

# SPIN-ORBIT COUPLING: AN ENDLESS SOURCE OF EXOTIC MAGNETISM IN 2D MAGNETS



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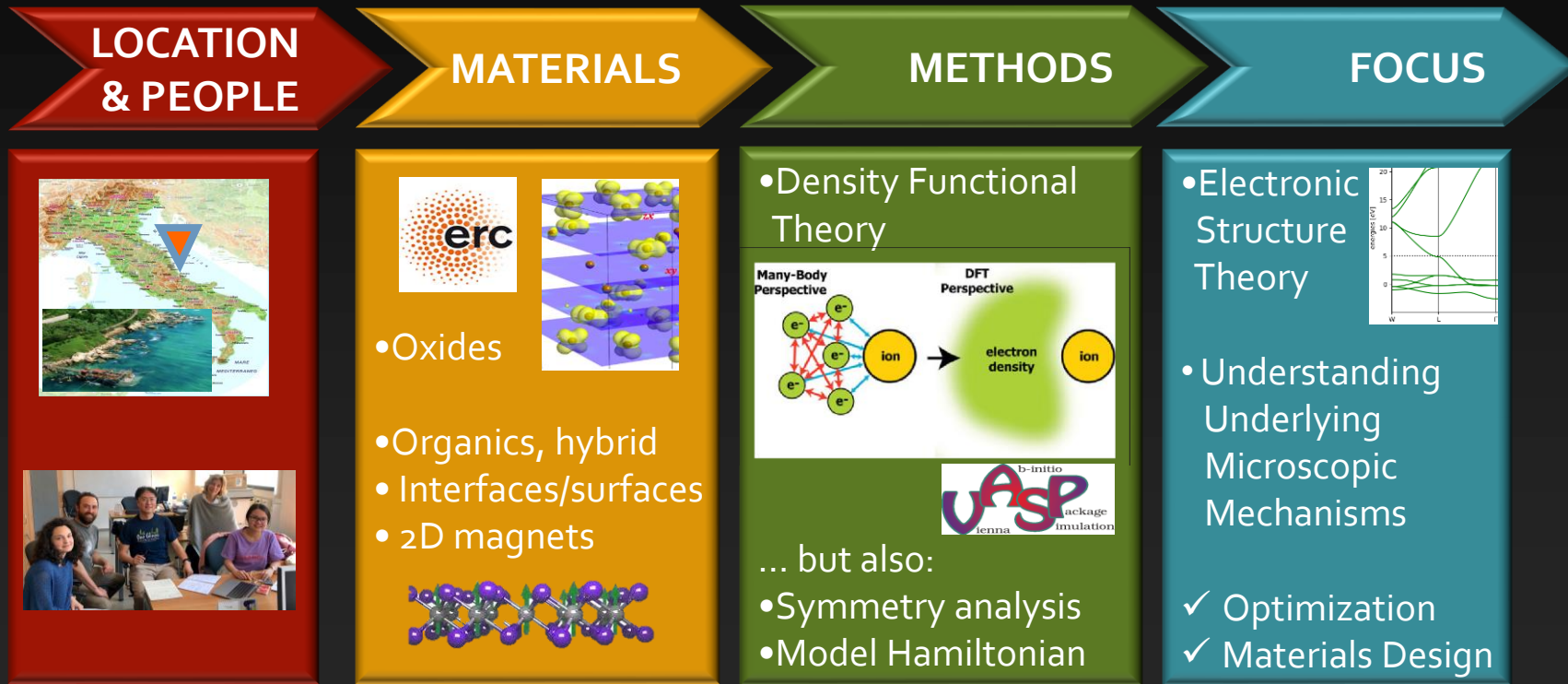
## OUTLINE:

- Introduction: ***Spin-orbit coupling***
- Focus on: **"Rashba Physics"** in Ferroelectrics  
Exotic Spin texture in 2D magnets  
Multiferroicity in 2D magnets

# MODEM (MOdelling and Design of functional Materials)

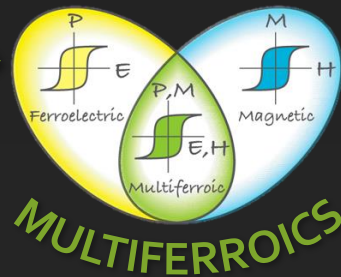
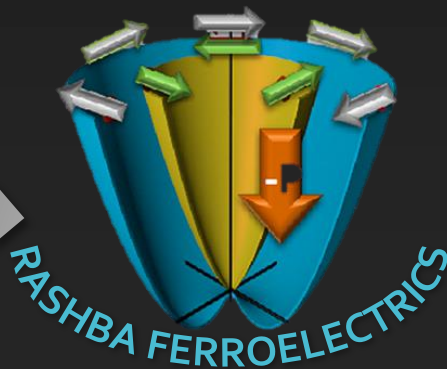


<https://sites.google.com/site/silviapicozzi/>



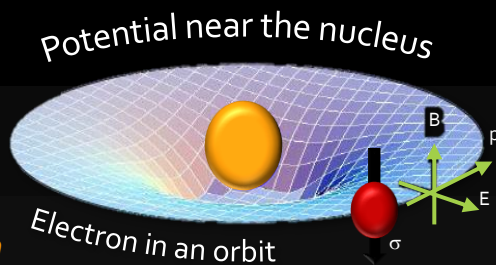
# CROSS-COUPLING IN MULTIFUNCTIONAL FERROICS

Our expertise: study *intertwined* phenomena



# SPIN-ORBIT COUPLING

.... a small interaction  
leading to rich physics ....



Relativistic interaction linking spin and orbital momenta (i.e. spin space and real space)

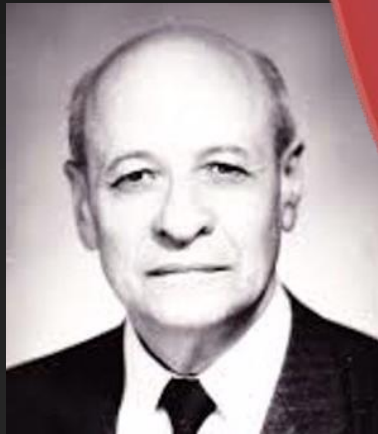
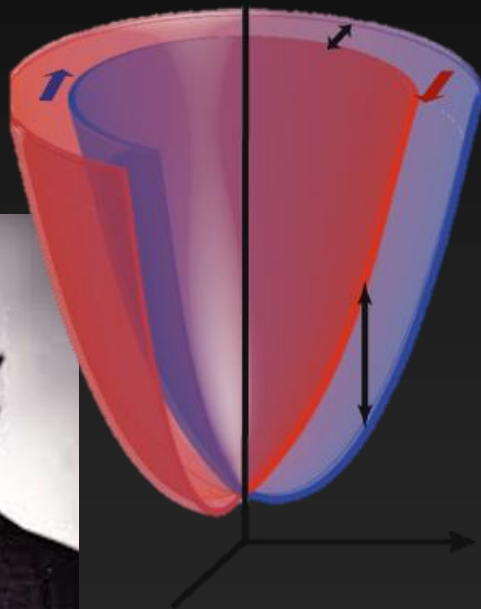
$$\underbrace{\frac{\mu_B}{2mcr} \frac{dV(r)}{dr}}_{\xi} \vec{\sigma} \cdot (\vec{r} \times \vec{p}) = \xi \vec{\sigma} \cdot \vec{L}$$



## Spin-Orbit Coupling in Solids

# THE RASHBA EFFECT

*(on the occasion of  
Rashba's 95<sup>th</sup> birthday)*



EDITORIAL | [Published: 09 December 2022](#)

## 95th Birthday of Emmanuel Rashba

[Journal of Experimental and Theoretical Physics](#) **135**, 387 (2022) |

**2022 Oliver E. Buckley Condensed Matter Physics Prize  
Recipient**

**Emmanuel I. Rashba**  
**Harvard University**

**Citation:**

*"For pioneering research on spin-orbit coupling in crystals, particularly the foundational discovery of chiral spin-orbit interactions, which continue to enable new developments in spin transport and topological materials."*



# SYMMETRY PROPERTIES IN BAND STRUCTURE : SPACE/TIME INVERSION

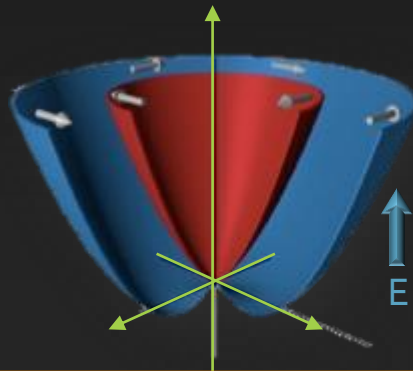
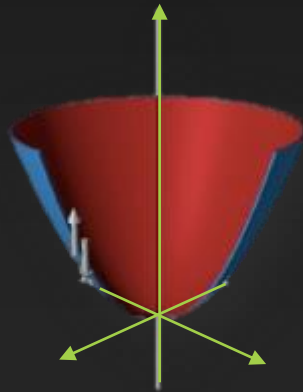
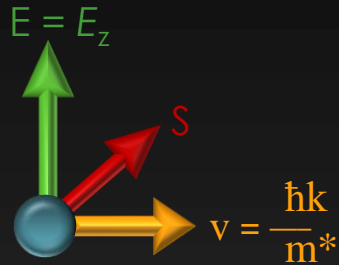
Time reversal symmetry:  $\epsilon_{k\uparrow} = \epsilon_{-k\downarrow}$

