

Cooperative quantum optics with molecules

Claudiu Genes

Max Planck Institute for the Science of Light

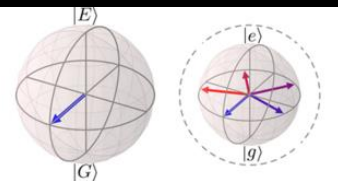
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MAX PLANCK INSTITUTE
for the science of light

SPICE-Workshop on Quantum Spinoptics

-- 13.06.2023 --

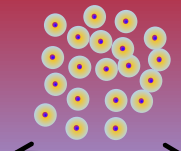


Genes Research Group
Cooperative Quantum Phenomena

Quantum at the **collective** level (from **simple** to **complex** quantum emitters)

1950s

Dicke superradiance

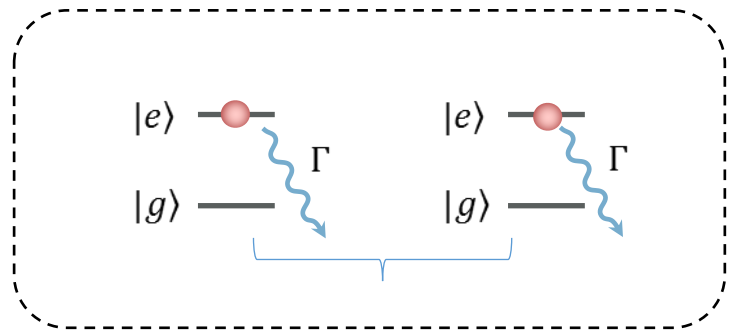


< 1 micron

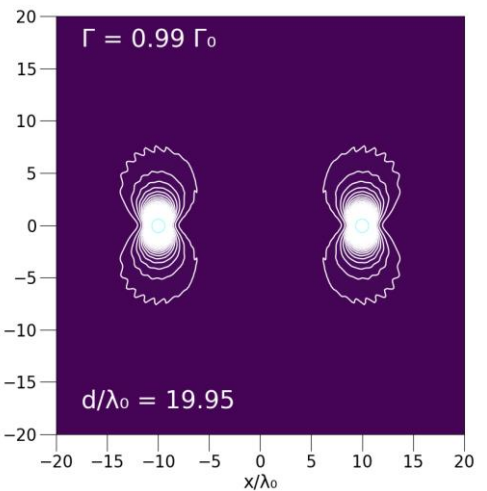
Enhanced collective emission

Two quantum emitters: superradiance and subradiance

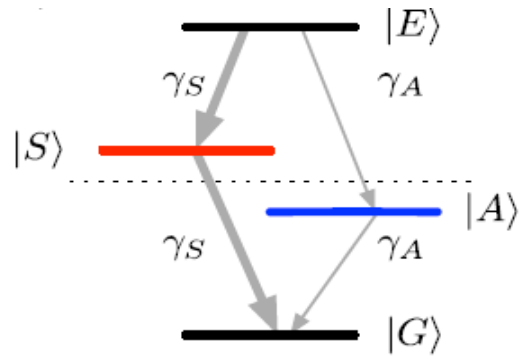
$r \ll \lambda$



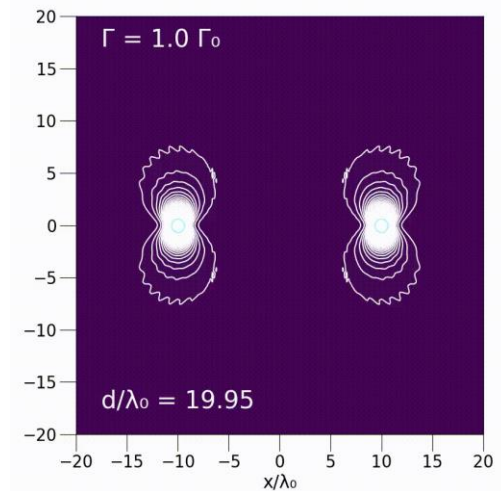
$|S\rangle = |eg\rangle + |ge\rangle$



Courtesy of Raphael Holzinger



$|A\rangle = |eg\rangle - |ge\rangle$



Robust states – quantum metrology, quantum information

State of the art

Cooperative Quantum Phenomena in Light-Matter Platforms

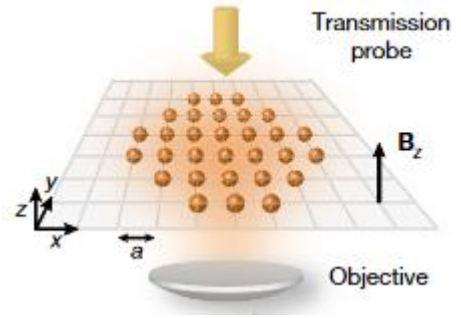
Michael Reitz^{1,2}, Christian Sommer^{1,†} and Claudiu Genes^{1,2,*}

PRX QUANTUM (TUTORIAL) 3, 010201 (2022) [arxiv: 2107.02674](https://arxiv.org/abs/2107.02674)

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A subradiant optical mirror formed by a single structured atomic layer

<https://doi.org/10.1038/s41586-020-2463-x> Jun Rui^{1,2,✉}, David Wei^{1,2}, Antonio Rubio-Abadal^{1,2}, Simon Hollerith^{1,2}, Johannes Zeiher², Dan M. Stamper-Kurn², Christian Gross^{1,2,4} & Immanuel Bloch^{1,2,5}
Received: 3 January 2020



- Strong and narrow cooperative subradiant response
- Only a few hundred atoms (extremely small mass)
- Efficient optical metamaterial engineering
- Applications in low-mass hybrid nano-optomechanics

