi, M. Ito (Saitama U.)

S. Yamashita, Y. Nakazawa (Osaka)

F. Pratt (Rutherford-Appleton)

Y. Kohama, A. Miyake, T. Nomura (ISSP)

B. Mikche, M. Dressel (Stuttgart U.)

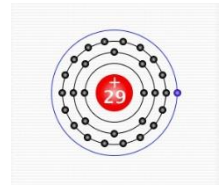
H. Mori (ISSP)

M. Tamura (Tokyo Sci. Univ.)

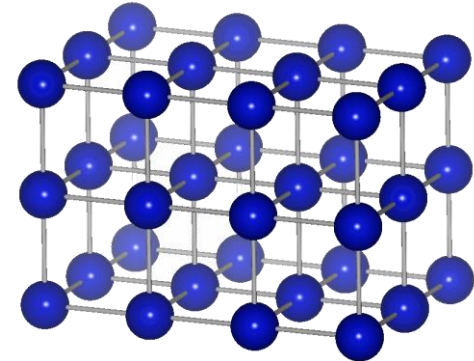
# Organic materials → flexible & controllable lattice geometry

Inorganic materials

atom

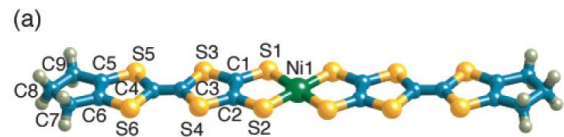


lattice



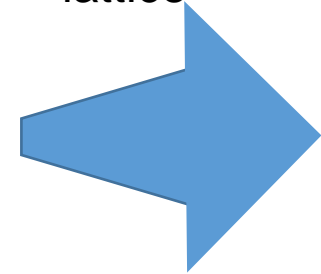
Orbital degeneracy  
Spin-orbit coupling  
Hunt coupling  
.....

Organic materials

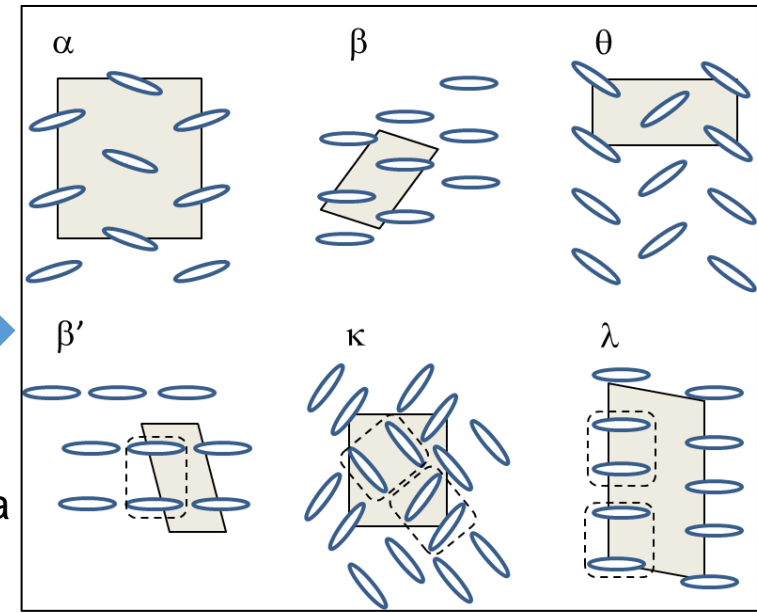


Frontier orbital  
(K. Fukui)

lattice



Kino-Fukuyama



# Organic materials → Physics of interaction and geometry

Various in-plane structures



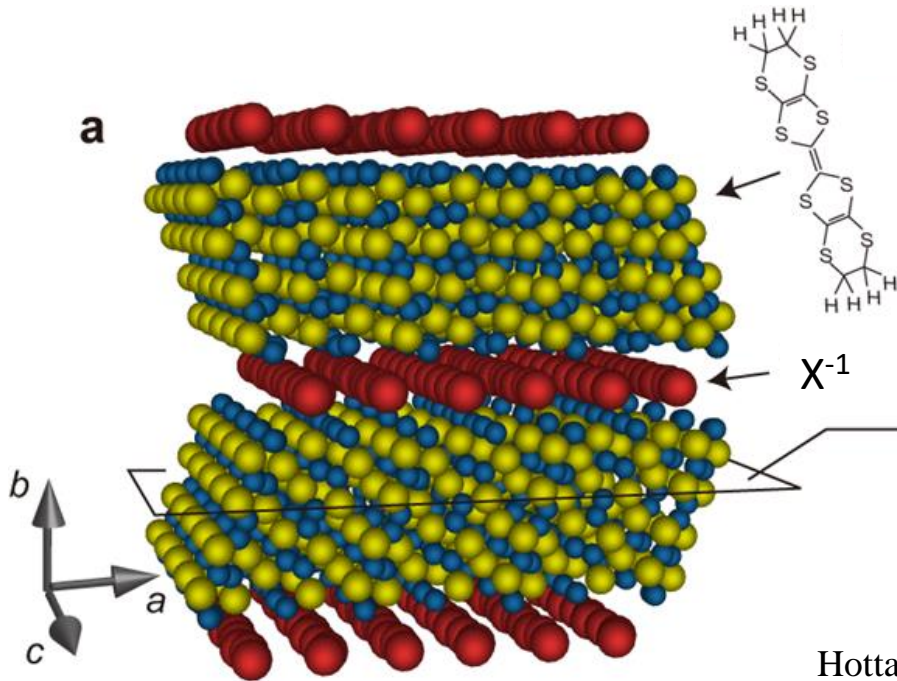
Diverse correlation phenomena



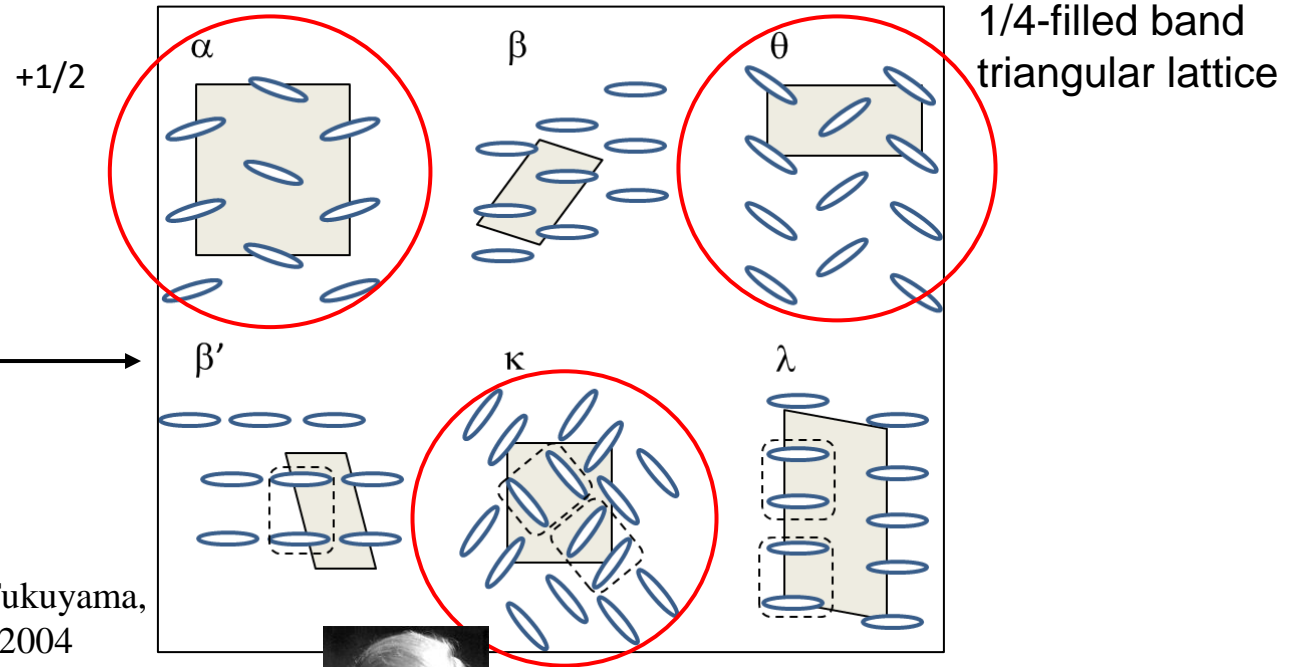
Massless Dirac ele.



Wigner Xtal/glass



Hotta, Seo, Fukuyama, Chem. Rev., 2004



Mott physics

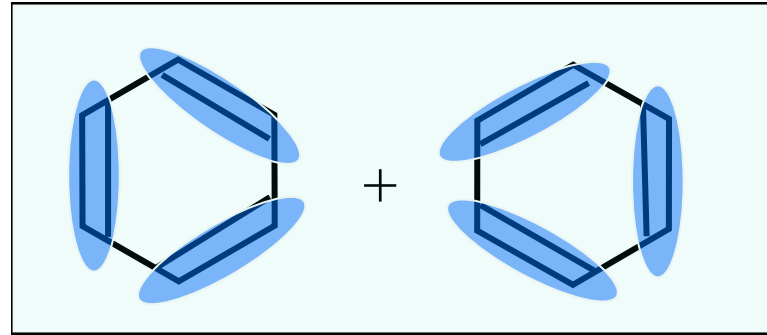
1/2-filled band triangular lattice

# Resonating valence bond (RVB) state as a QSL

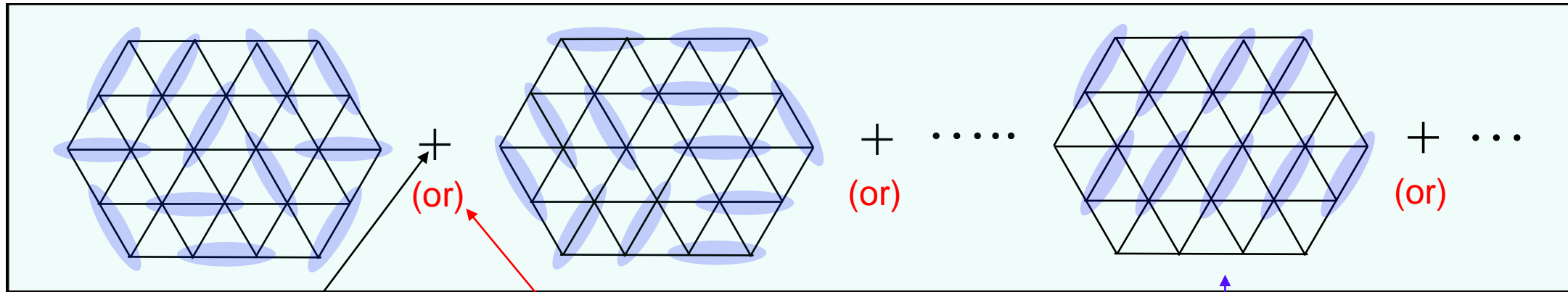


P. W. Anderson

benzene



Triangular  
lattice



RVB

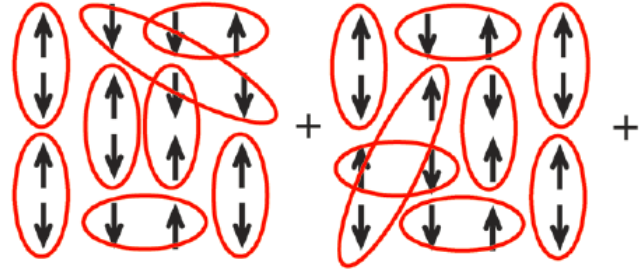
VBG  
(Valence bond glass)

VBC (or VBS)  
(valence bond crystal (or solid))

# Possible variation of QSLs

(according to Ogata)

( $P_G$ : projection operator to remove double occupancies)

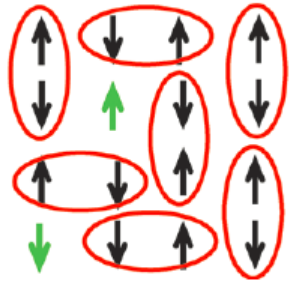


$$|RVB\rangle = P_G |BCS\rangle$$

gapped

$$|\text{spinon FS}\rangle = P_G |BCS; \Delta \rightarrow 0\rangle$$

gapless



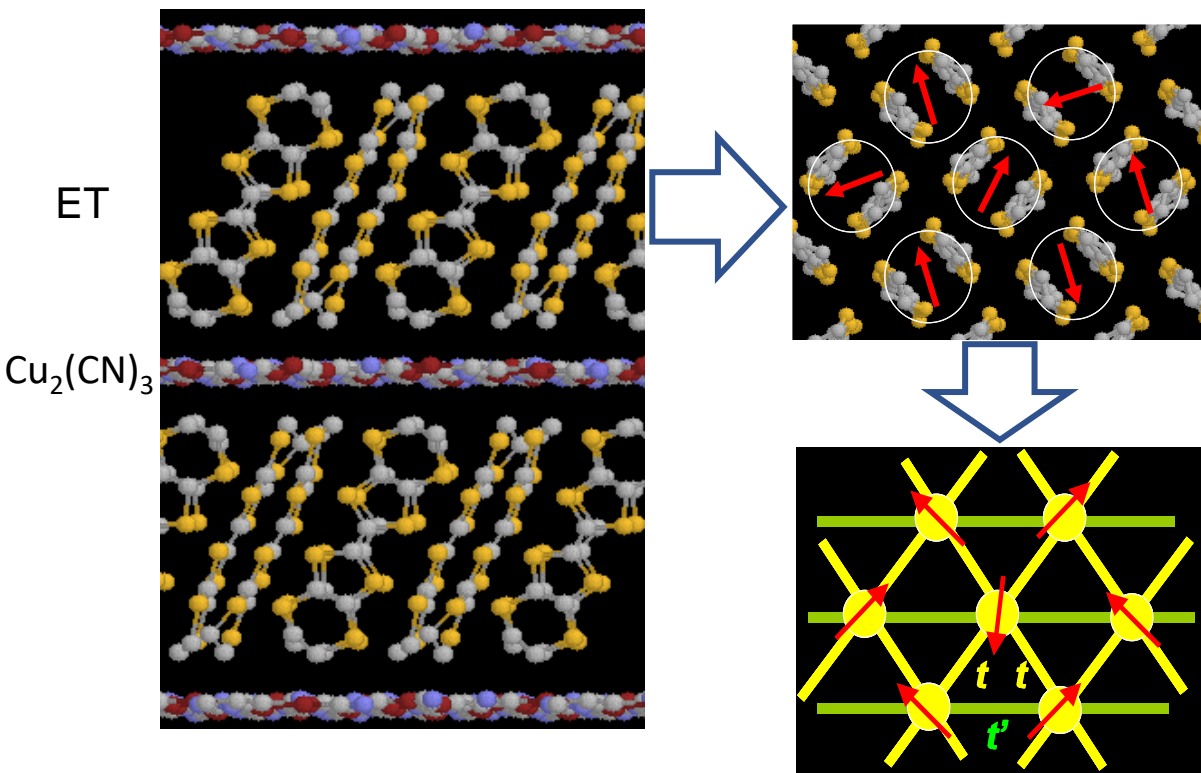
$$|\text{spinon Dirac cone}\rangle = P_G |nodal BCS\rangle$$

gapless  
(Dirac point)

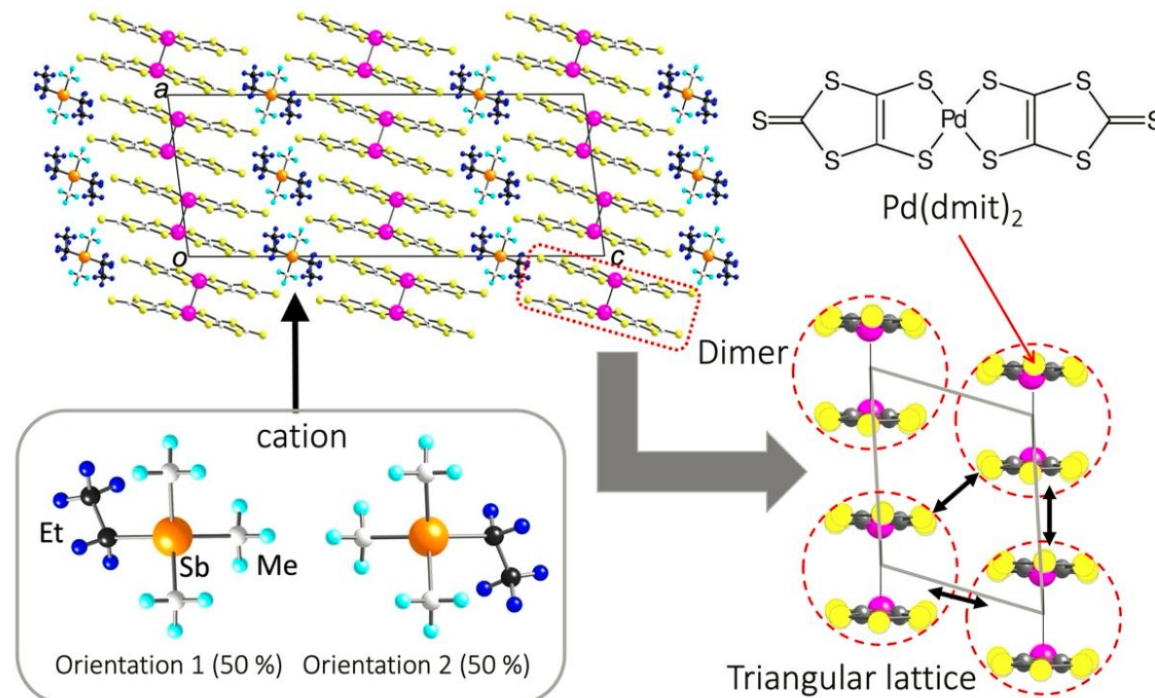
$$|\text{Chiral spin liquid}\rangle = P_G |chiral SC\rangle \quad (?)$$

gapped

# Quantum spin liquid (QSL) candidates with a triangular lattice

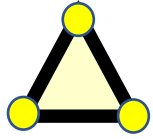


Kato, RIKEN



# QSL manifestations

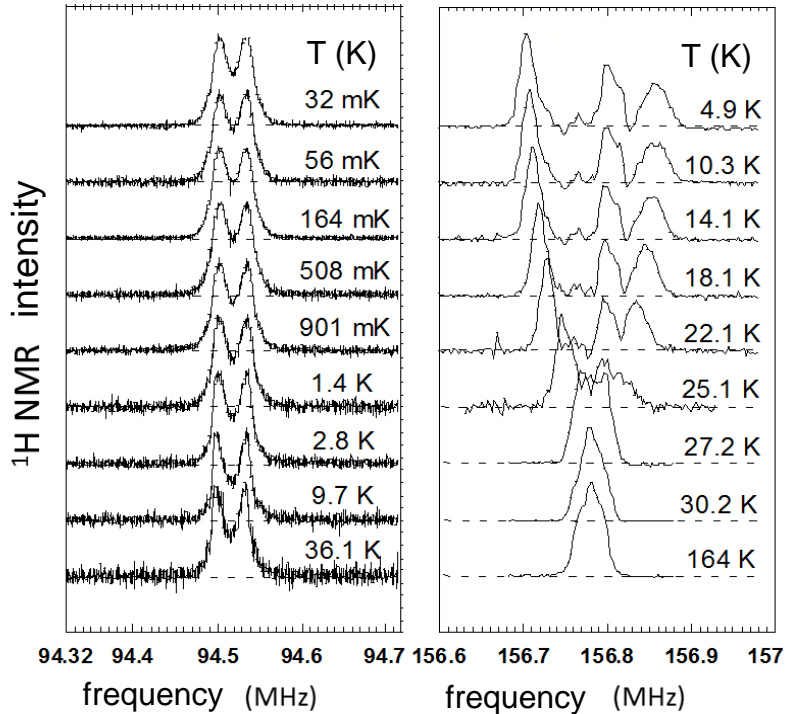
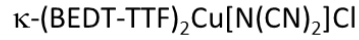
## $^1\text{H}$ NMR spectra



Triangular lattice



Deformed triangular lattice



No magnetic order



**QSL !**

Magnetic order

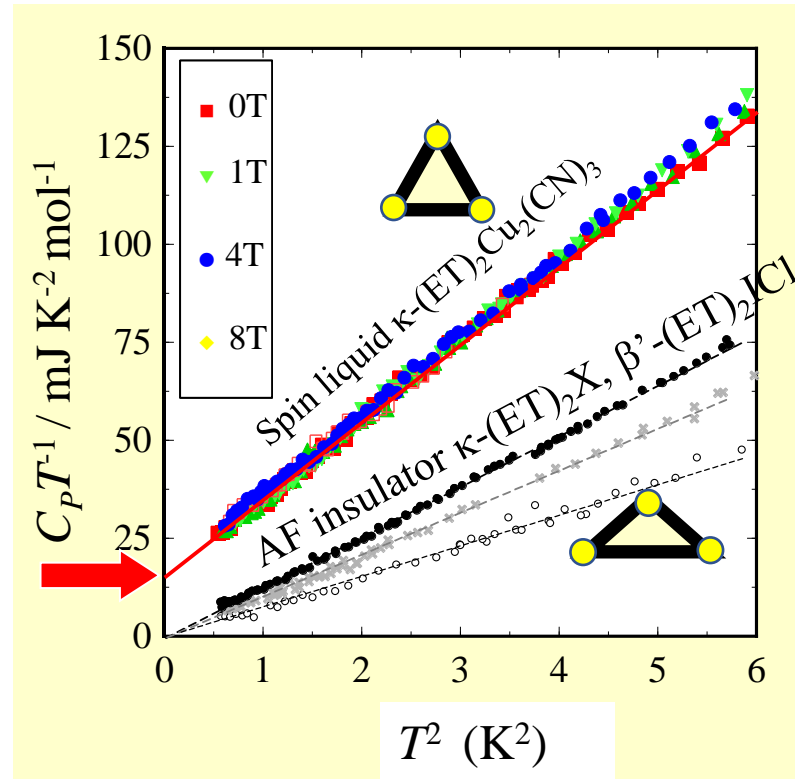


AFM

Shimizu et al., Phys. Rev. Lett. (2003)

## Specific heat

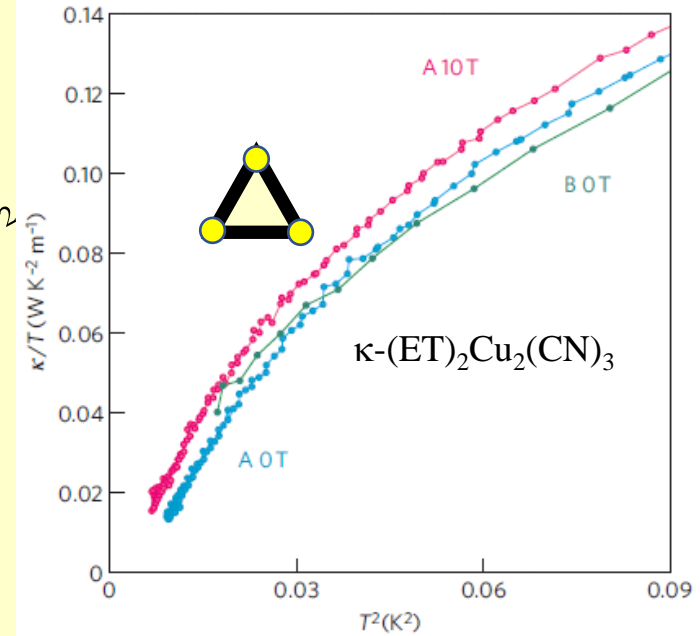
Gapless:  $\gamma = 13 \text{ mJ/K}^2\text{mol}$



