

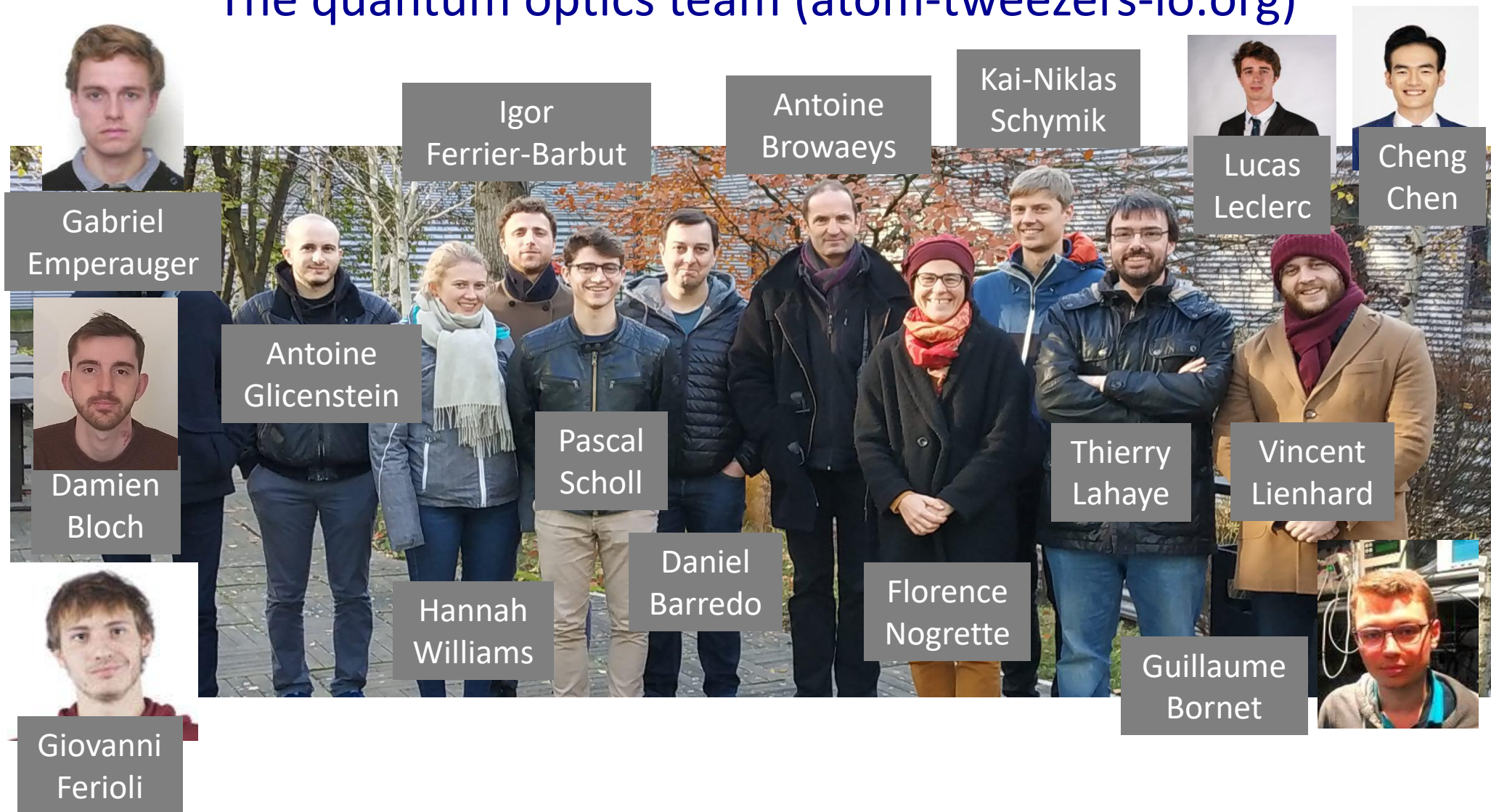


Observation of a superradiant phase transition in free space

Feroli Giovanni

**23-06-22, SPICE workshop
Ingelheim**

The quantum optics team (atom-tweezers-io.org)

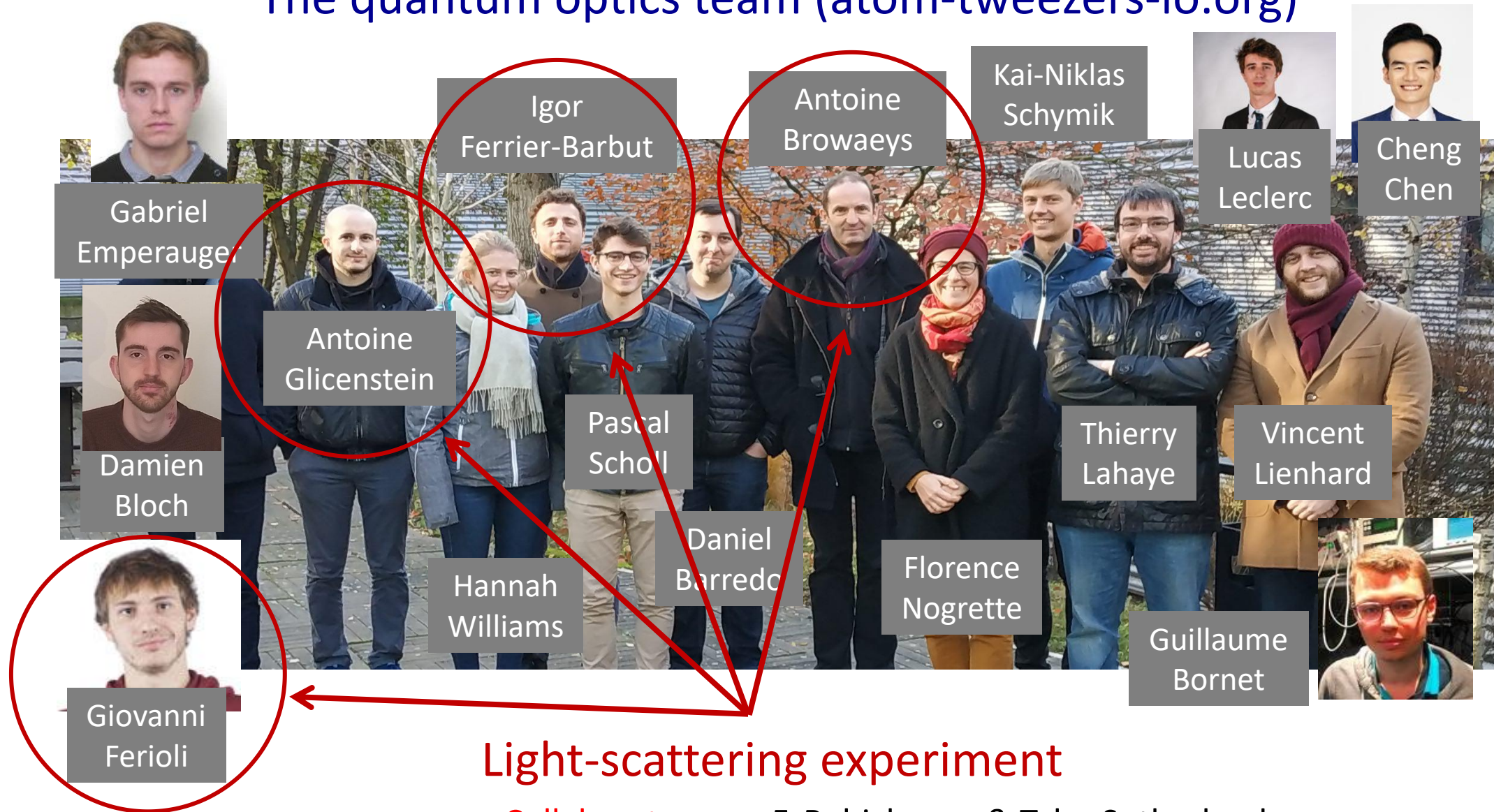


Collaborators

F. Robicheaux & Tyler Sutherland



The quantum optics team (atom-tweezers-io.org)



Light-scattering experiment

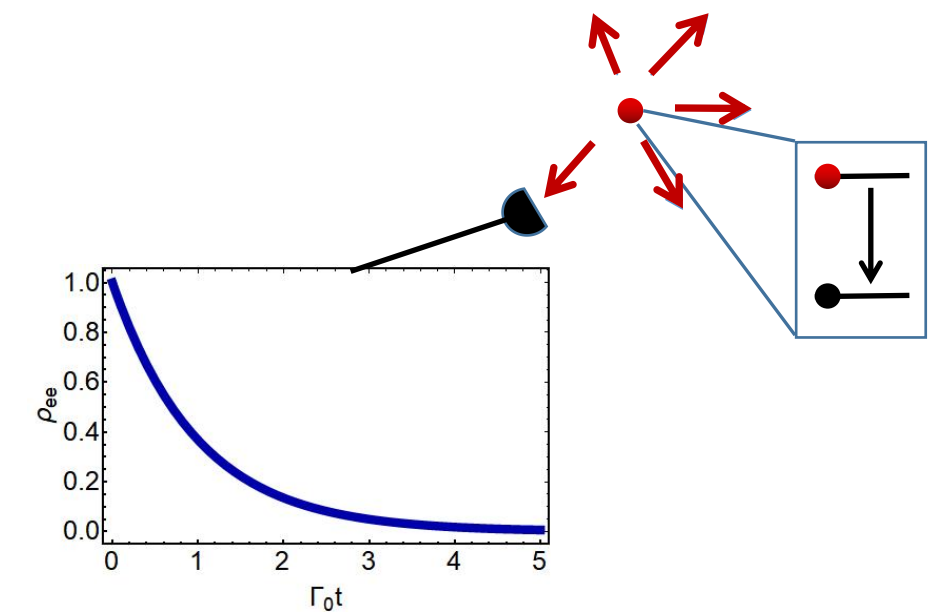
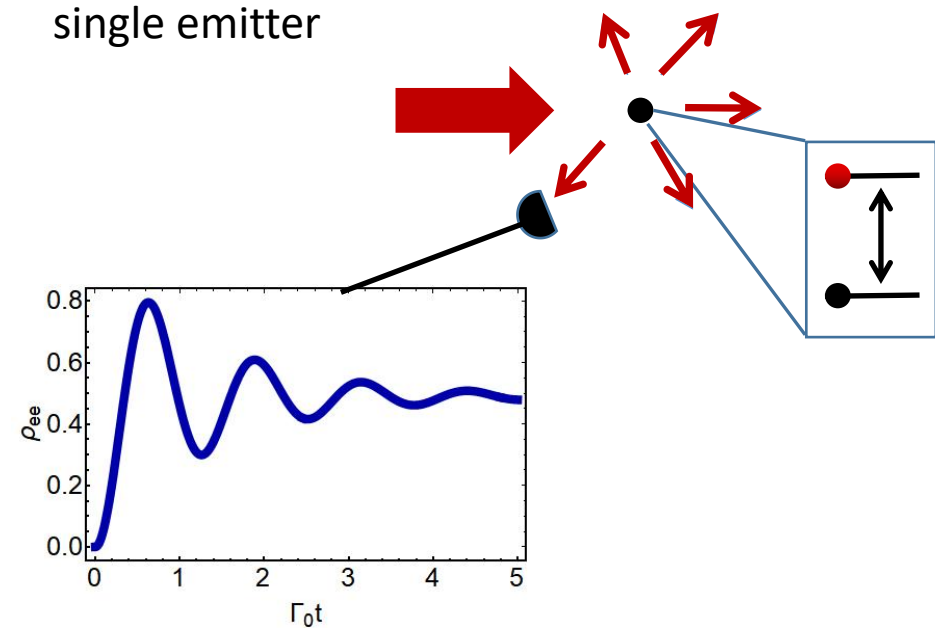
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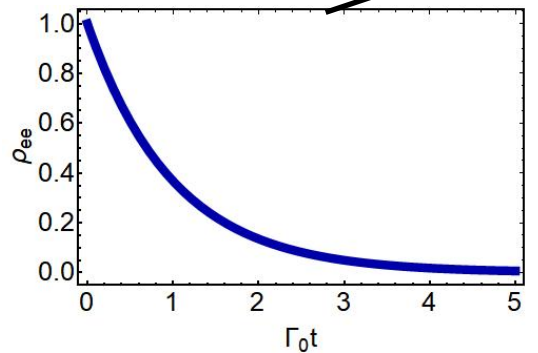
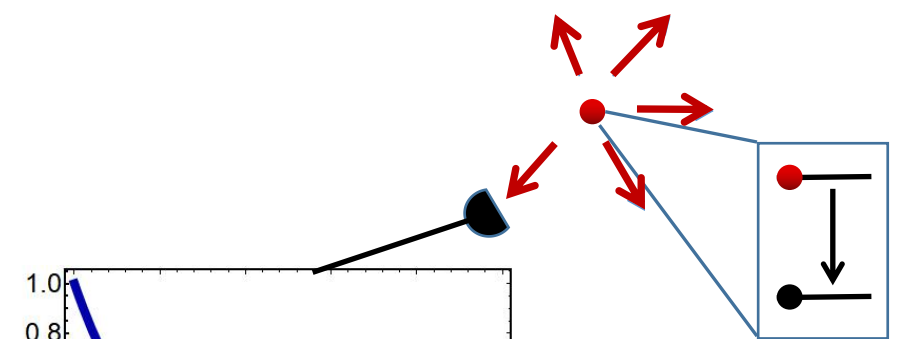
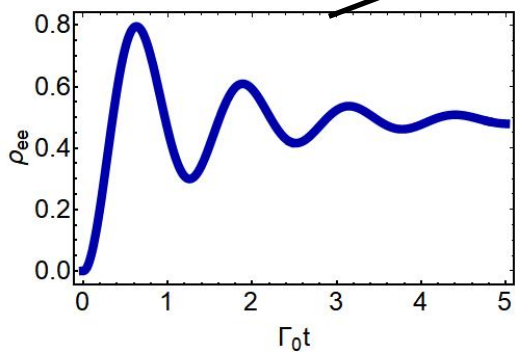
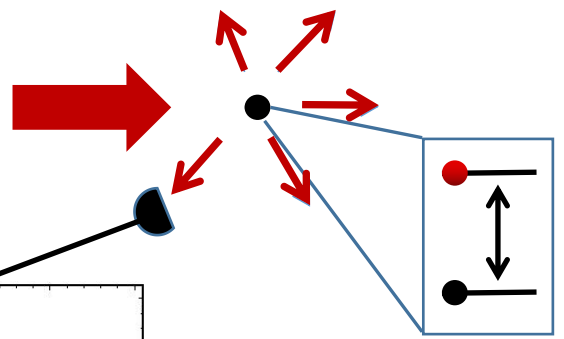
light + atoms: a many-body system

single emitter



light + atoms: a many-body system

single emitter



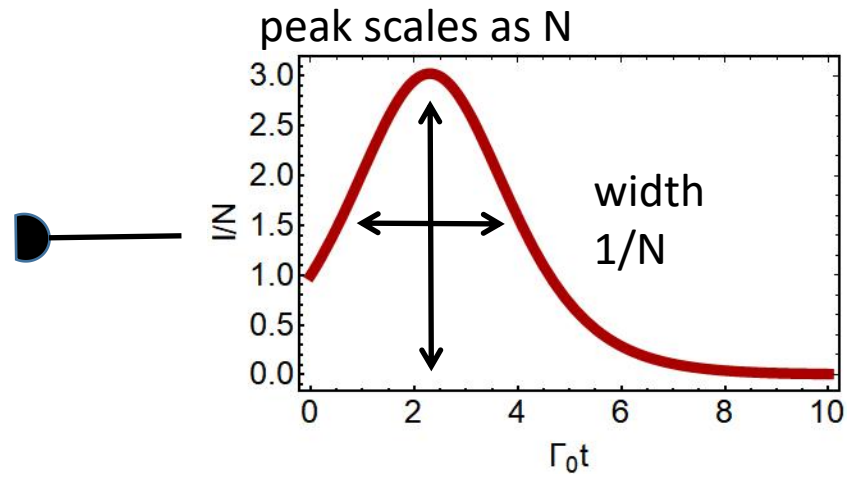
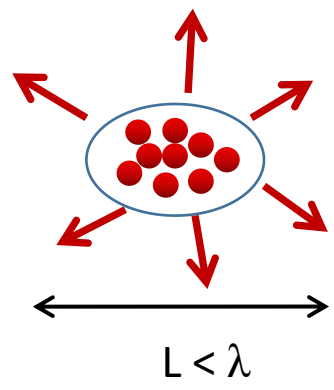
many emitters: much more complex system!!