(Space) inversion symmetry:  $\epsilon_{k\uparrow} = \epsilon_{-k\uparrow}$

# WHAT IS THE RASHBA EFFECT ?

SOC effect: particle in electric field  $E$  experiences internal effective magnetic field  $B_{\text{eff}} \propto \mathbf{v} \times E$  in its moving frame

NB:  $E$  could be external (i.e. 2DEG), or “effective” (as in FE)

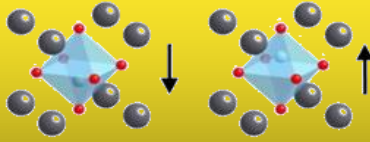


*E. Rashba, Sov. Phys. Solid State 2, 1109 (1960)*

# KEY CONCEPT & MAIN MESSAGE

(S. Picozzi, *Frontiers in Physics* 2, 10 (2013))

## FERROELECTRICITY



Permanent and switchable P, controllable via E

## SPIN-ORBIT COUPLING

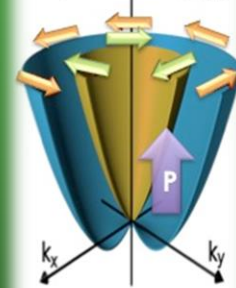


Relativistic interaction linking spin and lattice

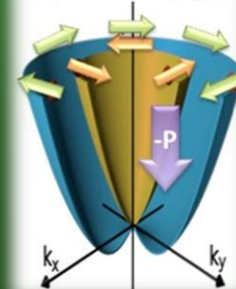
## RASHBA EFFECT

SPINTEXTURE: LINKED to P (via SOC) → CONTROL and SWITCH via E in a permanent (non volat.) way

a) Rashba ( $P_{up}$ )



b) Rashba ( $P_{dw}$ )

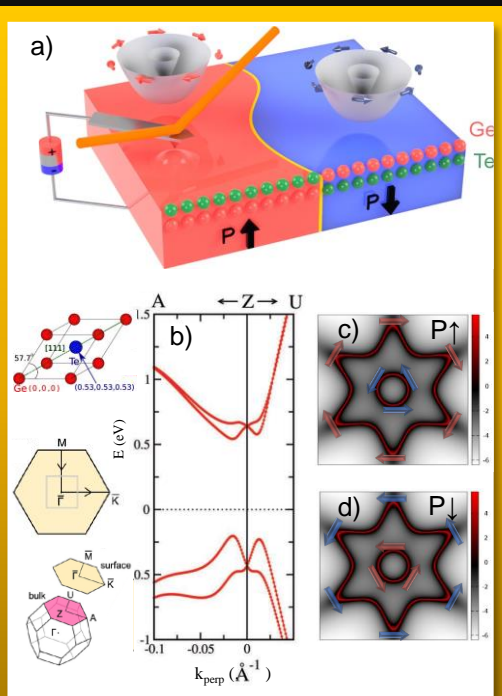




2013



## THEORY &amp; MODELLING

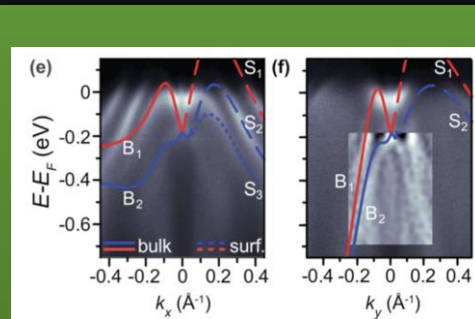


Di Sante, ... Bertacco, SP, Adv Mat (2013)

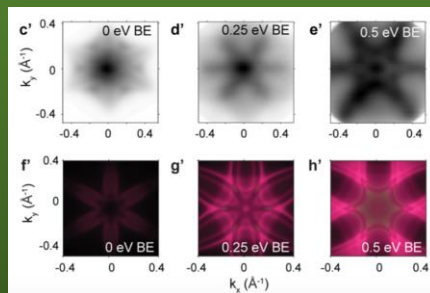
2016-18



## ADVANCED CHARACTERIZ.



Liebmann ... Bertacco, Panacione, SP, ... Adv Mat (2016)

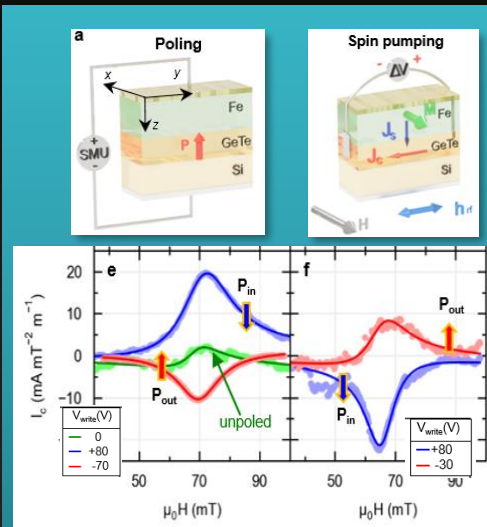


Rinaldi, ..., Panacione, SP, Bertacco, Nanoletters (2018)

2021



## TOWARDS DEVICES



Varotto, ... SP, ... Bertacco, Nature Electronics (2021)

# SPIN-ORBIT COUPLING: AN ENDLESS SOURCE OF EXOTIC MAGNETISM IN 2D MAGNETS

## OUTLINE:

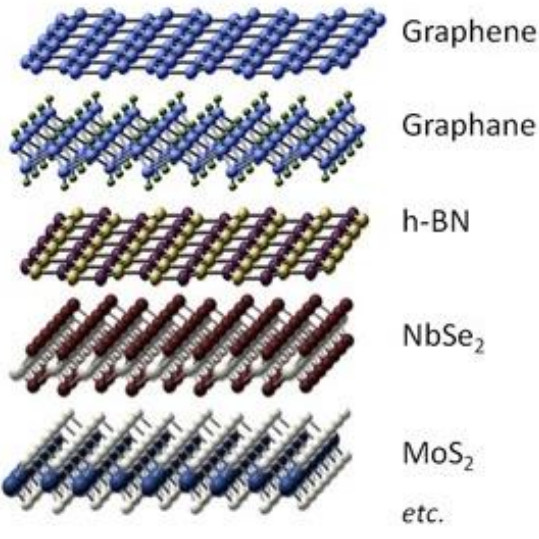
- Introduction: *Spin-orbit coupling*
- Focus on: “Rashba Physics” in Ferroelectrics

