

Topological transport of magnon polarons

Shu Zhang

Okinawa Institute of Science and Technology (OIST) Graduate School

Okinawa, Japan

@ SPICE-Workshop on

Quantum Geometry and Transport of Collective Excitations in (Non-)Magnetic Insulators

May. 6th 2025



OKINAWA INSTITUTE OF SCIENCE AND TECHNOLOGY
GRADUATE UNIVERSITY

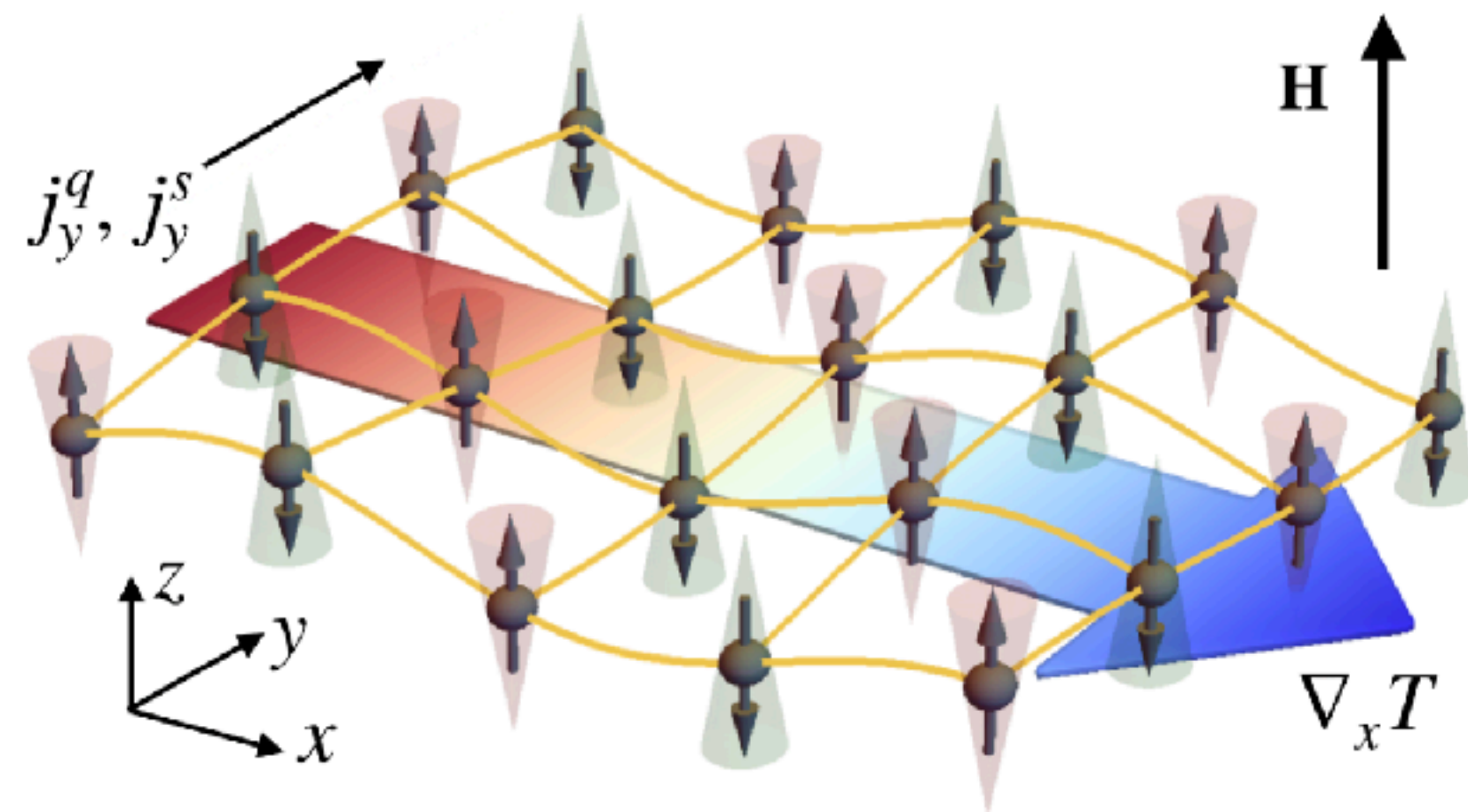


“Collective Dynamics and Quantum Transport” Unit
Contact: shu.zhang@oist.jp

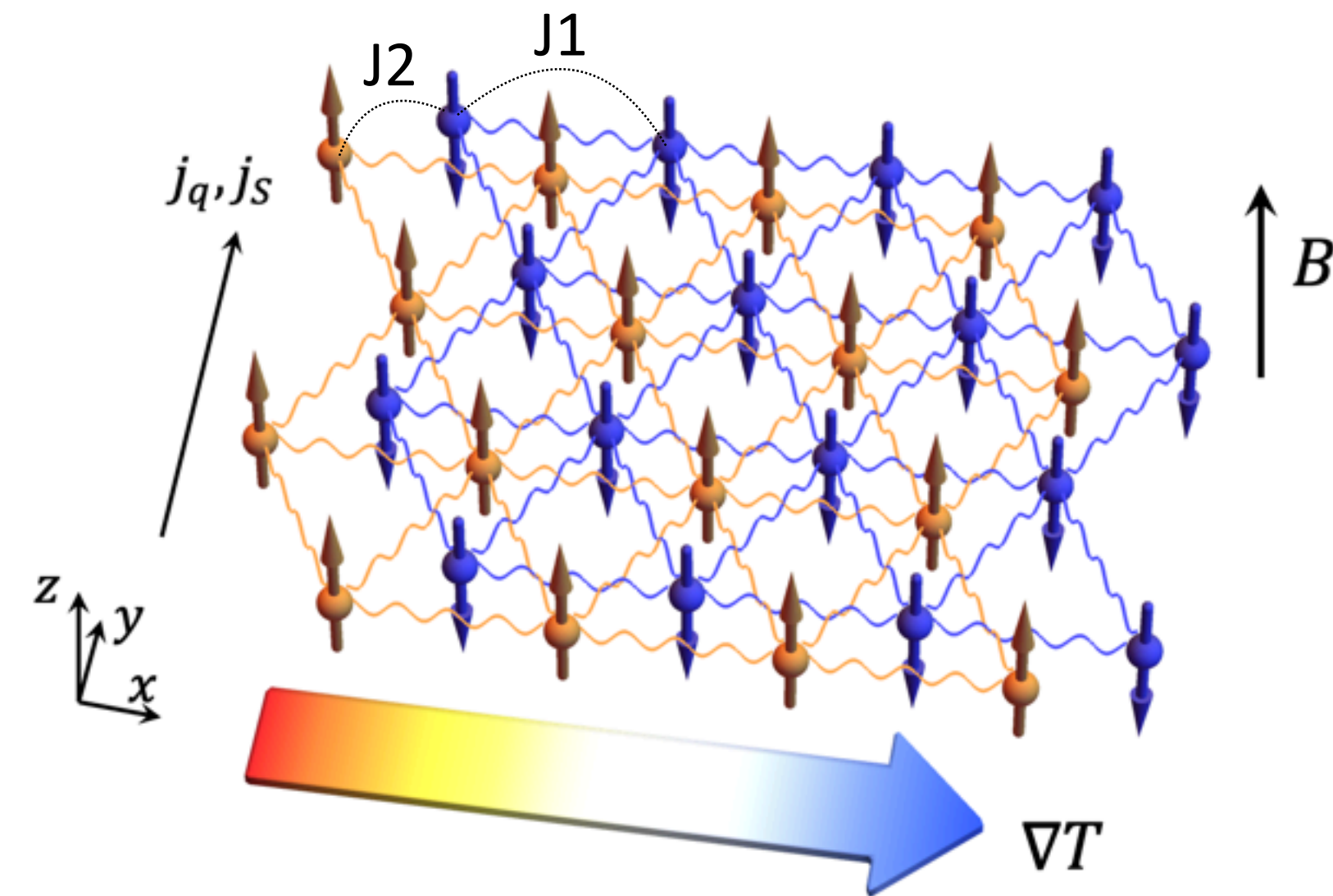
- Quantum matter and quantum transport
- Nonequilibrium dynamics and light-matter couplings
- Open quantum systems and quantum optics

Outline

- Topological magnon-phonon induced by magnetoelastic coupling
- Generically in collinear antiferromagnet: monolayer/bilayer
- Thermal Hall and Spin Nernst effects



SZ, Go, Lee, Kim, *Phys. Rev. Lett.* 124, 147204 (2020)



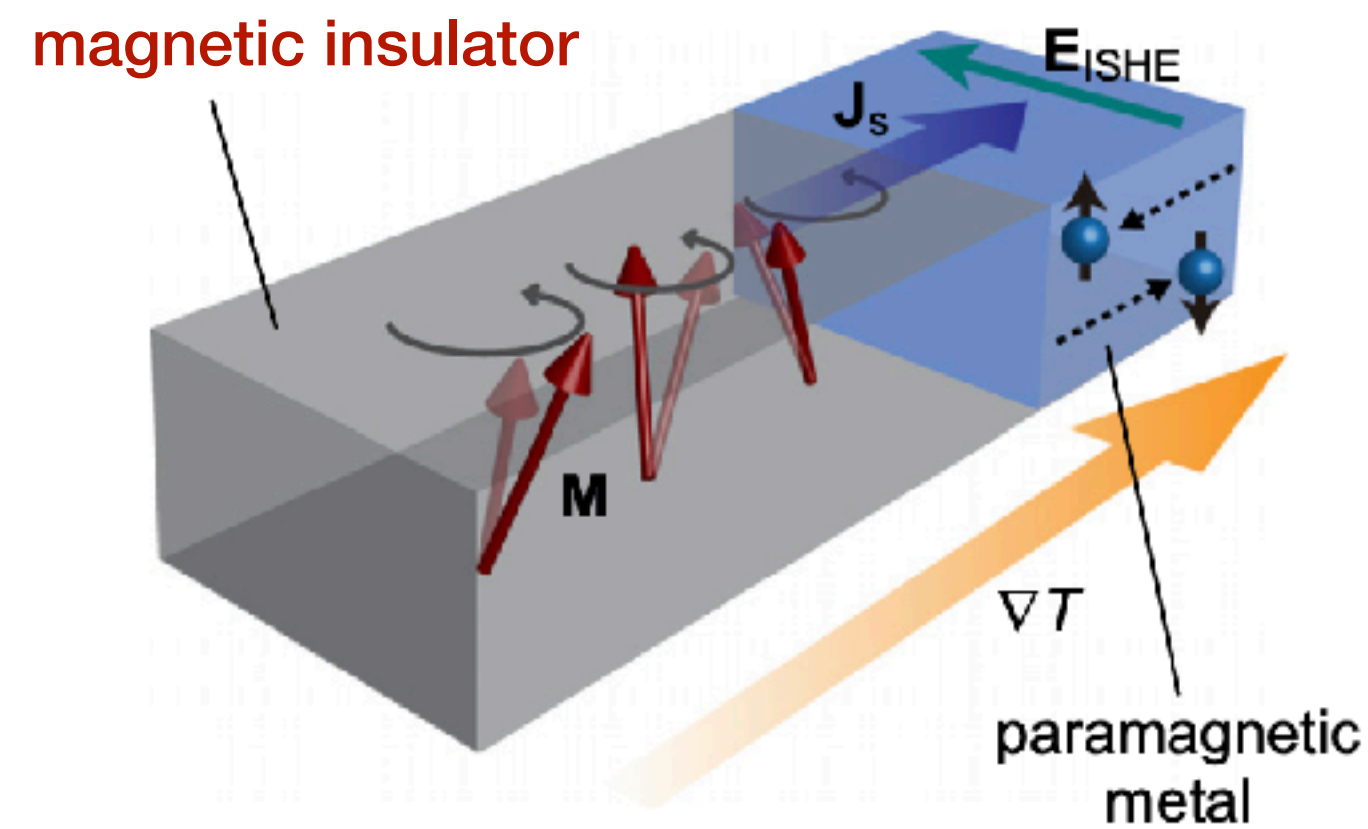
Lin and SZ, *Appl. Phys. Lett.* 124, 132402 (2024)

Spincaloritronics

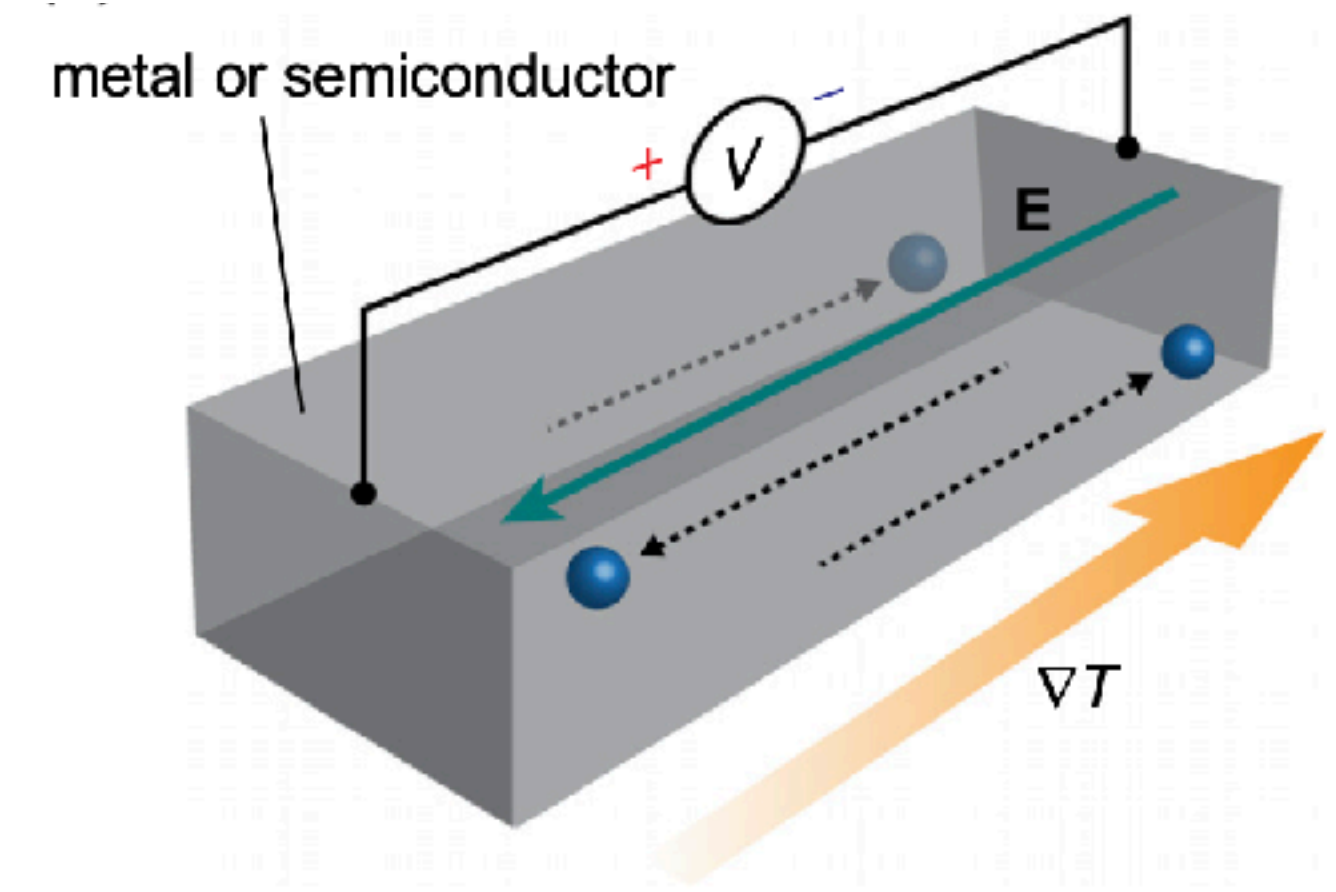
Transport of spin and heat:

