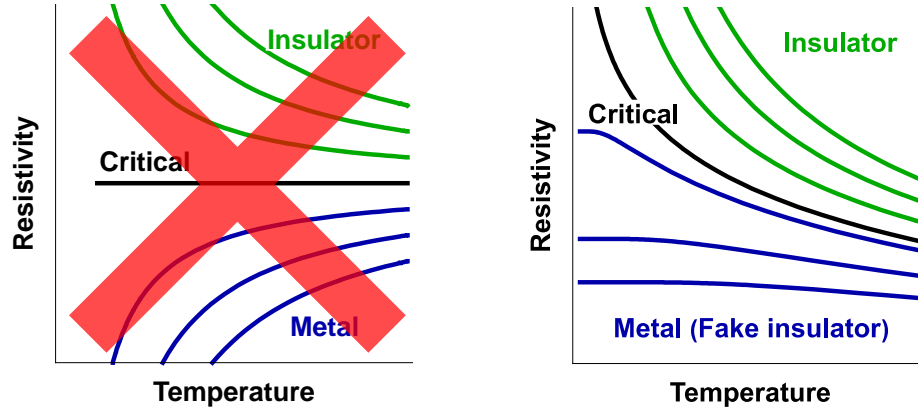


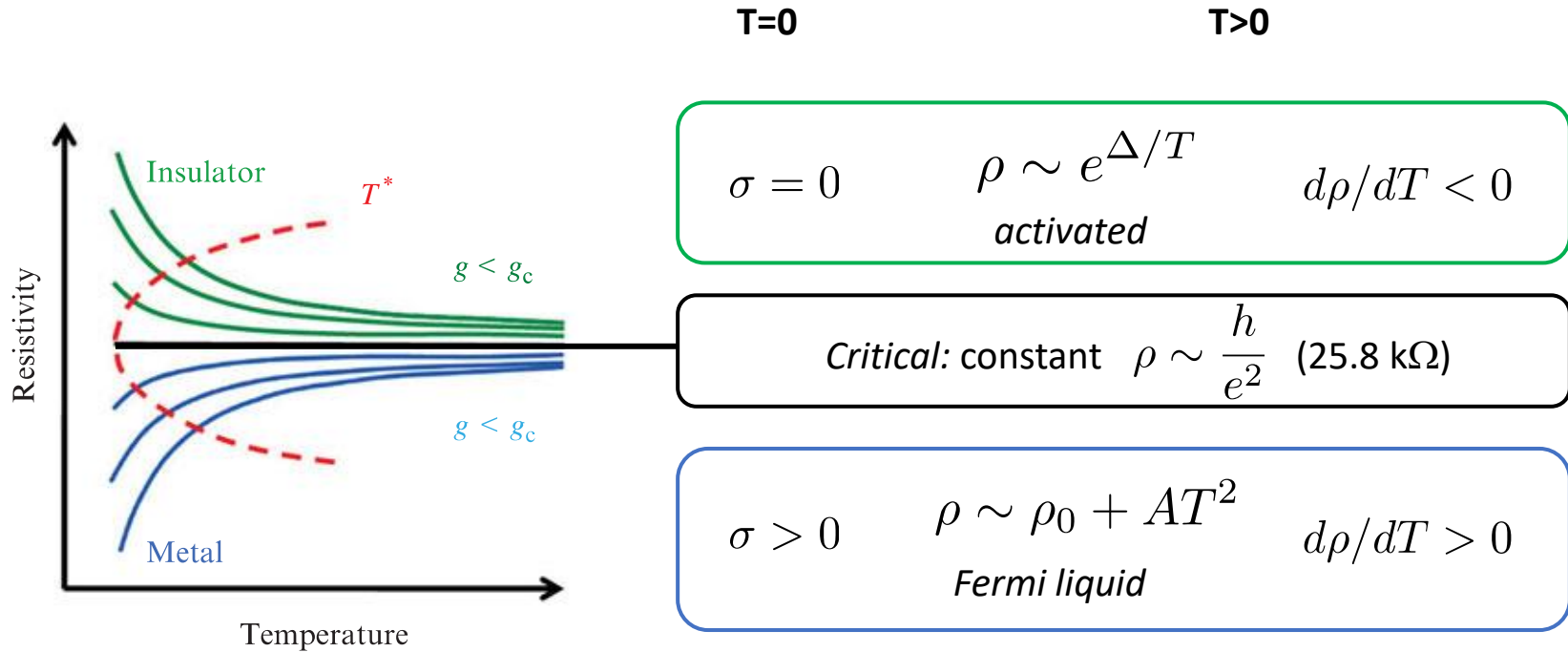
Fake Insulators



What are they, and how to spot them?