S. Yamashita *et al.*,  
Nat. Phys. 4 (2008) 459

## Thermal conductivity

gapped:  $\Delta = 0.46 \text{ K}$



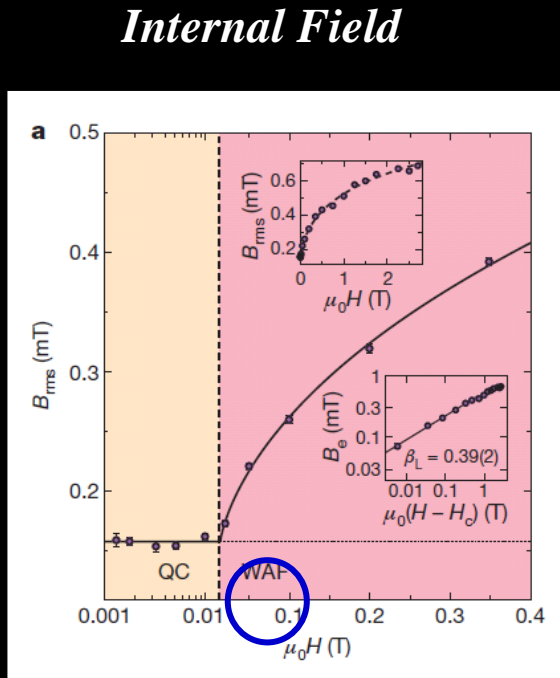
M. Yamashita *et al.*,  
Nat. Phys. 5 (2009) 44



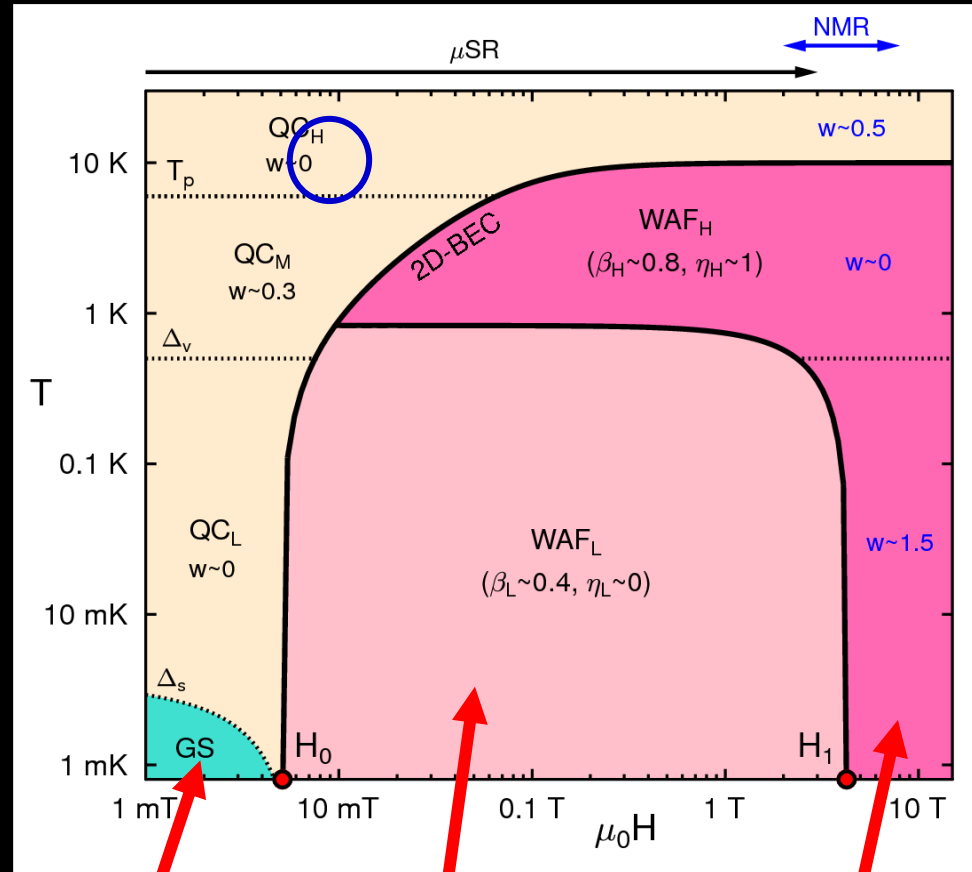
# H-T phase diagram determined by $\mu$ SR

Pratt et al. *Nature* **471** (2011)612

Inhomogeneous internal field induced by external field



T = 120 mK

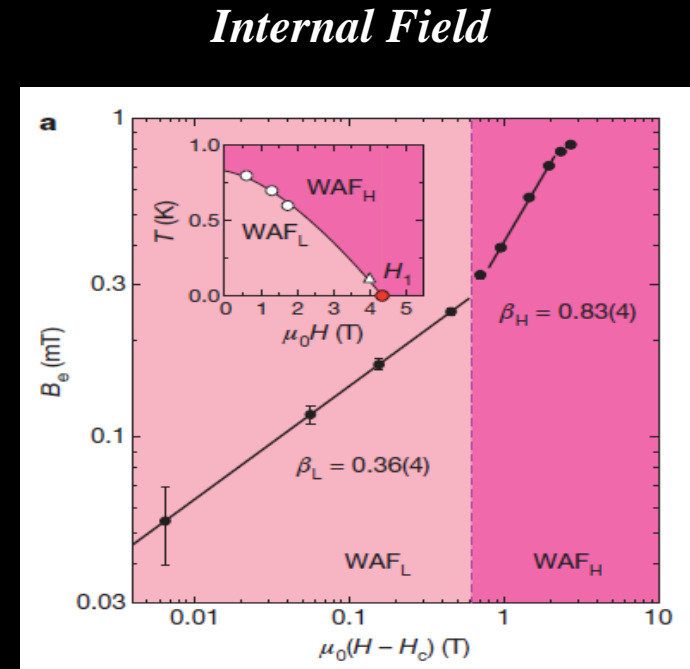


Spin gapped (4 mK)

BEC of Bosonic spinons ?  
cf. BaCuSi<sub>2</sub>O<sub>6</sub>

Deconfined Spinons ?  
Fermionic ?

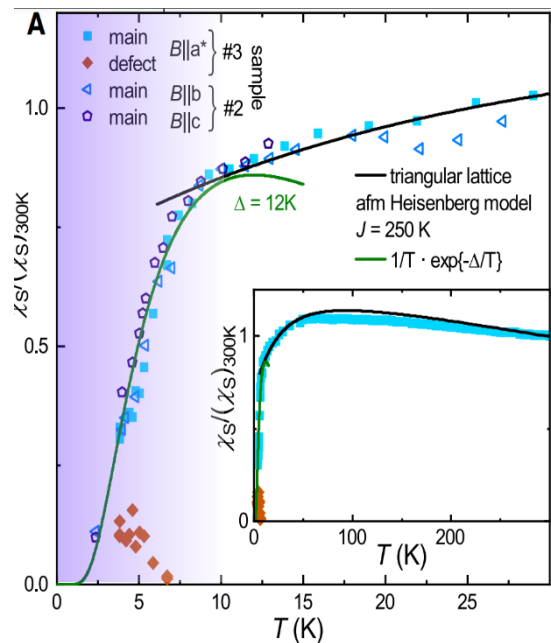
Bosonic spinons  
Qi, Xu, Sachdev PRL102(2009)176401



# Spin gapped or not at low temperatures ? ESR and NMR

## EPR

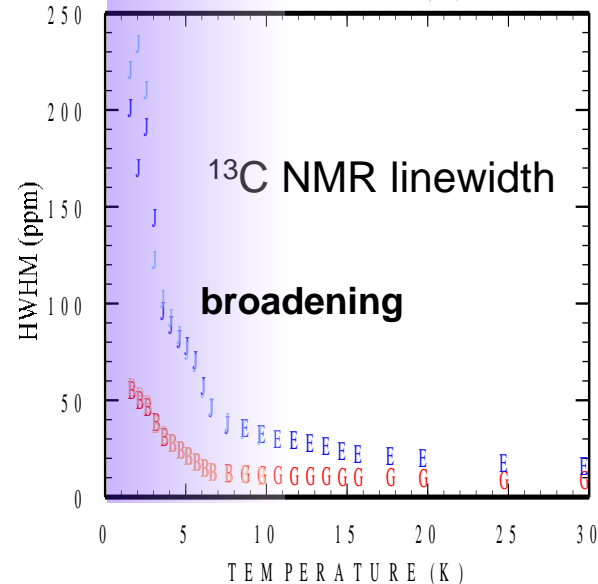
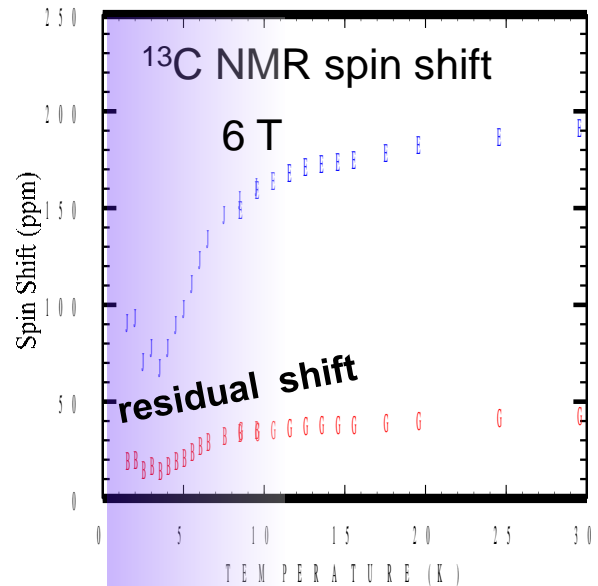
### Paramagnetic spins die



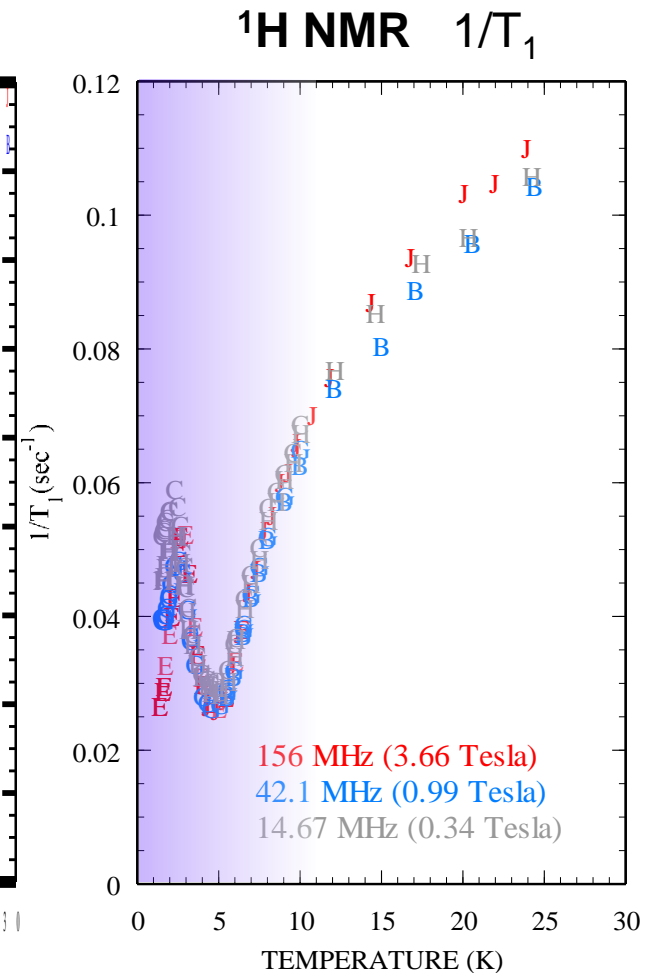
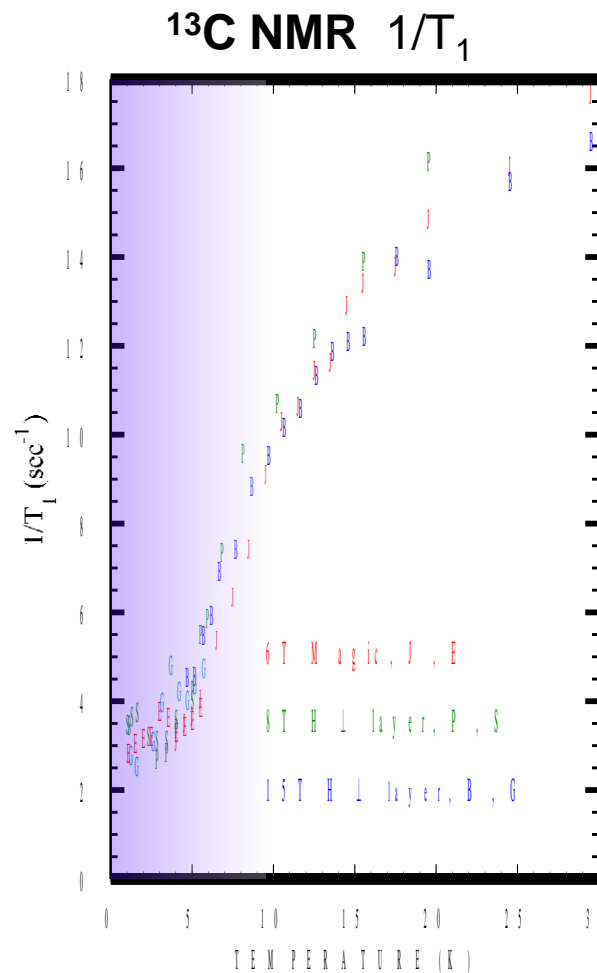
Miksch et al. Science 372, 276 (2021)

$\Delta \sim 10 \text{ K}$

## NMR spectra



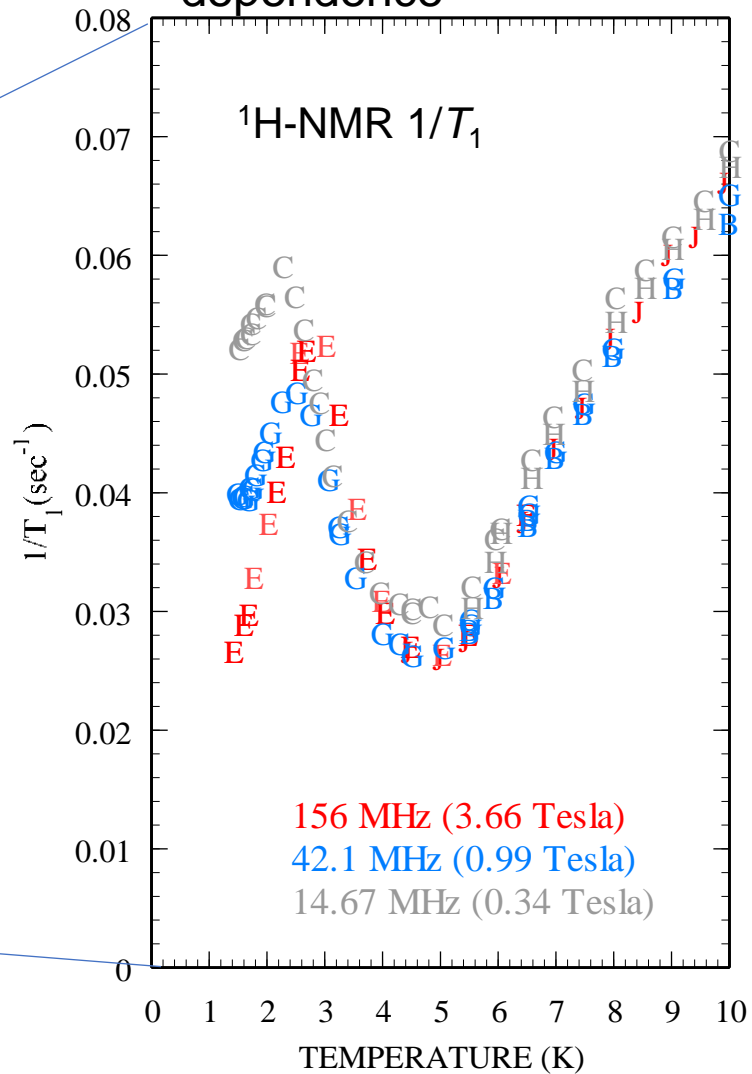
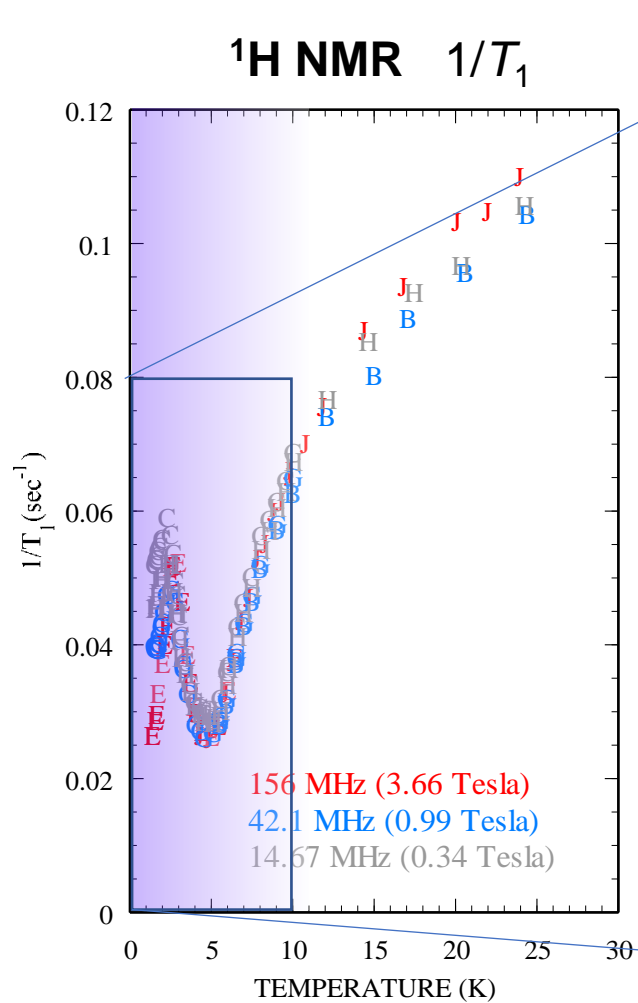
## NMR relaxation rate



# $^1\text{H}$ NMR relaxation rate

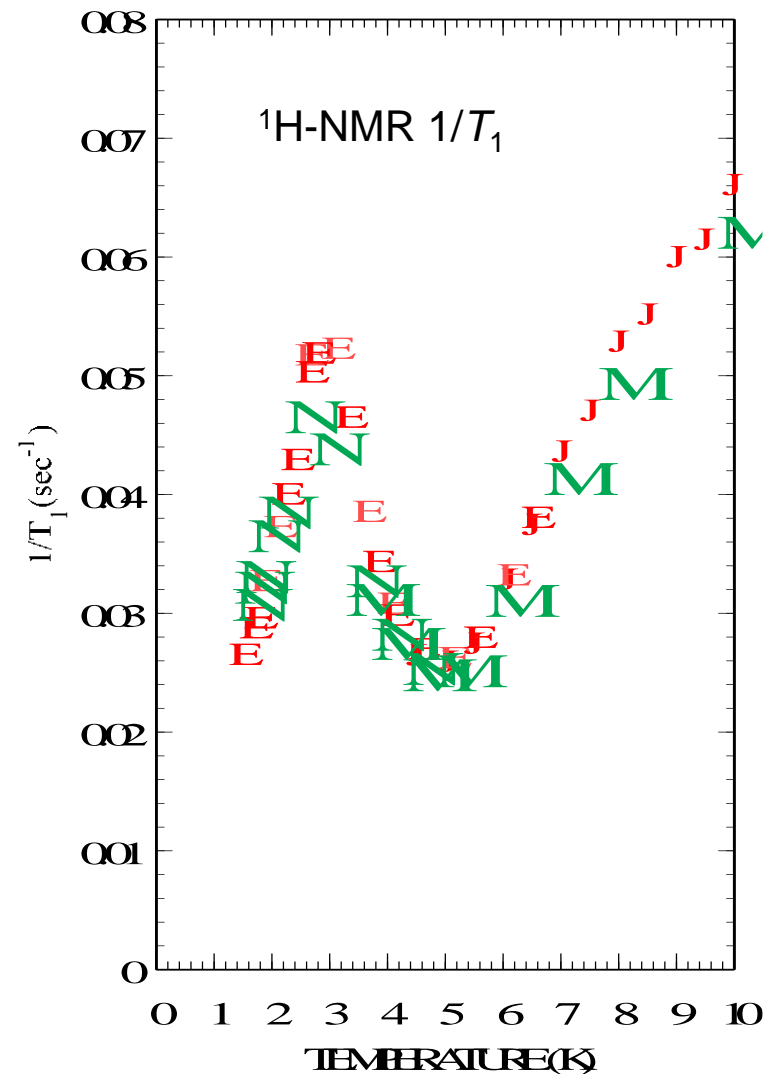


Magnetic field (frequency)  
dependence



Field-insensitive above 5 K

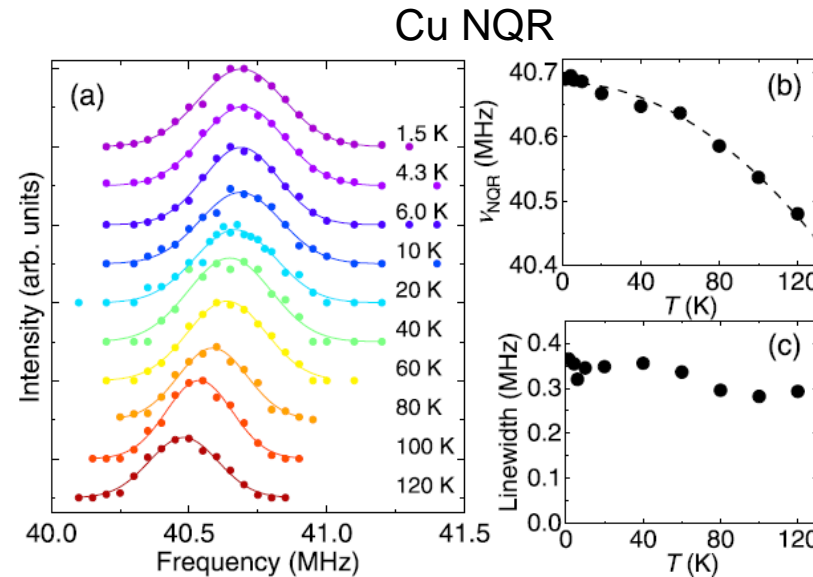
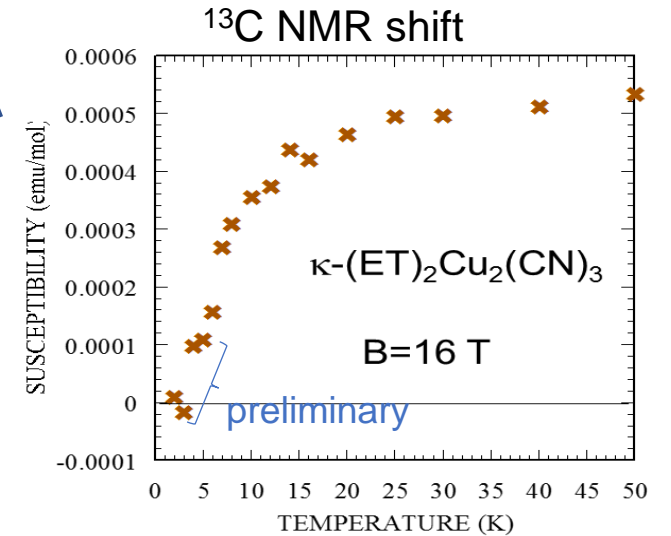
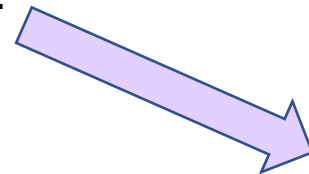
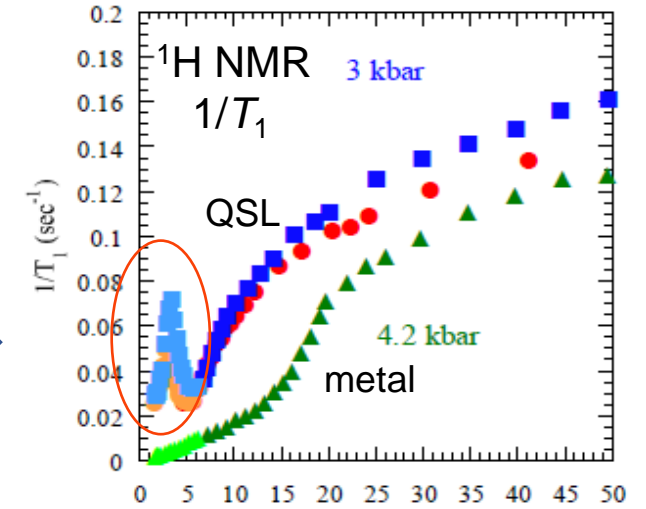
Nearly reproducible  
in separate samples



# Unconventional spin gapped state: instability of QSL ?

1. Knight shift and  $1/T_1$  do not vanish at low-T and line is broadened.
2.  $1/T_1$  forms a sharp peak after spin gapped.  
The peak disappears in the metallic phase.
3. The spin-gapped feature is robust even against 16 T.
4. No change in NQR spectra across 6 K.