- Spintronic thermal devices
- Thermal management
 - Waste heat recycle

Spin Seebeck effect

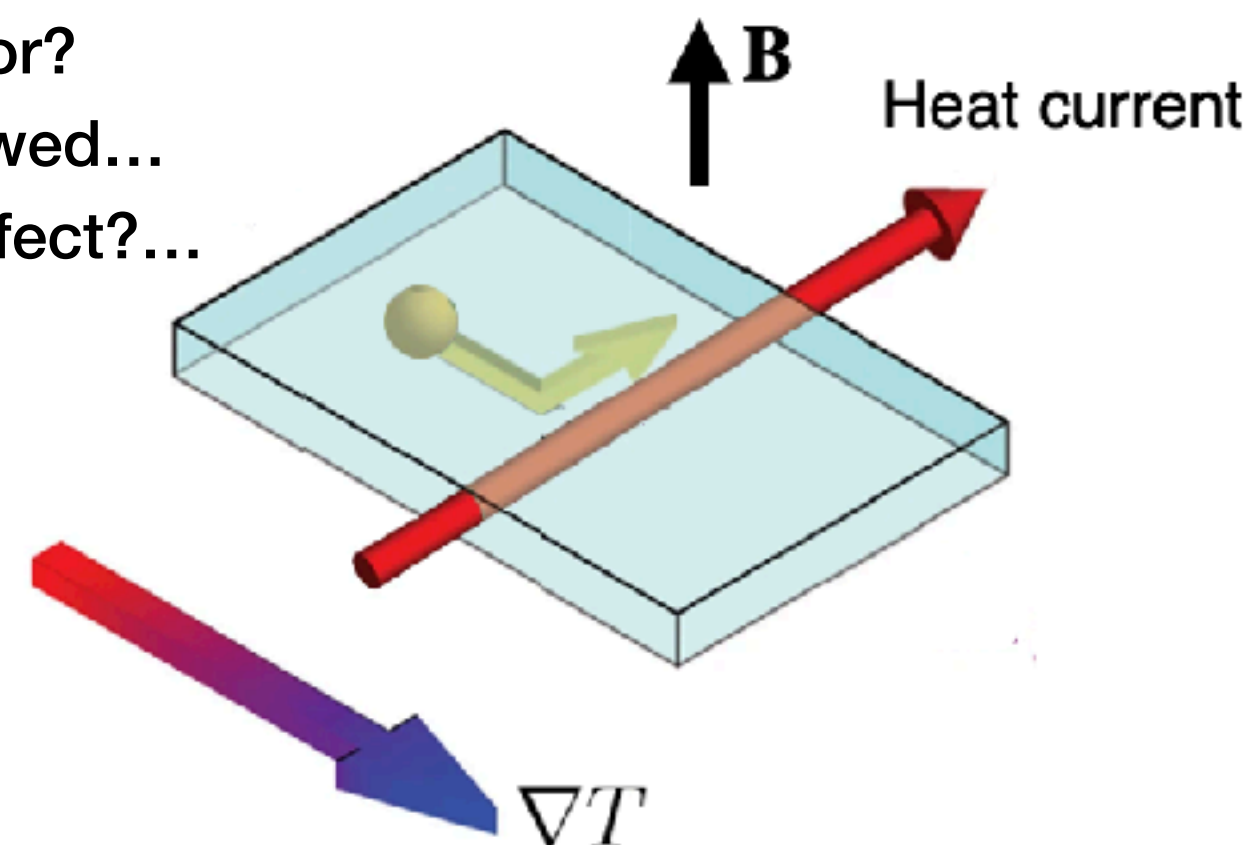


Seebeck effect

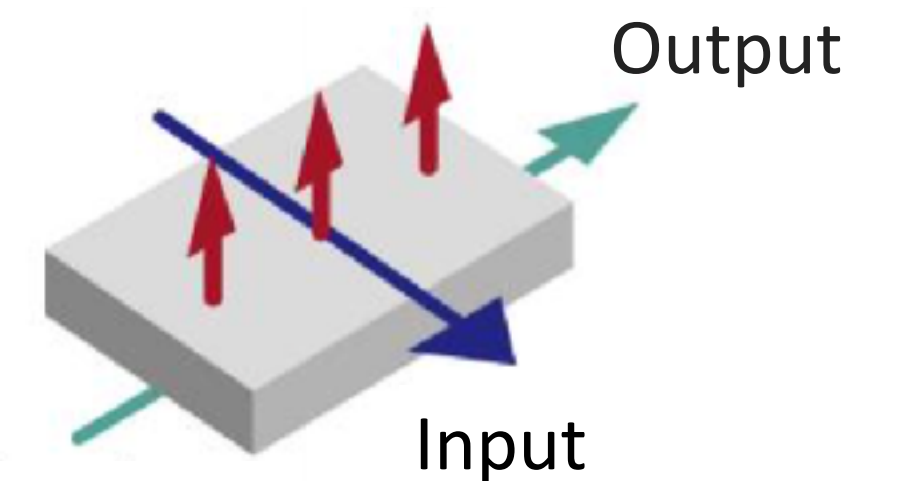
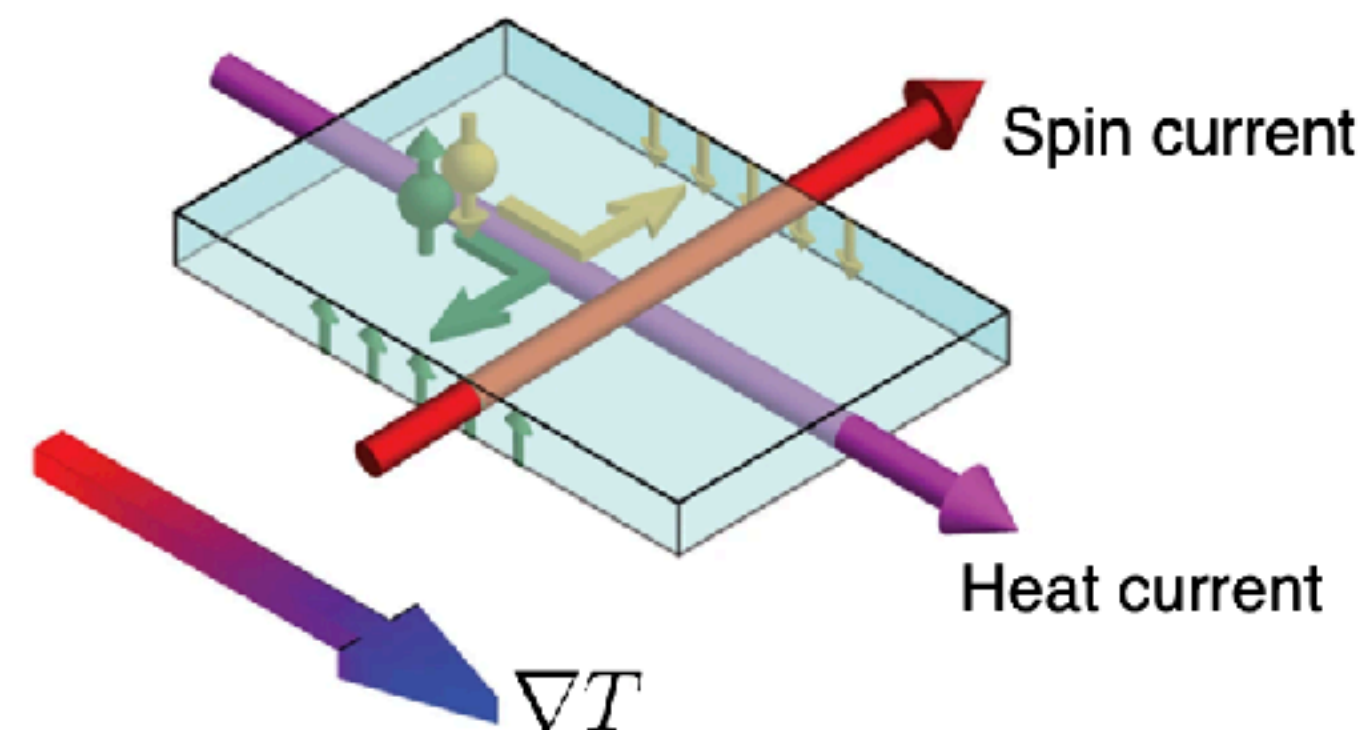


Transverse effects: Thermal Hall effect

In a magnetic insulator?
Yes! If symmetry allowed...
Model? Size of the effect?...



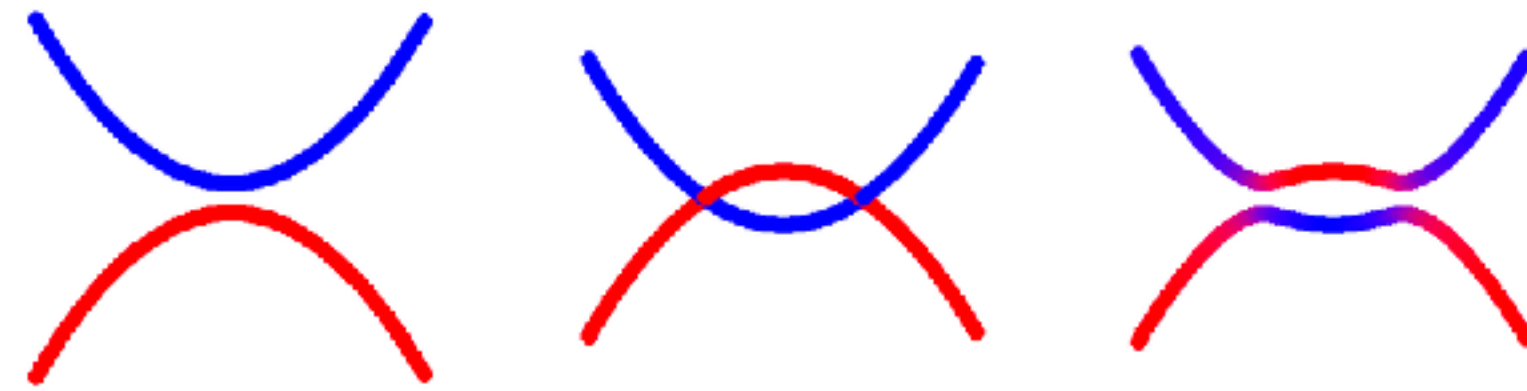
Spin Nernst effect



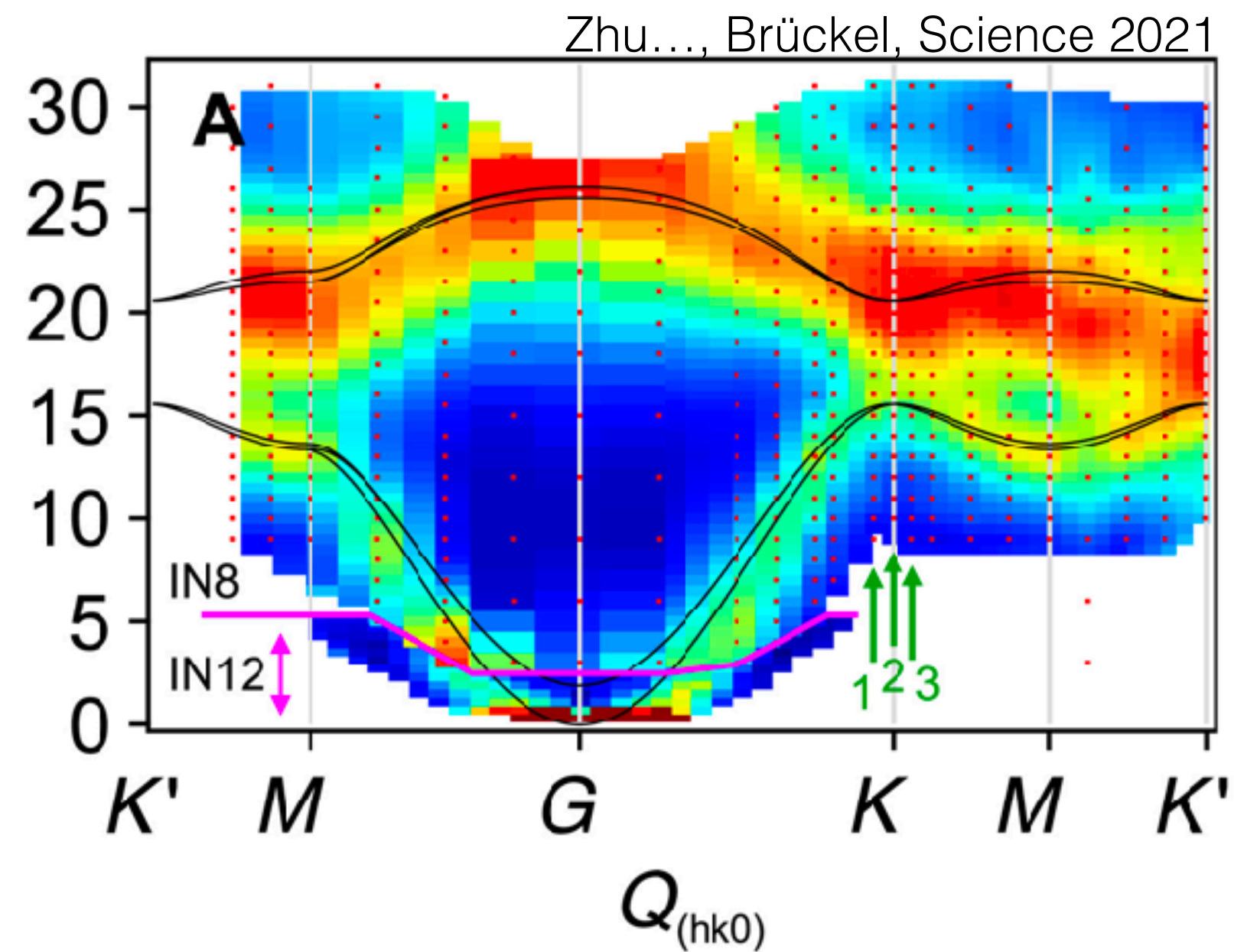
Meyer, ... Goennenwei 2017
Uchida et. al. 2012, 2010, 2021

Topological magnons

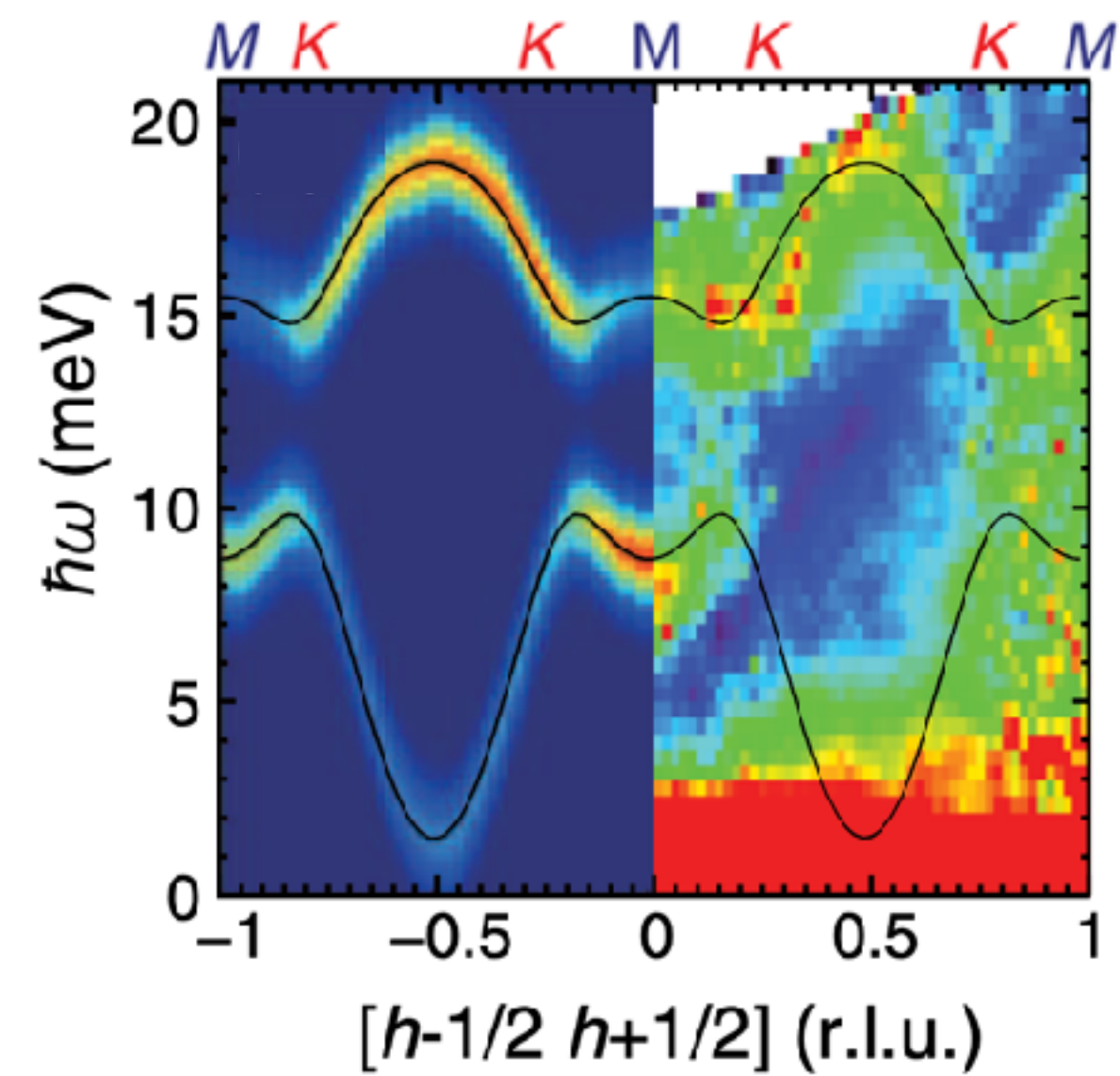
- Band inversion



CrGeTi3



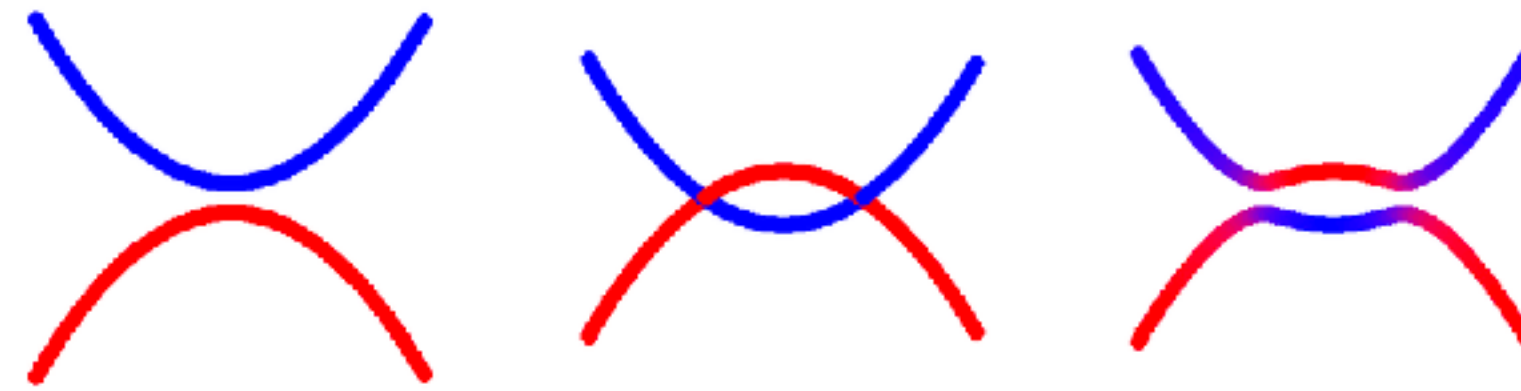
CrI3



Chen, ..., Dai, PRX 2018

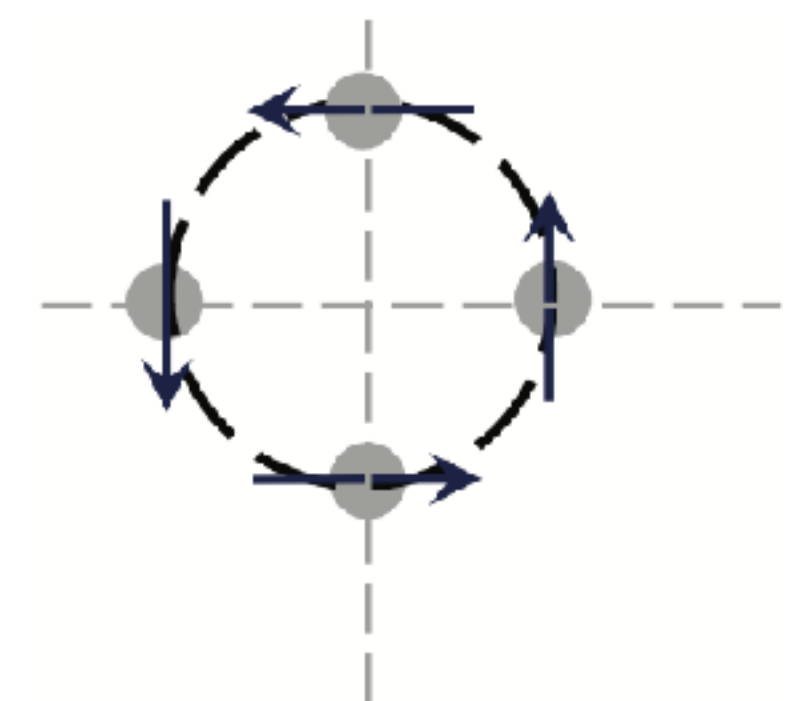
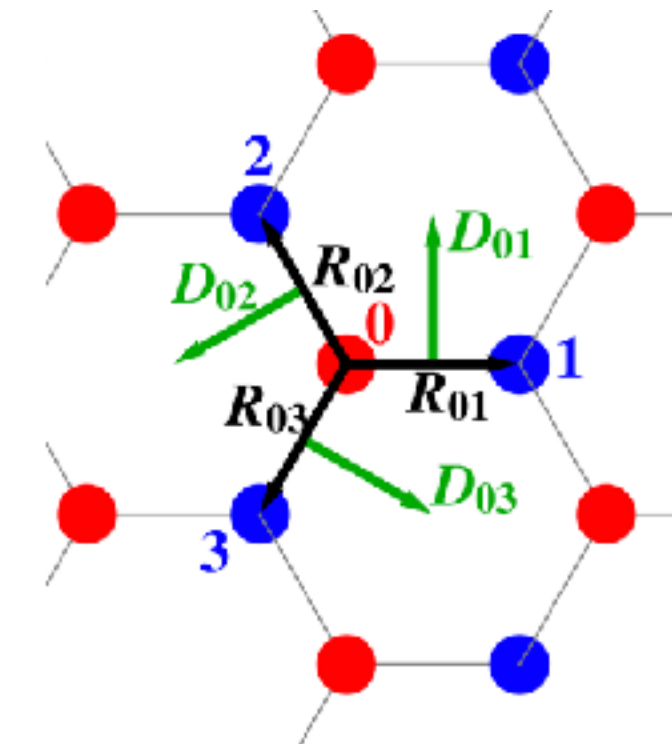
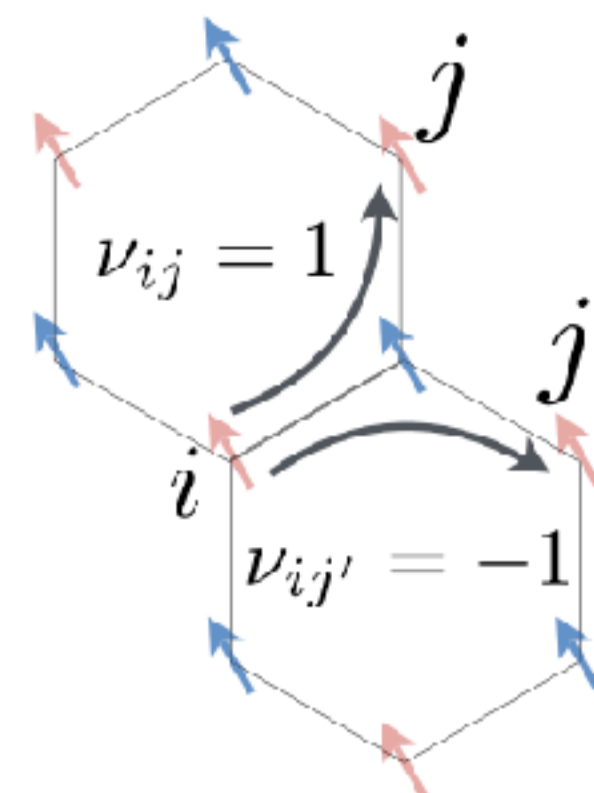
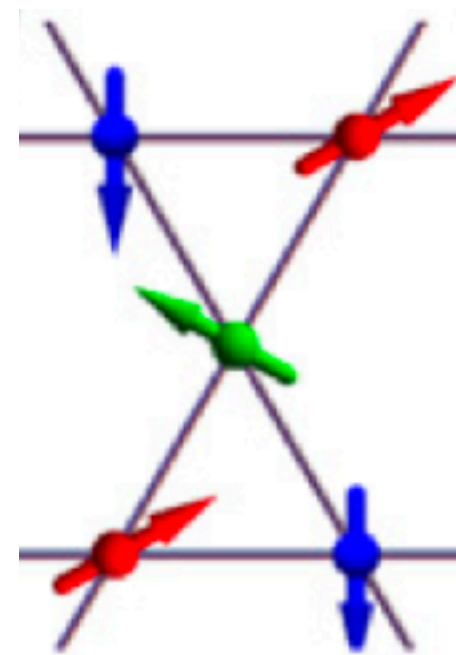
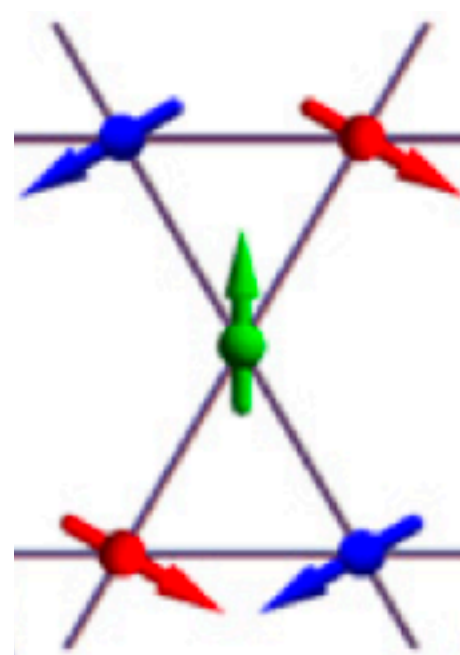
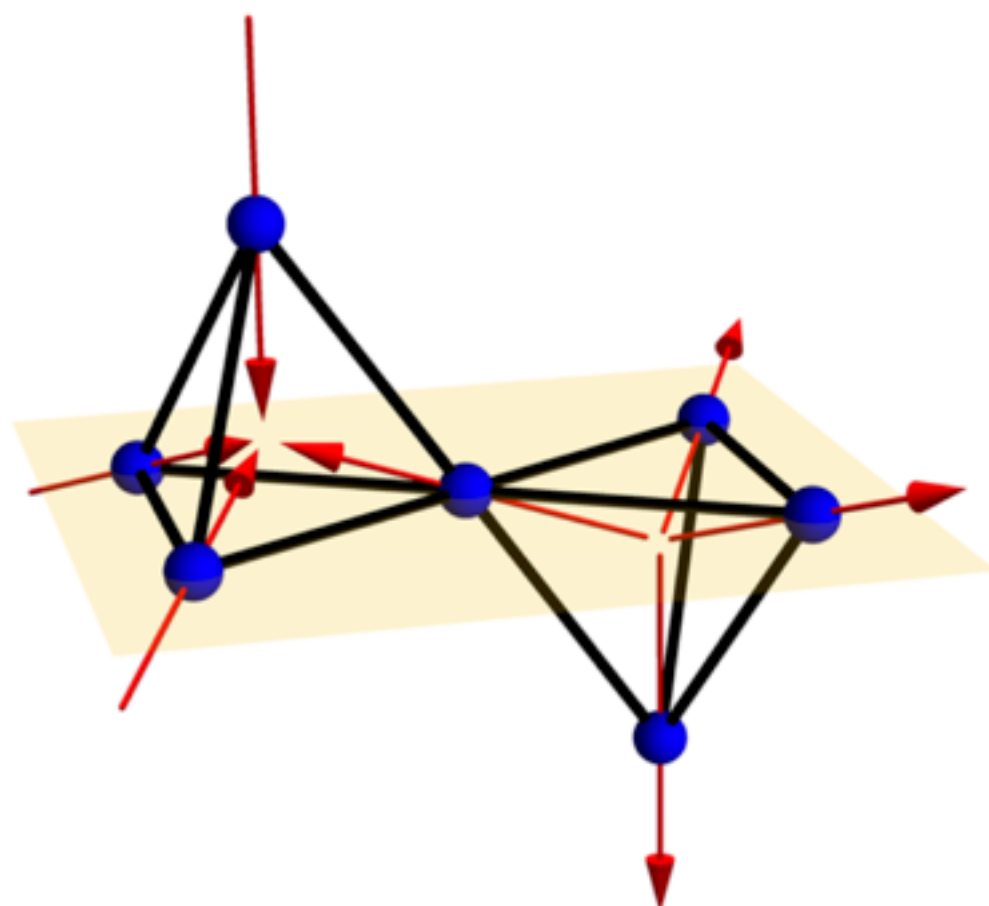
Topological magnons