first example by Dicke in 1954:

PHYSICAL REVIEW VOLUME 93, NUMBER 1 JANUARY 1, 1954

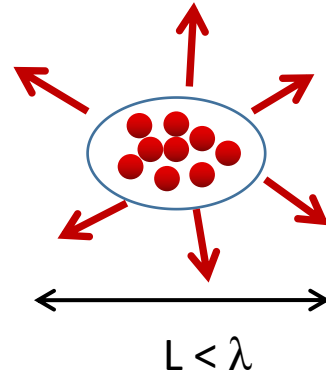
Coherence in Spontaneous Radiation Processes

R. H. DICKE
Palmer Physical Laboratory, Princeton University, Princeton, New Jersey
 (Received August 25, 1953)



Dicke's superradiance

What is the main idea? use the proper basis: symmetric states!!



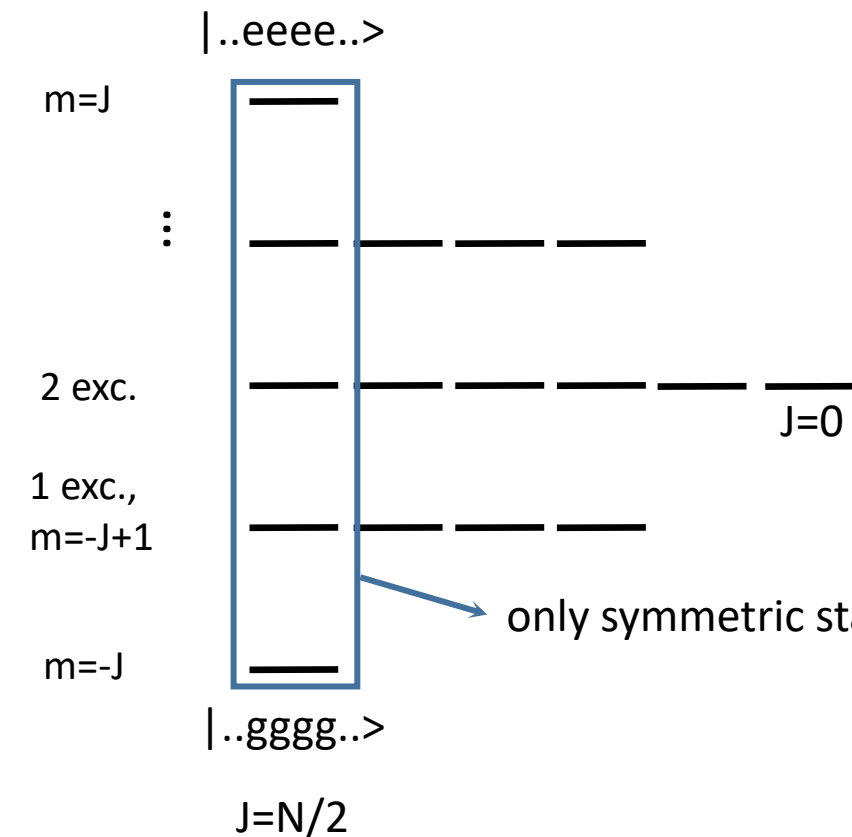
Collective dipole operator

$$H = - \sum_i^{Nat} d_i E(r_i) = - E \sum_i^{Nat} d_i = - E D$$

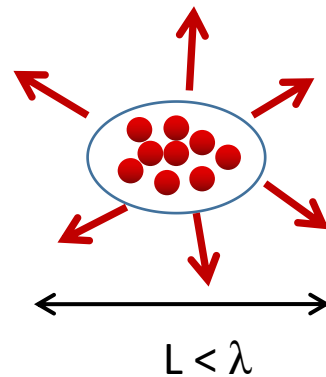
Even classically the hamiltonian is symmetric w.r.t. particle exchange

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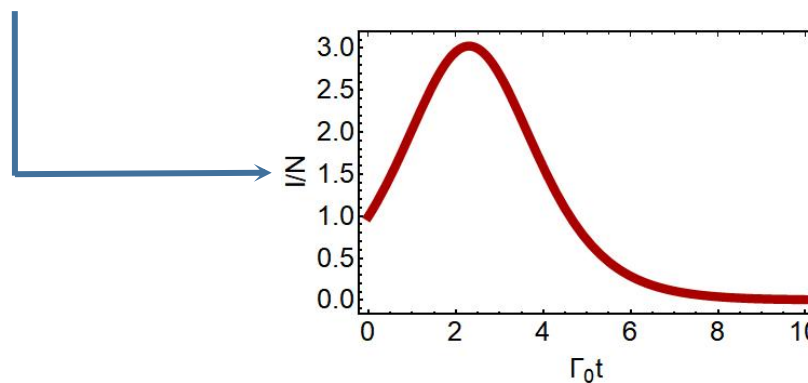
only symmetric states, equivalent to spin system $|J,m\rangle$, $J=N/2$ and $m=-J, \dots, J$



Collective dipole operator

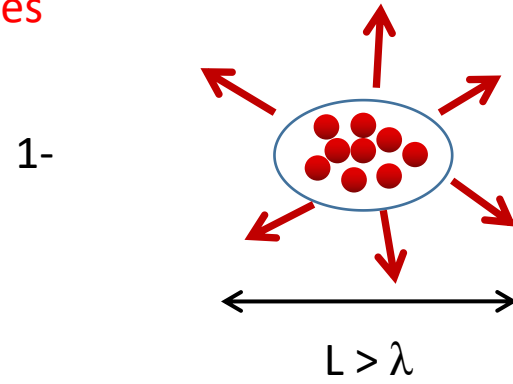
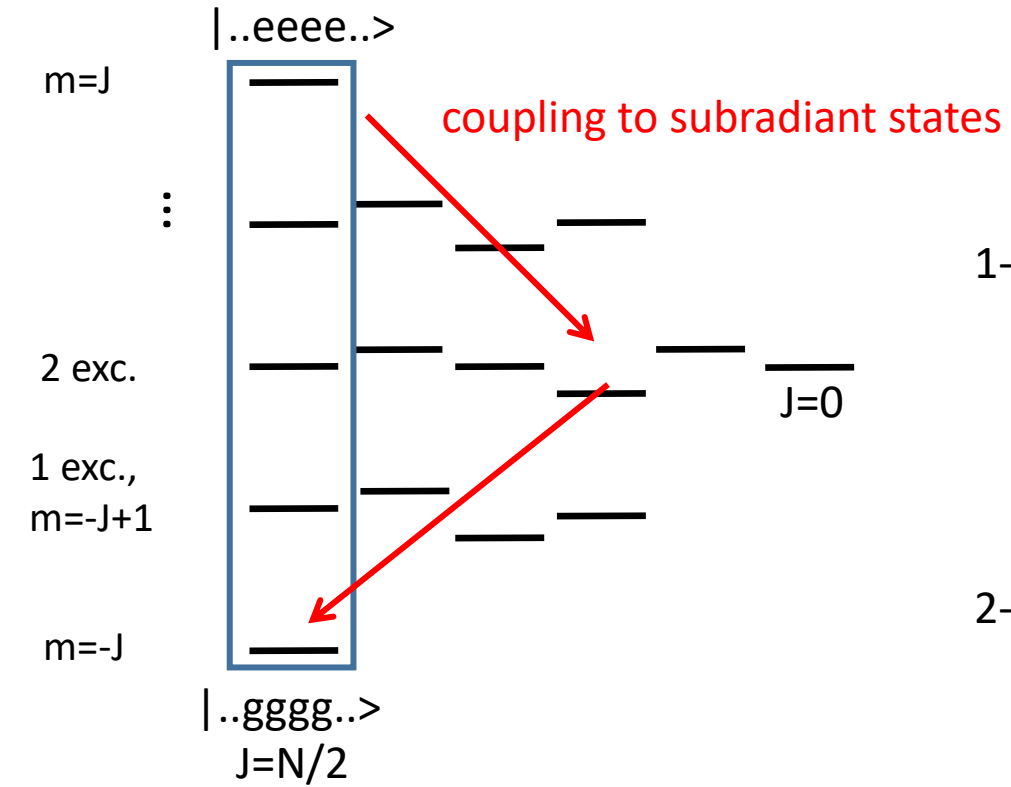
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$I \sim N^2$

Dicke's superradiance, Is it the full story??

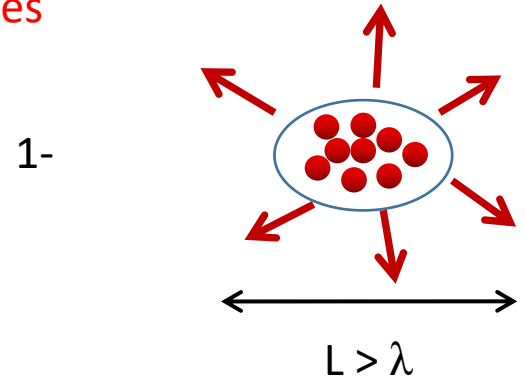
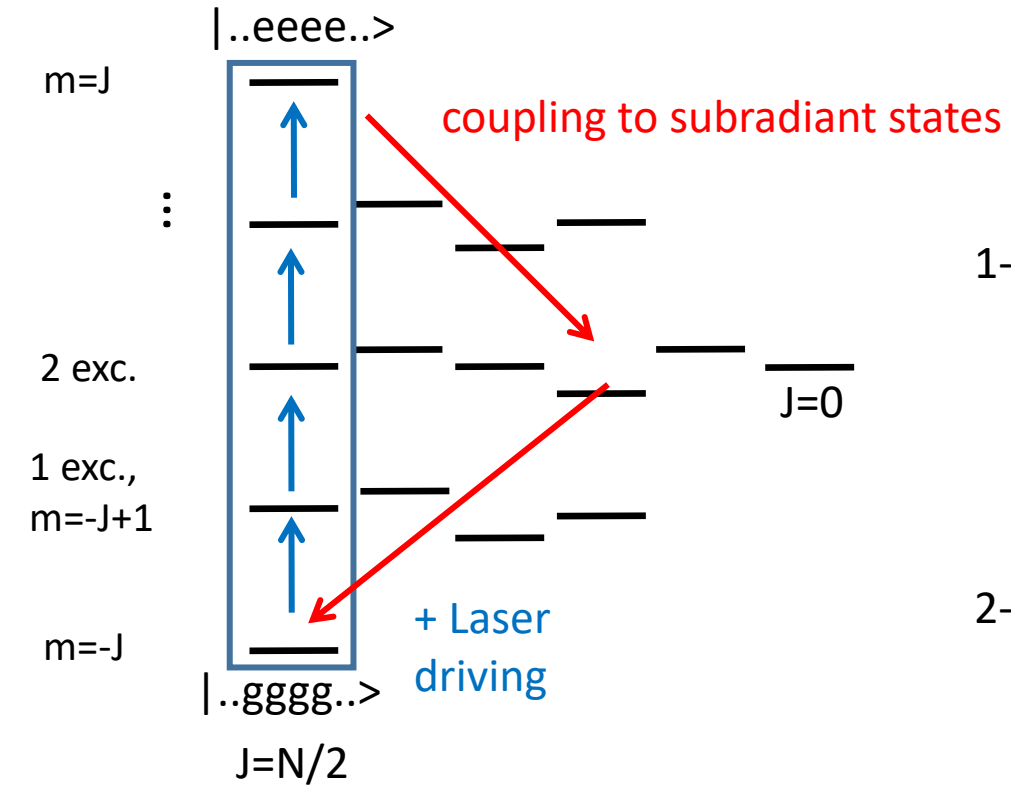


Finite size effects

2-
$$V_{dd} = \sum_{i,j} \Omega_{i,j} \sigma_i^+ \sigma_j^-$$

(light induced) dipole-dipole interaction

Dicke's superradiance, Is it the full story??



Finite size effects

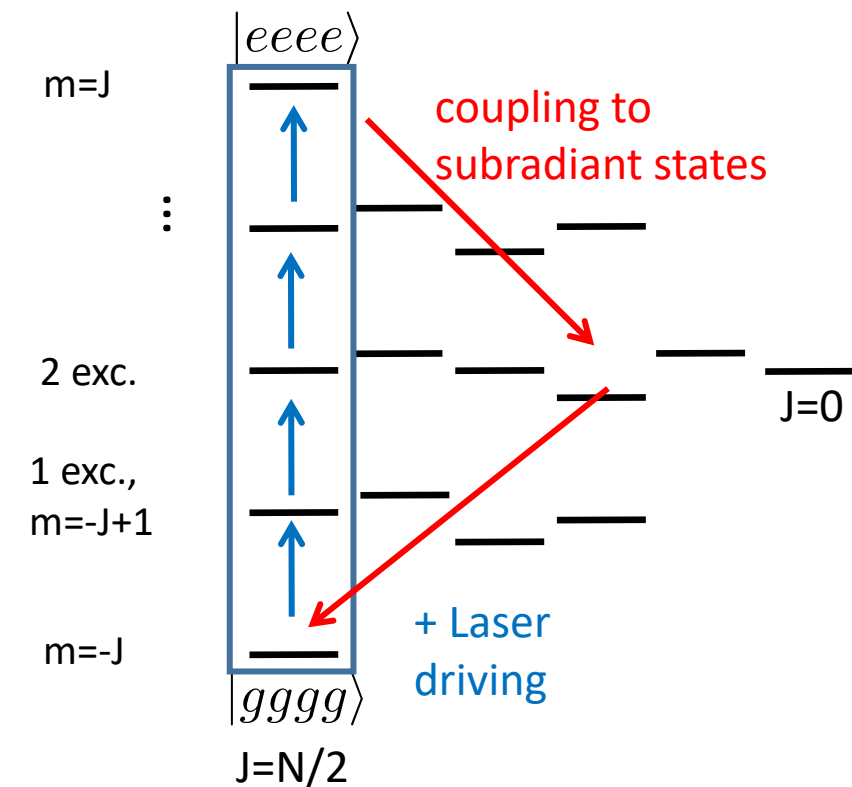
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3- What is the effect of an external driving??