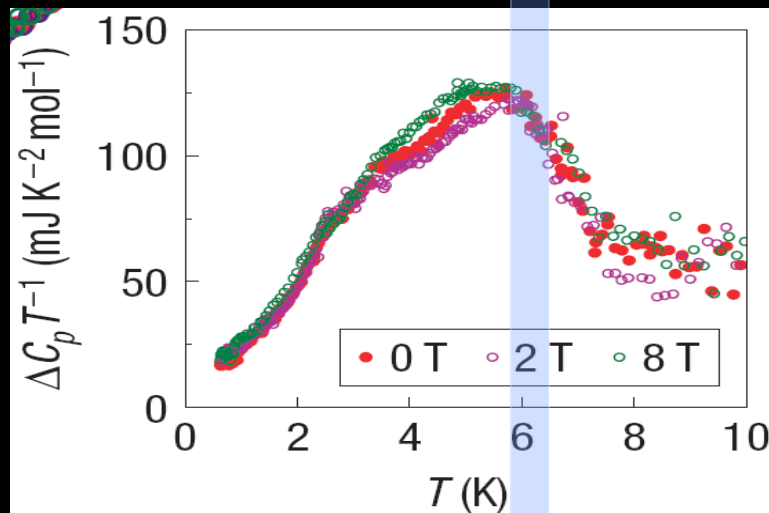
VBC (VBS) ?



# 6K-anomaly in $\kappa\text{-(ET)}_2\text{Cu}_2(\text{CN})_3$

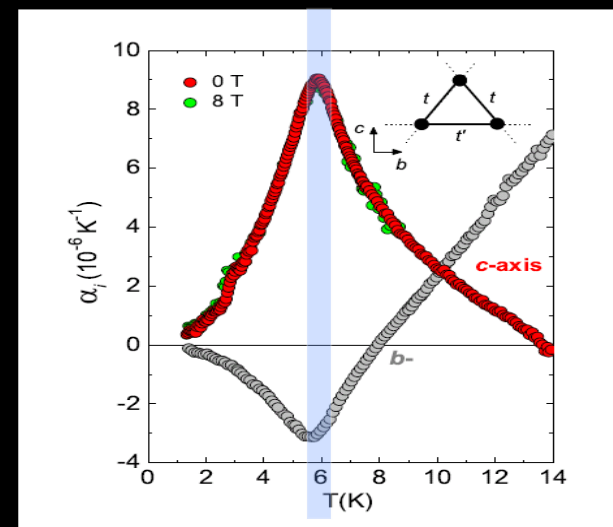
## Specific heat

S. Yamashita *et al.*,  
*Nature Phys.* 4 (2008) 459



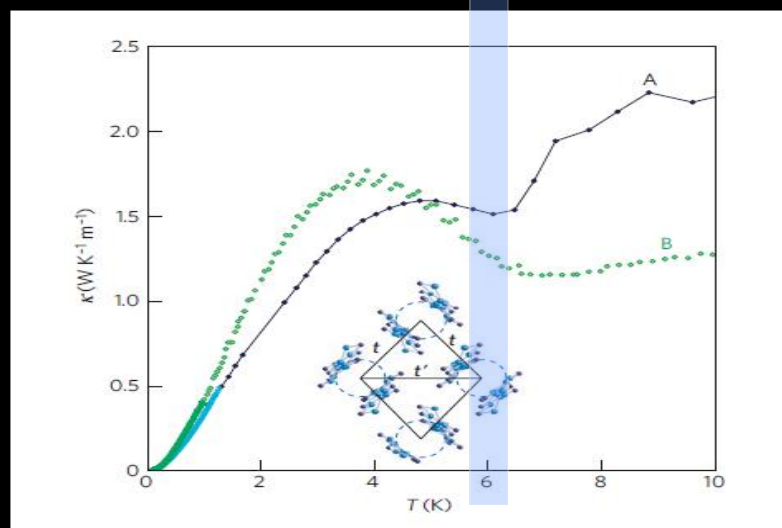
## Thermal expansion coefficient

Manna *et al.*, *PRL* 104 (2010) 016403



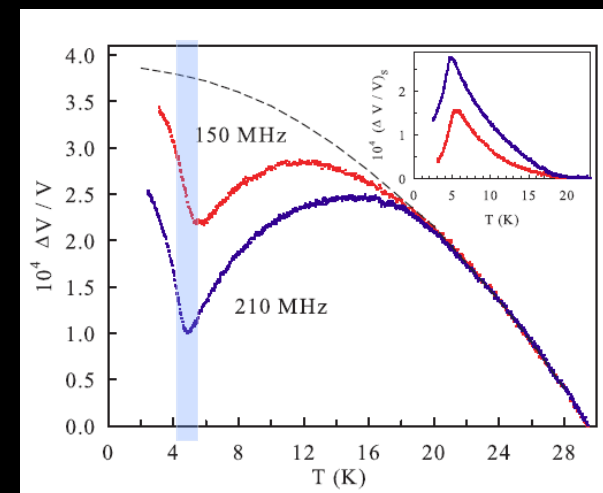
## Thermal conductivity

M. Yamashita *et al.*,  
*Nature Phys.* 5 (2009) 44



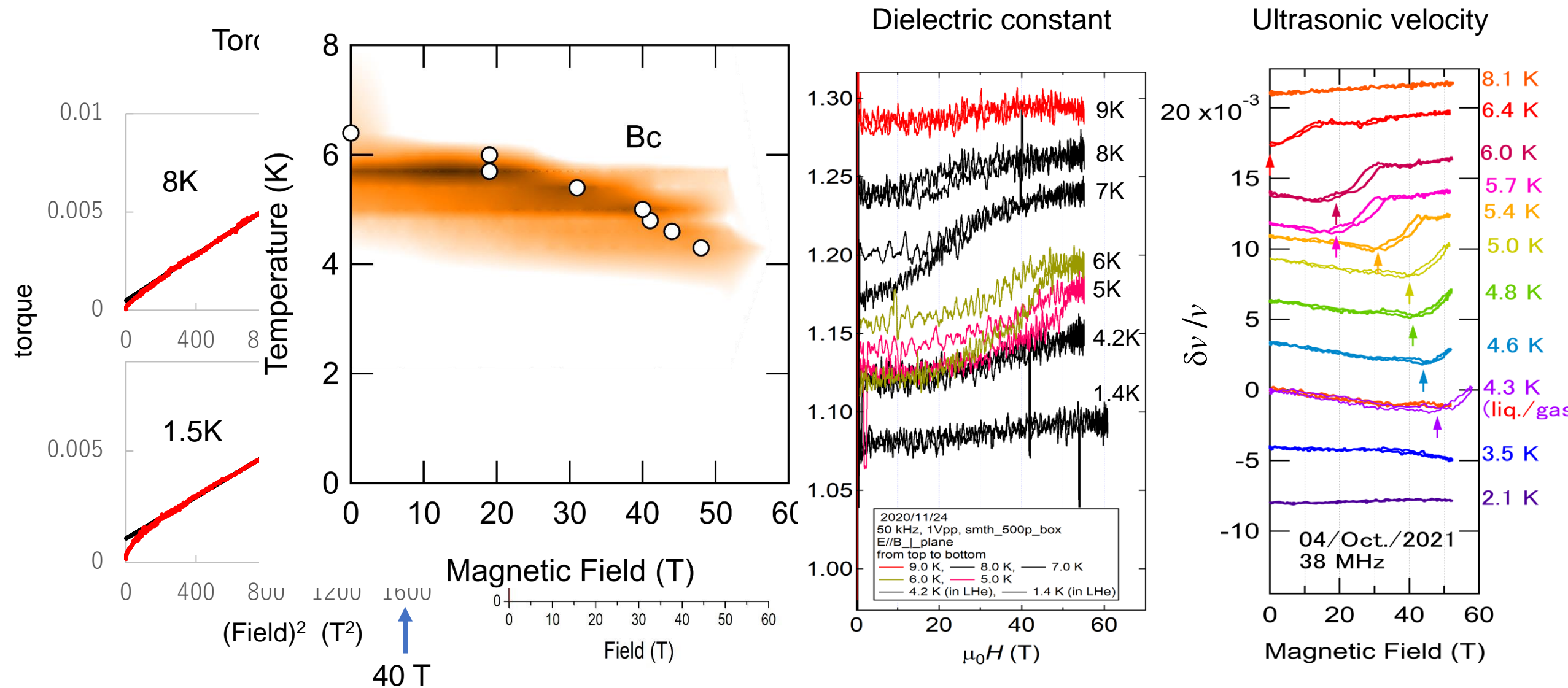
## Ultrasound velocity

Poirier *et al.*,



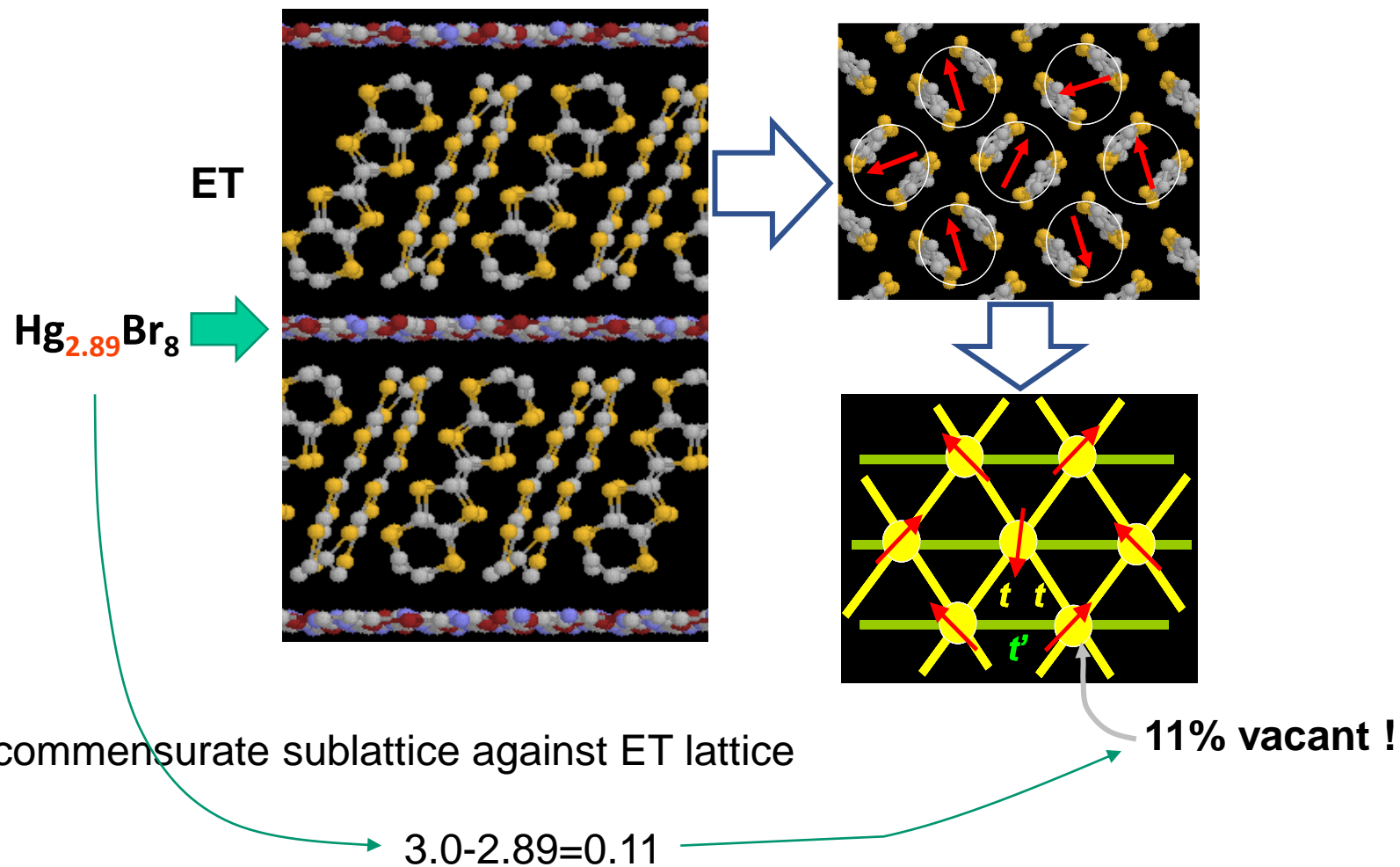
# Search for quantum oscillations in $\kappa$ -(ET)<sub>2</sub>Cu<sub>2</sub>(CN)<sub>3</sub> with magnetic fields up to 60 Tesla at ISSP

Kohama, Nomura, Miyake, Urai



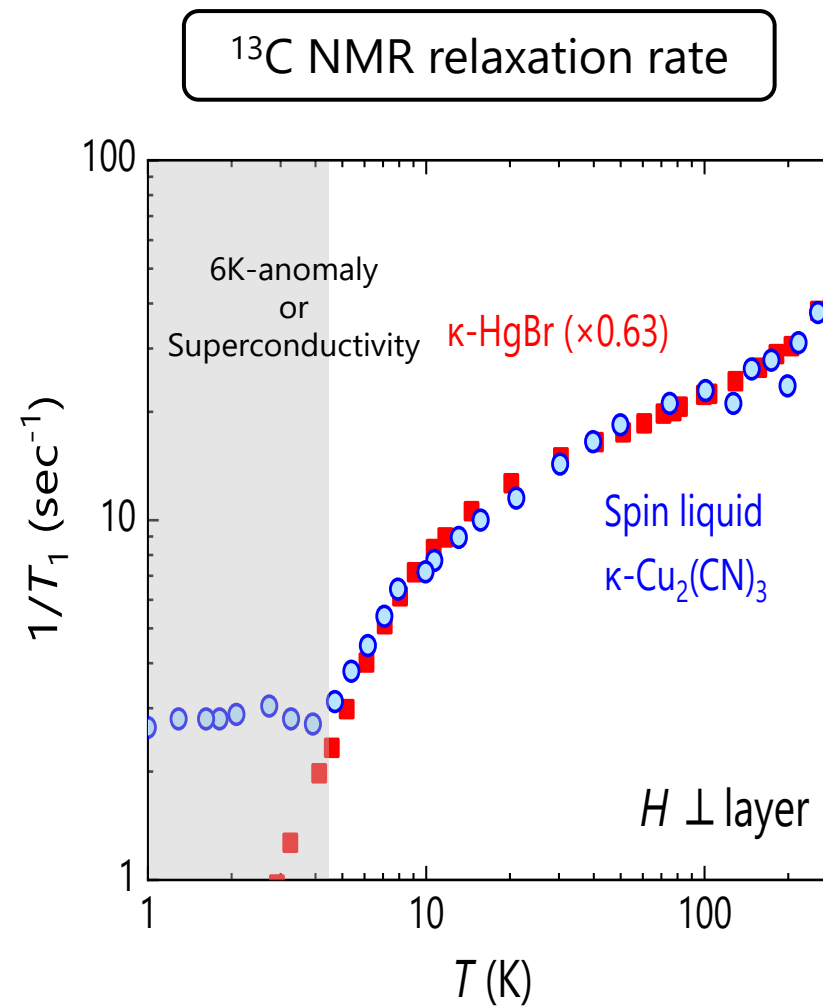
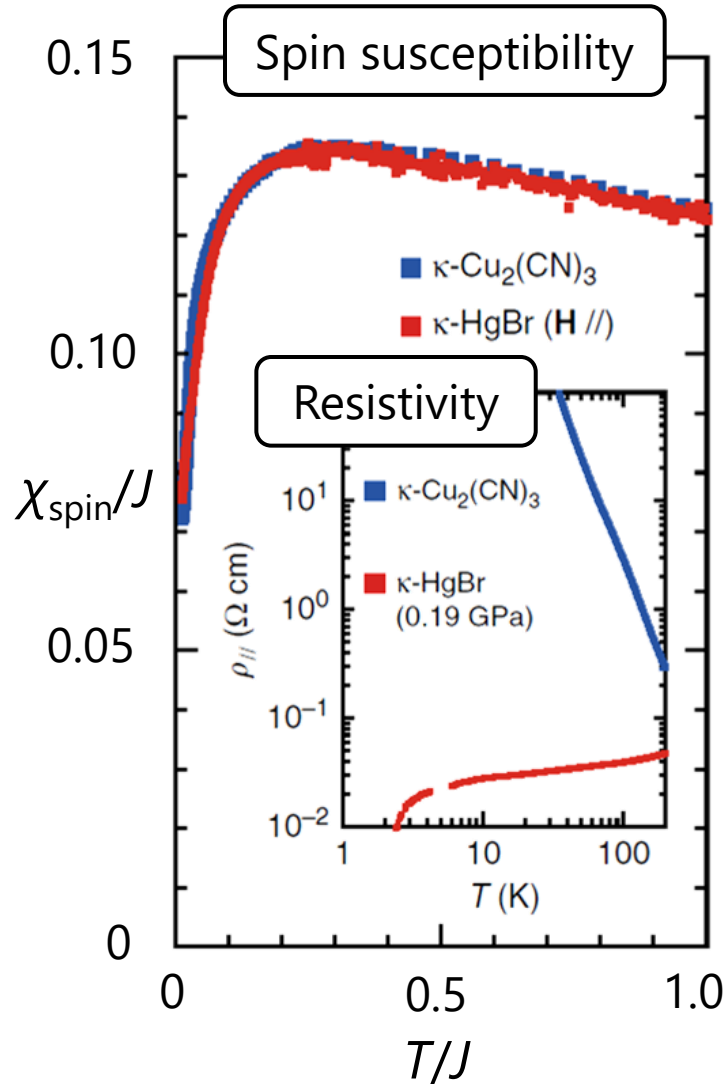
# Doped spin liquid candidate $\kappa\text{-(ET)}_4\text{Hg}_{2.89}\text{Br}_8$ (11% hole doping)

Nonstoichiometric compound  $\kappa\text{-(ET)}_4\text{Hg}_{2.89}\text{Br}_8$



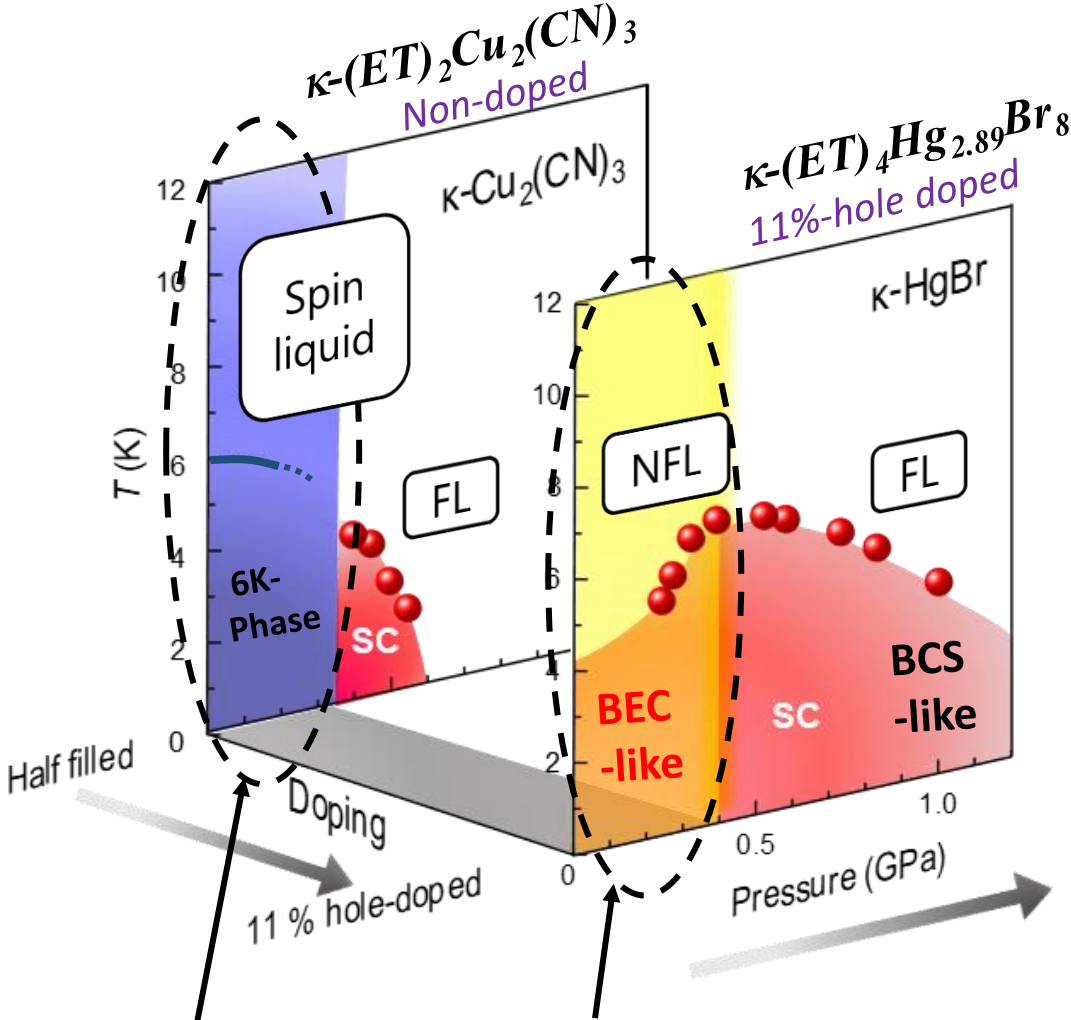
# Non-doped and doped QSL candidates

Contrasting conductivity, similar magnetism  $\longrightarrow$  Doped QSL





# Phase diagram : non-doped and doped spin liquid materials



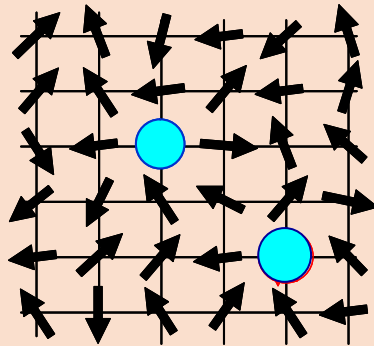
QSL phase	→	non-Fermi liquid
6-K phase	→	superconducting phase