**Exotic Spin texture in 2D magnets**

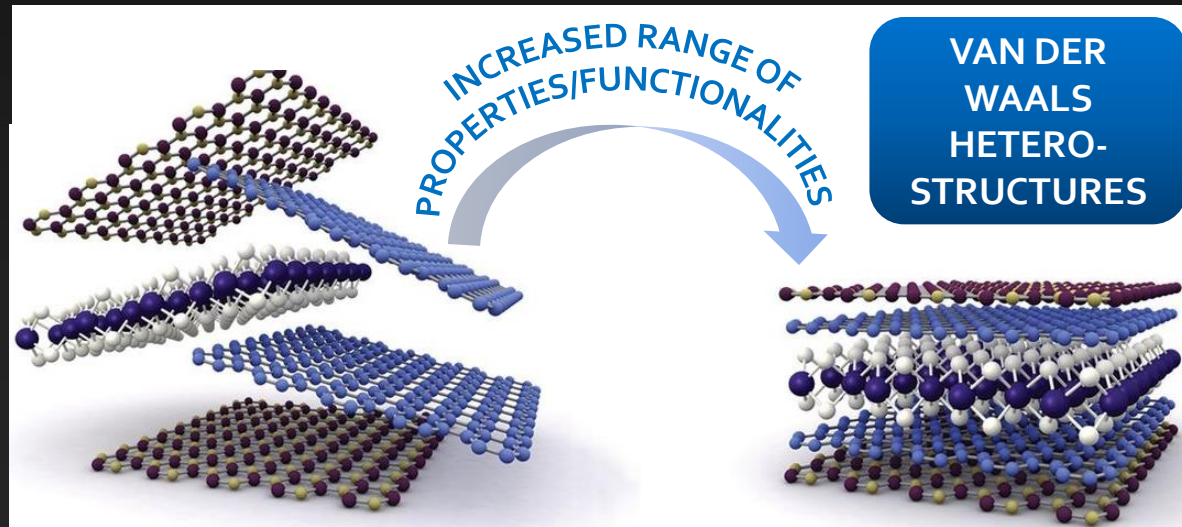
Multiferroicity in 2D magnets

# THE FLAT-LAND

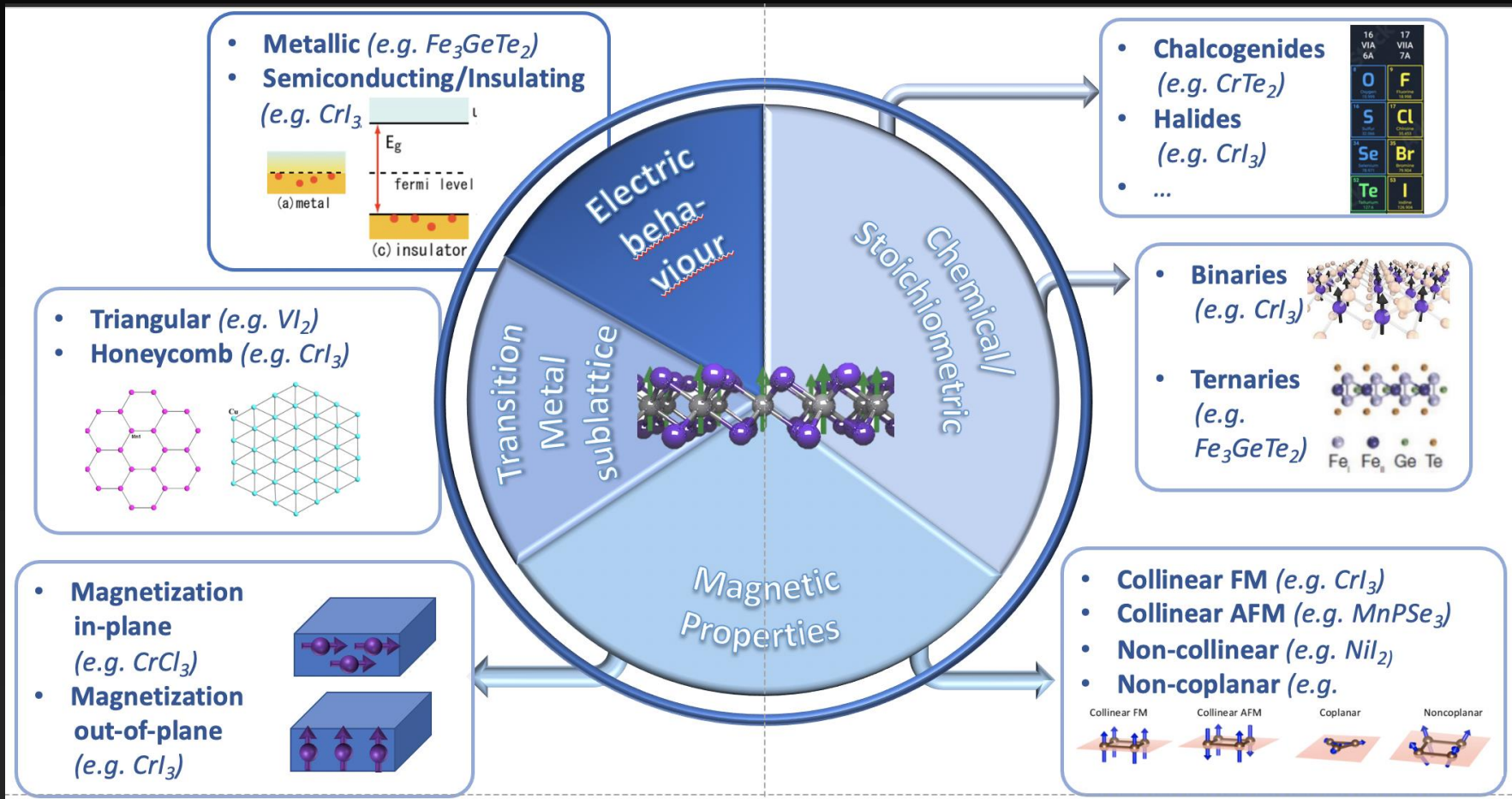
- ✓ One-atom-thick (or *few-atoms-thick*) systems
- ✓ Layers held together by (weak) Van der Waals forces
- ✓ Extended range of properties and functionalities
- ✓ Properties of 2D materials different from 3D counterparts



.... and you can play LEGO with 2D-materials !!



# 2D MAGNETS: A RICH PLAYGROUND



# CHALLENGES IN 2D MAGNETS & MERMIN WAGNER THEOREM

- Need to increase Curie temperature  $T_C$
- Need to improve air-stability & scalability
- **Need for improved understanding/modelling**

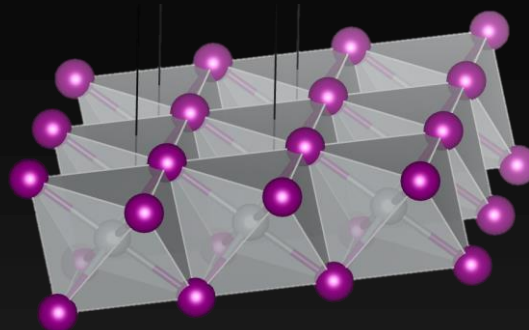
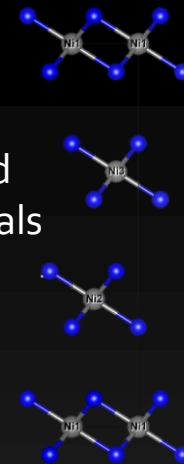


*"At any non-zero temperature, a one- or two-dimensional isotropic spin Heisenberg model with finite-range exchange interaction can be neither ferromagnetic nor antiferromagnetic."*

*N.D. Mermin and H. Wagner, Phys. Rev. Lett. 17, 1133 (1996)*

🔗 2D magnetism relies on **Anisotropic effects** 🔗 **Spin-orbit Coupling**

# BACKGROUND ON NiX<sub>2</sub> (X = Cl, Br, I): 3D vs 2D (ML)

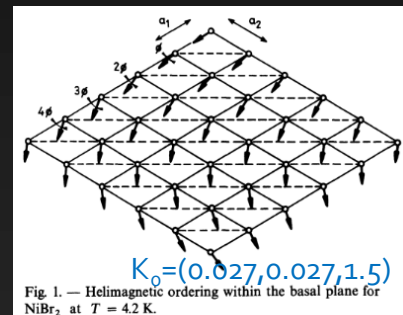
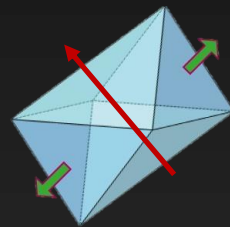


## MONOLAYER STRUCTURE

- ✓ Triangular lattice
- ✓ Edge-Shared octahedra:
  - small trigonal compression

## ELECTRON FILLING

- Ni 3p<sup>6</sup> 3d<sup>8</sup> 4s<sup>2</sup>
- Cl 3s<sup>2</sup> 3p<sup>5</sup>
- Br 4s<sup>2</sup> 4p<sup>5</sup>
- I 5s<sup>2</sup> 5p<sup>5</sup>



Régnault et al, J. Physique (1982)

## CRYSTAL FIELD SPLITTING: Ni d<sup>8</sup>



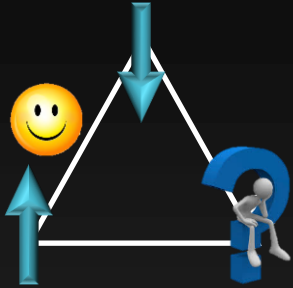
## MAGNETIC MOMENTS

- Localized moments on TM (high spin)
- Sizeable (positive) moment on halogen

**COMPLEX MAGNETISM!**

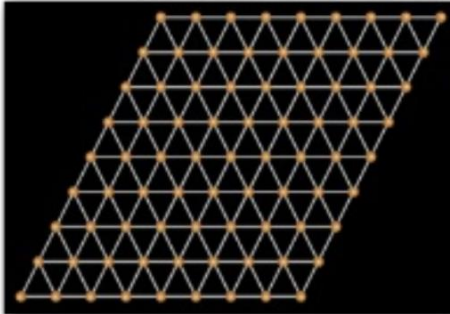
# FRUSTRATION IN MAGNETS: TRIANGLE

Spins on a triangular lattice with AFM coupling

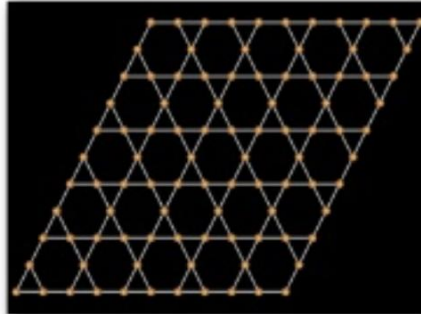


*What about  
the third  
spin ????*

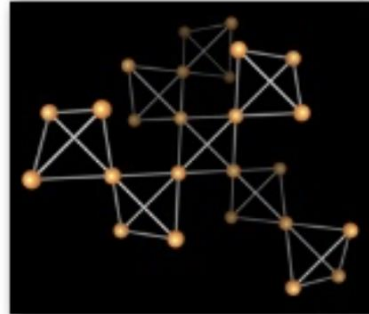
**triangular lattice**



**kagome lattice**

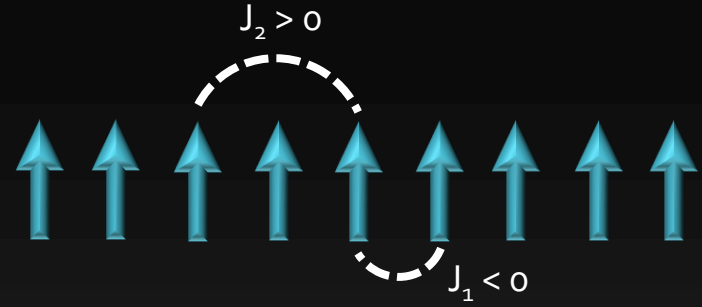


**pyrochlore lattice**



# FRUSTRATION IN MAGNETS: SPIN-CHAIN

- ✓ Simplest case: Frustrated spin chains with the **nearest-neighbour FM  $J_1$**  and **next-nearest-neighbour AFM  $J_2$**  interactions  $J_2$ .