Dicke's superradiance, Is it the full story??



Ferioli, et Al., PRX 2021
Ferioli, et Al. PRL 2021
Glicenstein, et Al., Optics Letter 2022

1- Finite size effects

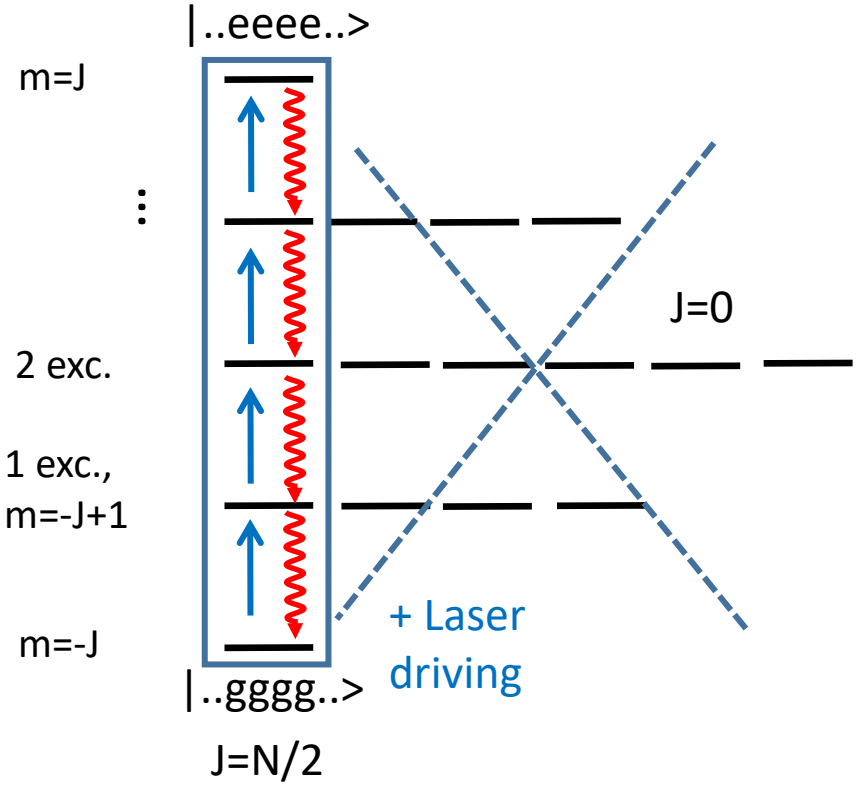
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 (light induced) dipole-dipole interaction

This talk

3- **What is the effect of an external driving??**

Ferioli et al. , in preparation

Driven Dicke model:



- ~~1- Finite size effects~~
- ~~2- (light induced) dipole-dipole interaction~~
- 3- **What is the effect of an external driving??**

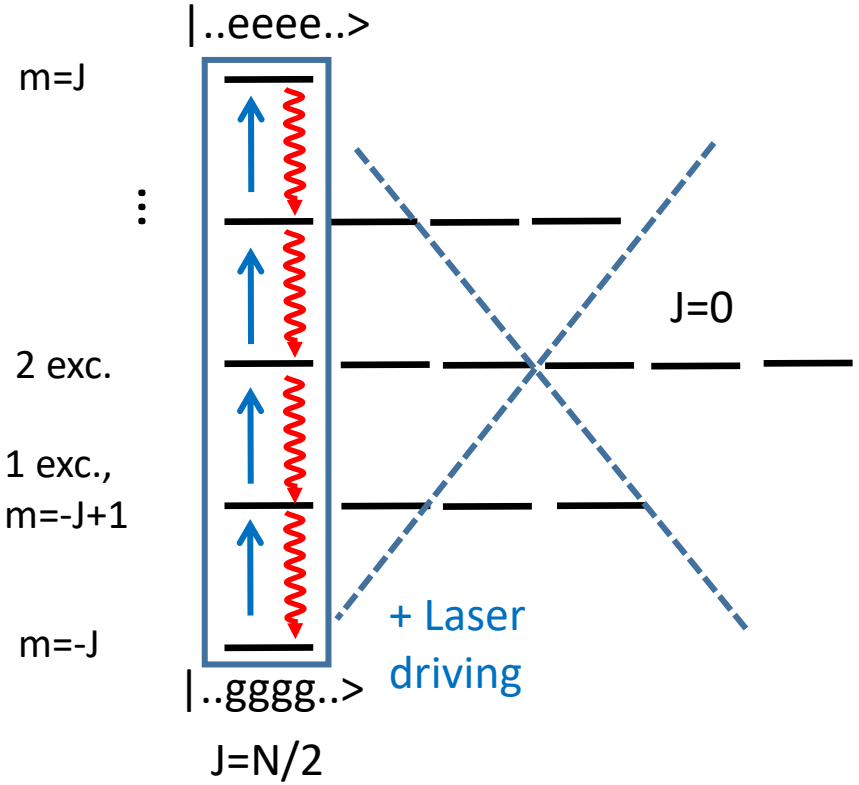
$$H = \Omega_D (S^+ + S^-)$$

Narducci PRA 1978
 Walls, Agarwal...
 Carmichael

$$\frac{d\rho}{dt} = -i\Omega_D [S^+ + S^-, \rho] + \frac{\Gamma}{2} (2S^- \rho S^+ - S^+ S^- \rho - \rho S^+ S^-)$$

1. Solve dynamics and steady-state up to 50 atoms

Driven Dicke model:



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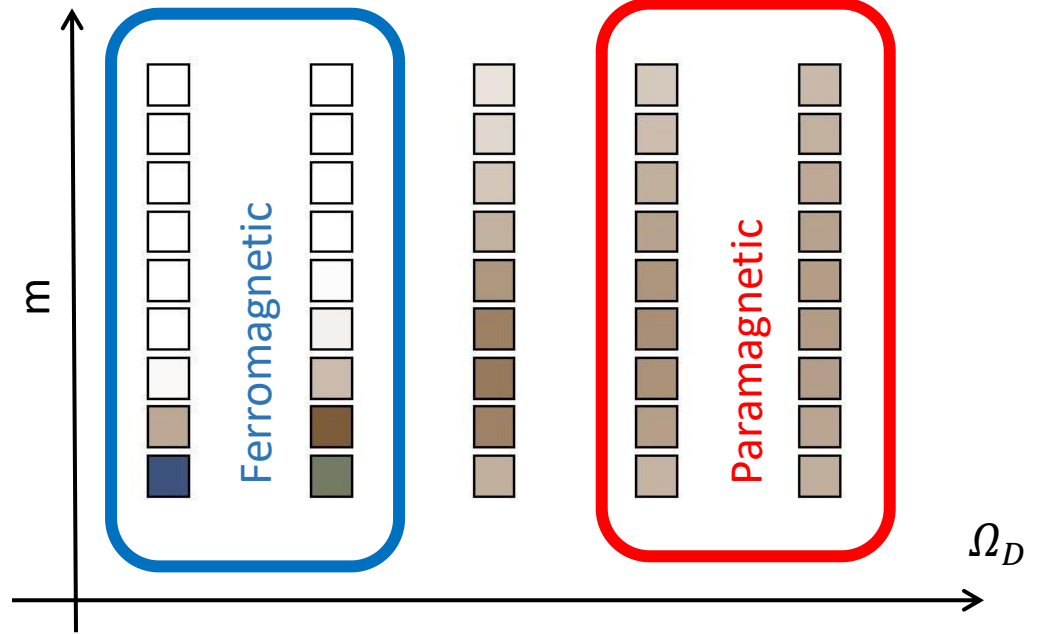
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N=8

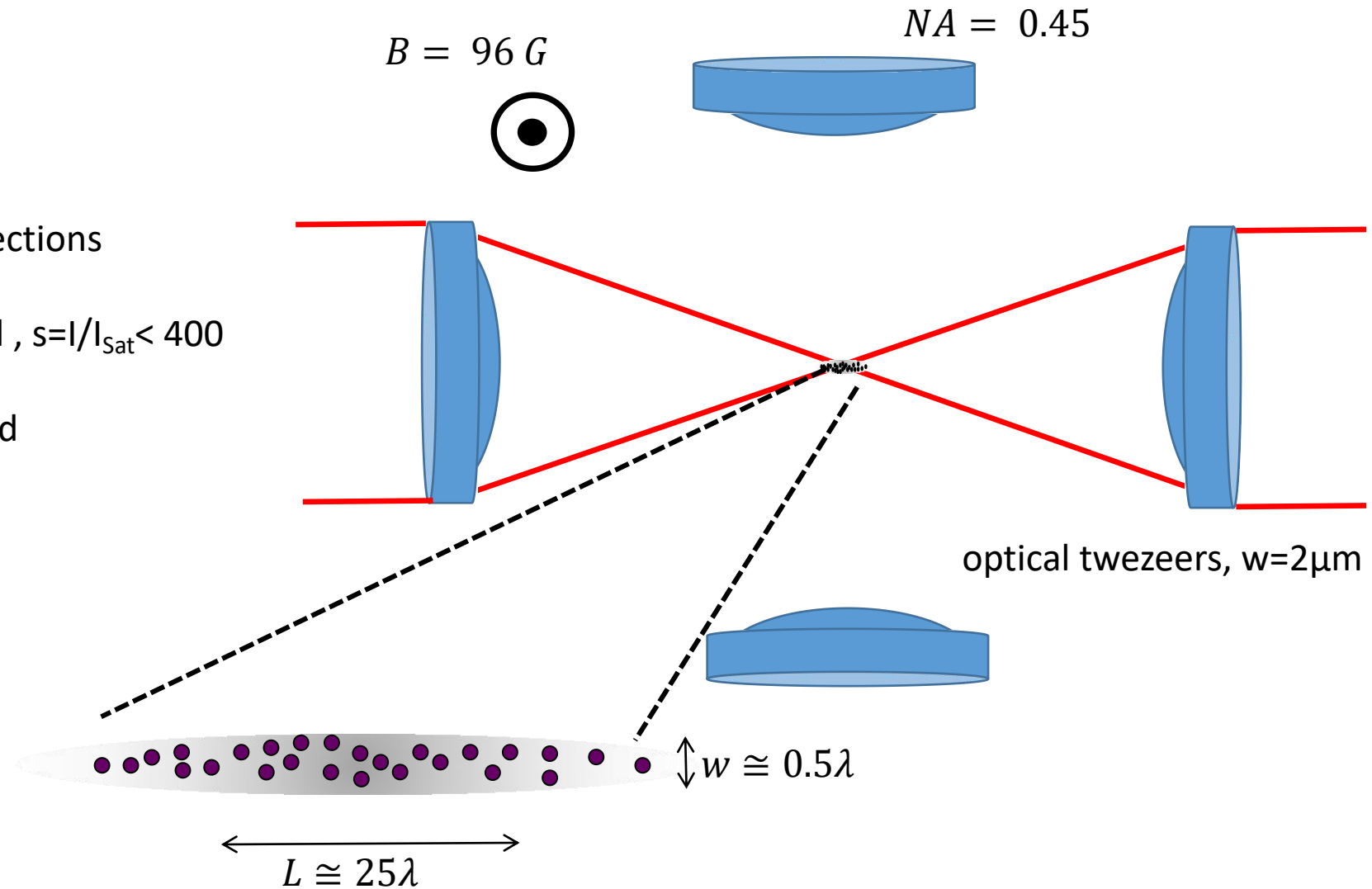
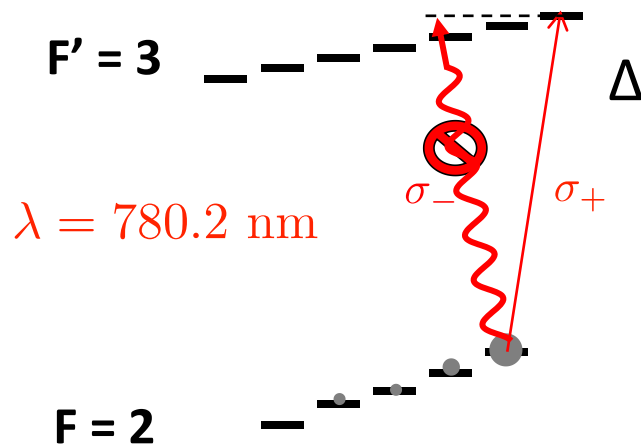
1. Solve dynamics and steady-state up to 50 atoms
2. Existence of two (non-equilibrium) phases



