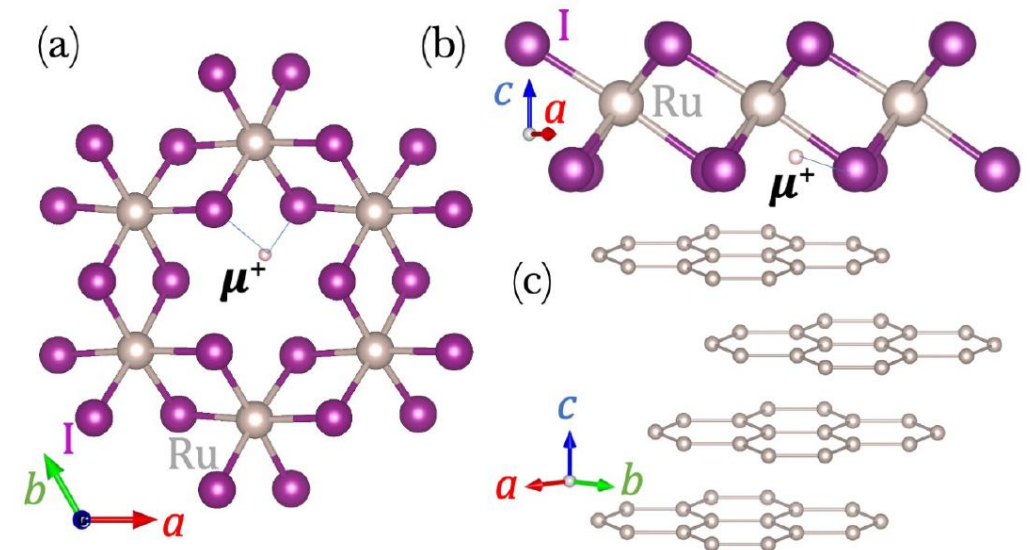
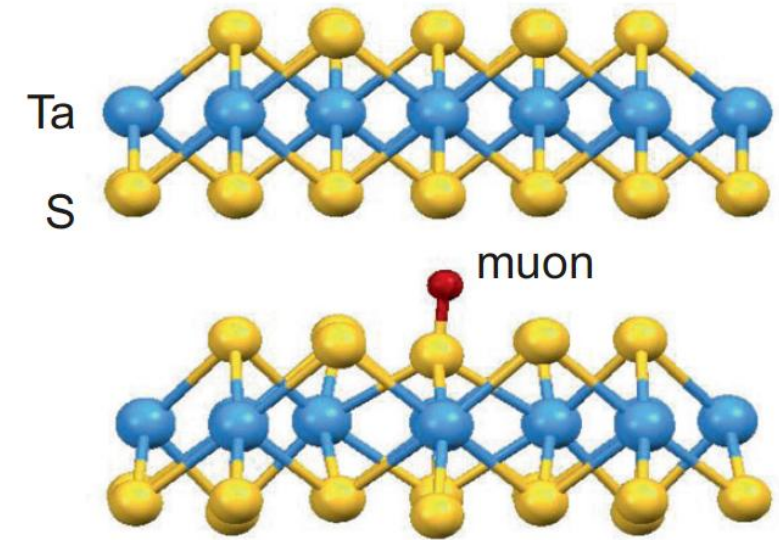


Quantum spin liquids in van der Waals materials

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Young Research Leaders Group
Workshop 2025



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Hank Wu

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ISIS Neutron and Muon Source

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Eugenio Coronado



Danrui Ni

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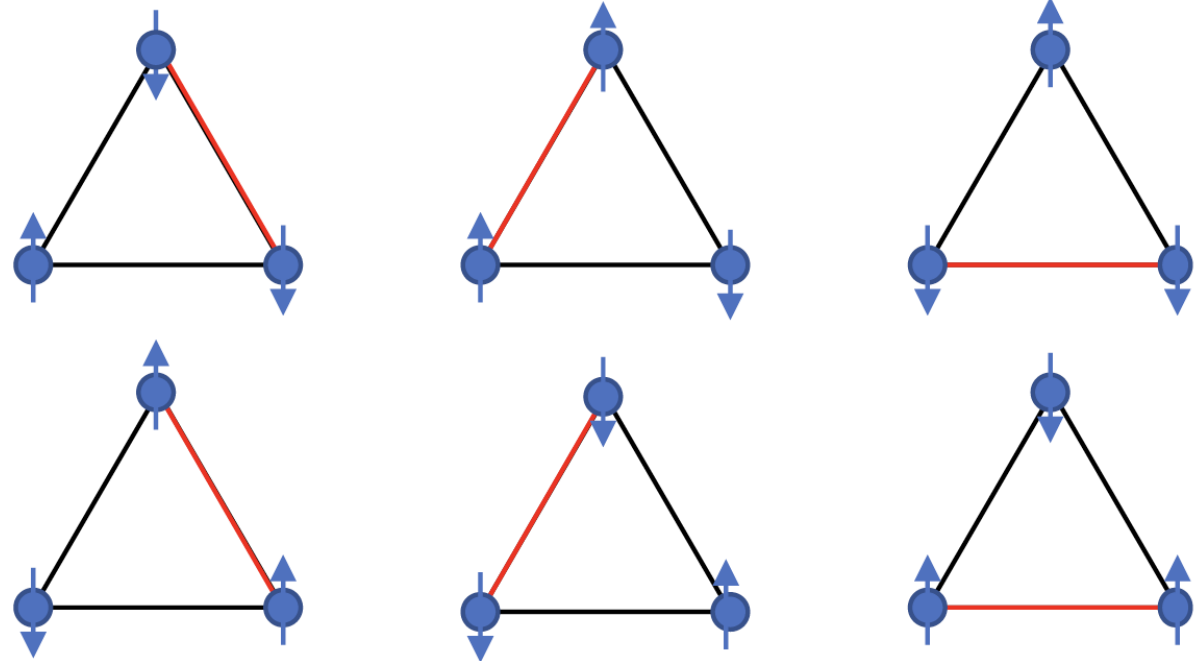
1. Introduction to quantum spin liquids (QSLs)
2. The muon-spin spectroscopy (μ SR) technique
3. μ SR studies of candidate QSLs
 - I. Triangular-lattice 1T-TaS₂
 - II. Honeycomb-lattice α -RuI₃

Quantum spin liquids

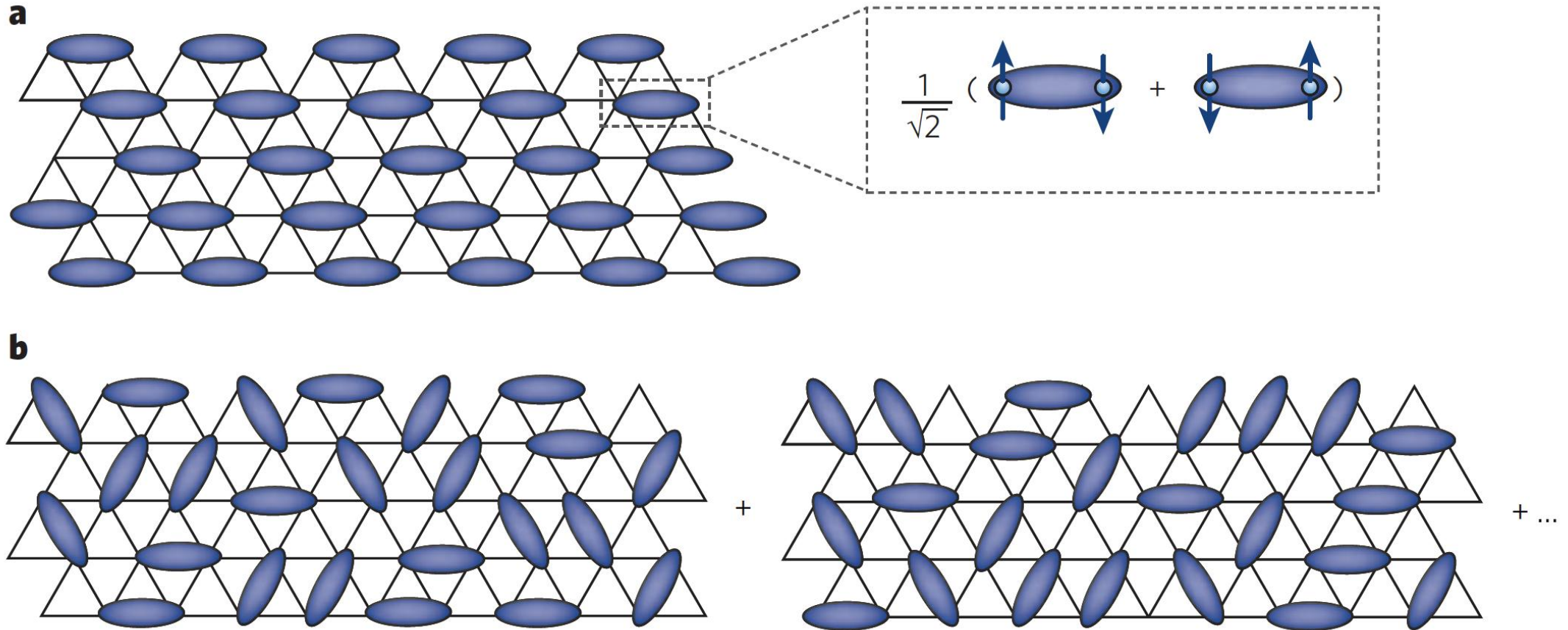
- A quantum spin liquid (QSL) is a system of interacting localized electronic moments for which strong quantum fluctuations prevent their ordering even down to $T = 0$ K.
- Such systems are characterized by a high-degree of quantum entanglement and fractionalized excitations.
- Interactions in dimensions $d < 3$ are more effective at destabilizing magnetic order.

Geometrical frustration

- Cannot simultaneously satisfy antiferromagnetic interactions between Ising spins on a triangle.
- Results in six degenerate ground states.

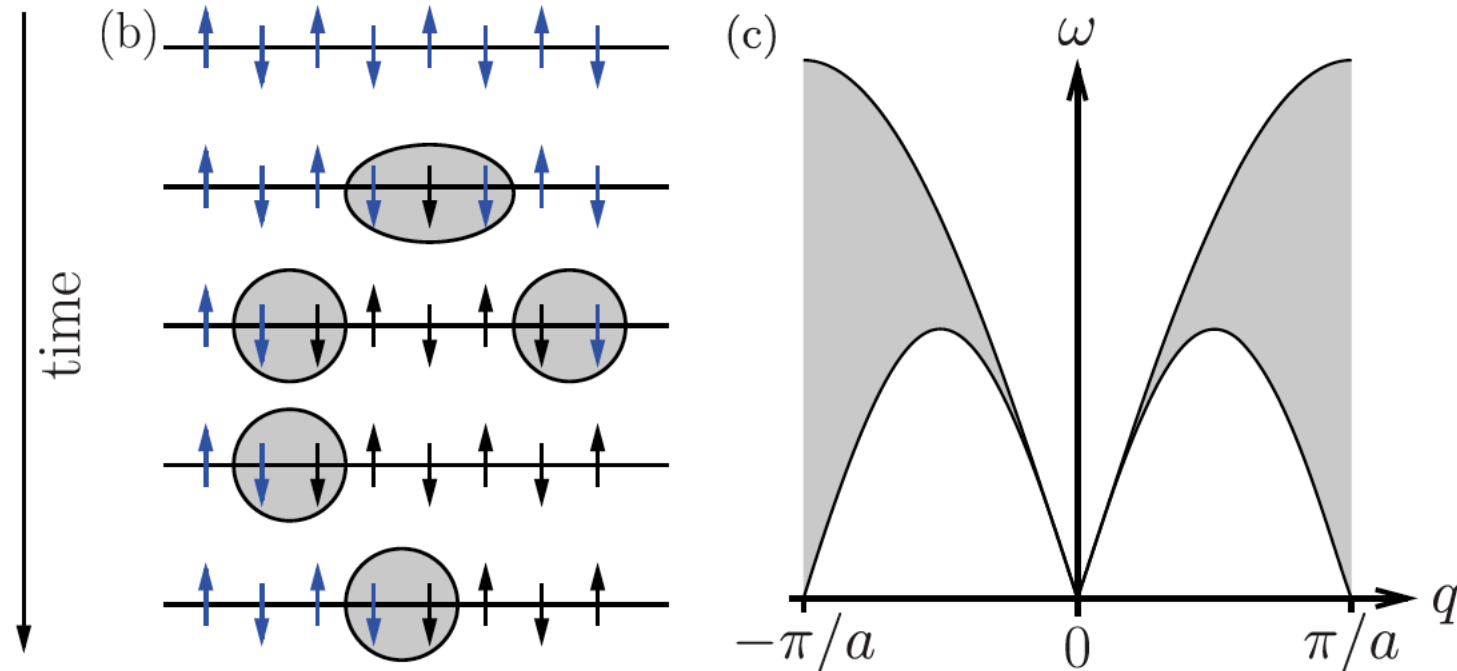


Resonating valence bonds



Spinons

- Magnon ($s = 1$) not stable in 1D, but instead splits into two $s = 1/2$ spinons that can propagate by flips of pairs of spins
- Gives rise to a continuum of excitations



Muon-spin spectroscopy

What is a muon?

