Hardware requirements for useful superconducting quantum computers

Manuel Pino García, 22/05/2024 Universidad de Salamanca

QUANTUM MATTER FOR QUANTUM TECHNOLOGIES

In collaboration:

J. J. García Ripoll, G. Jaumá Quinfog CSIC (Madrid), M. Hita-Pérez Quilimanjaro Quantum Tech.

Quantum materials for quantum technologies

Quantum materials for quantum technologies

Superconducting circuits

Quantum materials for quantum technologies

Superconducting circuits **Superconducting circuits** Quantum computing

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I. Siddiqi, Nat. Rev. Mat. 6.10 (2021): 875-891

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$2\pi\phi/\Phi_0$ $\ket{\pm} = \frac{\ket{1} \pm \ket{-1}}{\sqrt{2}}$

- Hita-Pérez, Orellana, García-Ripoll M. Pino PRA (2023)

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- Weak or too "simple" qubit-qubit couplings This talk is all about this

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- Minimal form of 2 qubit coupling (Biamonte, Love 2008, ...)
- We need minimum complexity for qubit-qubit interactions! For instance:

$$
\mathrm{H}=\textstyle\sum\Delta_i\sigma_i^z+\textstyle\sum J_{ij}^{yy}\sigma_i^y\sigma_j^y+\textstyle\sum J_{ij}^{xx}\sigma_i^x\sigma_j^x
$$

This is all about the first part of the talk: Strength and form of qubit-qubit couplings

Qubit-qubit:

Strong coupling Quantum Monte-Carlo suffers sign problem (non-stoquastic)

Qubit-resonator:

New phenomena for LC-qubit strongly coupled in two directions

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Qubit-resonator:

New phenomena for LC-qubit strongly coupled in two directions

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H = \Delta \sigma^z + \omega b^{\dagger} b + g^x \sigma^x (a + a^{\dagger}) + ig^y \sigma^y (a - a^{\dagger})
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Harris et. al. (D-wave) PRB (2009)

Ozfidan, ...Amin (D-wave) PRApp (2020)

Yamamoto,… Nakamura NJP 2014

Charge-charge coupling

- Only focuss on charge coupling

$$
H = H_0 + \frac{q_1 q_2}{\overline{c}_g}
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 $q_q = \frac{\Phi_0}{2\pi} \frac{C_q \Delta \varphi_\star}{\hbar} \sigma_i^y$

$$
q_r=\sqrt{\tfrac{\hbar}{2Z}}i(b-b^\dagger)
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$$
H_0 = \Delta \sigma^z + \omega_r a_r^{\dagger} a_r
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Usual approach, project on non-interacting qubit subspace

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- Qubit-qubit coupling $H_{q\bar{q}} \approx g^{yy} \sigma_1^y \sigma_2^y$

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\tfrac{g^{yy}}{\Delta} = \tfrac{\overline{c}_q \varphi_{\star}^2}{\overline{c}_g} \tfrac{\Delta}{4E_C^q}
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- Qubit-qubit coupling $H_{aa}\approx g^{yy}\sigma_1^y\sigma_2^y$ - Qubit-resonator $H_{qr}\approx ig^{yy}\sigma_1^y(a-a^\dagger)$ $\frac{g_{qr}}{\Delta} = \frac{c_g}{\overline{c}_g} \frac{\varphi^{\star}}{2} \sqrt{\frac{1}{G_0 \mathcal{Z}}}$

$$
H_q = P_0 H_c P_0 + \sum_{n=1,...} \gamma^n \mathcal{M}_n
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|\mathcal{M}_n| \sim \left(\tfrac{V_{qe}}{\hbar \omega_q}\right)^m
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LC-resonator
\n
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\begin{array}{c}\n\downarrow \qquad \qquad \downarrow \qquad \qquad \downarrow \qquad \qquad \downarrow \
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- At strong coupling $\gamma \sim 1$

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Qubit-resonator coupling. YES!

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Qubit-resonator coupling. $YES!$ Qubit-qubit coupling. $NO!$ – > Need to sum up full series

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- Strong and Non-Stoquastic couplings

- Future work: similar technics to understand effective qubits coupling in other setups

Hita-Pérez, Jaumá, Pino, García-Ripoll PRApp (2022), Hita-Pérez, Jaumá, Pino, García-Ripoll. Appl. Phys. Lett (2021)

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1D nearest-neighbours --- > Trivial

Fully connected --- > Spin-glass (NP-hard)

A. D. King, … Amin (2023), Computational supremacy in quantum simulation (2024)

- Try to look for spin-glasses not fully connected:

Non-complanar qasi-2D graphs

- Spin-glass state at T=0. Fernandez et al JPA (2019) Low-energy may be easy to approxmate
- Chimera, Pegasus, Zaphyr (d-wave graphs)

Mean field glasses $\mathrm{D} \approx \infty$

- Random regular graphs
- Small-world networks Katzgraber PRAPP(2018)

- Is there any change to obtain classically difficult problems in a 2D Ising? Yes!

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Time to perform Paralell Tempering "exploit" below the pseudo-critical temperature

Look for higher pseudo-critical temperature! Jaumá, García-Ripoll,Pino. Adv. Quant. Tech. (2023)

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	- General form of qubit couplings (Non-stoquastic) We worked to analyze and understand capacitive couplings in flux qubits
	- Long-range but simpler qubit couplings (spin-glasses) Our work shows that planar graphs connections may be usefull

The end

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-

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Hita-Pérez, Jaumá, Pino, García-Ripoll PRApp (2022)

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Hita-Pérez, Jaumá, Pino, García-Ripoll PRApp (2022)

Different conclussion in Yoshiara, … Semba Nat. Comm. (2022)

Numerical results for coupling extracted with full SW transformation Hita-Pérez, Jaumá, Pino, García-Ripoll PRApp (2022),

- First order does not work! Diagrams

- We compute spin-glass phase transition via Paralell Tempering

- There is no phase spin-glass in D-wave lattice

 Are D-wave lattice very bad!? Katzgraber, et al. PRX (2015) Additional problems, temperature Chaos. Martin-Mayor et al. Sci. Rep. (2015)