# Pressure dependence of Hall coefficient: from doped QSL to correlated metal



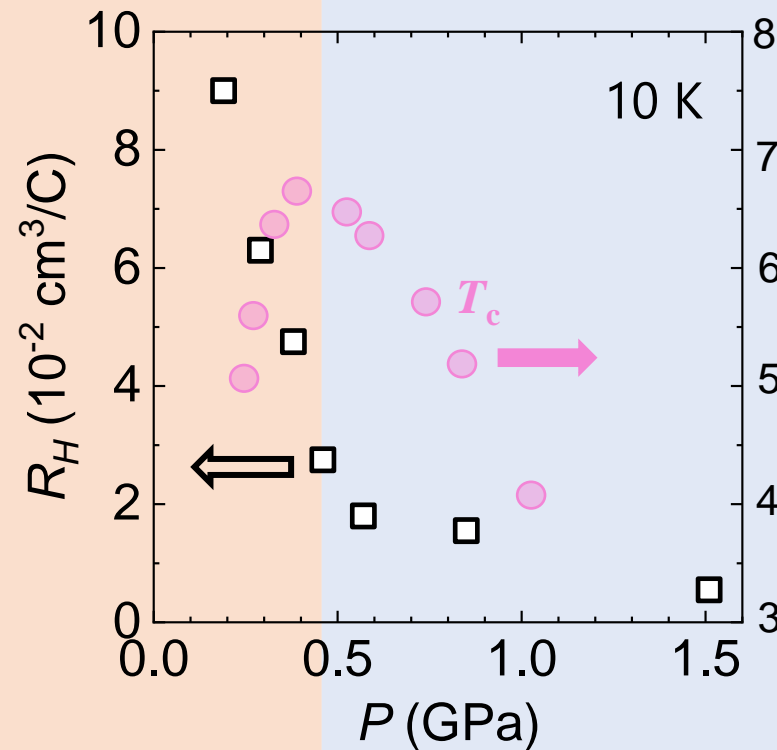
*Hall coefficient*  $\sim$  (*carrier number*)<sup>-1</sup>

Double occupancy  
Prohibited

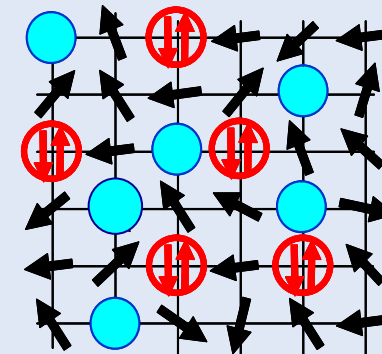


Low carrier density

*Doped Mott*



Double occupancy  
Allowed

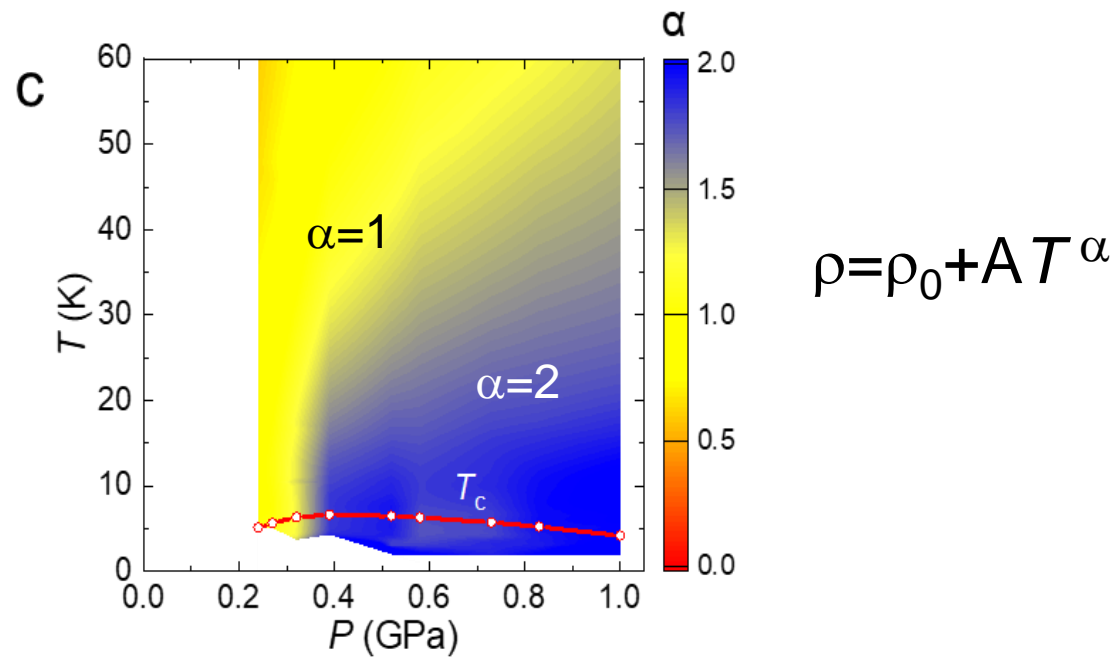
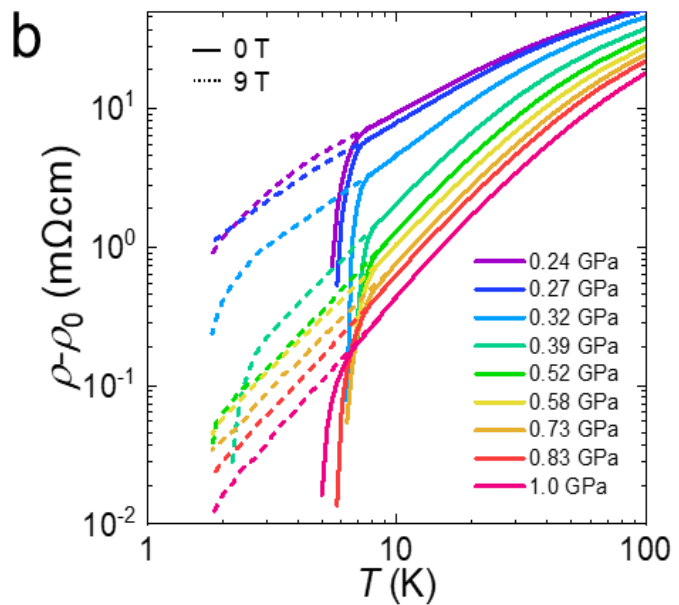
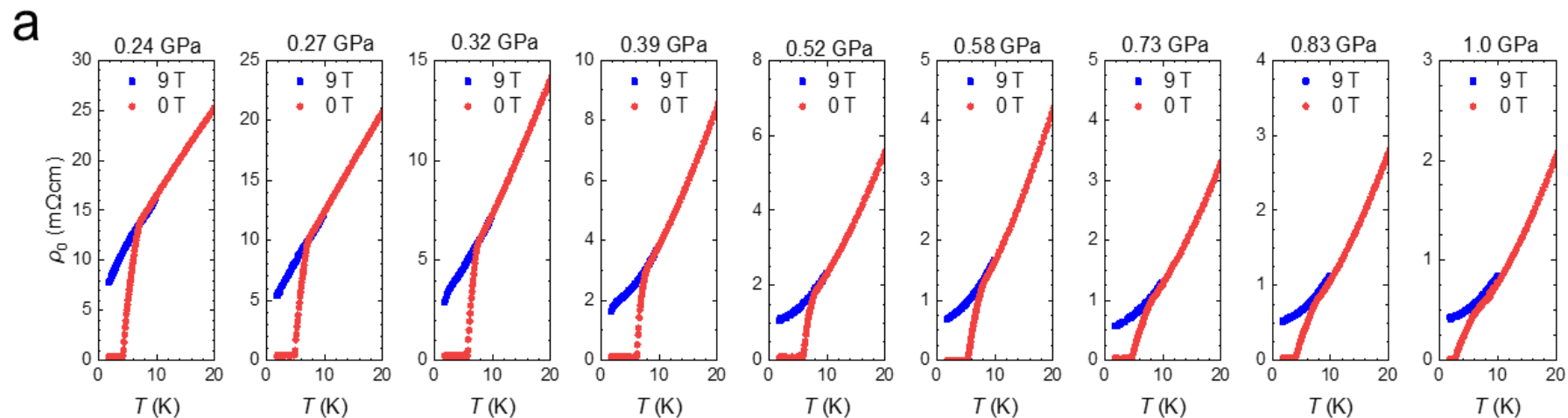


High carrier density

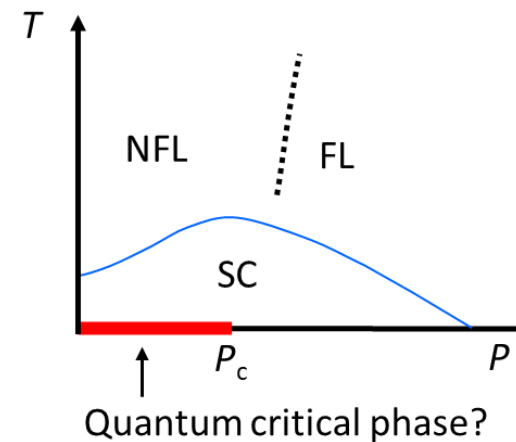
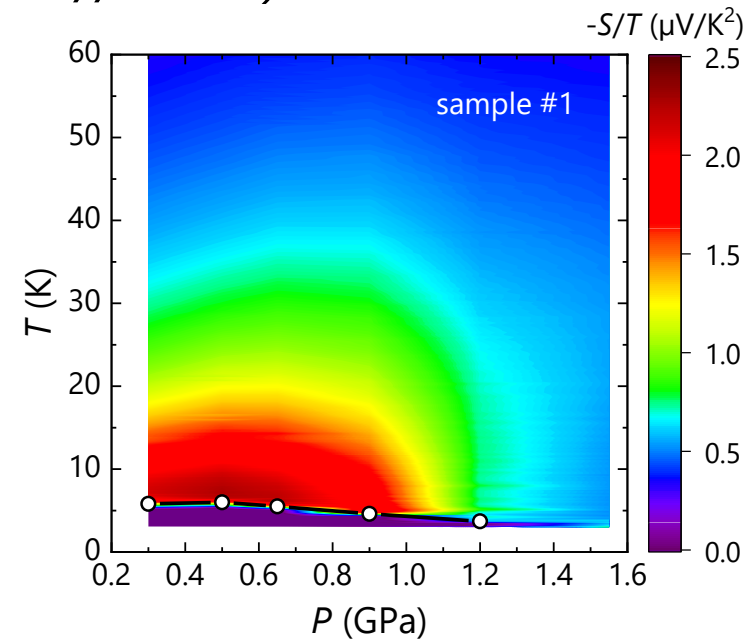
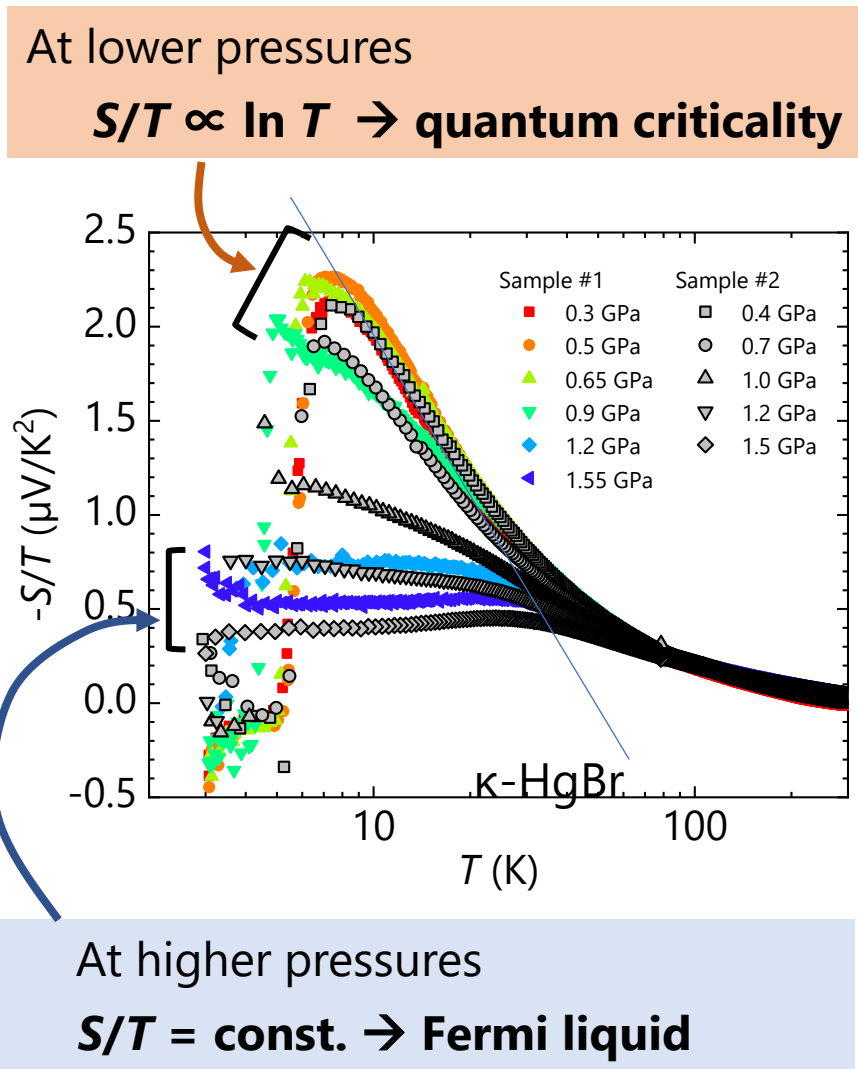
*Correlated metal*

# Non-Fermi liquid to Fermi liquid crossover

$\kappa\text{-(ET)}_4\text{Hg}_{2.89}\text{Br}_8$



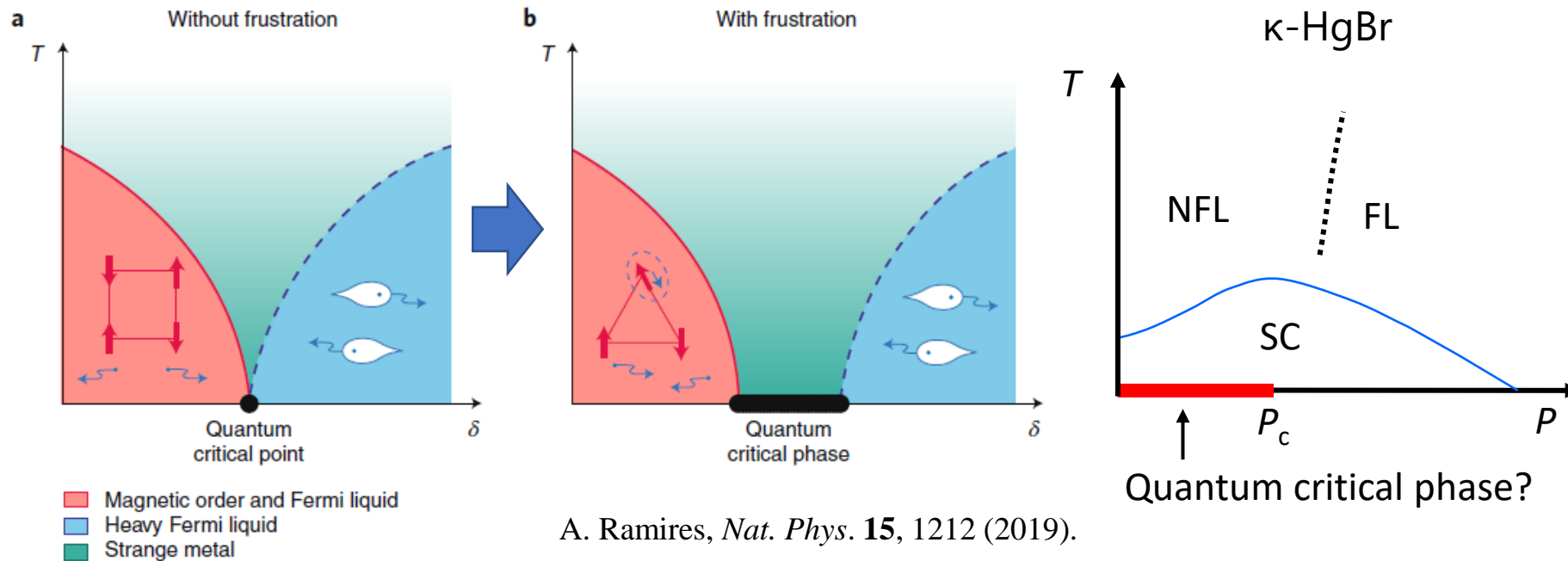
Seebeck coefficient  $S$  ( $\nabla T // c\text{-axis}$ )



# Quantum critical "phase"

CePdAl (Heavy fermion system with Kagome lattice)  
→ Emergence of quantum critical *phase*, (not a point)  
H. Zhao, *et al.*, *Nat. Phys.* **15**, 1261 (2019).

## Frustration makes QC point to QC phase



A. Ramires, *Nat. Phys.* **15**, 1212 (2019).

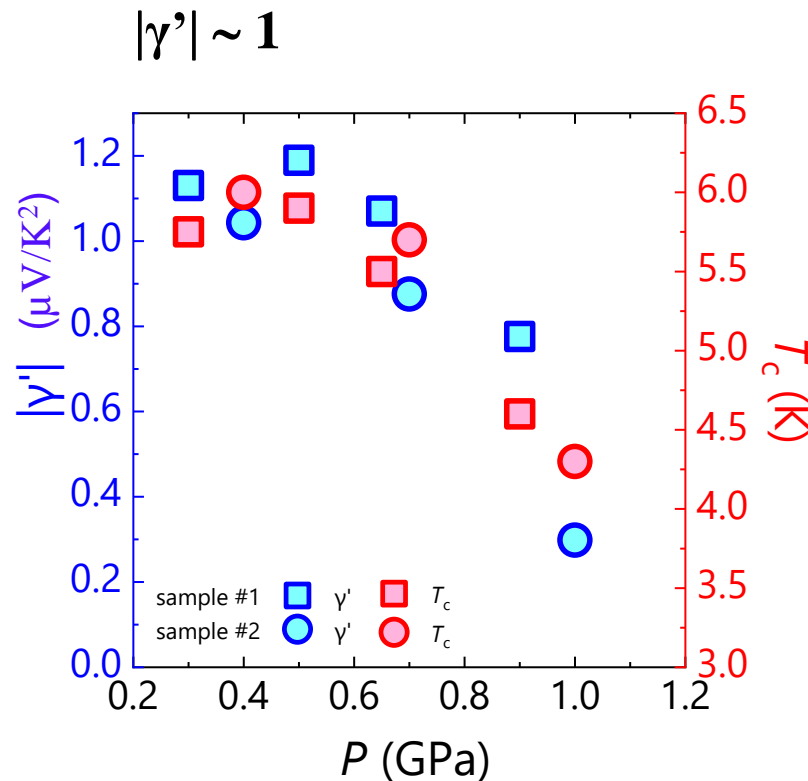
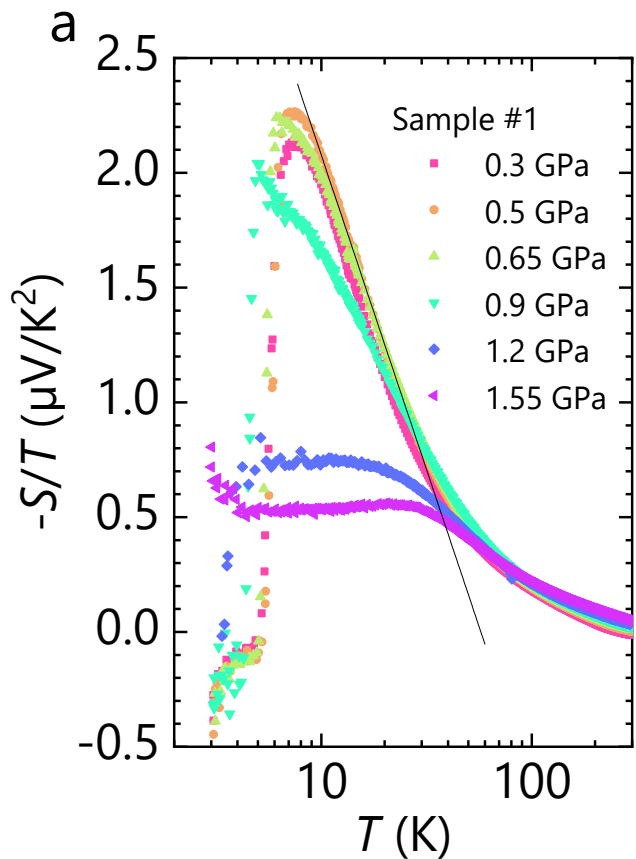
M. Vojta, *Rep. Prog. Phys.* **81**, 064501 (2018)

# Strength of Quantum criticality



Table S1 |  $|\gamma'|$  values in the logarithmic part of  $-S/T$   
The  $|\gamma'|$  values in  $S/T = \gamma' \ln(T/T_0)$  in the unit of  $\mu\text{V}/\text{K}^2$ .