- First discovered as constituent of cosmic rays
- Spin-1/2 lepton
- Unstable, average lifetime $\tau = 2.2 \mu\text{s}$
- In μ^+ SR we use the positive muon (antimuon)

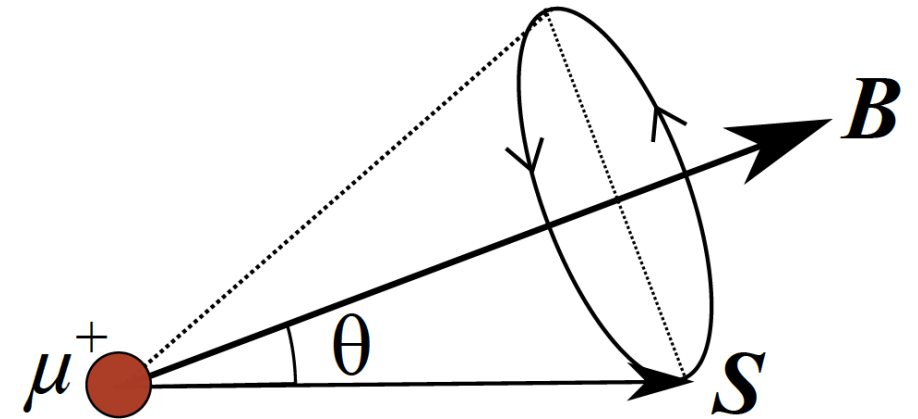
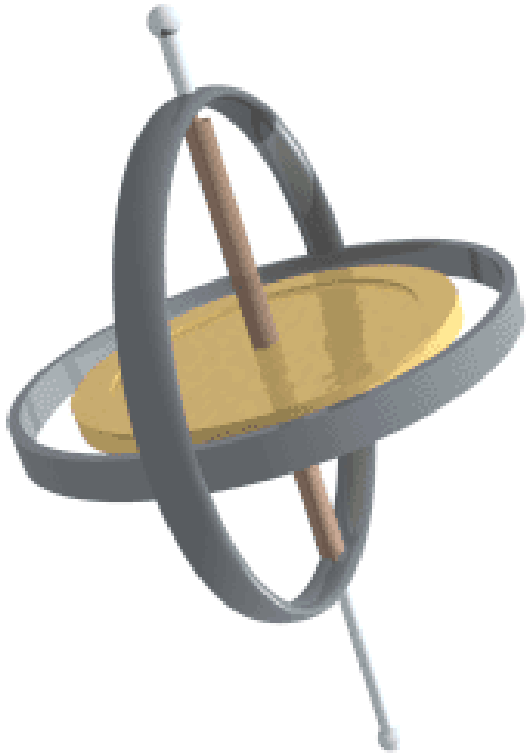
QUARKS

u	s	t
d	c	b

LEPTONS

e	μ	τ
ν_e	ν_μ	ν_τ

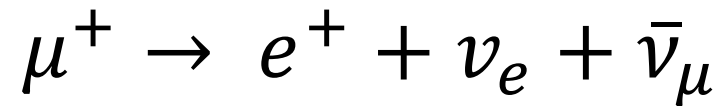
Spin precession



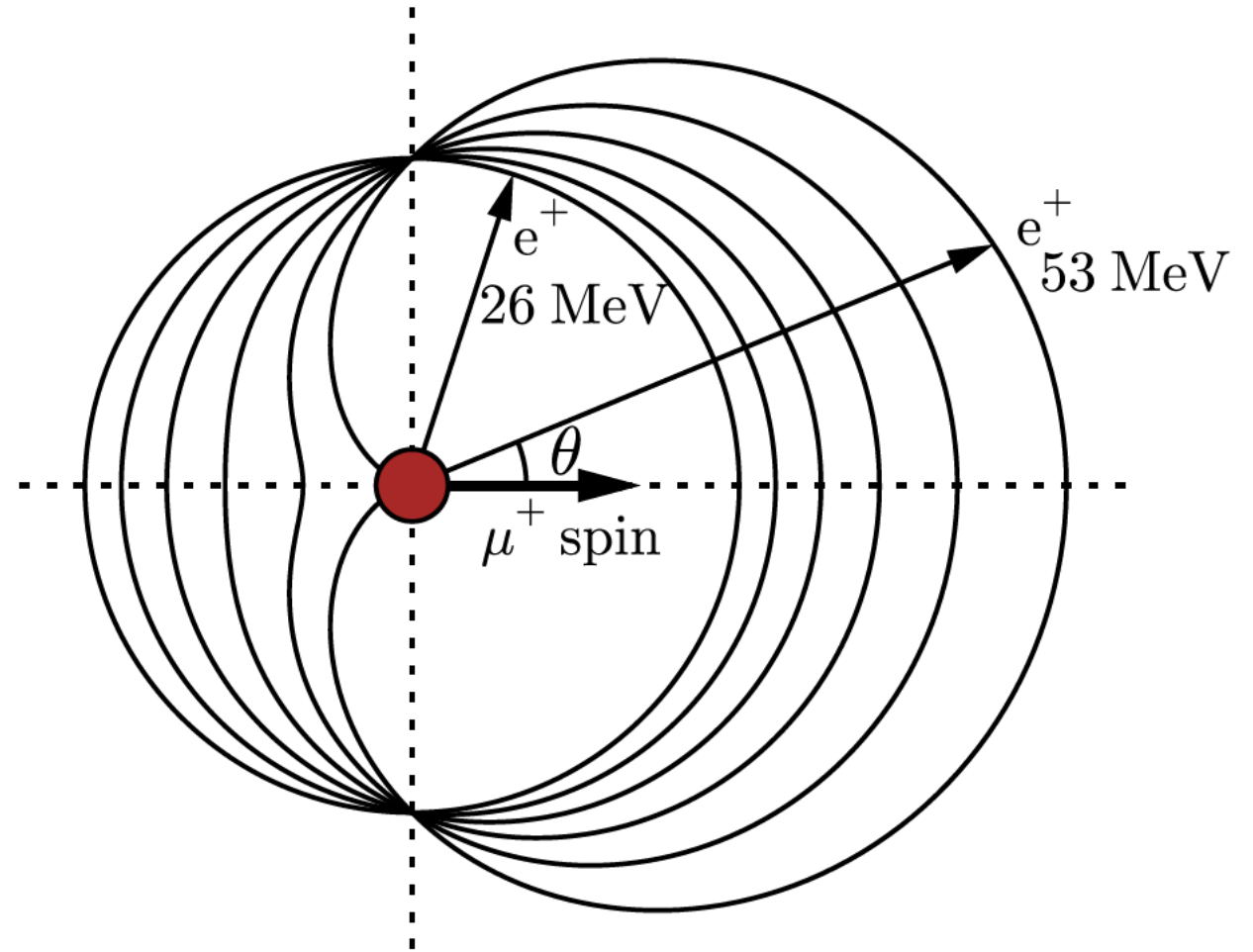
$$\frac{d\langle \mathbf{S} \rangle}{dt} = \gamma_{\mu} \langle \mathbf{S} \rangle \times \mathbf{B}$$

$$P(t) = \cos^2 \theta + \sin^2 \theta \cos(\gamma_{\mu} B t)$$

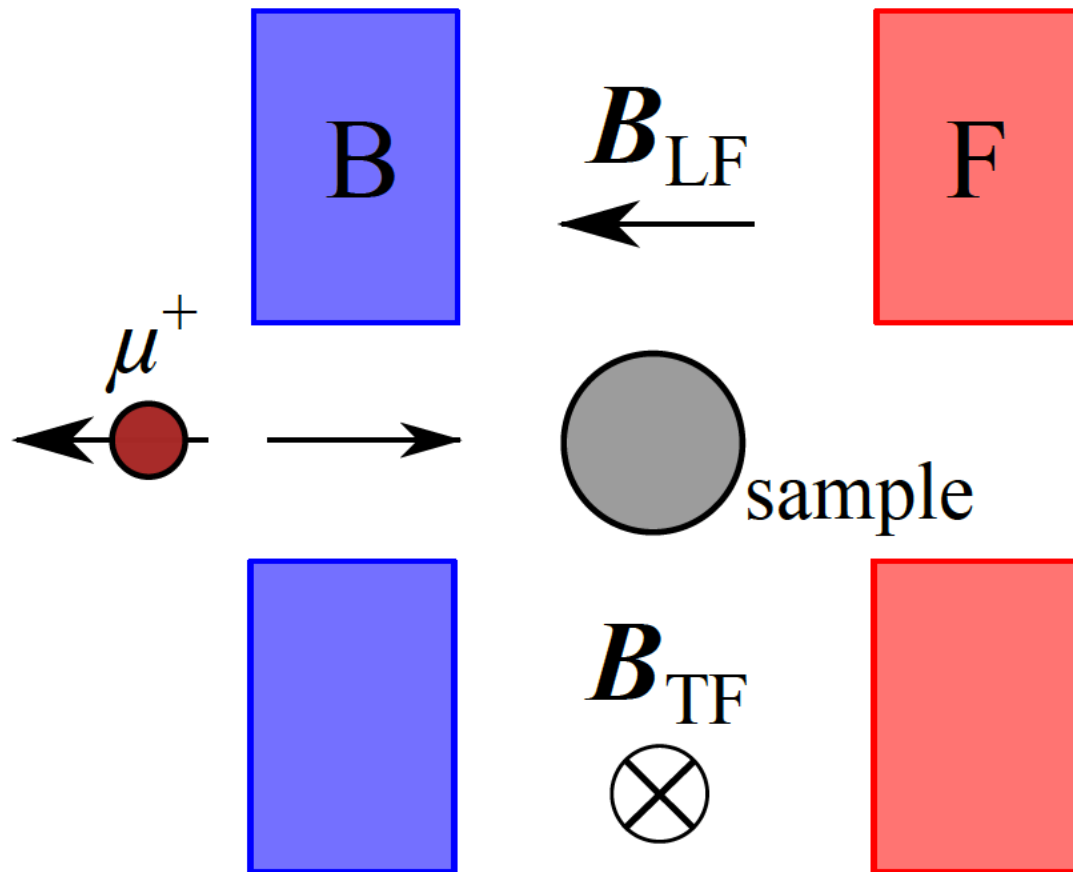
μ SR is not a scattering technique



$$\tau = 2.2 \mu\text{s}$$



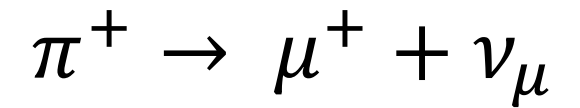
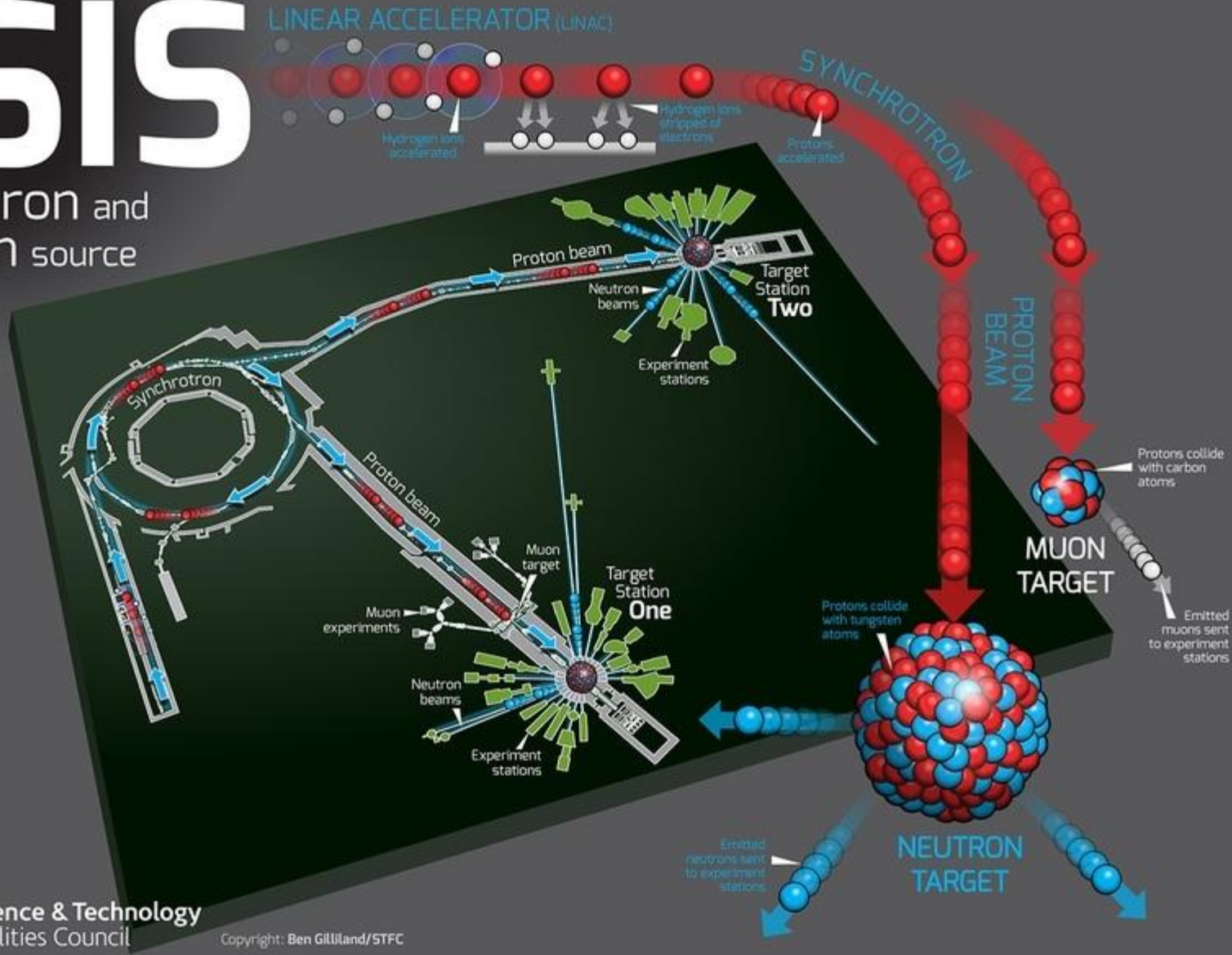
Experimental setup