- Band inversion



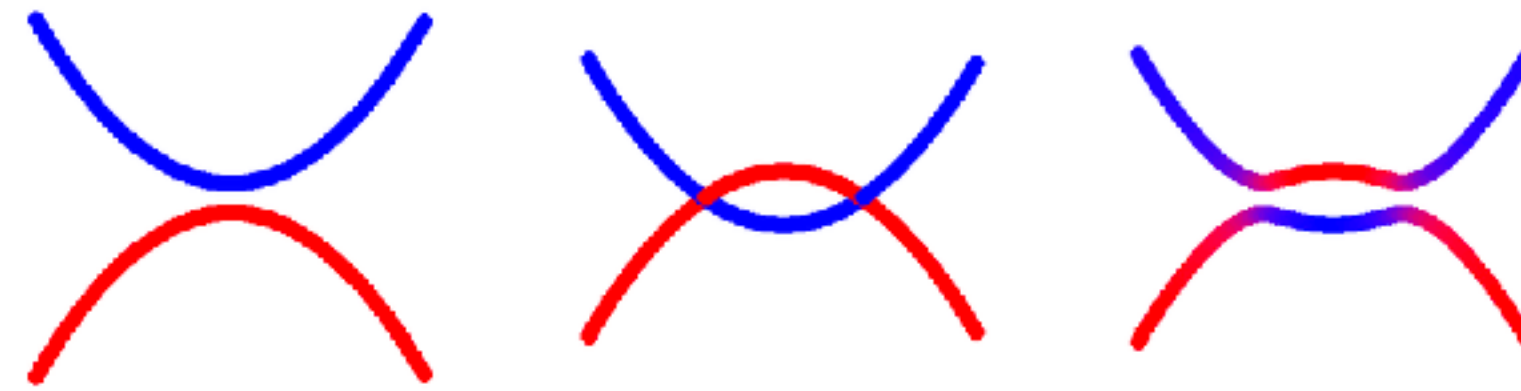
- Chirality Noncoplanar/noncollinear ground states
Inversion-breaking Dzyaloshinskii-Moriya interactions,
Long-range dipolar interactions, ...

Sindou, et. al. 2013, 2014
Mook, Mertig, et. al. 2014, 2016, 2017, 2019
Kim, Ochoa, Zarzuela, Tserkovnyak 2016
Fiete, et. al. 2017, 2018, 2021
Zhang, ..., Xiao 2019; Park, Nagoya, Yang 2020



Topological magnons

- Band inversion



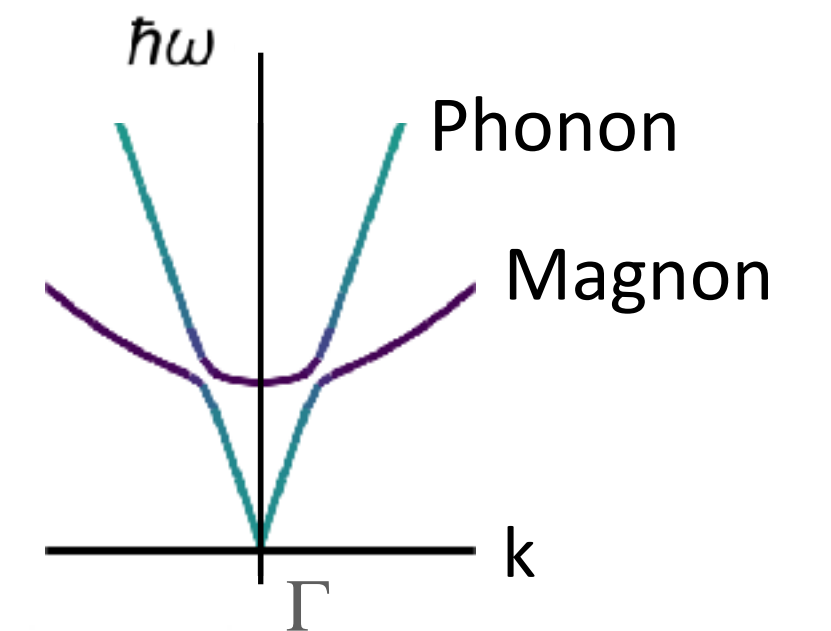
- Chirality

- Transport Thermal Hall effect

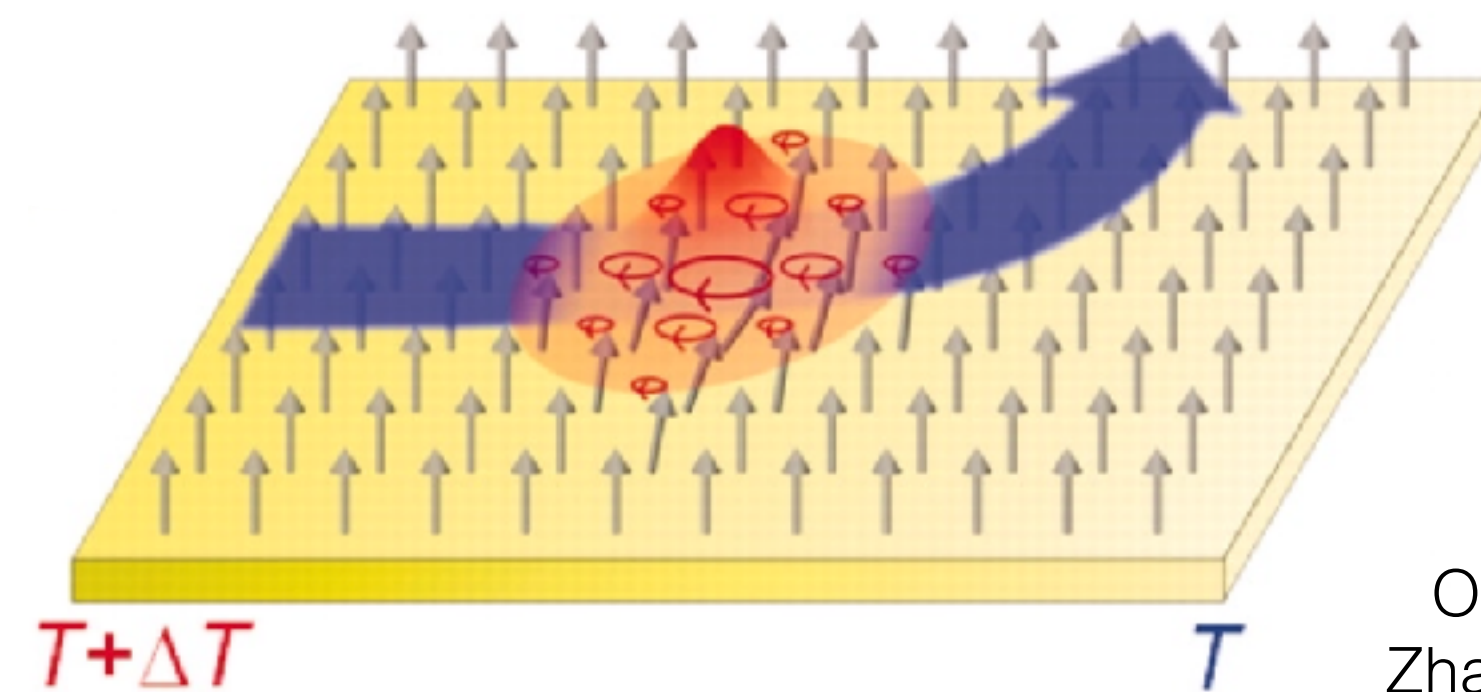
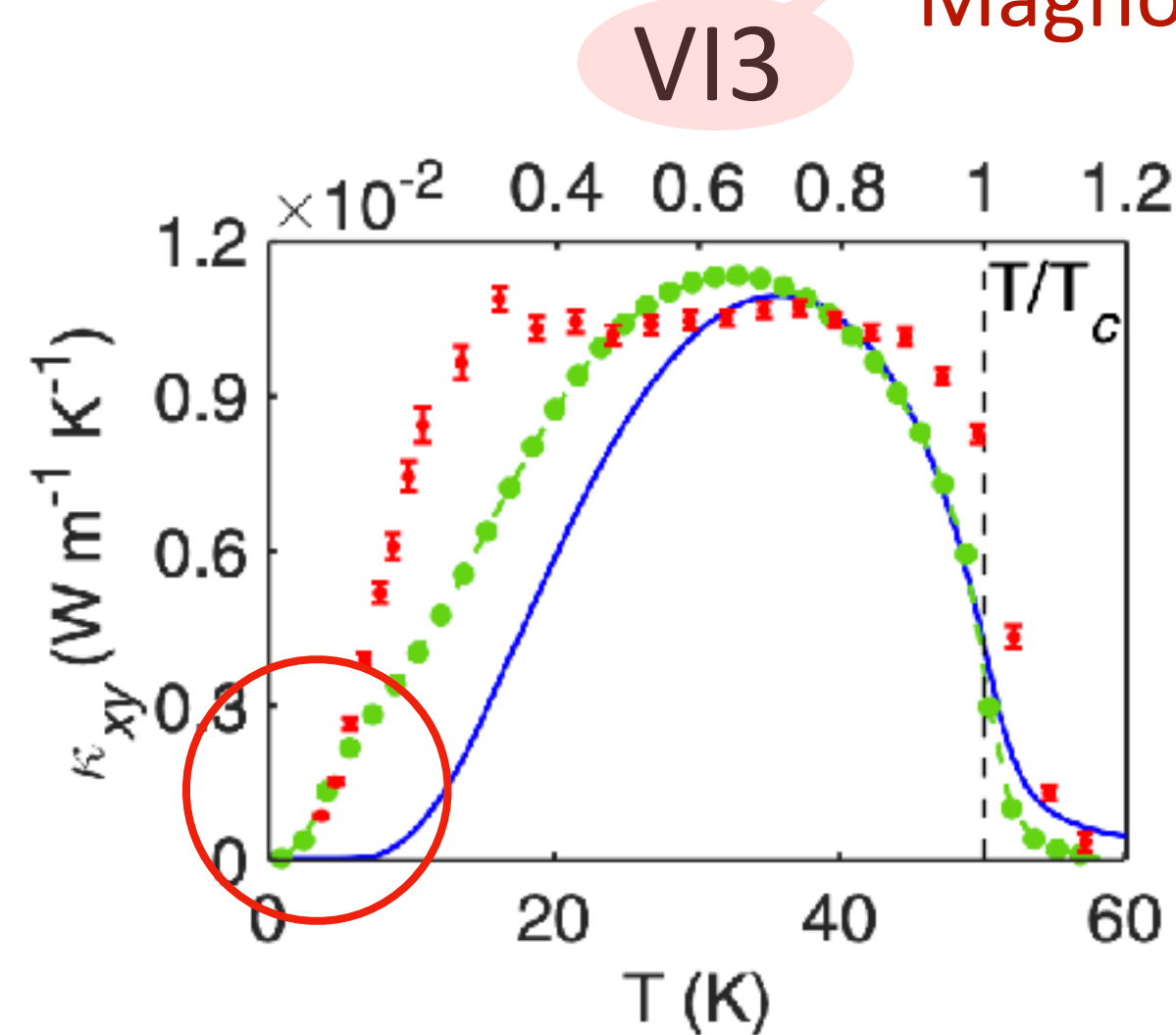
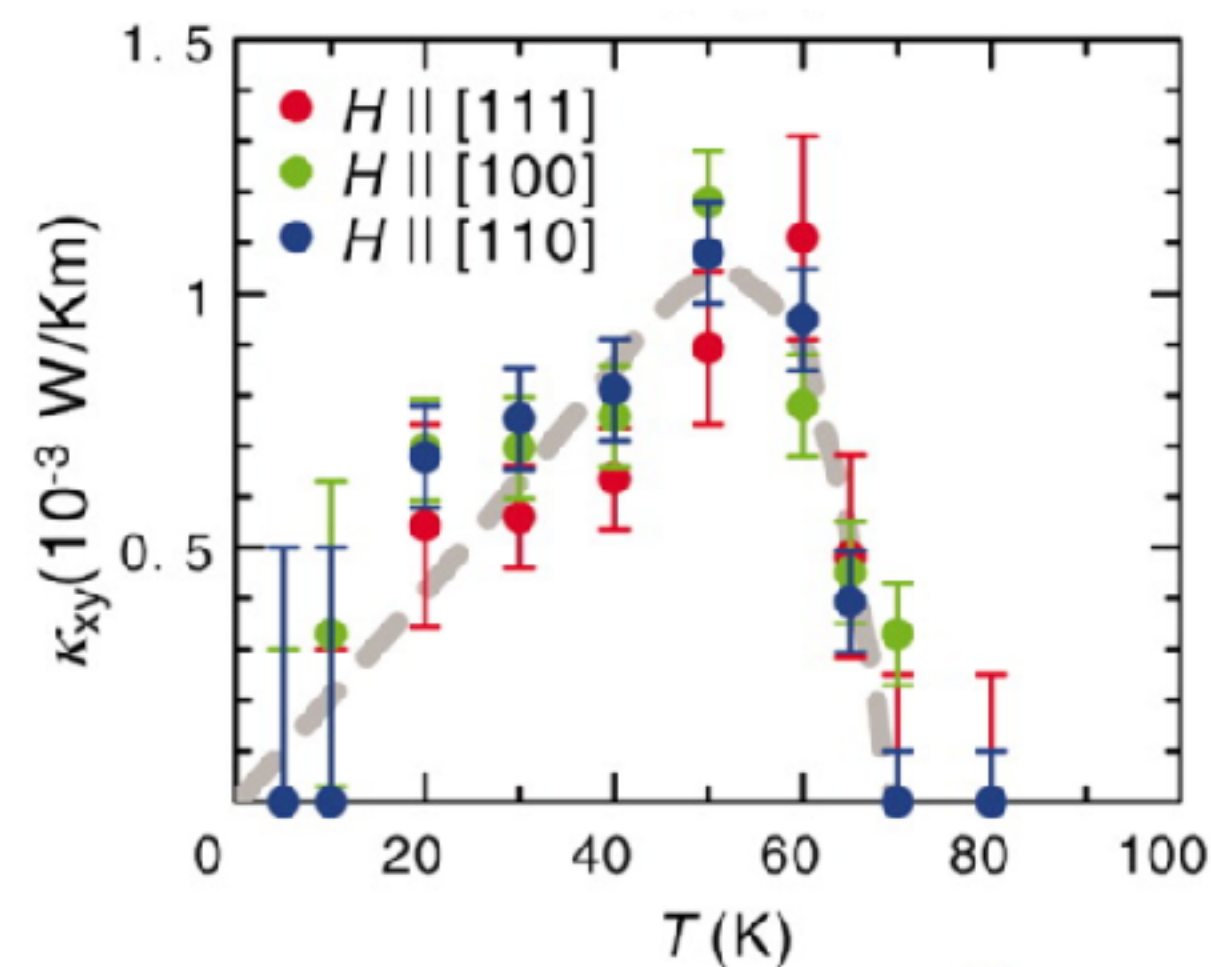
Magnetic ordering temperature $\sim 50\text{K}$

Debye temperature $\sim 140\text{K}$

Magnon-phonon coupling!



