



JOHANNES GUTENBERG  
UNIVERSITÄT MAINZ



# On the origins of transport in altermagnets

Yuriy Mokrousov

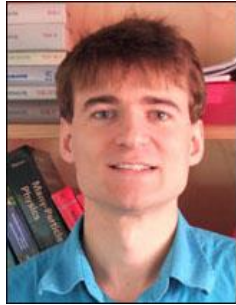
Peter Grünberg Institute, Forschungszentrum Jülich, Germany

Institute of Physics, University of Mainz, Germany

# Thanks



**Thodoris  
Adamantopoulos**



**Frank  
Freimuth**



**Max  
Merte**



**Marjana  
Ležaić**



**Kartik  
Samanta**

**Marjana Ležaić  
Dongwook Go  
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Hongbin Zhang  
Peter Schmitz  
Mahmoud Zeer  
Fabian Lux  
Yugui Yao  
Run-Wu Zhang  
Olena Gomonyay  
Lukasz Plucinski**



**Wanxiang  
Feng**



**Libor  
Šmejkal**



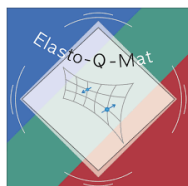
**Xiadong  
Zhou**



**Jairo  
Sinova**



**Stefan  
Blügel**

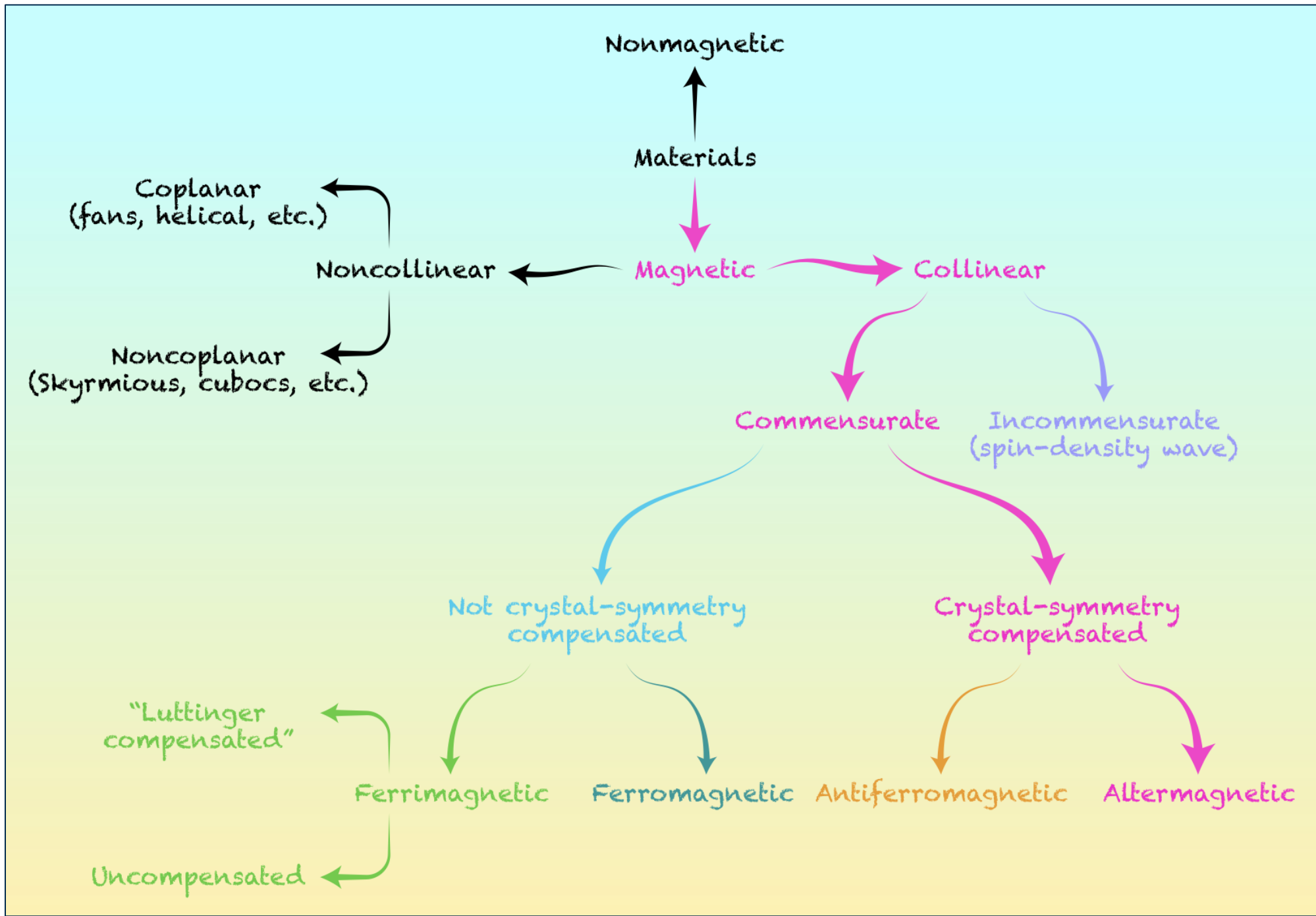


**SPIN+X**  
SFB/TRR 173  
Kaiserslautern • Mainz



**TopDyn**

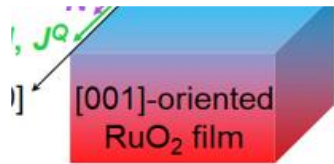
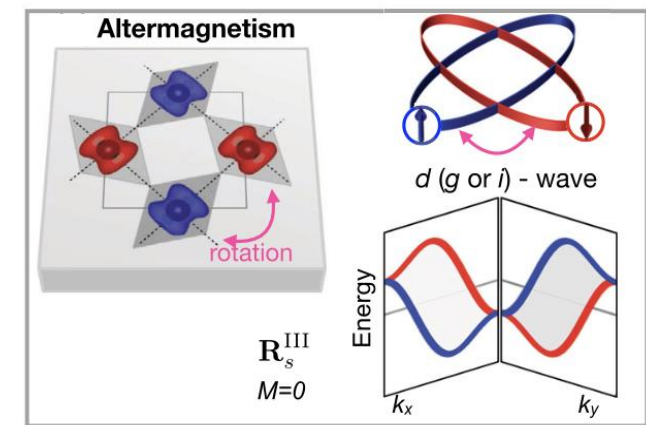
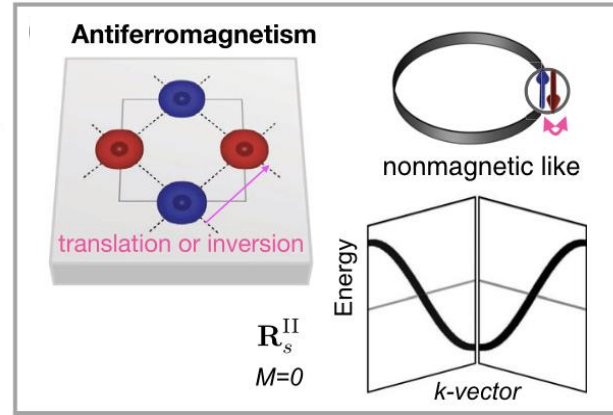
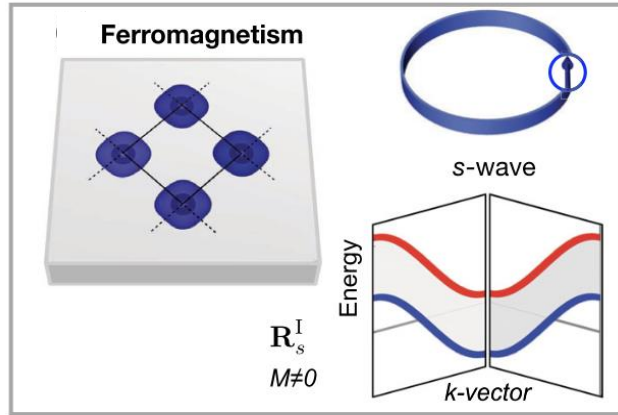




# Altermagnetism

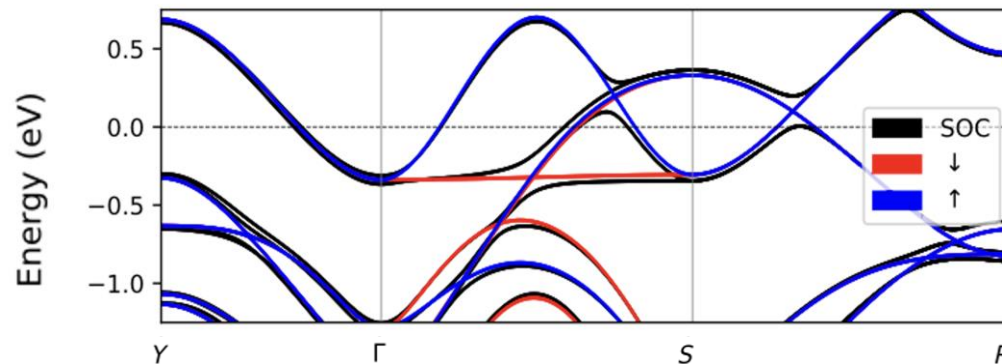
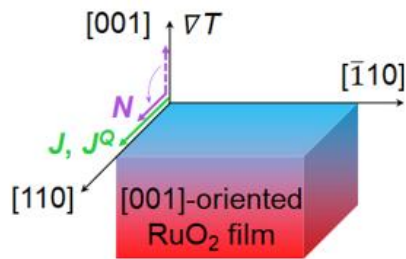
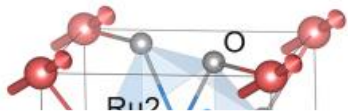
Šmejkal, Sinova & Jungwirth **PRX** 12, 031042 (2022); 12, 040501 (2022)

Libor Šmejkal *et al.* **Sci. Adv.** 6, eaaz8809 (2020)