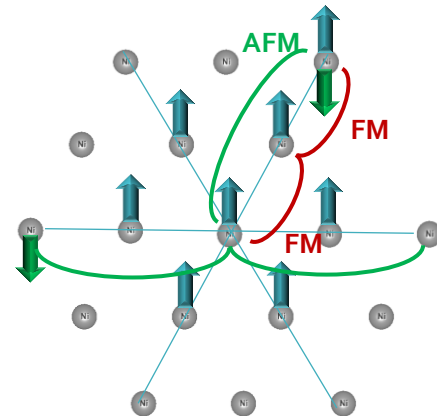
# EXCHANGE COUPLING CONSTANTS

Let's start with *Heisenberg Hamiltonian* (no SOC)

$$\mathcal{H} = -\frac{1}{2} \sum_{\substack{i,j \\ i \neq j}} J(\vec{r}_{ij}) \hat{S}_i \cdot \hat{S}_j$$

- ✓ Magnetic interaction strength varies with the ligand
- ✓ Longer ranged interaction in NiI<sub>2</sub> (5p) than in NiCl<sub>2</sub> (3p)

☞ Large exchange frustration  $J_3/J_1$  (increases with ligand)  
☞ EXPECTED NON-COLLINEARITY !!!



....NOT ONLY HEISENBERG

$$H = - \frac{1}{2} \sum_{i,j} J_{ij} \mathbf{S}_i \cdot \mathbf{S}_j$$

# INTERSITE EXCHANGE-COUPLING MATRIX

$$H = - \frac{1}{2} \sum_{i,j} J_{ij} \mathbf{S}_i \cdot \mathbf{S}_j + \sum_{i,j} D_{ij} \mathbf{S}_i \times \mathbf{S}_j + \sum_{i,j} \mathbf{S}_i \Gamma_{ij} \mathbf{S}_j$$

isotropic      Antisymmetric      (Traceless) Symmetric

Heisenberg      DM      Anisotropic exchange

# INTERSITE EXCHANGE-COUPLING MATRIX

$$H = -\frac{1}{2} \sum_{i,j} J_{ij} \mathbf{S}_i \cdot \mathbf{S}_j + \sum_{i,j} D_{ij} \mathbf{S}_i \times \mathbf{S}_j + \sum_{i,j} \mathbf{S}_i \Gamma_{ij} \mathbf{S}_j$$

isotropic Antisymmetric (Traceless) Symmetric  
Heisenberg DM Anisotropic exchange



# NiX<sub>2</sub>: ANISOTROPIC EXCHANGE AND SINGLE-ION ANISOTROPY

$$\mathcal{H} = \mathcal{H}_{\text{ex}} + \mathcal{H}_{\text{si}} = \frac{1}{2} \sum_{ij} S_i \cdot \mathcal{J}_{ij} \cdot S_j + \sum_i S_i \cdot \mathcal{A}_{ii} \cdot S_i$$

(Inter-site) Symmetric Anisotropic Exchange matrix (in meV)

-5.1	0	0
0	-5.1	0
0	0	-5.1

NiCl<sub>2</sub>

-6.0	0	0
0	-5.8	-0.1
0	-0.1	-5.9

NiBr<sub>2</sub>

-8.0	0	0
0	-5.6	-1.4
0	-1.4	-7.3

NiI<sub>2</sub>

J <sub>xx</sub>	0	0
0	J <sub>yy</sub>	J <sub>yz</sub>
0	J <sub>yz</sub>	J <sub>zz</sub>

Symmetry-allowed exchange tensor

17	Cl	Chlorine	Halogen
35	Br	Bromine	Halogen
53	I	Iodine	Halogen

✓ Anisotropies in 1<sup>st</sup> NN interaction in NiI<sub>2</sub>: anisotropic diagonal and large off-diagonal.  SOC of ligand: important!

# FROM EXCHANGE CONSTANTS TO THE SPIN-TEXTURE

$$\mathcal{H} = \mathcal{H}_{\text{ex}} + \mathcal{H}_{\text{si}} = \frac{1}{2} \sum_{ij} S_i \cdot \mathcal{J}_{ij} \cdot S_j + \sum_i S_i \cdot \mathcal{A}_{ii} \cdot S_i$$

Exchange Coupling Tensor

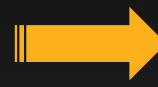
Single-Ion Anisotropy (SIA)

## MULTISCALE APPROACH

Plug DFT values into MonteCarlo simulations

☞ access to:

- 1) Larger (space) scales
- 2) Finite temperatures

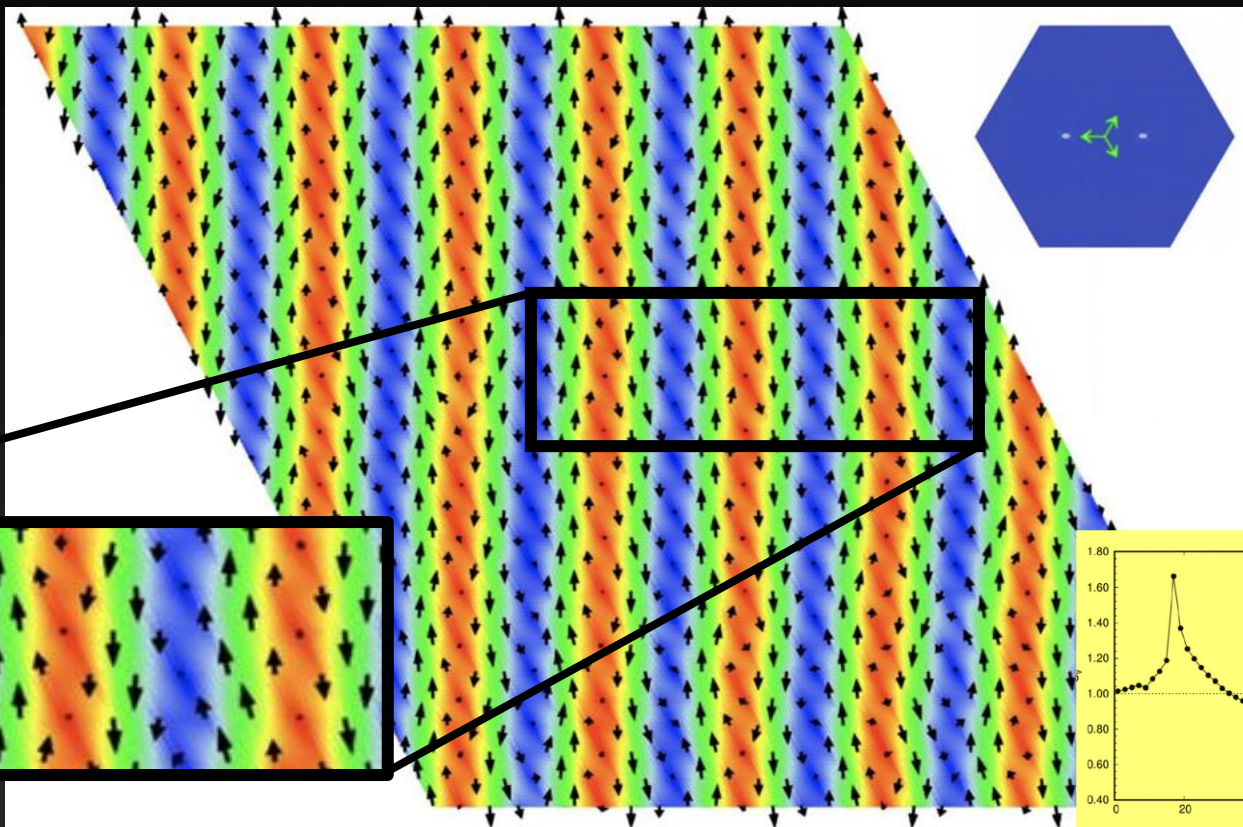


(Real-space)  
SPIN TEXTURE

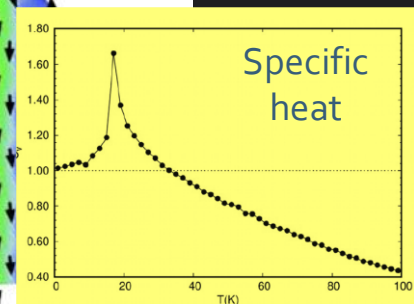
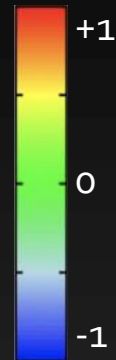
# NON-COLLINEARITY IN NiBr<sub>2</sub>


Results of MonteCarlo simulations  
(24x24)