Experimental platform - close to Dicke's regime

More details in:
Glicenstein, PRA 2021, PRL 2020

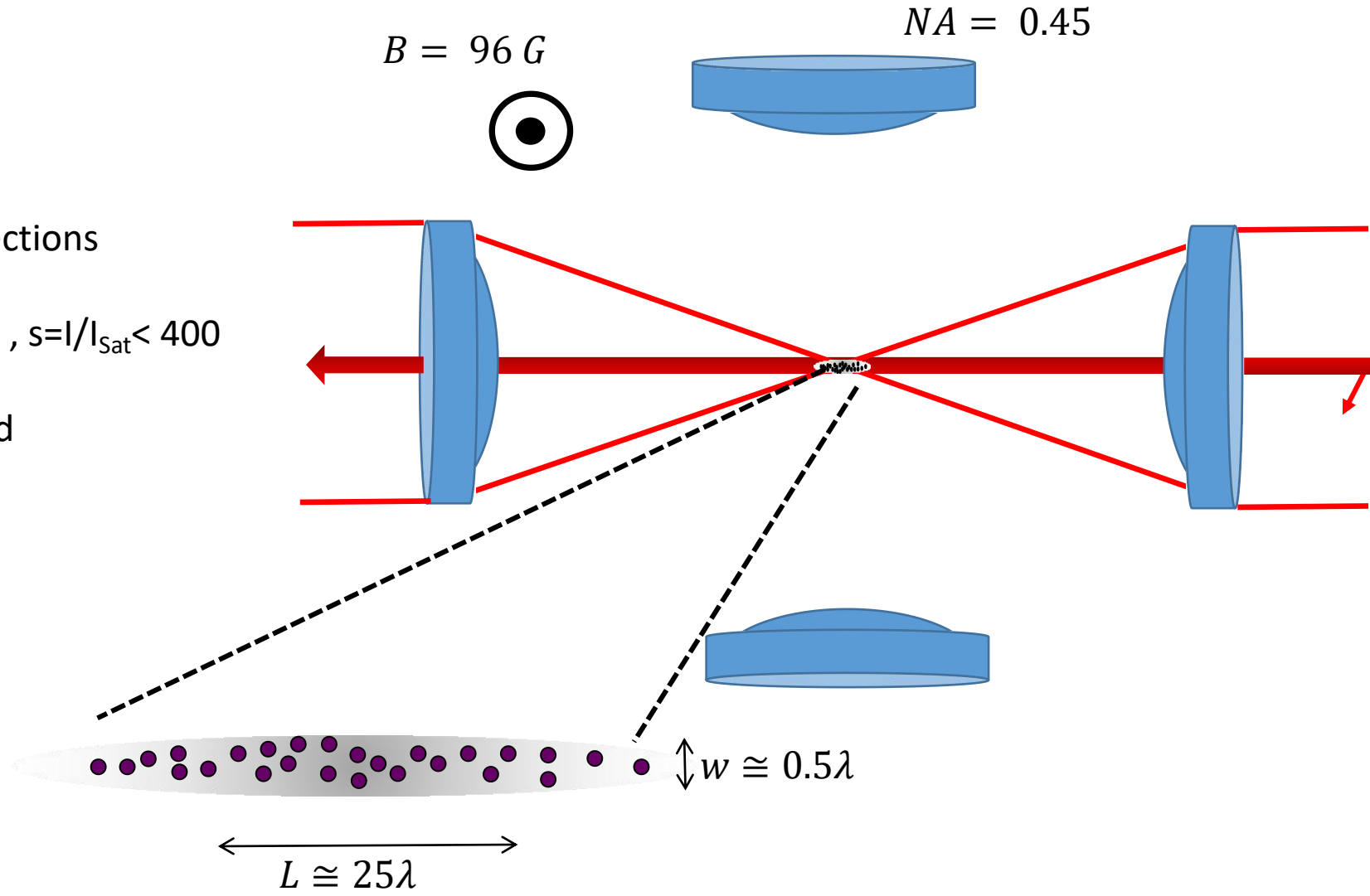
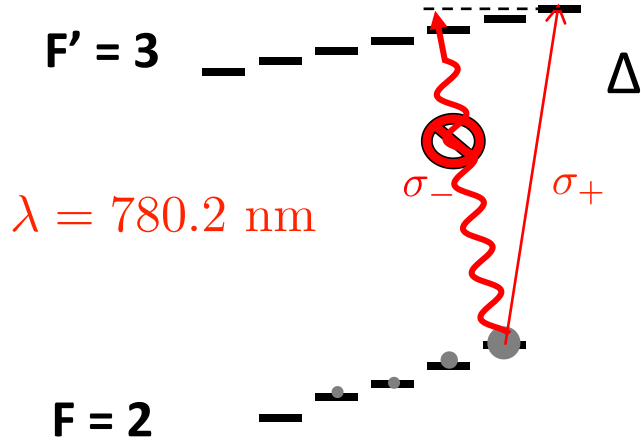
- 1- $N = 2000$ atoms, $T = 200 \mu\text{K}$
- 2- Dense cloud: $n \sim 10^{14} \text{ at/cm}^3$
- 3- Volume $\sim \lambda^3$, Close to Dicke limit
- 4- Repetition rate $> 2\text{Hz}$
- 5- Detecting (and manipulating) in two directions
- 6- Driving: resonant light linearly polarized, $s = I/I_{\text{sat}} < 400$
- 7- clean 2 level system, large magnetic field



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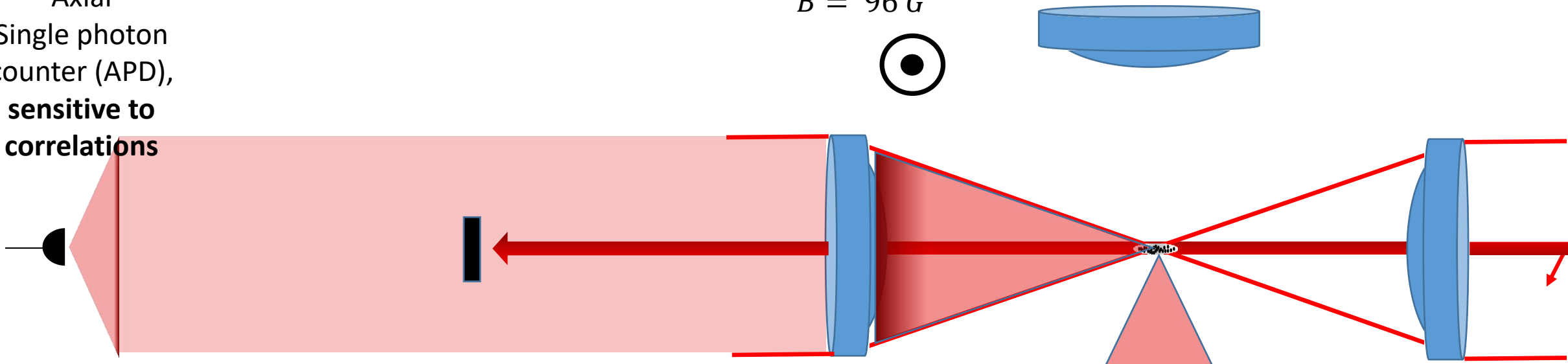
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$$\gamma(k) = \sum_i^N \langle \sigma_i^z \rangle(t) + \sum_{i \neq j}^N \langle \sigma_i^+ \sigma_j^- \rangle(t) e^{ik(R_i - R_j)}$$

Axial
Single photon
counter (APD),
sensitive to
correlations

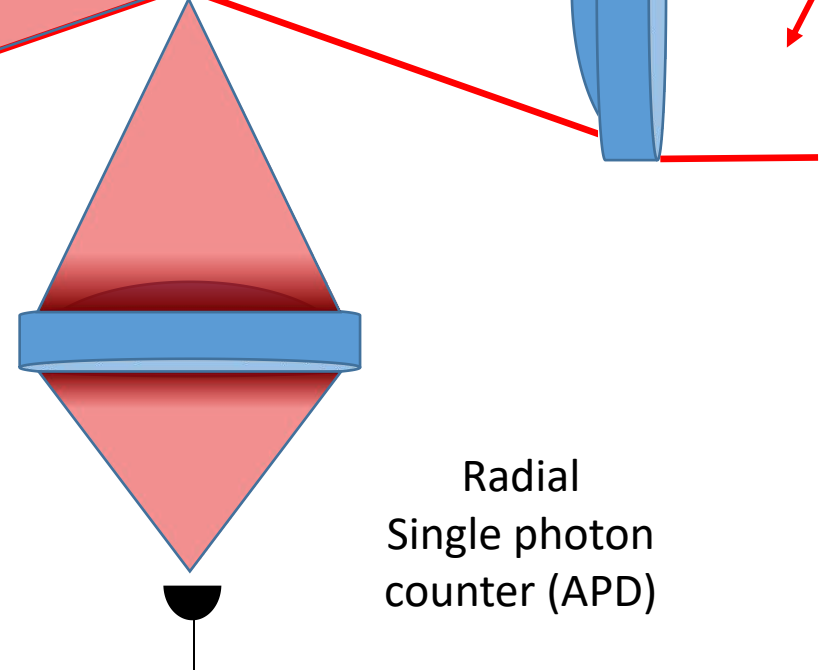
$B = 96 \text{ G}$

$NA = 0.45$



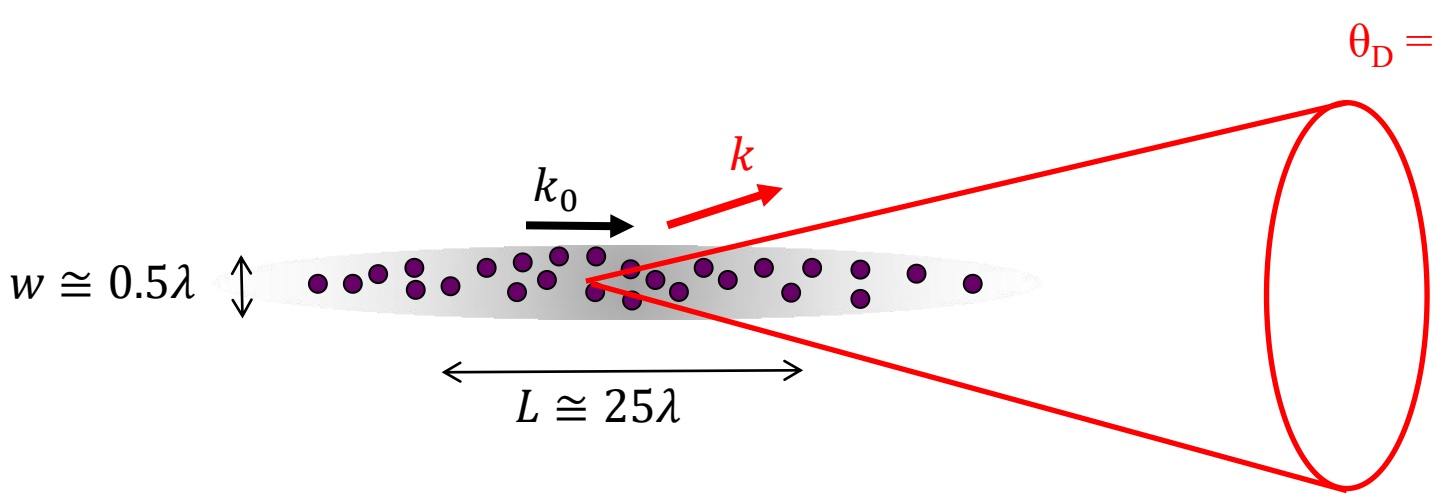
No coherent response, sensitive to the population of the excited state

~~$$\gamma(k) = \sum_i^N \langle \sigma_i^z \rangle(t) + \sum_{i \neq j}^N \langle \sigma_i^+ \sigma_j^- \rangle(t) e^{ik(R_i - R_j)}$$~~



Radial
Single photon
counter (APD)

Experimental platform - close to Dicke's regime



$\theta_D = \text{diffraction angle } \frac{\lambda}{w}$

$$E_{Sc}(k) = \sum_m^N E_0 e^{i(k-k_0)R_m}$$

Power radiated in the diffraction mode

$$P_N = \vartheta_D N E_0^2 + E_0^2 \int dk \sum_{m \neq n}^N e^{i(k-k_0)(R_m - R_n)}$$

$$= \vartheta_D N E_0^2 + E_0^2 N^2 \int dk \frac{1}{N^2} \sum_{m \neq n}^N e^{i(k-k_0)(R_m - R_n)}$$

Structure factor

Effective number of atoms emitting in the diffraction mode:

$$\tilde{N} = \frac{P_N}{N E_0^2} \cong N \mu$$

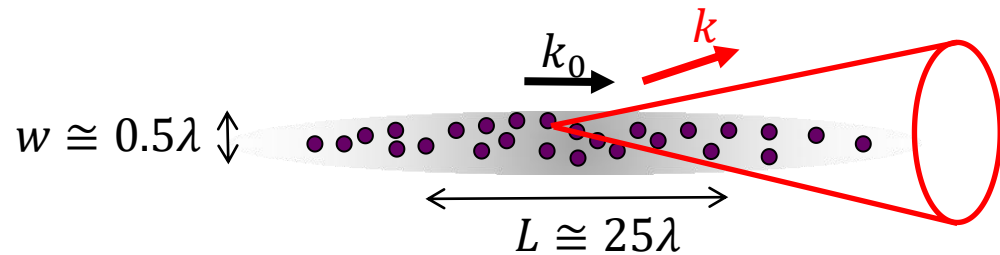
μ is the (integral of the) structure factor, in our case is about **0.004(2)**

Power radiated by N independent atoms

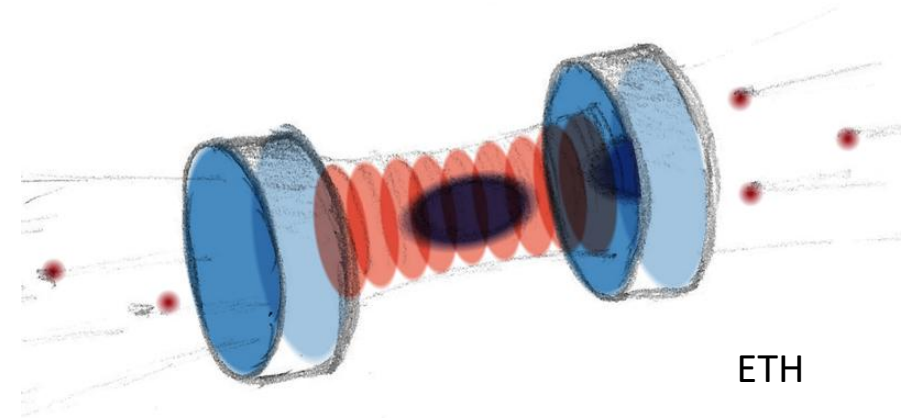
Allen and Eberly, 1987
 Gross and Haroche, 1982
 NE Rehler, JH Eberly PRA 1971

As a cQED system.... but in free space

$$\tilde{N} = \frac{P_N}{\vartheta_D N E_0^2} \cong N \mu \quad \text{effective atom number depends on the cloud geometry}$$



=

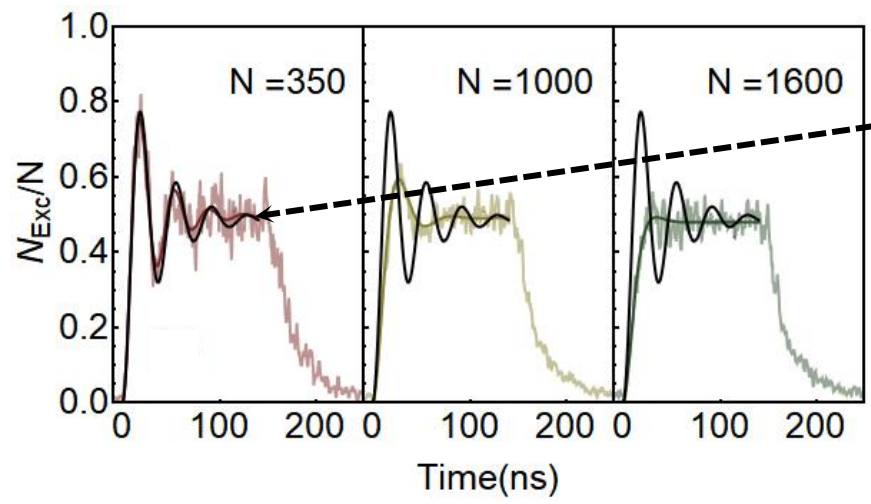
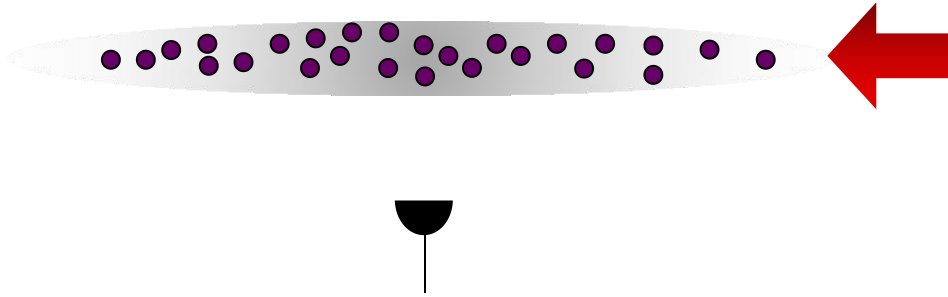