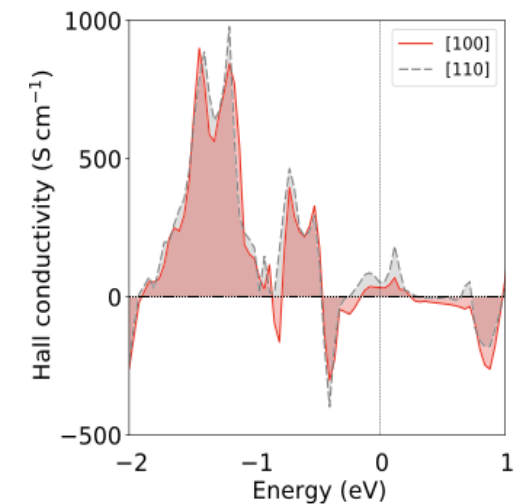
Prototype altermagnet: RuO2

*What drives transport in altermagnets microscopically?*



**Crystal Hall effect**

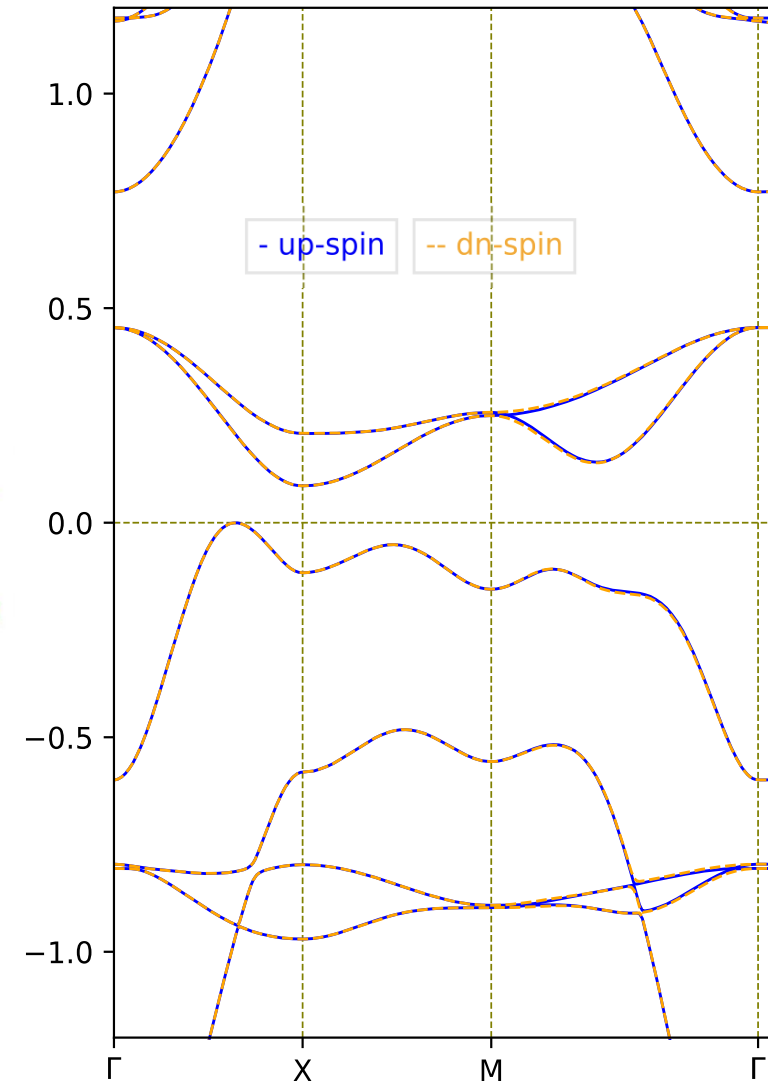
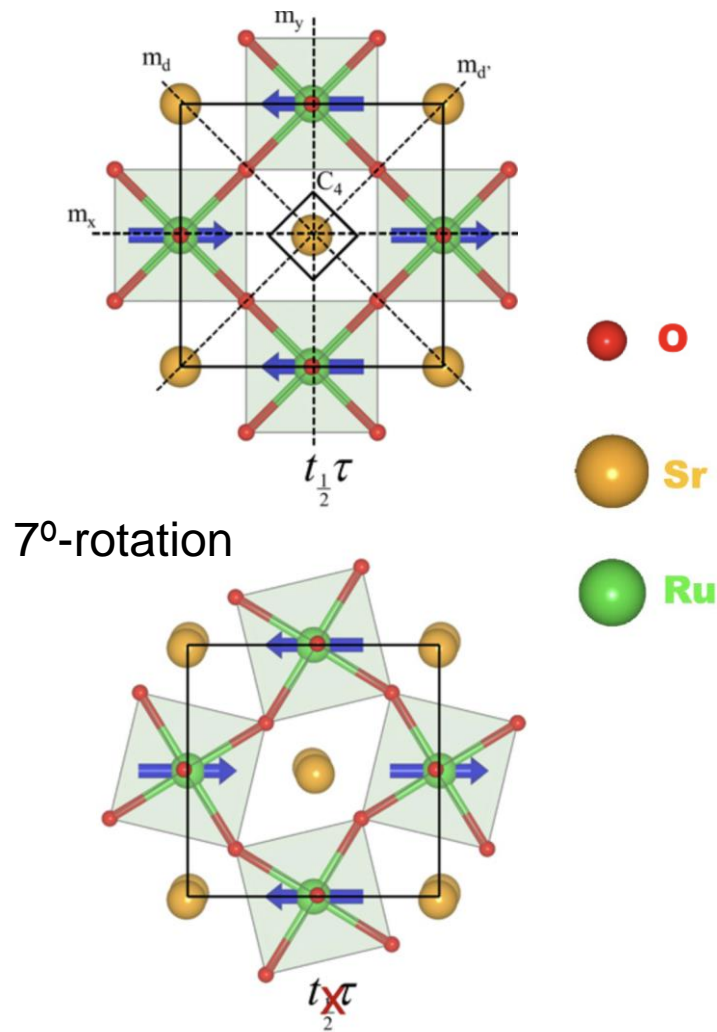
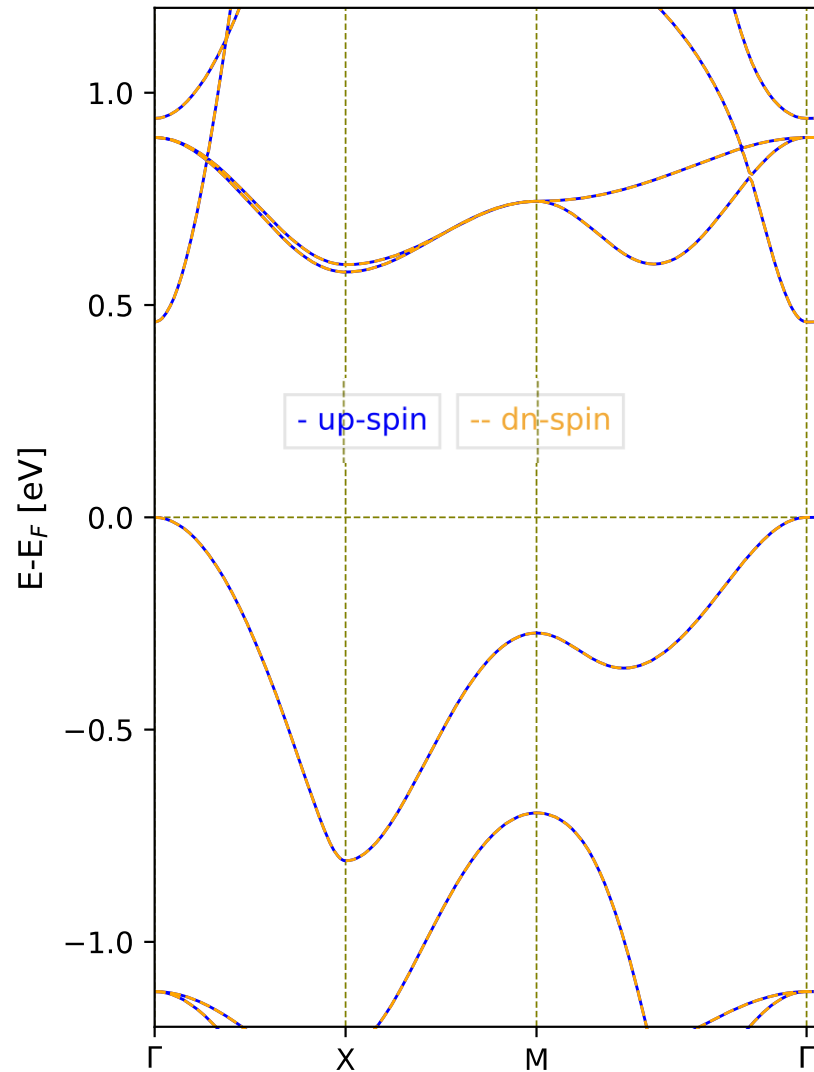
*odd in crystal chirality*



# A case of SrRuO<sub>3</sub>

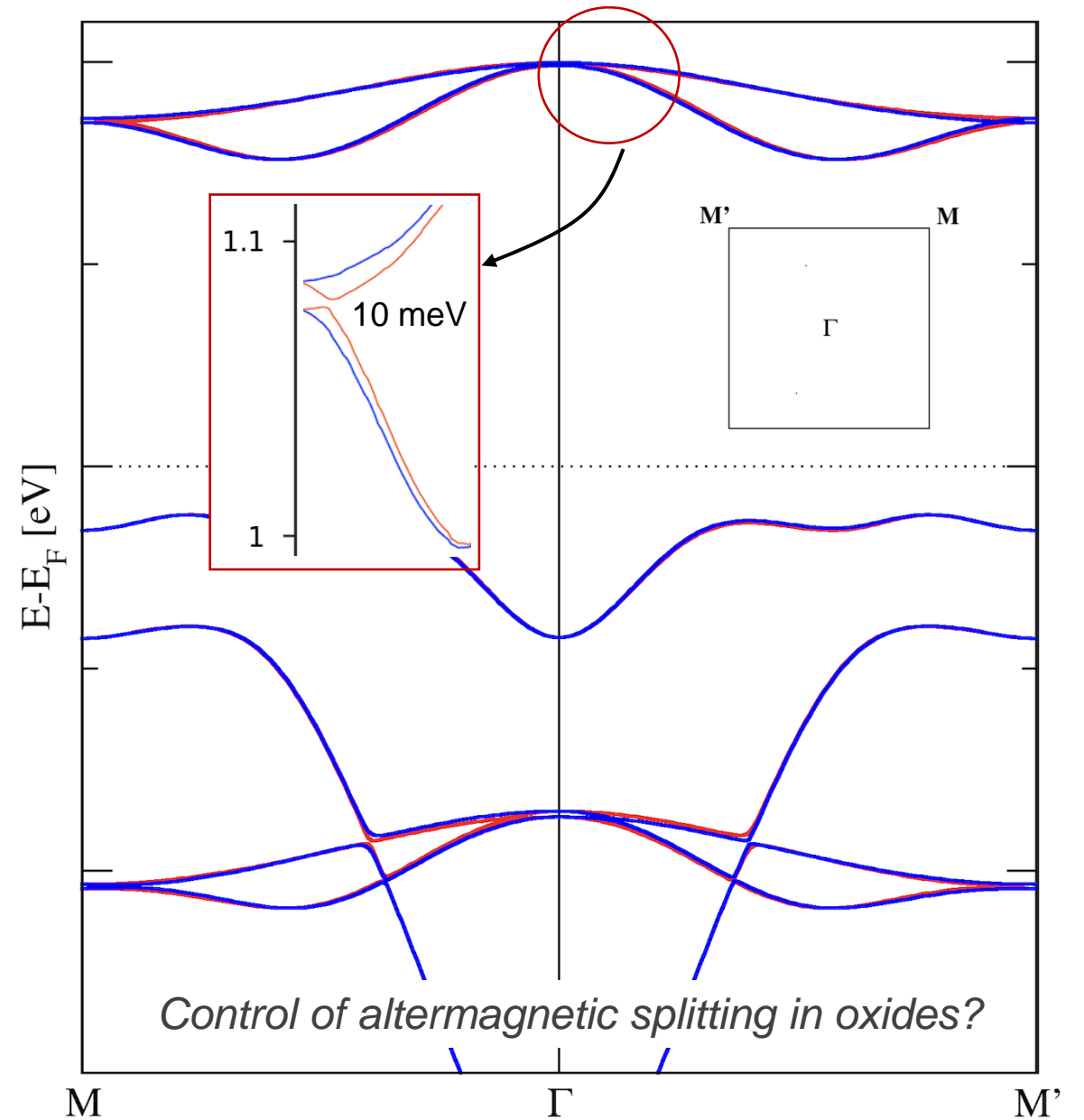
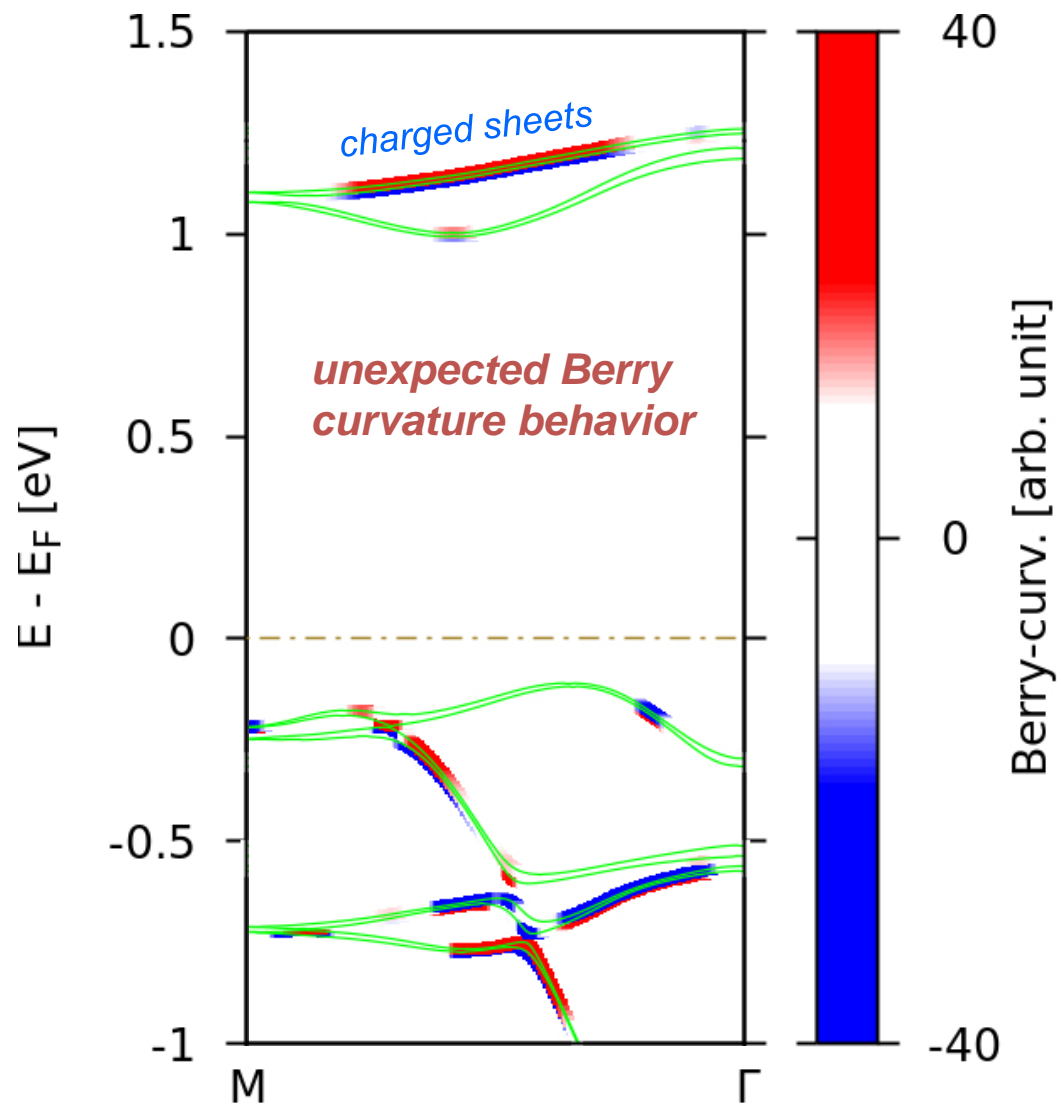
Samanta, Lezaic, Freimuth, Blügel, YM, JAP **127**, 213904 (2020)