Optical metasurfaces

State of the art

Cooperative Quantum Phenomena in Light-Matter Platforms

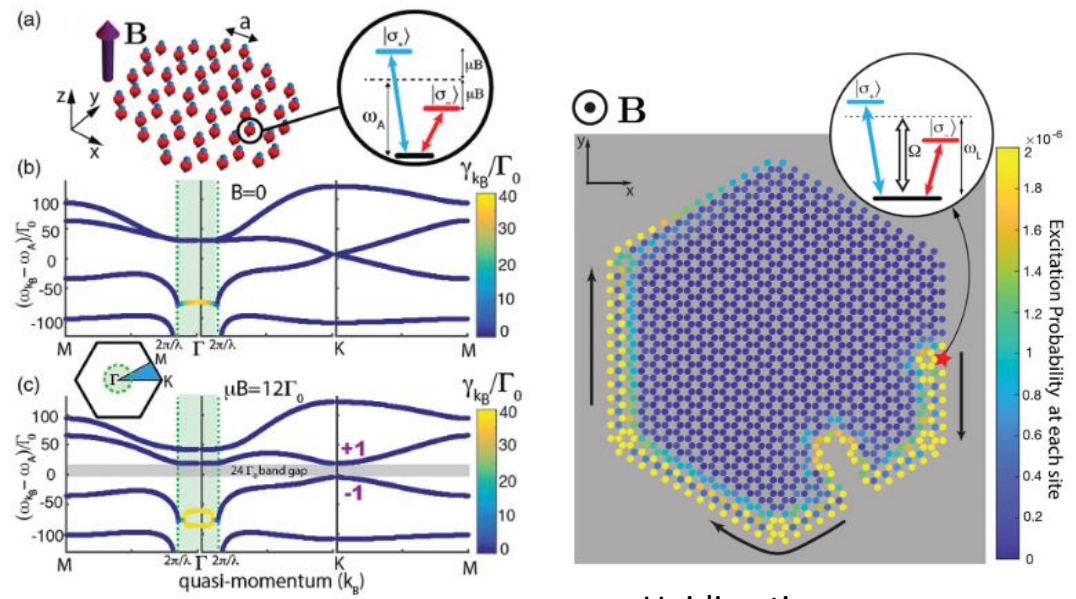
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Topological Quantum Optics in Two-Dimensional Atomic Arrays

J. Perczel,^{1,2} J. Borregaard,² D. E. Chang,³ H. Pichler,^{2,4} S. F. Yelin,^{2,5} P. Zoller,^{6,7} and M. D. Lukin²



○ Unidirection energy transport around large defects

Platforms for excitation transport

Quantum at the **collective** level (from **simple** to **complex** quantum emitters)

1930s 1950s

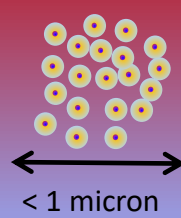
Molecular aggregates

PIC chloride

CCN(CC)C1=CC=C2C=CC(=C12)C=C3C=CC(=C4C=CC(=C34)N(CC)C)Cl

Supramolecular structures

Dicke superradiance



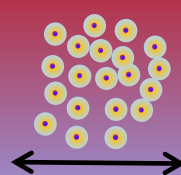
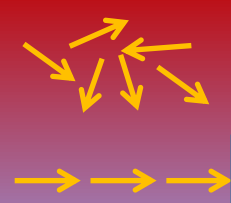

< 1 micron

Enhanced collective emission

E. E. Jelley 1936
G. Scheibe 1937

- Type of dye with increased absorption coefficient after aggregation (aided by solvent)

Quantum at the **collective** level (from **simple** to **complex** quantum emitters)

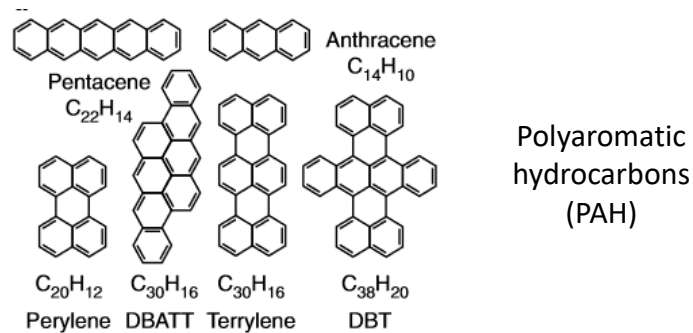
1930s	1950s	1950s	2000s -2020s
<h3>Molecular aggregates</h3>	<h3>Dicke superradiance</h3>	<h3>Kasha's theory</h3>	<h3>Cavity quantum materials</h3>
<p>PIC chloride</p> <chem>CCN(CC)C1=CC=CC=C1C=C(C=C2C=CC=CC=C2N(CC)C)C3=CC=CC=C3.[Cl-]</chem> <p>Supramolecular structures</p>	 <p>< 1 micron</p> <p>Enhanced collective emission</p>	 <p>monomers</p> <p>aggregates</p> <p>Extremely large dipole moments</p> <ul style="list-style-type: none">• <u>Collective dipole</u> absorption• Inhibition of fluorescence in H-aggregates	 <p>Fabry-Pérot / planar cavities</p> <p>Sanvitto & Kéna-Cohen, Nat. Mater. 15, 1061 (2016)</p> <p>Strong <u>collective</u> light-matter interactions</p>

Why molecules

Single organic molecules for photonic quantum technologies

NATURE MATERIALS | VOL 20 | DECEMBER 2021 | 1615-1628 |

C. Toninelli^{1,2}, I. Gerhardt³, A. S. Clark⁴, A. Reserbat-Plantey⁵, S. Götzinger^{6,7}, Z. Ristanović⁸, M. Colautti^{1,2}, P. Lombardi^{1,2}, K. D. Major⁴, I. Deperasińska⁹, W. H. Pernice¹⁰, F. H. L. Koppens^{5,11}, B. Kozankiewicz⁹, A. Gourdon¹², V. Sandoghdar^{6,7} and M. Orrit⁸



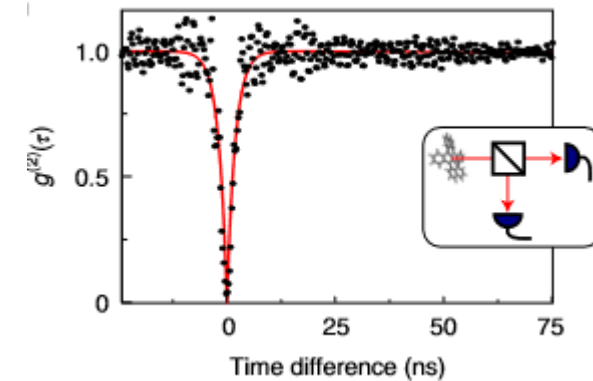
Advantages

- Good isolation in solid state host matrices
- Flexibility in synthesis – wide palette of emission wavelengths
- Optimized interaction with light

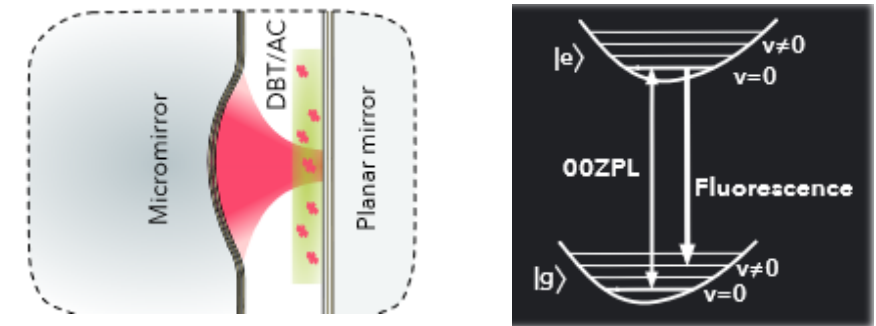
Promises

- Single photon sources
- Nonlinear elements with competitive performance in terms of coherence, scalability and compatibility with diverse integrated platforms
- Transducers – promise of single quanta resolution in the sensing of charges and motion

Photon antibunching



Qubit - closed two level system



Wang, D. et al. Turning a molecule into a coherent two-level quantum system. Nat. Phys. 15, 483–489 (2019)

Why molecules

Use light (*vacuum field*) to modify material properties?