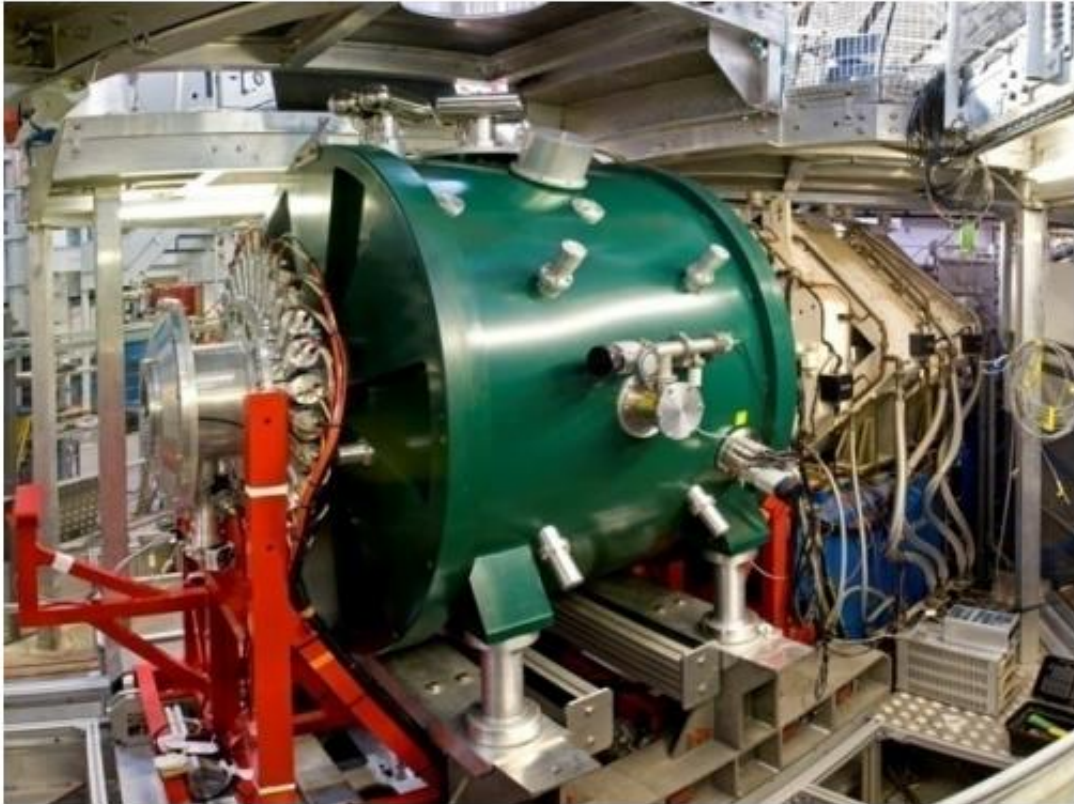
$$A(t) = \frac{N_B(t) - N_F(t)}{N_B(t) + N_F(t)}$$

ISIS

Neutron and
Muon source



μ SR spectrometers



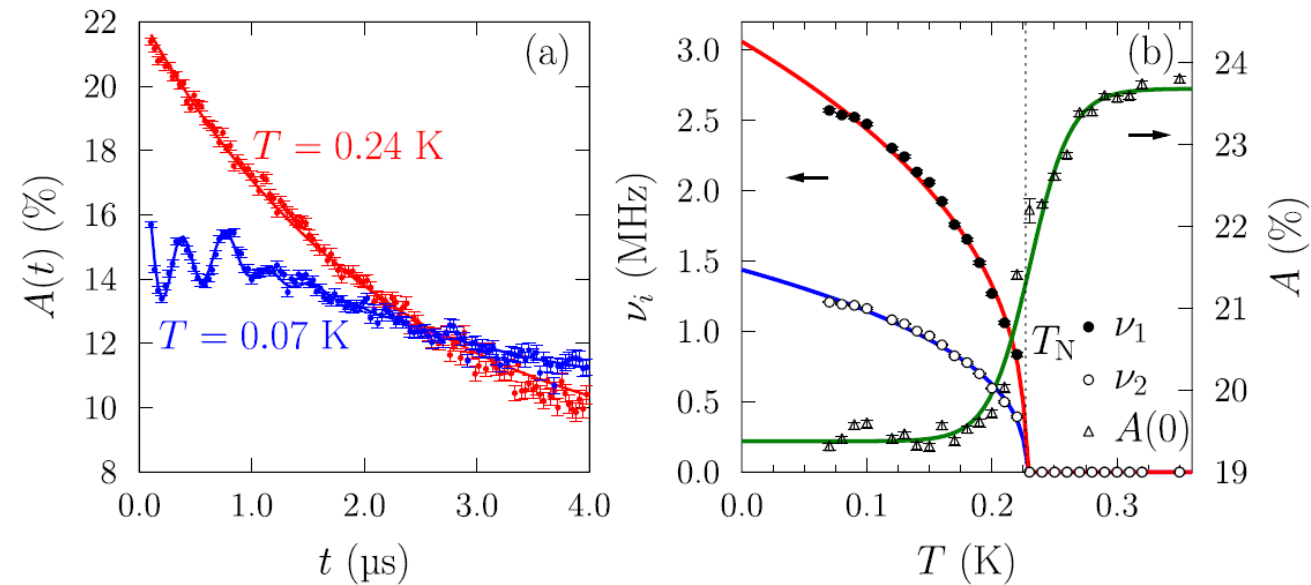
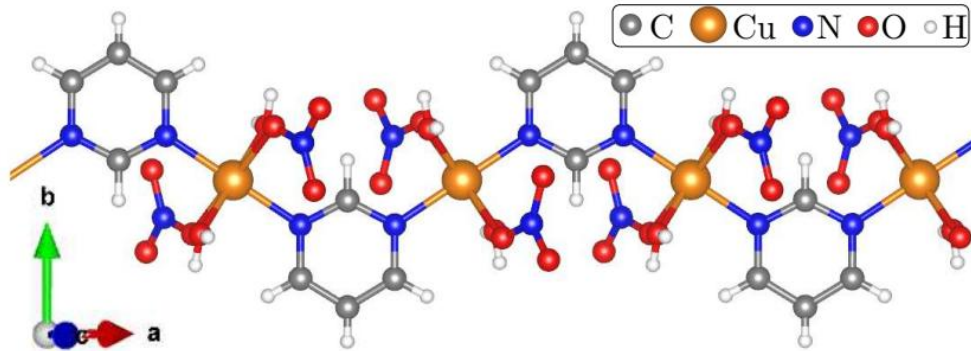
HiFi (ISIS)



GPS (PSI)

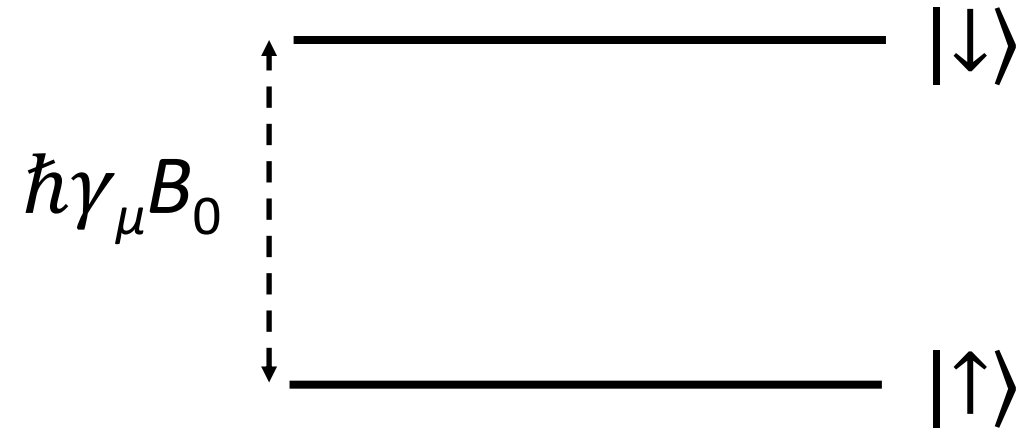
Magnetism

- Muons precess at a frequency $\omega = \gamma_\mu B$
- Fields as small as ≈ 0.04 mT are measurable
- Muons are a *local* probe



Magnetisation dynamics

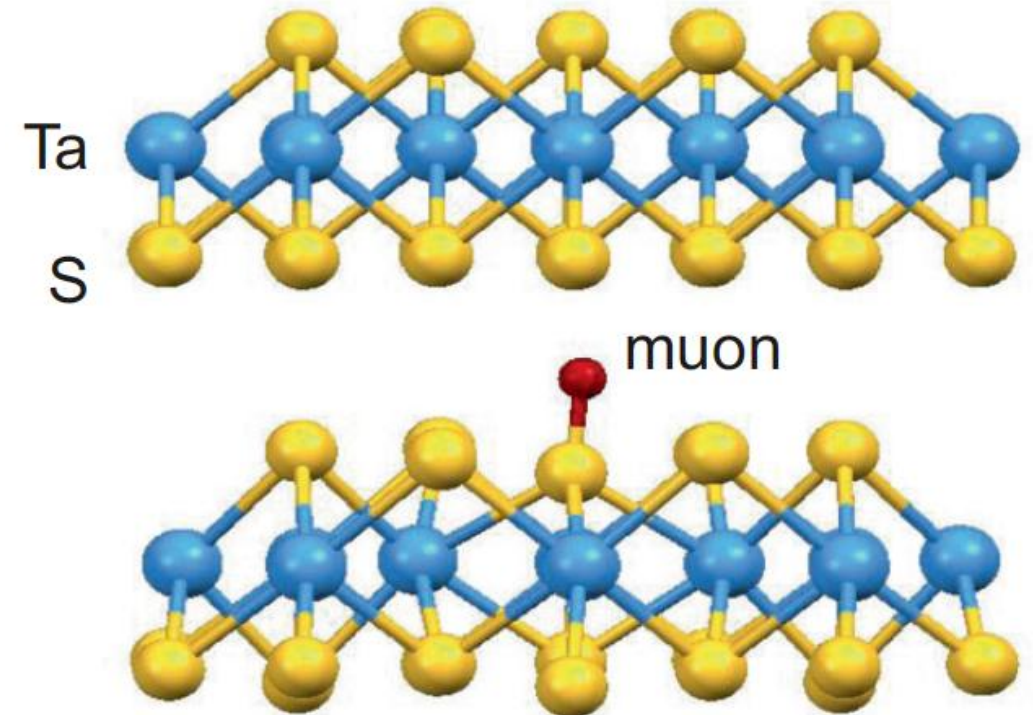
- A magnetic field applied parallel to the muon spin creates an energy gap between the spin states
- Fluctuating magnetic fields can cause transitions between up and down states
- Leads to a relaxation of the polarisation $P_z(t) \propto (n_\uparrow - n_\downarrow)$