Antiferromagnetic up to 4 monolayers  
*Xia et al. PRB 79 (2009)*



# A case of SrRuO<sub>3</sub>

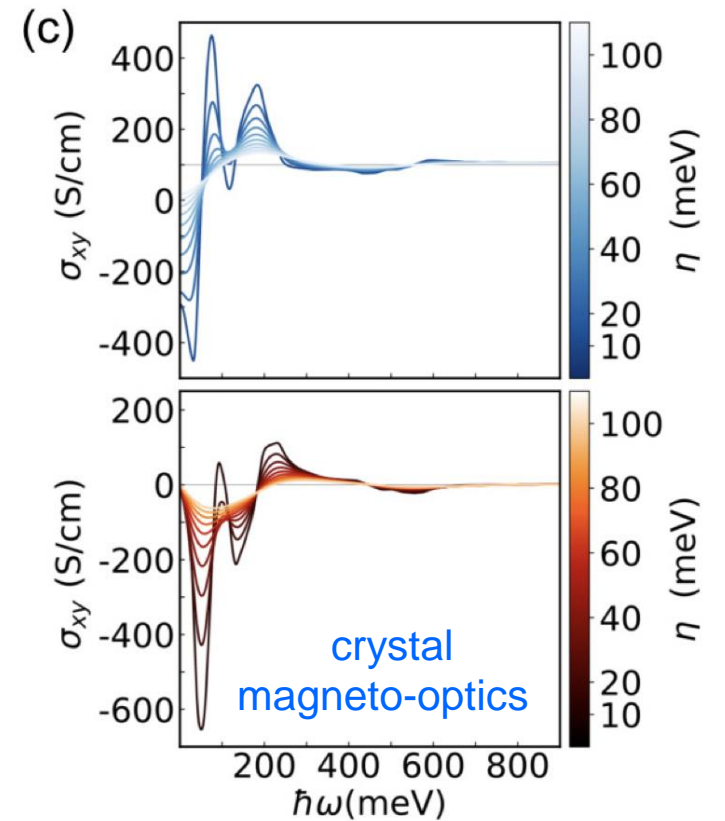
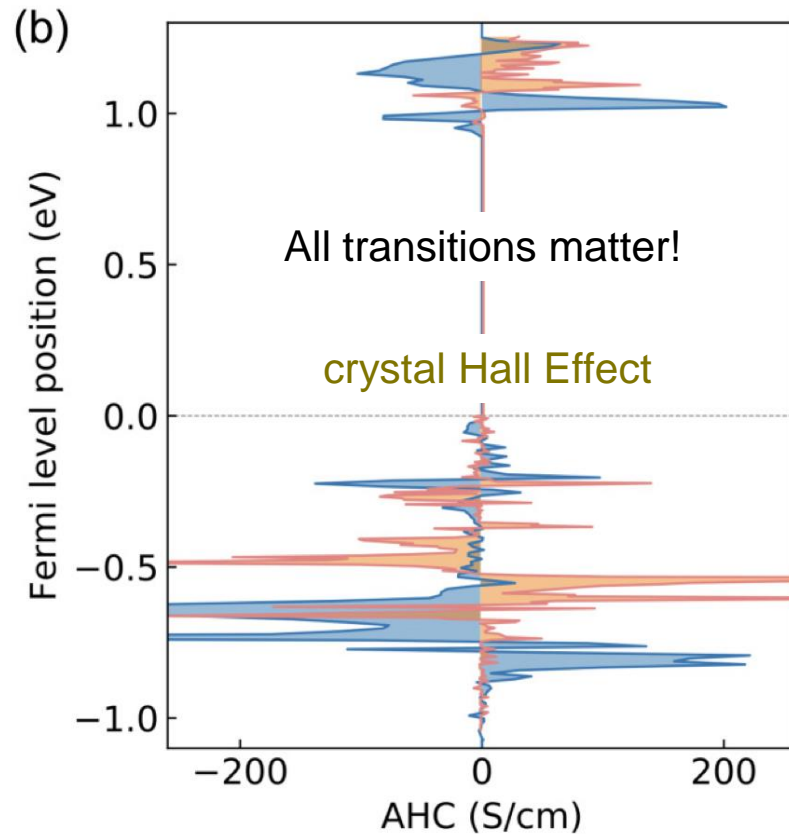
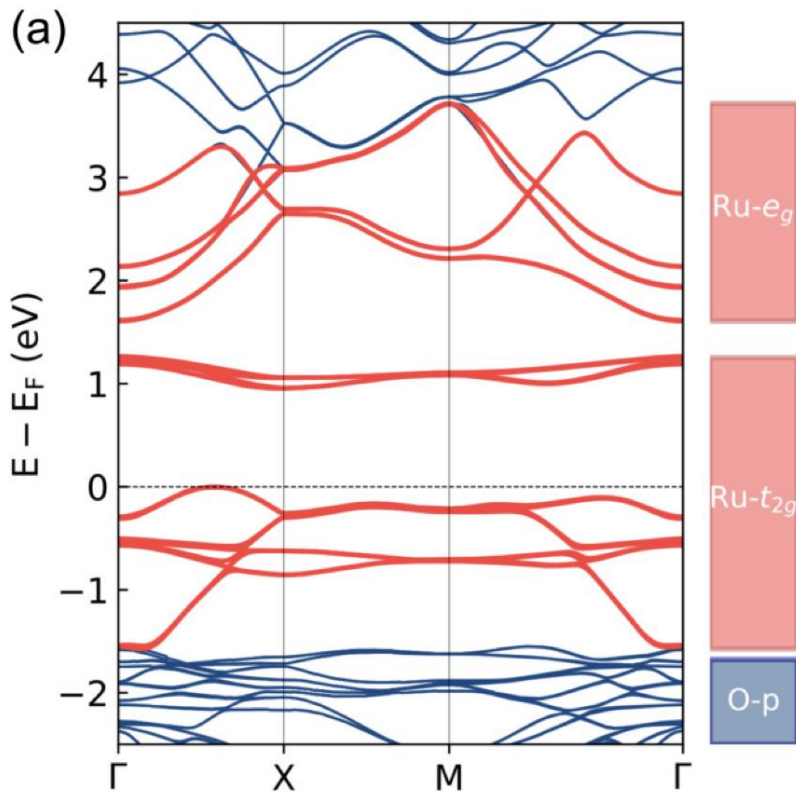
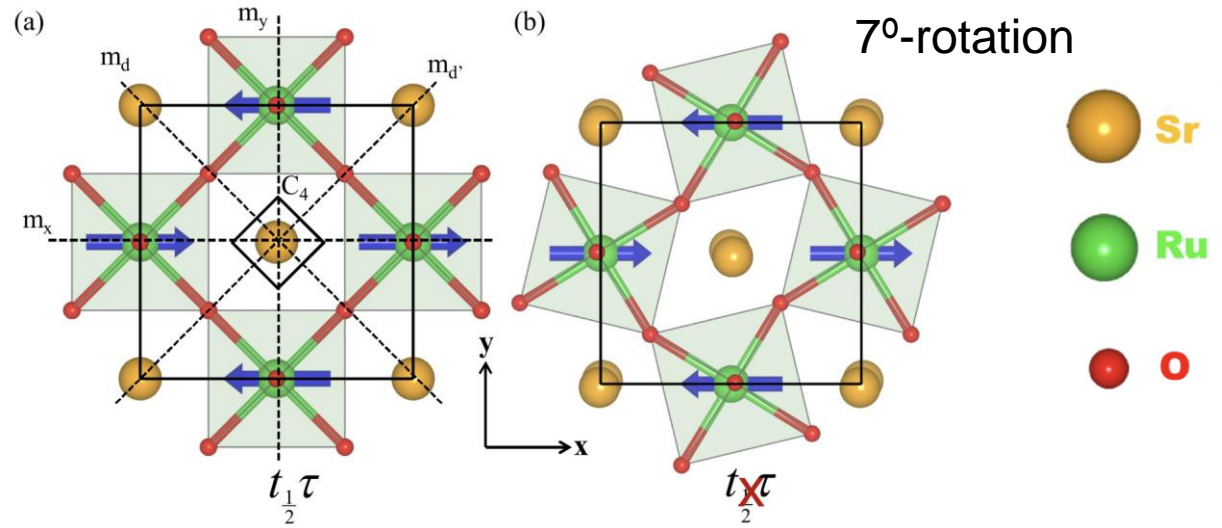
Samanta, Lezaic, Freimuth, Blügel, YM, JAP **127**, 213904 (2020)



# A case of SrRuO<sub>3</sub>

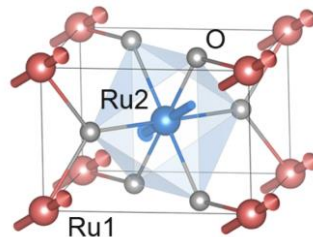
Samanta, Lezaic, Freimuth, Blügel, YM, JAP **127**, 213904 (2020)

Large *crystal Hall effect*  
*crystal magneto-optical effect*  
upon a “mininal” octahedral distortion