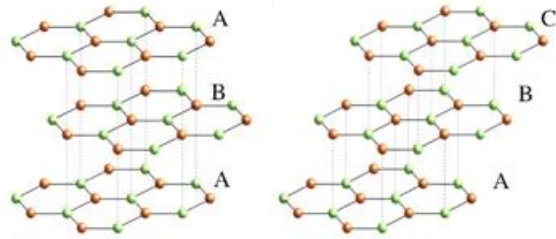
Louk Rademaker, SPICE, 26 May 2022

Metal vs. Insulator

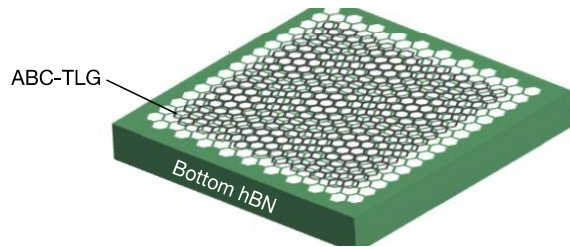


ABC Trilayer Graphene on hBN

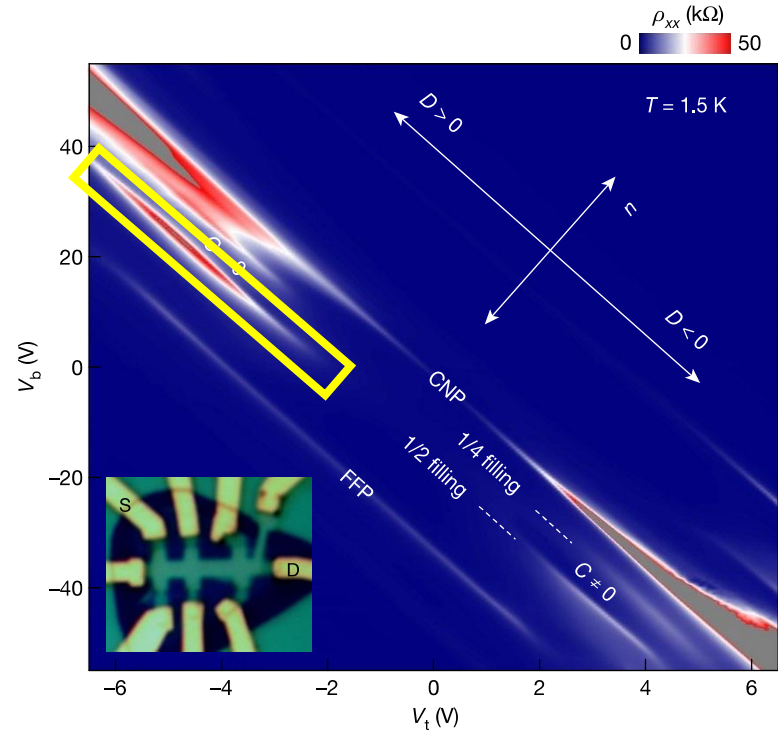
ABC trilayer graphene: k^3 dispersion



hBN substrate: flat moiré bands

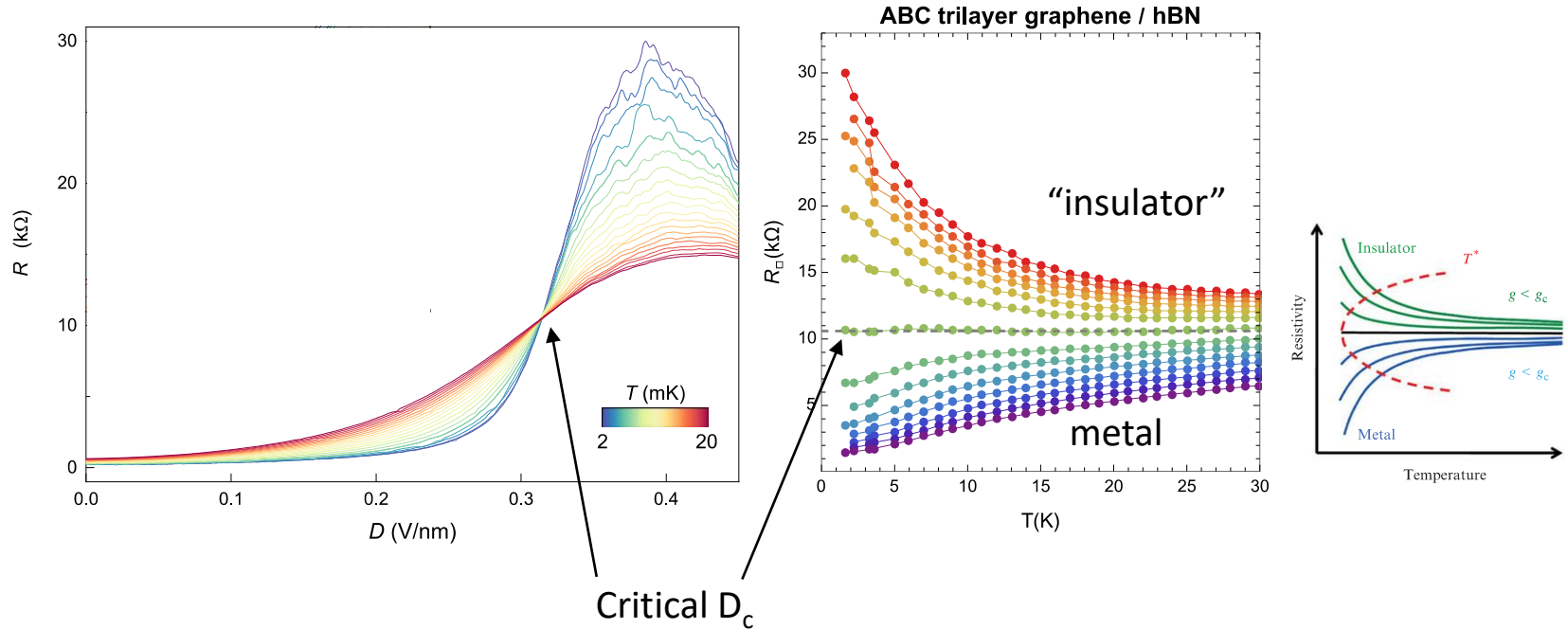


tune displacement field (D) & density (n)



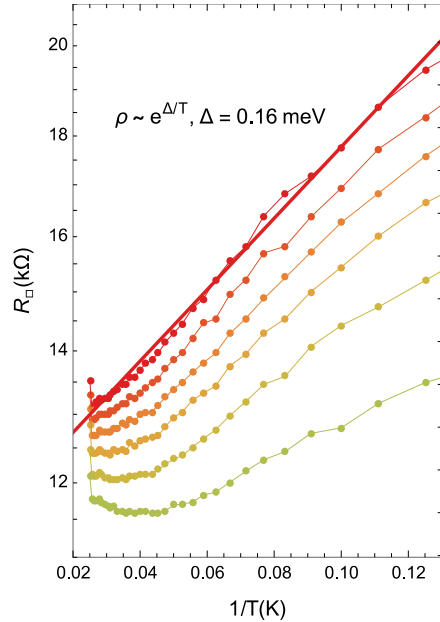
Metal-Insulator Transition

Resistivity as a function of **temperature** and **displacement field**

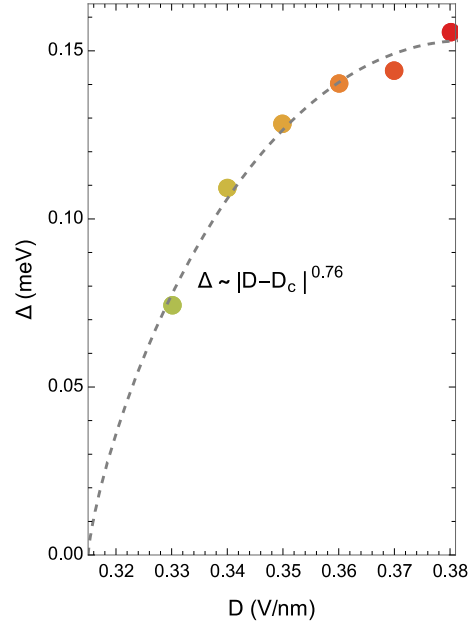


Insulator side

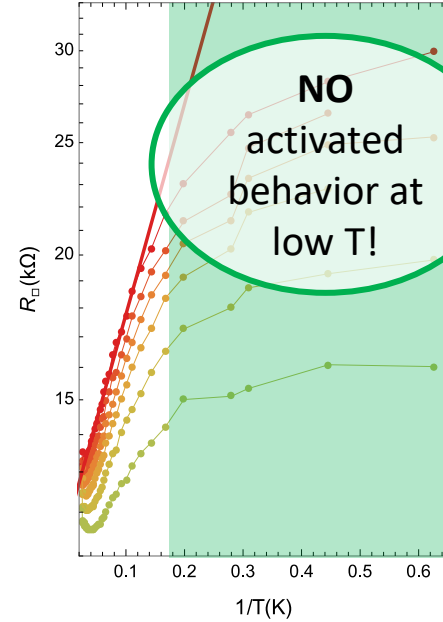
Arrhenius plot to extract insulating gap