Lu₂V₂O₇



Onose, ..., Tokura 2010
Zhang, ..., Xiao, Ke 2021
Kong, ... Cava 2019

Magnetoelastic coupling

$$\kappa \sum_{\ell, \delta} S_{\ell}^z (\mathbf{S}_{\ell} \cdot \hat{\mathbf{e}}_{\delta}) (u_{\ell}^z - u_{\ell+\delta}^z)$$

Bond direction Displacement

- **Symmetry!** Kittel 1949, 1958

Magnon-Phonon Interaction

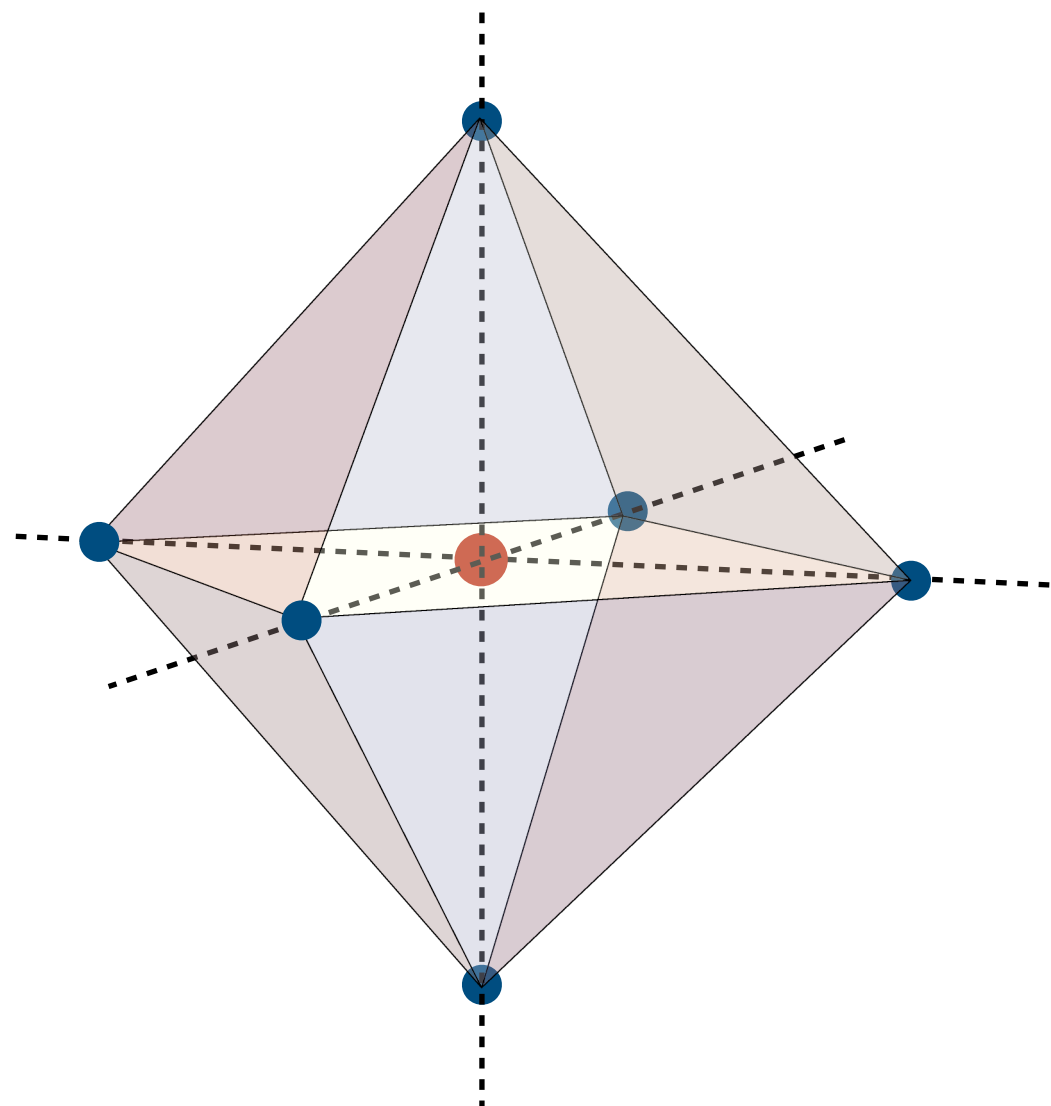
The interaction between magnetization direction and elastic strain (as observed as magnetostriction) is described by the magnetoelastic coupling.⁵ To the first order in the strain components S_{ij} and to the second order in the direction cosines, the coupling in a *cubic* crystal is described by the magnetoelastic energy density

$$f_{\text{me}} = b_1 (\alpha_x^2 S_{xx} + \alpha_y^2 S_{yy} + \alpha_z^2 S_{zz}) + 2b_2 (\alpha_x \alpha_y S_{xy} + \alpha_y \alpha_z S_{yz} + \alpha_z \alpha_x S_{zx}). \quad (20)$$

Spin Strain

$$S_{yz} \equiv \frac{1}{2} \left(\frac{\partial R_y}{\partial z} + \frac{\partial R_z}{\partial y} \right); \quad S_{zx} \equiv \frac{1}{2} \left(\frac{\partial R_z}{\partial x} + \frac{\partial R_x}{\partial z} \right).$$

Magnetocrystalline anisotropy



Magnetoelastic coupling

$$\kappa \sum_{\ell, \delta} S_{\ell}^z (\mathbf{S}_{\ell} \cdot \hat{\mathbf{e}}_{\delta}) (u_{\ell}^z - u_{\ell+\delta}^z)$$

Bond direction Displacement

Generally applicable

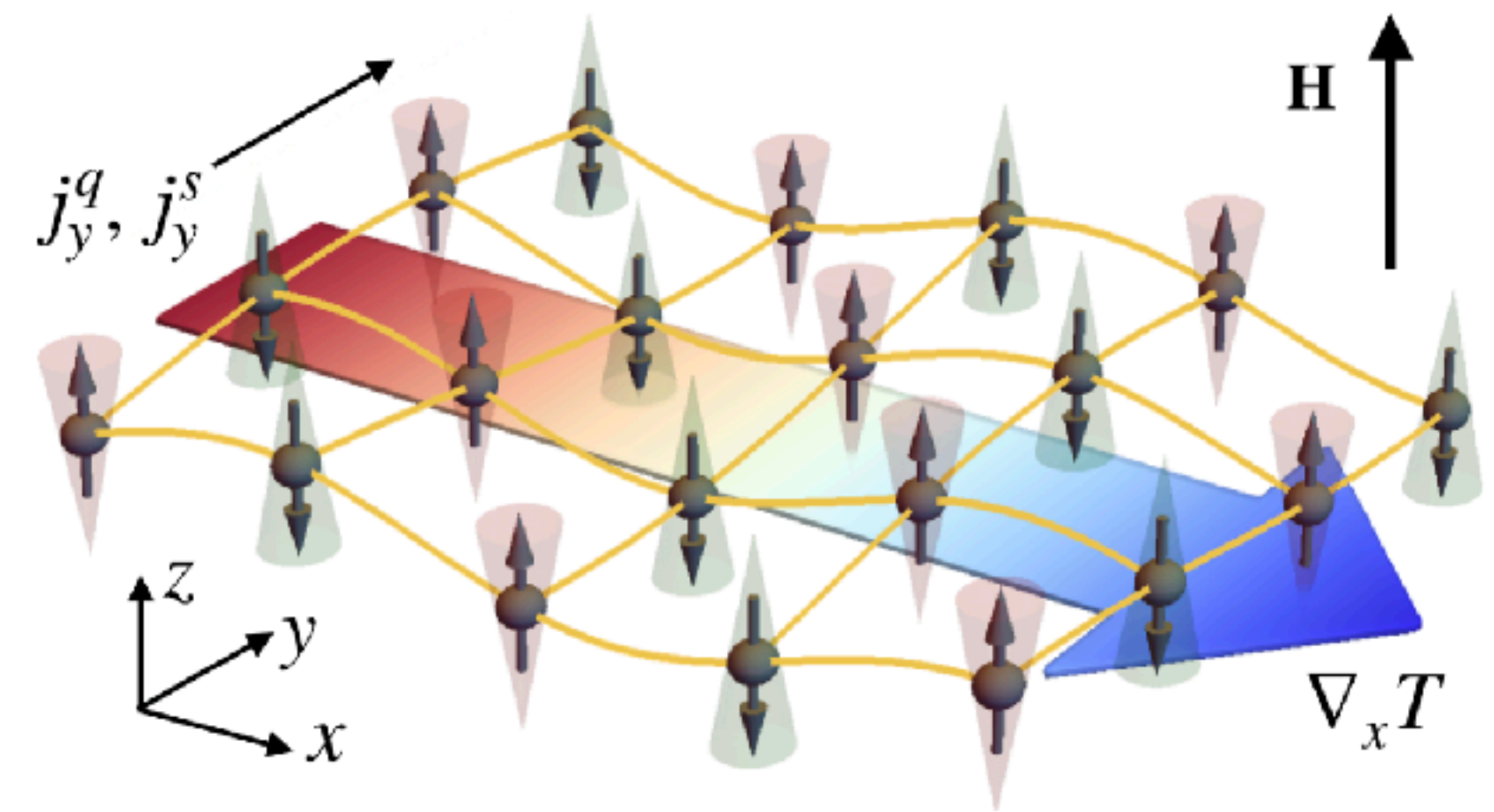
First order in both magnon and phonon fluctuations

Kittel 1949, 1958

Thingstad, Kamra, Brataas, Sudbø PRL 2019

Go, Kim, Lee PRL 2019

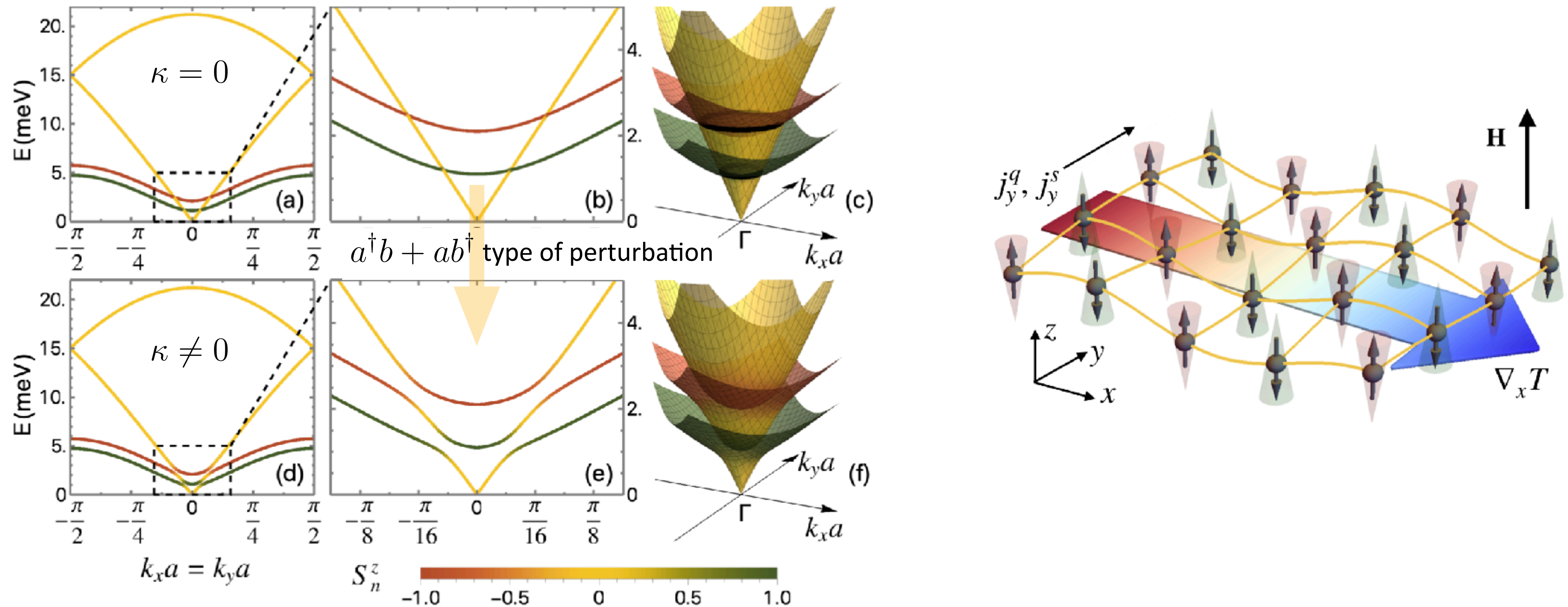
SZ, Go, Lee, Kim PRL 2020: **A 2D collinear antiferromagnet**



Topological magnon-phonon hybridization

A 2D collinear antiferromagnet (Heisenberg interaction + Easy-axis anisotropy)

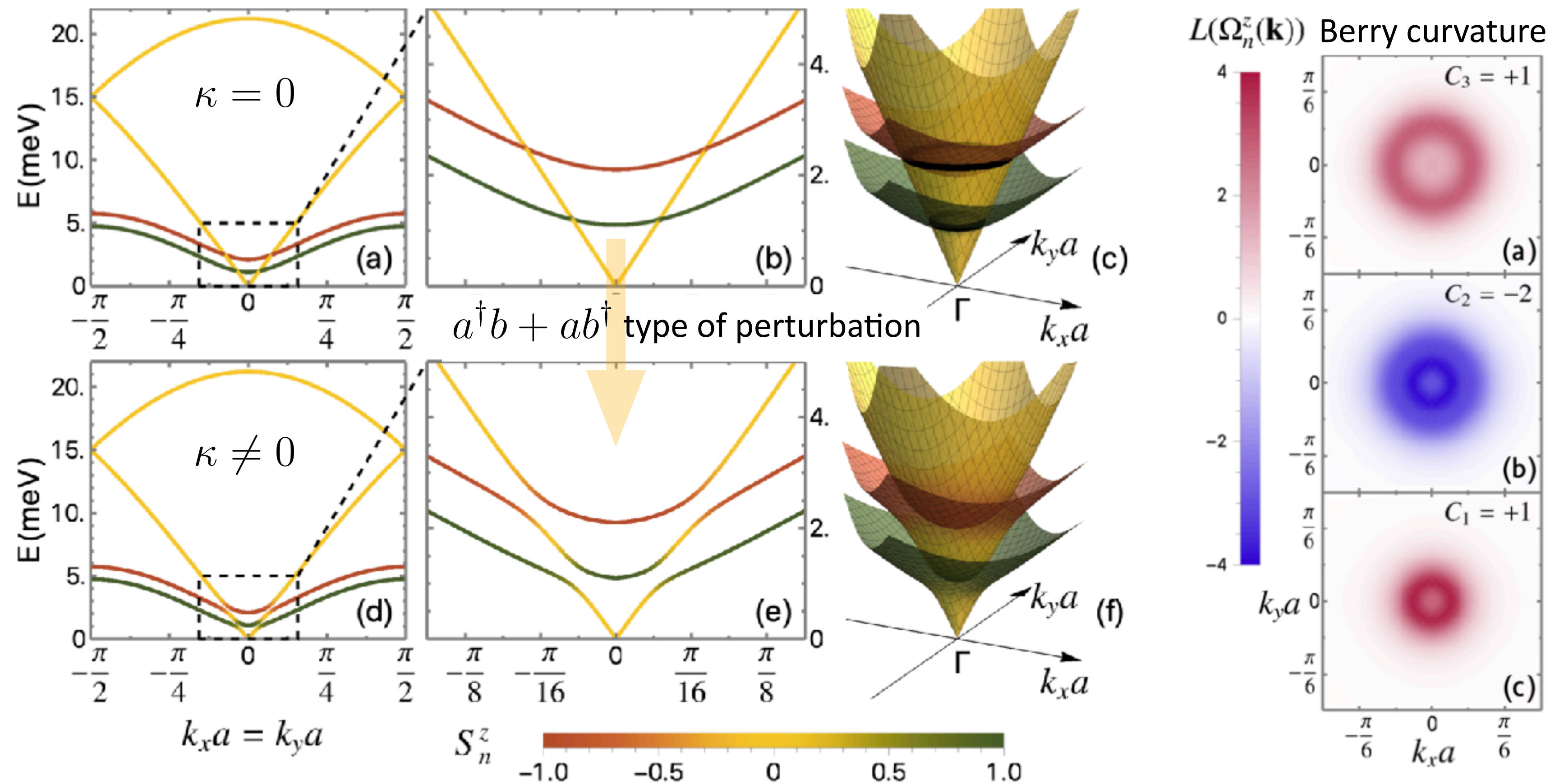
SZ, Go, Lee, Kim Phys. Rev. Lett. 124, 147204 (2020)



Topological magnon-phonon hybridization

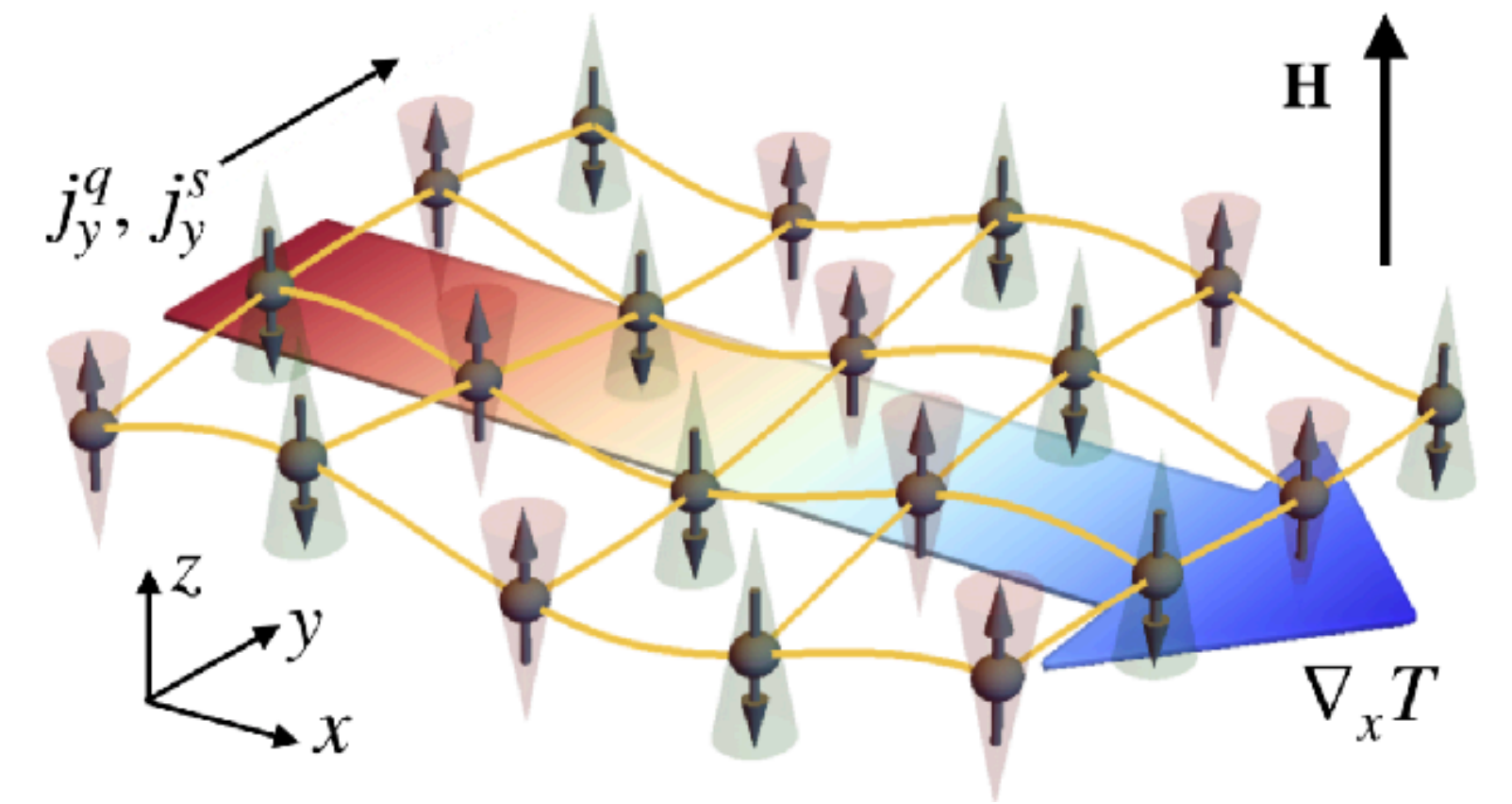
A 2D collinear antiferromagnet (Heisenberg interaction + Easy-axis anisotropy)

SZ, Go, Lee, Kim Phys. Rev. Lett. 124, 147204 (2020)



In the long-wavelength limit...