Zoom of  
Helical  
phase

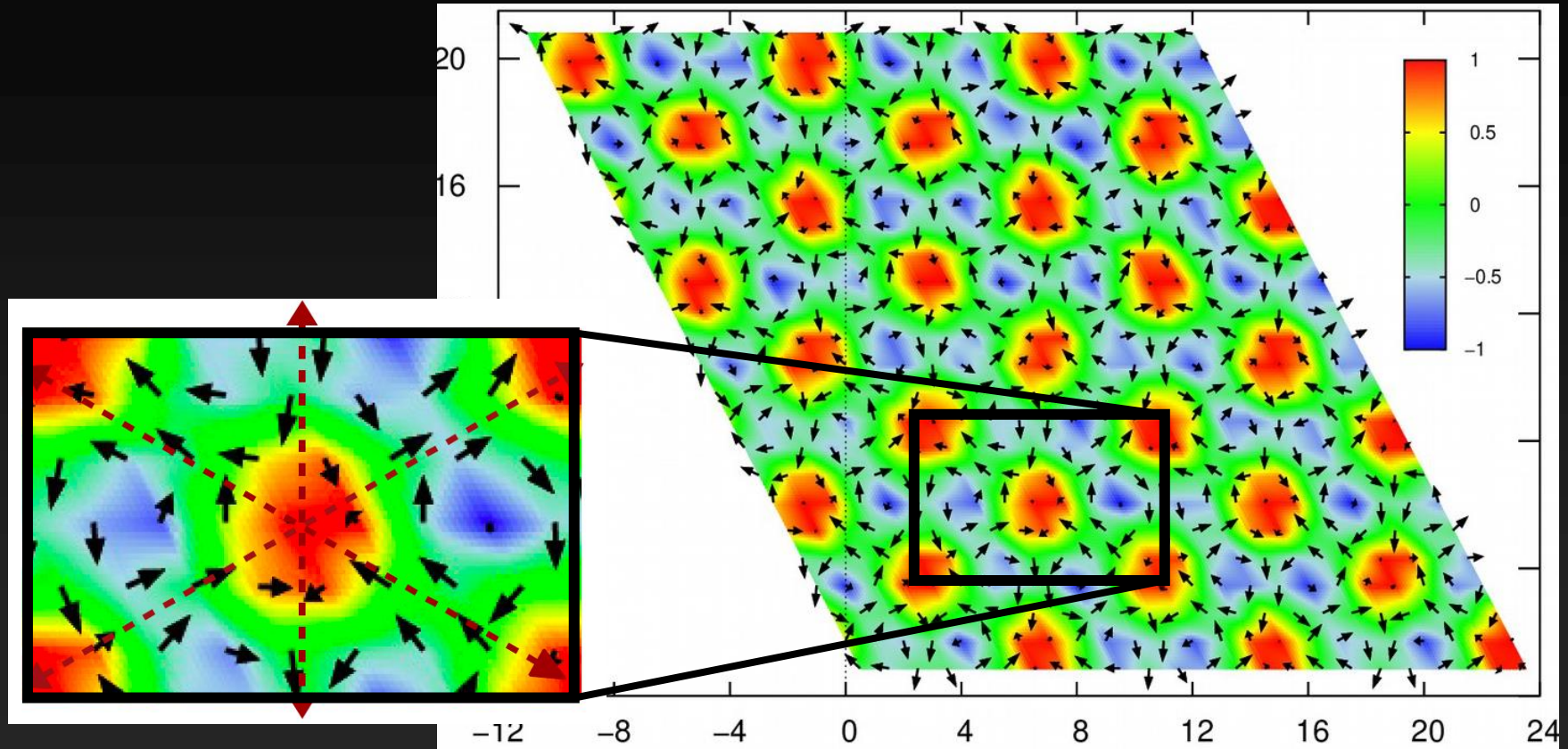


Color scale:  
S<sub>z</sub> (out-of-  
plane spins)



Single-q state along  $\mathbf{q}_3 = (-2\delta, \delta)$   **SPIN HELIX**

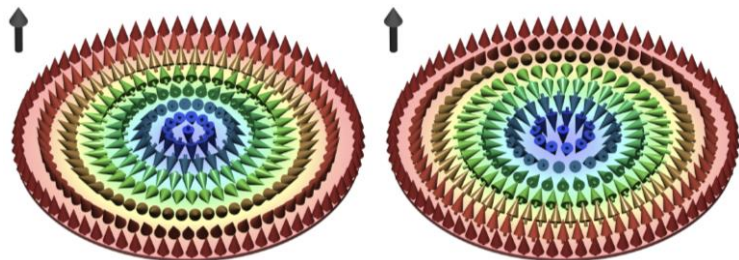
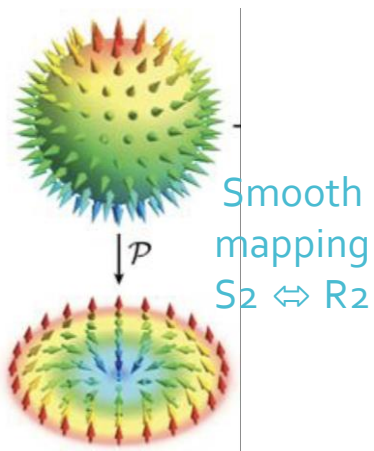
# $\text{NiI}_2$ : EXOTIC NON-COPLANAR SPIN-ORDER !!!



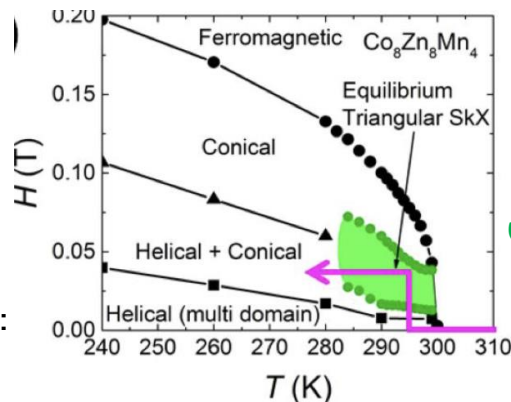


# WHAT IS A MAGNETIC SKYRMION ?

Particle-like nanometre-sized spin texture of topological origin (*Bogdanov, 1989*)



Different handedness (or rotational sense):  
Counterlockwise vs clockwise



Phase diagram

## TOPOLOGICAL CHARGE (discrete approx.)

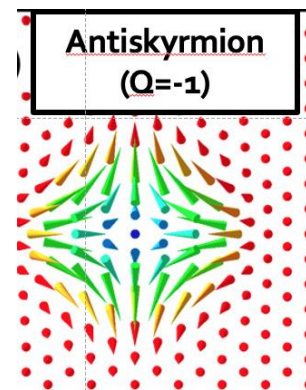
➤ (Classical) Spins  $\mathbf{m}_i$  on atomic sites

➤ Topological charge  $Q = \sum q_i$

$$\tan\left(\frac{1}{2}q\right) = \frac{[\mathbf{m}_1 \mathbf{m}_2 \mathbf{m}_3]}{1 + \mathbf{m}_1 \mathbf{m}_2 + \mathbf{m}_1 \mathbf{m}_3 + \mathbf{m}_2 \mathbf{m}_3}$$

Triple-scalar product  
(or scalar spin-chirality)  
 $= \mathbf{m}_1 \cdot (\mathbf{m}_2 \times \mathbf{m}_3)$

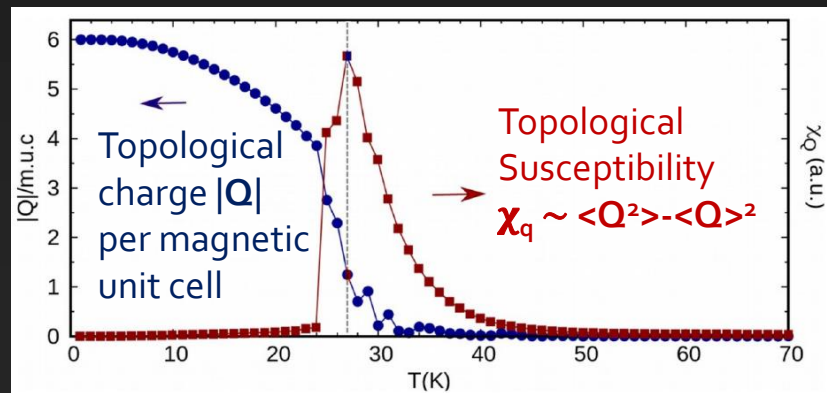
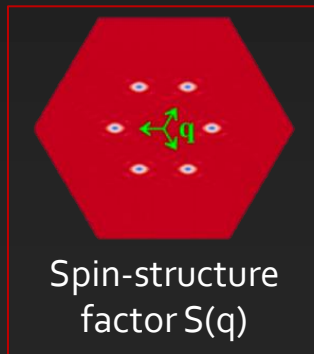
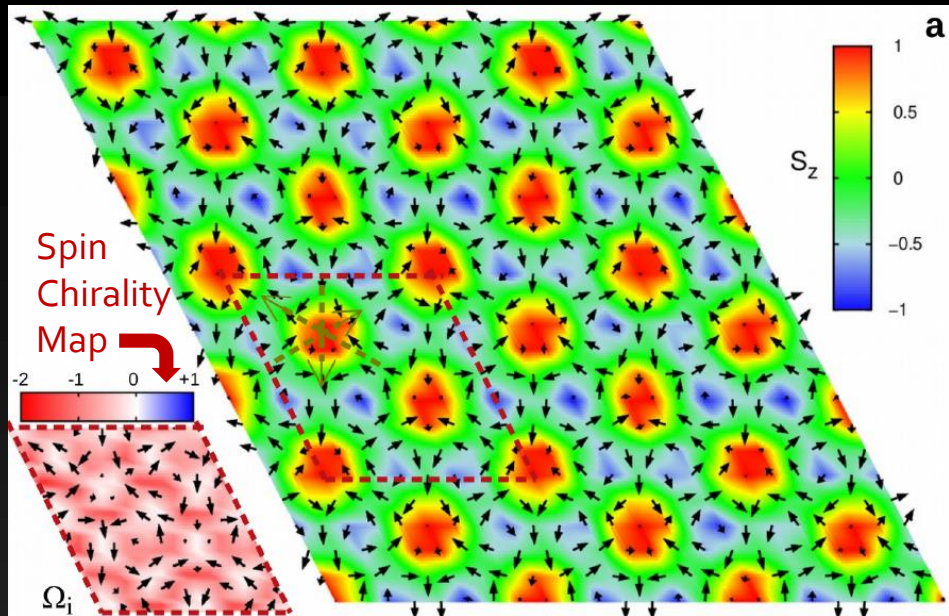
**Antiskyrmion:**  
change of rotational sense  
for two high symmetry directions