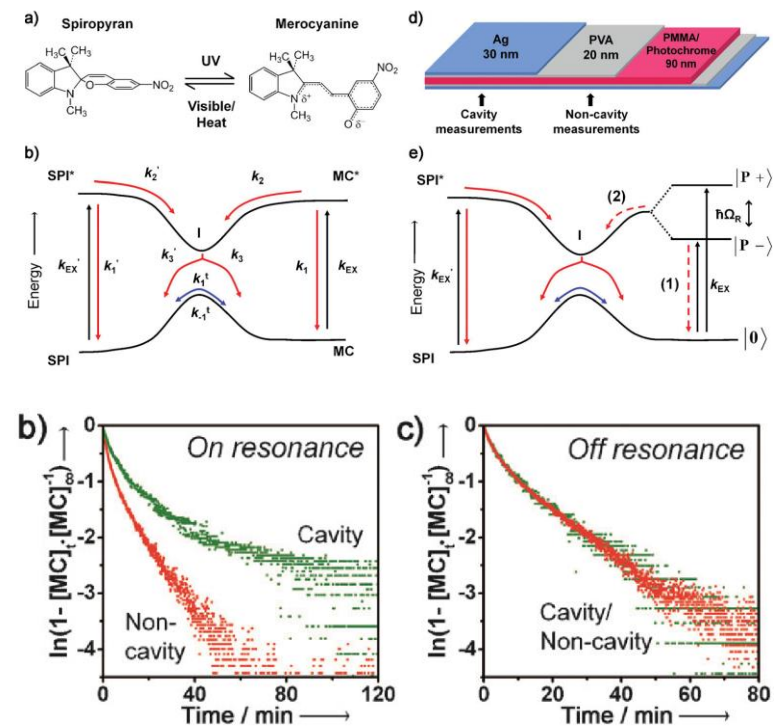
Confine light in space to get strong **few-photon** interaction with **interesting materials**

Many molecules / macroscopic

- Promises**
- "Easy" to reach collective strong coupling
 - Modifications of electronic properties
 - Tunable chemistry
 - Could integrate in devices

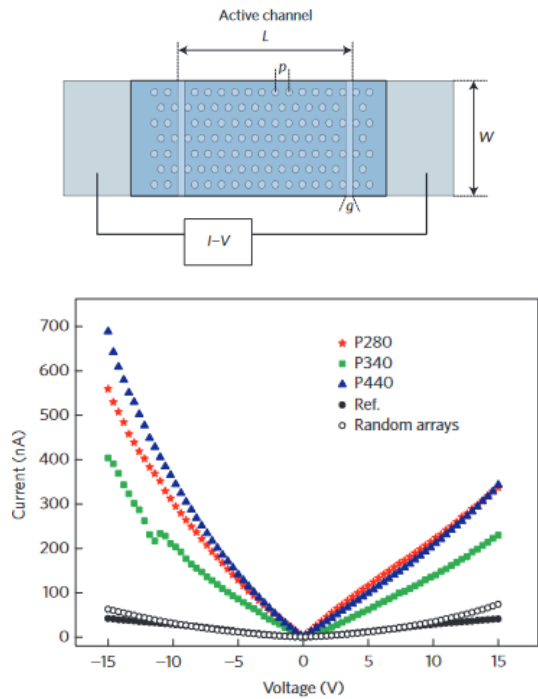
Modify photochemical reaction rates

J. A. Hutchison *et al.*, *Angew. Chemie* **124**, 1624 (2012)

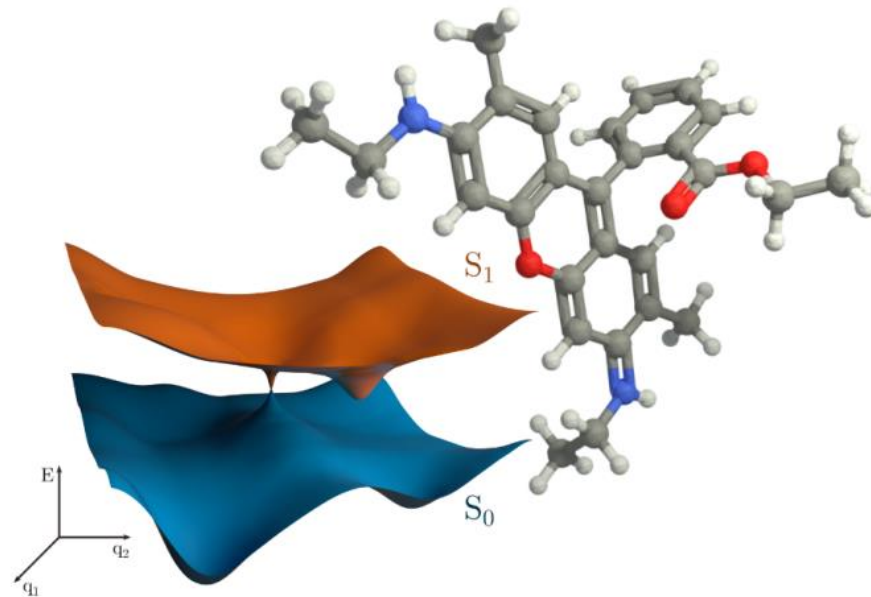
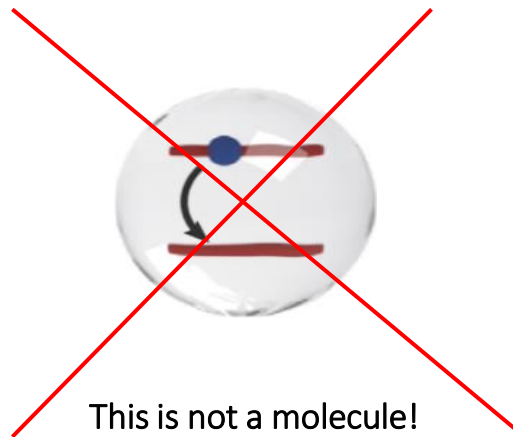