Gap dependence on displacement field

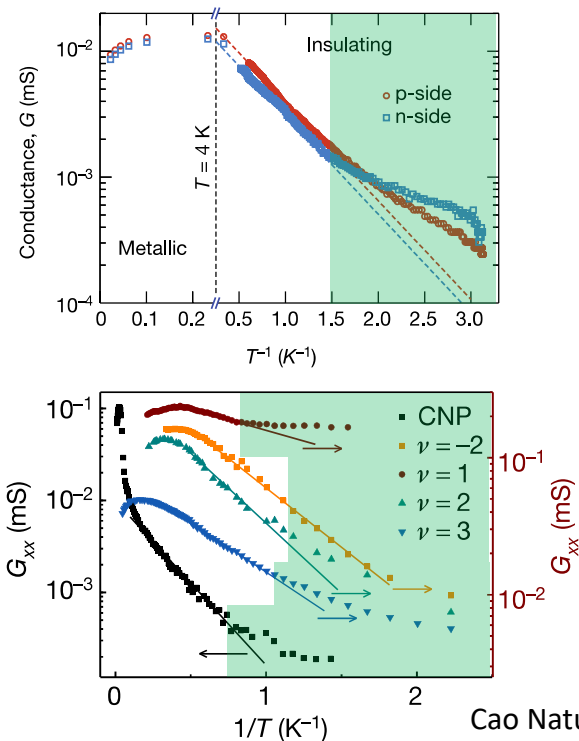


... but it's **WRONG!!**

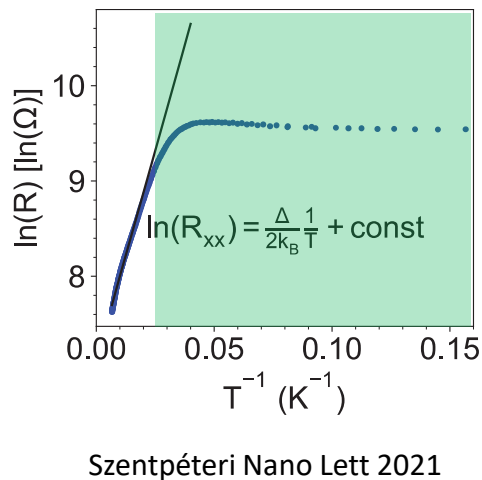


Fake insulators are everywhere

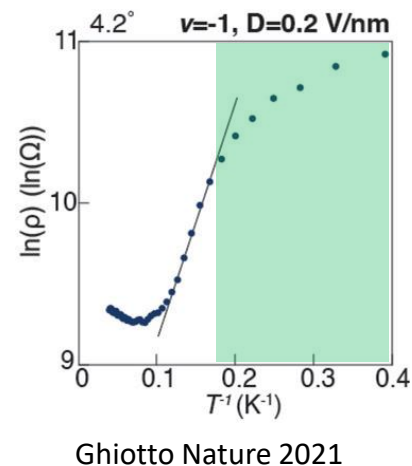
Twisted bilayer graphene



Twisted double bilayer graphene



Twisted bilayer WSe2



Band theory of MIT: Kubo formula

Kubo formula:
(w/o vertex)

$$\sigma = \frac{\pi}{2} \sum_{\alpha=x,y} \int \frac{d^2p}{(2\pi)^2} \int dz \text{Tr} \left[\underbrace{A(\mathbf{p}, z)}_{\text{Density of states}} \underbrace{\mathbf{j}_\alpha(\mathbf{p})}_{\text{Current operator}} \underbrace{A(\mathbf{p}, z') \mathbf{j}_\alpha(\mathbf{p})}_{\text{Density of states}} \right] \underbrace{\left(-\frac{\partial n_F(z)}{\partial z} \right)}_{\text{Fermi function}}$$

Apply to **band transition:**

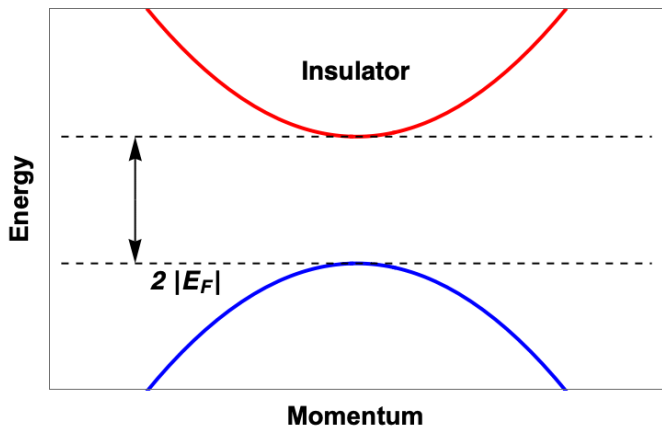
Density of states $A(\mathbf{p}, z) = \frac{1}{\pi} \frac{-\text{Im}\Sigma(z)}{(z - \xi_{\mathbf{p}})^2 + (\text{Im}\Sigma(z))^2}$

with **weak disorder** $-\text{Im}\Sigma(z) = 1/\tau$

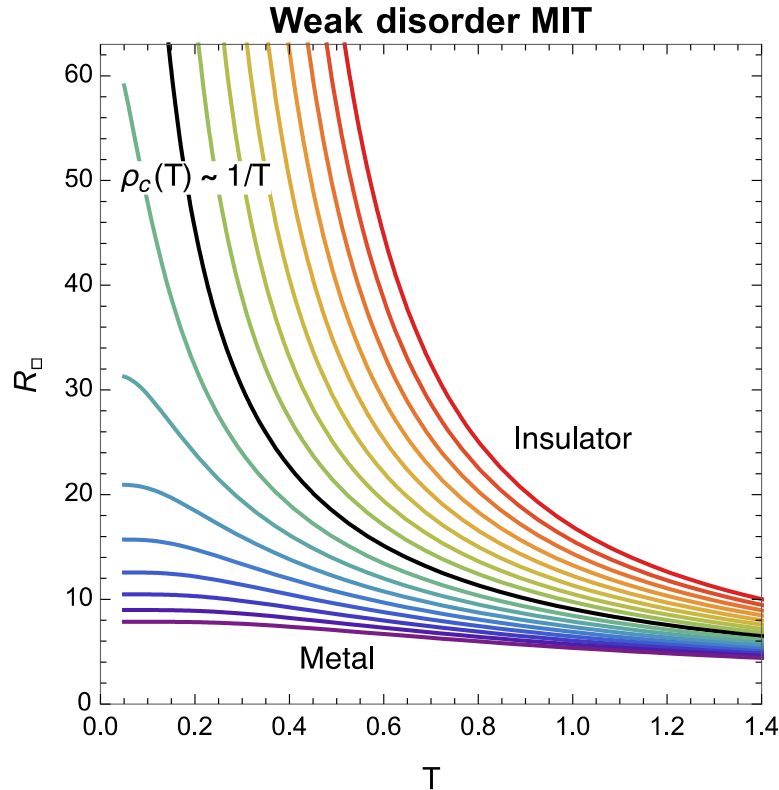
Drude formula

$$\sigma(T=0) = \frac{e^2 n \tau}{m}$$

Particle density
Scattering rate
Effective mass



Band theory of MIT: Exact Solution



$$\sigma(T) = \frac{e^2 \tau}{2\pi} T \left(\frac{E_F}{T} + \log \left[1 + e^{-\frac{E_F}{T}} \right] \right)$$