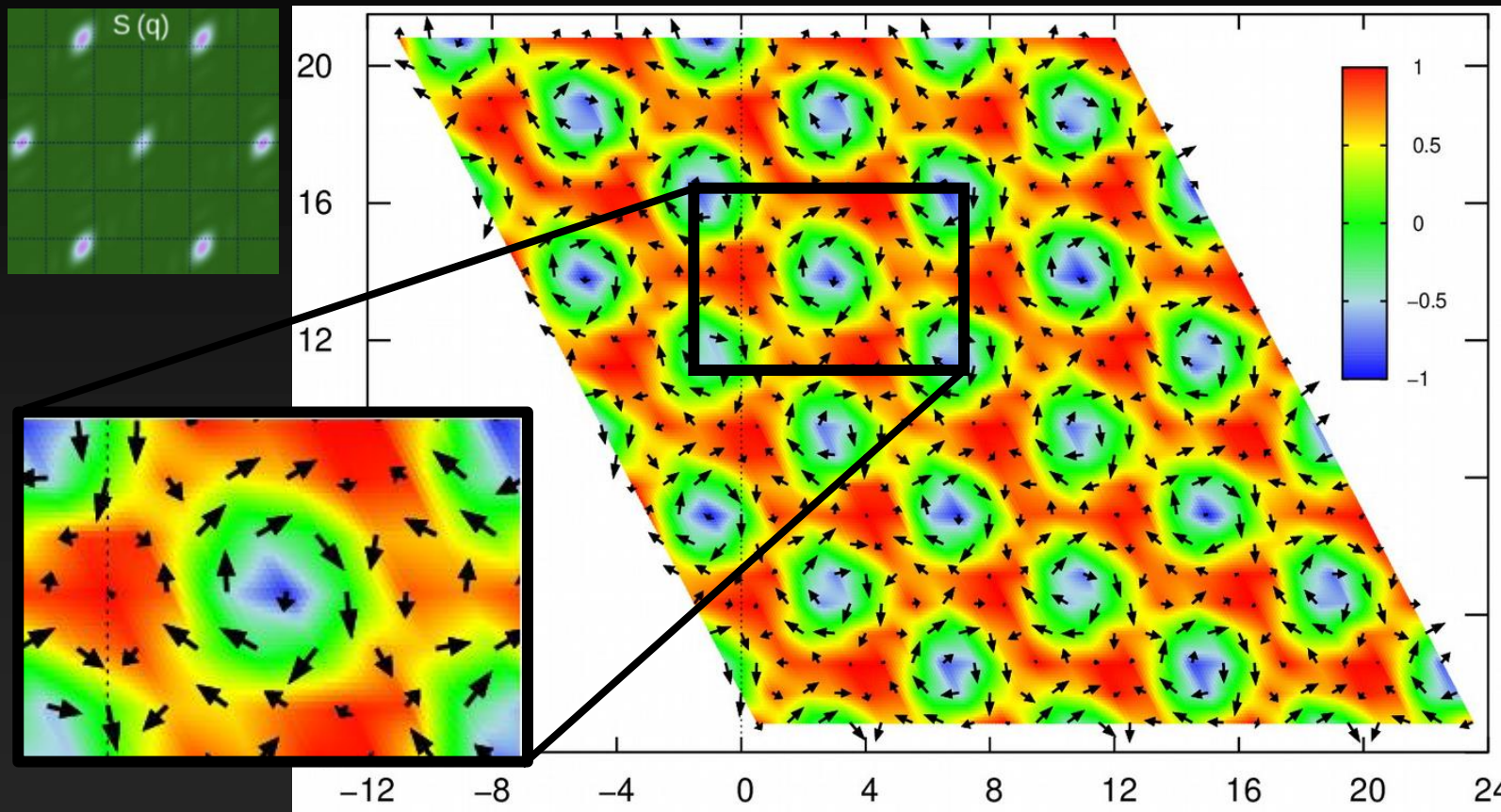
# TOPOLOGICAL CHARGE

☞  $|Q|=2$  Higher-order antiskyrmion!

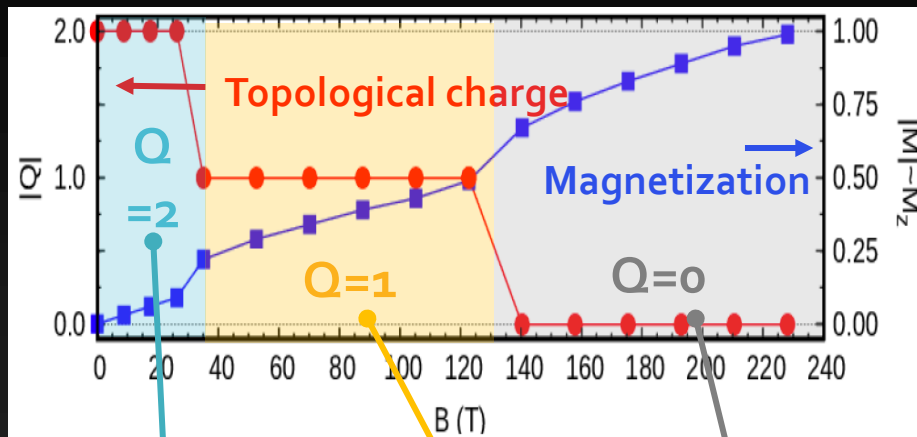
- ✓ Topological state without B field
- ✓ First example in 2D magnets
- ✓ Not driven by Dzyaloshinskii-Moriya



# WHAT HAPPENS UNDER MAGNETIC FIELD?



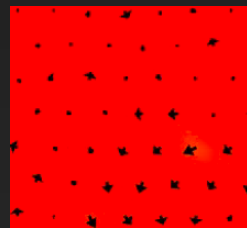
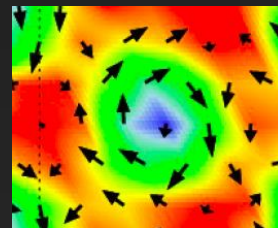
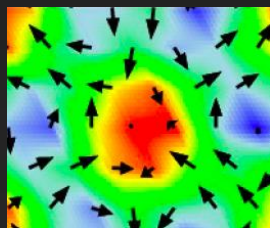
# WHAT HAPPENS UNDER MAGNETIC FIELD?



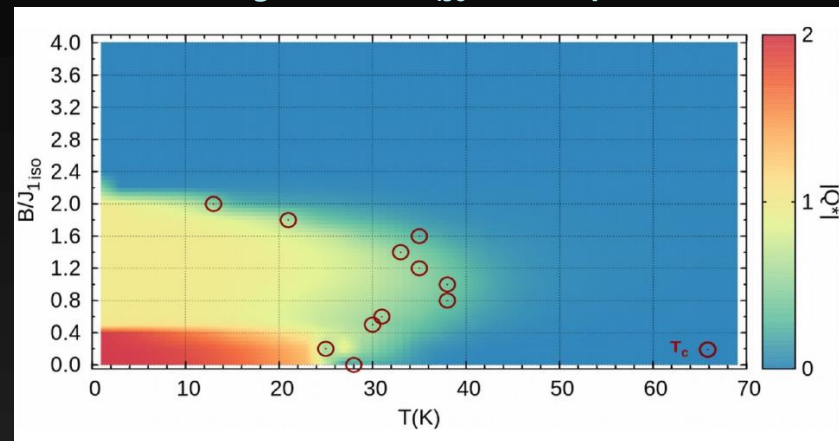
$|Q|=2$  skyrmion

$|Q|=1$  skyrmion

FM ( $|Q|=0$ )



## Phase Diagram of $B/J_{iso}$ vs Temperature



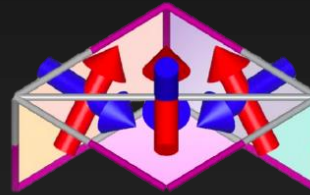
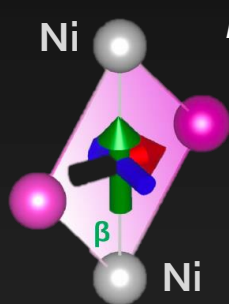
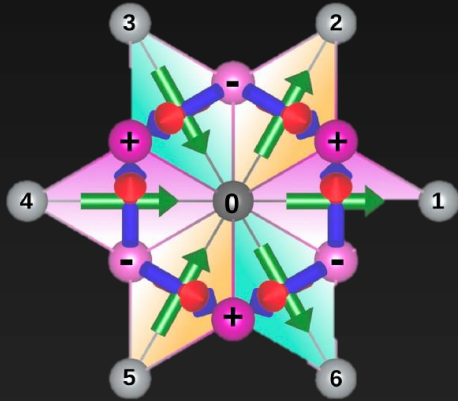
Sharp topological transition to «conventional» ( $|Q|=1$ ) skyrmion!