Conductivity in organic semiconductors hybridized with the vacuum field

E. Orgiu *et al.*, *Angew. Nat Mat* **14**, 1123 (2015)



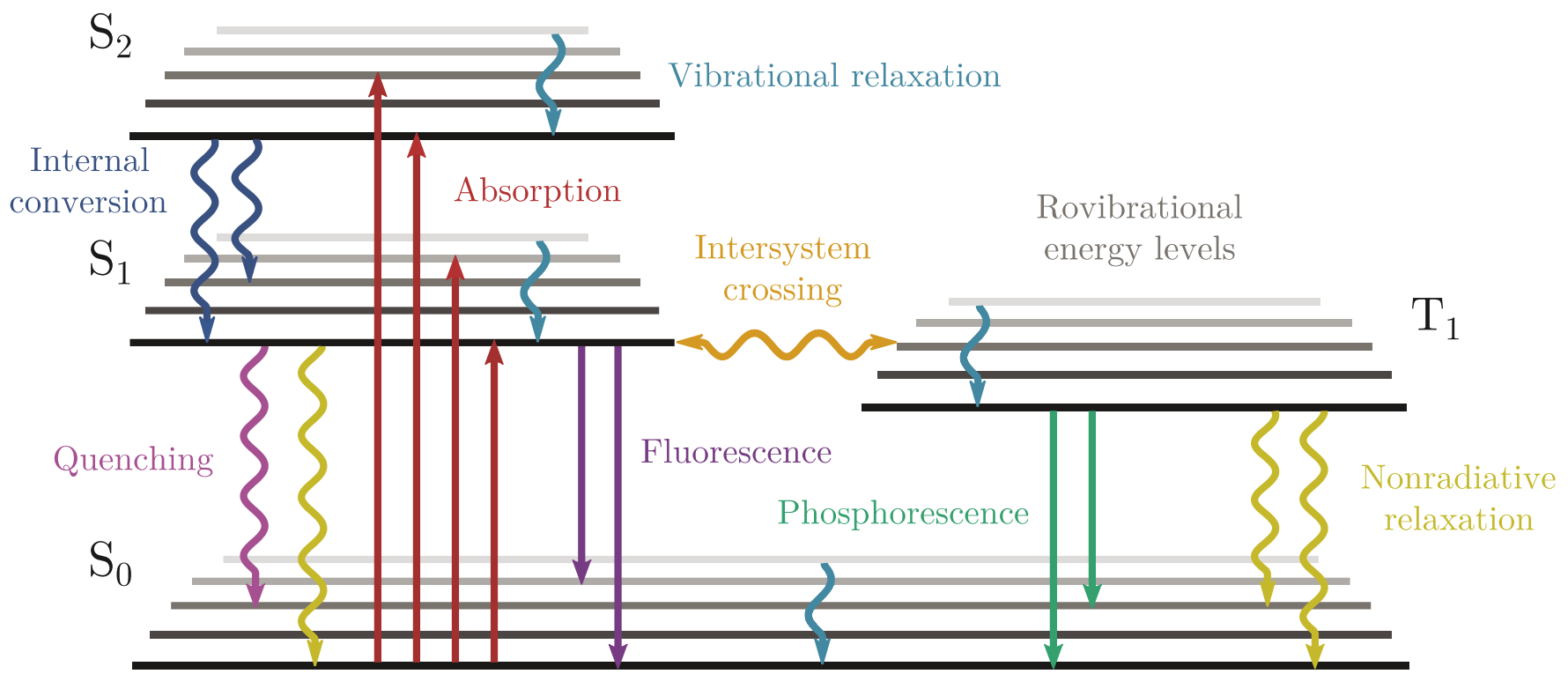
The complex nature of molecules



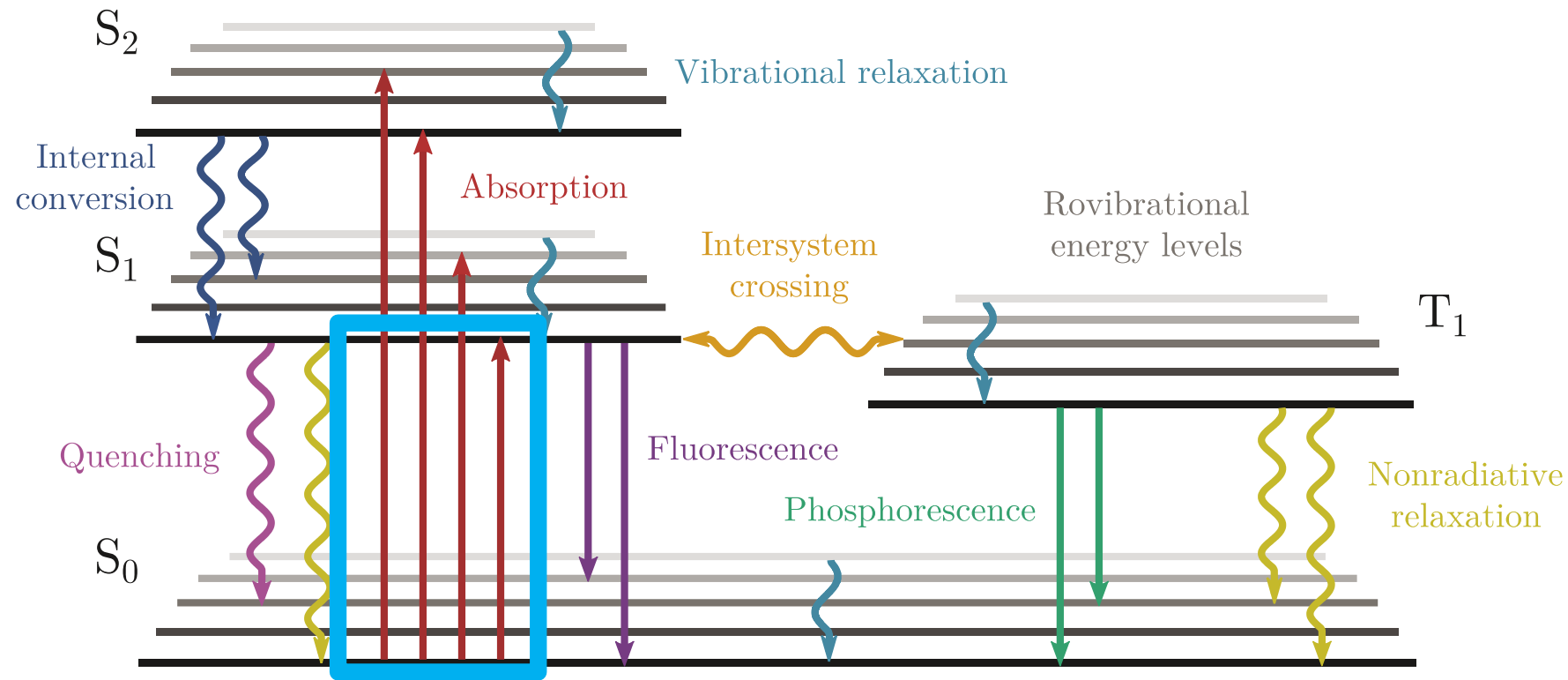
Fundamental aspects

- Photon-electron coupling strongly perturbed by additional vibrational degrees of freedom
- Radiative emission can compete with non-radiative pathways of relaxation