$$S/T = \gamma' \ln(T/T_0) \quad (10 \text{ K} < T < 30 \text{ K})$$



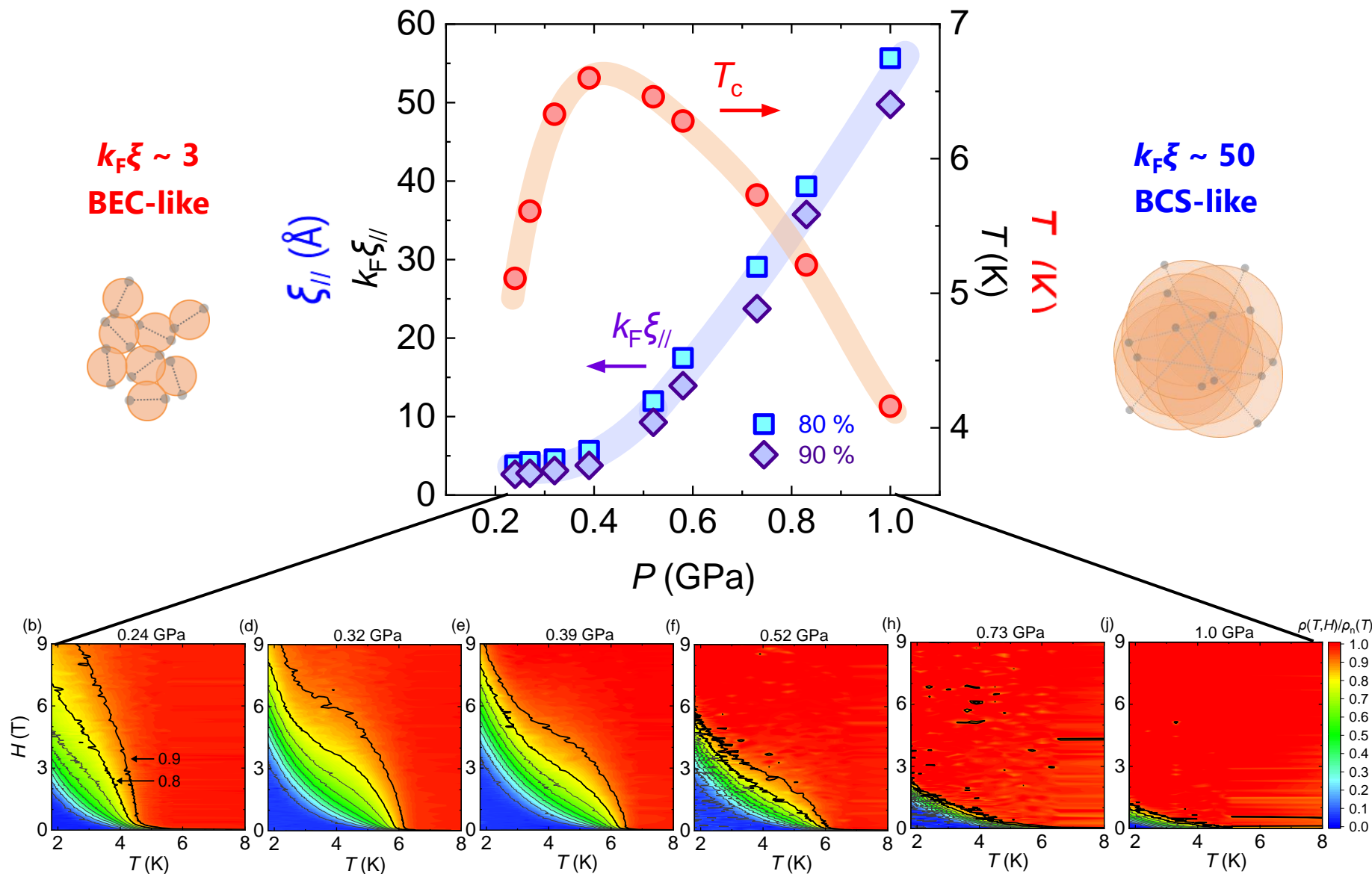
$T_c$  and  $\gamma'$  are scaled to each other

Material	Slope value
Nd-LSCO ( $p = 0.24$ ) (ref. <sup>6</sup> )	0.11
Eu-LSCO ( $p = 0.24$ ) (ref. <sup>7</sup> )	0.16
Bi2201 ( $p = 0.39$ ) (ref. <sup>8</sup> )	0.05
PCCO ( $x = 0.16\text{-}0.19$ ) (ref. <sup>9</sup> )	0.012-0.038
LCCO ( $x = 0.15\text{-}0.17$ ) (ref. <sup>9</sup> )	0.0095 – 0.049
[BiBa <sub>0.66</sub> K <sub>0.36</sub> O <sub>2</sub> ]CoO <sub>2</sub> (ref. <sup>10</sup> )	0.62
Ba(Fe <sub>1-x</sub> Co <sub>x</sub> ) <sub>2</sub> As <sub>2</sub> ( $p=0.022\text{-}0.13$ ) (ref. <sup>11</sup> )	0.32 - 0.895
EuFe <sub>2</sub> (As <sub>1-y</sub> P <sub>y</sub> ) <sub>2</sub> ( $y=0.26, 0.36$ ) (ref. <sup>18</sup> )	0.077, 0.16
UCoGe (H=11.1 T) (ref. <sup>12</sup> )	2.3
YbRh <sub>2</sub> Si <sub>2</sub> (ref. <sup>13</sup> )	4.5
CeCu <sub>5.9</sub> Au <sub>0.1</sub> (ref. <sup>14</sup> )	6.2
Ce <sub>2</sub> PdIn <sub>8</sub> (ref. <sup>15</sup> )	1.6
YbAgGe (ref. <sup>16</sup> )	4.7
YbPtBi (ref. <sup>17</sup> )	0.25

# Pressure-induced BEC to BCS

$\kappa\text{-(ET)}_4\text{Hg}_{2.89}\text{Br}_8$

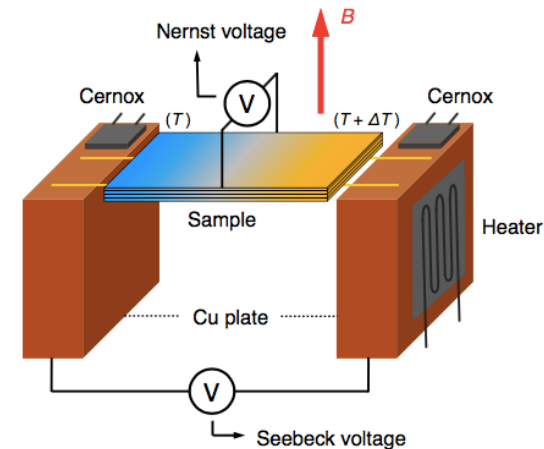
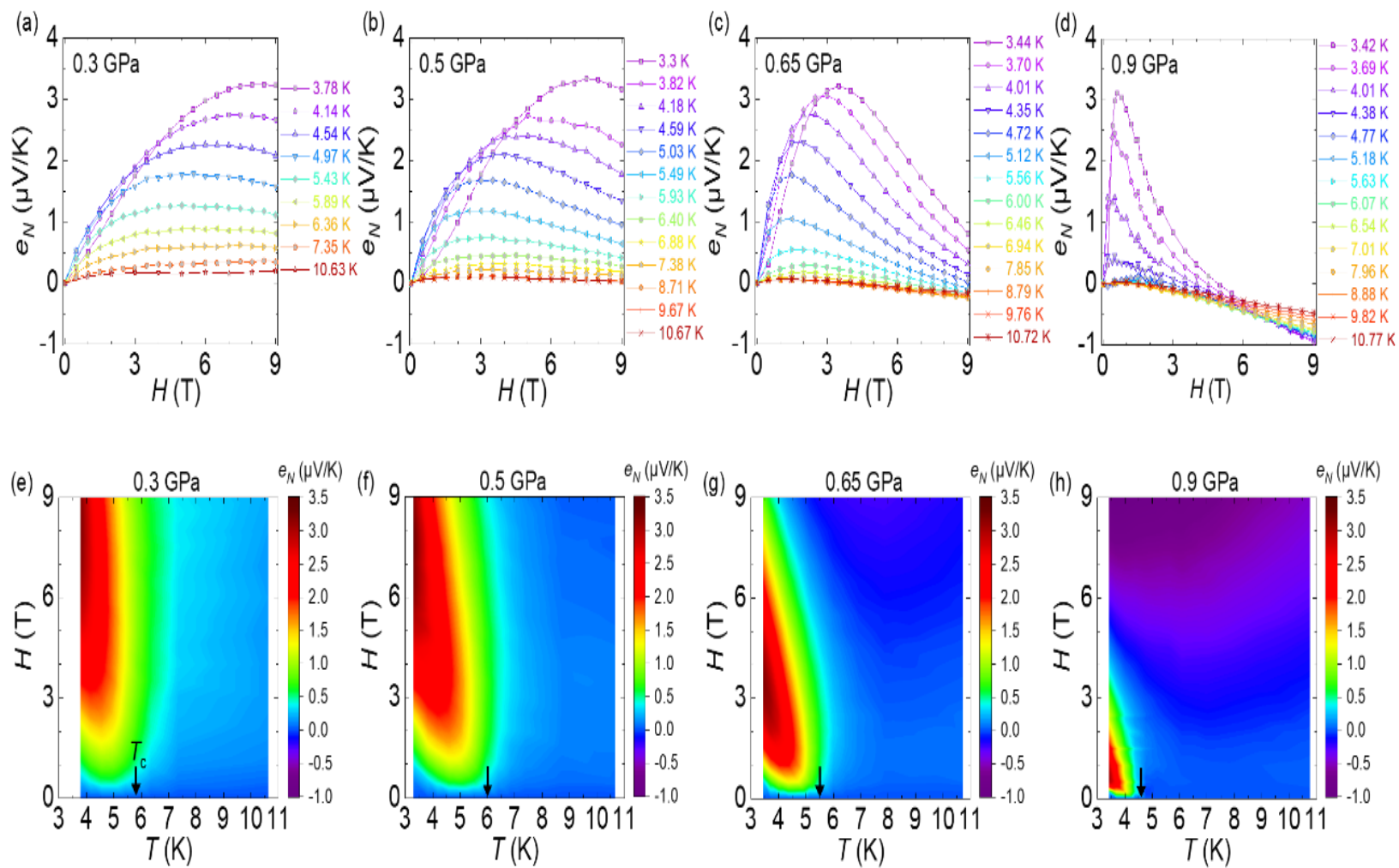
Y. Suzuki *et al.*, Phys. Rev. X **12**, 011016 (2022).



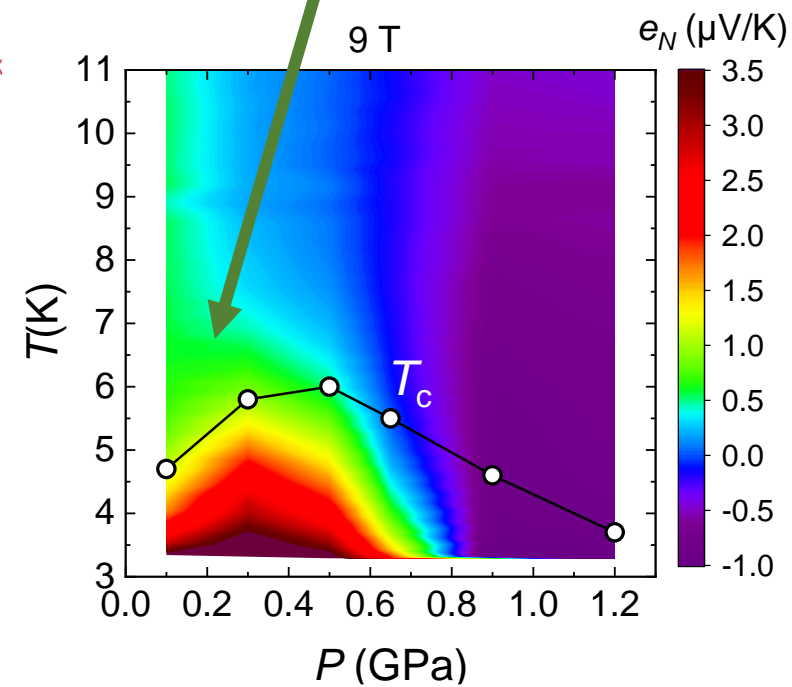
# Nernst effect



## Field-robust superconductivity

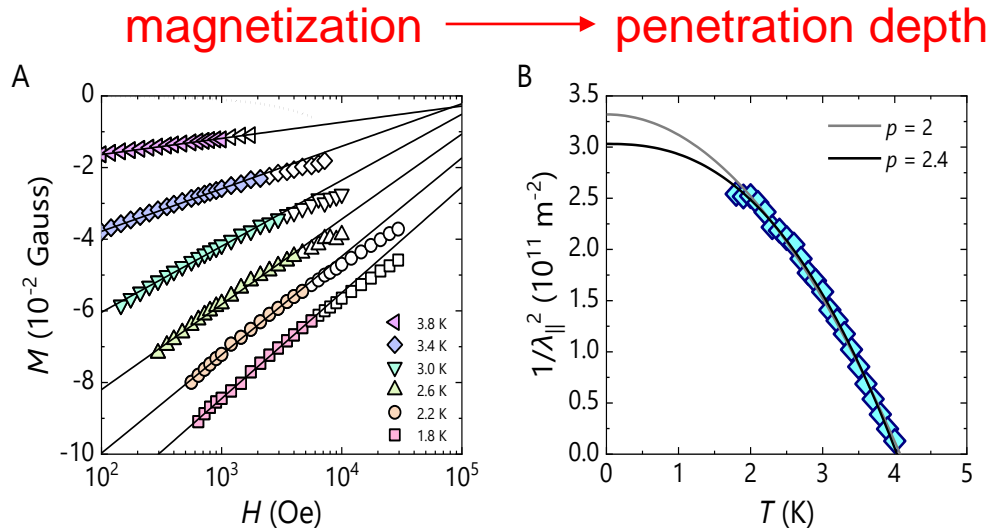


## Preformed pairs





# Superfluid density

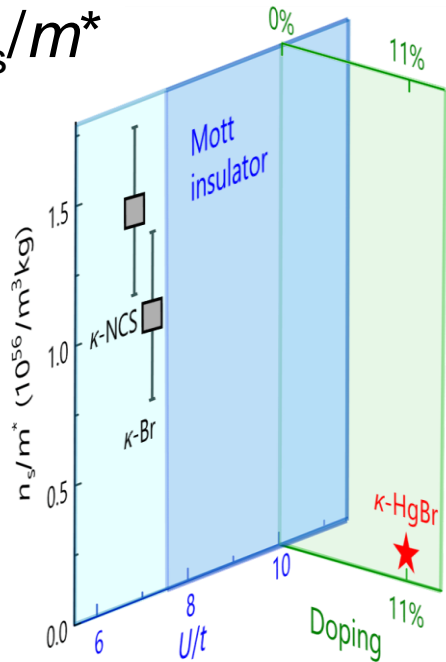


$$-4\pi M = \frac{\varphi_0}{8\pi\lambda^2} \ln\left(\frac{\beta H_{c2}}{H}\right)$$

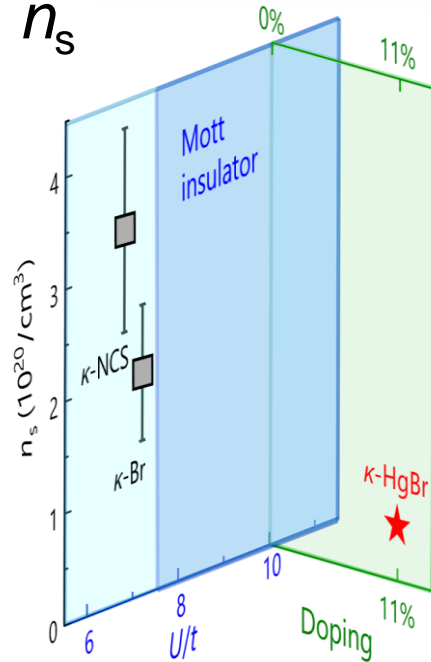
cf. M. Lang et al., *Phys. Rev. B* **46**, 5822-5825 (1992).

$$\frac{n_s}{m^*} = \frac{c^2}{4\pi e^2} \frac{1}{\lambda_L^2}$$

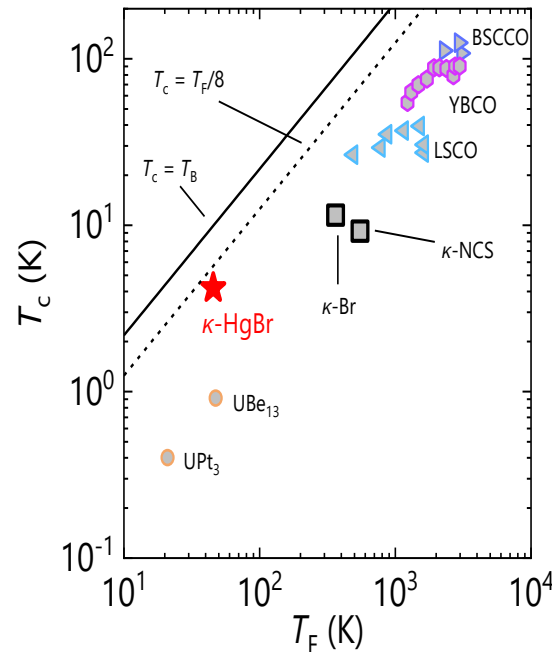
$n_s/m^*$



$n_s$



Uemura plot



**Reduced superfluid density**

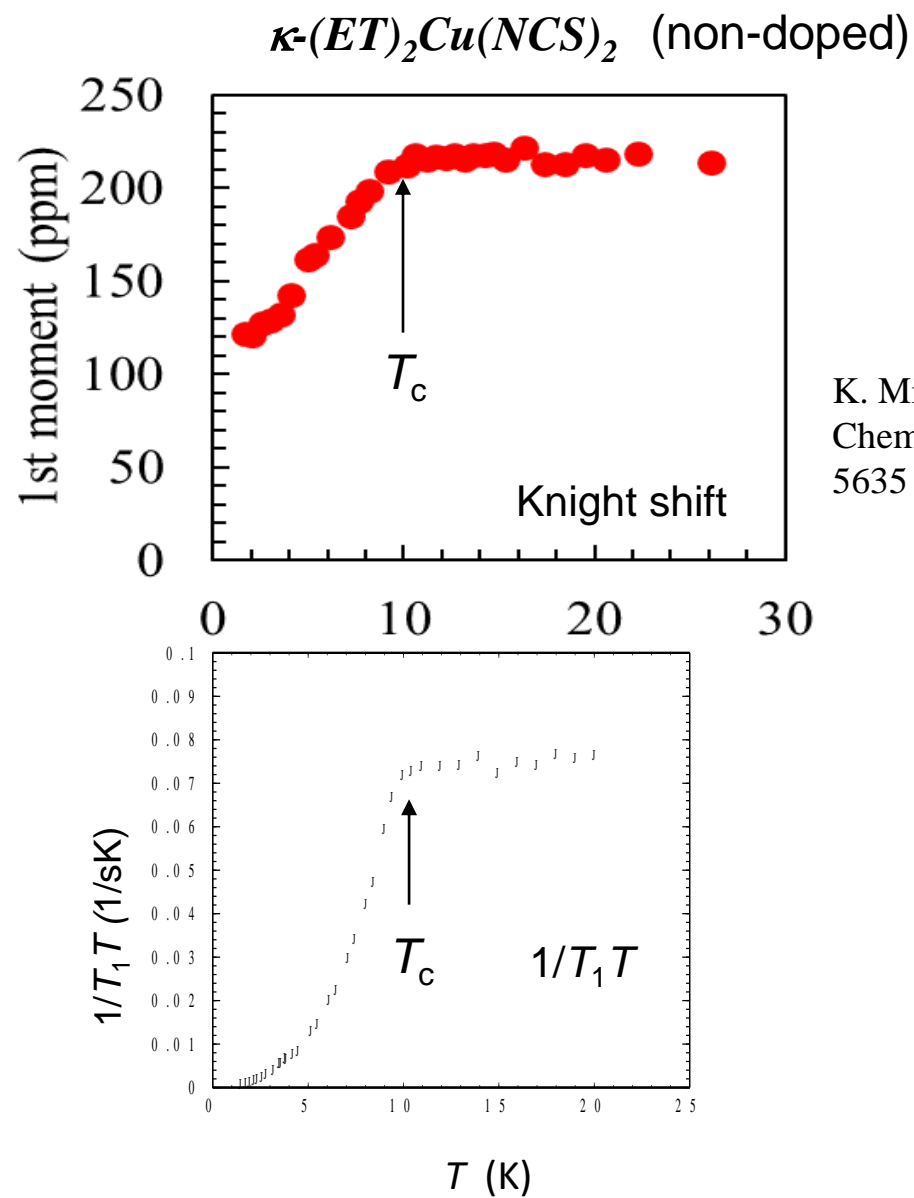
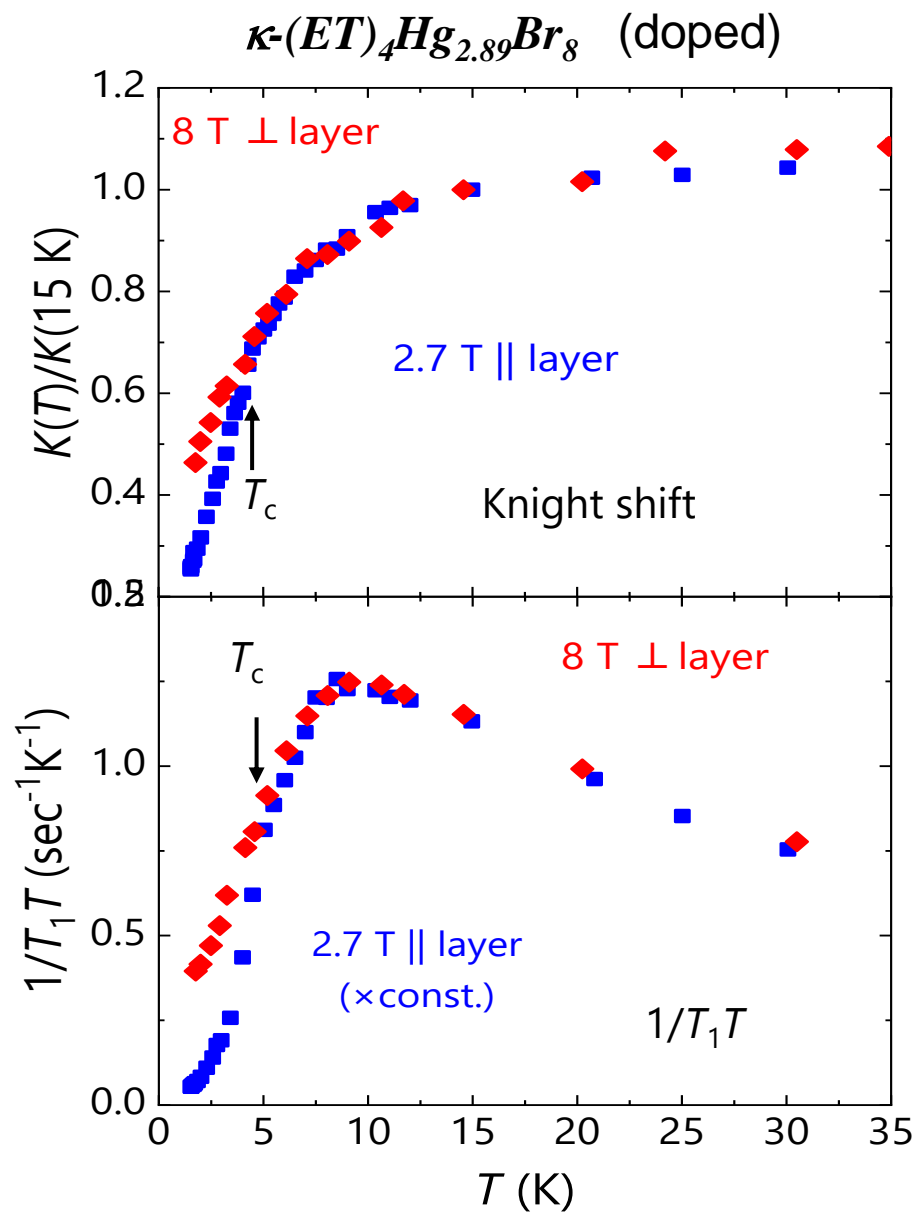
$n_s \sim 15\text{-}25\%$  of total carriers