Insulator: activated

$$\rho \sim e^{|E_F|/T}$$

Critical: not constant

$$\rho_c \sim 1/T$$

Metal: negative slope!

$$d\rho/dT < 0$$

"fake insulator"

Band theory of MIT: Scaling

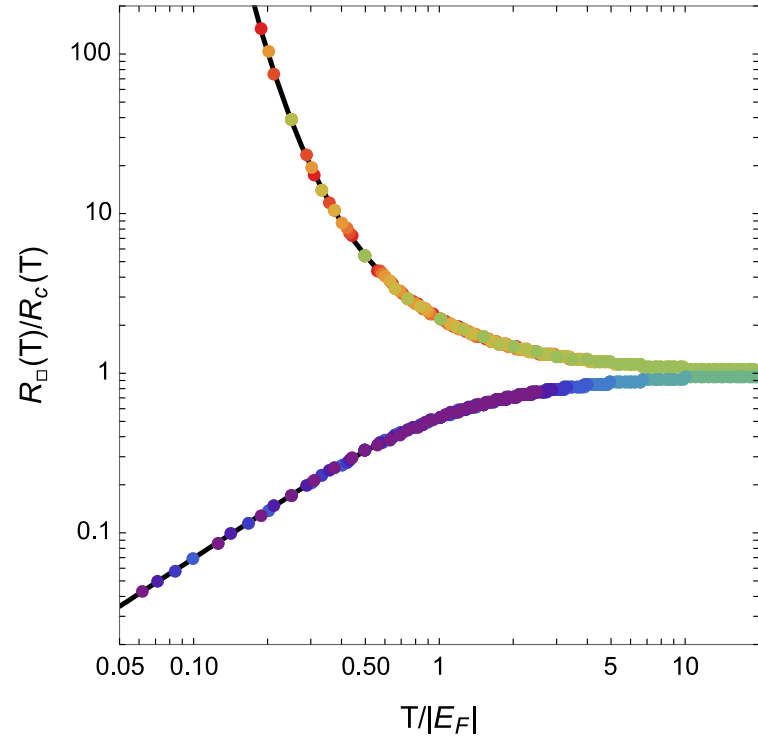
Exact solution

$$\sigma(T) = \frac{e^2 \tau}{2\pi} T \left(\frac{E_F}{T} + \log \left[1 + e^{-\frac{E_F}{T}} \right] \right)$$

has **scaling form**

$$\sigma(T) = T^\alpha f \left(\frac{E_F}{T} \right)$$

leading to **universal resistivity curves**
close to the metal-insulator transition

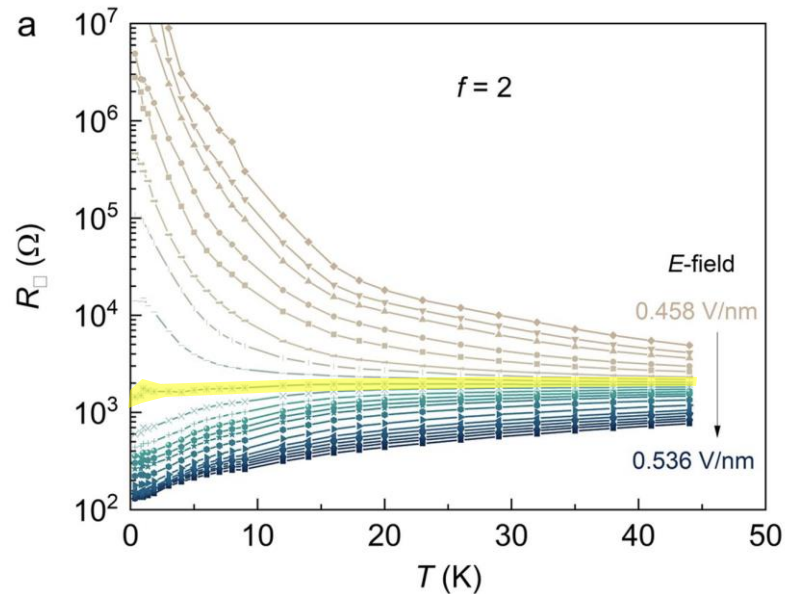
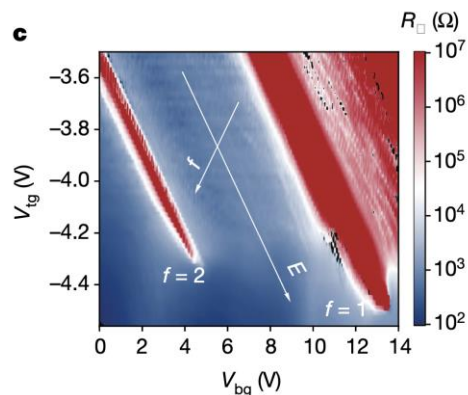
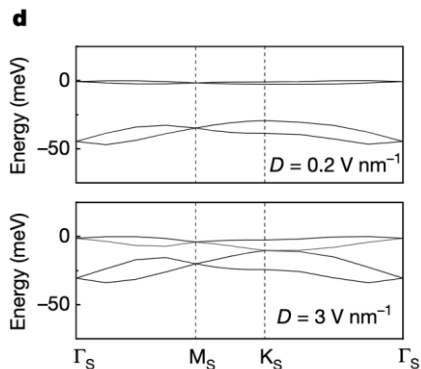


Application: MoTe₂/WSe₂



Aligned TMD heterobilayer
MoTe₂/WSe₂

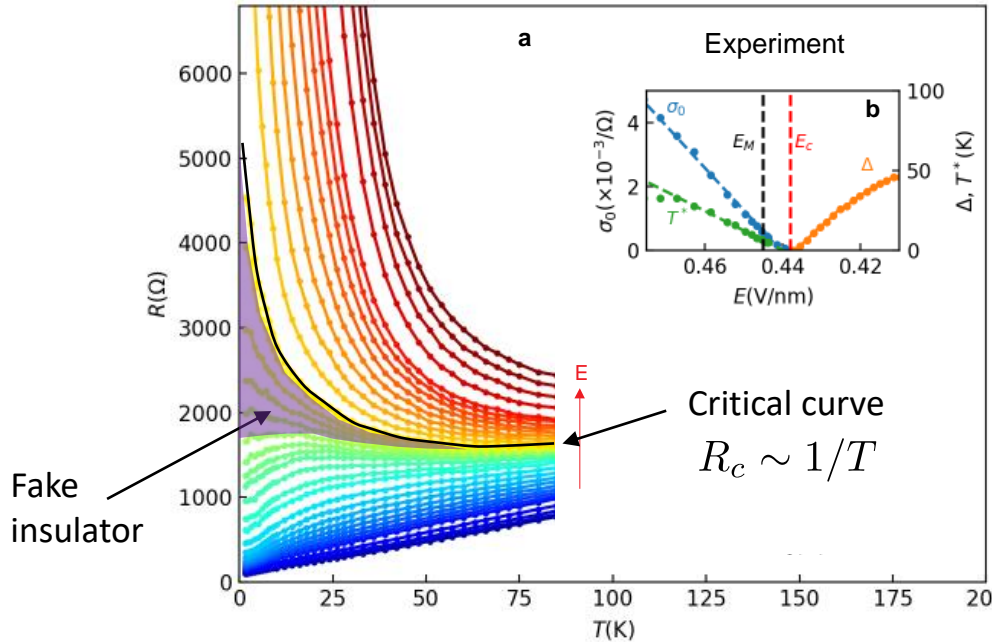
Bandwidth can be tuned by displacement field