# ROLE OF ANISOTROPIC EXCHANGE IN EXOTIC MAGNETISM

$J_{xx}$	0	0
0	$J_{yy}$	$J_{yz}$
0	$J_{yz}$	$J_{zz}$

Diagonalize

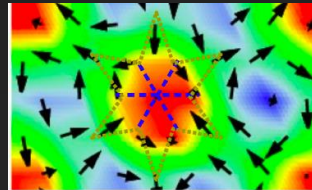
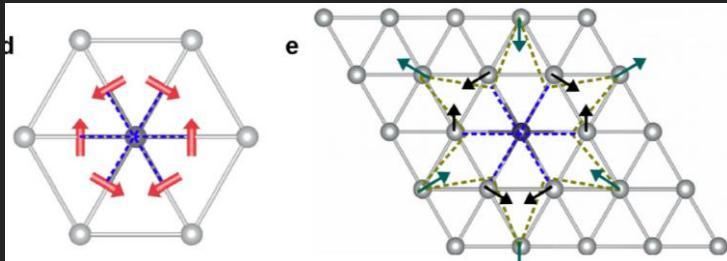
$J_\alpha$	0	0
0	$J_\beta$	0
0	0	$J_\gamma$



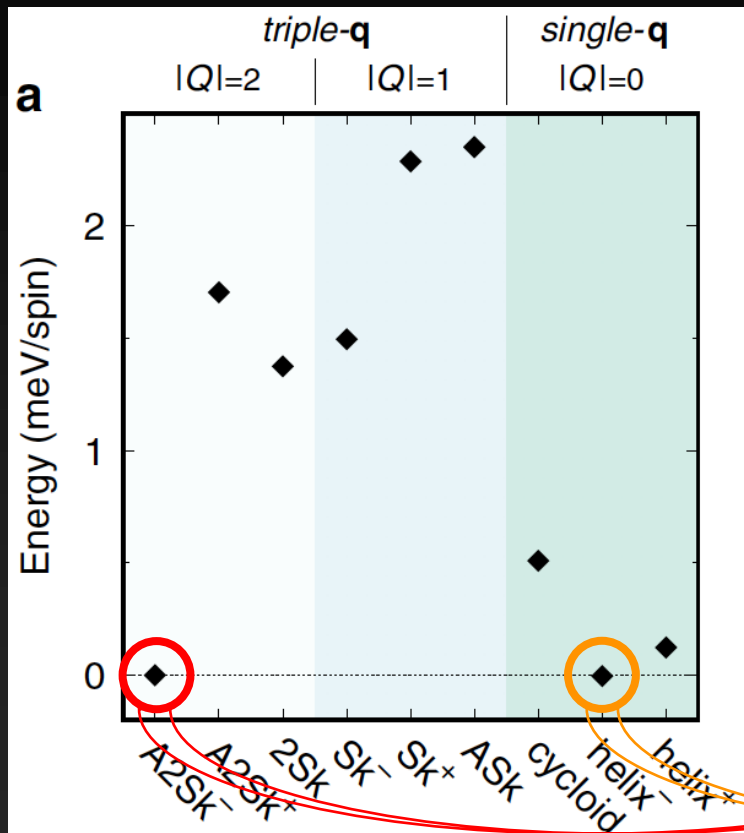
Two eigenvectors in the Ni-I-Ni plane

- One along I-I ligands
- One along Ni-Ni

Third eigenvector  $\perp$  to the Ni-I-Ni-I plaquette

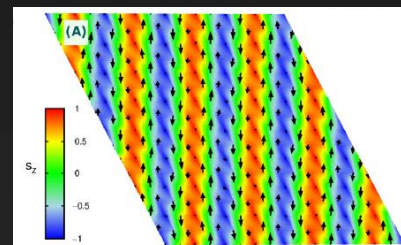
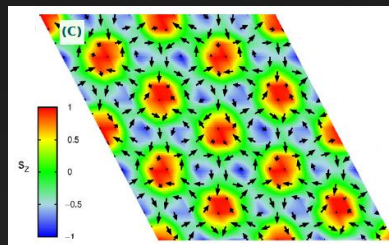


# TOTAL ENERGIES OF SELECTED SPIN CONFIGURATIONS



- Superscript  $\pm$  : chiral partners of the given spin texture, related by a reflection with respect to the xy plane
- Single-q spin configurations generated by MC simulations artificially tuning the two-site anisotropy term.

Energy degeneracy between Antiskyrmion and Spin-Helix !



# SPIN-ORBIT COUPLING: AN ENDLESS SOURCE OF EXOTIC MAGNETISM IN 2D MAGNETS

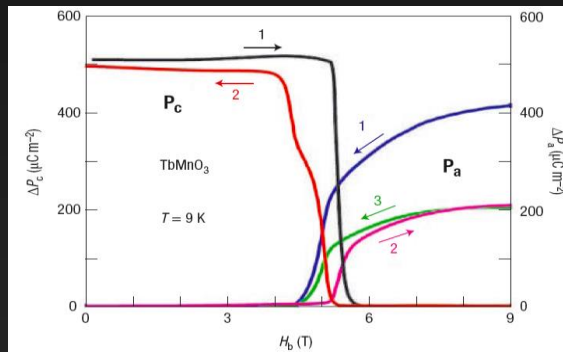
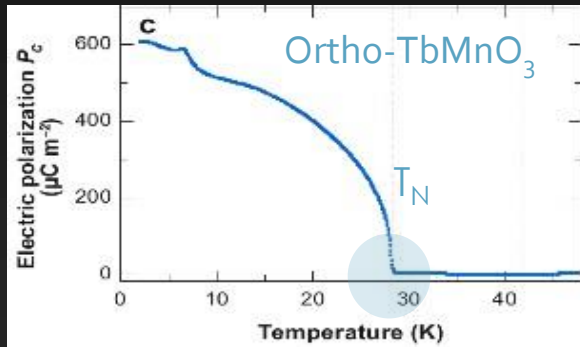
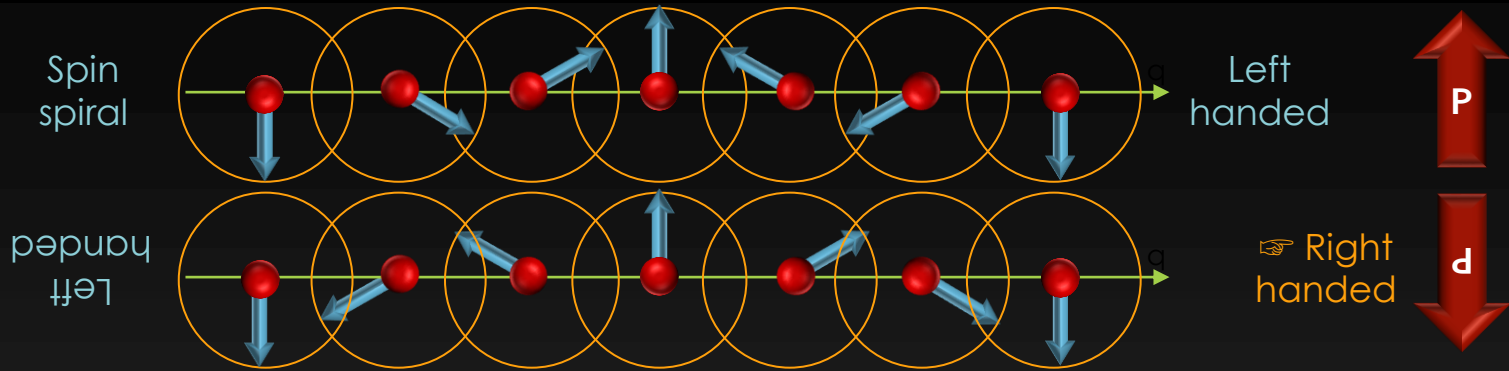
## OUTLINE:

- Introduction: *Spin-orbit coupling*
- Focus on: “Rashba Physics” in Ferroelectrics