**Large  $T_c/T_F$  ratio**

$T_c/T_F \sim 0.1$

# $^{13}\text{C}$ NMR Knight shift and relaxation rate $1/T_1$

## Preformed pairs (and pseudo-gapped metal)

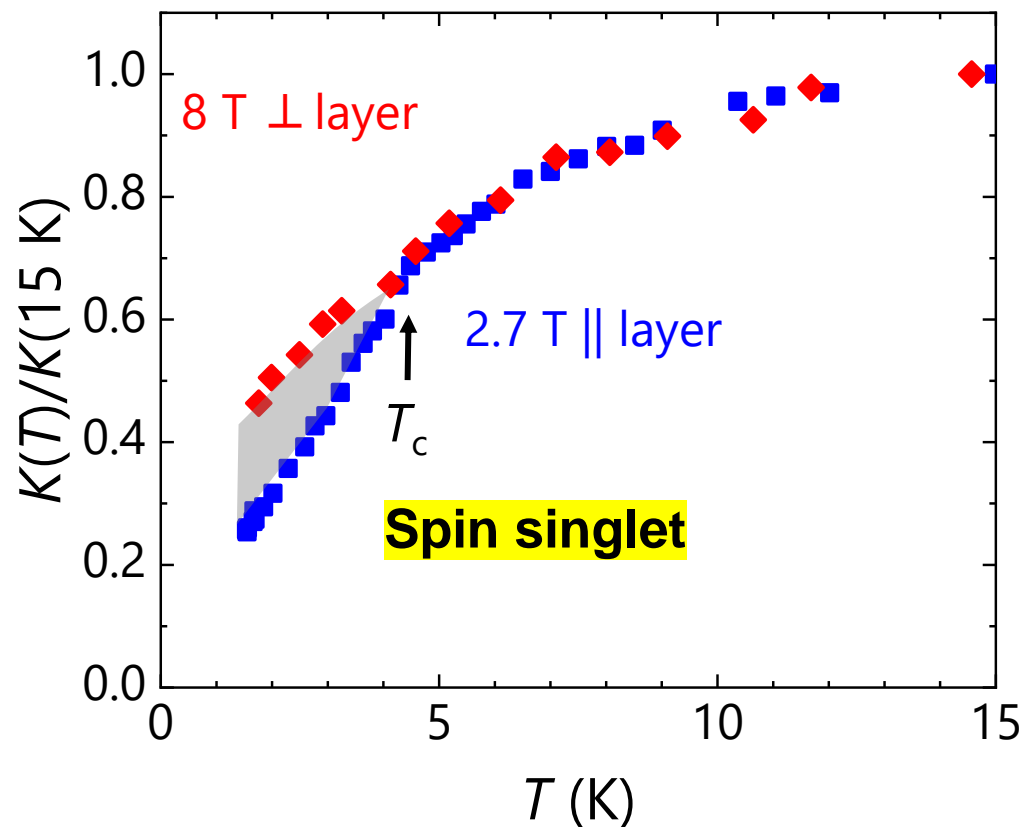


K. Miyagawa *et al.*,  
Chem. Rev. **104**,  
5635 (2004).

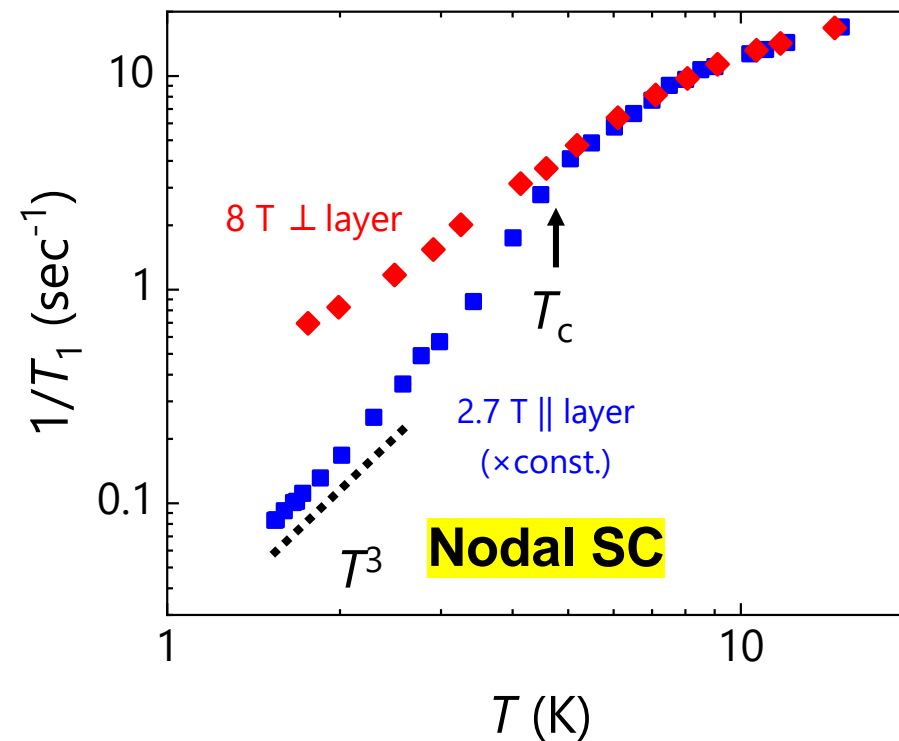
# Pairing symmetry: $^{13}\text{C}$ NMR



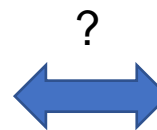
## Knight shift



## Relaxation rate

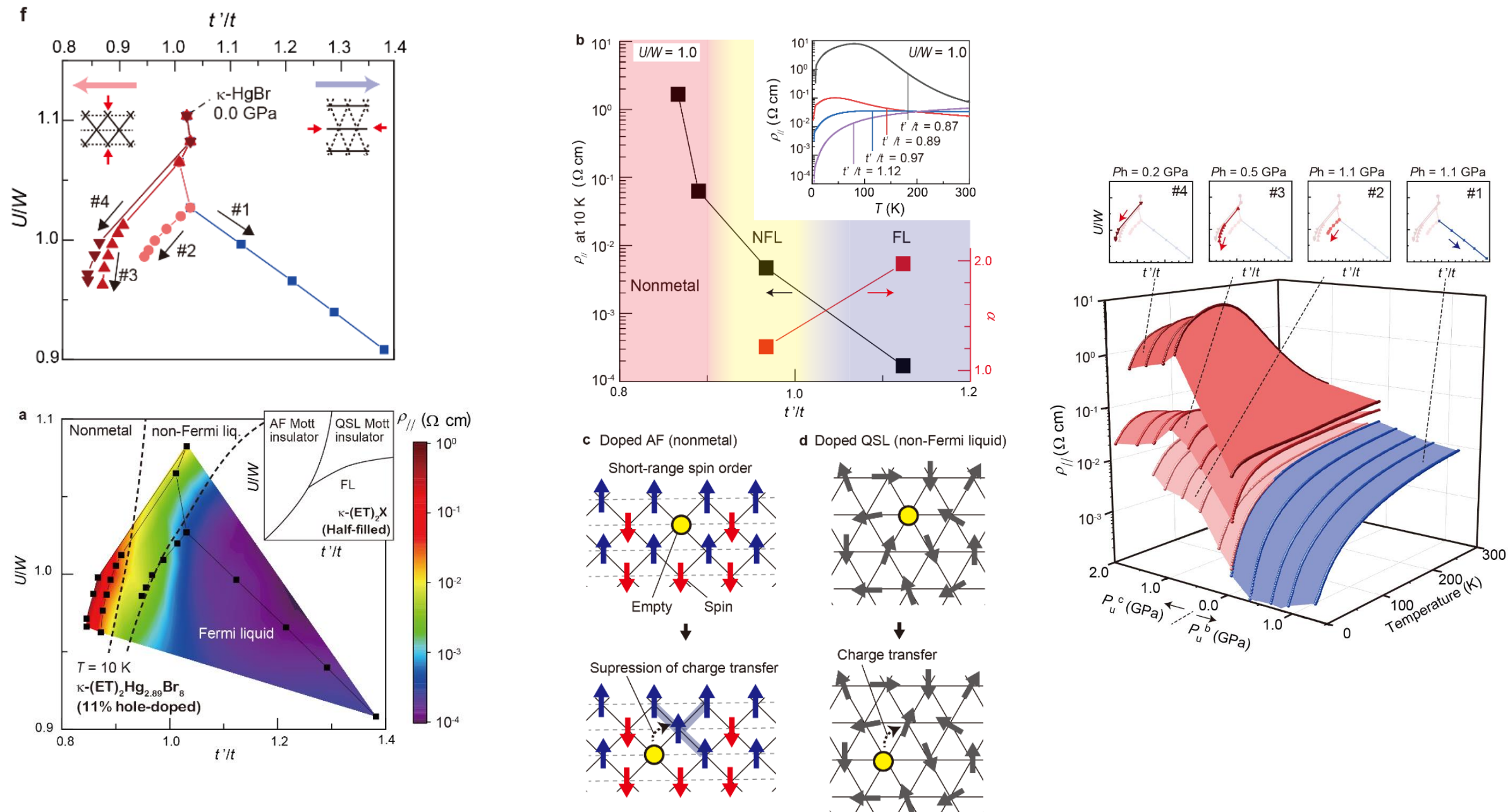


Spin-singlet nodal superconductivity ?



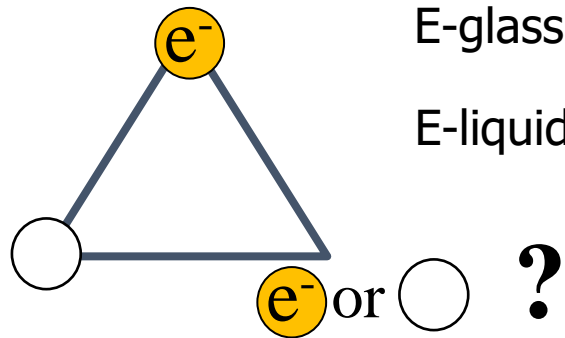
BEC-like pairing

# Combination of hydrostatic and uniaxial pressures: variations of $U/t$ and $t'/t$



# Electron (charge) glass

Quarter-filled band electrons  
on triangular lattice



Charge frustration

Electronic version of soft matters

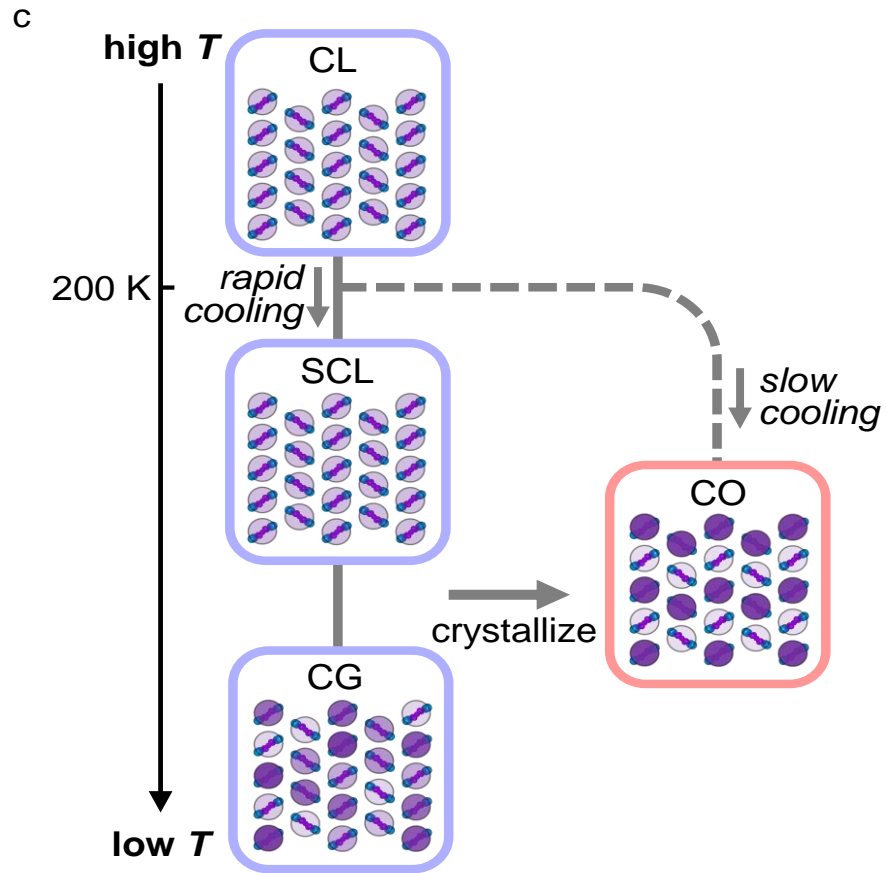
J. Schmalian<sup>1</sup> and P. G. Wolynes, PRL 85, 836 (2000)

**Self-Generated Randomness**

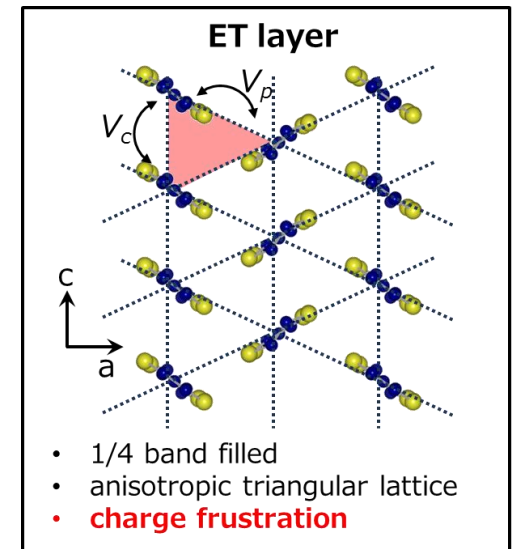
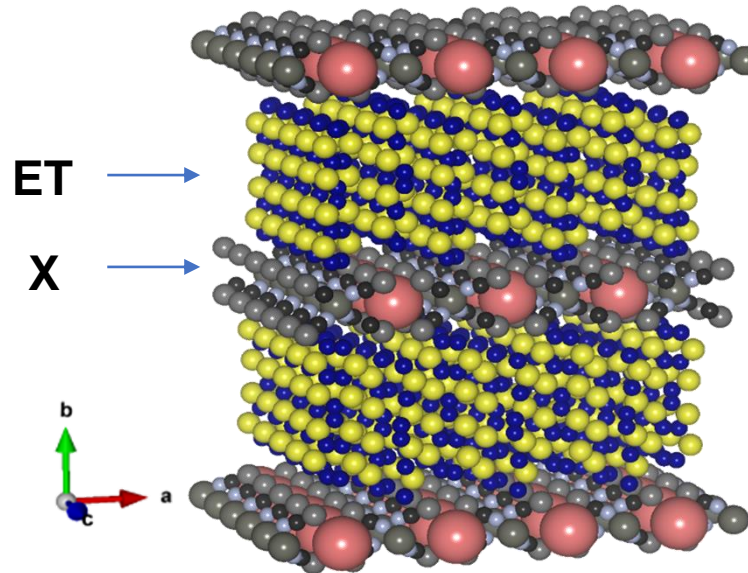
**Electronic mayonese**

# Electron glass

- ✓ Quantum nature
- ✓ Controllable lattice geometry



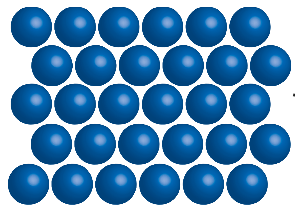
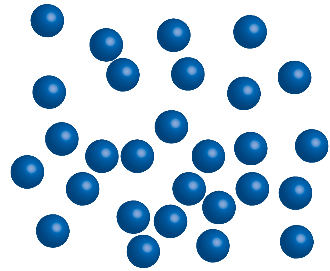
## Charge frustrated materials, $\theta$ -(ET)<sub>2</sub>X



# Non-Equilibrium in Supercooled Liquid

Frustration is a key to holding supercooled liquid and glass

Non-equilibrium



Volume

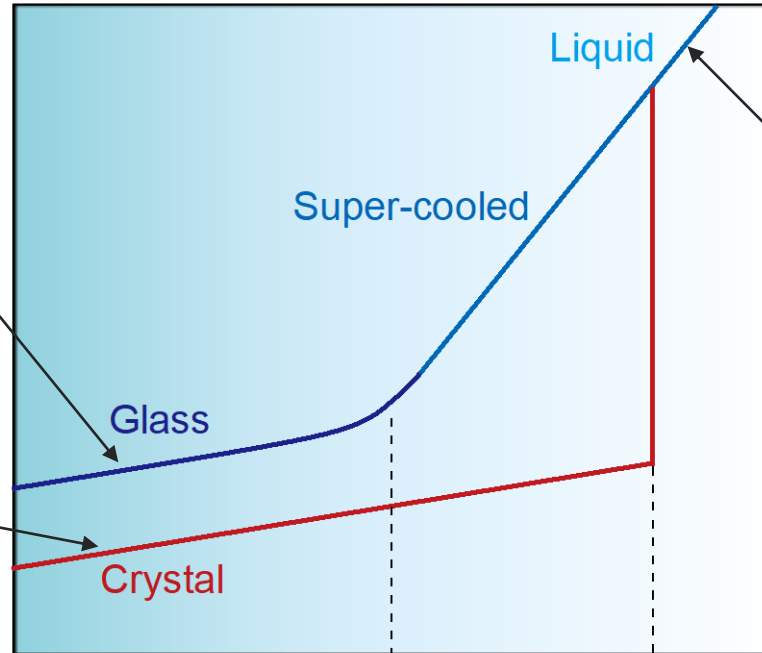
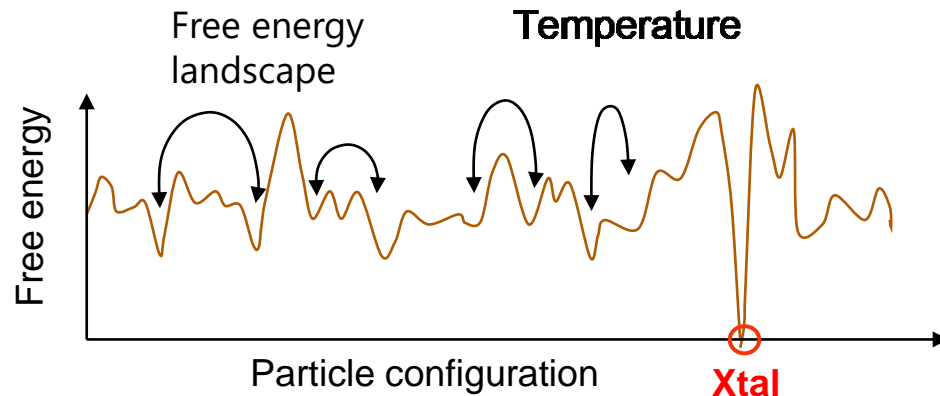
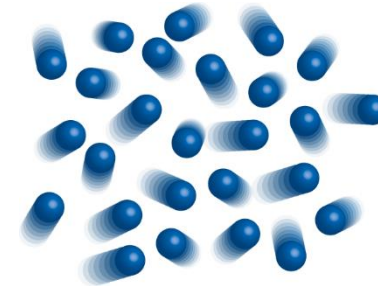


figure from  
Dobenedetti & Stillinger  
*Nature* 410, 259 (2001).