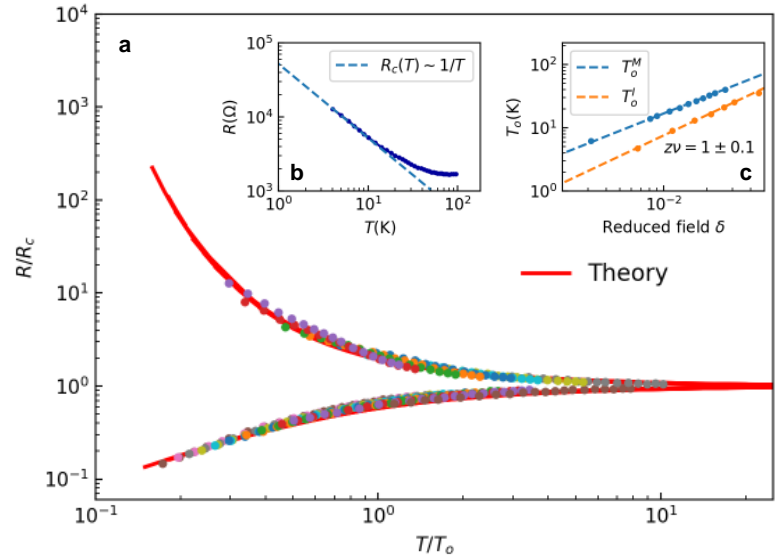
Extended Data Fig. 2 | Metal-insulator transition at $f=2$. a, Temperature dependence of square resistance at varying electric fields at $f=2$. MIT is observed near 0.49 V nm^{-1} . Compared to the MIT at $f=1$, strong effective mass

Scaling in MoTe₂/WSe₂

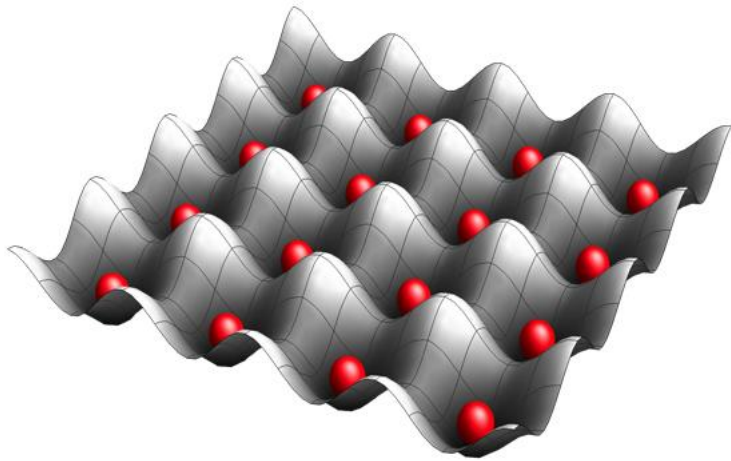
Extrapolating the zero-temperature conductivity and insulating gap gives critical D_c



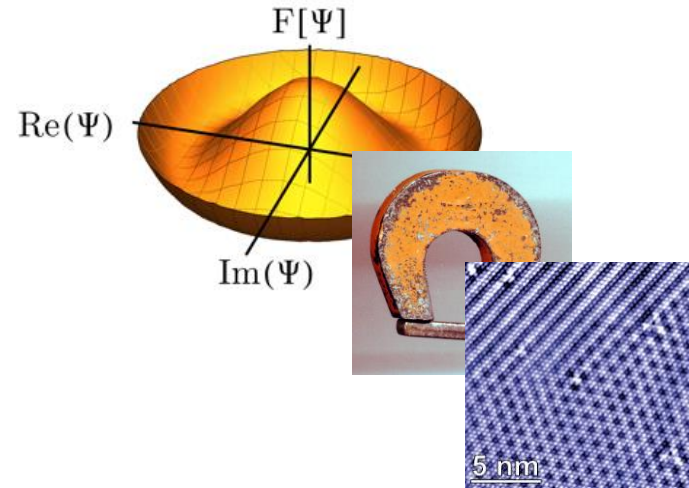
With **scaling** of the resistivity curves



Insulators at half-filling

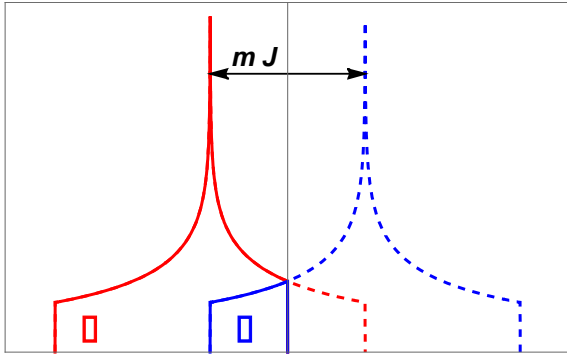


Mott insulator



Spontaneous Symmetry Breaking

Simplest example: Stoner ferromagnetism

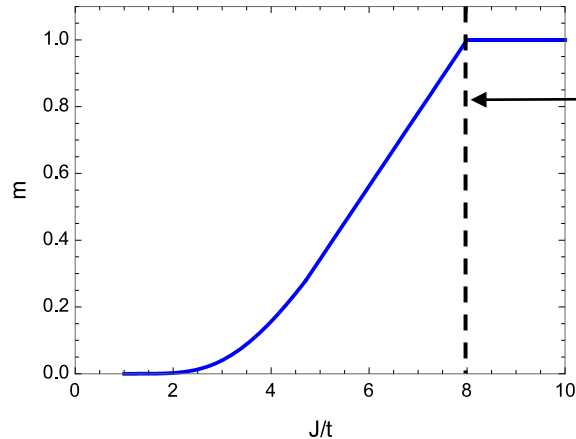


Ferromagnetic direct exchange $-J\vec{S} \cdot \vec{S}$

Spontaneous **polarization** shifts bands for up/down spins

Self-consistent Stoner **mean field theory**

$$m = n_{\uparrow} - n_{\downarrow} = \int d\omega A(\omega) \left[n_F(\omega - \frac{1}{2}mJ) - n_F(\omega + \frac{1}{2}mJ) \right]$$