Magnetoelastic coupling $H_{\text{me}} = \kappa \sum_{\ell, \delta} S_{\ell}^z (\mathbf{S}_{\ell} \cdot \hat{\mathbf{e}}_{\delta}) (u_{\ell}^z - u_{\ell+\delta}^z)$



Form of a spin-orbit coupling $\rightarrow -\frac{2\kappa S^2}{a} \mathbf{n} \cdot \nabla u^z$

Staggered magnetization (pointing to $\mathbf{n}$)

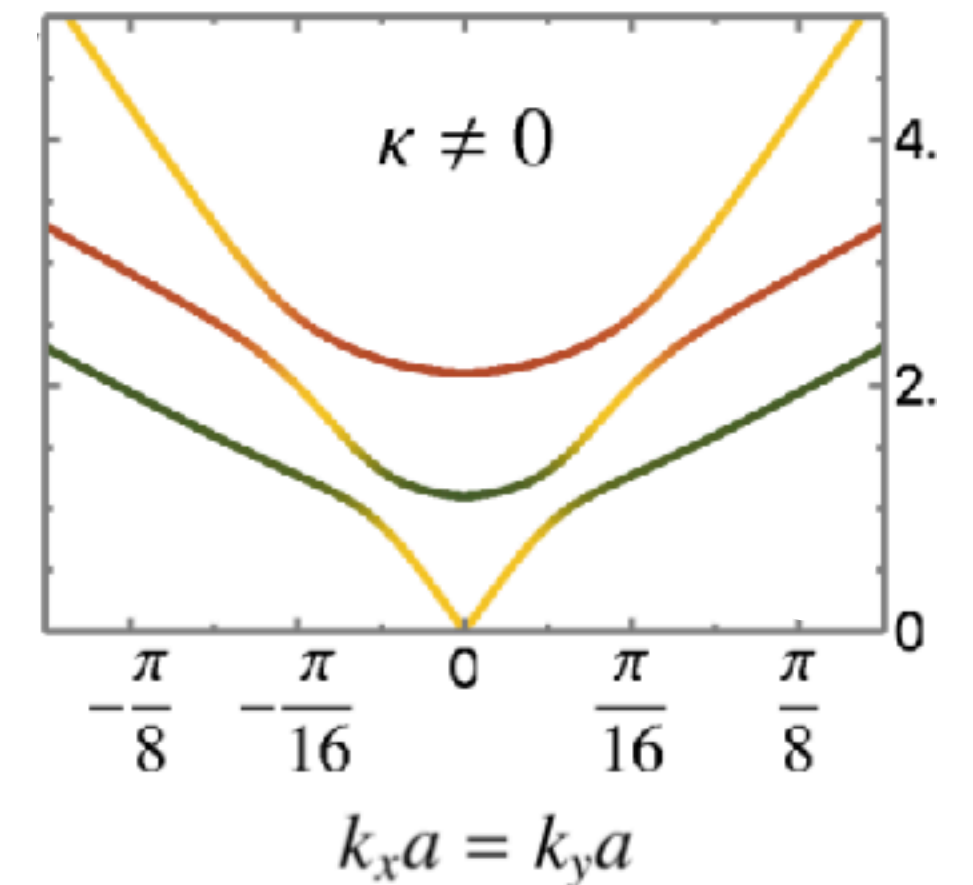
Lattice constant (pointing to a)

Continuum model **Insensitive to lattice details**

3-component field

$$\mathcal{S}[\Psi] \approx \frac{1}{2} \int d^2 \mathbf{k} \int d\omega \Psi_{\mathbf{k}, \omega}^{\dagger} (\hbar\omega - \mathcal{G}_{\mathbf{k}, \omega}) \Psi_{\mathbf{k}, \omega}$$

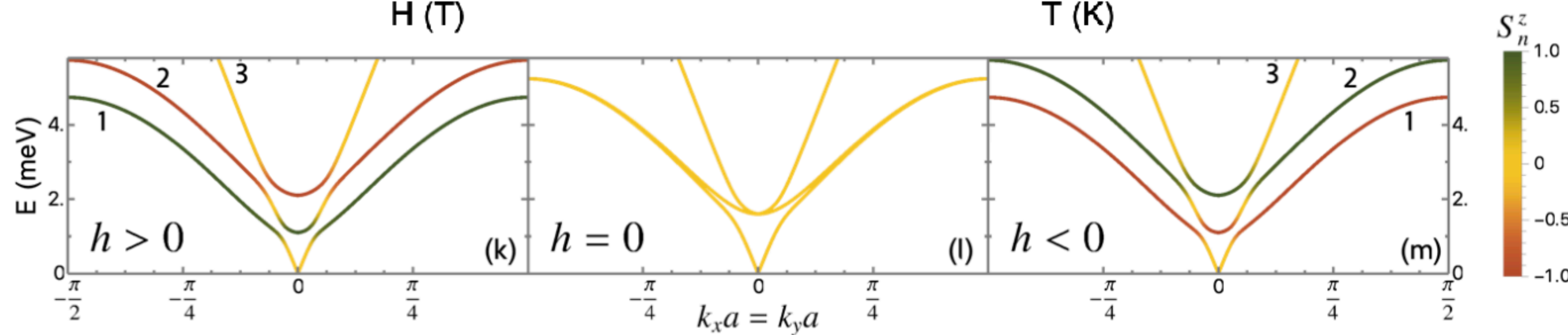
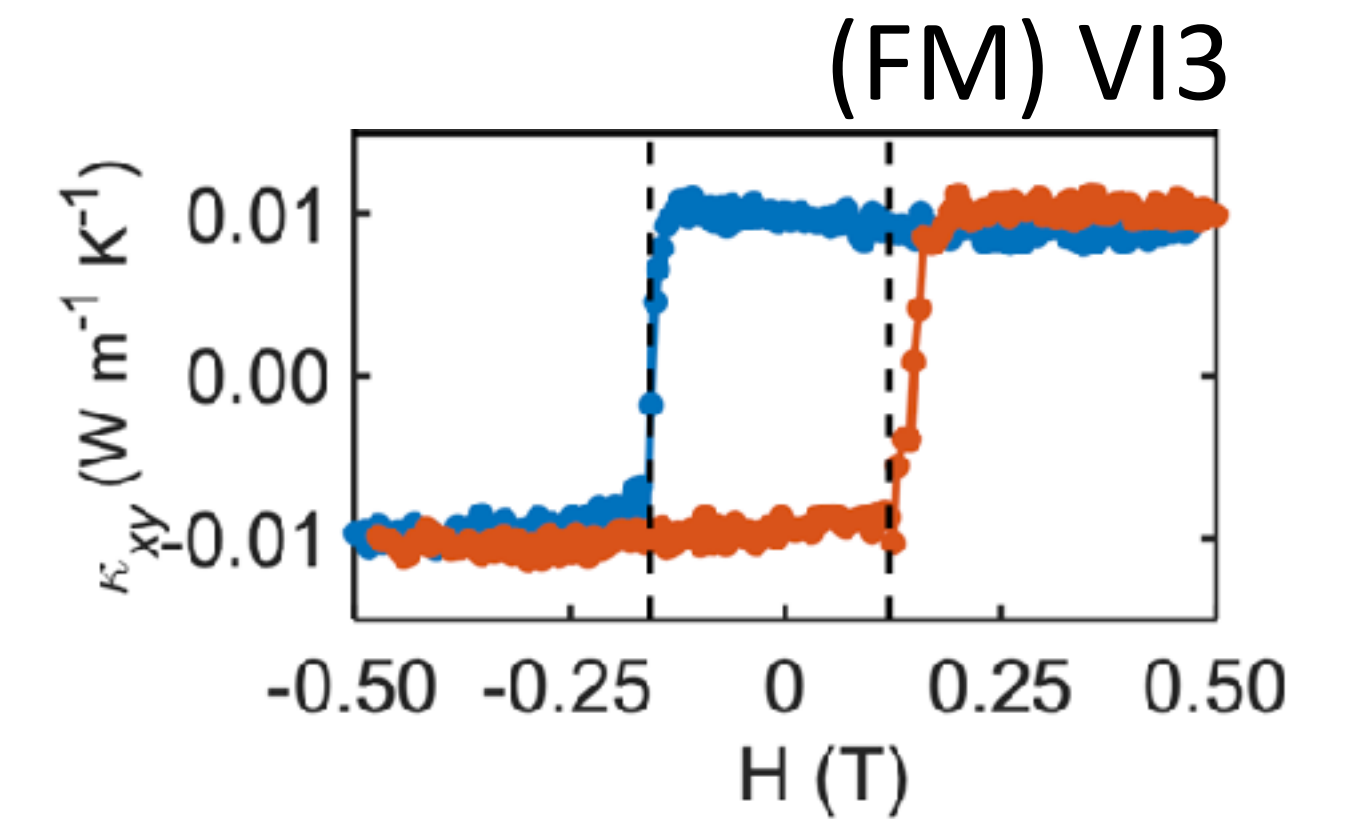
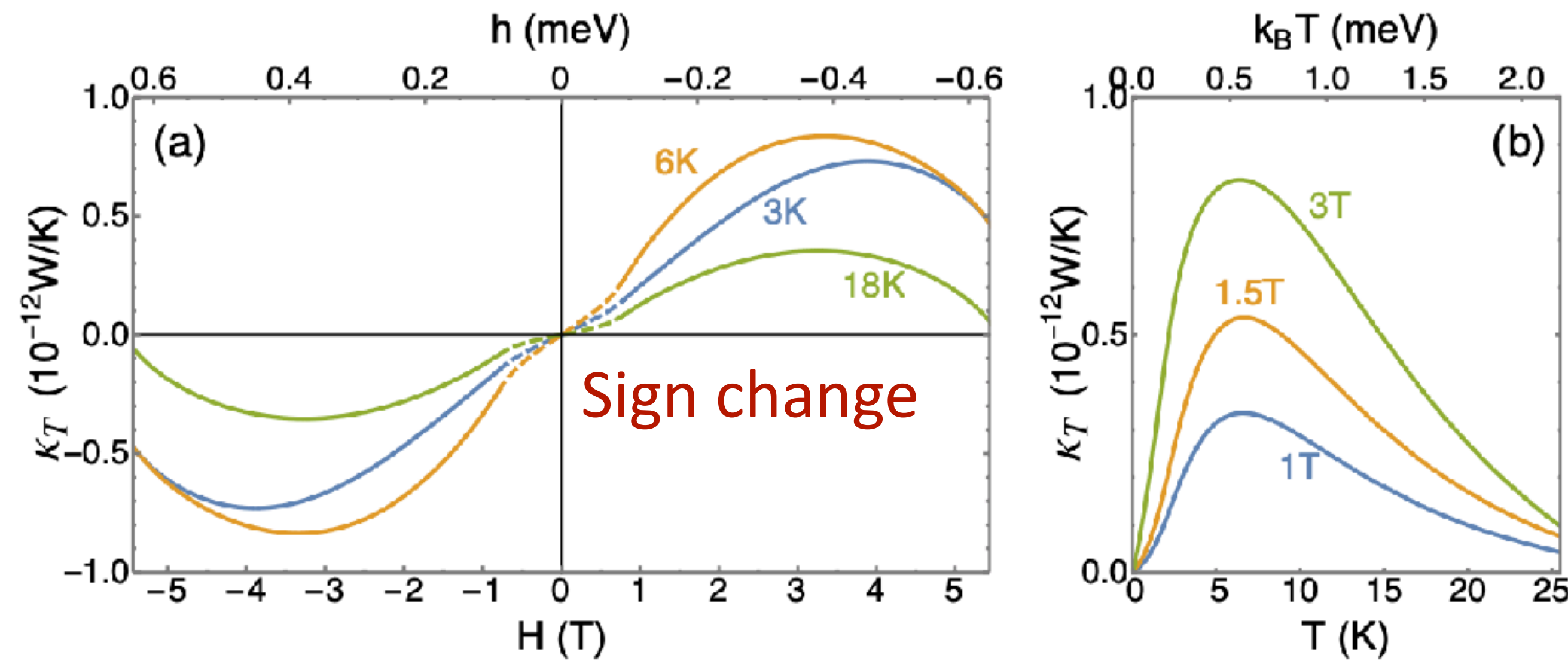
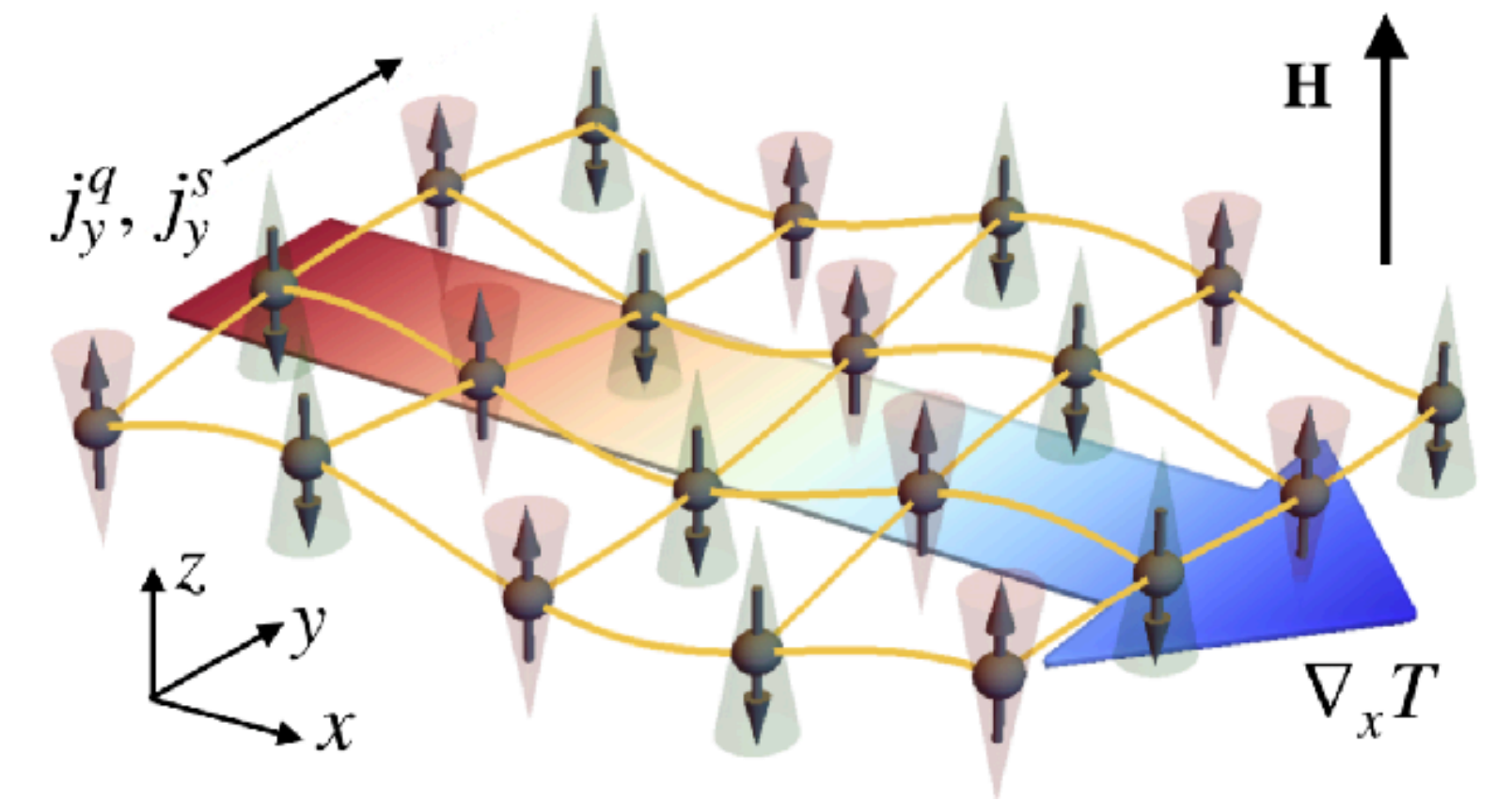
Inverse of Green's function containing the topological structure (pointing to $\mathcal{G}_{\mathbf{k}, \omega}$)



SZ, Go, Lee, Kim 2020

Thermal Hall effect

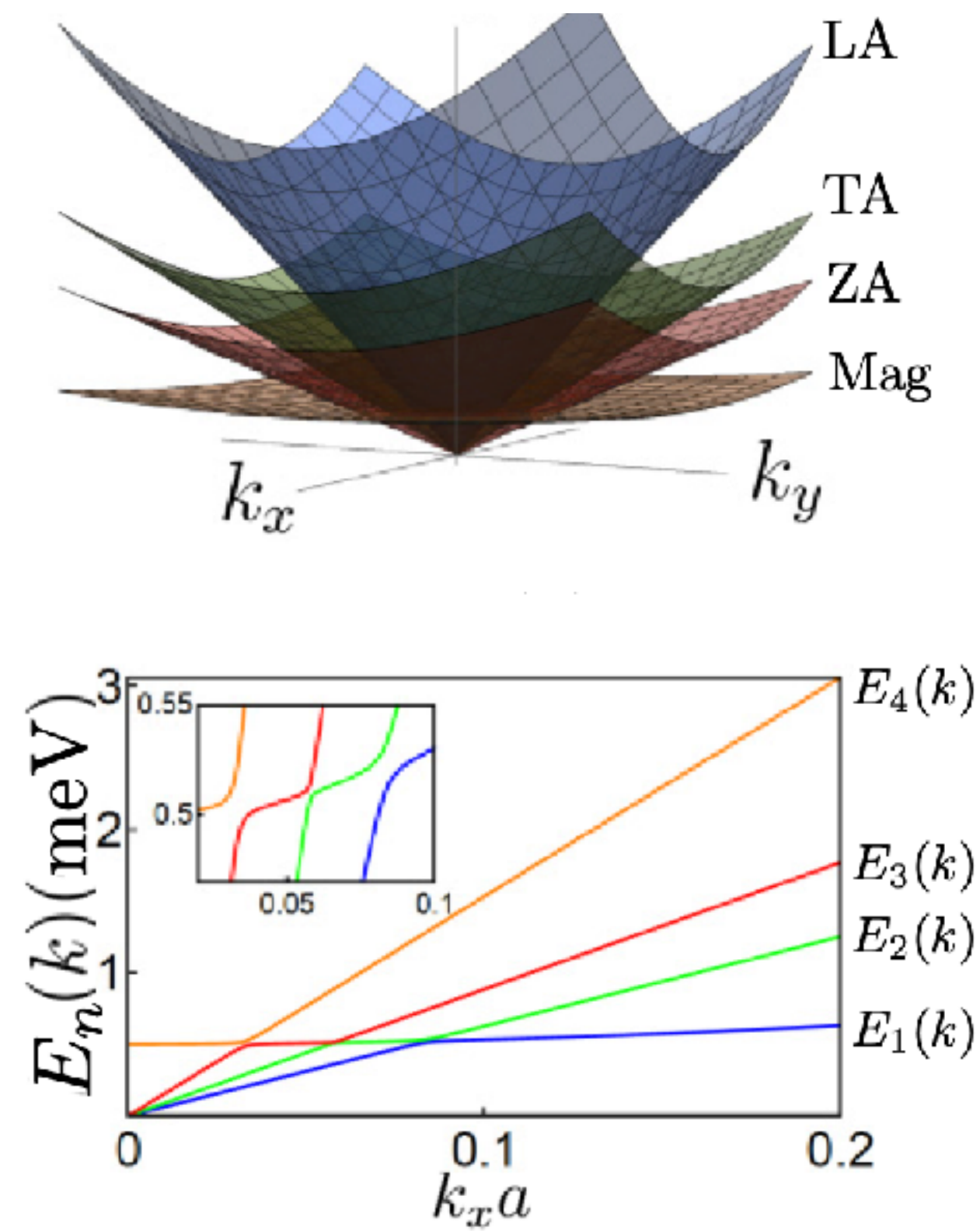
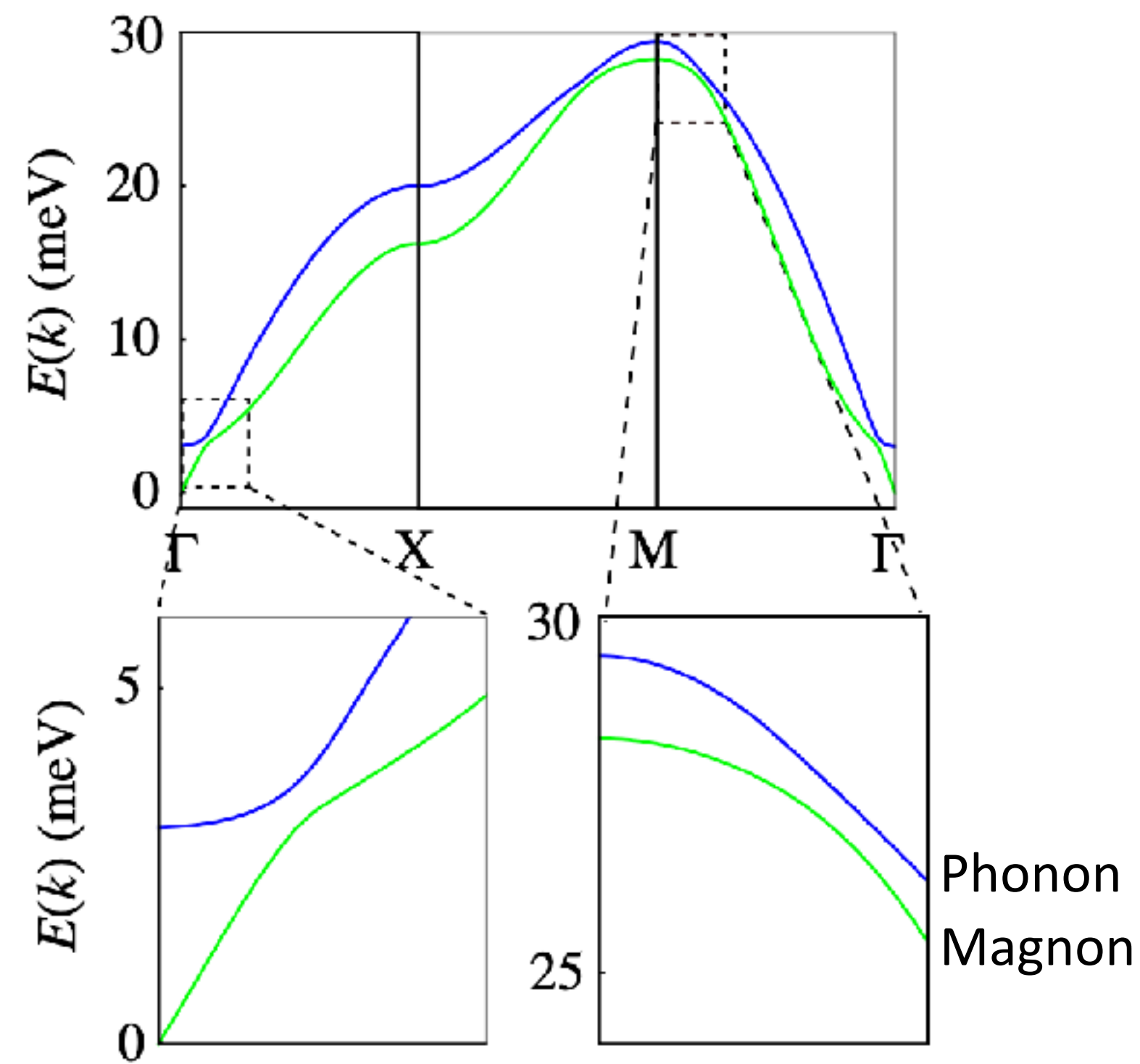
Predictions for MnPS3