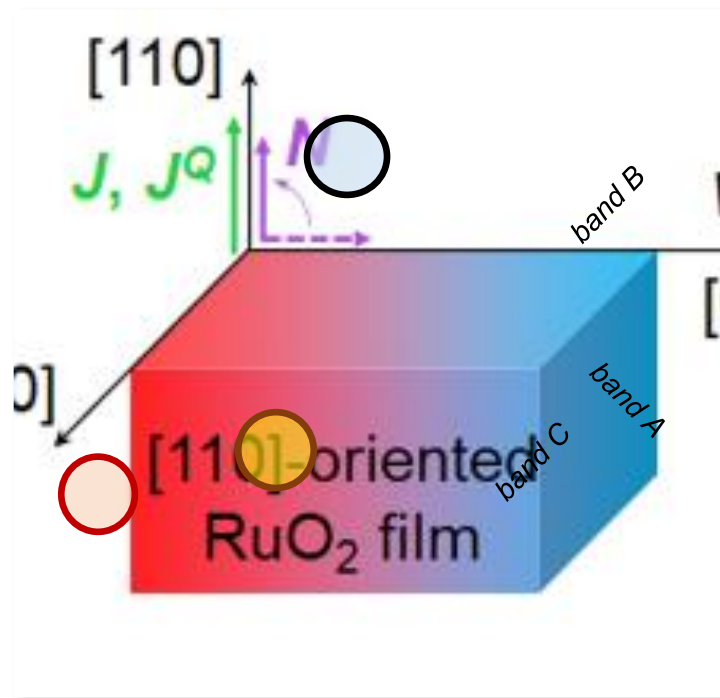
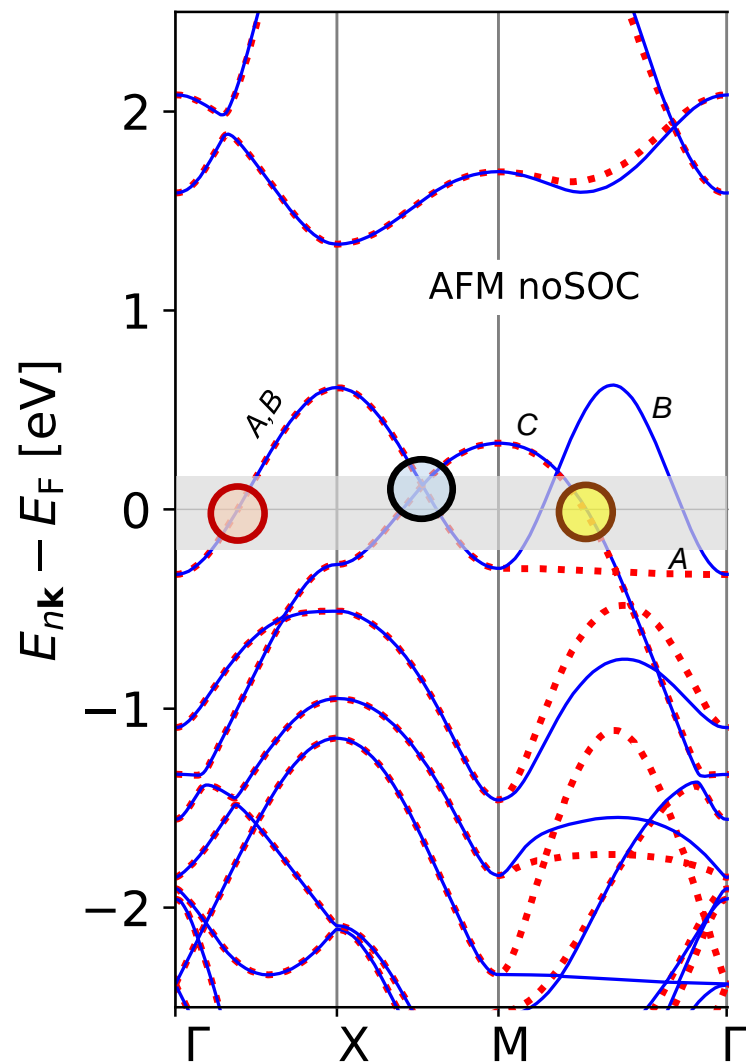
# Band Topology of RuO<sub>2</sub>

Zhou, Feng, LS, JS, YM et al., arXiv:2305.01410

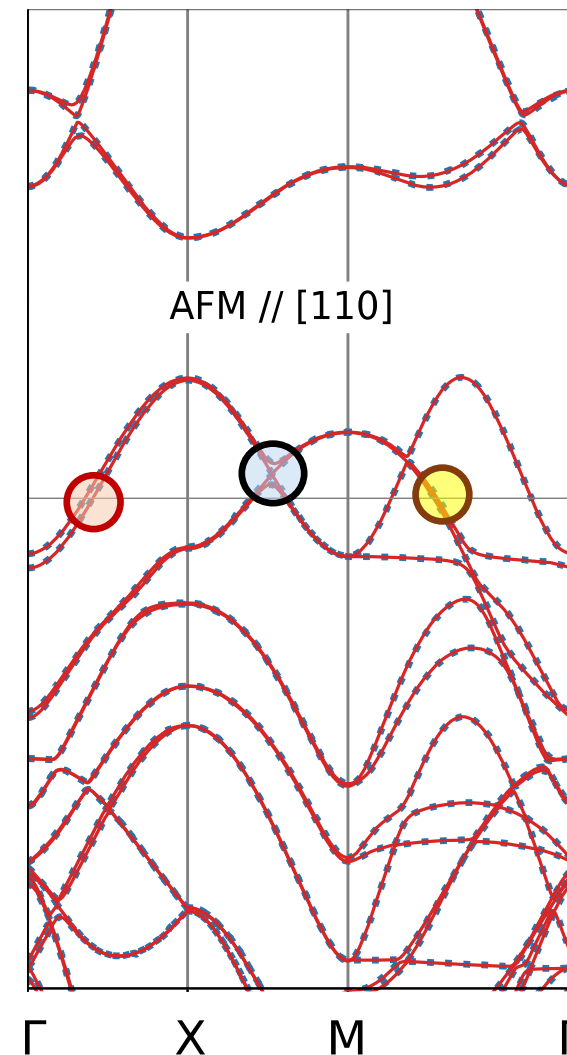


Bands A-B : strong altermagnetism

Bands C : weak altermagnetism



- **Type I** : bands A/B – C
- **Type II** : bands A – B
- **Type III** : bands C

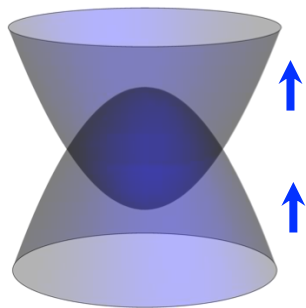




# Altermagnetic Transitions

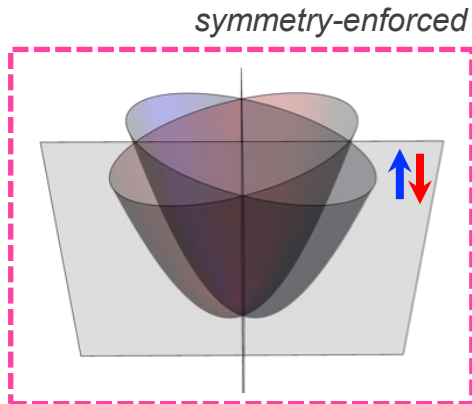
Zhou, Feng, LS, JS, YM et al., arXiv:2305.01410

**Type I**



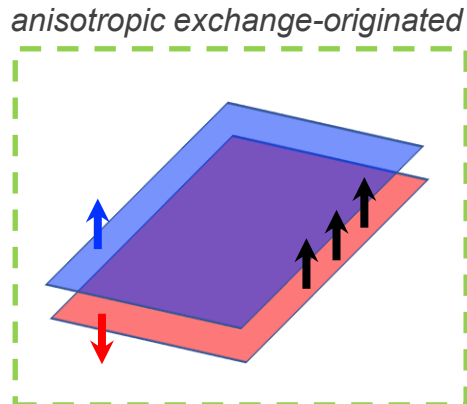
Weyl  
pseudo-nodal lines

**Type II**

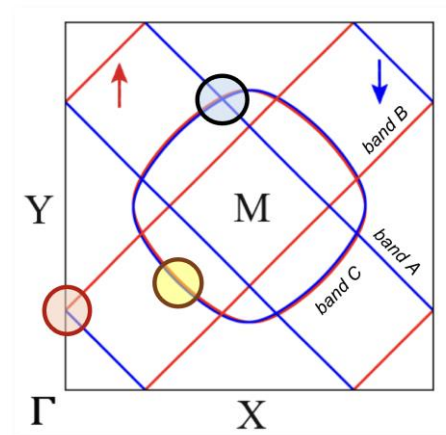


Strong altermagnetism  
pseudo-nodal surfaces

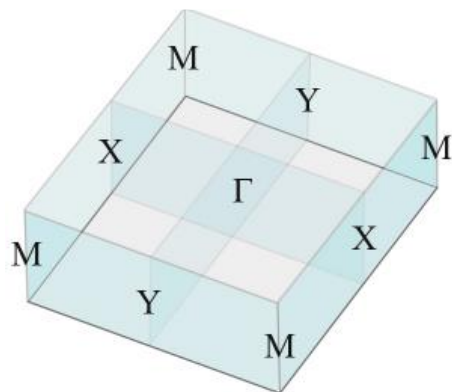
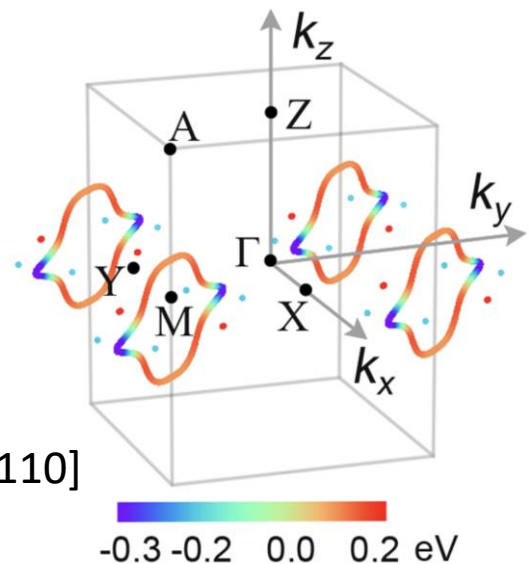
**Type III**



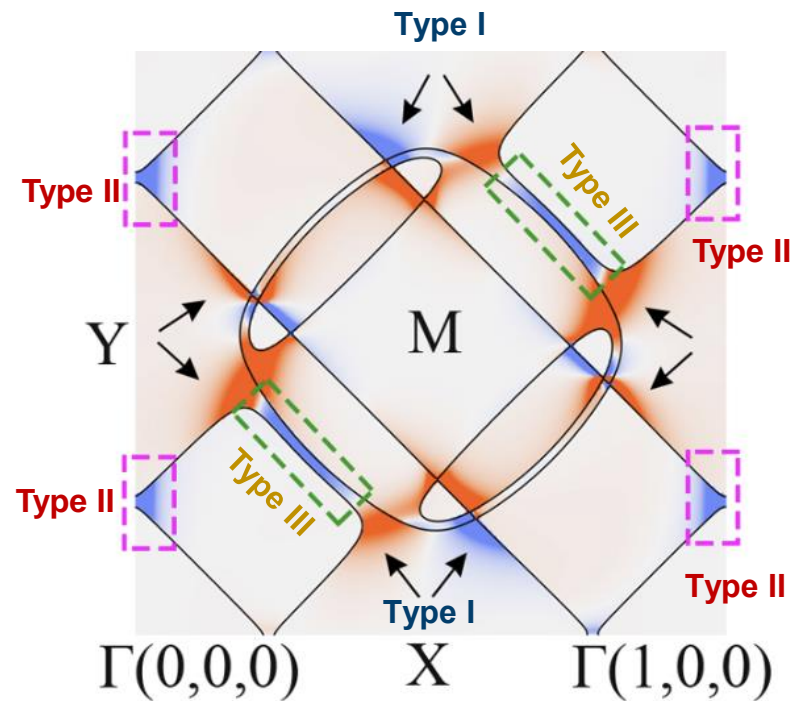
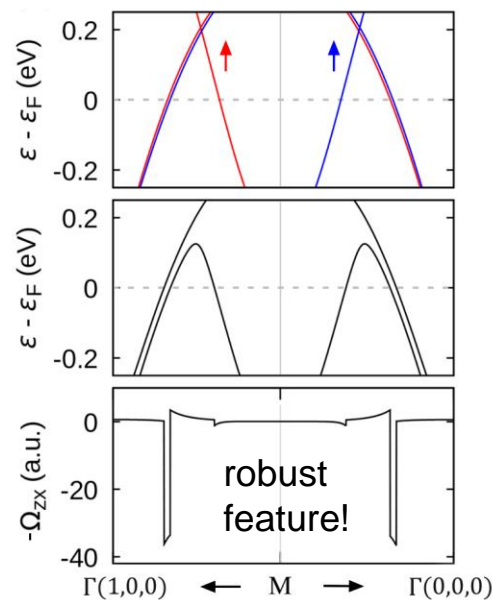
Ladder transitions  
weak altermagnetism



$N \parallel [110]$



Type II and III :  
altermagnetic!