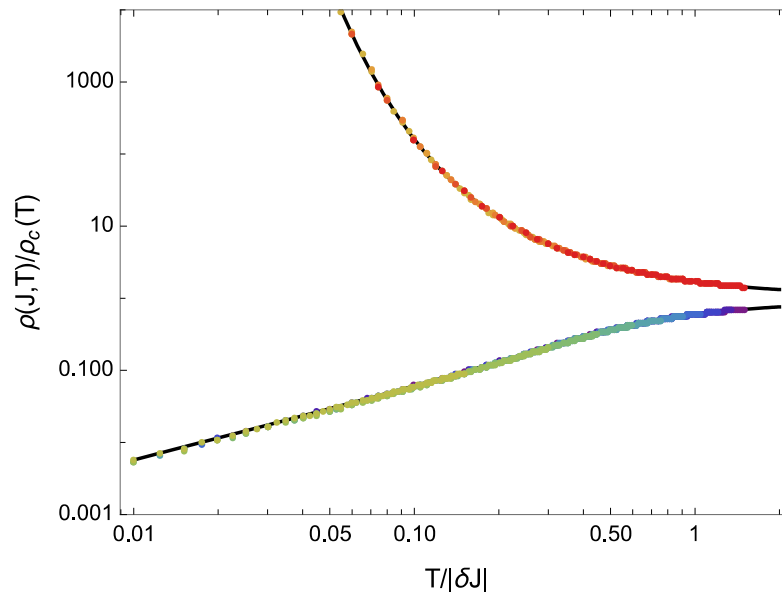
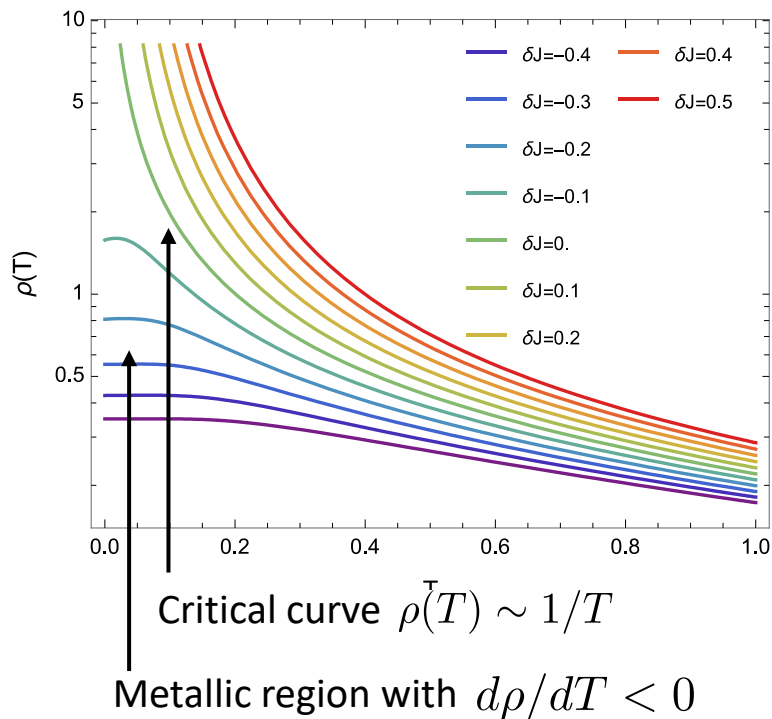


Metal-insulator transition when $mJ = W$ (bandwidth)

from *itinerant partially polarized* ferromagnet
to *insulating fully polarized* ferromagnet

Resistivity scaling near SSB-MIT

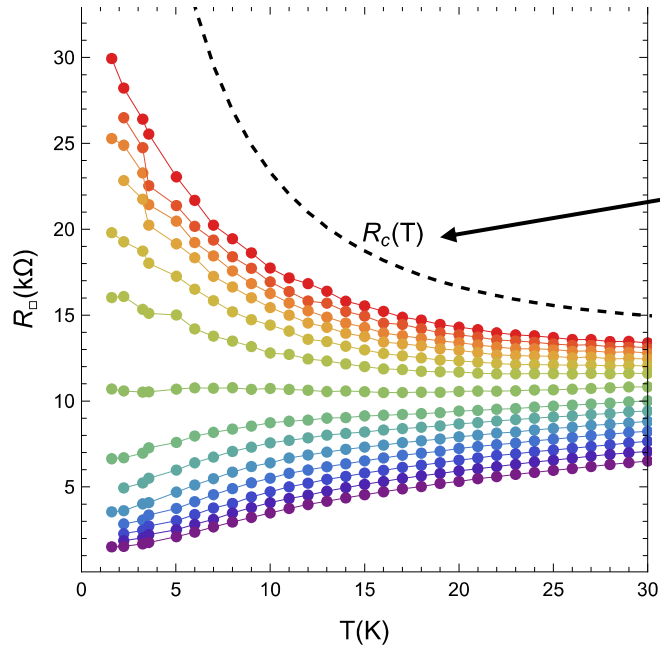
Resistivity close to “full polarization MIT” displays “fake insulators” and scaling



Application: ABC Trilayer Graphene

ABC trilayer graphene is ferromagnetic:

low-density two-dimensional electron systems¹⁻⁵. Here we show that gate-tuned van Hove singularities in **rhombohedral trilayer graphene**⁶ drive spontaneous **ferromagnetic polarization** of the electron system into one or more spin and valley flavours. Using capacitance and transport measurements, we observe a cascade of



Observed curves **never diverge** as $1/T$

This is how a **critical curve** would look like

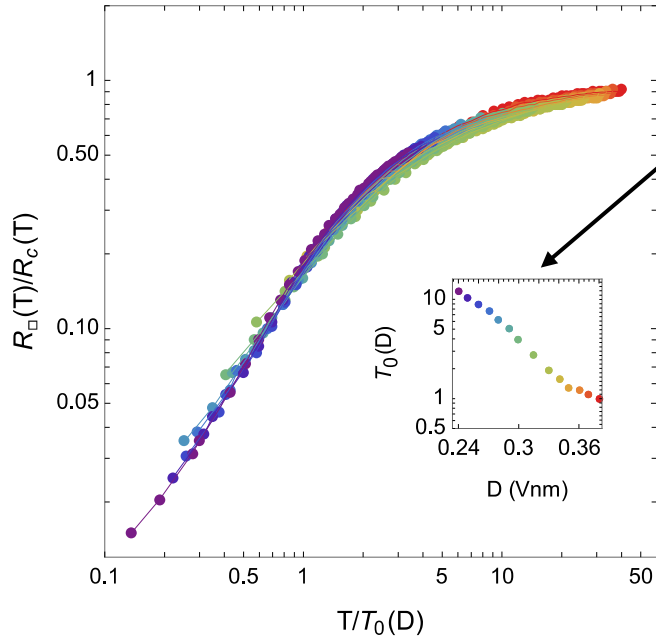
$$R_c(T) = \frac{a}{T} + b + cT$$

Hypothesis:

all resistivity curves correspond to the *metallic* side of a full polarization transition!