$$P_z(t) = P_z(0)e^{-\lambda t}$$

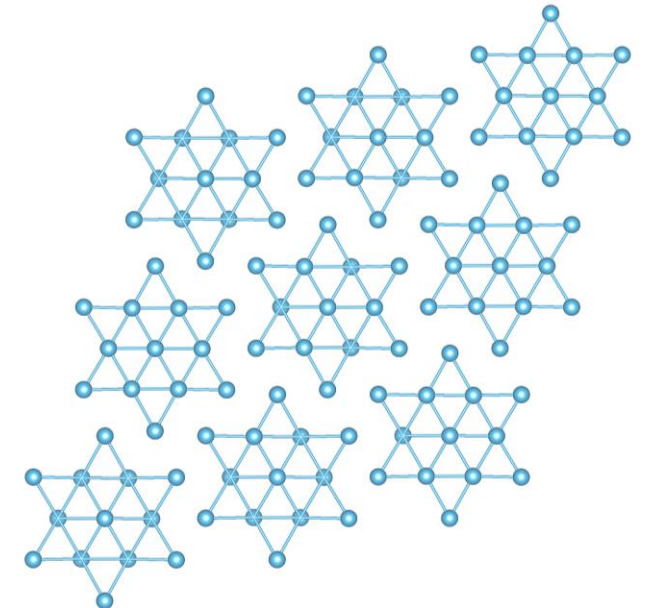
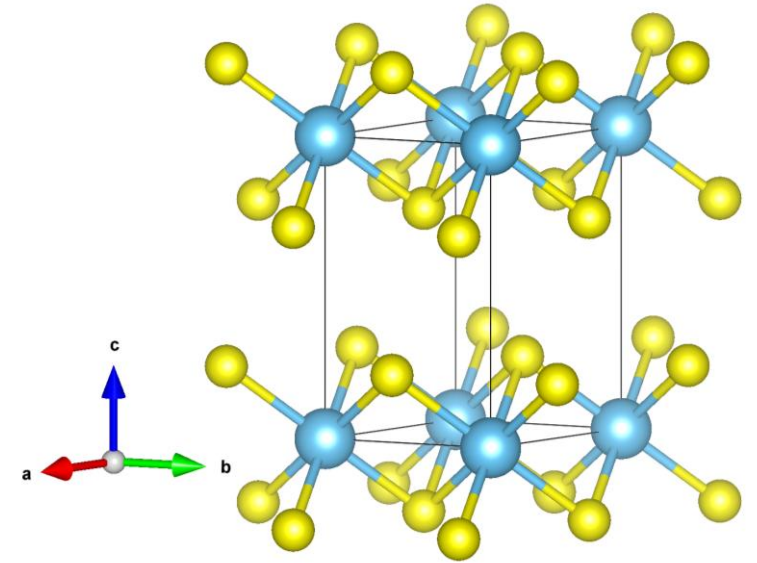
1T-TaS₂

A candidate
triangular-
lattice QSL

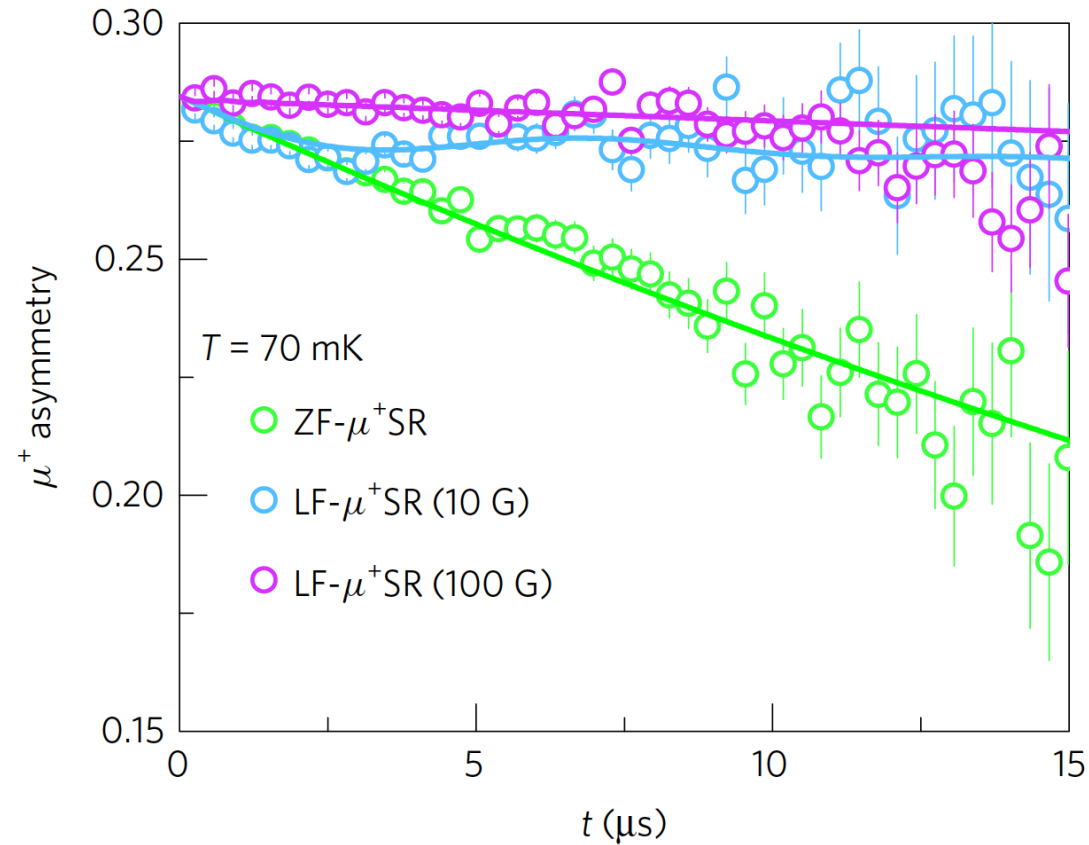


1T-TaS₂

- Layered compound that undergoes a series of charge-density-wave (CDW) instabilities.
- For commensurate CDW (C-CDW) phase below 200 K, Ta atoms form a triangular lattice of Star-of-David clusters, with one unpaired spin-1/2 per cluster.



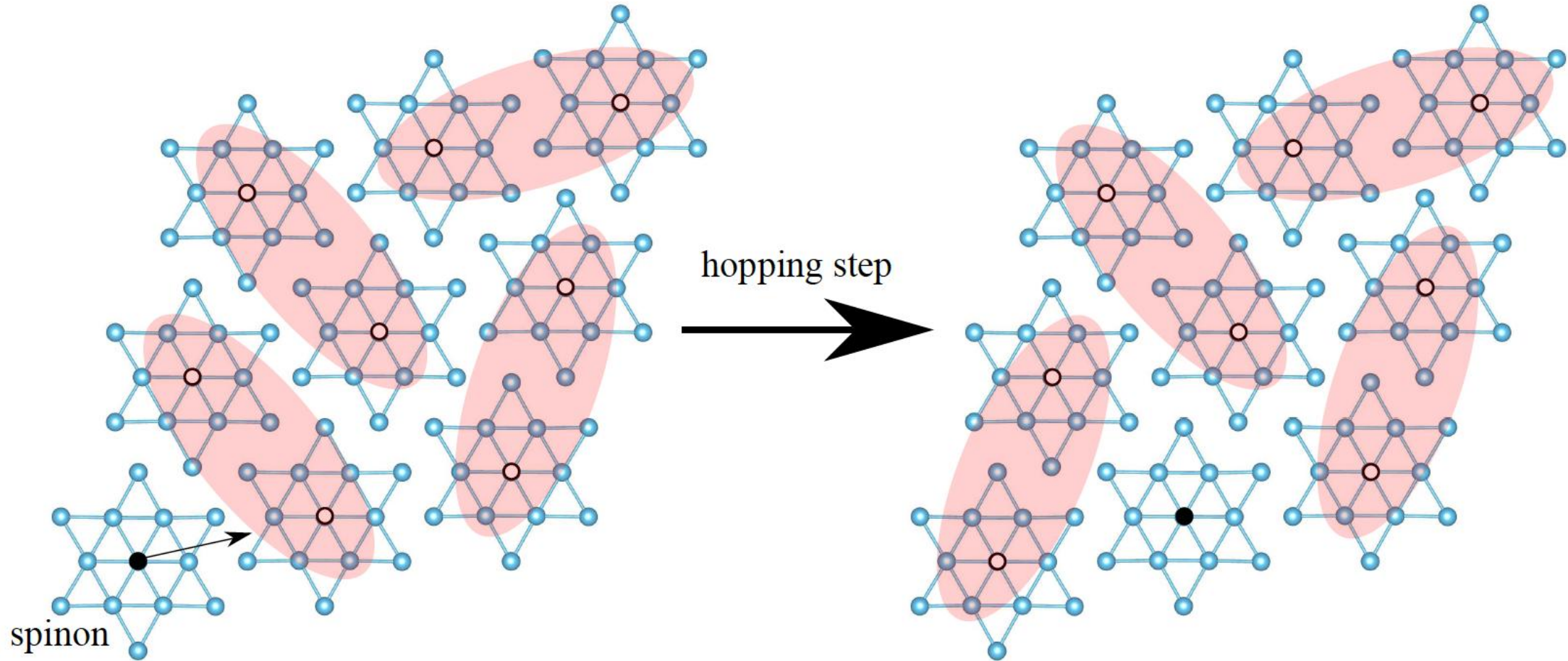
Absence of magnetic order



M. Klanjšek *et al.* Nat. Phys. **13**, 1130 (2017)

Here we instead focus on the **dynamics**

Spinon diffusion



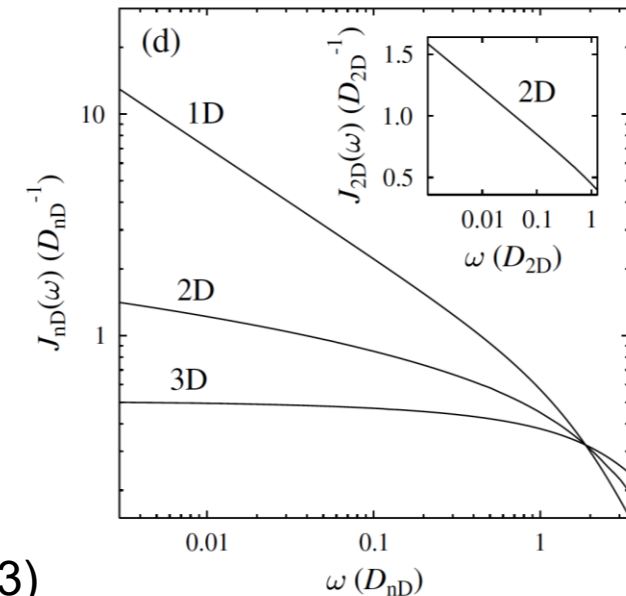
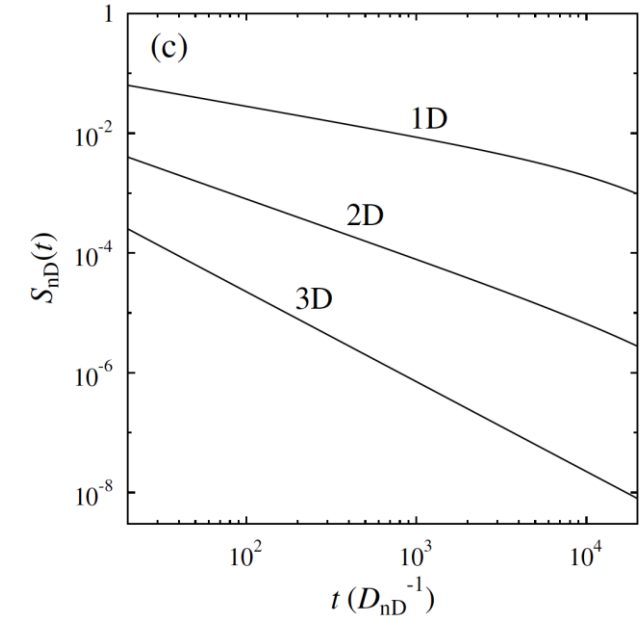
Studying spin diffusion with LF μ SR