# Spin-flip and spin-conserving AHE

$$\mathbf{L} \cdot \mathbf{S} = L_{\hat{n}} S_{\hat{n}} + \frac{1}{2} (L_{\hat{n}}^+ S_{\hat{n}}^- + L_{\hat{n}}^- S_{\hat{n}}^+) \Rightarrow \sigma_H = \sigma^{\uparrow} \pm \sigma^{\downarrow}?$$

- spin relaxation phenomena
- proper definition of the spin current

Shi *et al.*, PRL **96**, 76604 (2006)

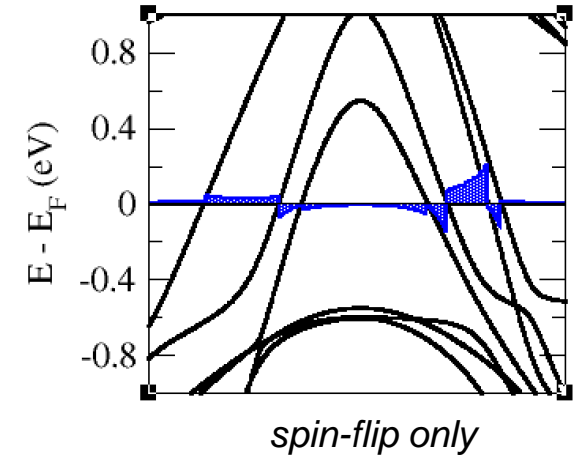
Gradhand *et al.*, PRL **104**, 186403 (2010)

netic metals [4]). The second mechanism involves spin-orbit driven transitions between bands with similar dispersion which are split in energy across the Fermi level. We shall refer to them as **ladder transitions**. Both occur at low frequencies, of the order of the spin-orbit coupling strength.

Zhang, Freimuth, Blügel, Souza, Mokrousov, PRL **106**, 117202 (2011)

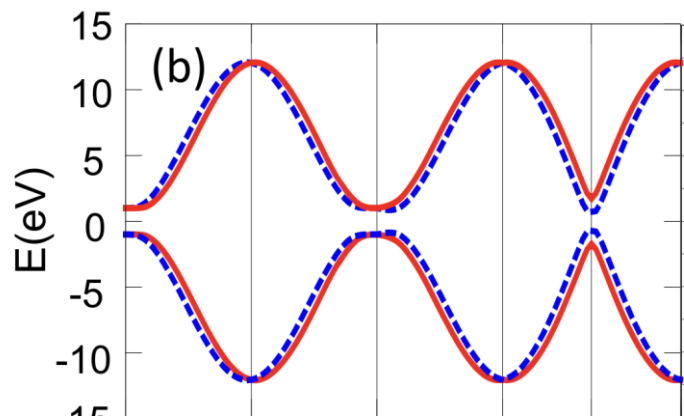
$$\sigma_z = \frac{e^2 \hbar}{4\pi^3} \text{Im} \int_{\text{BZ}} d\mathbf{k} \sum_{n,m}^{o,e} \frac{\langle \psi_{n\mathbf{k}} | v_x | \psi_{m\mathbf{k}} \rangle \langle \psi_{m\mathbf{k}} | v_y | \psi_{n\mathbf{k}} \rangle}{(\epsilon_{m\mathbf{k}} - \epsilon_{n\mathbf{k}})^2}$$

L1<sub>0</sub> FePt

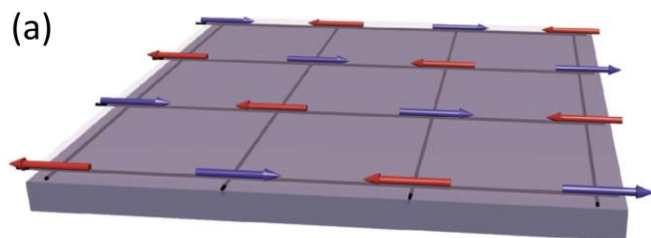


*spectral AHC*

**Psi-K Workshop,  
Halle, 2011**



SOC ↔ crystal symmetry



Chiral Hall effect in  
AFM

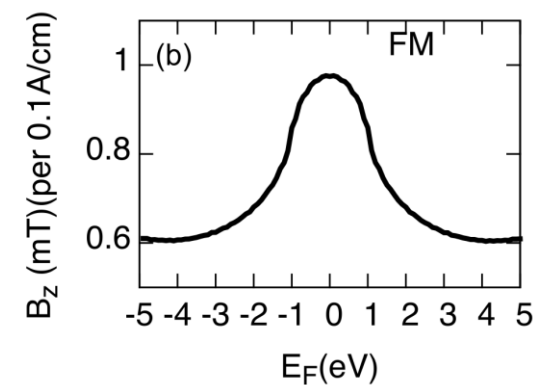
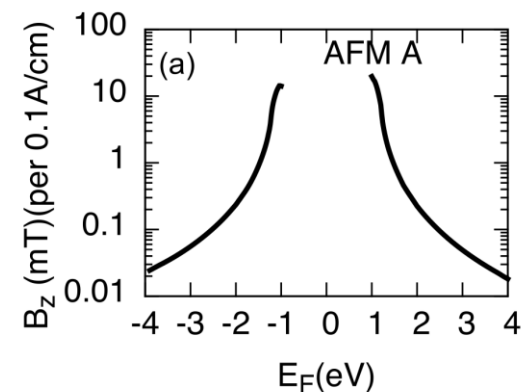
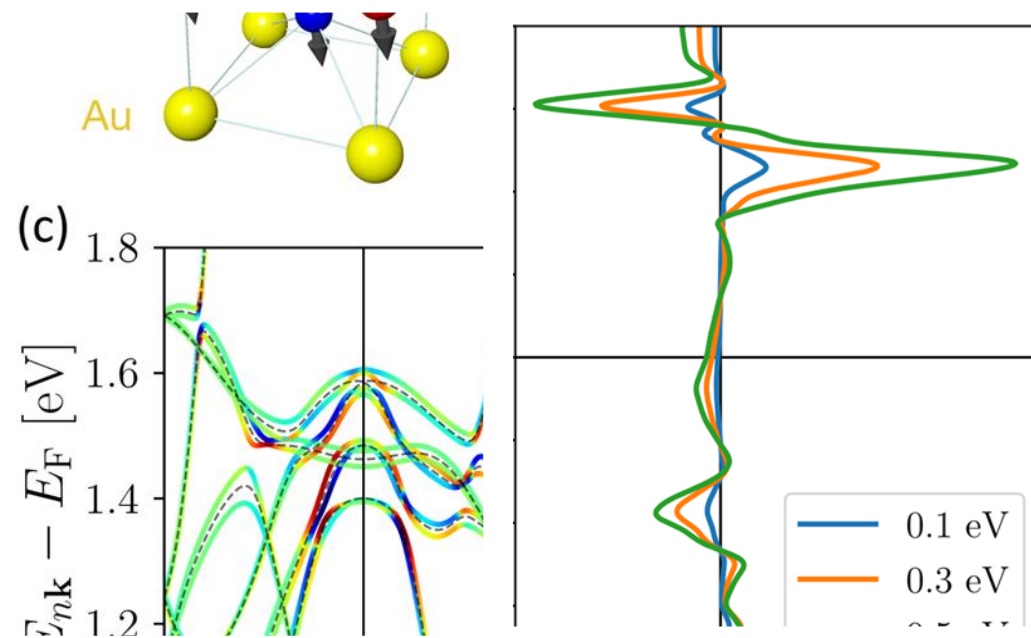
canting ↔ crystal symmetry  
can be gigantic

Kipp, YM et al. Comm. Phys. 4, 99 (2021)

### Relativistic Néel-Order Fields Induced by Electrical Current in Antiferromagnets

J. Železný,<sup>1,2</sup> H. Gao,<sup>3</sup> K. Výborný,<sup>1</sup> J. Zemen,<sup>4</sup> J. Mašek,<sup>5</sup> Aurélien Manchon,<sup>6</sup> J. Wunderlich,<sup>1,7</sup>  
Jairo Sinova,<sup>8,1,3</sup> and T. Jungwirth<sup>1,9</sup>

spin-axis angles, as shown in Figs. 3(e) and 3(f). Another important feature, illustrated in Figs. 4(a) and 4(b), is that the interband NSOT in the AFM can be significantly larger than its FM SOT counterpart. The interband nature of the term  $\delta\vec{s}^{\text{inter}}$  from Eq. (5) implies that its magnitude is large when two subbands linked by spin-orbit coupling have a small energy spacing. In the calculations shown in Figs. 3(e) and



Ladder transitions  
are universal

# Type II, III : Spin-flip Transitions

YM, Zhang, Freimuth et al., JPCM **25**, 163201 (2013)

$$\frac{\xi}{(\varepsilon_n^{(1)} - \varepsilon_m^{(1)})^2} \langle \psi_{n,0}^{\sigma'} | v_x | \psi_{m,0}^{\sigma} \rangle \quad LS^{\uparrow\uparrow}$$

$$\times \sum_{l \neq n; \sigma''} \frac{\langle \psi_{l,0}^{\sigma''} | \mathbf{L} \cdot \mathbf{S} | \psi_{n,0}^{\sigma'} \rangle}{\varepsilon_{n,0} - \varepsilon_{l,0}} \langle \psi_{m,0}^{\sigma} | v_y | \psi_{l,0}^{\sigma''} \rangle$$