Take-home message: a cQED system.... but in free space!!

our cloud is a system of \tilde{N} atoms coupled to a single radiation mode, as in a cavity (but without it)

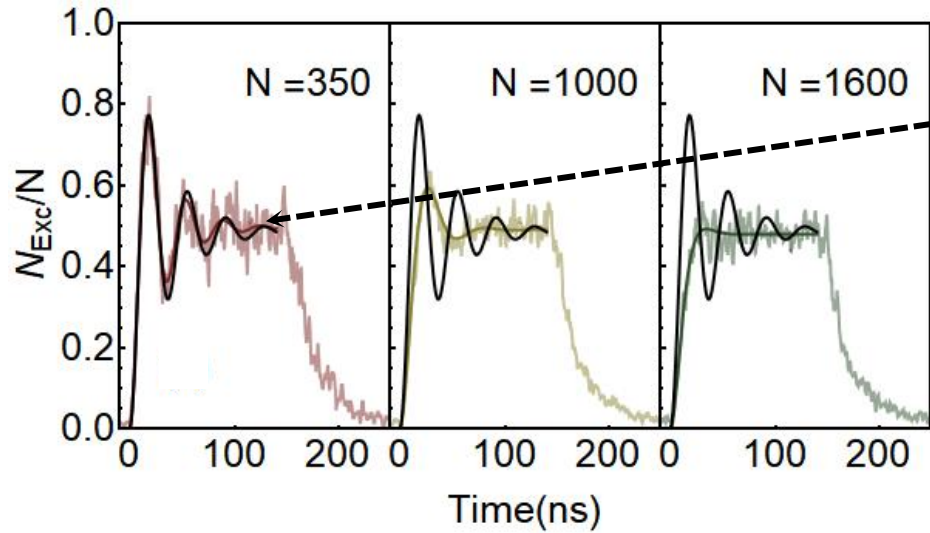
Dynamics of the excited state population

Preliminary results



Black: Optical Bloch Equation,
single atom response
(a) fixed driving strength
 $s = 35$

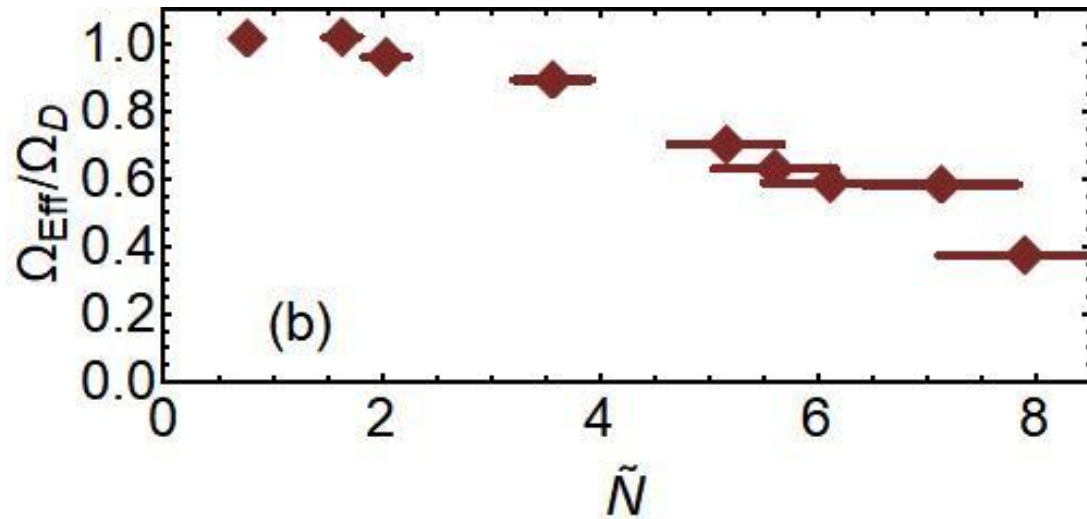
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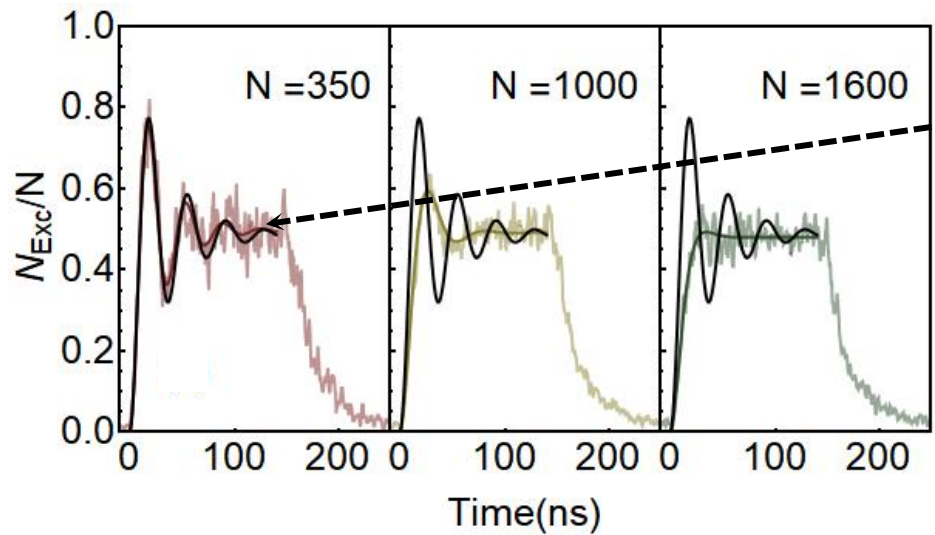
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Reduction of Rabi
frequency
increasing N



Dynamics of the excited state population

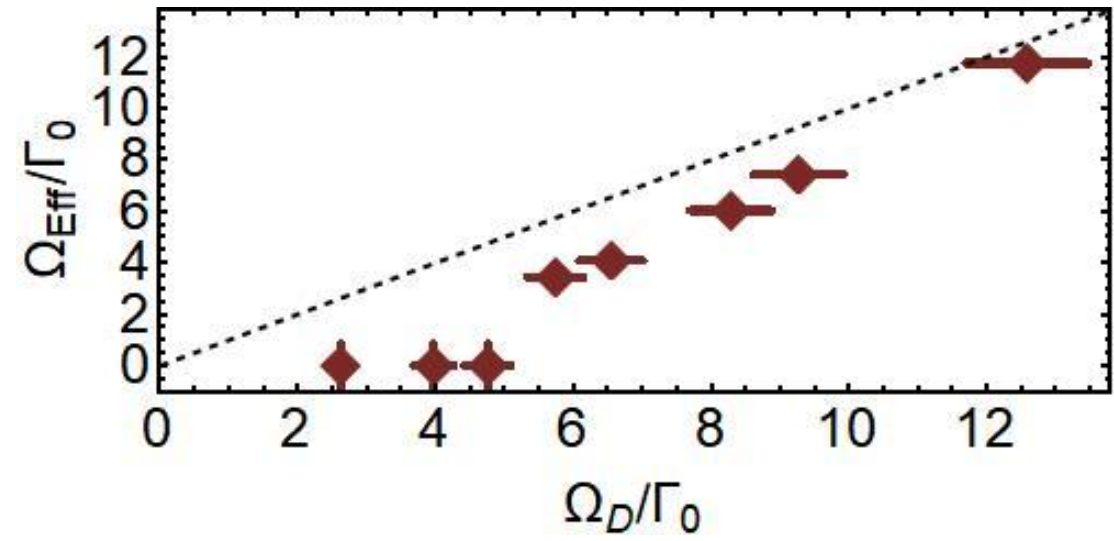
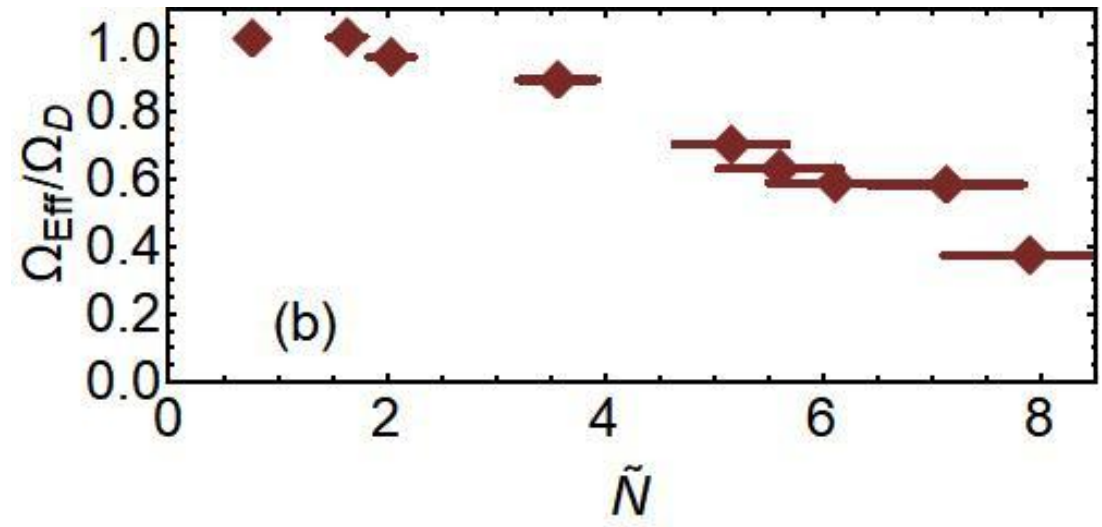
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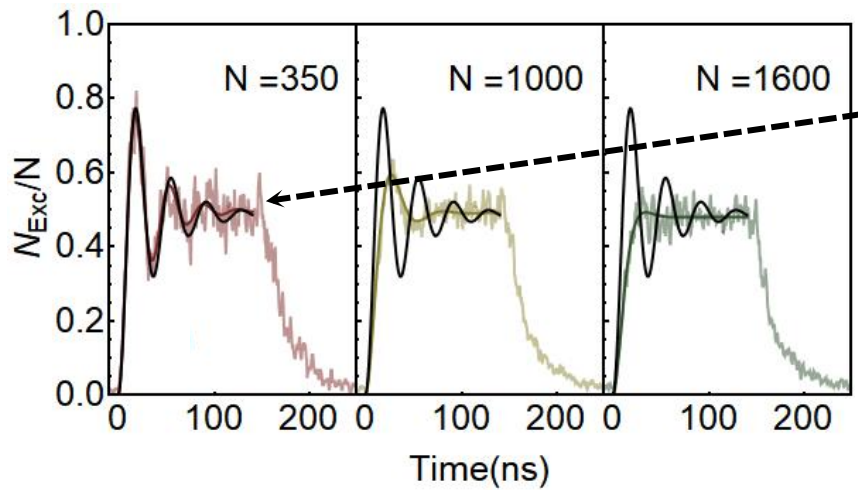
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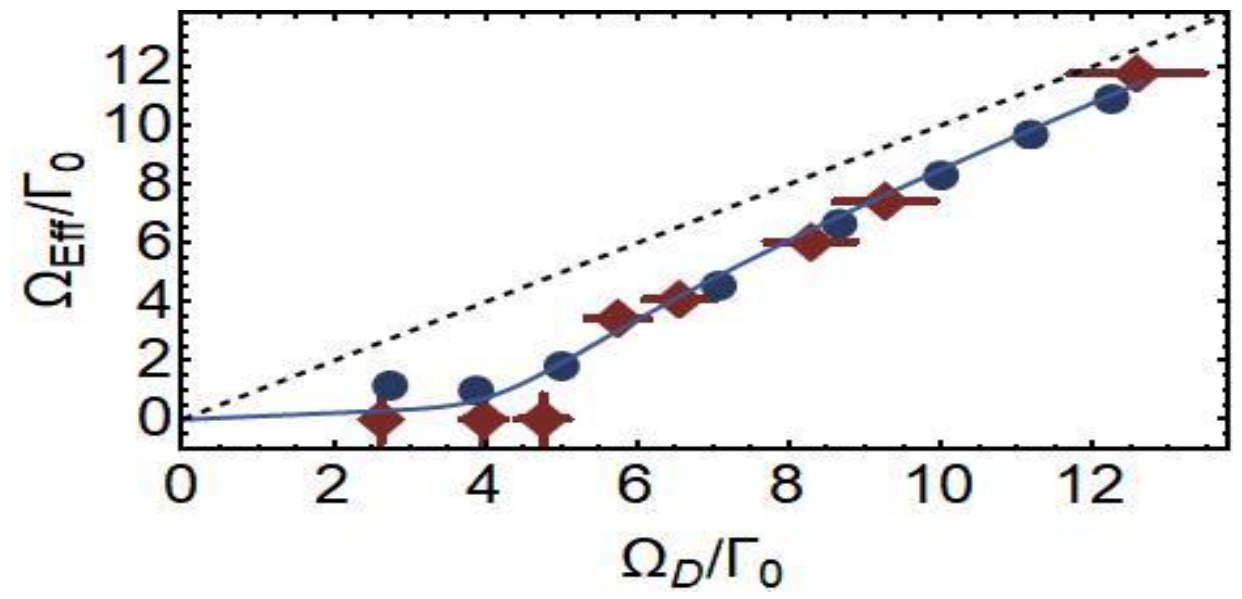
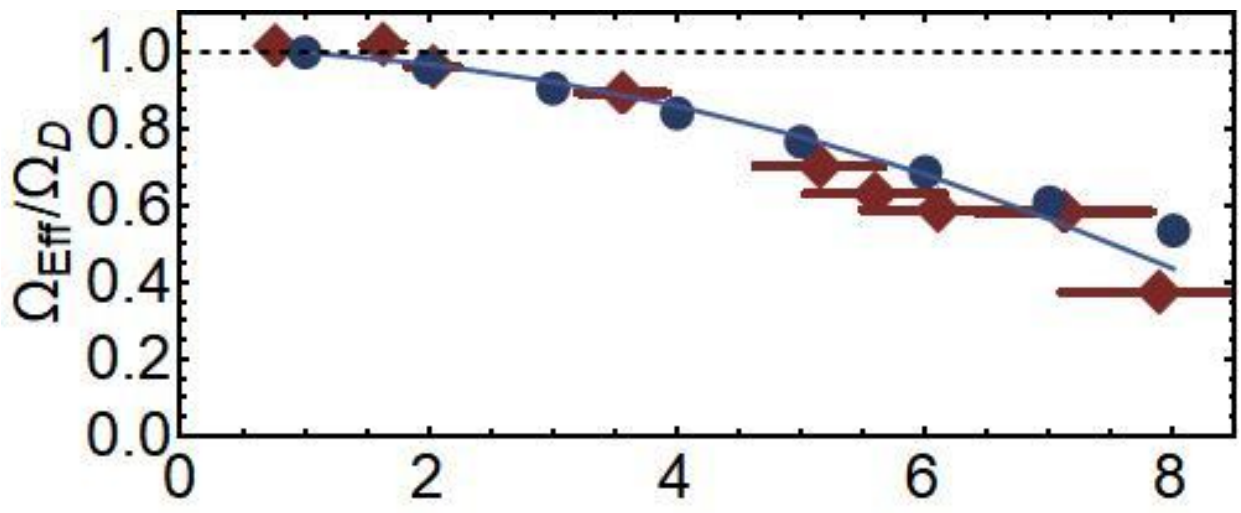
Preliminary results