- The spin autocorrelation function for diffusion in n dimensions has the form

$$S_{nD}(t) = [\exp(-2D_{nD}t)I_0(2D_{nD}t)]^n,$$

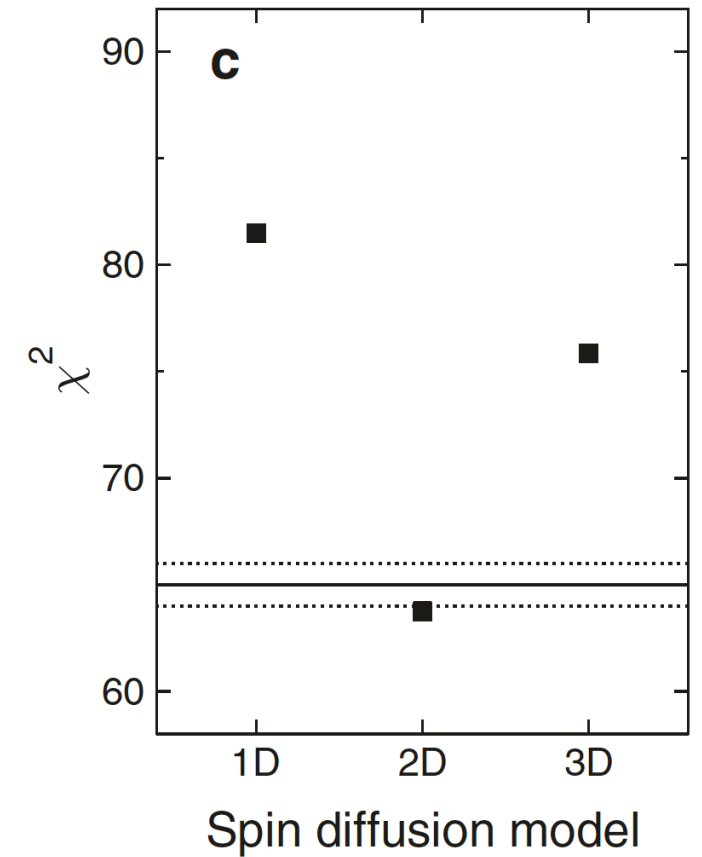
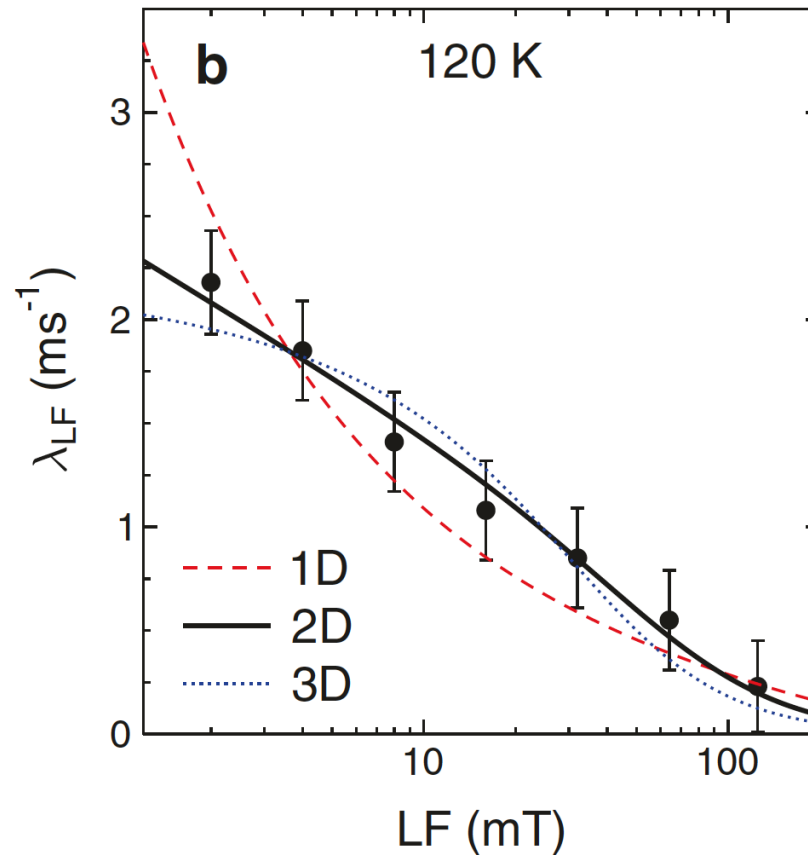
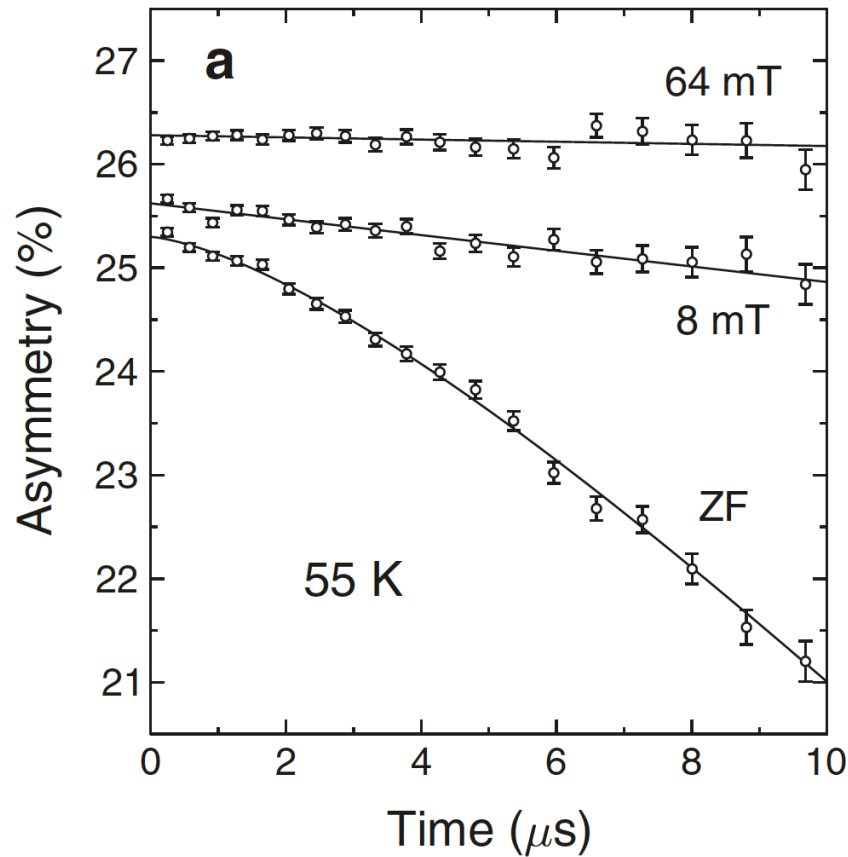
where I_0 is a zeroth order Bessel function.

- The relaxation rate $\lambda(B) \propto J_{nD}(\omega)$
 - spectral density $J_{nD}(\omega) = \text{FT}[S_{nD}(t)]$
 - probe frequency $\omega = \gamma_e B$



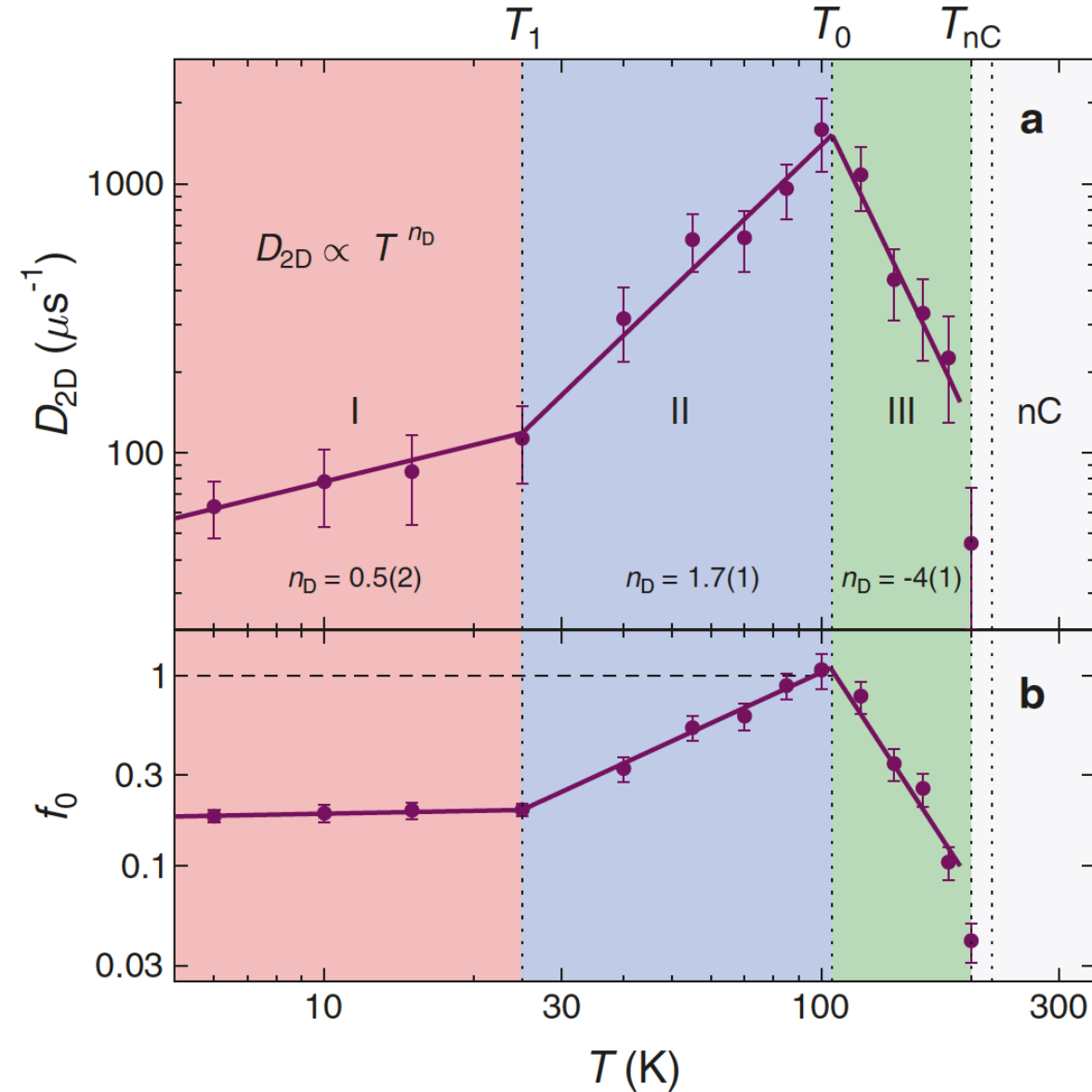
Spinon diffusion in 1T-TaS₂

$$A(t) = A_0 \exp(-\lambda_{LF} t)$$

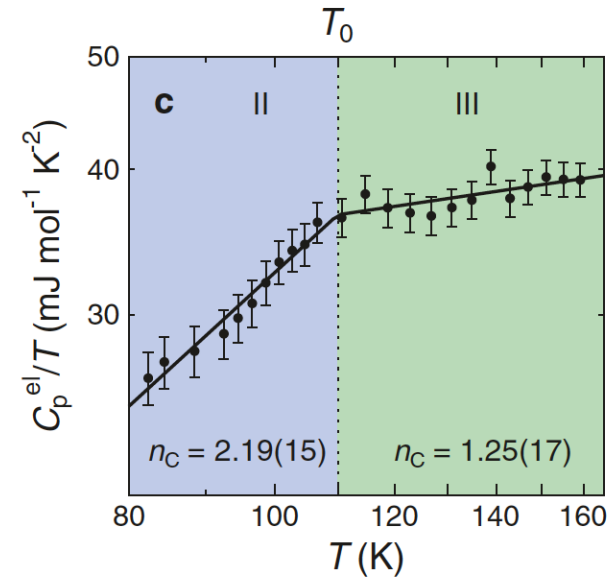
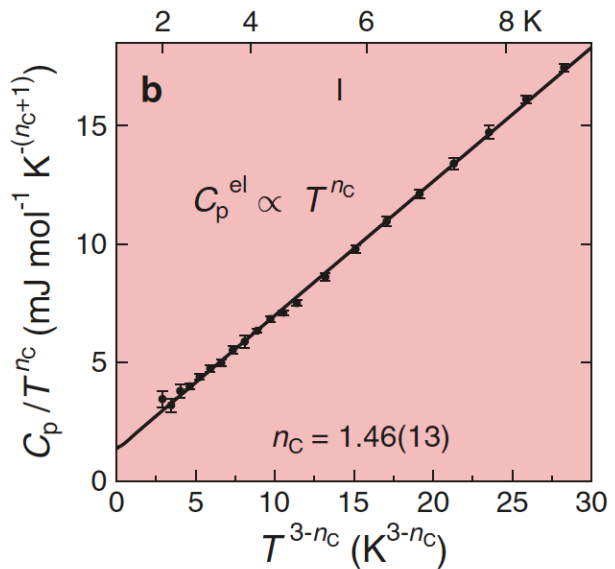
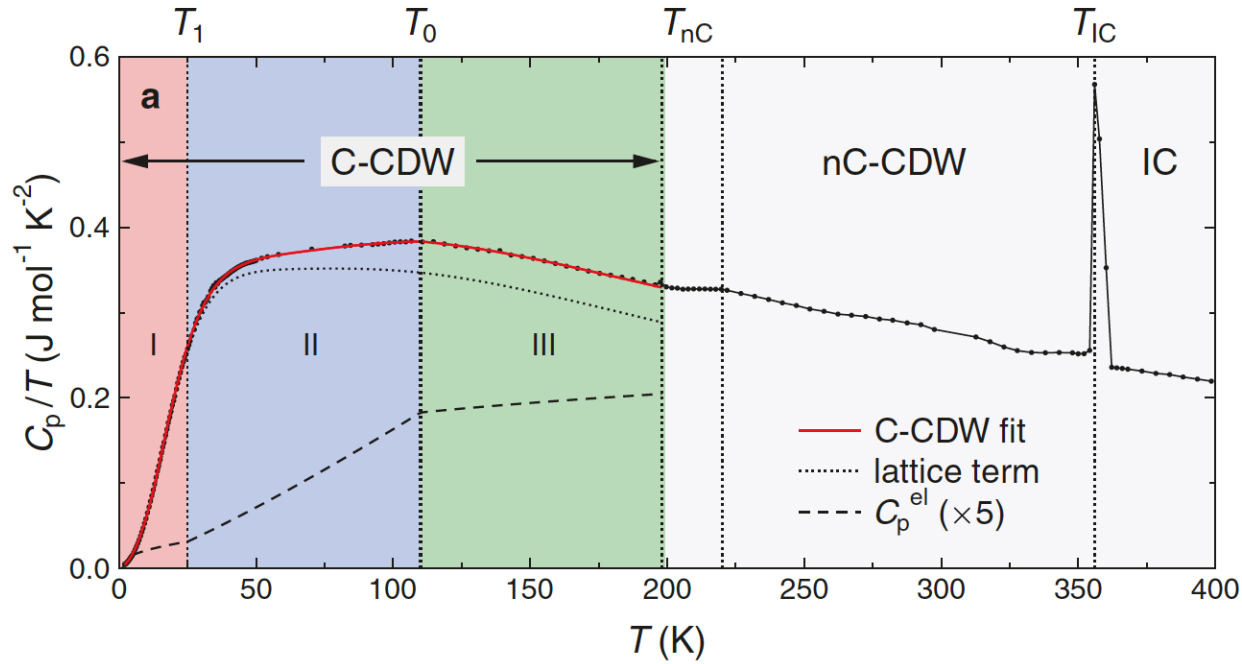