Zhang, ..., Xiao, Ke 2021
SZ, Go, Lee, Kim 2020

Tunability

Magnon band is generally tunable by magnetic field



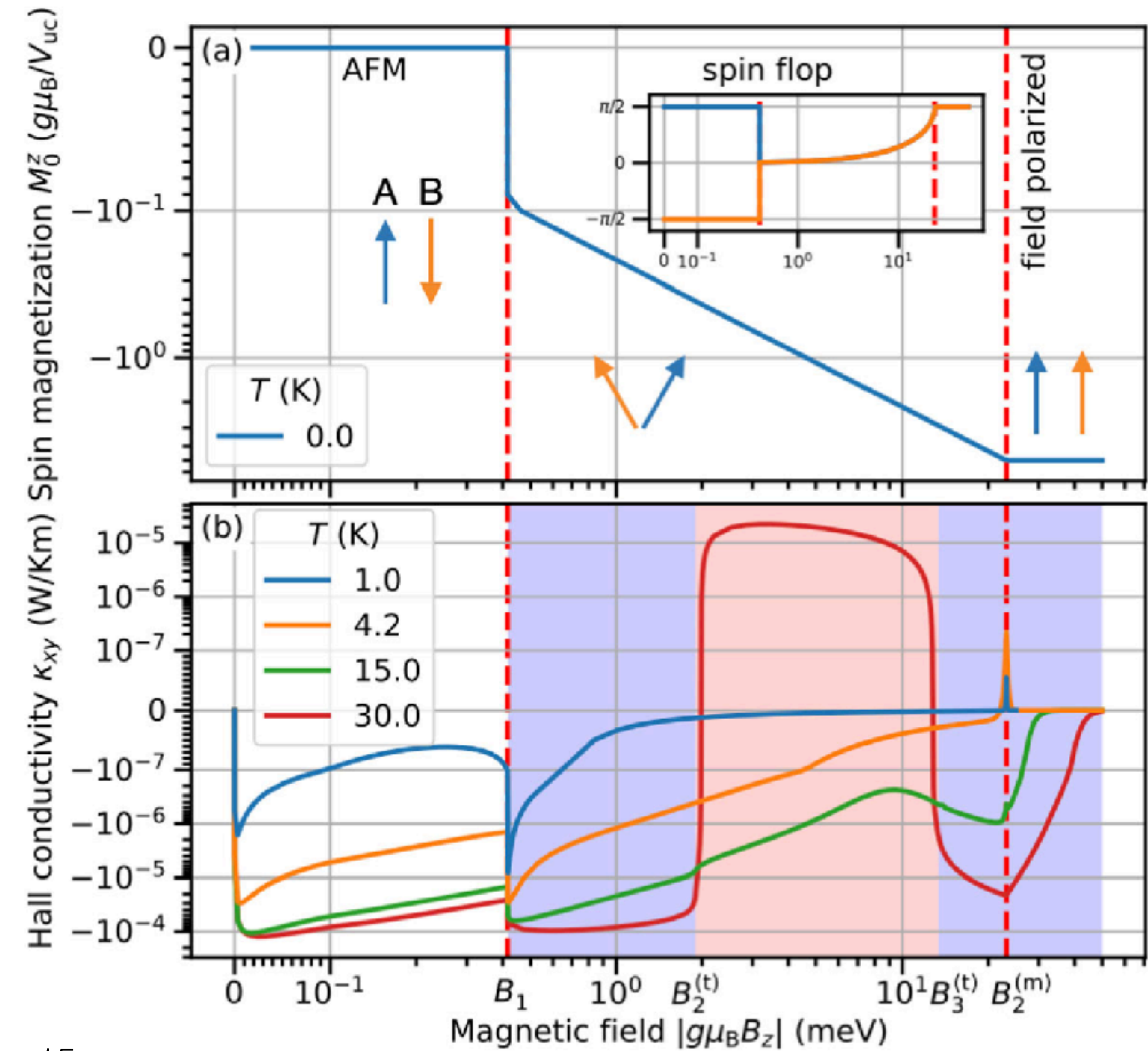
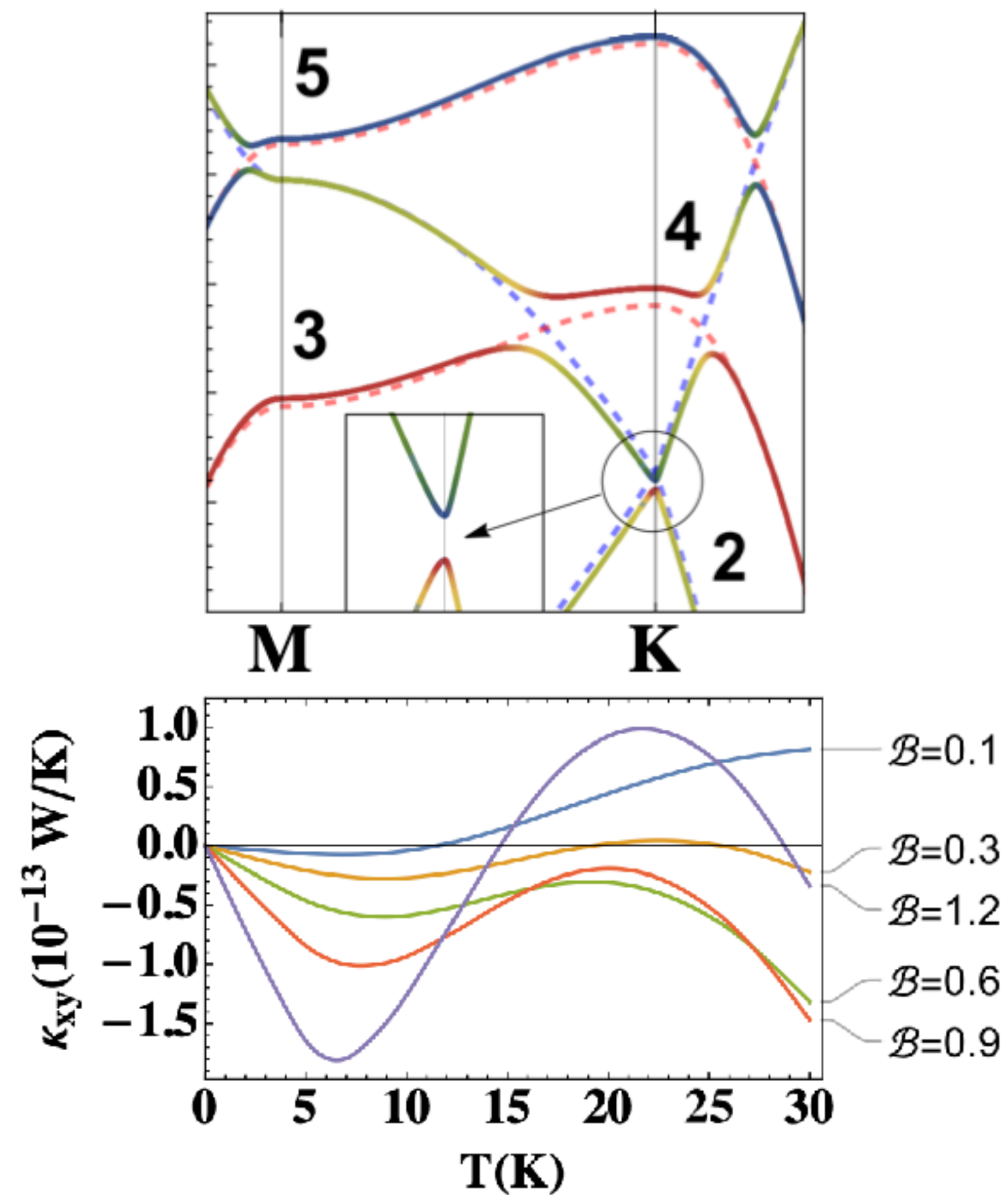
Go, Kim, Lee 2019
Shen, Kim 2020

Tunability

By temperature change & across magnetic phase transition...

Ma, Fiete 2021

Neumann, Mook, Henk, Mertig 2022



Bilayer van der Waals magnet

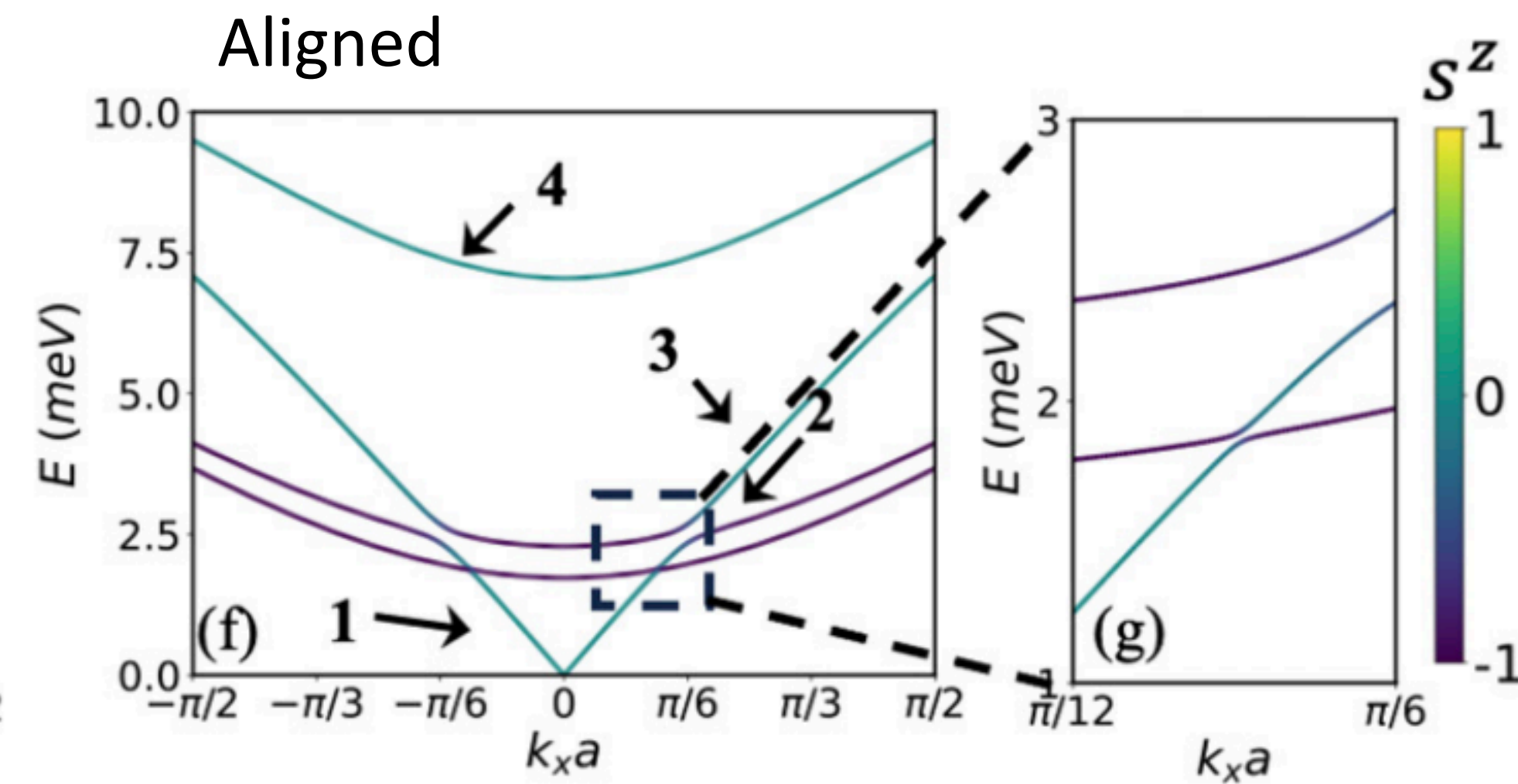
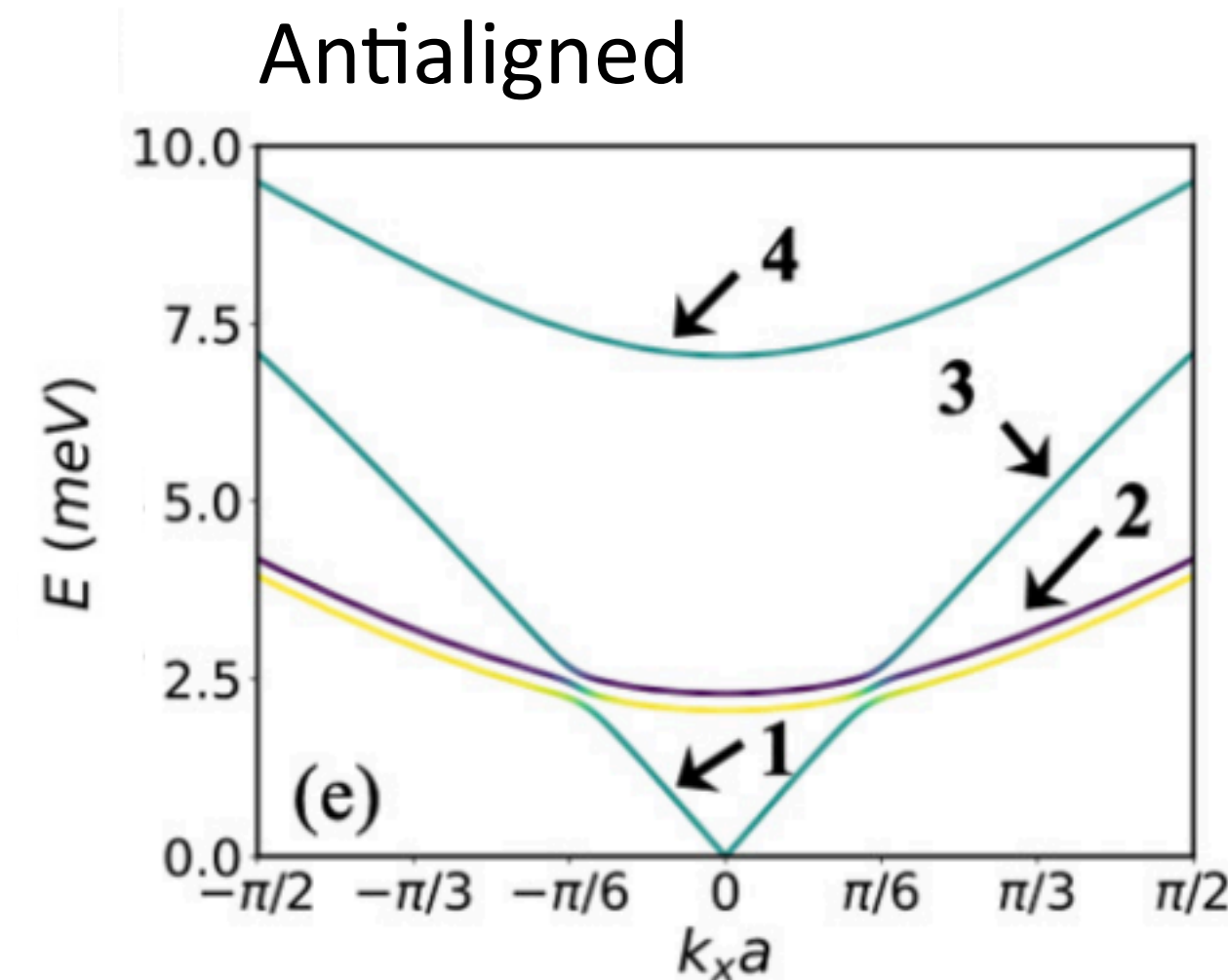
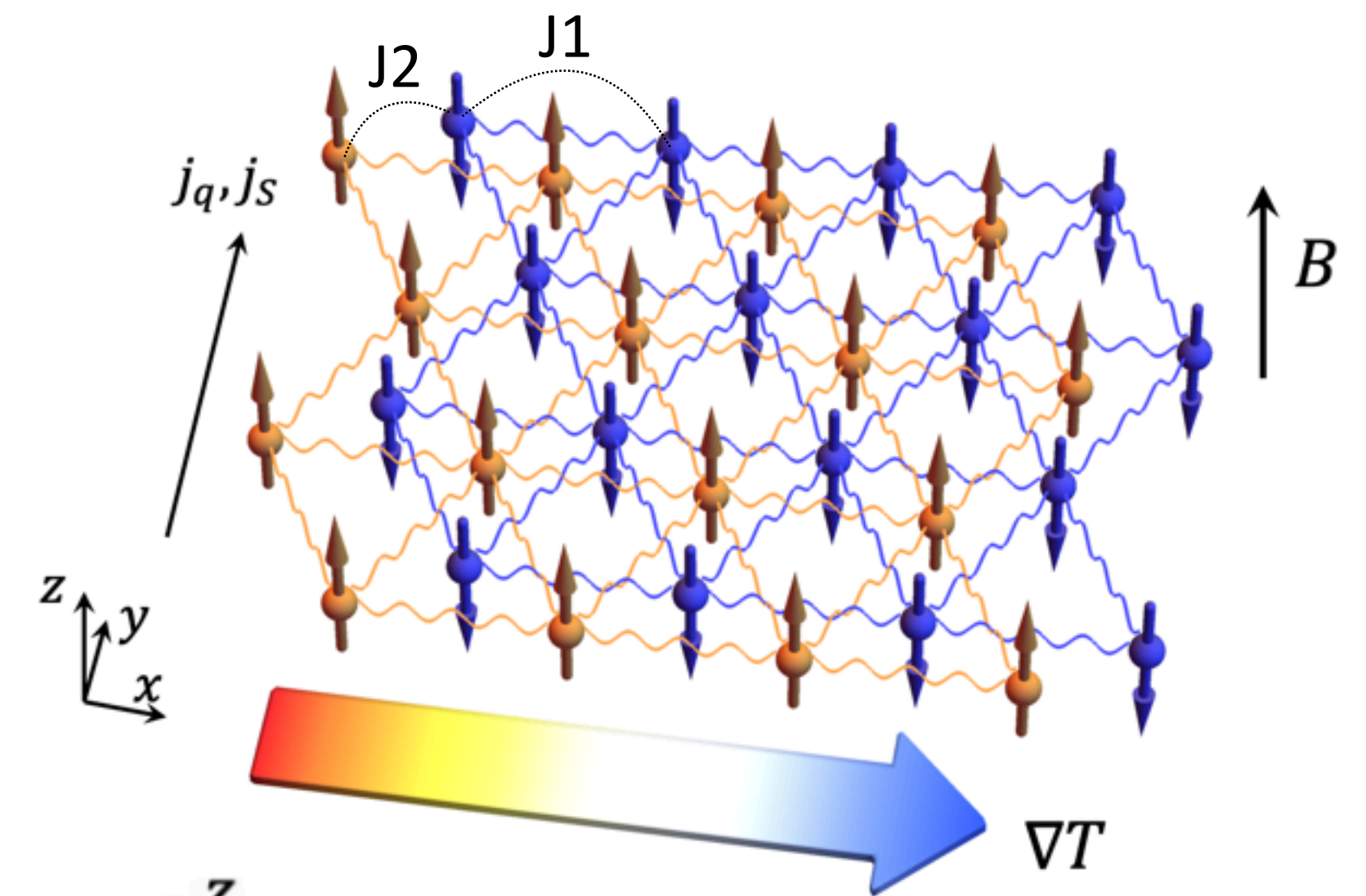
FM intralayer $J_1 \gg$ AFM interlayer $J_2 \sim$ Magnetoelastic coupling κ