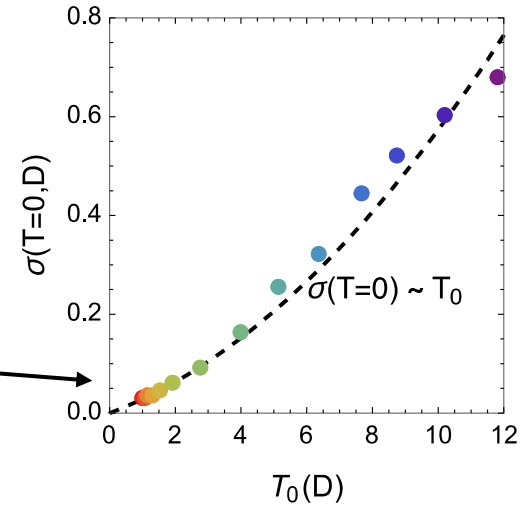
Scaling in ABC Trilayer Graphene

Indeed, **all** curves can be collapsed using a **scaling ansatz** of being close to MIT

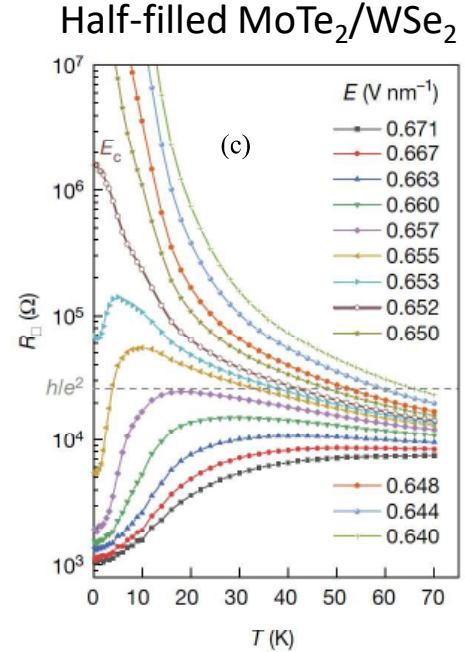
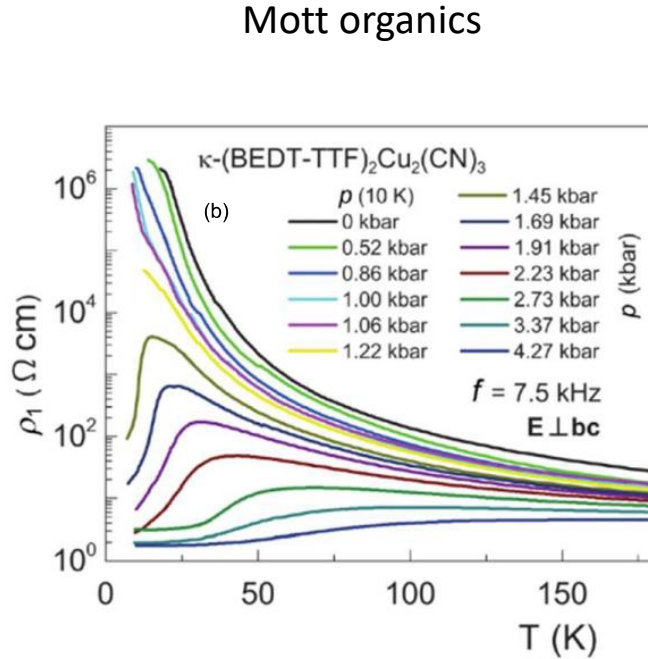
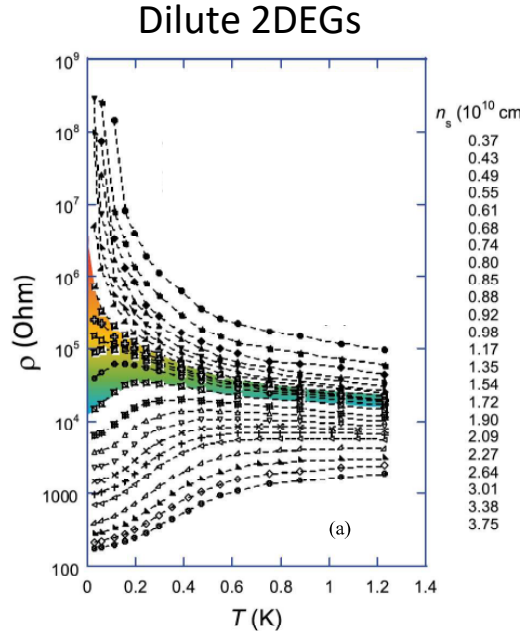


“Distance to MIT” is measured by scaling parameter T_0

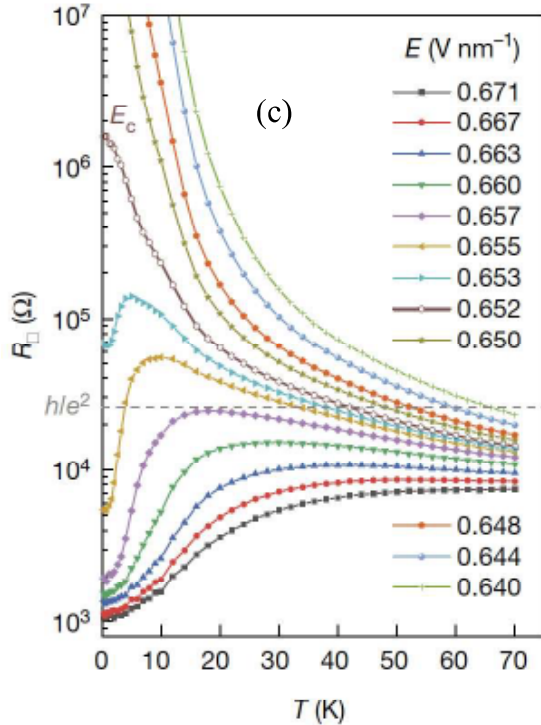
Zero T conductivity will vanish when T_0 vanishes



Mott metal-insulator transition



Mott metal-insulator transition in MoTe₂/WSe₂

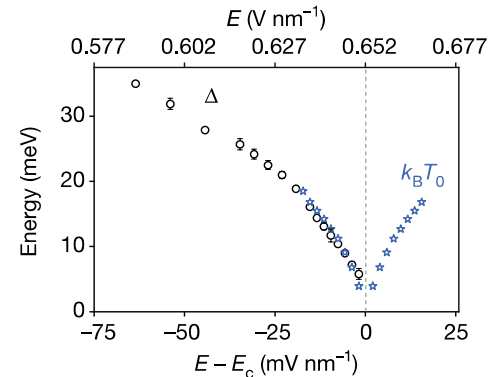


1. **Powerlaw** critical resistivity curve $R_c(T) \sim T^{-\alpha}$, $\alpha = 1.2$