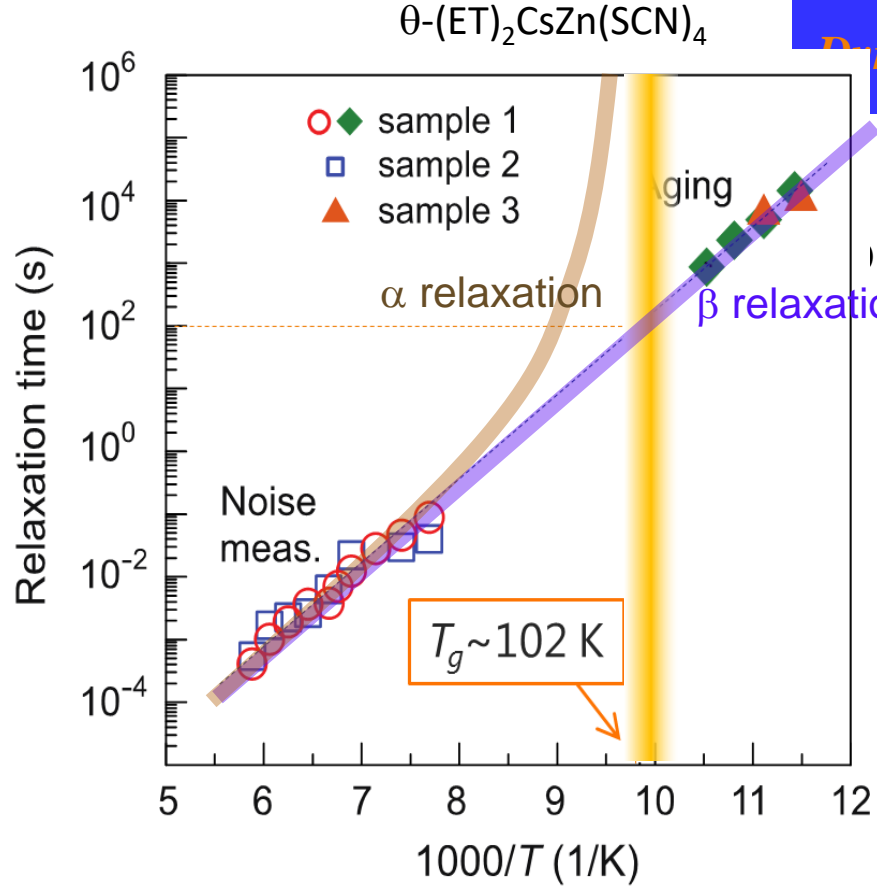


## Hallmarks of Glass

- Slow dynamics
- Non-equilibrium
- Short/middle-range correlation

# Hallmarks of Glass

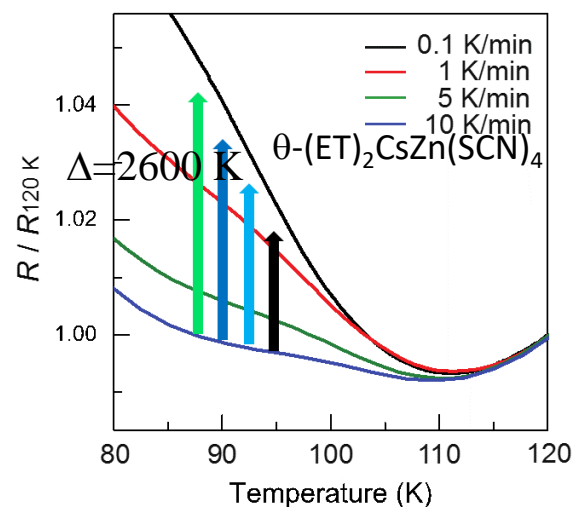
Kagawa *et al.*, *Nat. Phys.* **9**, 419 (2013).  
 Sato *et al.*, *PRB* **89**, 121102 (2014)  
 Sato *et al.*, *JPSJ* **83**, 083602 (2014)  
 Sato *et al.*, *JPSJ* **85**, 123702 (2016)



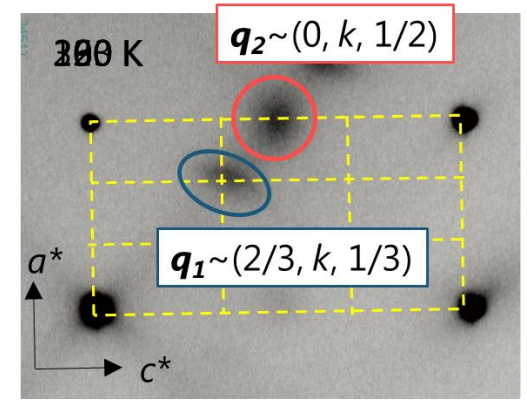
Non-equilibrium nature

middle-range correlation

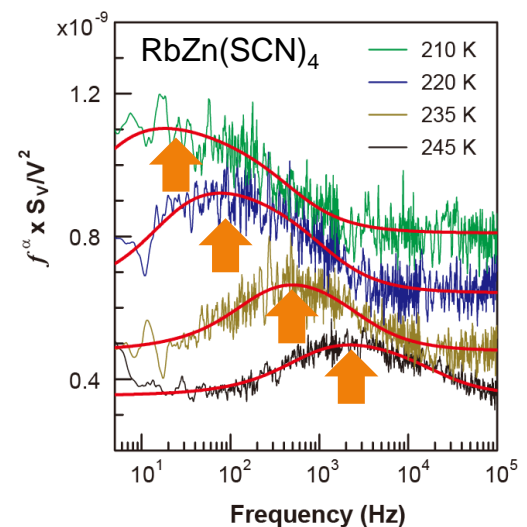
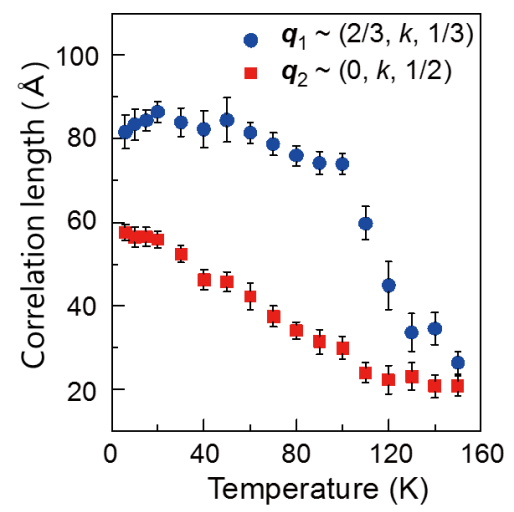
$\rho$  depends on cooling rate



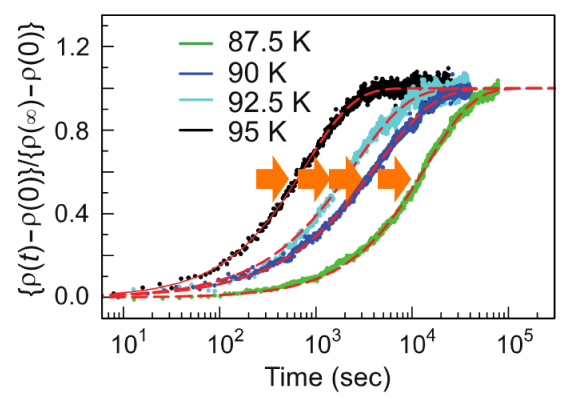
X-ray diffuse scattering



Correlation length levelling off



Aging

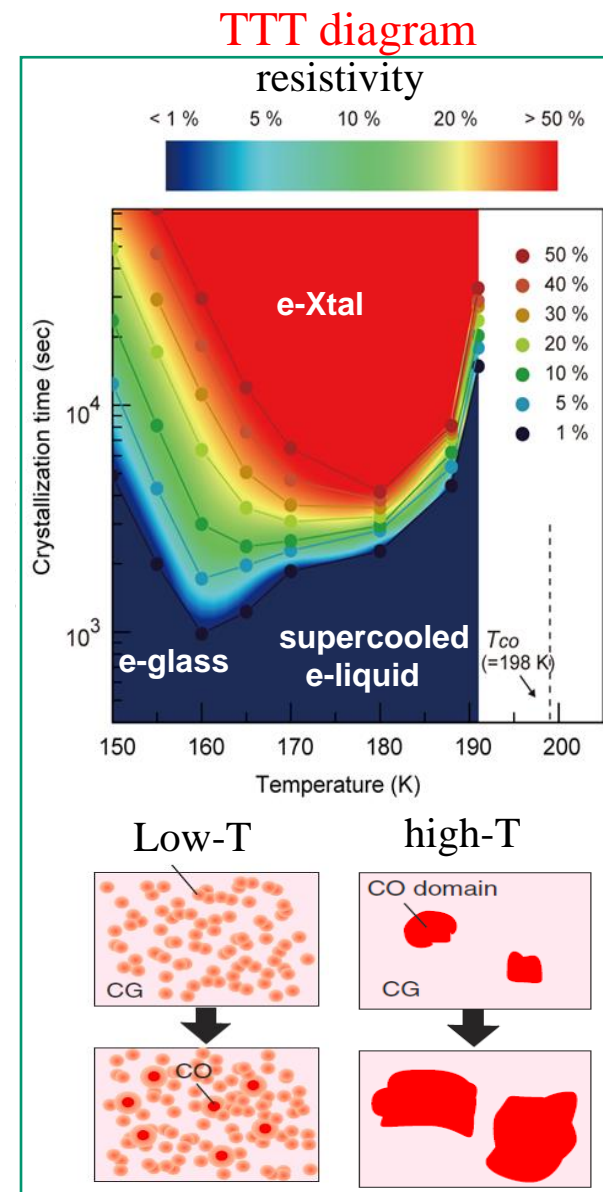
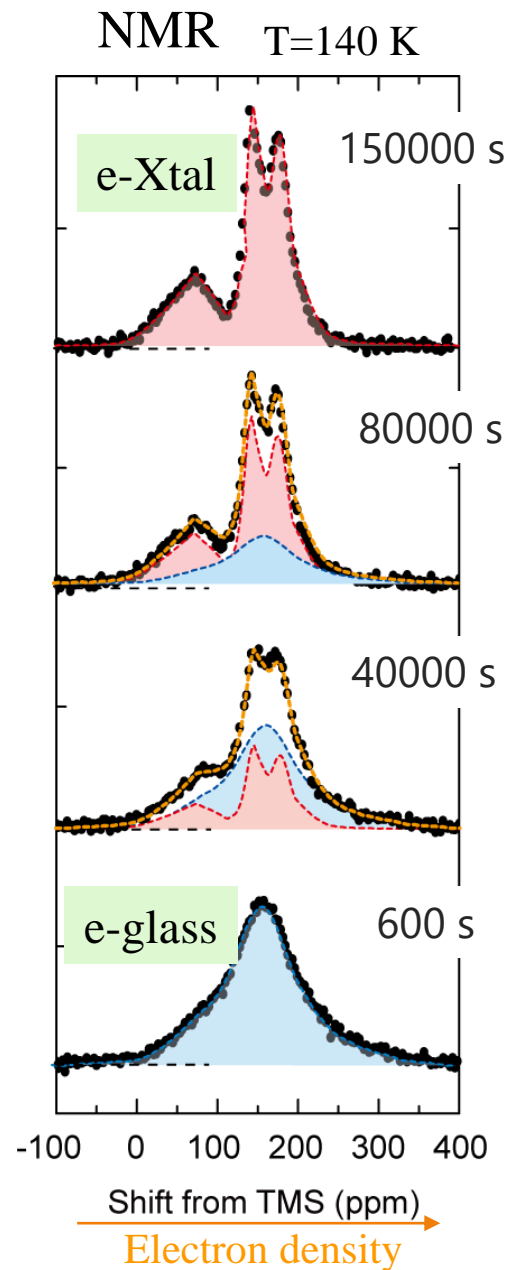
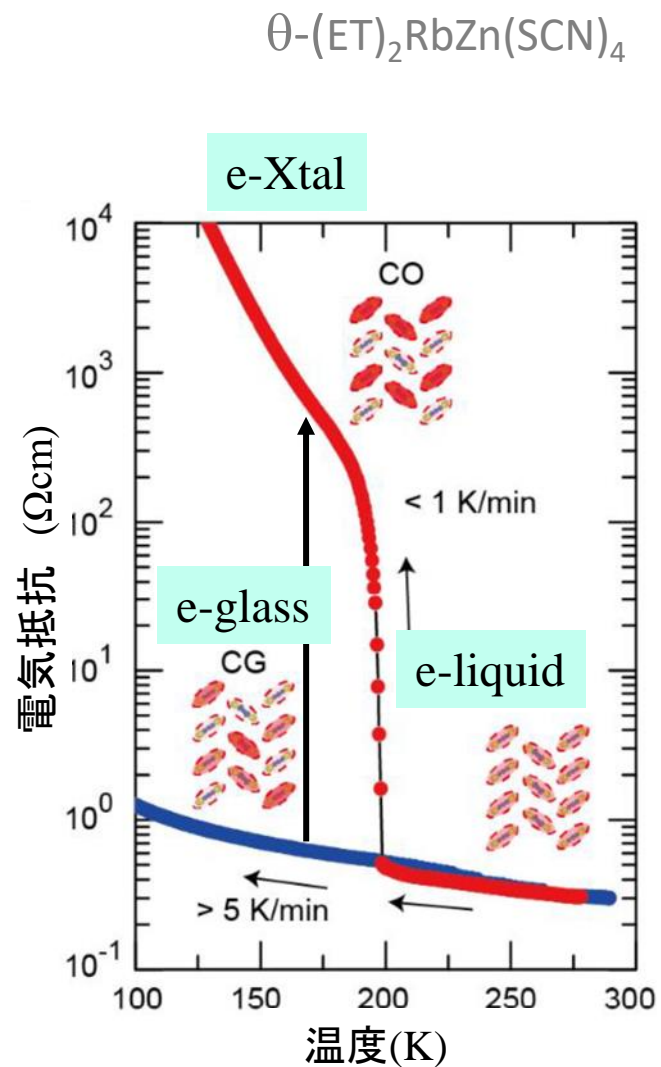




# Electronic crystallization: $\rho$ and NMR

*T. Sato et al., Science 357, 1378 (2017)*

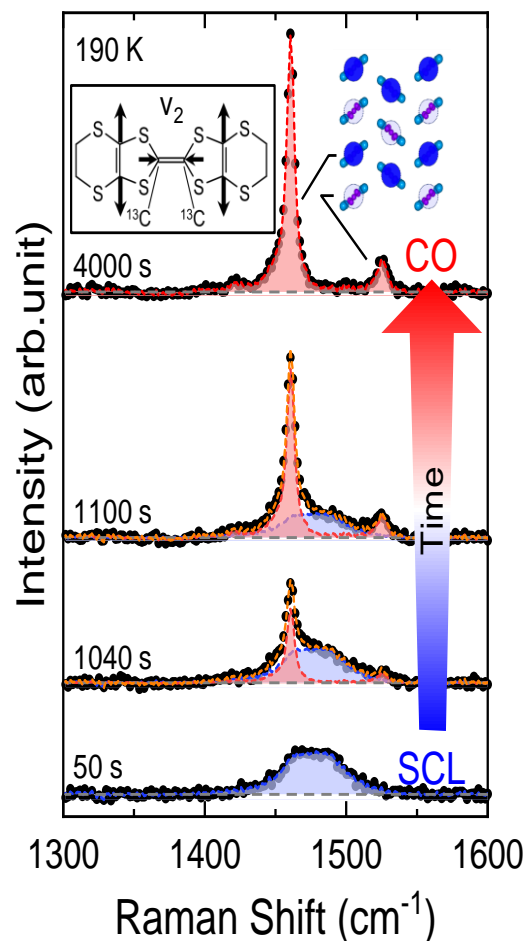
(*cf. S. Sasaki et al., Science 357, 1381 (2017)*)



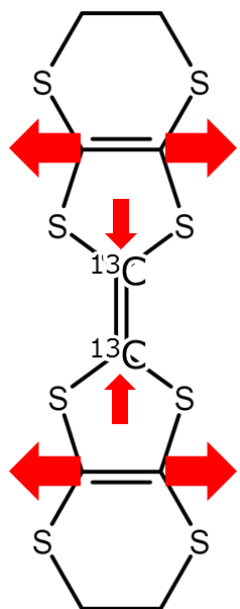
# Electronic crystallization: Raman spectroscopy



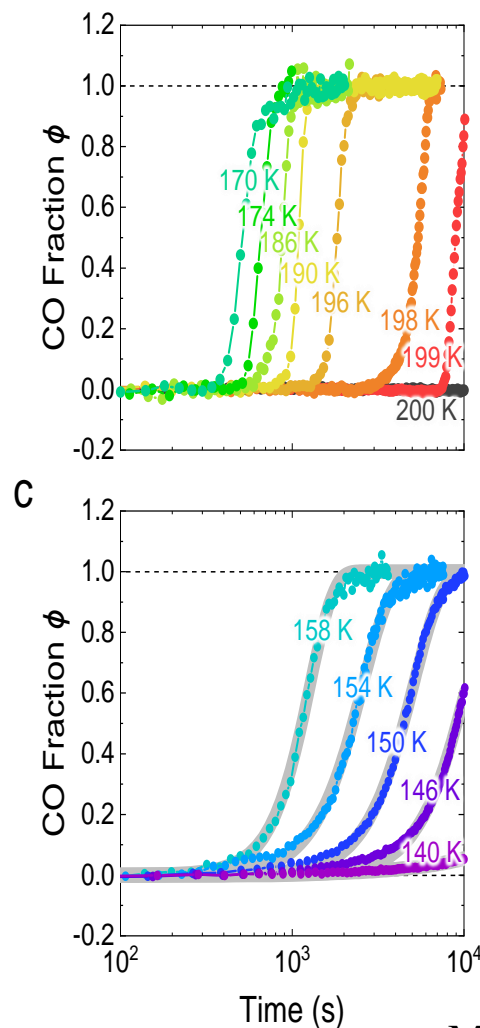
## Evolution of Raman spectrum during E-crystallization



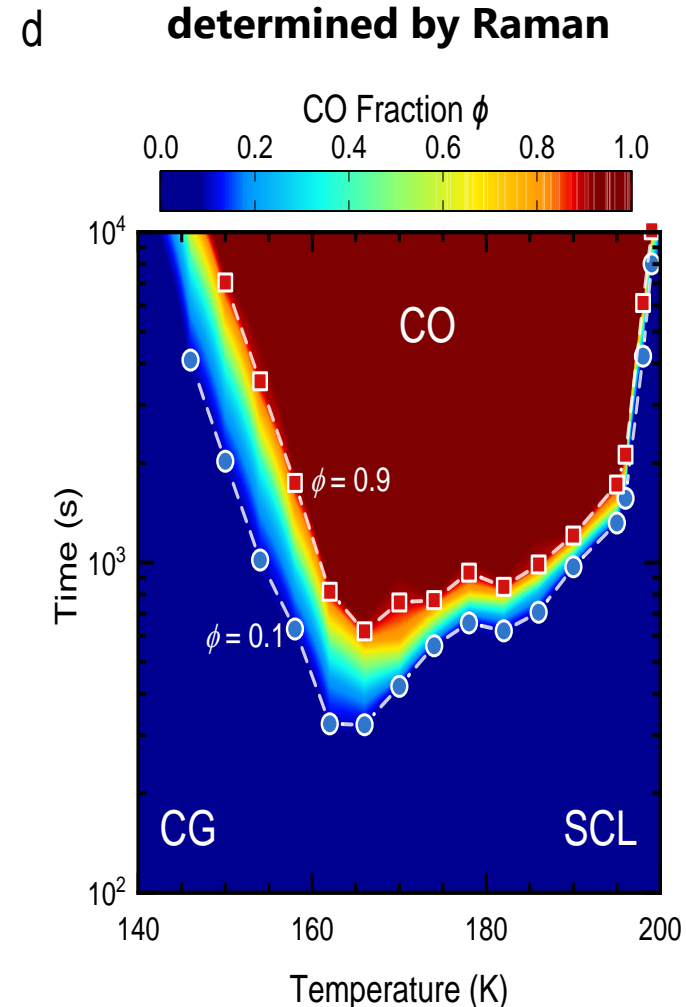
## Charge-sensitive $v_2$ mode



## Time evolution of E-Xtal fraction



## TTT diagram determined by Raman



# Raman imaging of E-crystallization at high T

村瀬、荒井、平川

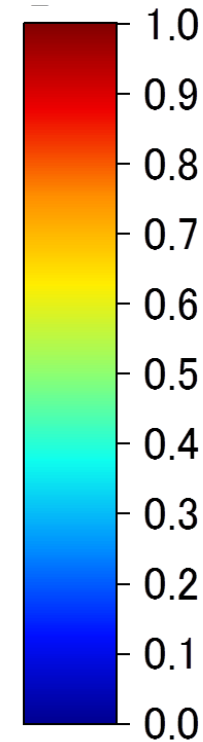
$$T_q = 195 \text{ K}$$

150 s interval  
 $6.5 \times 6.5 \mu\text{m}^2/\text{pixel}$

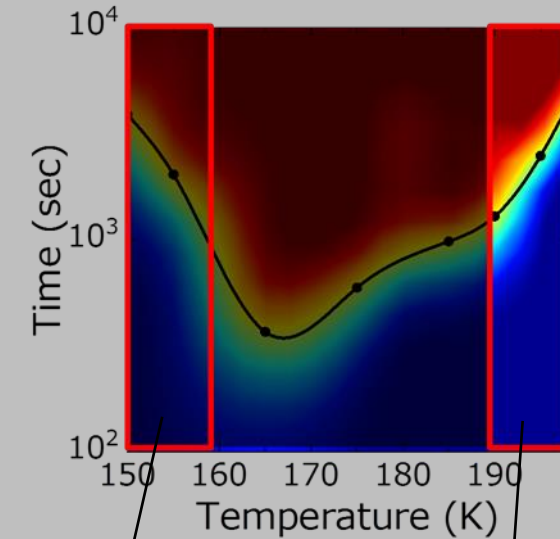
  
20  $\mu\text{m}$



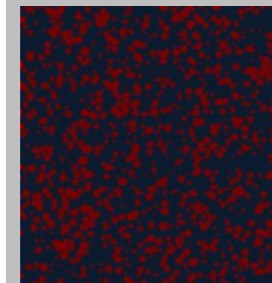
Fraction  
of Xtal



**Macroscopically  
inhomogeneous**

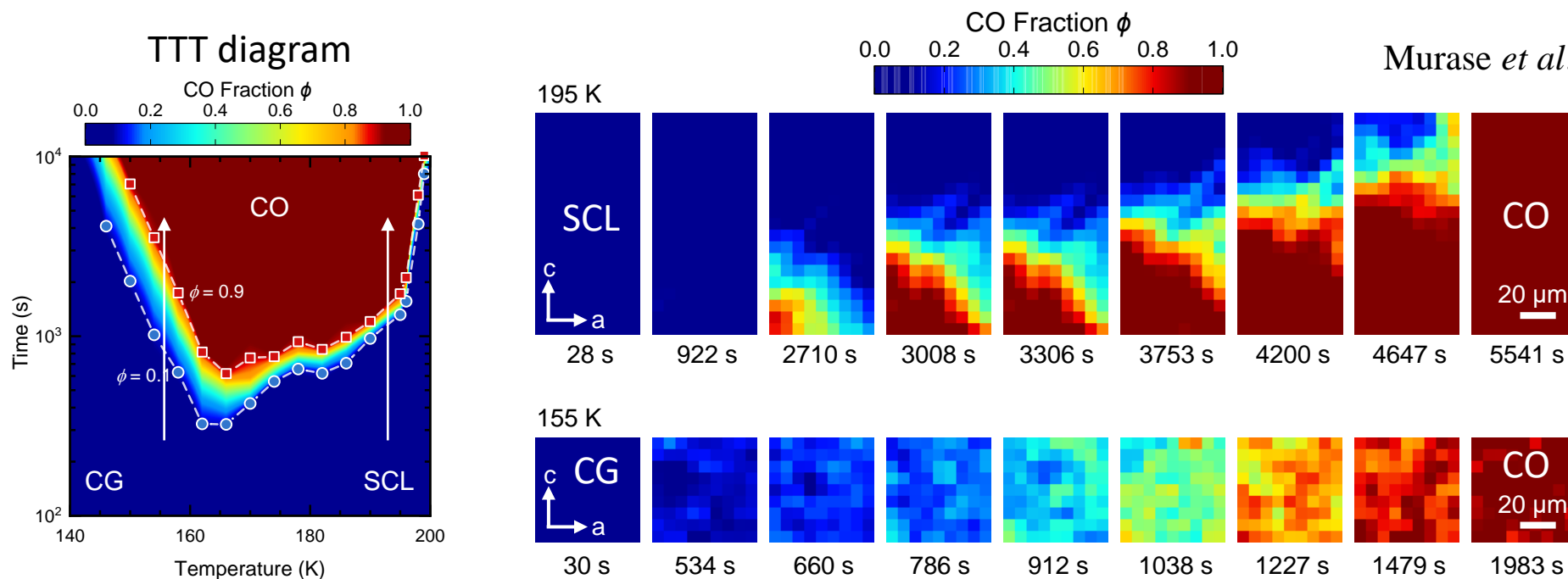


Expected  
spatial profile

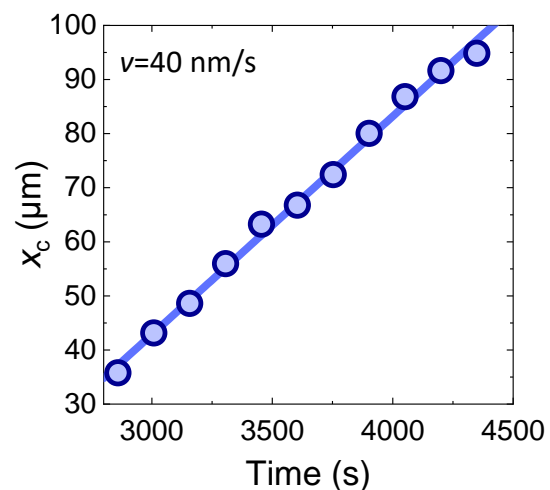
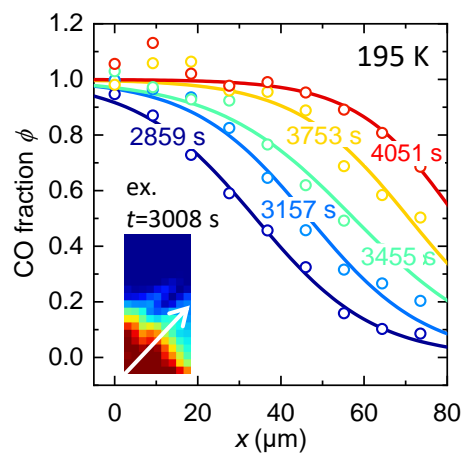