Field induced metamagnetic transition

Candidate: FeCl₂ with splitting at hybridization $\sim 0.32\text{meV}$

Siebeck and Houmann 1976

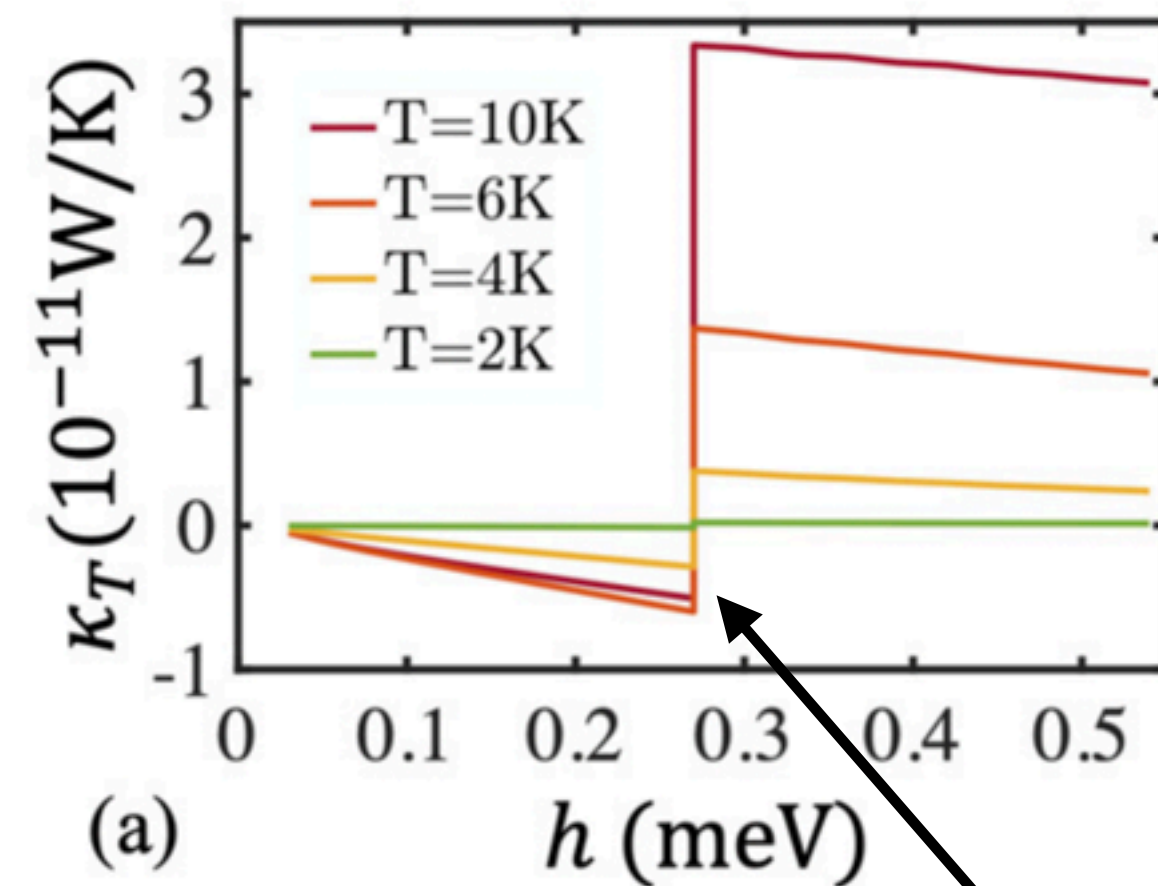
Lin, SZ, Appl. Phys. Lett. 2024



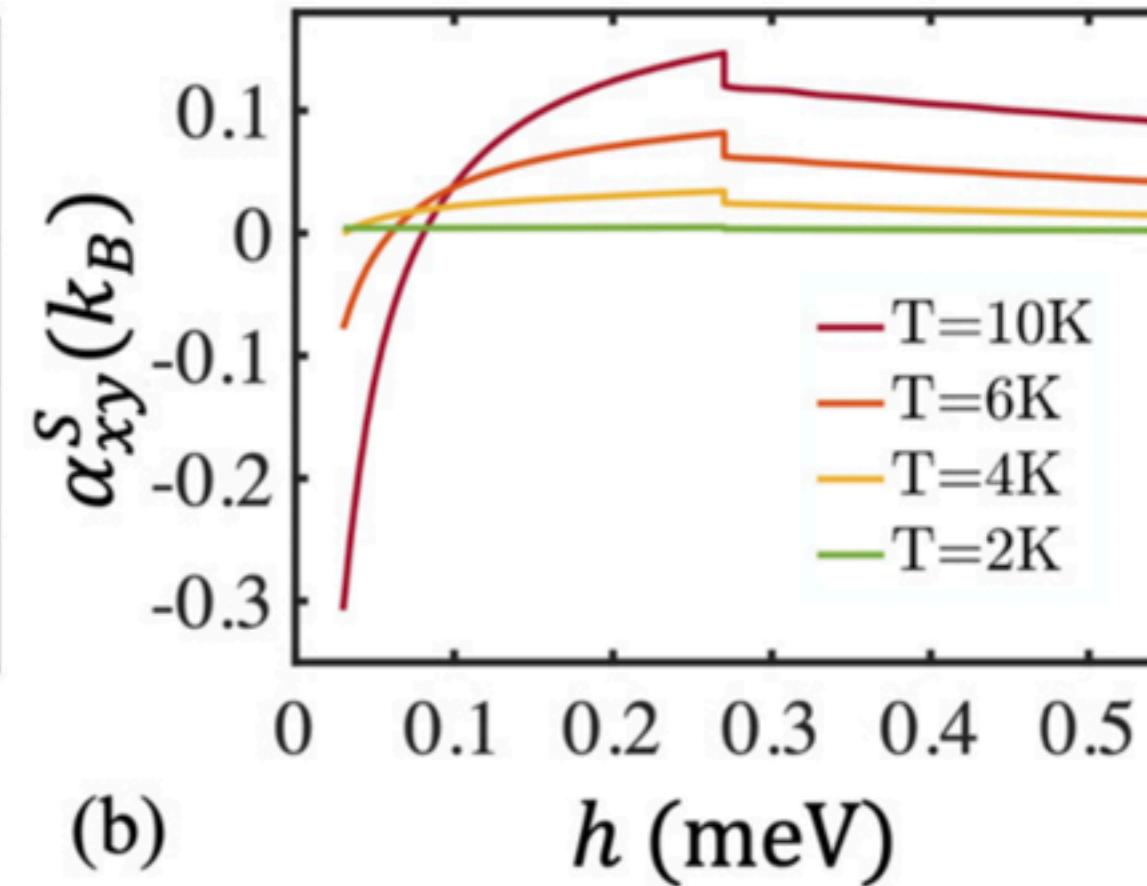
Transport across metamagnetic transition

Lin, SZ, Appl. Phys. Lett. 2024

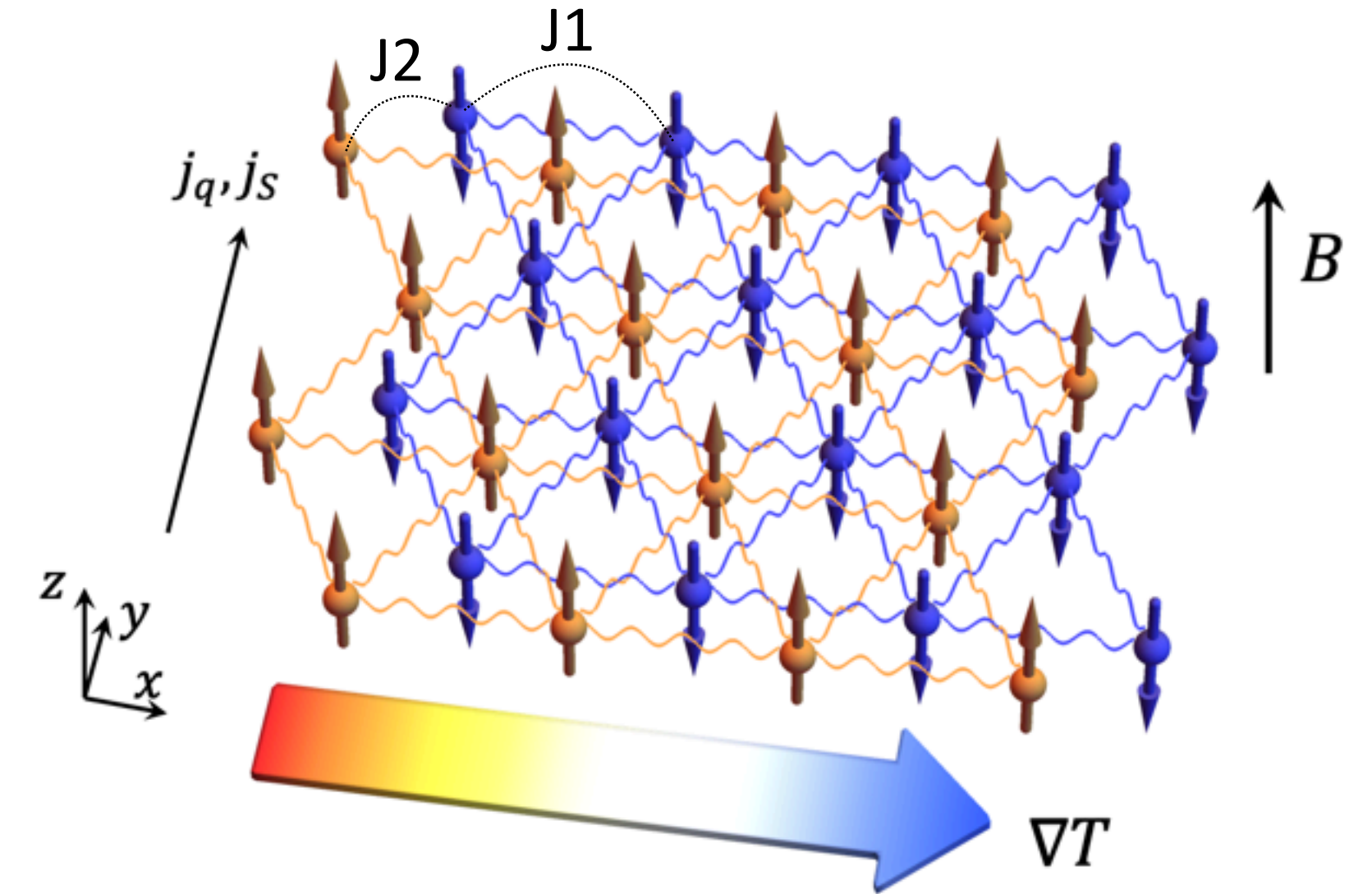
FeCl₂: Thermal Hall



Spin Nernst



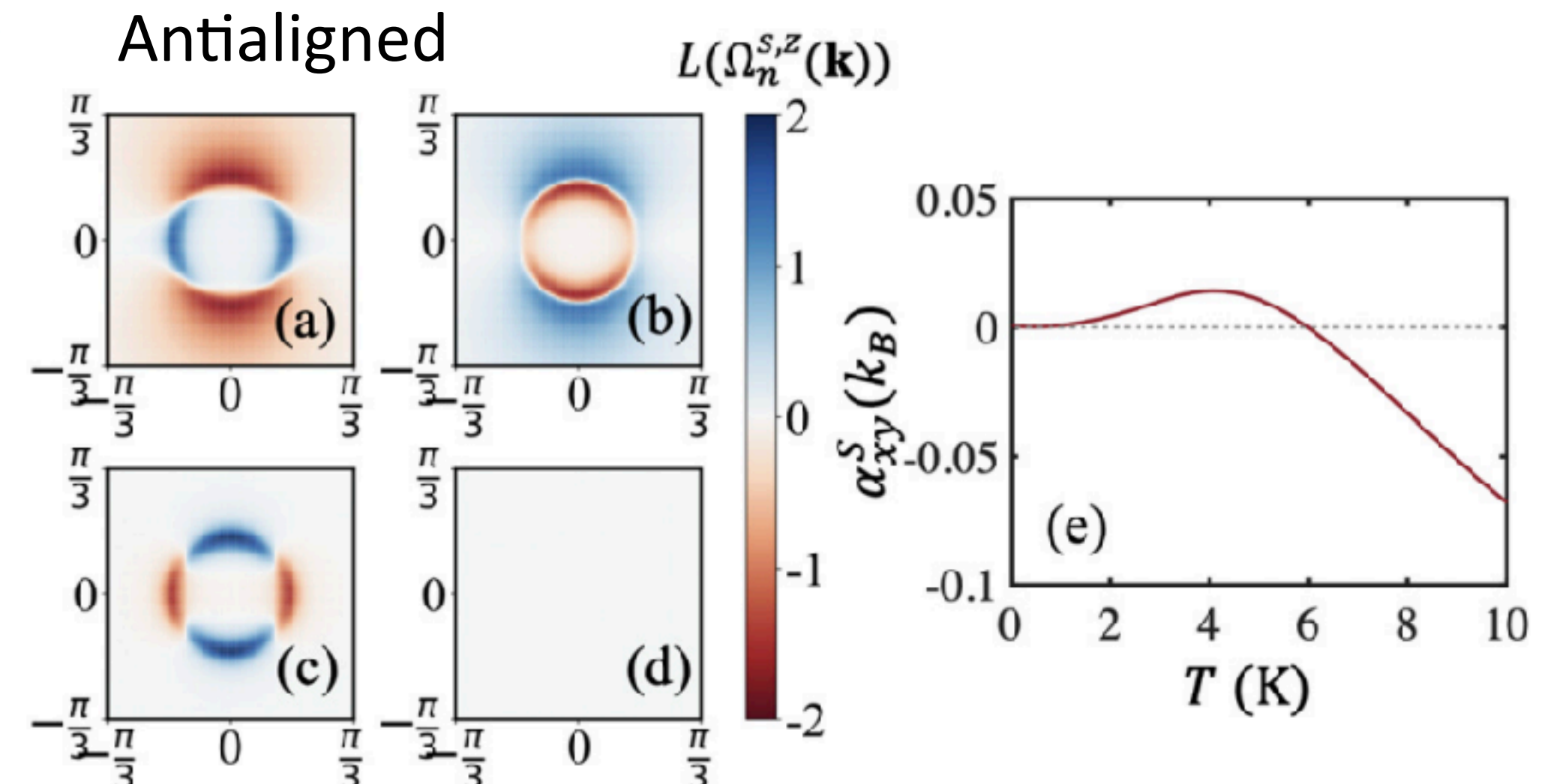
Metamagnetic transition



$$\Omega_n^z(\mathbf{k}) = - \sum_{m \neq n} \frac{2 \text{Im} \langle n | v_x | m \rangle \langle m | v_y | n \rangle g_{nn} g_{mm}}{[g_{nn} E_n(\mathbf{k}) - g_{mm} E_m(\mathbf{k})]^2}$$

Spin current Magnon current

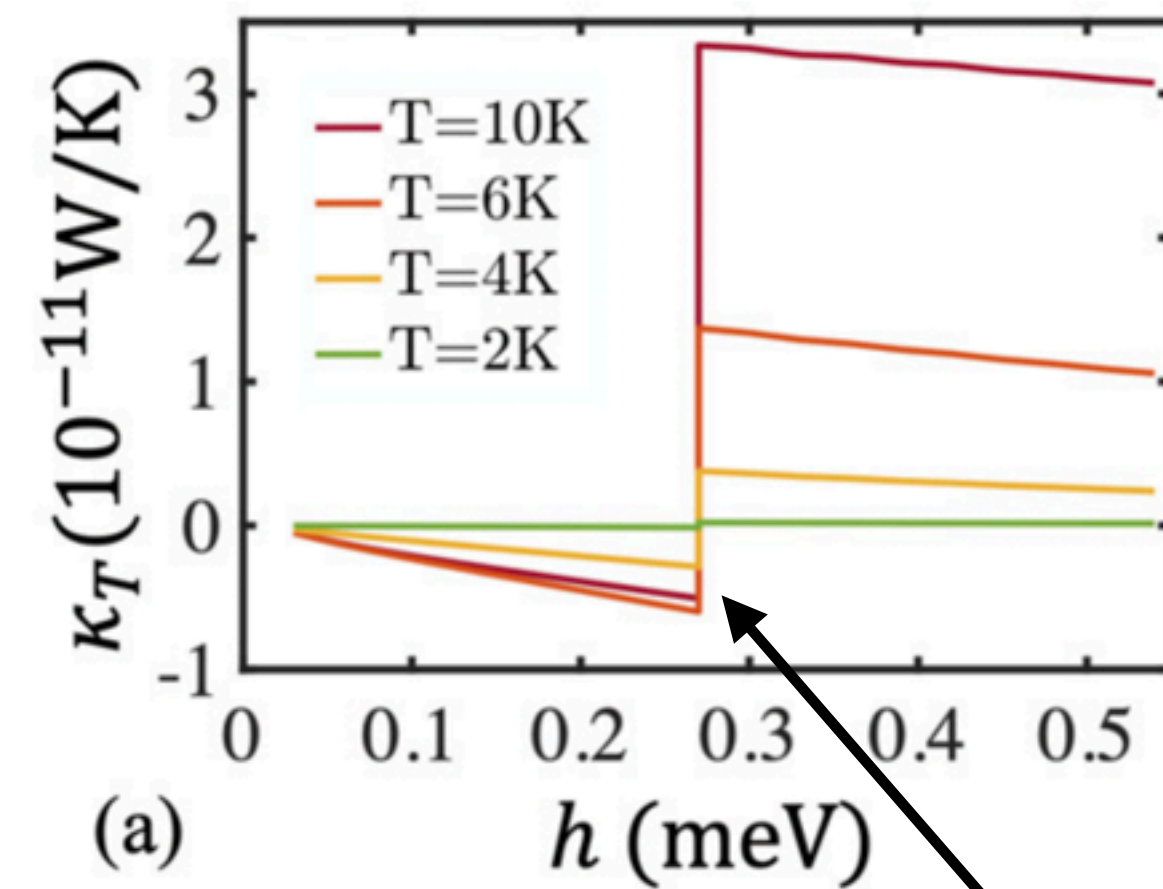
$$\Omega_n^{s,z}(\mathbf{k}) = - \sum_{m \neq n} \frac{2 \text{Im} \langle n | \theta_x | m \rangle \langle m | v_y | n \rangle g_{nn} g_{mm}}{[g_{nn} E_n(\mathbf{k}) - g_{mm} E_m(\mathbf{k})]^2} \quad \text{BdG normalization}$$