Diffusion rate

- Obtain D_{2D} from fits to $\lambda(B)$ at each temperature.
- $D_{2D} \propto T^{n_D}$
- Find three distinct regions in temperature.
- n_D can be related to predictions of QSL models.



Heat capacity

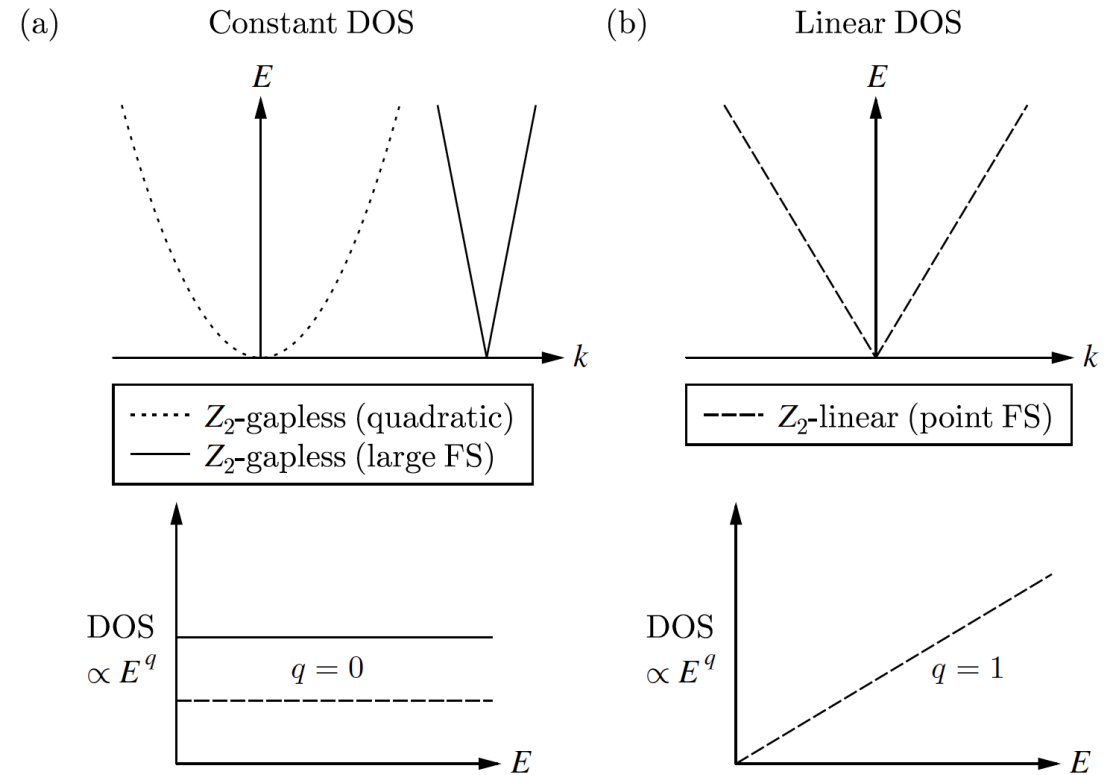
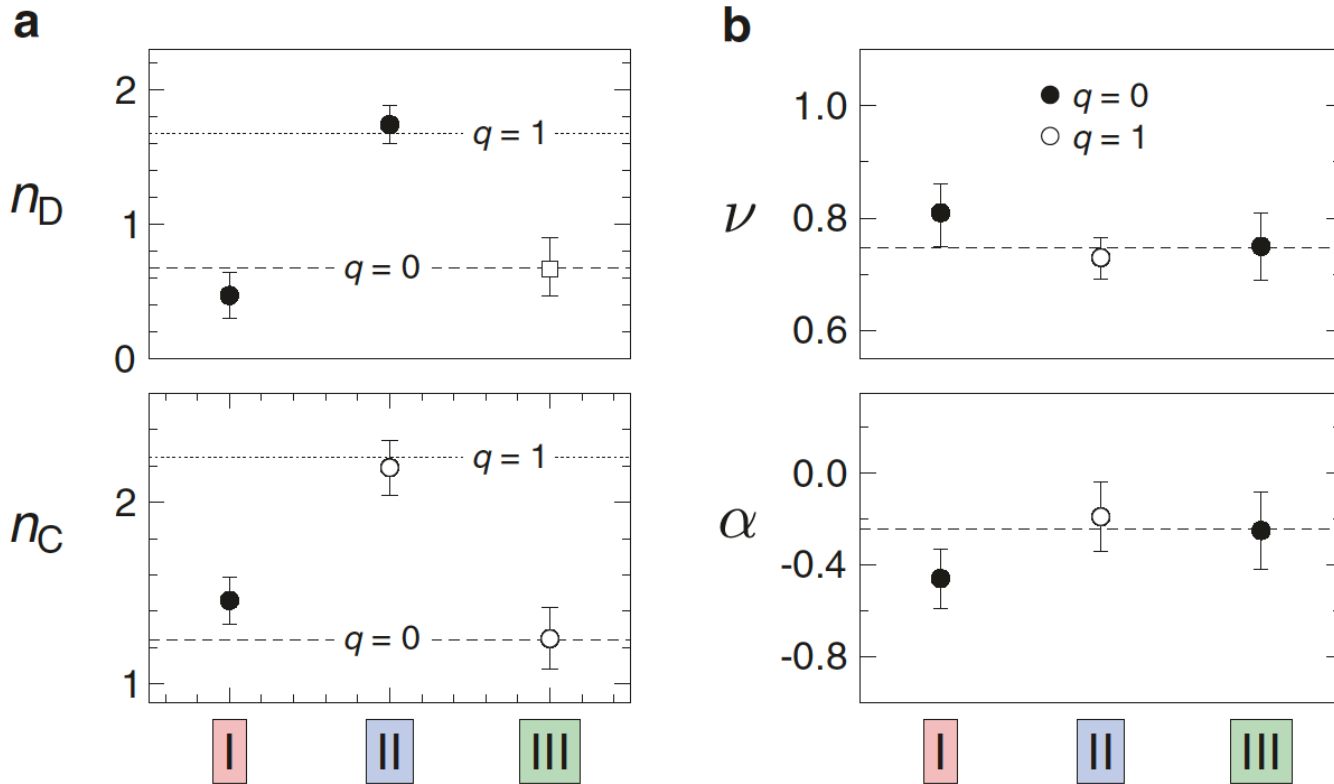


- In region I phonon contribution given by a simple Debye T^3 term.
- In regions II and III require anisotropic Debye term for acoustic phonons and two Einstein terms for optical phonons.
- Electronic contribution to the heat capacity $C_p^{el} \propto T^{n_c}$

Critical parameters

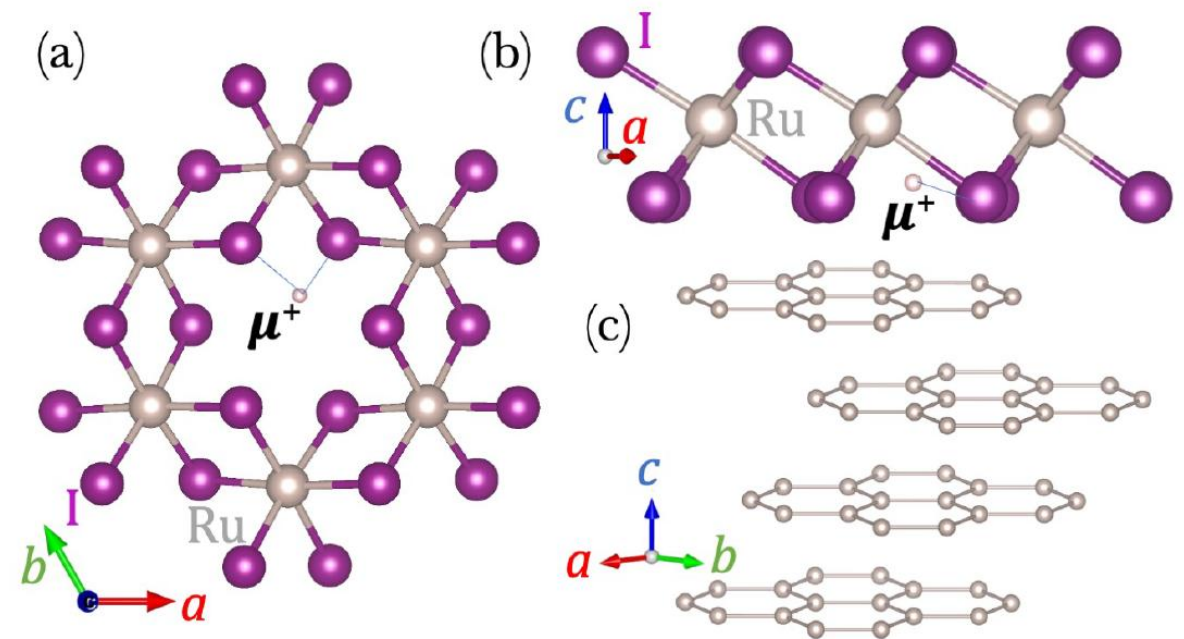
$$n_D = \frac{2}{\nu} - 2 + q$$

$$n_C = 1 - \alpha + q$$



α -RuI₃

A candidate Kitaev QSL

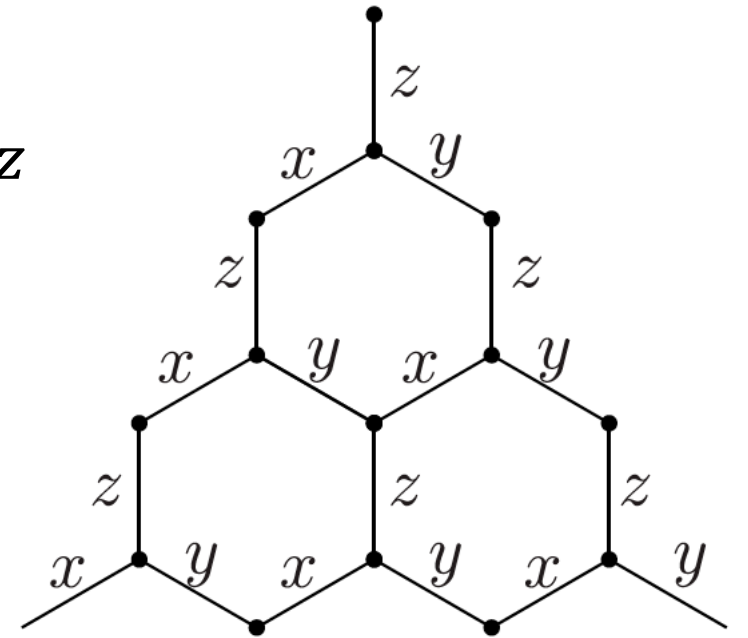


The Kitaev model

- The Kitaev model is an exactly solvable model with a QSL ground state.

$$\hat{H} = -J_x \sum_x \hat{\sigma}_i^x \hat{\sigma}_j^x - J_y \sum_y \hat{\sigma}_i^y \hat{\sigma}_j^y - J_z \sum_z \hat{\sigma}_i^z \hat{\sigma}_j^z$$

- This is an example of exchange frustration, rather than geometrical frustration.