The complex nature of molecules



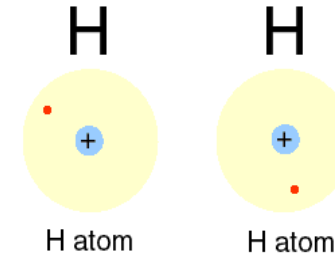
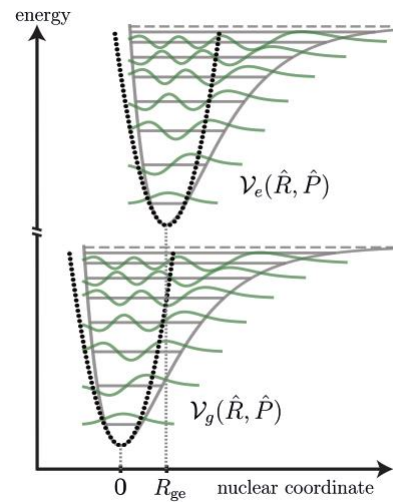
The complex nature of molecules



Coupling at optical frequencies

- Experimentally: photo-physics, (photo) chemistry, charge/exciton transport, etc.
- Theory: **role of vibrations**, Tavis-Cummings-Holstein model, polariton cross-talk, etc...

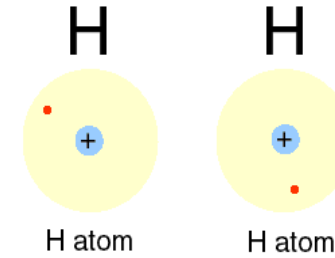
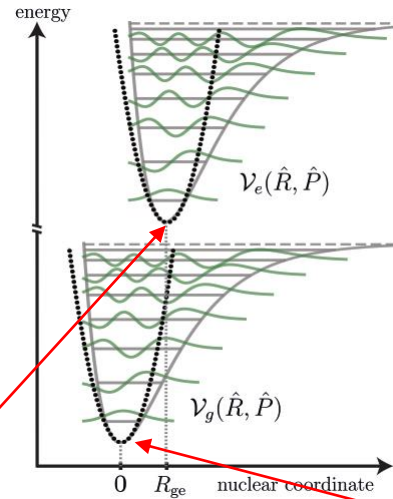
Quantum optics approach to molecules: a simple model



Minimal model

- Expansion of the molecular potential landscapes along the nuclear coordinate
- Harmonic approximation
- Difference between minima gives rise to electron-vibron coupling

Quantum optics approach to molecules: a simple model



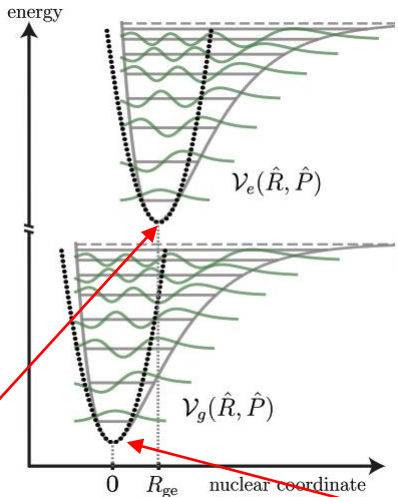
$$H = \left(\omega_e + \frac{p^2}{2\mu} + \frac{1}{2} \mu \nu^2 (R - R_e)^2 \right) \sigma^\dagger \sigma + \left(\frac{p^2}{2\mu} + \frac{1}{2} \mu \nu^2 (R - R_g)^2 \right) \sigma \sigma^\dagger$$

Electronic operators (spin algebra)

Minimal model

- Expansion of the molecular potential landscapes along the nuclear coordinate
- Harmonic approximation
- Difference between minima gives rise to electron-vibron coupling

Quantum optics approach to molecules



$$H = \left(\omega_e + \frac{p^2}{2\mu} + \frac{1}{2}\mu\nu^2 (R - R_e)^2 \right) \sigma^\dagger \sigma + \left(\frac{p^2}{2\mu} + \frac{1}{2}\mu\nu^2 (R - R_g)^2 \right) \sigma \sigma^\dagger$$

Electronic operators (spin algebra)

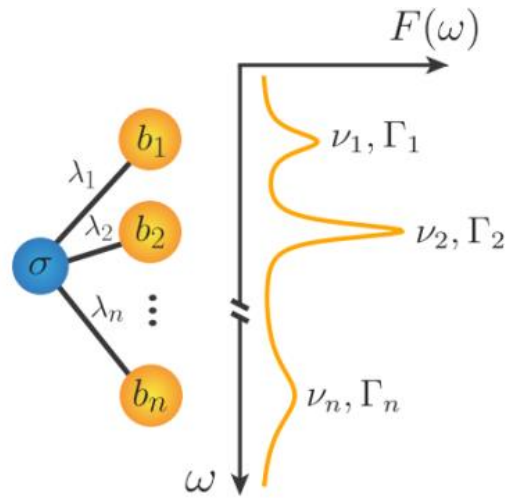
Holstein Hamiltonian

$$H = \nu b^\dagger b + (\omega_e + \lambda^2 \nu) \sigma^\dagger \sigma + \lambda \nu (b^\dagger + b) \sigma^\dagger \sigma$$

Bosonic operators (for vibrations)

Huang-Rhys factor

Quantum Langevin equations



$$\frac{db_k(t)}{dt} = -(\Gamma_k + i\nu_k)b_k(t) + \sqrt{2\Gamma_k}b_{in}^k(t),$$

$$\frac{d\tilde{\sigma}(t)}{dt} = -[\gamma - i(\omega_\ell - \omega_e)]\tilde{\sigma}(t) + \sqrt{2\gamma}\mathcal{D}^\dagger(t)\Sigma_{in}(t)$$

Polaron operator

$$\tilde{\sigma}(t) = \sigma(t)\mathcal{D}^\dagger(t)$$

$$\mathcal{D}^\dagger = \mathcal{D}_1^\dagger \dots \mathcal{D}_n^\dagger$$

Thermal reservoir

$$\langle b_{in}^\dagger(t)b_{in}(t') \rangle = \Gamma n_T \delta(t - t')$$

$$\langle b_{in}(t)b_{in}^\dagger(t') \rangle = \Gamma(n_T + 1)\delta(t - t')$$

$$n_T = [\exp(\hbar\nu/(k_B T)) - 1]^{-1}$$

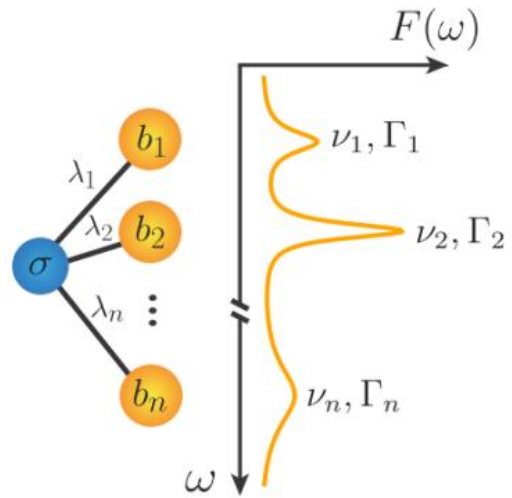
Input non-zero noise

$$\Sigma_{in}(t) = \eta_e/\sqrt{2\gamma} + \sigma_{in}(t)$$

Solution

$$\sigma(t) = \sigma(0)\mathcal{D}(t)\mathcal{D}^\dagger(0)e^{-[\gamma - i(\omega_\ell - \omega_e)]t} + \sqrt{2\gamma} \int_0^t dt' e^{-[\gamma - i(\omega_\ell - \omega_e)](t-t')} \Sigma_{in}(t')\mathcal{D}(t)\mathcal{D}^\dagger(t')$$