Black: Optical Bloch Equation, single atom response

(a) fixed driving strength $s = 35$

Driven-Dicke results, (almost) No adjustable parameter
First experimental realization!



$$\frac{d\rho}{dt} = -i\Omega_D[S^+ + S^-, \rho] + \frac{\Gamma}{2}(2S^-\rho S^+ - S^+S^-\rho - \rho S^+S^-)$$

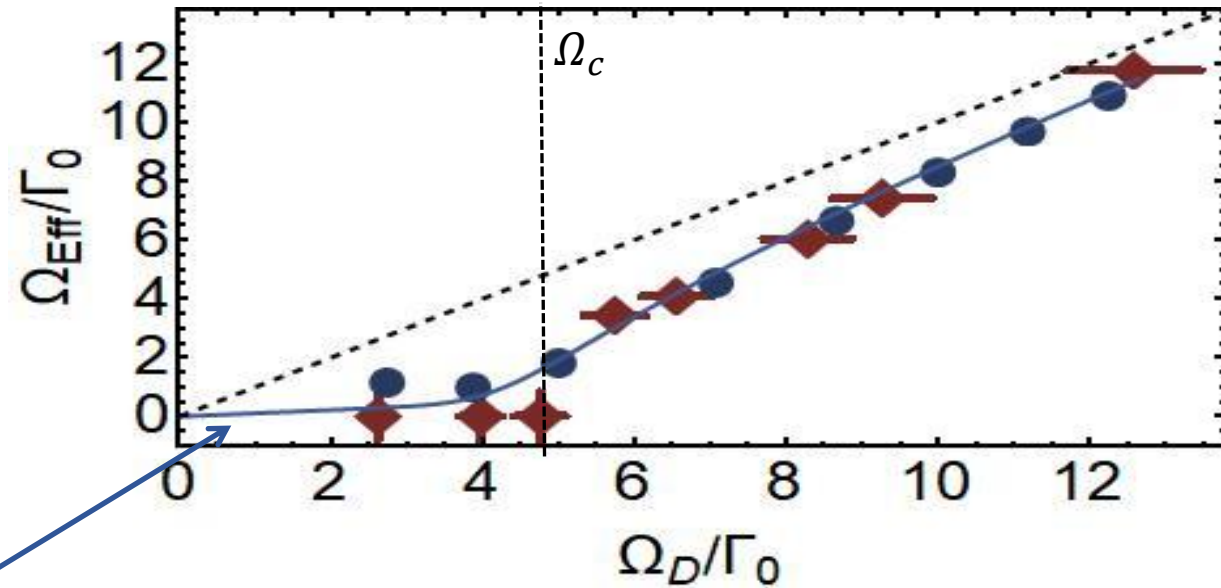
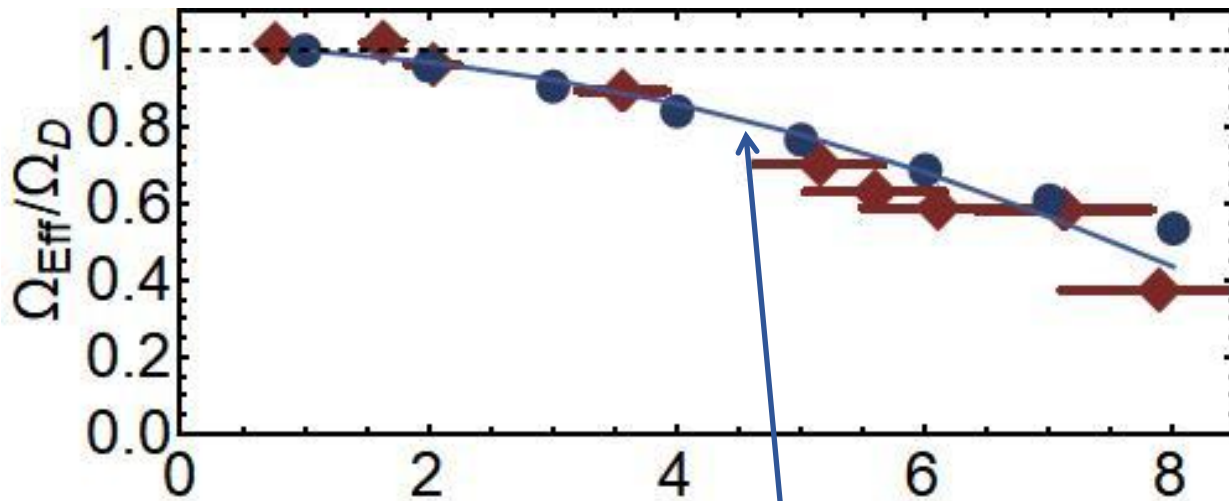
Dynamics of the excited state population

Origin: collective screening effect

$$\Omega_{Eff} = \Omega_D + \frac{2\pi}{\hbar E_S} = \Omega_D - i\Gamma_0 \langle S^- \rangle < \Omega_D$$

Field radiated by the other atoms

max collective dipole: $\langle S^- \rangle = -iN/2 \longrightarrow \Omega_D > \Omega_c = \Gamma_0 N/2$

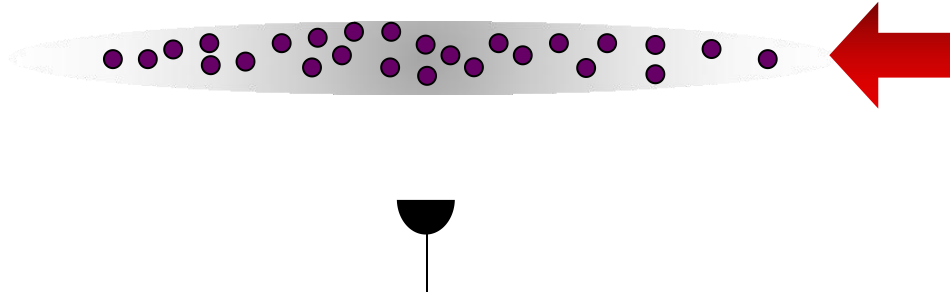


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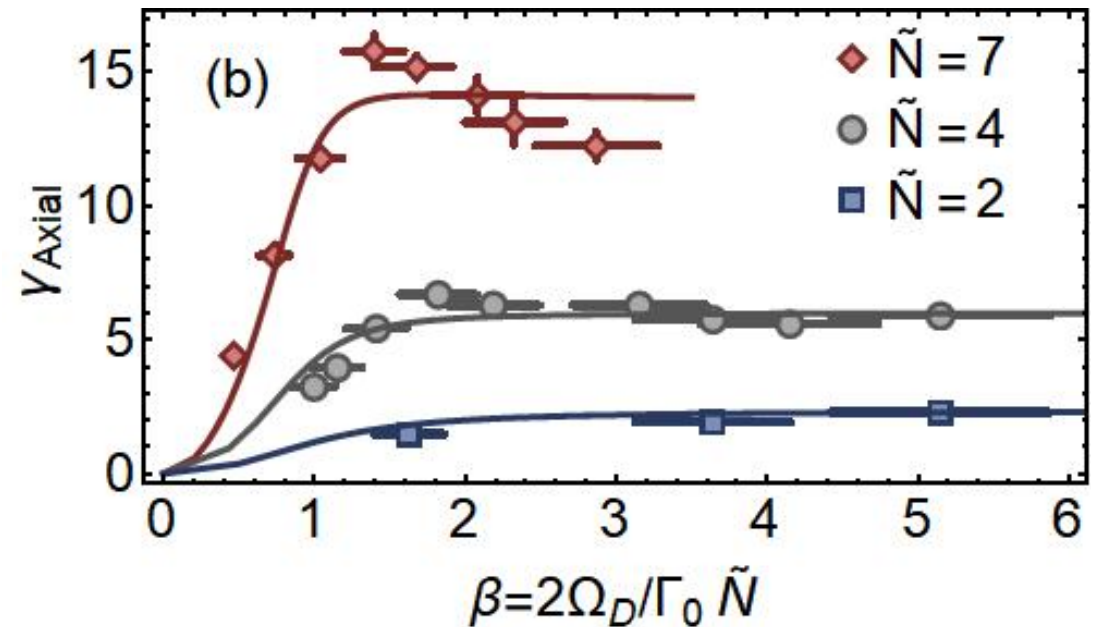
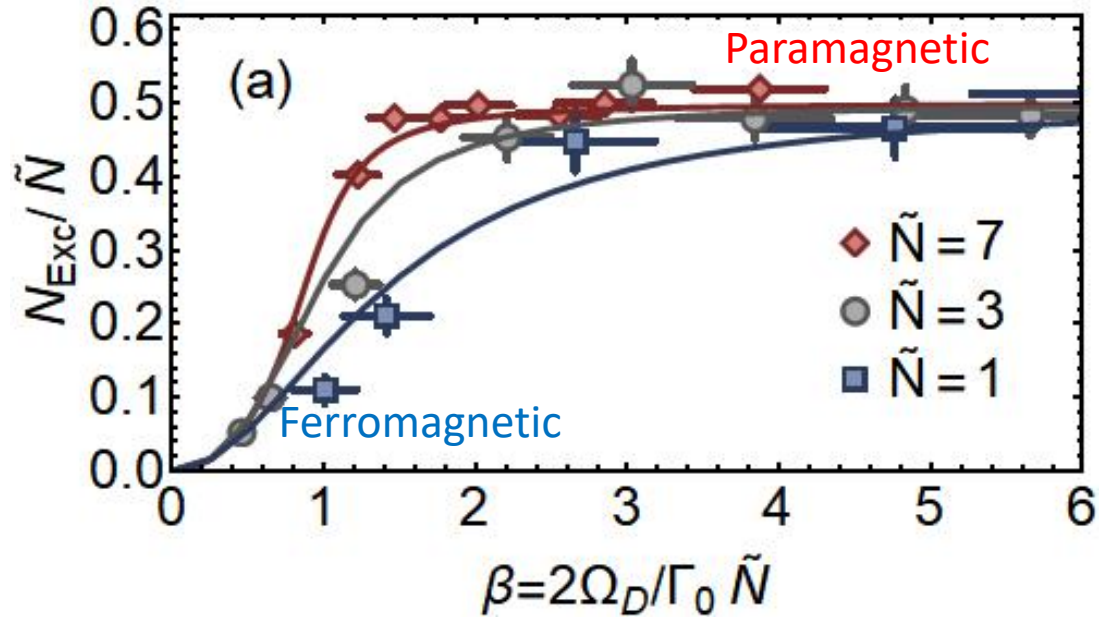
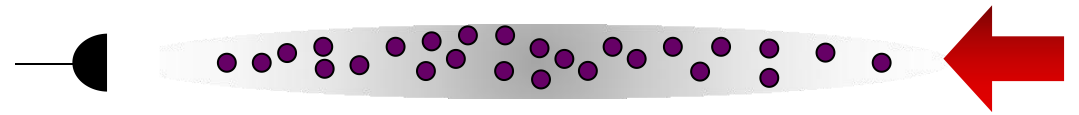
Steady-State properties

Natural "scale" : $\beta = \frac{2}{\Gamma \tilde{N}} \Omega_D$ ^{driving}

Excitations hosted in the atoms



Photons emitted in the superradiant mode

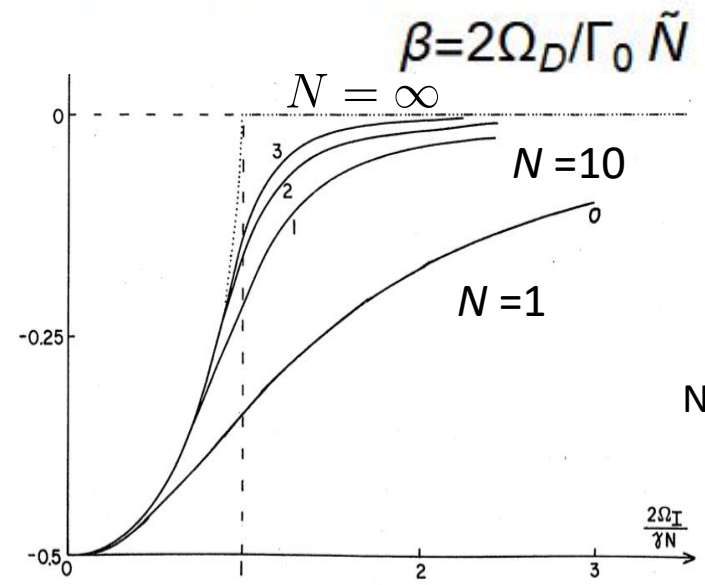
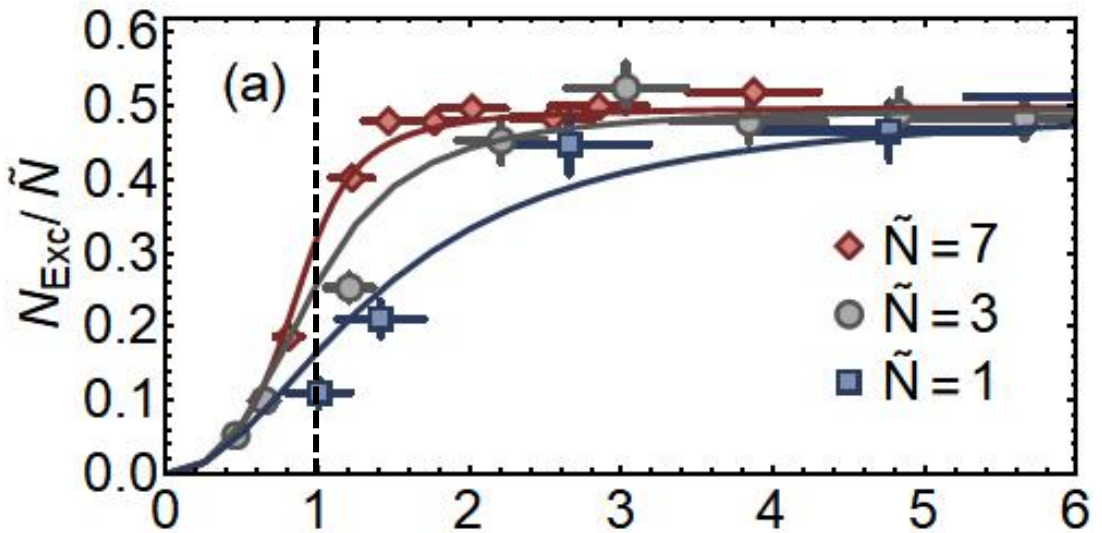