# Spaciotemporal observation of electronic crystallization: classical glass

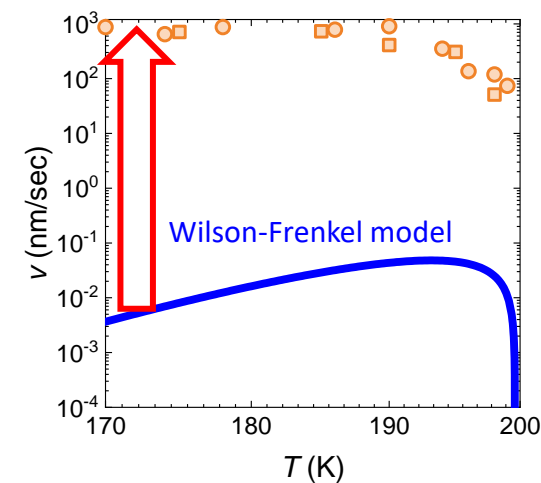
Murase *et al.*, arXiv:2201.04855



## Ultrafast crystal growth: quantum effect ?



**five orders of magnitude faster than expected in the classical model !**



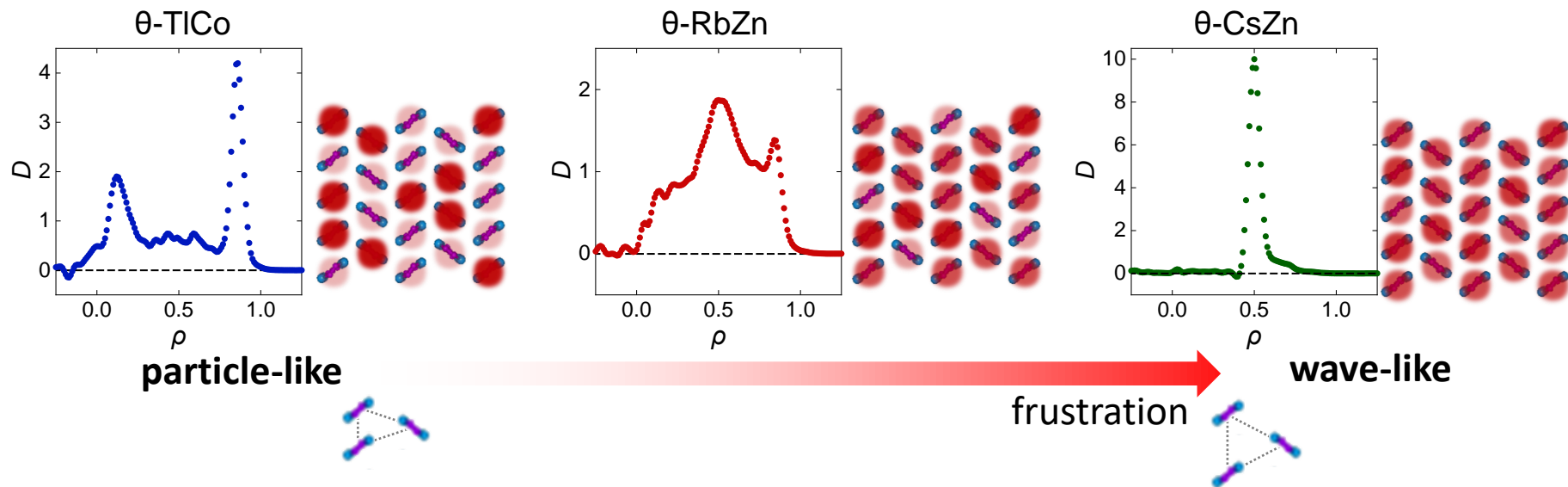
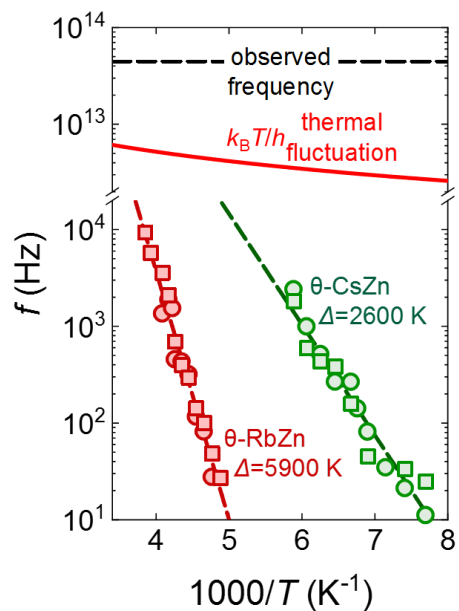
# From classical to quantum charge glass

Murase *et al.*, unpublished

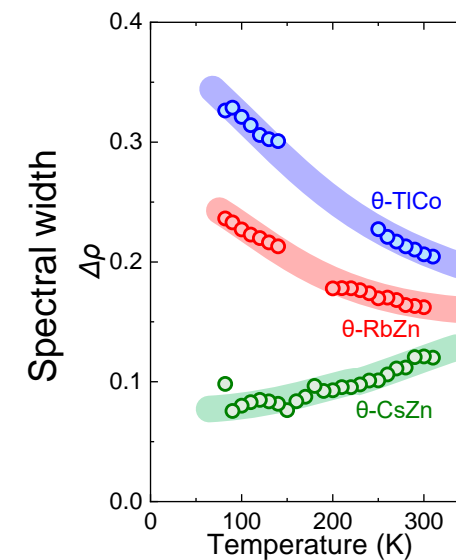
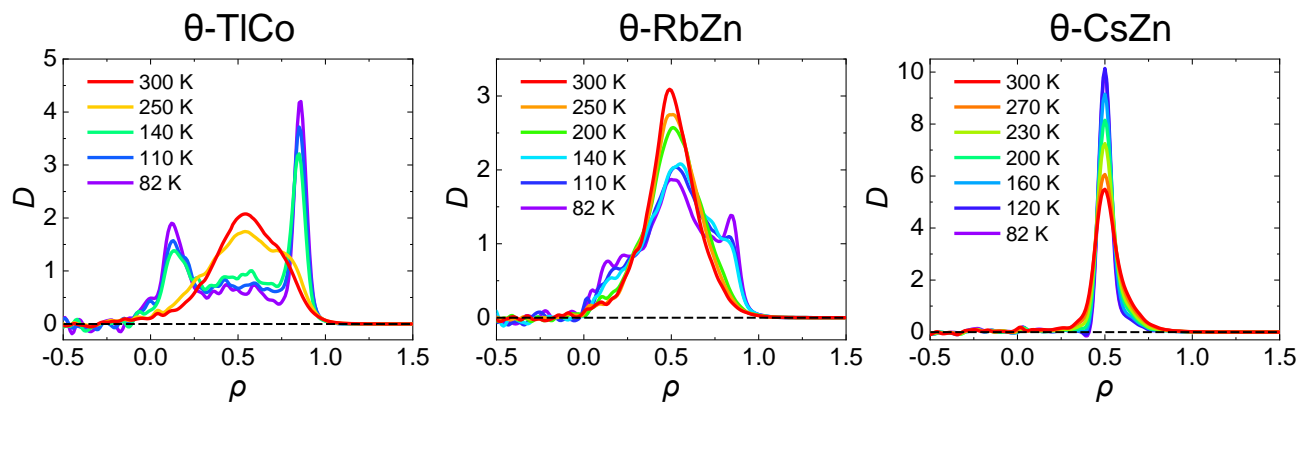
## Frustration dependence of charge density in CG at 82 K

### Observation time scale

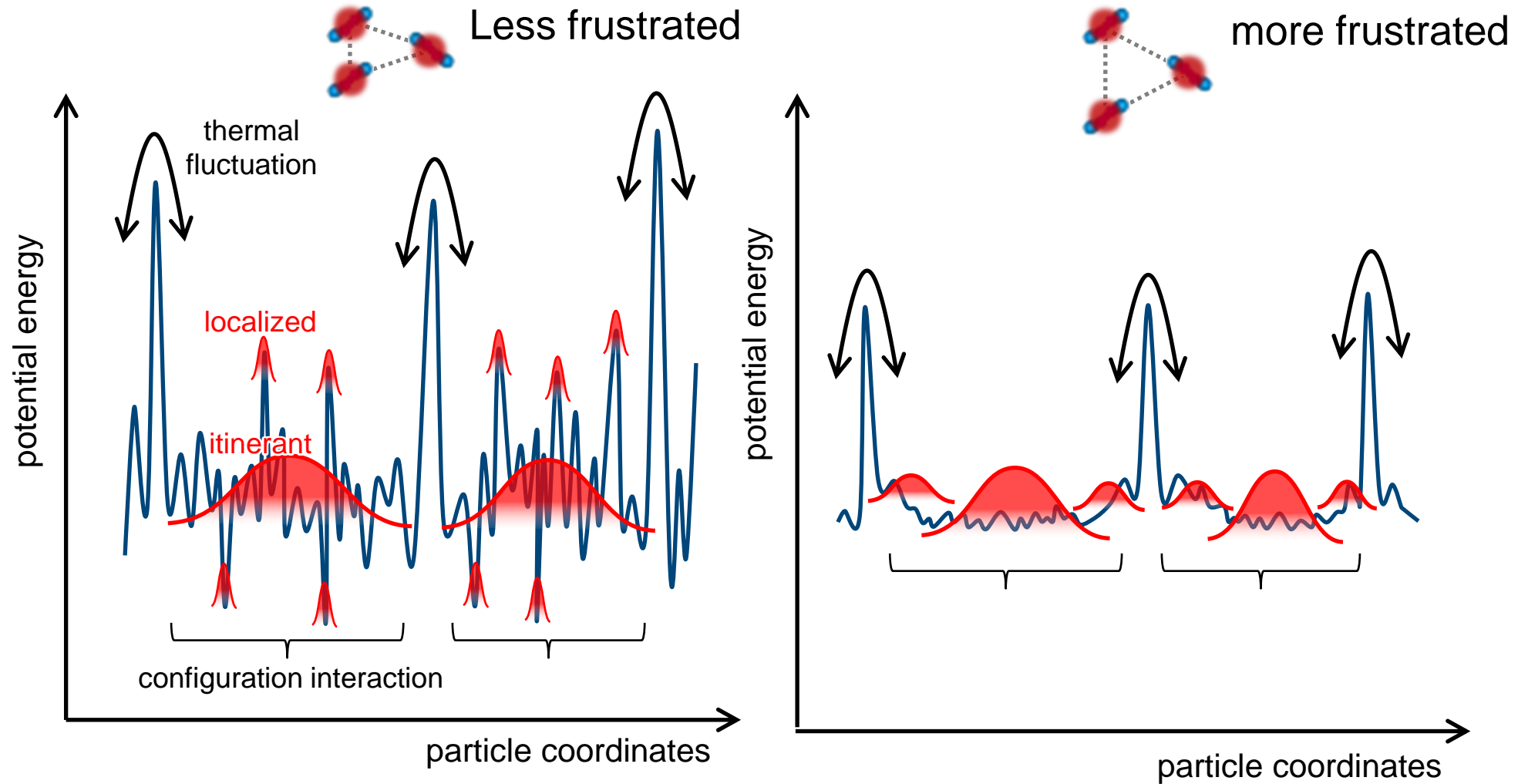
$$f_{\text{obs}} \gg f_{\text{thermal}} \gg \gg f_{\text{glass}}$$



## Temperature dependence of charge density



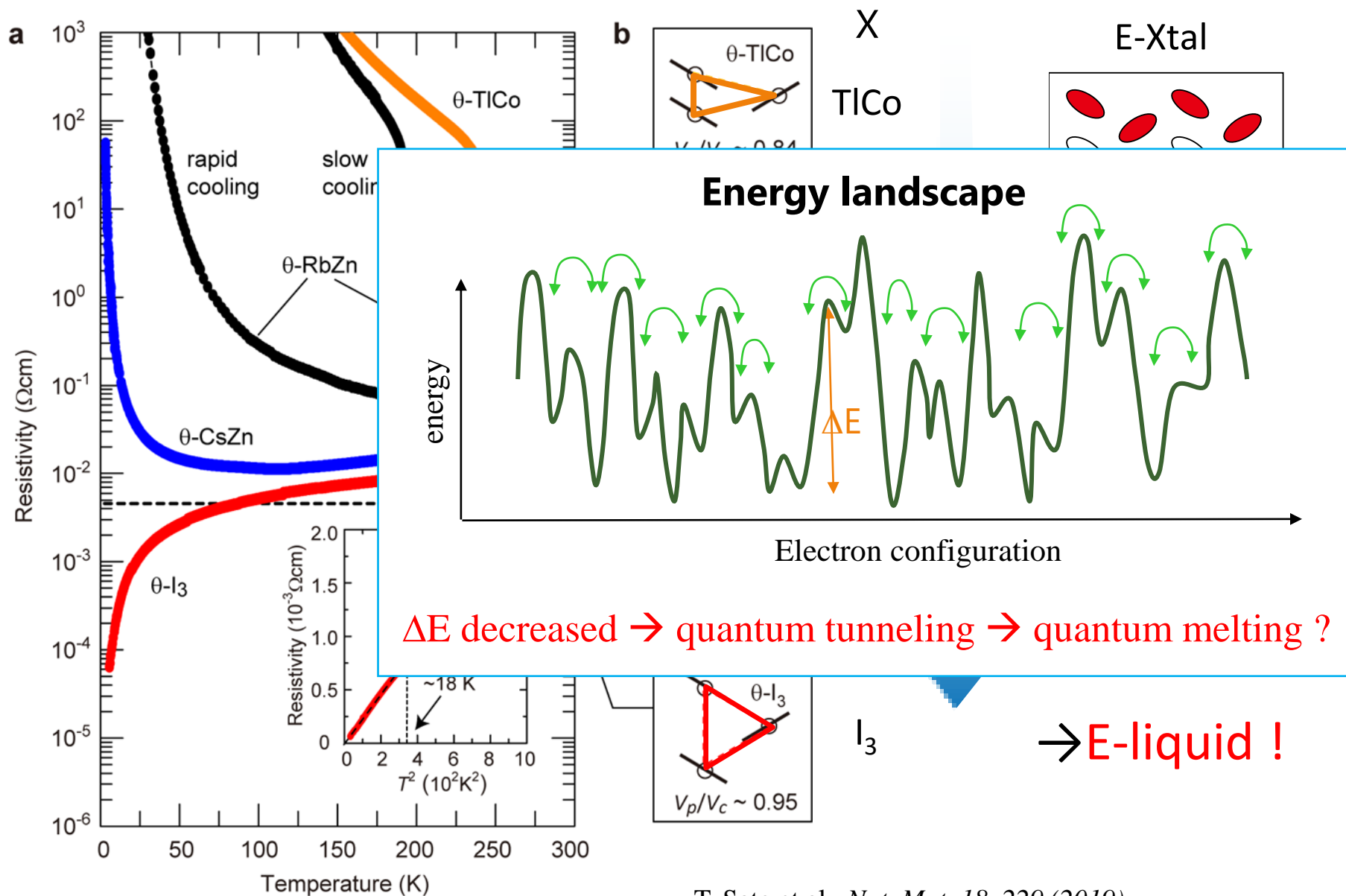
# Discussion | Energy landscape



**Classical glass**

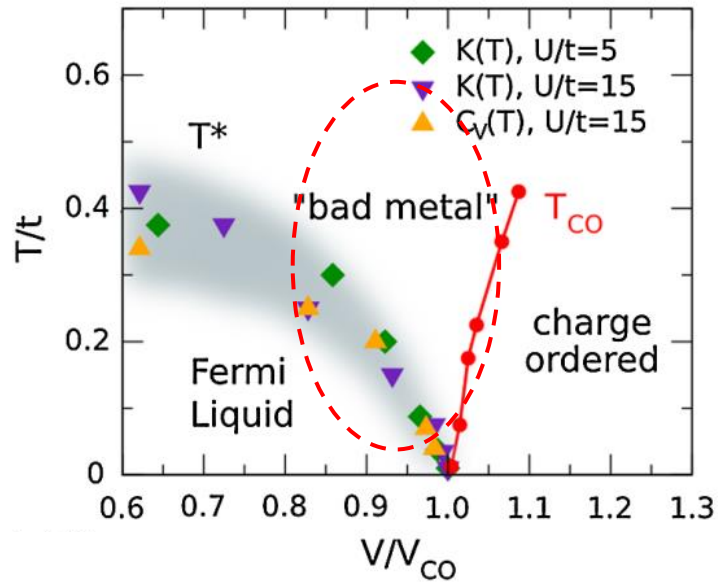
**Quantum glass**

# Possible quantum melting of E-glass

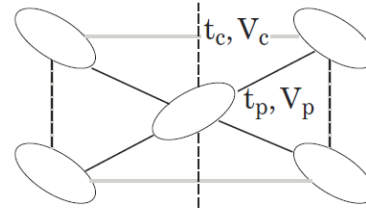


# Strange metal arising from frustration-driven charge instability

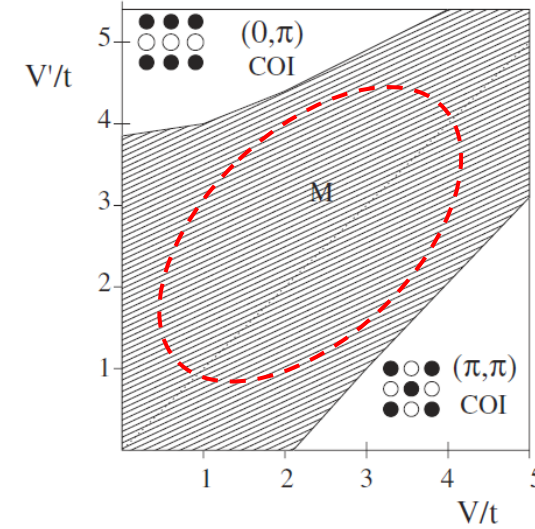
L. Cano-Cortes, et al, PRL **105**, 036405 (2010)  
PRB **84**, 155115 (2011)



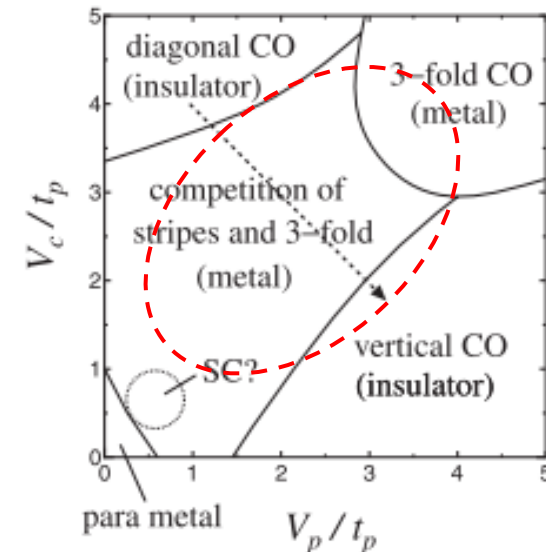
theoretical



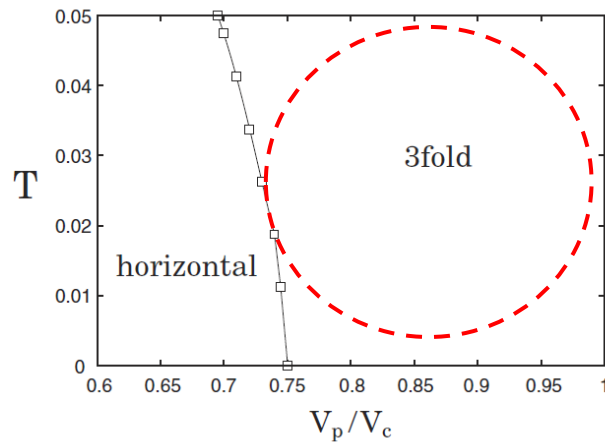
J. Merino et al, PR B **71**, 125111 (2005)



H. Watanabe, et al, JPSJ (2006)



Y. Tanaka & K. Yonemitsu JPSJ (2007)





# Diverse electronic states spring from a single molecular species, ET, only by changing its arrangement

## Massless Dirac electrons

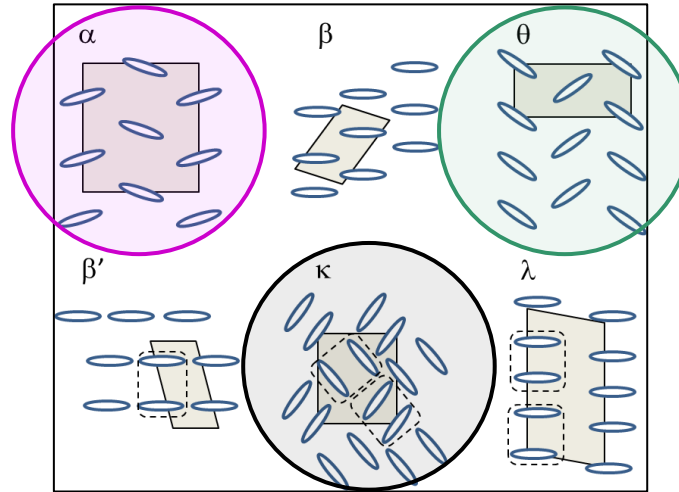
Dirac cone reshaping  
Unusual spin correlation  
Dynamic mass generation

Particle physics

## Electronic Xtal/glass

Non-equilibrium  
Slow dynamics  
Crystal growth  
Quantum glass

Soft matter physics



## Mott physics

Quantum Mott criticality  
Preformed Cooper pairs  
Spin liquid  
BEC-BCS crossover