Quantum Langevin equations



$$\frac{db_k(t)}{dt} = -(\Gamma_k + i\nu_k)b_k(t) + \sqrt{2\Gamma_k}b_{in}^k(t),$$

$$\frac{d\tilde{\sigma}(t)}{dt} = -[\gamma - i(\omega_\ell - \omega_e)]\tilde{\sigma}(t) + \sqrt{2\gamma}\mathcal{D}^\dagger(t)\Sigma_{in}(t)$$

Polaron operator

$$\tilde{\sigma}(t) = \sigma(t)\mathcal{D}^\dagger(t)$$

$$\mathcal{D}^\dagger = \mathcal{D}_1^\dagger \dots \mathcal{D}_n^\dagger$$

Thermal reservoir

From here on:

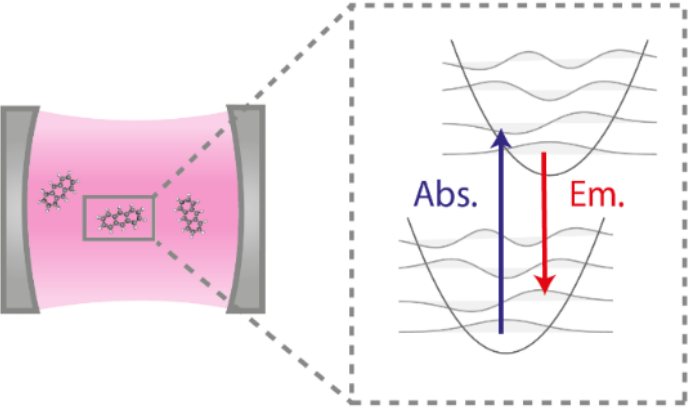
- Follow standard quantum optics techniques
- Two-time correlations lead to absorption and emission spectra
- Easy to add dynamics inside optical cavities

Solution

$$\sigma(t) = \sigma(0)\mathcal{D}(t)\mathcal{D}^\dagger(0)e^{-[\gamma - i(\omega_\ell - \omega_e)]t}$$

Results

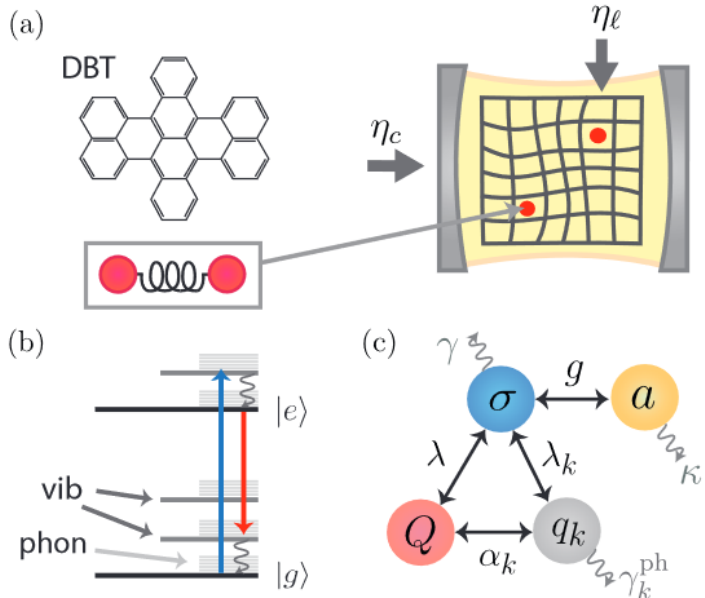
Cavity QED with single or few molecules



Results

- Analytical approach to electron-photon-vibron
- Polariton cross-talk rates
- Turning a molecule into a single closed qubit
- Cavity modified Förster resonance energy transfer

M. Reitz, C. Sommer and C. Genes, **Phys. Rev. Lett.** **122**, 203602 (2019)
Langevin approach to quantum optics with molecules