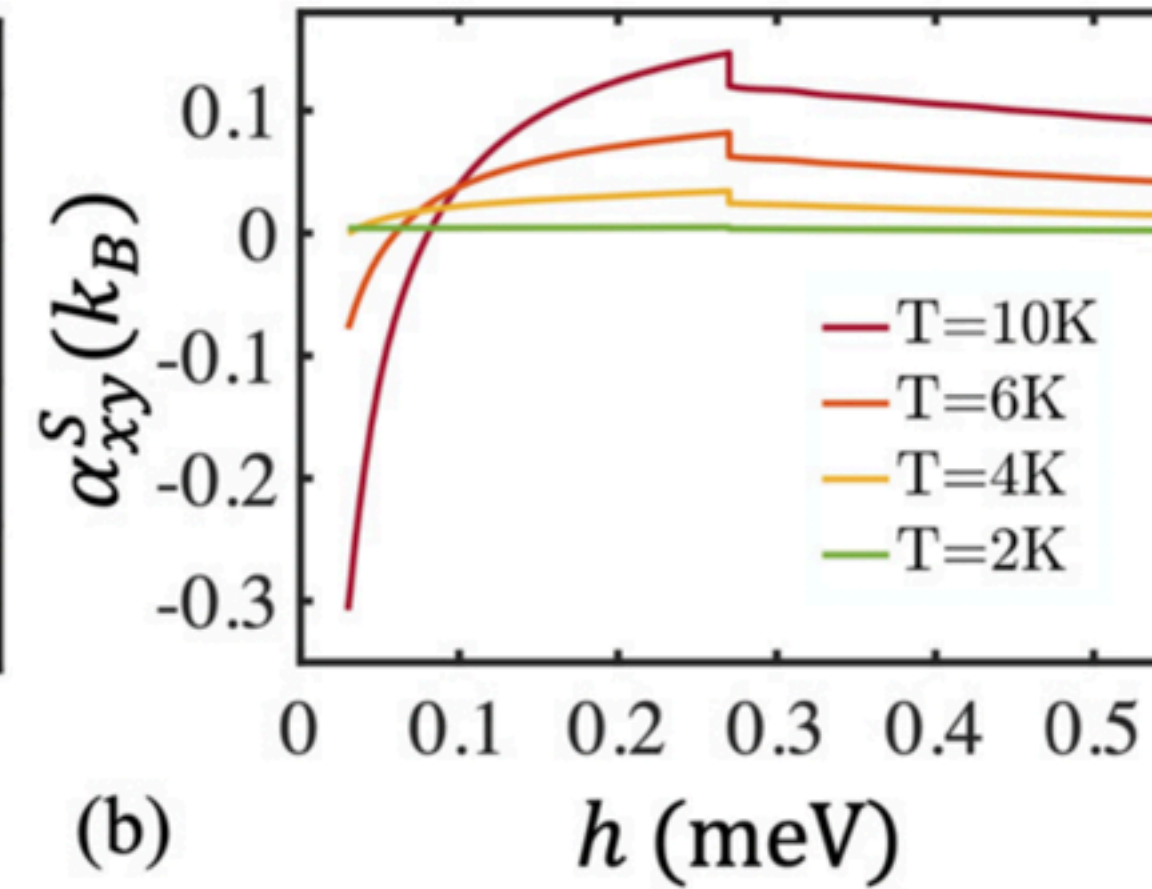
Experimental observation

Lin, SZ, Appl. Phys. Lett. 2024

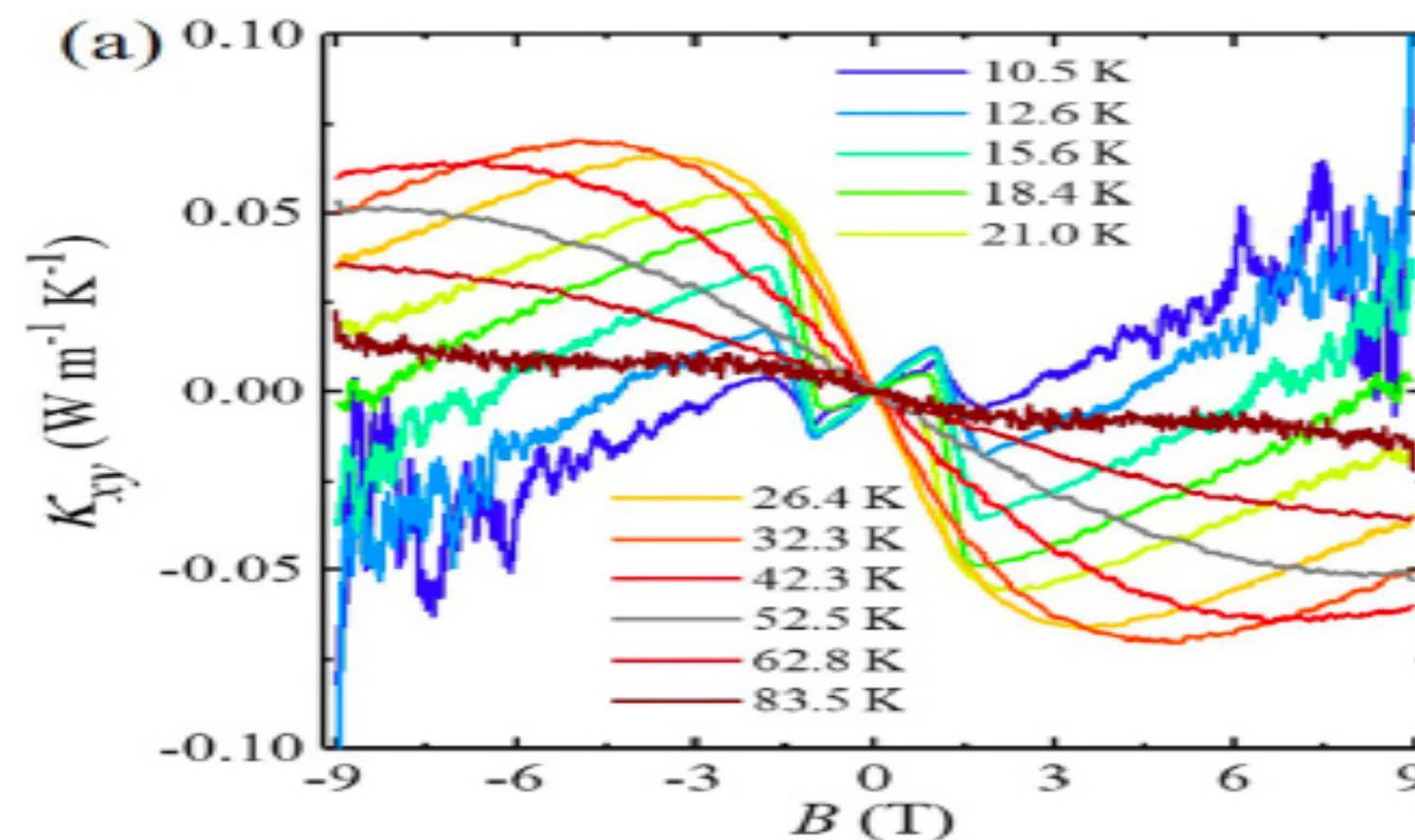
FeCl₂: Thermal Hall



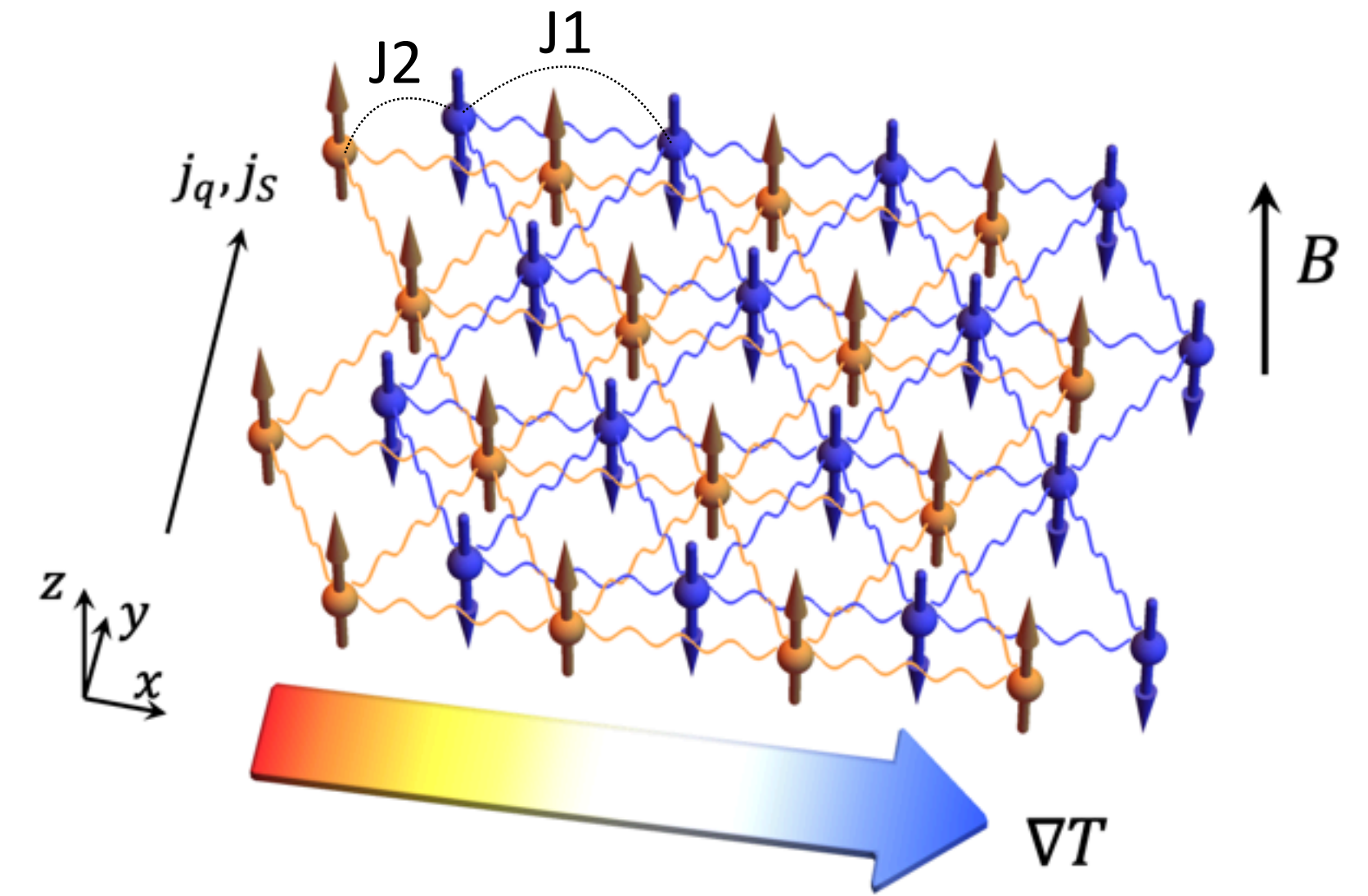
Spin Nernst



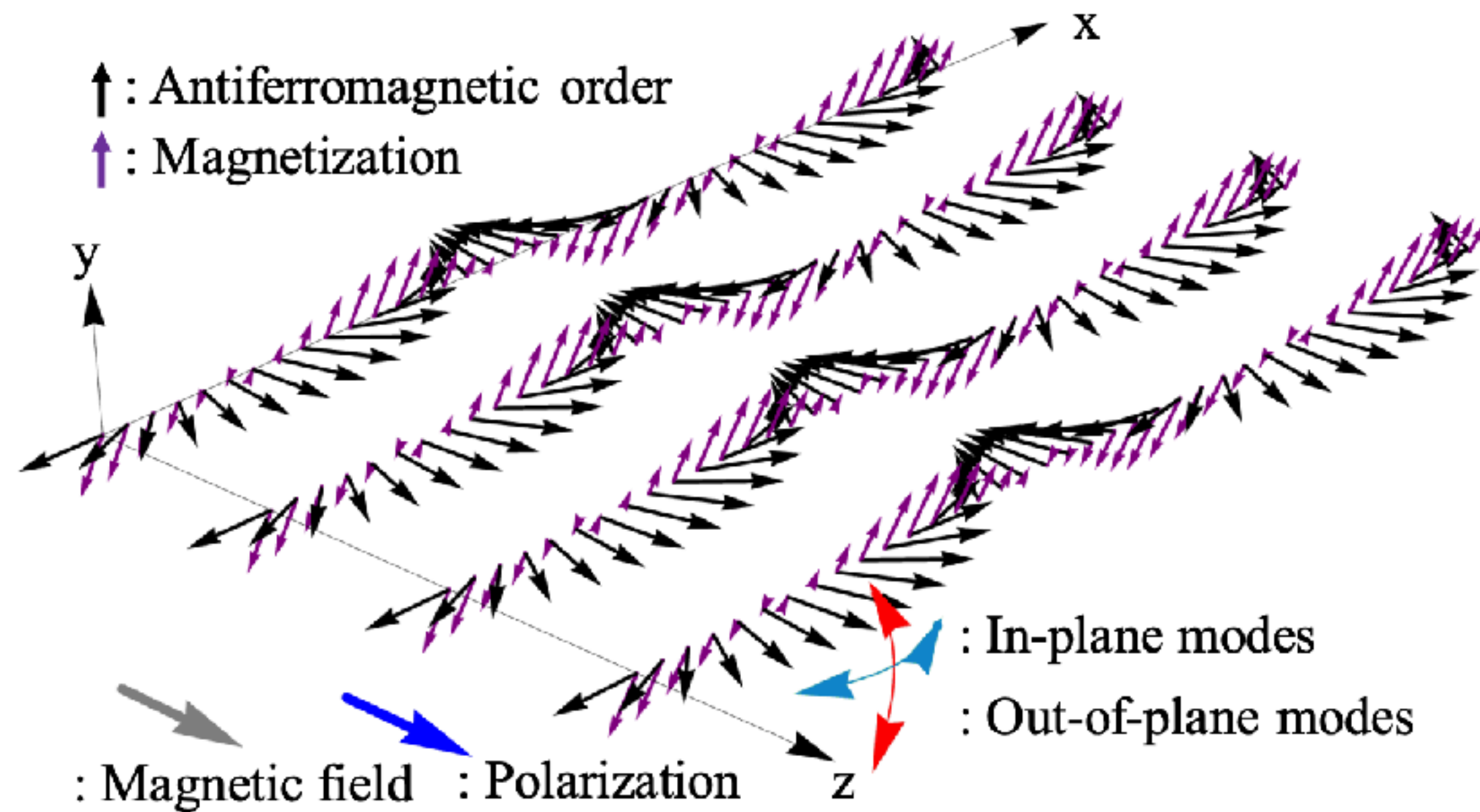
Metamagnetic transition



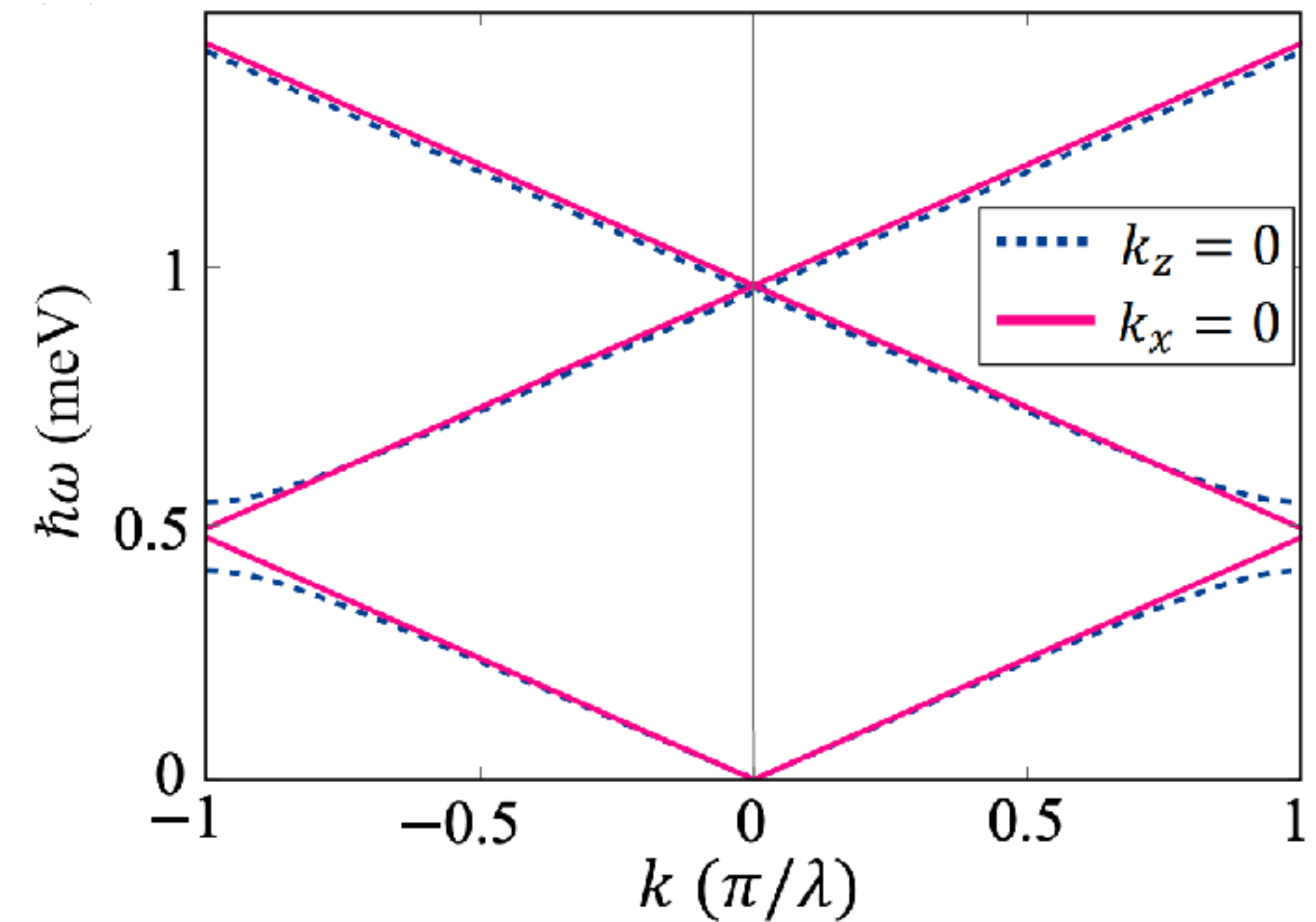
Xu, et. al. PRB Letter, 2023



Magnons in (multiferroic) spin cycloids



H. W. Park, SZ, ... S. K. Kim, arXiv:2503.11135

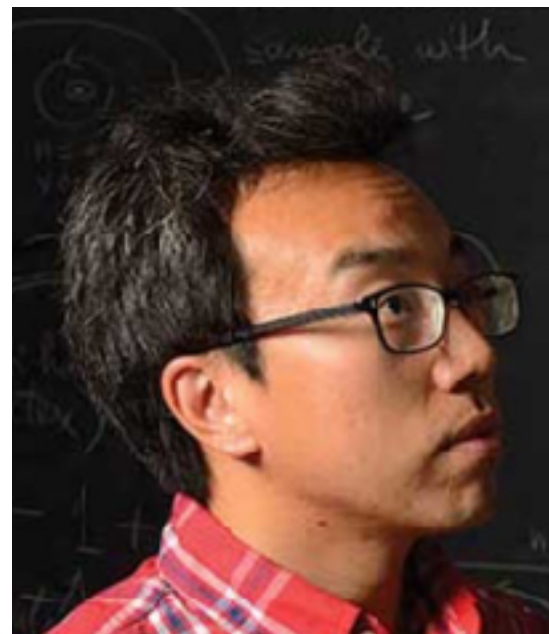


$\uparrow$
 Period of the cycloid superlattice

Summary

- Magnetoelastic coupling induced topological magnon-phonon hybridization
- Collinear antiferromagnet: monolayer/bilayer
SZ, Go, Lee, Kim, *Phys. Rev. Lett.* 124, 147204 (2020)
Lin and SZ, *Appl. Phys. Lett.* 124, 132402 (2024)
- Thermal Hall and Spin Nernst effects

Acknowledgement



Se Kwon Kim
@ KAIST



Zhi-Xing Lin
@ Princeton