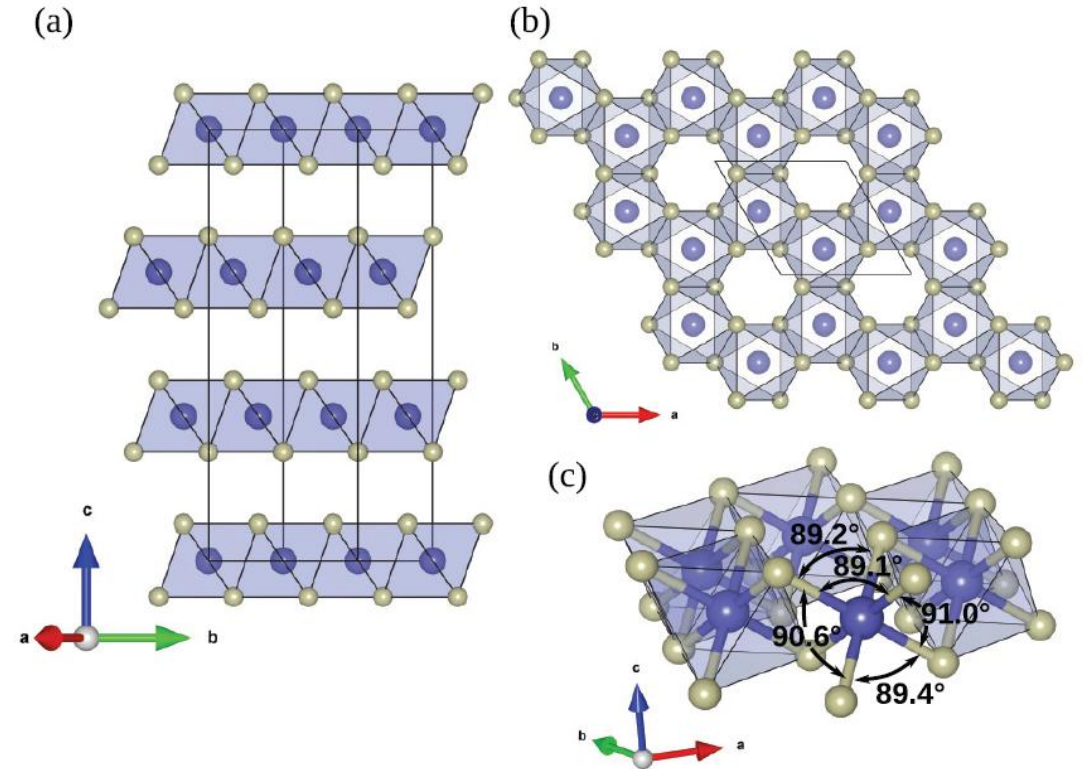


A. Kitaev, Ann. Phys. (N. Y.) **321**, 127 (2006)

T. Lancaster, Contemp. Phys. **64**, 127 (2023)

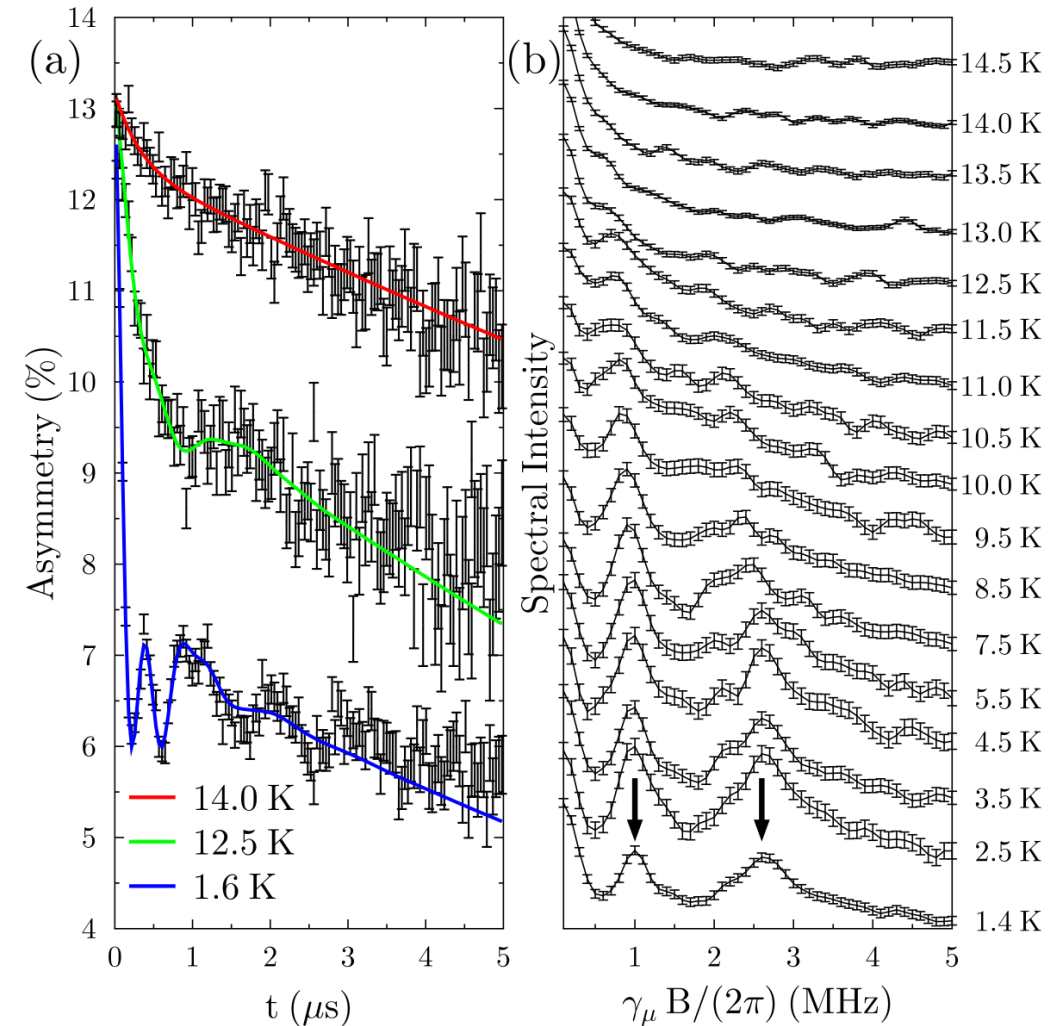
Candidate Kitaev QSLs

- Materials with $S=1/2$ spins on a honeycomb lattice and significant spin-orbit-coupling are good candidates for hosting Kitaev QSLs
- In α - RuCl_3 , indirect hopping through Cl gives rise to a Kitaev interaction.



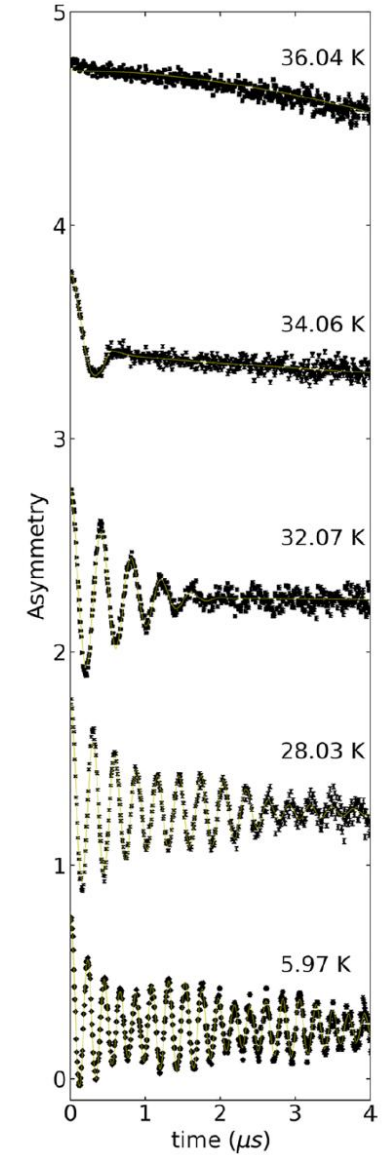
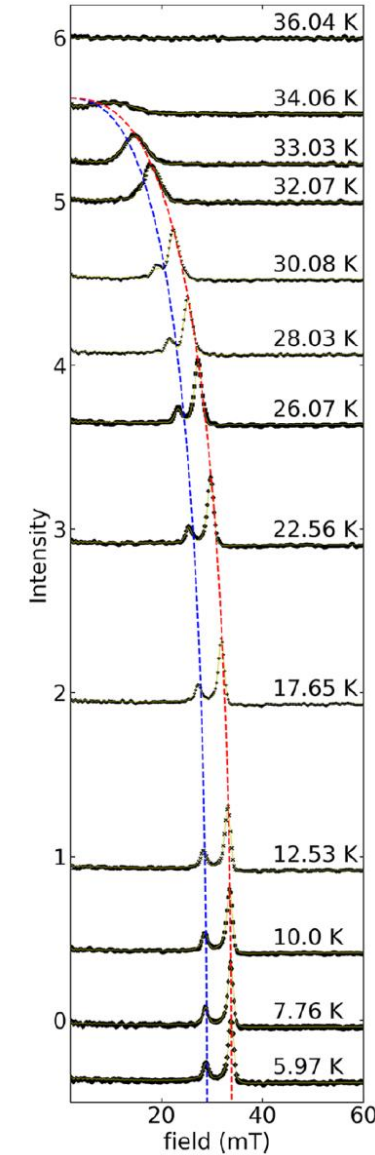
Candidate Kitaev QSLs: α -RuCl₃

- α -RuCl₃ orders magnetically into a zigzag antiferromagnetic state at around 7 to 14 K in zero-field.
- The ordering temperature is sample-dependent and possibly depends on stacking faults.



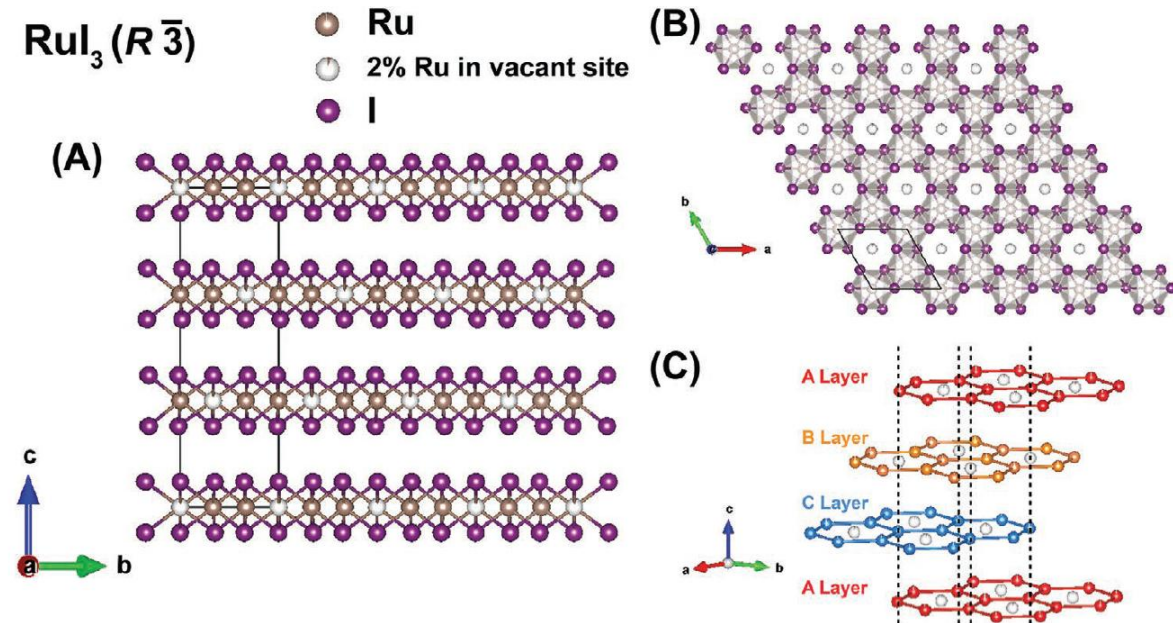
Candidate Kitaev QSLs: α -RuBr₃

- α -RuBr₃ was found also to possess a zigzag antiferromagnetic ground state with a higher transition temperature at 34 K.
- The magnetic ordering in both compounds has been attributed to non-Kitaev interactions in the Hamiltonian.