Preliminary results

Steady-State properties

Preliminary results

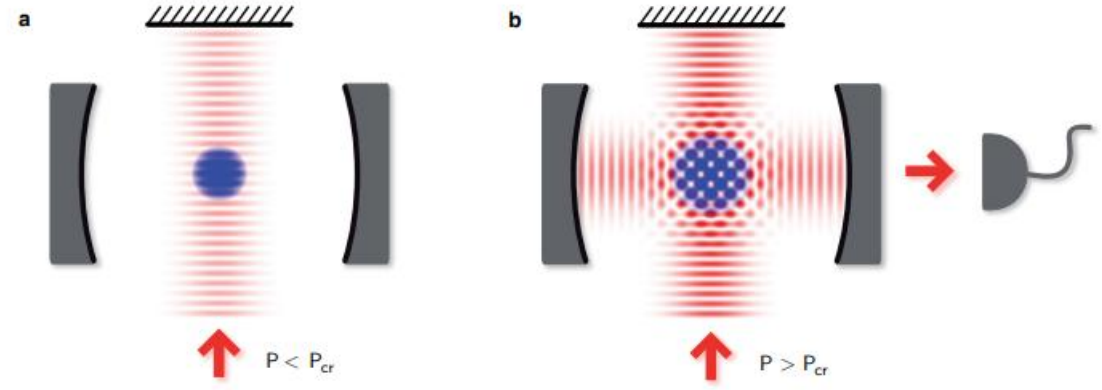
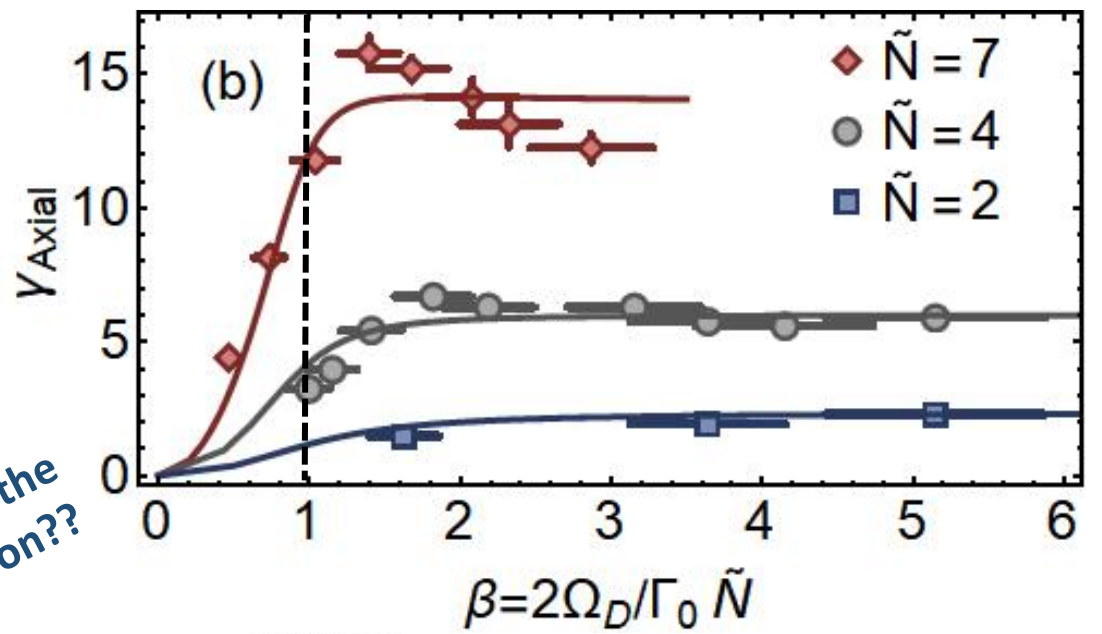
Atomic part



Observation of the onset of the superradiant phase transition??

Narducci, PRA 1978

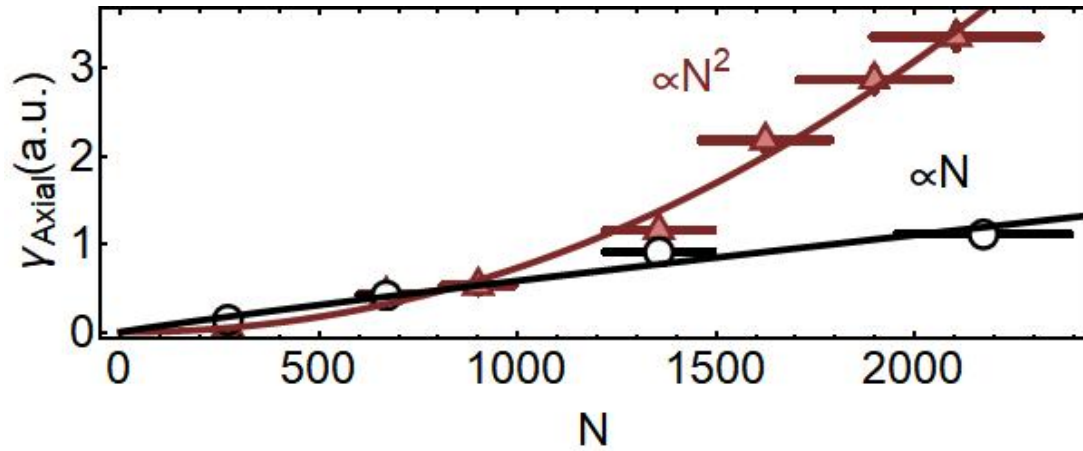
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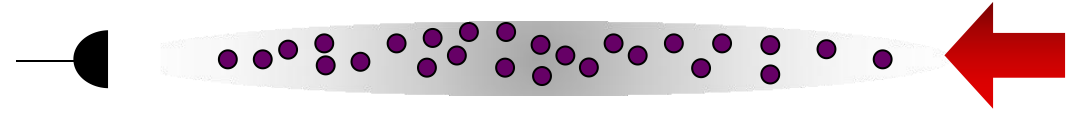
Esslinger team, Nature 2012

Superradiant Phase-Transition in steady-state

Can we really observe two different phases?



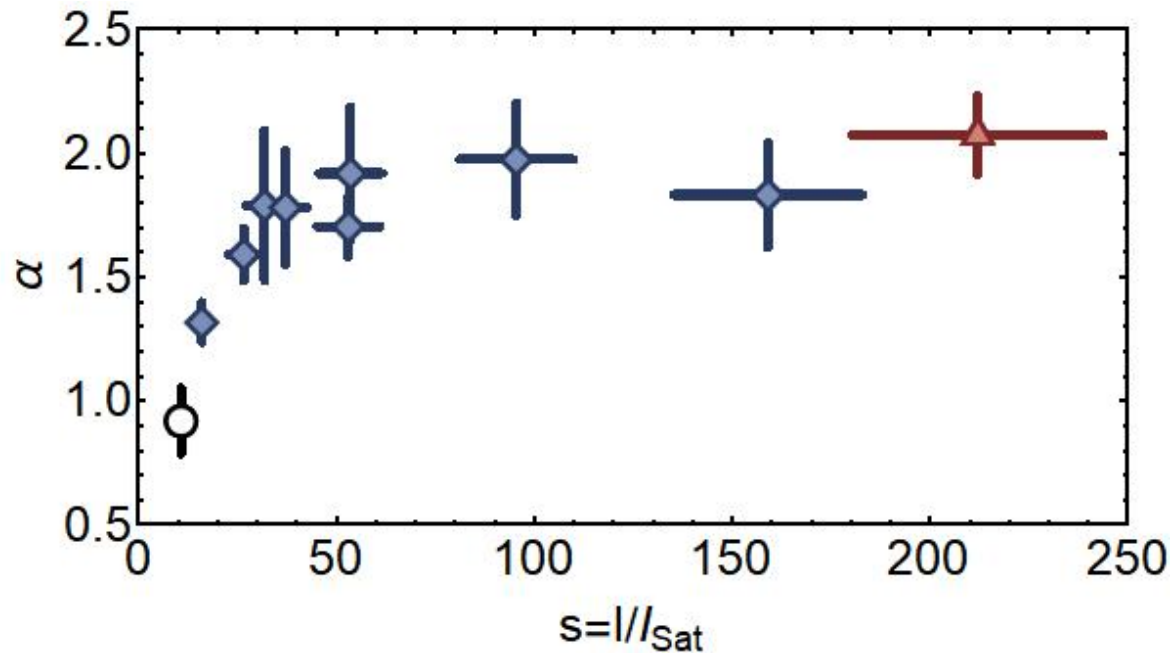
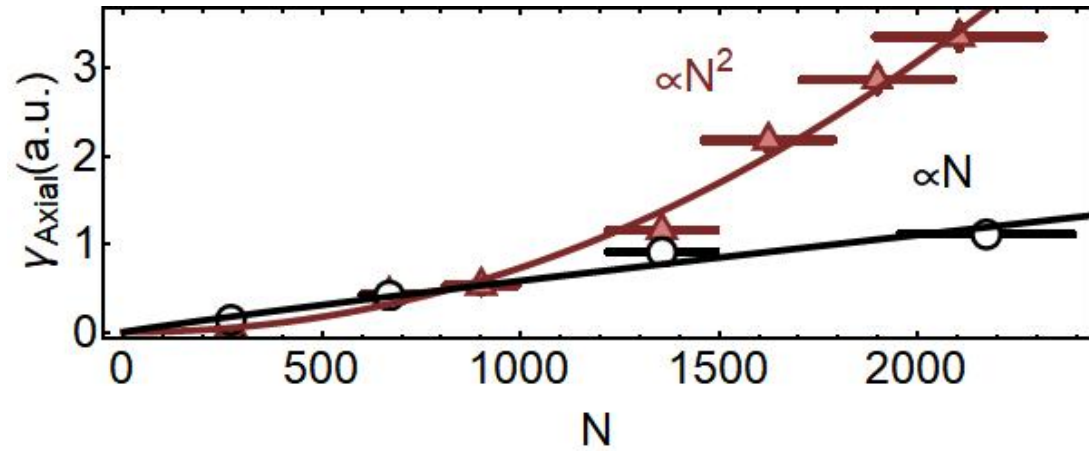
Preliminary results



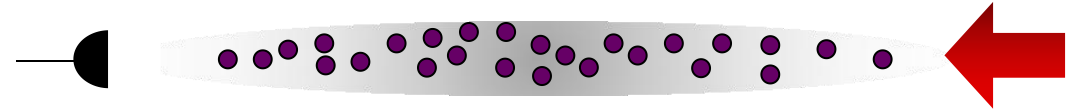
Crossing-over to a superradiant phase driven by the strength of the pump

Superradiant Phase-Transition in steady-state

Can we really observe two different phases?



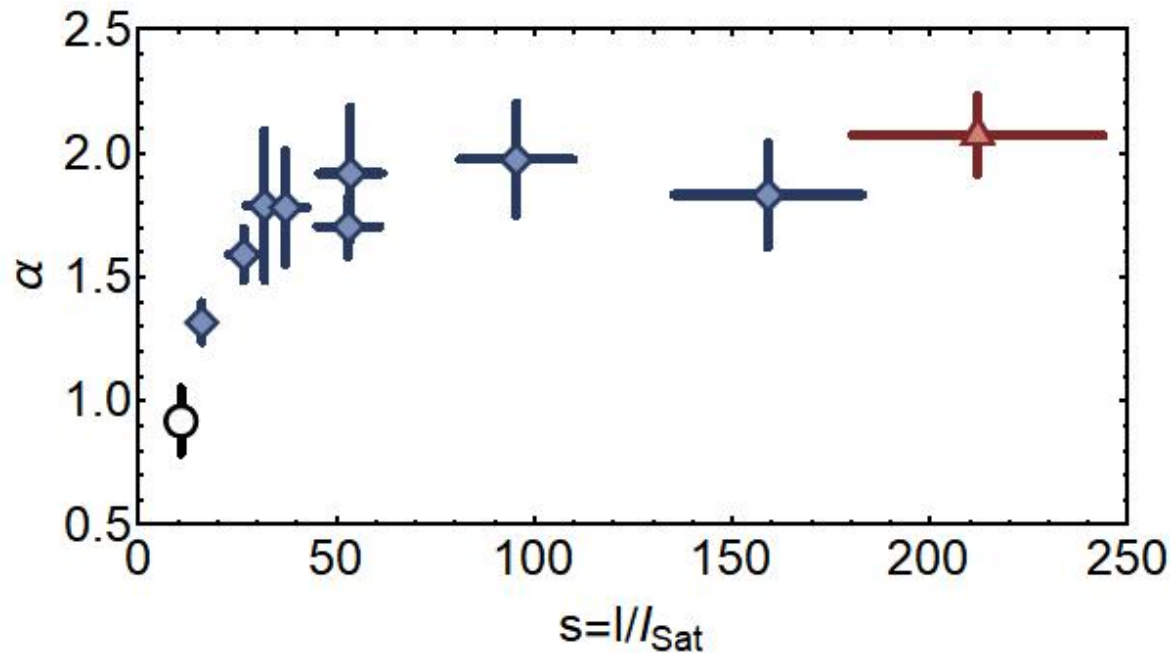
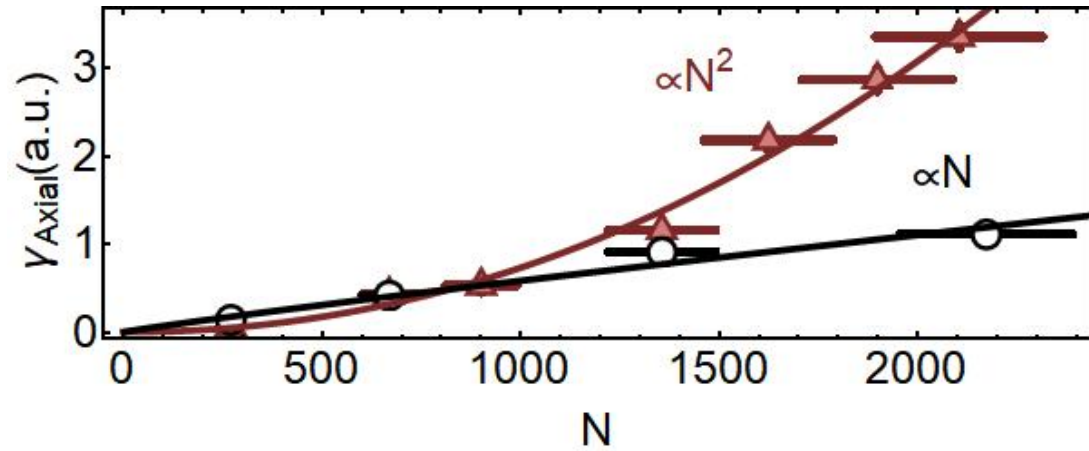
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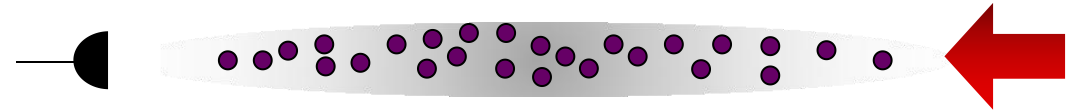
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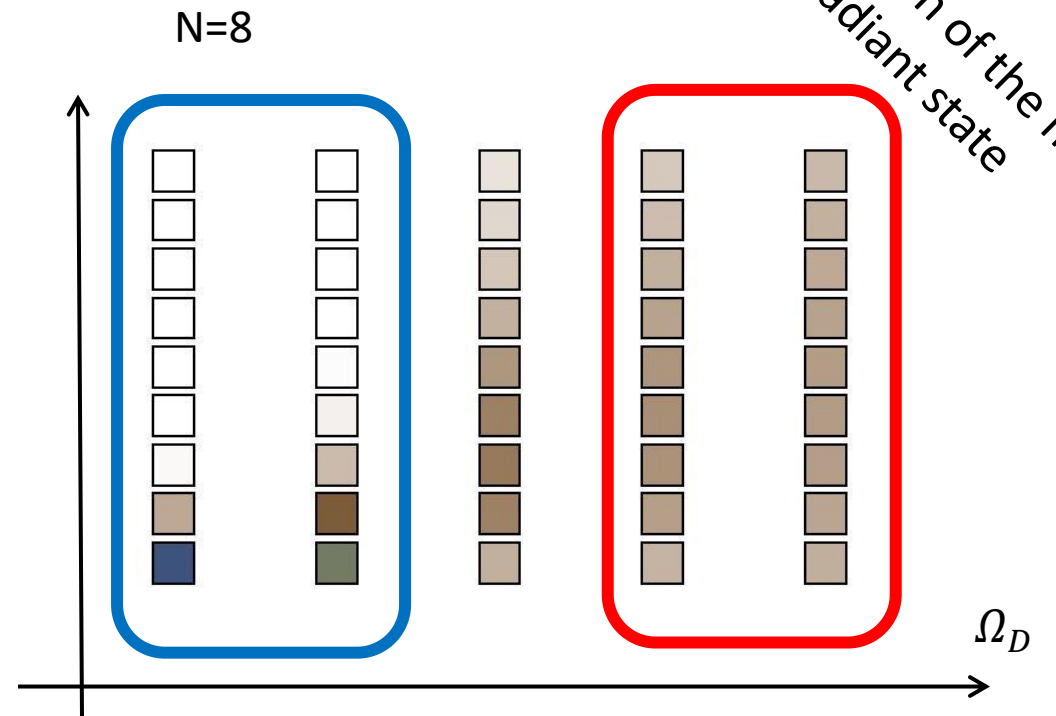