No "fake insulator" regime, but

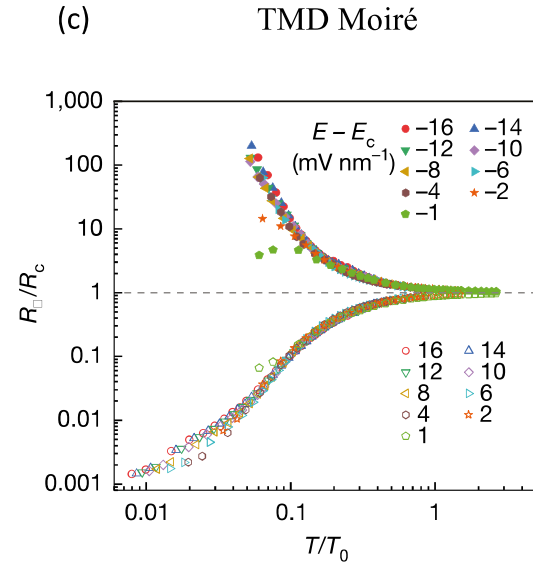
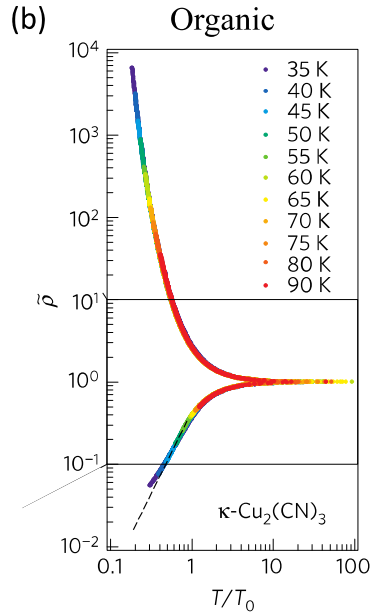
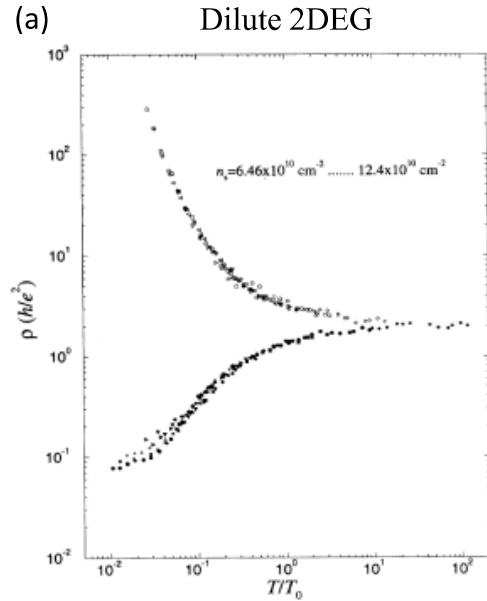
2. Crossover scale T_0 signaling end of Fermi liquid with a **resistivity maximum**

3. Insulator has continuous **vanishing gap Δ**



Scaling near Mott metal-insulator transition

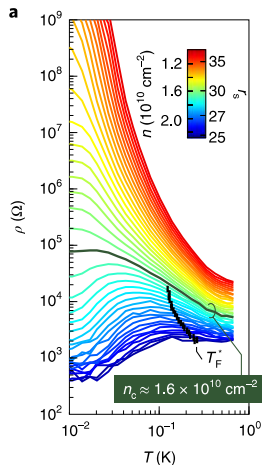
4. Perfect **scaling** of insulating and metallic curves



Theory of continuous Mott M-I-T

Theory predictions	2D Spinon theory	DMFT	Percolation theory
Transition Type	continuous	weakly first order (at $T < T_c \sim 0.01T_F$)	first order
Δ	$ g - g_c S^{\nu z}$, $\nu z = 0.67$	$ U - U_{c1} ^{\nu z}$, $\nu z \approx 0.8$	remains finite
m^*	weak: $\ln \frac{1}{ g - g_c }$	strong: $ U - U_{c2} ^{-1}$	no divergence
$A/(m^*)^2$?	constant (KW law obeyed)	diverges: $(x_0 - x_c)^{-t}$; $t = s/m$
T_{FL}	$ g - g_c ^{2\nu}$	$ U - U_{c2} $	$T^* \sim x_0 - x_c $
T_{max}	$T_{max} = \infty$	$ U - U_{c2} $	$T^* \sim x_0 - x_c $

Caveats / Open problems



Fake fake insulators

Low temperature saturation in insulators can come from experimental issues

quantum resistance value h/e^2 . Data for $T \lesssim 20$ mK deviate from the systematic behaviour at higher temperatures, most likely due to the common issue of decoupling of the electron temperature from that of the immersion cryogen. The effect of an in-plane magnetic

Ref: Falson, Nat Mater 2022

Anderson insulation?

Standard theory predicts Anderson insulation at low density in presence of disorder in 2d

Phonons? Electron-electron interactions?

Still work to do in including further interactions mechanisms.

Are there different **universality classes** associated with scaling close to the MIT?

Collaborators

Theory collaborators:



Vlad Dobrosavljevic & Yuting Tan
Florida State U, USA

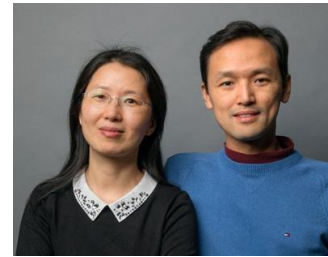


Simone Fratini
Grenoble, France

Experimental data from:

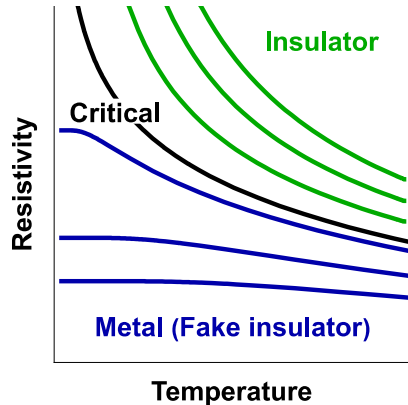
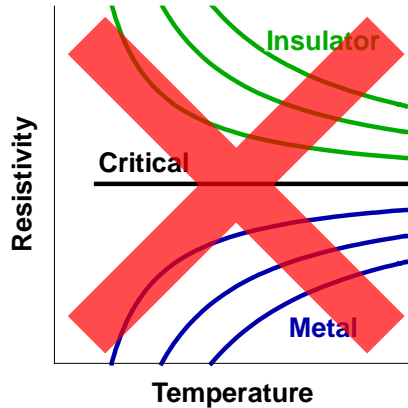


Guorui Chen
Shanghai Jiao Tong U, China



Jie Shan, Kin Fai Mak
Cornell U, USA

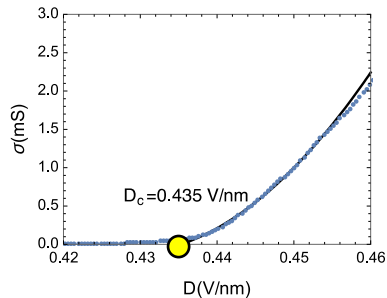
Conclusions: A New Perspective on Metal-Insulator Transitions



- Critical resistivity is **not constant** but diverges as a **powerlaw**
- Close to the MIT there is a **metallic regime** with $d\rho/dT < 0$ (“**fake**” insulator)
- Close to the MIT there is **universal scaling** of resistivity curves
$$\rho(T)/\rho_c(T) = f(T/T_0(\delta))$$
- Theory: weak disorder band transitions (with or without SSB)
- Applicable to experiments in **moiré systems** (graphene, TMDs)
- **Mott** MIT has different properties

Scaling in MoTe₂/WSe₂

Extrapolating the
zero-temperature conductivity
gives critical D_c



where the resistivity follows

$$R_c \sim 1/T$$