α -RuI₃

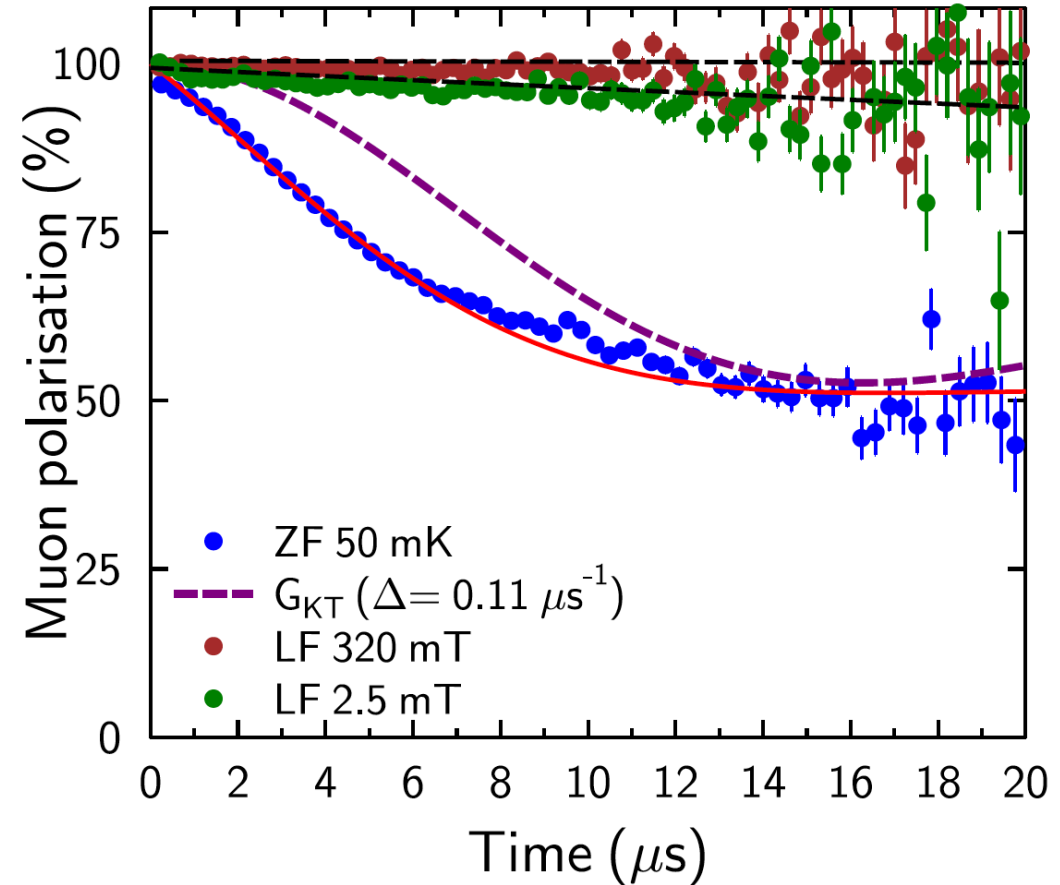
- The isostructural iodide α -RuI₃ has only recently been synthesized and has shown promising potential for being a candidate QSL.
- The material is synthesised at moderately elevated pressures and is stable under ambient conditions.
- No long-range magnetic order down to 0.35 K.



D.Ni et al., Adv. Mater. **34**, 2106831 (2022)

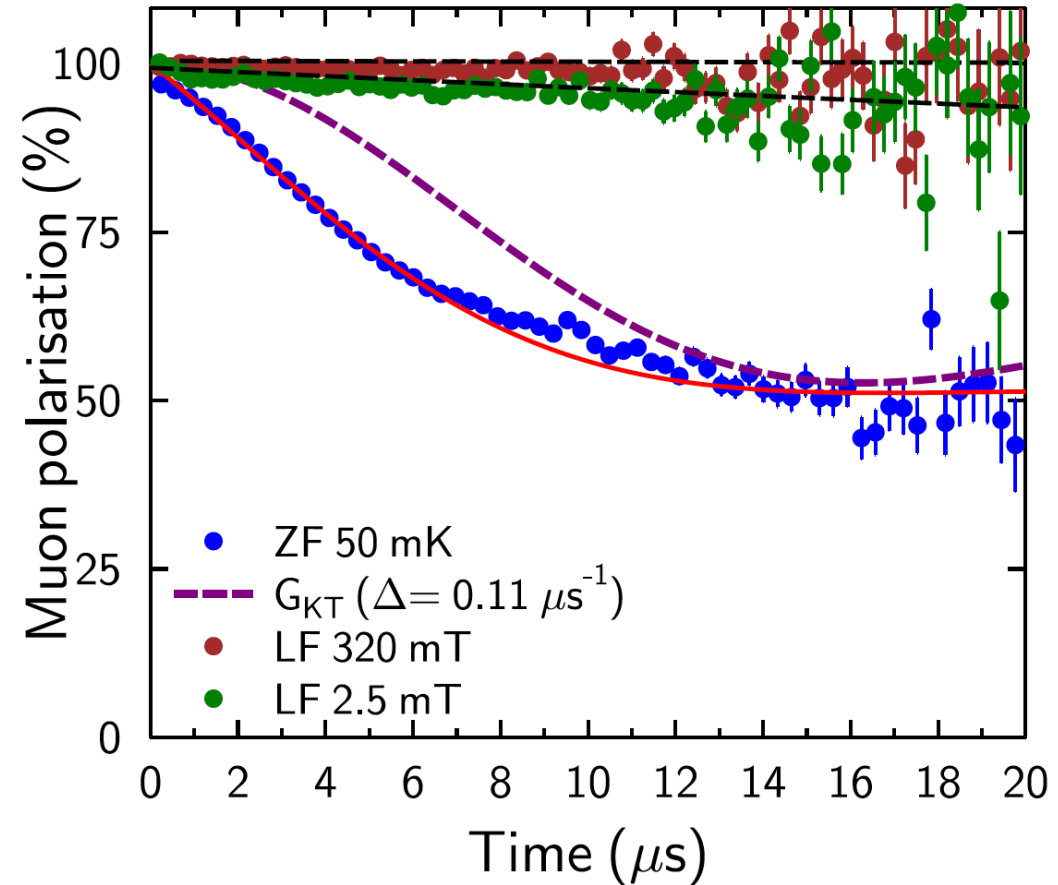
α -RuI₃: absence of magnetic order

- No oscillations in the muon polarization down to 50 mK
→ Suggests no LRO.
- Nuclear broadening at muon site insufficient to explain this relaxation, must be additional relaxation processes occurring.



α -RuI₃: longitudinal field μ SR

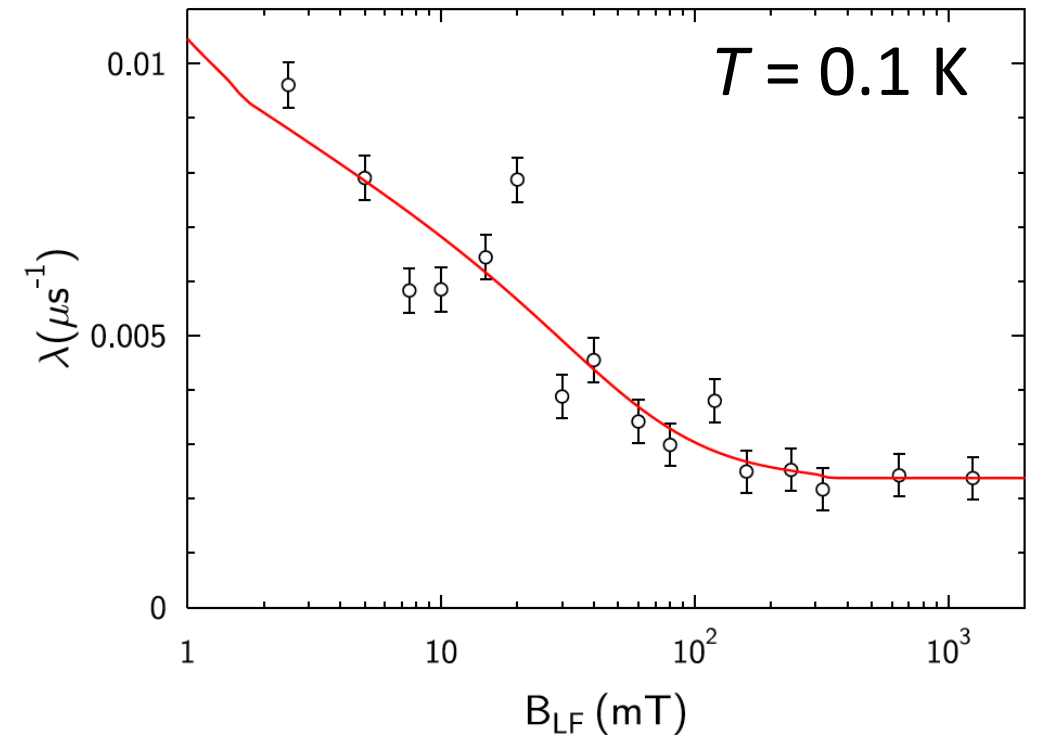
- Applying LF quenches contribution of the nuclear moments, but some exponential relaxation remains, which is due to the fluctuating Ru³⁺ moments.
- The dynamical relaxation weakens with increasing longitudinal field.



α -RuI₃: field-dependent relaxation rate

$$\lambda(B_{\text{LF}}) = \lambda_{2\text{D}}(B_{\text{LF}}) + \lambda_0$$

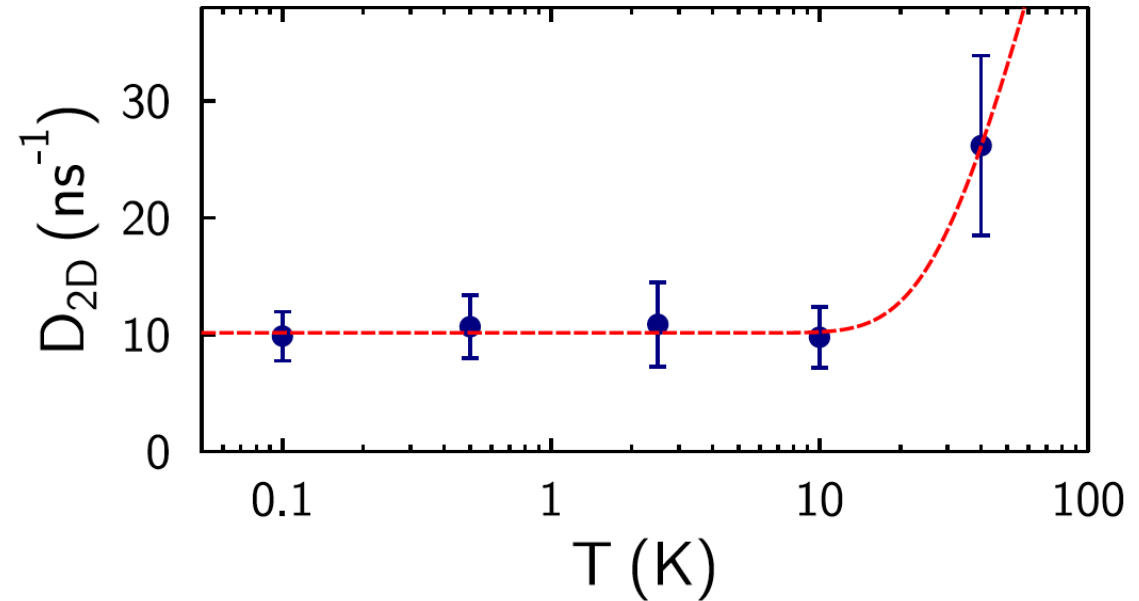
- Field-dependent term due to excitations diffusing in 2D
- 0D field-independent term due to localized excitations
- $\lambda_{2\text{D}}$ obtained from the Fourier transform of the autocorrelation function for 2D spin diffusion



α -RuI₃: spinon diffusion

- Diffusion rate approximately constant up to 10 K, but then rises rapidly at 40 K.

- Diffusion coefficient $D = \frac{1}{2}vl = D_{2D}l^2$
so that $D_{2D} = \frac{v}{2l}$



- Rising diffusion rate suggests falling mean free path l .
- **High-T**: Ru³⁺ moments correlated only to nearest neighbours (classical regime)
→ $l = a$
- **Low-T**: QSL state with long-range entanglement between spin pairs → $l = \xi$

Summary

- The reduced dimensionality of van der Waals magnets makes them promising candidate for realizing a quantum spin liquid.
- Muons are highly sensitive probes of magnetic fields and are therefore an excellent tool for confirming the absence of magnetic order.
- Muons are also sensitive to dynamics associated with spinon diffusion through the field-dependence of the LF relaxation rate.
- Following the diffusion rate as a function of temperature allows comparison to predictions of various QSL models and a measure of the quantum entanglement length.