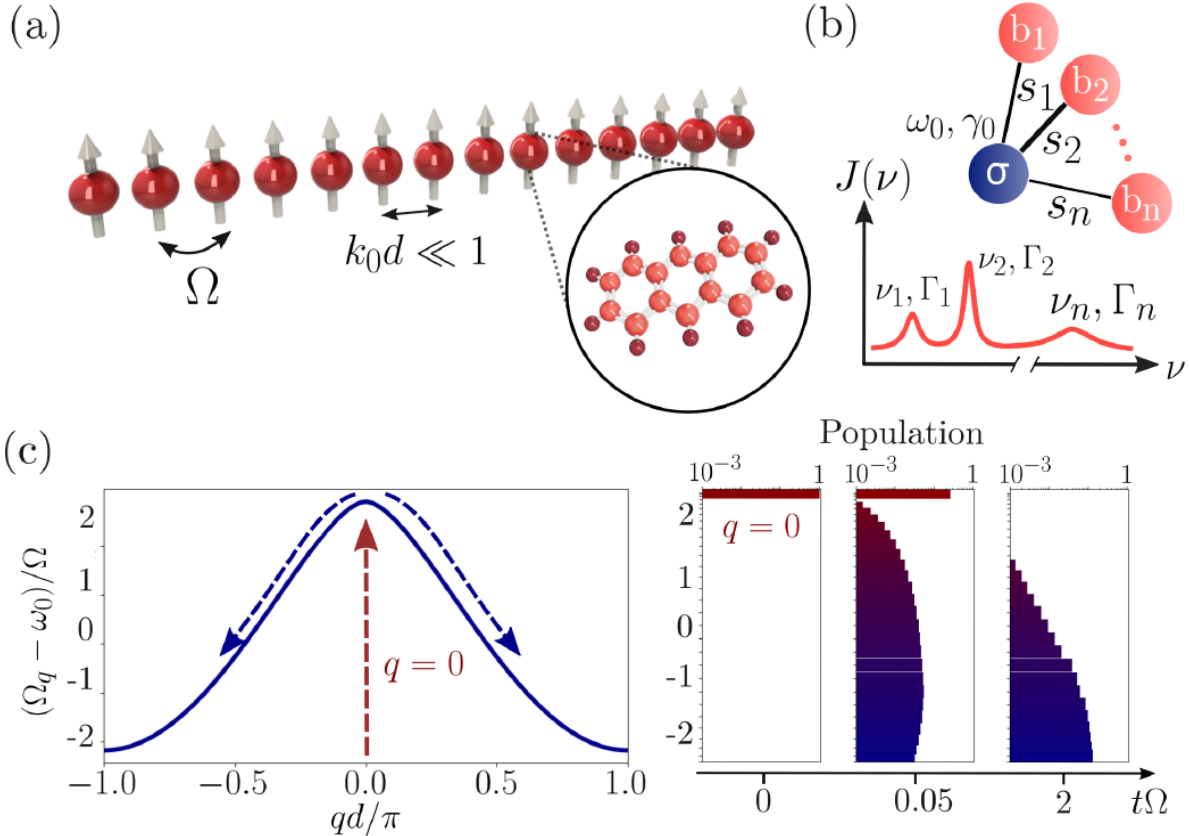


Results

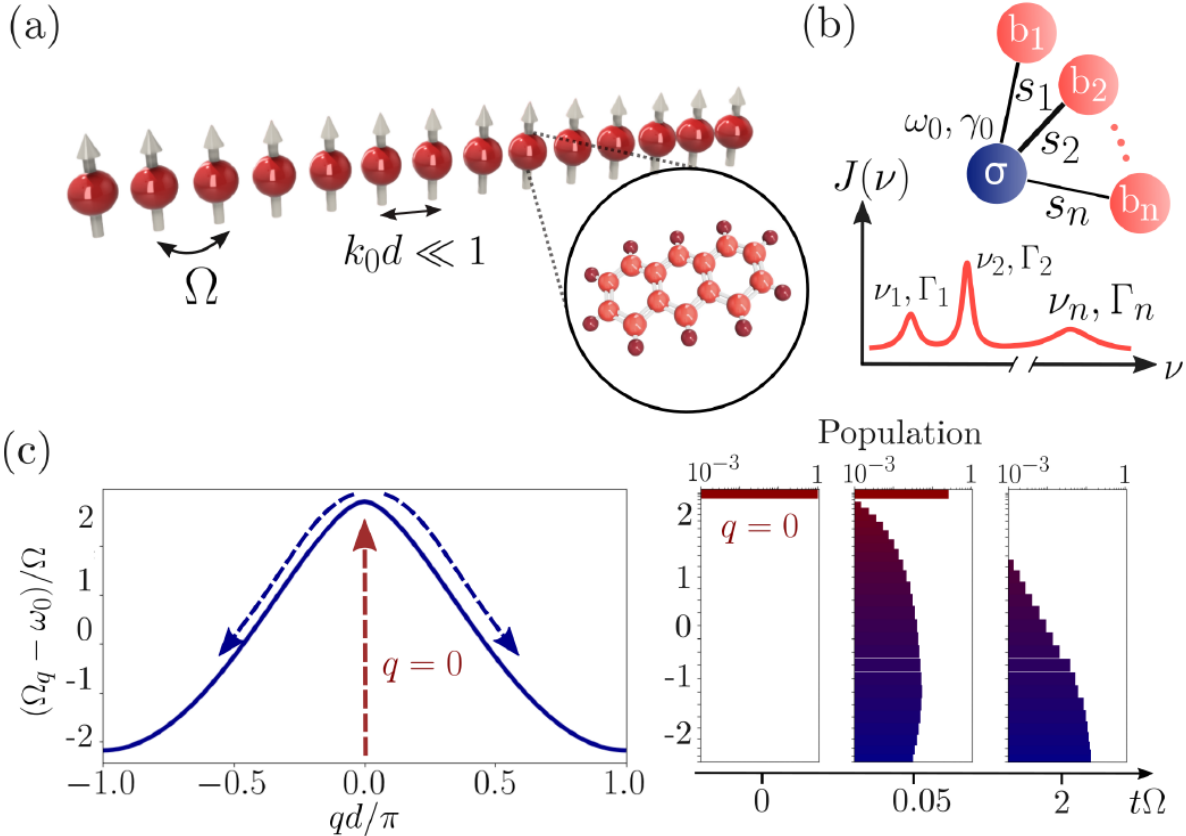
- Analytical approach to electron-photon-vibron-phonon interactions
- Vibrational collective decoupling

M. Reitz, C. Sommer, B. Gurlek, V. Sandoghdar, D. Martin-Cano and C. Genes, **Phys. Rev. Research** **2**, 033270 (2020)
Molecule-photon interactions in phononic environments