Preliminary results



Crossing-over to a superradiant phase driven by the strength of the pump

macroscopic occupation of the most superradiant state

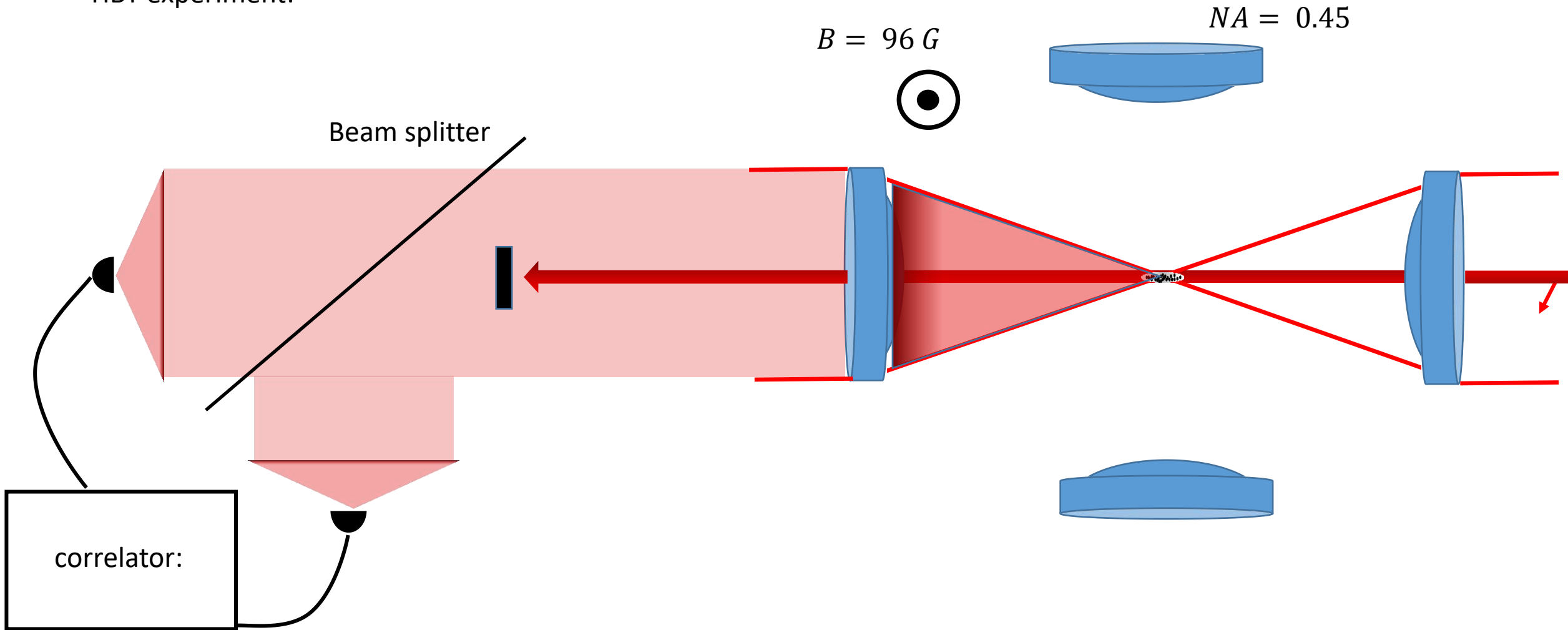


Intensity correlation

Preliminary results

Superradiance is originated by correlations, are they present also in the light emitted?

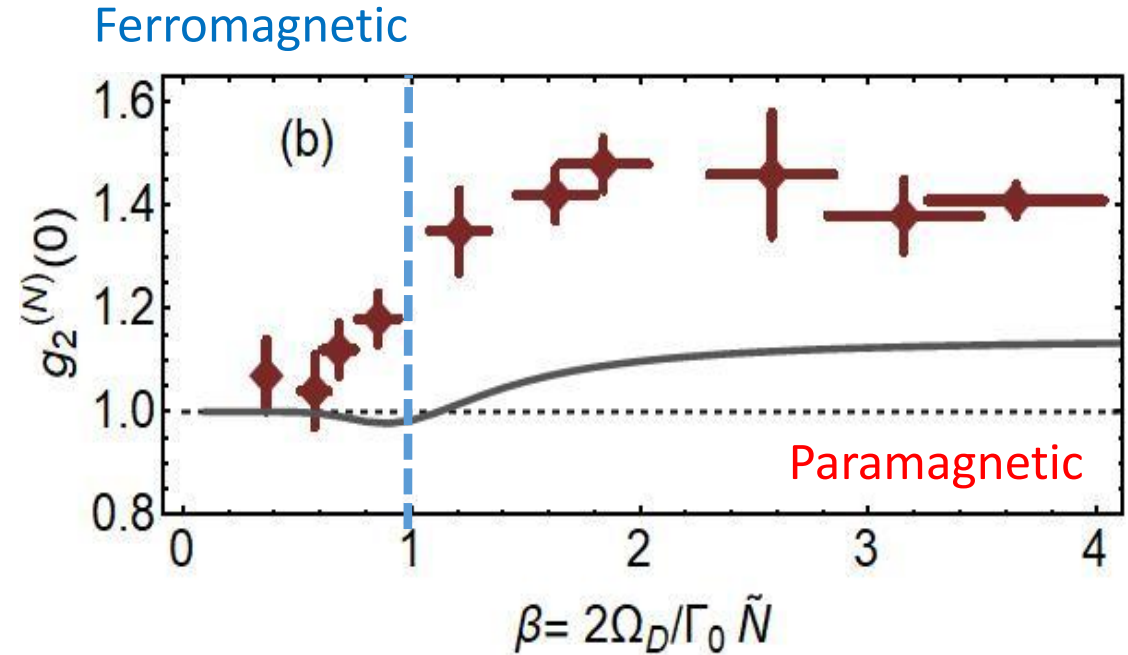
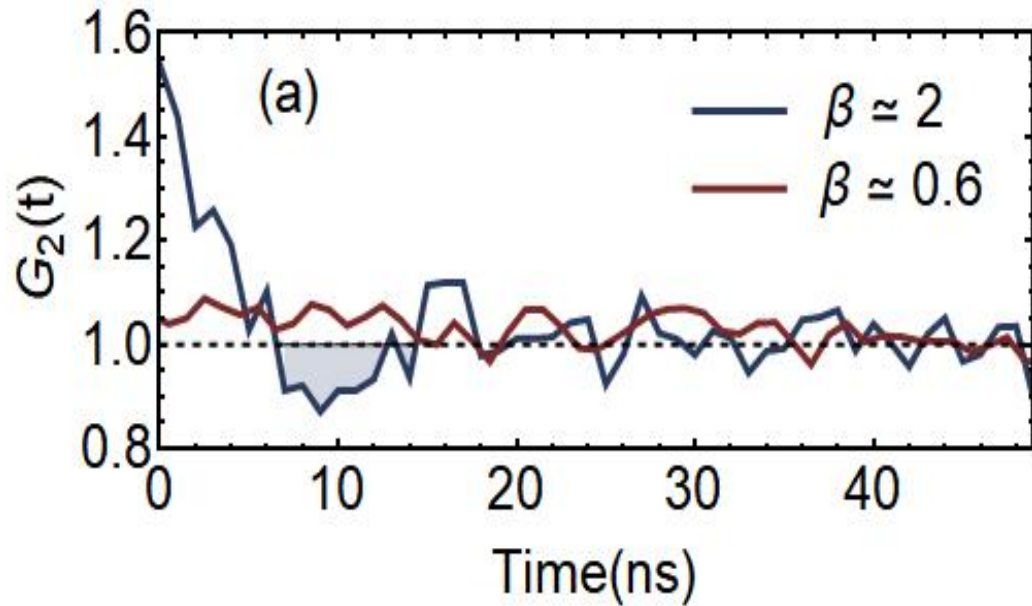
HBT experiment:



Intensity correlation

Preliminary results

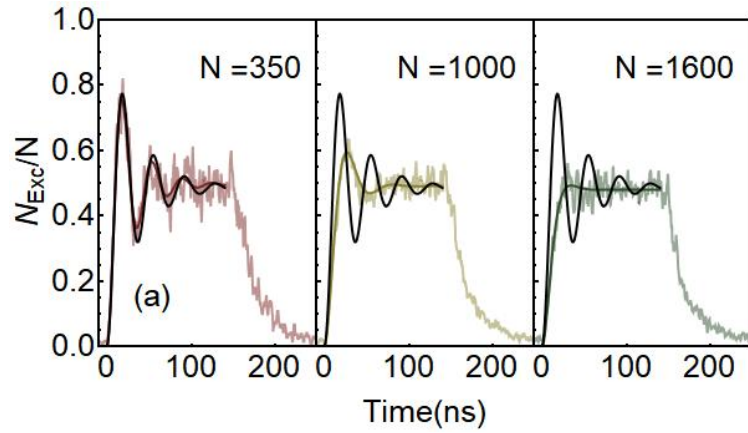
Superradiance is originated by correlations, are they present also in the light emitted?



Violation of Siegert relation: correlated system

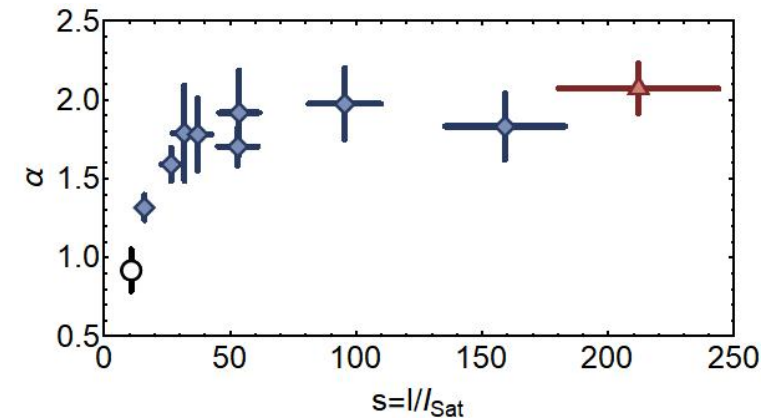
Two phases possess also different photon statistic

Conclusions

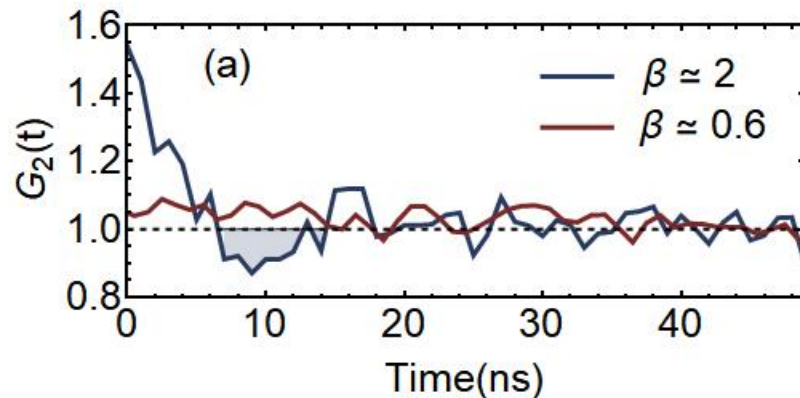


(1) first experimental observation of Driven-Dicke model in free space and observation of the collective screening effect

(2) observation of crossing over to a superradiant phase driven by the pump strength (as in cQED)



(3) Correlated system (beyond mean field)



Outlooks

(1) Is there a microscopic theoretical justification of the model?

(2) is our system a superradiant laser?

Thanks for the attention!!

Antoine Glicenstein



Igor Ferrier-Barbut



Antoine Browaeys



Collaborators

F. Robicheaux & Tyler Sutherland



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