## Hardware requirements for useful superconducting quantum computers

Manuel Pino García, 22/05/2024 Universidad de Salamanca





#### QUANTUM MATTER FOR QUANTUM TECHNOLOGIES



#### In collaboration:

J. J. García Ripoll, G. Jaumá Quinfog CSIC (Madrid), M. Hita-Pérez Quilimanjaro Quantum Tech.



Quantum materials for quantum technologies



Quantum materials for quantum technologies

Superconducting circuits





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Superconducting circuits







What are bottleneck in superconducting hardware? How to overcome them?



- Superconducting qubit use Josephson junction



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I. Siddiqi, Nat. Rev. Mat. 6.10 (2021): 875-891



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#### <u>Fluxoniums</u> $T \approx 0.1 ms$

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# $|\pm angle=rac{|1 angle\pm|-1 angle}{\sqrt{2}}$

- Hita-Pérez, Orellana, García-Ripoll <u>M. Pino</u>PRA (2023)



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- No at the level 1 qubit. Problems comes when coupling qubts
- Sensibility to external fields --- > Open the door to noise
  - Topological (ptotection + manipulation) Kitaev (2001), Kouwenhoven Nature (2023), R. Aguado, La Rivista del Nuovo Cimento (2017)
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- <u>Weak or too "simple" qubit-qubit couplings</u> This talk is all about this

	× ×	/
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T(ms)





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- Adiabatic quantum computing:
- Hamiltonian with two body interactions (Julia Kempe, Alexei Kitaev & Oded Regev )
- Minimal form of 2 qubit coupling (Biamonte, Love 2008, ...)
- We need minimum complexity for qubit-qubit interactions! For instance:

$$\mathbf{H} = \sum \Delta_i \sigma_i^z + \sum J_{ij}^{yy} \sigma_i^y \sigma_j^y + \sum J_{ij}^{xx} \sigma_i^x \sigma_j^x$$

This is all about the first part of the talk: <u>Strength and form of qubit-qubit couplings</u>



<u>Qubit-qubit</u>:

Strong coupling Quantum Monte-Carlo suffers sign problem (non-stoquastic)

<u>Qubit-resonator</u>:

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$$\mathbf{H} = \Delta \sigma^{z} + \omega b^{\dagger} b + g^{x} \sigma^{x} \left( a + a^{\dagger} \right) + i g^{y} \sigma^{y} \left( a - a^{\dagger} \right)$$



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Harris et. al. (D-wave) PRB (2009)



Ozfidan, ...Amin (D-wave) PRApp (2020)



Yamamoto,... Nakamura NJP 2014



Charge-charge coupling

- Only focuss on charge coupling

$$H = H_0 + \frac{q_1 q_2}{\overline{c}_g}$$


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$$q_q = \frac{\Phi_0}{2\pi} \frac{C_q \Delta \varphi_\star}{\hbar} \sigma_i^y$$

$$q_r = \sqrt{\frac{\hbar}{2Z}}i(b - b^{\dagger})$$



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- Qubit-resonator  $H_{qr} \approx i g^{yy} \sigma_1^y (a - a^{\dagger})$  $\frac{g_{qr}}{\Delta} = \frac{c_g}{\overline{c}_g} \frac{\varphi^{\star}}{2} \sqrt{\frac{1}{G_0 \mathcal{Z}}}$ 





$$\mathbf{H}_q = P_0 H_c P_0 + \sum_{n=1,\dots} \gamma^n \mathcal{M}_n$$

$$|\mathcal{M}_n| \sim \left(\frac{V_{qe}}{\hbar\omega_q}\right)^m$$



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- Does this projections work well? Sure for small coupling. For larger, Schreiffel-Wolf:

$$\begin{aligned} \mathbf{H}_{q} &= P_{0}H_{c}P_{0} + \sum_{n=1,\dots} \gamma^{n}\mathcal{M}_{n} \\ |\mathcal{M}_{n}| \sim \left(\frac{V_{qe}}{\hbar\omega_{q}}\right)^{m} \end{aligned}$$



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Qubit-qubit coupling.  $\underline{NO!} - > Need to sum up full series$ 

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- Future work: similar technics to understand effective qubits coupling in other setups

Hita-Pérez, Jaumá, Pino, García-Ripoll PRApp (2022), Hita-Pérez, Jaumá, Pino, García-Ripoll. Appl. Phys. Lett (2021)



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Graph of connections in quantum annealers

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 $H = sH_{p} + (1 - s) \sum \sigma_{i}^{z}$  $H_{P} = \sum \Delta_{i}\sigma_{i}^{x} + \sum J_{ij}\sigma_{i}^{x}\sigma_{j}^{x}$ 

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1D nearest-neighbours --- > Trivial

Fully connected --- > Spin-glass (NP-hard)

A. D. King, ... Amin (2023), Computational supremacy in quantum simulation (2024)







- Try to look for spin-glasses not fully connected:

Non-complanar qasi-2D graphs

- Spin-glass state at T=0. Fernandez et al JPA (2019) Low-energy may be easy to approxmate
- Chimera, Pegasus, Zaphyr (d-wave graphs)

Mean field glasses  $D{\approx\infty}$ 

- Random regular graphs
- Small-world networks Katzgraber PRAPP(2018)





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Time to perform Paralell Tempering "exploit" below the pseudo-critical temperature

Look for higher pseudo-critical temperature! Jaumá, García-Ripoll, Pino. Adv. Quant. Tech. (2023)





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## The end





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Hita-Pérez, Jaumá, Pino, García-Ripoll PRApp (2022)







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Hita-Pérez, Jaumá, Pino, García-Ripoll PRApp (2022)

Different conclussion in Yoshiara, ... Semba Nat. Comm. (2022)



## Numerical results for coupling extracted with full SW transformation Hita-Pérez, Jaumá, Pino, García-Ripoll PRApp (2022),





- <u>First order does not work</u>! Diagrams



Hita-Pérez, Jaumá, Pino, García-Ripoll PRApp (2022)



- We compute spin-glass phase transition via Paralell Tempering



- There is no phase spin-glass in D-wave lattice

Are D-wave lattice very bad!? Katzgraber, et al. PRX (2015) Additional problems, temperature Chaos. Martin-Mayor et al. Sci. Rep. (2015)