1<sup>st</sup> order perturbation theory: **purely spin-conserving**

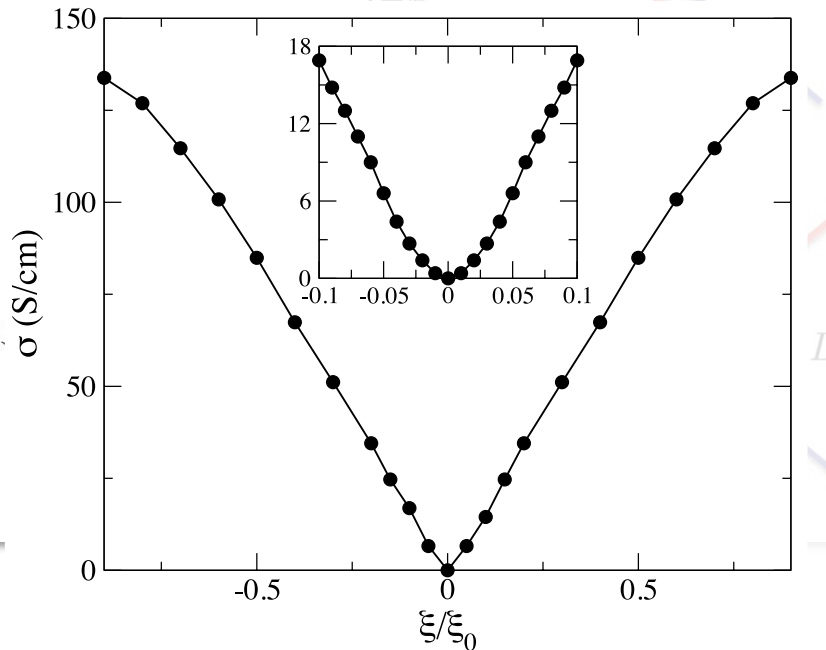
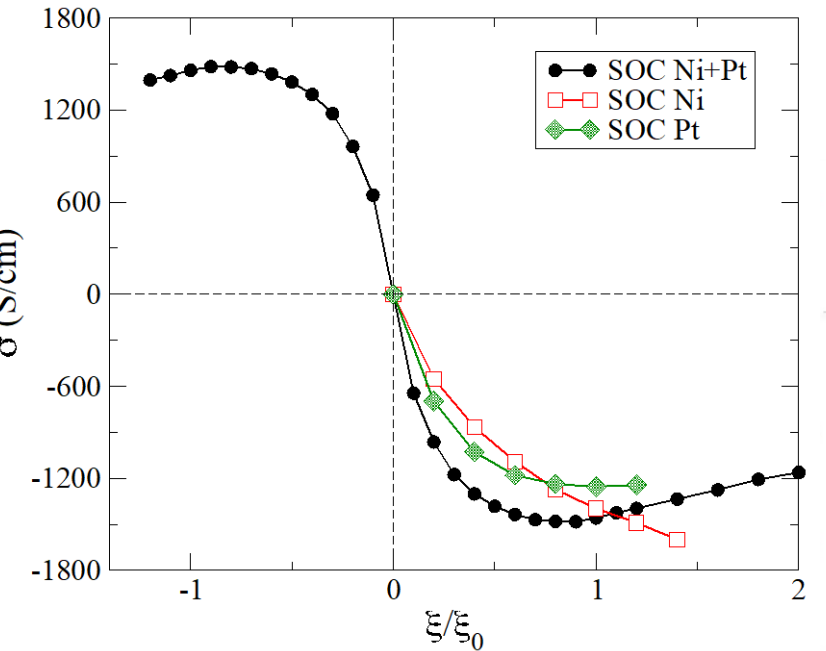
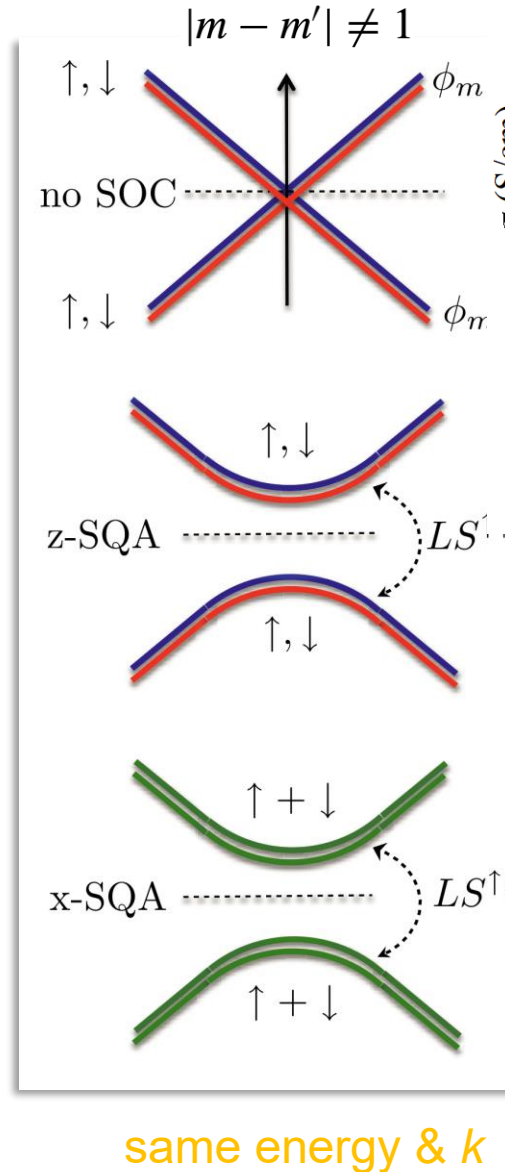
**Strong anisotropy expected**

*Fermi surface, properties*

2<sup>nd</sup> order perturbation theory: **purely spin-flip**

$$\frac{\xi^2}{(\varepsilon_n^{(1)} - \varepsilon_m^{(1)})^2} \sum_{p \neq m; \sigma'''} \frac{\langle \psi_{p,0}^{\sigma'''} | \mathbf{L} \cdot \mathbf{S} | \psi_{m,0}^{\sigma} \rangle}{\varepsilon_{m,0} - \varepsilon_{p,0}} \langle \psi_{n,0}^{\sigma'} | v_x | \psi_{p,0}^{\sigma'''} \rangle$$

$$LS^{\uparrow\downarrow} \times \sum_{l \neq n; \sigma''} \frac{\langle \psi_{l,0}^{\sigma''} | \mathbf{L} \cdot \mathbf{S} | \psi_{n,0}^{\sigma'} \rangle}{\varepsilon_{n,0} - \varepsilon_{l,0}} \langle \psi_{m,0}^{\sigma} | v_y | \psi_{l,0}^{\sigma''} \rangle$$

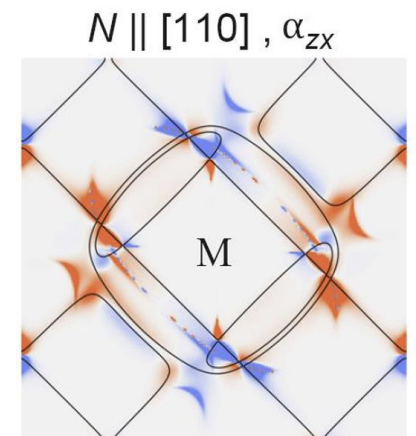
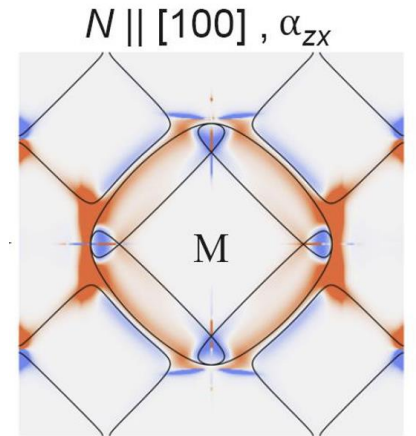
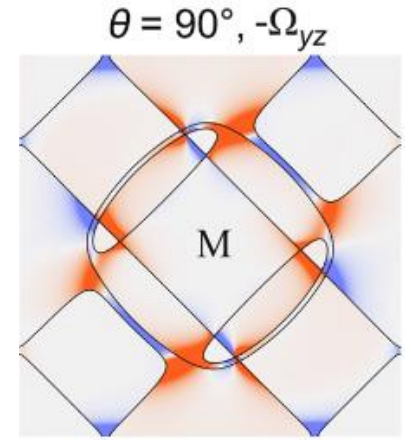
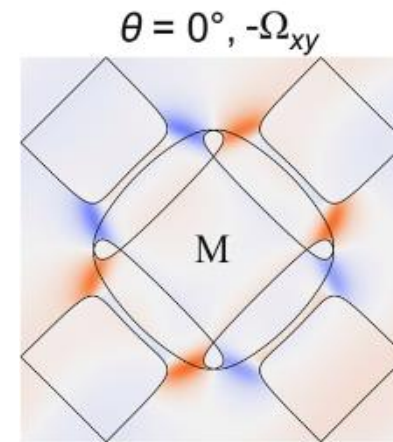
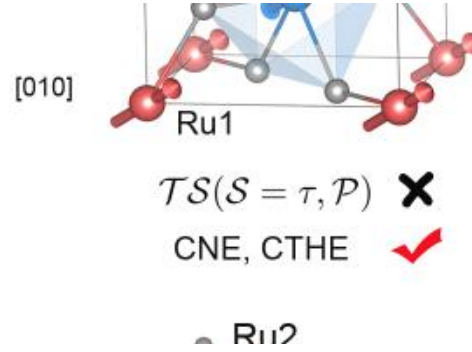


# Anisotropy in RuO<sub>2</sub>

Zhou, Feng, LS, JS, YM et al., arXiv:2305.01410

Access thermal phenomena:

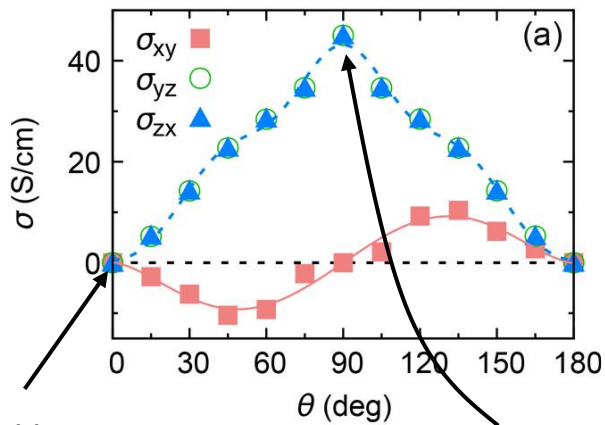
$$R_{ij}^{(n)} = \int_{-\infty}^{\infty} (\varepsilon - \mu)^n \left(-\frac{\partial f}{\partial \varepsilon}\right) \sigma_{ij}^{T=0}(\varepsilon) d\varepsilon$$



*anomalous Hall conductivity*

$$\sigma_{ij} = R_{ij}^{(0)}$$

Crystal Hall effect



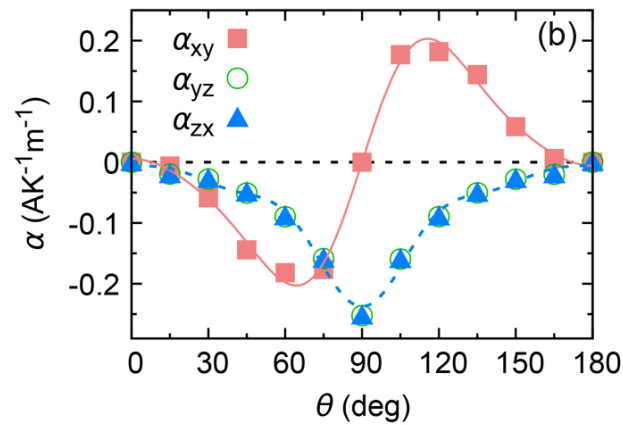
$N \parallel [001]$

$N \parallel [110]$

*anomalous Nernst conductivity*

$$\alpha_{ij} = -R_{ij}^{(1)} / eT$$

Crystal Nernst effect

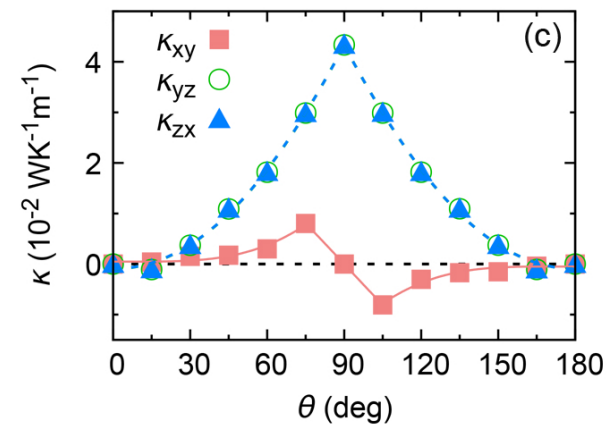


compare to **0.2 – 0.3**

*anomalous thermal Hall conductivity*

$$\kappa_{ij} = R_{ij}^{(2)} / e^2 T$$

Crystal thermal Hall effect



**1.5 – 4.5** in Mn<sub>3</sub>X

# Wiedemann-Franz Law

Zhou, Feng, LS, JS, YM et al., arXiv:2305.01410

Sommerfeld expansion  $\sigma_{ij} \hat{=} \sigma_{ij}^{T=0}(\mu)$   $\kappa_{ij} \hat{=} \frac{\pi^2 k_B^2 T}{3e^2} \sigma_{ij}^{T=0}(\mu)$