Exotic Spin texture in 2D magnets

**Multiferroicity in 2D magnets**

# HOW THE HYPE ON (ELECTRONIC) MULTIFERROICS STARTED ...



*T.Kimura & al., Nature 425, 55 (03);  
S.W.Cheong & M.Mostovoy, Nature Mater. 6, 13 (07)*



nature

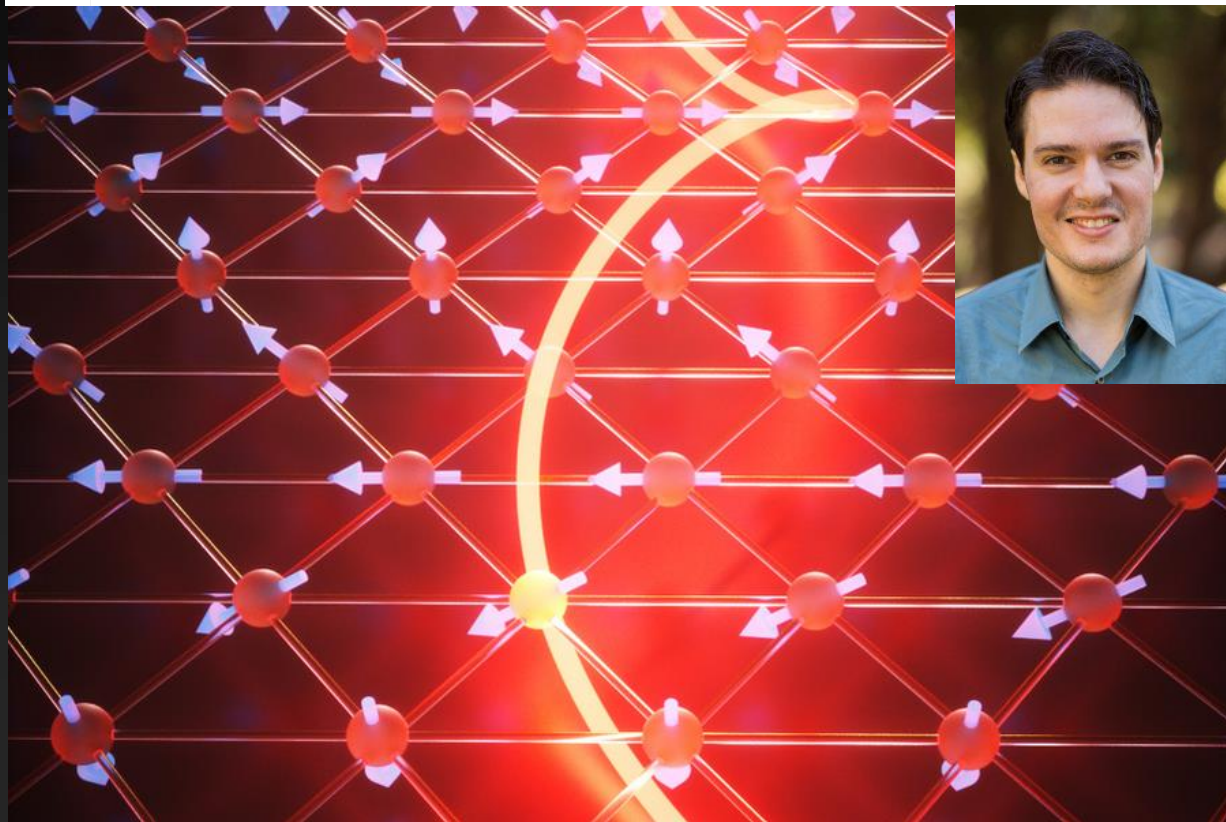
## Evidence for a single-layer van der Waals multiferroic

[Qian Song](#), [Connor A. Occhialini](#), [Emre Ergeçen](#), [Batyr Ilyas](#), [Danila Amoroso](#), [Paolo Barone](#), [Jesse](#)

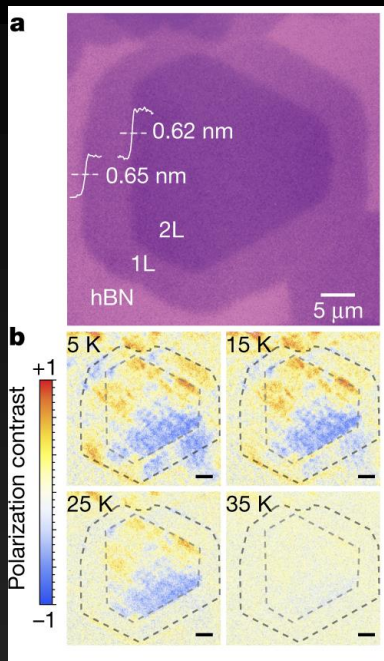
[Kapeghian](#), [Kenji Watanabe](#), [Takashi Taniguchi](#), [Antia S. Botana](#), [Silvia Picozzi](#), [Nuh Gedik](#) & [Riccardo Comin](#)

*Nature* **602**, 601–605 (2022) | [Cite this article](#)

Can Multi-Ferroicity persist down to the ultimate monolayer limit ?

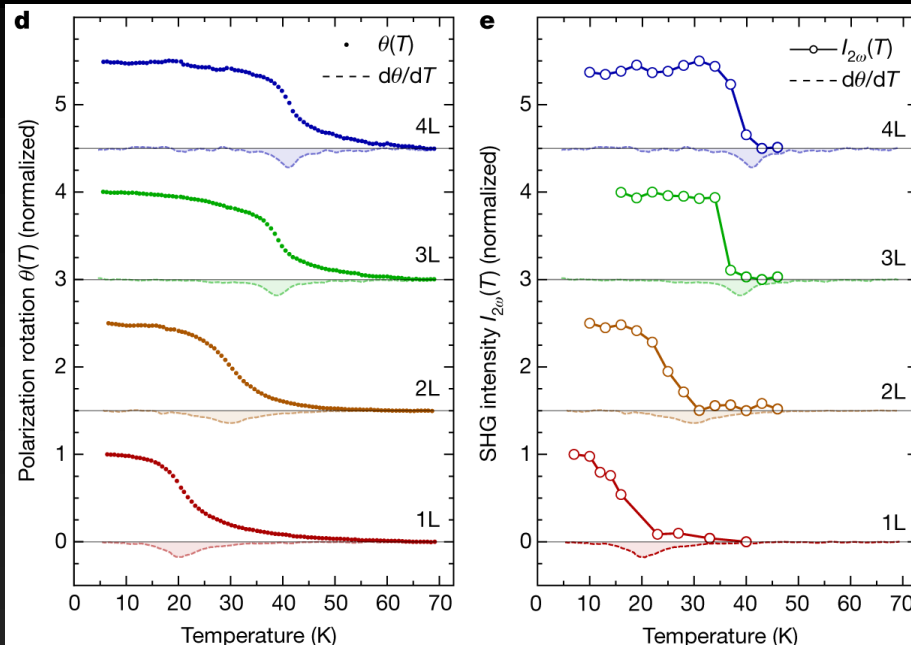


# OPTICAL CHARACTERIZATION OF FEW-LAYERS $\text{NiI}_2$

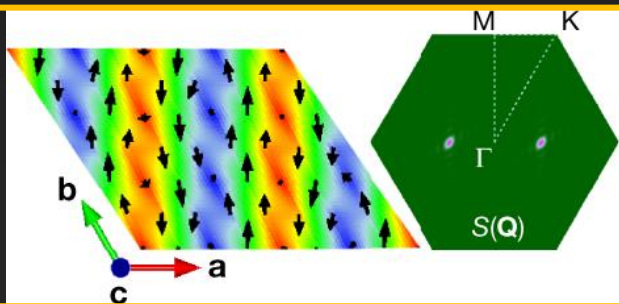


Optical image  
 $\text{NiI}_2$  samples  
grown on hBN

Temperature-  
dependent  
polarized  
microscopy



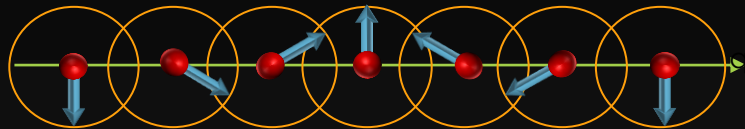
Spin-helix:  
likely spin  
ground  
state!



d. Temperature-dependent, birefringence-induced polarization rotation  $\vartheta(T)$  in monodomain regions.  
e. Temperature-dependent ED-SHG. Data normalized to value at 5 K and offset vertically for clarity.

# SPIN-INDUCED FERROELECTRICITY: SPIN CURRENT MODEL

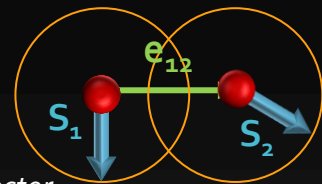
Spin cycloid (spins in a plane containing  $e_{12}$ )



*Katsura, Nagaosa, Balatsky (PRL 2005)*

$$P_{12} = e_{12} \times (S_1 \times S_2)$$

$e_{12}$ : spiral propagation vector



# MAGNETOELECTRIC TENSOR (DFT)

$$\mathbf{P}_{12} = \mathbf{M}(\mathbf{S}_1 \times \mathbf{S}_2)$$

$$\begin{pmatrix} M_{11} & M_{12} & M_{13} \\ M_{21} & M_{22} & M_{23} \\ M_{31} & M_{32} & M_{33} \end{pmatrix} = \begin{pmatrix} 20 & 0 & 32 \\ 0 & 348 & -520 \\ 0 & 25 & 0 \end{pmatrix}$$

Units:  $10^{-5}$  e Ang

Large “non-KNB”  
terms!

# We now have a 2D multiferroic !

2d-Materials  
LEGO

Thanks for  
your attention  
!