Molecular aggregates



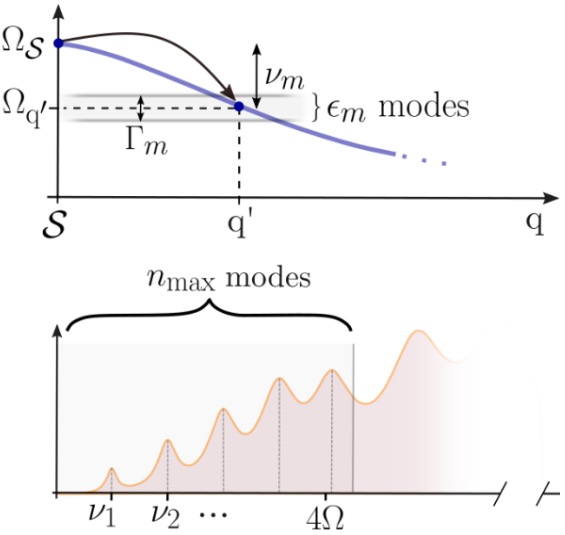
Molecular aggregates



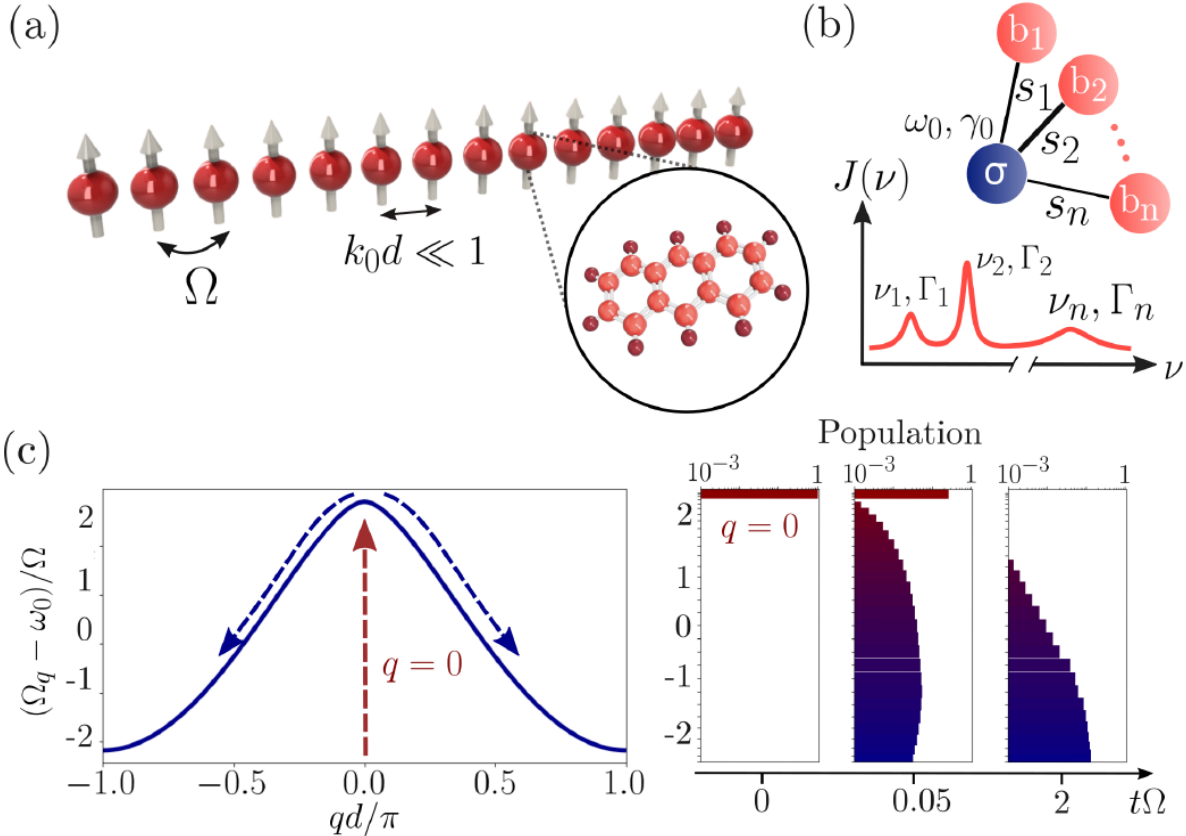
Rate equations

$$\dot{p}_S = -(\gamma_S + \kappa_S)p_S + \sum_{q \neq 0} \kappa_{q \rightarrow S} p_q,$$

$$\dot{p}_q = -\kappa_q p_q + \sum_{q' \neq q} \kappa_{q' \rightarrow q} p_{q'}.$$

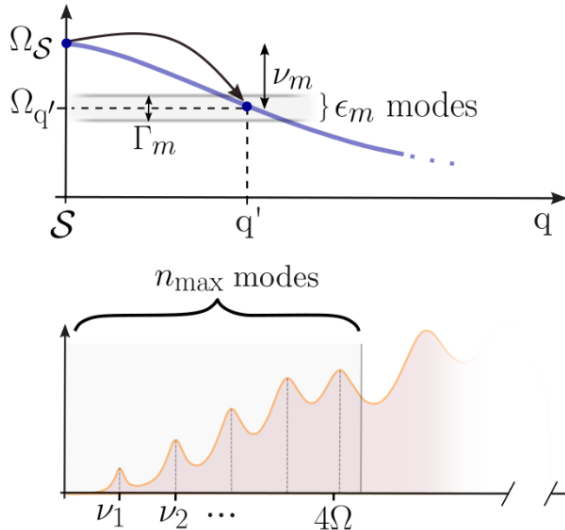


Molecular aggregates

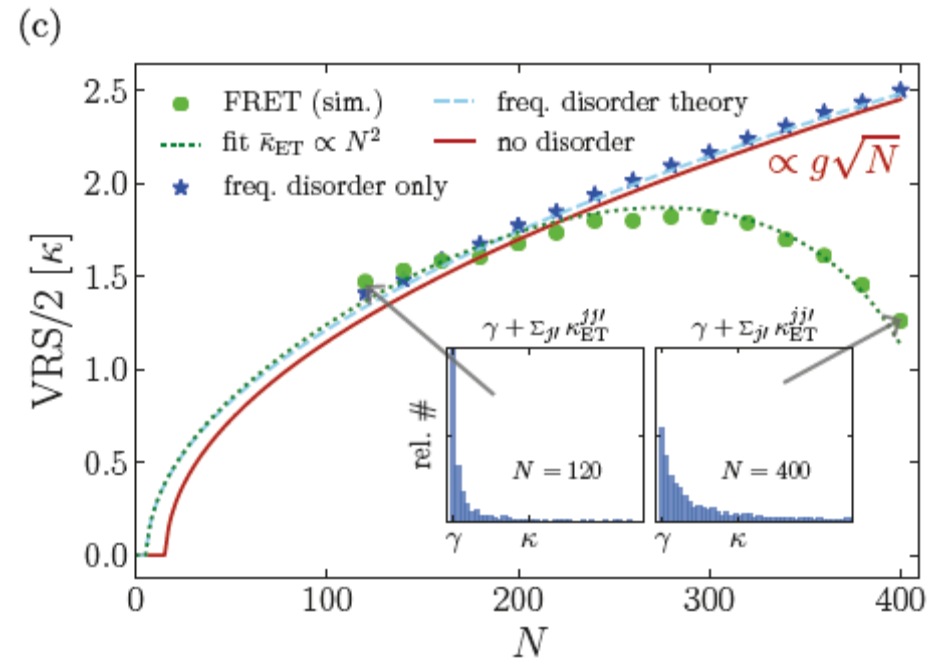
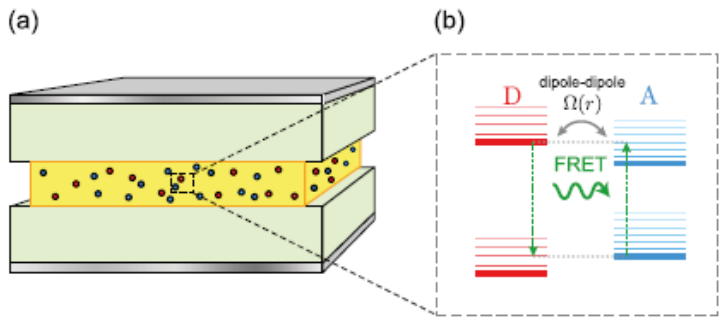


Scaling

$$\kappa_S \approx \frac{4s\Omega}{3} \frac{(n_{\max} + 1)(2n_{\max} + 1)}{n_{\max}}$$



Cavity QED with mesoscopic ensembles



Results

- Disorder provides loss of polaritons
- Disorder plus vibrations can reduce the Vacuum Rabi Splitting

C. Sommer, M. Reitz, F. Mineo and C. Genes, **Phys. Rev. Research 3, 033141 (2021)**
Molecular polaritonics in dense mesoscopic disordered ensembles

Thank you!