**Lorentz ratio:**  $L_{ij} = \kappa_{ij} / \sigma_{ij} T$ , Sommerfeld constant

$$L_{ij}(T \rightarrow 0) = L_0 = \pi^2 k_B^2 / 3e^2$$

*inelastic*

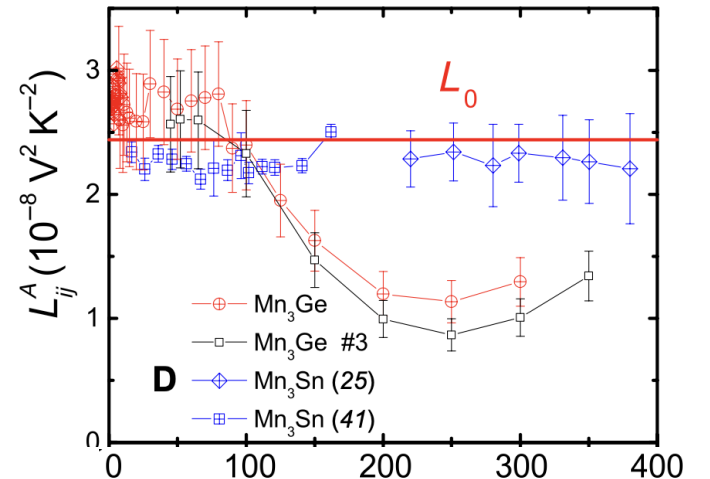
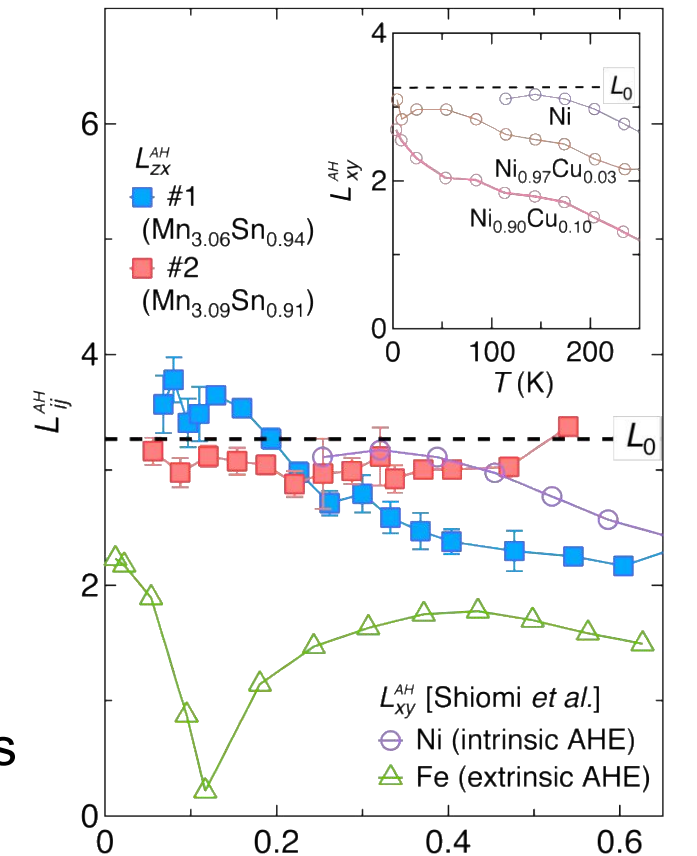
Traditionally believed to give an estimate for **extrinsic / intrinsic** origins

*small-angle inelastic scattering has stronger impact on heat flow than electron momentum flow [Ziman, 1972]*

**Mn<sub>3</sub>Sn** and **Mn<sub>3</sub>Ge**: intrinsic by far, negligible inelastic scattering

**Where does WF law violation come from?**

Sugii et al. arXiv:1902.06601 (2019)



# Wiedemann-Franz Law Violation

Zhou, Feng, LS, JS, YM et al., arXiv:2305.01410

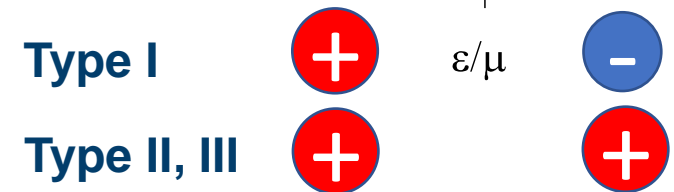
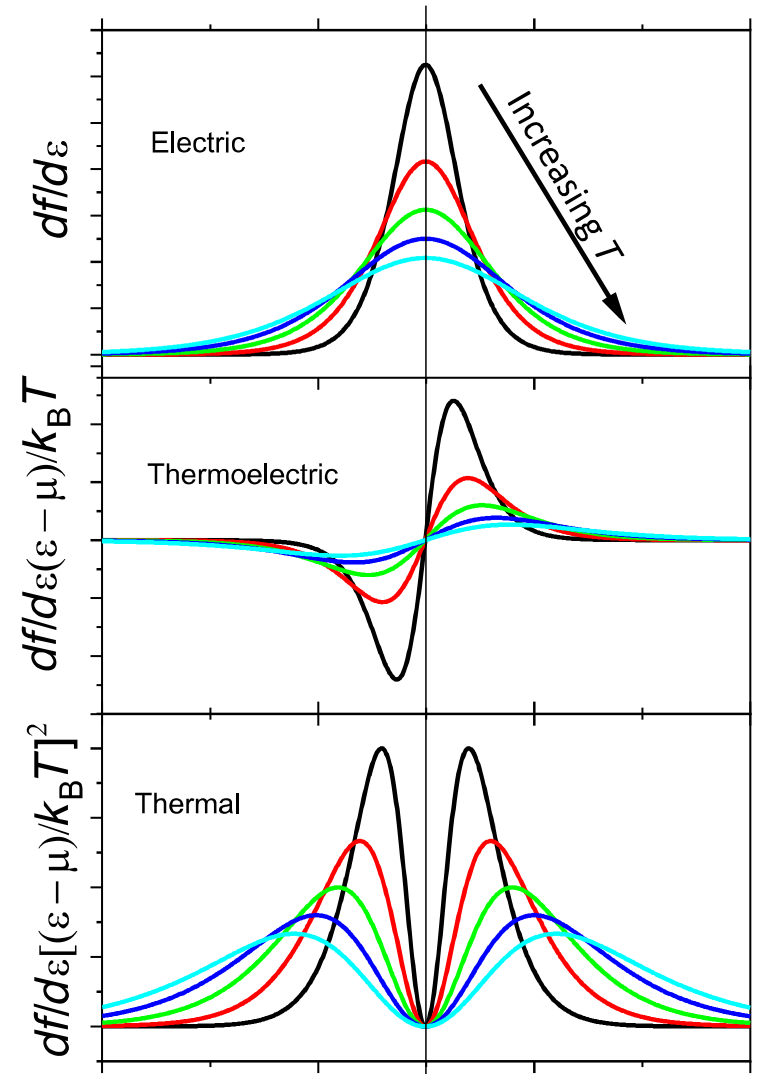
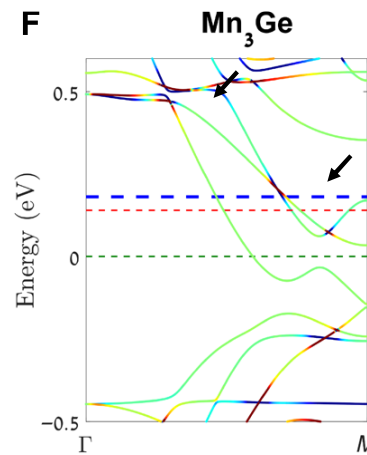
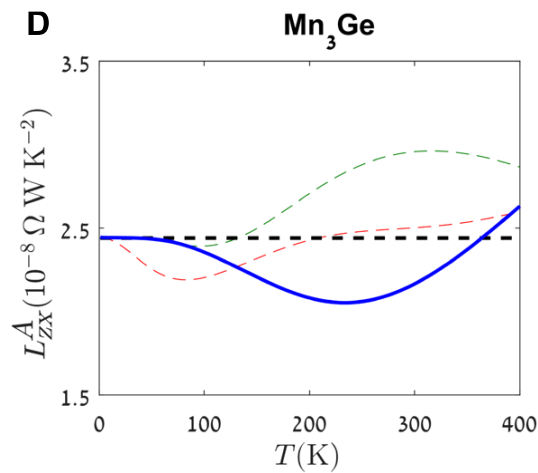
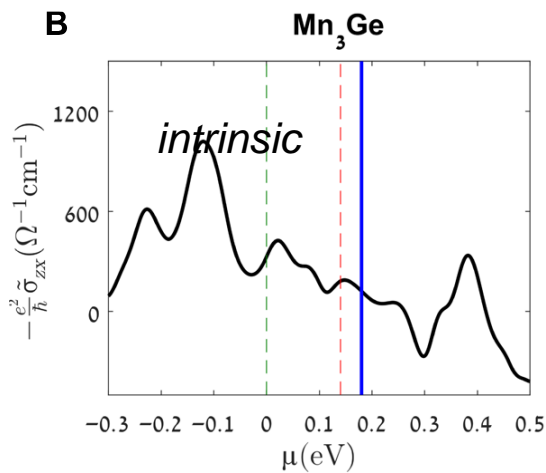
At  $T = 0$  pondering function gives WF law:  $F_n(\varepsilon) = \left( \frac{\varepsilon - \mu}{k_B T} \right)^n \frac{\partial f}{\partial \varepsilon}$

WF law deviations can be caused by pondering function

Purely antisymmetric AHC around the chemical potential:  
**WF law is satisfied**

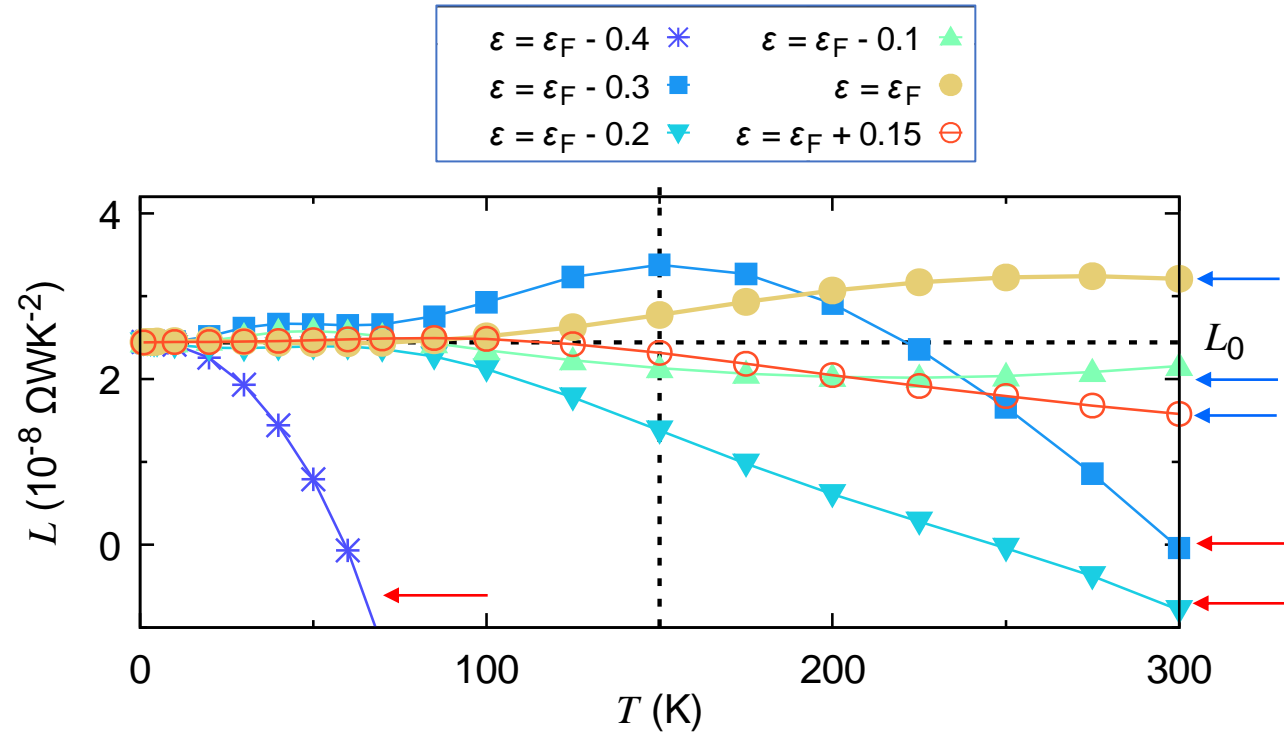
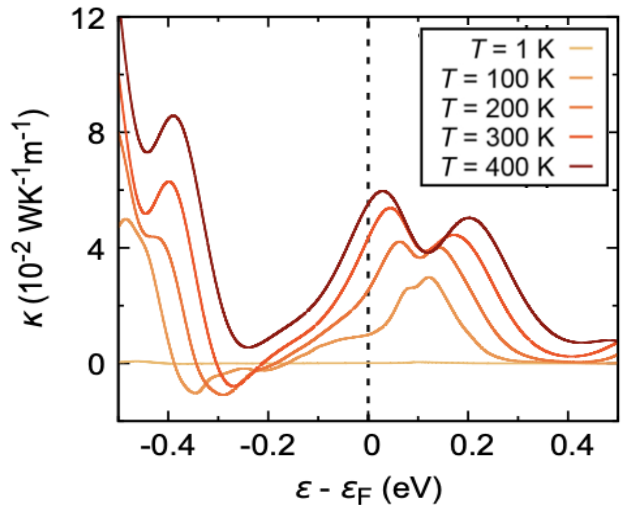
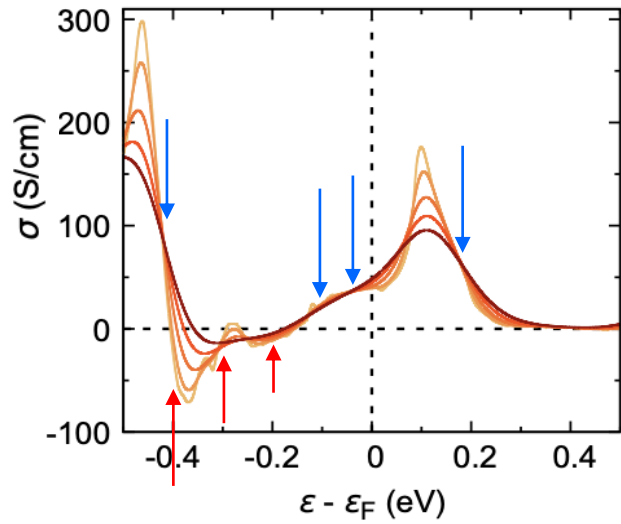
**WF law is satisfied**

*WF nodes in  $Mn_3Sn$*



# Wiedemann-Franz Law in RuO<sub>2</sub>

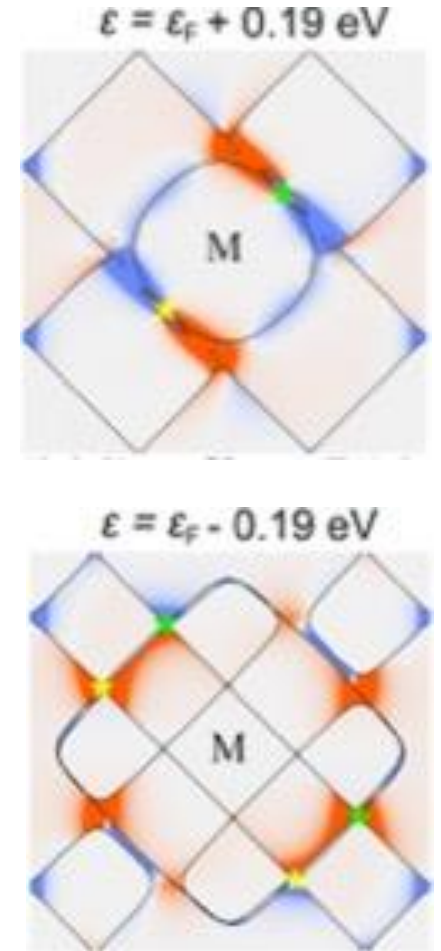
Zhou, Feng, LS, JS, YM et al., arXiv:2305.01410



*WF ratio is very sensitive to band filling*

Use WF law to identify the type of transitions?

Anisotropy of electrical & thermal transport:  
**position and character of different types of features?**

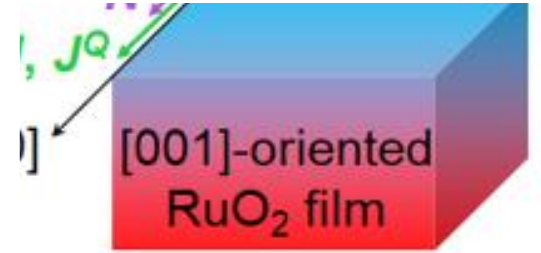




# Photophysics with RuO<sub>2</sub>?

Adamantopoulos, YM, WF, LS, JS et al. (2023)

*actually has  
inversion symmetry...*



PHYSICAL REVIEW LETTERS **130**, 166302 (2023)

## Time-Reversal-Even Nonlinear Current Induced Spin Polarization

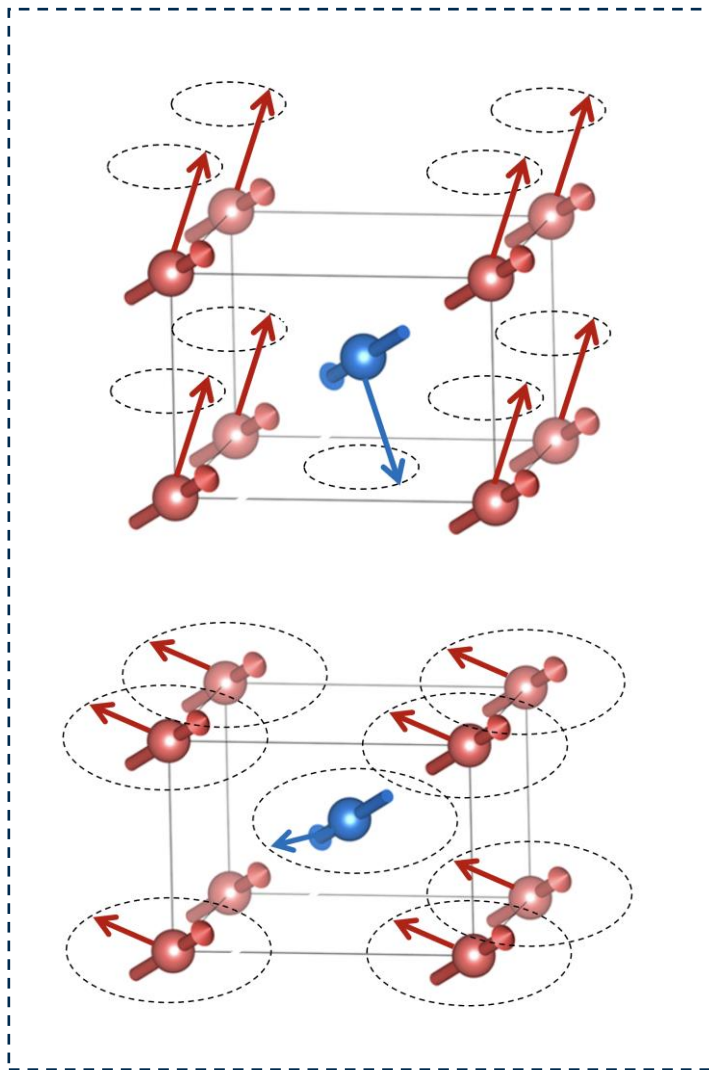
Cong Xiao<sup>1,2,\*</sup>, Weikang Wu<sup>3,\*</sup>, Hui Wang<sup>4,\*</sup>, Yue-Xin Huang<sup>4,\*</sup>, Xiaolong Feng<sup>4</sup>, Huiying Liu<sup>5,4,‡</sup>,  
Guang-Yu Guo<sup>6,7,§</sup>, Qian Niu<sup>8</sup> and Shengyuan A. Yang<sup>4</sup>



<i>Linear in electric field</i>	✓	✗	✗
<i>Quadratic in electric field (photo)</i>	✗	✓	✓
	<i>Orbital Hall Spin Hall Anomalous Hall</i>	<i>Orbital, spin accumulation</i>	<i>Torques</i>

# Photo Orbital Magnetism : RuO<sub>2</sub>

Adamantopoulos, YM, WF, LS, JS et al. (2023)



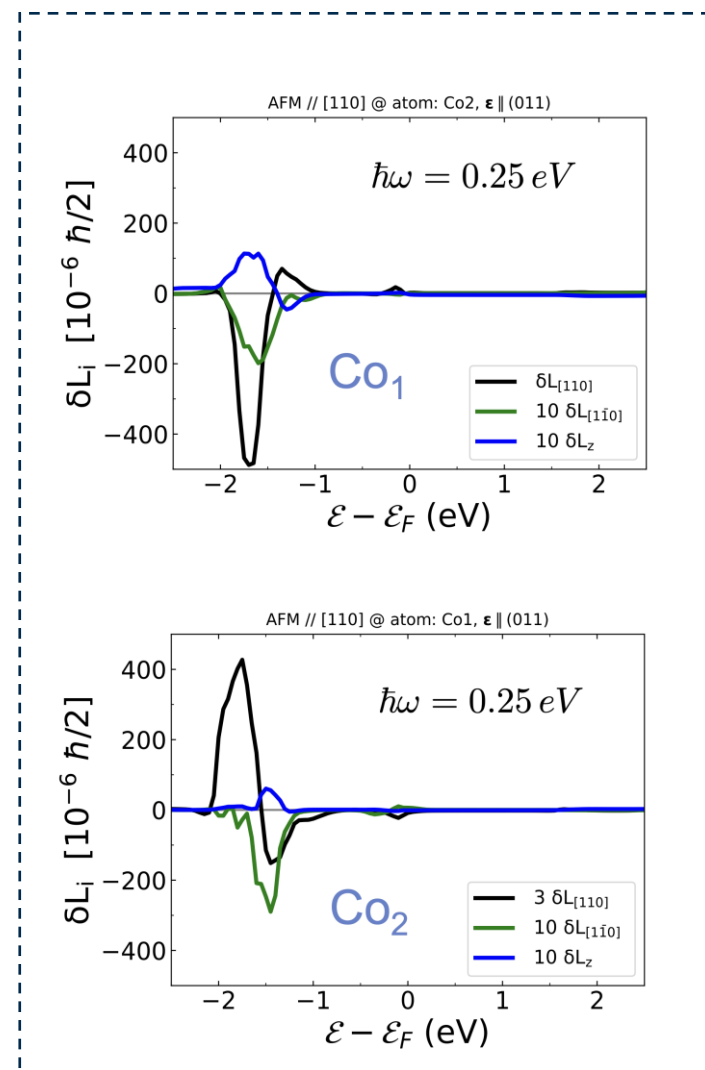
Poster  
session

RuO<sub>2</sub>

CoF<sub>2</sub>

*Strong canting in RuO<sub>2</sub>*

*Giant induced moments in CoF<sub>2</sub>*



# Outlook

- ✓ Clearly, altermagnets combine properties of FMs,  $PT$ -AFMs, and NC-AFMs
- ✓ Crystal symmetries play a role in **classification** of topological features / excitations
- ✓ Electrically and thermally altermagnets are not worse than (e.g.)  $Mn_3X$  type
- ✓ Canting properties in ground state and out of equilibrium: anisotropic!  
*may give a handle on dynamics driven by magnetic field*
- ✓ Expect some exciting **orbital properties**
- ✓ **Sublattice-dependent** currents and response may be more relevant
- ✓ Interplay of structural and magnetic chirality: new ideas for **magno-phononics**?